Compton scattering from Protons and Light Nuclei: pinning down the nucleon polarizabilities

Judith McGovern

University of Manchester

Work done in collaboration with Harald Grießhammer, Daniel Phillips,

Vadim Lensky, Mike Birse, Jerry Feldman , Luke Myers *et al.*

Prog. Nucl. Part. Phys. **67** 841 (2012)

Eur. Phys. J. A **49** 12(2013)   PhysṘev. Lett. **113,** 262506 (2014)

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(2) Quick review of EFT calculations

(3) State of current calculations and fits and future directions

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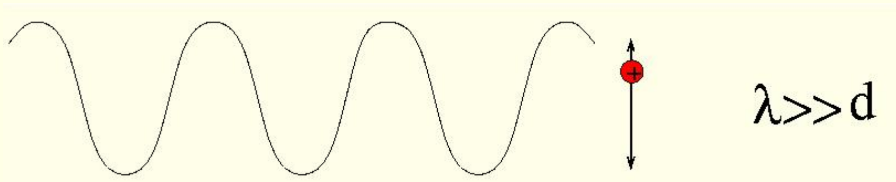
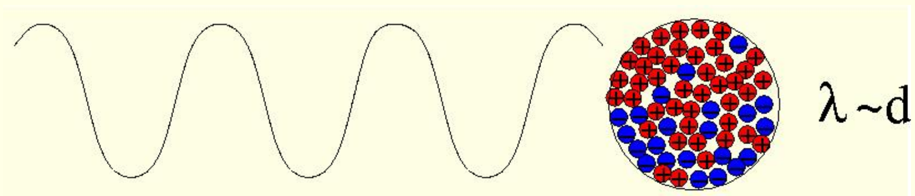
Compton Scattering

For large wavelengths, only sensitive to overall charge: Thomson scattering



But for smaller wavelengths, the target is polarised by the electric and magnetic fields



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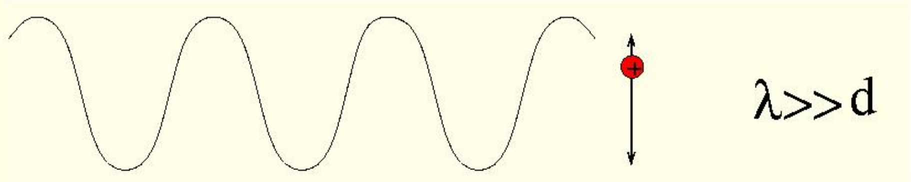

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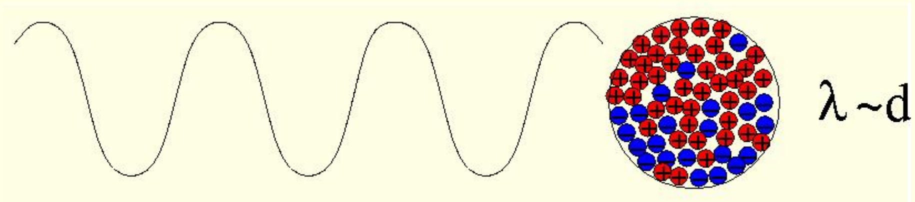
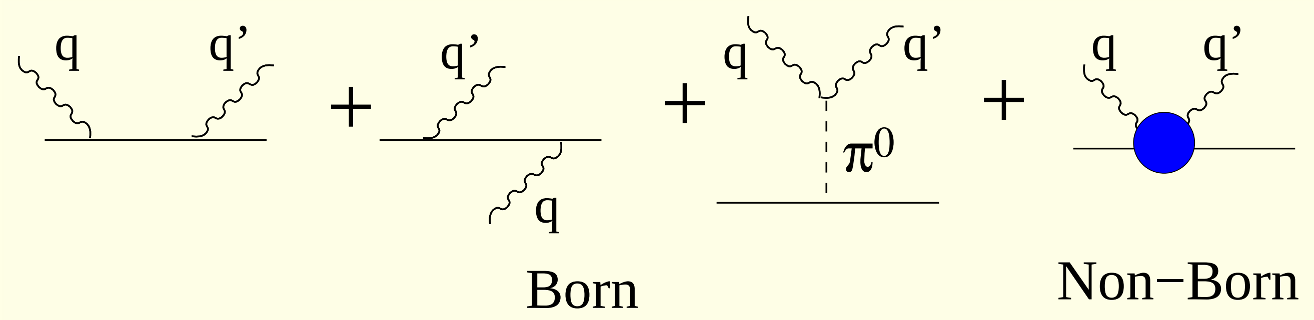


To leading order

$$
\begin{aligned}
H_{eff} &= \frac{(\mathbf{p}-Q\mathbf{A})^2}{2m} + Q\phi - \frac{1}{2}4\pi\Big(\alpha\vec{E}^2 + \beta\vec{H}^2 \\
&+ \gamma_{E1}\vec{\sigma}\cdot\vec{E}\times\dot{\vec{E}} + \gamma_{M1}\vec{\sigma}\cdot\vec{H}\times\dot{\vec{H}} - 2\gamma_{E2}E_{ij}\sigma_i H_j + 2\gamma_{M2}H_{ij}\sigma_i E_j\Big)
\end{aligned}
$$

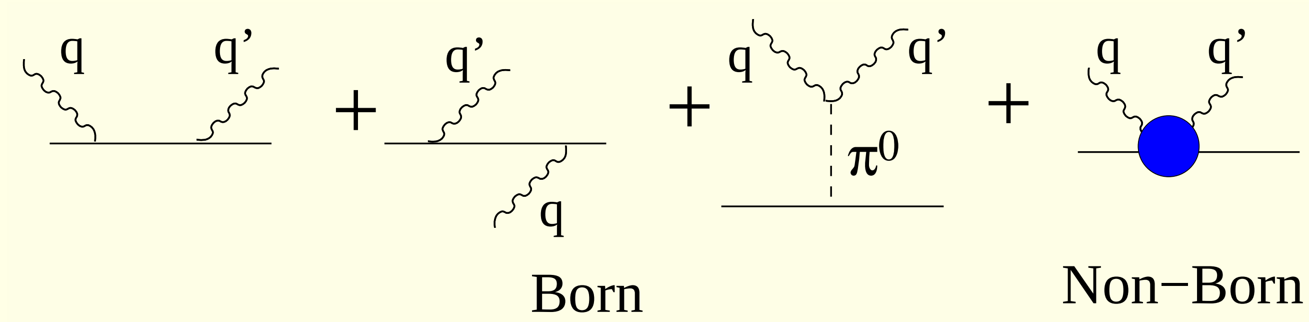
where $E_{ij} = \frac{1}{2}(\nabla_i E_j + \nabla_j E_i)$ and $H_{ij} = \frac{1}{2}(\nabla_i H_j + \nabla_j H_i)$

Compton Scattering from the nucleon



The scattering amplitude has Born and non-Born pieces. The latter probe the structure of the nucleon; polarisabilities are leading signs of non-pointlike nucleons as we increase the photon energy.

Compton Scattering from the nucleon



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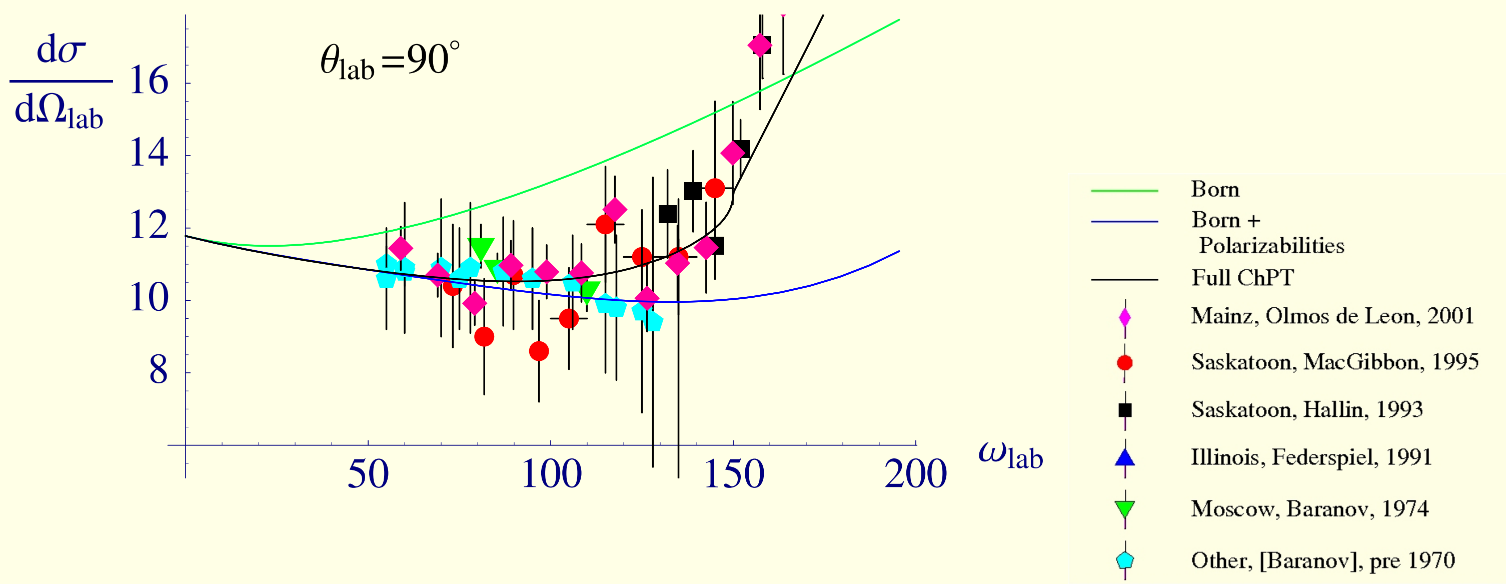

MANCHESTER 1824
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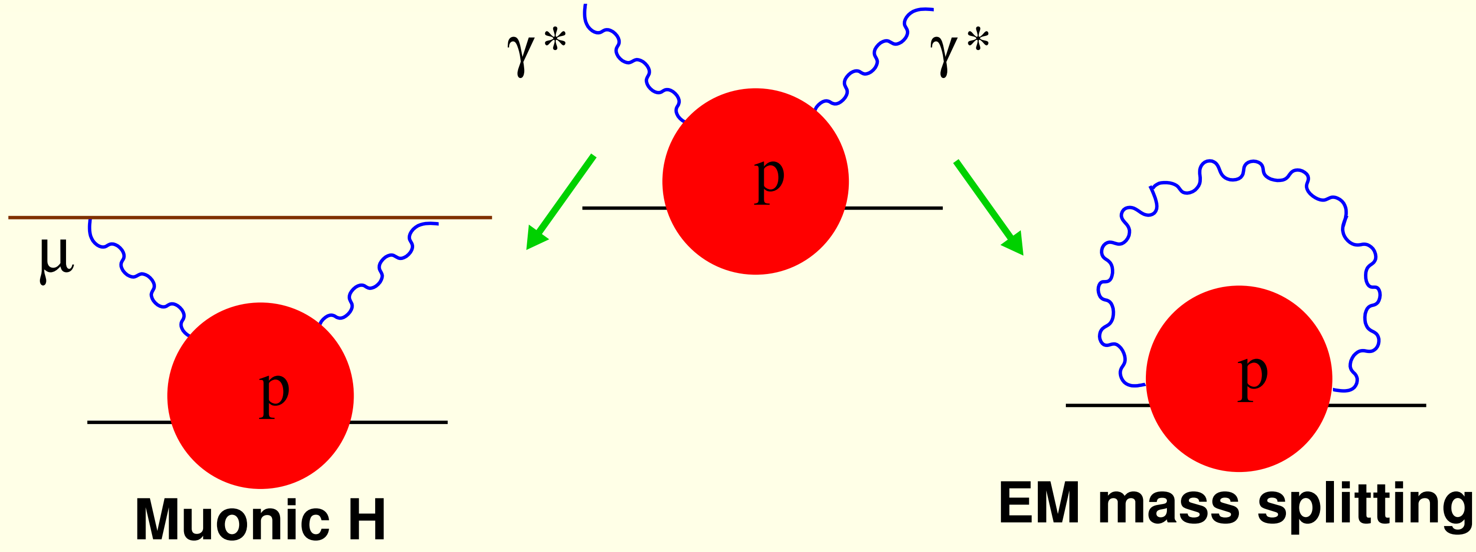
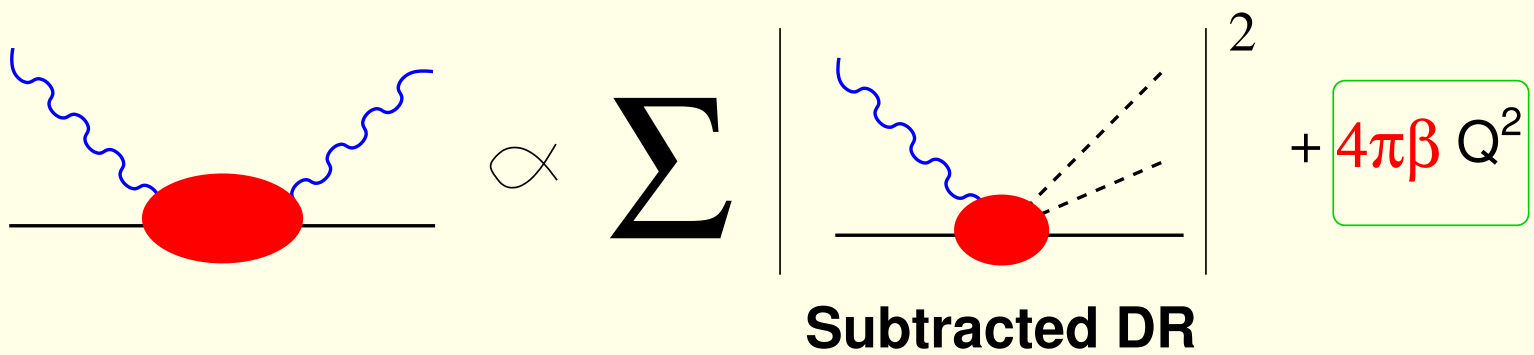
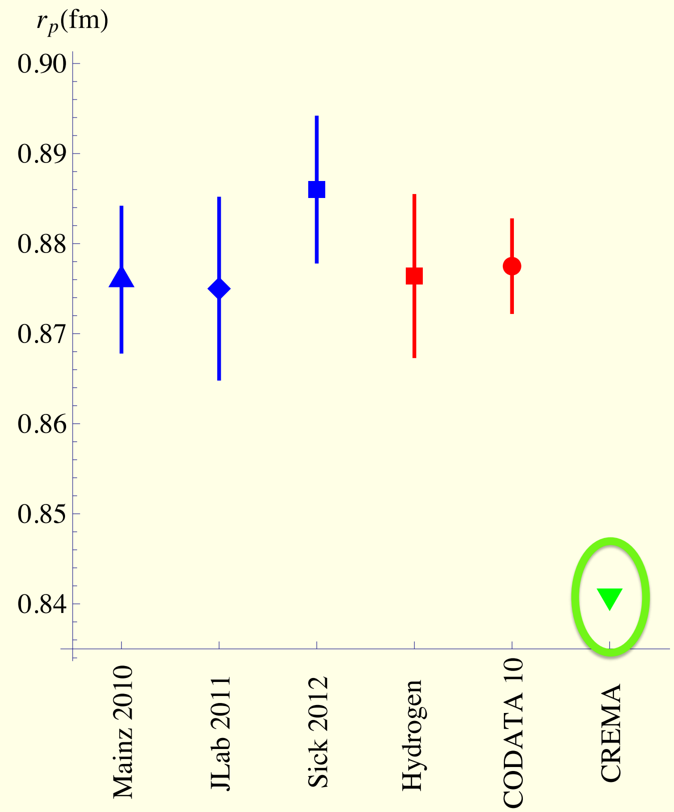
Why β matters





$$\overline{T}_1(\nu,Q^2) = -\nu^2 \int_{\nu_{th}^2}^{\infty} \frac{d\nu'^2}{\nu'^2} \frac{W_1(\nu',Q^2)}{\nu'^2-\nu^2} + 4\pi\beta Q^2 + O(Q^4)$$

Proton radius puzzle



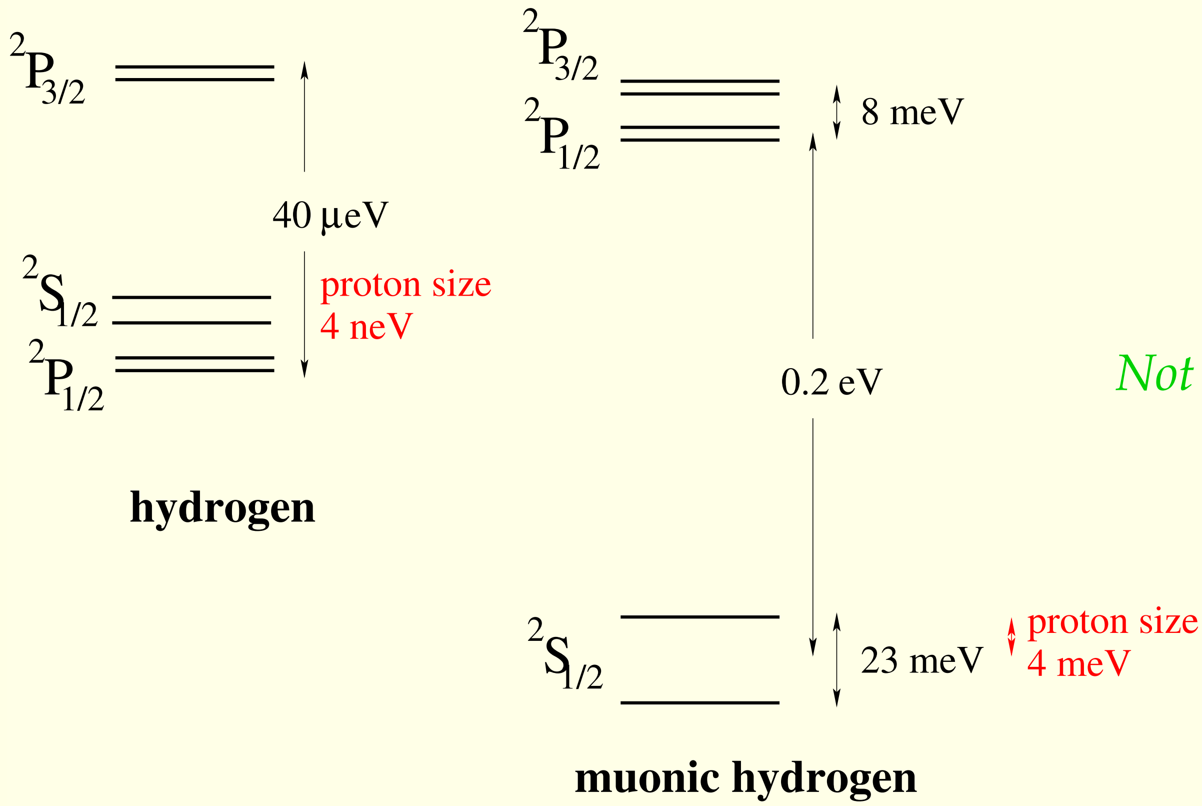
Hydrogen etc: $r_p = 0.8775(51)$ fm, CODATA 2010

Muonic hydrogen: $r_p = 0.84087 \pm 0.00039$ fm

Pohl et al, Nature **466**, 213 (2010)Antognini et al, Science **339** 417

7σ deviation!

Lamb shift



Not to scale!

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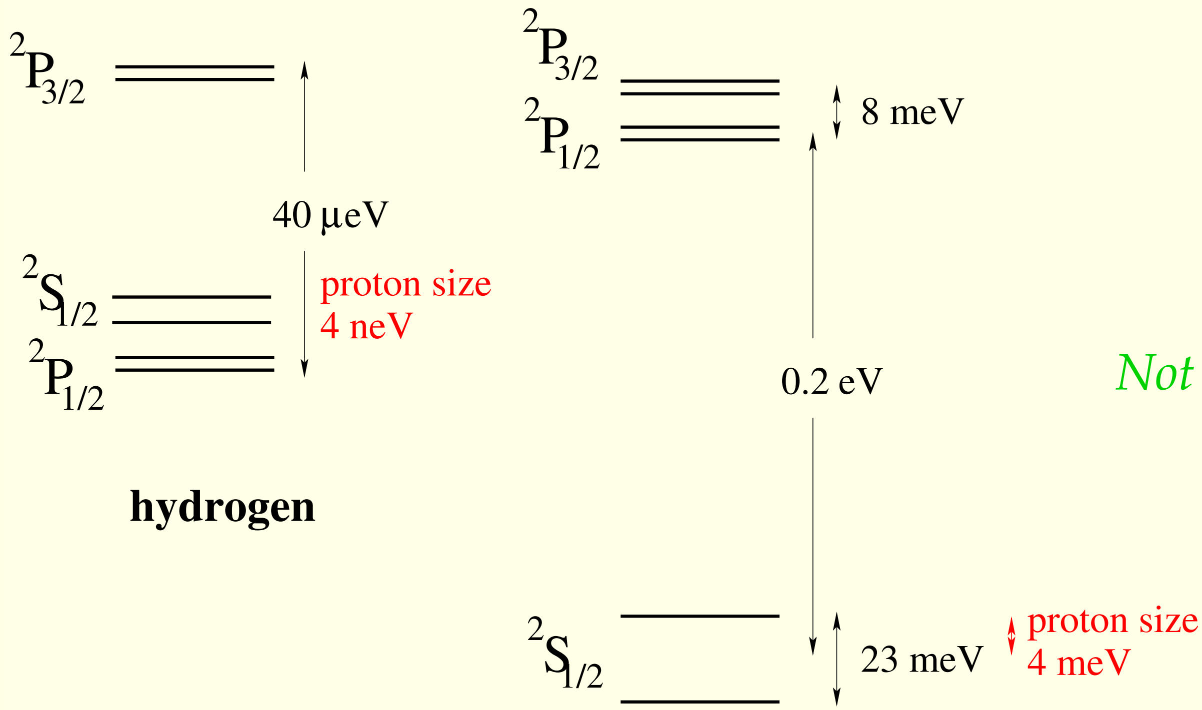
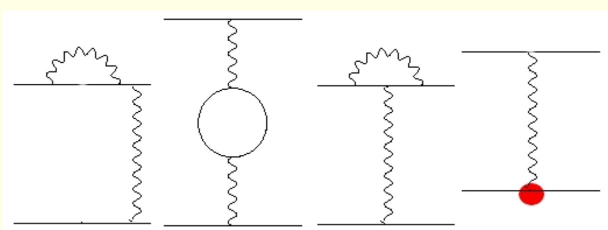


hydrogen

muonic hydrogen

Not to scale!



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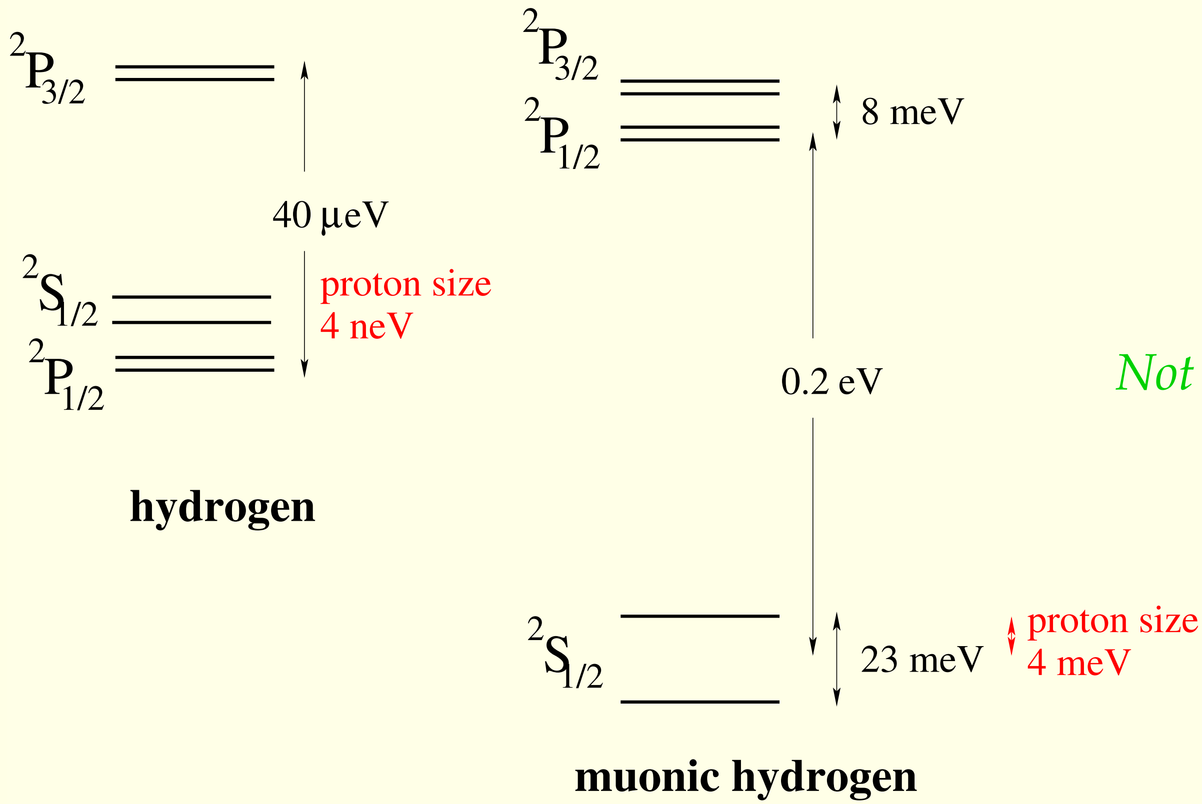

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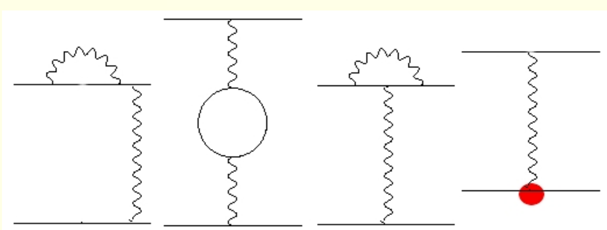

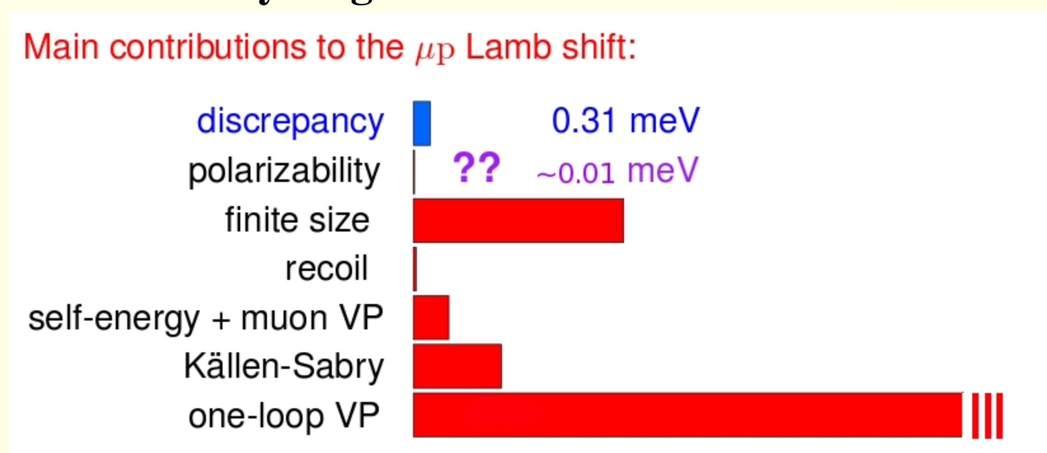

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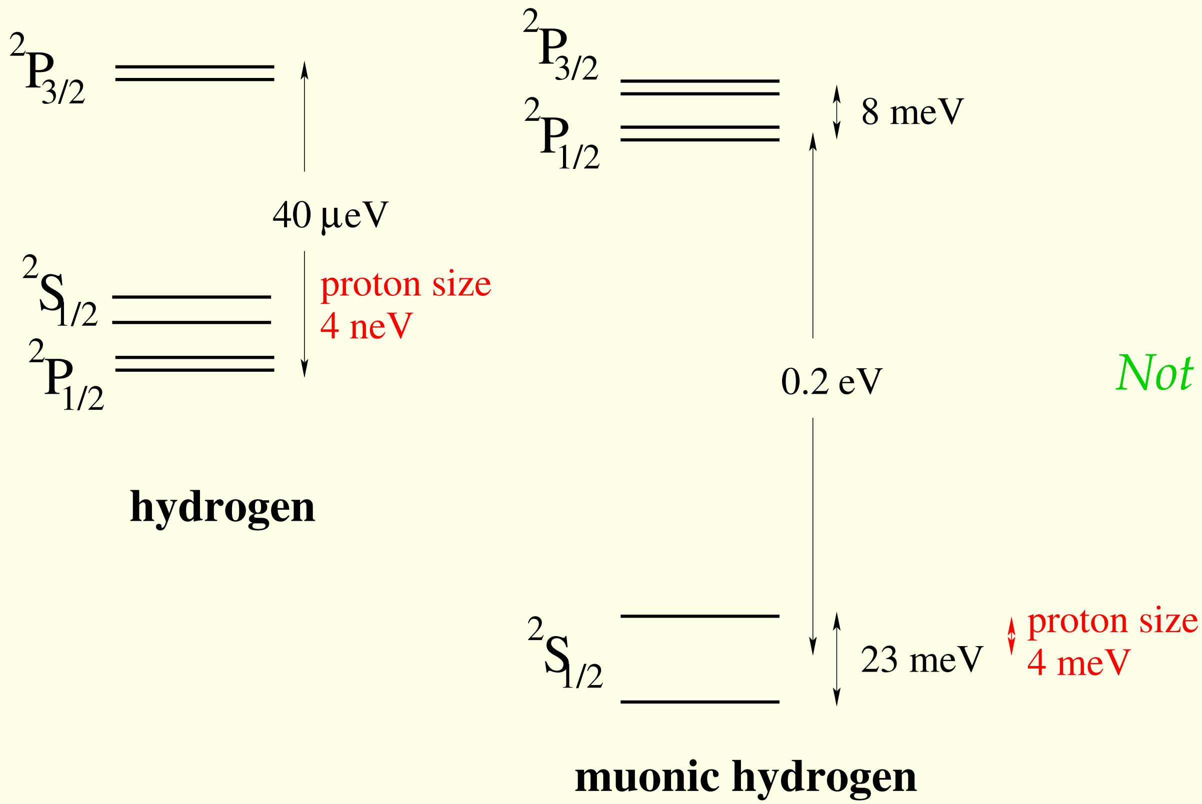

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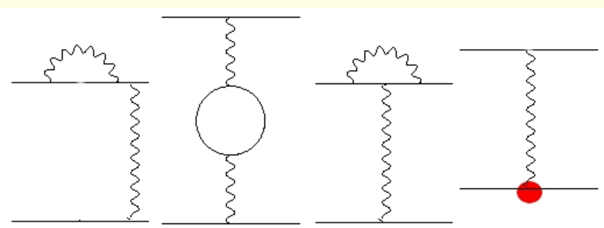
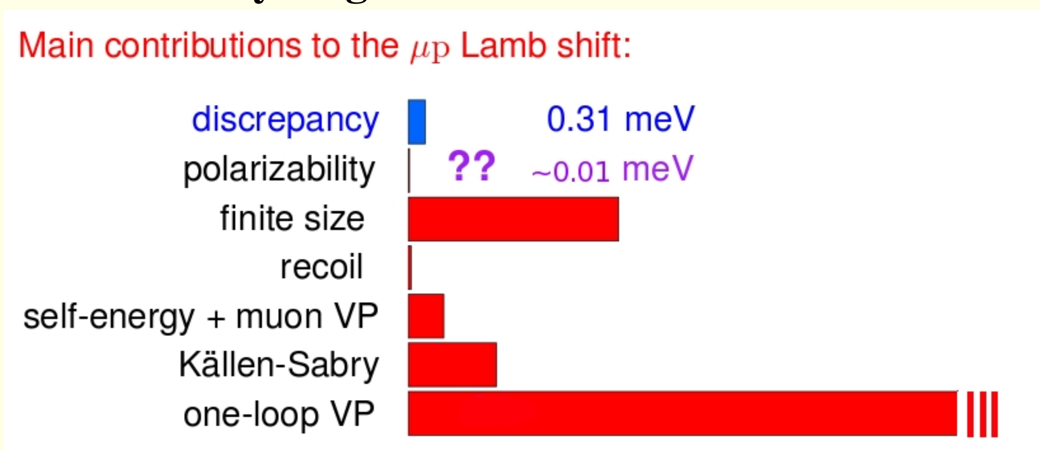


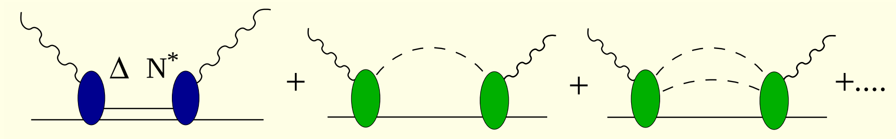


$\beta = 3.1 \pm 0.5 \implies$

$\Delta E_{\rm pol} = -0.0085(11)\,{\rm meV}$

M. Birse & JMcG, Eur. Phys. J. A **48** (2012) 120

At a hadronic level, we consider Compton scattering from the nucleon as probing its excitations and particularly its pionic cloud.



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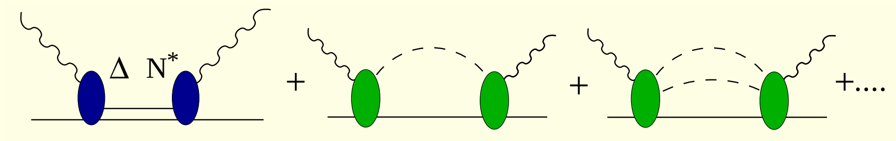
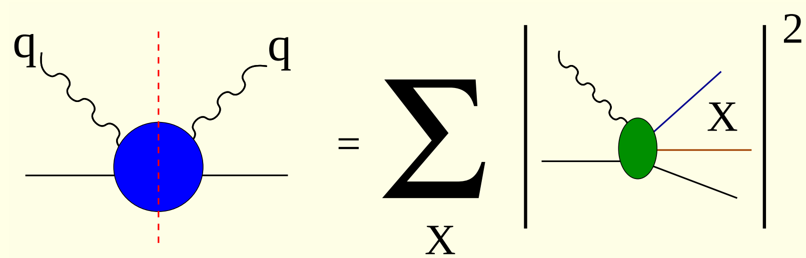


Optical theorem leads to sum rules for forward scattering



Baldin SR: $$\alpha+\beta=\frac{1}{2\pi^2}\int_{\omega_{th}}^{\infty}\frac{\sigma_{tot}(\omega)}{\omega^2}d\omega$$ and $$\gamma_0=\frac{1}{4\pi^2}\int_{\omega_{th}}^{\infty}\frac{\sigma_{1/2}(\omega)-\sigma_{3/2}(\omega)}{\omega^3}d\omega$$

Both quite accurately evaluated for the proton:
$\alpha^{(p)}+\beta^{(p)}=(13.8\pm 0.4)\times 10^{-4}$ fm^3 Olmos de Léon *et al.* EPJA **10** 207 (2001);
$\gamma_0=(-0.90\pm 0.08(\text{stat})\pm 0.11(\text{sys}))\times 10^{-4}$ fm^4 as byproduct of GDH expt. at MAMI and ELSA. Pasquini *et al.* Phys. Lett. B **687** 160 (2010)

Non-forward scattering

For the full non-Born contribution (6 independent amplitudes) need different approach.

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Chiral Perturbation Theory is a field theory which treats pions and nucleons as basic degrees of freedom

Both have difficulties with parameter-free predictions; both can be used to fit Compton scattering data and extract polarisabiltiies.

Chiral Perturbation theory

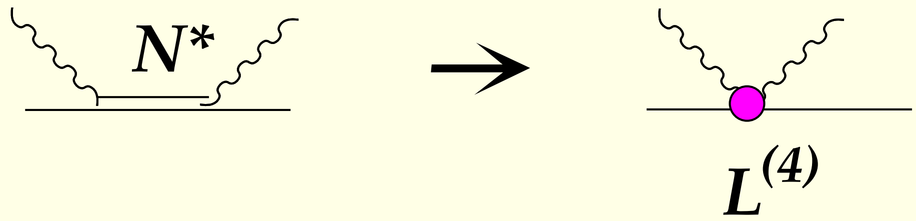
Effective field theory of QCD– relies on separation of scales

- pions are light ($m_\pi \ll m_\rho$)
- low-energy pions interact weakly with other matter ($L_{\pi NN} \propto \overline{N}\partial_\mu \pi N$).

Thus pion loops are suppressed by $\approx m_\pi^2/\Lambda^2$ where $\Lambda \approx m_\rho$. The Lagrangian contains infinitely many terms:

$$\mathcal{L} = \sum_n \mathcal{L}^{(n)}(c_i^{(n)})$$

Non-pionic nucleon structure shows up in low energy constants $c_i^{(n)}$, but is suppressed by power of momentum: $(k/\Lambda)^n$:



Calculations to nth order involve vertices from $\mathcal{L}^{(n)}$ and pion loops with vertices from $\mathcal{L}^{(n-2)}$; truncation errors are $\sim (k/\Lambda)^{(n+1)}$.

χPT for Compton Scattering from the nucleon

We include nucleons, pions and the Delta in our Lagrangian.

$$\mathcal{L}_{\pi N}^{(4),\mathrm{CT}} = 2\pi e^2 H^\dagger \left[\left(\delta\beta_{M1}^{(s)} + \delta\beta_{M1}^{(v)} \tau_3 \right) \left(\tfrac{1}{2} g_{\mu\nu} - v_\mu v_\nu \right) - \left(\delta\alpha_{E1}^{(s)} + \delta\alpha_{E1}^{(v)} \tau_3 \right) v_\mu v_\nu \right] F^{\mu\rho} F^\nu_{\ \rho} H.$$

Counterterms shift α_{E1} and β_{M1} at 4th order. Counterterms for spin pols at 5th order.

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$\Delta \equiv M_\Delta - M_N \approx 271$ MeV is a rather small scale. Traditionally it is counted as $\Delta/\Lambda_\chi \sim m_\pi/\Lambda_\chi$ ("SSE"). But in Compton scattering the pion is clearly important at lower energies than the Delta.

Alternative: count $$\frac{m_\pi}{\Delta} \sim \frac{\Delta}{\Lambda_\chi} \quad \Rightarrow \quad \delta^2 \equiv \left(\frac{\Delta}{\Lambda_\chi}\right)^2 \sim \frac{m_\pi}{\Lambda_\chi}$$

Then graphs with one Δ propagator are one order of δ higher than the corresponding nucleon graphs in low energy region.

Pascalutsa and Phillips, Phys. Rev. C67 (2003) 055202

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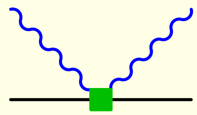
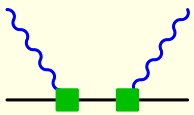
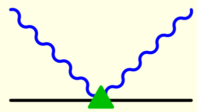
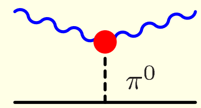
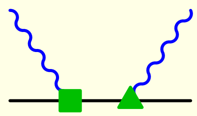
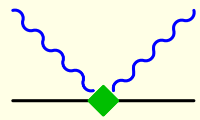
Different counting in resonance region; we work to at least NLO in both.

Tree graphs

Born terms give the Thomson term and spin-dependent LETs (ensured by gauge and Lorentz invariance)

contribution with typical size				$\omega \sim m_\pi$	$\omega \sim \Delta$
(i)				$e^2\delta^0$ (LO)	$e^2\delta^0$
(ii)	(a) 	(b) 	(c) 	$e^2\delta^2$	$e^2\delta^1$
(iii)	(a) 	(b) 		$e^2\delta^4$	$e^2\delta^2$

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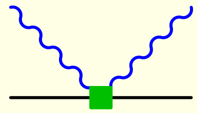
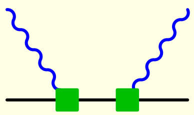
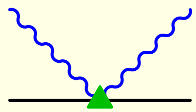
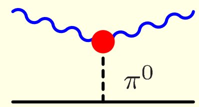
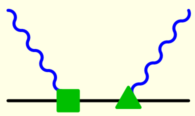
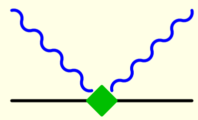
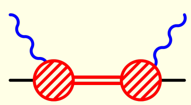
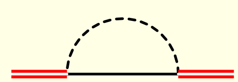
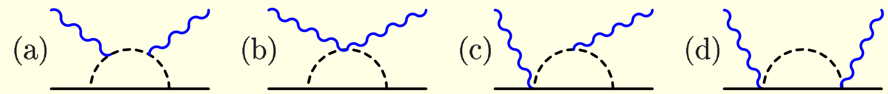
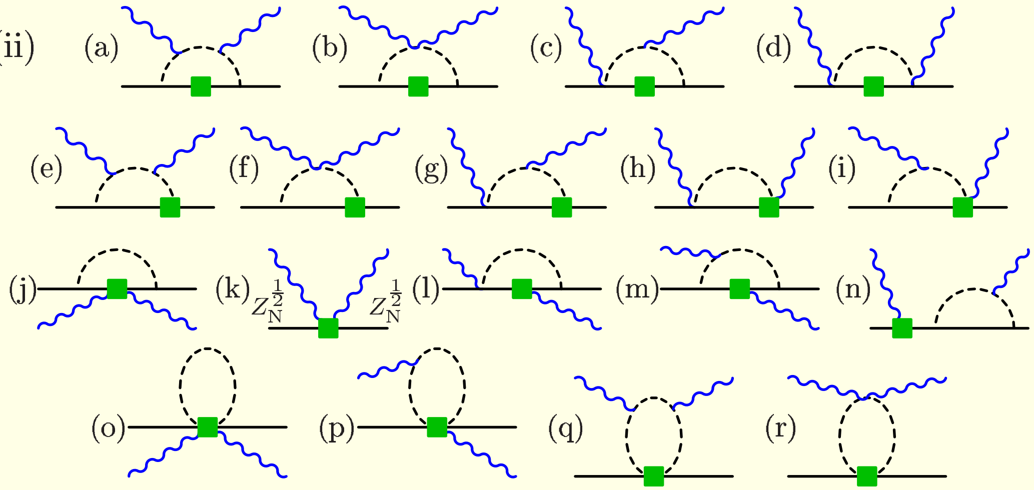
(i)		$e^2\delta^0$ (LO)	$e^2\delta^0$
(ii)	(a)  (b)  (c) 	$e^2\delta^2$	$e^2\delta^1$
(iii)	(a)  (b) 	$e^2\delta^4$	$e^2\delta^2$

In resonance region Delta-pole graph dominates

(i)		$e^2\delta^3$	$e^2\delta^{-1}$ (LO)

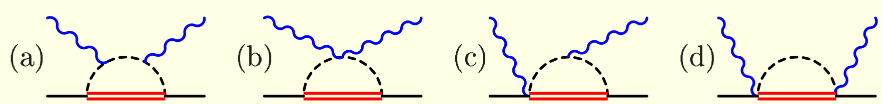
Include Delta width by resuming self-energy: 

Loops

contribution with typical size	$\omega \sim m_\pi$	$\omega \sim \Delta$
(i) 	$e^2\delta^2$	$e^2\delta^1$
(ii) 	$e^2\delta^4$	$e^2\delta^2$

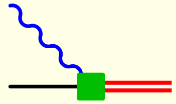
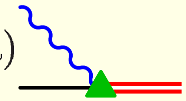
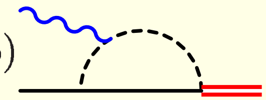
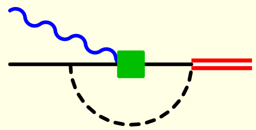
At 4th order we have $1/M$ corrections and c_i contributions

Delta loops are less important in low-energy region

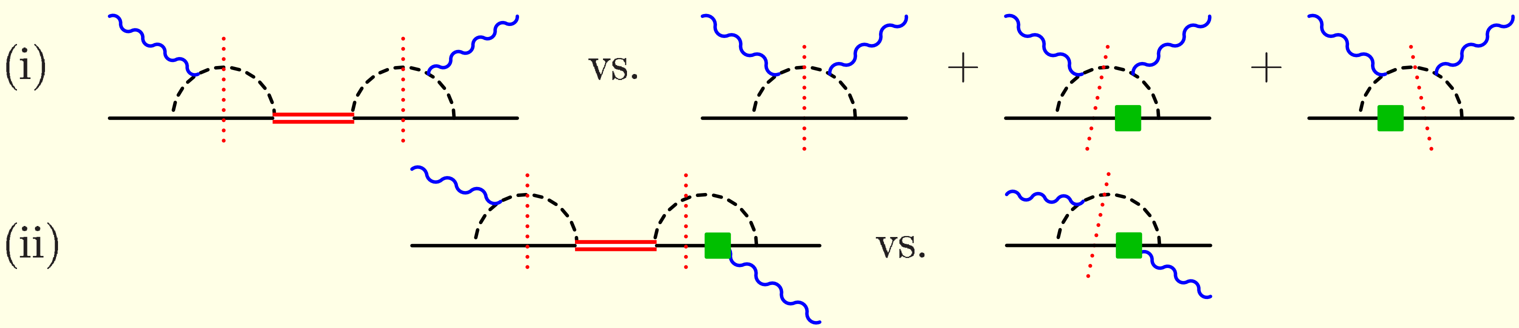
(ii) 	$e^2\delta^3$	$e^2\delta^1$

Important: predicts full energy-dependent amplitudes, not just polarisabilities

Running of γNΔ vertex

contribution with typical size		$\omega \sim m_\pi$	$\omega \sim \Delta$
(i)		$e\delta^2$	$e\delta^1$
(ii)	(a)  (b) 	$e\delta^4$	$e\delta^2$
(iii)		$e\delta^6$	$e\delta^3$

The inclusion of the imaginary part of running vertices satisfies Watson's theorem
- cancellation of $I = 3/2$ loops at resonance



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Anatomy of Compton amplitude—reminder

$$
\begin{aligned}
T(\omega,z) \;=\; & A_1(\omega,z)\,(\vec{\varepsilon}\,'^{*}\cdot\vec{\varepsilon}) + A_2(\omega,z)\,(\vec{\varepsilon}\,'^{*}\cdot\hat{\vec{k}})\,(\vec{\varepsilon}\cdot\hat{\vec{k}}') \\
& + \mathrm{i}A_3(\omega,z)\,\vec{\sigma}\cdot\left(\vec{\varepsilon}\,'^{*}\times\vec{\varepsilon}\right) + \mathrm{i}A_4(\omega,z)\,\vec{\sigma}\cdot\left(\hat{\vec{k}}'\times\hat{\vec{k}}\right)(\vec{\varepsilon}\,'^{*}\cdot\vec{\varepsilon}) \\
& + \mathrm{i}A_5(\omega,z)\,\vec{\sigma}\cdot\left[\left(\vec{\varepsilon}\,'^{*}\times\hat{\vec{k}}\right)(\vec{\varepsilon}\cdot\hat{\vec{k}}') - \left(\vec{\varepsilon}\times\hat{\vec{k}}'\right)(\vec{\varepsilon}\,'^{*}\cdot\hat{\vec{k}})\right] \\
& + \mathrm{i}A_6(\omega,z)\,\vec{\sigma}\cdot\left[\left(\vec{\varepsilon}\,'^{*}\times\hat{\vec{k}}'\right)(\vec{\varepsilon}\cdot\hat{\vec{k}}') - \left(\vec{\varepsilon}\times\hat{\vec{k}}\right)(\vec{\varepsilon}\,'^{*}\cdot\hat{\vec{k}})\right] .
\end{aligned}
$$

ω - photon energy, $z = \cos\theta$; Breit or cm frame

Non-Born pieces:

$$
\begin{aligned}
\bar{A}_1(\omega,\,z) &= 4\pi\,[\alpha_{E1} + z\beta_{M1}]\,\omega^2 + \ldots \\
\bar{A}_2(\omega,\,z) &= -4\pi\,\beta_{M1}\,\omega^2 + \ldots \\
\bar{A}_3(\omega,\,z) &= -4\pi\,[\gamma_{E1E1} + z\gamma_{M1M1} + \gamma_{E1M2} + z\gamma_{M1E2}]\,\omega^3 + \ldots \\
\bar{A}_4(\omega,\,z) &= 4\pi\,[-\gamma_{M1M1} + \gamma_{M1E2}]\,\omega^3 + \ldots \\
\bar{A}_5(\omega,\,z) &= 4\pi\,\gamma_{M1M1}\,\omega^3 + \ldots \\
\bar{A}_6(\omega,\,z) &= 4\pi\,\gamma_{E1M2}\,\omega^3 + \ldots
\end{aligned}
$$

If we write $\alpha_{E1} \to \alpha_{E1}(\omega)$ etc we have $l = 1$ in a multipole expansion

Multipoles

We can predict the full energy-dependence of the amplitudes, and only the value at the origin for α, β and γ_{M1M1} are fitted.

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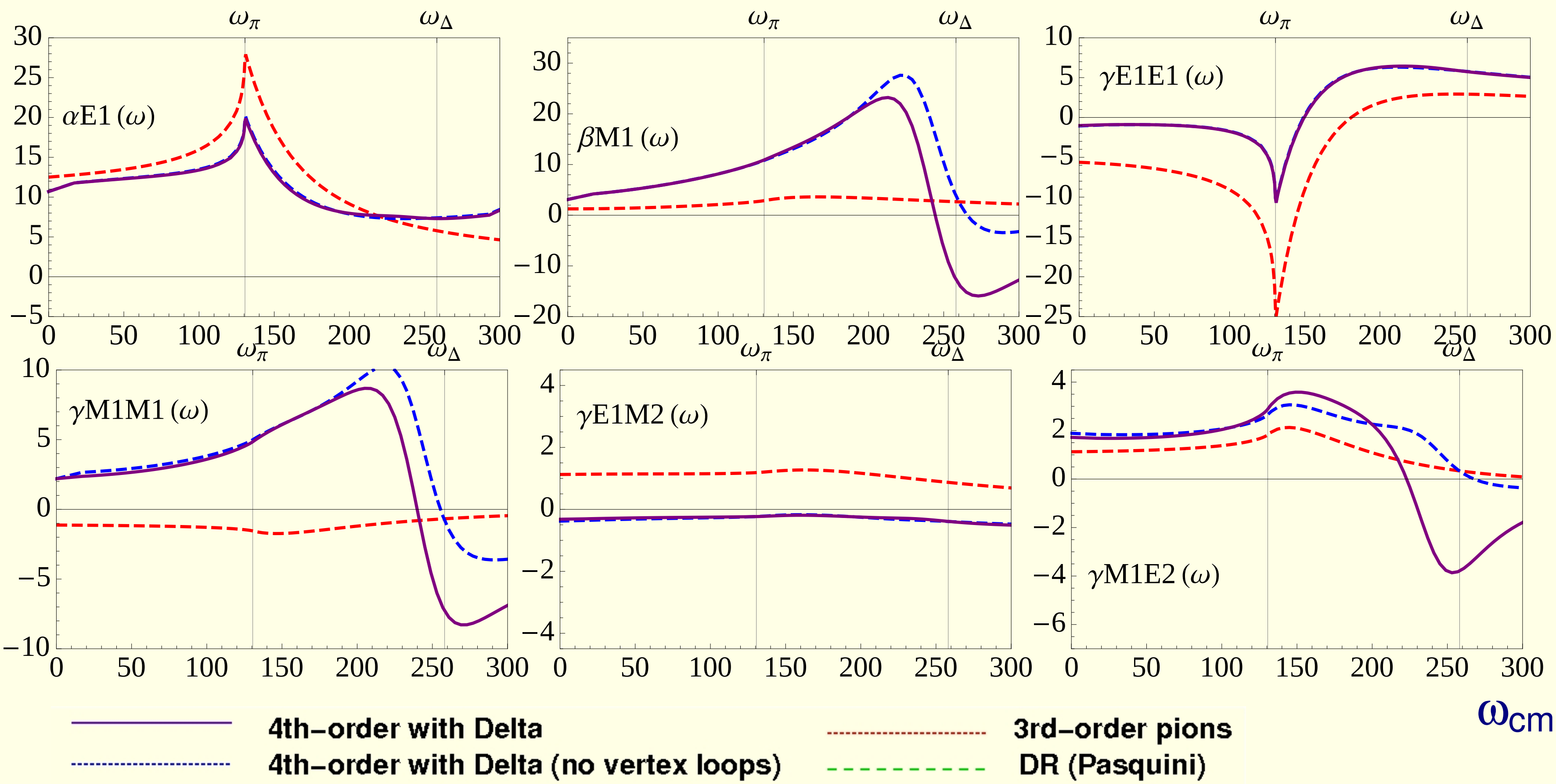

Note contribution of Delta, and also of the running of the γNΔ vertex.

JMcG *et al.* , in preparation

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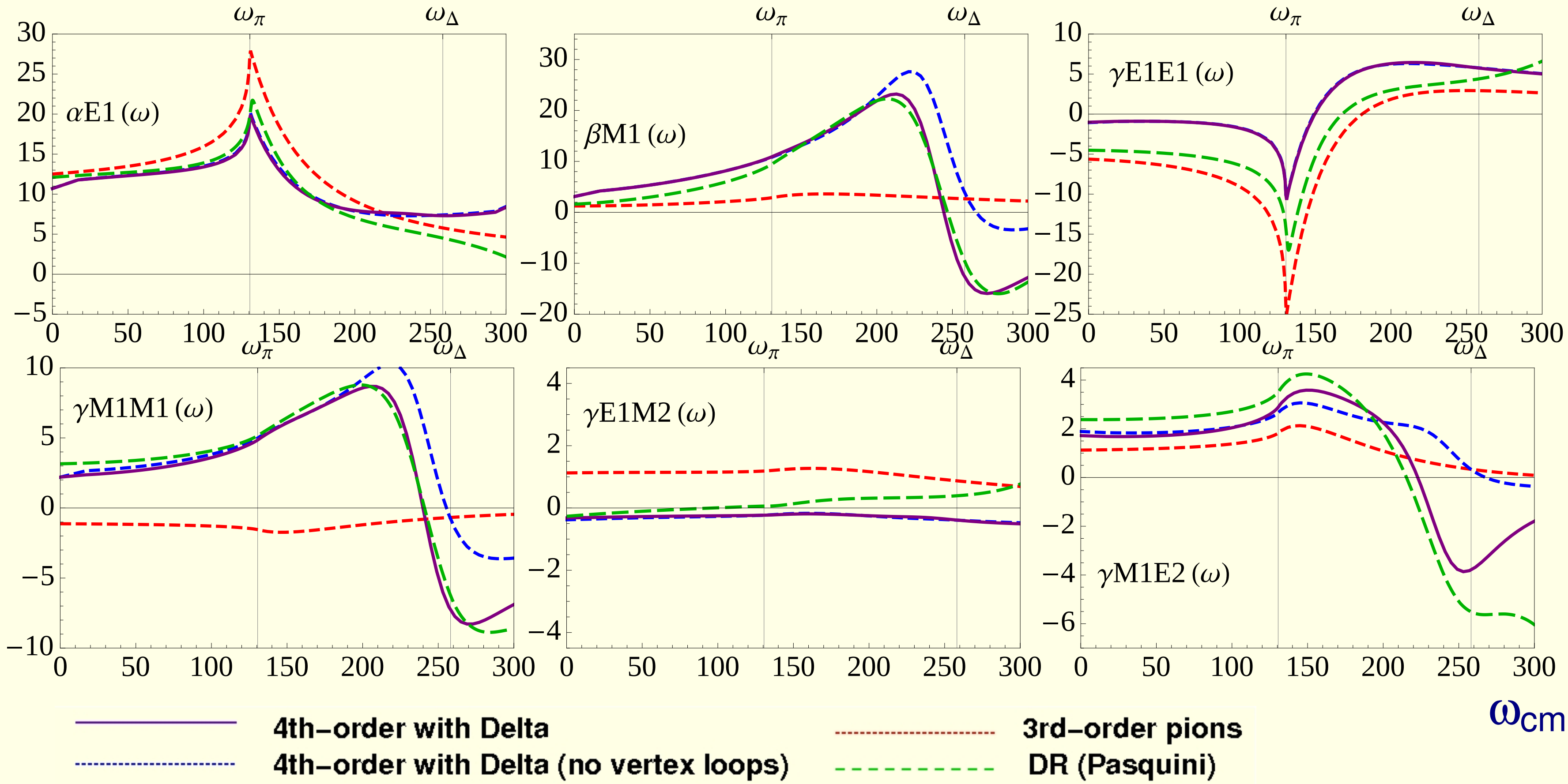

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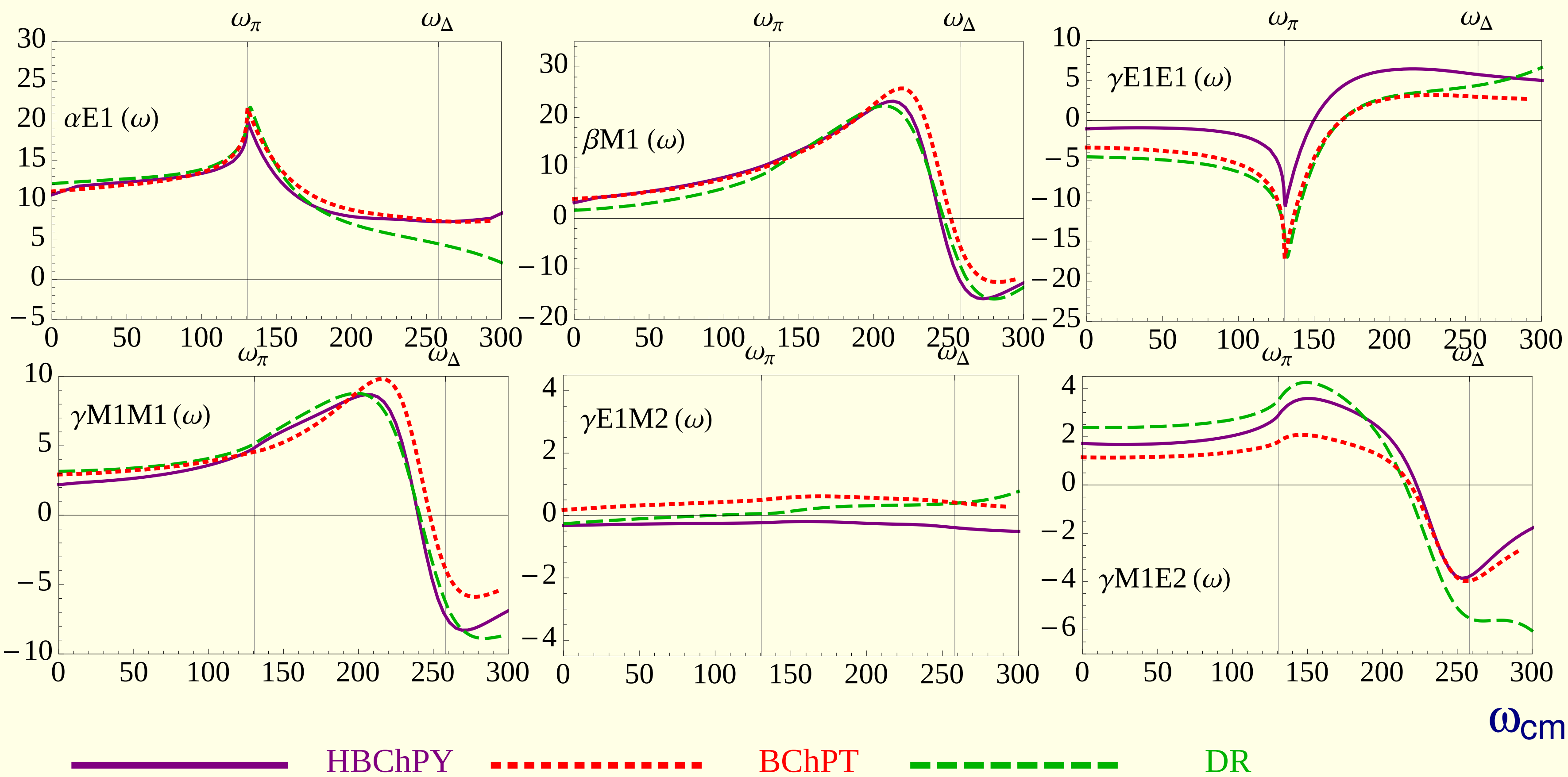
Aside: Comparison of Multipoles

Different predictions do not fully agree on the physical origins of the polarisabilities. But Chiral and DR predictions agree very well for the shape of the energy dependence of corresponding multipoles



DR: Hildebrandt *et al.* , Eur. Phys. J. A **20** 293 (2004) Chiral: JMcG *et al.* , V Lensky *et al.* in preparation

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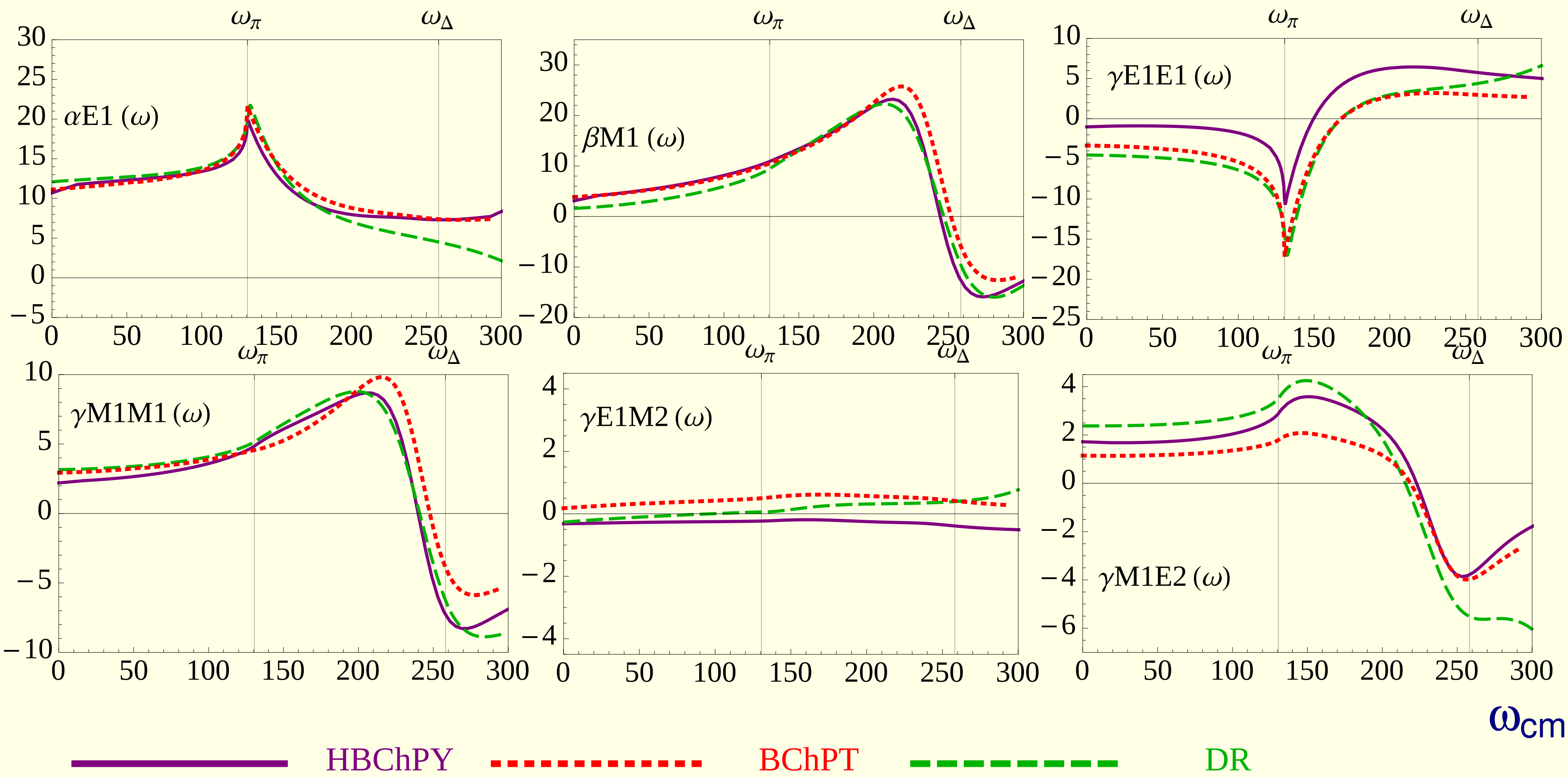

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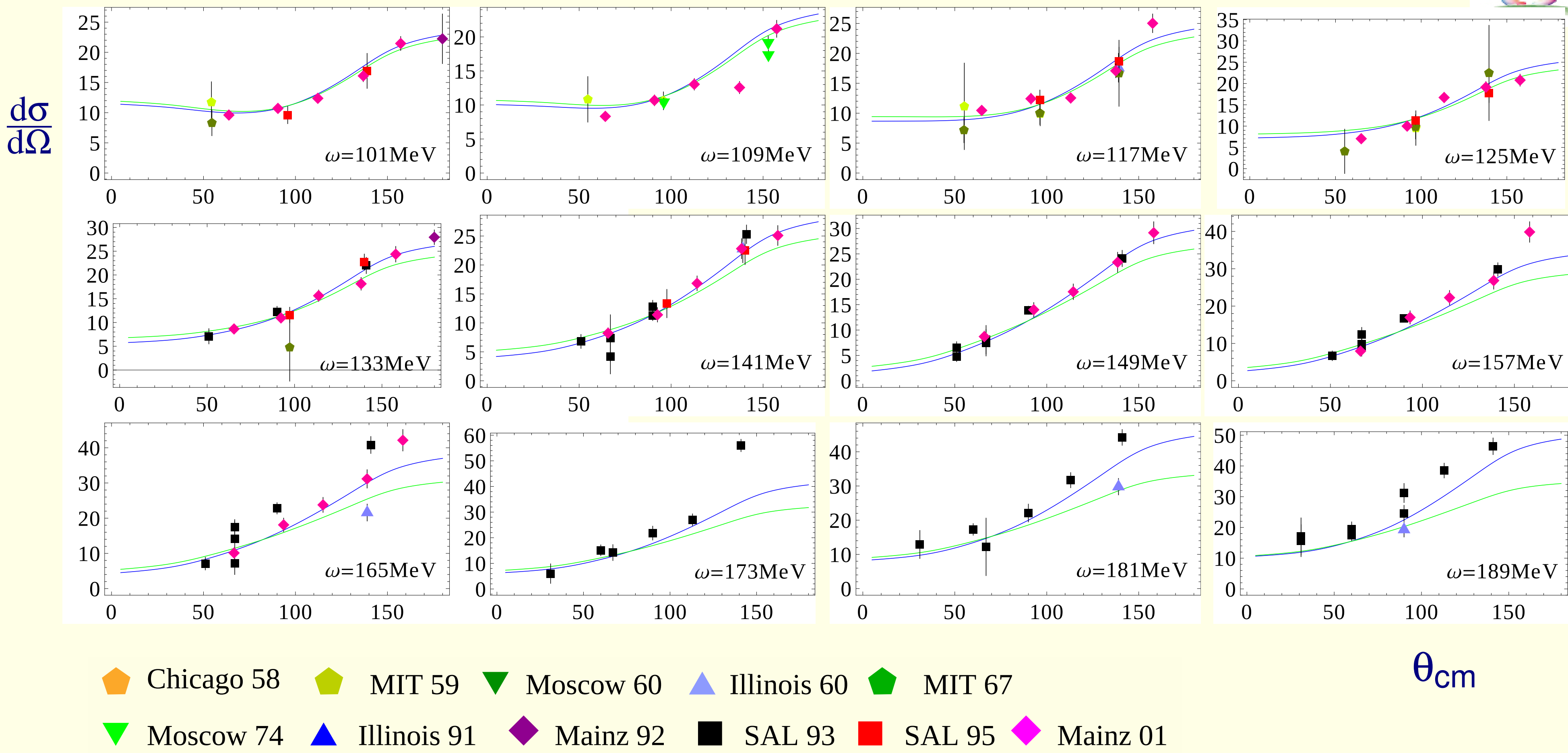
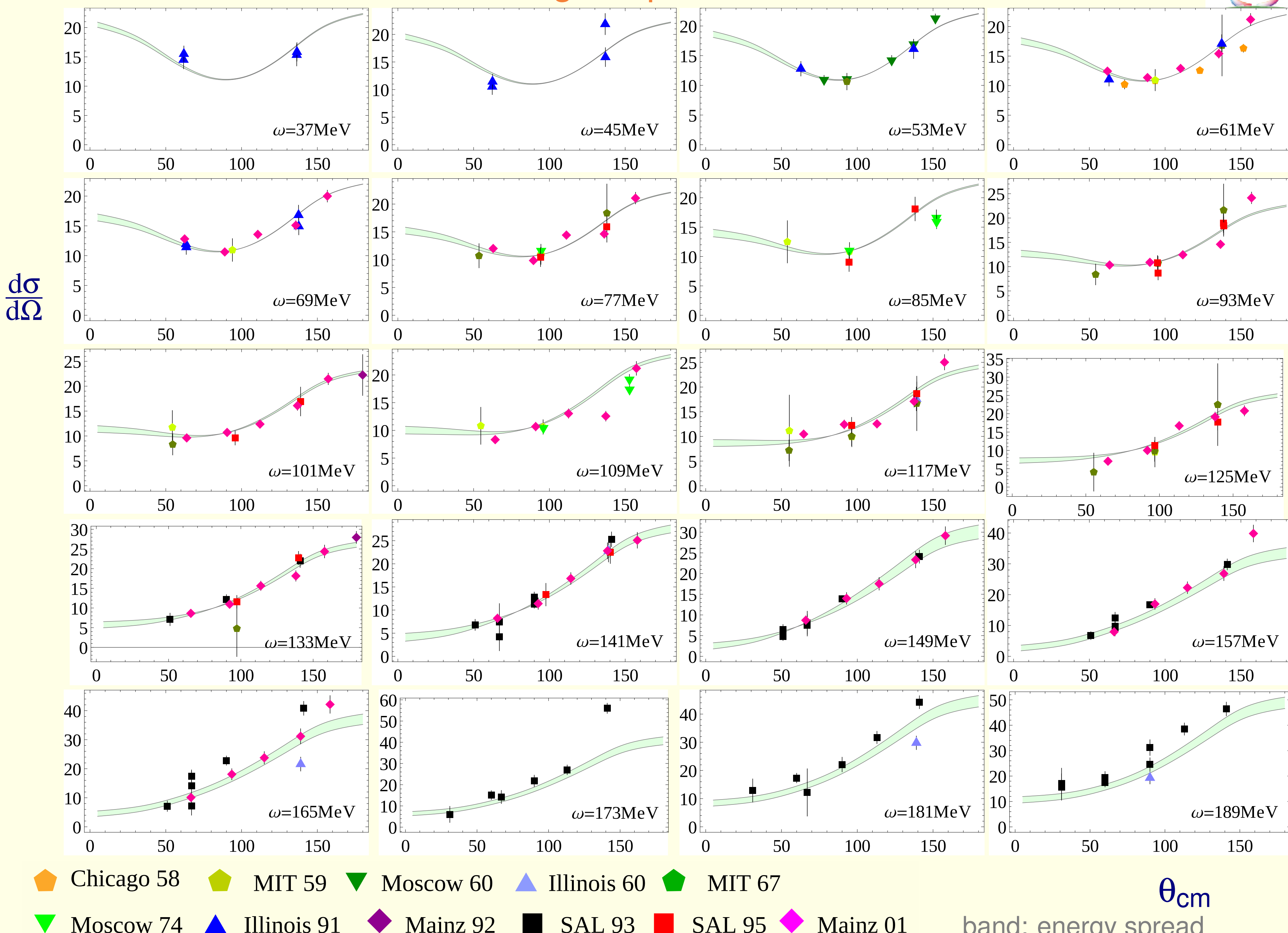
Our strategy: Static polarisabilities best obtained from Compton scattering.

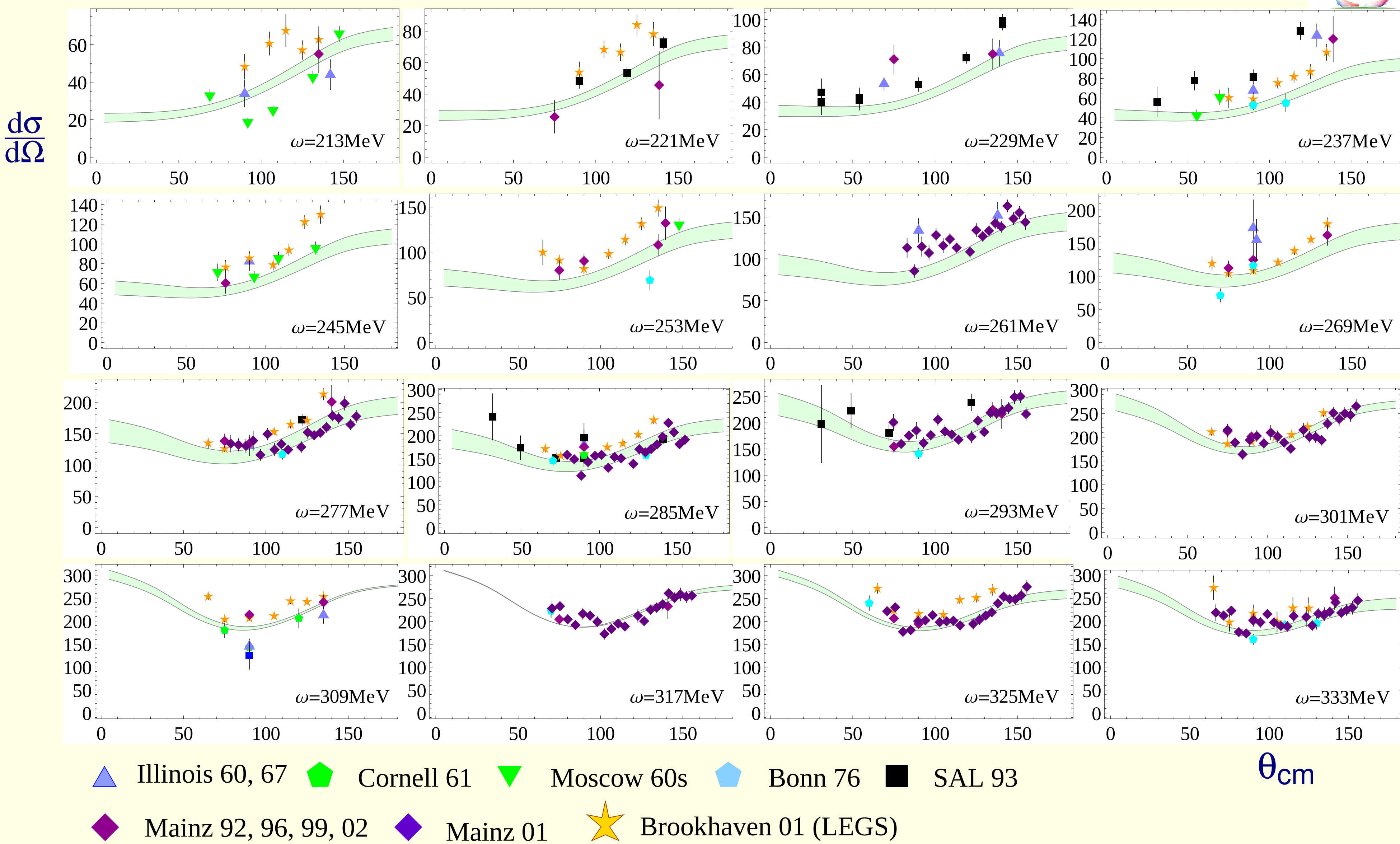
Effects of Delta



Δ significant from around 140MeV upward—especially at backward angles

Fitting the proton data





band gives spread of theory curve due to energy binning

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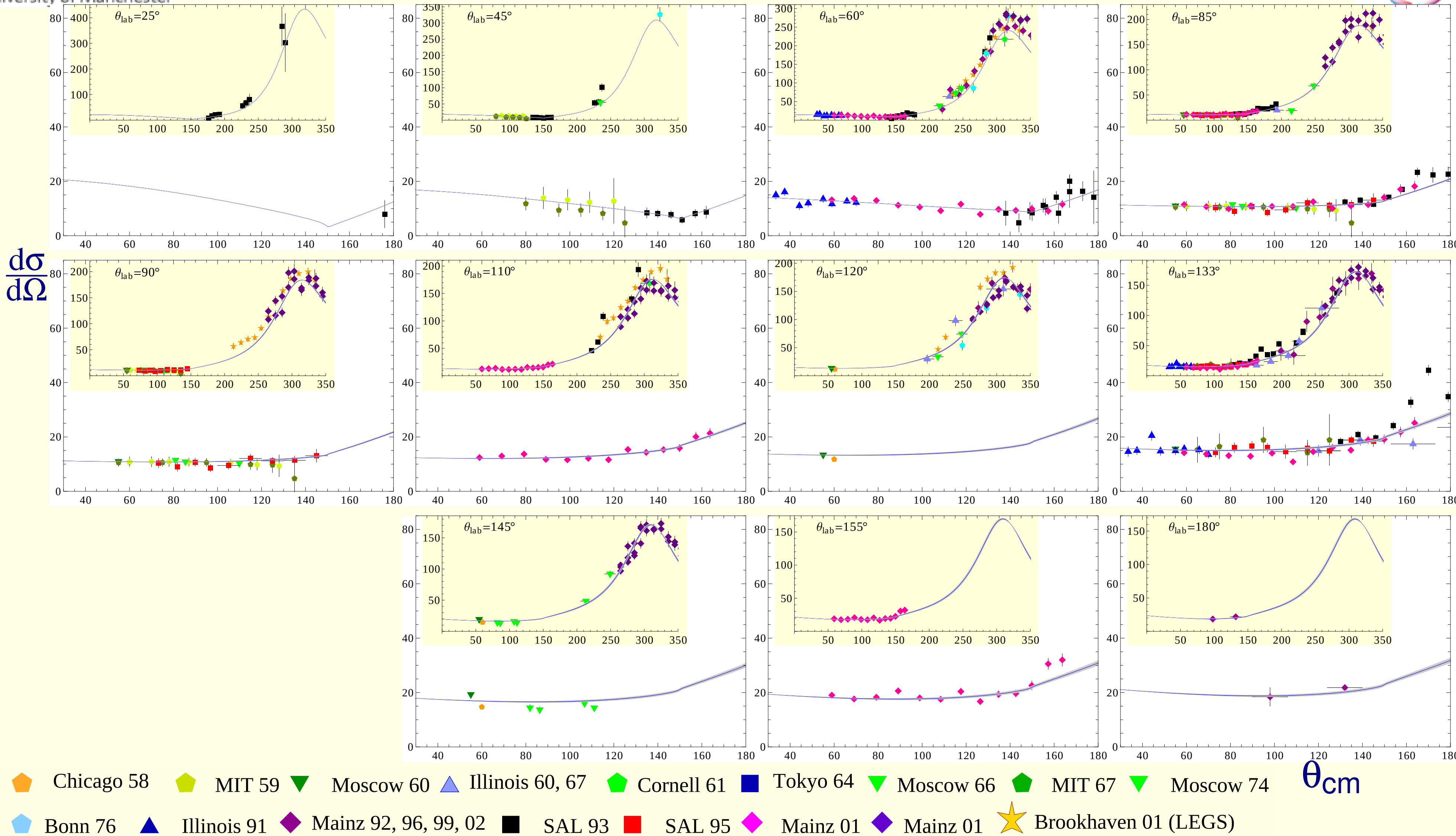

Constraining $\alpha+\beta$ with Baldin Sum rule and fitting consistent data set up to 170 MeV:

$$\alpha_p = (10.65 \pm 0.35(\text{stat}) \pm 0.2(\text{Bald}) \pm 0.3(\text{theory})) \times 10^{-4}\,\text{fm}^3$$

$$\beta_p = (3.15 \mp 0.35(\text{stat}) \pm 0.2(\text{Bald}) \mp 0.3(\text{theory})) \times 10^{-4}\,\text{fm}^3$$

Comparison

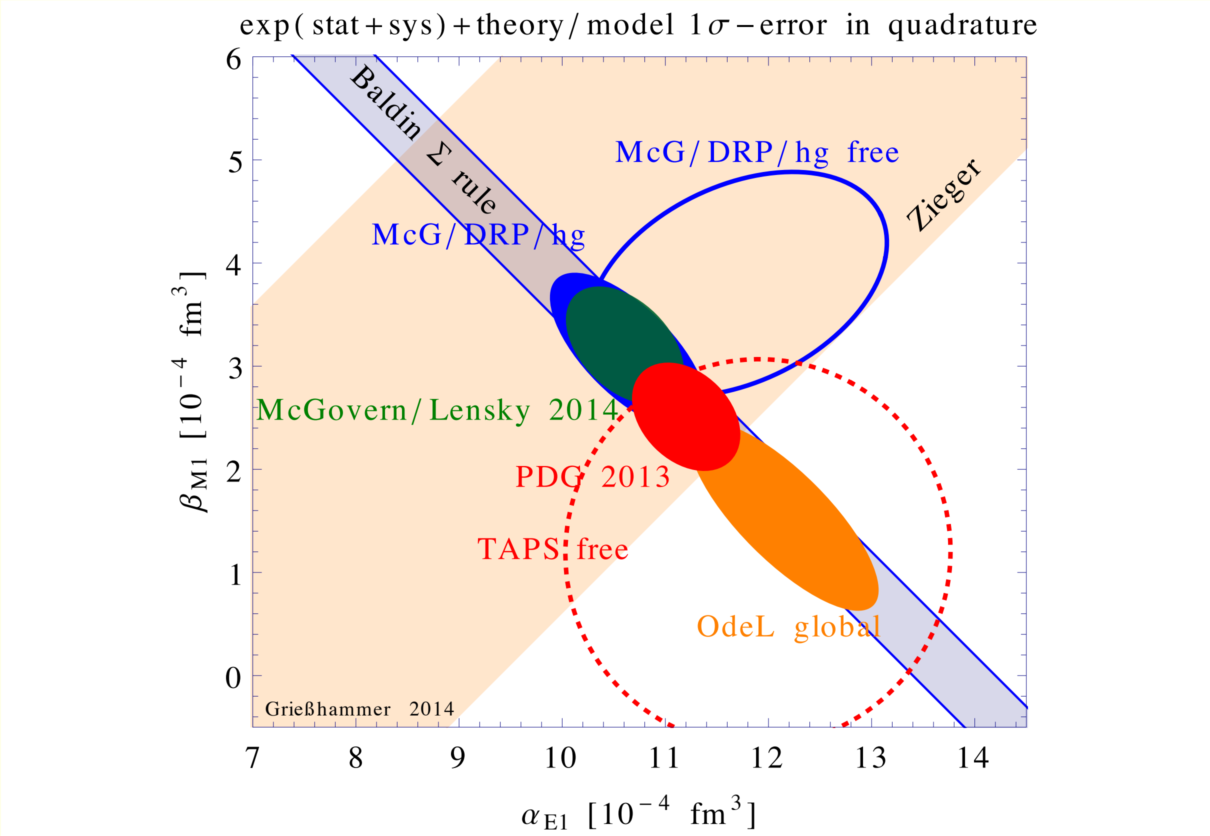

figure courtesy of H. Grießhammer

Details of fit

Resonance region—very sensitive to magnetic γNΔ coupling ($\sim g_M^4$). We iteratively fit g_M; value 10% lower than fit to photo production.

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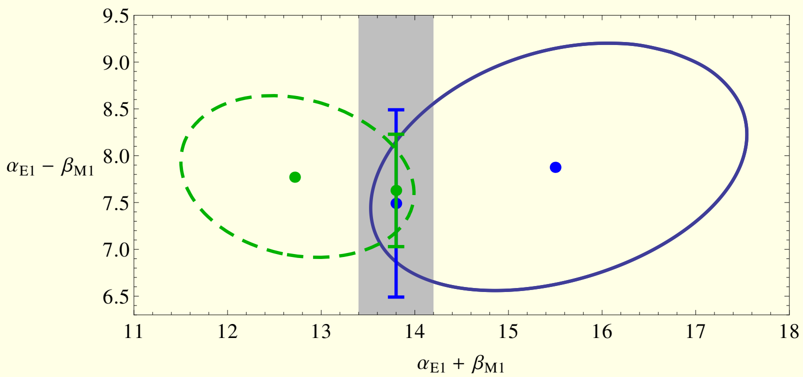
We FIT it to give $\gamma_{M1M1} = 2.2 \pm 0.5(\text{stat})$. Final fit good: χ^2=113.2 for 135 d.o.f.

4th-order statistical errors on $\alpha - \beta$ are larger than 3rd order.



Deduce theory error from convergence:

LO ($O(e^2\delta)$, BKM) $\alpha - \beta = 11.25$

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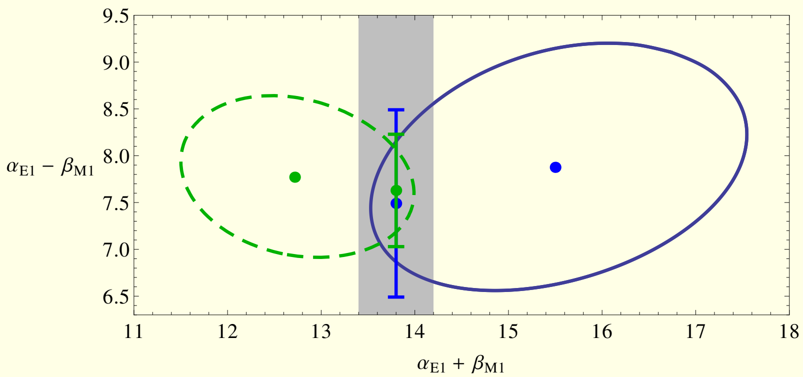

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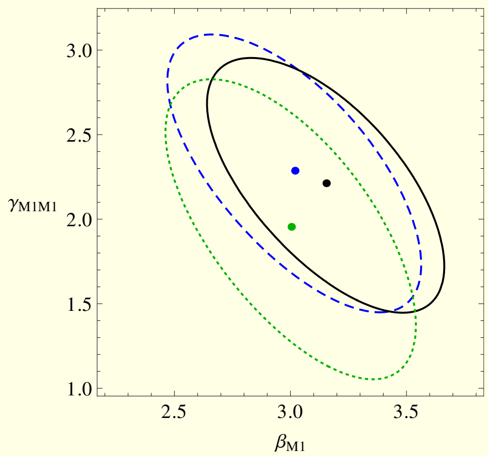
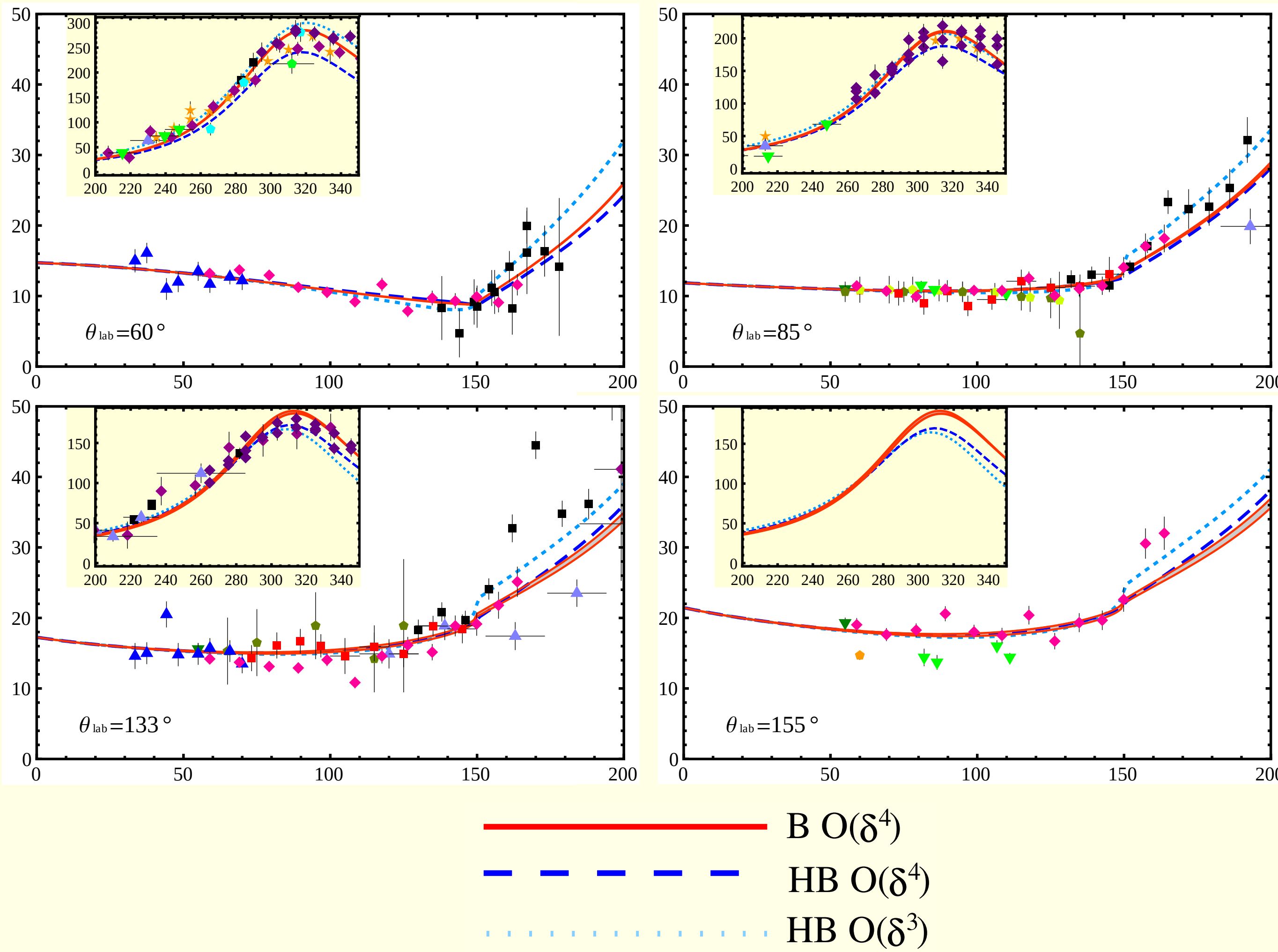


Also check sensitivity to data: need to be somewhat selective of old data sets to get a good χ^2, can't fit Hallin data above 150MeV.

Checking in covariant framework (3rd order)



$$\alpha_p = (10.6 \pm 0.25(\text{stat}) \pm 0.2(\text{Bald}) \pm 0.4(\text{theory})) \times 10^{-4}\,\text{fm}^3$$
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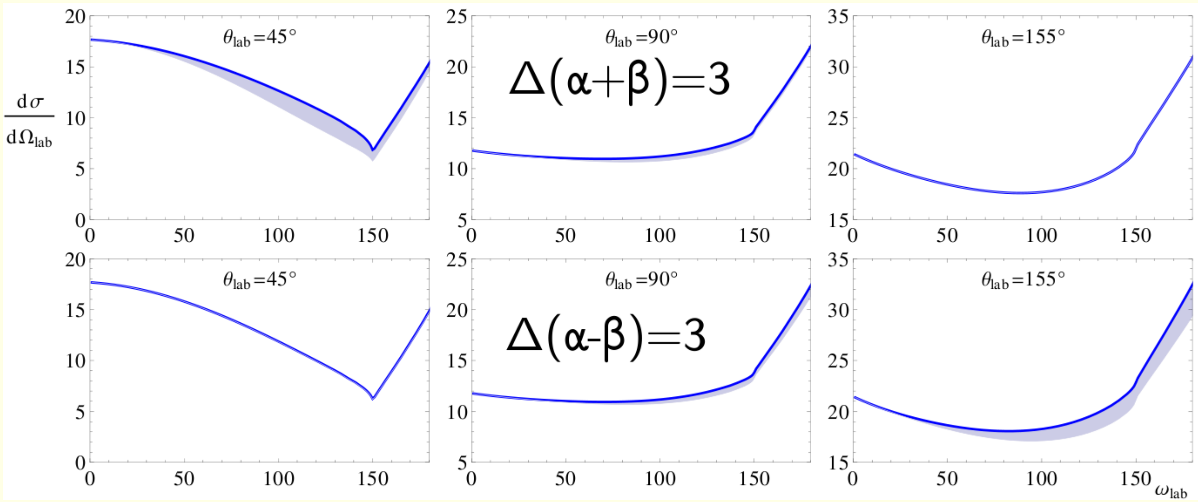
V. Lensky & JMcG Phys. Rev. **C89** 032202 (2014) ; V. Lensky *et al.* Phys. Rev. **C86** 048201 (2012)

More data needed?

We fit to low-energy data (up to 180-200 MeV), but with constraints from the higher-energy data to ensure the Δ parameters are sensible.

In spite of the amount of data, the sensitivity to the polarisabilities especially β is not very high. Magnetic response varies rapidly with energy and zero-energy value is only a small fraction of the total by 150 MeV.

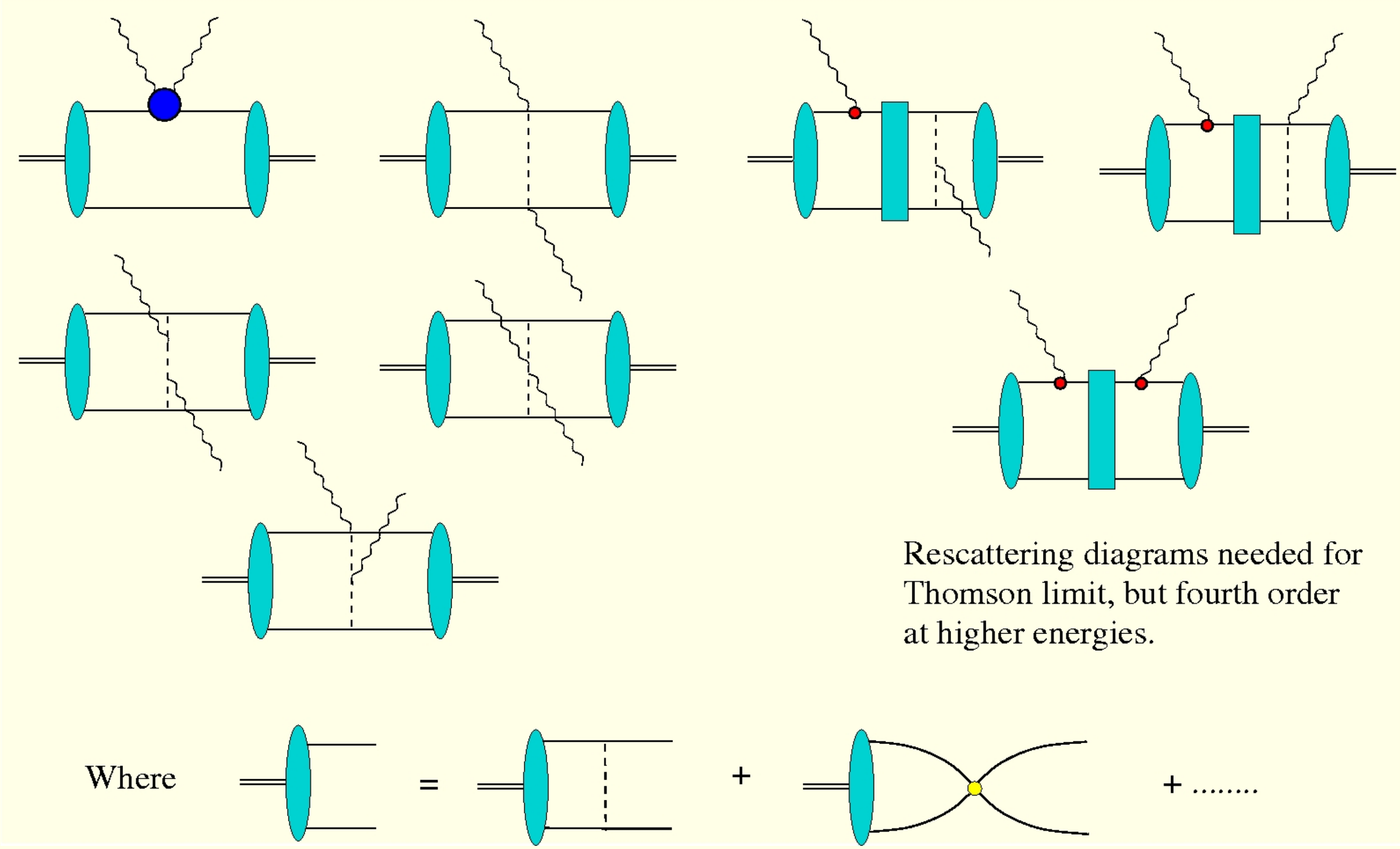


What would help

- Better data! (Theorist's view...)
- More data in the region 160-250 MeV
- More data at forward and backward angles
- Data for polarised scattering (beam and target)

Deuteron

Consistent treatment of one- and two-body diagrams



The Δ only enters in  at this order.

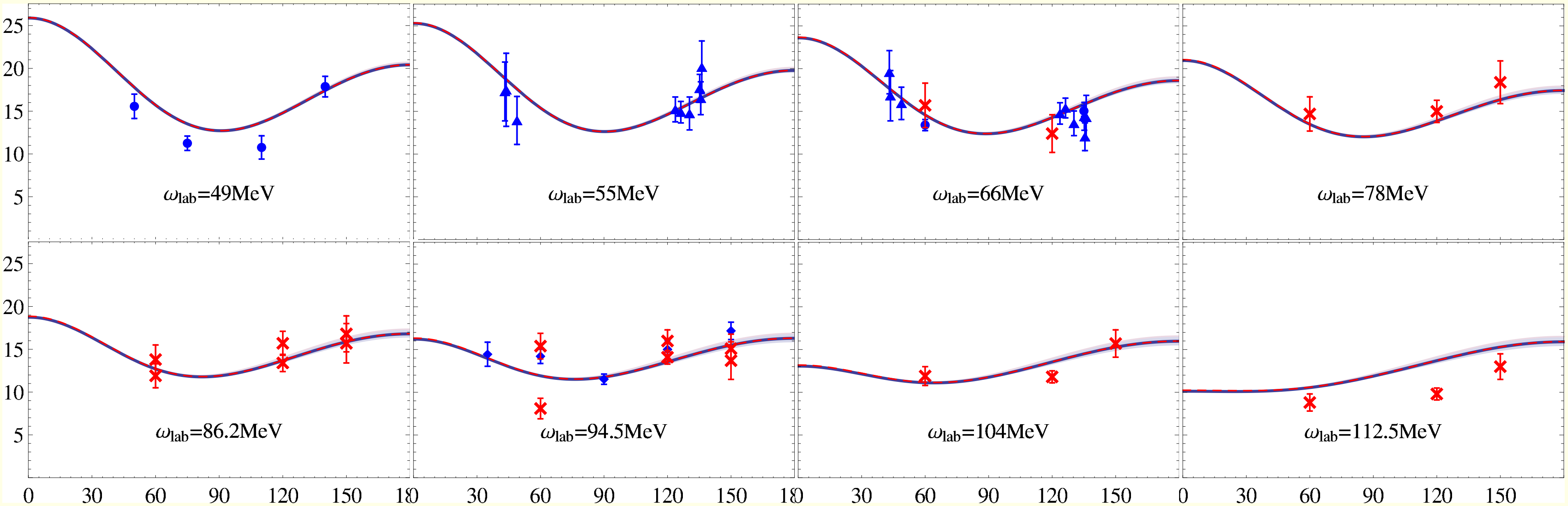
Ensuring correct Thomson limit for deuteron is important even at 50-60 MeV.

Extraction of isoscalar polarisabilities

So far only $O(Q^3)$; further work required to go above pion threshold.

Older data from Illinois ●, Saskatoon, ◆ and Lund ▲ (29 pts in total)

New data from Lund ×, 23 points. Myers *et al.* , Phys. Rev. Lett. **113,** 262506 (2014)



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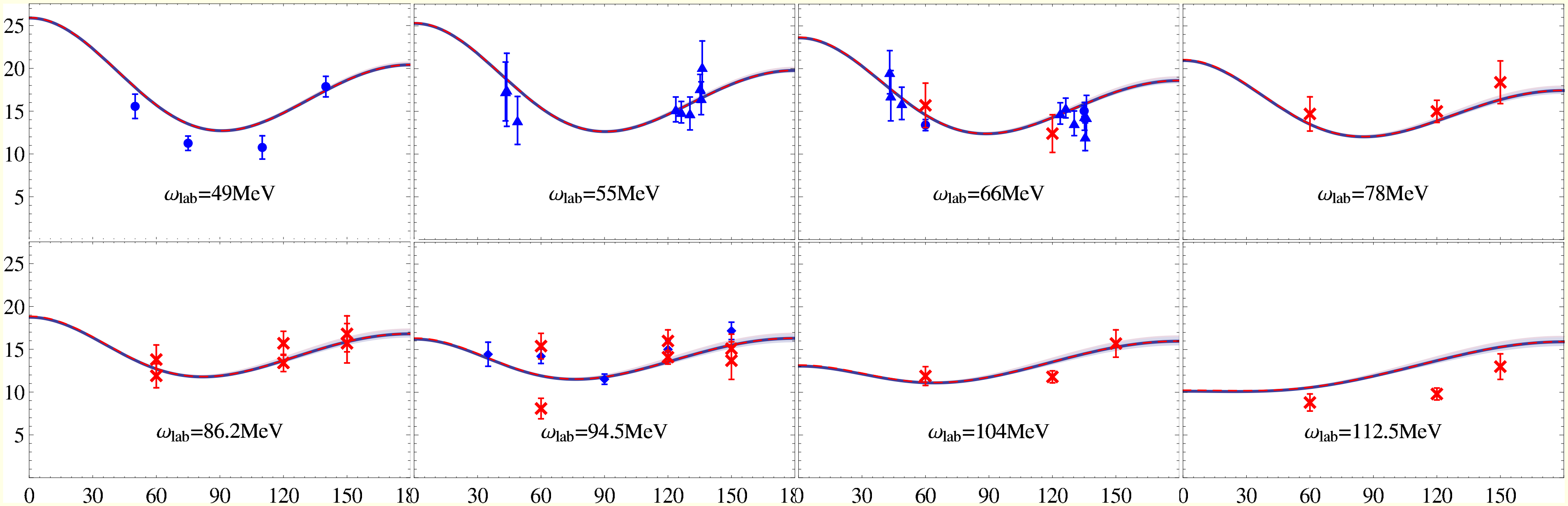


$$\alpha_s = 11.1 \pm 0.6(\text{stat}) \pm 0.2(\text{BSR}) \pm 0.8(\text{th})$$
$$\beta_s = 3.4 \mp 0.6(\text{stat}) \pm 0.2(\text{BSR}) \mp 0.8(\text{th}).$$

$$\alpha_n = 11.65 \pm 1.25(\text{stat}) \pm 0.2(\text{BSR}) \pm 0.8(\text{th})$$
$$\beta_n = 3.55 \mp 1.25(\text{stat}) \pm 0.2(\text{BSR}) \mp 0.8(\text{th})$$

Comparison

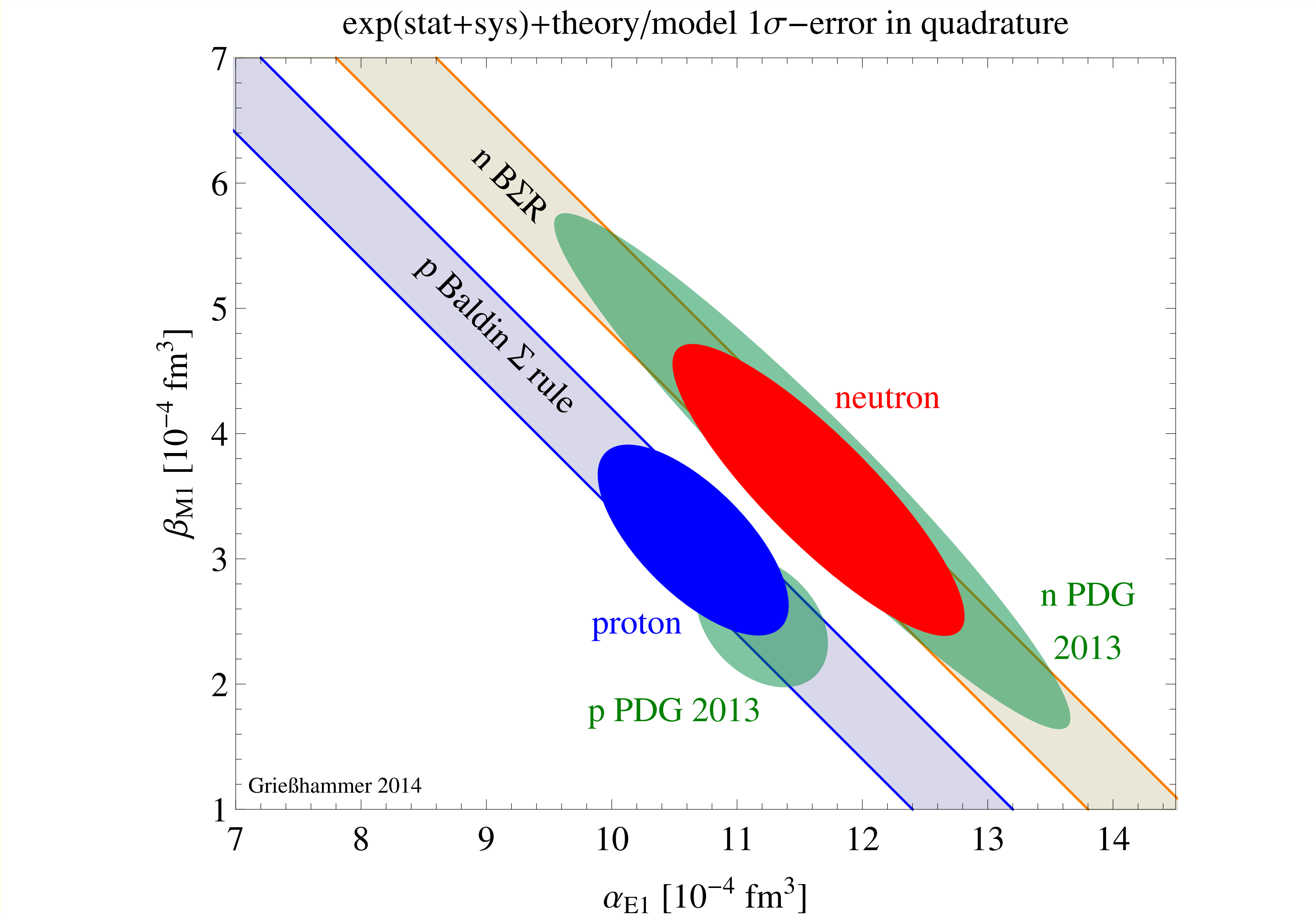
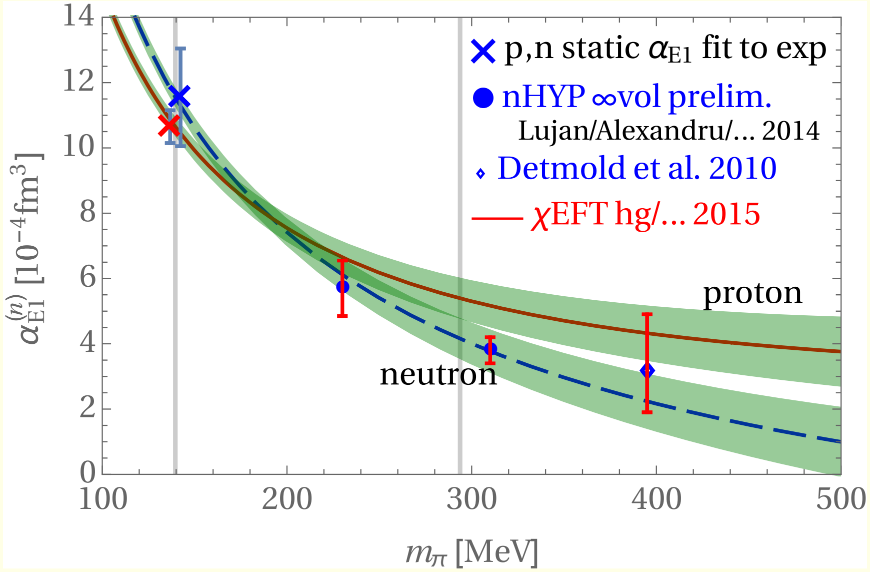
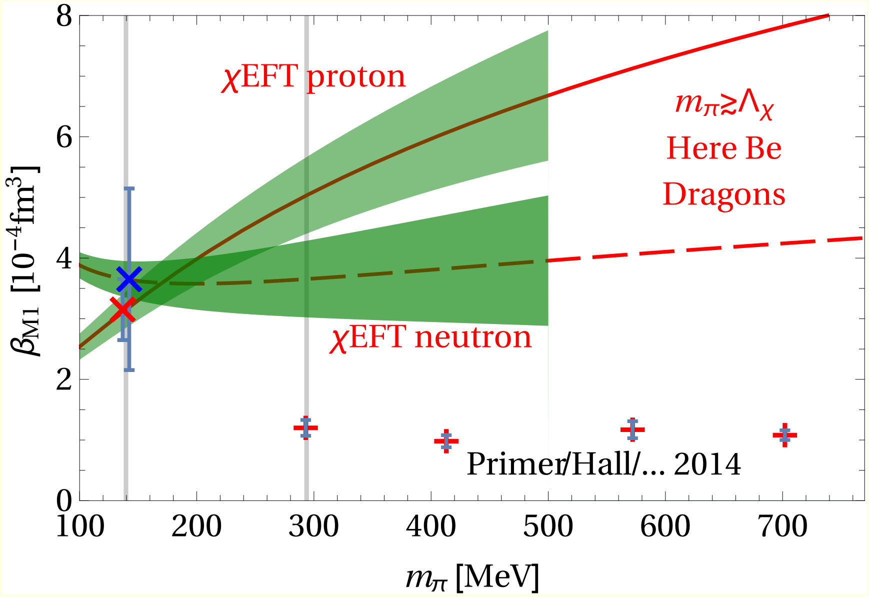


figure courtesy of H. Grießhammer

Lattice and chiral extrapolations





figures courtesy of H. Grießhammer

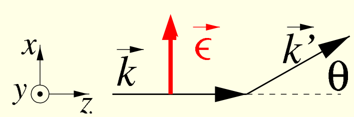
Spin-dependent Compton scattering

$$H_{\text{eff}} = \frac{(\mathbf{p}-Q\mathbf{A})^2}{2m} + Q\phi - \frac{(Q+\kappa)}{2m}\sigma\cdot H - \frac{1}{2}4\pi\left(\alpha\vec{E}^2 + \beta\vec{H}^2\right.$$
$$\left. + \gamma_{E1}\vec{\sigma}\cdot\vec{E}\times\dot{\vec{E}} + \gamma_{M1}\vec{\sigma}\cdot\vec{H}\times\dot{\vec{H}} - 2\gamma_{E2}E_{ij}\sigma_i H_j + 2\gamma_{M2}H_{ij}\sigma_i E_j\right)$$

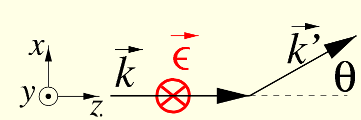
Spin-polarisabities have most influence if the beam or target or both are polarised.

Linearly polarised beam $\Sigma_3 = \dfrac{\sigma^{\parallel}-\sigma^{\perp}}{\sigma^{\parallel}+\sigma^{\perp}}$

$\left[\dfrac{d\sigma}{d\Omega}\right]^{\text{lin}}_x$:

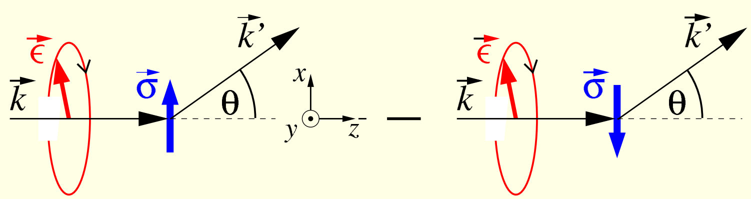


$\left[\dfrac{d\sigma}{d\Omega}\right]^{\text{lin}}_y$:

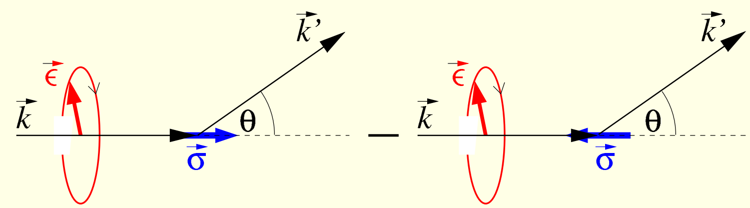


Circular beam, polarised target $\qquad \Sigma_{2x} = \dfrac{\sigma^R_{\perp}-\sigma^L_{\perp}}{\sigma^R_{\perp}+\sigma^L_{\perp}} \qquad \Sigma_{2z} = \dfrac{\sigma^R_{\parallel}-\sigma^L_{\parallel}}{\sigma^R_{\parallel}+\sigma^L_{\parallel}}$

Δ_x^{circ}:

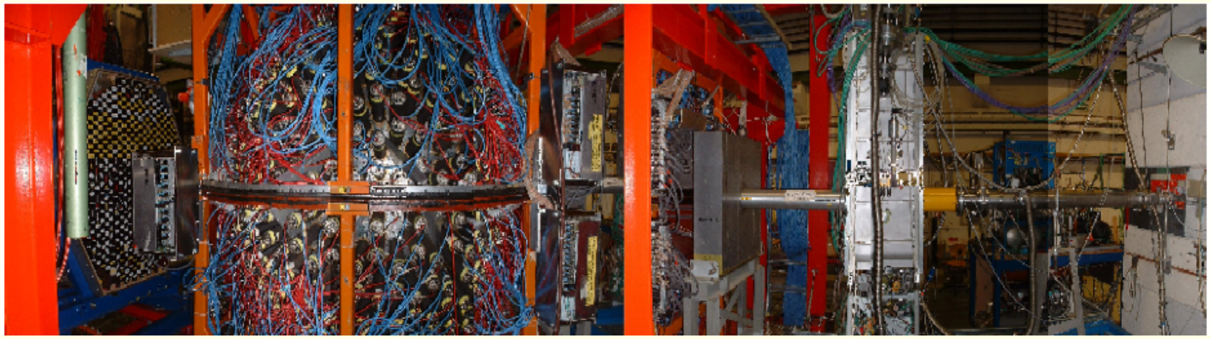


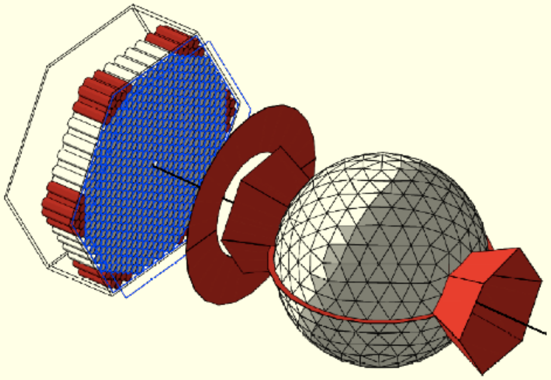
Δ_z^{circ}:



Compton @MAMI

New programme at A2 experiment using Crystal Ball and TAPS detectors

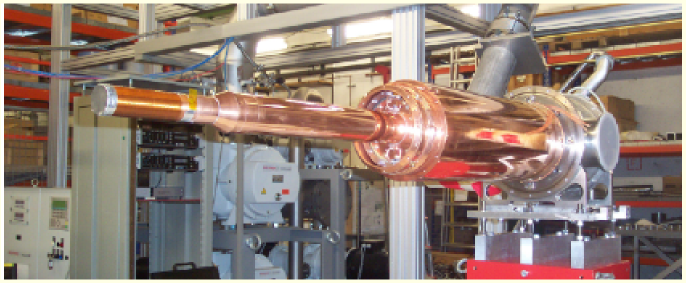




Large-acceptance detector

Tagged photon beam, circ. or lin. polarised or unpolarised,

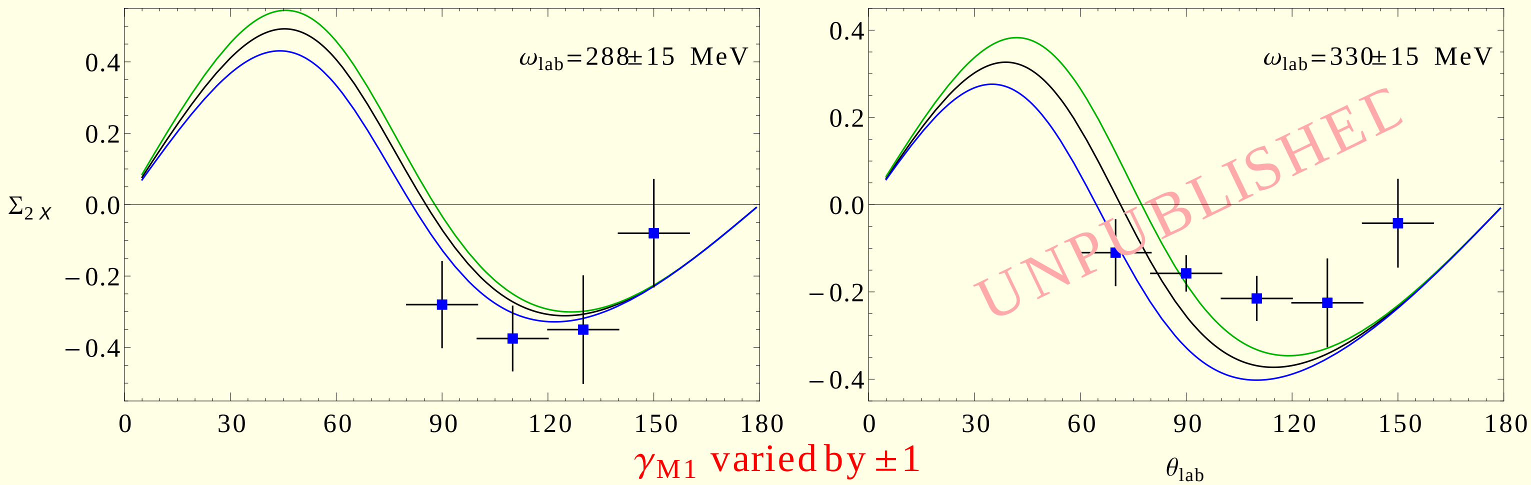
Unpolarised (liquid hydrogen)...



or polarised (butanol) protons

First results from MAMI

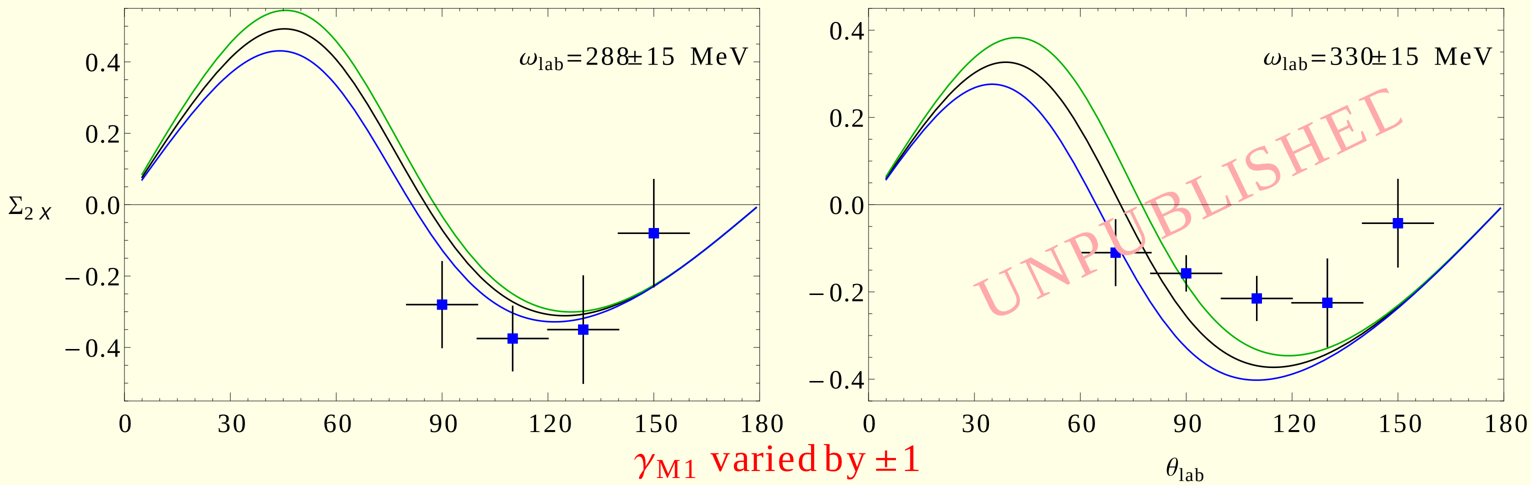
Σ_{2x}: Target polarised perpendicular to reaction plane, RH or LH circularly polarised photons P. Martell, PhD thesis



γ_{M1} varied by ±1

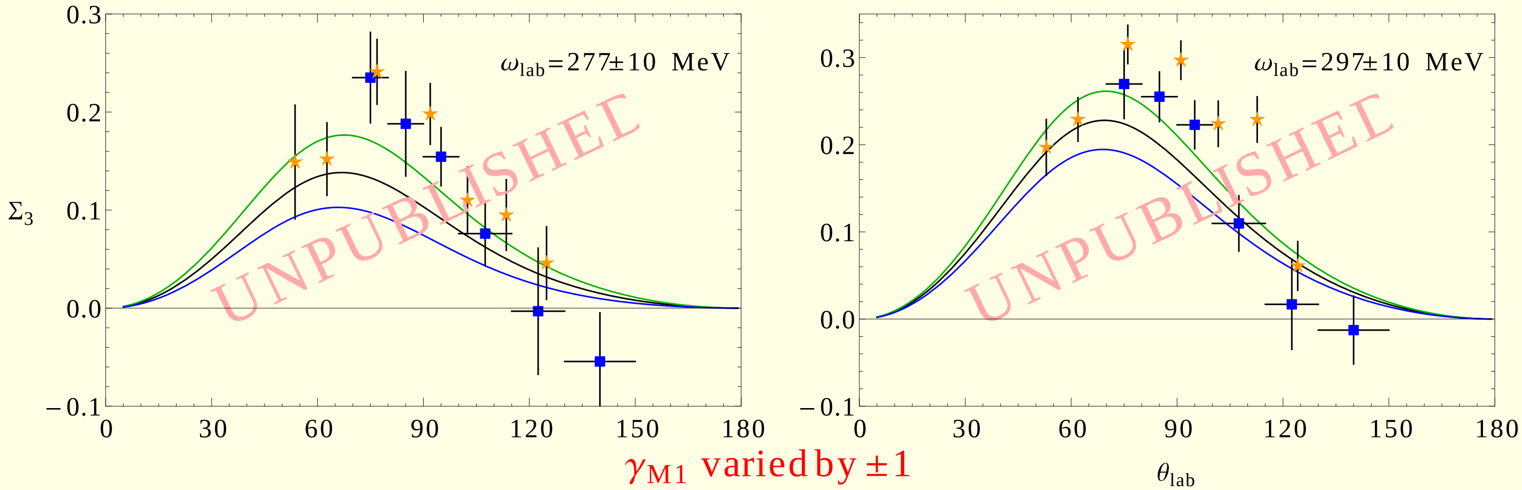
First results from MAMI

Σ_{2x}: Target polarised perpendicular to reaction plane, RH or LH circularly polarised photons P. Martell, PhD thesis



Σ_3: Unpolarised target, photons polarised in or perpendicular to reaction plane

■ C. Collicott, PhD thesis (LEGS data ☆)



Predictions and fits for proton polarisabilities

Chiral prediction (δ^3, BChPT, Lensky) and NLO (δ^4, HBChPT, JMcG) papers pending

	$\alpha+\beta$	$\alpha-\beta$	γ_0	γ_π
δ^3 B	15.1	7.3	-0.9	$[-46.4]+7.2$
δ^4 HB	13.8 ± 0.4	$7.5\pm0.7\pm0.6$	-2.6^*	$[-46.4]+5.5^*$
SR/DR	13.8 ± 0.4	10.7 ± 0.2	-0.9 ± 0.14	$[-46.4]+7.6\pm1.8$

DR: fixed-angle, Drechsel *et al.* Phys. Rep. **378** 99;

	γ_{E1E1}	γ_{M1M1}	γ_{E1M2}	γ_{M1E2}
δ^3 B	-3.4	3.0	0.2	1.1
δ^4	-1.1 ± 1.8	$2.2\pm0.5_{\text{stat}}\pm0.7^*_{\text{th}}$	-0.4 ± 0.4	1.9 ± 0.4
DR	-3.85 ± 0.45	2.8 ± 0.1	-0.15 ± 0.15	2.0 ± 0.1
MAMI1	-3.5 ± 1.2	3.2 ± 0.9	-0.7 ± 1.2	2.0 ± 0.3
MAMI2	-5.0 ± 1.5	3.1 ± 0.9	1.7 ± 1.7	1.3 ± 0.4

DR: fixed-t, summarised in HG, JMcG, DP & GF Prog. Nucl. Part. Phys. **67** 841 (2012)

MAMI1: published extraction from MAMI Σ_{2x} and LEGS Σ_3 Martel

MAMI2: unpublished extraction from Σ_{2x} and Σ_3 Collicott

δ^4: theory errors from convergence. *: γ_{M1M1} from fit, otherwise $\gamma_{M1M1}=6.4$

Note errors mean different things in different lines; DR especially only reflect spred from two databases

Predictions and fits for neutron polarisabilities

Chiral prediction (δ^3, BChPT, Lensky) and NLO (δ^4, HBChPT, JMcG) papers pending

	$\alpha+\beta$	$\alpha-\beta$	γ_0	γ_π
δ^3 B	18.3	9.1	0	$[46.4]+8.9$
δ^4 HB	15.2 ± 0.4	$8.1\pm2.5\pm0.8$	0.5^*	$[46.4]+7.7^*$
SR/DR	15.2 ± 0.4	11.5	-0.25	$[46.4]\pm13.35$

DR: fixed-t, Drechsel *et al.* Phys. Rep. **378** 99;

	γ_{E1E1}	γ_{M1M1}	γ_{E1M2}	γ_{M1E2}
δ^3 B	-4.7	2.9	0.2	1.5
δ^4	-4.0 ± 1.8	$1.3\pm0.5_{\text{stat}}\pm0.7^*_{\text{th}}$	-0.1 ± 0.4	2.4 ± 0.4
DR	-5.75 ± 0.15	3.8 ± 0.1	-0.8 ± 0.1	3.0 ± 0.1

DR: fixed-t, Holstein *et al.* , Babusci *et al.*

δ^4: theory errors as proton. *: including input from proton fit.

But not just polarisabilities

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Σ_3: Unpolarised target, photons polarised in or perpendicular to reaction plane

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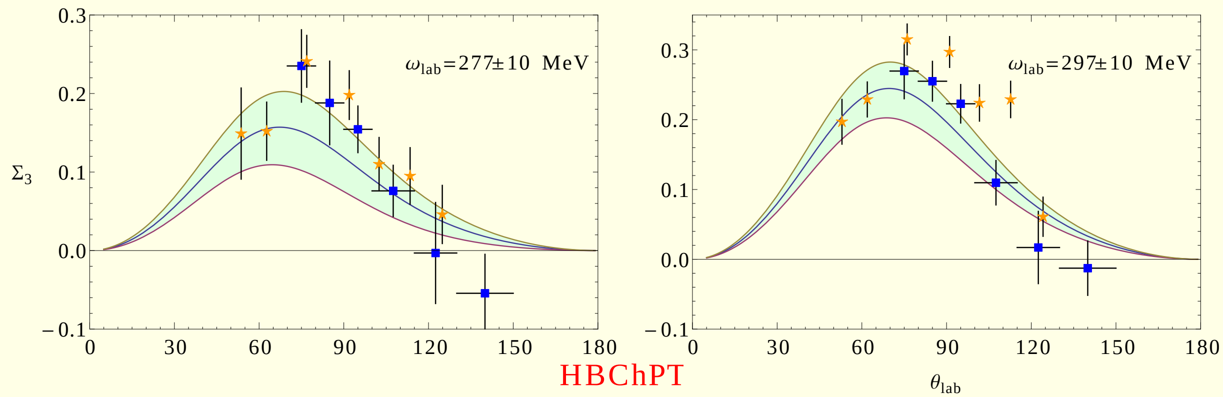

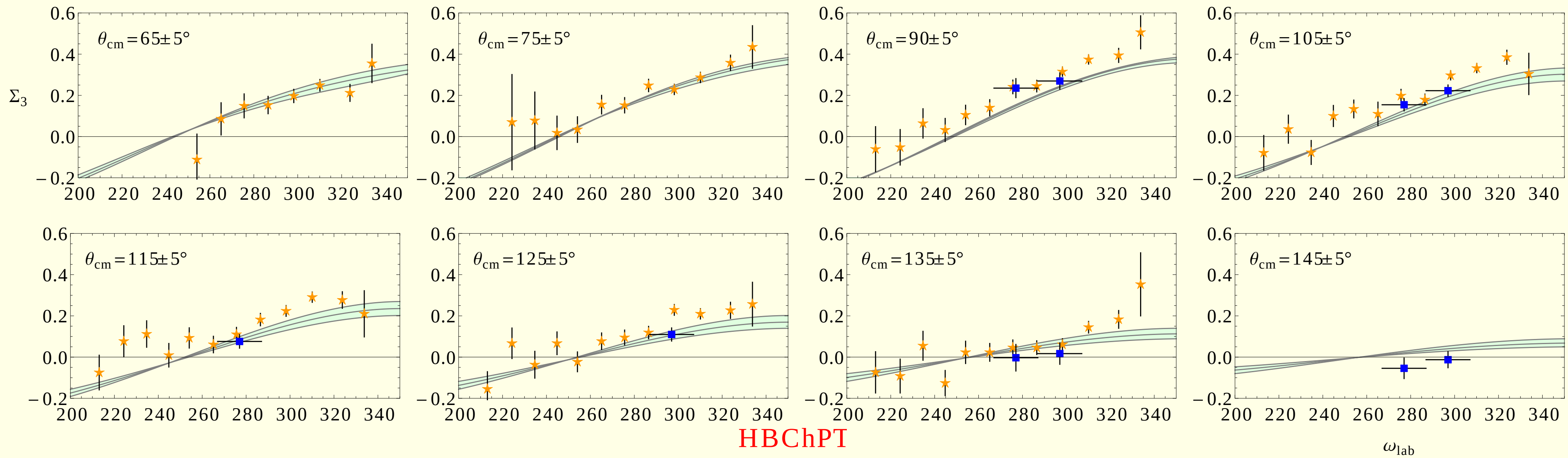

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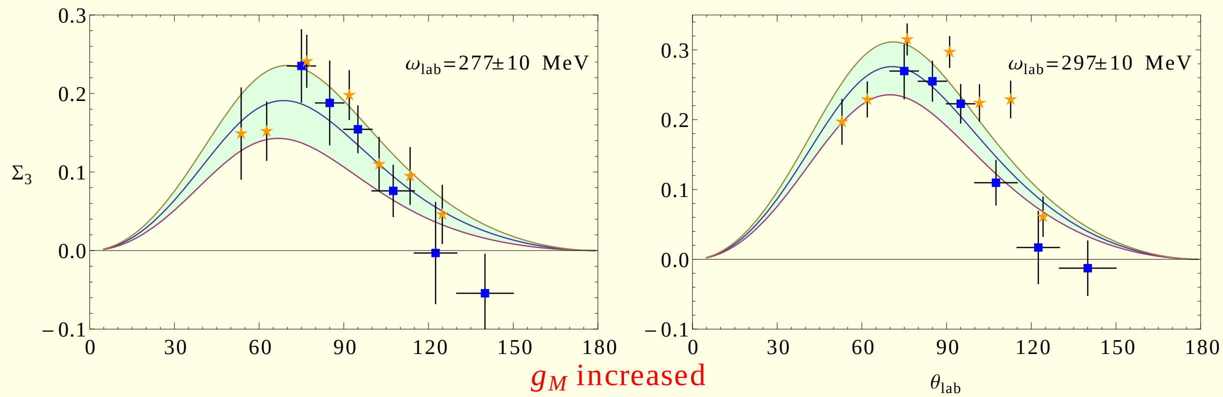

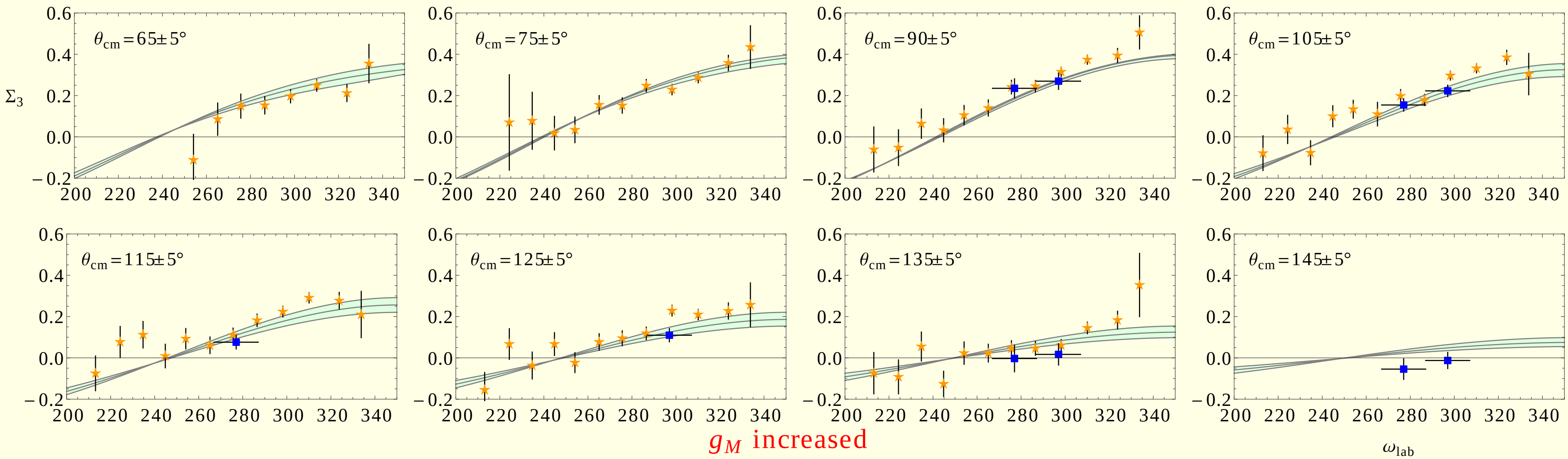

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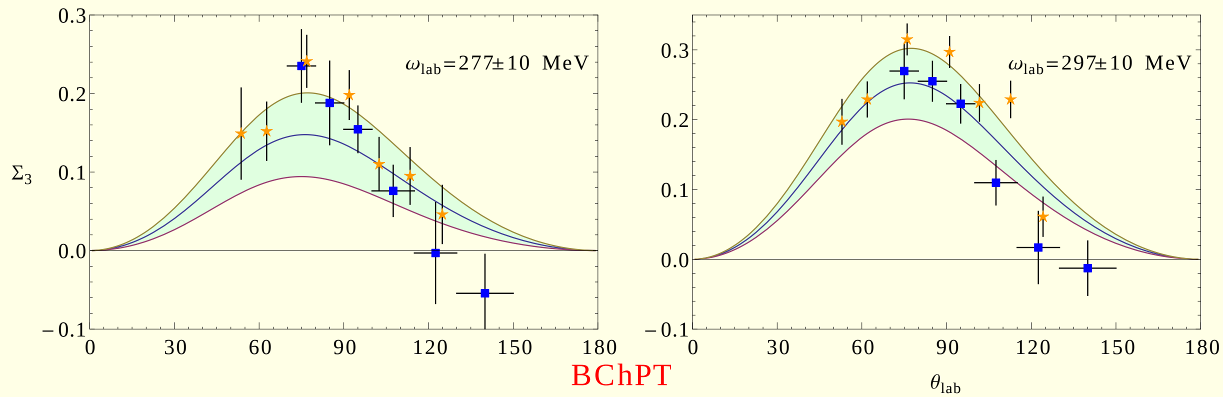
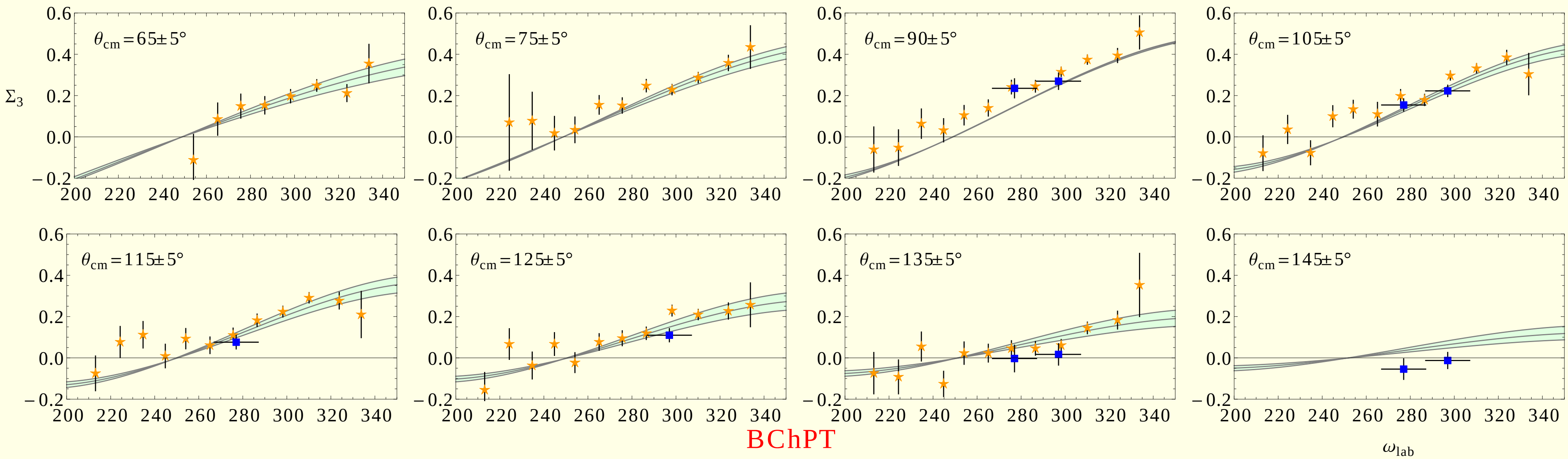
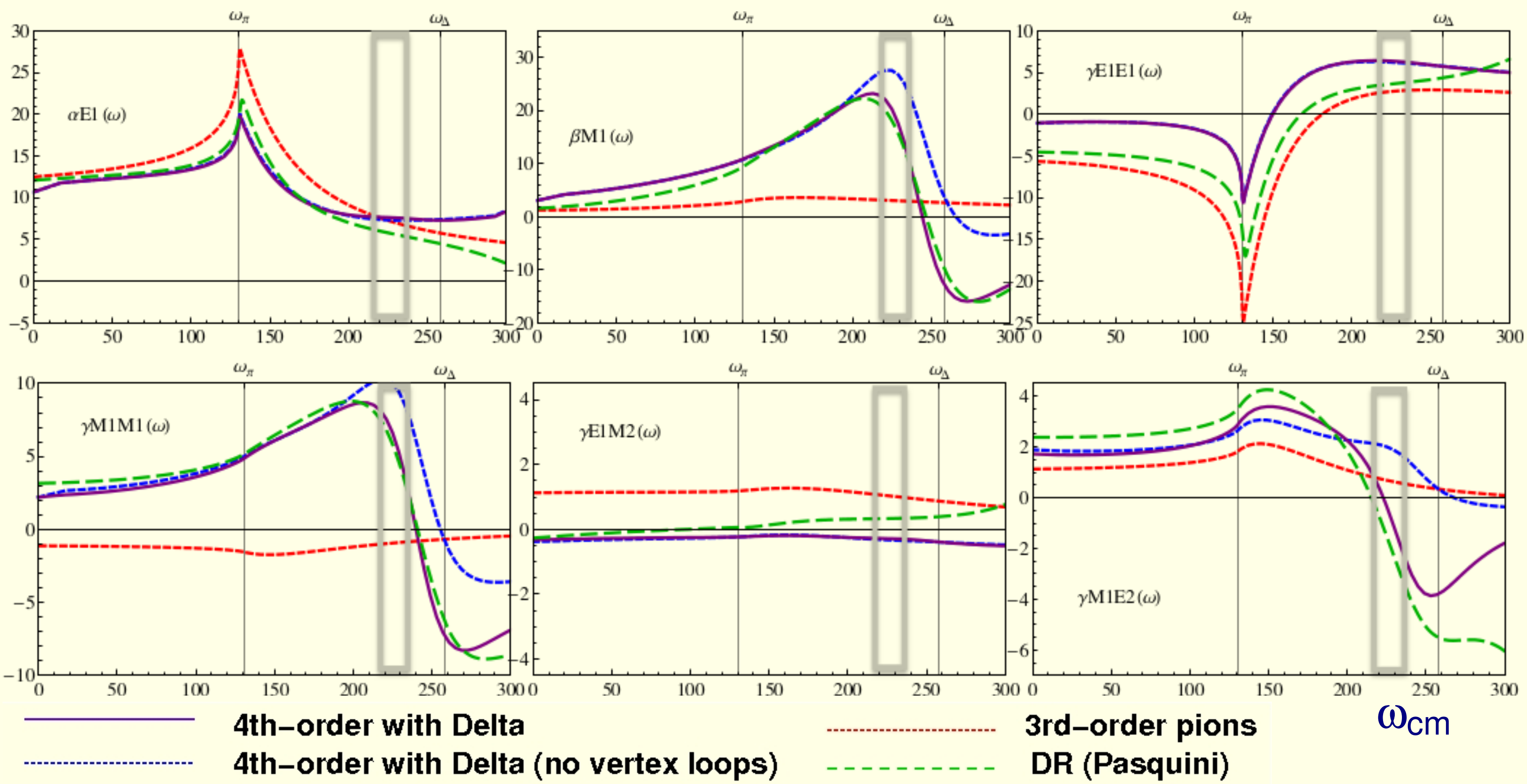




Multipoles again

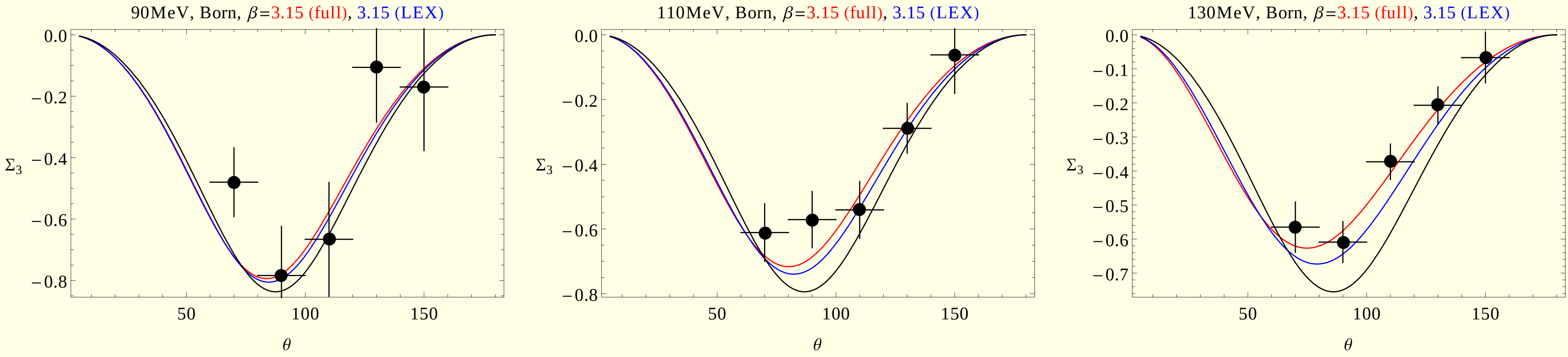
MAMI data is taken well into the resonance region....

Not ideal for extracting zero-energy polarisabilities!



Lower energy experiments

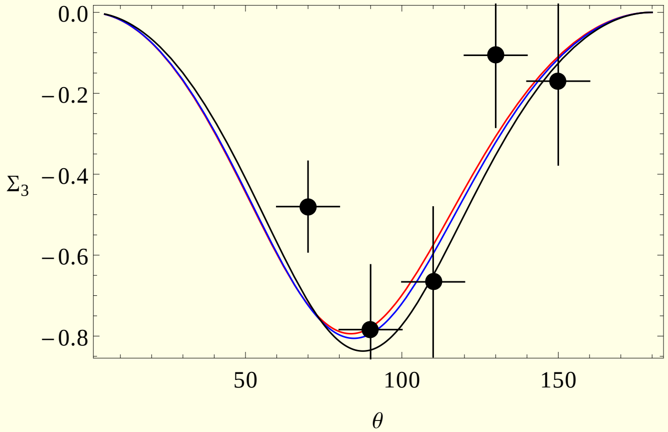
Some PRELIMINARY data on Σ_3 from MAMI V. Sokhoyan and E. Downie



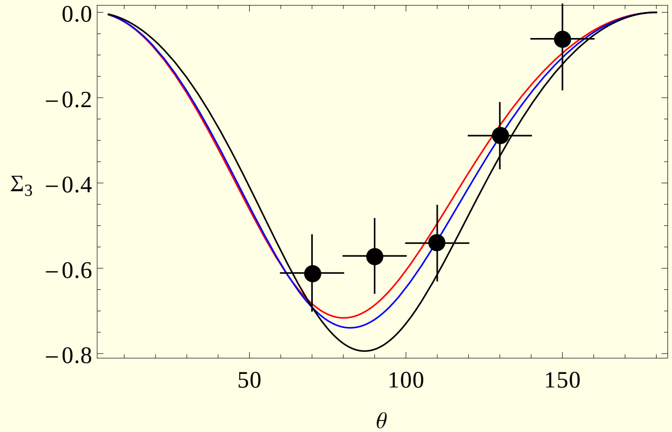
Lower energy experiments

Some PRELIMINARY data on Σ_3 from MAMI V. Sokhoyan and E. Downie

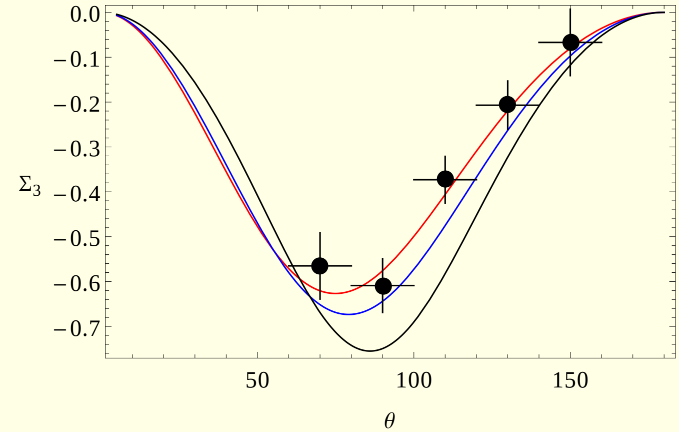
90MeV, Born, β=3.15 (full), 3.15 (LEX)



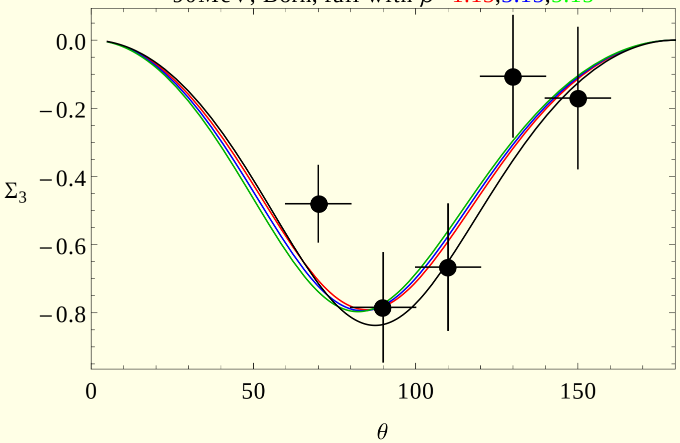
110MeV, Born, β=3.15 (full), 3.15 (LEX)



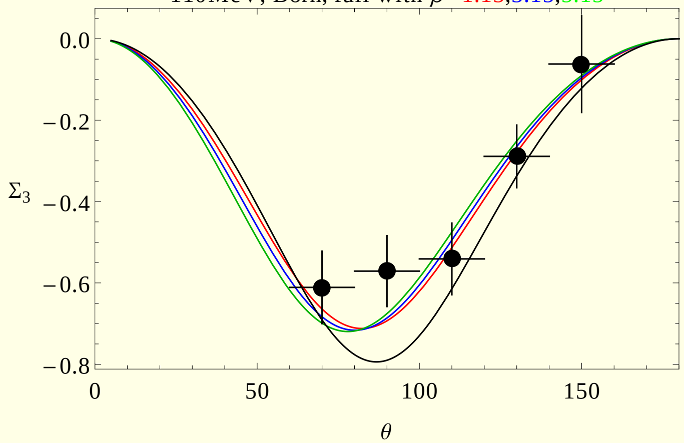
130MeV, Born, β=3.15 (full), 3.15 (LEX)



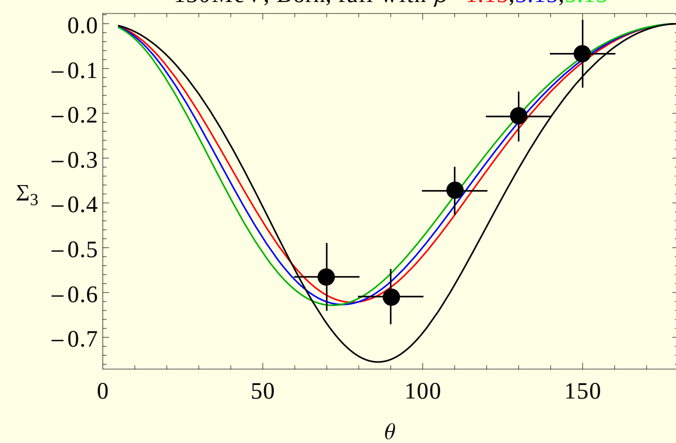
90MeV, Born, full with β=1.15,3.15,5.15



110MeV, Born, full with β=1.15,3.15,5.15



130MeV, Born, full with β=1.15,3.15,5.15



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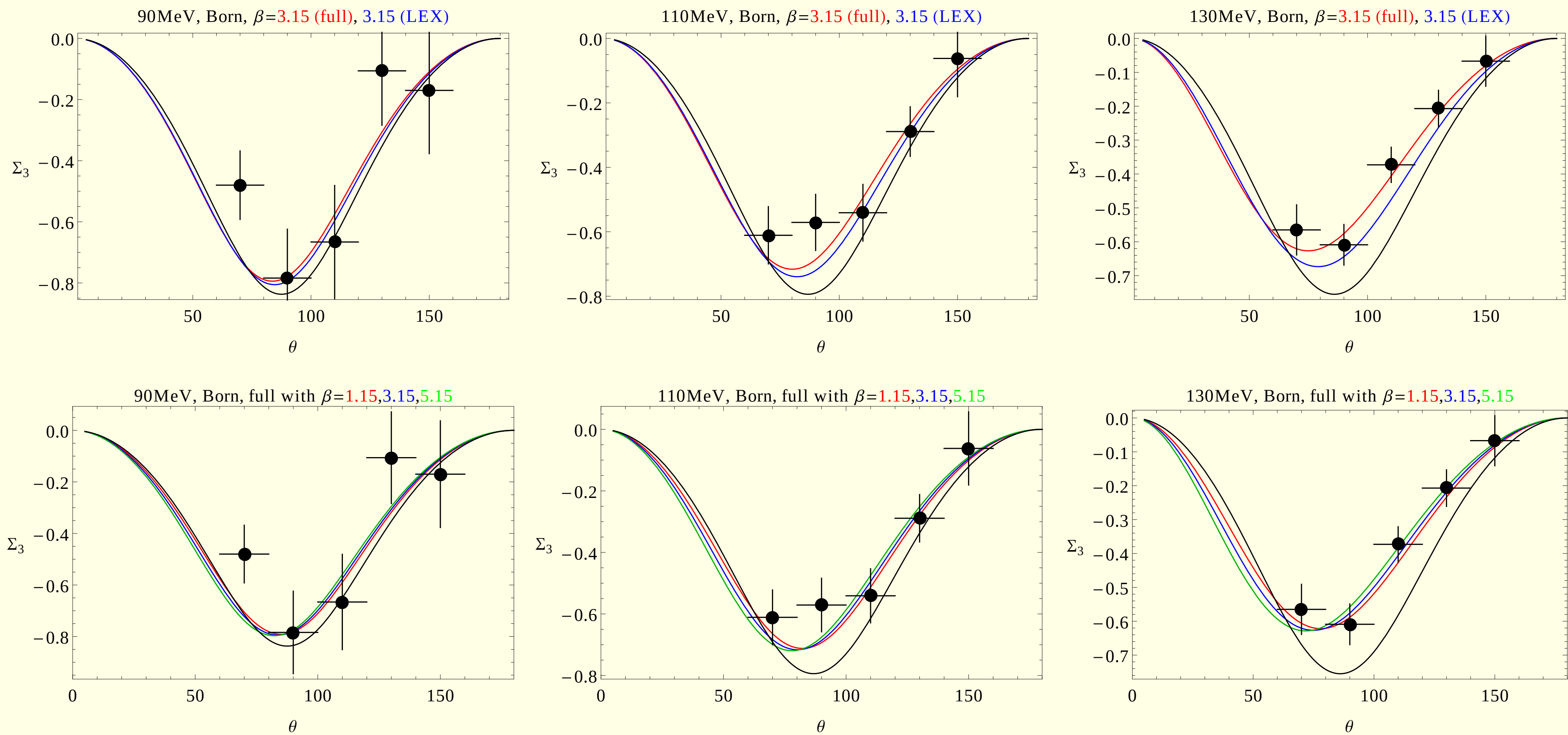
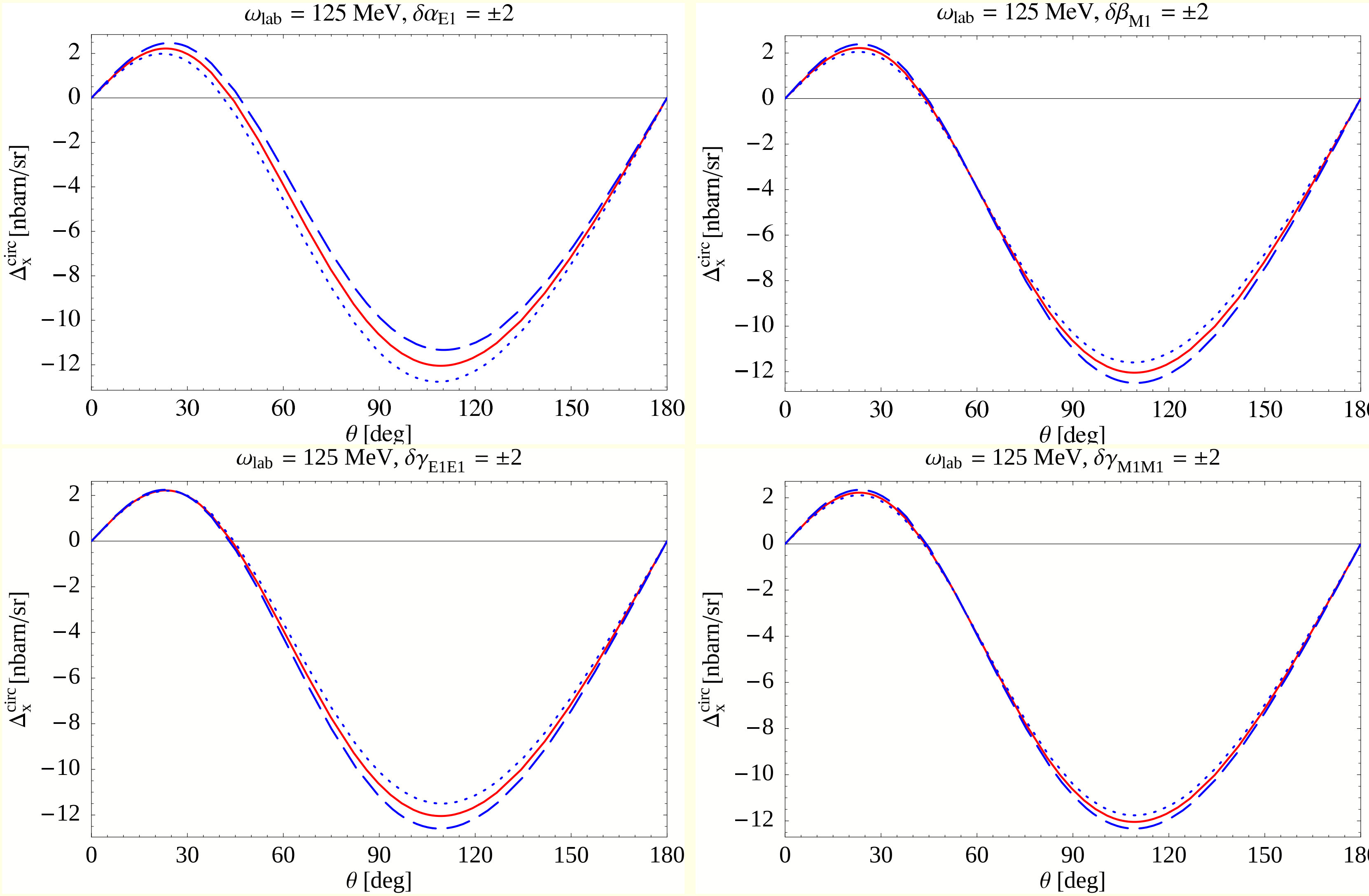


Experiments also planned at HIγS @TUNL

low energy–up to about 100 MeV currently, 150 MeV after upgrades.

Polarised scattering from deuterium

$$\Delta_x^{\text{circ}} = \frac{d\sigma}{d\Omega}_{\uparrow\rightarrow} - \frac{d\sigma}{d\Omega}_{\uparrow\leftarrow}$$



Δ included, 3rd order.

source: Griesshammer and Shukla Eur. Phys. J. A46:249, 2010

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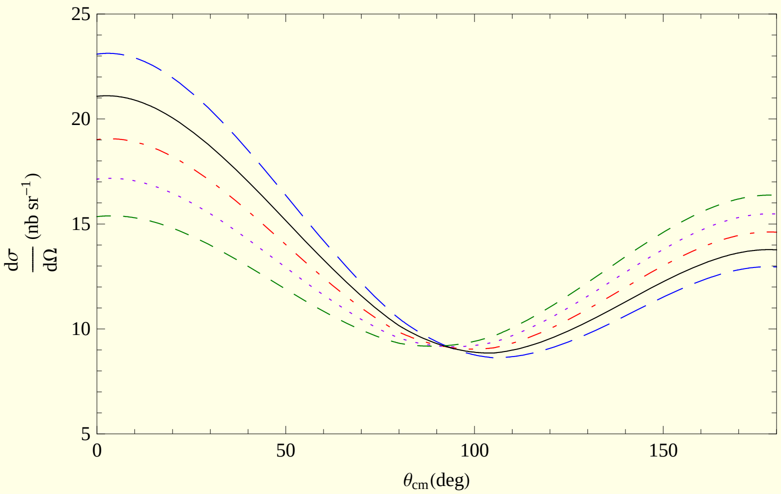
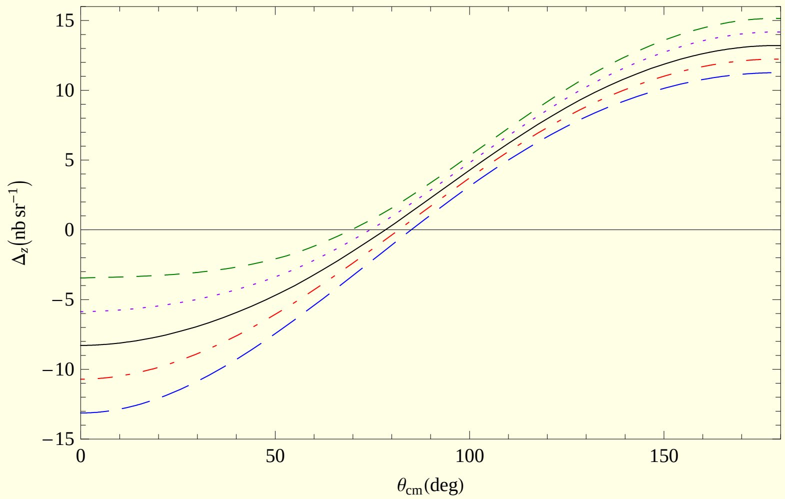
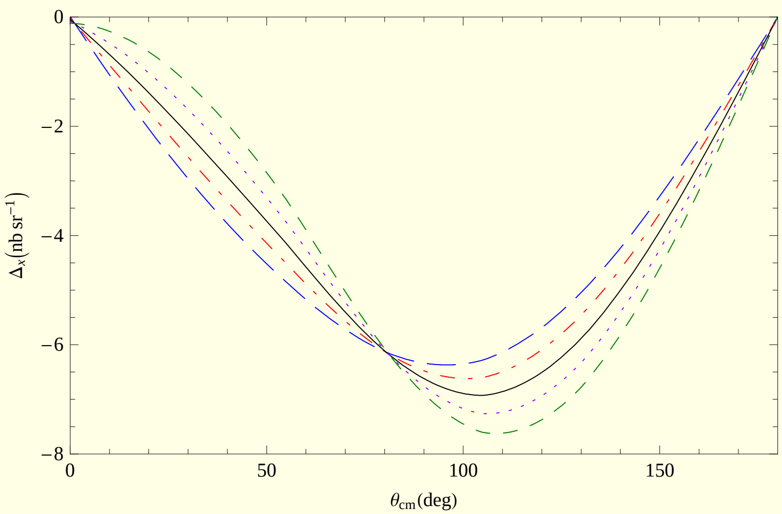
Polarised scattering from ^{3}He

Unpolarised, varying β_n

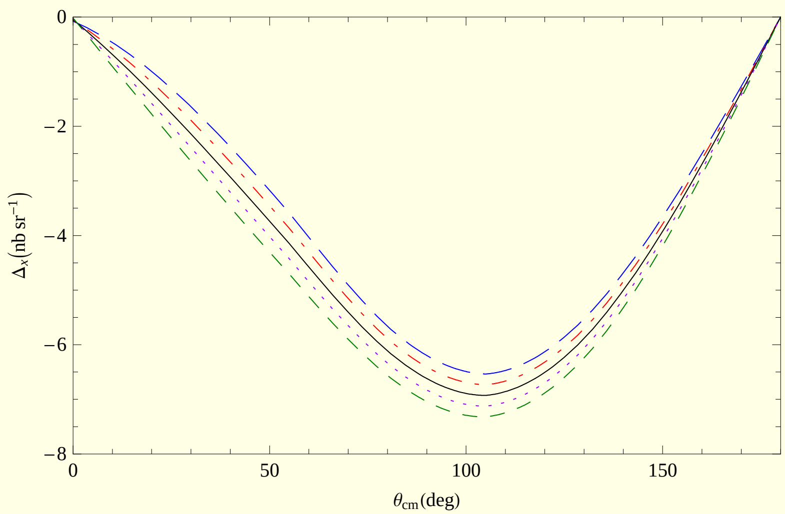


Δ_z, varying γ_{1n}





Δ_x, varying γ_{1n}



Δ_x, varying γ_{4n}

120 MeV, 3rd order, no Δ

source: Shukla, Nogga and Phillips Nucl. Phys. A 819 (2009) 98

Future

Experimental programme at MAMI, MAXlab and HIγS

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Polarised γp scattering at MAMI: data being analysed; 120 MeV data especially interesting for polarisabilities. Active target being developed for double-polarised experiments at low energies

Plans for ^{3}He

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Should soon know much more about the polarisabilities of the proton and neutron!

For more details....

See the slides of

Evie Downie Compton scattering and the nucleon polarizabilities

Gerald Feldman
New results for Compton scattering on deuterium: A better determination of the neutron electromagnetic polarizabilities

Haiyan Gao Latest results on few-body physics from HIγS

John Annand Compton scattering from 3He and 4He using an active target

Harald Grießhammer
Compton scattering and nucleon polarisabilities in chiral EFT: The next steps
Assessing theory errors using residual cutoff dependence (also Daniel Phillips)

Berhan Demissie Extracting neutron polarizabilities from Compton scattering on quasi-free neutron in $\gamma d \to \gamma n p$

And also talks by Franziska Hagelstein, Nadiia Krupina, Jose Manuel Alarcon, Kalyan Allada . . .