

Impact of the $\Delta(1232)$ in $\gamma + p \rightarrow \pi^0 p$ in χ PT.

Lloyd W. Cawthorne
Judith A. McGovern

The University of Manchester

lloyd.cawthorne@postgrad.manchester.ac.uk

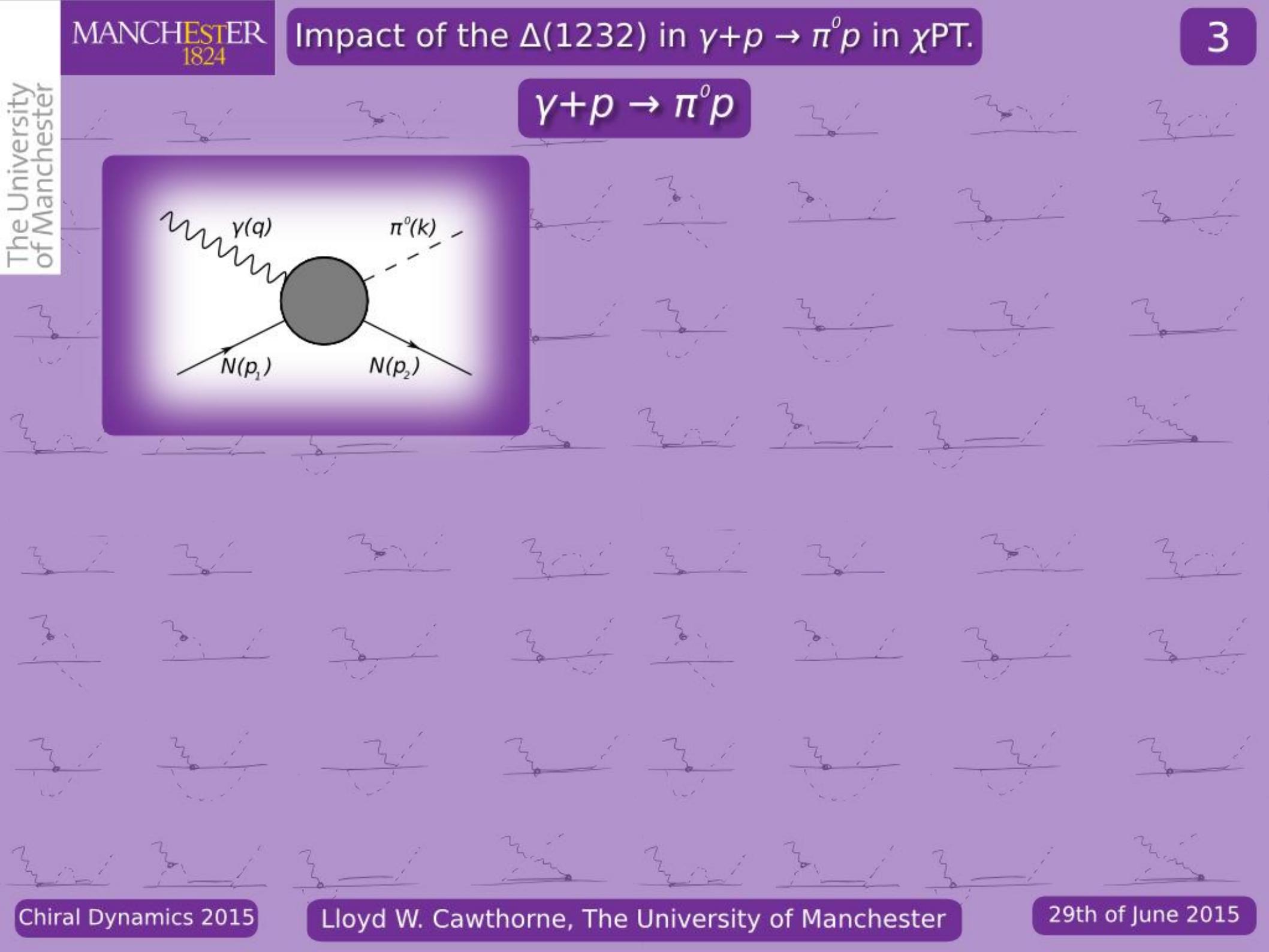
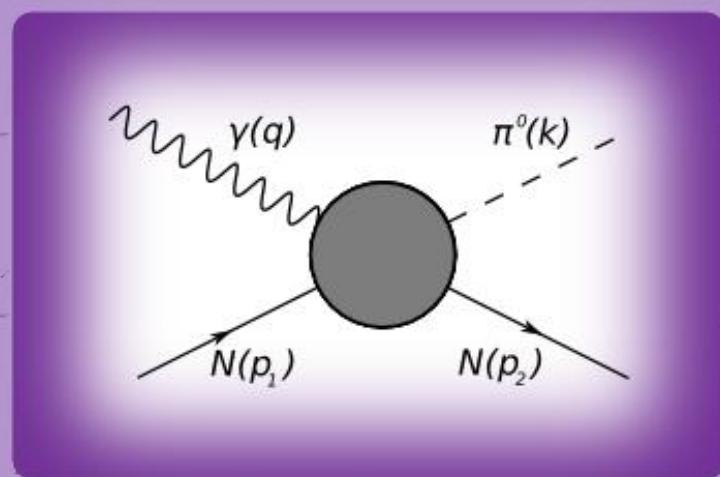
29th of June 2015

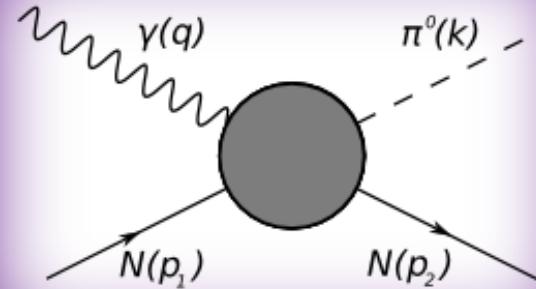
Importance of D-waves

Importance of D-waves

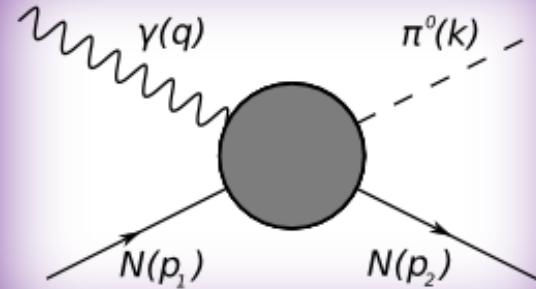
Working to energies approaching $\Delta(1232)$

$\gamma + p \rightarrow \pi^0 p$ 

$\gamma + p \rightarrow \pi^0 p$ 

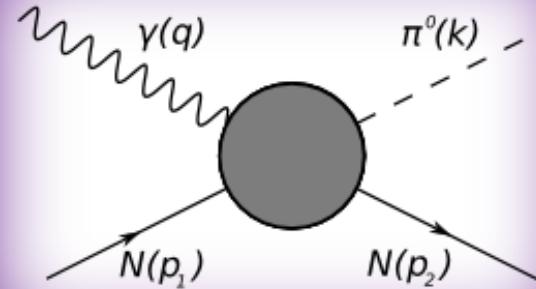
$\gamma + p \rightarrow \pi^0 p$ 

Has been studied using χ PT since the early 90s.

$\gamma + p \rightarrow \pi^0 p$ 

Has been studied using χ PT since the early 90s.

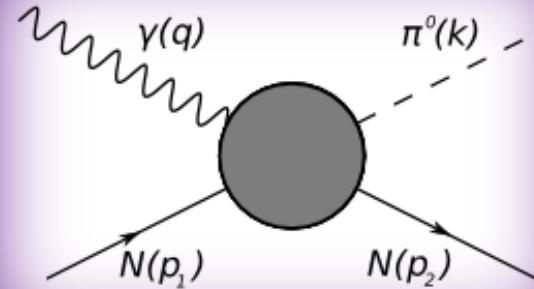
Requires the inclusion of pion loops for an adequate description.

$\gamma + p \rightarrow \pi^0 p$ 

Has been studied using χ PT since the early 90s.

Requires the inclusion of pion loops for an adequate description.

More physics required to go beyond the threshold region.



Has been studied using χ PT since the early 90s.

Requires the inclusion of pion loops for an adequate description.

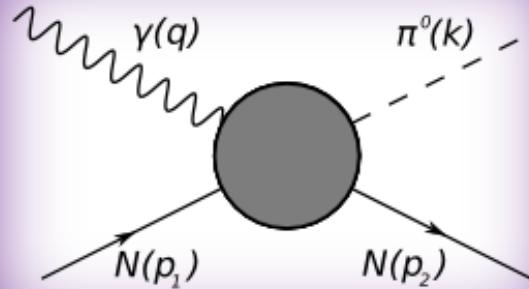
More physics required to go beyond the threshold region.

More accurate studies can be performed thanks to data from MAMI.

$$\frac{d\sigma}{d\Omega} \Sigma = \frac{d\sigma^\perp - d\sigma^\parallel}{d\sigma^\perp + d\sigma^\parallel}$$

Hornidge et al (2013) PRL

$$\gamma + p \rightarrow \pi^0 p$$



Has been studied using χ PT since the early 90s.

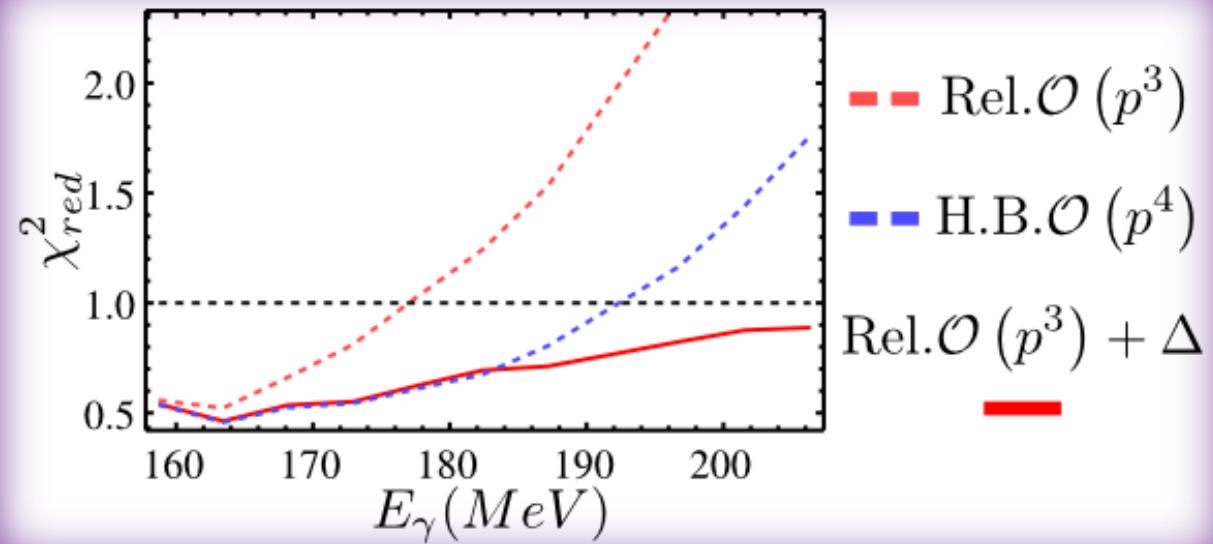
Requires the inclusion of pion loops for an adequate description.

More physics required to go beyond the threshold region.

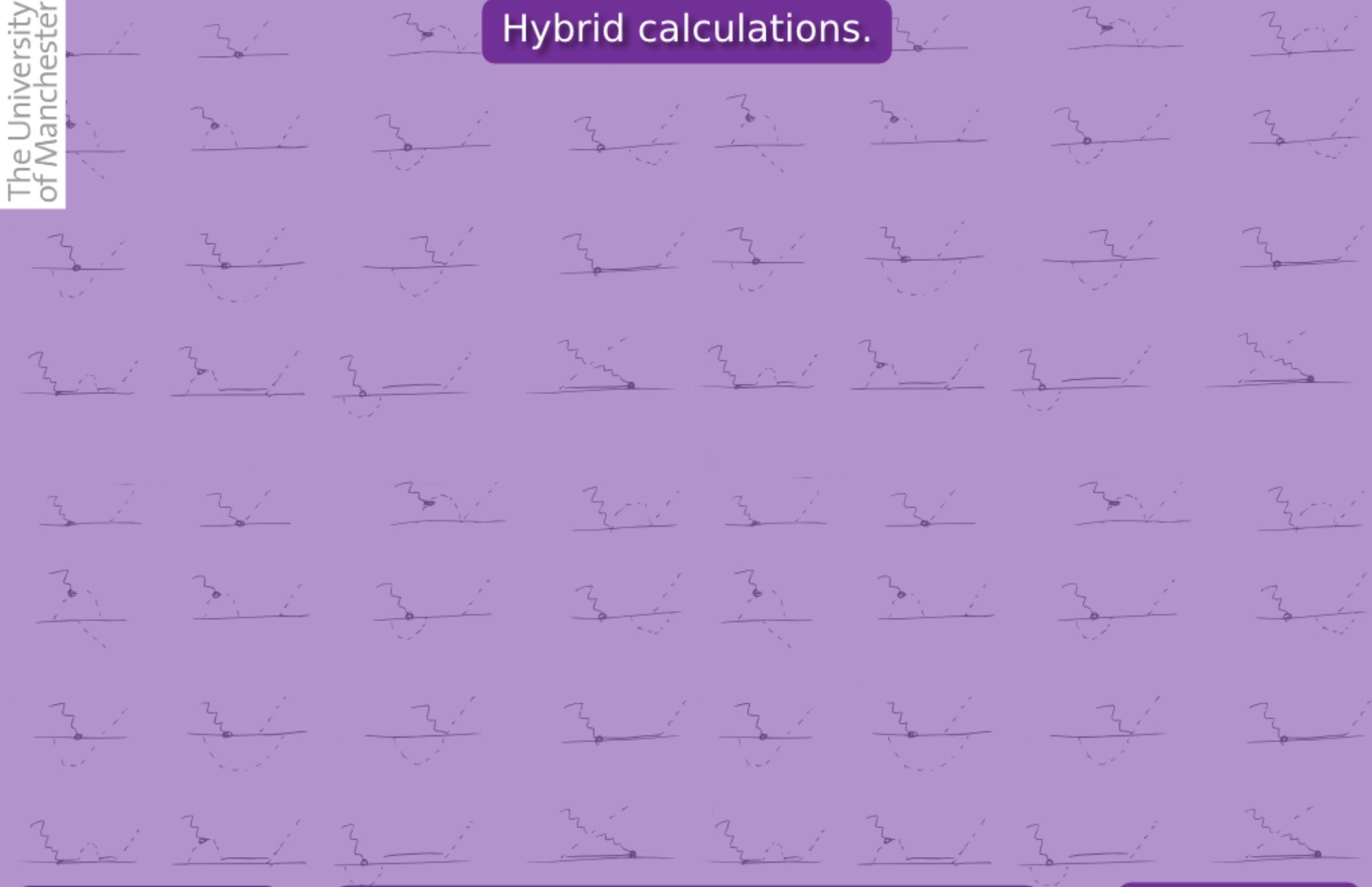
More accurate studies can be performed thanks to data from MAMI.

$$\frac{d\sigma}{d\Omega} \Sigma = \frac{d\sigma^\perp - d\sigma^\parallel}{d\sigma^\perp + d\sigma^\parallel}$$

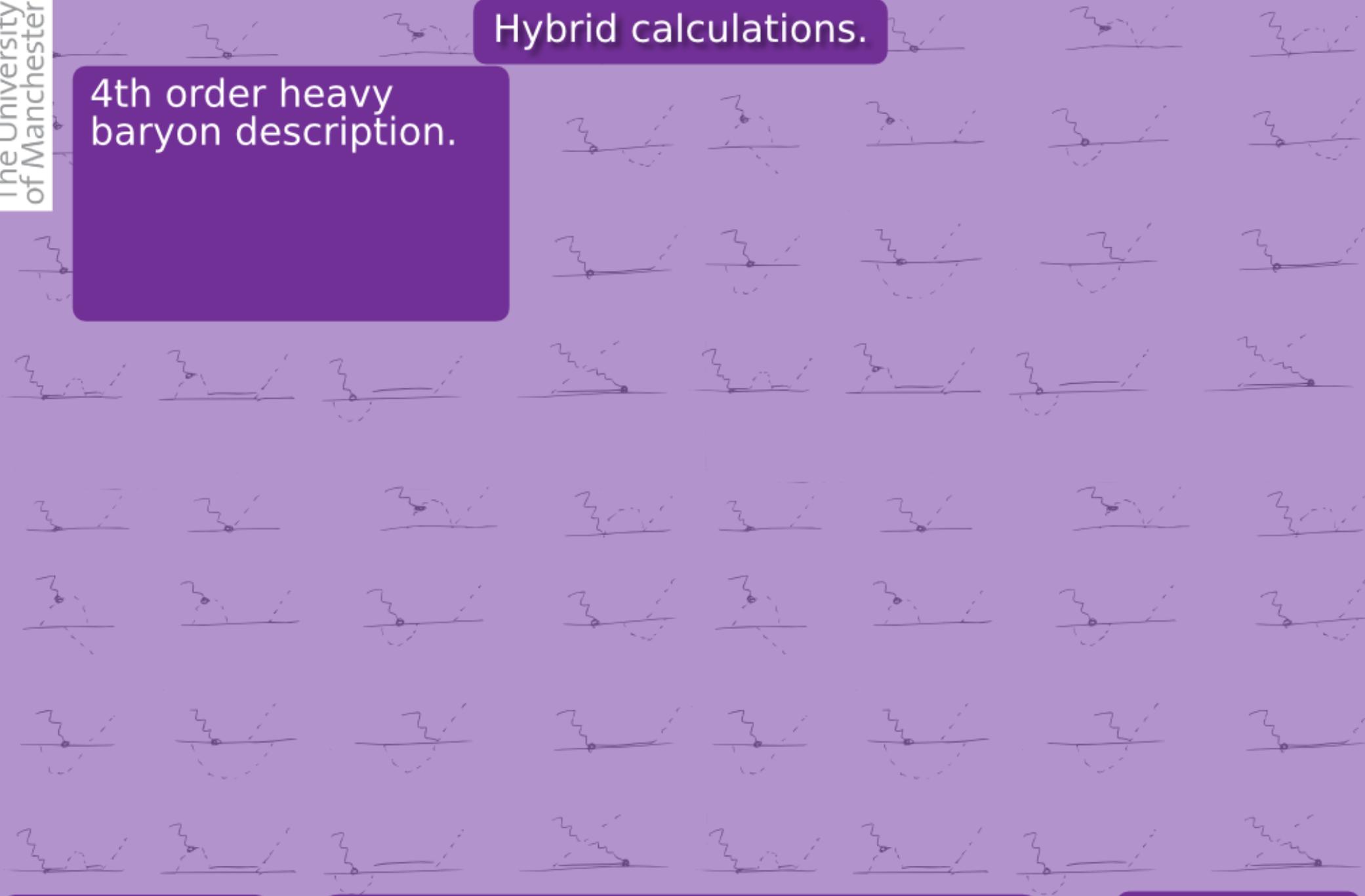
Hornidge et al (2013) PRL



Hybrid calculations.

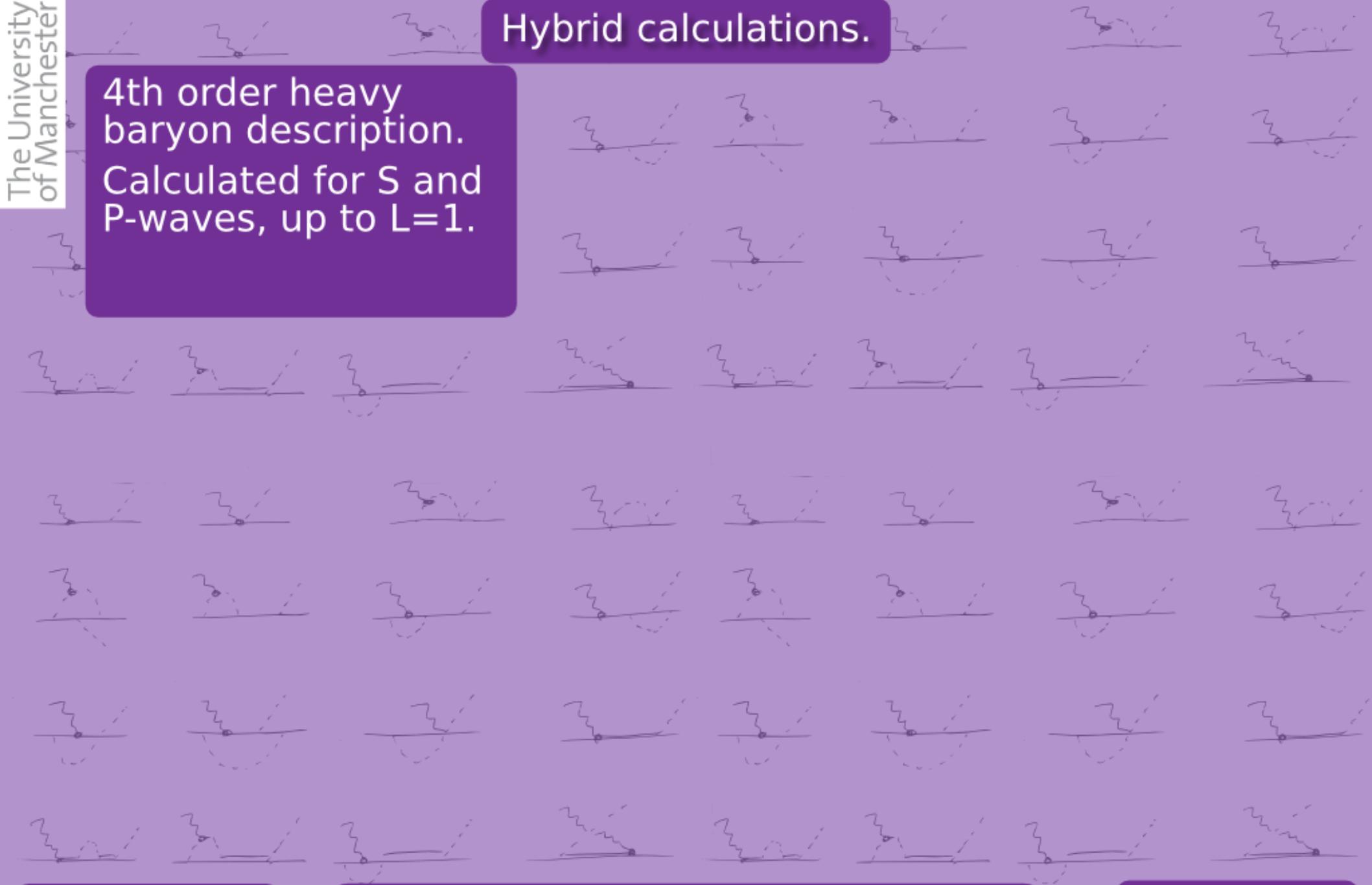


Hybrid calculations.

4th order heavy
baryon description.

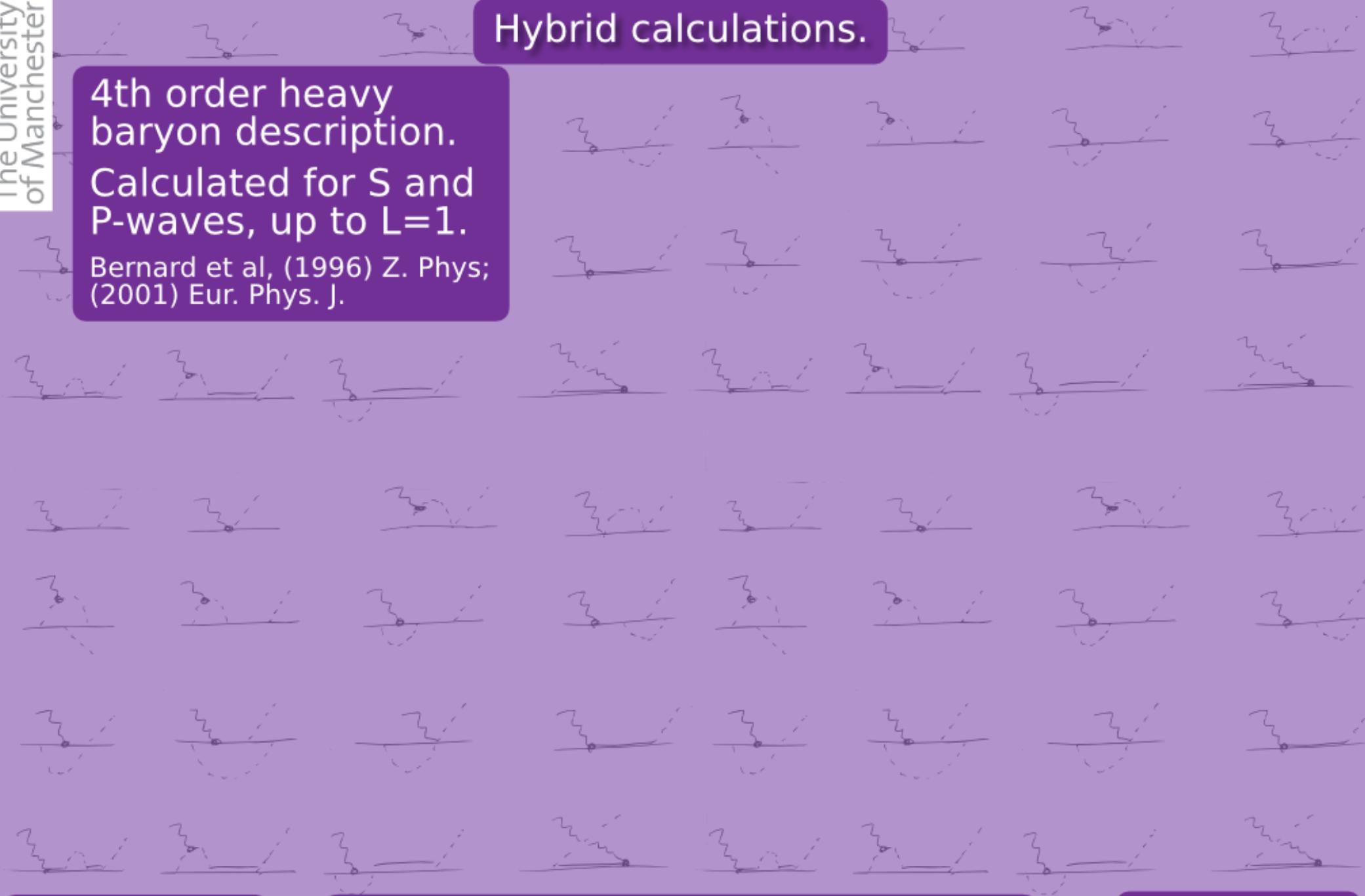
Hybrid calculations.

4th order heavy baryon description.
Calculated for S and P-waves, up to L=1.



Hybrid calculations.

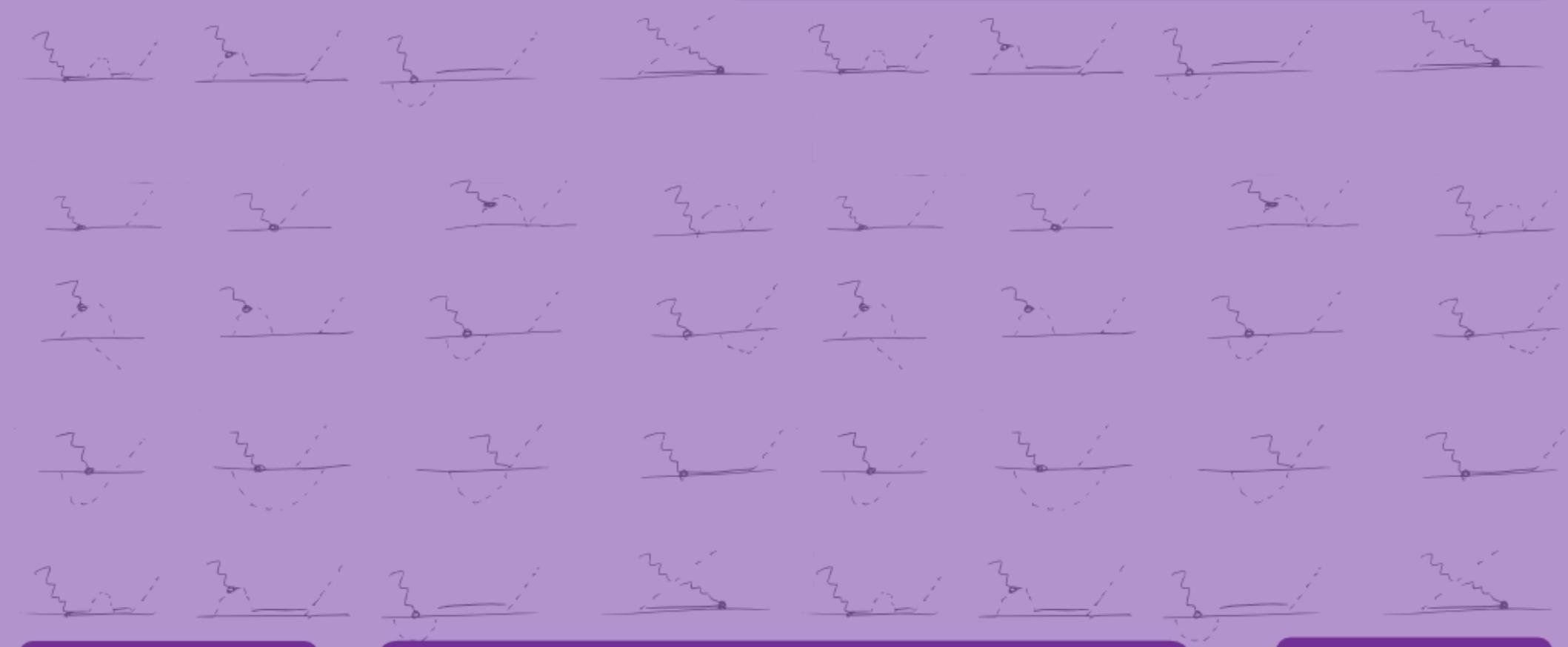
4th order heavy baryon description.
Calculated for S and P-waves, up to L=1.
Bernard et al, (1996) Z. Phys;
(2001) Eur. Phys. J.



Hybrid calculations.

4th order heavy baryon description.
Calculated for S and P-waves, up to L=1.
Bernard et al, (1996) Z. Phys;
(2001) Eur. Phys. J.

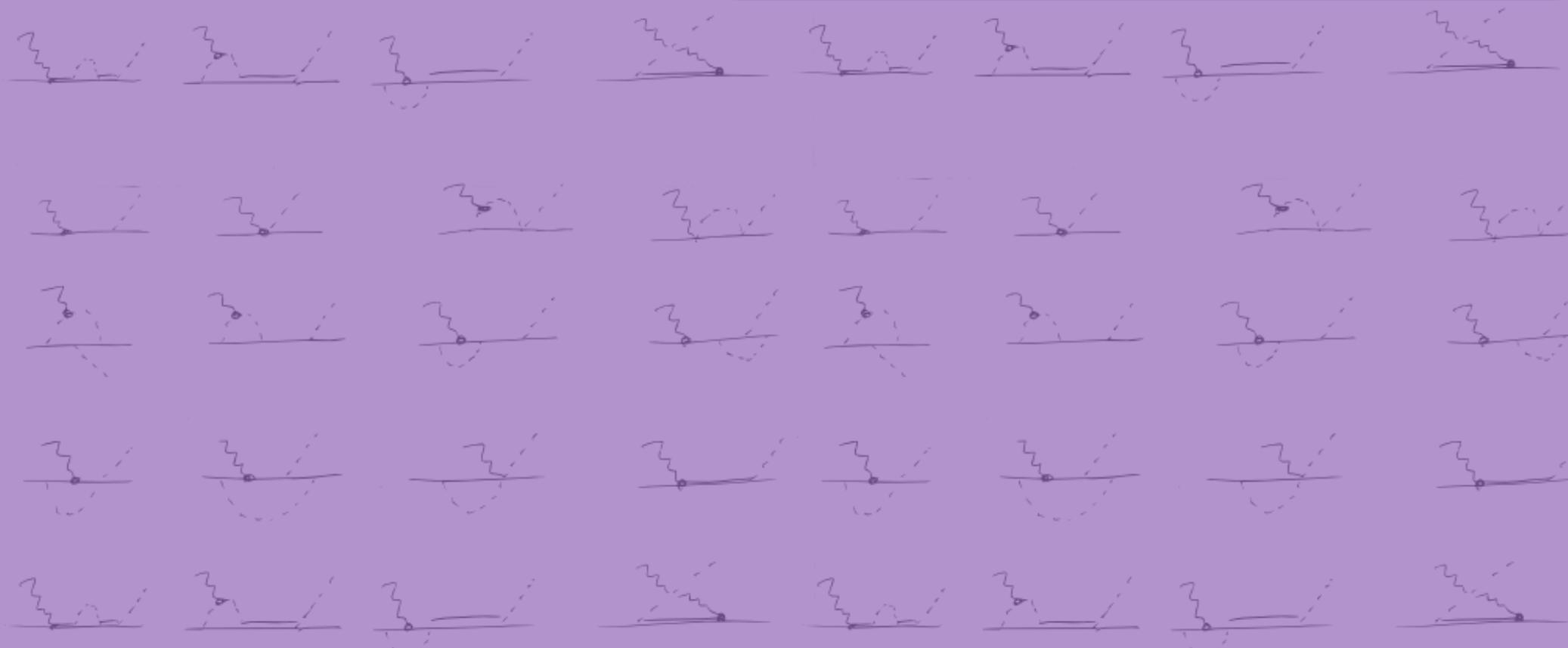
3rd order covariant theory.



Hybrid calculations.

4th order heavy baryon description.
Calculated for S and P-waves, up to L=1.
Bernard et al, (1996) Z. Phys;
(2001) Eur. Phys. J.

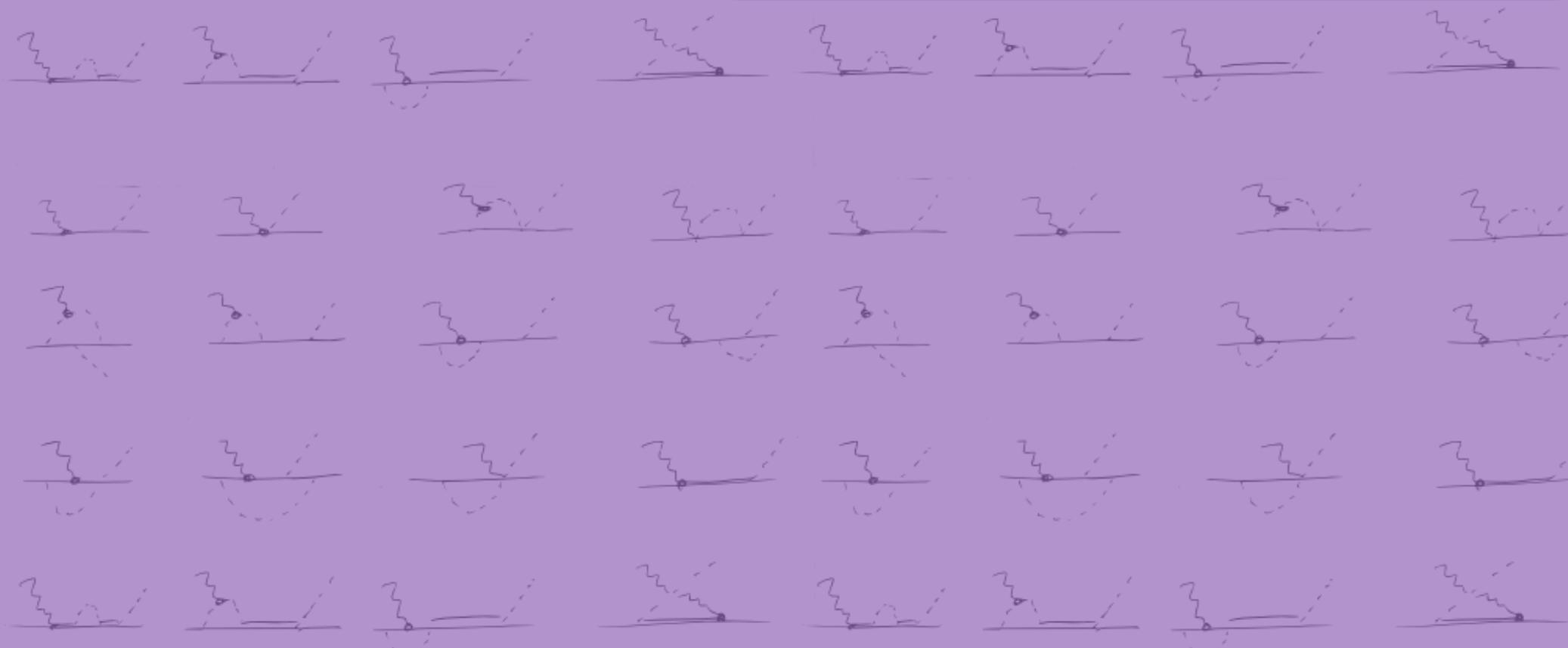
3rd order covariant theory.
No truncation of angular momentum.



Hybrid calculations.

4th order heavy baryon description.
Calculated for S and P-waves, up to L=1.
Bernard et al, (1996) Z. Phys;
(2001) Eur. Phys. J.

3rd order covariant theory.
No truncation of angular momentum.
Can extract D-waves and beyond.



Hybrid calculations.

4th order heavy baryon description.
Calculated for S and P-waves, up to L=1.
Bernard et al, (1996) Z. Phys;
(2001) Eur. Phys. J.

3rd order covariant theory.
No truncation of angular momentum.
Can extract D-waves and beyond.
Bernard et al, (1992) Nucl. Phys. B;
(1994) Phys. Rep.

Hybrid calculations.

4th order heavy baryon description.
Calculated for S and P-waves, up to L=1.
Bernard et al, (1996) Z. Phys;
(2001) Eur. Phys. J.

3rd order covariant theory.
No truncation of angular momentum.
Can extract D-waves and beyond.
Bernard et al, (1992) Nucl. Phys. B;
(1994) Phys. Rep.

4th order LECs used:

$$E_{0+}^{ct} = ea_2\omega^3 + ea_1\omega M_\pi^2$$

$$P_1^{ct} = \frac{eg_A |\vec{k}_\pi| \omega^2}{m_N (4\pi F_\pi)^3} \xi_1$$

$$P_2^{ct} = \frac{eg_A |\vec{k}_\pi| \omega^2}{m_N (4\pi F_\pi)^3} \xi_2$$

$$P_3^{ct} = e |\vec{k}_\pi| b_P \left(\omega - \frac{M_\pi^2}{2m} \right)$$

Hybrid calculations.

4th order heavy baryon description.
Calculated for S and P-waves, up to L=1.
Bernard et al, (1996) Z. Phys;
(2001) Eur. Phys. J.

3rd order covariant theory.
No truncation of angular momentum.
Can extract D-waves and beyond.
Bernard et al, (1992) Nucl. Phys. B;
(1994) Phys. Rep.

4th order LECs used:

$$E_{0+}^{ct} = ea_2\omega^3 + ea_1\omega M_\pi^2$$

$$P_1^{ct} = \frac{eg_A |\vec{k}_\pi| \omega^2}{m_N (4\pi F_\pi)^3} \xi_1$$

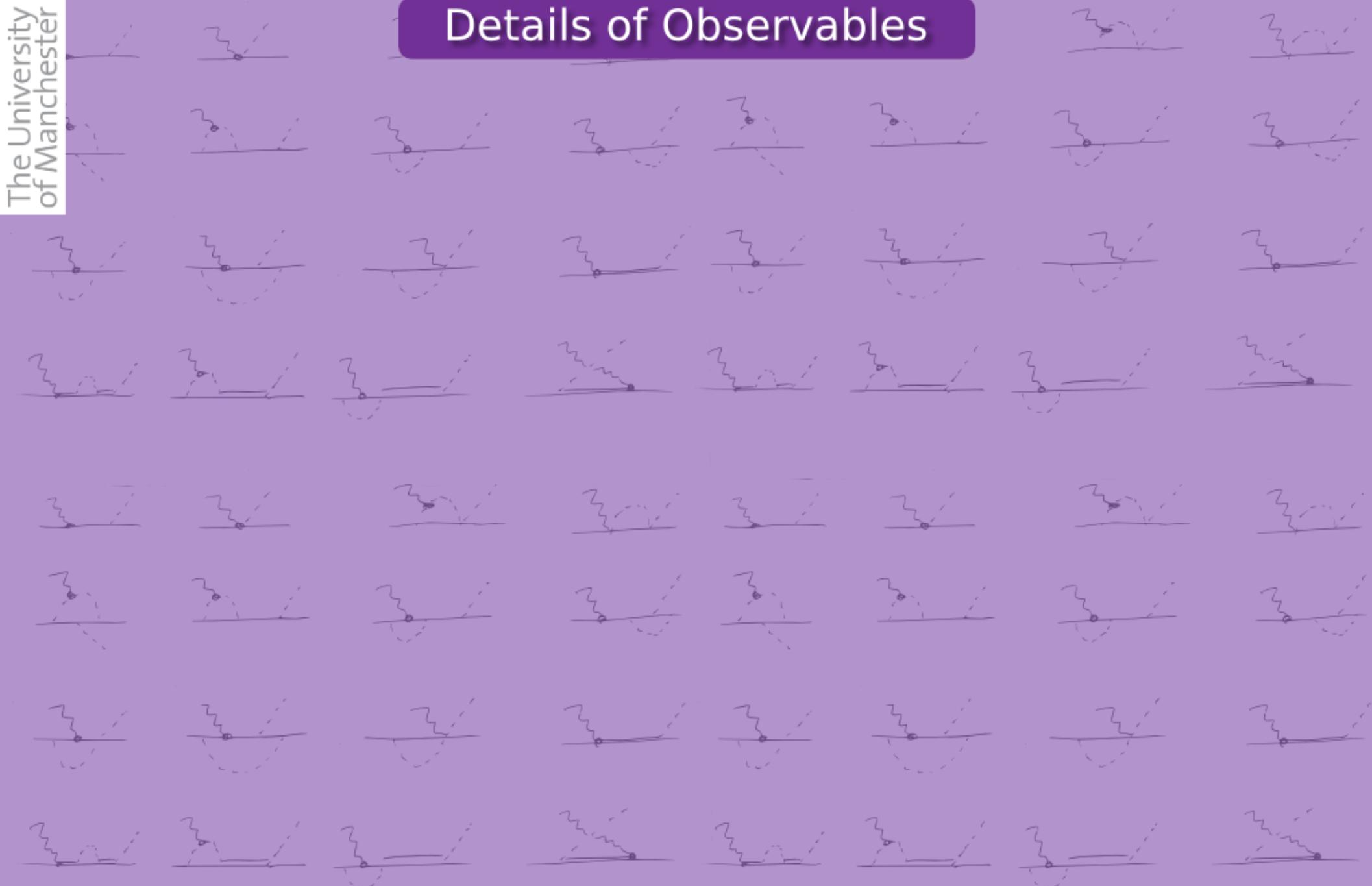
$$P_2^{ct} = \frac{eg_A |\vec{k}_\pi| \omega^2}{m_N (4\pi F_\pi)^3} \xi_2$$

$$P_3^{ct} = e |\vec{k}_\pi| b_P \left(\omega - \frac{M_\pi^2}{2m} \right)$$

We extract the relativistic D-waves to construct a hybrid theory.

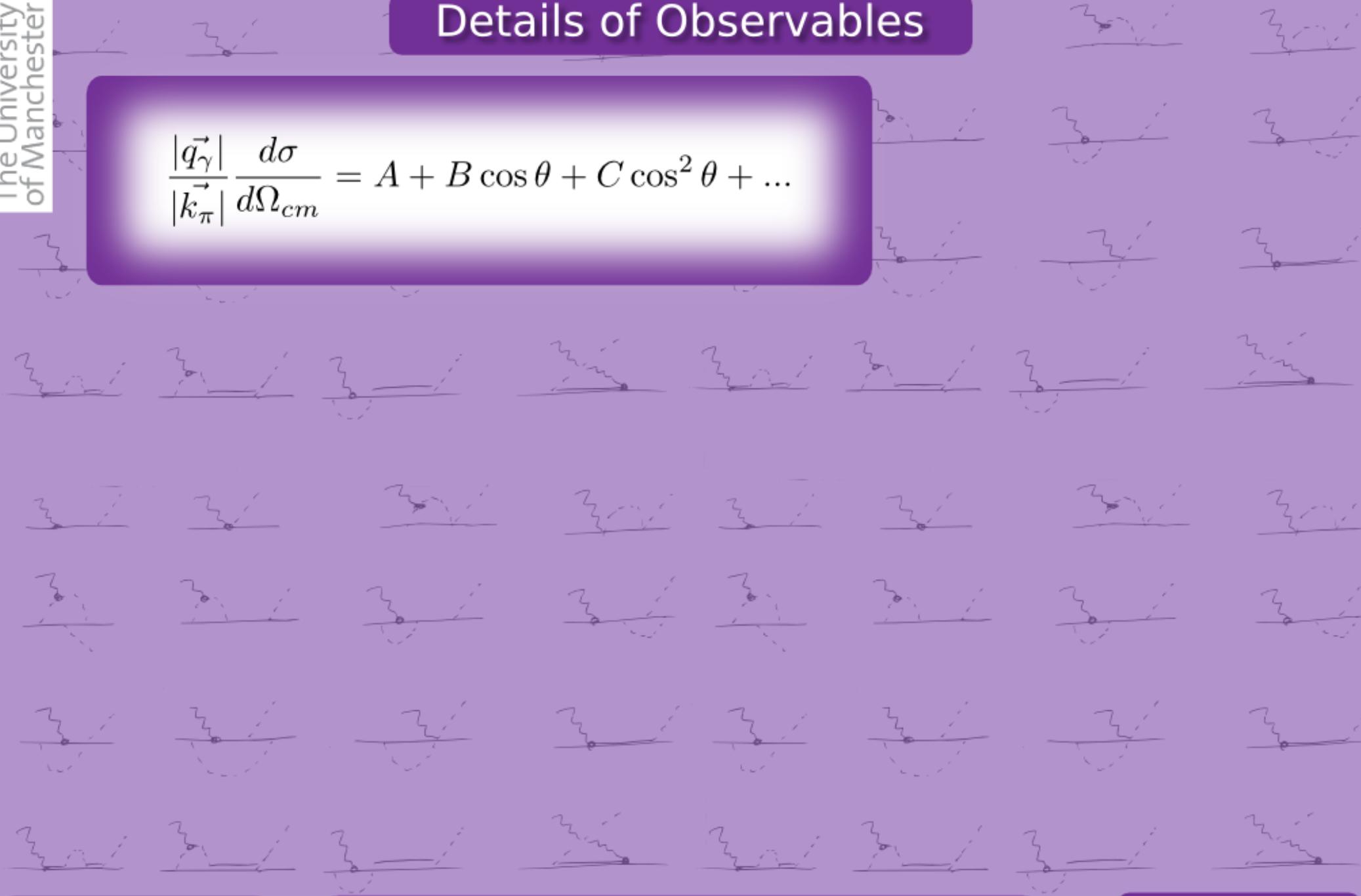
We expect D-waves to be suppressed in the HB description.

Details of Observables



Details of Observables

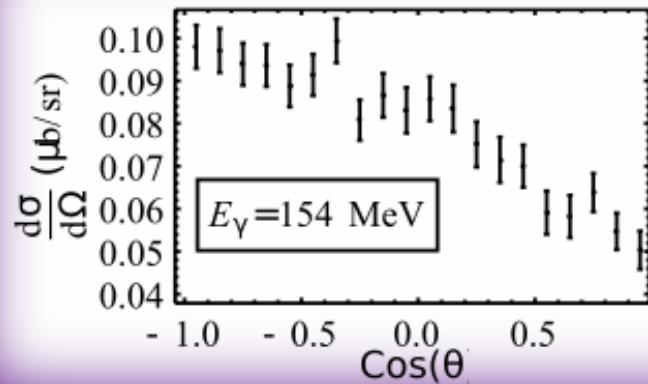
$$\frac{|\vec{q}_\gamma|}{|\vec{k}_\pi|} \frac{d\sigma}{d\Omega_{cm}} = A + B \cos \theta + C \cos^2 \theta + \dots$$



Details of Observables

$$\frac{|\vec{q}_\gamma|}{|\vec{k}_\pi|} \frac{d\sigma}{d\Omega_{cm}} = A + B \cos \theta + C \cos^2 \theta + \dots$$

Looking at the data from MAMI:

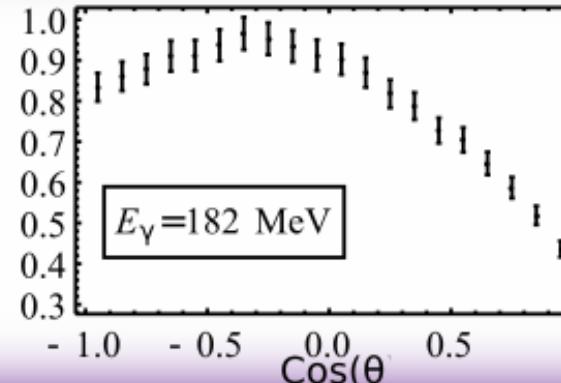
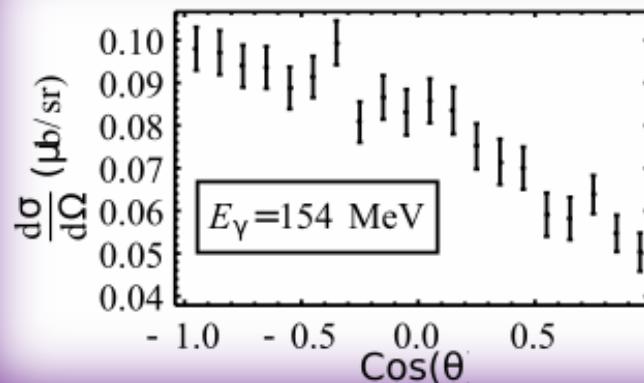


Hornidge et al, (2013) PRL

Details of Observables

$$\frac{|\vec{q}_\gamma|}{|\vec{k}_\pi|} \frac{d\sigma}{d\Omega_{cm}} = A + B \cos \theta + C \cos^2 \theta + \dots$$

Looking at the data from MAMI:

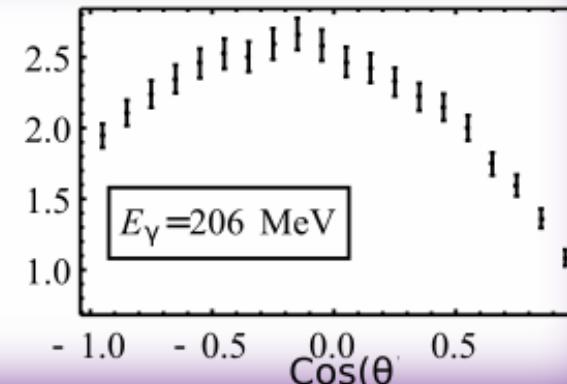
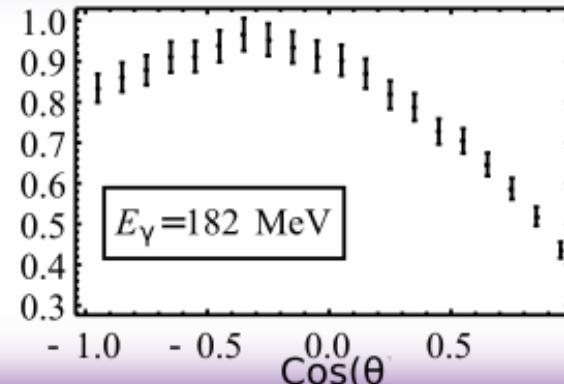
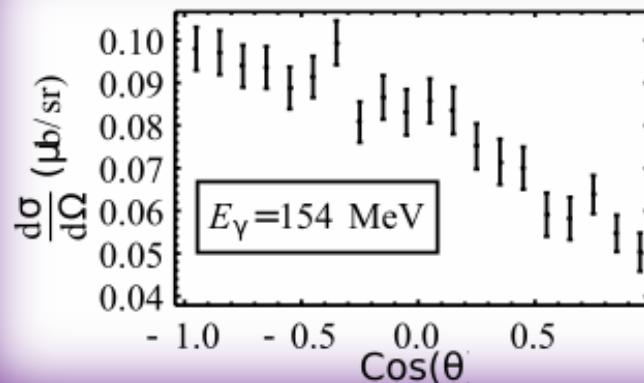


Hornidge et al, (2013) PRL

Details of Observables

$$\frac{|\vec{q}_\gamma|}{|\vec{k}_\pi|} \frac{d\sigma}{d\Omega_{cm}} = A + B \cos \theta + C \cos^2 \theta + \dots$$

Looking at the data from MAMI:



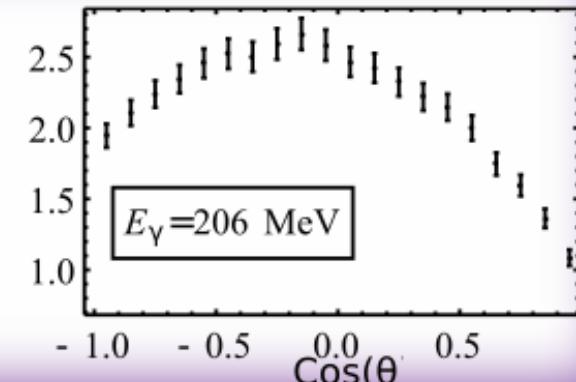
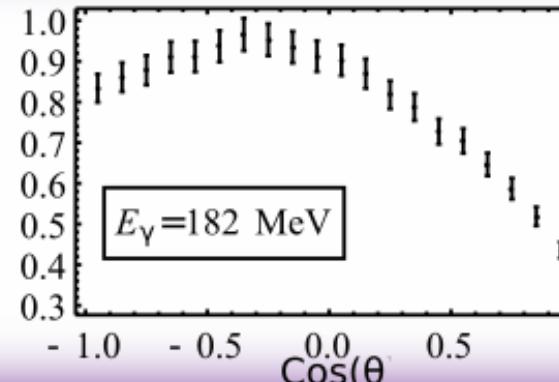
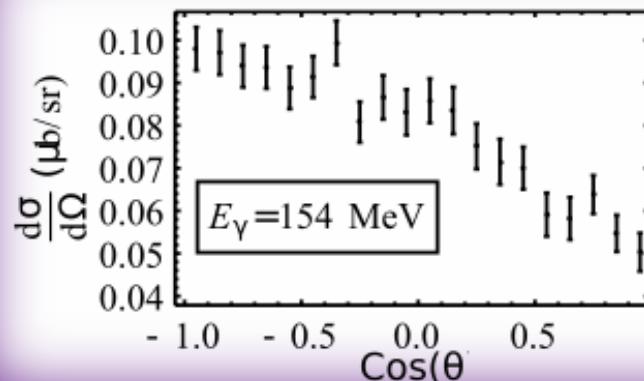
Hornidge et al, (2013) PRL

Details of Observables

$$\frac{|\vec{q}_\gamma|}{|\vec{k}_\pi|} \frac{d\sigma}{d\Omega_{cm}} = A + B \cos \theta + C \cos^2 \theta + \dots$$

Increasing energy allows access to more multipoles, changing the shape.

Looking at the data from MAMI:



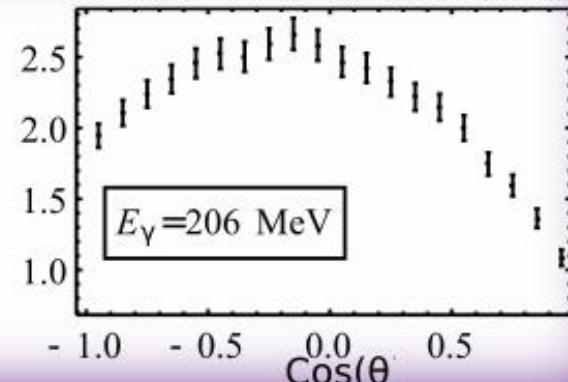
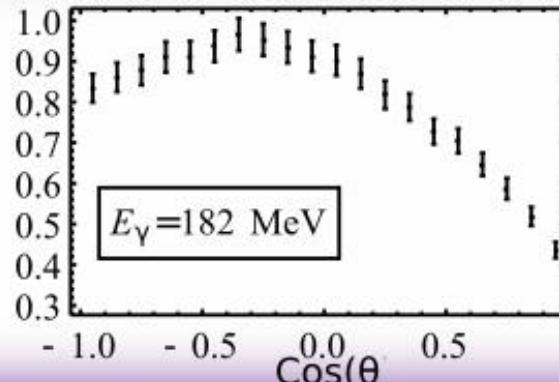
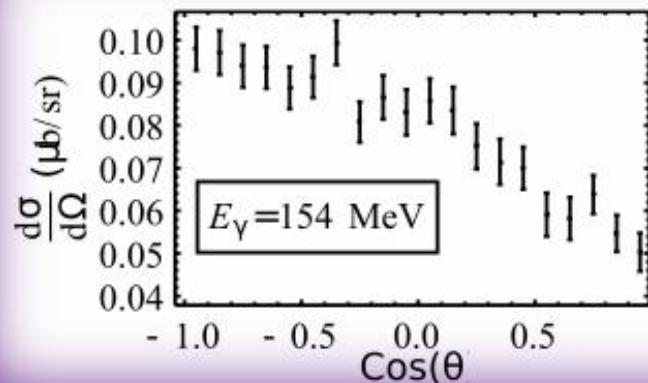
Hornidge et al, (2013) PRL

Details of Observables

$$\frac{|\vec{q}_\gamma|}{|\vec{k}_\pi|} \frac{d\sigma}{d\Omega_{cm}} = A + B \cos \theta + C \cos^2 \theta + \dots$$

Increasing energy allows access to more multipoles, changing the shape.

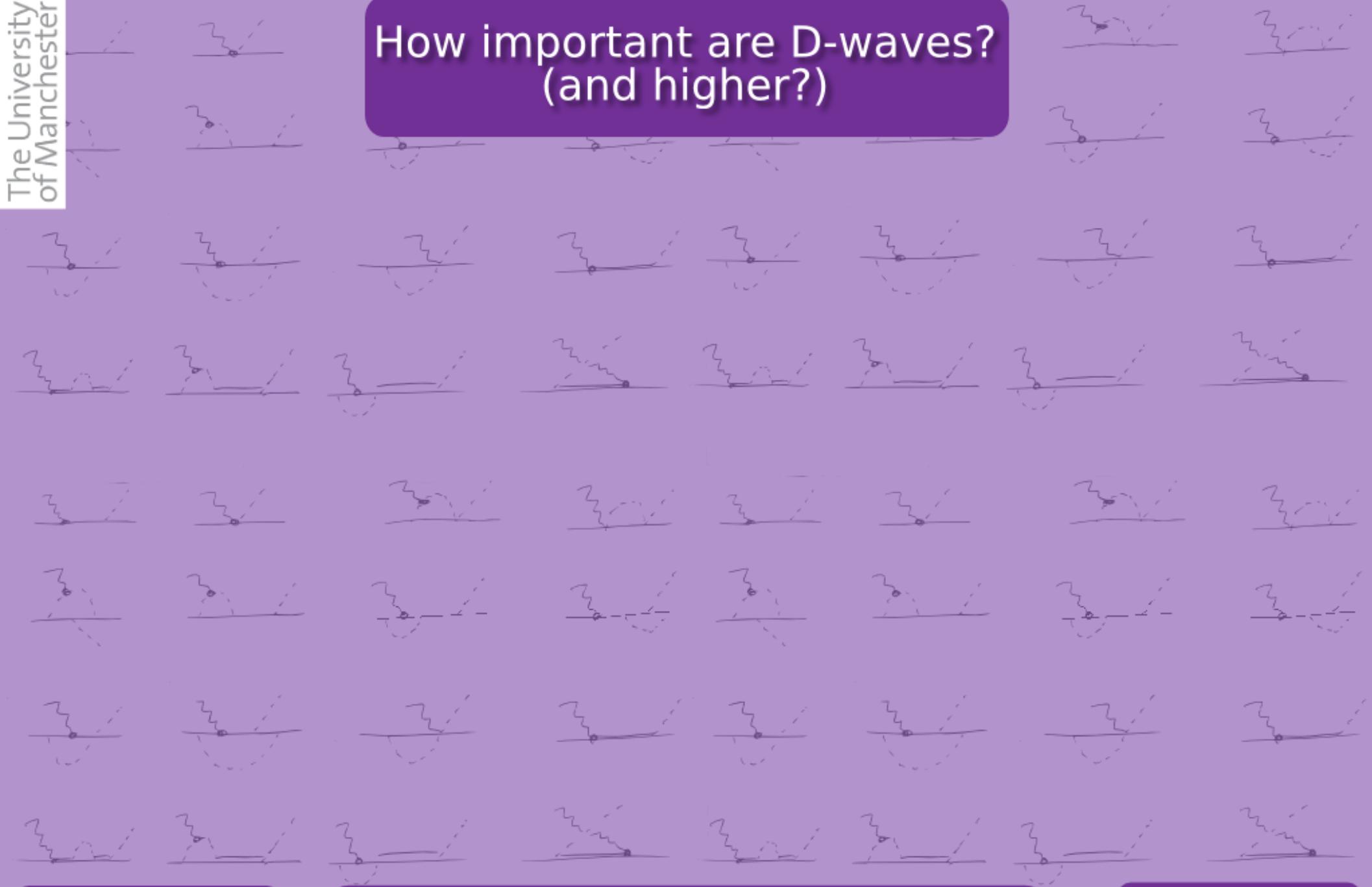
Looking at the data from MAMI:



Hornidge et al, (2013) PRL

$$\Sigma = \frac{d\sigma^\perp - d\sigma^\parallel}{d\sigma^\perp + d\sigma^\parallel} = \frac{|\vec{k}_\pi| \sin^2 \theta}{2|\vec{q}_\gamma|} \left(\frac{d\sigma}{d\Omega_{cm}} \right)^{-1} (|P_3|^2 - |P_2|^2 + \dots)$$

How important are D-waves?
(and higher?)



How important are D-waves?
(and higher?)

$$\frac{|\vec{q}_\gamma|}{|\vec{k}_\pi|} \frac{d\sigma}{d\Omega_{cm}} = T_0(W) + T_1(W)\mathcal{P}_1(\theta) + T_2(W)\mathcal{P}_2(\theta) + T_3(W)\mathcal{P}_3(\theta) + \dots$$

How important are D-waves?
(and higher?)

$$\frac{|\vec{q}_\gamma|}{|\vec{k}_\pi|} \frac{d\sigma}{d\Omega_{cm}} = T_0(W) + T_1(W)\mathcal{P}_1(\theta) + T_2(W)\mathcal{P}_2(\theta) + T_3(W)\mathcal{P}_3(\theta) + \dots$$

$$T_0 = S \times S + P \times P + D \times D + \dots$$

How important are D-waves? (and higher?)

$$\frac{|\vec{q}_\gamma|}{|\vec{k}_\pi|} \frac{d\sigma}{d\Omega_{cm}} = T_0(W) + T_1(W)\mathcal{P}_1(\theta) + T_2(W)\mathcal{P}_2(\theta) + T_3(W)\mathcal{P}_3(\theta) + \dots$$

$$T_0 = S \times S + P \times P + D \times D + \dots$$

$$T_1 = S \times P + P \times P + D \times F + \dots$$

How important are D-waves? (and higher?)

$$\frac{|\vec{q}_\gamma|}{|\vec{k}_\pi|} \frac{d\sigma}{d\Omega_{cm}} = T_0(W) + T_1(W)\mathcal{P}_1(\theta) + T_2(W)\mathcal{P}_2(\theta) + T_3(W)\mathcal{P}_3(\theta) + \dots$$

$$T_0 = S \times S + P \times P + D \times D + \dots$$

$$T_1 = S \times P + P \times P + D \times F + \dots$$

$$T_2 = S \times D + P \times P + D \times D + P \times F \dots$$

How important are D-waves? (and higher?)

$$\frac{|\vec{q}_\gamma|}{|\vec{k}_\pi|} \frac{d\sigma}{d\Omega_{cm}} = T_0(W) + T_1(W)\mathcal{P}_1(\theta) + T_2(W)\mathcal{P}_2(\theta) + T_3(W)\mathcal{P}_3(\theta) + \dots$$

$$T_0 = S \times S + P \times P + D \times D + \dots$$

$$T_1 = S \times P + P \times P + D \times F + \dots$$

$$T_2 = S \times D + P \times P + D \times D + P \times F \dots$$

$$T_3 = P \times D + \dots \quad T_4 = D \times D + \dots$$

How important are D-waves? (and higher?)

$$\frac{|\vec{q}_\gamma|}{|\vec{k}_\pi|} \frac{d\sigma}{d\Omega_{cm}} = T_0(W) + T_1(W)\mathcal{P}_1(\theta) + T_2(W)\mathcal{P}_2(\theta) + T_3(W)\mathcal{P}_3(\theta) + \dots$$

$$T_0 = S \times S + P \times P + D \times D + \dots$$

$$T_1 = S \times P + P \times P + D \times F + \dots$$

$$T_2 = S \times D + P \times P + D \times D + P \times F \dots$$

$$T_3 = P \times D + \dots \quad T_4 = D \times D + \dots$$

D-wave amplitudes
are small.

How important are D-waves? (and higher?)

$$\frac{|\vec{q}_\gamma|}{|\vec{k}_\pi|} \frac{d\sigma}{d\Omega_{cm}} = T_0(W) + T_1(W)\mathcal{P}_1(\theta) + T_2(W)\mathcal{P}_2(\theta) + T_3(W)\mathcal{P}_3(\theta) + \dots$$

$$T_0 = S \times S + P \times P + D \times D + \dots$$

$$T_1 = S \times P + P \times P + D \times F + \dots$$

$$T_2 = S \times D + P \times P + D \times D + P \times F \dots$$

$$T_3 = P \times D + \dots \quad T_4 = D \times D + \dots$$

D-wave amplitudes
are small.
Interference from
D-waves might not be.

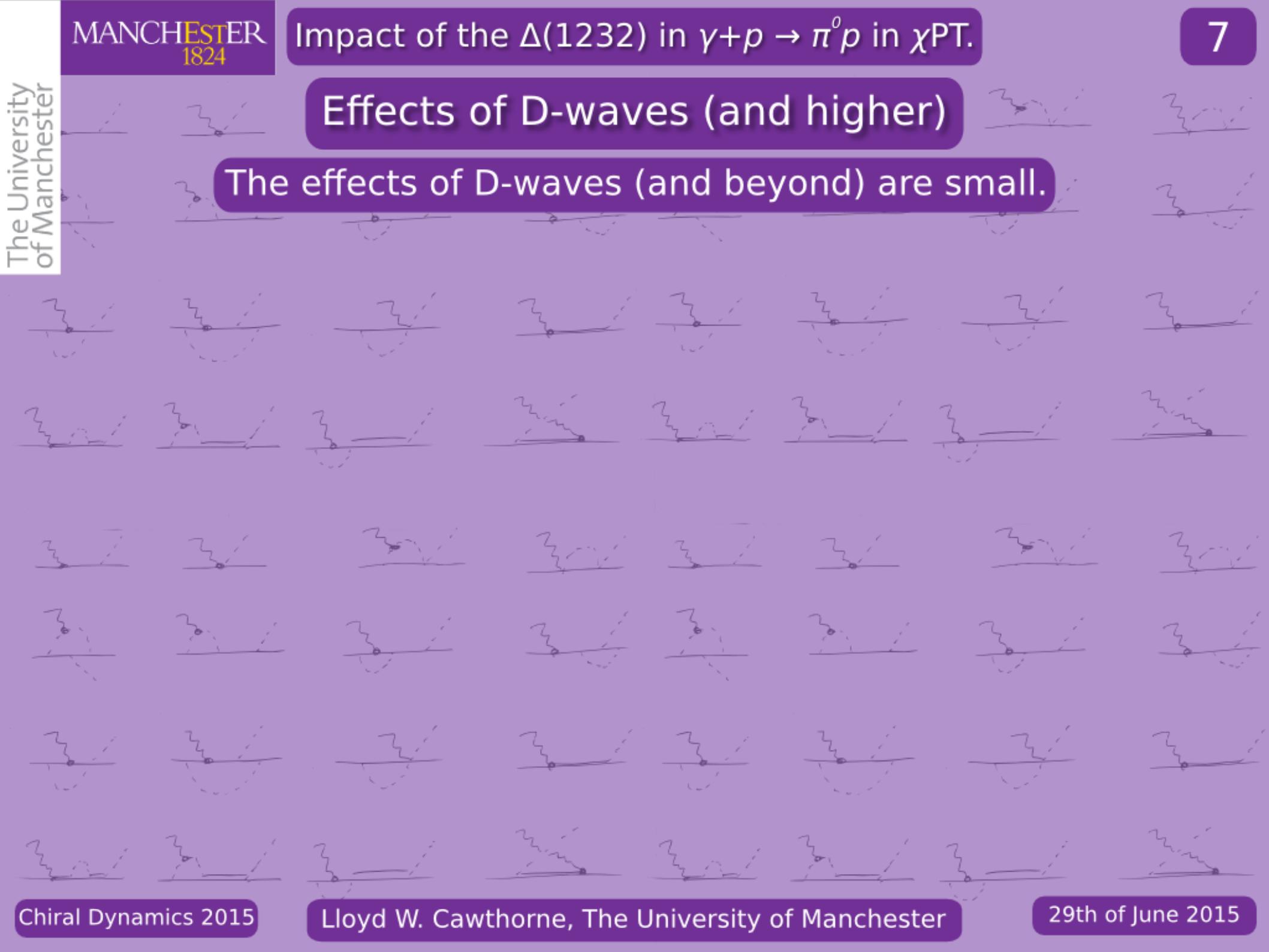
Fernández-Ramírez, et al.
(2009) Phys. Rev. C.

Effects of D-waves (and higher)



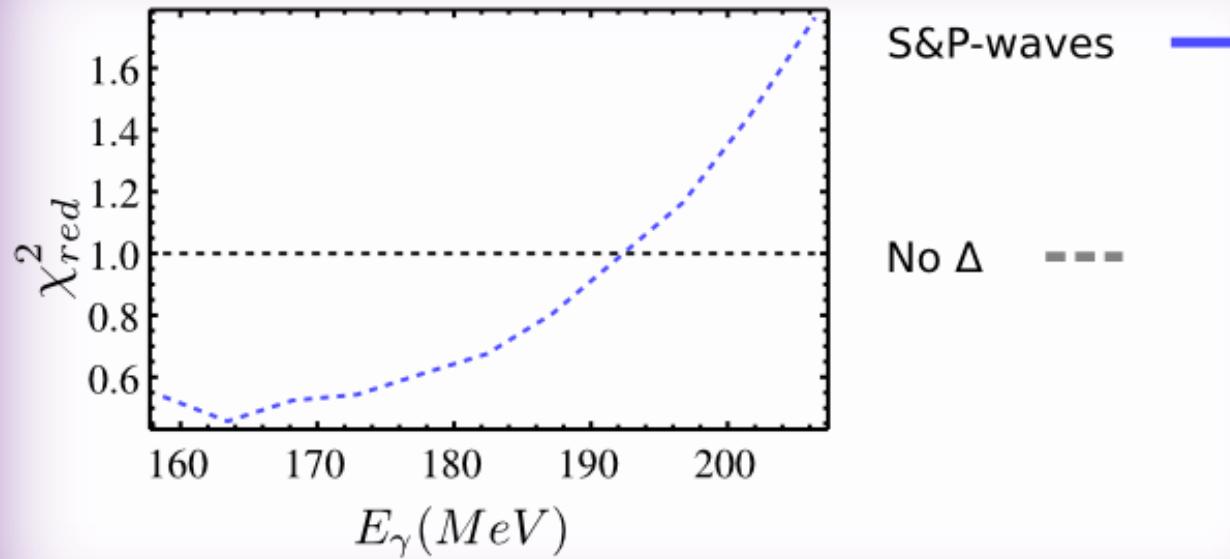
Effects of D-waves (and higher)

The effects of D-waves (and beyond) are small.



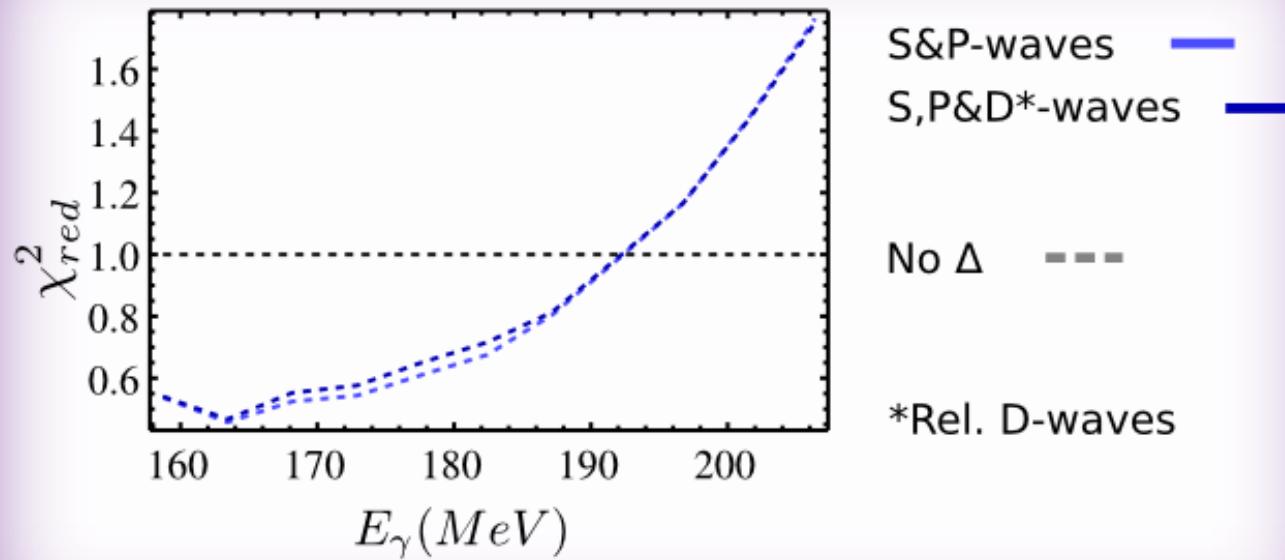
Effects of D-waves (and higher)

The effects of D-waves (and beyond) are small.



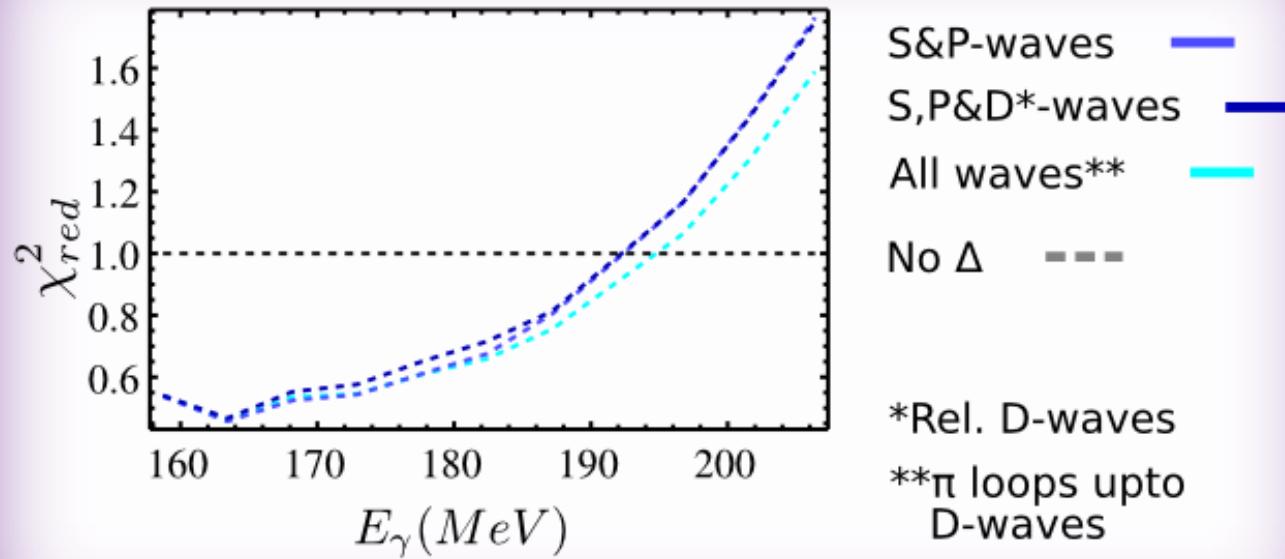
Effects of D-waves (and higher)

The effects of D-waves (and beyond) are small.



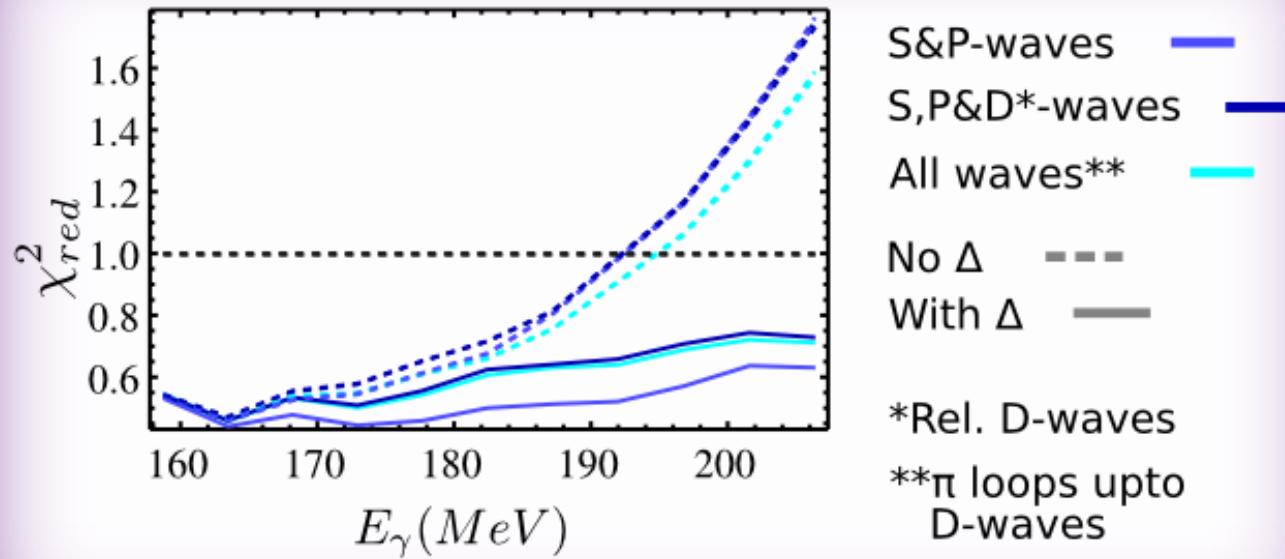
Effects of D-waves (and higher)

The effects of D-waves (and beyond) are small.



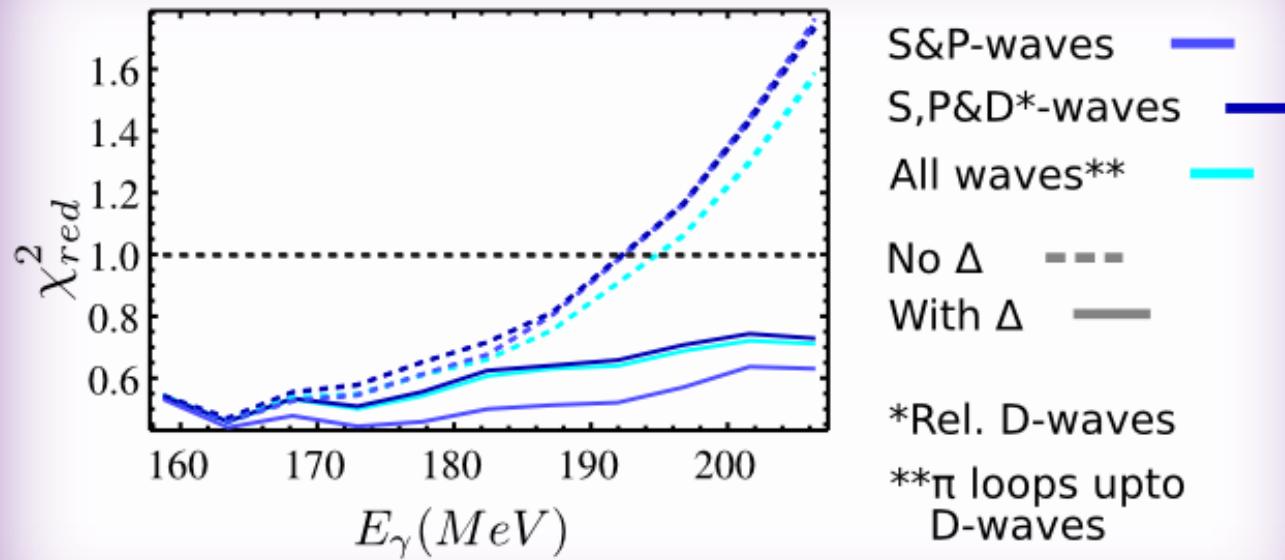
Effects of D-waves (and higher)

The effects of D-waves (and beyond) are small.



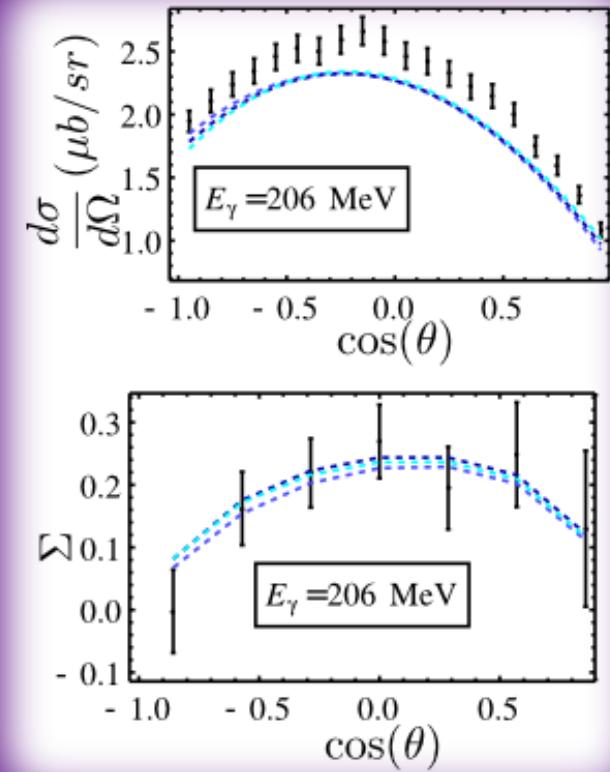
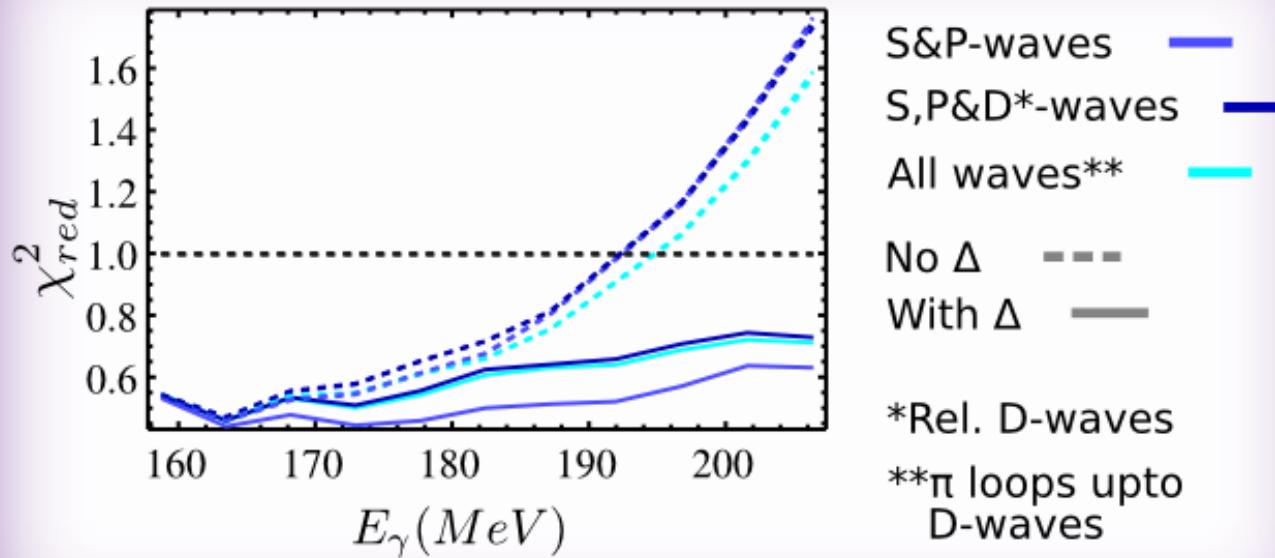
Effects of D-waves (and higher)

The effects of D-waves (and beyond) are small.

The small effect of L=2 states (and above) are dwarfed by the Δ .

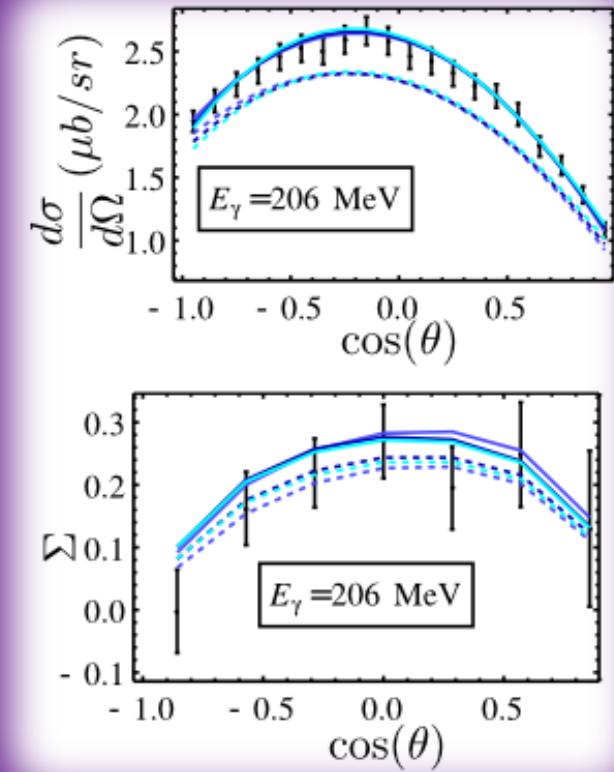
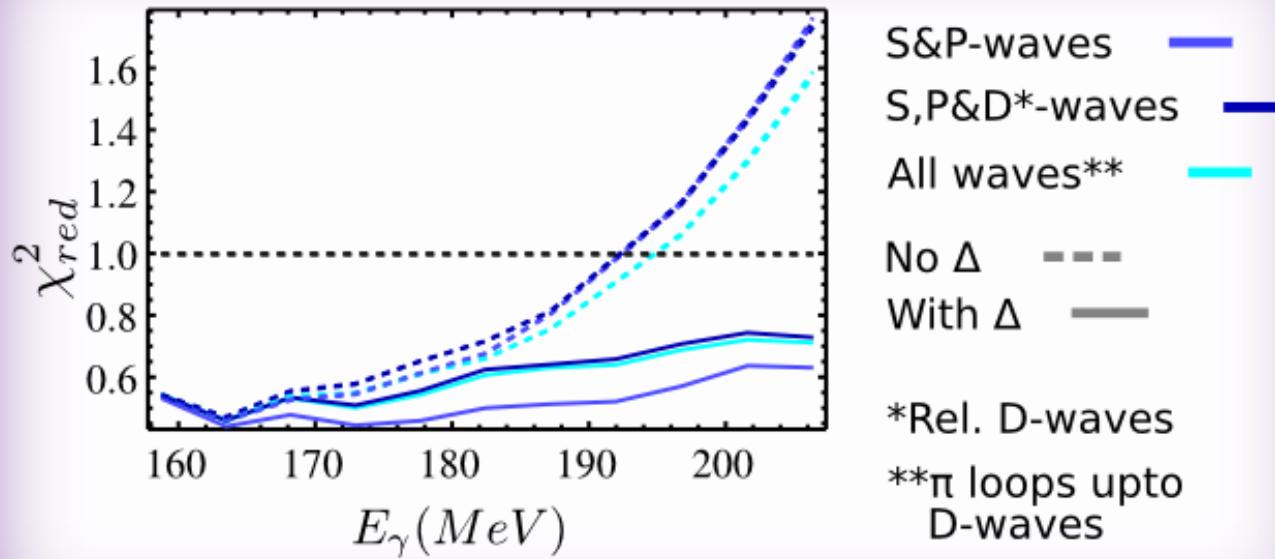
Effects of D-waves (and higher)

The effects of D-waves (and beyond) are small.

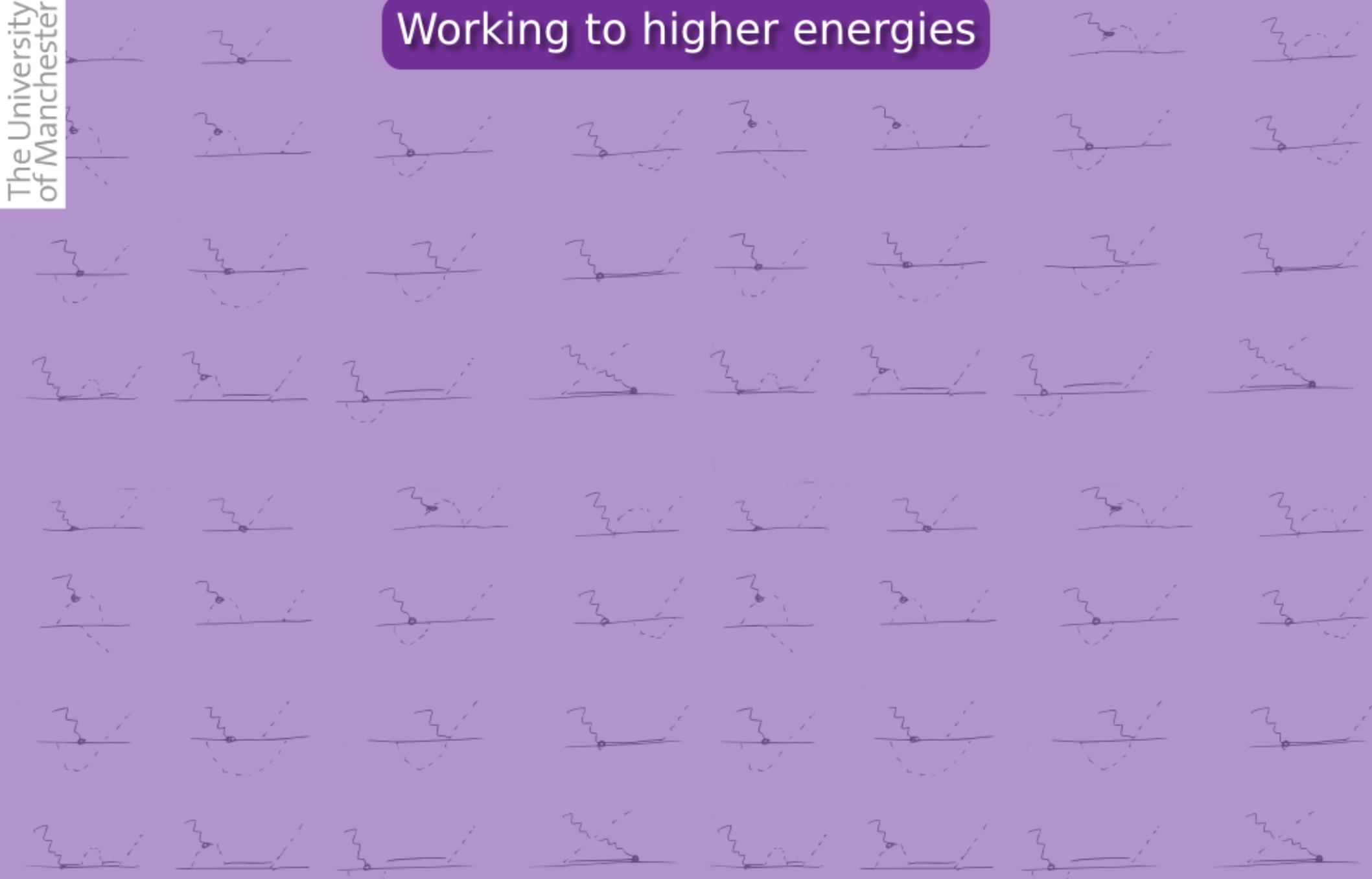
The small effect of L=2 states (and above) are dwarfed by the Δ .

Effects of D-waves (and higher)

The effects of D-waves (and beyond) are small.

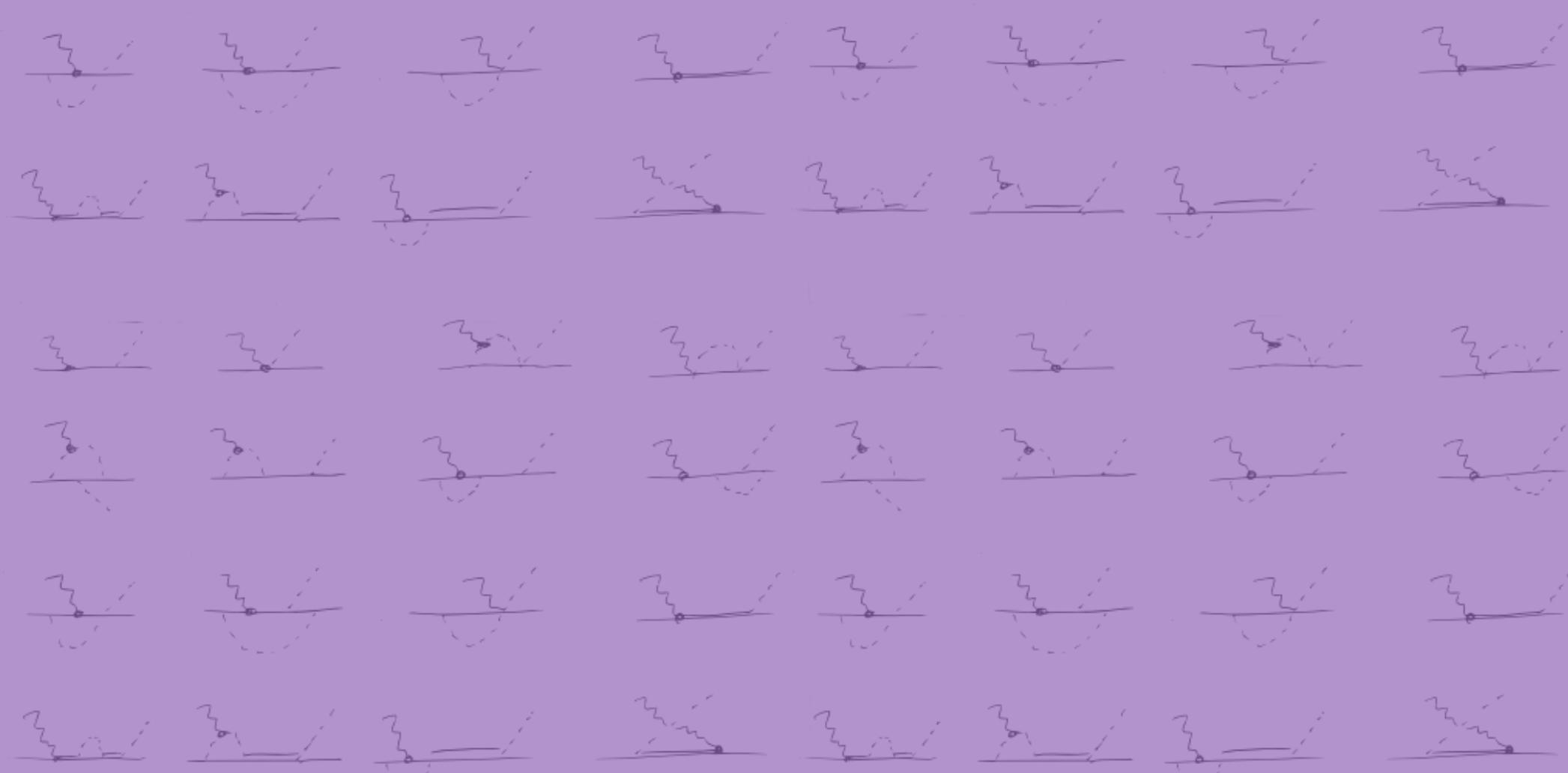
The small effect of L=2 states (and above) are dwarfed by the Δ .

Working to higher energies



Working to higher energies

One can include π loop diagrams containing a Δ propagator.



Working to higher energies

One can include π loop diagrams containing a Δ propagator.

Close to threshold: $\omega \sim M_\pi \approx 140 MeV$

Working to higher energies

One can include π loop diagrams containing a Δ propagator.

Close to threshold: $\omega \sim M_\pi \approx 140\text{MeV}$ SB scale: $\Lambda_{SB} \approx 700\text{MeV}$

Working to higher energies

One can include π loop diagrams containing a Δ propagator.

Close to threshold: $\omega \sim M_\pi \approx 140\text{MeV}$ SB scale: $\Lambda_{SB} \approx 700\text{MeV}$

Mass difference: $\Delta_M = m_\Delta - m_N \approx 290\text{MeV}$

Pascalutsa, et al. (2006), Phys. Rev. D

Working to higher energies

One can include π loop diagrams containing a Δ propagator.

Close to threshold: $\omega \sim M_\pi \approx 140\text{MeV}$ SB scale: $\Lambda_{SB} \approx 700\text{MeV}$

Mass difference: $\Delta_M = m_\Delta - m_N \approx 290\text{MeV}$ $M_\pi \ll \Delta_M$

Pascalutsa, et al. (2006), Phys. Rev. D

Working to higher energies

One can include π loop diagrams containing a Δ propagator.

Close to threshold: $\omega \sim M_\pi \approx 140\text{MeV}$ SB scale: $\Lambda_{SB} \approx 700\text{MeV}$

Mass difference: $\Delta_M = m_\Delta - m_N \approx 290\text{MeV}$ $M_\pi \ll \Delta_M$

Two scales:

Pascalutsa, et al. (2006), Phys. Rev. D

Working to higher energies

One can include π loop diagrams containing a Δ propagator.

Close to threshold: $\omega \sim M_\pi \approx 140\text{MeV}$ SB scale: $\Lambda_{SB} \approx 700\text{MeV}$

Mass difference: $\Delta_M = m_\Delta - m_N \approx 290\text{MeV}$ $M_\pi \ll \Delta_M$

$$P = \frac{M_\pi}{\Lambda} \approx 0.2$$

Two scales:

Pascalutsa, et al. (2006), Phys. Rev. D

Working to higher energies

One can include π loop diagrams containing a Δ propagator.

Close to threshold: $\omega \sim M_\pi \approx 140\text{MeV}$ SB scale: $\Lambda_{SB} \approx 700\text{MeV}$

Mass difference: $\Delta_M = m_\Delta - m_N \approx 290\text{MeV}$ $M_\pi \ll \Delta_M$

$$P = \frac{M_\pi}{\Lambda} \approx 0.2$$

Two scales:

$$\epsilon = \frac{\Delta_M}{\Lambda} \approx 0.4$$

Pascalutsa, et al. (2006), Phys. Rev. D

Working to higher energies

One can include π loop diagrams containing a Δ propagator.

Close to threshold: $\omega \sim M_\pi \approx 140\text{MeV}$ SB scale: $\Lambda_{SB} \approx 700\text{MeV}$

Mass difference: $\Delta_M = m_\Delta - m_N \approx 290\text{MeV}$ $M_\pi \ll \Delta_M$

$$P = \frac{M_\pi}{\Lambda} \approx 0.2$$

Two scales:

$$\epsilon = \frac{\Delta_M}{\Lambda} \approx 0.4$$

$$\delta \approx \frac{\Delta_M}{\Lambda} \approx \left(\frac{M_\pi}{\Lambda}\right)^{1/2}$$

Pascalutsa, et al. (2006), Phys. Rev. D

Working to higher energies

One can include π loop diagrams containing a Δ propagator.

Close to threshold: $\omega \sim M_\pi \approx 140\text{MeV}$ SB scale: $\Lambda_{SB} \approx 700\text{MeV}$

Mass difference: $\Delta_M = m_\Delta - m_N \approx 290\text{MeV}$ $M_\pi \ll \Delta_M$

$$P = \frac{M_\pi}{\Lambda} \approx 0.2$$

Two scales:

$$\epsilon = \frac{\Delta_M}{\Lambda} \approx 0.4$$

$$\delta \approx \frac{\Delta_M}{\Lambda} \approx \left(\frac{M_\pi}{\Lambda}\right)^{1/2} \quad P \approx \delta^2$$

Pascalutsa, et al. (2006), Phys. Rev. D

Working to higher energies

One can include π loop diagrams containing a Δ propagator.

Close to threshold: $\omega \sim M_\pi \approx 140\text{MeV}$ SB scale: $\Lambda_{SB} \approx 700\text{MeV}$

Mass difference: $\Delta_M = m_\Delta - m_N \approx 290\text{MeV}$ $M_\pi \ll \Delta_M$

$$P = \frac{M_\pi}{\Lambda} \approx 0.2$$

Two scales:

$$\epsilon = \frac{\Delta_M}{\Lambda} \approx 0.4$$

$$\delta \approx \frac{\Delta_M}{\Lambda} \approx \left(\frac{M_\pi}{\Lambda}\right)^{1/2} \quad P \approx \delta^2$$

Propagator: $S_\Delta(\omega \sim M_\pi) \propto \frac{1}{\Delta_M \pm \omega}$

Pascalutsa, et al. (2006), Phys. Rev. D

Working to higher energies

One can include π loop diagrams containing a Δ propagator.

Close to threshold: $\omega \sim M_\pi \approx 140\text{MeV}$ SB scale: $\Lambda_{SB} \approx 700\text{MeV}$

Mass difference: $\Delta_M = m_\Delta - m_N \approx 290\text{MeV}$ $M_\pi \ll \Delta_M$

$$P = \frac{M_\pi}{\Lambda} \approx 0.2$$

Two scales:

$$\epsilon = \frac{\Delta_M}{\Lambda} \approx 0.4$$

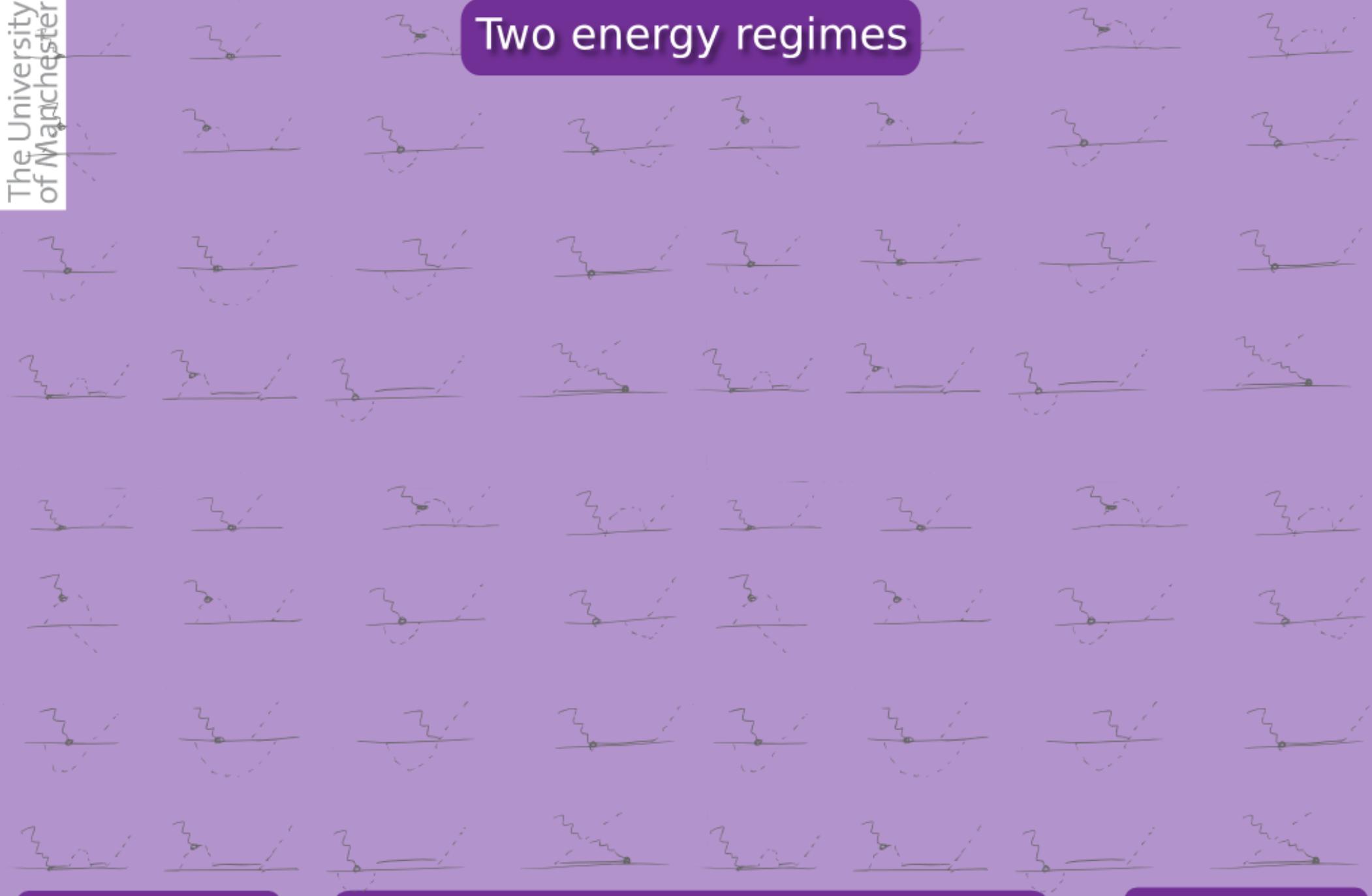
$$\delta \approx \frac{\Delta_M}{\Lambda} \approx \left(\frac{M_\pi}{\Lambda}\right)^{1/2}$$

$$P \approx \delta^2$$

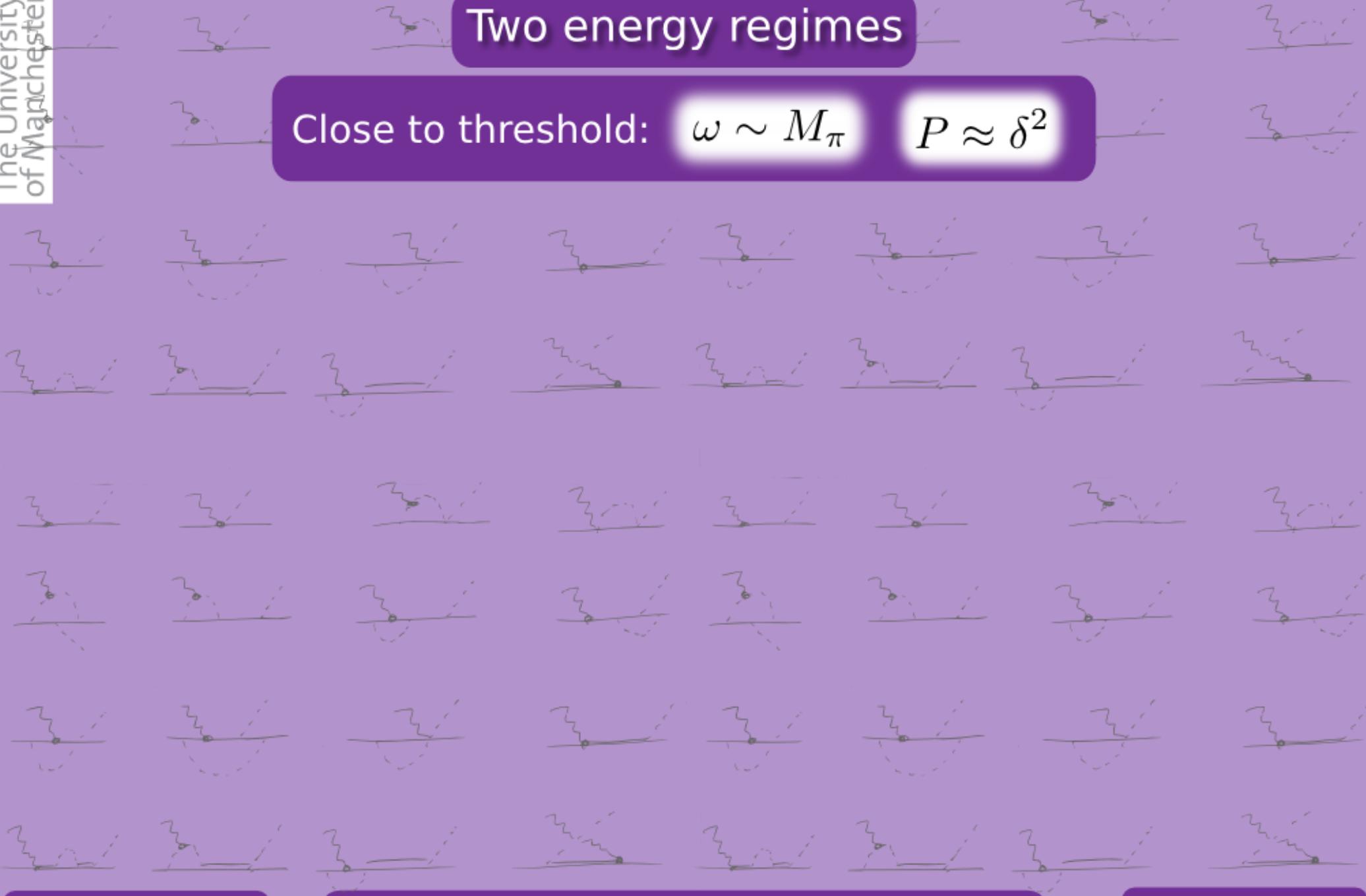
Propagator: $S_\Delta(\omega \sim M_\pi) \propto \frac{1}{\Delta_M \pm \omega}$ scales as δ^{-1}

Pascalutsa, et al. (2006), Phys. Rev. D

Two energy regimes



Two energy regimes

Close to threshold: $\omega \sim M_\pi$ $P \approx \delta^2$ 

Two energy regimes

Close to threshold: $\omega \sim M_\pi$ $P \approx \delta^2$

Close to resonance: $\omega \sim \Delta_M$

Pascalutsa, et al. (2006) Phys. Rev. D

Two energy regimes

Close to threshold: $\omega \sim M_\pi$ $P \approx \delta^2$

Close to resonance: $\omega \sim \Delta_M$

Scales change: $P = \frac{\omega}{\Lambda} \approx \frac{\Delta_M}{\Lambda} = \delta$

Pascalutsa, et al. (2006) Phys. Rev. D

Two energy regimes

Close to threshold: $\omega \sim M_\pi$ $P \approx \delta^2$ Close to resonance: $\omega \sim \Delta_M$

Scales change: $P = \frac{\omega}{\Lambda} \approx \frac{\Delta_M}{\Lambda} = \delta$

Propagator:

$$S_\Delta (\omega \sim \Delta_M) \propto \frac{1}{\Delta_M + i\text{Im}\Sigma_\Delta - \omega}$$

Pascalutsa, et al. (2006) Phys. Rev. D

Two energy regimes

Close to threshold: $\omega \sim M_\pi$ $P \approx \delta^2$ Close to resonance: $\omega \sim \Delta_M$

Scales
change: $P = \frac{\omega}{\Lambda} \approx \frac{\Delta_M}{\Lambda} = \delta$

Self energy: Σ_Δ

Propagator:

$$S_\Delta (\omega \sim \Delta_M) \propto \frac{1}{\Delta_M + i\text{Im}\Sigma_\Delta - \omega}$$

Pascalutsa, et al. (2006) Phys. Rev. D

Two energy regimes

Close to threshold: $\omega \sim M_\pi$ $P \approx \delta^2$ Close to resonance: $\omega \sim \Delta_M$

Scales
change: $P = \frac{\omega}{\Lambda} \approx \frac{\Delta_M}{\Lambda} = \delta$

Propagator:

Self energy: Σ_Δ

given by:

$$S_\Delta (\omega \sim \Delta_M) \propto \frac{1}{\Delta_M + i\text{Im}\Sigma_\Delta - \omega}$$



Pascalutsa, et al. (2006) Phys. Rev. D

Two energy regimes

Close to threshold: $\omega \sim M_\pi$ $P \approx \delta^2$ Close to resonance: $\omega \sim \Delta_M$

Scales change: $P = \frac{\omega}{\Lambda} \approx \frac{\Delta_M}{\Lambda} = \delta$

Propagator:

Self energy: Σ_Δ

given by:

$$S_\Delta (\omega \sim \Delta_M) \propto \frac{1}{\Delta_M + i\text{Im}\Sigma_\Delta - \omega}$$

scales as: δ^3

Pascalutsa, et al. (2006) Phys. Rev. D

Two energy regimes

Close to threshold: $\omega \sim M_\pi$ $P \approx \delta^2$ Close to resonance: $\omega \sim \Delta_M$

Scales change: $P = \frac{\omega}{\Lambda} \approx \frac{\Delta_M}{\Lambda} = \delta$

Propagator:

Self energy: Σ_Δ

given by:

$$S_\Delta(\omega \sim \Delta_M) \propto \frac{1}{\Delta_M + i\text{Im}\Sigma_\Delta - \omega}$$

scales as: δ^3

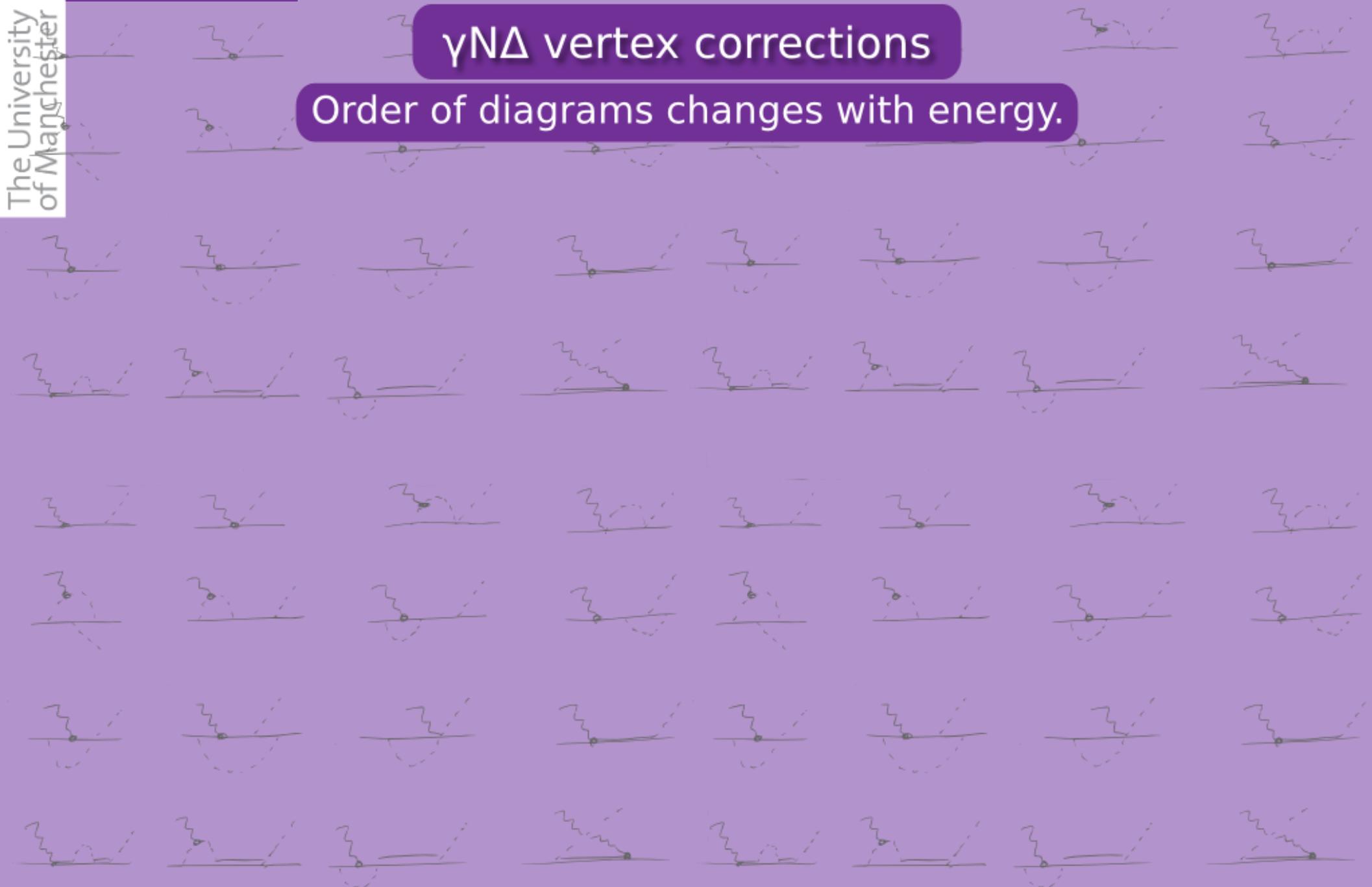
$$S_\Delta(\omega \sim \Delta_M) \text{ scales as: } \delta^{-3}$$

Pascalutsa, et al. (2006) Phys. Rev. D

$\gamma N\Delta$ vertex corrections

$\gamma N\Delta$ vertex corrections

Order of diagrams changes with energy.



$\gamma N\Delta$ vertex corrections

Order of diagrams changes with energy.

McGovern, et al. (2013) Eur. Phys. J; Pascalutsa, et al. (2006) Phys. Rev. D

$\gamma N\Delta$ vertex corrections

Order of diagrams changes with energy.

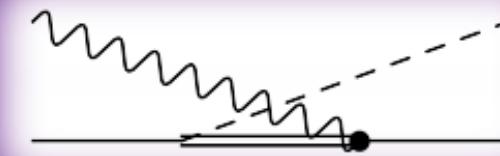
Tree level:

McGovern, et al. (2013) Eur. Phys. J.; Pascalutsa, et al. (2006) Phs. Rev. D

$\gamma N\Delta$ vertex corrections

Order of diagrams changes with energy.

Tree level:



McGovern, et al. (2013) Eur. Phys. J.; Pascalutsa, et al. (2006) Phys. Rev. D

$\gamma N\Delta$ vertex corrections

Order of diagrams changes with energy.

Tree level:



$$\omega \sim M_\pi \quad eP^2\delta^{-1} \rightarrow e\delta^3$$



McGovern, et al. (2013) Eur. Phys. J; Pascalutsa, et al. (2006) Phs. Rev. D

$\gamma N\Delta$ vertex corrections

Order of diagrams changes with energy.

Tree level:



$$\omega \sim M_\pi \quad eP^2\delta^{-1} \rightarrow e\delta^3$$



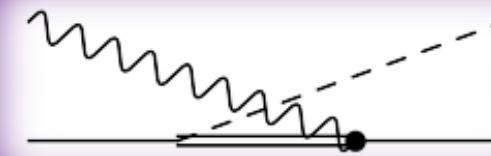
$$eP^2\delta^{-1} \rightarrow e\delta^3$$

McGovern, et al. (2013) Eur. Phys. J.; Pascalutsa, et al. (2006) Phs. Rev. D

$\gamma N\Delta$ vertex corrections

Order of diagrams changes with energy.

Tree level:



$$\omega \sim M_\pi \quad eP^2\delta^{-1} \rightarrow e\delta^3$$

$$\omega \sim \Delta_M \quad eP^2\delta^{-3} \rightarrow e\delta^{-1}$$

McGovern, et al. (2013) Eur. Phys. J.; Pascalutsa, et al. (2006) Phs. Rev. D

$\gamma N\Delta$ vertex corrections

Order of diagrams changes with energy.

Tree level:



$$\omega \sim M_\pi \quad eP^2\delta^{-1} \rightarrow e\delta^3$$

$$\omega \sim \Delta_M \quad eP^2\delta^{-3} \rightarrow e\delta^{-1}$$

$$eP^2\delta^{-1} \rightarrow e\delta^3$$

$$eP^2\delta^{-1} \rightarrow e\delta$$

McGovern, et al. (2013) Eur. Phys. J.; Pascalutsa, et al. (2006) Phs. Rev. D

$\gamma N\Delta$ vertex corrections

Order of diagrams changes with energy.

Tree level:



$$\omega \sim M_\pi \quad eP^2\delta^{-1} \rightarrow e\delta^3$$

$$\omega \sim \Delta_M \quad eP^2\delta^{-3} \rightarrow e\delta^{-1}$$

$$eP^2\delta^{-1} \rightarrow e\delta^3$$

$$eP^2\delta^{-1} \rightarrow e\delta$$

Loop
corrections:

McGovern, et al. (2013) Eur. Phys. J; Pascalutsa, et al. (2006) Phs. Rev. D

$\gamma N\Delta$ vertex corrections

Order of diagrams changes with energy.

Tree level:

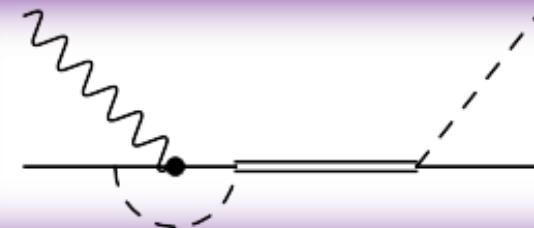


$$\omega \sim M_\pi \quad eP^2\delta^{-1} \rightarrow e\delta^3$$

$$\omega \sim \Delta_M \quad eP^2\delta^{-3} \rightarrow e\delta^{-1}$$

$$eP^2\delta^{-1} \rightarrow e\delta^3$$

$$eP^2\delta^{-1} \rightarrow e\delta$$

Loop
corrections:

McGovern, et al. (2013) Eur. Phys. J; Pascalutsa, et al. (2006) Phs. Rev. D

$\gamma N\Delta$ vertex corrections

Order of diagrams changes with energy.

Tree level:



$$\omega \sim M_\pi \quad eP^2\delta^{-1} \rightarrow e\delta^3$$

$$\omega \sim \Delta_M \quad eP^2\delta^{-3} \rightarrow e\delta^{-1}$$

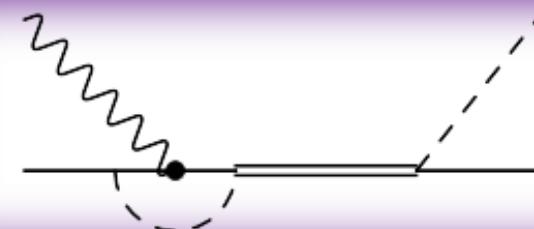


$$eP^2\delta^{-1} \rightarrow e\delta^3$$

$$eP^2\delta^{-1} \rightarrow e\delta$$

Loop
corrections:

$$\omega \sim M_\pi \quad eP^3\delta^{-1} \rightarrow e\delta^5$$



McGovern, et al. (2013) Eur. Phys. J; Pascalutsa, et al. (2006) Phs. Rev. D

$\gamma N\Delta$ vertex corrections

Order of diagrams changes with energy.

Tree level:



$$\omega \sim M_\pi \quad eP^2\delta^{-1} \rightarrow e\delta^3$$

$$\omega \sim \Delta_M \quad eP^2\delta^{-3} \rightarrow e\delta^{-1}$$



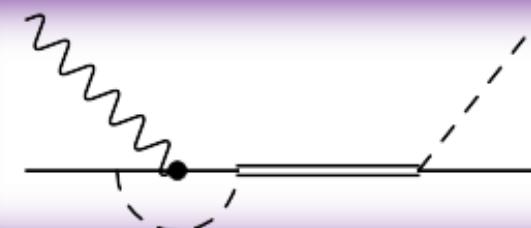
$$eP^2\delta^{-1} \rightarrow e\delta^3$$

$$eP^2\delta^{-1} \rightarrow e\delta$$

Loop
corrections:



$$\omega \sim M_\pi \quad eP^3\delta^{-1} \rightarrow e\delta^5$$



$$eP^4\delta^{-1} \rightarrow e\delta^6$$

McGovern, et al. (2013) Eur. Phys. J; Pascalutsa, et al. (2006) Phs. Rev. D

$\gamma N\Delta$ vertex corrections

Order of diagrams changes with energy.

Tree level:



$$\omega \sim M_\pi \quad eP^2\delta^{-1} \rightarrow e\delta^3$$

$$\omega \sim \Delta_M \quad eP^2\delta^{-3} \rightarrow e\delta^{-1}$$



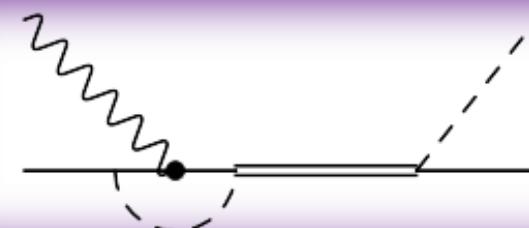
$$eP^2\delta^{-1} \rightarrow e\delta^3$$

$$eP^2\delta^{-1} \rightarrow e\delta$$

Loop
corrections:

$$\omega \sim M_\pi \quad eP^3\delta^{-1} \rightarrow e\delta^5$$

$$\omega \sim \Delta_M \quad eP^3\delta^{-3} \rightarrow e\delta^0$$



$$eP^4\delta^{-1} \rightarrow e\delta^6$$

McGovern, et al. (2013) Eur. Phys. J; Pascalutsa, et al. (2006) Phs. Rev. D

$\gamma N\Delta$ vertex corrections

Order of diagrams changes with energy.

Tree level:



$$\omega \sim M_\pi \quad eP^2\delta^{-1} \rightarrow e\delta^3$$

$$\omega \sim \Delta_M \quad eP^2\delta^{-3} \rightarrow e\delta^{-1}$$



$$eP^2\delta^{-1} \rightarrow e\delta^3$$

$$eP^2\delta^{-1} \rightarrow e\delta$$

Loop
corrections:

$$\omega \sim M_\pi \quad eP^3\delta^{-1} \rightarrow e\delta^5$$

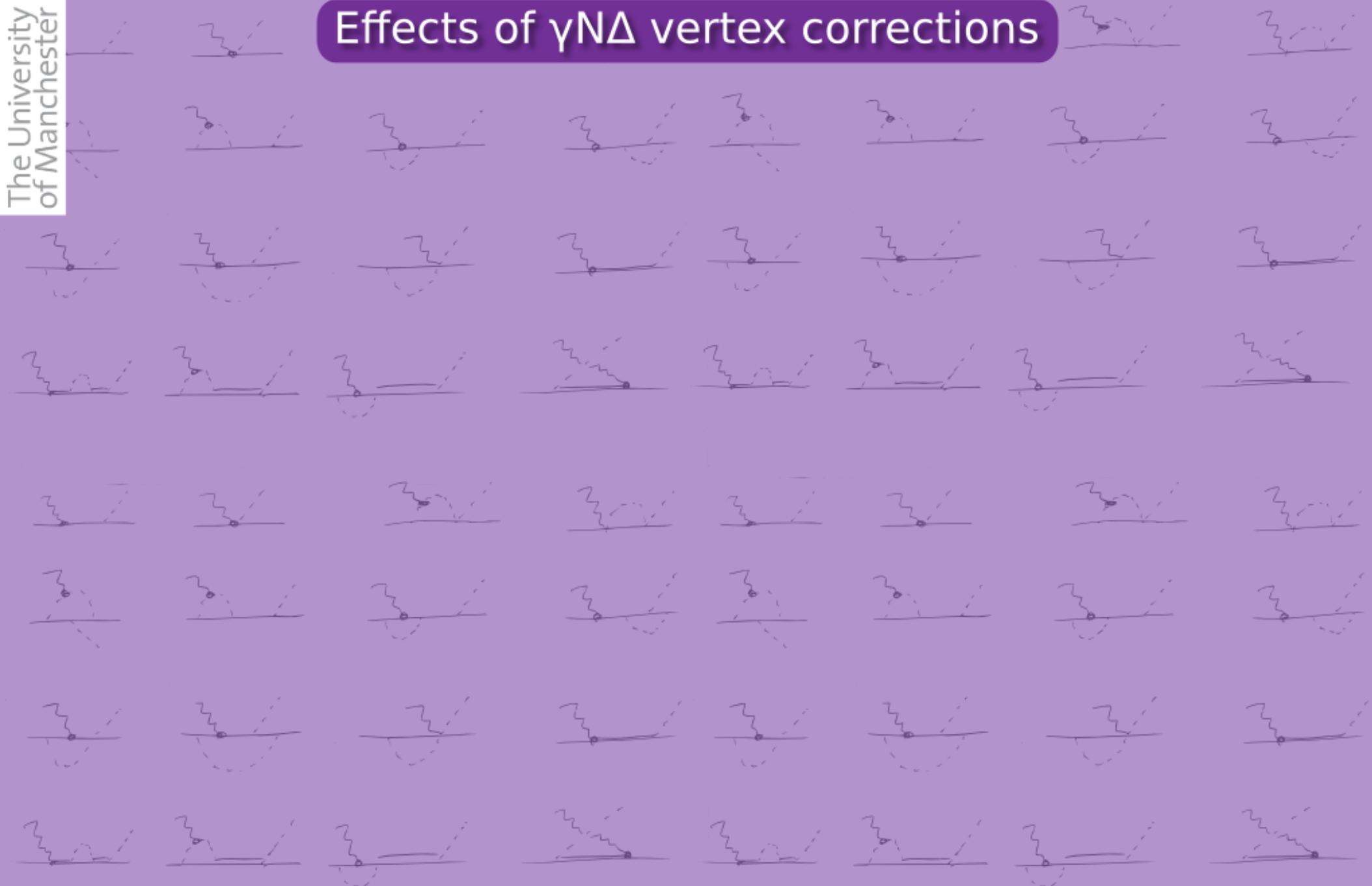
$$\omega \sim \Delta_M \quad eP^3\delta^{-3} \rightarrow e\delta^0$$



$$eP^4\delta^{-1} \rightarrow e\delta^6$$

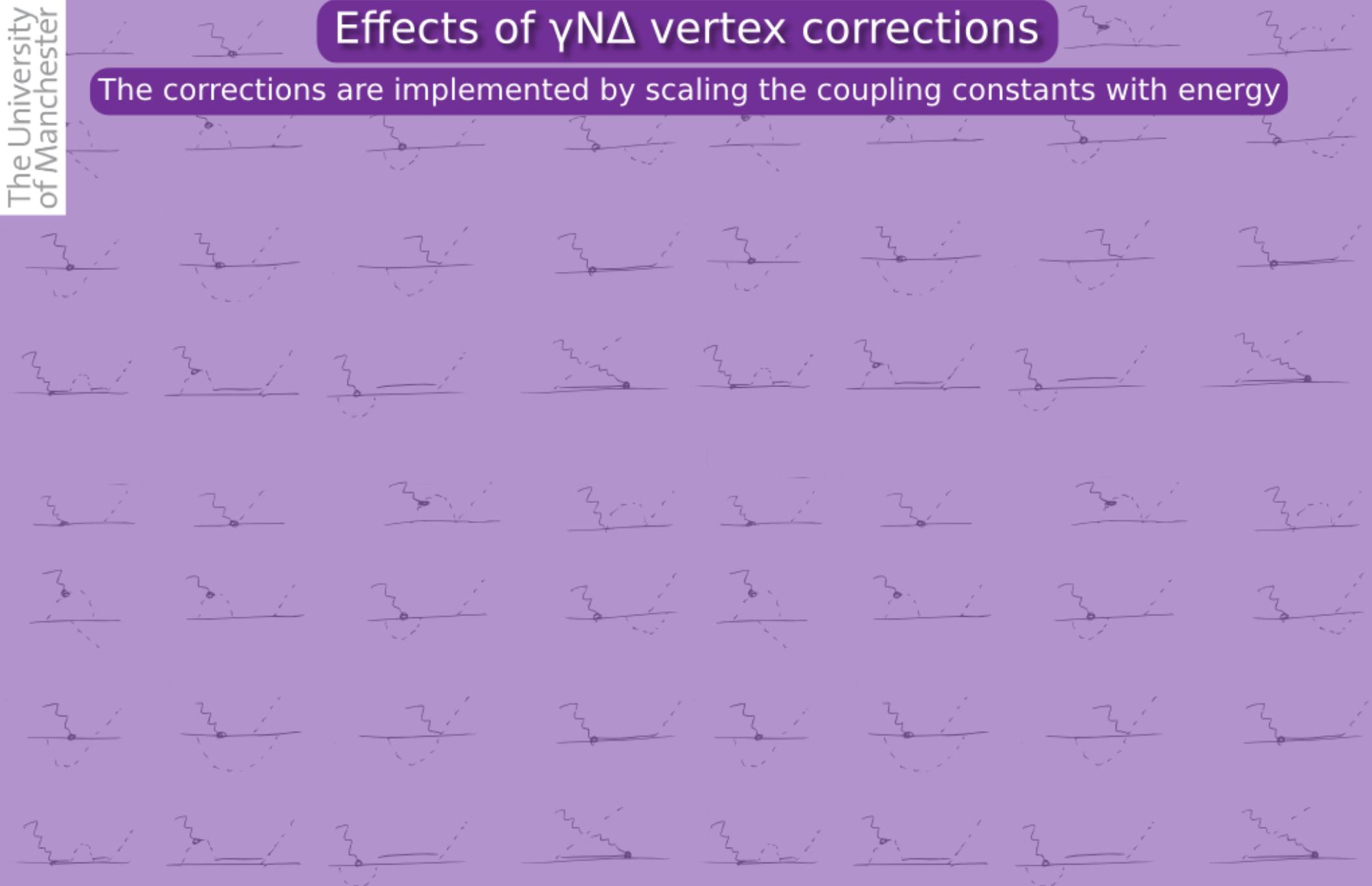
$$eP^4\delta^{-3} \rightarrow e\delta$$

McGovern, et al. (2013) Eur. Phys. J; Pascalutsa, et al. (2006) Phs. Rev. D

Effects of $\gamma N\Delta$ vertex corrections

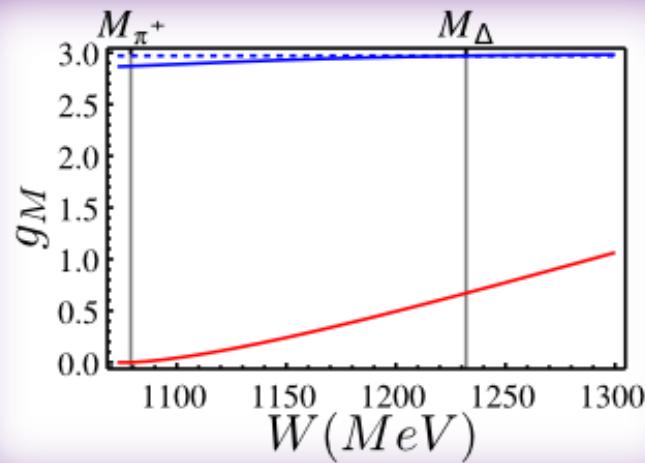
Effects of $\gamma N\Delta$ vertex corrections

The corrections are implemented by scaling the coupling constants with energy

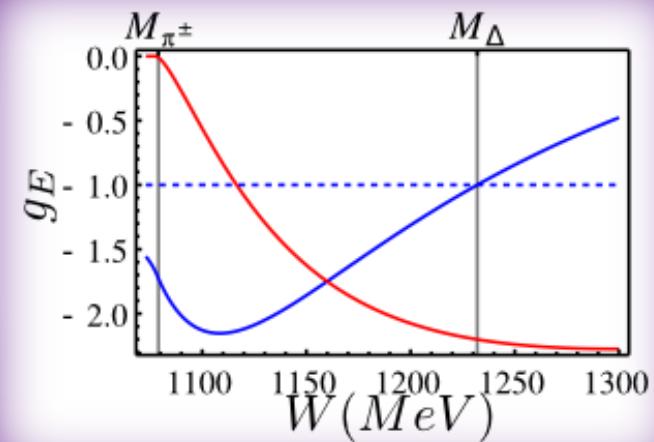


Effects of $\gamma N\Delta$ vertex corrections

The corrections are implemented by scaling the coupling constants with energy

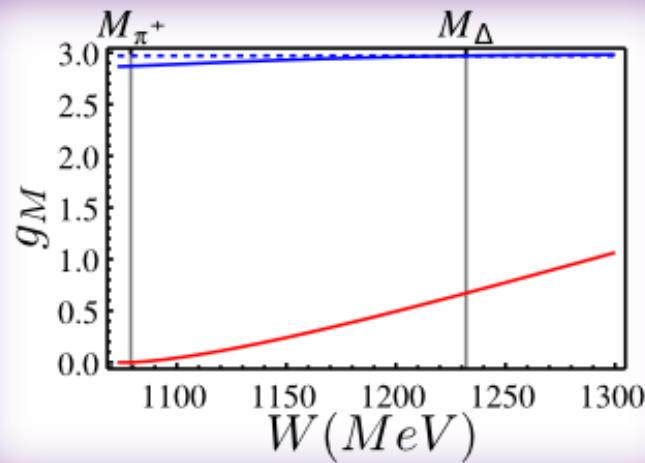


Re: █
Im: █
No corrections: █ █
McGovern,
et al. (2013)
Eur. Phys. J.



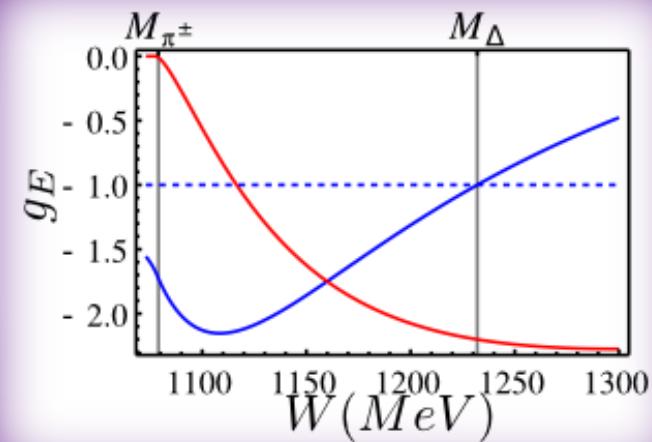
Effects of $\gamma N\Delta$ vertex corrections

The corrections are implemented by scaling the coupling constants with energy



Re: —
Im: —
No corrections: - - -

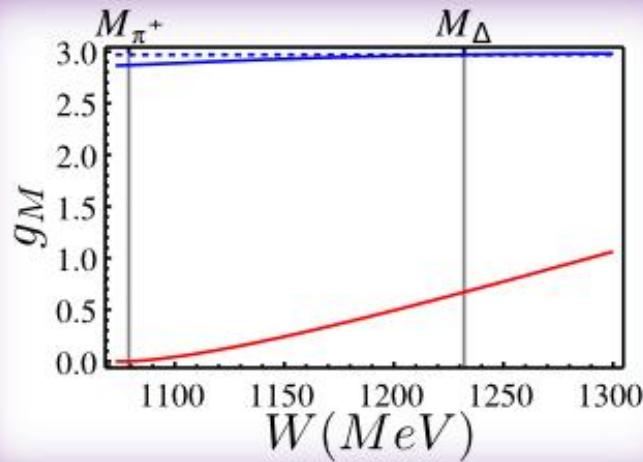
McGovern,
et al. (2013)
Eur. Phys. J.



They restore Watson's theorem.

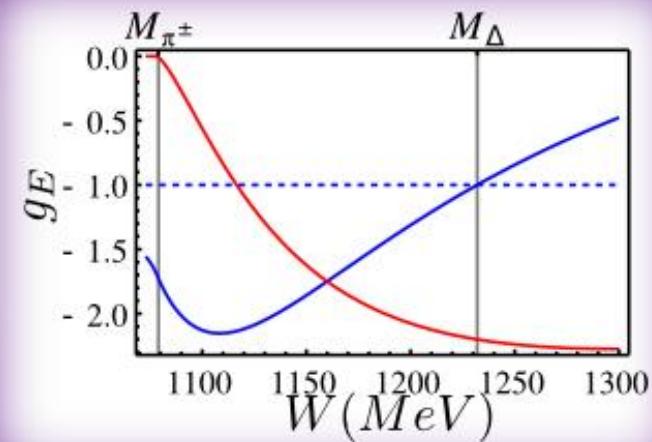
Effects of $\gamma N\Delta$ vertex corrections

The corrections are implemented by scaling the coupling constants with energy

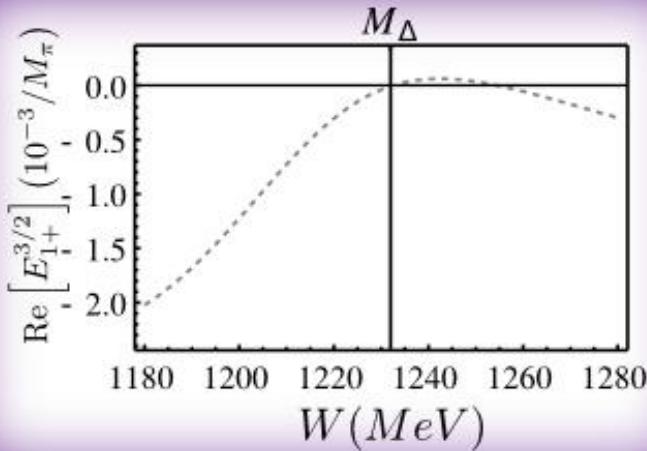


Re: —
Im: —
No corrections: - - -

McGovern,
et al. (2013)
Eur. Phys. J.

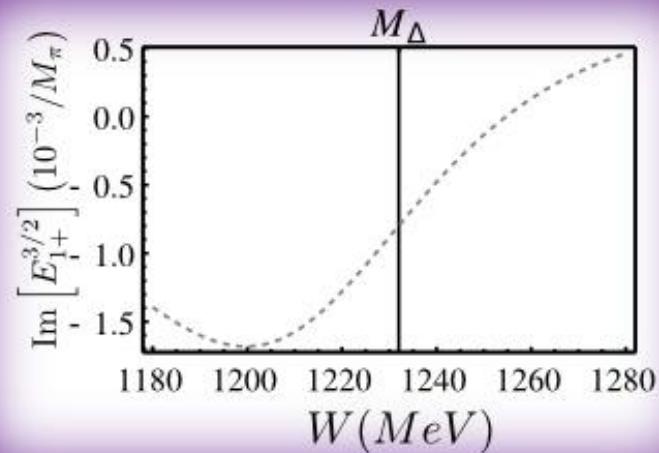


They restore Watson's theorem.



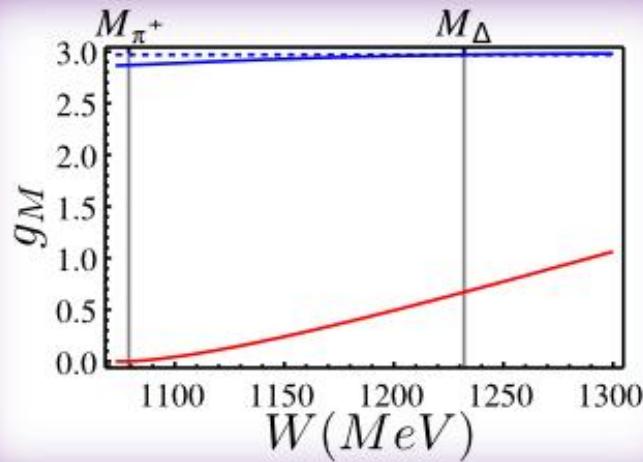
MAID: - - -

Pascalutsa, et al.
(2006) Phys. Rev. D



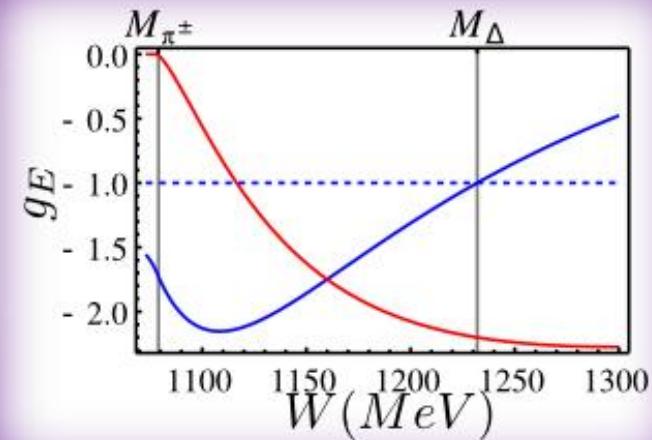
Effects of $\gamma N\Delta$ vertex corrections

The corrections are implemented by scaling the coupling constants with energy

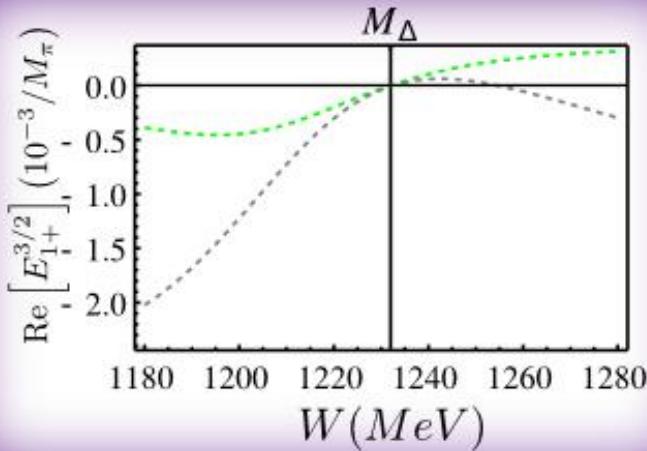


Re: —
Im: —
No corrections: - - -

McGovern,
et al. (2013)
Eur. Phys. J.

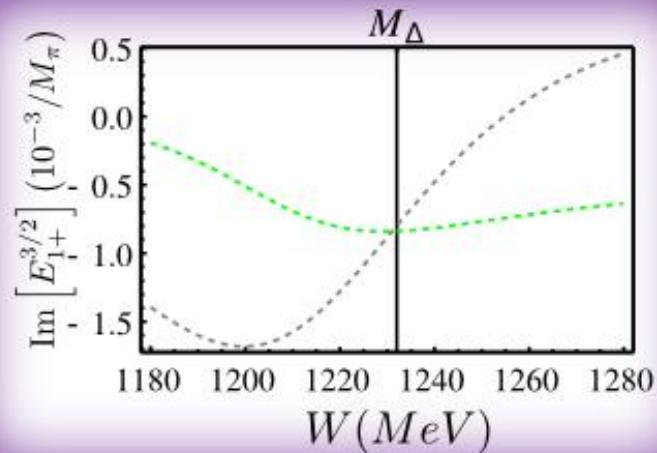


They restore Watson's theorem.



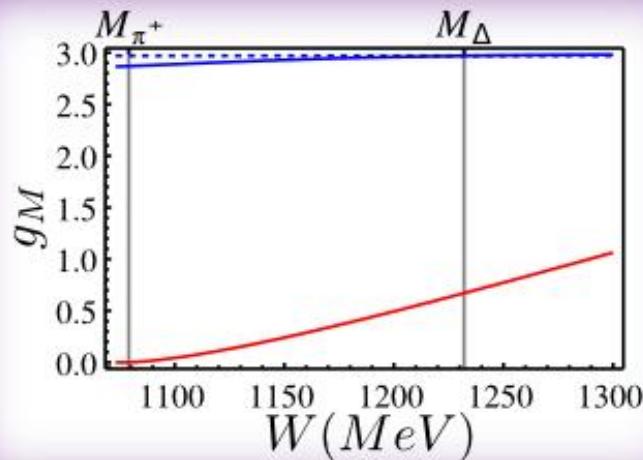
MAID: ---
 Δ : ---

Pascalutsa, et al.
(2006) Phys. Rev. D



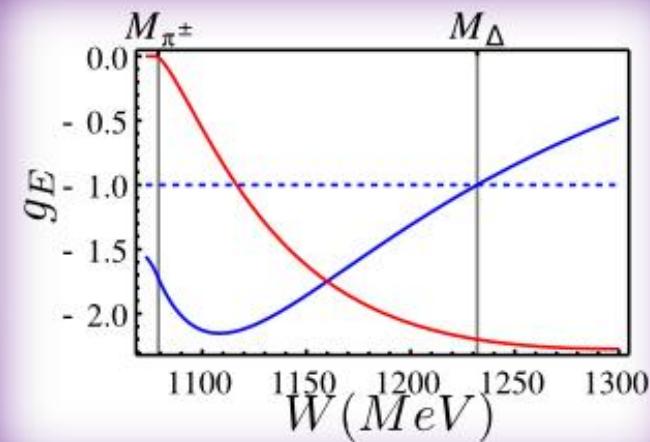
Effects of $\gamma N\Delta$ vertex corrections

The corrections are implemented by scaling the coupling constants with energy

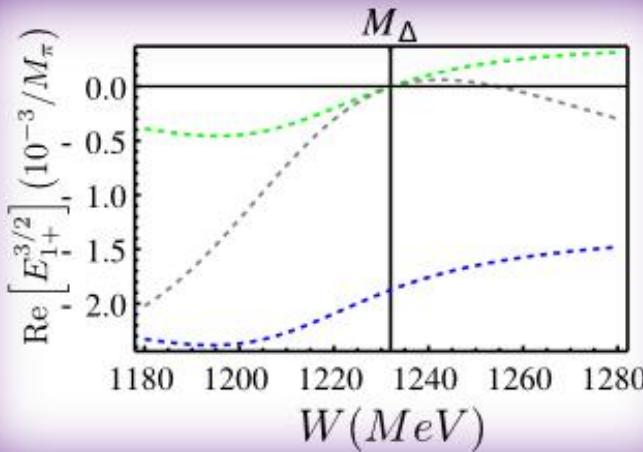


Re: 
Im: 
No
corrections: 

McGovern,
et al. (2013)
Eur. Phys. J.

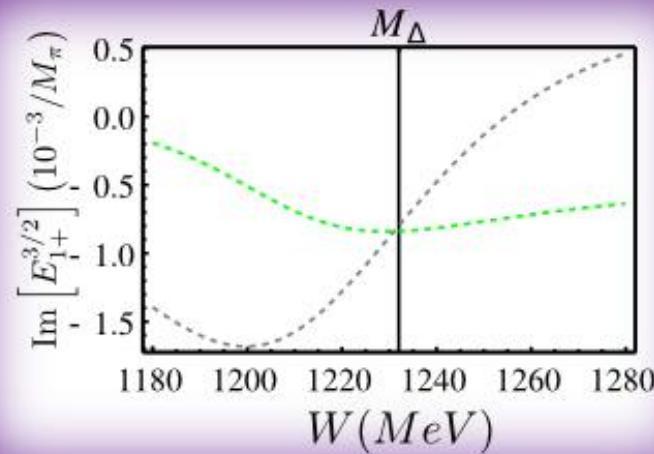


They restore Watson's theorem.



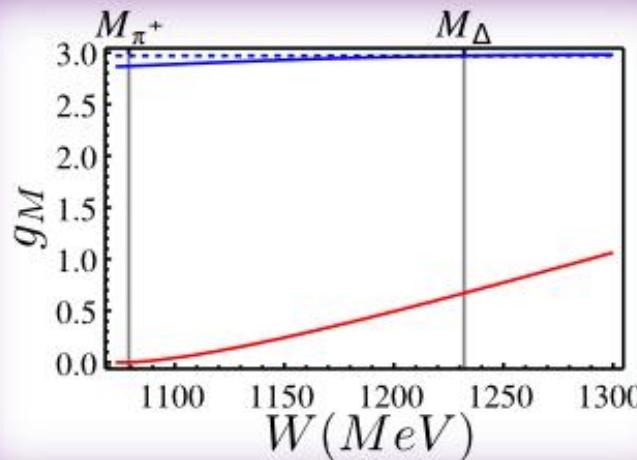
MAID: - - -
Δ: - - -
Δ+Tree: - - -

Pascalutsa, et al.
(2006) Phys. Rev. D



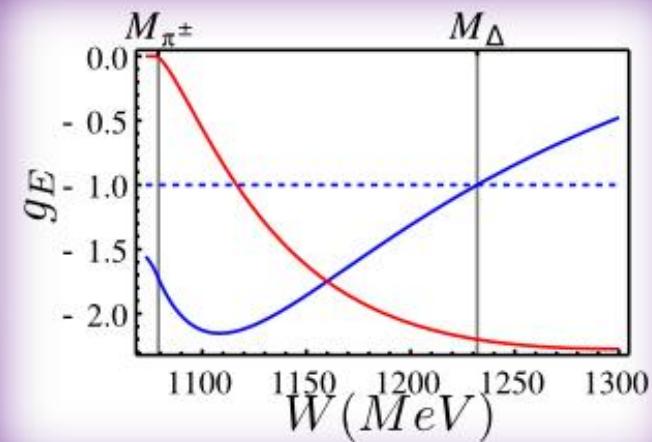
Effects of $\gamma N\Delta$ vertex corrections

The corrections are implemented by scaling the coupling constants with energy

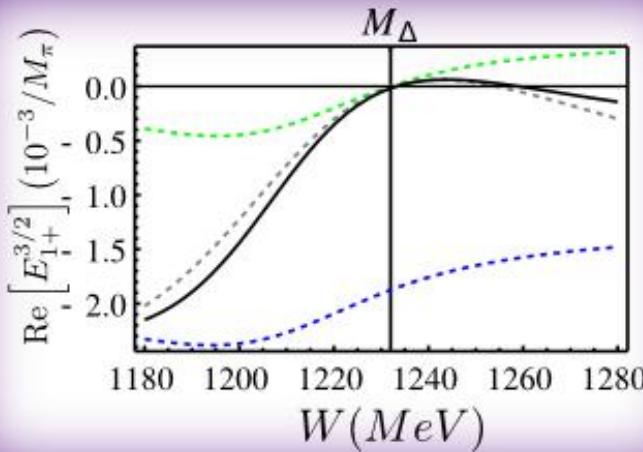


Re: 
Im: 
No
corrections: 

McGovern,
et al. (2013)
Eur. Phys. J.

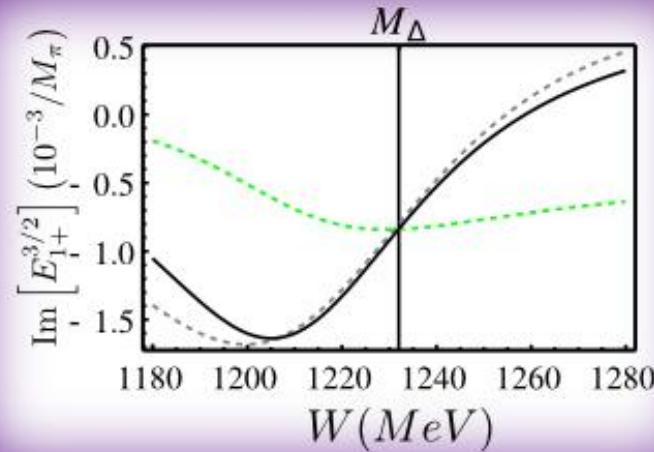


They restore Watson's theorem.

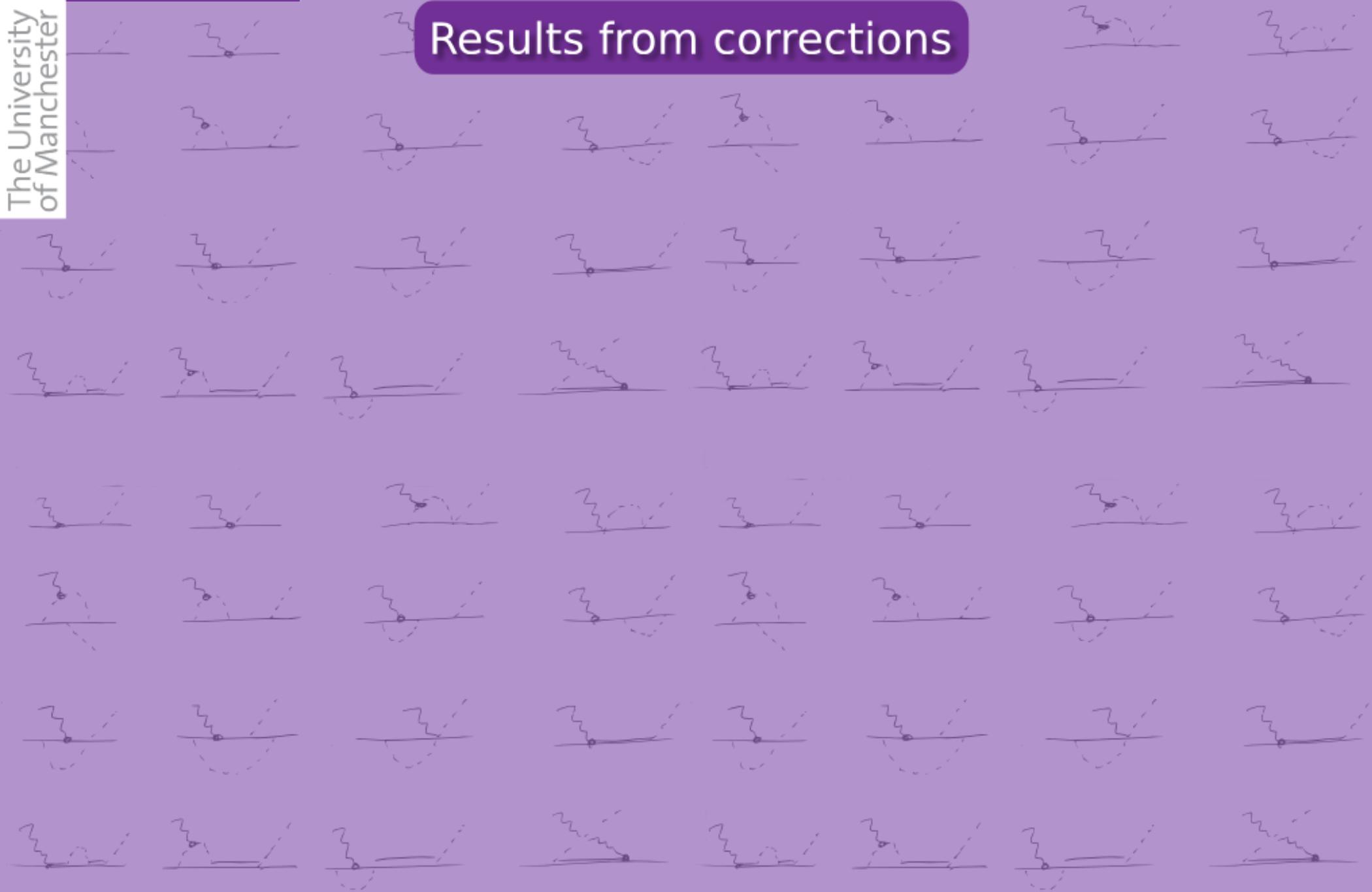


MAID: - - -
 Δ : - - -
 $\Delta + \text{Tree}$: - - -
 $\Delta + \text{Tree} + \text{V.C.}$: -

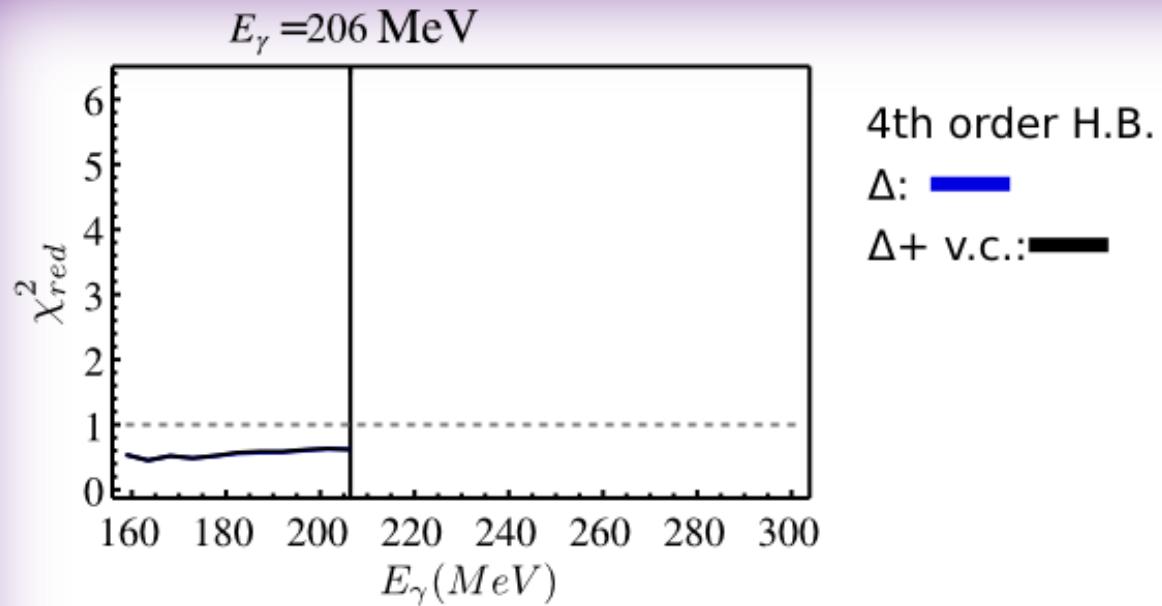
Pascalutsa, et al.
(2006) Phys. Rev. D



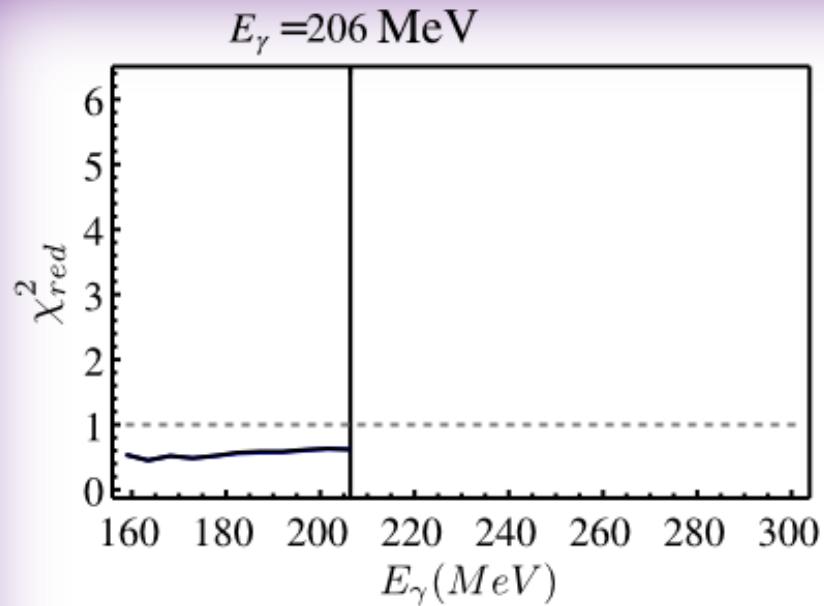
Results from corrections



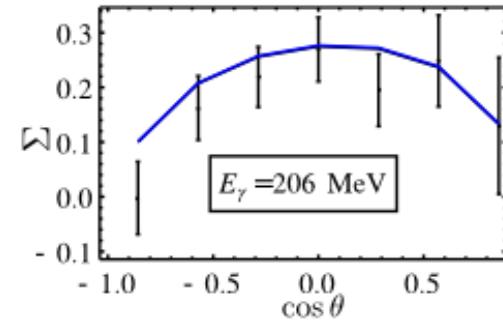
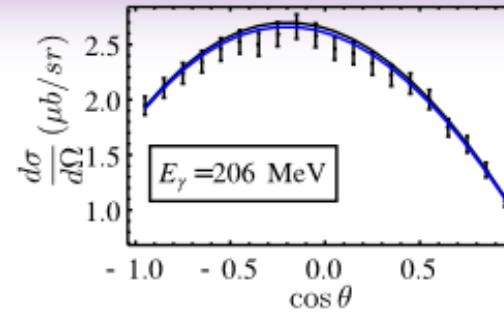
Results from corrections



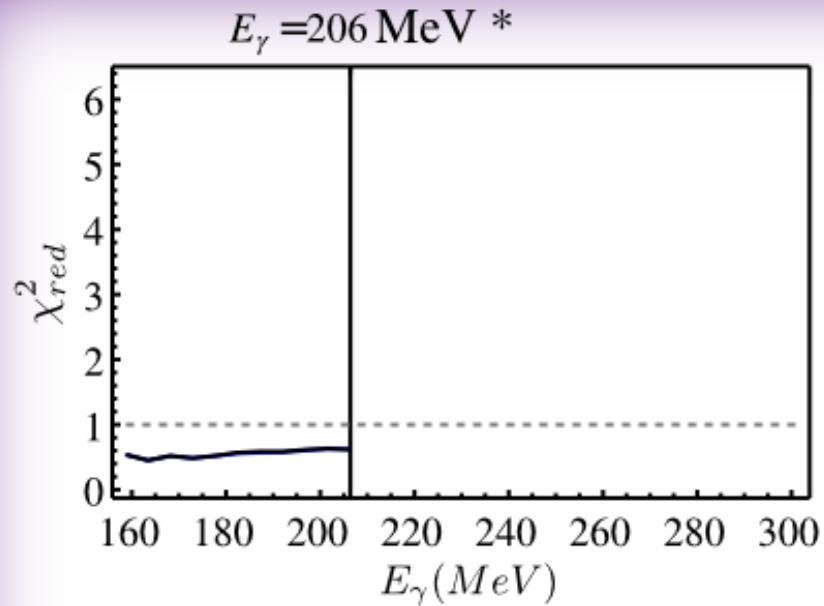
Results from corrections



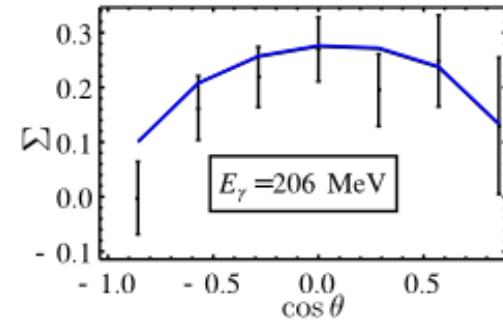
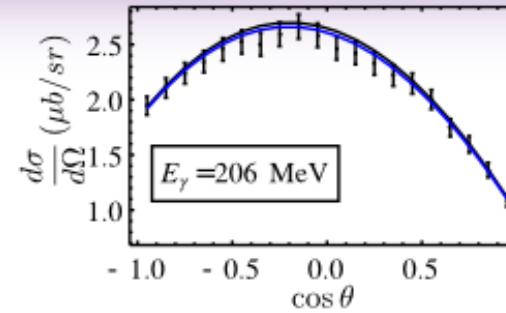
4th order H.B.
 Δ : 
 $\Delta + \text{V.C.}$: 



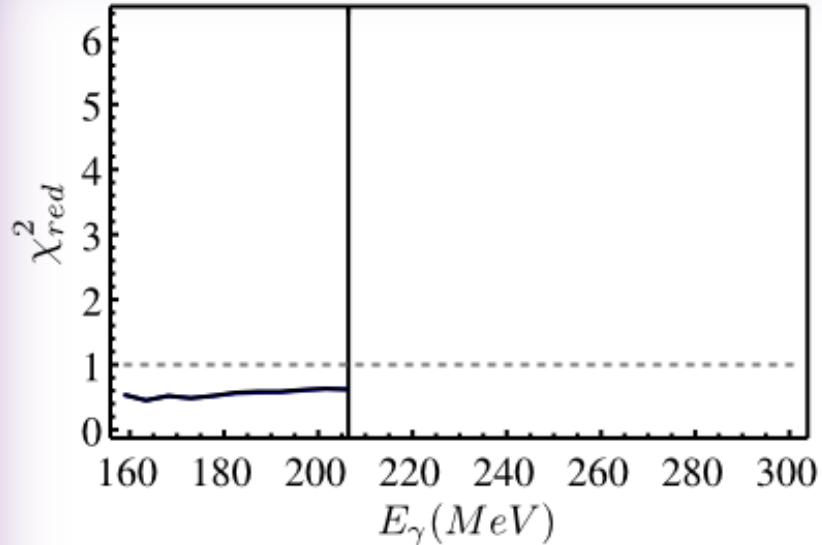
Results from corrections



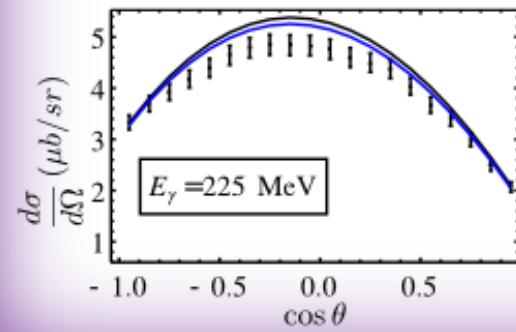
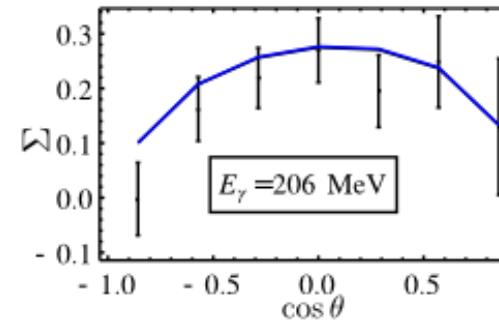
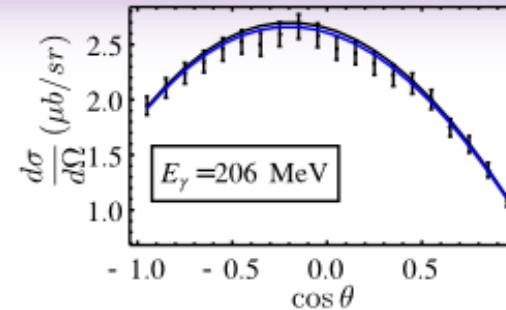
4th order H.B.

 Δ : ■ $\Delta + \text{V.C.}$: ■*Fix LECs at
206 MeV.

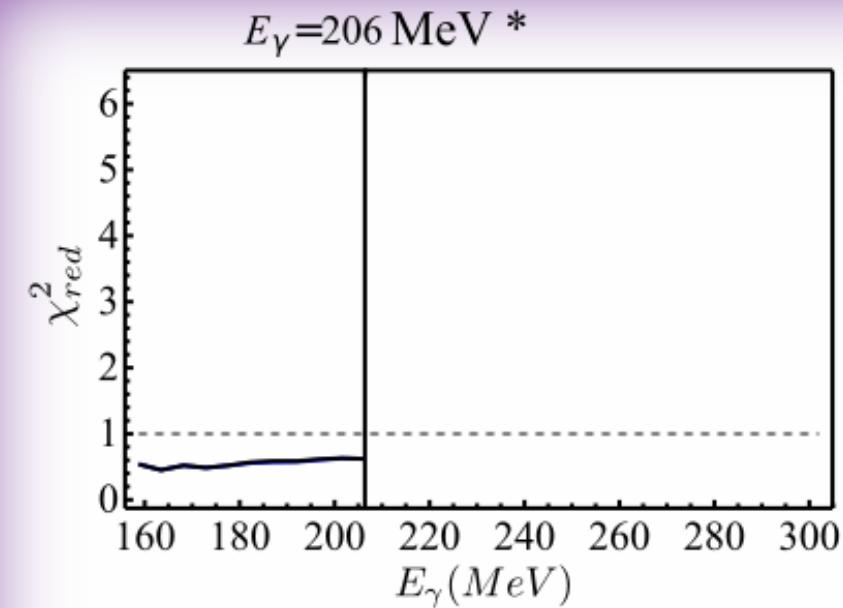
Results from corrections

 $E_\gamma = 206 \text{ MeV} *$ 

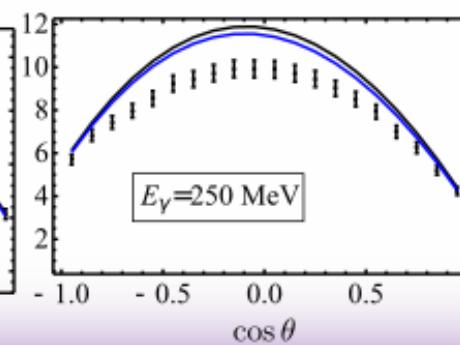
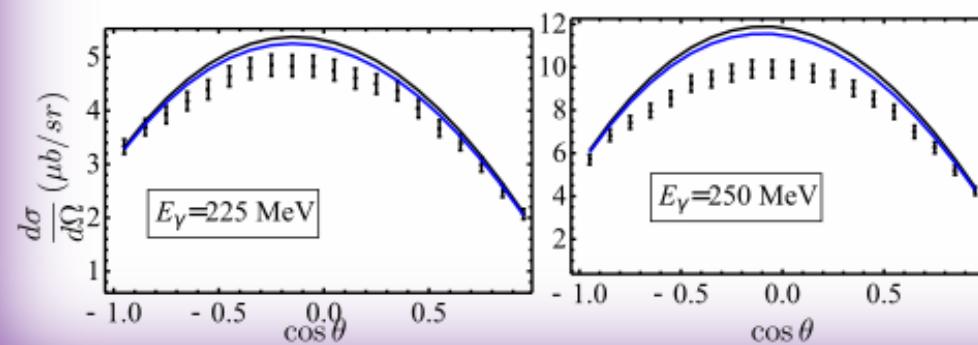
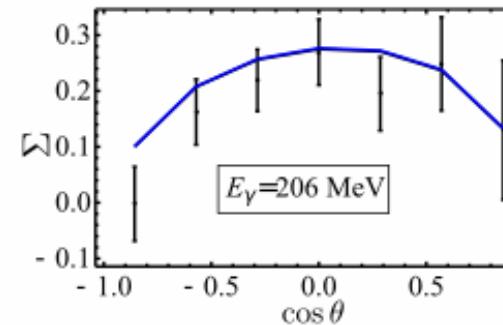
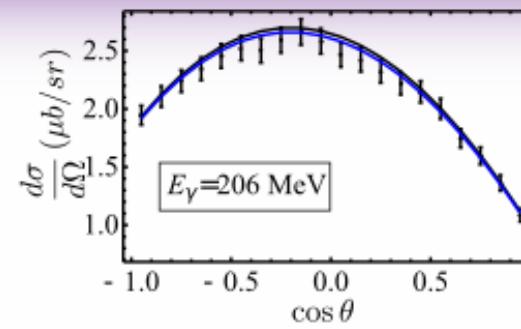
4th order H.B.

 Δ : ■ $\Delta + \text{V.C.}$: ■*Fix LECs at
206 MeV.

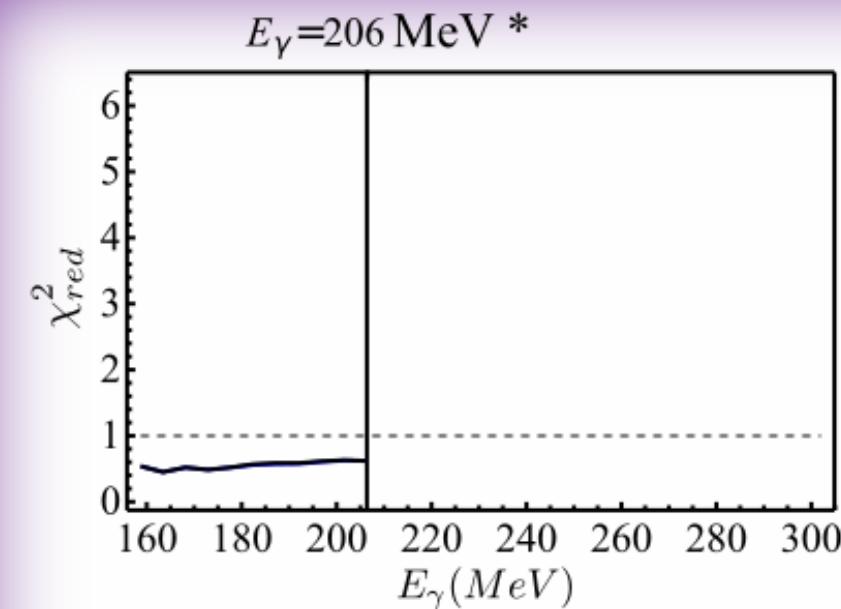
Results from corrections



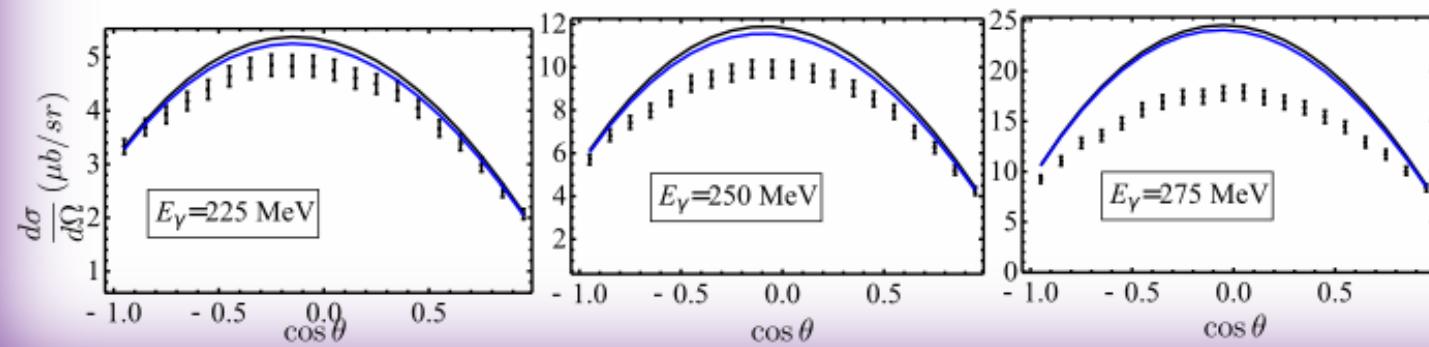
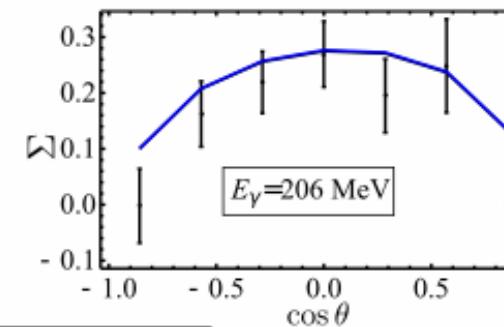
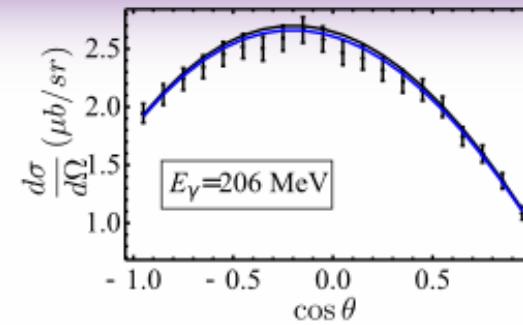
4th order H.B.

 Δ : ■ $\Delta + \text{V.C.}$: ■*Fix LECs at
206 MeV.

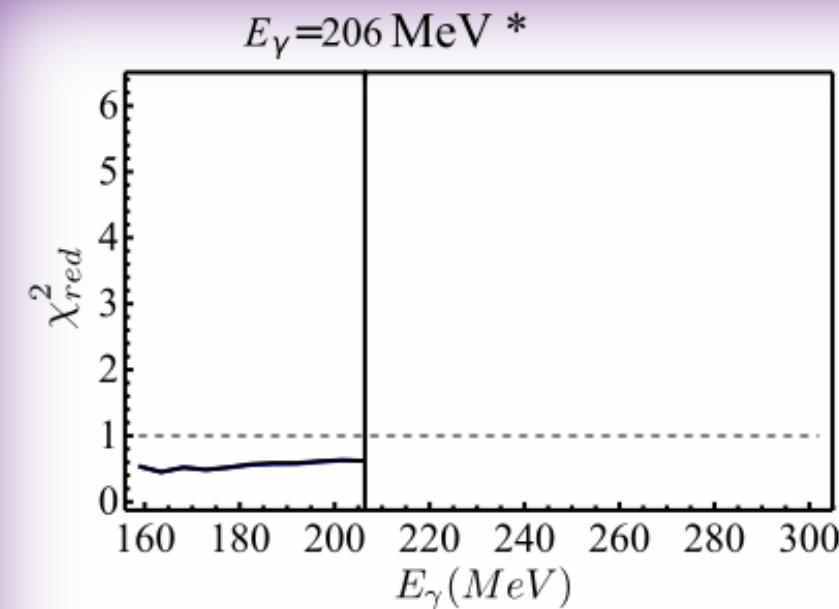
Results from corrections



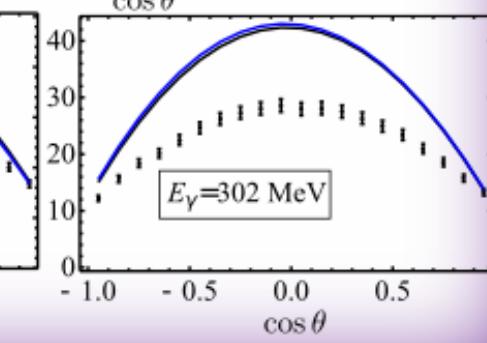
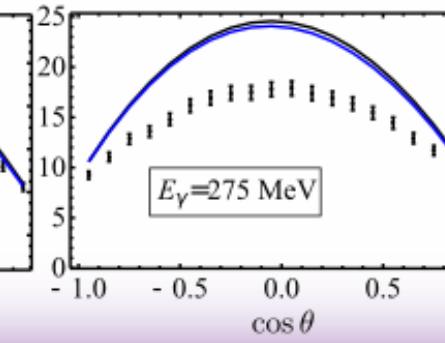
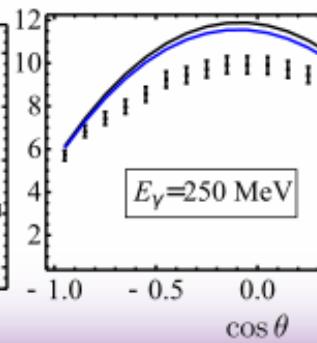
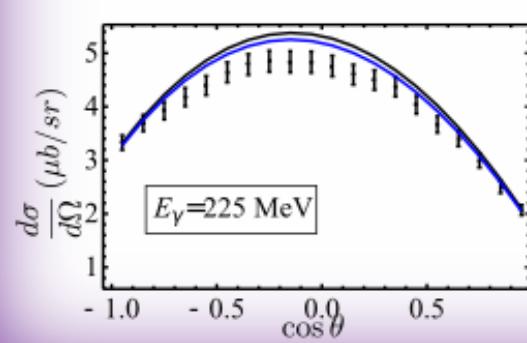
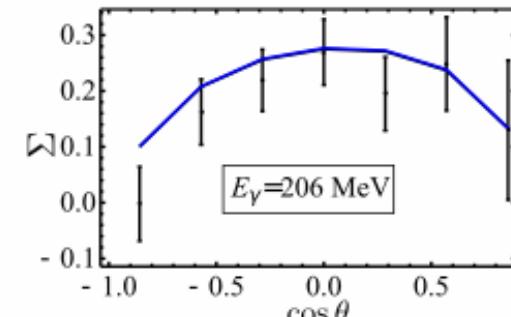
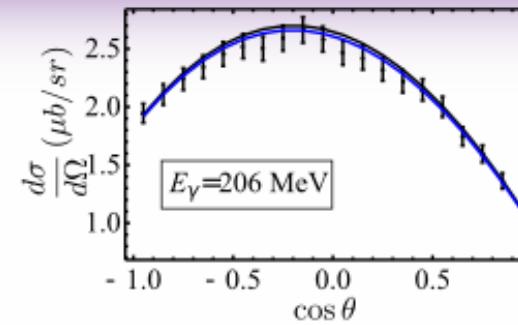
4th order H.B.

 Δ : — $\Delta + \text{V.C.}$: —*Fix LECs at
206 MeV.

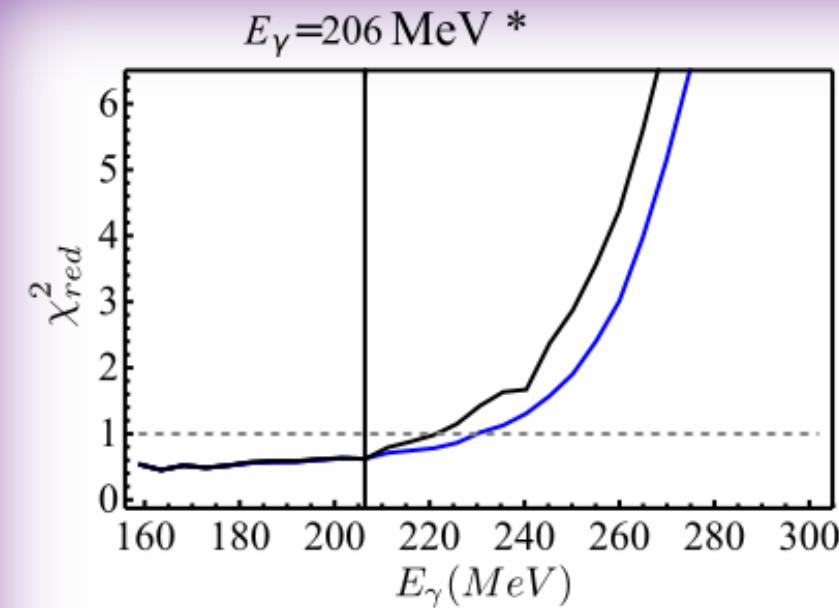
Results from corrections



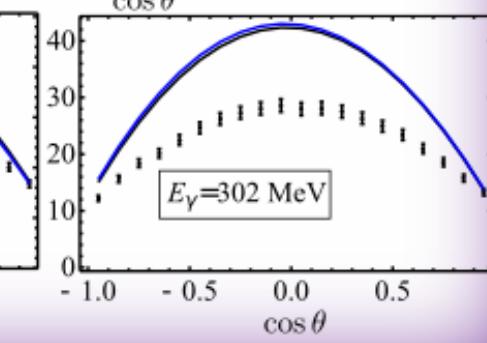
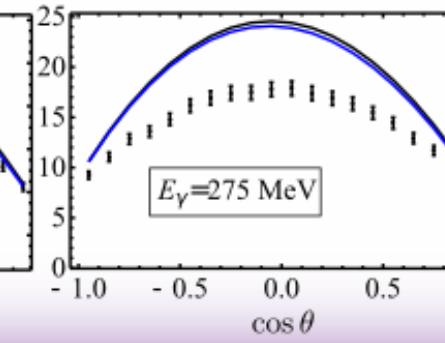
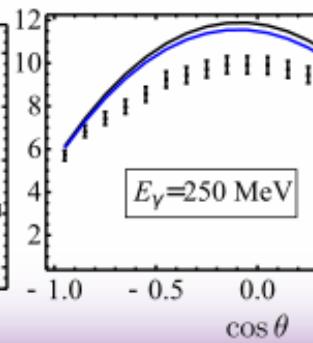
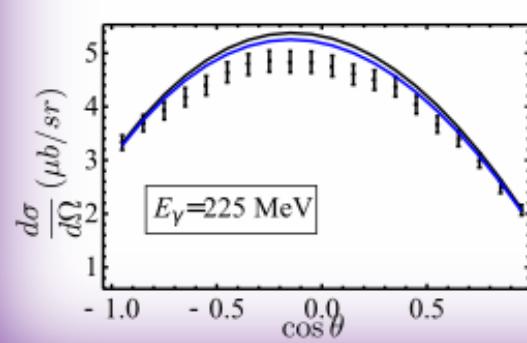
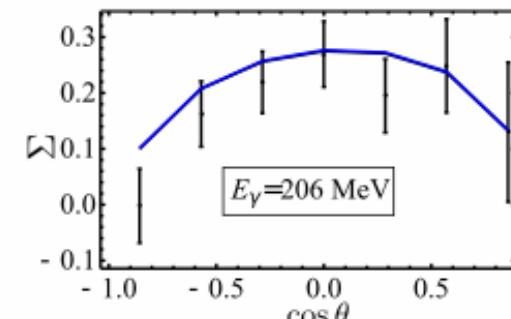
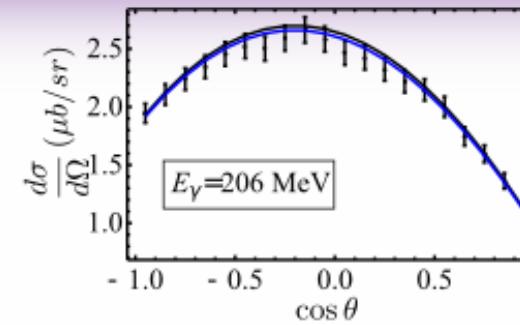
4th order H.B.

 Δ : — $\Delta + \text{V.C.}$: —*Fix LECs at
206 MeV.

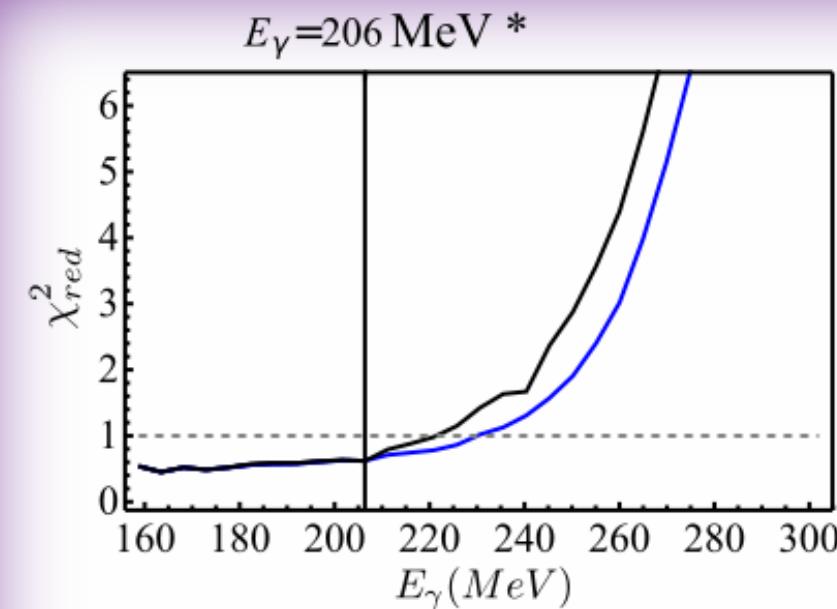
Results from corrections



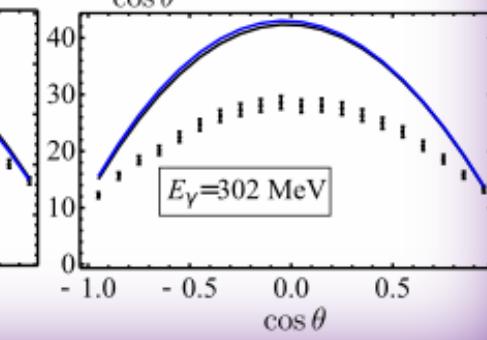
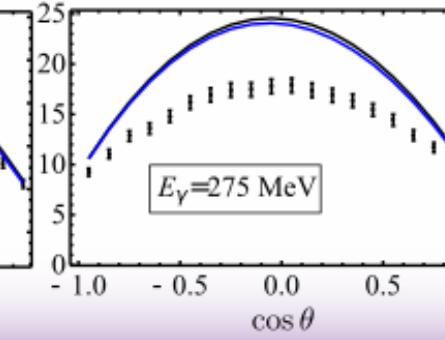
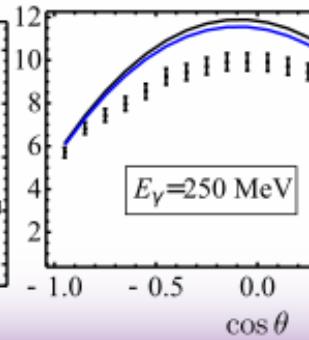
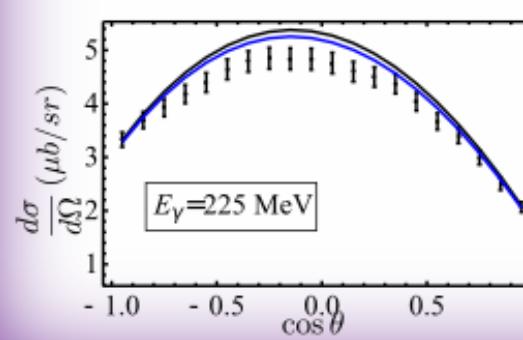
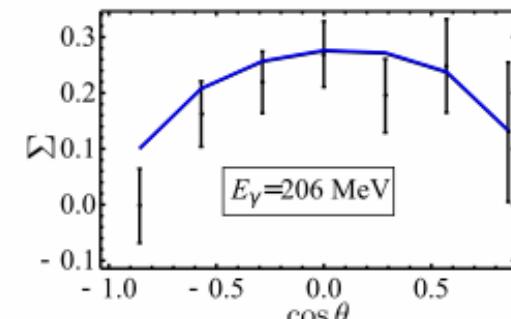
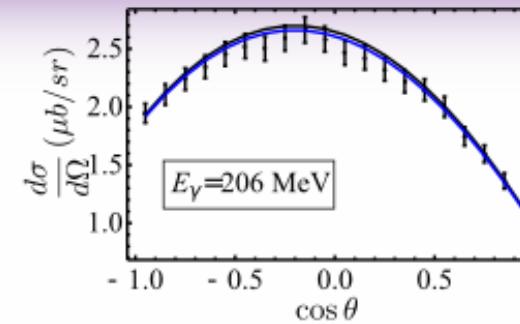
4th order H.B.

 Δ : — $\Delta + \text{V.C.}$: —*Fix LECs at
206 MeV.

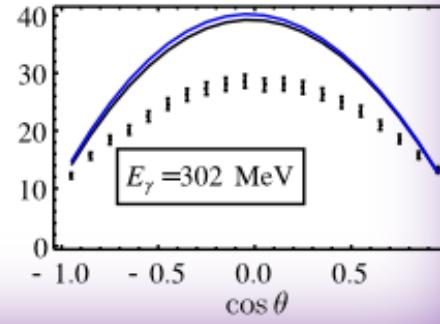
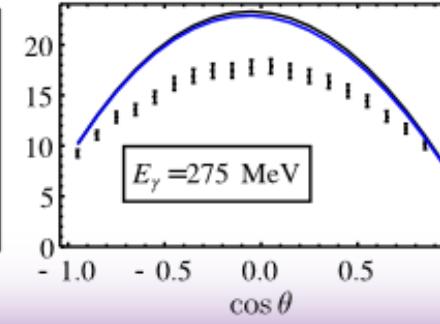
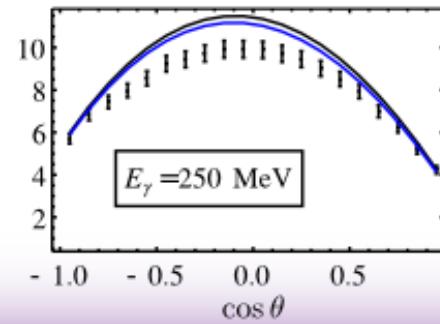
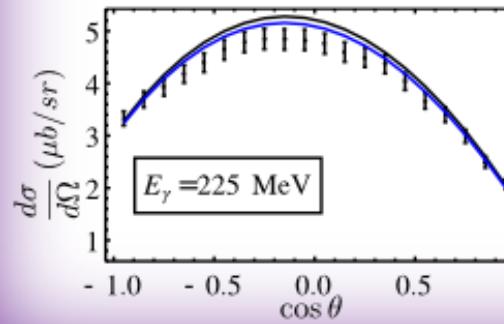
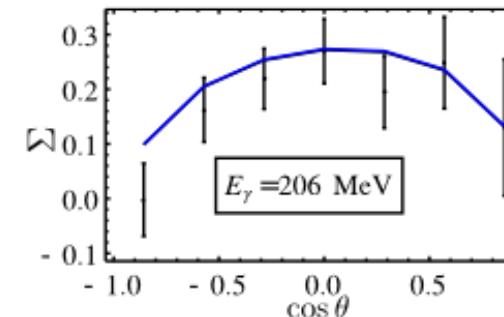
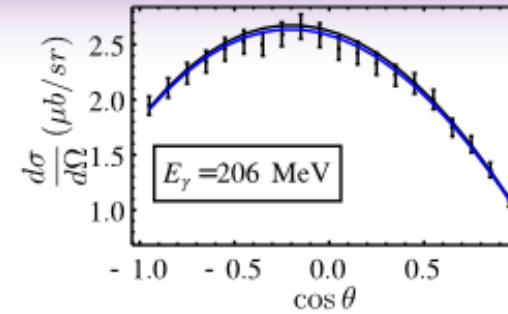
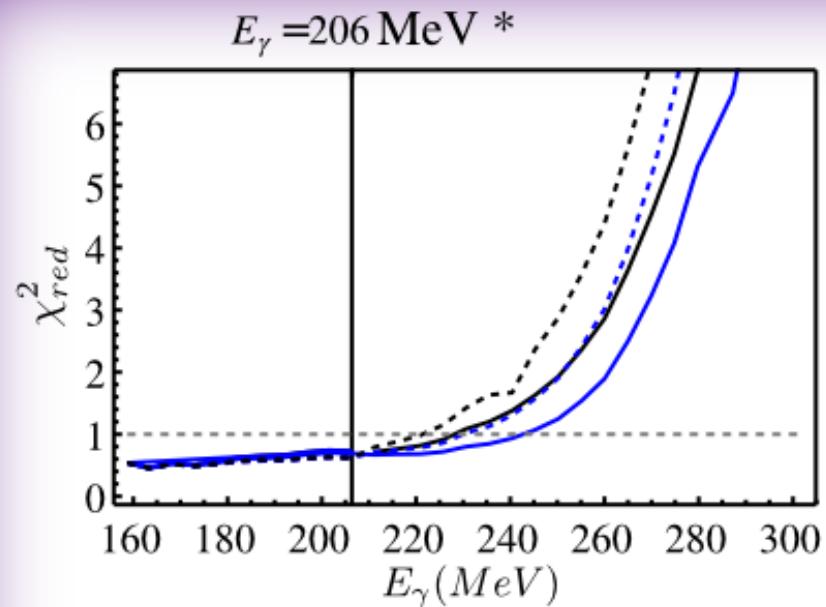
Results from corrections

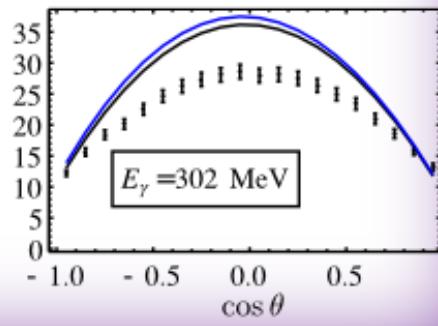
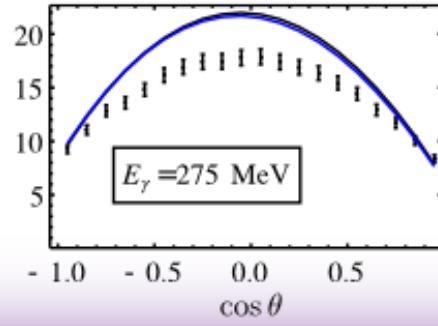
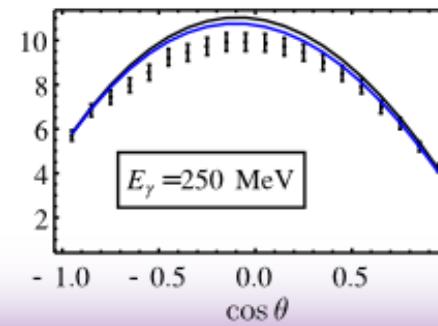
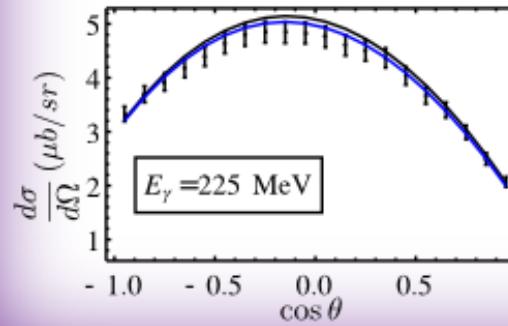
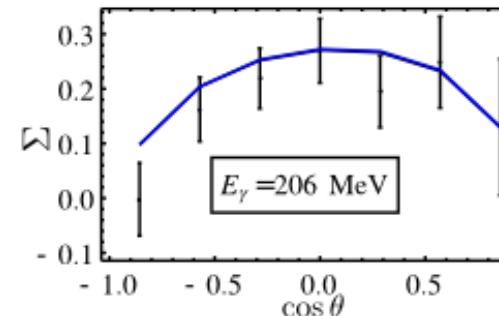
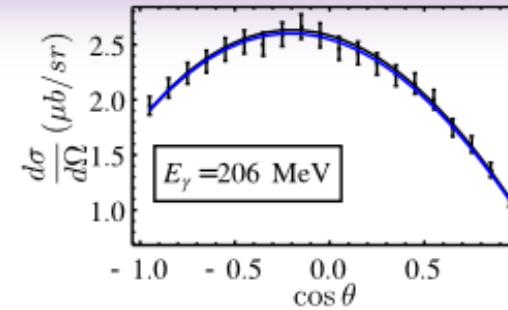
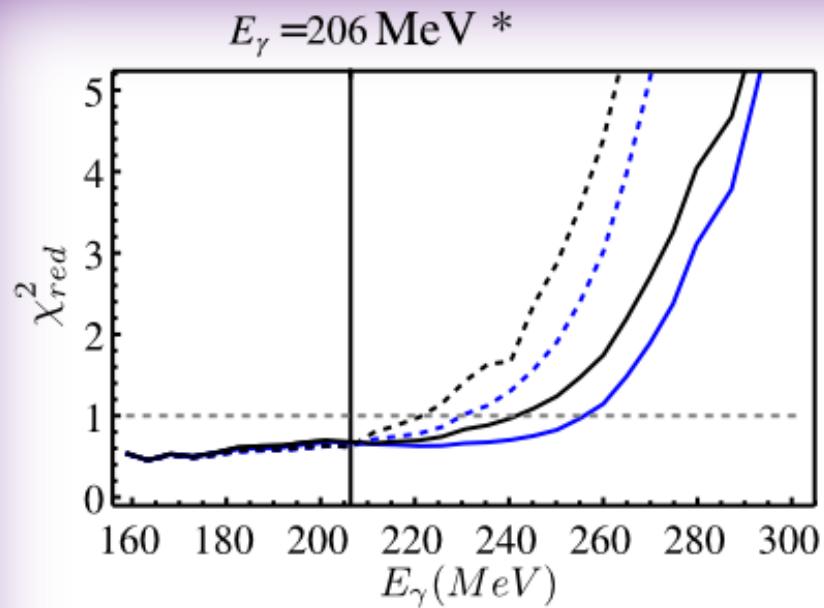


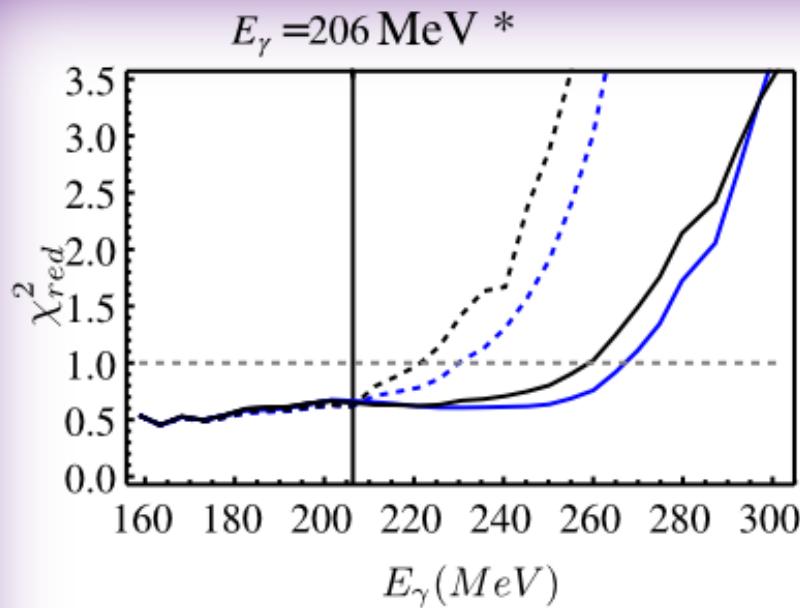
4th order H.B.

 Δ : — $\Delta + \text{V.C.}$: —*Fix LECs at
206 MeV.

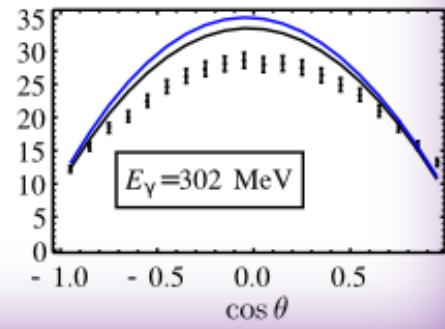
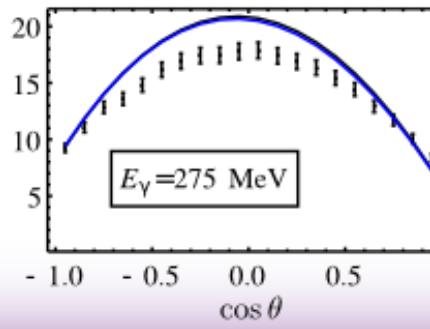
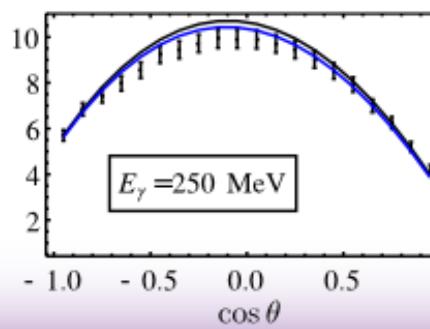
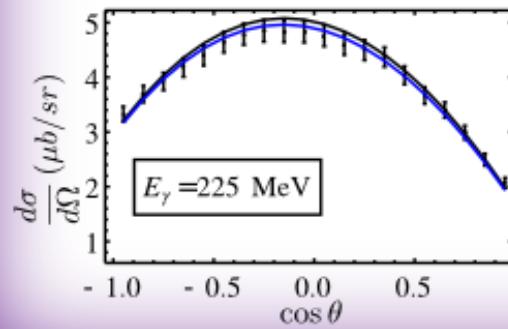
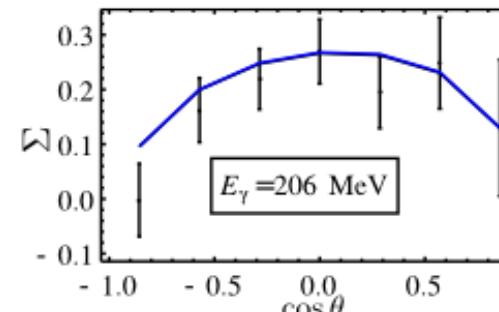
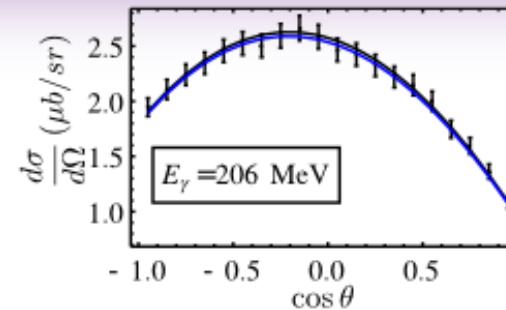
We are overestimating the data. Can we do better?

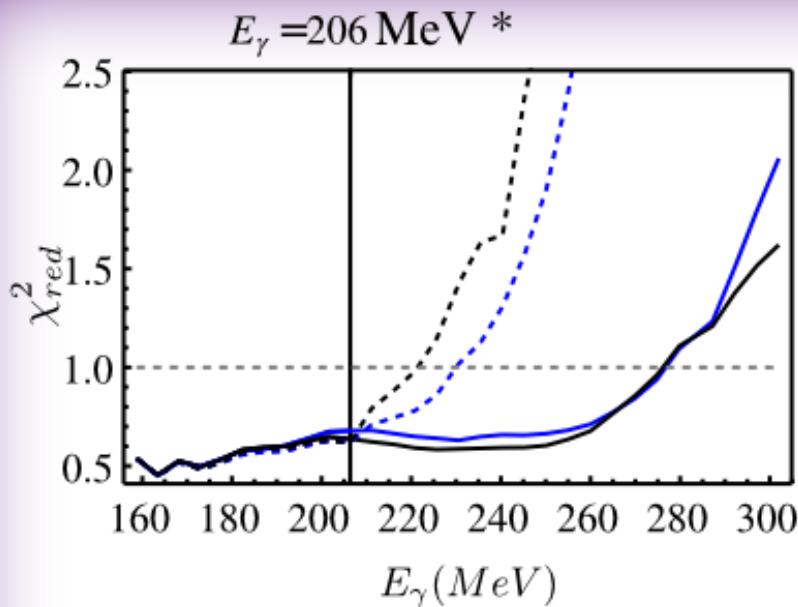
Varying g_M 

Varying g_M 

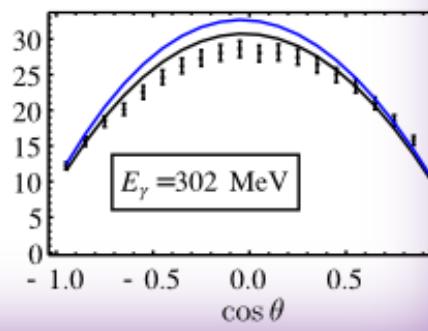
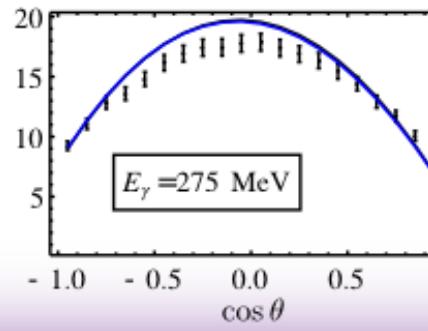
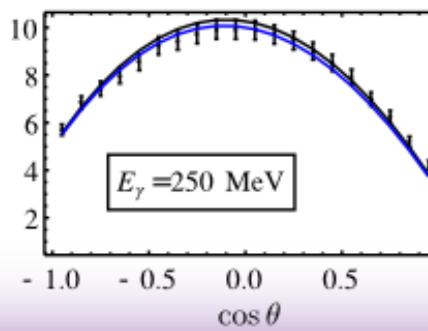
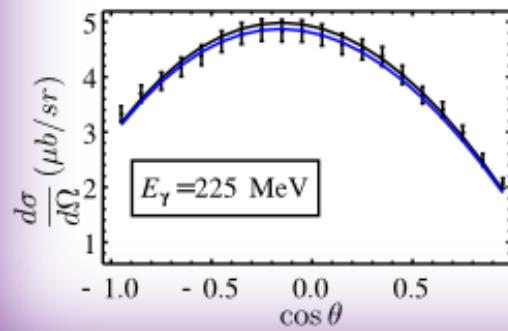
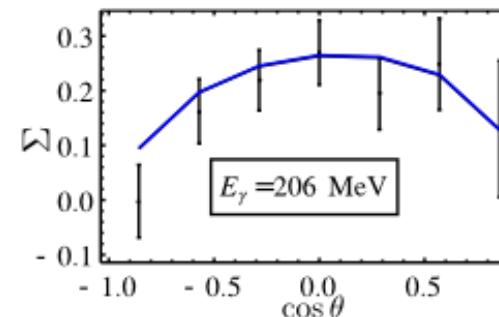
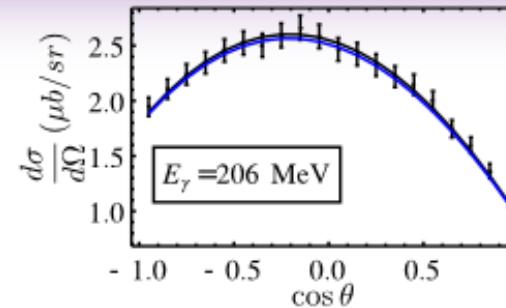
Varying g_M 

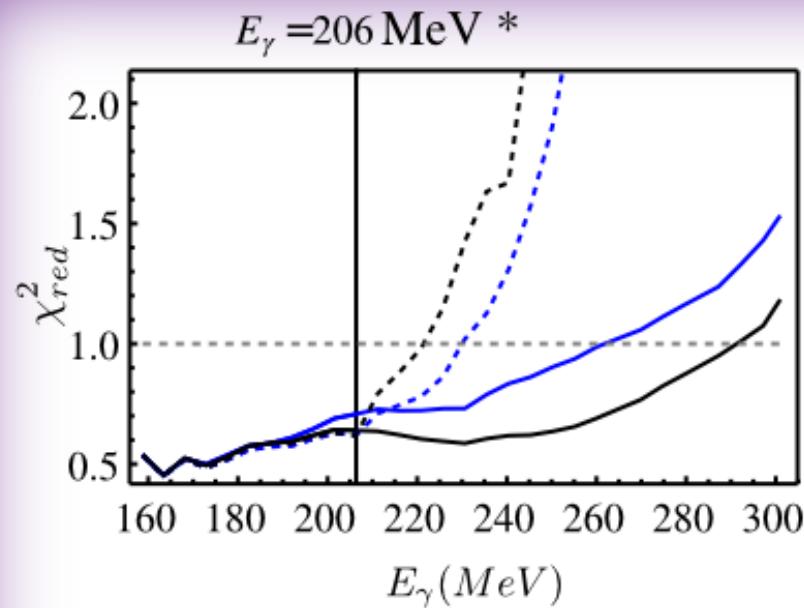
4th order H.B.

 Δ : — $\Delta + \text{V.C.}$: —*Fix LECs at
206 MeV. $g_M = 2.97$ — $g_M = 2.4$ —

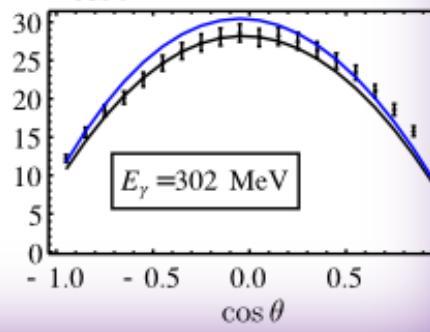
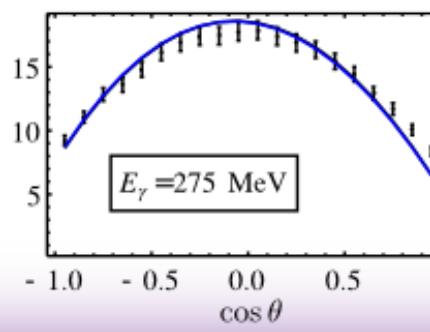
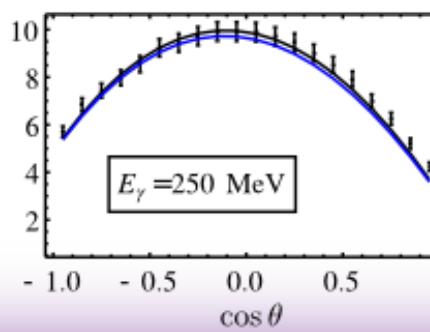
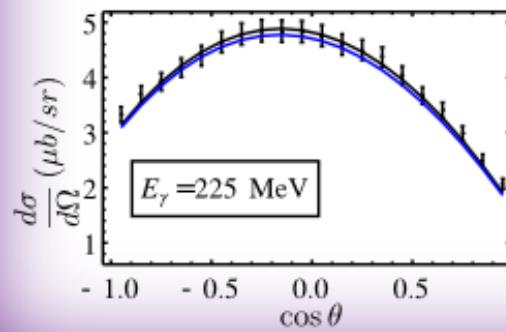
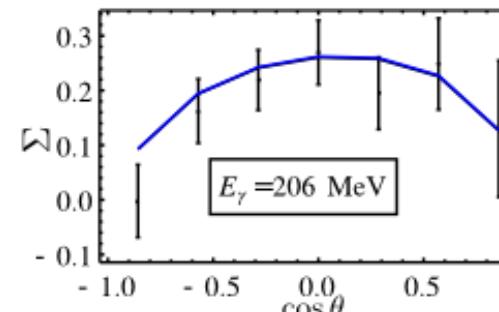
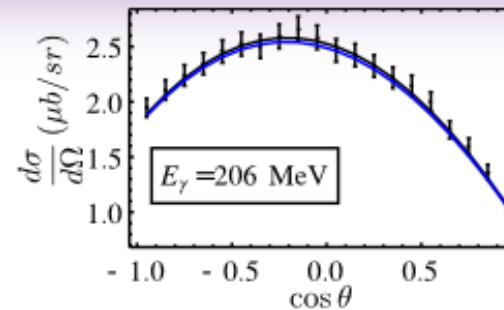
Varying g_M 

4th order H.B.

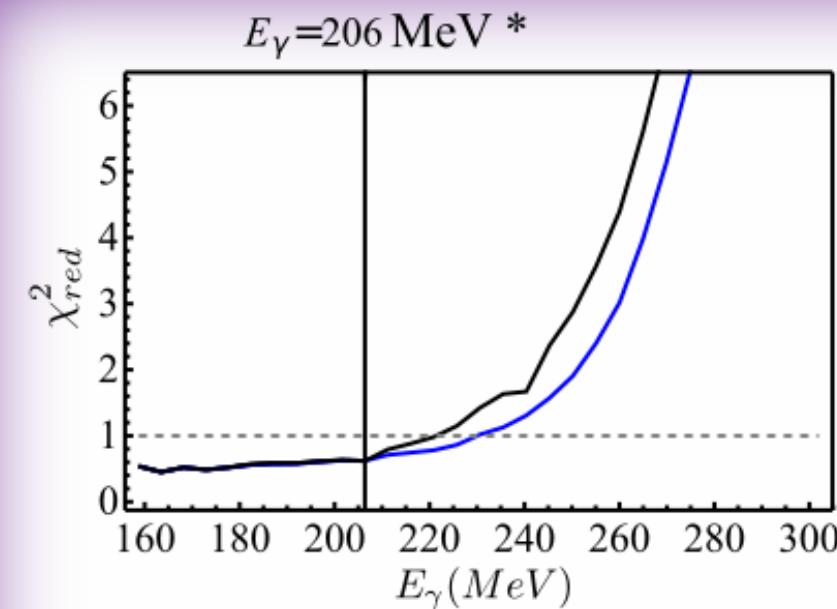
 Δ : — $\Delta + \text{V.C.}$: —*Fix LECs at
206 MeV. $g_M = 2.97$ — $g_M = 2.2$ —

Varying g_M 

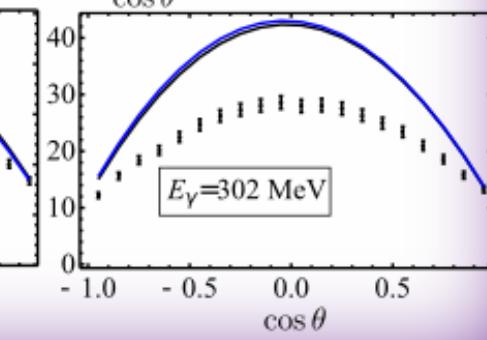
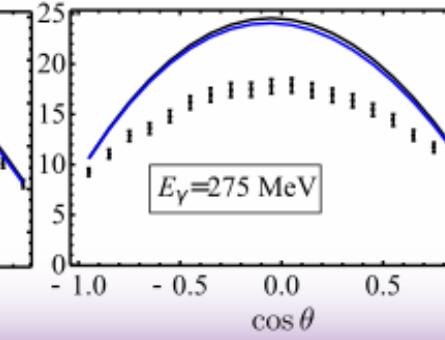
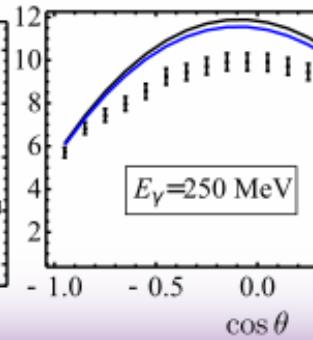
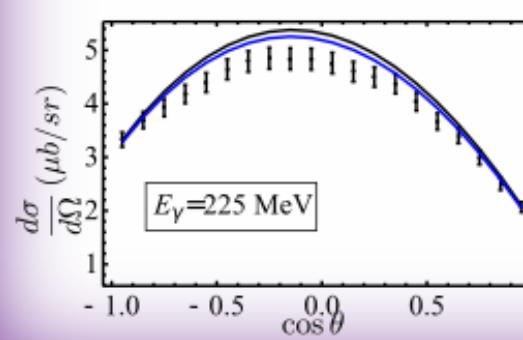
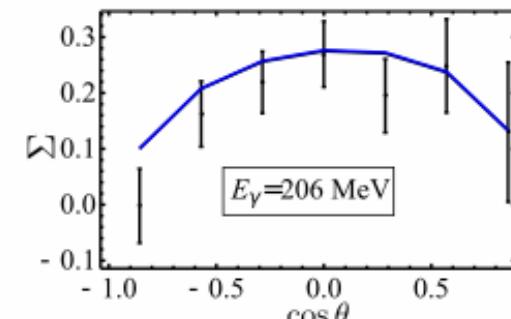
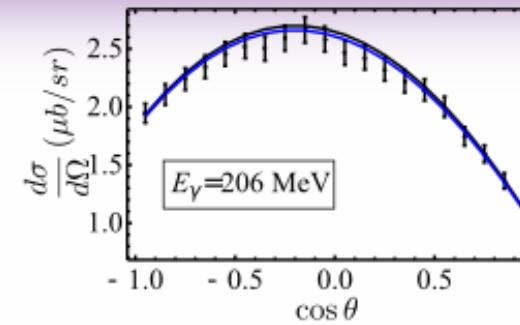
4th order H.B.

 Δ : $\Delta + V.C.$:*Fix LECs at
206 MeV. $g_M = 2.97$ — $g_M = 2.0$ —

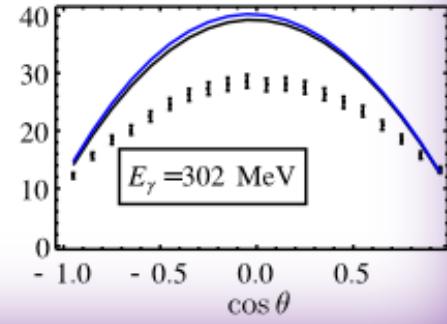
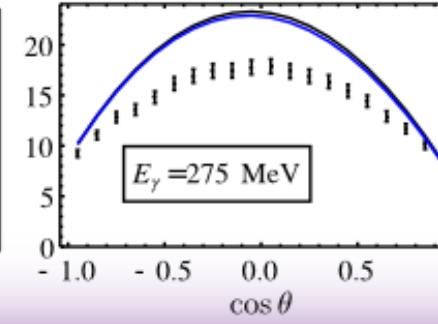
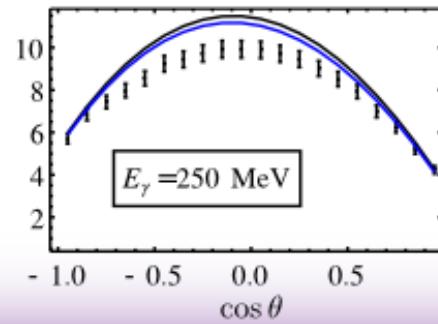
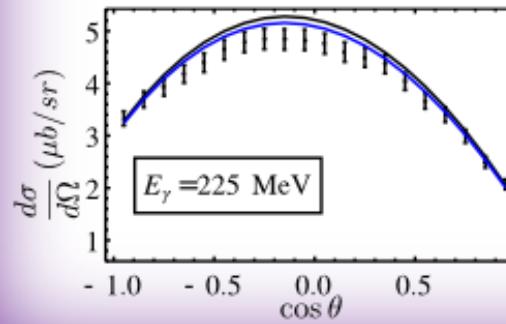
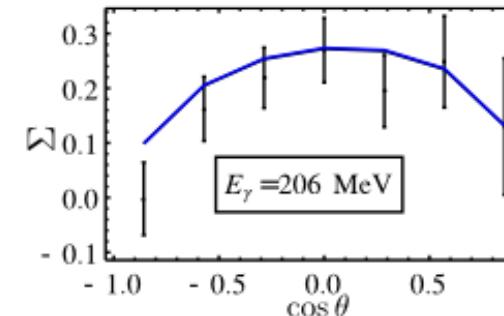
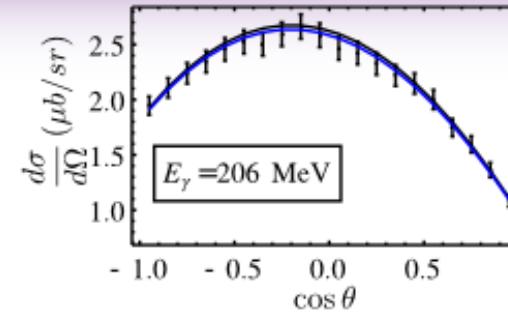
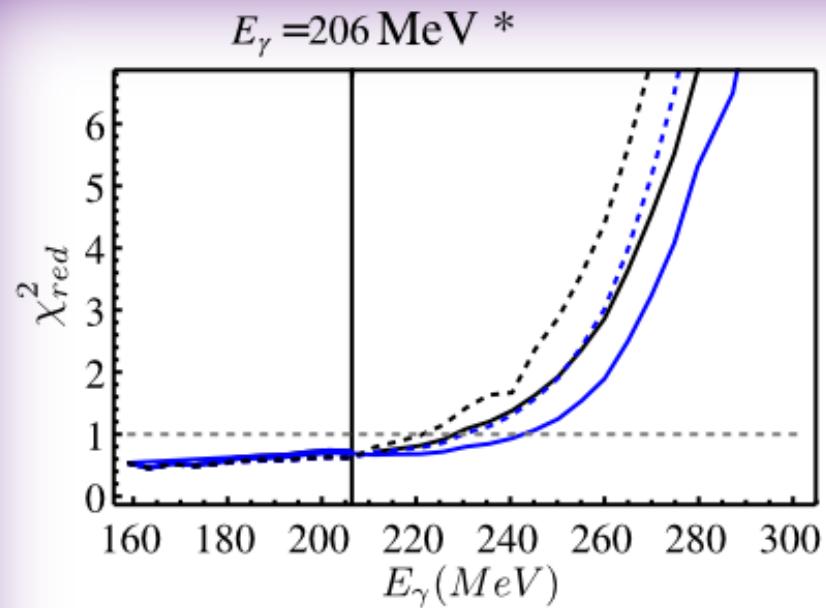
Results from corrections

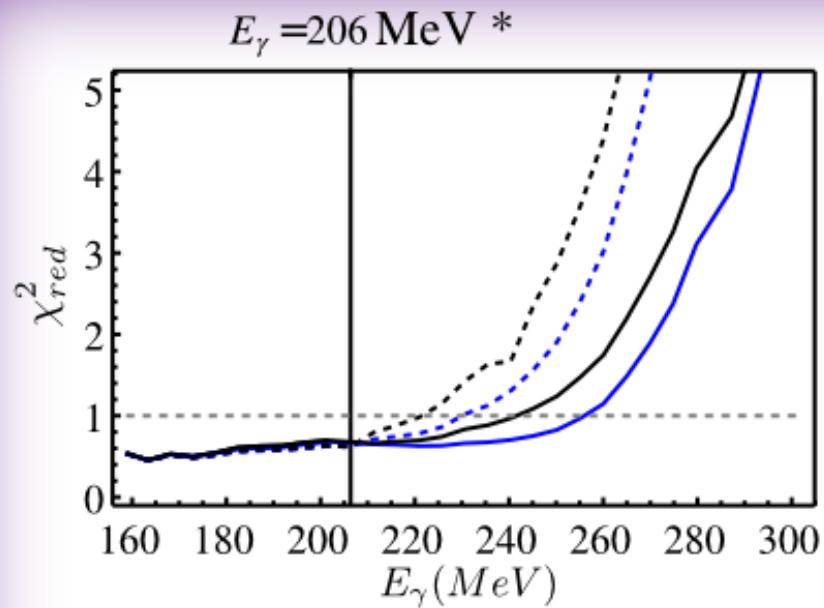


4th order H.B.

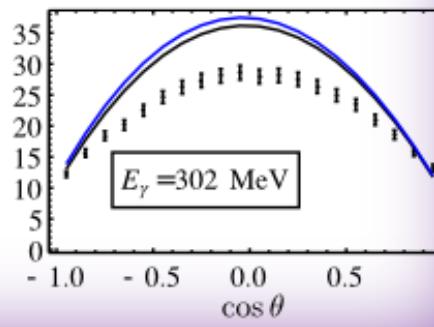
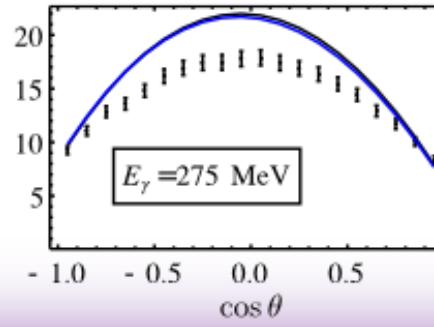
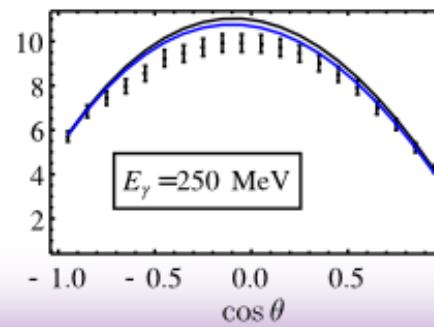
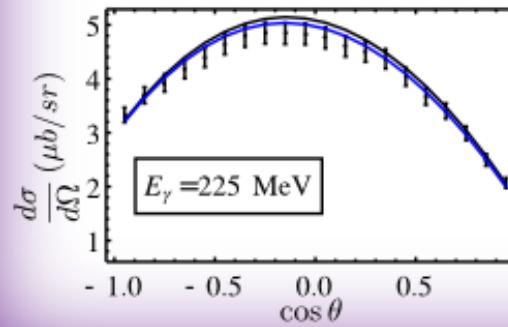
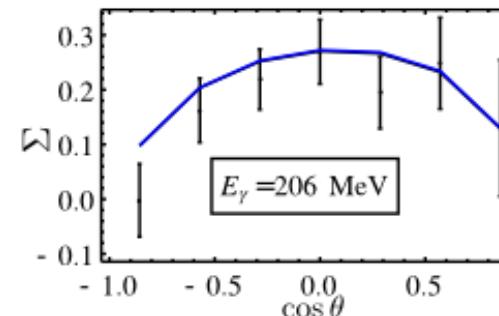
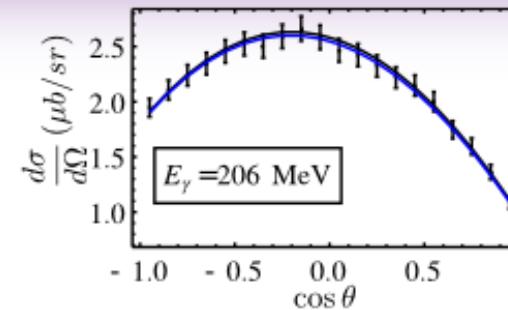
 Δ : — $\Delta + \text{V.C.}$: —*Fix LECs at
206 MeV.

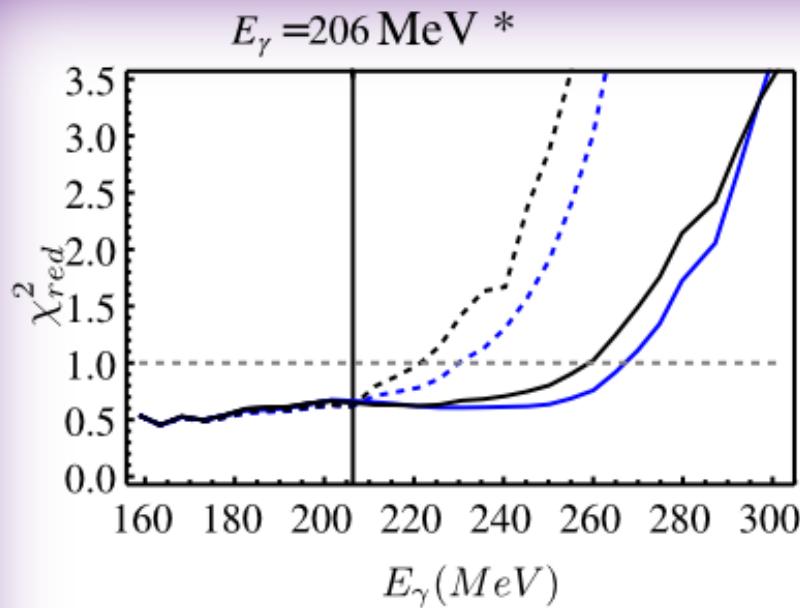
We are overestimating the data. Can we do better?

Varying g_M 

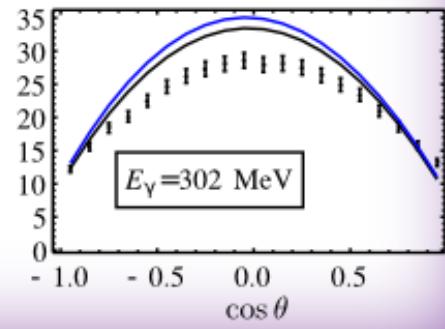
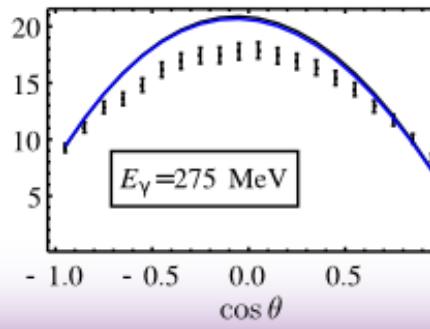
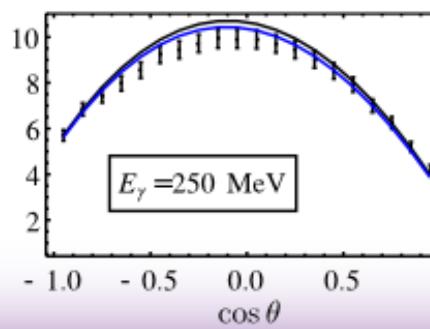
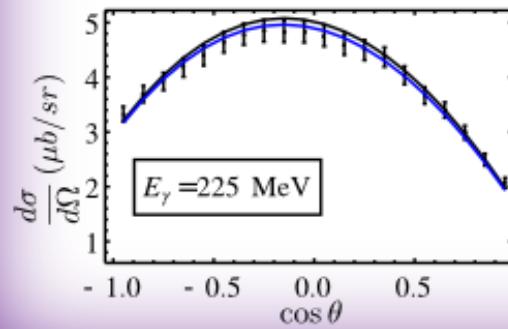
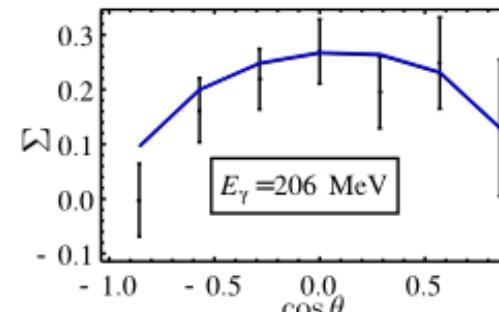
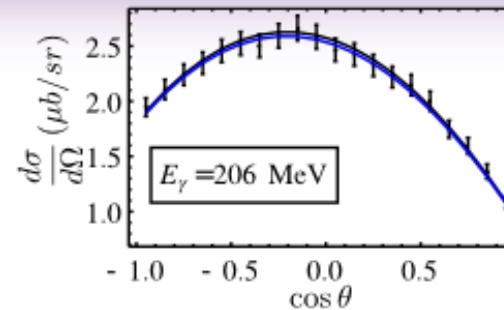
Varying g_M 

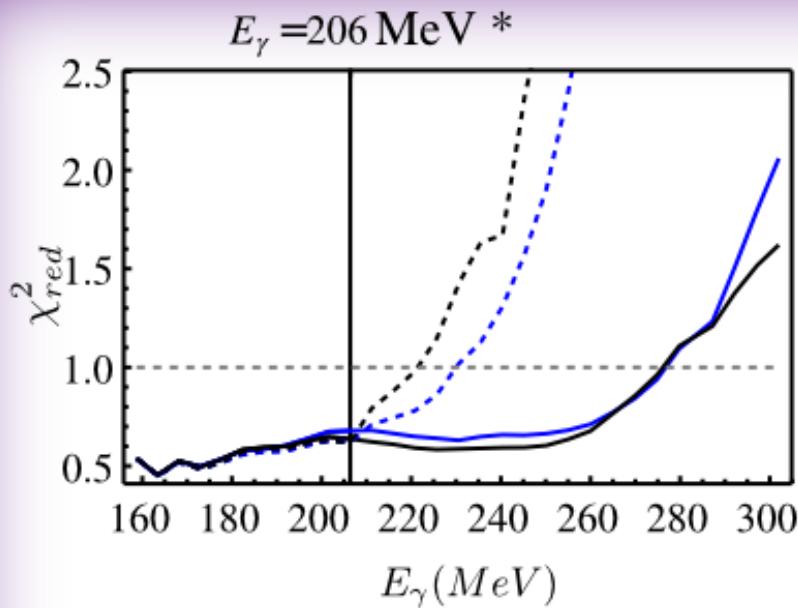
4th order H.B.

 Δ : — $\Delta + \text{V.C.}$: —*Fix LECs at
206 MeV. $g_M = 2.97$ — $g_M = 2.6$ —

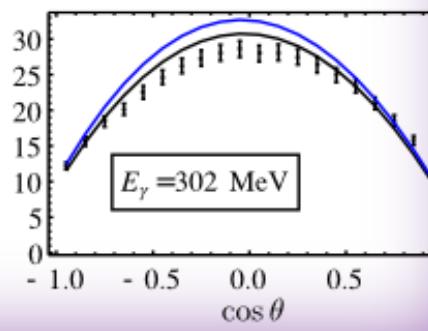
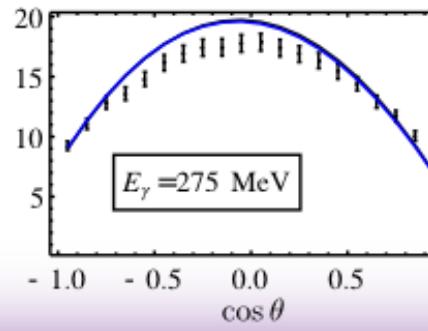
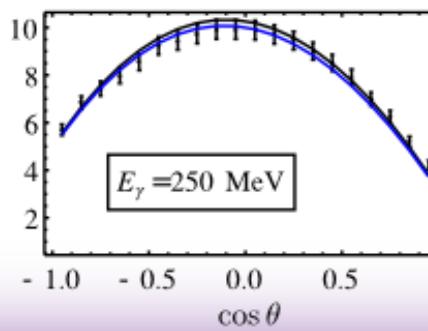
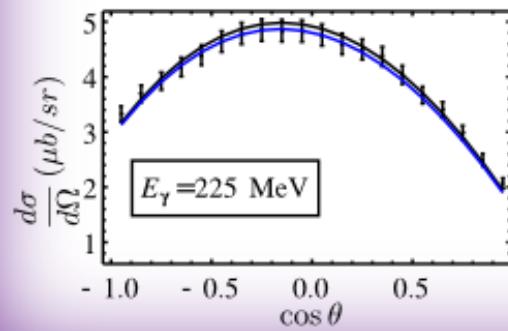
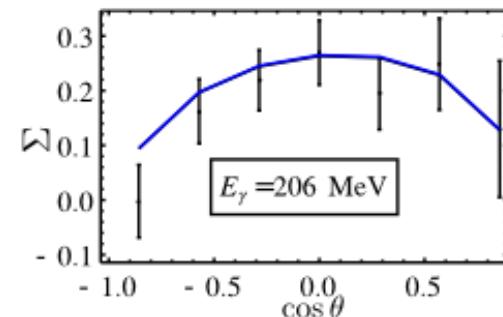
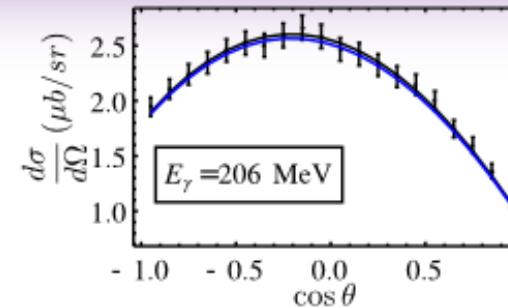
Varying g_M 

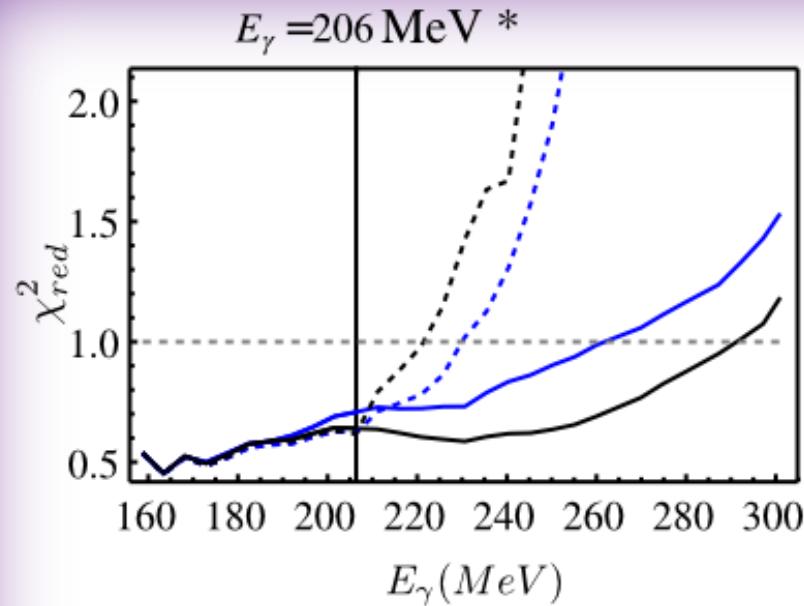
4th order H.B.

 Δ : — $\Delta + \text{V.C.}$: —*Fix LECs at
206 MeV. $g_M = 2.97$ — $g_M = 2.4$ —

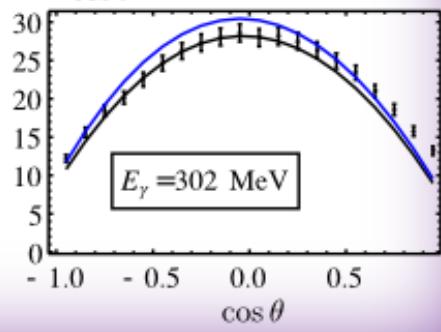
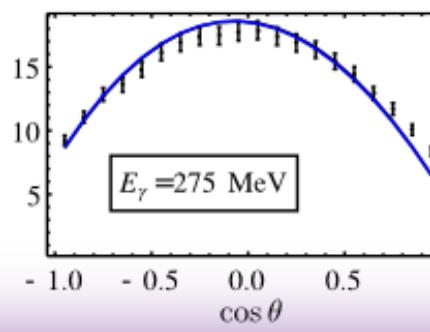
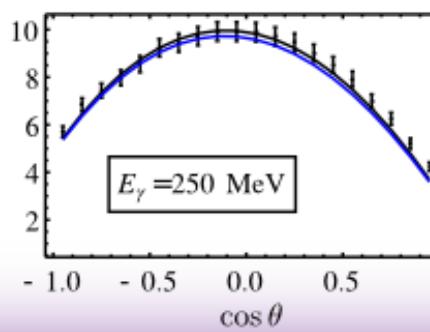
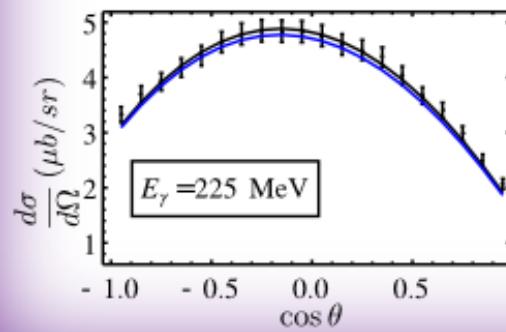
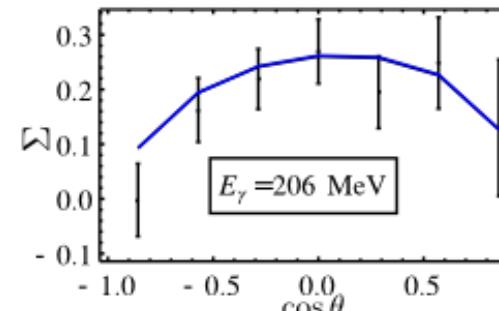
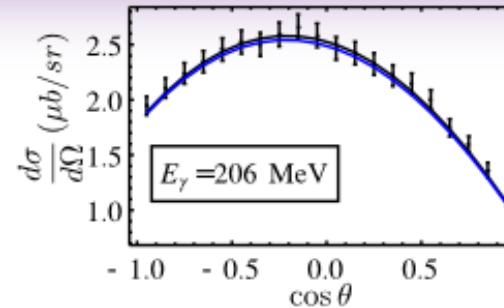
Varying g_M 

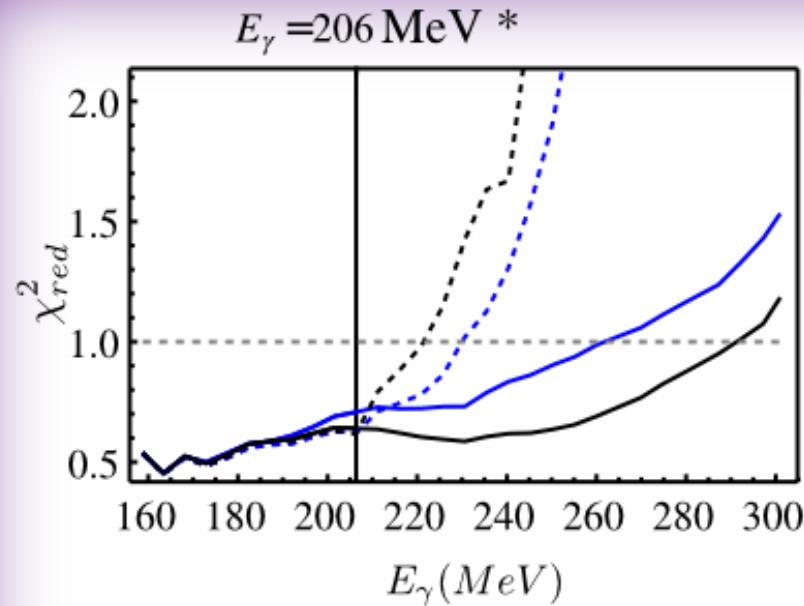
4th order H.B.

 Δ : — $\Delta + \text{V.C.}$: —*Fix LECs at
206 MeV. $g_M = 2.97$ — $g_M = 2.2$ —

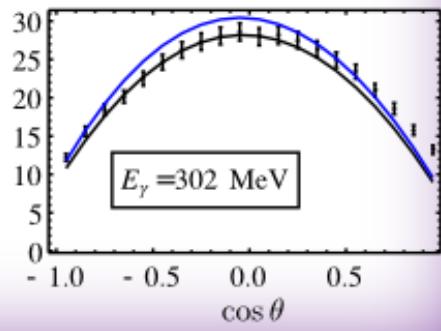
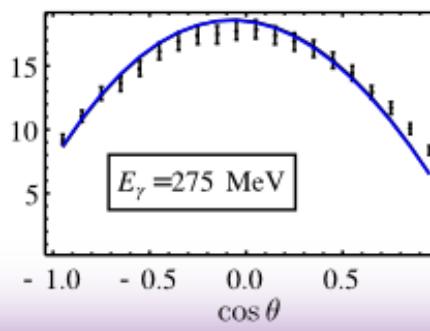
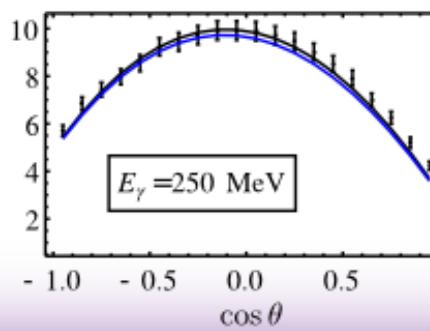
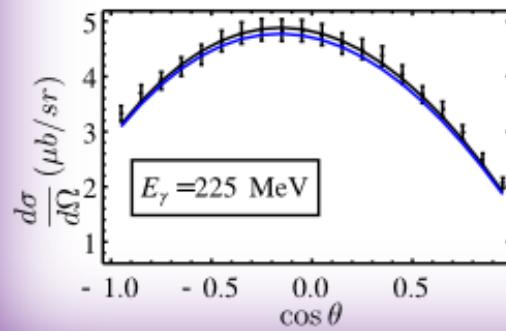
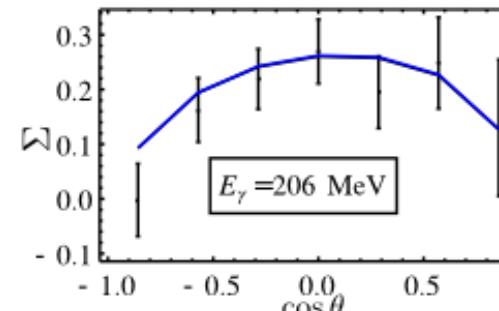
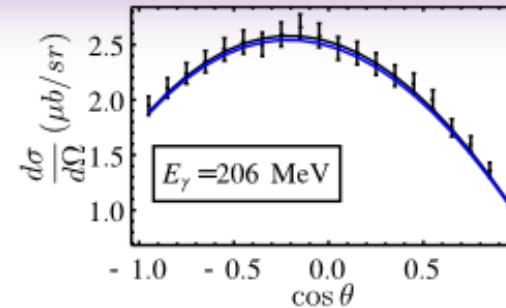
Varying g_M 

4th order H.B.

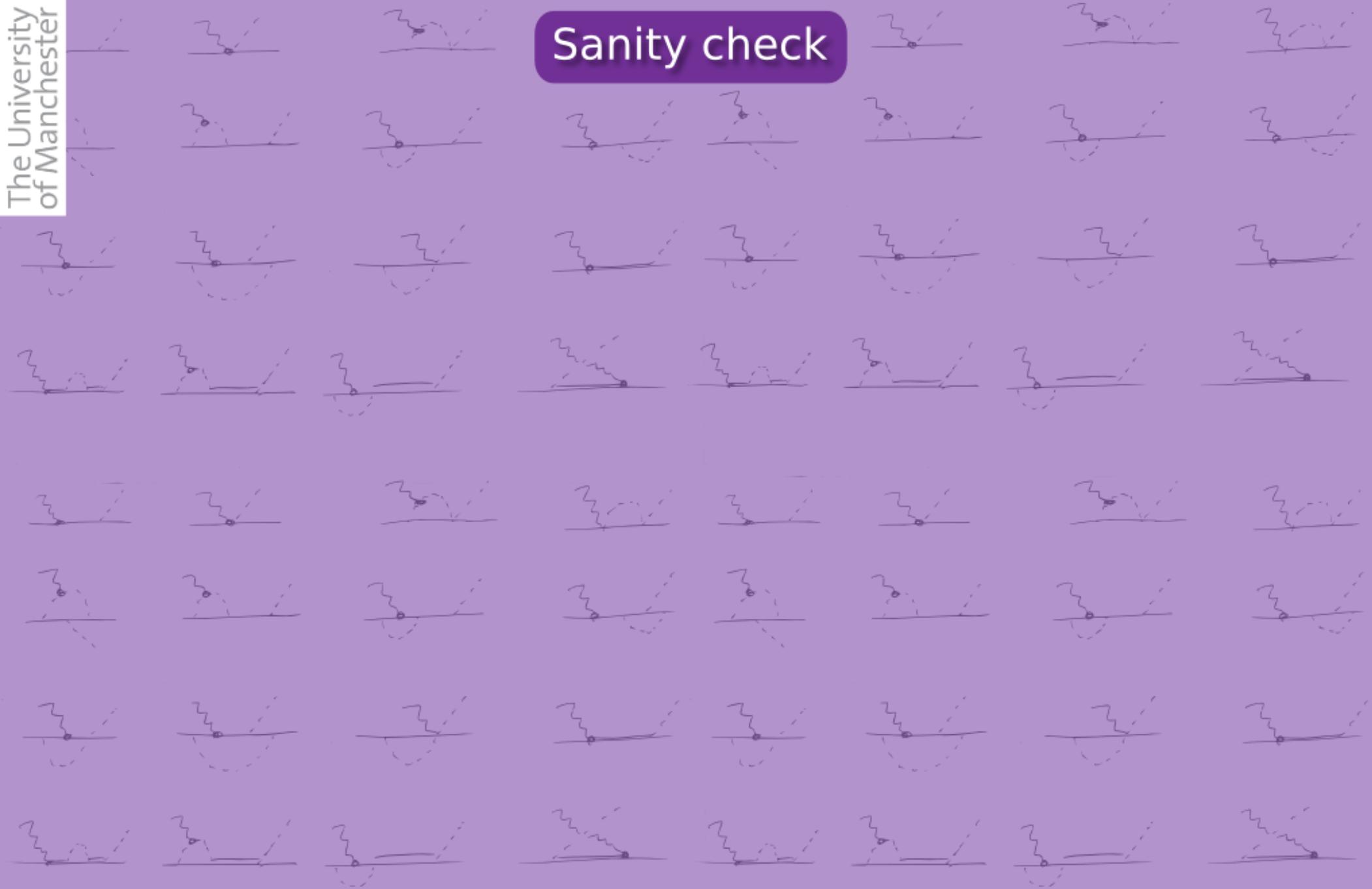
 Δ : $\Delta + V.C.$:*Fix LECs at
206 MeV. $g_M = 2.97$ — $g_M = 2.0$ —

Varying g_M 

4th order H.B.

 Δ : — $\Delta + V.C.$: -·-*Fix LECs at
206 MeV. $g_M = 2.97$ -·- $g_M = 2.0$ —Are we free to vary g_M so much?

Sanity check

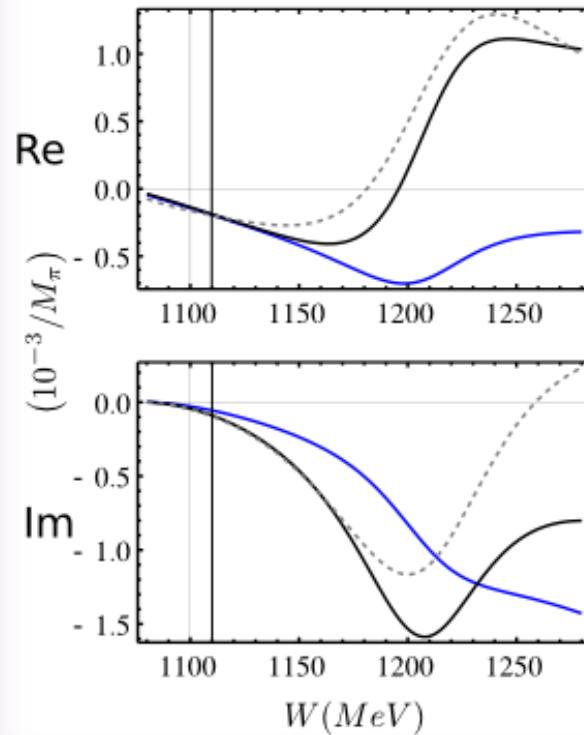


Sanity check

$g_M = 2.97$ 4th order H.B. Δ : — $\Delta + v.c.$: — MAID: - -

E_{1+}

$W = 1125 \text{ MeV}$

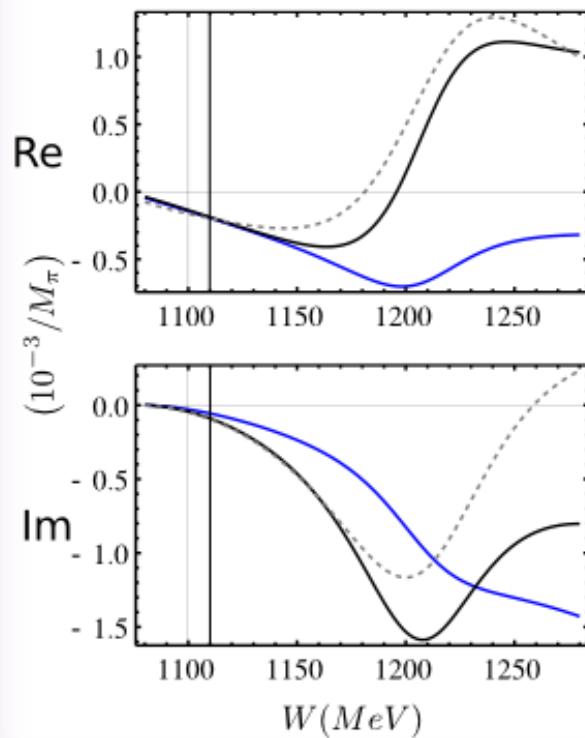


*Fix LECs at 1125 MeV.

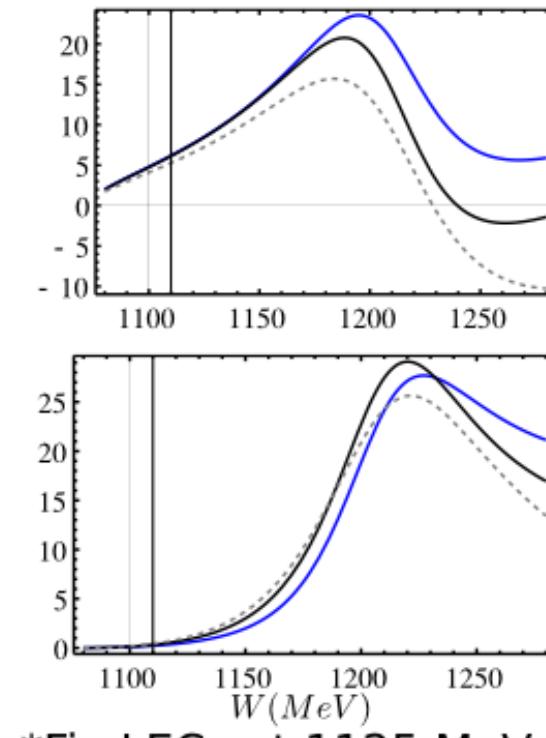
Sanity check

 $g_M = 2.97$

4th order H.B.

 E_{1+} $W = 1125 \text{ MeV}$  Δ : — $\Delta + \text{v.c.}$: —

MAID: - -

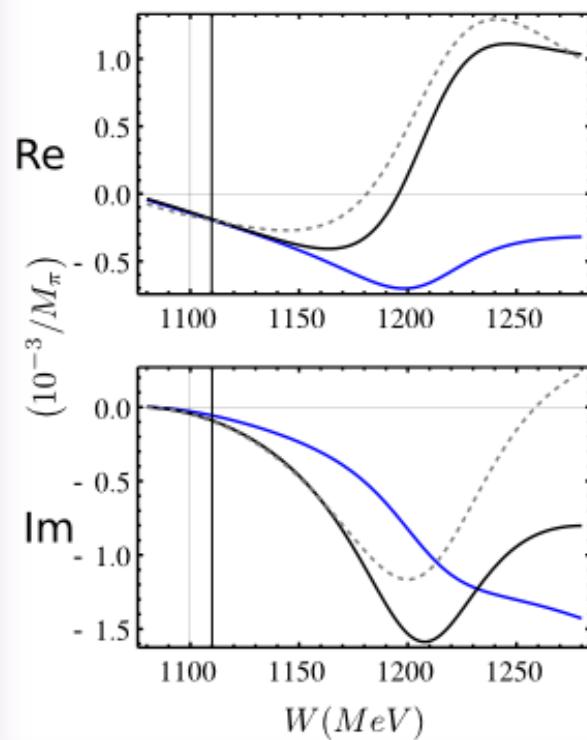
 M_{1+} $W = 1125 \text{ MeV}$ 

*Fix LECs at 1125 MeV.

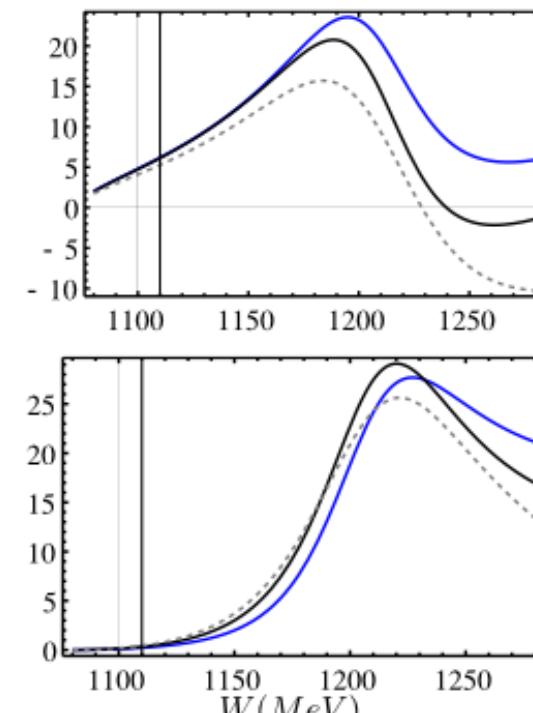
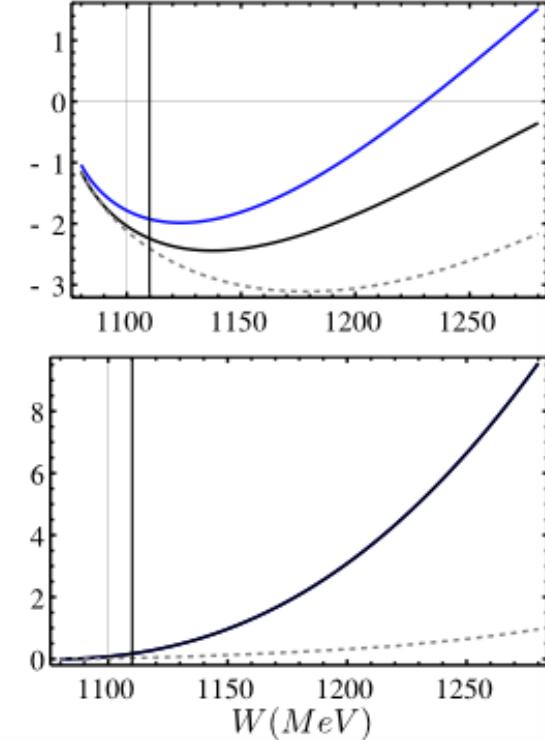
Sanity check

 $g_M = 2.97$

4th order H.B.

 E_{1+} $W = 1125 \text{ MeV}$  Δ : $\Delta + \text{v.c.}$:

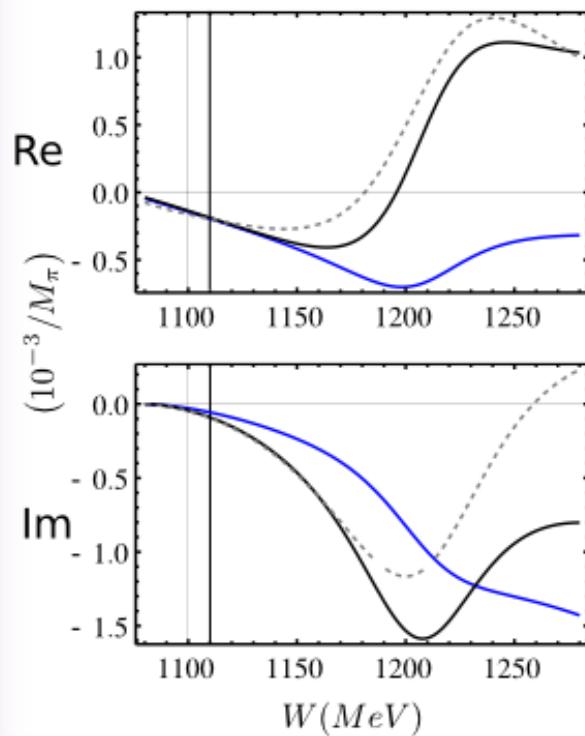
MAID:

 M_{1+} $W = 1125 \text{ MeV}$  M_{1-} $W = 1125 \text{ MeV}$ ***Fix LECs at 1125 MeV.**

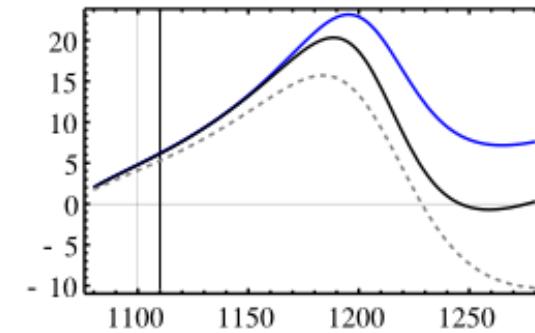
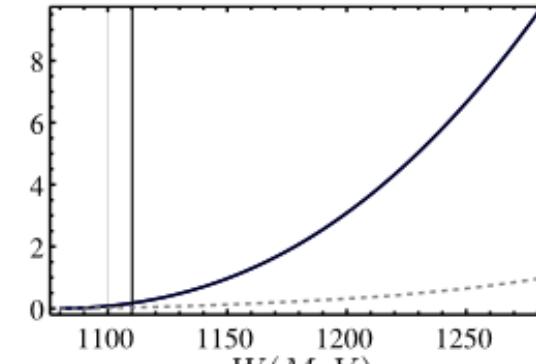
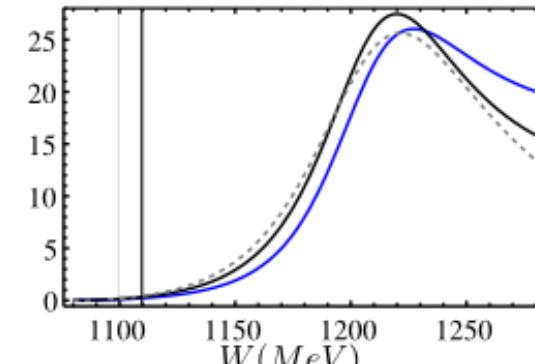
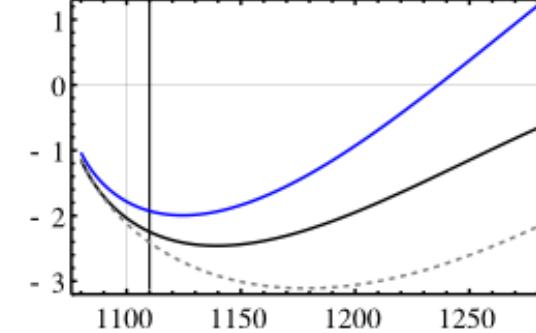
Sanity check

 $g_M = 2.8$

4th order H.B.

 E_{1+} $W = 1125 \text{ MeV}$  Δ : $\Delta + \text{v.c.}$:

MAID:

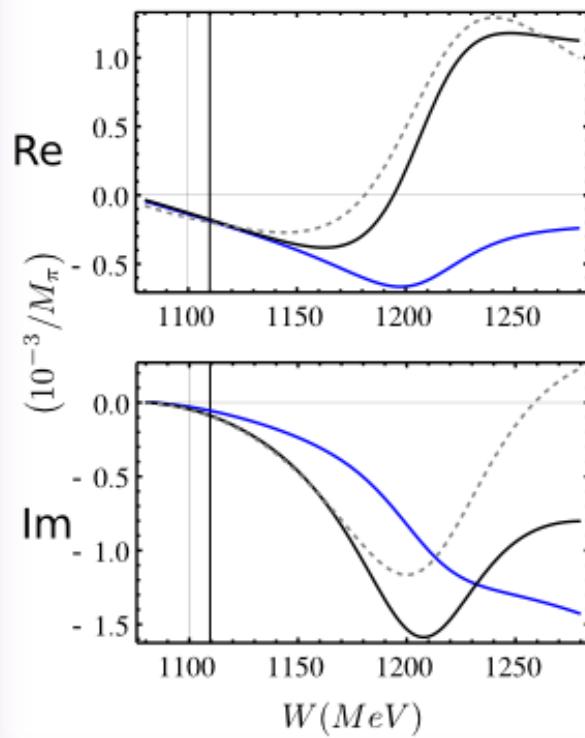
 M_{1+} $W = 1125 \text{ MeV}$  M_{1-} $W = 1125 \text{ MeV}$ 

*Fix LECs at 1125 MeV.

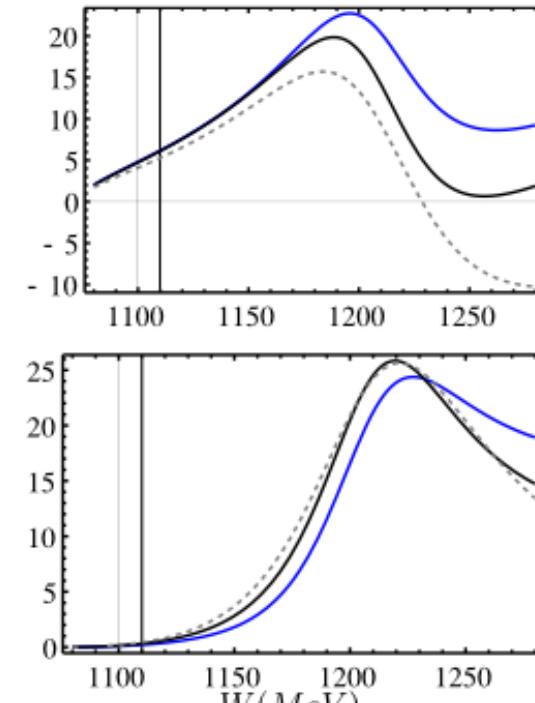
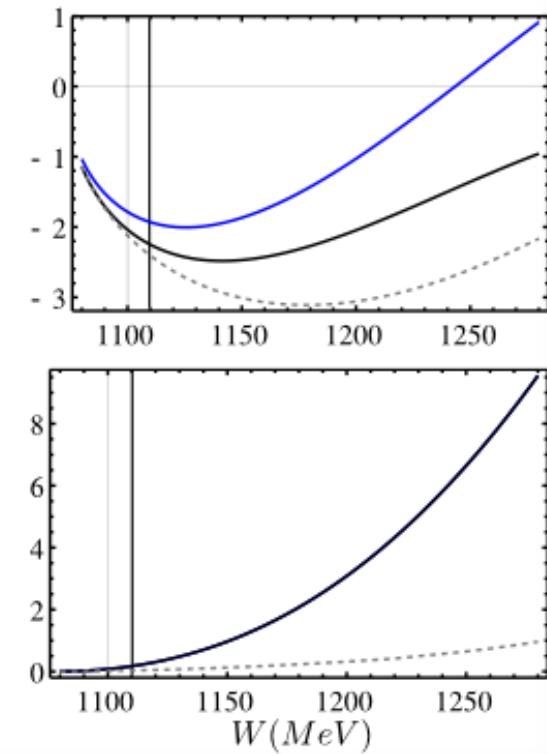
Sanity check

 $g_M = 2.6$

4th order H.B.

 E_{1+} $W = 1125 \text{ MeV}$  Δ : $\Delta + \text{v.c.}$:

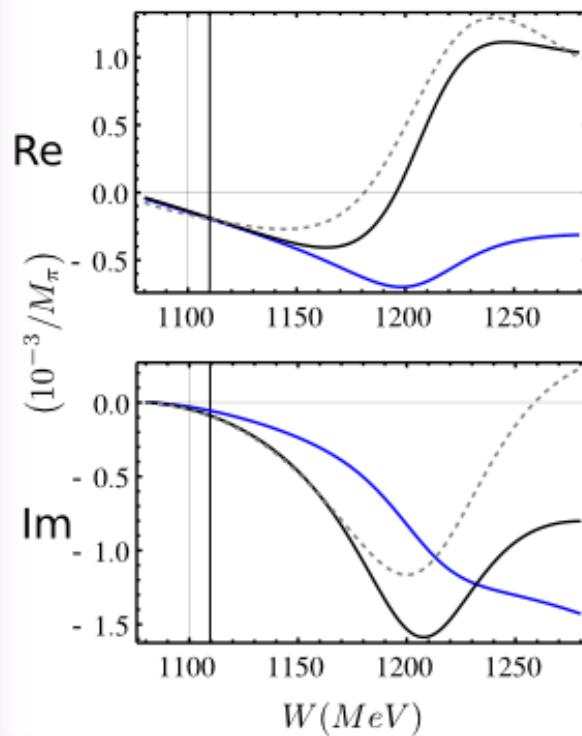
MAID:

 M_{1+} $W = 1125 \text{ MeV}$  M_{1-} $W = 1125 \text{ MeV}$ ***Fix LECs at 1125 MeV.**

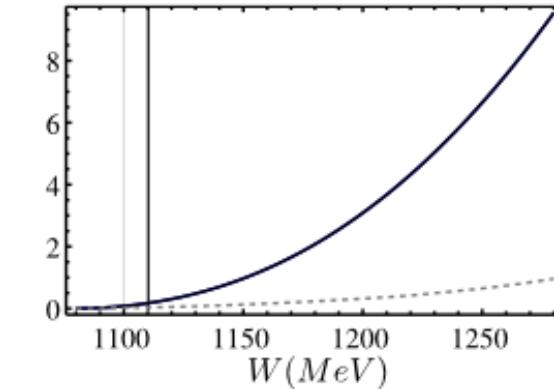
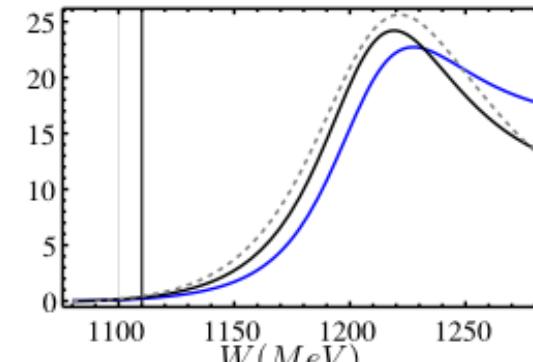
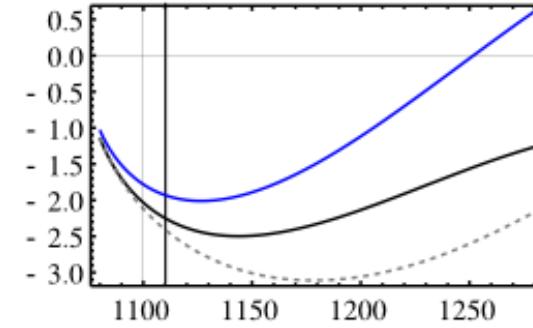
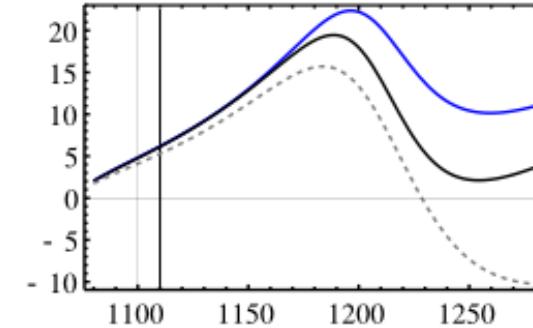
Sanity check

 $g_M = 2.4$

4th order H.B.

 E_{1+} $W = 1125 \text{ MeV}$  Δ : $\Delta + \text{v.c.}$:

MAID:

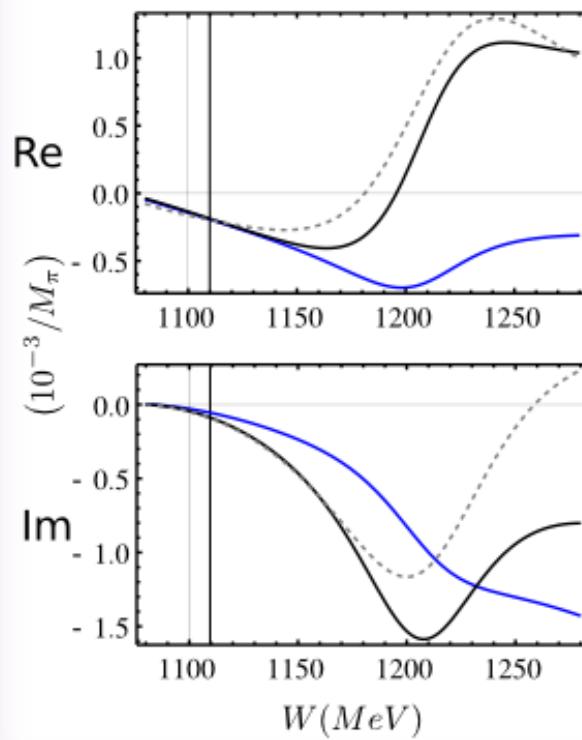
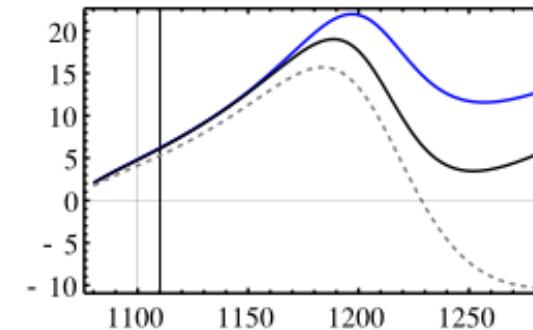
 M_{1+} M_{1-} $W = 1125 \text{ MeV}$ $W = 1125 \text{ MeV}$ 

*Fix LECs at 1125 MeV.

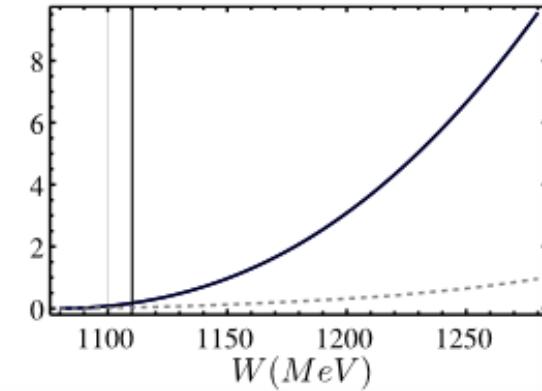
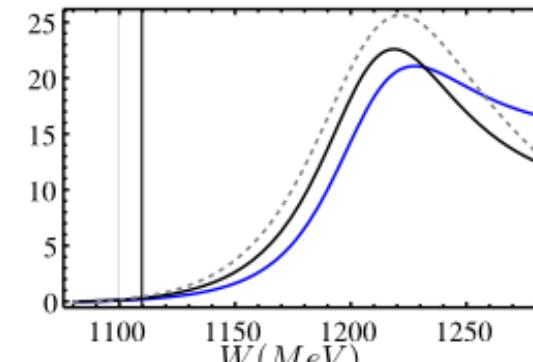
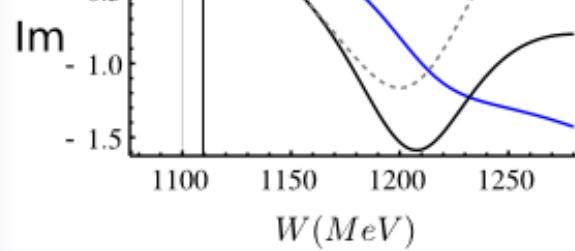
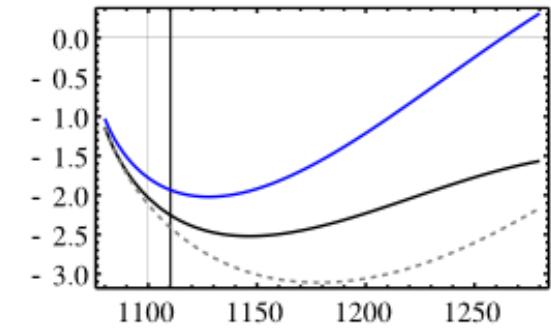
Sanity check

 $g_M = 2.2$

4th order H.B.

 E_{1+} $W = 1125 \text{ MeV}$  Δ : $\Delta + \text{v.c.}$: M_{1+} $W = 1125 \text{ MeV}$ 

MAID:

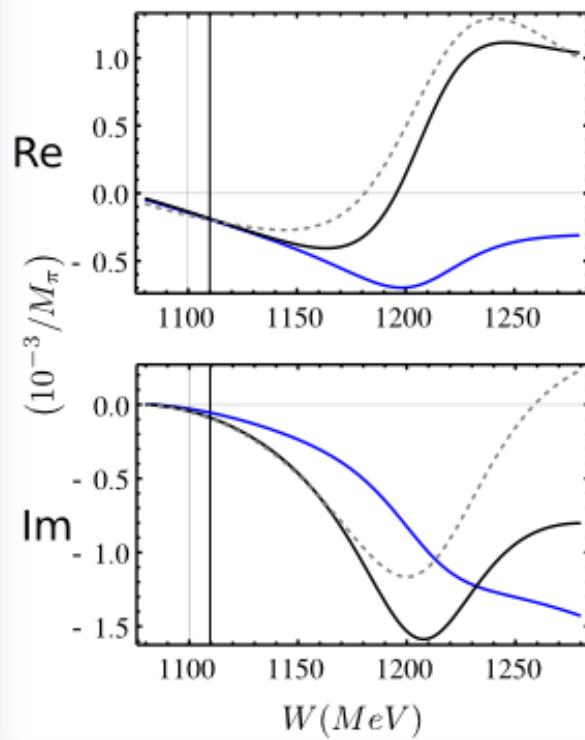
 M_{1-} $W = 1125 \text{ MeV}$ 

*Fix LECs at 1125 MeV.

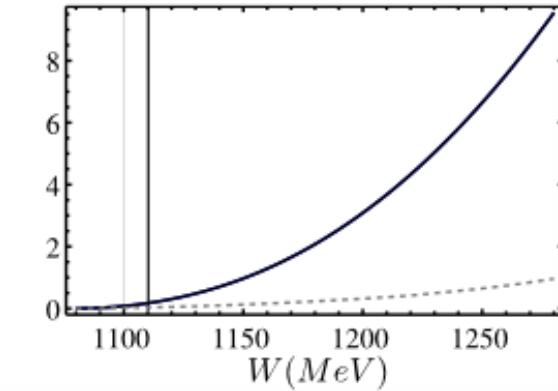
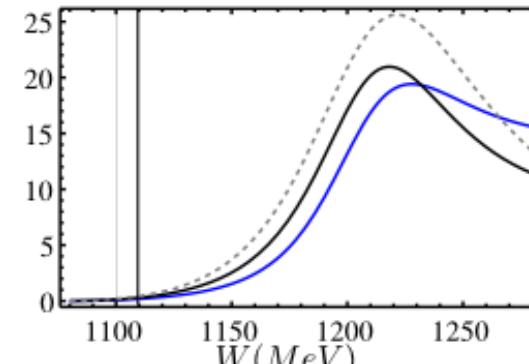
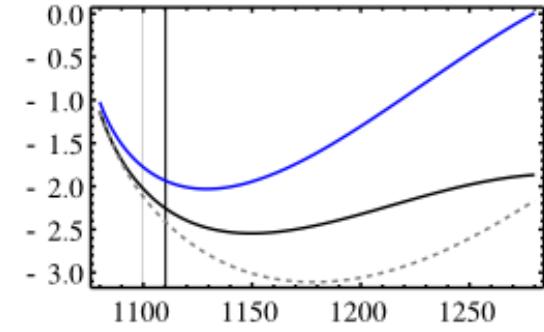
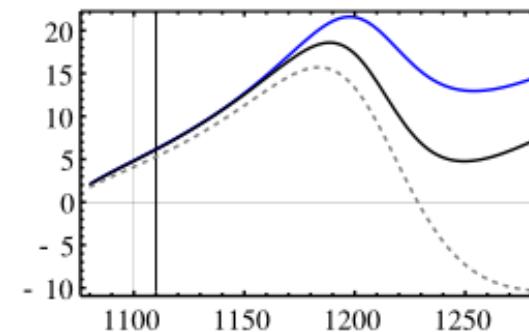
Sanity check

 $g_M = 2.0$

4th order H.B.

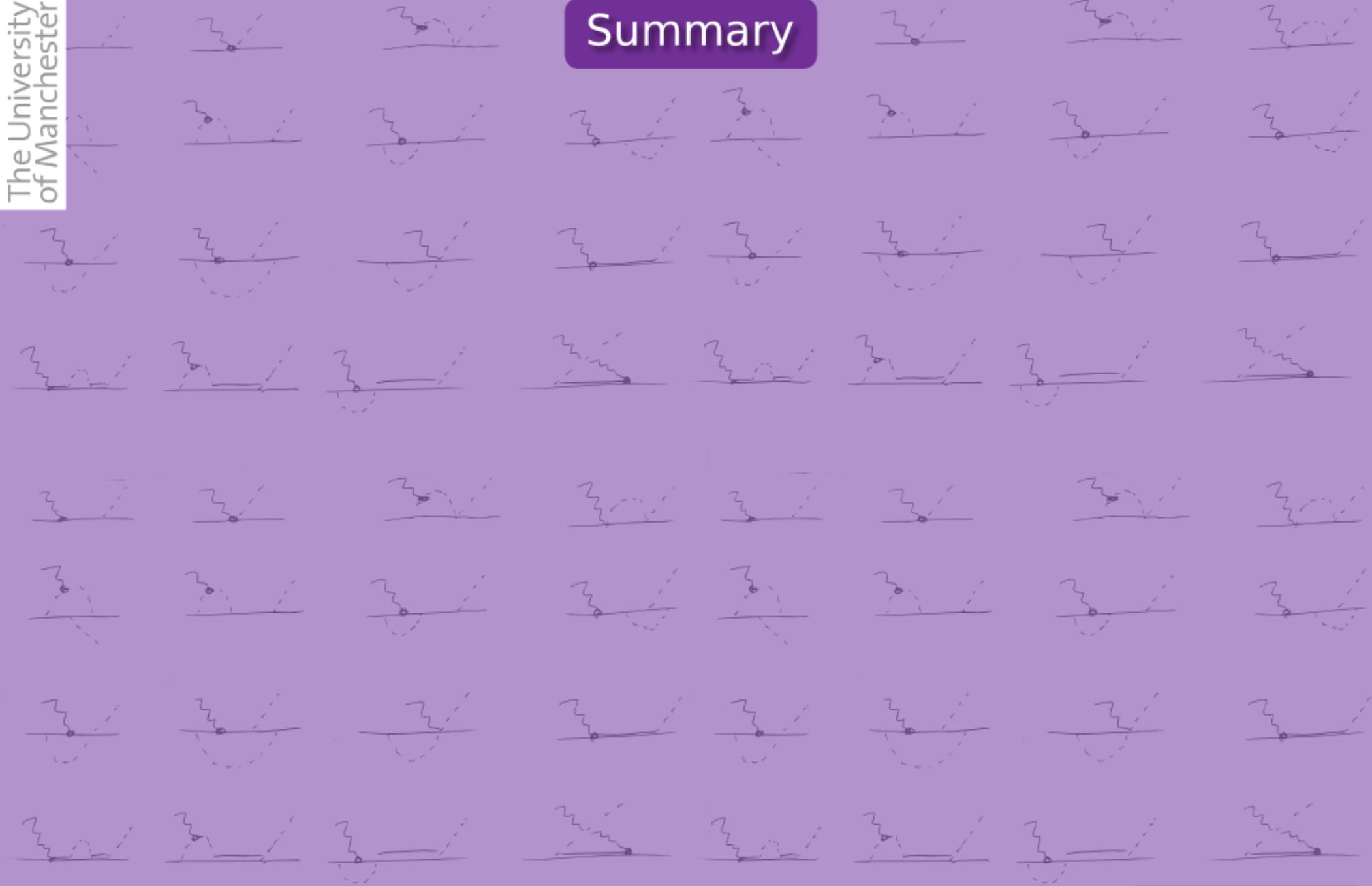
 E_{1+} $W = 1125 \text{ MeV}$  Δ : $\Delta + \text{v.c.}$:

MAID:

 M_{1+} M_{1-} $W = 1125 \text{ MeV}$ 

*Fix LECs at 1125 MeV.

Summary



Summary

It is possible to describe neutral pion photoproduction from threshold to energies approaching the $\Delta(1232)$ resonance.

Summary

It is possible to describe neutral pion photoproduction from threshold to energies approaching the $\Delta(1232)$ resonance.

D-waves (and higher) do not appear to have a significant effect.

More data on more observables could change this.

Summary

It is possible to describe neutral pion photoproduction from threshold to energies approaching the $\Delta(1232)$ resonance.

D-waves (and higher) do not appear to have a significant effect.

More data on more observables could change this.

Vertex corrections to $\gamma N\Delta$ coupling constants show good agreement with MAID at high energies.

Summary

It is possible to describe neutral pion photoproduction from threshold to energies approaching the $\Delta(1232)$ resonance.

D-waves (and higher) do not appear to have a significant effect.

More data on more observables could change this.

Vertex corrections to $\gamma N\Delta$ coupling constants show good agreement with MAID at high energies.

Extend 4th order heavy baryon calculations to all states of angular momentum.

Test theories against data at even higher energies.

Summary

It is possible to describe neutral pion photoproduction from threshold to energies approaching the $\Delta(1232)$ resonance.

D-waves (and higher) do not appear to have a significant effect.

More data on more observables could change this.

Vertex corrections to $\gamma N\Delta$ coupling constants show good agreement with MAID at high energies.

Extend 4th order heavy baryon calculations to all states of angular momentum.

Test theories against data at even higher energies.

Thank you to David Hornidge for providing us with the data and the STFC for funding this work.

Impact of the $\Delta(1232)$ in $\gamma + p \rightarrow \pi^0 p$ in χ PT.

Lloyd W. Cawthorne
Judith A. McGovern

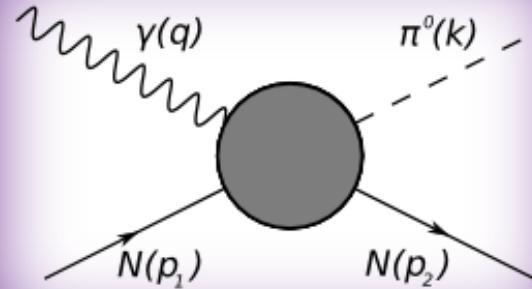
The University of Manchester

lloyd.cawthorne@postgrad.manchester.ac.uk

29th of June 2015

Importance of D-waves

Working to energies approaching $\Delta(1232)$



Has been studied using χ PT since the early 90s.

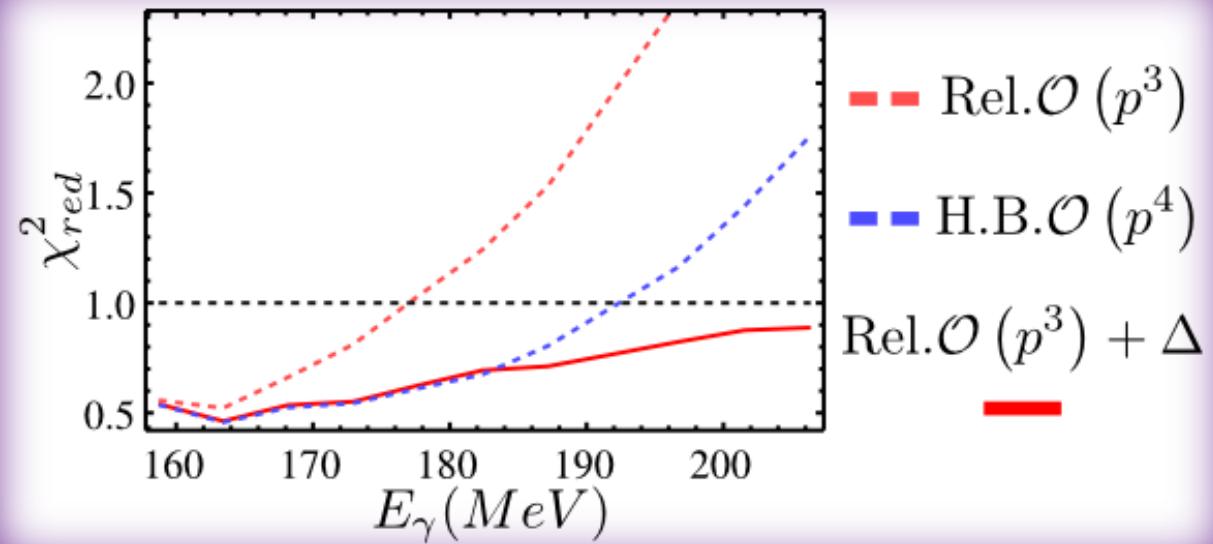
Requires the inclusion of pion loops for an adequate description.

More physics required to go beyond the threshold region.

More accurate studies can be performed thanks to data from MAMI.

$$\frac{d\sigma}{d\Omega} \Sigma = \frac{d\sigma^\perp - d\sigma^\parallel}{d\sigma^\perp + d\sigma^\parallel}$$

Hornidge et al (2013) PRL



Hybrid calculations.

4th order heavy baryon description.
Calculated for S and P-waves, up to L=1.
Bernard et al, (1996) Z. Phys;
(2001) Eur. Phys. J.

3rd order covariant theory.
No truncation of angular momentum.
Can extract D-waves and beyond.
Bernard et al, (1992) Nucl. Phys. B;
(1994) Phys. Rep.

4th order LECs used:

$$E_{0+}^{ct} = ea_2\omega^3 + ea_1\omega M_\pi^2$$

$$P_1^{ct} = \frac{eg_A |\vec{k}_\pi| \omega^2}{m_N (4\pi F_\pi)^3} \xi_1$$

$$P_2^{ct} = \frac{eg_A |\vec{k}_\pi| \omega^2}{m_N (4\pi F_\pi)^3} \xi_2$$

$$P_3^{ct} = e |\vec{k}_\pi| b_P \left(\omega - \frac{M_\pi^2}{2m} \right)$$

We extract the relativistic D-waves to construct a hybrid theory.

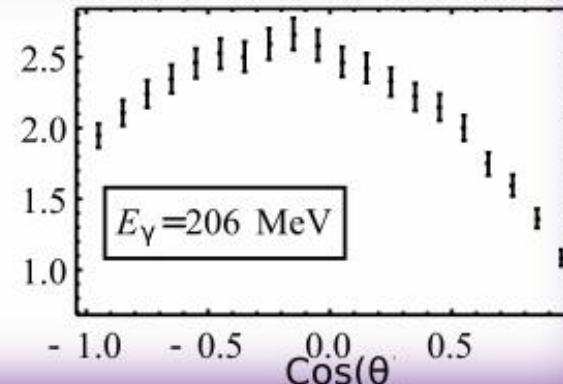
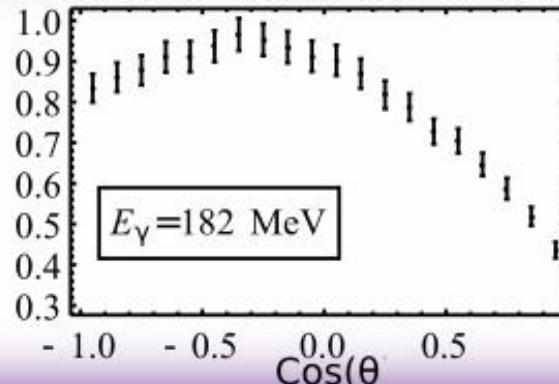
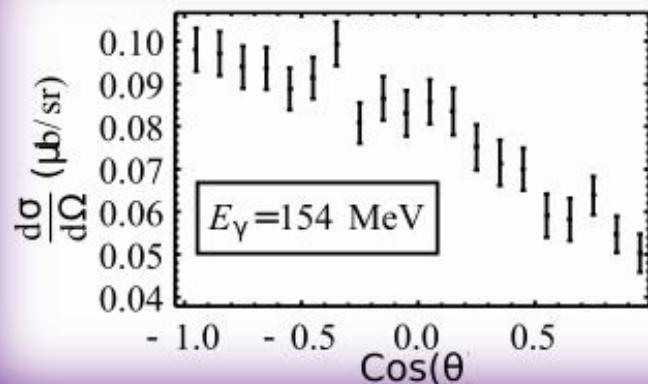
We expect D-waves to be suppressed in the HB description.

Details of Observables

$$\frac{|\vec{q}_\gamma|}{|\vec{k}_\pi|} \frac{d\sigma}{d\Omega_{cm}} = A + B \cos \theta + C \cos^2 \theta + \dots$$

Increasing energy allows access to more multipoles, changing the shape.

Looking at the data from MAMI:



Hornidge et al, (2013) PRL

$$\Sigma = \frac{d\sigma^\perp - d\sigma^\parallel}{d\sigma^\perp + d\sigma^\parallel} = \frac{|\vec{k}_\pi| \sin^2 \theta}{2|\vec{q}_\gamma|} \left(\frac{d\sigma}{d\Omega_{cm}} \right)^{-1} (|P_3|^2 - |P_2|^2 + \dots)$$

How important are D-waves? (and higher?)

$$\frac{|\vec{q}_\gamma|}{|\vec{k}_\pi|} \frac{d\sigma}{d\Omega_{cm}} = T_0(W) + T_1(W)\mathcal{P}_1(\theta) + T_2(W)\mathcal{P}_2(\theta) + T_3(W)\mathcal{P}_3(\theta) + \dots$$

$$T_0 = S \times S + P \times P + D \times D + \dots$$

$$T_1 = S \times P + P \times P + D \times F + \dots$$

$$T_2 = S \times D + P \times P + D \times D + P \times F \dots$$

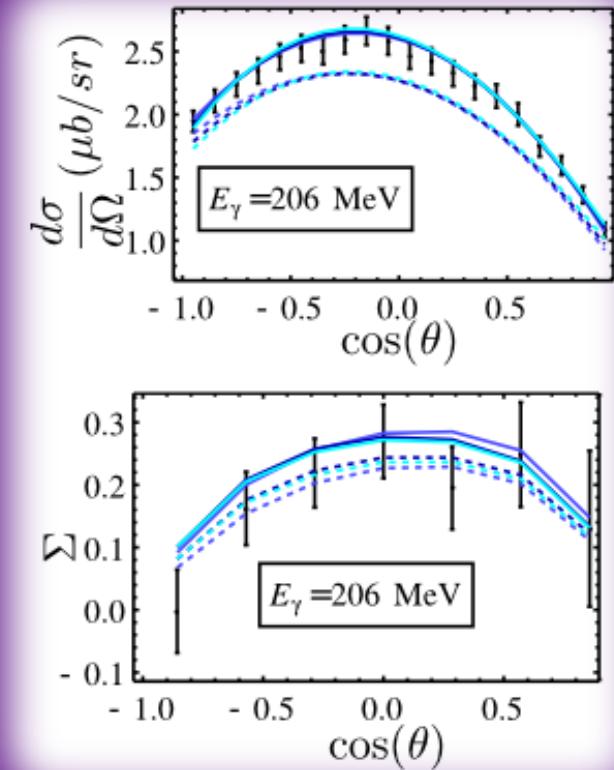
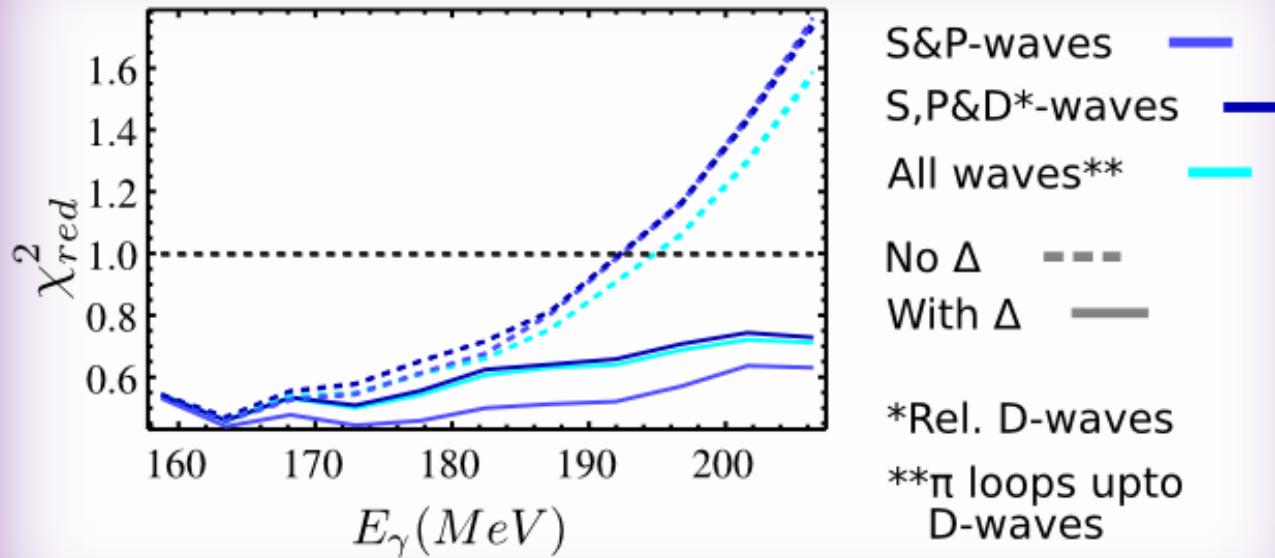
$$T_3 = P \times D + \dots \quad T_4 = D \times D + \dots$$

D-wave amplitudes
are small.
Interference from
D-waves might not be.

Fernández-Ramírez, et al.
(2009) Phys. Rev. C.

Effects of D-waves (and higher)

The effects of D-waves (and beyond) are small.

The small effect of L=2 states (and above) are dwarfed by the Δ .

Working to higher energies

One can include π loop diagrams containing a Δ propagator.

Close to threshold: $\omega \sim M_\pi \approx 140\text{MeV}$ SB scale: $\Lambda_{SB} \approx 700\text{MeV}$

Mass difference: $\Delta_M = m_\Delta - m_N \approx 290\text{MeV}$ $M_\pi \ll \Delta_M$

$$P = \frac{M_\pi}{\Lambda} \approx 0.2$$

Two scales:

$$\epsilon = \frac{\Delta_M}{\Lambda} \approx 0.4$$

$$\delta \approx \frac{\Delta_M}{\Lambda} \approx \left(\frac{M_\pi}{\Lambda}\right)^{1/2} \quad P \approx \delta^2$$

Propagator: $S_\Delta(\omega \sim M_\pi) \propto \frac{1}{\Delta_M \pm \omega}$ scales as δ^{-1}

Pascalutsa, et al. (2006), Phys. Rev. D

Two energy regimes

Close to threshold: $\omega \sim M_\pi$ $P \approx \delta^2$ Close to resonance: $\omega \sim \Delta_M$

Scales change: $P = \frac{\omega}{\Lambda} \approx \frac{\Delta_M}{\Lambda} = \delta$

Propagator:

$$S_\Delta(\omega \sim \Delta_M) \propto \frac{1}{\Delta_M + i\text{Im}\Sigma_\Delta - \omega}$$

Self energy: Σ_Δ

given by:

scales as: δ^3

$$S_\Delta(\omega \sim \Delta_M) \text{ scales as: } \delta^{-3}$$

Pascalutsa, et al. (2006) Phys. Rev. D

$\gamma N\Delta$ vertex corrections

Order of diagrams changes with energy.

Tree level:



$$\omega \sim M_\pi \quad eP^2\delta^{-1} \rightarrow e\delta^3$$

$$\omega \sim \Delta_M \quad eP^2\delta^{-3} \rightarrow e\delta^{-1}$$



$$eP^2\delta^{-1} \rightarrow e\delta^3$$

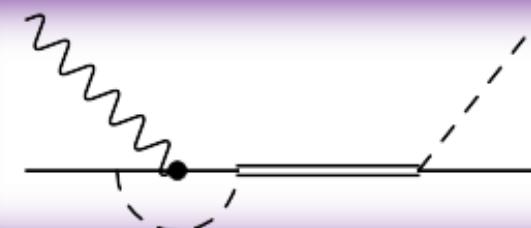
$$eP^2\delta^{-1} \rightarrow e\delta$$

Loop
corrections:



$$\omega \sim M_\pi \quad eP^3\delta^{-1} \rightarrow e\delta^5$$

$$\omega \sim \Delta_M \quad eP^3\delta^{-3} \rightarrow e\delta^0$$



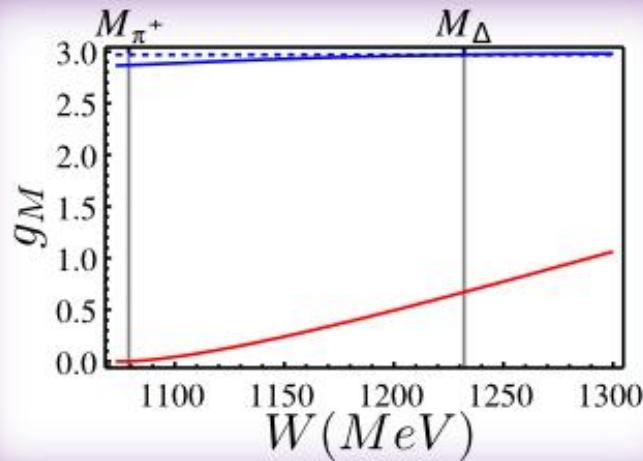
$$eP^4\delta^{-1} \rightarrow e\delta^6$$

$$eP^4\delta^{-3} \rightarrow e\delta$$

McGovern, et al. (2013) Eur. Phys. J; Pascalutsa, et al. (2006) Phs. Rev. D

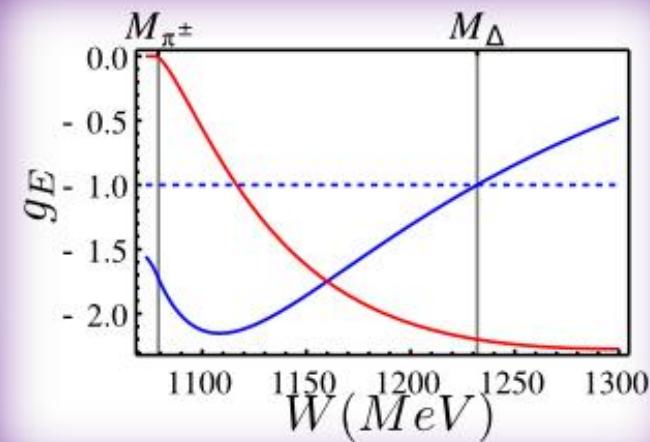
Effects of $\gamma N\Delta$ vertex corrections

The corrections are implemented by scaling the coupling constants with energy

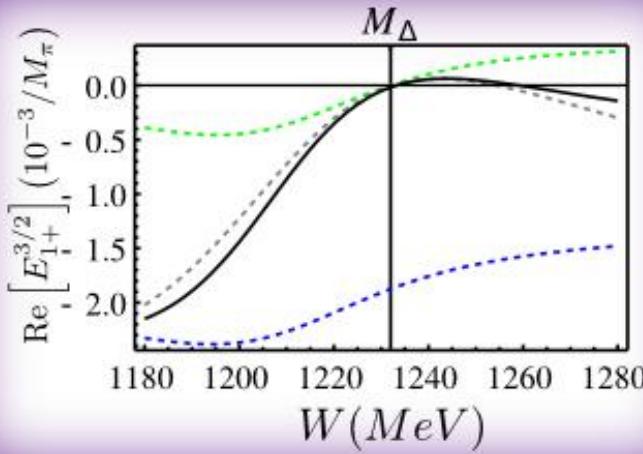


Re: —
Im: —
No corrections: - - -

McGovern,
et al. (2013)
Eur. Phys. J.

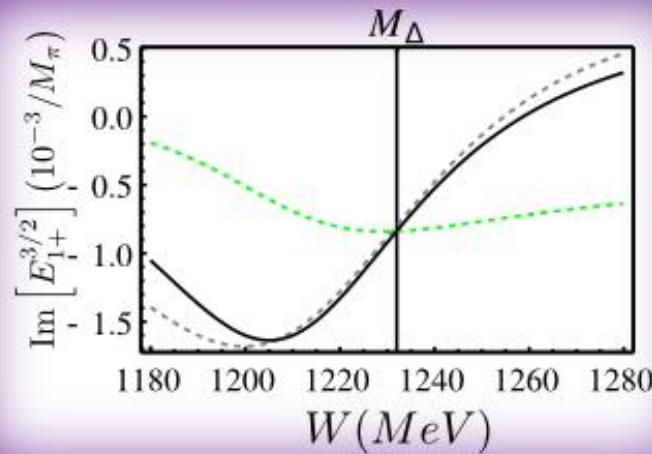


They restore Watson's theorem.

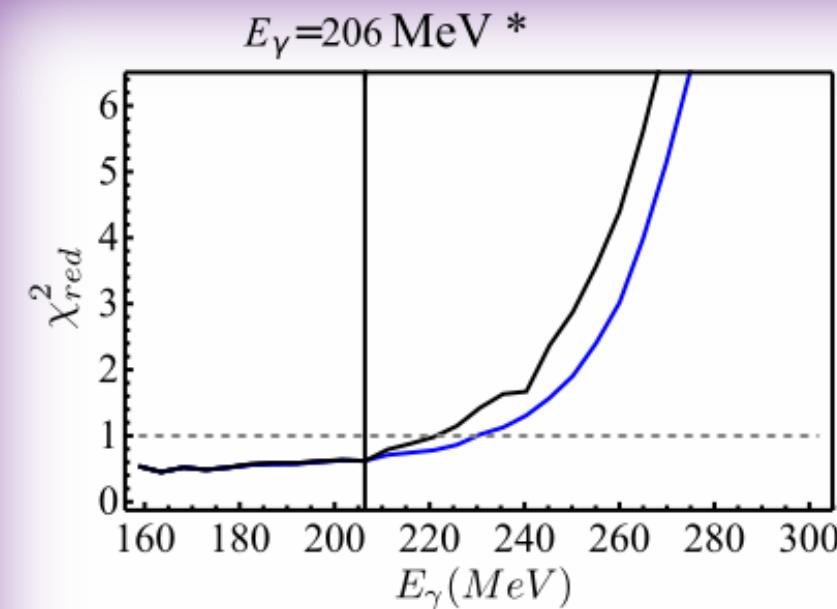


MAID: ---
 Δ : ----
 $\Delta + \text{Tree}$: - - -
 $\Delta + \text{Tree} + \text{V.C.}$: —

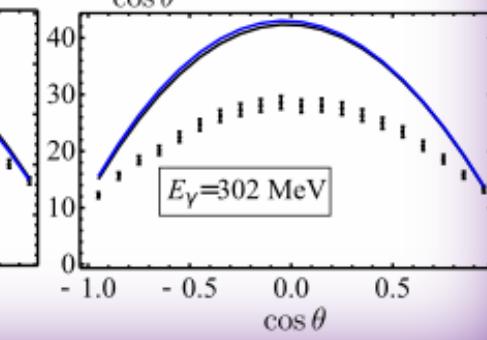
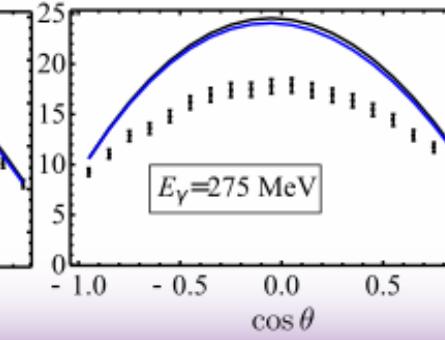
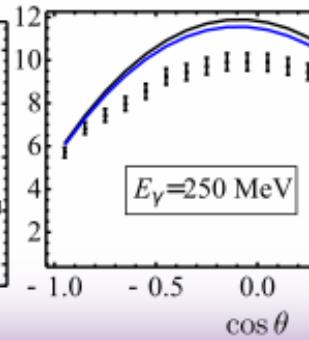
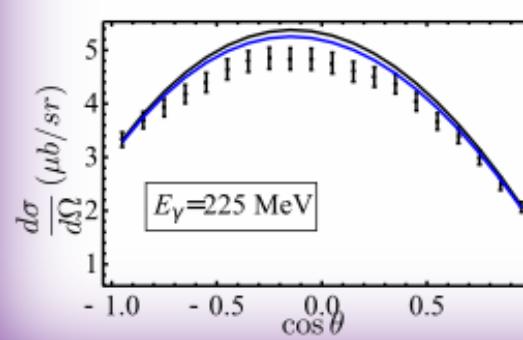
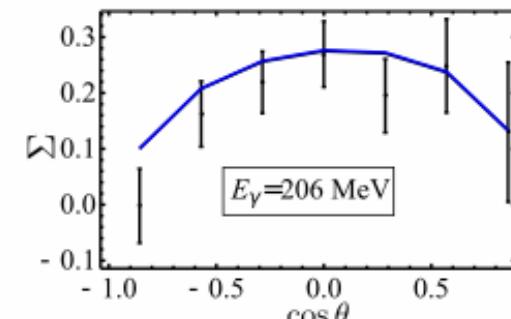
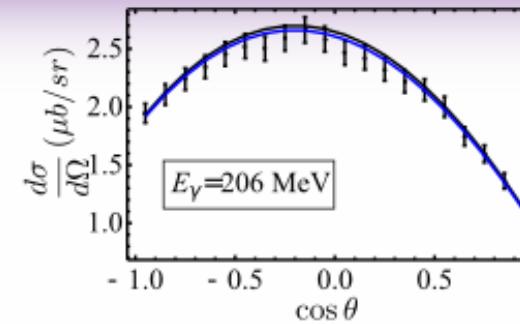
Pascalutsa, et al.
(2006) Phys. Rev. D



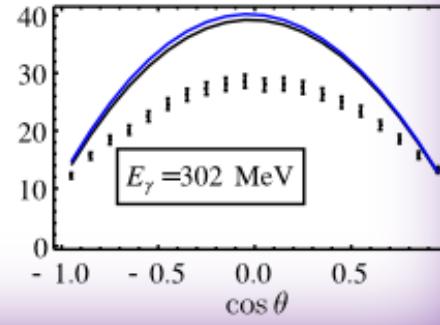
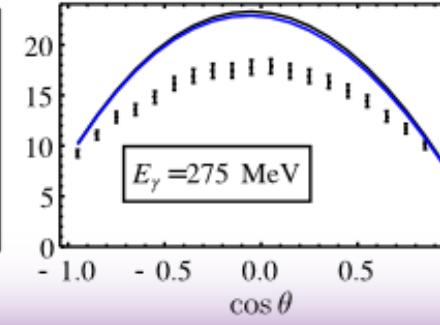
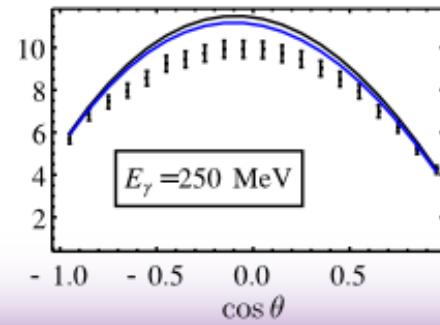
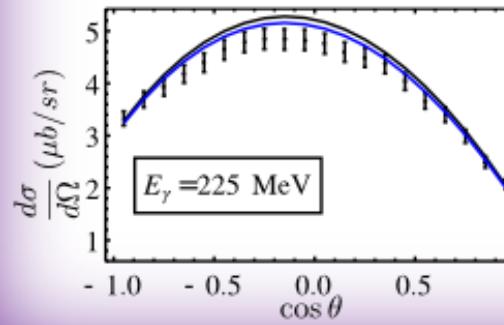
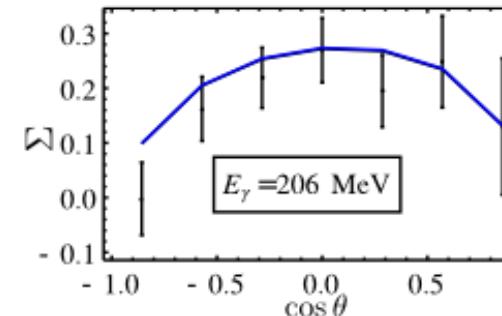
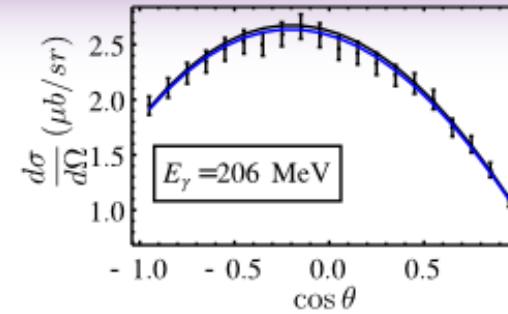
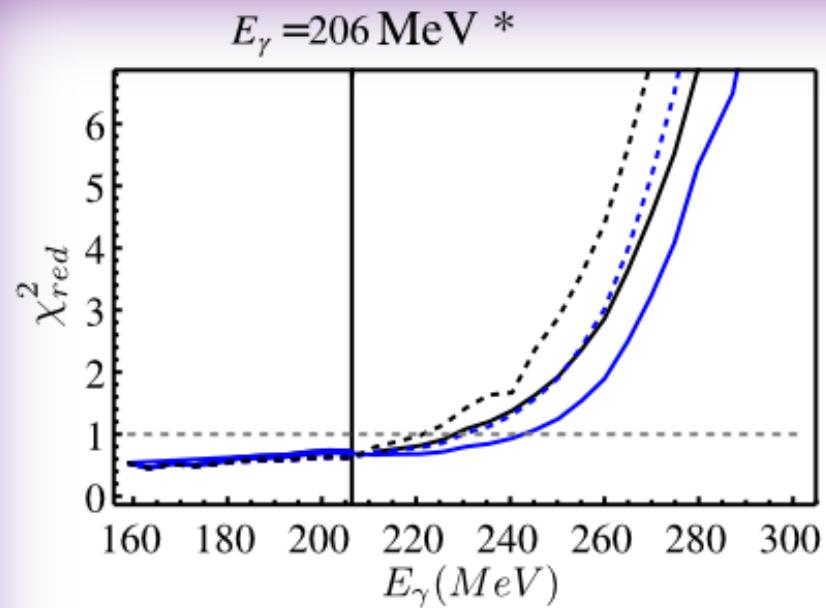
Results from corrections

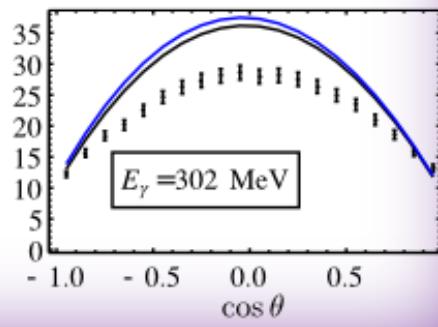
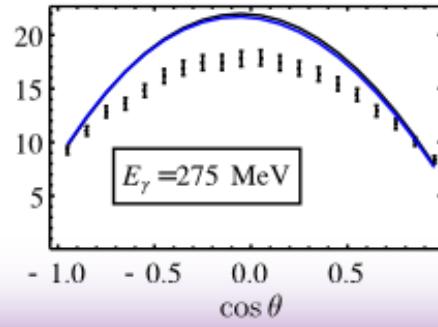
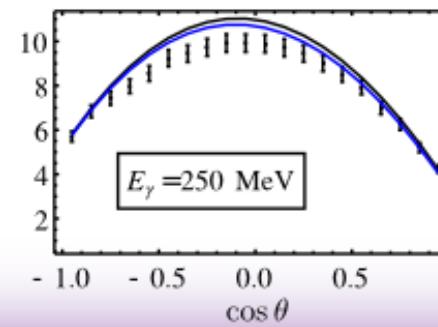
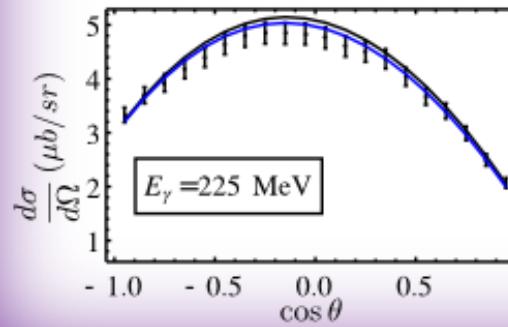
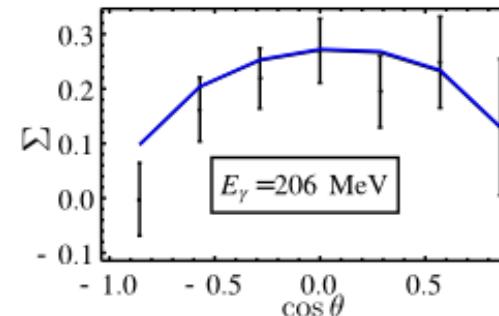
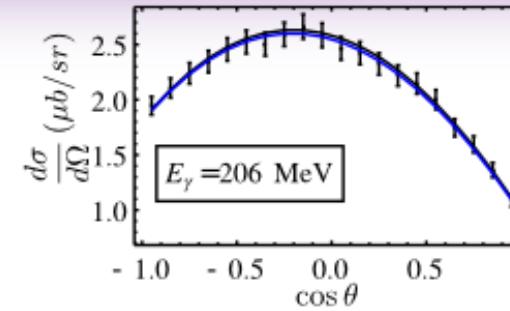
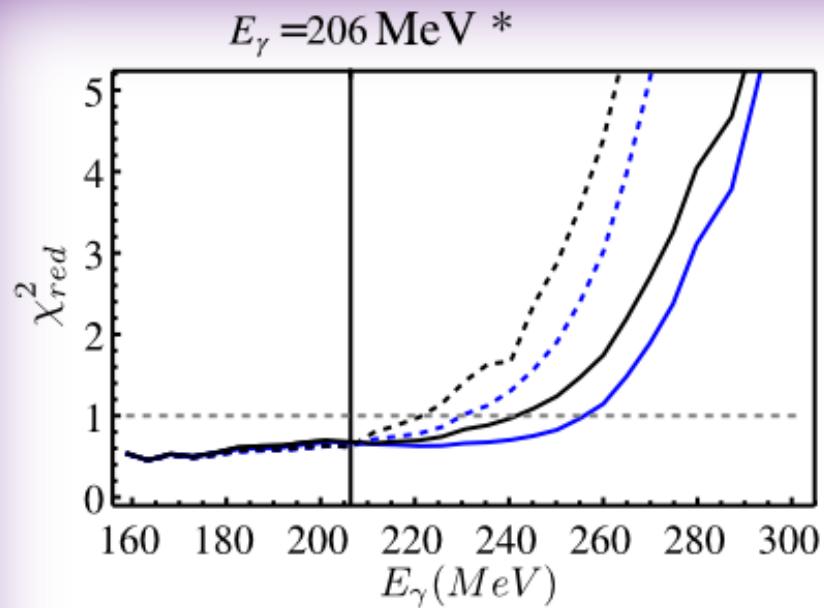


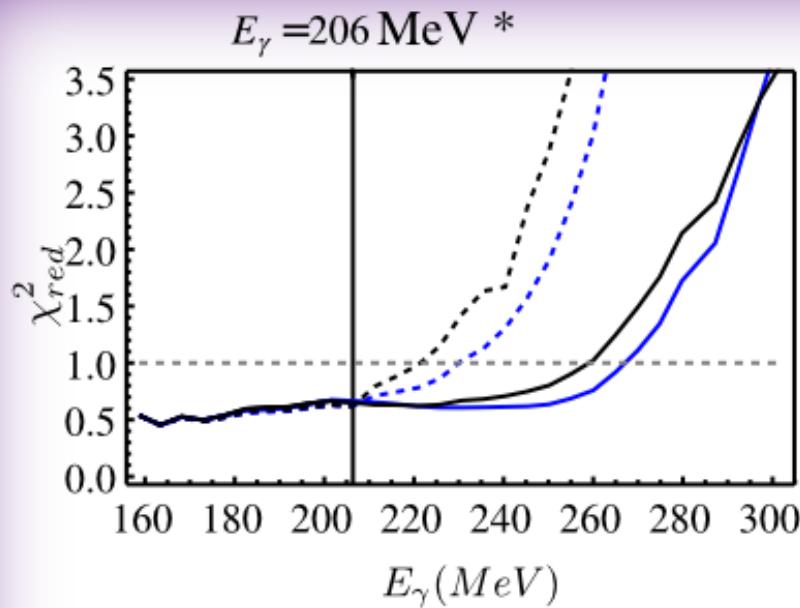
4th order H.B.

 Δ : — $\Delta + \text{V.C.}$: —*Fix LECs at
206 MeV.

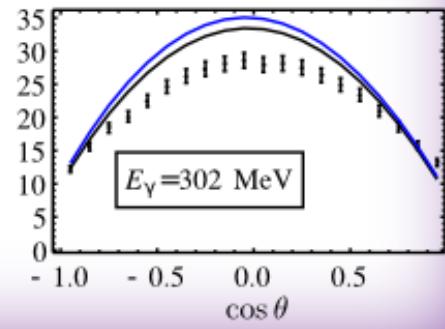
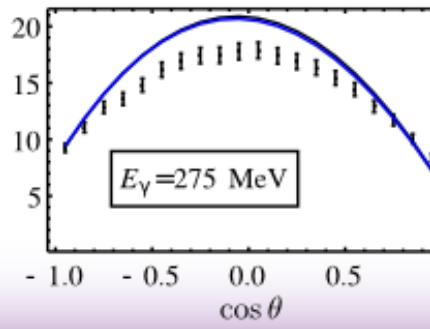
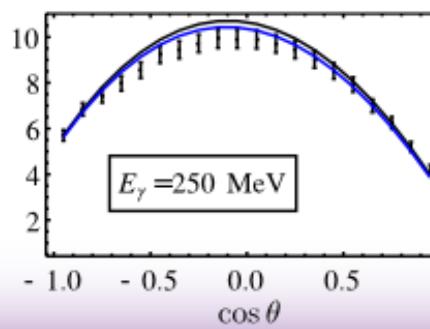
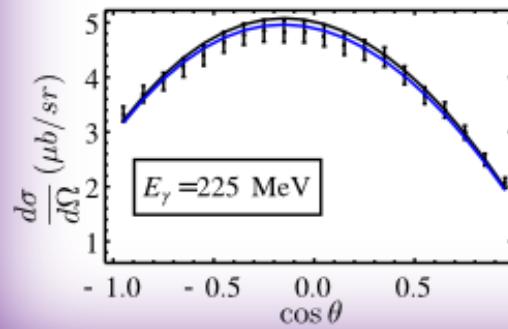
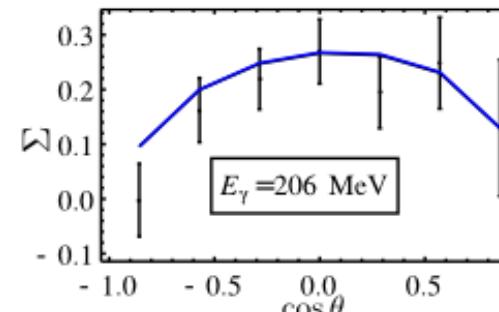
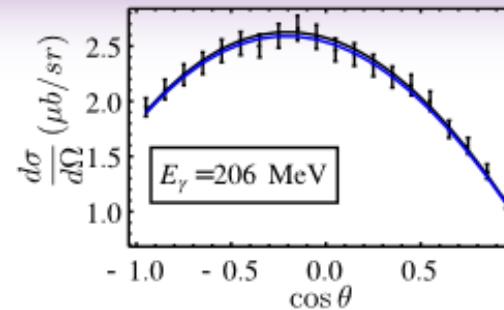
We are overestimating the data. Can we do better?

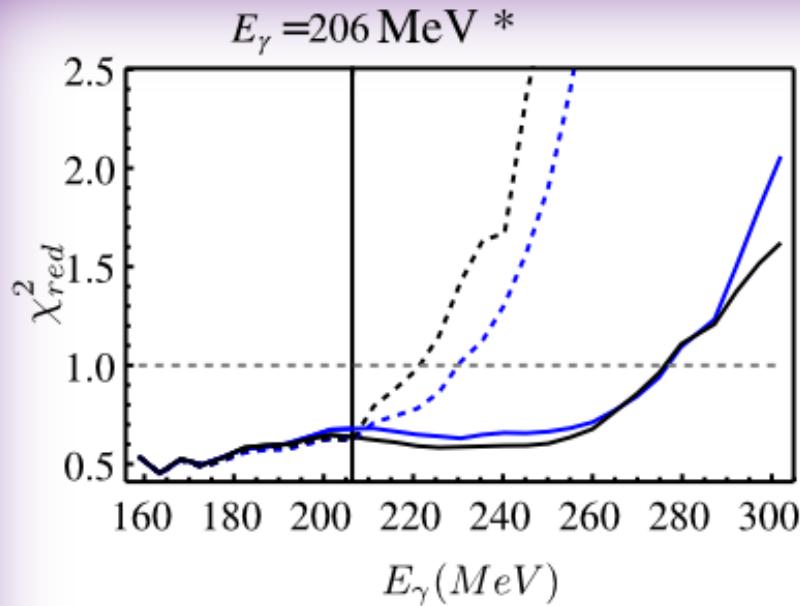
Varying g_M 

Varying g_M 

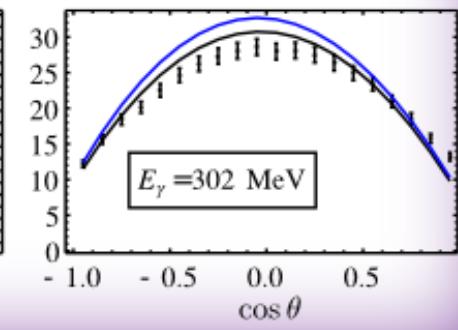
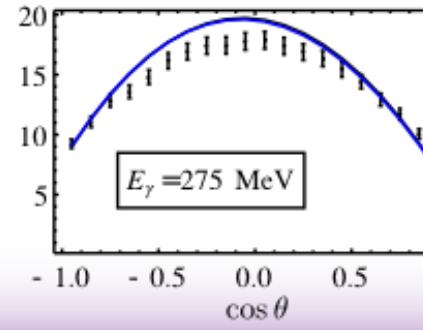
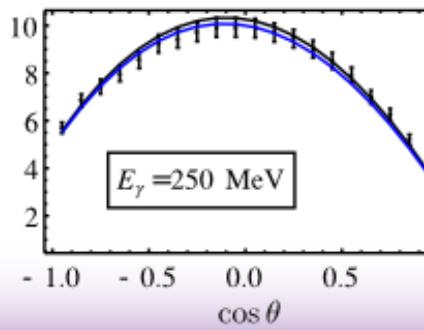
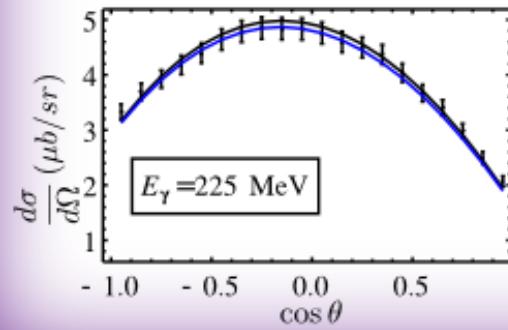
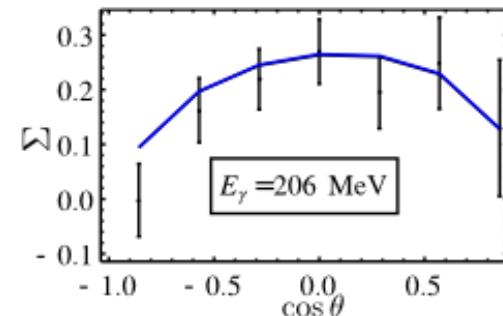
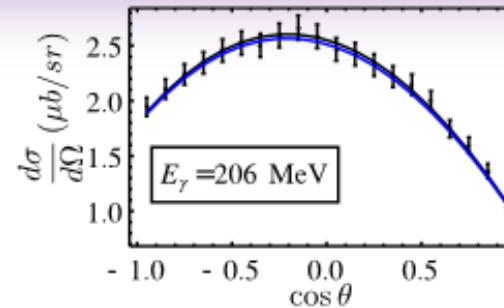
Varying g_M 

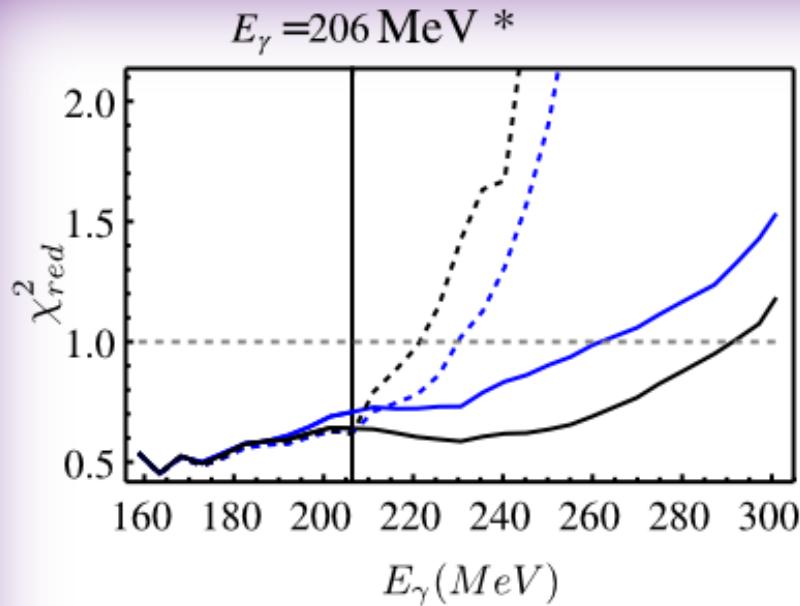
4th order H.B.

 Δ : — $\Delta + \text{V.C.}$: —*Fix LECs at
206 MeV. $g_M = 2.97$ — $g_M = 2.4$ —

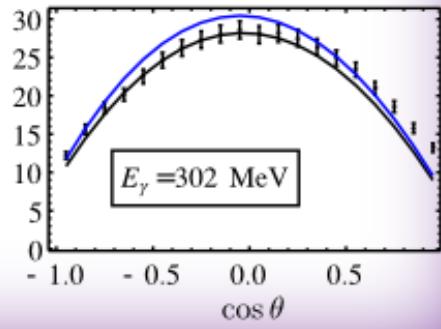
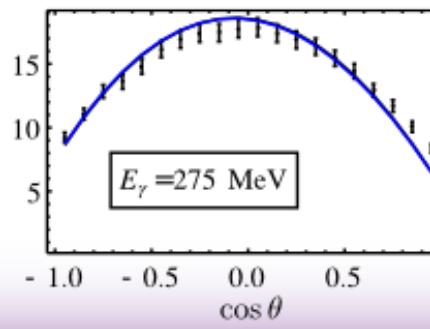
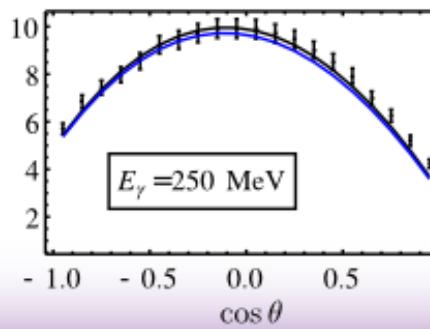
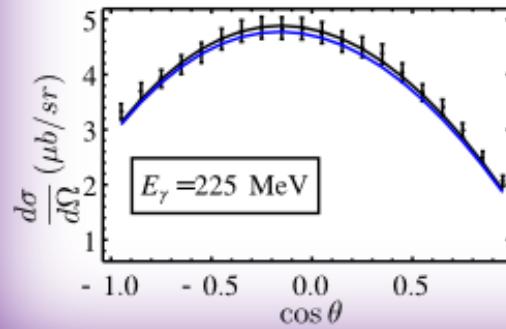
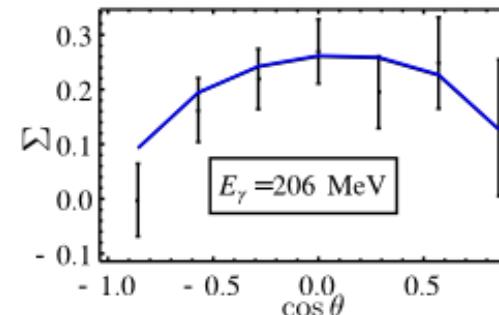
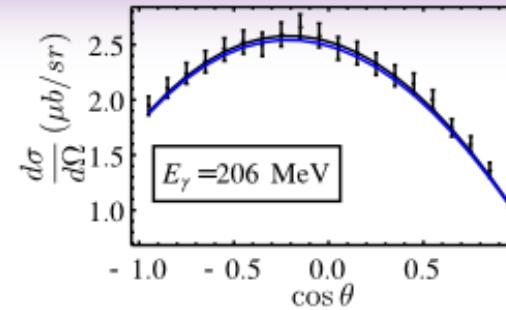
Varying g_M 

4th order H.B.

 Δ : — $\Delta + \text{V.C.}$: —*Fix LECs at
206 MeV. $g_M = 2.97$ — $g_M = 2.2$ —

Varying g_M 

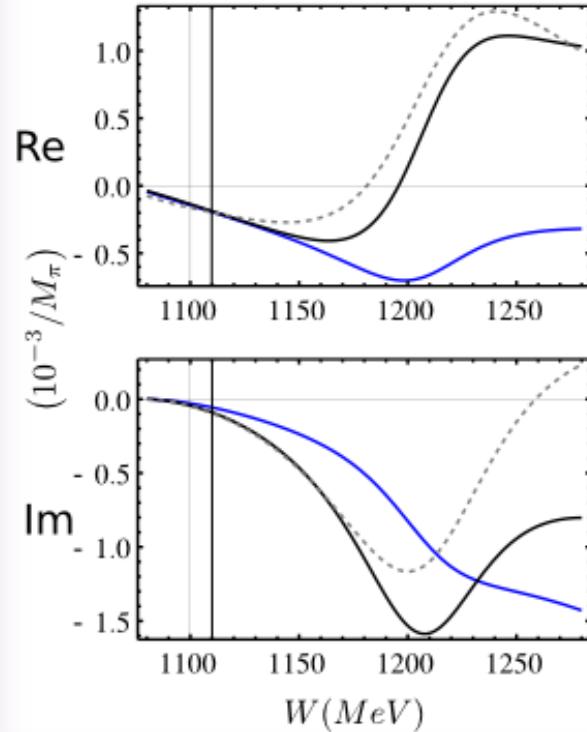
4th order H.B.

 Δ : — $\Delta + V.C.$: -·-*Fix LECs at
206 MeV. $g_M = 2.97$ -·- $g_M = 2.0$ —Are we free to vary g_M so much?

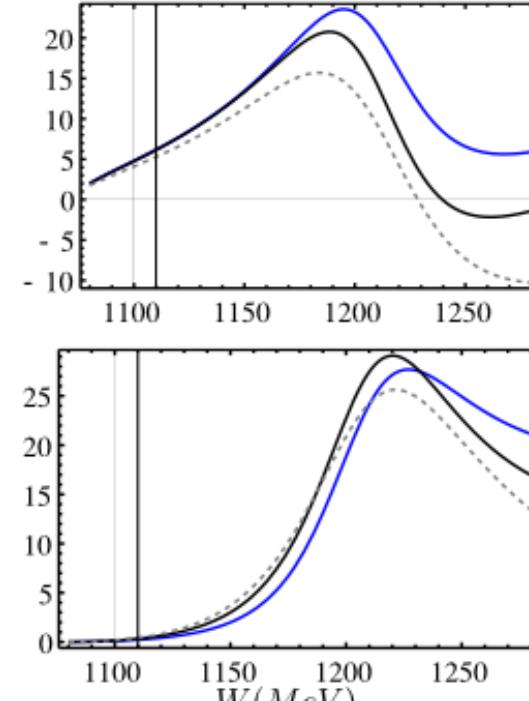
Sanity check

 $g_M = 2.97$

4th order H.B.

 E_{1+} $W = 1125 \text{ MeV}$  Δ : $\Delta + \text{v.c.}$:

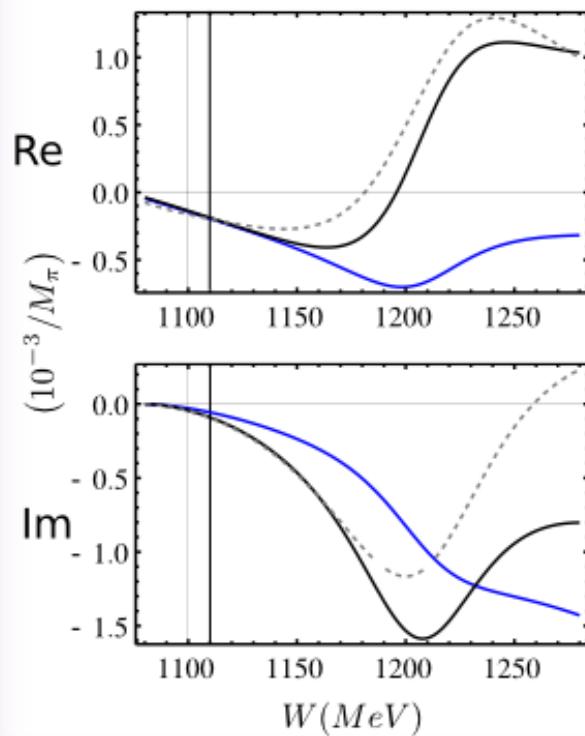
MAID:

 M_{1+} M_{1-} $W = 1125 \text{ MeV}$ $W = 1125 \text{ MeV}$ ***Fix LECs at 1125 MeV.**

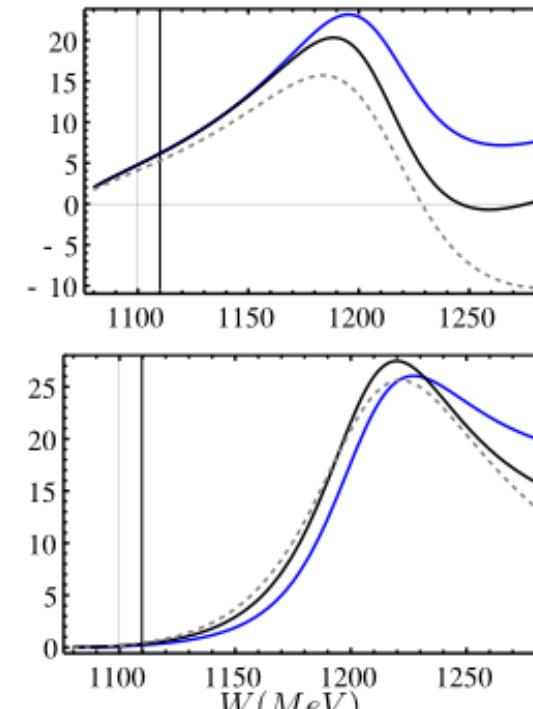
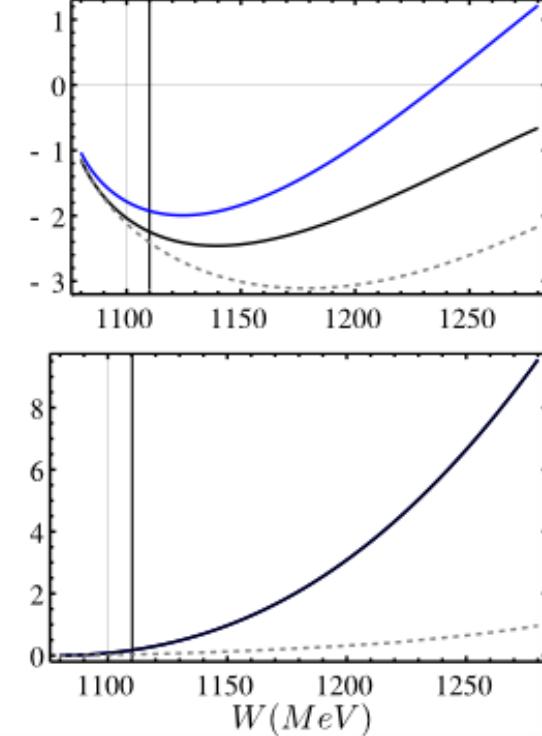
Sanity check

 $g_M = 2.8$

4th order H.B.

 E_{1+} $W = 1125 \text{ MeV}$  Δ : $\Delta + \text{v.c.}$:

MAID:

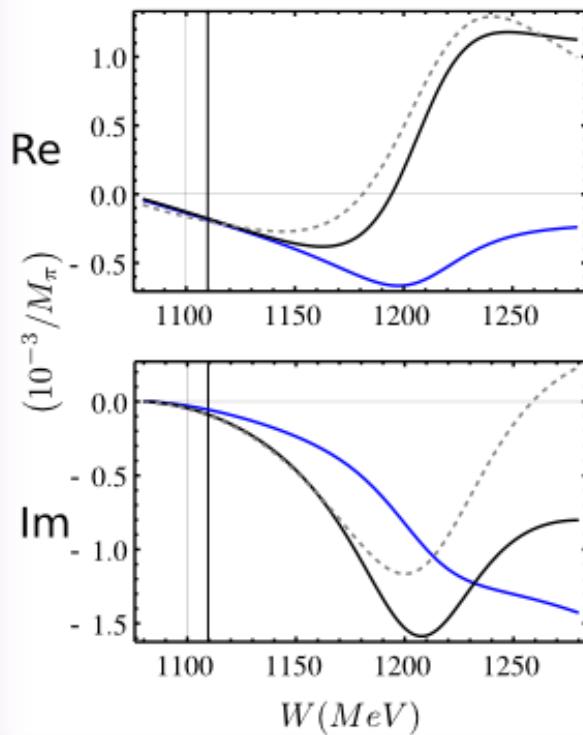
 M_{1+} $W = 1125 \text{ MeV}$  M_{1-} $W = 1125 \text{ MeV}$ 

*Fix LECs at 1125 MeV.

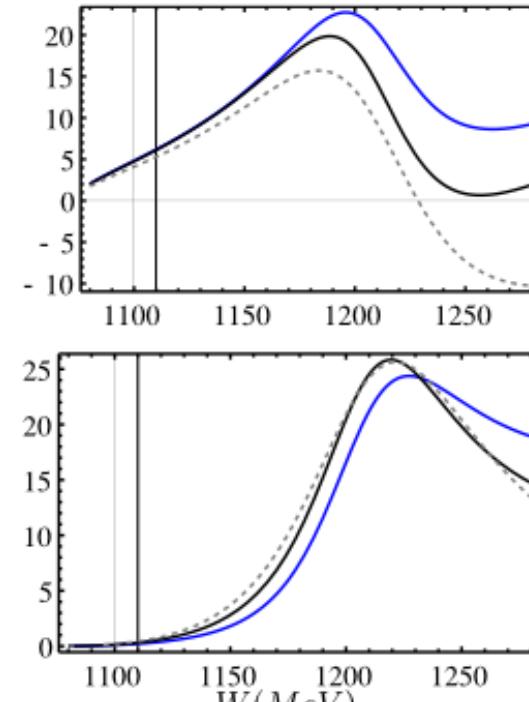
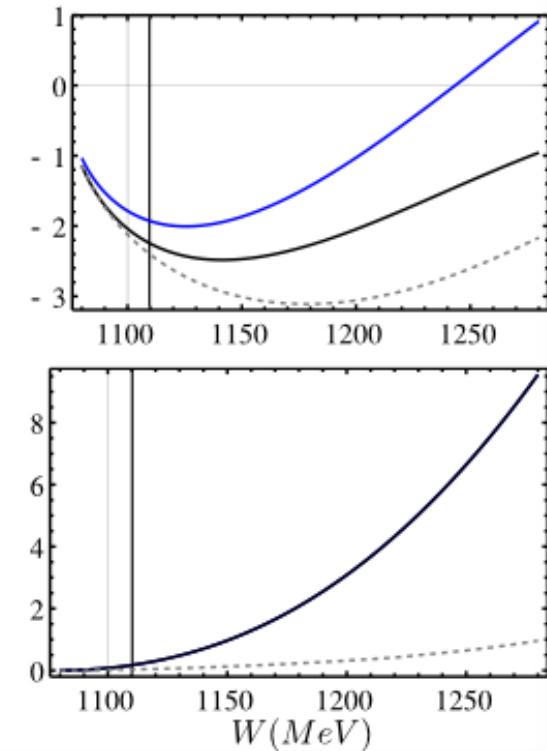
Sanity check

 $g_M = 2.6$

4th order H.B.

 E_{1+} $W = 1125 \text{ MeV}$  Δ : $\Delta + \text{v.c.}$:

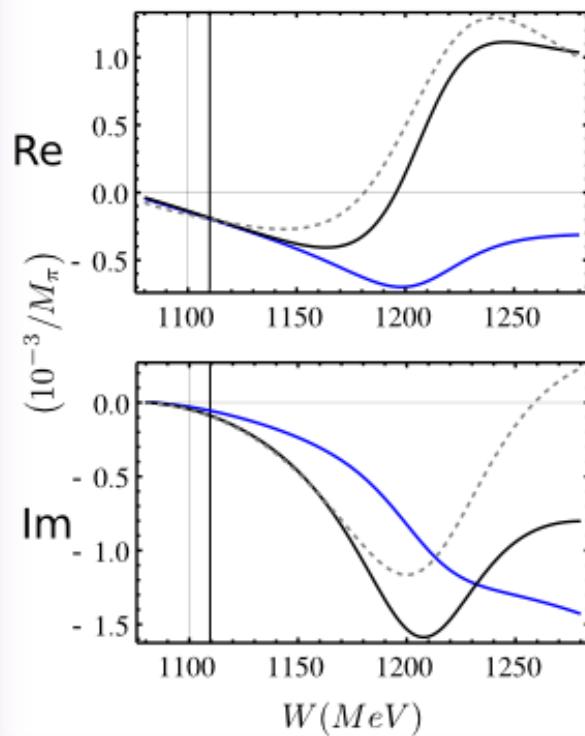
MAID:

 M_{1+} $W = 1125 \text{ MeV}$  M_{1-} $W = 1125 \text{ MeV}$ ***Fix LECs at 1125 MeV.**

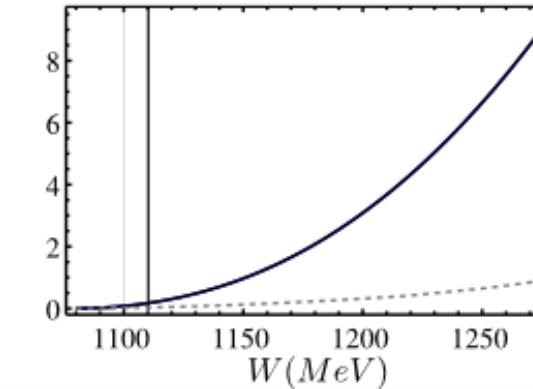
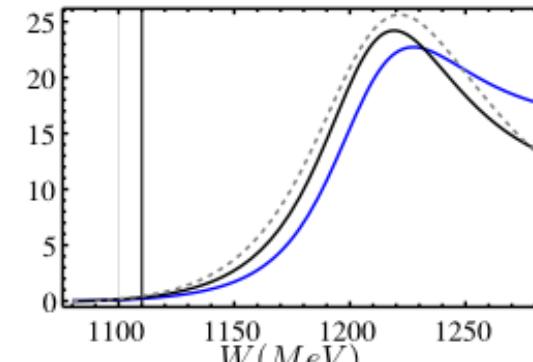
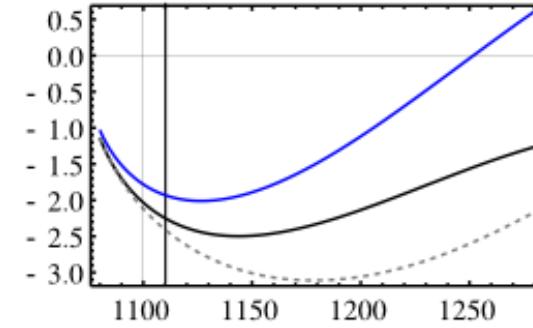
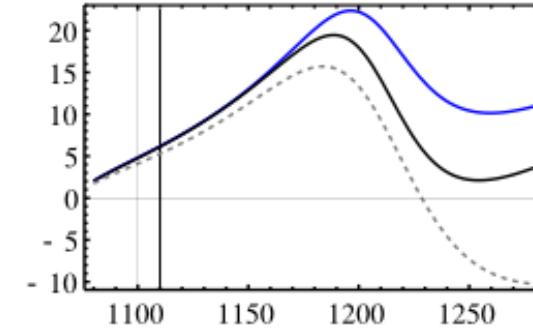
Sanity check

 $g_M = 2.4$

4th order H.B.

 E_{1+} $W = 1125 \text{ MeV}$  Δ : $\Delta + \text{v.c.}$:

MAID:

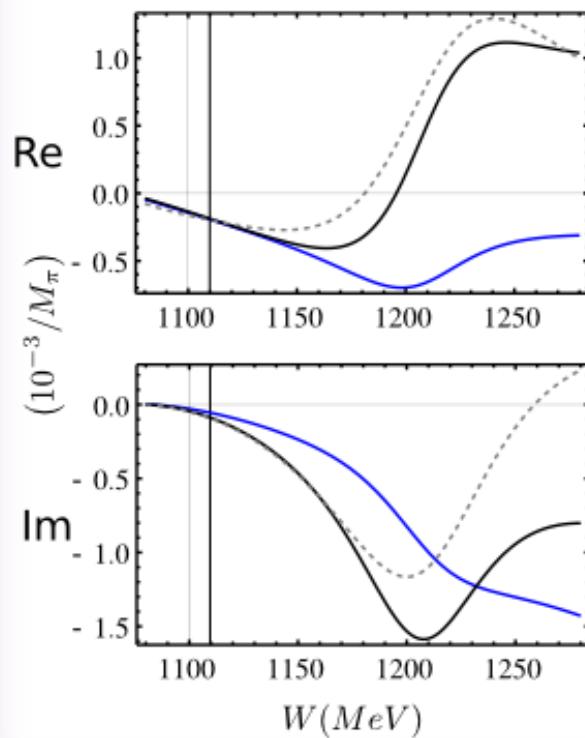
 M_{1+} $W = 1125 \text{ MeV}$ M_{1-} $W = 1125 \text{ MeV}$ 

*Fix LECs at 1125 MeV.

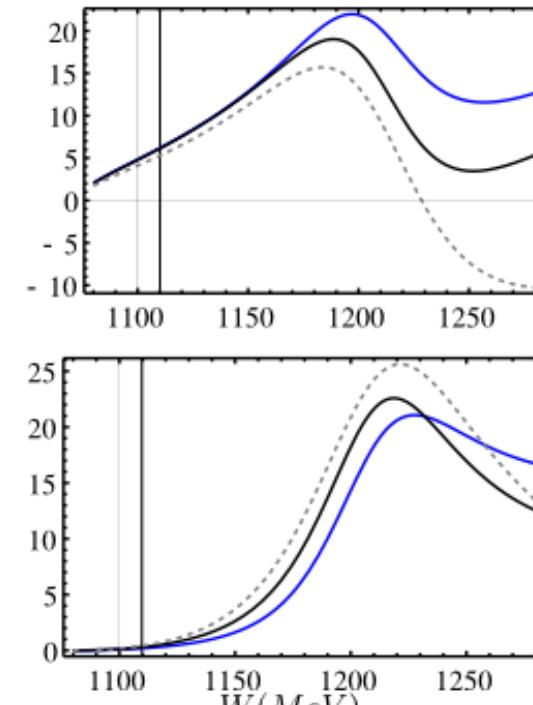
Sanity check

 $g_M = 2.2$

4th order H.B.

 E_{1+} $W = 1125 \text{ MeV}$  Δ : $\Delta + \text{v.c.}$:

MAID:

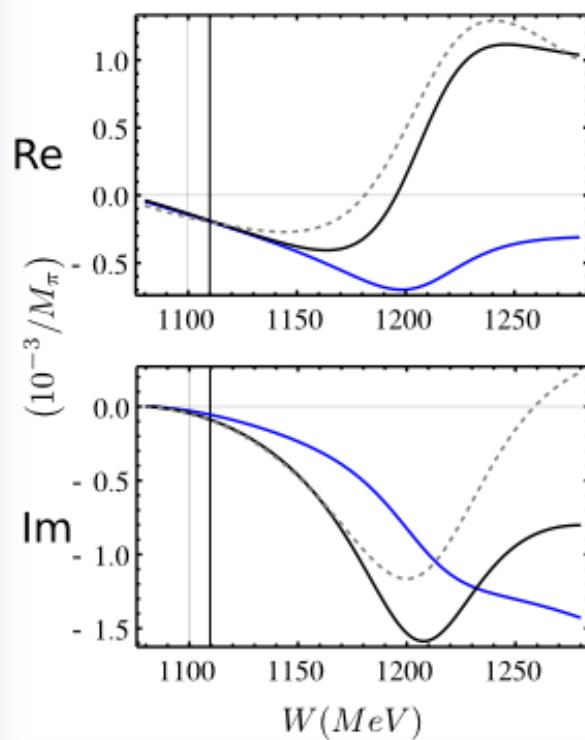
 M_{1+} M_{1-} $W = 1125 \text{ MeV}$ M_{1-} $W = 1125 \text{ MeV}$ 

*Fix LECs at 1125 MeV.

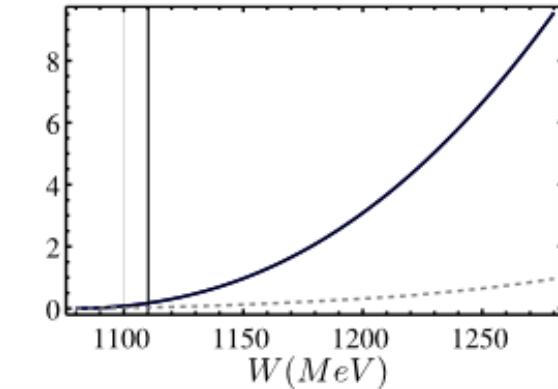
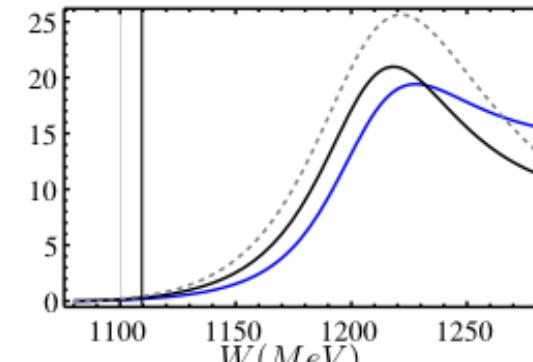
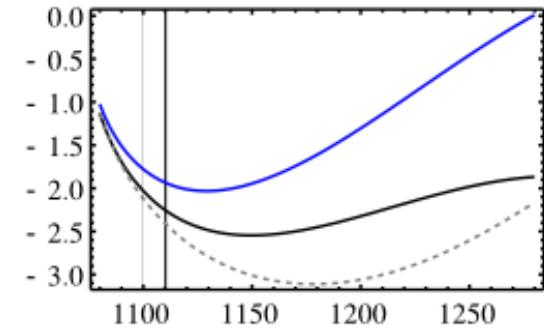
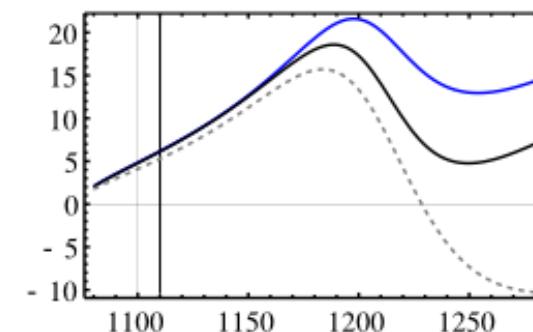
Sanity check

 $g_M = 2.0$

4th order H.B.

 E_{1+} $W = 1125 \text{ MeV}$  Δ : $\Delta + \text{v.c.}$:

MAID:

 M_{1+} M_{1-} $W = 1125 \text{ MeV}$ 

*Fix LECs at 1125 MeV.

Summary

It is possible to describe neutral pion photoproduction from threshold to energies approaching the $\Delta(1232)$ resonance.

D-waves (and higher) do not appear to have a significant impact once the Delta is included.
More data on more observables could change this.

Vertex corrections to $\gamma N\Delta$ coupling constants show good agreement with data at high energies..

Extend 4th order heavy baryon calculations to all states of angular momentum.

Test theories against data at even higher energies.

Thank you to David Hornidge for providing us with the data and the STFC for funding this work.