

Pion photo- and electroproduction and the chiral MAID interface

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¹Phys. Rev. C **87**, 045204 (2013), Phys. Rev. C **88**, 055207 (2013)

1. Introduction

2. Renormalization and power counting

3. Application to pion photo- and electroproduction

4. Summary and outlook

1. Introduction

Perturbative calculations in effective field theory require **two main ingredients**

1. Knowledge of the **most general effective Lagrangian**

(a) Mesonic ChPT $[\text{SU}(3) \times \text{SU}(3)]^2 (\pi, K, \eta)$

$$\underbrace{\mathcal{O}(q^2)}_2 + \underbrace{\mathcal{O}(q^4)}_{10+2} + \underbrace{\mathcal{O}(q^6)}_{90+4+23} + \dots$$

- q : Small quantity such as a pion mass
- Even powers
- Two-loop level

²Gasser, Leutwyler (1985), Fearing, Scherer (1996), Bijnens, Colangelo, Ecker (1999), Ebertshäuser, Fearing, Scherer (2002) Bijnens, Girlanda, Talavera (2002)

(b) Baryonic ChPT $[\text{SU}(2) \times \text{SU}(2) \times \text{U}(1)]^3 (\pi, N)$

$$\underbrace{\mathcal{O}(q)}_2 + \underbrace{\mathcal{O}(q^2)}_7 + \underbrace{\mathcal{O}(q^3)}_{23} + \underbrace{\mathcal{O}(q^4)}_{118} + \dots$$

- Odd and even powers (spin)
- One-loop level

Each term comes with an independent low-energy constant
(LEC)

Lowest-order Lagrangians: $F, M^2 = 2B\hat{m}, m, g_A$

Higher-order Lagrangians: $l_i, c_i, d_i, e_i, \dots$

³Gasser, Sainio, Švarc (1988), Bernard, Kaiser, Meißner (1995), Ecker, Mojžiš (1996), Fettes, Meißner, Mojžiš, Steininger (2000)

2. Consistent **expansion scheme** for observables

- (a) Tree-level diagrams, loop diagrams \rightsquigarrow ultraviolet divergences, regularization (of infinities)
- (b) Renormalization condition
- (c) Power counting scheme for renormalized diagrams
- (d) Remove regularization

ChPT: Momentum and quark mass expansion at fixed ratio

$$m_{\text{quark}}/q^2 \text{ } ^4$$

⁴J. Gasser and H. Leutwyler, Annals Phys. **158**, 142 (1984)

2. Renormalization and power counting

- Most general Lagrangian

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_\pi + \mathcal{L}_{\pi N} = \mathcal{L}_\pi^{(2)} + \mathcal{L}_\pi^{(4)} + \dots + \mathcal{L}_{\pi N}^{(1)} + \mathcal{L}_{\pi N}^{(2)} + \dots$$

Basic Lagrangian

$$\mathcal{L}_{\pi N}^{(1)} = \bar{\Psi} \left(i\gamma_\mu \partial^\mu - \boxed{m} \right) \Psi - \frac{1}{2} \boxed{\frac{g_A}{F}} \bar{\Psi} \gamma_\mu \gamma_5 \tau^a \partial^\mu \pi^a \Psi + \dots$$

m , g_A , and F denote the chiral limit of the physical nucleon mass, the axial-vector coupling constant, and the pion-decay constant, respectively

- **Power counting:** Associate chiral order D with a diagram

- Square of the lowest-order pion mass:

$$M^2 = B(m_u + m_d) \sim \mathcal{O}(q^2)$$

- Nucleon mass in the chiral limit $m \sim \mathcal{O}(q^0)$

- Loop integration in n dimensions $\sim \mathcal{O}(q^n)$

- Vertex from $\mathcal{L}_\pi^{(2k)} \sim \mathcal{O}(q^{2k})$

- Vertex from $\mathcal{L}_{\pi N}^{(k)} \sim \mathcal{O}(q^k)$

- Nucleon propagator $\sim \mathcal{O}(q^{-1})$

- Pion propagator $\sim \mathcal{O}(q^{-2})$

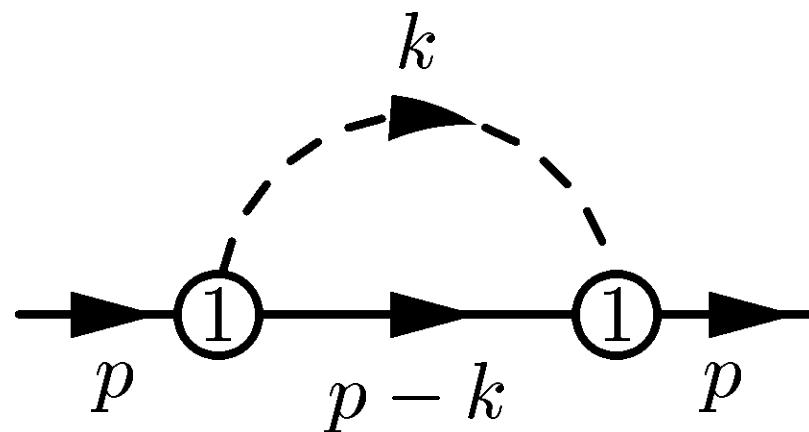
- Renormalization

- Regularize (typically dimensional regularization)

$$\begin{aligned} I(M^2, \mu^2, n) &= \mu^{4-n} \int \frac{d^n k}{(2\pi)^n} \frac{i}{k^2 - M^2 + i0^+} \\ &= \frac{M^2}{16\pi^2} \left[R + \ln \left(\frac{M^2}{\mu^2} \right) \right] + O(n-4), \\ R &= \frac{2}{n-4} - [\ln(4\pi) + \Gamma'(1)] - 1 \rightarrow \infty \end{aligned}$$

- Adjust counterterms such that they absorb all the divergences occurring in the calculation of loop diagrams
- Renormalization prescription: Adjust finite pieces such that renormalized diagrams satisfy a given power counting

- Example: Contribution to nucleon mass



Goal: $D = n \cdot 1 - 2 \cdot 1 - 1 \cdot 1 + 2 \cdot 1 = n - 1$

$$\Sigma = -\frac{3g_{A0}^2}{4F_0^2} \left[(\not{p} + m) I_N + M^2 (\not{p} + m) I_{N\pi}(-p, 0) + \dots \right]$$

Apply $\widetilde{\text{MS}}$ renormalization scheme

$$\begin{aligned} \Sigma_r &= -\frac{3g_{Ar}^2}{4F_r^2} [M^2 (\not{p} + m) \underbrace{I_{N\pi}^r(-p, 0)}_1 + \dots] = \boxed{\mathcal{O}(q^2)} \\ &= -\frac{1}{16\pi^2} + \dots \end{aligned}$$

GSS⁵: It turns out that loops have a much more complicated low-energy structure if baryons are included. Because the nucleon mass m_N does not vanish in the chiral limit, the mass scale m (nucleon mass in the chiral limit) occurs in the effective Lagrangian $\mathcal{L}_{\pi N}^{(1)}$ This complicates life a lot.

⁵J. Gasser, M. E. Sainio, A. Švarc, Nucl. Phys. **B307**, 779 (1988)

One possible solution: Extended on-mass-shell (EOMS) scheme⁶

Main idea: Perform additional subtractions such that renormalized diagrams satisfy the power counting

Motivation for this approach⁷

Terms violating the power counting are analytic in small quantities (and can thus be absorbed in a renormalization of counterterms)

- Example (chiral limit)

$$H(p^2, m^2; n) = - \int \frac{d^n k}{(2\pi)^n} \frac{i}{[(k-p)^2 - m^2 + i0^+][k^2 + i0^+]}$$

⁶T. Fuchs, J. Gegelia, G. Japaridze, S. Scherer, Phys. Rev. D **68**, 056005 (2003)

⁷J. Gegelia and G. Japaridze, Phys. Rev. D **60**, 114038 (1999)

Small quantity

$$\Delta = \frac{p^2 - m^2}{m^2} = \mathcal{O}(q)$$

We want the **renormalized integral** to be of order

$$D = n - 1 - 2 = n - 3$$

Result of integration

$$H \sim F(n, \Delta) + \Delta^{n-3} G(n, \Delta)$$

- F and G are hypergeometric functions
- analytic in Δ for arbitrary n

Observation⁸

F corresponds to **first** expanding the integrand in small quantities and **then** performing the integration

⇒ **Algorithm:** Expand integrand in small quantities and subtract those (integrated) terms whose order is **smaller** than suggested by the power counting

⁸J. Gegelia, G. Japaridze, K. S. Turashvili, Theor. Math. Phys. **101**, 1313 (1994)

Here:

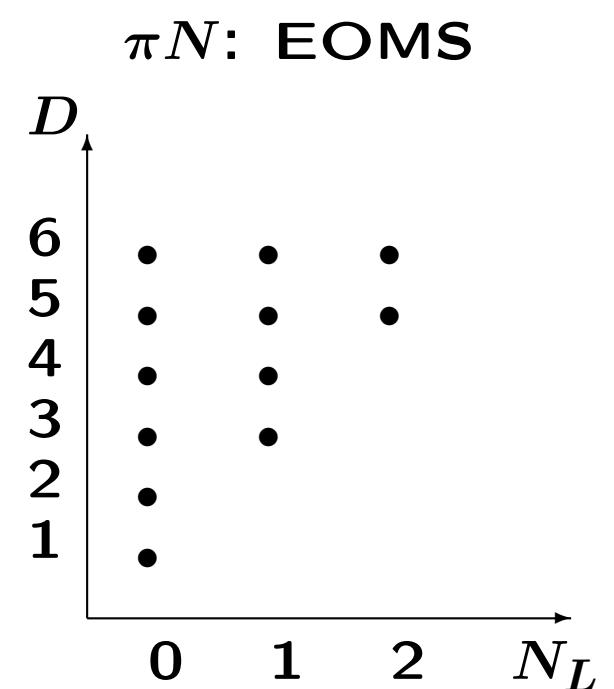
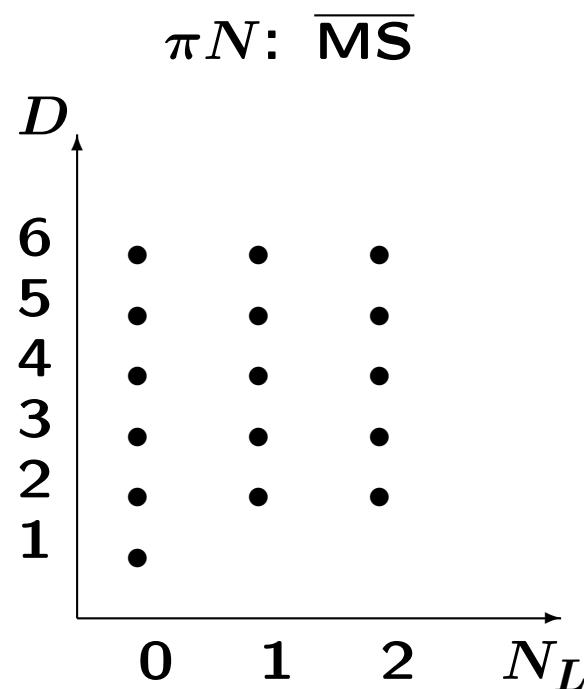
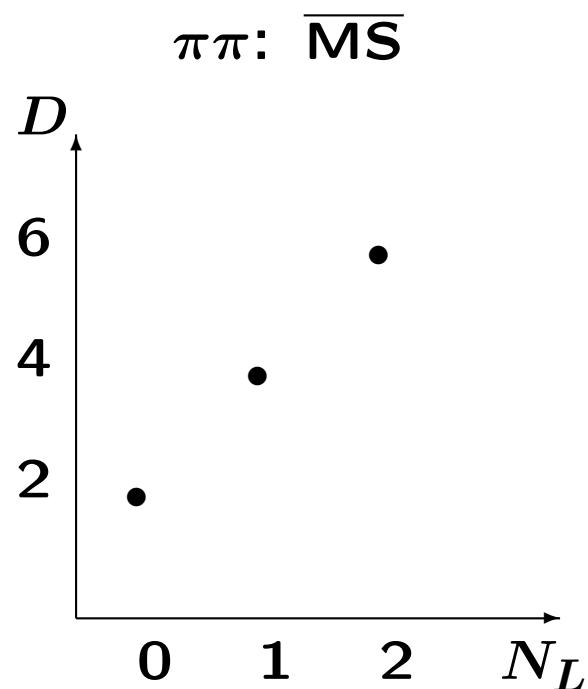
$$\begin{aligned} H^{\text{subtr}} &= - \int \frac{d^n k}{(2\pi)^n} \frac{i}{(k^2 - 2k \cdot p + i0^+)(k^2 + i0^+)} \Big|_{p^2=m^2} \\ &= -2\bar{\lambda} + \frac{1}{16\pi^2} + O(n-4) \end{aligned}$$

where

$$\bar{\lambda} = \frac{m^{n-4}}{(4\pi)^2} \left\{ \frac{1}{n-4} - \frac{1}{2} [\ln(4\pi) + \Gamma'(1) + 1] \right\}$$

$$H^R = H - H^{\text{subtr}} = \mathcal{O}(q^{n-3})$$

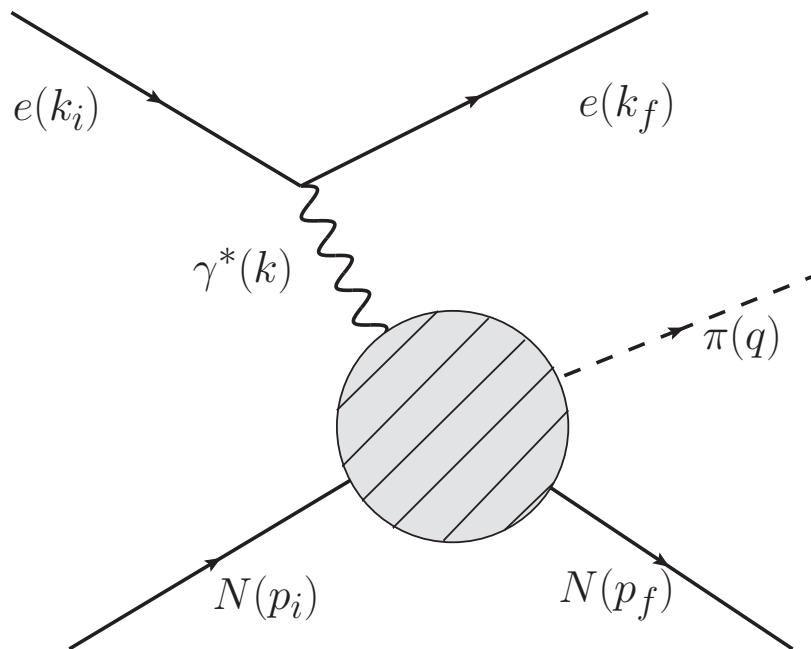
Chiral versus loop expansion



3. Application to pion photo- and electroproduction

$$e(k_i) + N(p_i) \rightarrow e(k_f) + N(p_f) + \pi(q)$$

One-photon-exchange approximation



Invariant amplitude

$$\mathcal{M} = \text{leptonic vertex} \times i \text{ propagator} \times \text{hadronic vertex} = \epsilon_\mu \mathcal{M}^\mu$$

$$\epsilon_\mu = e \frac{\bar{u}(k_f) \gamma_\mu u(k_i)}{k^2}, \quad \mathcal{M}^\mu = -ie \langle N(p_f), \pi(q) | J^\mu(0) | N(p_i) \rangle$$

Current conservation

$$k_\mu \mathcal{M}^\mu = 0$$

Parameterization in terms of **six** invariant amplitudes

$$\mathcal{M}^\mu = \bar{u}(p_f, s_f) \left(\sum_{i=1}^6 \boxed{A_i(s, t, u)} M_i^\mu \right) u(p_i, s_i), \quad u(p, s): \text{Dirac spinor}$$

Mandelstam variables

$$\begin{aligned} s &= (p_i + k)^2, \\ t &= (p_i - q)^2, \\ u &= (p_i - p_f)^2, \\ s + t + u &= 2m_N^2 + M_\pi^2 - Q^2, \quad Q^2 = -k^2 \end{aligned}$$

Lorentz structures

$$\begin{aligned}
M_1^\mu &= -\frac{i}{2}\gamma_5(\gamma^\mu k - k\gamma^\mu), \\
M_2^\mu &= 2i\gamma_5 \left[P^\mu k \cdot \left(q - \frac{1}{2}k \right) - \left(q^\mu - \frac{1}{2}k^\mu \right) k \cdot P \right], \\
M_3^\mu &= -i\gamma_5(\gamma^\mu k \cdot q - kq^\mu), \\
M_4^\mu &= -2i\gamma_5(\gamma^\mu k \cdot P - kP^\mu) - 2m_N M_1^\mu, \\
M_5^\mu &= i\gamma_5(k^\mu k \cdot q - q^\mu k^2), \\
M_6^\mu &= -i\gamma_5(kk^\mu - \gamma^\mu k^2),
\end{aligned}$$

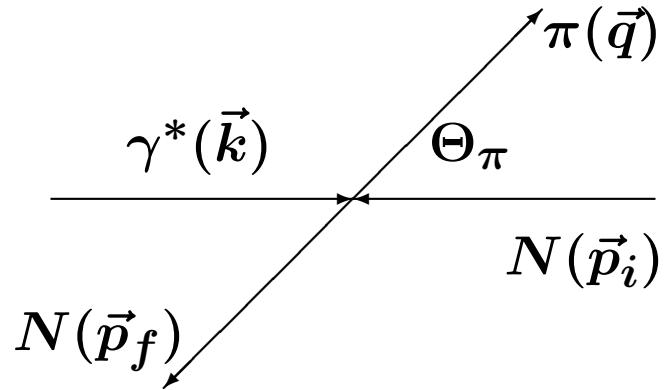
where

$$P = \frac{1}{2}(p_i + p_f)$$

Current conservation

$$k_\mu M_i^\mu = 0, \quad i = 1, \dots, 6.$$

cm frame: $\vec{k} = -\vec{p}_i$, $\vec{q} = -\vec{p}_f$



$$\mathcal{M} = \epsilon_\mu \bar{u}(p_f, s_f) \left(\sum_{i=1}^6 A_i M_i^\mu \right) u(p_i, s_i) = \frac{4\pi W}{m_N} \chi_f^\dagger \boxed{\mathcal{F}} \chi_i$$

- χ : Pauli spinor, $W = \sqrt{s}$
- Gauge transformation (\rightsquigarrow longitudinal multipoles)

$$a^\mu = \epsilon^\mu - k^\mu \frac{\epsilon_0}{k_0}$$

Six CGLN amplitudes⁹

$$\begin{aligned}\mathcal{F} = i\vec{\sigma} \cdot \vec{a}_\perp & \boxed{\mathcal{F}_1(W, \Theta_\pi, Q^2)} + \vec{\sigma} \cdot \hat{q} \vec{\sigma} \cdot \hat{k} \times \vec{a}_\perp \mathcal{F}_2 \\ & + i\vec{\sigma} \cdot \hat{k} \hat{q} \cdot \vec{a}_\perp \mathcal{F}_3 + i\vec{\sigma} \cdot \hat{q} \hat{q} \cdot \vec{a}_\perp \mathcal{F}_4 \\ & + i\vec{\sigma} \cdot \hat{k} \hat{k} \cdot \vec{a}_\parallel \mathcal{F}_5 + i\vec{\sigma} \cdot \hat{q} \hat{k} \cdot \vec{a}_\parallel \mathcal{F}_6\end{aligned}$$

Multipole expansion of \mathcal{F}_i in terms of Legendre polynomials

$$\mathcal{F}_1 = \sum_{l=0}^{\infty} \left\{ [lM_{l+} + E_{l+}] P'_{l+1}(x) + [(l+1)M_{l-} + E_{l-}] P'_{l-1}(x) \right\}, \quad \dots$$

$$x = \cos \Theta_\pi = \hat{q} \cdot \hat{k}$$

$E_{l\pm}, M_{l\pm}, L_{l\pm}$: functions of W and Q^2

Total angular momentum of final state: $j = l \pm \frac{1}{2}$

Reduced multipole

$$\overline{\mathcal{M}}_{l\pm} = \frac{\mathcal{M}_{l\pm}}{|\vec{q}|^l}$$

⁹Chew, Goldberger, Nambu, Low

Isospin decomposition: four physical channels

$$A_i(\gamma^{(*)} p \rightarrow n\pi^+) = \sqrt{2} \left(A_i^{(-)} + A_i^{(0)} \right),$$

$$A_i(\gamma^{(*)} p \rightarrow p\pi^0) = A_i^{(+)} + A_i^{(0)},$$

$$A_i(\gamma^{(*)} n \rightarrow p\pi^-) = -\sqrt{2} \left(A_i^{(-)} - A_i^{(0)} \right),$$

$$A_i(\gamma^{(*)} n \rightarrow n\pi^0) = A_i^{(+)} - A_i^{(0)},$$

expressed in terms of three isospin amplitudes (0), (+), and (-)

1. Number of diagrams

- $\mathcal{O}(q^3)$: 15 tree-level diagrams + 50 one-loop diagrams
- $\mathcal{O}(q^4)$: 20 tree-level diagrams + 85 one-loop diagrams

2. Calculate loop contributions numerically using CAS MATHEMATICA with FeynCalc and LoopTools packages

3. Checks: Current conservation and crossing symmetry

4. LECs from other processes (mesonic and baryonic Lagrangians)

LEC	Source
l_3	$M_\pi = 134.977 \text{ MeV}$
l_4, l_6	pion form factor
c_1	proton mass $m_p = 938.272 \text{ MeV}$
c_2, c_3, c_4	pion-nucleon scattering
c_6, c_7	magnetic moment of proton ($\mu_p = 2.793$) and neutron ($\mu_n = -1.913$)
$d_6, d_7,$ e_{54}, e_{74}	world data for nucleon electromagnetic form factors ($Q^2 < 0.3 \text{ GeV}^2$)
d_{16}	axial-vector coupling constant $g_A = 1.2695$
d_{18}	pion-nucleon coupling
d_{22}	axial radius of the nucleon $\langle r_A^2 \rangle = 12/M_A^2$, $M_A = 1.026 \text{ GeV}$

$$l_i: \mathcal{L}_\pi^{(4)},$$

$$c_i: \mathcal{L}_{\pi N}^{(2)}, \quad d_i: \mathcal{L}_{\pi N}^{(3)}, \quad e_i: \mathcal{L}_{\pi N}^{(4)}$$

5. Analytic expressions for the contact diagrams

(a) 4 LECs at $\mathcal{O}(q^3)$

isospin

$$\mathcal{L}_{\pi N}^{(3)} = \frac{\textcolor{red}{d_8}}{2m} \left(i\bar{\Psi} \epsilon^{\mu\nu\alpha\beta} \text{Tr} \left(\tilde{f}_{\mu\nu}^+ u_\alpha \right) D_\beta \Psi + \text{H.c.} \right) \quad (+)$$

$$+ \frac{\textcolor{red}{d_9}}{2m} \left(i\bar{\Psi} \epsilon^{\mu\nu\alpha\beta} \text{Tr} \left(f_{\mu\nu}^+ + 2v_{\mu\nu}^{(s)} \right) u_\alpha D_\beta \Psi + \text{H.c.} \right) \quad (0)$$

$$- \frac{\textcolor{red}{d_{20}}}{8m^2} \left(i\bar{\Psi} \gamma^\mu \gamma_5 \left[\tilde{f}_{\mu\nu}^+, u_\lambda \right] D^{\lambda\nu} \Psi + \text{H.c.} \right) \quad (-)$$

$$+ i \frac{\textcolor{red}{d_{21}}}{2} \bar{\Psi} \gamma^\mu \gamma_5 \left[\tilde{f}_{\mu\nu}^+, u^\nu \right] \Psi \quad (-)$$

Structures contribute to **photoproduction**, no free parameters for **electroproduction**

(b) 15 LECs at $\mathcal{O}(q^4)$

$$\begin{aligned}\mathcal{L}_{\pi N}^{(4)} = & -\frac{e_{48}}{4m} \left(i\bar{\Psi} \text{Tr} \left(f_{\lambda\mu}^+ + 2v_{\lambda\mu}^{(s)} \right) h_\nu^\lambda \gamma_5 \gamma^\mu D^\nu \Psi + \text{H.c.} \right) \\ & + \text{14 more terms}\end{aligned}$$

- photoproduction

isospin channel	(0)	(+)	(-)
# LECs	5	5	1

- electroproduction

isospin channel	(0)	(+)	(-)
# LECs	2	2	0

6. Web interface chiral MAID

[<http://www.kph.uni-mainz.de/MAID/chiralmaid/>]

MAID

Photo- and Electroproduction of Pions, Etas and Kaons on the Nucleon

Institut für Kernphysik, Universität Mainz
Mainz, Germany

MAID2007	unitary isobar model for (e,e'p)
DMT2001	dynamical model for (e,e'p)
KAON-MAID	isobar model for (e,e'K)
ETA-MAID	isobar model for (e,e'h) reggeized isobar model for (q,h)
ChiralMAID <small>NEW</small>	chiral perturbation theory approach for (e,e'p)
2-PION-MAID	isobar model for (q,pp)
archive	MAID2000 MAID2003 DMT2001original ETAprime2003

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M A X I D

[ChiralMAID info and updates \(please read first\)](#)

Pion Photo- and Electroproduction on the Nucleon in relativistic chiral perturbation theory

[M. Hilt](#), [S. Scherer](#), [L. Tiator](#)

- [Electromagnetic Multipoles \(\$E_H, M_H, L_H, S_H\$ \)](#)
- [Amplitudes \(\$F_1, \dots, F_6, H_1, \dots, H_6, A_1, \dots, A_6\$ \)](#)
- [Differential Cross Sections \(\$ds_T, ds_L, ds_{LT}, ds_{TT}, \dots\$ \)](#)
- [5-fold Diff. Cross Section \(\$d^5s, G, ds^V = ds_T + e ds_L + e ds_{TT} \cos 2f + \dots\$ \)](#)
- [Total Cross Sections \(\$s_T, s_L, s_{LT}, s_{TT}, \dots\$ \)](#)
- [Transverse Polarization Observables \(\$ds/dW, T, S, P, E, F, G, H, \dots\$ \)](#)

External services:

[MAID Homepage](#) [MAID2003](#) [DMT2001](#) [KAON-MAID](#) [ETA-MAID2000](#) [ETA-MAID2003](#) [ETA'-MAID](#)

[A1 kinematics calculator for electroproduction \(Java\)](#)

[SAID Partial-Wave Analyses](#)

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Multipoles

The multipoles can be given in 4 unique sets of isospin or charge channels ([click here for a larger image](#)):

$$\begin{aligned} & \left(A_p^{1/2}, A_n^{1/2}, A^{3/2} \right), \left(A^{1/2}, A^0, A^{3/2} \right), \left(A^0, A^+, A^- \right), \left(A_{\pi^+ n}, A_{\pi^- p}, A_{\pi^0 p}, A_{\pi^0 n} \right) \\ & A_{\pi^+ n} = \sqrt{2} (A^- + A^0) = \sqrt{2} (A_p^{1/2} - \frac{1}{3} A^{3/2}) = \sqrt{2} (A^0 + \frac{1}{3} A^{1/2} - \frac{1}{3} A^{3/2}) \\ & A_{\pi^- p} = -\sqrt{2} (A^- - A^0) = \sqrt{2} (A_n^{1/2} + \frac{1}{3} A^{3/2}) = \sqrt{2} (A^0 - \frac{1}{3} A^{1/2} + \frac{1}{3} A^{3/2}) \\ & A_{\pi^0 p} = A^+ + A^0 = A_p^{1/2} + \frac{2}{3} A^{3/2} = A^0 + \frac{1}{3} A^{1/2} + \frac{2}{3} A^{3/2} \\ & A_{\pi^0 n} = A^+ - A^0 = -A_n^{1/2} + \frac{2}{3} A^{3/2} = -A^0 + \frac{1}{3} A^{1/2} + \frac{2}{3} A^{3/2} \end{aligned}$$

Further details can be found in D. Drechsel and L. Tiator, J. Phys. G 18 (1992) 449-497. ([scanned version](#))

Type of the multipoles: (p(1/2), n(1/2), 3/2) (1/2, 0, 3/2) (0, +, -) charge channels

Choose pion angular momentum l : El+ El- MI+ MI- LI+ LI- SI+ SI-

Reduced multipoles:

Choose kinematical variables

choose an independent (running) variable: Q² W

choose values for Q², W, step size and maximum value:

Q ² (GeV/c) ²	W (MeV)	increment	upper value	click here	
0	1074	1	1100	Calculate	Reset

Change of model parameters:

O(q^3) (all couplings in GeV $^{-2}$)

0	+	-	
d ₉	d ₈	d ₂₀	d ₂₁
-1.216	-1.092	4.337	-4.260

O(q^4) (all couplings in GeV $^{-3}$)**Isospin 0**

e ₄₈	e ₄₉	e ₅₀	e ₅₁	e ₅₂	e ₅₃	e ₁₁₂
5.235	0.925	2.205	6.629	-4.103	-2.654	9.342

Isospin +

e ₆₇	e ₆₈	e ₆₉	e ₇₁	e ₇₂	e ₇₃	e ₁₁₃
-8.269	-0.925	-1.035	-4.352	10.539	2.120	-13.745

Isospin -

e ₇₀
3.910

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Remark: $O(q^3)$ refers to corresponding LECs (this is not a $O(q^3)$ calculation)

Multipoles

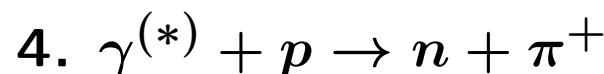
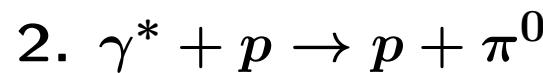
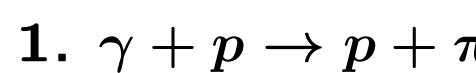
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M. Hilt, S. Scherer, L. Tiator
Institut fuer Kernphysik, Universitaet Mainz

Pion angular momentum l= 0

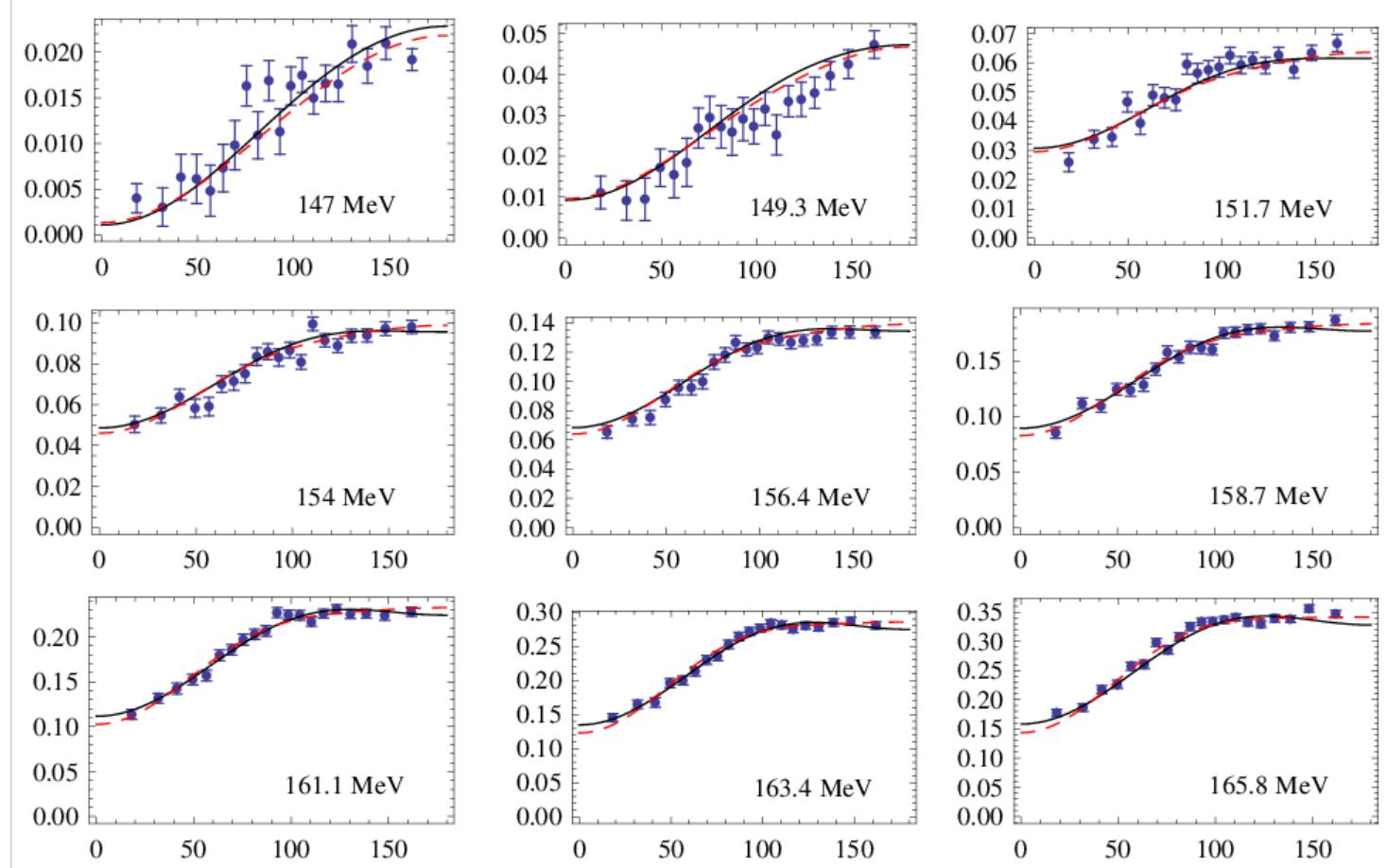
All multipoles are given in $10^{-3}/M_{\pi^+}$

Q^2 = .000 (GeV/c)^2				e,gA,F[GeV],gpiN=gA*mp/F			
*****				d8,d9,d20,d21 [GeV^-2]			
.3028	1.2695	.0924	13.2100				
-1.0920	-1.2160	4.3370	-4.2600				
5.2350	.9250	2.2050	6.6290	-4.1030	-2.6540	e48,e49,e50,e51,e52,e53 [GeV^-3]	
-8.2690	-.9250	-1.0350	3.9100	-4.3520	10.5390	2.1200	e67,e68,e69,e70,e71,e72,e73 [GeV^-3]
9.3420	-13.7450						e112,e113 [GeV^-3]
W	E0+(pi0_p)	E0+(pi0_n)	E0+(pi+_n)	E0+(pi-_p)	E(lab)	q(cm)	
(MeV)	Re	Im	Re	Im	Re	Im	(MeV)
1074.00	-1.0608	.0000	2.8400	.0000	27.1931	.0000	145.54
1075.00	-.9960	.0000	2.8898	.0000	26.9933	.0000	146.69
1076.00	-.9210	.0000	2.9504	.0000	26.7940	.0000	147.84
1077.00	-.8301	.0000	3.0279	.0000	26.5939	.0000	148.98
1078.00	-.7093	.0000	3.1376	.0000	26.3903	.0000	150.13
1079.00	-.4769	.0000	3.3685	.0000	26.1676	.0000	151.28
1080.00	-.3758	.3249	3.4564	.3534	25.9705	-.0617	152.43
1081.00	-.3959	.4764	3.4121	.5183	25.7986	-.0924	153.58
1082.00	-.4162	.5891	3.3672	.6412	25.6292	-.1166	154.74
1083.00	-.4367	.6826	3.3218	.7433	25.4625	-.1378	155.89
1084.00	-.4573	.7641	3.2758	.8323	25.2982	-.1573	157.04
1085.00	-.4780	.8371	3.2293	.9121	25.1364	-.1757	158.20
1086.00	-.4989	.9035	3.1822	.9849	24.9770	-.1933	159.36
1087.00	-.5199	.9649	3.1346	1.0523	24.8200	-.2104	160.52
1088.00	-.5410	1.0221	3.0864	1.1151	24.6654	-.2270	161.67
1089.00	-.5623	1.0758	3.0377	1.1741	24.5131	-.2433	162.83
1090.00	-.5837	1.1264	2.9884	1.2299	24.3630	-.2593	164.00
1091.00	-.6053	1.1745	2.9384	1.2828	24.2152	-.2752	165.16
1092.00	-.6271	1.2202	2.8880	1.3333	24.0695	-.2909	166.32

Fits to available experimental data



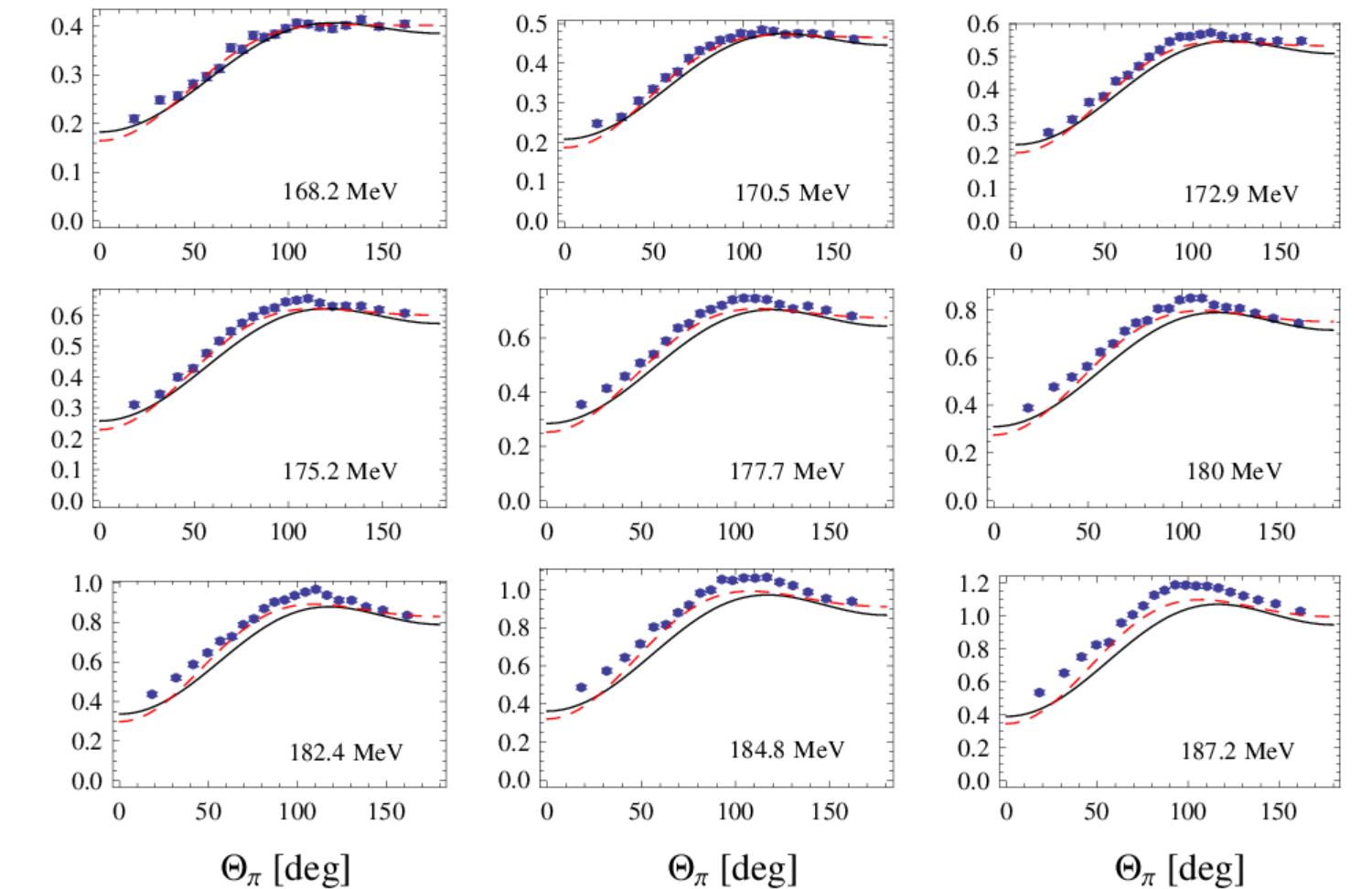
Differential cross sections $d\sigma/d\Omega_\pi$ in $\mu\text{b}/\text{sr}$ for $\gamma + p \rightarrow p + \pi^0$ ¹⁰



¹⁰Data taken from D. Hornidge et al., Phys. Rev. Lett. **111**, 062004 (2013)

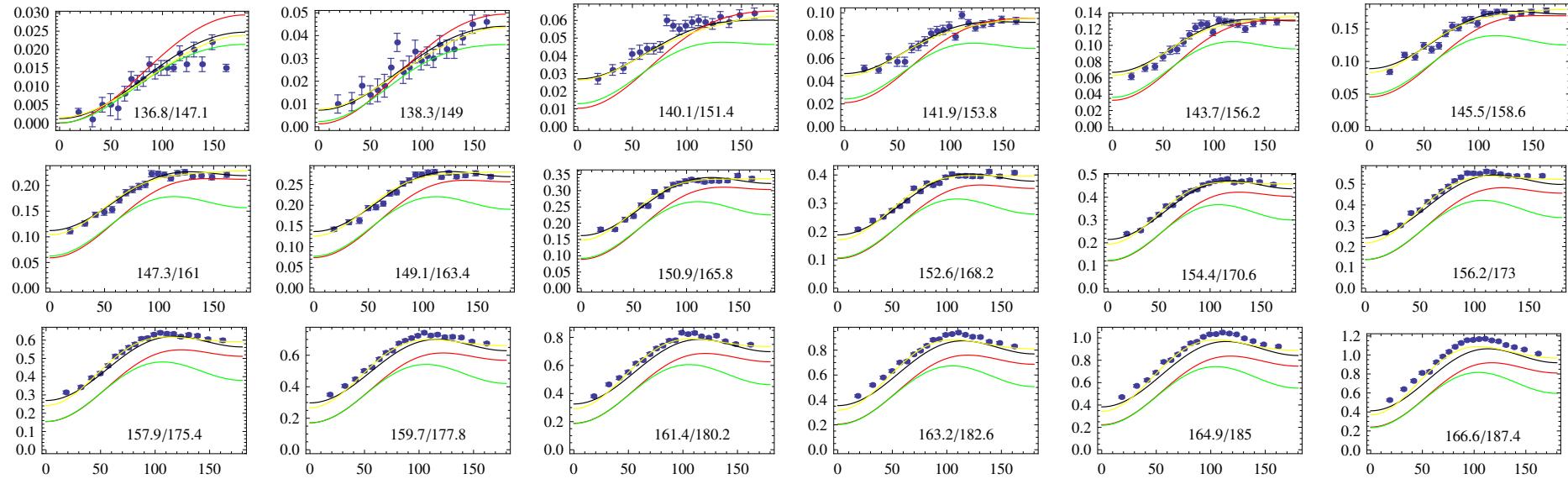
Differential cross sections $d\sigma/d\Omega_\pi$ in $\mu\text{b}/\text{sr}$ for $\gamma + p \rightarrow p + \pi^0$ ¹¹

Solid:
RChPT,
dashed
HBChPT



¹¹Data taken from D. Hornidge et al., Phys. Rev. Lett. **111**, 062004 (2013)

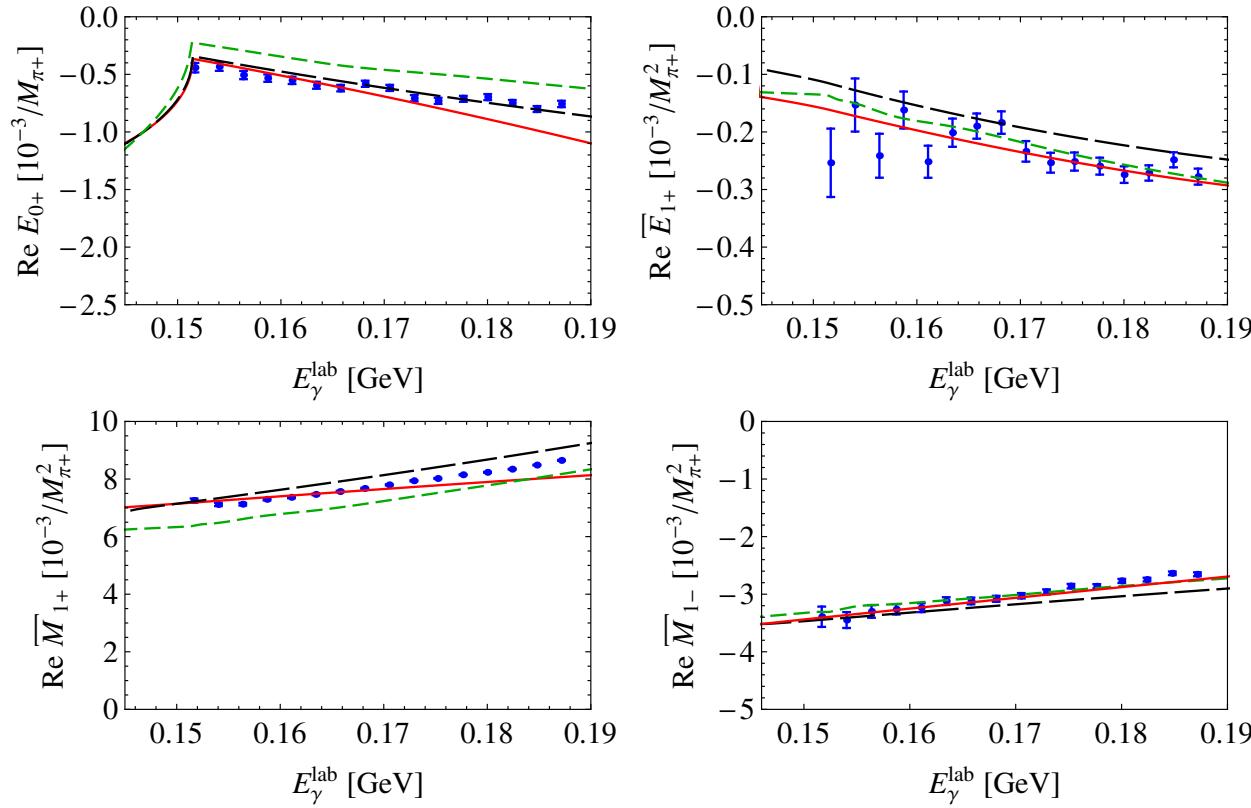
Comparison of $\mathcal{O}(q^3)$ with $\mathcal{O}(q^4)$ ¹²



**Black: RChPT $\mathcal{O}(q^4)$, red RChPT $\mathcal{O}(q^3)$, yellow HChPT $\mathcal{O}(q^4)$,
green RChPT + vector mesons $\mathcal{O}(q^3)$**

¹²Data taken from D. Hornidge et al., Phys. Rev. Lett. **111**, 062004 (2013)

S- and reduced P-wave multipoles for $\gamma + p \rightarrow p + \pi^0$

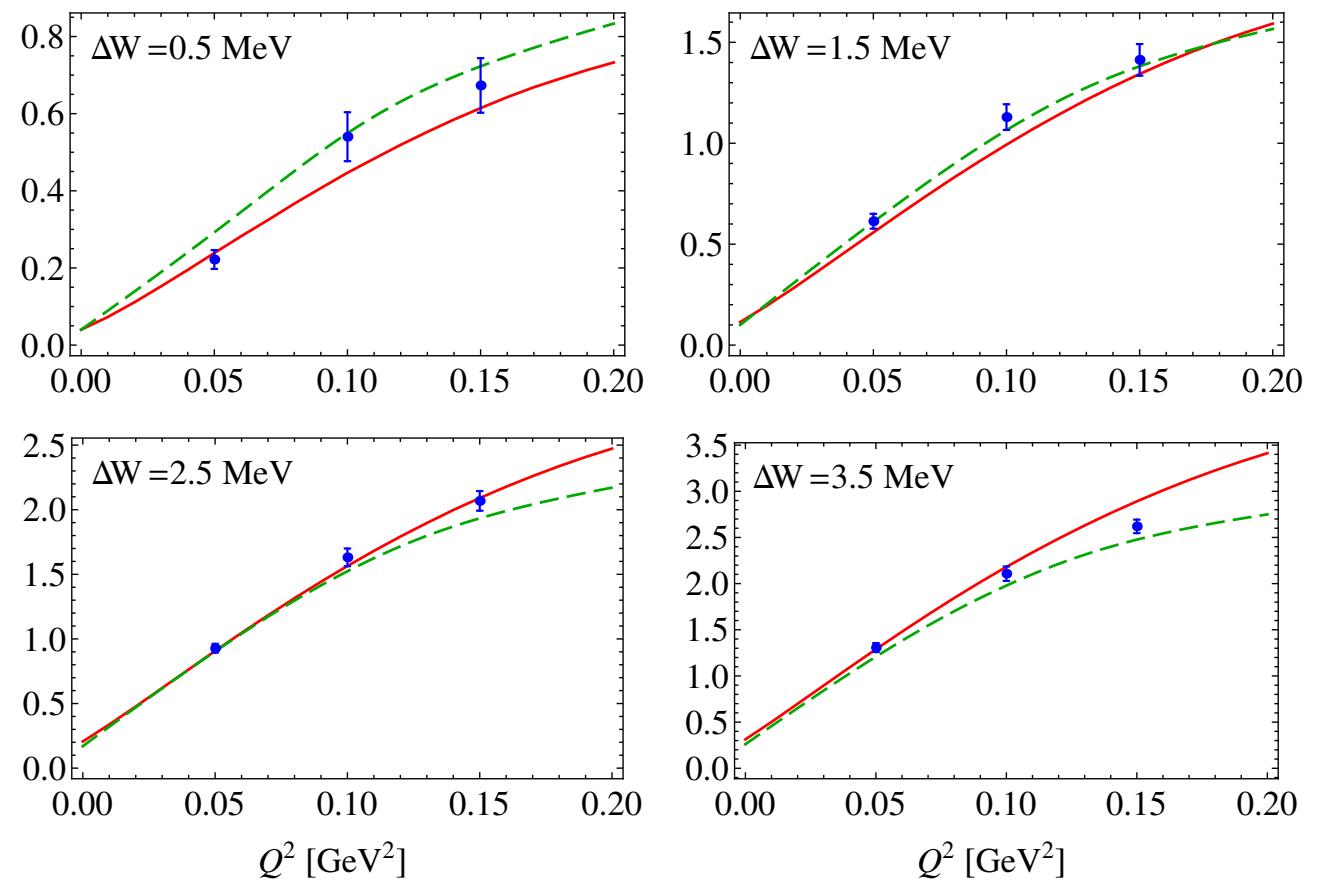


**Red RChPT; green DMT model¹³; black Gasparyan & Lutz¹⁴;
data from Hornidge et al. (2013)**

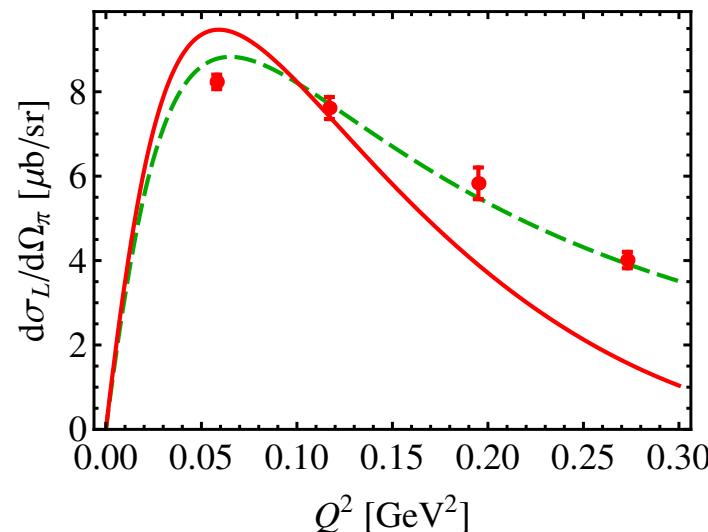
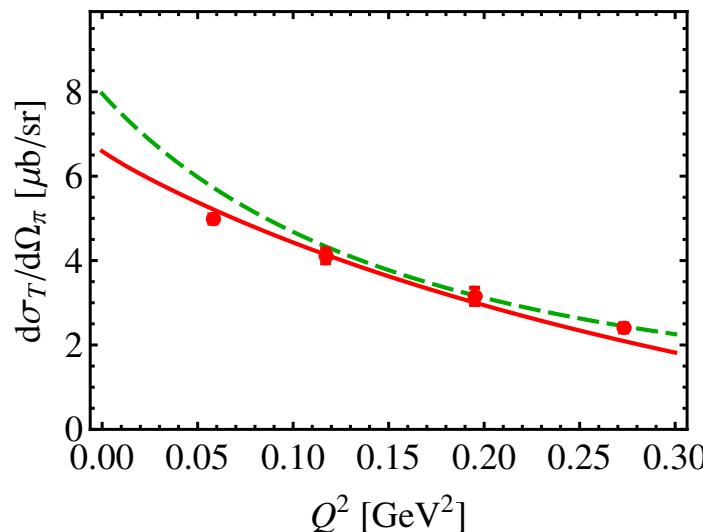
¹³S. S. Kamalov et al., Phys. Rev. C **64**, 032201 (2001)

¹⁴A. Gasparyan and M. F. M. Lutz, Nucl. Phys. **A848**, 126 (2010)

Total cross sections for $\gamma^* + p \rightarrow p + \pi^0$ in μb



Differential cross sections as a function of Q^2 for $\gamma^* + p \rightarrow n + \pi^+$ at $W = 1125$ MeV and $\Theta_\pi = 0^\circ$.



red RChPT; green DMT model;
data from Baumann (PhD thesis, JGU, 2005)

Isospin channel	LEC	Value
0	d_9 [GeV $^{-2}$]	-1.22 ± 0.12
0	e_{48} [GeV $^{-3}$]	5.2 ± 1.4
0	e_{49} [GeV $^{-3}$]	0.9 ± 2.6
0	e_{50} [GeV $^{-3}$]	2.2 ± 0.8
0	e_{51} [GeV $^{-3}$]	6.6 ± 3.6
0	e_{52}^* [GeV $^{-3}$]	-4.1
0	e_{53}^* [GeV $^{-3}$]	-2.7
0	e_{112} [GeV $^{-3}$]	9.3 ± 1.6
<hr/>		
from fits with all data		
+	d_8 [GeV $^{-2}$]	-1.09 ± 0.12
+	e_{67} [GeV $^{-3}$]	-8.3 ± 1.5
+	e_{68} [GeV $^{-3}$]	-0.9 ± 2.6
+	e_{69} [GeV $^{-3}$]	-1.0 ± 2.2
+	e_{71} [GeV $^{-3}$]	-4.4 ± 3.7
+	e_{72}^* [GeV $^{-3}$]	10.5
+	e_{73}^* [GeV $^{-3}$]	2.1
+	e_{113} [GeV $^{-3}$]	-13.7 ± 2.6
<hr/>		
-	d_{20} [GeV $^{-2}$]	4.34 ± 0.08
-	d_{21} [GeV $^{-2}$]	-3.1 ± 0.1
-	e_{70} [GeV $^{-3}$]	3.9 ± 0.3

4. Summary and outlook

- Baryonic ChPT: Renormalization condition \leftrightarrow consistent power counting
- Example: EOMS renormalization (manifestly Lorentz-invariant)
- Application to pion photo- and electroproduction
- 20 tree-level diagrams + 85 one-loop diagrams
- Chiral MAID interface

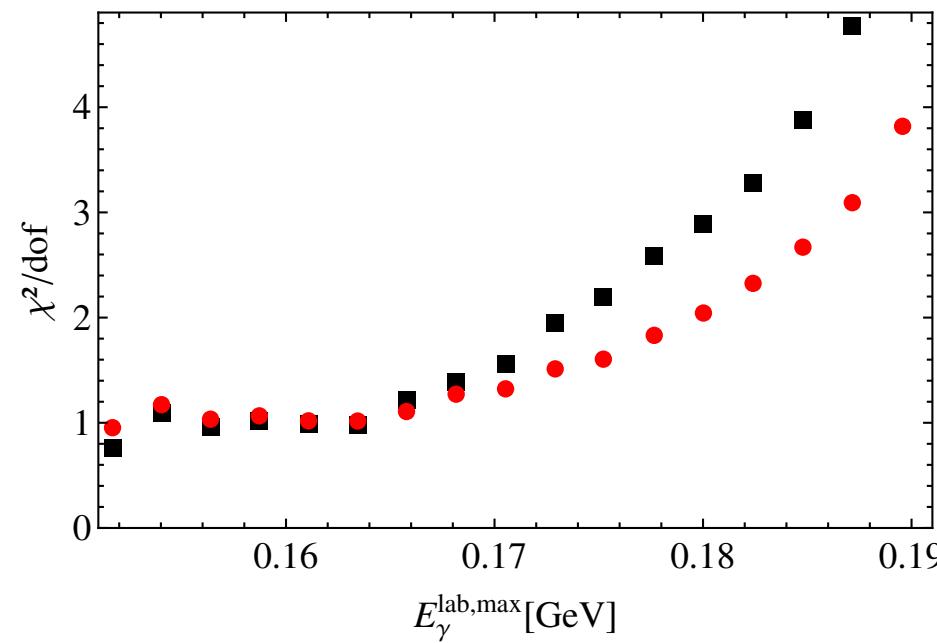
- Inclusion of heavy degrees of freedom (vector mesons, axial vector mesons, Δ ¹⁵)
- New data¹⁶ ↵ reanalysis of LECs

¹⁵A. N. Hiller Blin, T. Ledwig, and M. J. V. Vacas, Phys. Lett. B **747** (2015), 217,
see talks by A. N. Hiller Blin and L. Cawthorne

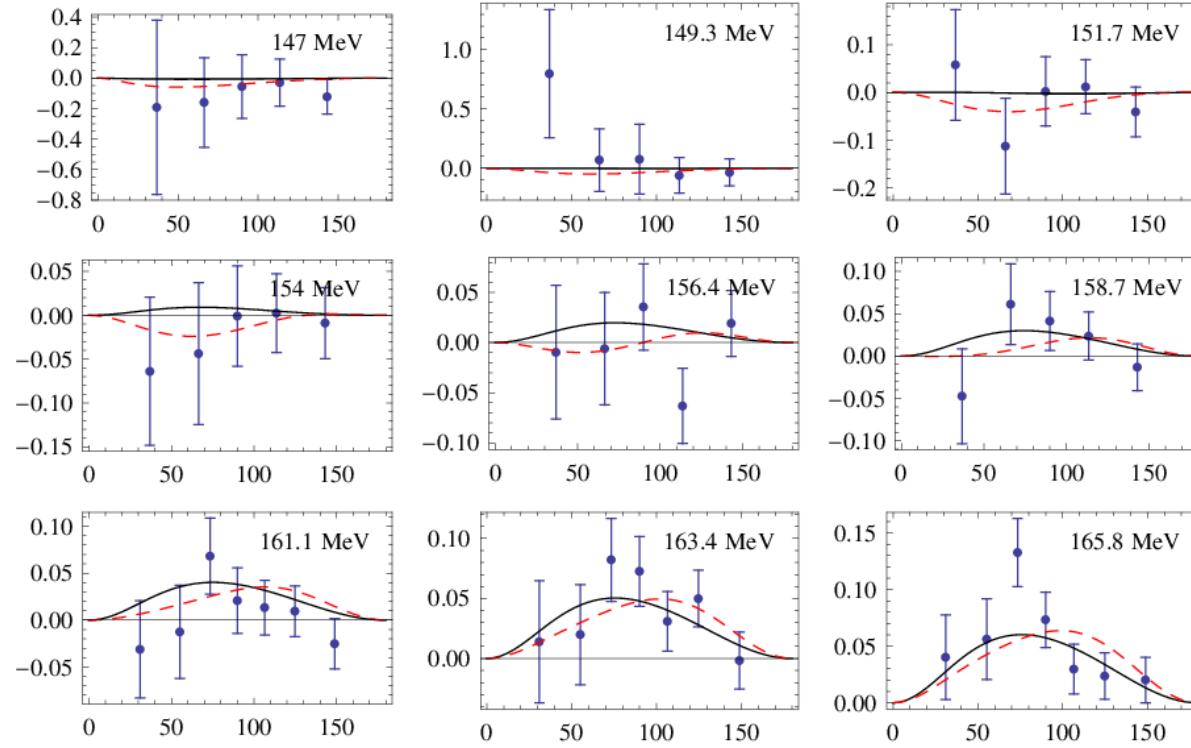
¹⁶K. Chirapatpimol *et al.*, $p(e, e'p)\pi^0$, Phys. Rev. Lett. **114**, 192503 (2015), I. Fricic,
 $p(e, e'\pi^+)n$, PhD thesis, University of Zagreb, 2015

Thank You!

χ^2_{red} as a function of the fitted energy range: RBChPT vs.
HBChPT



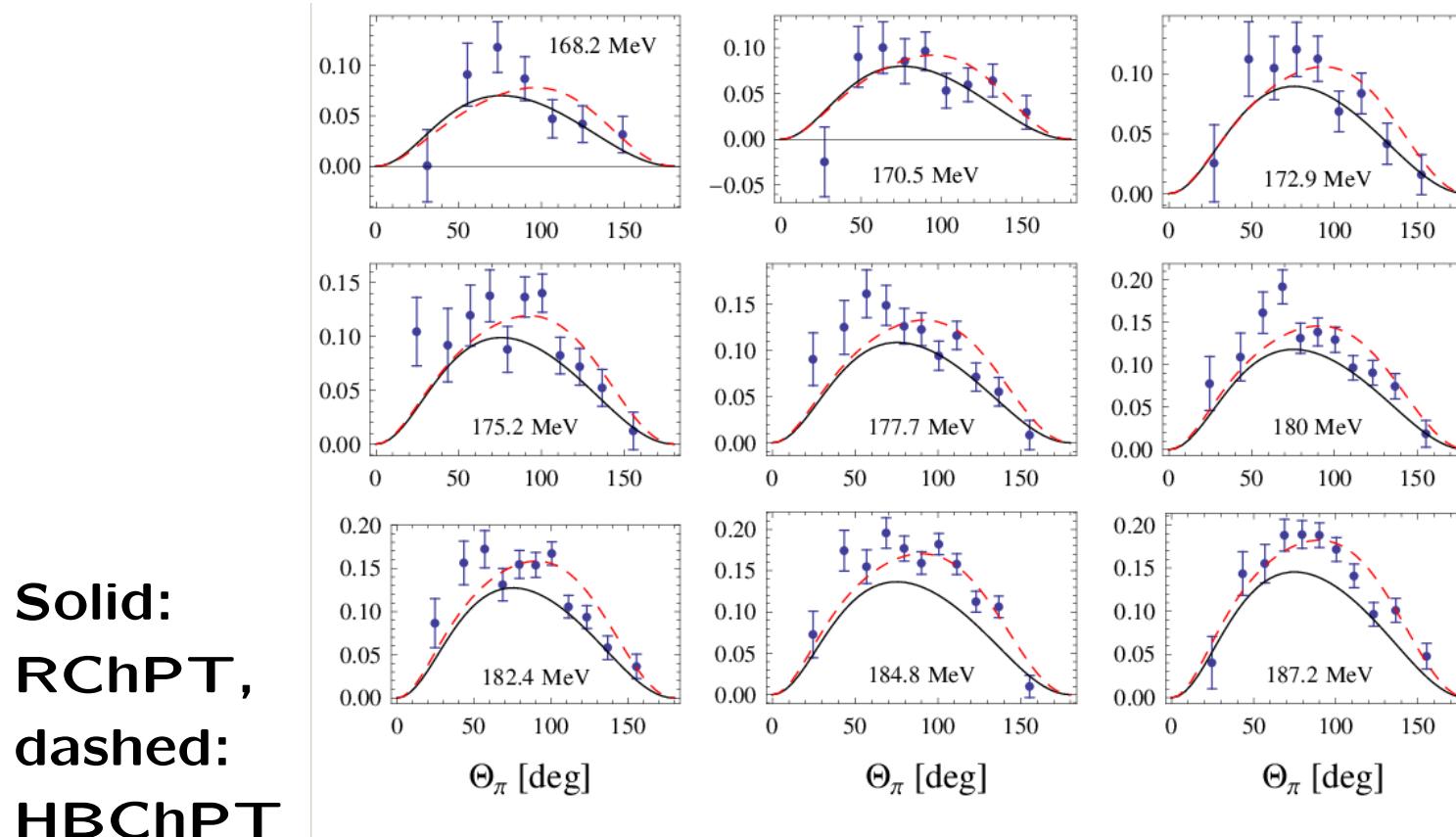
Photon asymmetries for $\gamma + p \rightarrow p + \pi^0$

¹⁷

Solid:
RChPT,
dashed
HBChPT

¹⁷Data taken from D. Hornidge et al., Phys. Rev. Lett. **111**, 062004 (2013)

Photon asymmetries for $\gamma + p \rightarrow p + \pi^0$



¹⁸Data taken from D. Hornidge et al., Phys. Rev. Lett. **111**, 062004 (2013)

Multipoles

The multipoles can be given in 4 unique sets of isospin or charge channels ([click here for a larger image](#)):

$$\begin{aligned} & \left(A_p^{1/2}, A_n^{1/2}, A^{3/2} \right), \left(A^{1/2}, A^0, A^{3/2} \right), \left(A^0, A^+, A^- \right), \left(A_{\pi^+ n}, A_{\pi^- p}, A_{\pi^0 p}, A_{\pi^0 n} \right) \\ & A_{\pi^+ n} = \sqrt{2} (A^- + A^0) = \sqrt{2} (A_p^{1/2} - \frac{1}{3} A^{3/2}) = \sqrt{2} (A^0 + \frac{1}{3} A^{1/2} - \frac{1}{3} A^{3/2}) \\ & A_{\pi^- p} = -\sqrt{2} (A^- - A^0) = \sqrt{2} (A_n^{1/2} + \frac{1}{3} A^{3/2}) = \sqrt{2} (A^0 - \frac{1}{3} A^{1/2} + \frac{1}{3} A^{3/2}) \\ & A_{\pi^0 p} = A^+ + A^0 = A_p^{1/2} + \frac{2}{3} A^{3/2} = A^0 + \frac{1}{3} A^{1/2} + \frac{2}{3} A^{3/2} \\ & A_{\pi^0 n} = A^+ - A^0 = -A_n^{1/2} + \frac{2}{3} A^{3/2} = -A^0 + \frac{1}{3} A^{1/2} + \frac{2}{3} A^{3/2} \end{aligned}$$

Further details can be found in D. Drechsel and L. Tiator, J. Phys. G 18 (1992) 449-497. ([scanned version](#))

Type of the multipoles: (p(1/2), n(1/2), 3/2) (1/2, 0, 3/2) (0, +, -) charge channels

Choose pion angular momentum l : 1 El+ El- MI+ MI- Li+ Li- SI+ SI-

Reduced multipoles:

Choose kinematical variables

choose an independent (running) variable: Q² W

choose values for Q², W, step size and maximum value:

Q ² (GeV/c) ²	W (MeV)	increment	upper value	click here	
0	1080	0.01	0.1	<input type="button" value="Calculate"/>	<input type="button" value="Reset"/>

Change of model parameters:

Multipoles

C h M A I D 2 0 1 2
M. Hilt, S. Scherer, L. Tiator
Institut fuer Kernphysik, Universitaet Mainz

Pion angular momentum l= 1

All multipoles are given in $10^{-3}/M_{\pi^+}$

W = 1080.000 (MeV)							

.3028	1.2695	.0924	13.2100			e,gA,F[GeV],gpiN=gA*mp/F	
-1.0920	-1.2160	4.3370	-4.2600			d8,d9,d20,d21 [GeV^-2]	
5.2350	.9250	2.2050	6.6290	-4.1030	-2.6540	e48,e49,e50,e51,e52,e53 [GeV^-3]	
-8.2690	-.9250	-1.0350	3.9100	-4.3520	10.5390	e67,e68,e69,e70,e71,e72,e73 [GeV^-3]	
9.3420	-13.7450					e112,e113 [GeV^-3]	
Q^2	E1+(pi0_p)	E1+(pi0_n)	E1+(pi+_n)	E1+(pi-_p)	E(lab)	q(cm)	
(GeV/c)^2	Re	Im	Re	Im	Re	Im	(MeV)
.00	-.0479	-.0001	-.0177	-.0002	1.4327	.0001	-.1.4755 -.0001
.01	-.0583	-.0001	-.0171	-.0002	1.4017	.0001	-.1.4600 -.0001
.02	-.0673	-.0001	-.0149	-.0001	1.3364	.0001	-.1.4106 -.0001
.03	-.0754	-.0001	-.0115	-.0001	1.2631	.0001	-.1.3536 .0000
.04	-.0831	-.0001	-.0071	-.0001	1.1903	.0001	-.1.2977 .0000
.05	-.0903	-.0001	-.0020	-.0001	1.1208	.0001	-.1.2457 .0000
.06	-.0973	-.0001	.0039	-.0001	1.0555	.0001	-.1.1985 .0000
.07	-.1040	-.0001	.0104	-.0001	.9944	.0001	-.1.1561 .0000
.08	-.1106	-.0001	.0174	-.0001	.9372	.0001	-.1.1183 .0000
.09	-.1171	-.0001	.0250	-.0001	.8836	.0001	-.1.0845 .0000
.10	-.1234	-.0001	.0331	-.0001	.8332	.0001	-.1.0545 .0000
Q^2	L1+(pi0_p)	L1+(pi0_n)	L1+(pi+_n)	L1+(pi-_p)	E(lab)	q(cm)	
(GeV/c)^2	Re	Im	Re	Im	Re	Im	(MeV)
.00	-.0393	-.0001	-.0168	-.0001	.7782	.0000	-.8101 .0000
.01	-.0440	-.0001	-.0169	-.0001	.6088	.0000	-.6471 .0000
.02	-.0468	.0000	-.0162	-.0001	.4781	.0000	-.5214 .0000
.03	-.0486	.0000	-.0151	.0000	.3797	.0000	-.4271 .0000
.04	-.0496	.0000	-.0138	.0000	.3047	.0000	-.3554 .0000
.05	-.0501	.0000	-.0124	.0000	.2465	.0000	-.2998 .0000

Coincidence cross sections σ_0 , σ_{TT} , and σ_{LT} in $\mu\text{b}/\text{sr}$ and beam asymmetry $A_{LT'}$ in % at constant $Q^2 = 0.05 \text{ GeV}^2$, $\Theta_\pi = 90^\circ$, $\Phi_\pi = 90^\circ$, and $\epsilon = 0.93$ as a function of ΔW above threshold.¹⁹
Solid (red): RChPT, dotted (black): HBChPT (Bernard et al., 1996) dashed (green): DMT

¹⁹Data taken from M. Weis et al., Eur. Phys. J. A **38**, 27 (2008).

