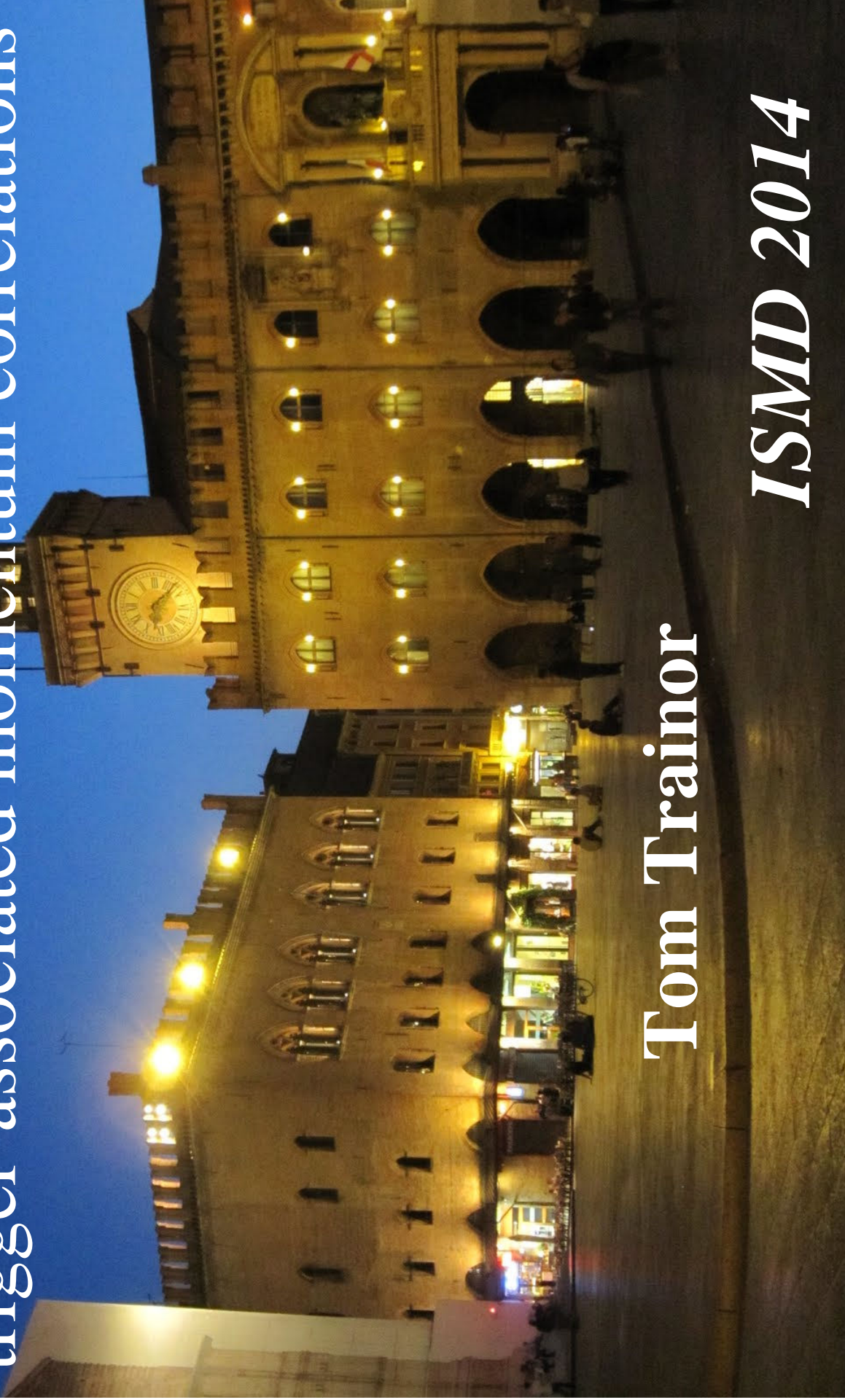


QCD prediction of jet structure in 2D
trigger-associated momentum correlations



Tom Trainor

ISMD 2014

Agenda

- *Define trigger-associated (TA) correlations*
- *Derive a TA two-component model (TCM)*
- *Extract a TA hard component (HC) → jet fragments*
- *Predict the TA HC via pQCD (MB jet spectrum, FFs)*
- *Identify kinematic limits on dijets in p-p collisions*
- *Isolate single triggered dijets from secondaries (MPI)*
- *Test underlying-event (UE) conjectures re dijets/MPI*

Trigger-associated (TA) Correlations

for each event with n_{ch} hadrons in $\Delta\eta$

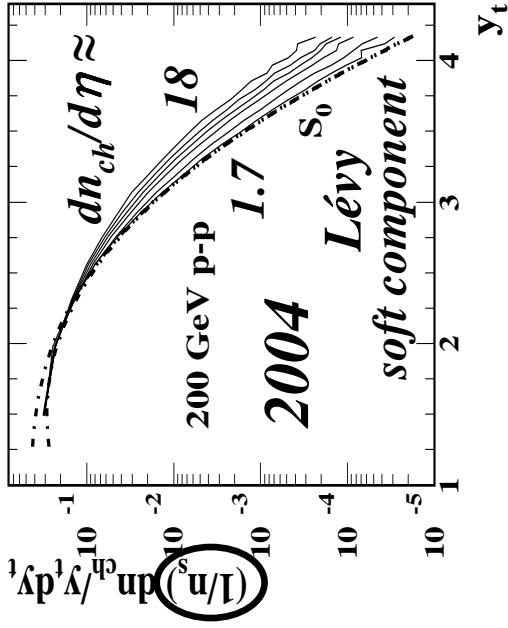
- *the highest- p_t hadron is the “trigger”*
- *$n_{ch}-1$ other hadrons are “associated”*
- *form all trigger-associated pairs (not self pairs)*
- *subtract calculated TCM TA soft components*
- *get conditional data hard component $A_{hh}(y_{ta}/y_{tt})$*
- *determine azimuth dependence relative to trigger*

no p_t cuts – all jets, all hadron pairs accepted

rapidities: $y \equiv \ln[(p + E)/m_\pi]$ $y_t \equiv \ln[(p_t + m_t)/m_\pi]$

p-p Spectrum TCM and Dijets

nucl-ex/0606028 *p-p* spectra for ten n_{ch} classes n



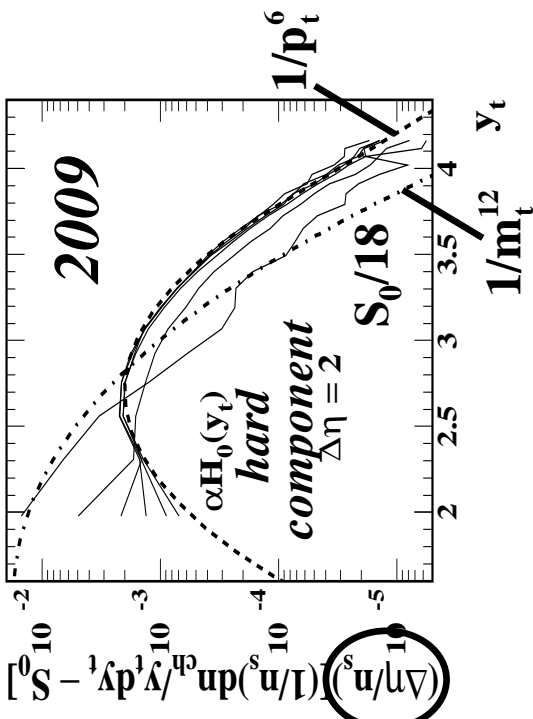
for $\Delta\eta = 1$

$$n_{ch} = n_s + n_h$$

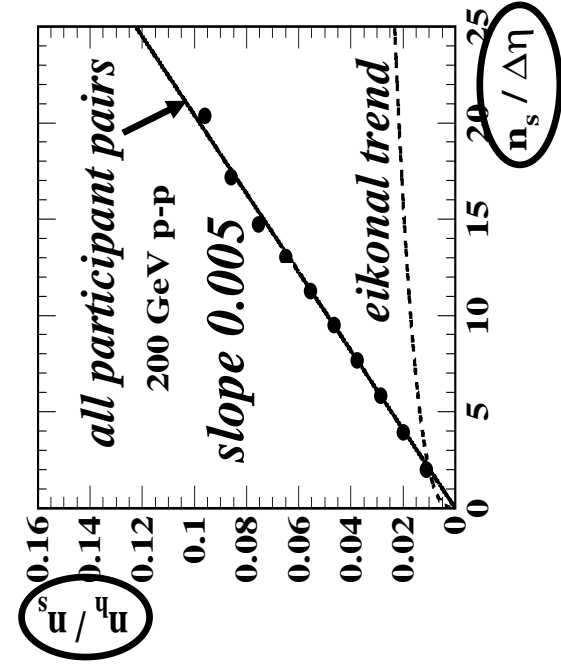
$$n_h \approx 0.005 n_s^2$$



subtract S_0



$$p(y_t, n_{ch}) = p_s(n_{ch}) S_0(y_t) + p_h(n_{ch}) H_0(y_t) \quad \text{factorized}$$

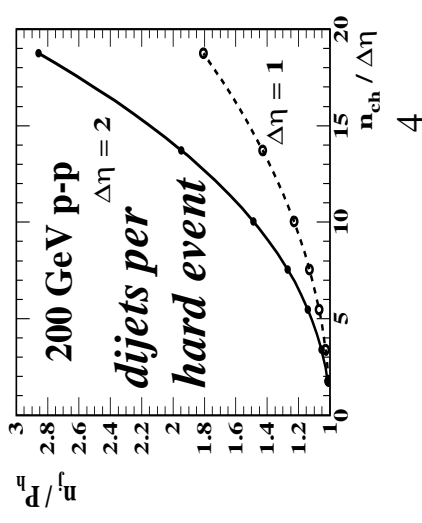


dijet number: $n_j \propto n_h \propto n_s^2 \propto N_{part}^2$

$$n_j \approx \Delta\eta \, 0.03 \, (n_s/2.5)^2$$

$$P_s(n_{ch}) = \exp[-n_j(n_{ch})]$$

$$P_h(n_{ch}) = 1 - P_s(n_{ch})$$



Trigger-associated TCM

within some $\Delta\eta$

arXiv:1307.1819

TCM for SP spectra:

$$\mathbf{F}(\mathbf{y}_t, \mathbf{n}_{\text{ch}}) = \mathbf{n}_s \mathbf{S}_0(\mathbf{y}_t) + \mathbf{n}_h \mathbf{H}_0(\mathbf{y}_t)$$

$$\mathbf{n}_{\text{ch}} = \mathbf{n}_s + \mathbf{n}_h \quad \mathbf{n}_h = \alpha \mathbf{n}_s^2 \quad \mathbf{n}_j \propto \mathbf{n}_h$$

trigger spectrum:

$$\mathbf{T}(\mathbf{y}_{\text{tt}}) = \mathbf{G}(\mathbf{y}_{\text{tt}}) \mathbf{F}(\mathbf{y}_{\text{tt}})$$

void probability: $\mathbf{G}(\mathbf{y}_{\text{tt}}) = \exp[-\mathbf{n}_{\Sigma}(\mathbf{y}_{\text{tt}})]$

joint TA distribution:

$$\mathbf{F}_{\text{ta}}(\mathbf{y}_{\text{ta}}, \mathbf{y}_{\text{tt}}) = \mathbf{T}(\mathbf{y}_{\text{tt}}) \mathbf{A}(\mathbf{y}_{\text{ta}} | \mathbf{y}_{\text{tt}})$$

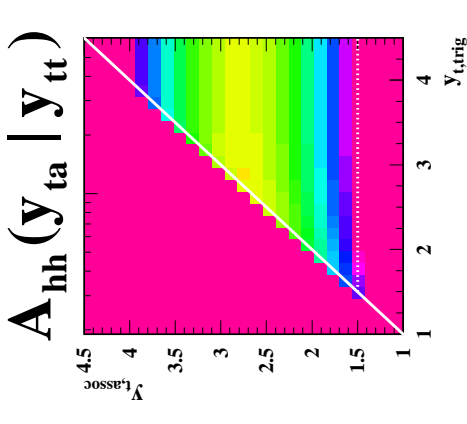
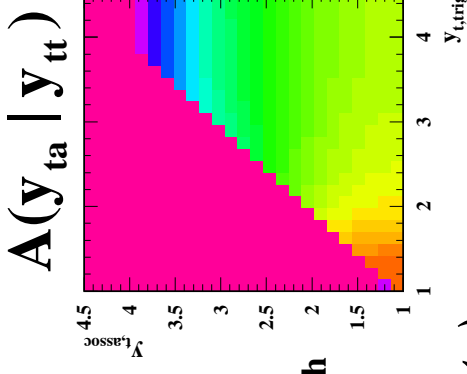
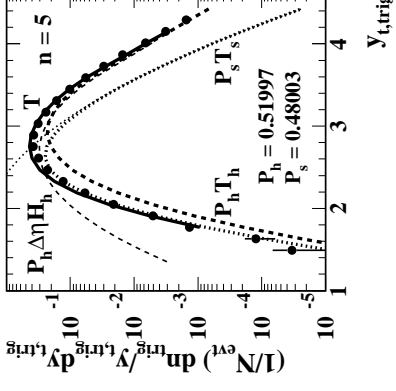
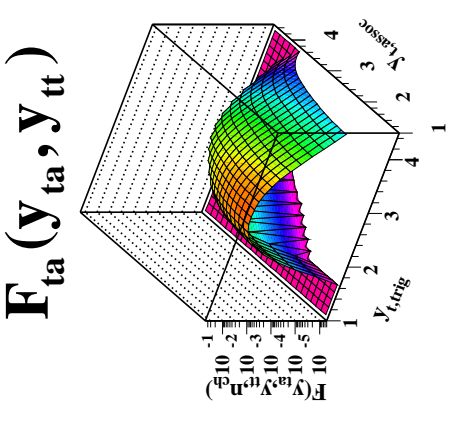
soft and hard event types:

$$\mathbf{A}(\mathbf{y}_{\text{ta}} | \mathbf{y}_{\text{tt}}, \mathbf{n}_{\text{ch}}) = \mathbf{P}_s(\mathbf{n}_{\text{ch}}) \mathbf{A}_s + \mathbf{P}_h(\mathbf{n}_{\text{ch}}) \mathbf{A}_h$$

$$\mathbf{P}_s(\mathbf{n}_{\text{ch}}) = \exp[-\mathbf{n}_j(\mathbf{n}_{\text{ch}})]$$

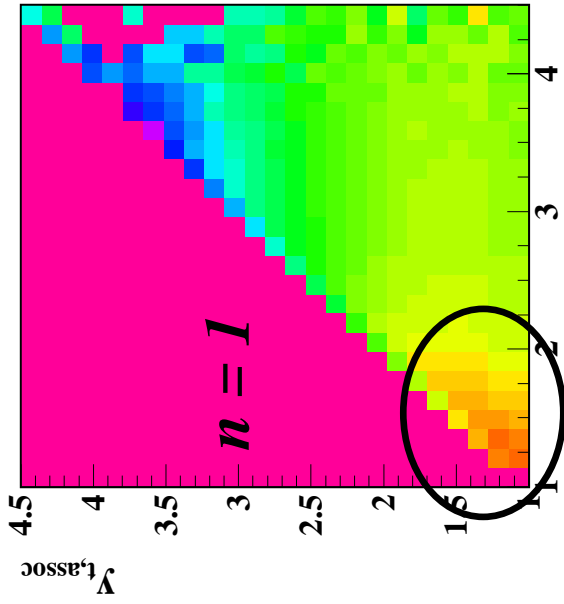
hard component of hard events (TCM or data):

$\mathbf{A}_{\text{hh}}(\mathbf{y}_{\text{ta}} | \mathbf{y}_{\text{tt}})$ *object of study: includes all dijet TA correlations*

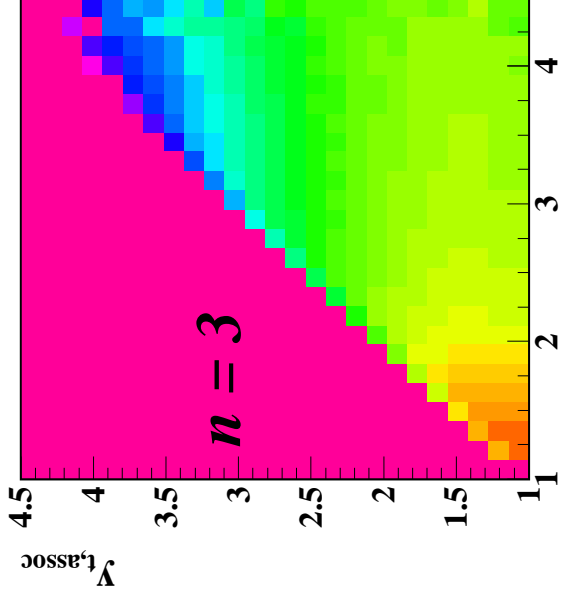


z axis logarithmic

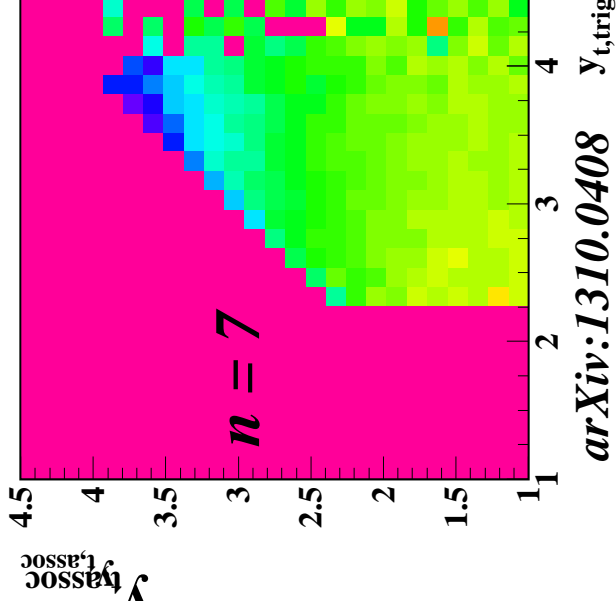
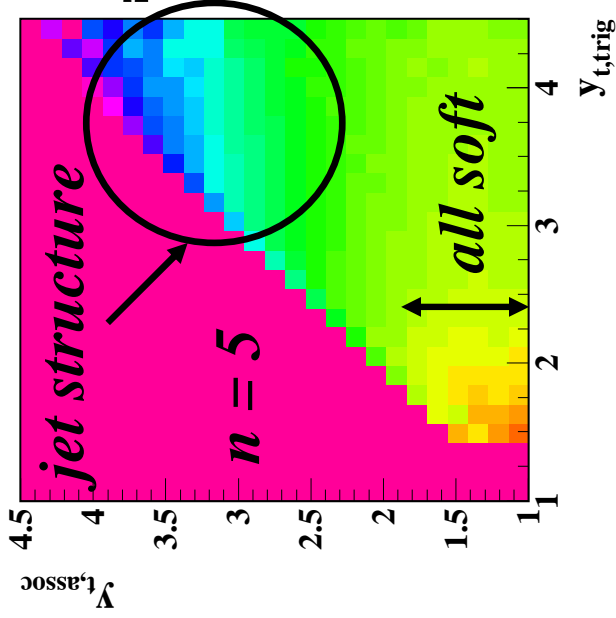
Associated-per-Trigger Ratios $A \equiv F/T$



due to $n_{ch}-1$ constraint



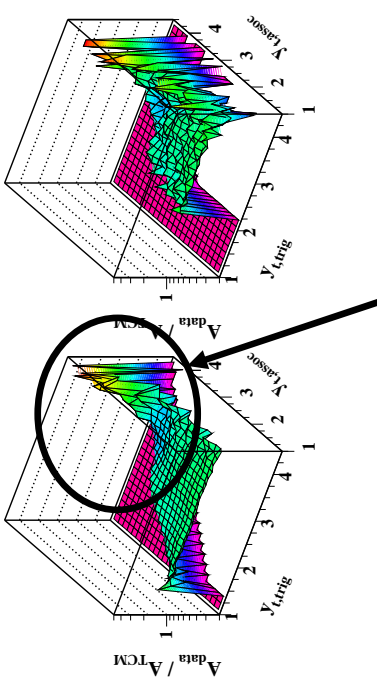
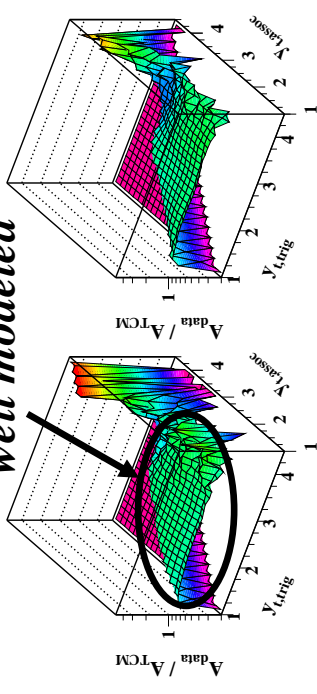
p-p data



$A_{\text{data}} / A_{\text{TCM}}$

data soft components

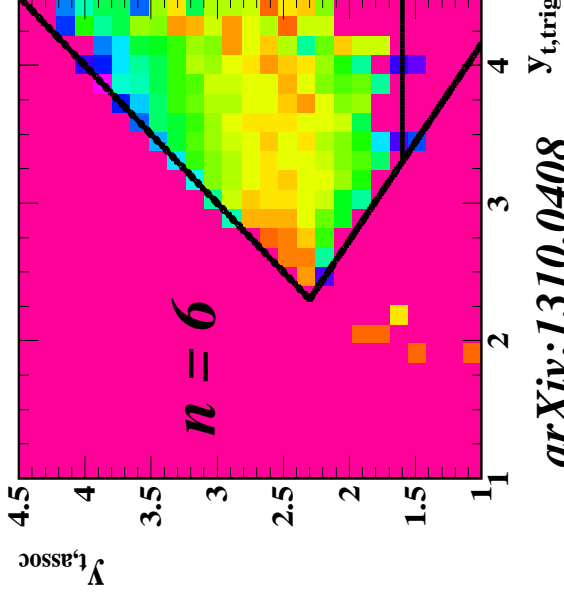
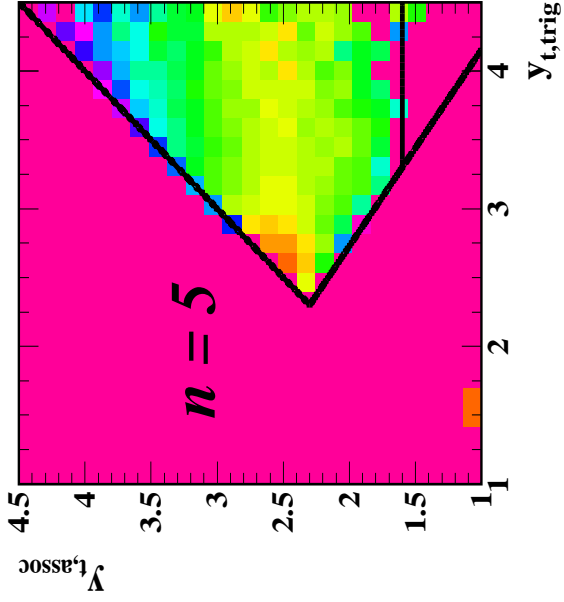
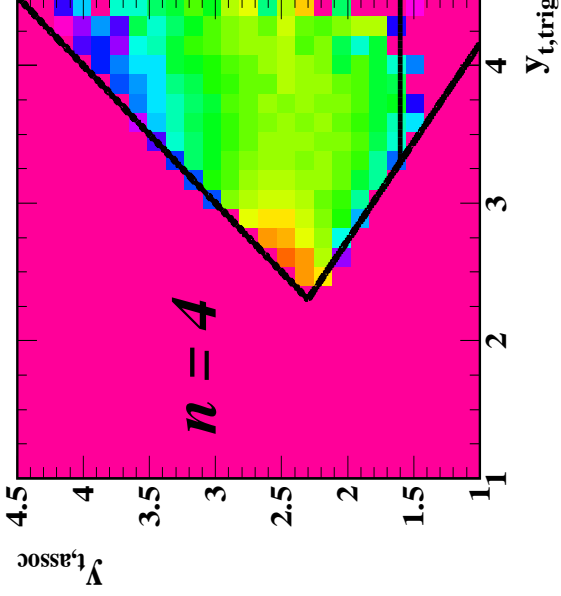
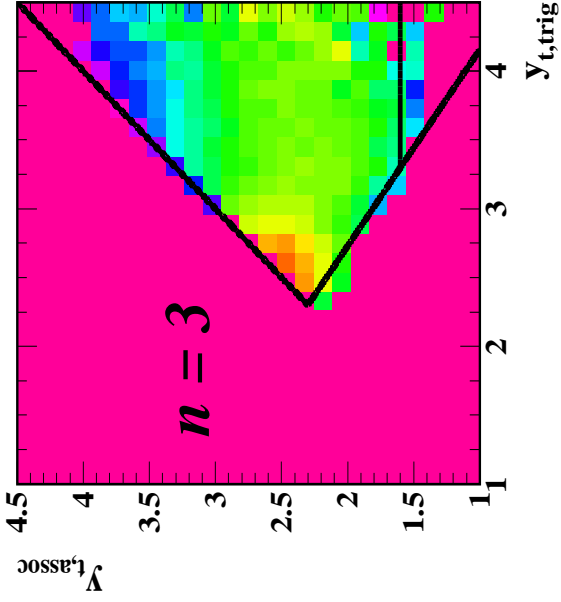
well modeled



*data hard component:
new information
on dijet structure*

Hard Component of $A \equiv F/T$

per hard event, dependent on n_{ch}



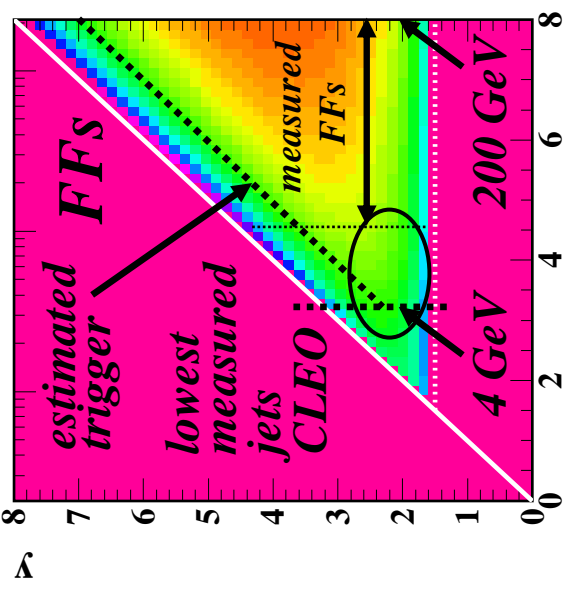
arXiv:1310.0408

**subtract TCM
soft components**

compare with
unbiased jet structure

hep-ph/0606249

measured FFs – 2006

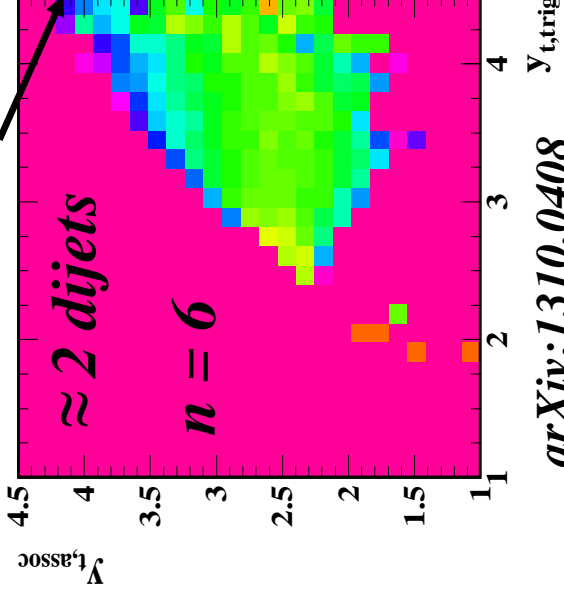
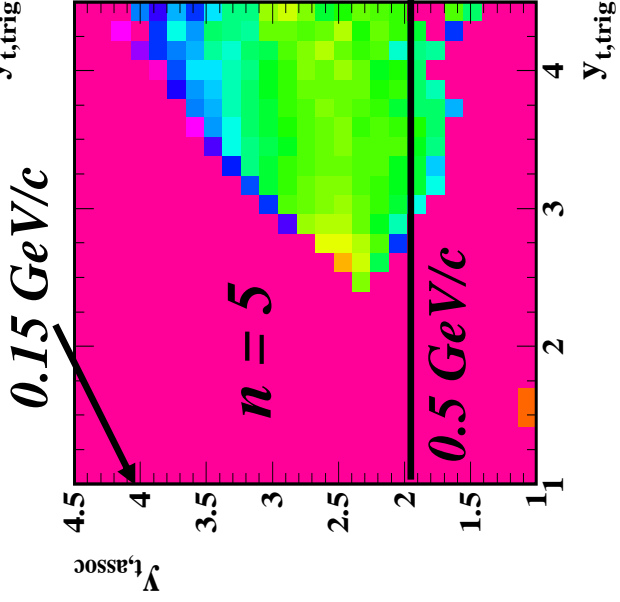
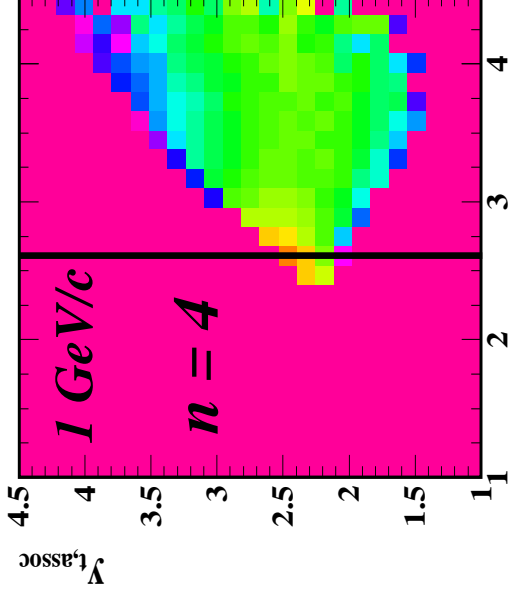
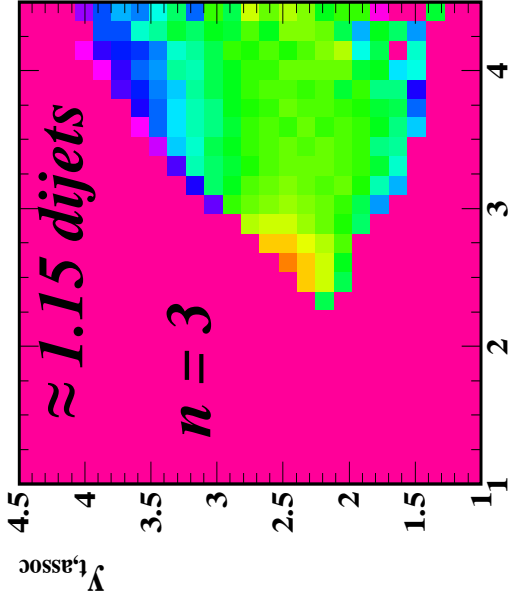


dijet energy y_{\max}

$y_{\max} \approx \ln(2E_{\text{parton}}/m_{\text{T}})$ 7

Hard Component of $A \equiv F/T$

per dijet, approximately independent of n_{ch} !



subtract TCM

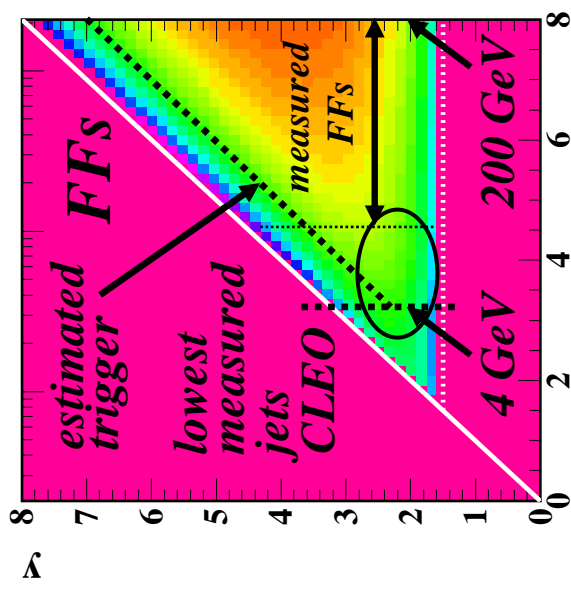
soft components

compare with

unbiased jet structure

hep-ph/0606249

measured FFs – 2006



dijet energy

$$y_{max} \approx \ln(2E_{parton}/m_T)$$

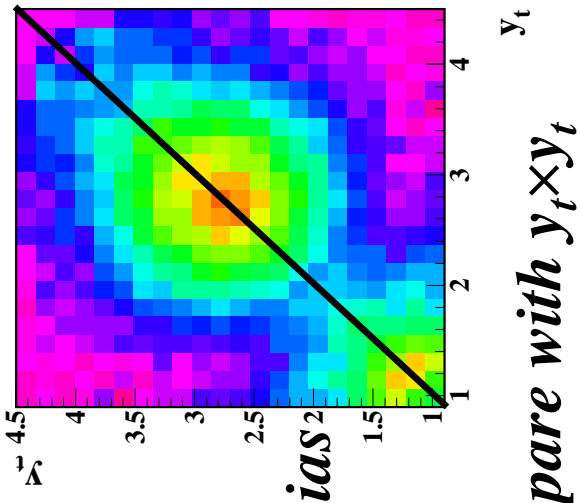
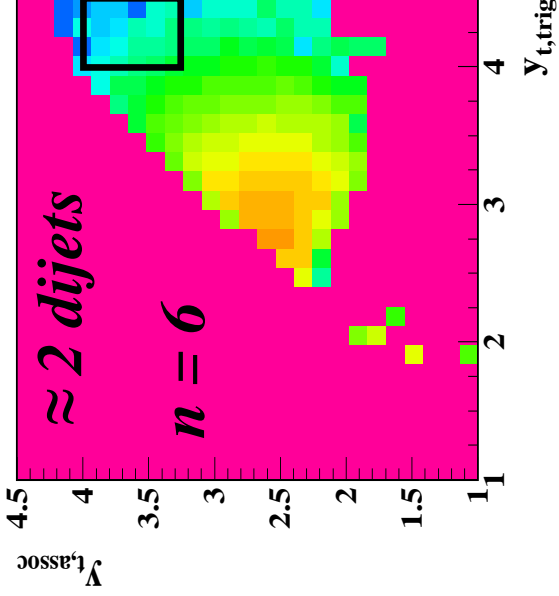
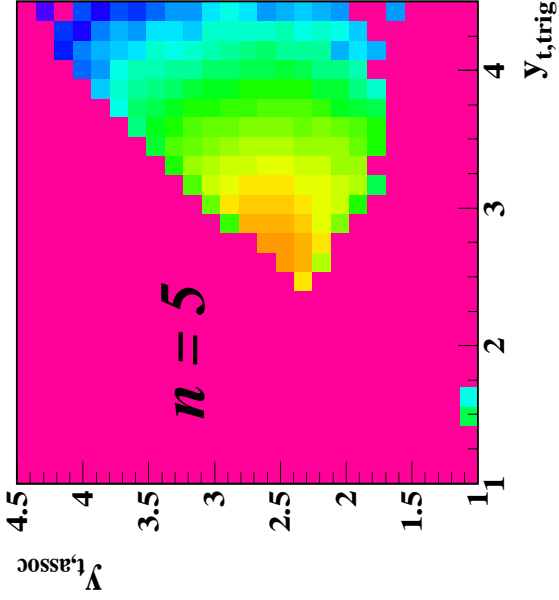
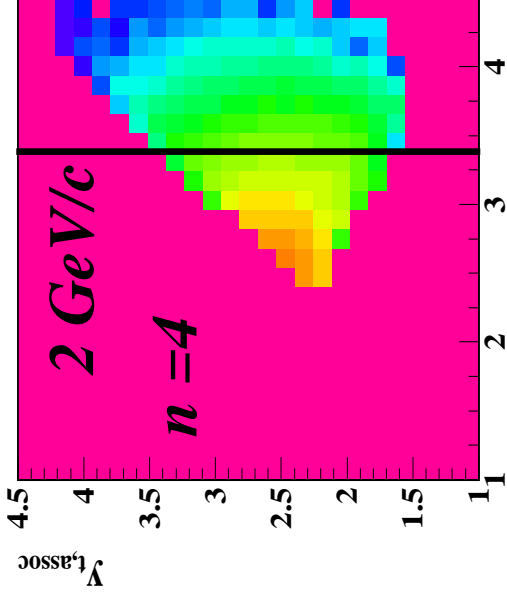
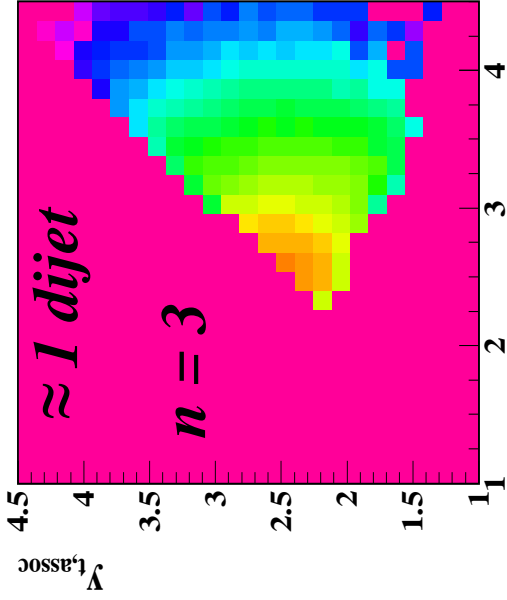
8

arXiv:1310.0408

Hard Component of $F \equiv TA$

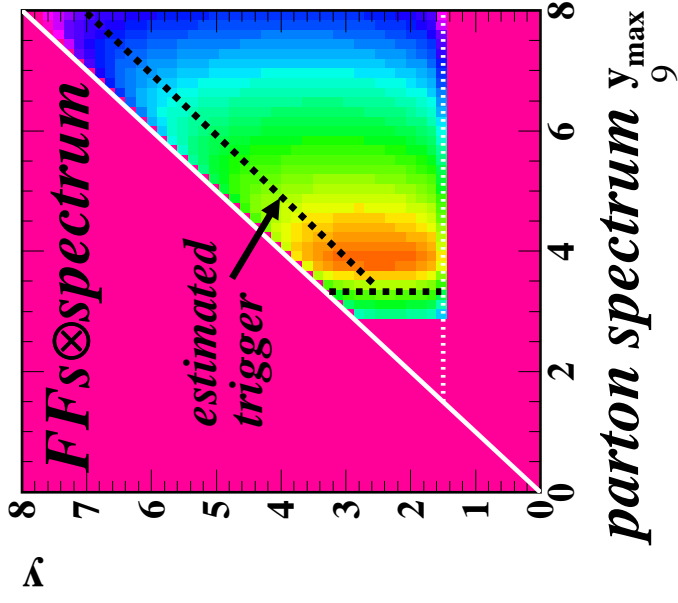
actual minbias trigger-associated HC

2004



*compare with $y_t \times y_t$
correlations and...*

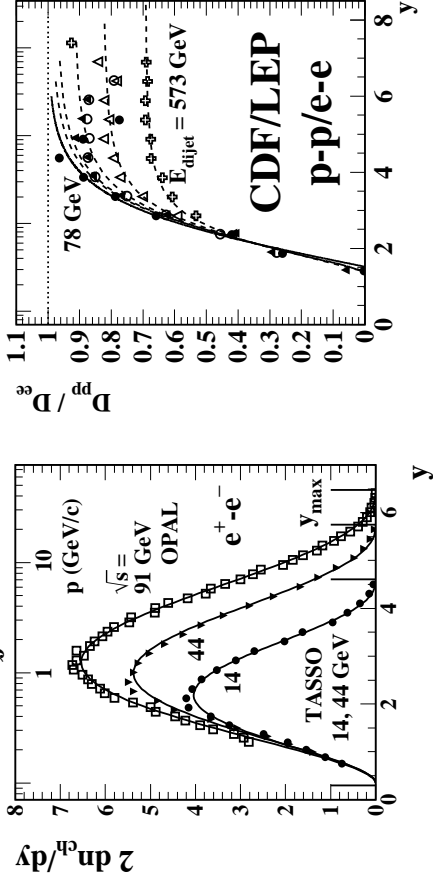
pQCD factorization



parton spectrum $y_{t,max}$

Fragmentation Functions – TA Partition

$2dn_{ch,j}/dy$ arXiv:1407.6422



FFs for given parton and hadron types:

$$D_{\pi}^{\text{f}}(y | y_{\text{max}}) = \ln(2E_{\text{jet}}/m_{\pi})$$

$$S_{\text{t}}(y_{\text{trig}} | y_{\text{max}})$$

trigger fragment from void probability:

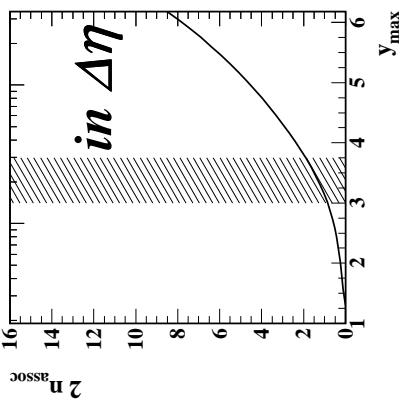
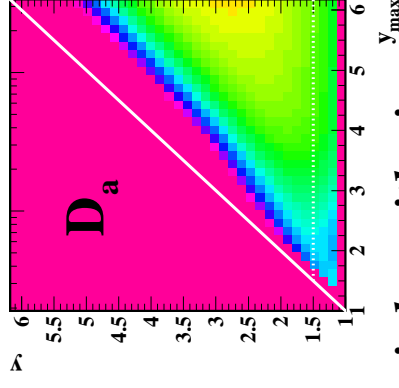
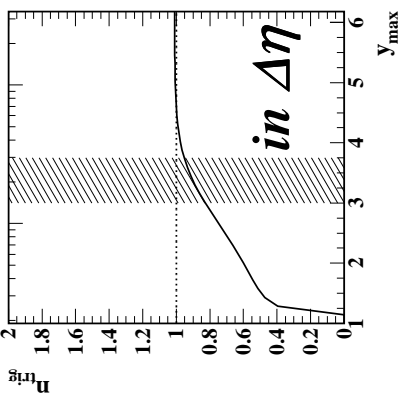
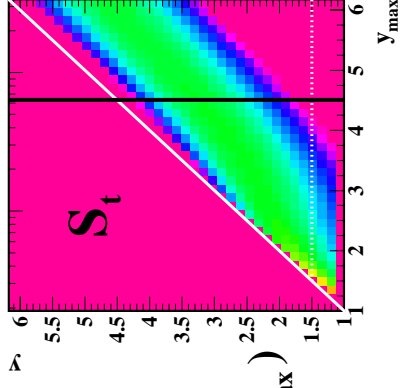
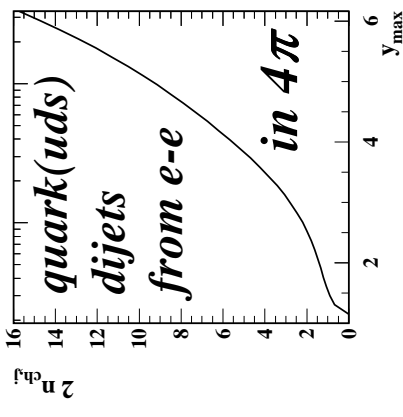
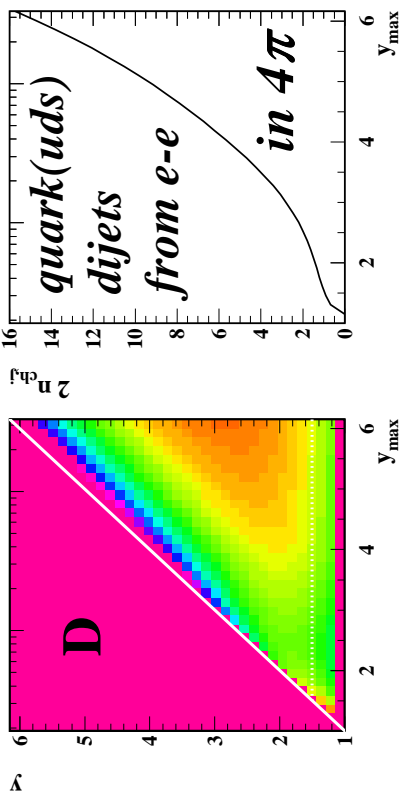
$$S_{\text{t}}(y | y_{\text{max}}) = G(y) \epsilon(\Delta\eta) D(y | y_{\text{max}})$$

complementary associated fragments:

$$D_{\text{a}}(y | y_{\text{max}}) = [1 - G(y)] \epsilon(\Delta\eta) D(y | y_{\text{max}})$$



dijet fraction in $\Delta\eta$

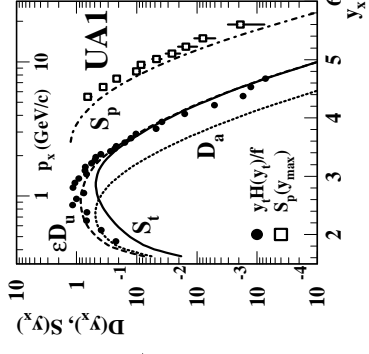
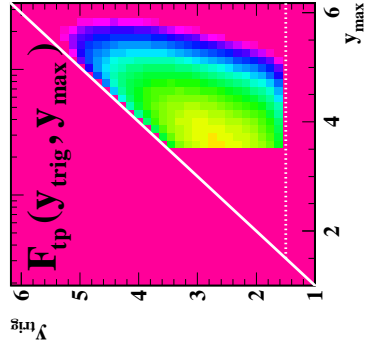


z axis logarithmic

Convolutions and Bayes' Theorem

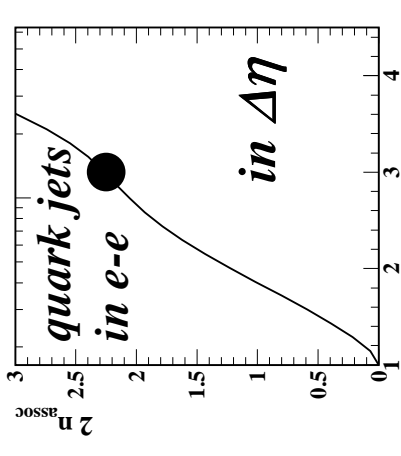
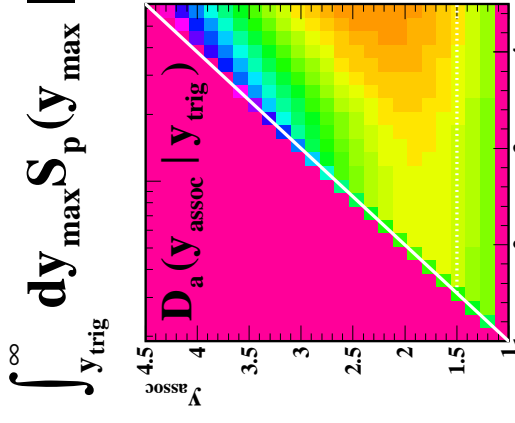
relate parton-fragment FF system to hadron-hadron TA system

$$F_{tp}(y_{trig}, y_{max}) = S_p(y_{max}) S_t(y_{trig} | y_{max})$$



project
onto y_{trig}

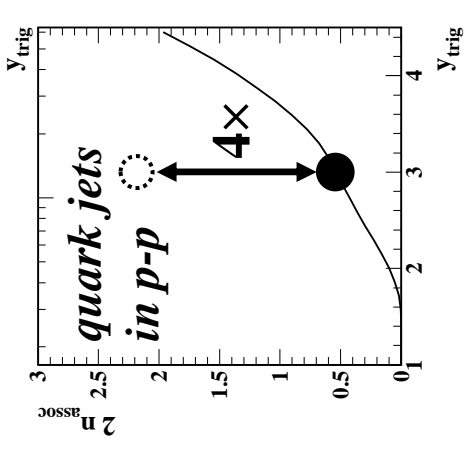
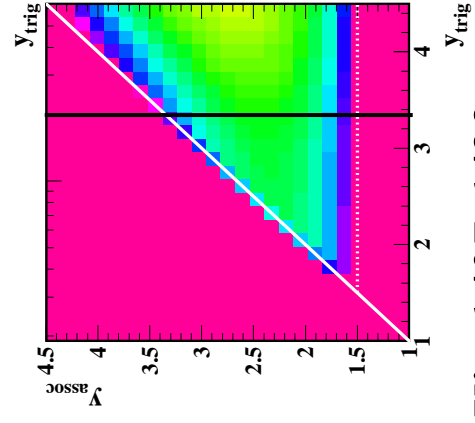
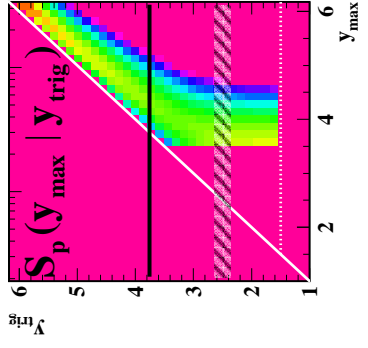
$$D_a(y_{assoc} | y_{trig}) = [\nu_S y_{ta} A_{hh}(y_{ta}/y_{tt})]$$



$$S_t(y_{trig}) = \int_{y_{trig}}^{\infty} dy_{max} S_p(y_{max}) S_t(y_{trig} | y_{max})$$

Bayes' theorem:

$$S_p(y_{max} | y_{trig}) = \frac{S_p(y_{max}) S_t(y_{trig} | y_{max})}{S_t(y_{trig})}$$



Isolating the Triggered Dijet

arXiv:1407.6422

$$R_x = T_x/T$$

$$\text{data } \overrightarrow{PR_h A_{hh}} = A - \overrightarrow{PR_s A_s} - \overrightarrow{PR_h A_{hs}}$$

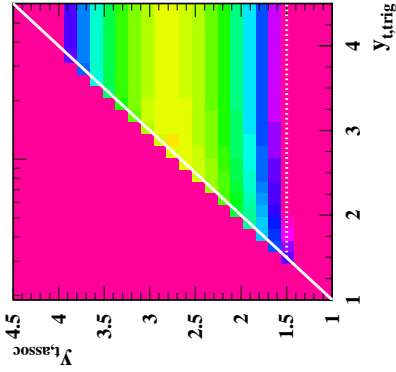
TCM soft components

$$n_j = I + \Delta n_j$$

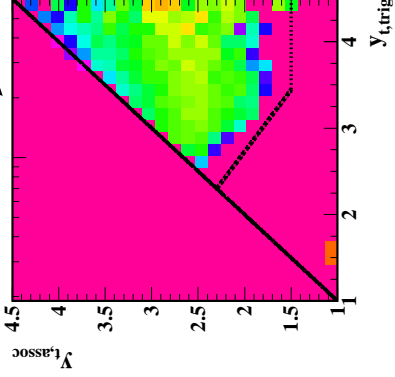
$$\overrightarrow{TA_{hh}} = \overrightarrow{G_{hh} T_{hs} A'_{hh}} + \overrightarrow{G_{hs} T_{hh} (A''_{hh} + A^*_{hh})}$$

untriggered dijets

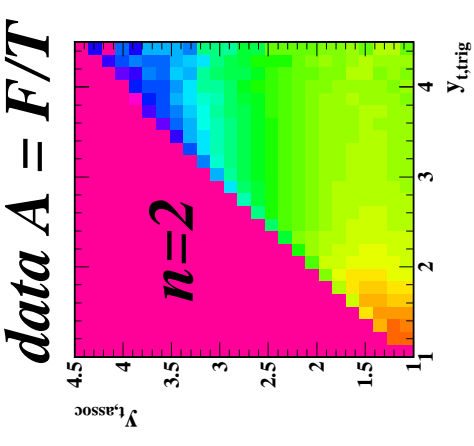
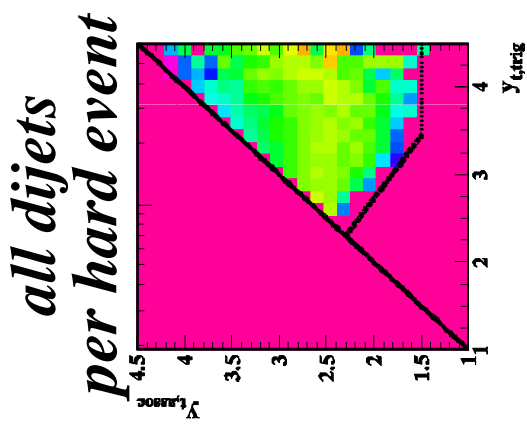
triggered



+



=



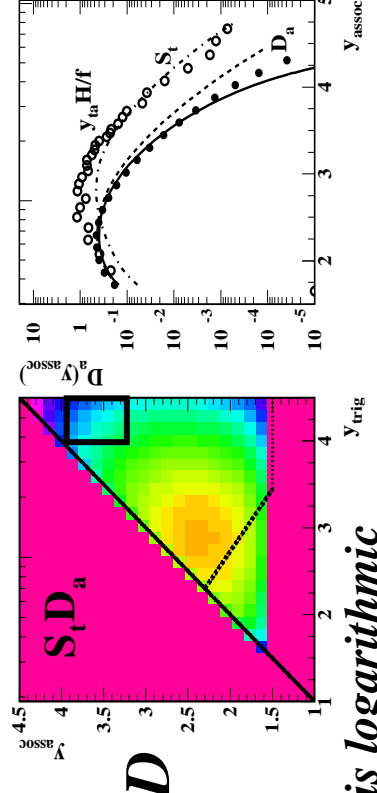
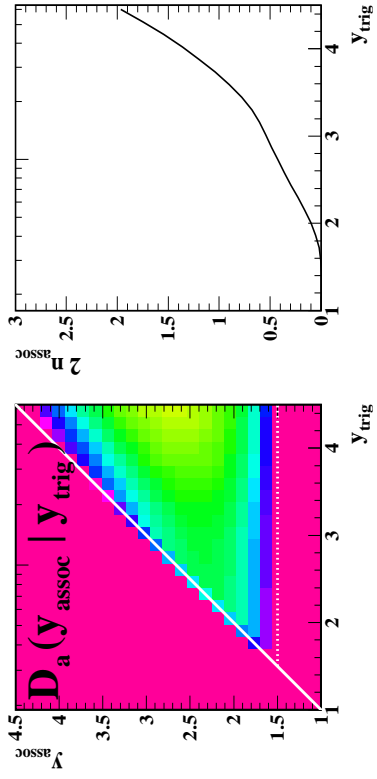
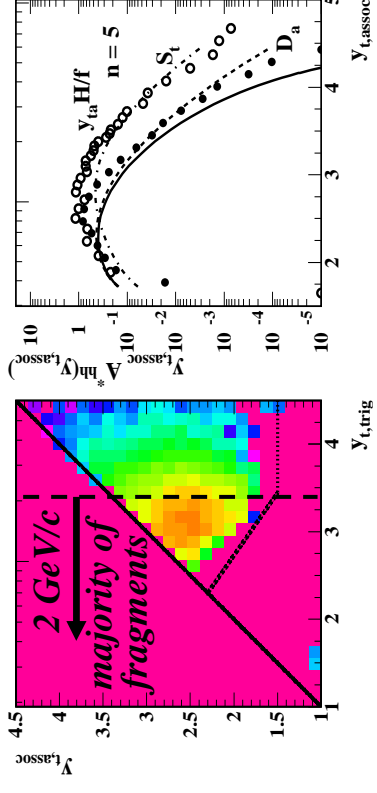
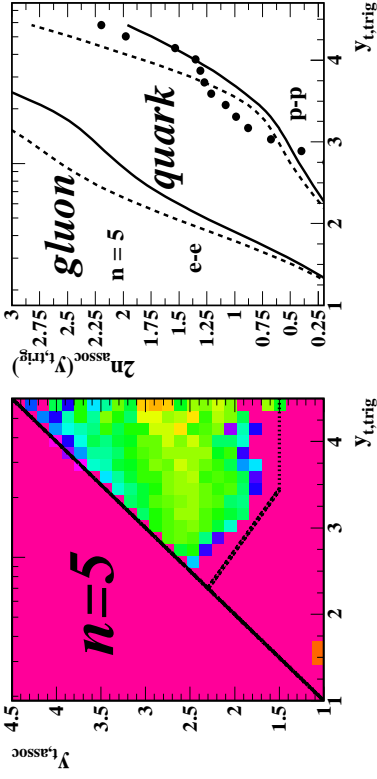
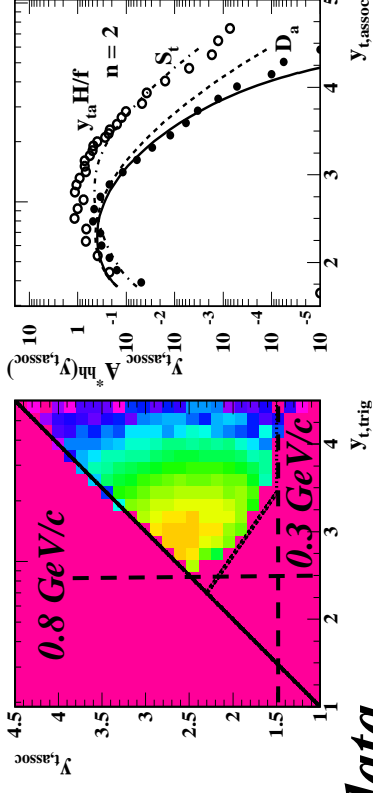
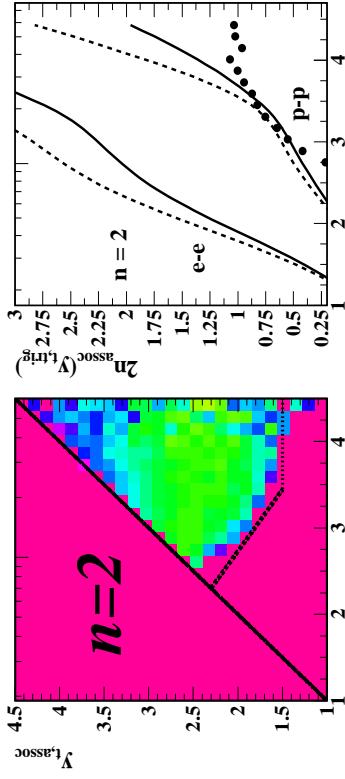
TCM: A'_{hh}, A''_{hh}

*data: A^*_{hh}*

*single triggered dijet
comparable to FFs*

TA Comparisons: FFs vs p-p Data

$$y_{ta} A_{hh}^*(y_{ta} | y_{tt}) \quad y_{ta} F_{hh}^*(y_{ta}, y_{tt}) = T_h(y_{tt}) y_{ta} A_{hh}^*(y_{ta} | y_{tt})$$

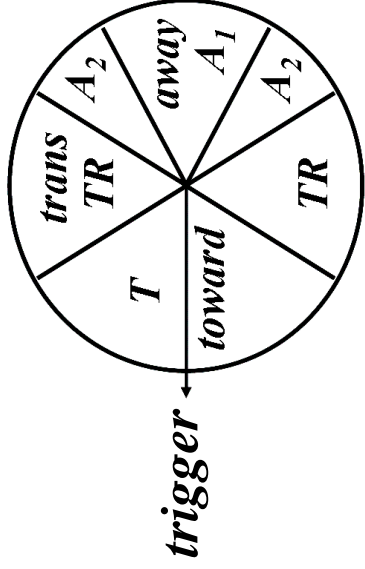


p-p data

pQCD

z axis logarithmic

A = F/T vs Azimuth Intervals

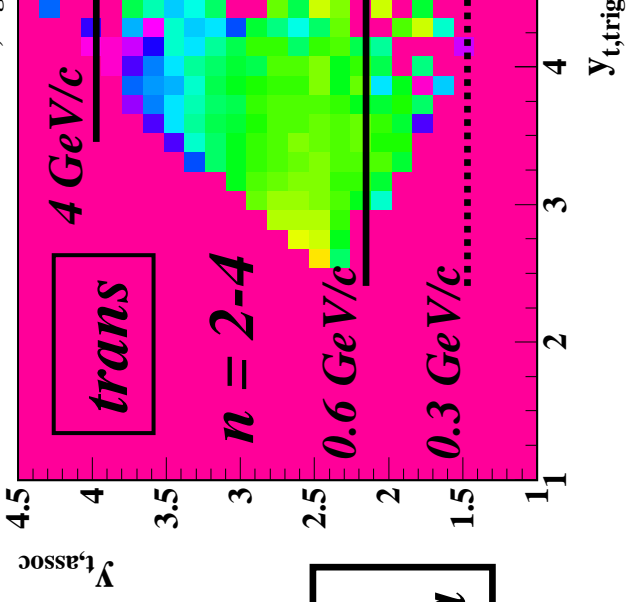
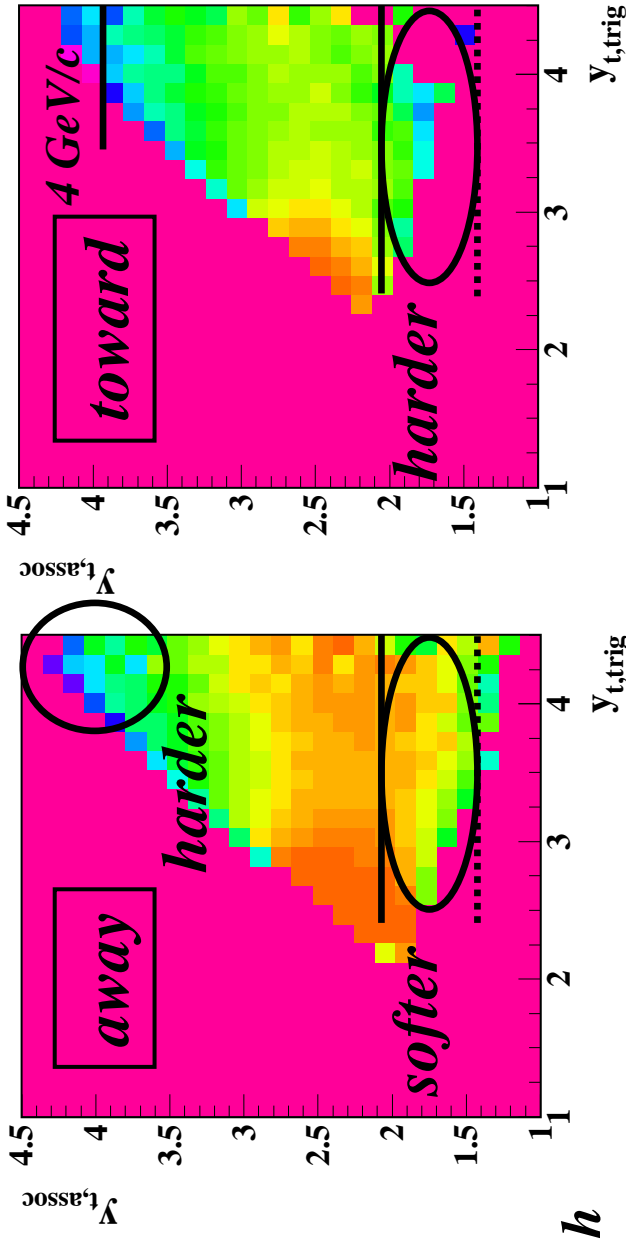


sum three low- n_{ch}

bins: $\underline{MPI < 15\%}$

$\Delta n_j < 0.15$

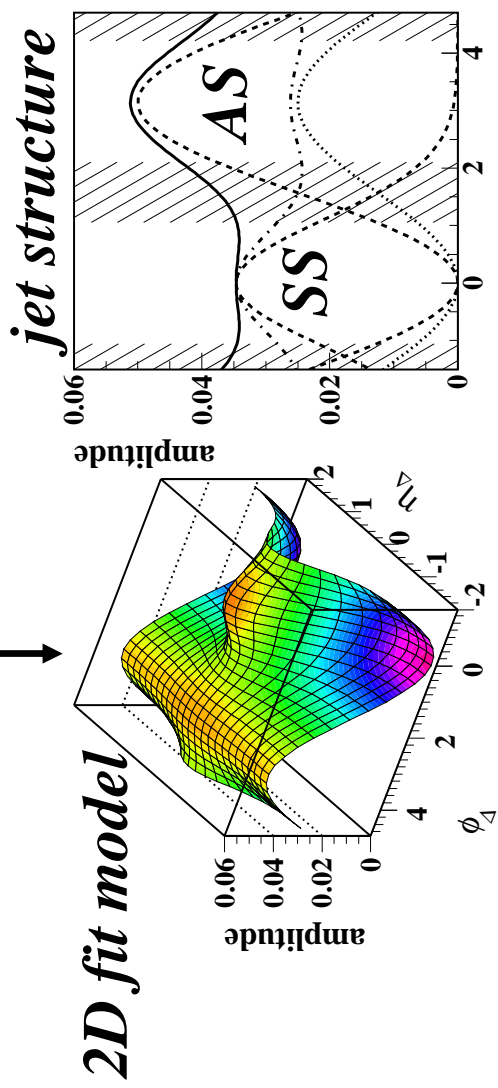
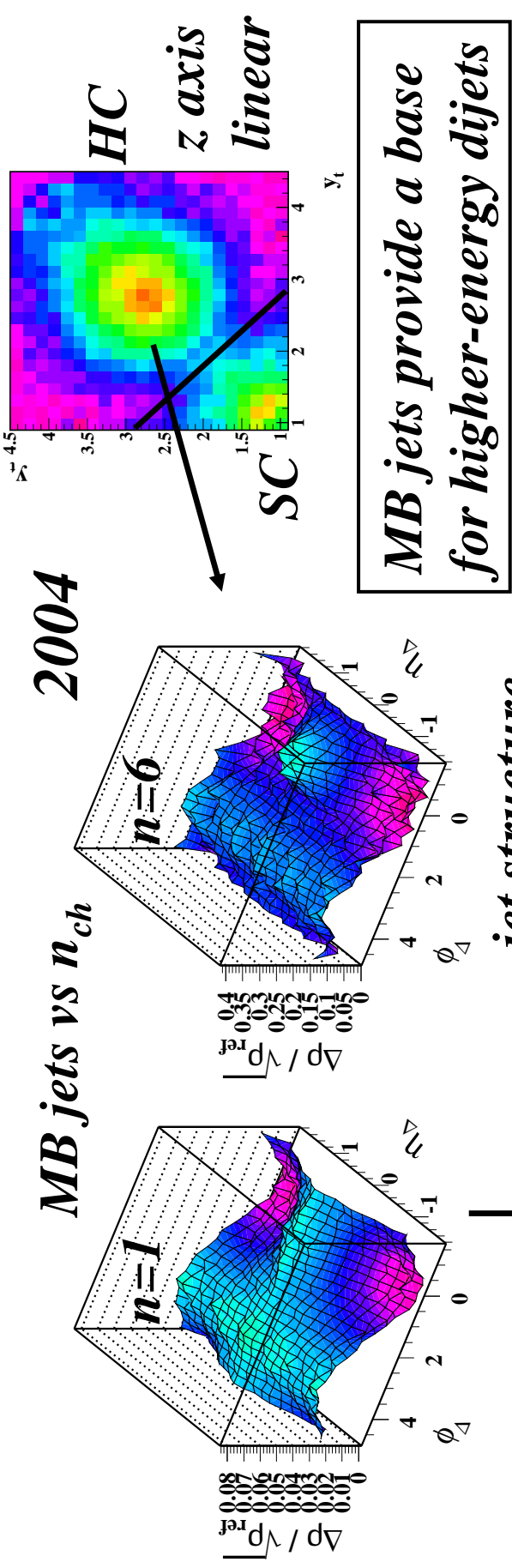
*UE MPI conjecture
inconsistent with data*



*jets in TR,
part of
triggered dijet*

arXiv:1310.0408

Dijet Structure in the “Trans” Region



\longleftrightarrow **TR = “trans”**, ϕ_{Δ}

*relative to MB jets:
for higher jet energies
hadrons added nearer
to the jet axis do not
contribute to the TR*

substantial overlap: same-side SS vs away-side AS

Summary

- *Define TCM for 1D T (trigger spectrum), 2D F = TA*
- *Hard components of F, A → MB dijets*
- *Distinguish single triggered dijets, secondaries = MPI*
- *Quantitative link: TA vs FFs + pQCD jet spectrum*
- *Establish kinematic lower bounds on MB dijets*
- *TA data confirm trigger dijet contribution to azimuth TR*
- *MB dijets make a large contribution to p-p, p-A, A-A*