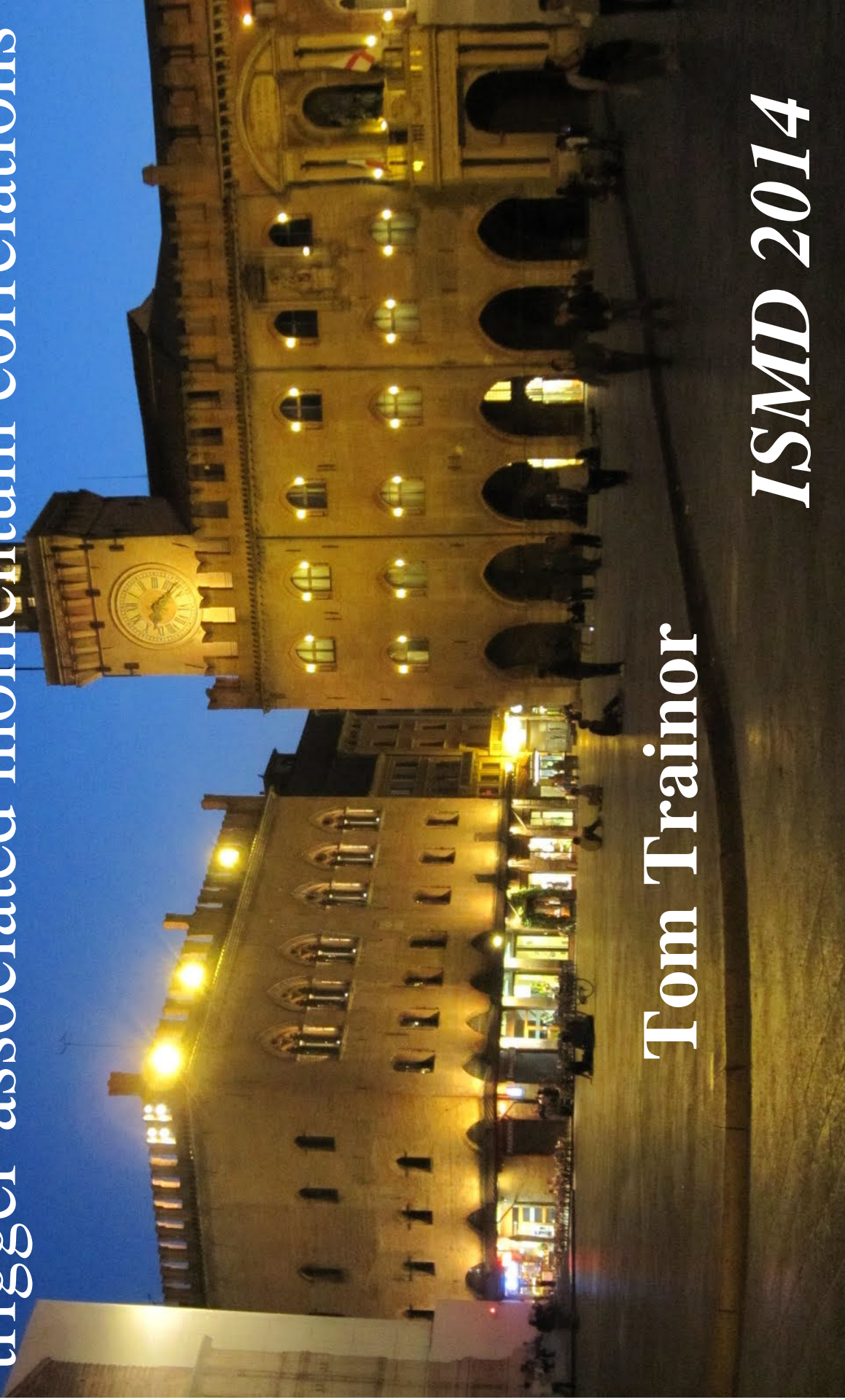


QCD prediction of jet structure in 2D  
trigger-associated momentum correlations



Tom Trainor

*ISMD 2014*

# Agenda

- *Define trigger-associated (TA) correlations*
- *Derive a TA two-component model (TCM)*
- *Extract a TA hard component (HC) → jet fragments*
- *Predict the TA HC via pQCD (MB jet spectrum, FFs)*
- *Identify kinematic limits on dijets in p-p collisions*
- *Isolate single triggered dijets from secondaries (MPI)*
- *Test underlying-event (UE) conjectures re dijets/MPI*

# Trigger-associated (TA) Correlations

*for each event with  $n_{ch}$  hadrons in  $\Delta\eta$*

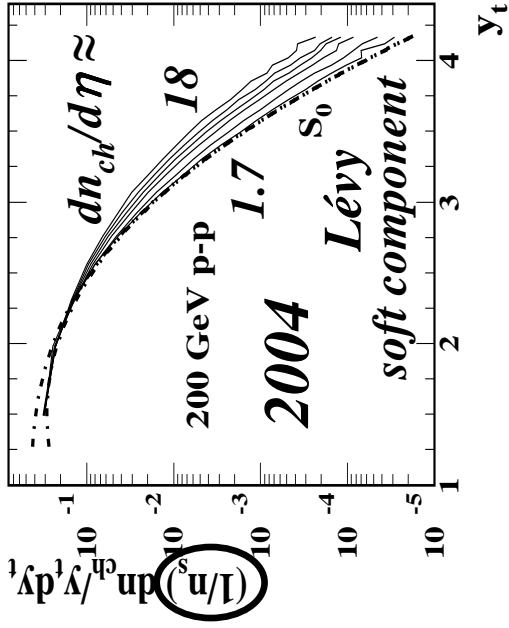
- *the highest- $p_t$  hadron is the “trigger”*
- *$n_{ch}-1$  other hadrons are “associated”*
- *form all trigger-associated pairs (not self pairs)*
- *subtract calculated TCM TA soft components*
- *get conditional data hard component  $A_{hh}(y_{ta}/y_{tt})$*
- *determine azimuth dependence relative to trigger*

**no  $p_t$  cuts – all jets, all hadron pairs accepted**

*rapidities:  $y \equiv \ln[(p + E)/m_\pi]$     $y_t \equiv \ln[(p_t + m_t)/m_\pi]$*

# *p-p* Spectrum TCM and Dijets

nucl-ex/0606028 *p-p* spectra for ten  $n_{ch}$  classes  $n$



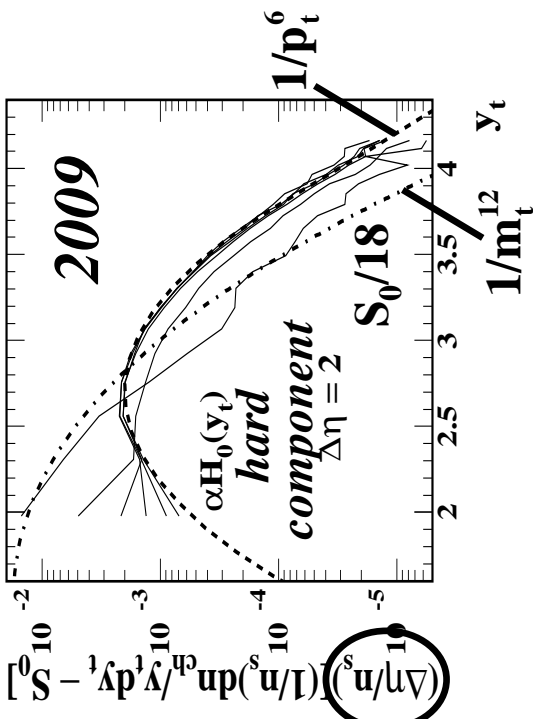
for  $\Delta\eta = 1$

$$n_{ch} = n_s + n_h$$

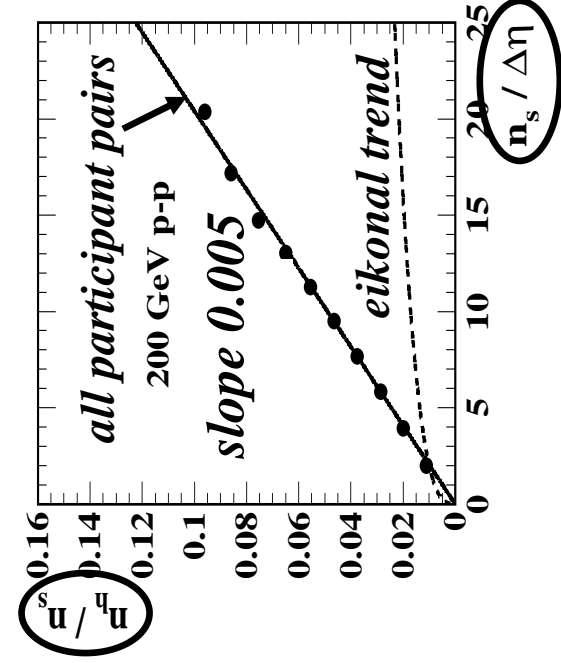
$$n_h \approx 0.005 n_s^2$$



subtract  $S_0$



$$p(y_t, n_{ch}) = p_s(n_{ch}) S_0(y_t) + p_h(n_{ch}) H_0(y_t) \quad \text{factorized}$$

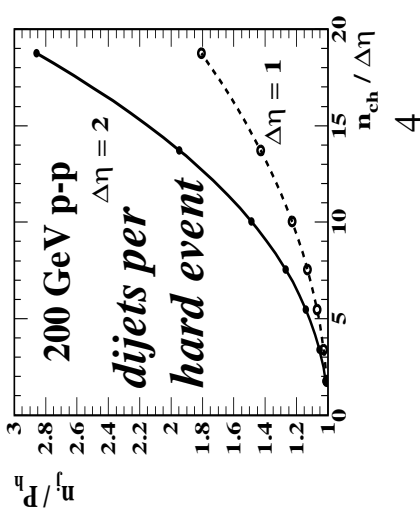


dijet number:  $n_j \propto n_h \propto n_s^2 \propto N_{part}^2$

$$n_j \approx \Delta\eta \, 0.03 \, (n_s / 2.5)^2$$

$$P_s(n_{ch}) = \exp[-n_j(n_{ch})]$$

$$P_h(n_{ch}) = 1 - P_s(n_{ch})$$



# Trigger-associated TCM

within some  $\Delta\eta$

*arXiv:1307.1819*

*TCM for SP spectra:*

$$\mathbf{F}(\mathbf{y}_t, \mathbf{n}_{\text{ch}}) = \mathbf{n}_s \mathbf{S}_0(\mathbf{y}_t) + \mathbf{n}_h \mathbf{H}_0(\mathbf{y}_t)$$

$$\mathbf{n}_{\text{ch}} = \mathbf{n}_s + \mathbf{n}_h \quad \mathbf{n}_h = \alpha \mathbf{n}_s^2 \quad \mathbf{n}_j \propto \mathbf{n}_h$$

*trigger spectrum:*

$$\mathbf{T}(\mathbf{y}_{\text{tt}}) = \mathbf{G}(\mathbf{y}_{\text{tt}}) \mathbf{F}(\mathbf{y}_{\text{tt}})$$

*void probability:  $\mathbf{G}(\mathbf{y}_{\text{tt}}) = \exp[-\mathbf{n}_{\Sigma}(\mathbf{y}_{\text{tt}})]$*

*joint TA distribution:*

$$\mathbf{F}_{\text{ta}}(\mathbf{y}_{\text{ta}}, \mathbf{y}_{\text{tt}}) = \mathbf{T}(\mathbf{y}_{\text{tt}}) \mathbf{A}(\mathbf{y}_{\text{ta}} | \mathbf{y}_{\text{tt}})$$

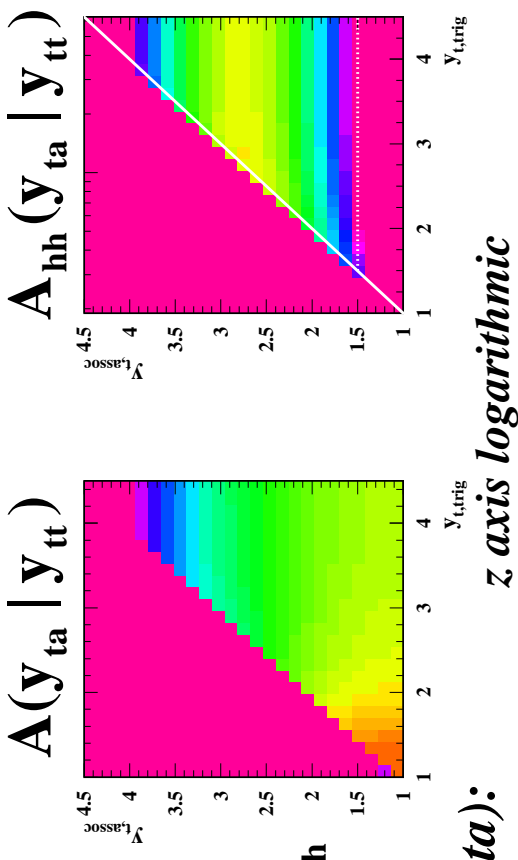
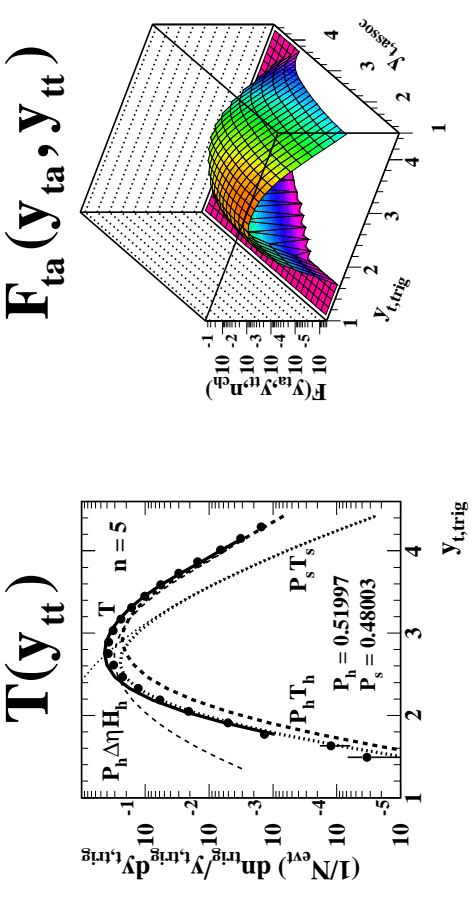
*soft and hard event types:*

$$\mathbf{A}(\mathbf{y}_{\text{ta}} | \mathbf{y}_{\text{tt}}, \mathbf{n}_{\text{ch}}) = \mathbf{P}_s(\mathbf{n}_{\text{ch}}) \mathbf{A}_s + \mathbf{P}_h(\mathbf{n}_{\text{ch}}) \mathbf{A}_h$$

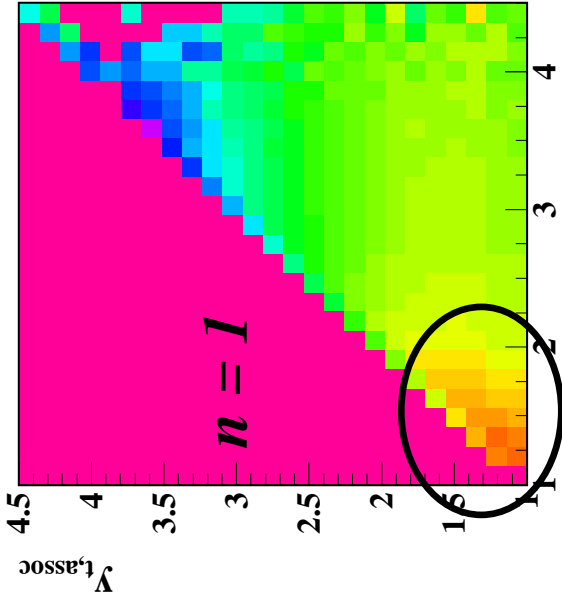
$$\mathbf{P}_s(\mathbf{n}_{\text{ch}}) = \exp[-\mathbf{n}_j(\mathbf{n}_{\text{ch}})]$$

*hard component of hard events (TCM or data):*

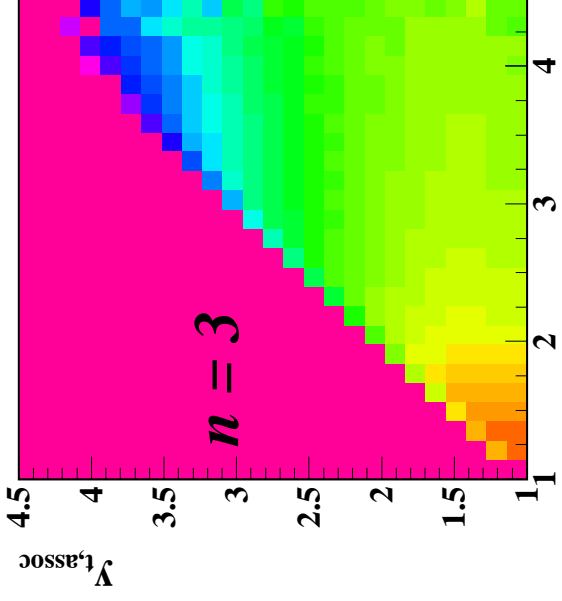
$\mathbf{A}_{\text{hh}}(\mathbf{y}_{\text{ta}} | \mathbf{y}_{\text{tt}})$  *object of study: includes all dijet TA correlations*



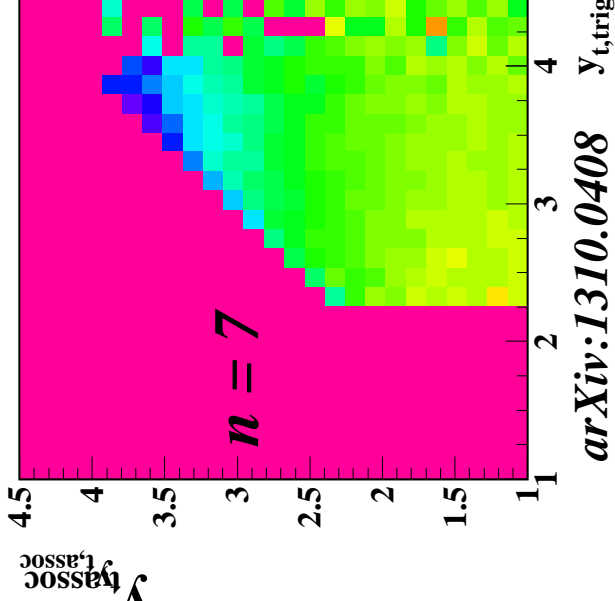
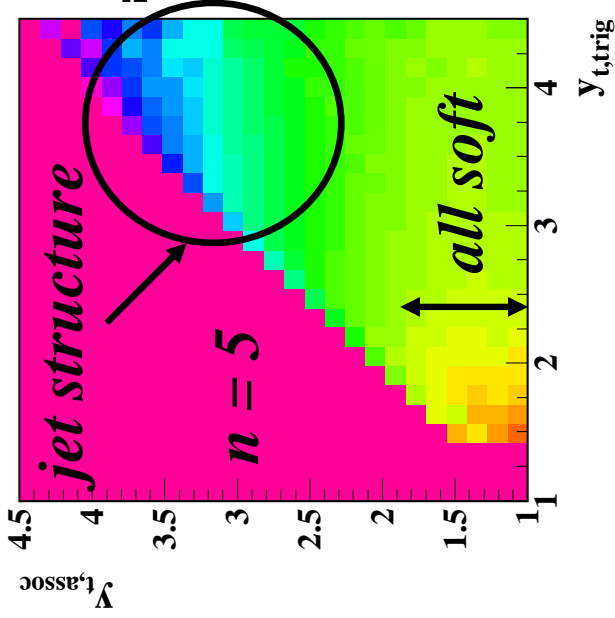
# Associated-per-Trigger Ratios $A \equiv F/T$



due to  $n_{ch}-1$  constraint



*p-p data*

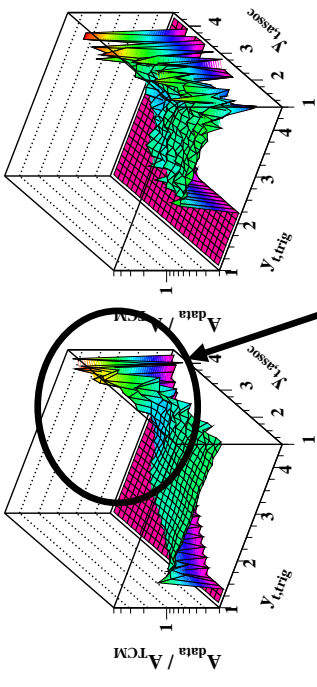
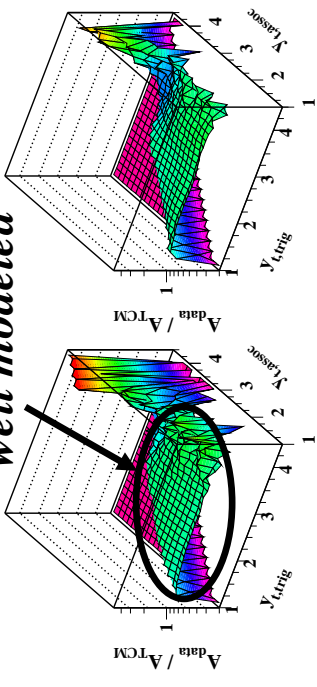


arXiv:1310.0408

$A_{\text{data}} / A_{\text{TCM}}$

*data soft components*

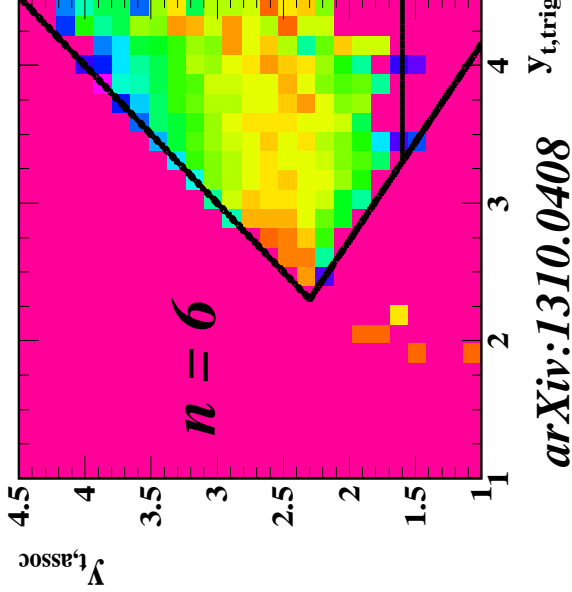
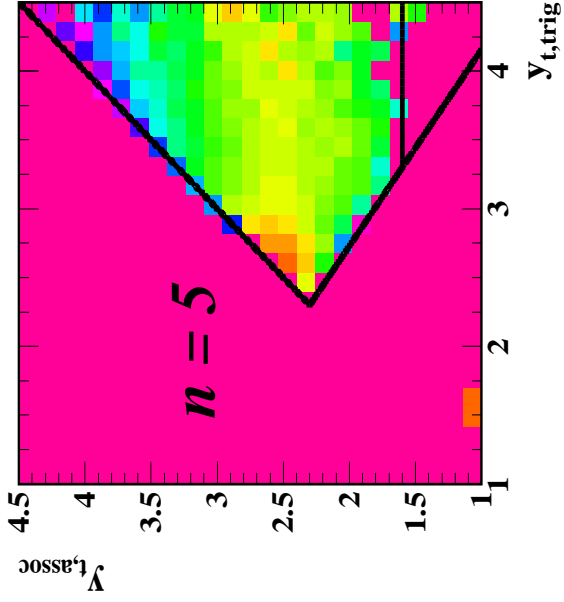
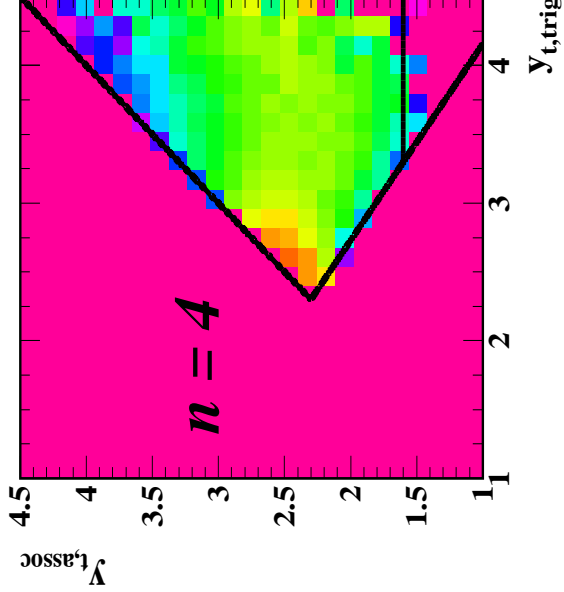
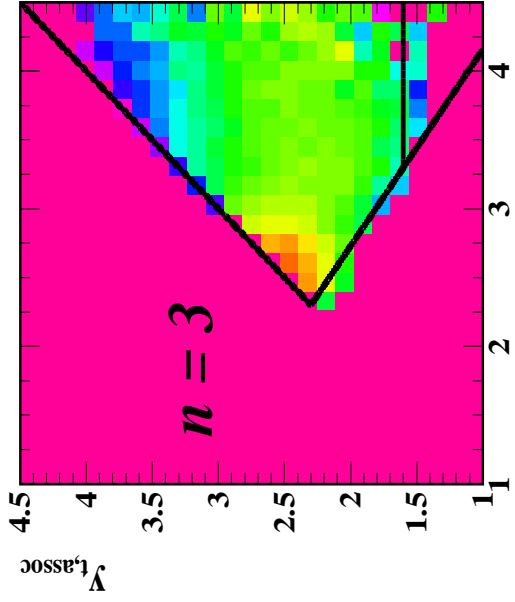
*well modeled*



*data hard component:  
new information  
on dijet structure*

# Hard Component of $A \equiv F/T$

per hard event, dependent on  $n_{ch}$



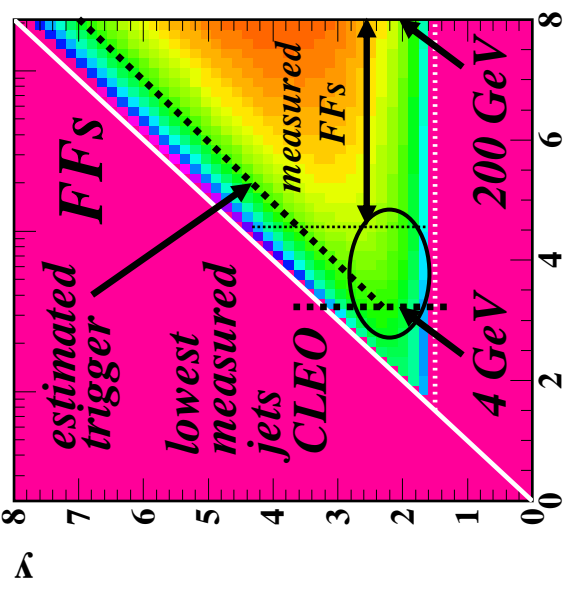
arXiv:1310.0408

**subtract TCM  
soft components**

*compare with  
unbiased jet structure*

hep-ph/0606249

**measured FFs – 2006**

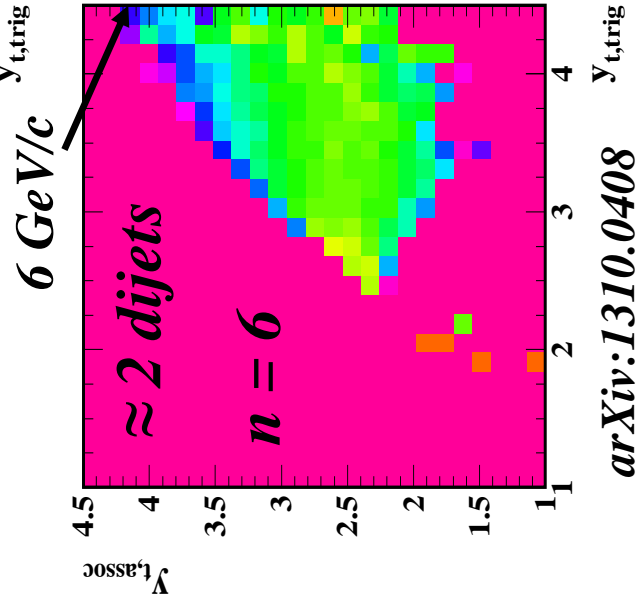
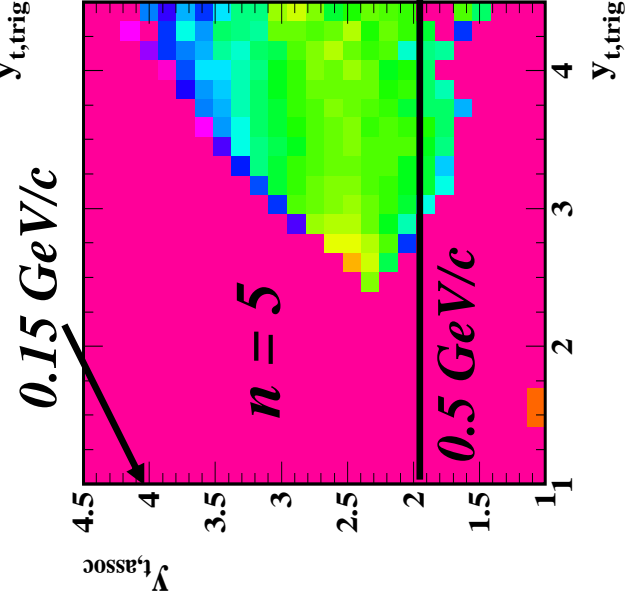
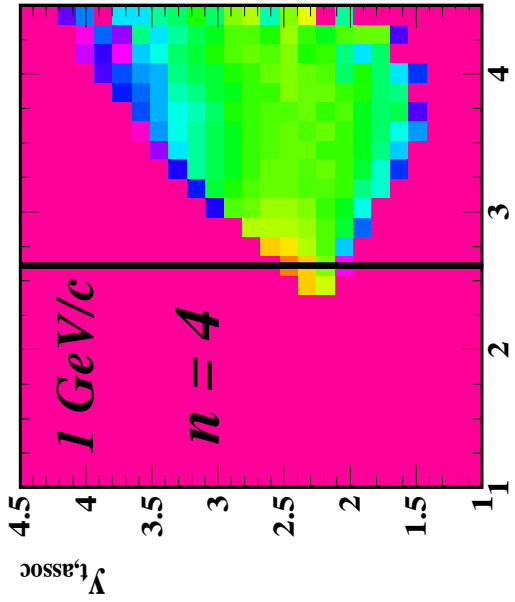
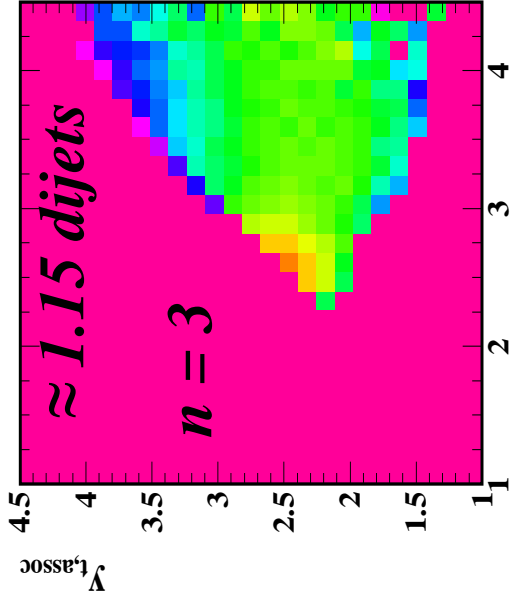


**dijet energy**  $y_{\max}$

$y_{\max} \approx \ln(2E_{\text{parton}}/m_{\pi})$  7

# Hard Component of $A \equiv F/T$

per dijet, approximately independent of  $n_{ch}$ !

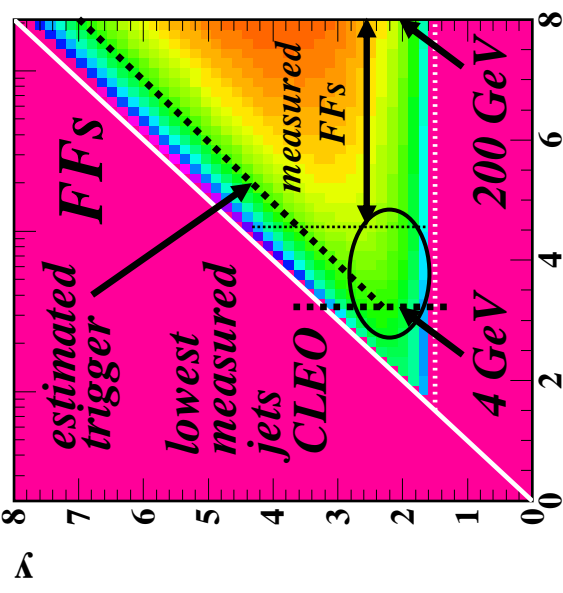


**subtract TCM  
soft components**

*compare with  
unbiased jet structure*

hep-ph/0606249

measured FFs – 2006



dijet energy  $y_{max}$   
 $y_{max} \approx \ln(2E_{parton}/m_T)$  8

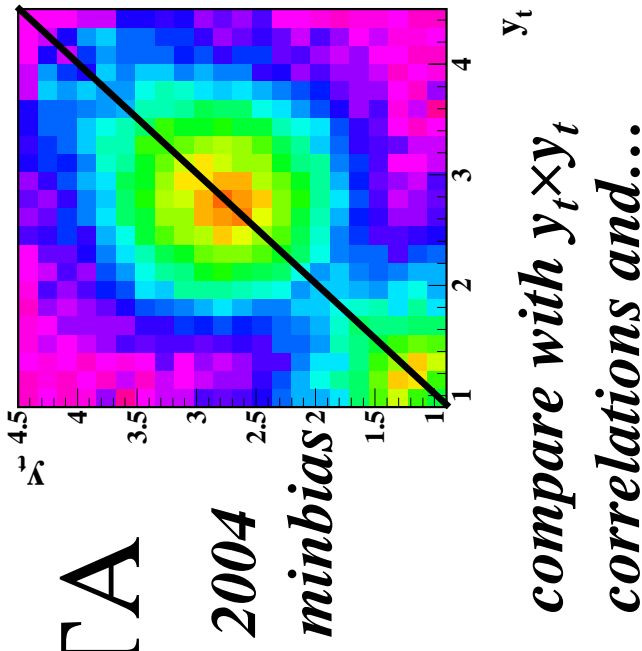
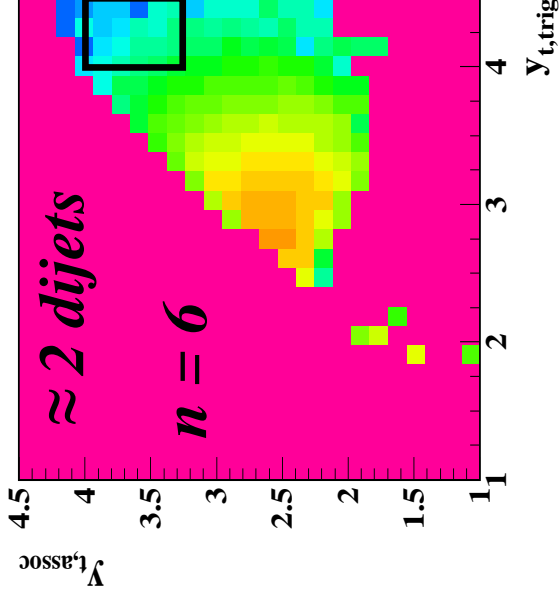
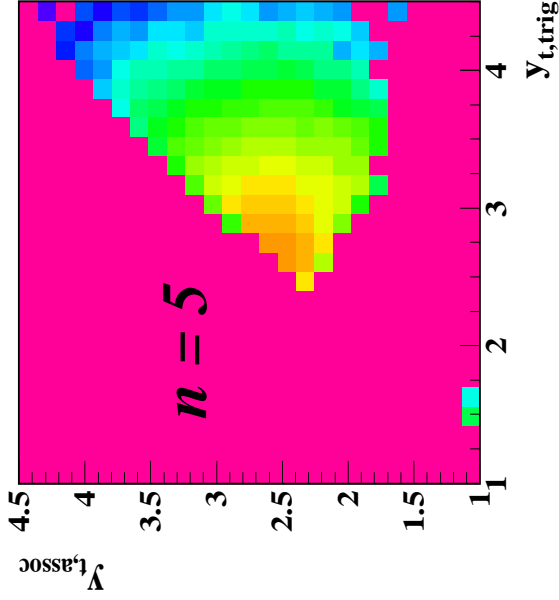
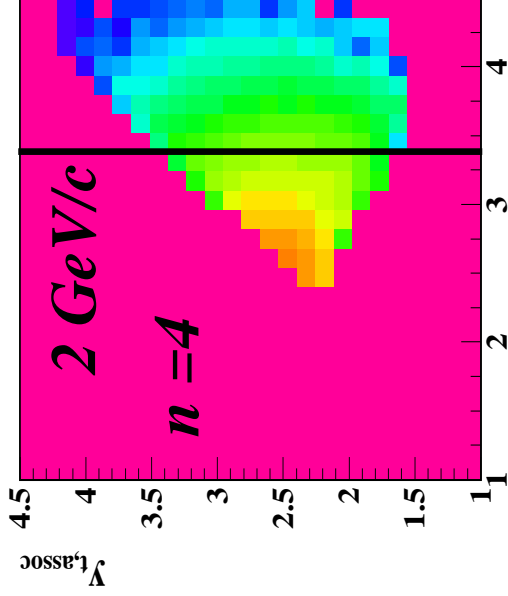
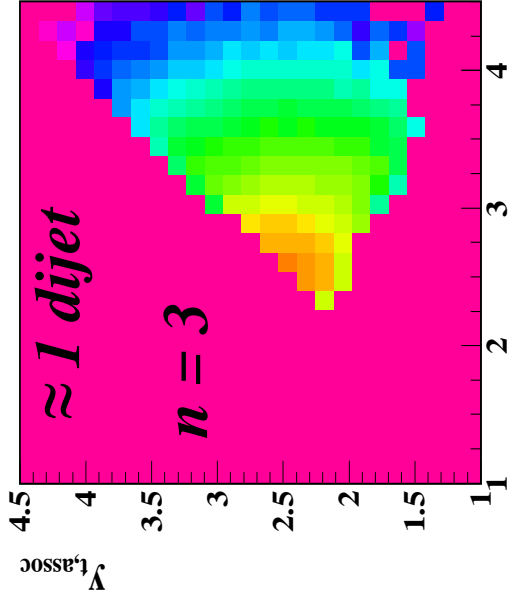
arXiv:1310.0408



# Hard Component of $F \equiv TA$

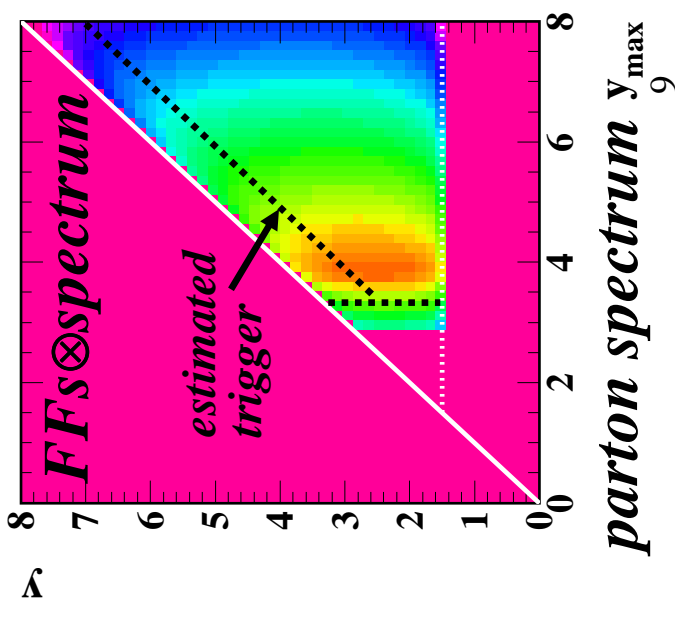
*actual minbias trigger-associated HC*

2004



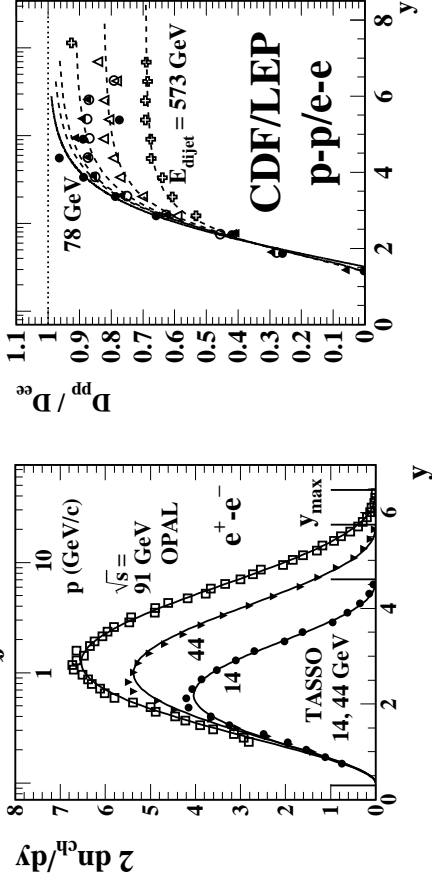
*compare with  $y_t \times y_t$   
correlations and...*

*pQCD factorization*



# Fragmentation Functions – TA Partition

$2dn_{ch,j}/dy$  arXiv:1407.6422



*FFs for given parton and hadron types:*

$$D_{\pi}^{\text{f}}(y | y_{\text{max}}) \quad y_{\text{max}} = \ln(2E_{\text{jet}}/m_{\pi})$$

$$S_{\text{t}}(y_{\text{trig}} | y_{\text{max}})$$

*trigger fragment from void probability:*

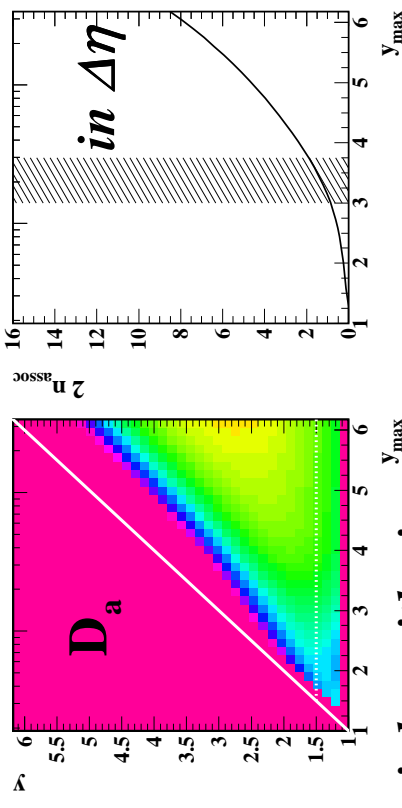
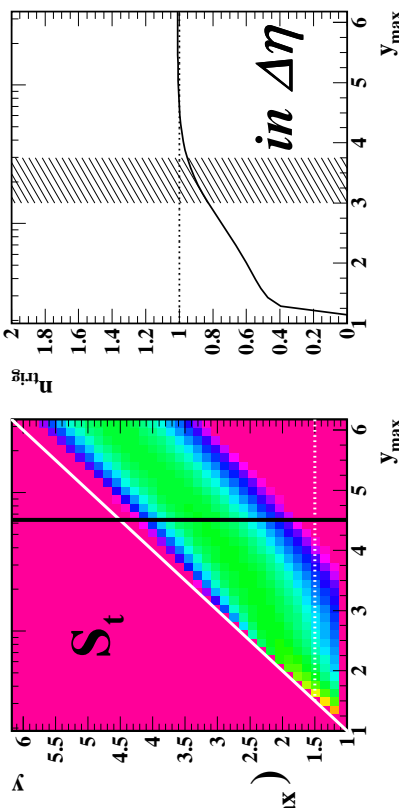
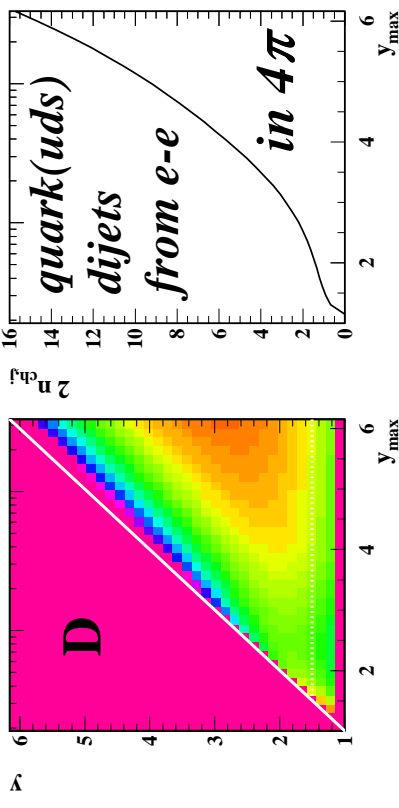
$$S_{\text{t}}(y | y_{\text{max}}) = G(y) \epsilon(\Delta\eta) D(y | y_{\text{max}})$$

*complementary associated fragments:*

$$D_{\text{a}}(y | y_{\text{max}}) = [1 - G(y)] \epsilon(\Delta\eta) D(y | y_{\text{max}})$$



*dijet fraction in  $\Delta\eta$*

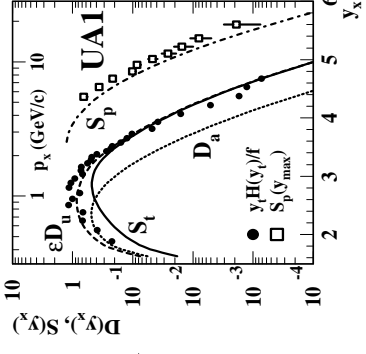
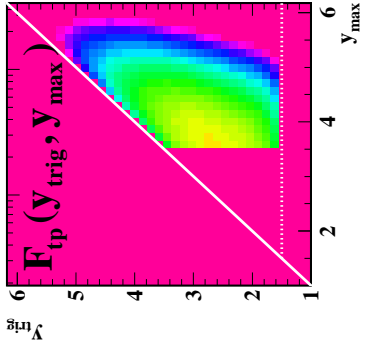


*z axis logarithmic*

# Convolutions and Bayes' Theorem

relate parton-fragment FF system to hadron-hadron TA system

$$F_{tp}(y_{trig}, y_{max}) = S_p(y_{max}) S_t(y_{trig} | y_{max})$$

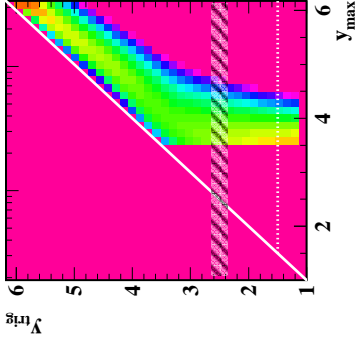
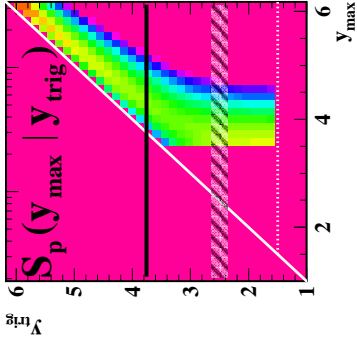


project  
onto  $y_{trig}$

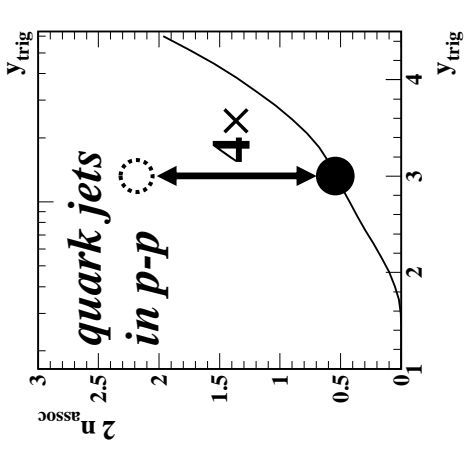
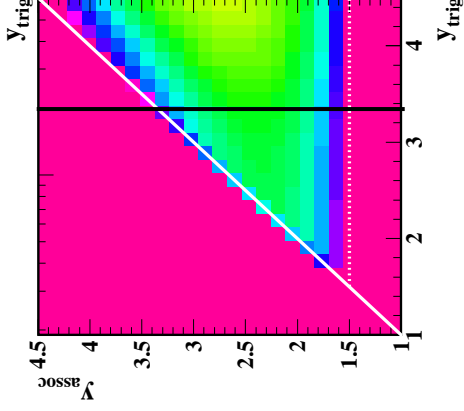
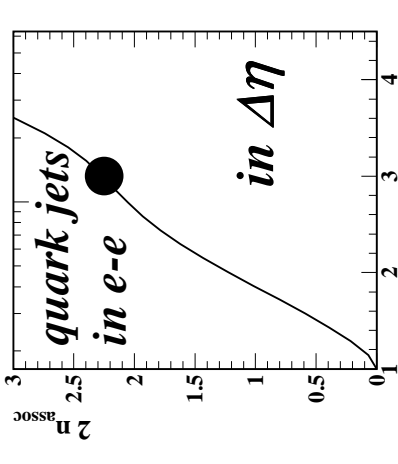
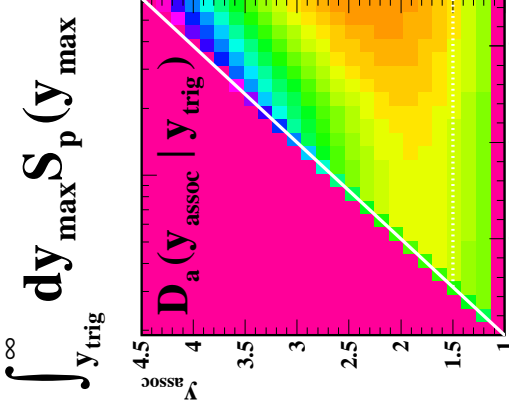
$$S_t(y_{trig}) = \int_{y_{trig}}^{\infty} dy_{max} S_p(y_{max}) S_t(y_{trig} | y_{max})$$

Bayes' theorem:

$$S_p(y_{max} | y_{trig}) = \frac{S_p(y_{max}) S_t(y_{trig} | y_{max})}{S_t(y_{trig})}$$



$$D_a(y_{assoc} | y_{trig}) = [\nu_S y_{ta} A_{hh}(y_{ta}/y_{tt})]$$



# Isolating the Triggered Dijet

*arXiv:1407.6422*

$$R_x = T_x/T$$

$$\text{data } \mathbf{P}_h \mathbf{R}_h \mathbf{A}_{hh} = \mathbf{A} - \mathbf{P}_s \mathbf{R}_s \mathbf{A}_s - \mathbf{P}_h \mathbf{R}_h \mathbf{A}_{hs}$$

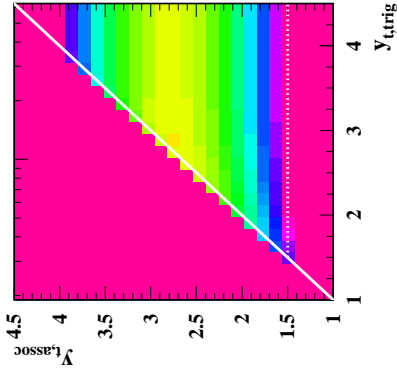
*TCM soft components*

$$n_j = I + \Delta n_j$$

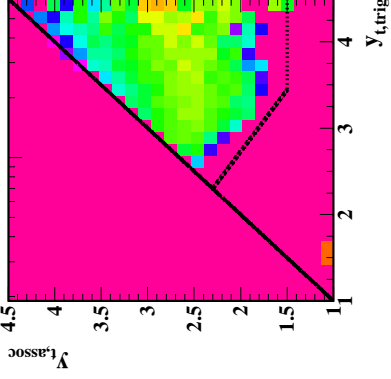
$$\mathbf{T}_h \mathbf{A}_{hh} = \mathbf{G}_{hh} \mathbf{T}_{hs} \mathbf{A}'_{hh} + \mathbf{G}_{hs} \mathbf{T}_{hh} \left( \mathbf{A}_{hh}'' + \mathbf{A}_{hh}^* \right)$$

*untriggered dijets*

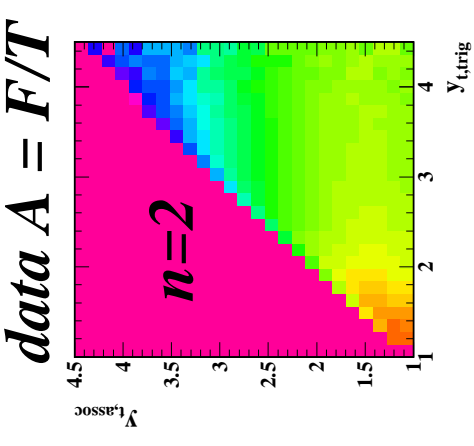
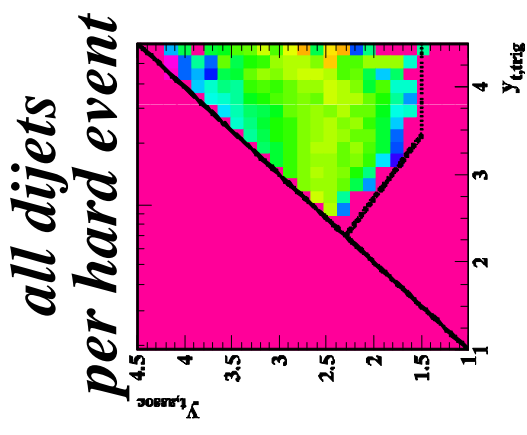
*triggered*



+



=



*TCM: A'\_{hh}, A''\_{hh}*

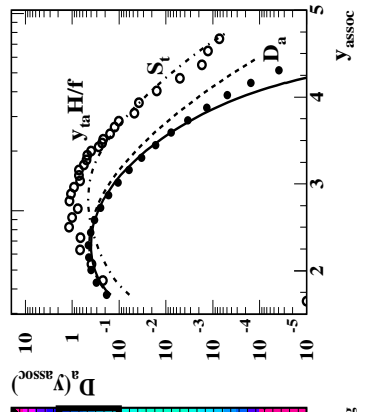
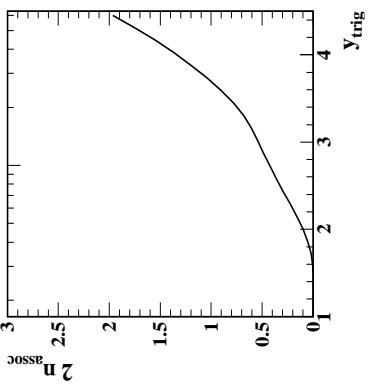
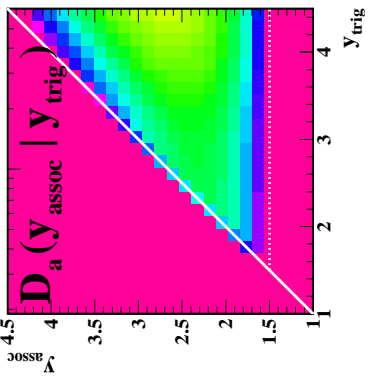
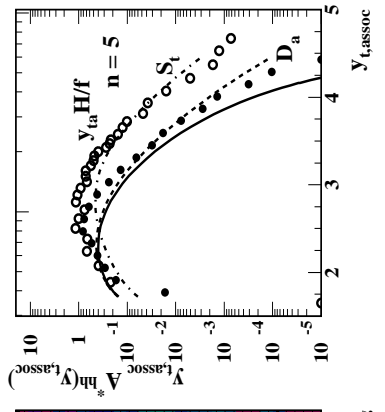
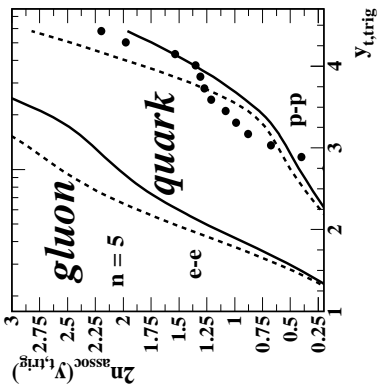
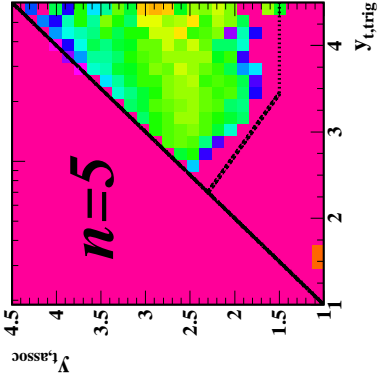
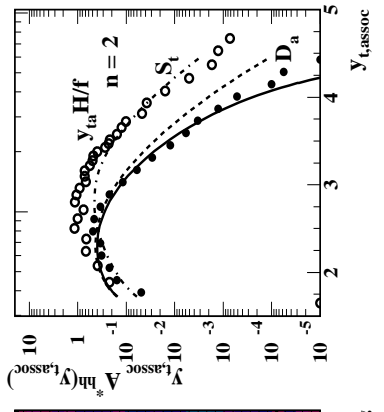
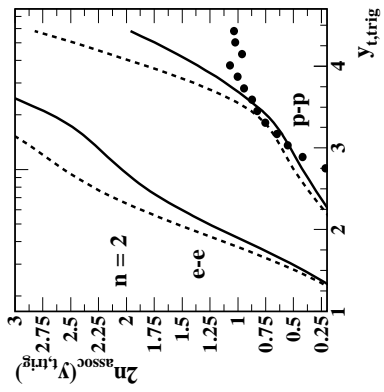
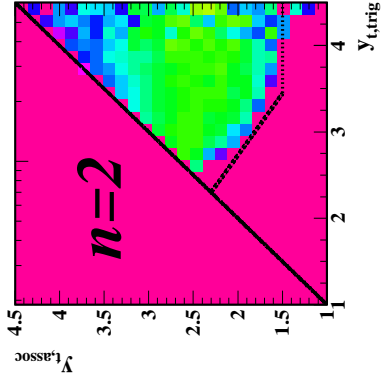
*data:*

$\mathbf{A}_{hh}^*$

*single triggered dijet  
comparable to FFs*

# TA Comparisons: FFs vs p-p Data

$$y_{ta} A_{hh}^*(y_{ta} | y_{tt}) \quad y_{ta} F_{hh}^*(y_{ta}, y_{tt}) = T_h(y_{tt}) y_{ta} A_{hh}^*(y_{ta} | y_{tt})$$

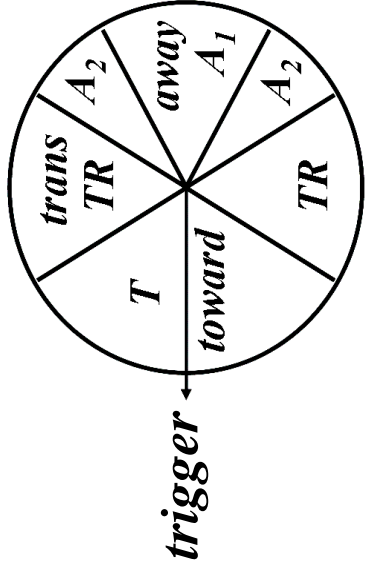


*p-p data*

*pQCD*

*z axis logarithmic*

# A = F/T vs Azimuth Intervals

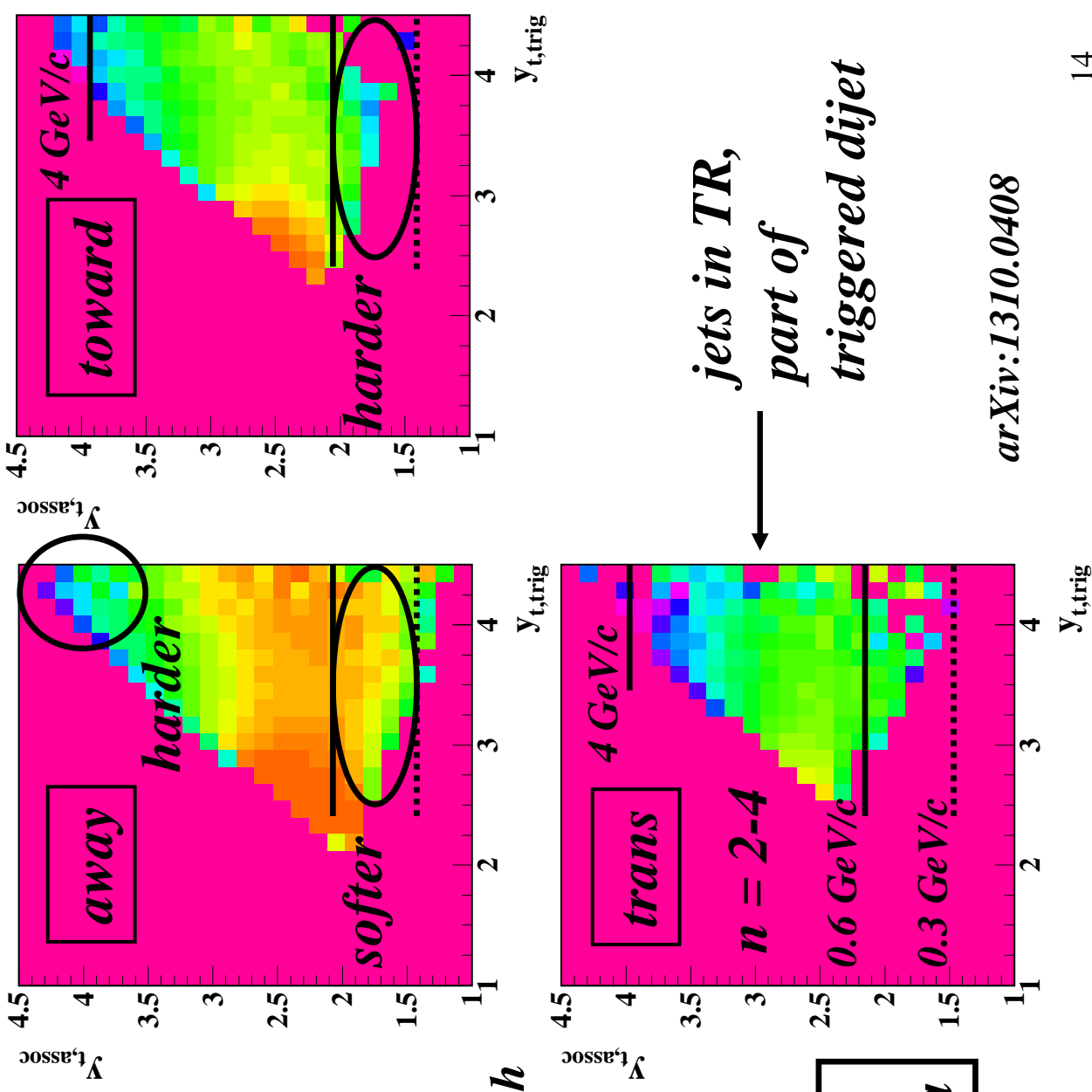


*sum three low- $n_{ch}$*

*bins:  $\underline{MPI < 15\%}$*

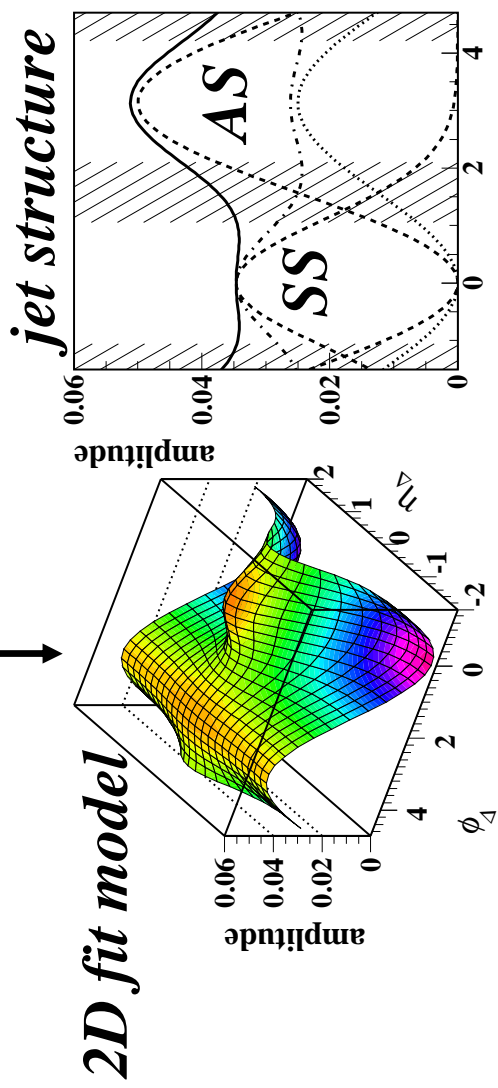
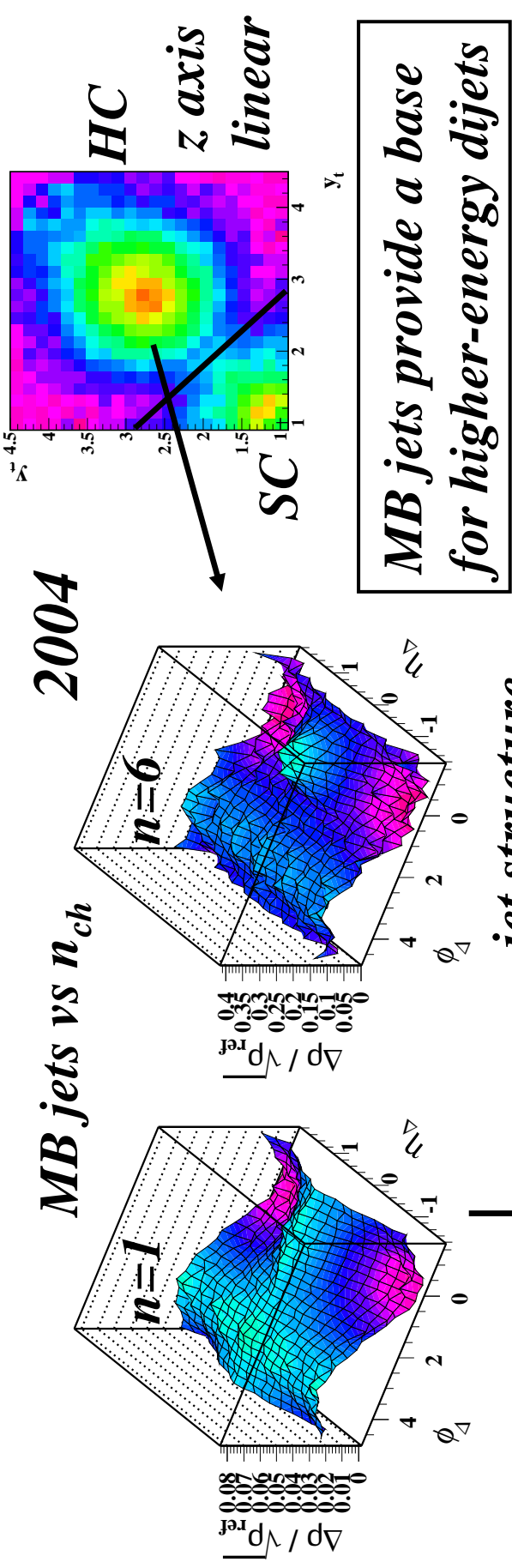
*$\Delta n_j < 0.15$*

*UE MPI conjecture  
inconsistent with data*



*arXiv:1310.0408*

# Dijet Structure in the “Trans” Region



*relative to MB jets:  
for higher jet energies  
hadrons added nearer  
to the jet axis do not  
contribute to the TR*

**TR = “trans”**  $\longleftrightarrow \phi_{\Delta}$

*substantial overlap: same-side SS vs away-side AS*

# Summary

- *Define TCM for 1D T (trigger spectrum), 2D F = TA*
- *Hard components of F, A → MB dijets*
- *Distinguish single triggered dijets, secondaries = MPI*
- *Quantitative link: TA vs FFs + pQCD jet spectrum*
- *Establish kinematic lower bounds on MB dijets*
- *TA data confirm trigger dijet contribution to azimuth TR*
- *MB dijets make a large contribution to p-p, p-A, A-A*