

SoftDrop

Grooming and tagging boosted jets with analytic control

Grégory Soyez

with Andrew Larkoski, Simone Marzani and Jesse thaler, arXiv:1402.2657

IPhT, CEA Saclay

ISMD 2014

Everything will be boosted

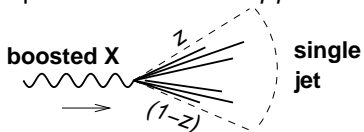
The near and distant futures looks like

- Higher energy
 - Higher luminosity
 - Larger bounds/scales for new physics searches/studies
- ⇒ particles at larger scales (p_t), *i.e.* boosted

This requires new approaches to final-state analyses
Especially for the hadronic final-state

What is special about boosted objects?

Example: boosted $X \rightarrow q\bar{q}$

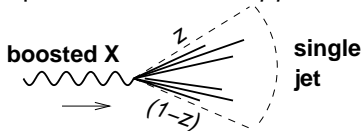


$$\Delta R_{q\bar{q}} \approx \frac{m}{\sqrt{z(1-z)}p_t} \sim \frac{2m}{p_t}$$

\Rightarrow single jet for $p_t \gg m$

What is special about boosted objects?

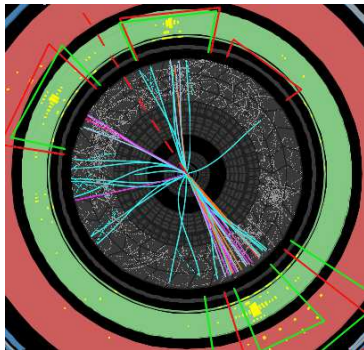
Example: boosted $X \rightarrow q\bar{q}$



$$\Delta R_{q\bar{q}} \approx \frac{m}{\sqrt{z(1-z)}p_t} \sim \frac{2m}{p_t}$$

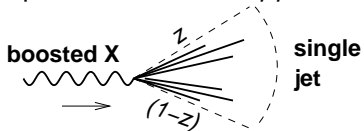
\Rightarrow single jet for $p_t \gg m$

What jet do we have here?



What is special about boosted objects?

Example: boosted $X \rightarrow q\bar{q}$

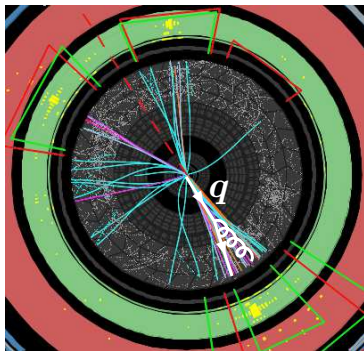


$$\Delta R_{q\bar{q}} \approx \frac{m}{\sqrt{z(1-z)}p_t} \sim \frac{2m}{p_t}$$

\Rightarrow single jet for $p_t \gg m$

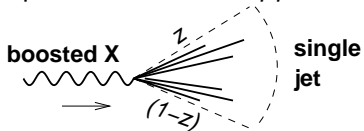
What jet do we have here?

- a quark?



What is special about boosted objects?

Example: boosted $X \rightarrow q\bar{q}$

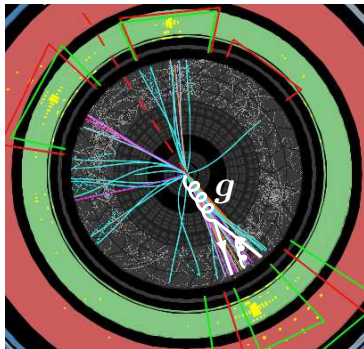


$$\Delta R_{q\bar{q}} \approx \frac{m}{\sqrt{z(1-z)}p_t} \sim \frac{2m}{p_t}$$

\Rightarrow single jet for $p_t \gg m$

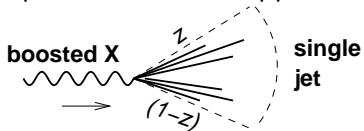
What jet do we have here?

- a quark?
- a gluon?



What is special about boosted objects?

Example: boosted $X \rightarrow q\bar{q}$

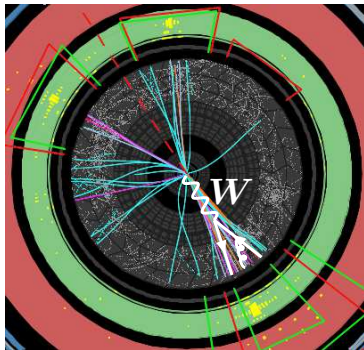


$$\Delta R_{q\bar{q}} \approx \frac{m}{\sqrt{z(1-z)}p_t} \sim \frac{2m}{p_t}$$

\Rightarrow single jet for $p_t \gg m$

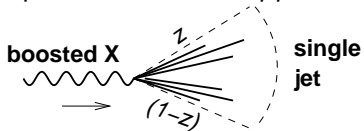
What jet do we have here?

- a quark?
- a gluon?
- a W/Z (or a Higgs)?



What is special about boosted objects?

Example: boosted $X \rightarrow q\bar{q}$

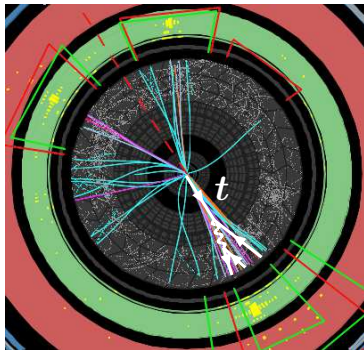


$$\Delta R_{q\bar{q}} \approx \frac{m}{\sqrt{z(1-z)}p_t} \sim \frac{2m}{p_t}$$

\Rightarrow single jet for $p_t \gg m$

What jet do we have here?

- a quark?
- a gluon?
- a W/Z (or a Higgs)?
- a top quark?



Paradigm and frequent tools

- one typically work with **fat jets**, *i.e.* jet with large radius
- **grooming**: removing soft radiation
Idea: QCD collimated \Rightarrow get rid of soft and large-angle radiation
Examples: trimming, pruning, ...
- **tagging**: disentangling signal (*e.g.* W) from backgrounds (QCD jets)
Idea: signal (*resp.* QCD) generates multi-core (*resp.* single-core) jets
Examples: MassDropTagger, John Hopking tagger, N -subjettiness, ...

Paradigm and frequent tools

- one typically work with **fat jets**, *i.e.* jet with large radius
- **grooming**: removing soft radiation
Idea: QCD collimated \Rightarrow get rid of soft and large-angle radiation
Examples: trimming, pruning, ...
- **tagging**: disentangling signal (*e.g.* W) from backgrounds (QCD jets)
Idea: signal (*resp.* QCD) generates multi-core (*resp.* single-core) jets
Examples: MassDropTagger, John Hopking tagger, N -subjettiness, ...

This talk: Soft Drop

a new tool: both a tagger and a groomer with analytic control

- Start with a given jet
- Re-cluster it with the Cambridge/Aachen algorithm ($d_{ij} = \Delta R_{ij}^2$)
- Recursively undo the last step of the clustering $j \rightarrow j_1 + j_2$
- if the **splitting is symmetric** enough stop (j is the result)

$$\frac{\min(p_{t1}, p_{t2})}{p_{t1} + p_{t2}} > z_{\text{cut}} \left(\frac{\Delta R_{12}}{R} \right)^\beta$$

- otherwise, repeat with the hardest of j_1 and j_2

- Start with a given jet
- Re-cluster it with the Cambridge/Aachen algorithm ($d_{ij} = \Delta R_{ij}^2$)
- Recursively undo the last step of the clustering $j \rightarrow j_1 + j_2$
- if the **splitting is symmetric** enough stop (j is the result)

$$\frac{\min(p_{t1}, p_{t2})}{p_{t1} + p_{t2}} > z_{\text{cut}} \left(\frac{\Delta R_{12}}{R} \right)^\beta$$

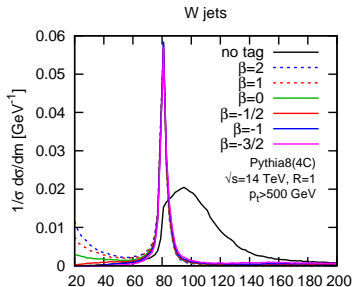
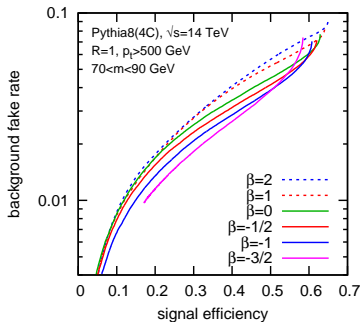
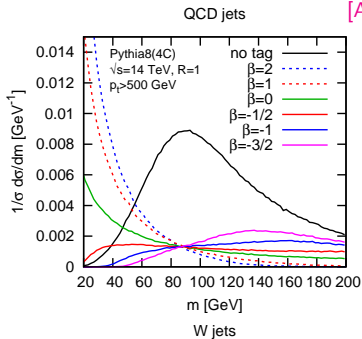
- otherwise, repeat with the hardest of j_1 and j_2

Notes

- β and z_{cut} are the two adjustable parameters
- $\beta = 0$ first introduced as the “modified Mass-Drop Tagger (mMDT)” by **M. Dasgupta, A. Fregoso, S. Marzani and G. Salam**

Performance as a tagger

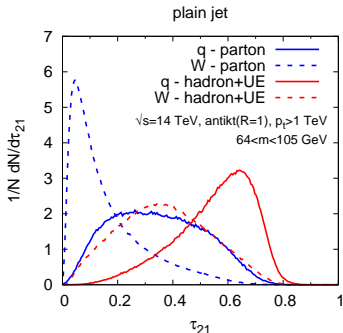
[A.Larkoski, S.Marzani, GS, J.Thaler, arXiv:1402.2657]



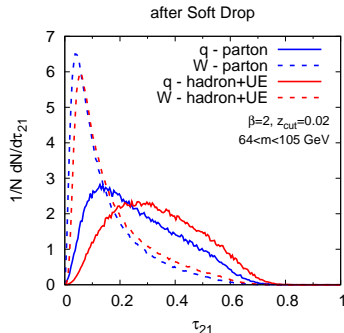
- W peak nicely reconstructed
- QCD background killed
- $\beta \leq 0$ works best

[M.Dasgupta, GS, G.Salam, arXiv:1402.2657]

Example: N -subjettiness distribution ($\tau_{21} \equiv$ tendency to have 2 prongs)



- discriminate between W (dashed) and QCD (solid)
- strongly affected by non-perturbative physics



- discriminate between W (dashed) and QCD (solid)
- non-perturbative effects largely reduced

Analytic properties

Crucial to understand the physics beyond Monte-Carlo simulations

Analytic properties

For a generic jet observable v (e.g. the jet mass)

$$P(< v) \equiv \Sigma(v) = \exp[-g_1(\alpha_s L)L - g_2(\alpha_s L) - \dots]$$

- $L = \log(1/v)$: log-enhanced terms need be **resummed** at all orders

Analytic properties

For a generic jet observable v (e.g. the jet mass)

$$P(< v) \equiv \Sigma(v) = \exp[-g_1(\alpha_s L)L - g_2(\alpha_s L) - \dots]$$

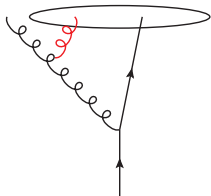
- $L = \log(1/v)$: log-enhanced terms need be **resummed** at all orders
- **Leading-log (LL)**: $g_1 = \alpha_s L^2 + \dots$
Typically a double logarithm (one collinear, one soft)

Analytic properties

For a generic jet observable v (e.g. the jet mass)

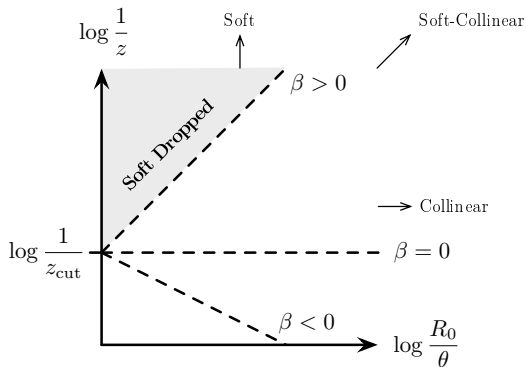
$$P(< v) \equiv \Sigma(v) = \exp[-g_1(\alpha_s L)L - g_2(\alpha_s L) - \dots]$$

- $L = \log(1/v)$: log-enhanced terms need be **resummed** at all orders
- **Leading-log (LL)**: $g_1 = \alpha_s L^2 + \dots$
Typically a double logarithm (one collinear, one soft)
- **Next-to-leading log (NLL)**: $g_2 = \alpha_s L + \dots$
 - contributions from hard collinear splittings ($\alpha_s L + \dots$)
 - contributions from multiple emissions ($\alpha_s^2 L^2 + \dots$)
 - running-coupling corrections
 - **potential non-global logarithms (nasty!)**



Phase-space for emissions (Leading-log \Rightarrow ordered emissions) :

SoftDrop cuts
soft-and-large-angle emissions



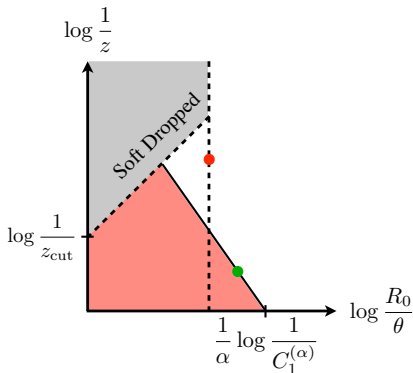
Analytic properties

Phase-space for emissions (Leading-log \Rightarrow ordered emissions) :

Sudakov: ($\rho = m^2/(p_t R)^2 < z_{\text{cut}}$)

$$\Sigma(m) = \exp \left[- \frac{\alpha_s C_F}{2\pi} \left(\frac{\beta}{2+\beta} \log^2(1/\rho) + \frac{4}{2+\beta} \log(1/\rho) \log(1/z_{\text{cut}}) - \frac{2}{2+\beta} \log^2(1/z_{\text{cut}}) \right) \right]$$

- double log in $\rho = m^2/(p_t R)^2$
- single-log for $\beta = 0$ (mMDT)



Analytic properties

- With running coupling, **hard-collinear splittings** and **multiple emissions**

$$\Sigma(m) = \frac{e^{-R(\rho) - \gamma_E R'(\rho)}}{\Gamma(1 + R'(\rho))}$$

$$R(\rho) = \frac{C_i}{2\pi\alpha_s\beta_0^2} \left[-\frac{W(1 - \lambda_c)}{1 + \beta} - \frac{\alpha W(1 - \frac{1}{\alpha}\lambda)}{\alpha - 1} - 2\alpha_s\beta_0 B_i \log(1 - \frac{1}{\alpha}\lambda) \right. \\ \left. + \frac{\alpha + \beta}{(\alpha - 1)(1 + \beta)} W\left(1 - \frac{1 + \beta}{\alpha + \beta}\lambda - \frac{\alpha - 1}{\alpha + \beta}\lambda_c\right) \right]$$

$$R'(\rho) = -\partial_{\log(\rho)} R(\rho) \quad W(x) = x \log(x) \quad \lambda_X = 2\alpha_s\beta_0 \log(1/X)$$

Analytic properties

- With running coupling, **hard-collinear splittings** and **multiple emissions**

$$\Sigma(m) = \frac{e^{-R(\rho) - \gamma_E R'(\rho)}}{\Gamma(1 + R'(\rho))}$$

$$R(\rho) = \frac{C_i}{2\pi\alpha_s\beta_0^2} \left[-\frac{W(1 - \lambda_c)}{1 + \beta} - \frac{\alpha W(1 - \frac{1}{\alpha}\lambda)}{\alpha - 1} - 2\alpha_s\beta_0 B_i \log(1 - \frac{1}{\alpha}\lambda) \right. \\ \left. + \frac{\alpha + \beta}{(\alpha - 1)(1 + \beta)} W\left(1 - \frac{1 + \beta}{\alpha + \beta}\lambda - \frac{\alpha - 1}{\alpha + \beta}\lambda_c\right) \right]$$

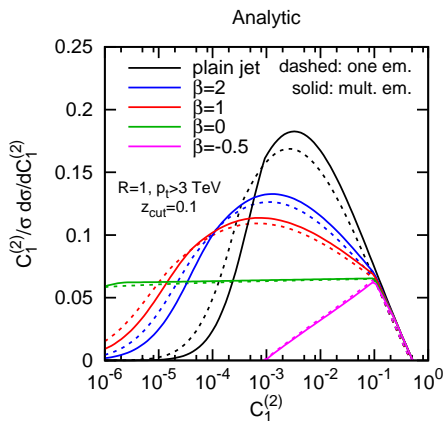
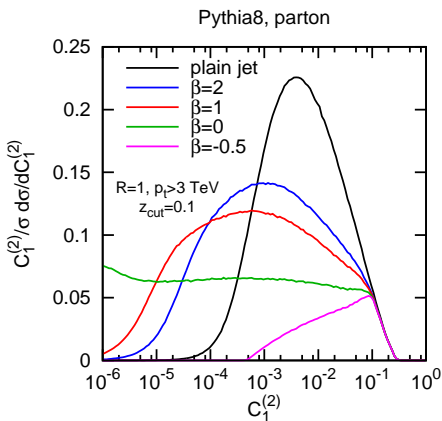
$$R'(\rho) = -\partial_{\log(\rho)} R(\rho) \quad W(x) = x \log(x) \quad \lambda_X = 2\alpha_s\beta_0 \log(1/X)$$

- Non-global logs are **power-suppressed** and **absent for mMDT** ($\beta = 0$)

$$\lim_{\rho \rightarrow 0} \frac{\rho}{\sigma} \frac{d\sigma^{\text{NG}}}{d\rho} = 4C_F C_A \left(\frac{\alpha_s}{2\pi}\right)^2 \frac{\beta}{2 + \beta} \left(\frac{\rho}{z_{\text{cut}}}\right)^{\frac{2}{2 + \beta}} \log(1/\rho)$$

Analytic properties

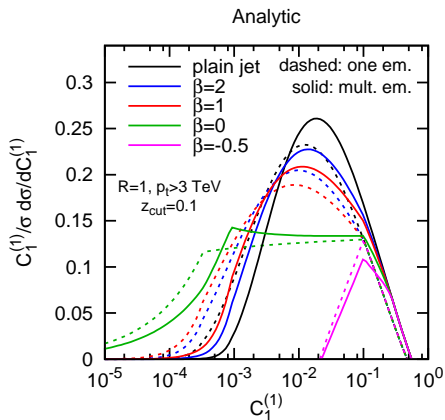
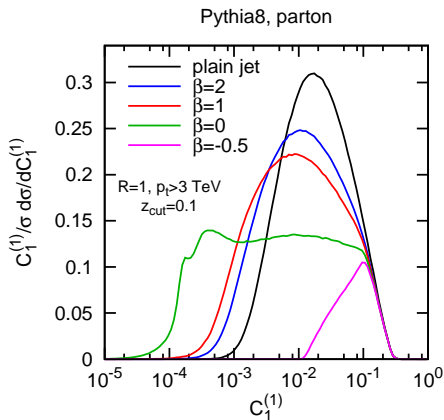
Reproduces what is seen in Monte-Carlo simulations



⇒ we understand the physics and can discuss theoretical uncertainties

Analytic properties

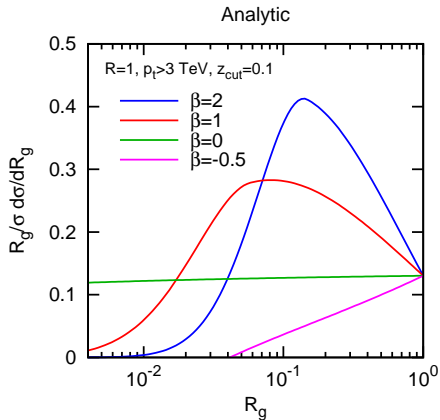
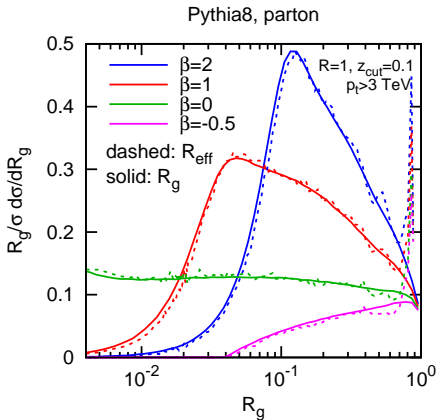
Also computable: [angularities](#)



Helpful e.g. for quark/gluon discrimination?

Analytic properties

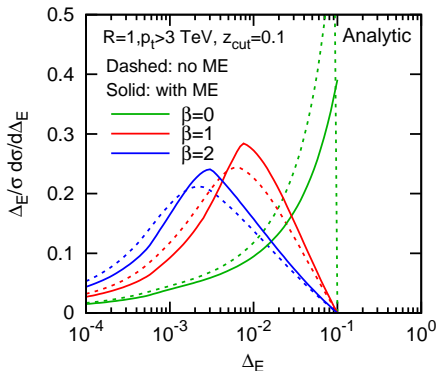
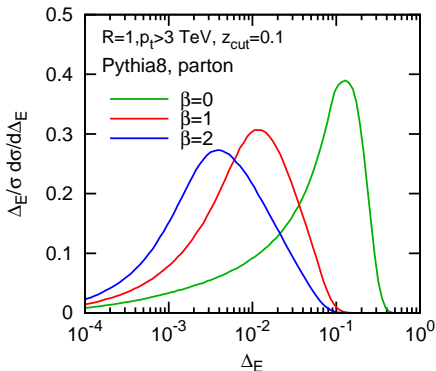
Also computable: angularities, [grooming radius](#)



Helpful e.g. for pileup contamination studies?

Analytic properties

Also computable: angularities, grooming radius and **jet energy loss**



Shows interesting features for future theoretical studies/measurements

Conclusions

Take-home message

Soft Drop combines many great features for modern substructure studies

- good tagging efficiencies
- powerful groomer (reduce poorly-controlled non-perturbative effects)
- shows a good analytic behaviour under control

Conclusions

Take-home message

Soft Drop combines many great features for modern substructure studies

- good tagging efficiencies
- powerful groomer (reduce poorly-controlled non-perturbative effects)
- shows a good analytic behaviour under control

Future prospects

study the phenomenology of Soft-Dropped jets, for example

- predictions with uncertainties for the SoftDrop mass spectrum
- q/g discrimination with Soft-Drop+e.g. angularities
- W tagging with Soft-Drop+e.g. N -subjettiness

Conclusions

Take-home message

Soft Drop combines many great features for modern substructure studies

- good tagging efficiencies
- powerful groomer (reduce poorly-controlled non-perturbative effects)
- shows a good analytic behaviour under control

Future prospects

study the phenomenology of Soft-Dropped jets, for example

- predictions with uncertainties for the SoftDrop mass spectrum
- q/g discrimination with Soft-Drop+e.g. angularities
- W tagging with Soft-Drop+e.g. N -subjettiness

thank you!