

# Universal geometrical scaling of the elliptic flow

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# Outline

- Experimental Scaling of Elliptic Flow of charged particles
- Scaling of Photons
- From Geometrical Scaling in pt Distributions to GS of Elliptic Flow
- $v_3$  Scaling?
- Possible implications(initial states or final states interaction)

$$\frac{1}{N_A} \frac{dN_{ch}}{dp_T^2} = \frac{1}{Q_0^2} F(\tau), \quad \tau = \frac{p_T^2}{(Q_s^A)^2}$$

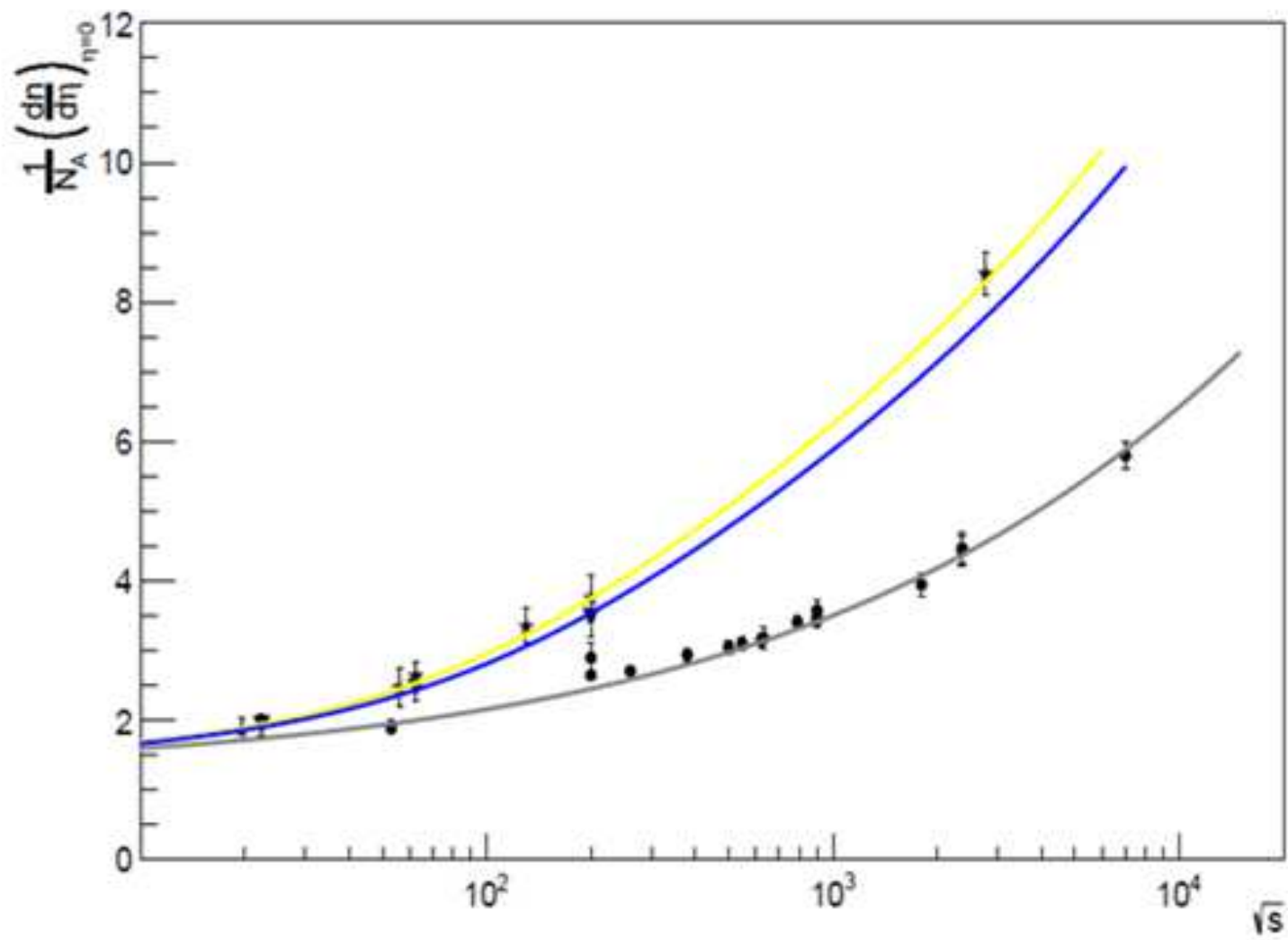
$$(Q_s^A)^2 = (Q_s^p)^2 A^{\alpha(s)/2} N_A^{1/6}$$

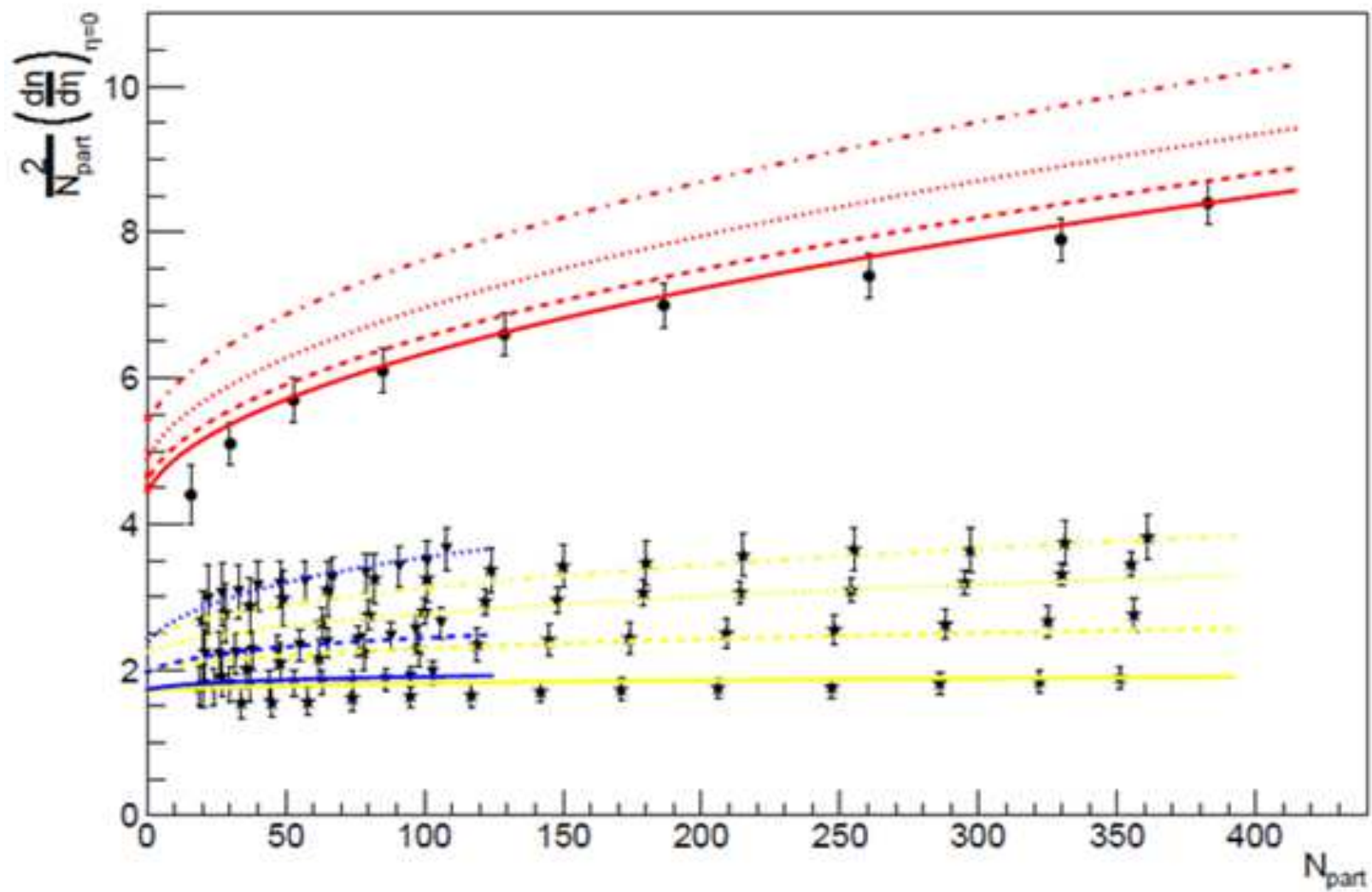
$$\alpha(s) = \frac{1}{3} \left( 1 - \frac{1}{1 + \ln(\sqrt{s/s_0} + 1)} \right)$$

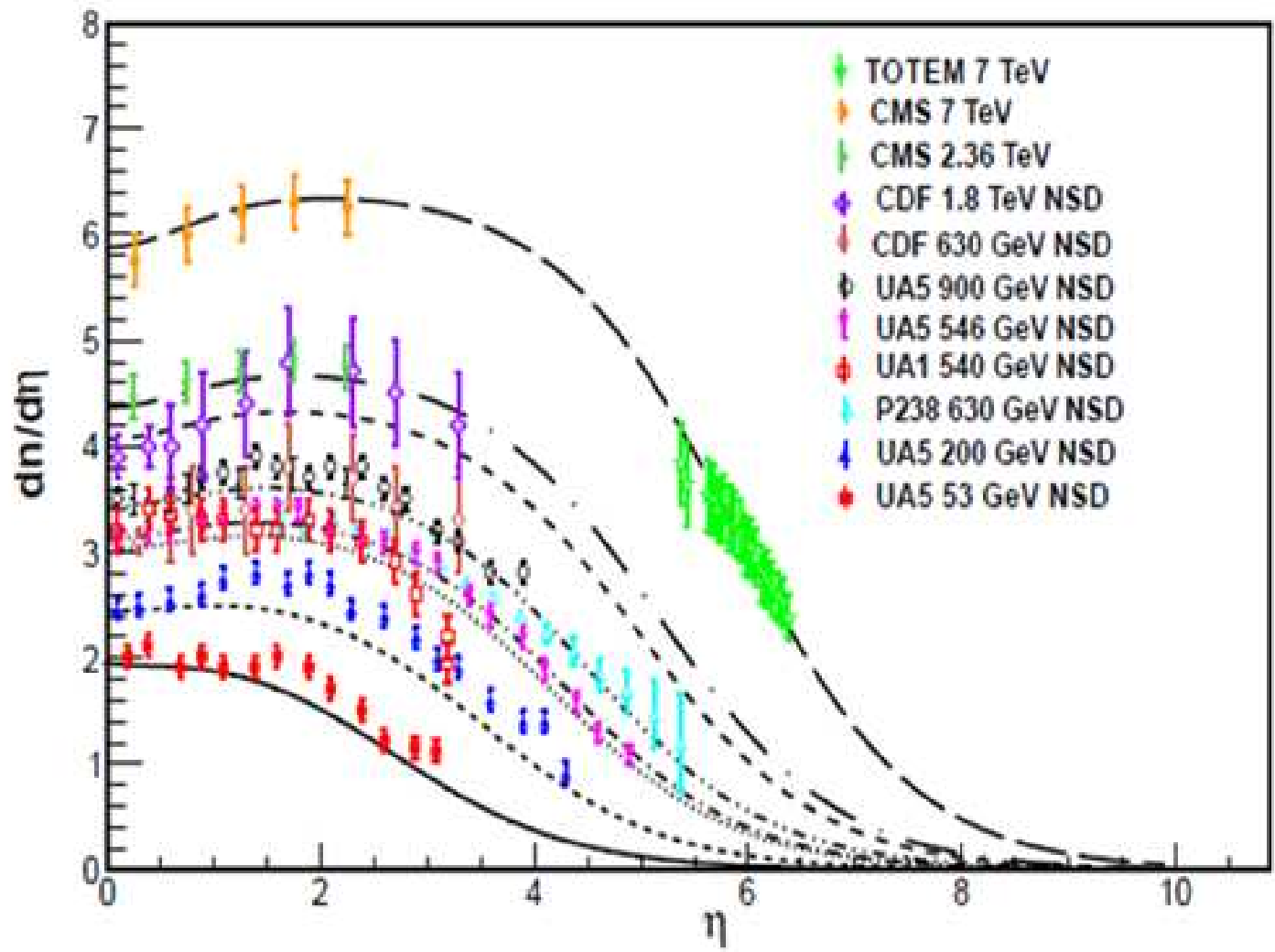
and

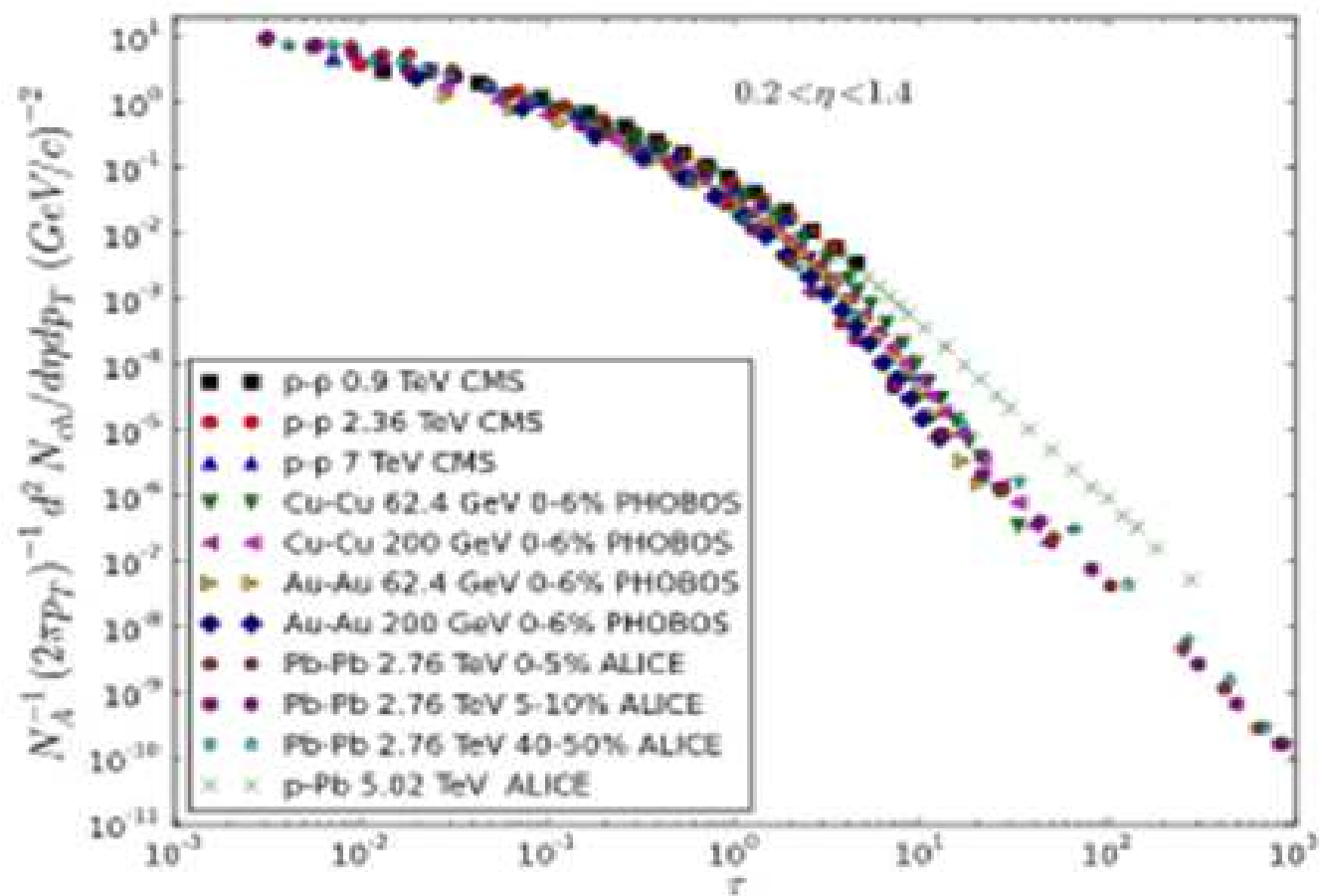
$$(Q_s^p)^2 = Q_0^2 \left( \frac{W}{p_T} \right)^\lambda,$$

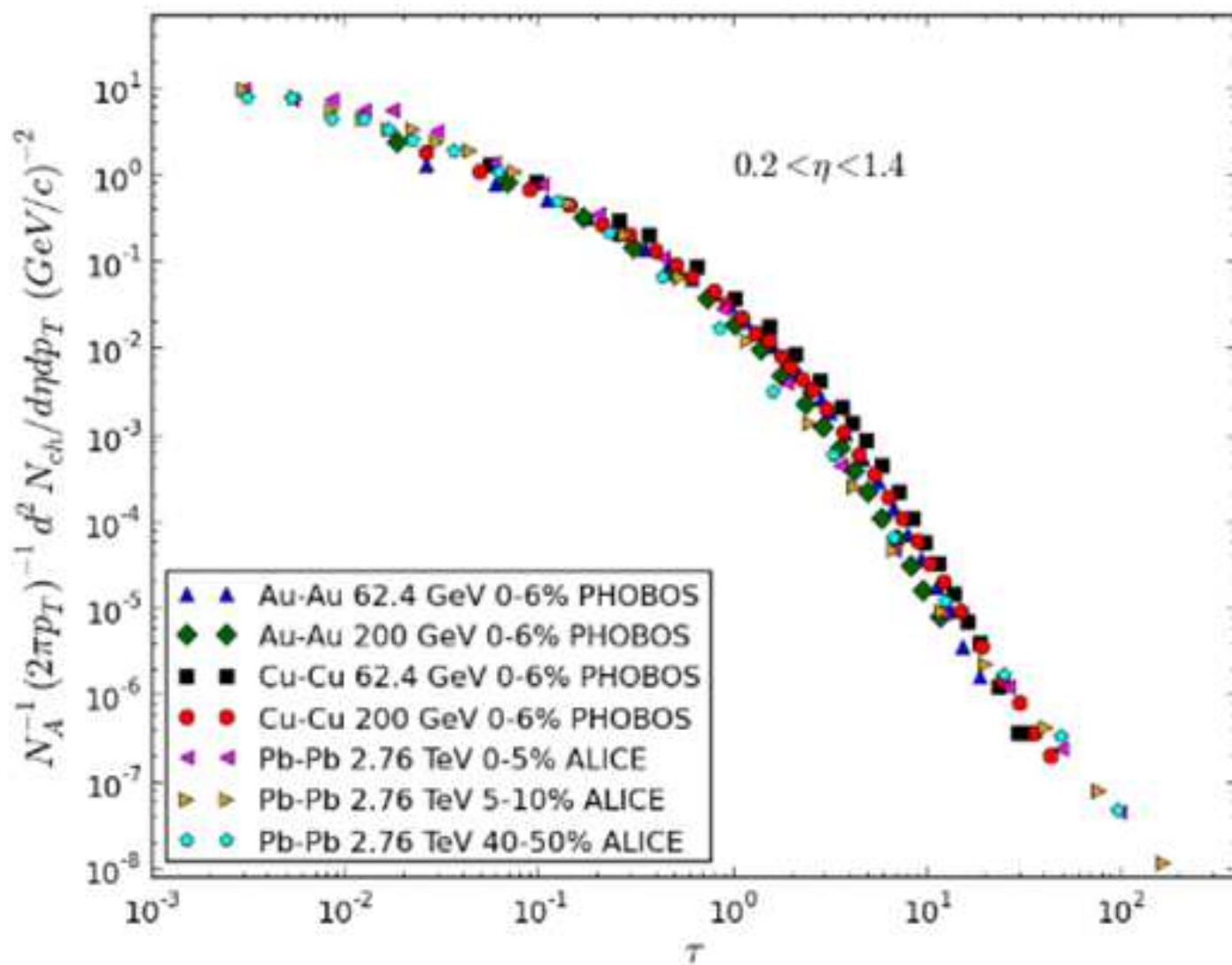
with  $Q_0 = 1 \text{ GeV}$ ,  $W = \sqrt{s} \times 10^{-3}$  and  $\lambda = 0.27$ .





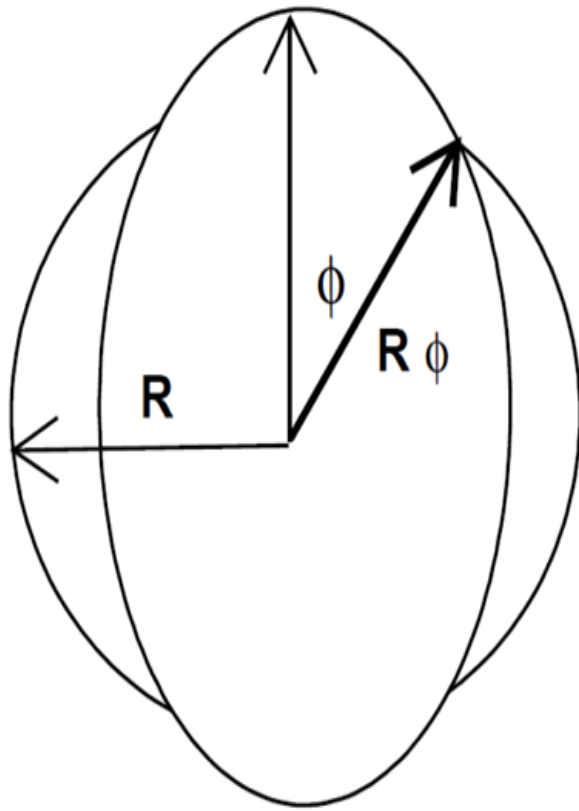








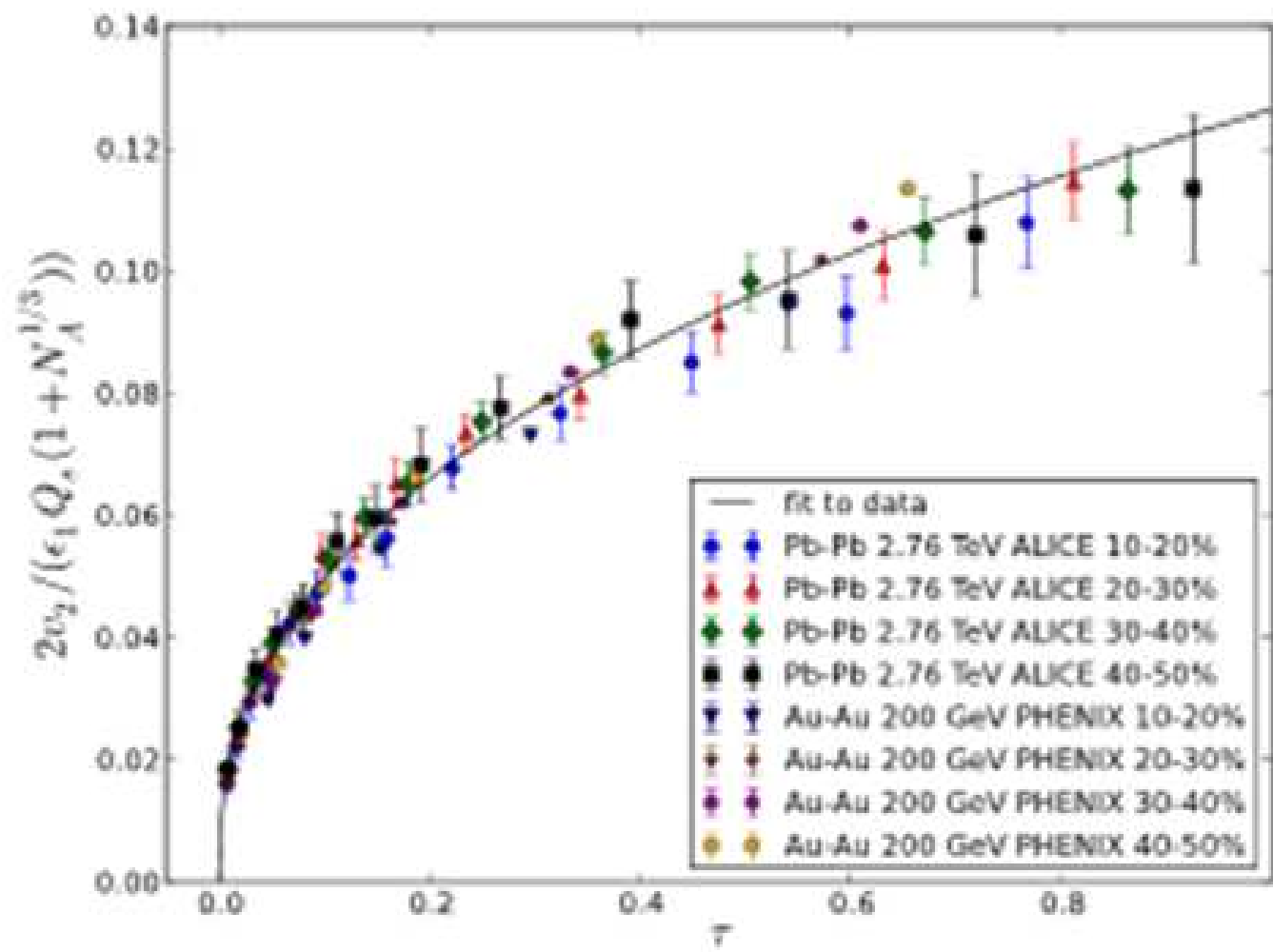
$$\frac{v_2(p_T)}{\epsilon_1 Q_s^A L} = f(\tau) \quad \text{or} \quad v_2 k_n = \epsilon_1 \tau \varphi(\tau) \quad k_n = \frac{\lambda_{mf} p}{L}$$

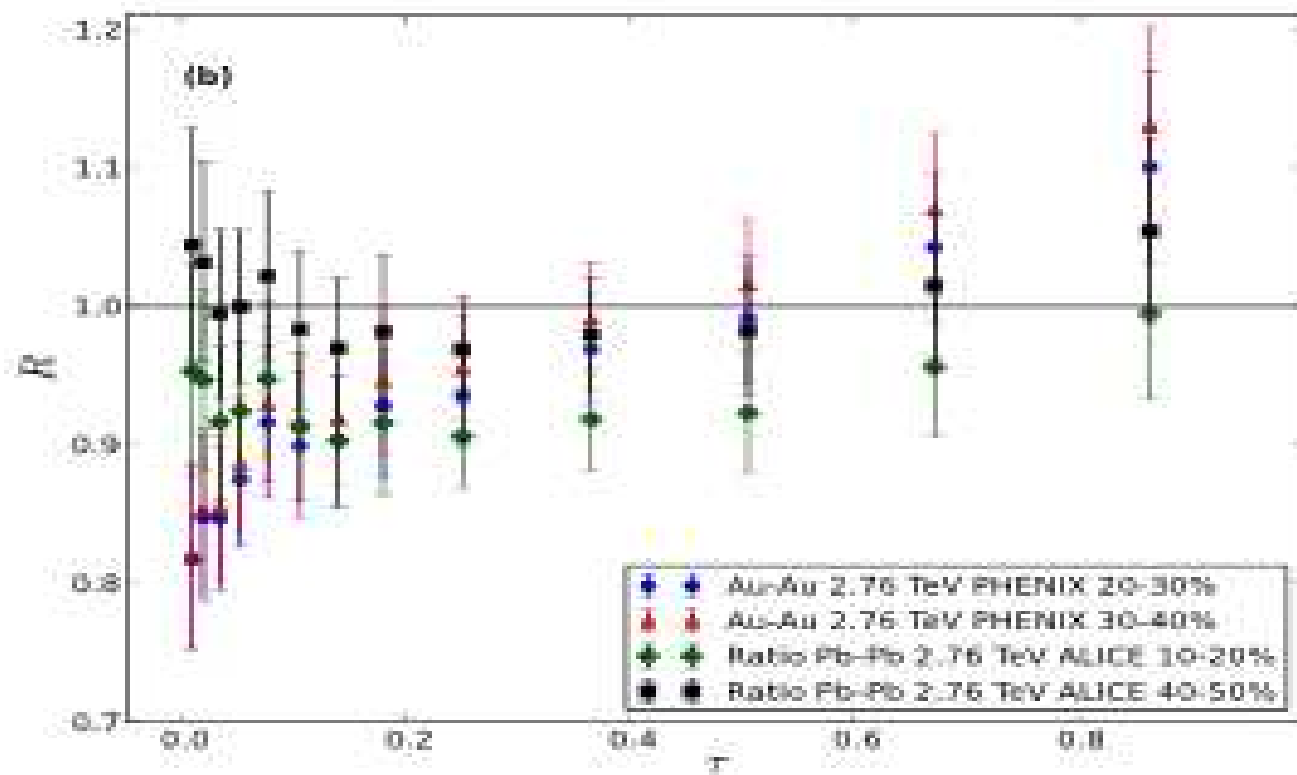


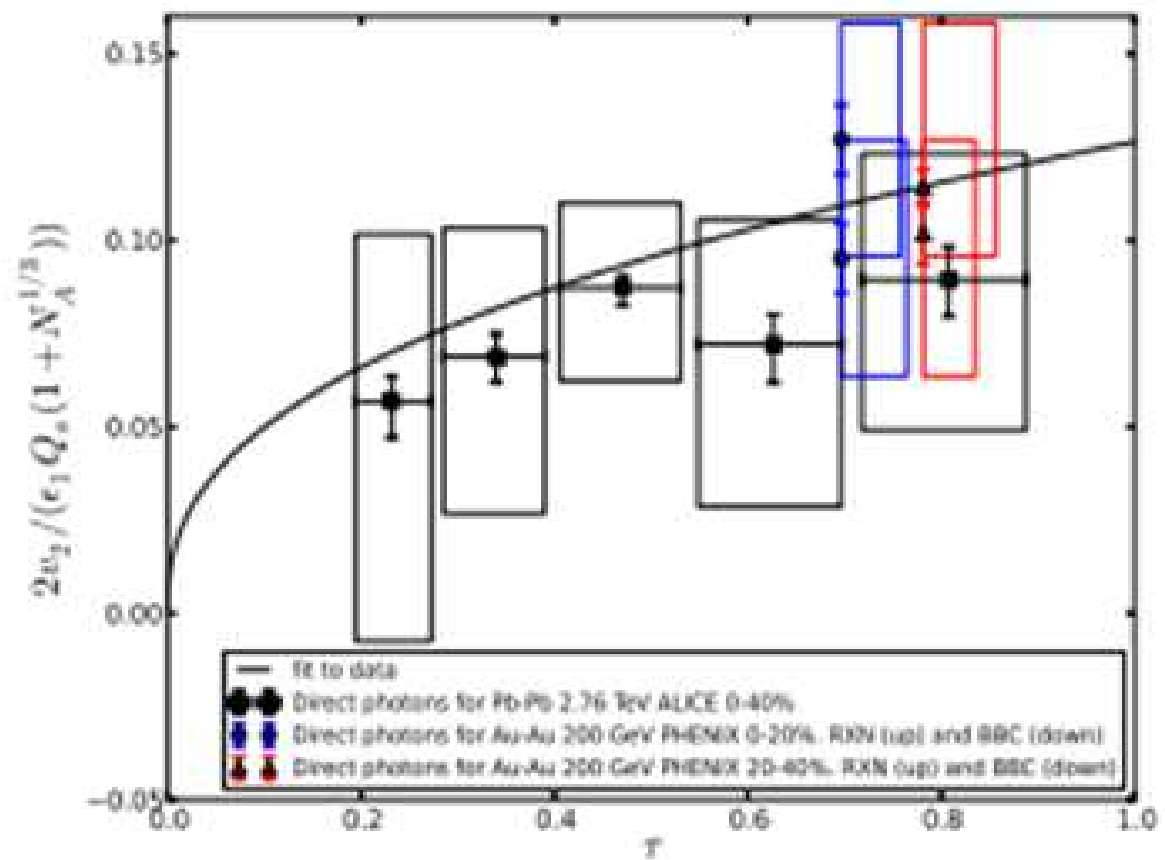
$$\epsilon_1 = \frac{2}{\pi} \int_0^{\pi/2} d\varphi \cos 2\varphi \frac{R^2 - R_\varphi^2}{R^2}, \quad R_\varphi = \frac{R_A \sin(\varphi - \alpha)}{\sin \varphi}$$

$$\alpha = \arcsin\left(\frac{b}{2R_A} \sin \varphi\right), \quad R^2 = \langle R_\varphi^2 \rangle = \frac{2}{\pi} \int_0^{\pi/2} d\varphi R_\varphi^2$$

$$L = (1 + N_A^{1/3})/2,$$







$$(Q_{s\varphi}^A)^2 \equiv \frac{L}{\lambda_{mf p}} \frac{1}{R_\varphi^2} = \frac{1}{k_n R_\varphi^2} = \frac{Q_s^A L}{R_\varphi^2}$$

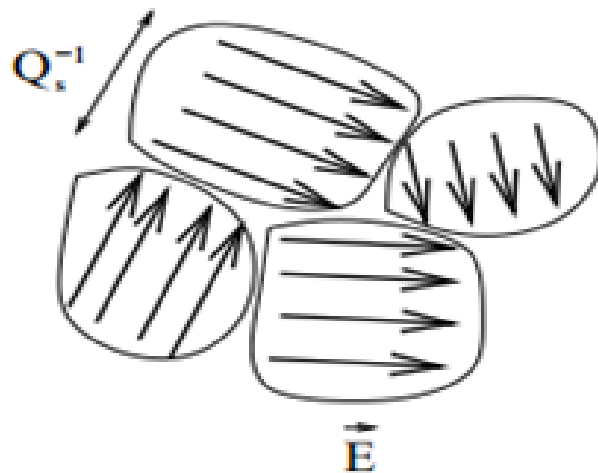
$$v_2 = \frac{\int_0^{\pi/2} d\varphi \cos 2\varphi \frac{dN}{dp_T^2 d\varphi}}{\frac{1}{2\pi} \frac{dN}{dp_T^2}} = \frac{\int_0^{\pi/2} d\varphi \cos 2\varphi F(\tau_\varphi)}{\frac{1}{2\pi} F(\tau)}$$

where

$$\tau_\varphi \equiv \frac{p_T^2}{(Q_{s\varphi}^A)^2} = \frac{p_T^2}{(Q_s^A)^2} \frac{R_\varphi^2}{L} Q_s^A = \tau \frac{R_\varphi^2}{L} Q_s^A$$

$$v_2 = \frac{2}{\pi} \int_0^{\pi/2} d\varphi \cos 2\varphi \frac{R^2 - R_\varphi^2}{R^2} \frac{1}{2\pi F(\tau)} \frac{dF}{d\tau} \tau Q_s^A L,$$

- Hydrodynamics, probably is not at the origin of encoding all the phi dependence in  $Q_s$  and only at most can preserve it
- It suggests models including gluon saturation(or string percolation)with a domain like structure(or cluster of strings structure)



--A parton interacts with the color fields of the cluster of strings(domain) in its way out, losing energy. This gives rise to the elliptic flow

--Two partons leaving the same cluster are correlated with a transverse correlation length( $1/Q_s$ ), and therefore are collimated in azimuthal angle(near side ridge structure)

A.Kovner et al Phys Rev C83 034017 2011

M.A.Braun et al Nucl Phys A 906 14 2013

and arXiv:1407.4590 hep-ph

# CONCLUSIONS

Elliptic flow of charged particles satisfies a scaling law

Photon data are lying on the same scaling line

This scaling is obtained encoding all the azimuthal dependence in an additional momentum saturation

The flow has to do also with initial state interaction

Study of possible scaling of the rest of harmonics