Precise QCD predictions for jet production at the LHC

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* based on:

"Second order QCD corrections to gluonic jet production at hadron colliders"

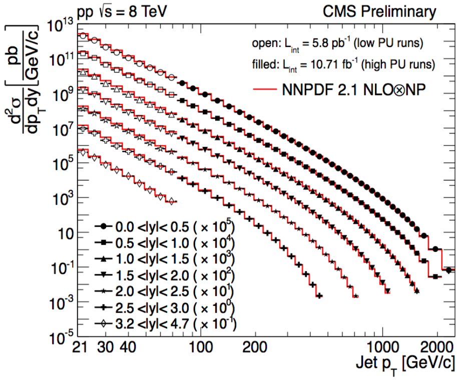
J. Currie, A. Gehrmann-De Ridder, T. Gehrmann, N. Glover, JP, S. Wells, arXiv:1407.5558

arXiv:1310.3993 JHEP 1401 (2014) 110, arXiv:1301.7310 Phys.Rev.Lett. 110 (2013) 16

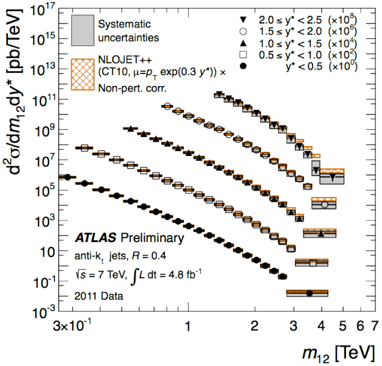
Inclusive jet and dijet cross sections

- look at the production of jets of hadrons with large transverse energy in
  - inclusive jet events $pp \to j + X$
  - exclusive dijet events $pp \to 2j$

- cross sections measured as a function of the jet p_T, rapidity y and dijet invariant mass m_{jj} in double differential form

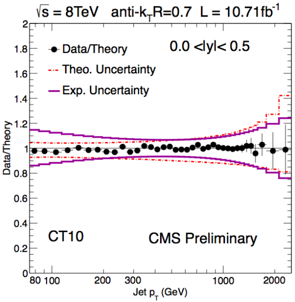


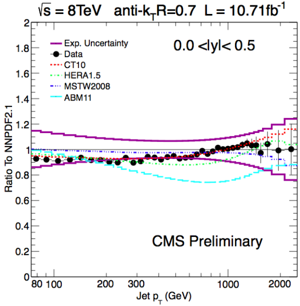
(CMS-PAS-SMP-12-012)



(ATLAS-CONF-2012-021)

Inclusive jet cross section

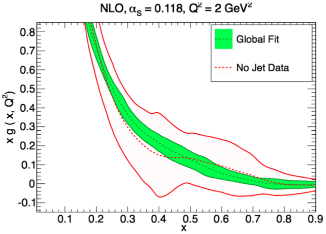




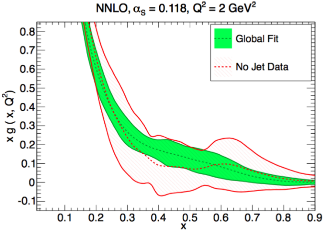
Motivation for NNLO

- experimental uncertainties at high-p_T smaller than theoretical $\rightarrow$ need pQCD predictions to NNLO accuracy

Inclusive jet cross section



NNPDF collaboration

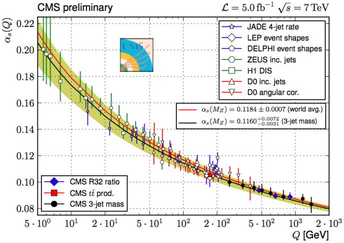


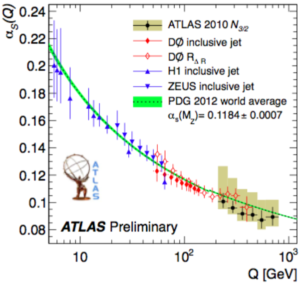
NNPDF collaboration

Motivation for NNLO

- experimental uncertainties at high-p_T smaller than theoretical $\rightarrow$ need pQCD predictions to NNLO accuracy
- collider jet data can be used to constrain parton distribution functions
- size of NNLO correction important for precise determination of PDF's
- inclusion of jet data in NNLO parton distribution fits requires NNLO corrections to jet cross sections

Inclusive jet cross section





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- α_s determination from hadronic jet observables limited by theoretical uncertainty due to scale choice

inclusive jet and dijet cross sections

State of the art:

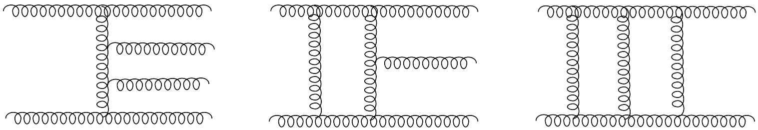
- dijet production is completely known in NLO QCD [Ellis, Kunszt, Soper ’92], [Giele, Glover, Kosower ’94], [Nagy ’02]
- NLO+Parton shower [Alioli, Hamilton, Nason, Oleari, Re ’11]
- NLO EW corrections [Dittmaier, Huss, Speckner ’12]
- approximate NNLO threshold corrections [Kidonakis, Owens ’00], [Florian, Hinderer, Mukherjee, Ringer, Vogelsang ’13]

Goal:

- obtain the jet cross sections at NNLO exact accuracy in double differential form

$$\frac{\mathrm{d}^2\sigma}{\mathrm{d}p_T\mathrm{d}|y|} \qquad \frac{\mathrm{d}^2\sigma}{\mathrm{d}m_{jj}\mathrm{d}y^*}$$

$pp \to 2j$ at NNLO: gluonic contributions



$A_6^{(0)}(gg \to gggg)$ $A_5^{(1)}(gg \to ggg)$ $A_4^{(2)}(gg \to gg)$

[Berends, Giele '87], [Mangano, Parke, Xu '87], [Britto, Cachazo, Feng '06]
[Bern, Dixon, Kosower '93]
[Anastasiou, Glover, Oleari, Tejeda-Yeomans '01],[Bern, De Freitas, Dixon '02]

$$\mathrm{d}\hat{\sigma}_{NNLO} = \int_{\mathrm{d}\Phi_4} \mathrm{d}\hat{\sigma}_{NNLO}^{RR} + \int_{\mathrm{d}\Phi_3} \mathrm{d}\hat{\sigma}_{NNLO}^{RV} + \int_{\mathrm{d}\Phi_2} \mathrm{d}\hat{\sigma}_{NNLO}^{VV}$$

- explicit infrared poles from loop integrations
- implicit poles in phase space regions for single and double unresolved gluon emission
- procedure to extract the infrared singularities and assemble all the parts in a parton-level generator
- differential cross sections→ kinematics of the final state intact to apply arbitrary phase space observable cuts

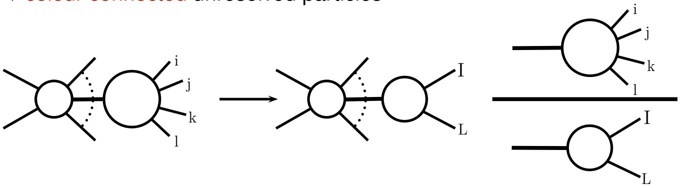
NNLO antenna subtraction

$$
\begin{aligned}
\mathrm{d}\hat{\sigma}_{NNLO} &= \int_{\mathrm{d}\Phi_4} \left(\mathrm{d}\hat{\sigma}^{RR}_{NNLO} - \mathrm{d}\hat{\sigma}^{S}_{NNLO}\right) \\
&+ \int_{\mathrm{d}\Phi_3} \left(\mathrm{d}\hat{\sigma}^{RV}_{NNLO} - \mathrm{d}\hat{\sigma}^{T}_{NNLO}\right) \\
&+ \int_{\mathrm{d}\Phi_2} \left(\mathrm{d}\hat{\sigma}^{VV}_{NNLO} - \mathrm{d}\hat{\sigma}^{U}_{NNLO}\right)
\end{aligned}
$$

- $\mathrm{d}\hat{\sigma}^{S}_{NNLO}$: real radiation subtraction term for $\mathrm{d}\hat{\sigma}^{RR}_{NNLO}$
- $\mathrm{d}\hat{\sigma}^{T}_{NNLO}$: one-loop virtual subtraction term for $\mathrm{d}\hat{\sigma}^{RV}_{NNLO}$
- $\mathrm{d}\hat{\sigma}^{U}_{NNLO}$: two-loop virtual subtraction term for $\mathrm{d}\hat{\sigma}^{VV}_{NNLO}$
- subtraction terms constructed using the antenna subtraction method at NNLO for hadron colliders $\rightarrow$ presence of initial state partons to take into account
- contribution in each of the round brackets is finite, well behaved in the infrared singular regions and can be evaluated numerically

NNLO antenna subtraction

- universal factorisation of both colour ordered matrix elements and the $(m+2)$- particle phase space $\rightarrow$ colour connected unresolved particles



$$|M_{m+4}(\ldots,i,j,k,l,\ldots)|^2 \; J(\{p_{m+4}\}) \;\longrightarrow |M_{m+2}(\ldots,I,L,\ldots)|^2 \; J(\{p_{m+2}\}) \;\cdot X_4^0(i,j,k,l)$$

- momentum map $\{p_i,p_j,p_k,p_l\} \rightarrow \{p_I,p_L\}$ enforces momentum conservation away from the unresolved limits
- phase-space factorisation

$$\begin{aligned} \mathrm{d}\Phi_{m+2}(p_a,\ldots,p_i,p_j,p_k,p_l,\ldots,p_{m+2}) &= \mathrm{d}\Phi_m(p_a,\ldots,p_I,p_L,\ldots,p_{m+2}) \\ &\quad \mathrm{d}\Phi_{X_{ijkl}}(p_i,p_j,p_k,p_l) \end{aligned}$$

- integrated antennae is the inclusive integral

$$\mathcal{X}^0_{ijkl}(s_{ijkl}) = \frac{1}{C(\epsilon)^2}\int \mathrm{d}\Phi_{X_{ijkl}}(p_i,p_j,p_k,p_l) X_4^0(i,j,k,l)$$

NNLO antenna subtraction

Implementation checks $pp \to 2j$ at NNLO:

- subtraction terms correctly approximate the matrix elements in all unresolved configurations of partons j, k

$$\boxed{\mathrm{d}\hat{\sigma}^{RR,RV}_{NNLO} \xrightarrow{\forall\{j,k\},\{j\}\to 0} \mathrm{d}\hat{\sigma}^{S,T}_{NNLO}}$$

- local (pointwise) analytic cancellation of all infrared explicit ϵ-poles when integrated subtraction terms are combined with one, two-loop matrix elements

$$\boxed{\mathcal{P}oles\left(\mathrm{d}\hat{\sigma}^{RV}_{NNLO} - \mathrm{d}\hat{\sigma}^{T}_{NNLO}\right) = 0}$$

$$\boxed{\mathcal{P}oles\left(\mathrm{d}\hat{\sigma}^{VV}_{NNLO} - \mathrm{d}\hat{\sigma}^{U}_{NNLO}\right) = 0}$$

- leading and subleading colour
- process independent NNLO subtraction scheme
- allows the computation of multiple differential distributions in a single program run

Jet production partonic channels

Fraction of jets per initial state contribution

LHC

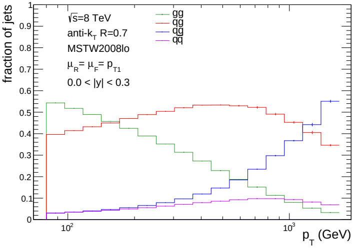
- $gg \to gg$ dominates at low p_T
- $qg \to qg$ important in all p_T regions
- $qq \to qq$ dominant at high p_T

Tevatron

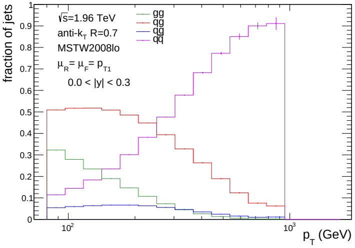
- qg and $q\bar{q}$ dominant

Present results at NNLO for

- $gg \to gg$ at leading colour
- $gg \to gg$ at subleading colour
- $q\bar{q} \to gg$ at leading colour



(LHC 8 TeV)



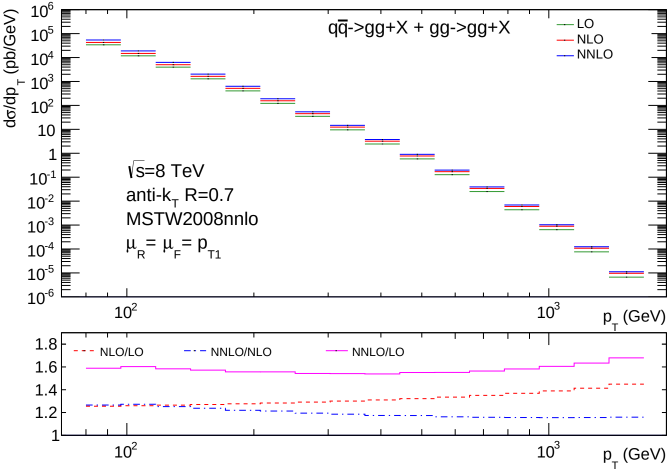
(Tevatron 1.96 TeV)

Numerical setup

(J.Currie, A. Gehrmann-De Ridder, T.Gehrmann, N. Glover, JP '13)

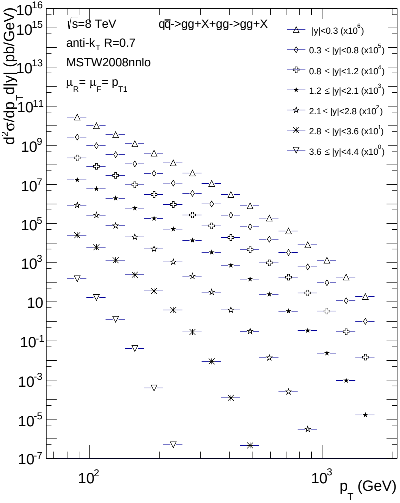
- pp collisions at $\sqrt{s} = 8$ TeV
- jets identified with the anti-k_T jet algorithm with resolution parameter $R = 0.7$
- jets accepted at rapidities $|y| < 4.4$
- leading jet with transverse momentum $p_T > 80$ GeV
- subsequent jets required to have at least $p_T > 60$ GeV
- MSTW2008nnlo PDF for all fixed-order predictions
- dynamical factorization and renormalization scales equal to the leading jet p_T $(\mu_R = \mu_F = \mu = p_{T1})$
- present results for full colour $gg \to gg$ scattering and $q\bar{q} \to gg$ leading colour combined at NNLO

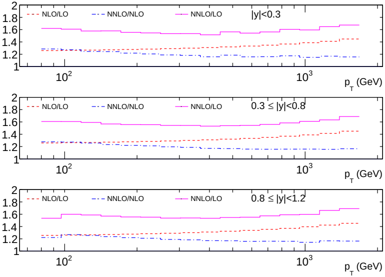
Inclusive jet p_T distribution at NNLO



- all jets in an event are binned
- NNLO correction stabilizes the NLO k-factor growth with p_T
- NNLO corrections $15 - 26\%$ with respect to NLO

Double differential inclusive jet p_T distribution at NNLO



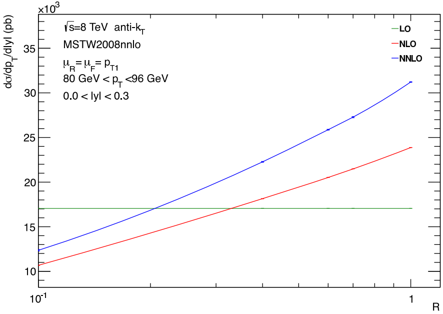


double differential k-factors

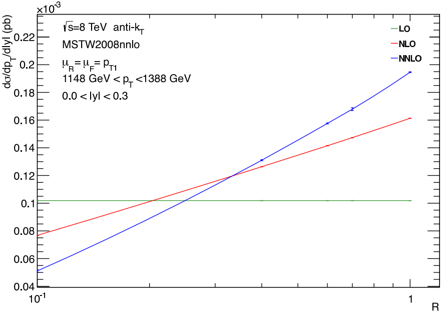
- NNLO prediction increases between 25% to 15% with respect to the NLO cross section
- similar behaviour between the rapidity slices

Inclusive jet p_T distribution

$80\text{GeV} < p_T < 96\text{GeV}$

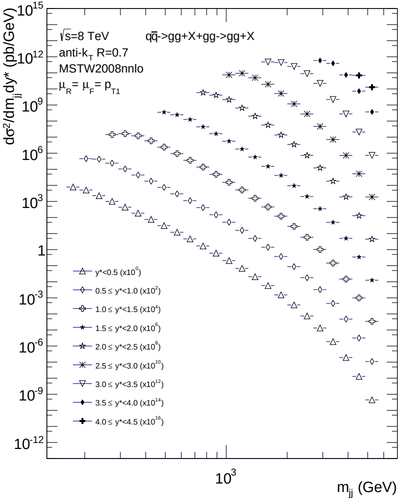


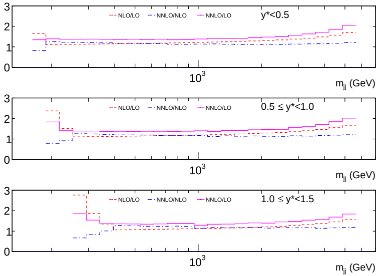
$1148\text{GeV} < p_T < 1388\text{GeV}$



- inclusive jet cross section versus R
- NNLO corrections smaller for small R but p_T dependent

Double differential exclusive dijet mass distribution at NNLO

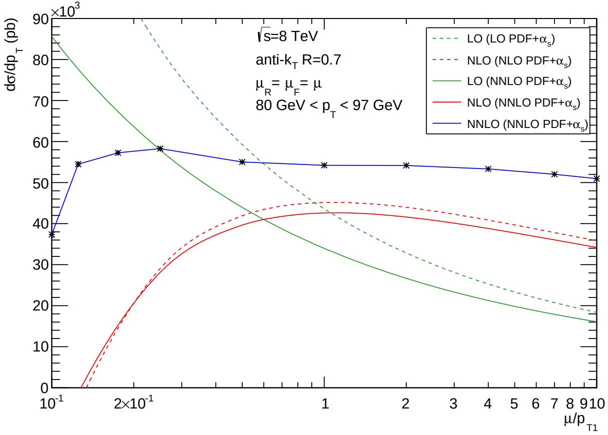




double differential k-factors

- NNLO corrections up to 20% with respect to the NLO cross section
- similar behaviour between the $y^* = 1/2|y_1 - y_2|$ slices

Inclusive jet p_T scale dependence $(gg \to gg + X)$



- scale dependence study gluons only $N_F = 0$ channel at leading colour
- dynamical scale choice: leading jet p_{T1}
- flat scale dependence at NNLO

Conclusions

- antenna subtraction method generalised for the calculation of NNLO QCD corrections for exclusive collider observables with partons in the initial-state
- explicit ϵ-poles in the matrix elements are analytically cancelled by the ϵ-poles in the subtraction terms
- non-trivial check of analytic cancellation of infrared singularities between double-real, real-virtual and double-virtual corrections
- successful inclusion of subleading colour contributions at NNLO with the antenna subtraction method
- first exact results for $gg \to gg + X$ and $q\bar{q} \to gg + X$ at NNLO

Future work:

- include remaining channels involving the quark contributions
  - qg channel - most important at the LHC
  - leading colour N_F pieces
  - qq channel - important at high p_T