

Flow Phenomena in dA and pA at RHIC and LHC

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Goal of Heavy Ion Physics

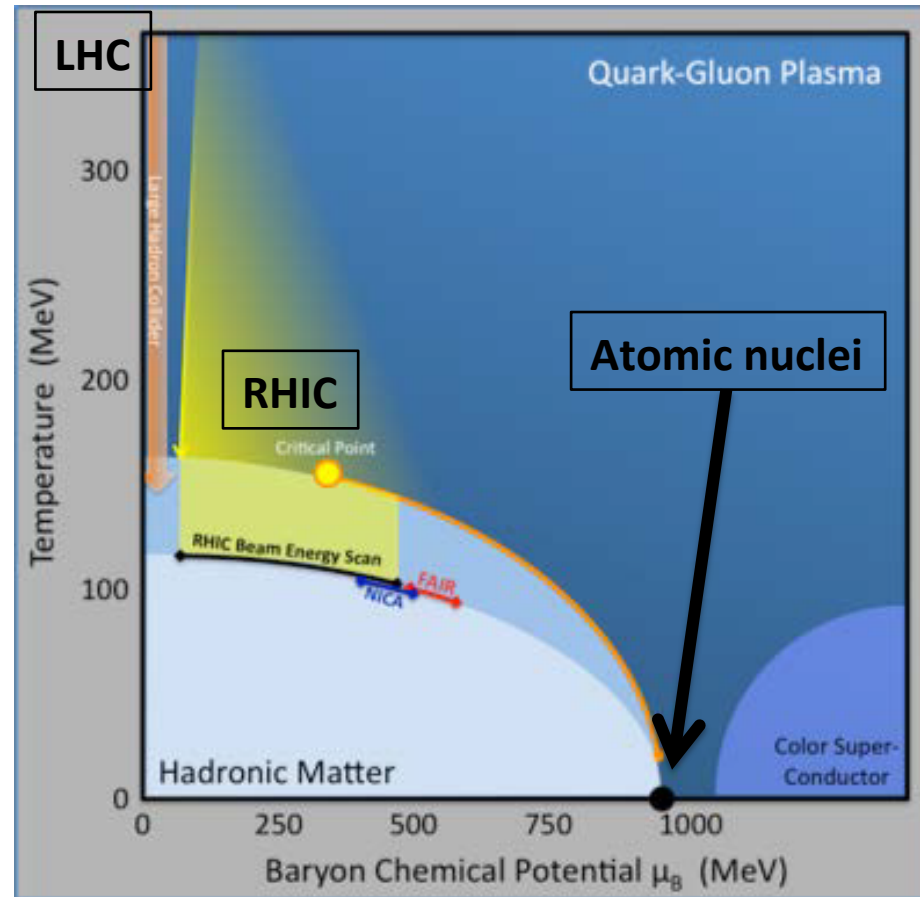
- QGP medium properties
 - Soft probes: collectivity, initial condition, thermal and transport properties (flow etc.)
 - Hard probes: modification of energetic partons, heavy quark bound states (Jet, quarkonium etc.)
 - Use pp and pA/dA as reference

Goal of Heavy Ion Physics

- QGP medium properties
 - Soft probes: collectivity, initial condition, thermal and transport properties (flow etc.)
 - Hard probes: modification of energetic partons, heavy quark bound states (Jet, quarkonium etc.)
 - Use pp and pA/dA as reference
- Why p(d)A collisions?
 - Cold nuclear effect, QGP not formed in small system?
 - 200 GeV dAu at RHIC
 - 5.02 TeV pPb at LHC

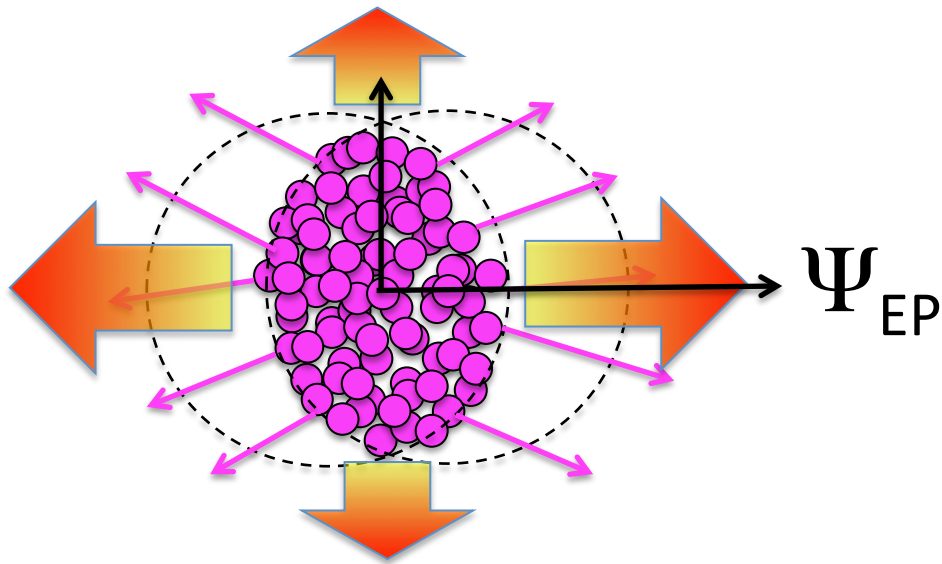
Discoveries of Heavy Ion Physics

- Soft-QCD, the least understood in SM
 - Hot nuclear matter
 - Deconfined and strongly interacting plasma at RHIC/LHC



Discoveries of Heavy Ion Physics

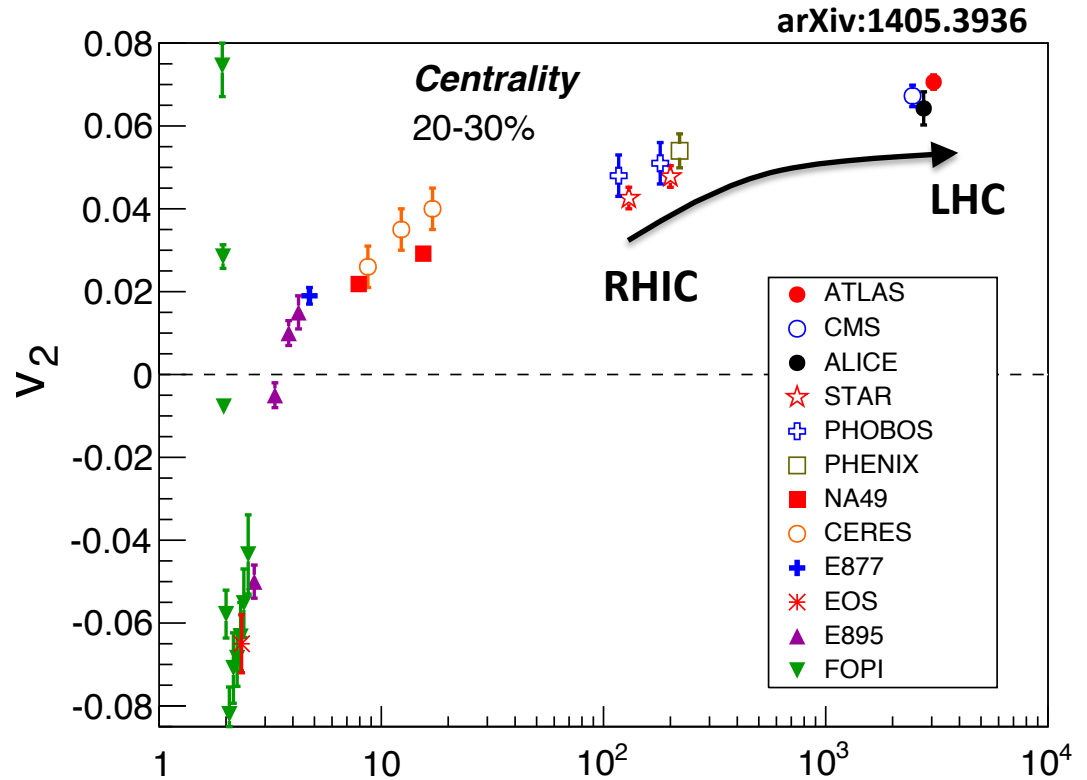
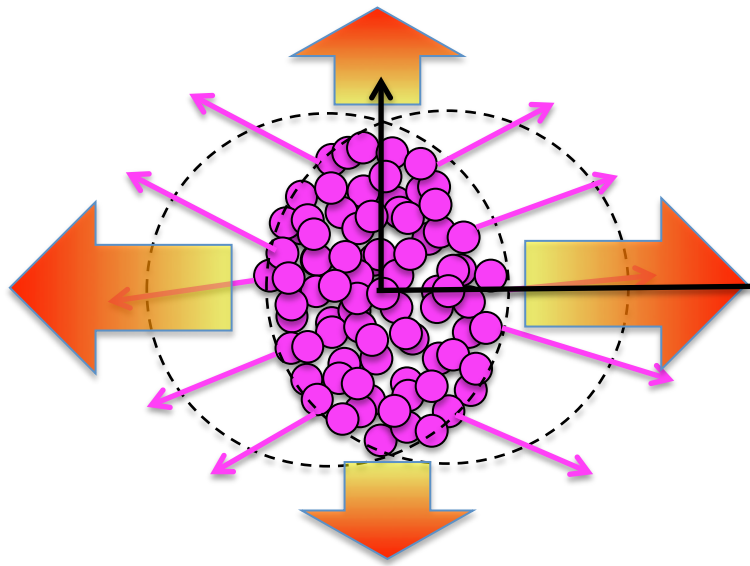
- Anisotropy of initial geometry to final-state particle momentum distribution



$$\frac{dN}{d\phi} \sim 1 + 2v_2 \cos 2(\phi - \psi_2) + 2v_3 \cos 3(\phi - \psi_3) + \dots$$

Discoveries of Heavy Ion Physics

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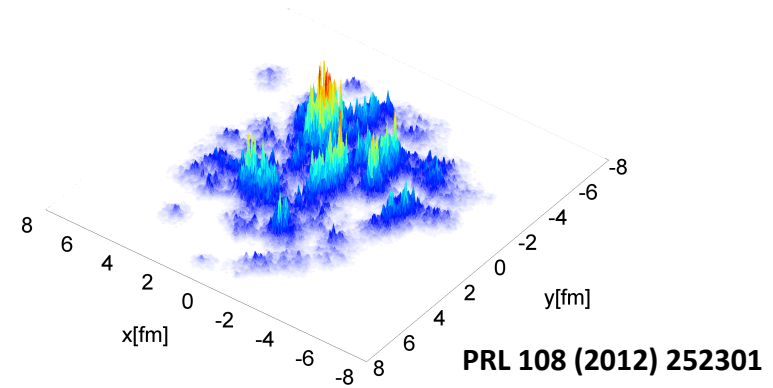


$$\frac{dN}{d\phi} \sim 1 + 2v_2 \cos 2(\phi - \psi_2) + 2v_3 \cos 3(\phi - \psi_3) + \dots \quad \sqrt{s_{NN}} \text{ [GeV]}$$

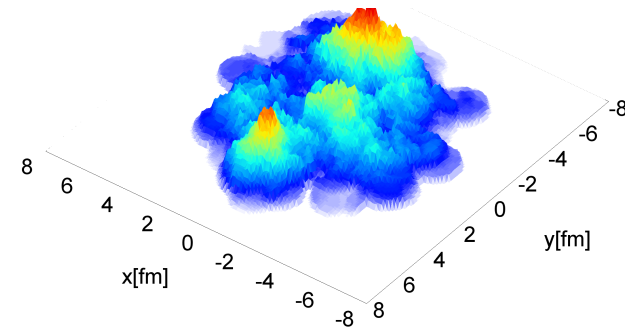
Discoveries of Heavy Ion Physics

- Evolution of the medium
 - Initial Condition
Glauber, CGC

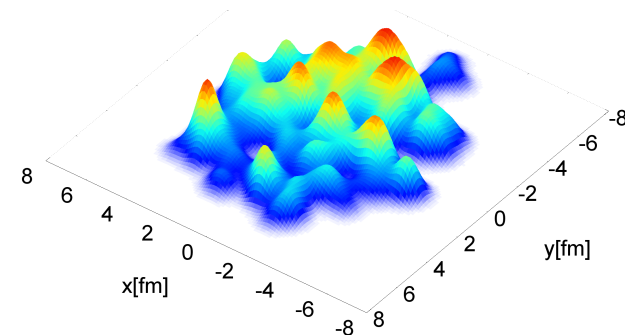
IP-Glasma



MC-KLN



MC-Glauber

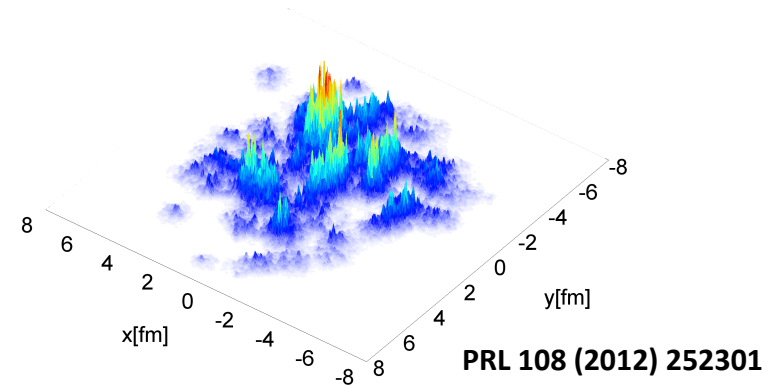


Discoveries of Heavy Ion Physics

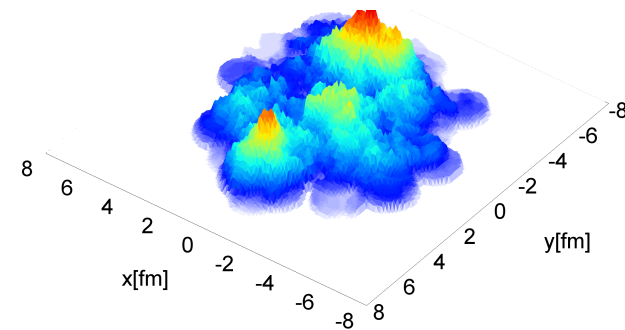
- Evolution of the medium

- Initial Condition
Glauber, CGC
- QGP Phase
 η/s 3+1D Hydrodynamics
- Hadronic Phase
 $\eta/s(T)$
- Freeze-out
Cooper-Frye

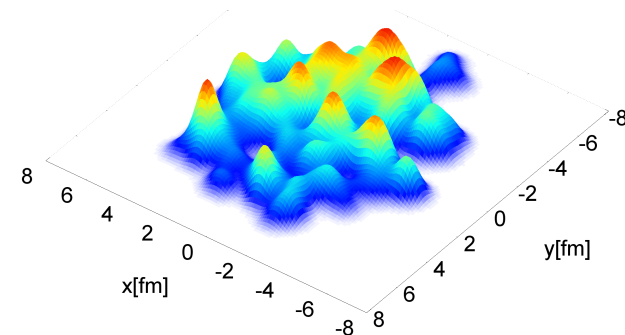
IP-Glasma



MC-KLN



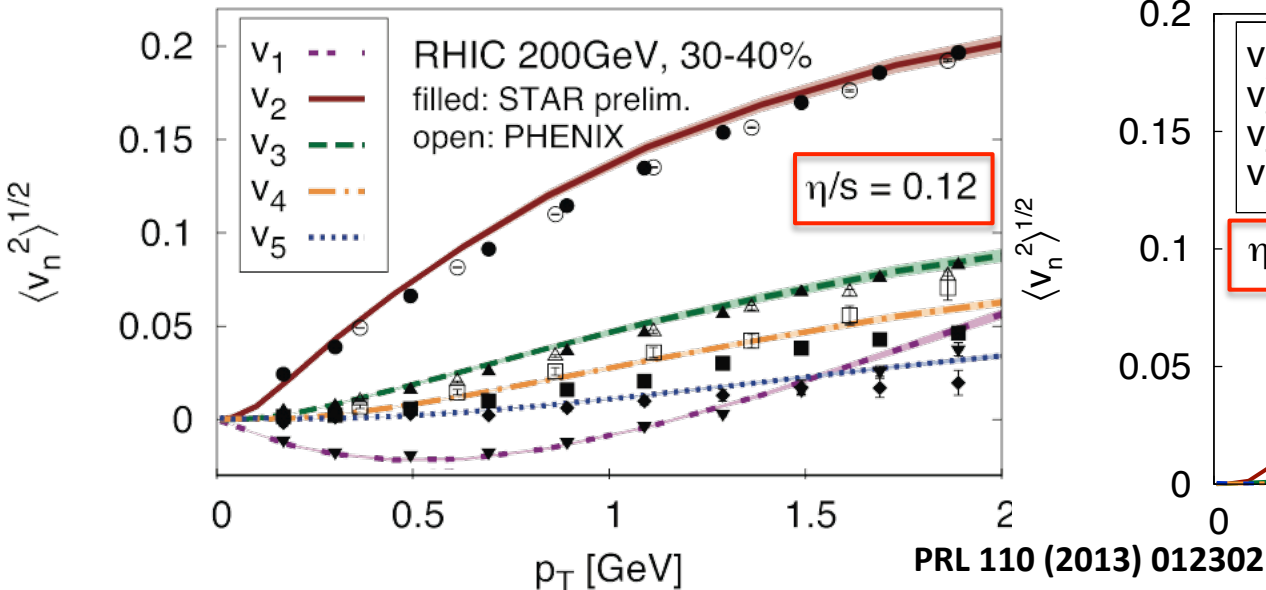
MC-Glauber



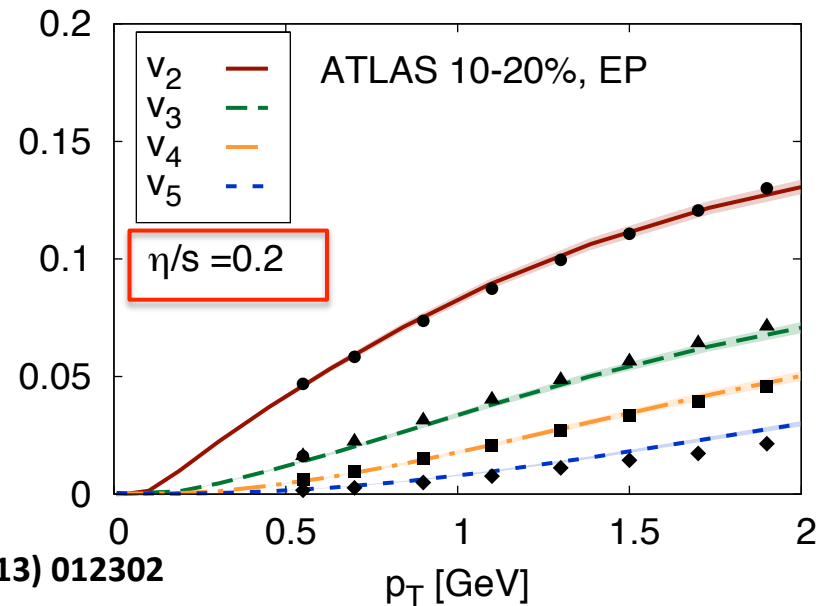
Discoveries of Heavy Ion Physics

- Nearly “perfect” liquid
 - $\eta/s \rightarrow$ Quantum limit $1/4\pi = 0.08$

RHIC AuAu 0.2 TeV



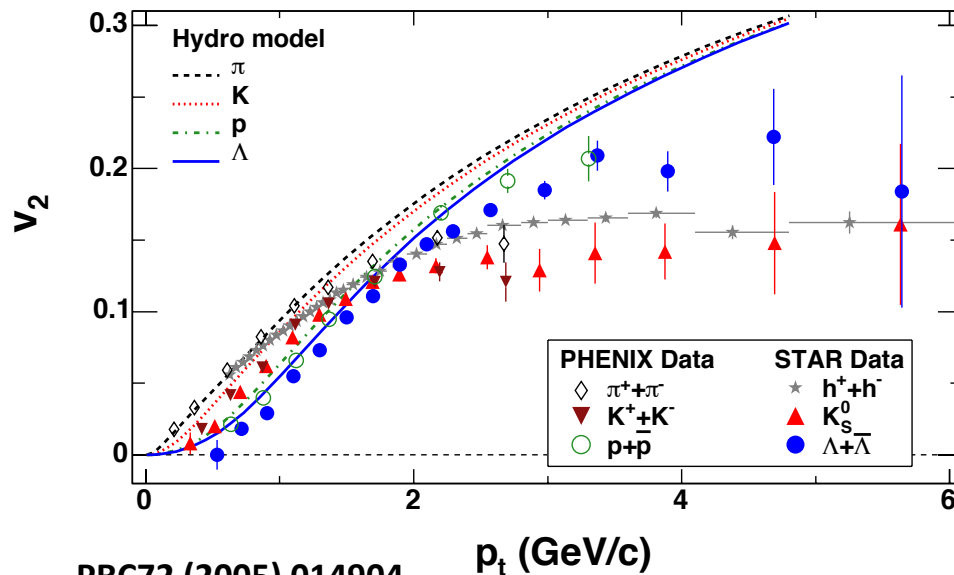
LHC PbPb 2.76 TeV



Discoveries of Heavy Ion Physics

- Mass ordering

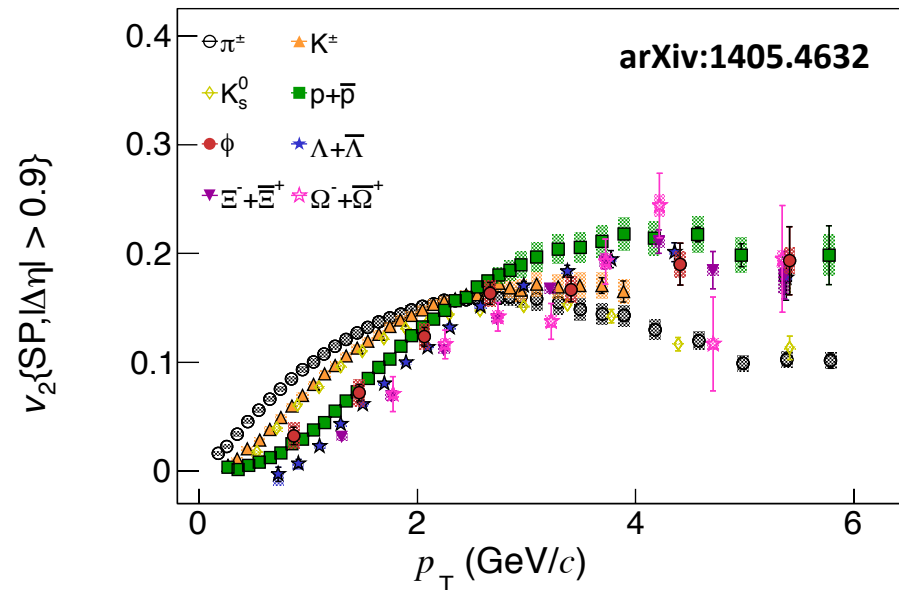
RHIC AuAu 0.2 TeV



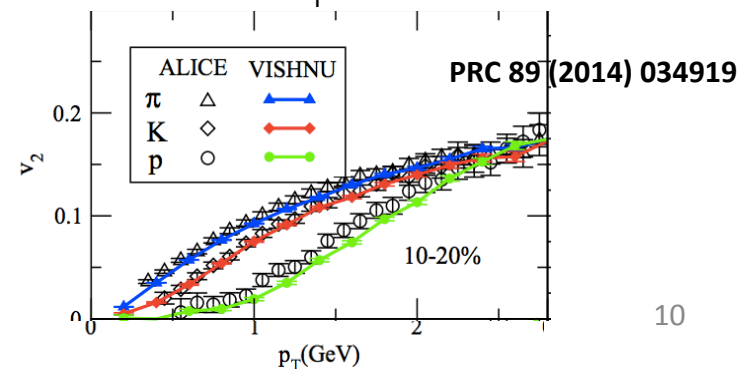
PRC72 (2005) 014904

LHC PbPb 2.76 TeV

ALICE 10-20% Pb-Pb $\sqrt{s_{NN}} = 2.76$ TeV



- Low p_T : light hadron larger v_2
- High p_T : $v_2\{\text{baryon}\} > v_2\{\text{meson}\}$



Why pA(dA) Collisions?

- Need a gauge to calibrate AA collisions
 - Cold nuclear effect
 - 200 GeV dAu at RHIC
 - 5.02 TeV pPb at LHC

Ridge and Angular Correlations

Signal pair distribution:

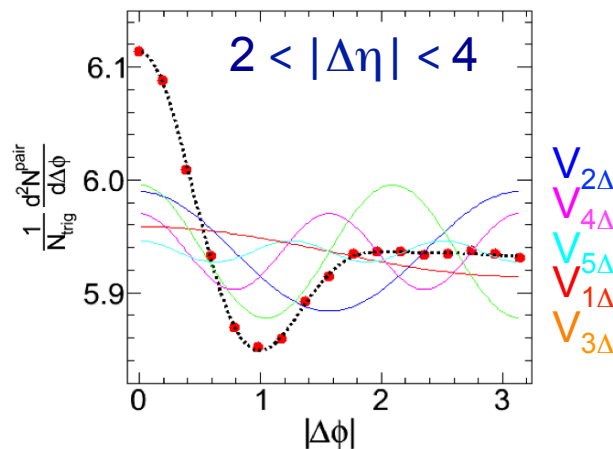
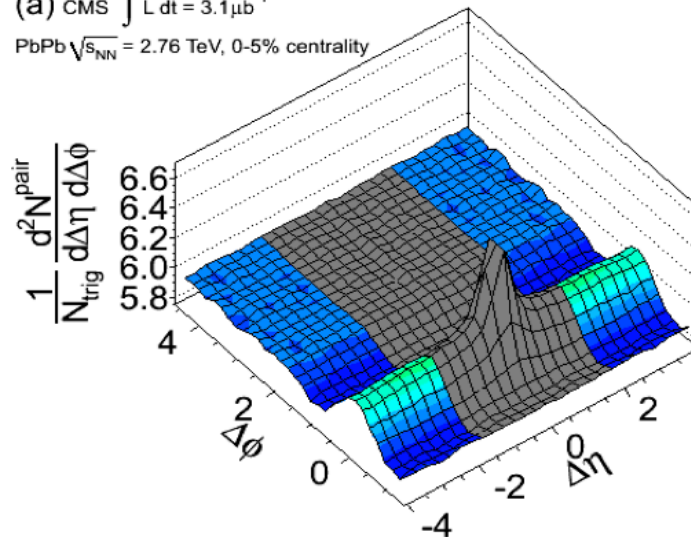
$$S(\Delta\eta, \Delta\phi) = \frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{same}}}{d\Delta\eta d\Delta\phi}$$

Background pair distribution:

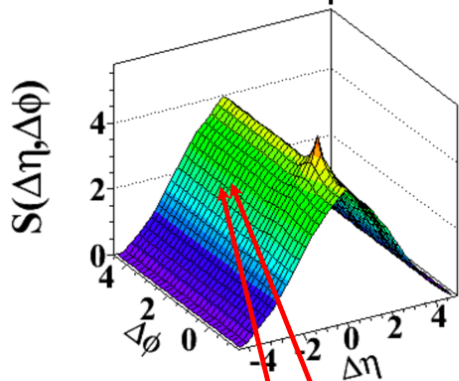
$$B(\Delta\eta, \Delta\phi) = \frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{mix}}}{d\Delta\eta d\Delta\phi}$$

Exclusion region in $\Delta\eta$

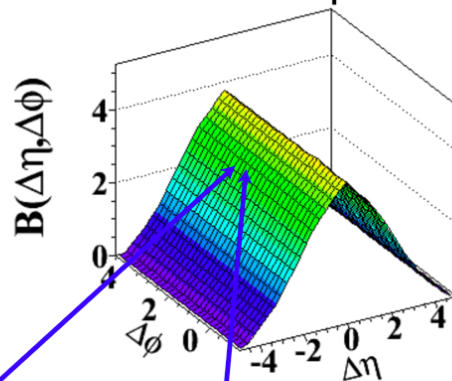
(a) CMS $\int L dt = 3.1 \mu\text{b}^{-1}$
PbPb $\sqrt{s_{\text{NN}}} = 2.76 \text{ TeV}$, 0-5% centrality



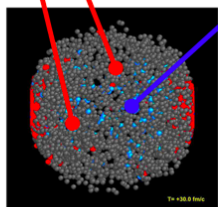
same event pairs



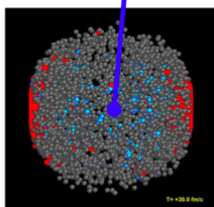
mixed event pairs



Event 1:



Event 2:

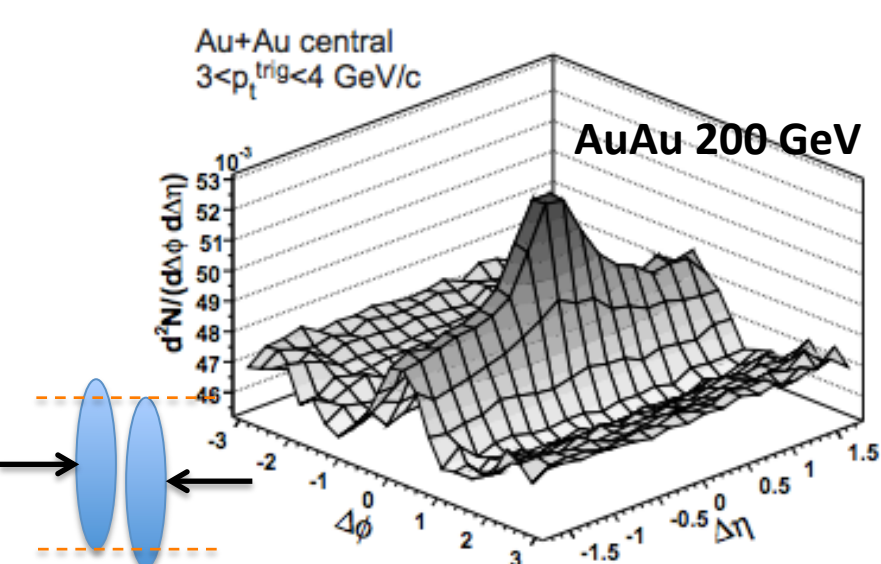


$$\Delta\eta = \eta^{\text{assoc}} - \eta^{\text{trig}}$$

$$\Delta\phi = \phi^{\text{assoc}} - \phi^{\text{trig}}$$

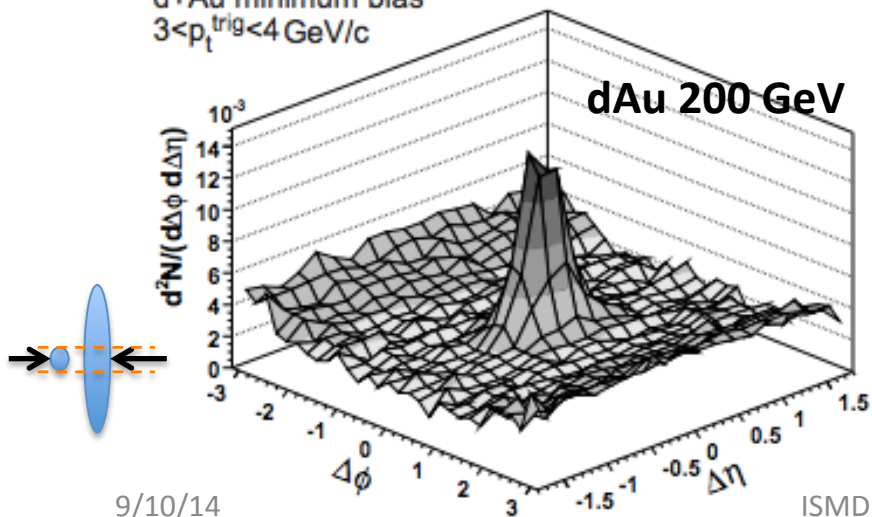
$$\frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{pair}}}{d\Delta\eta d\Delta\phi} = B(0,0) \times \frac{S(\Delta\eta, \Delta\phi)}{B(\Delta\eta, \Delta\phi)}$$

Ridge and Angular Correlations



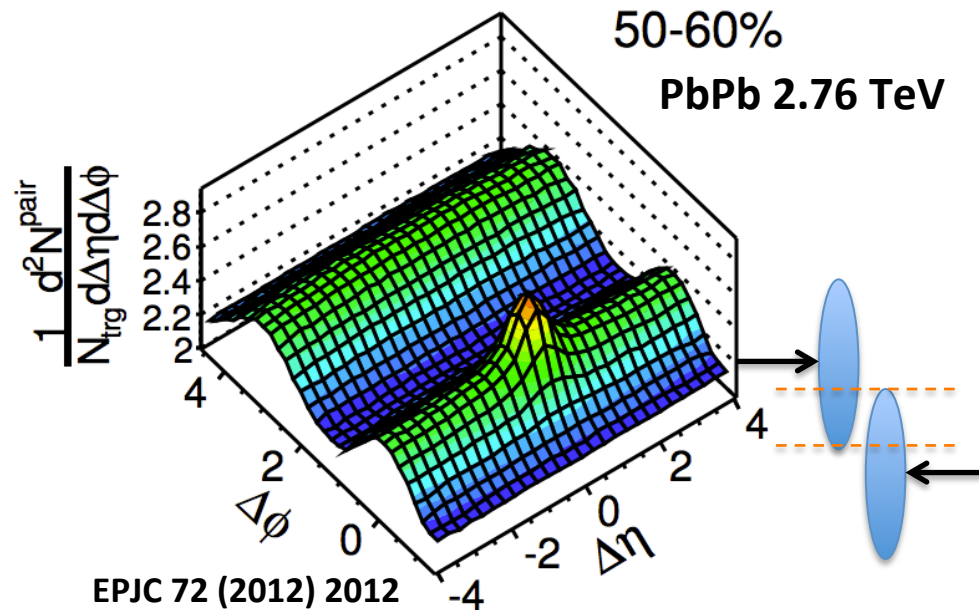
Phys.Rev. C80 (2009) 064912

d+Au minimum bias
 $3 < p_t^{\text{trig}} < 4 \text{ GeV}/c$



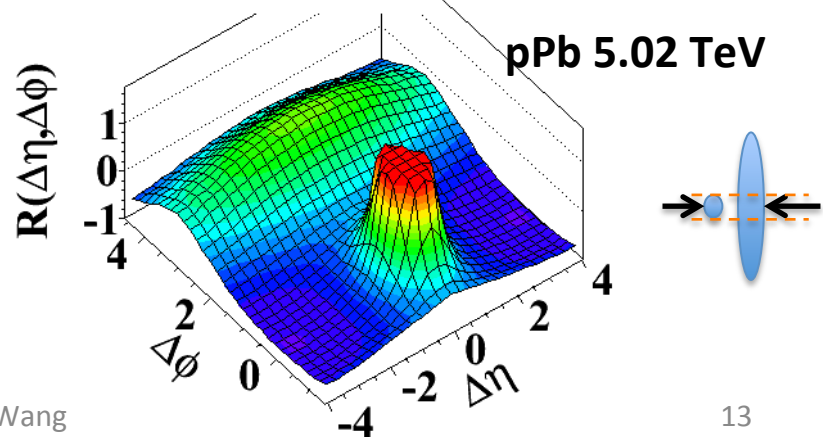
9/10/14

ISMD 2014 - Quan Wang



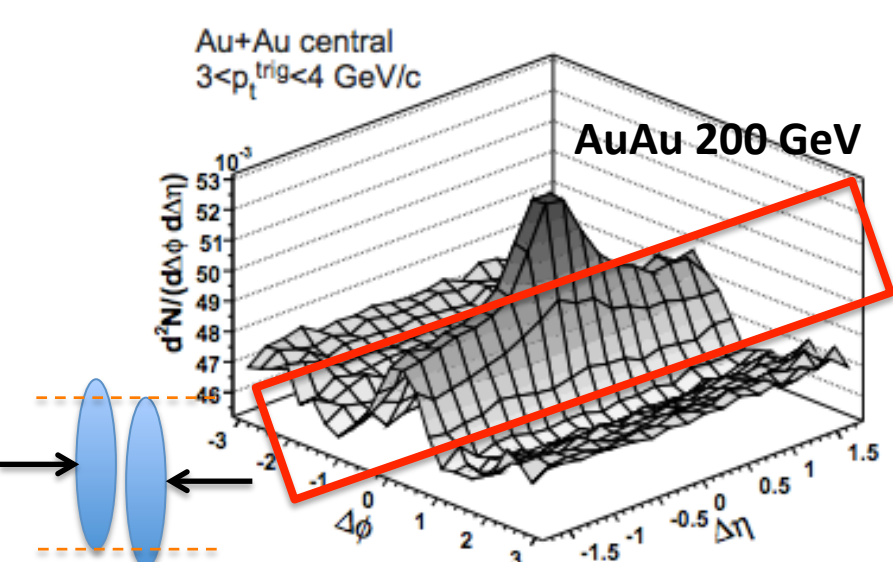
EPJC 72 (2012) 1212

(b) MinBias, $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



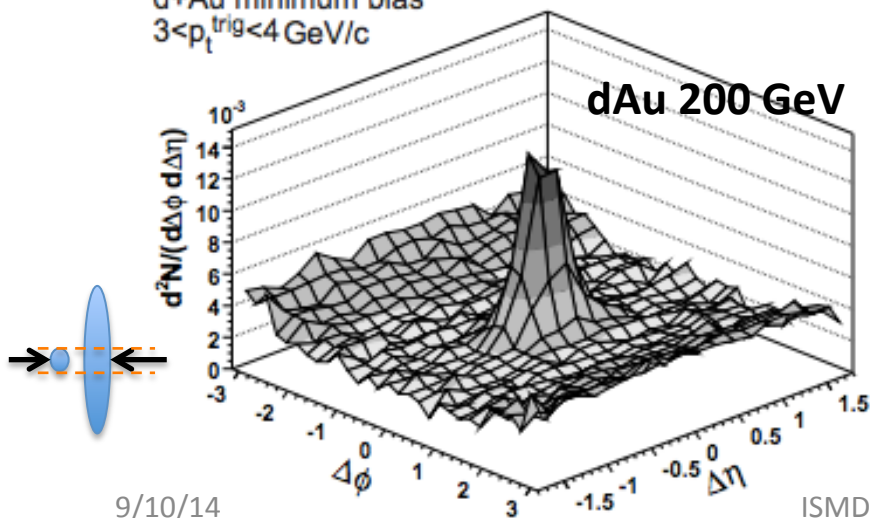
13

Ridge and Angular Correlations



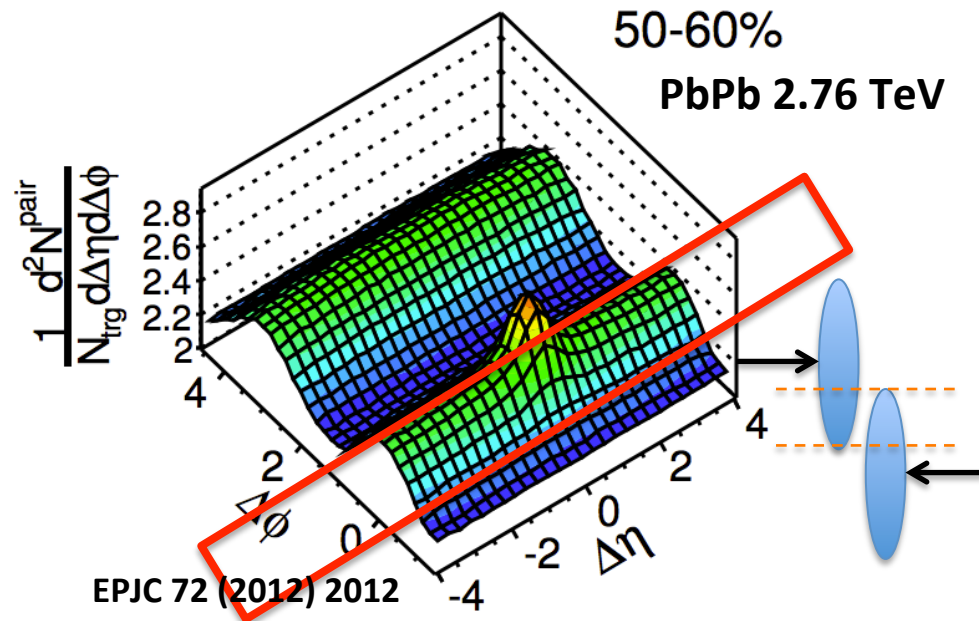
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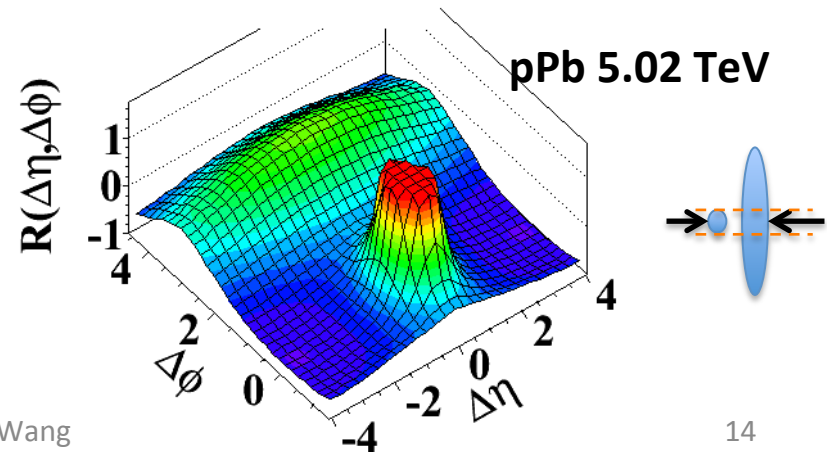
9/10/14

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EPJC 72 (2012) 2012

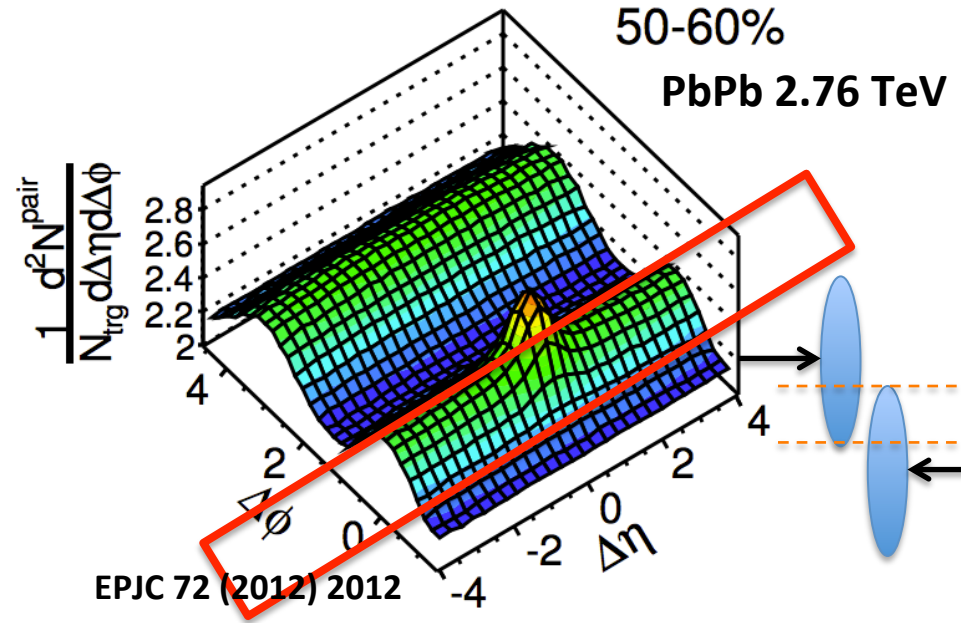
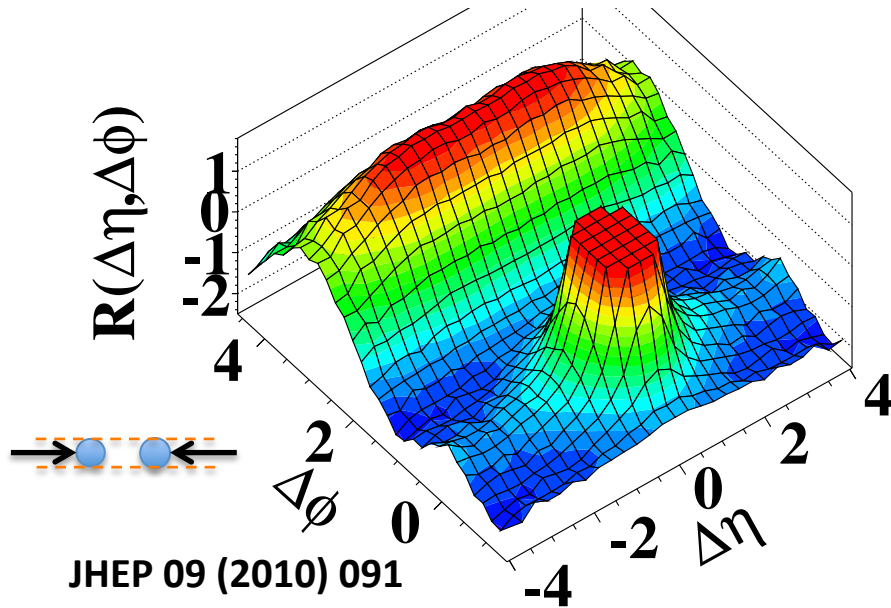
(b) MinBias, $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



14

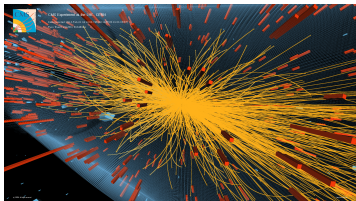
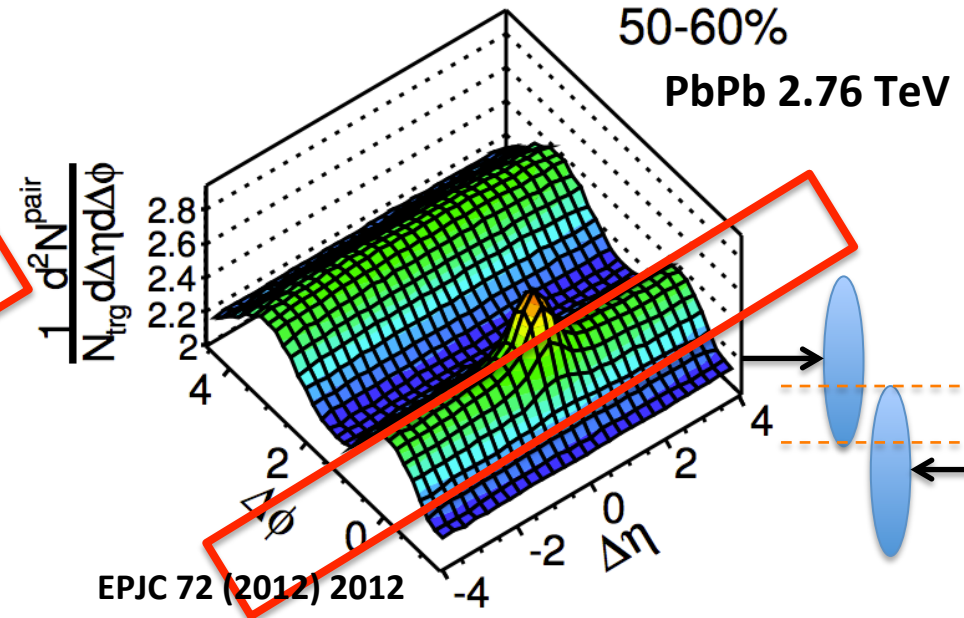
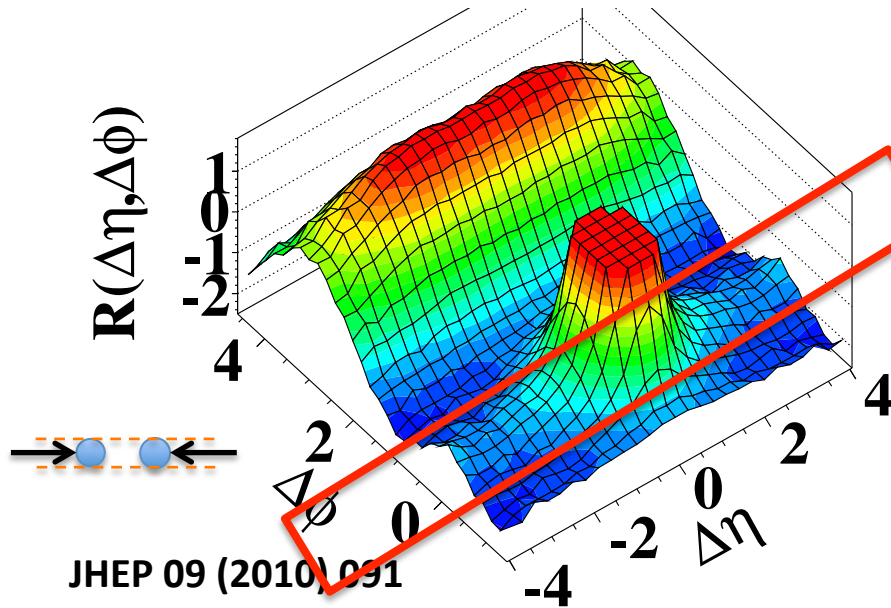
Ridge and Angular Correlations

pp 7 TeV, $N \geq 110$, $1 < p_T < 3 \text{ GeV}/c$



Ridge and Angular Correlations

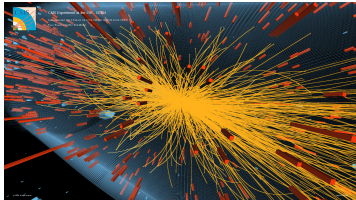
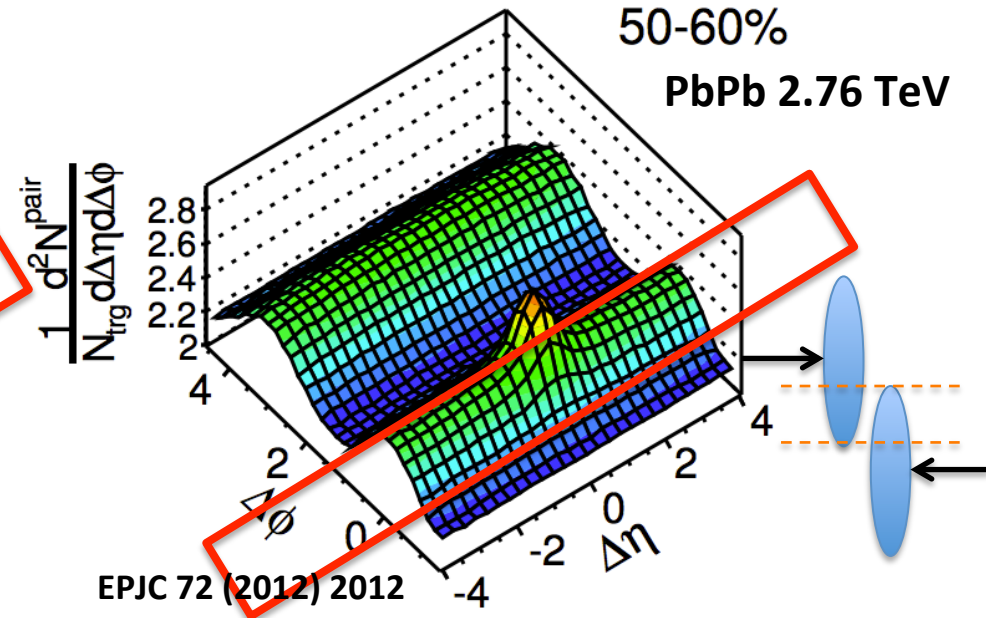
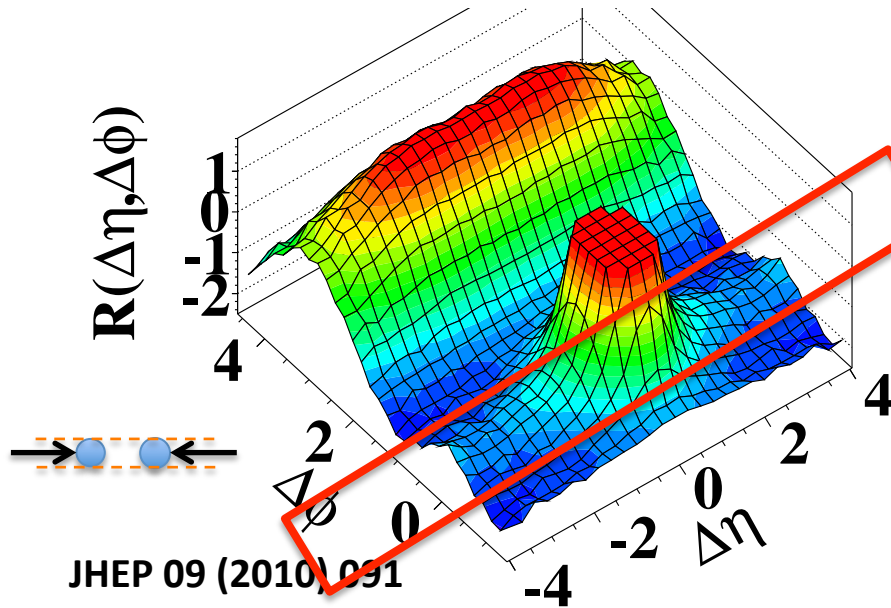
pp 7 TeV, $N \geq 110$, $1 < p_T < 3$ GeV/c



- Ridge in very high multiplicity pp events, $N \geq 110$

Ridge and Angular Correlations

pp 7 TeV, $N \geq 110$, $1 < p_T < 3$ GeV/c

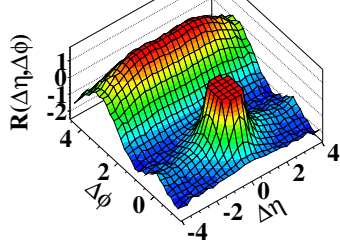


- **Ridge** in very high multiplicity **pp** events, $N \geq 110$
- Naturally expect ridge also in pPb high multi events

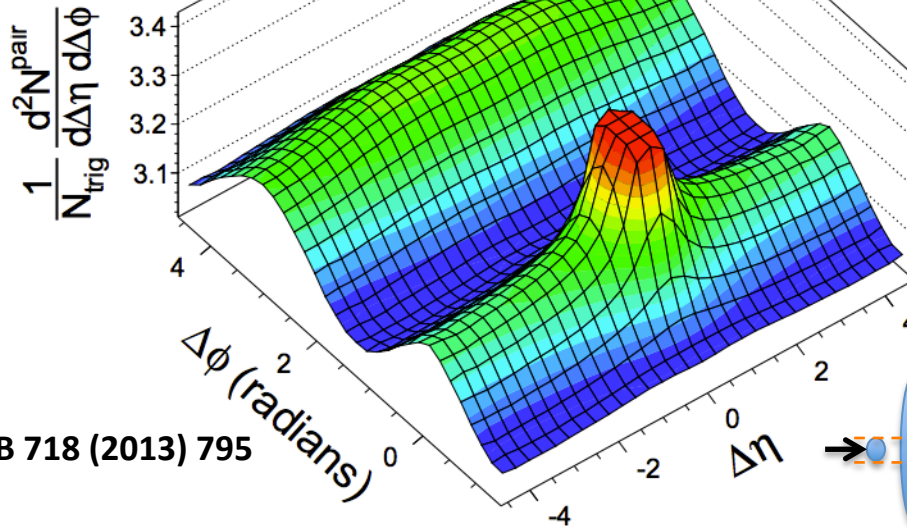
Ridge and Angular Correlations

pp 7 TeV, $N \geq 110$, $1 < p_T < 3 \text{ GeV}/c$

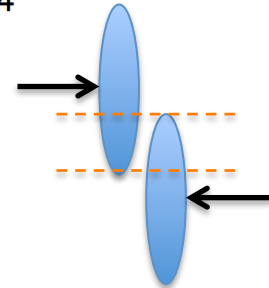
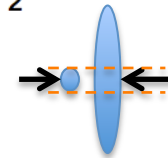
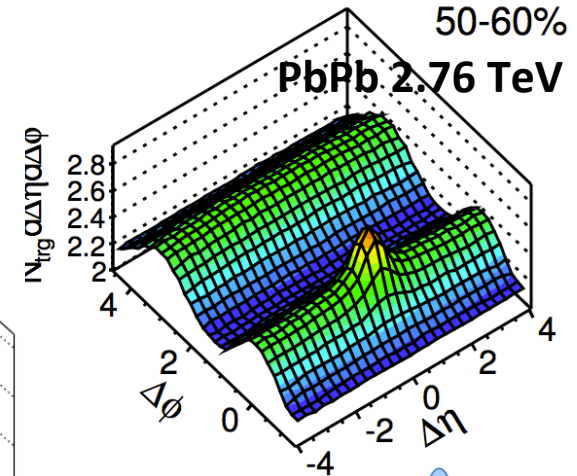
pPb 5.02 TeV $220 \leq N < 260$



$1 < p_T^{\text{trig}} < 3 \text{ GeV}/c$
 $1 < p_T^{\text{assoc}} < 3 \text{ GeV}/c$



PLB 718 (2013) 795

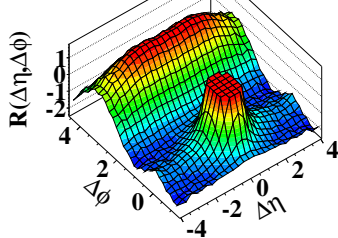


Ridge and Angular Correlations

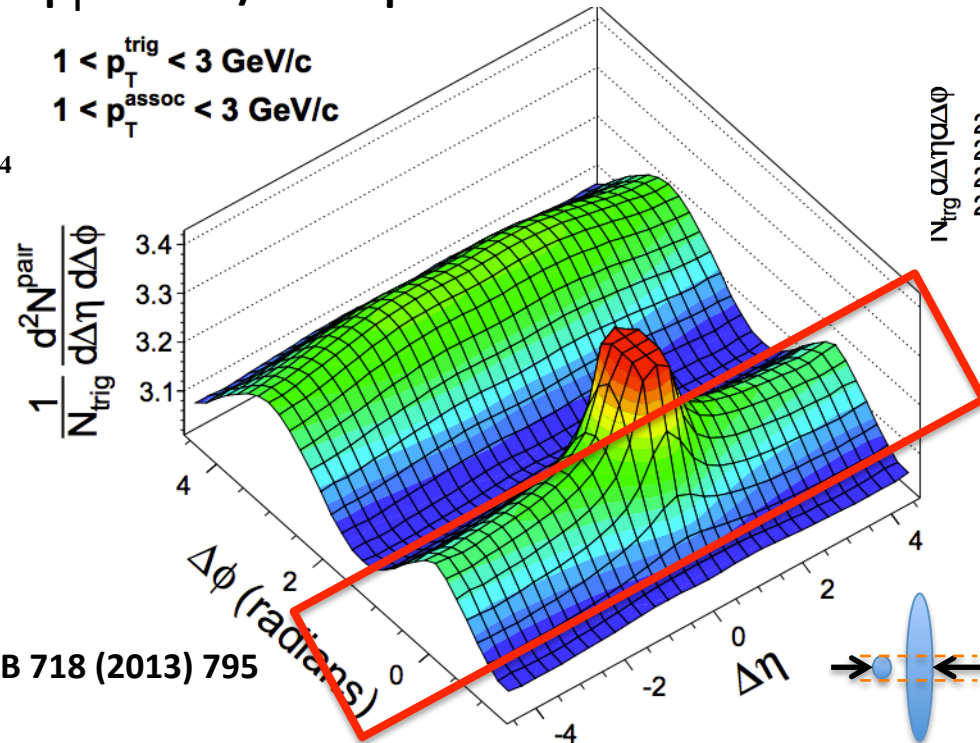
pp 7 TeV, $N \geq 110$, $1 < p_T < 3 \text{ GeV}/c$

pPb 5.02 TeV $220 \leq N < 260$

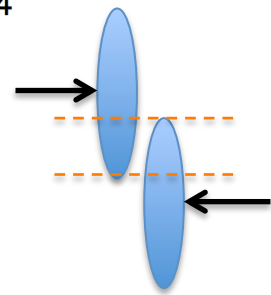
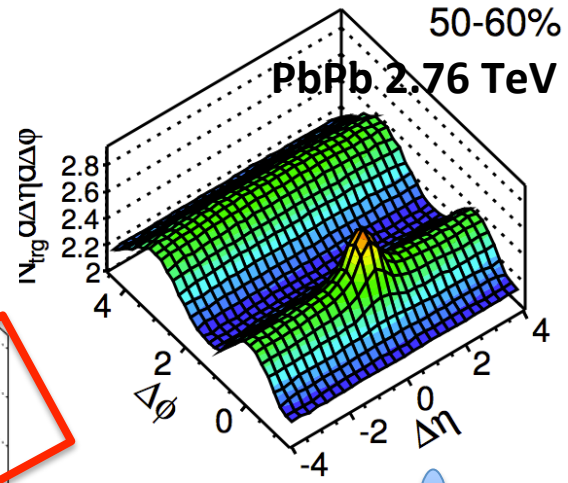
50-60%
PbPb 2.76 TeV



$1 < p_T^{\text{trig}} < 3 \text{ GeV}/c$
 $1 < p_T^{\text{assoc}} < 3 \text{ GeV}/c$



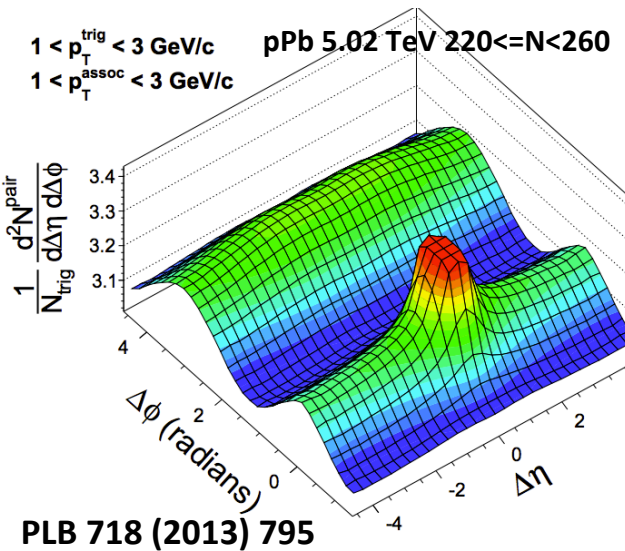
PLB 718 (2013) 795



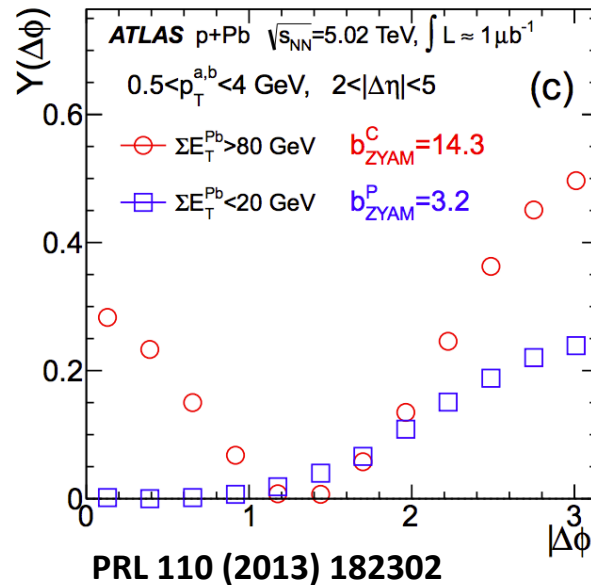
- **Strongly enhanced** ridge in pPb high multiplicity events

Ridge in pPb at the LHC

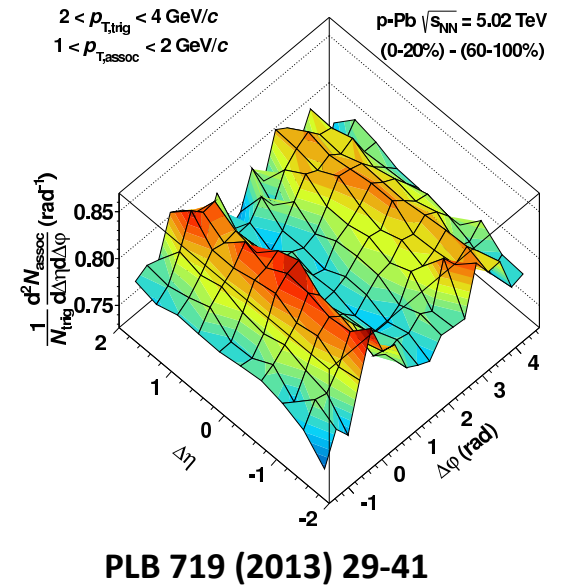
CMS



ATLAS

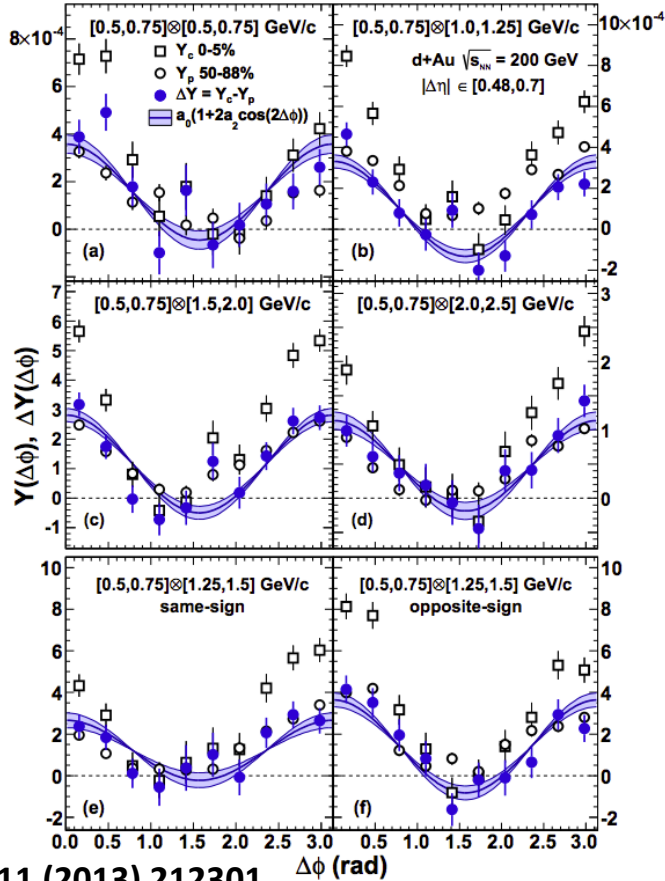


ALICE

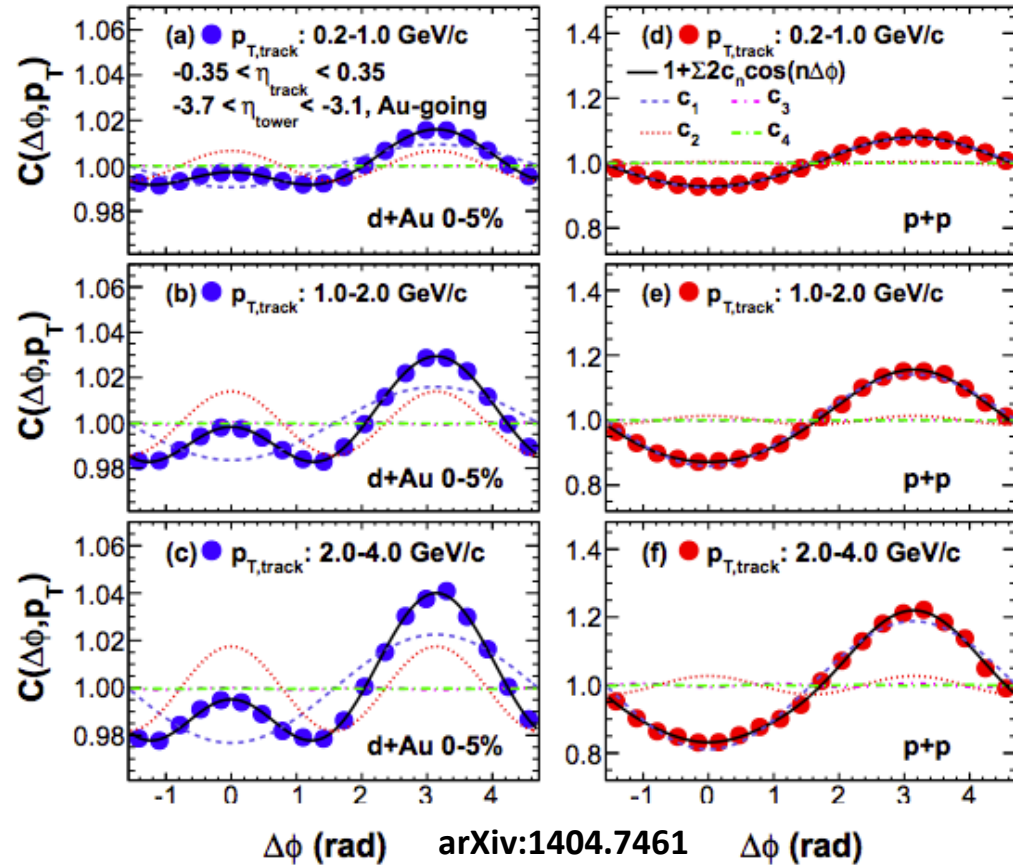


Look Back at dAu

PHNEX dAu 200 GeV



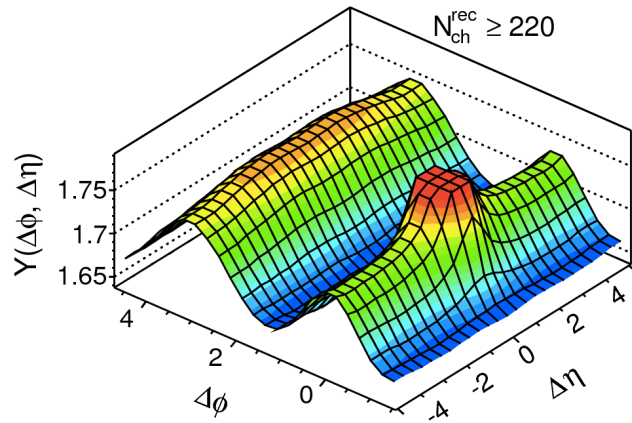
PHNEX dAu 200 GeV



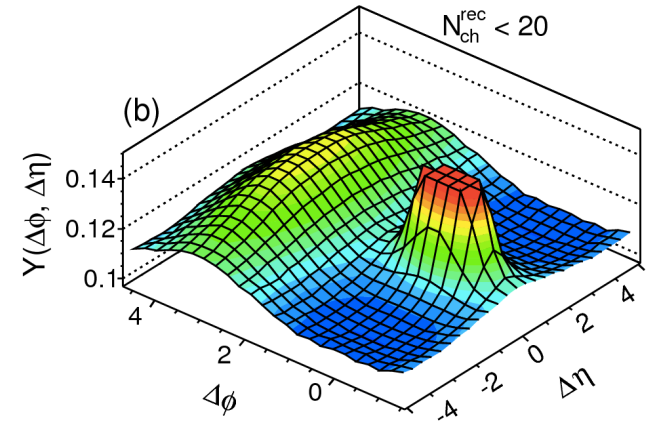
PRL 111 (2013) 212301

arXiv:1404.7461

Peripheral Subtraction

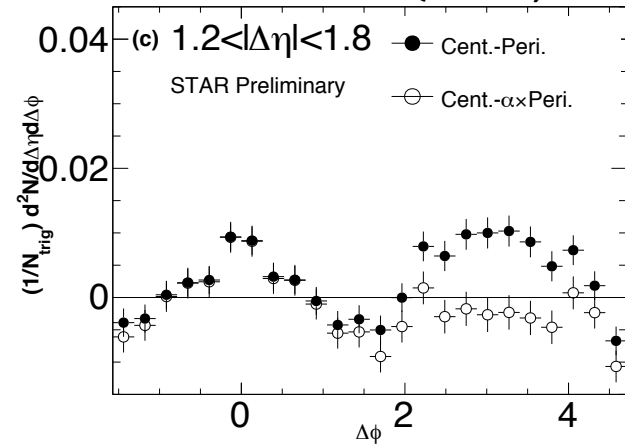
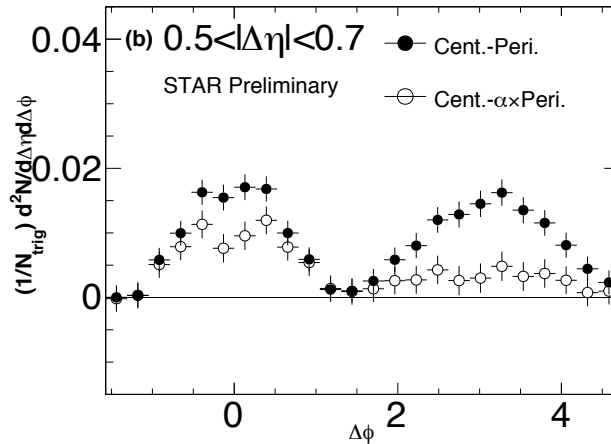
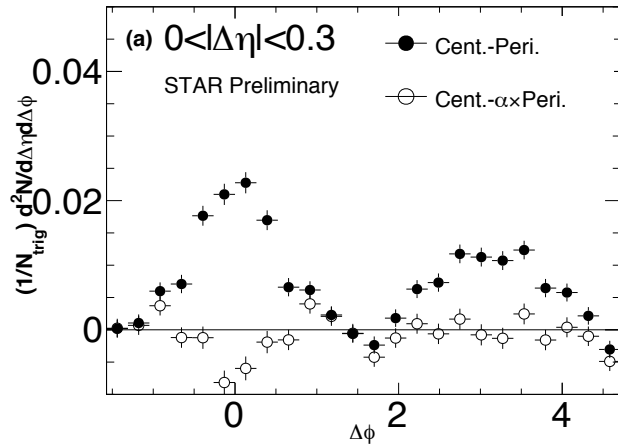


$$- \alpha \times$$

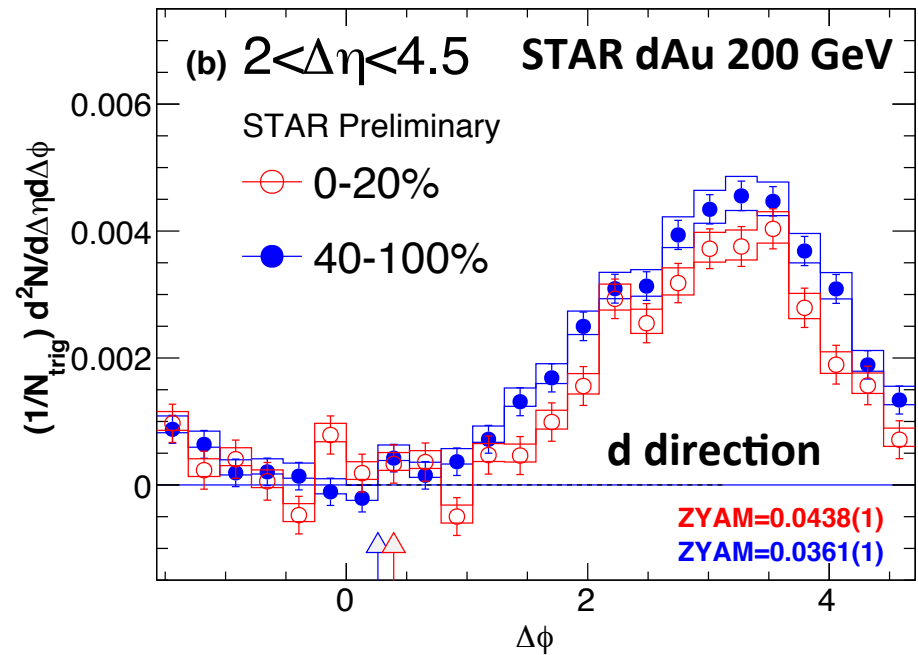
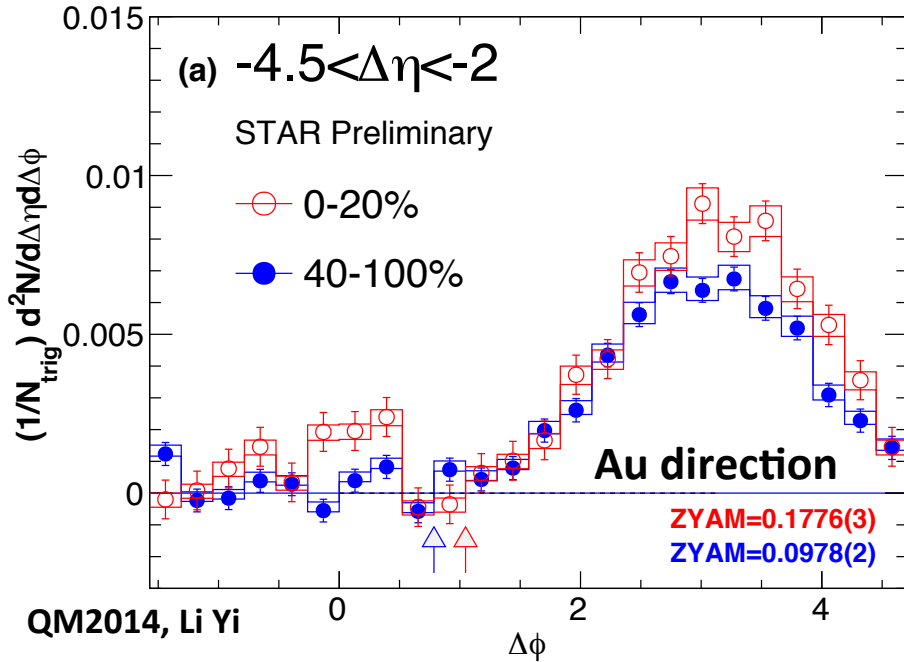


STAR dAu 200 GeV

QM2014, Li Yi

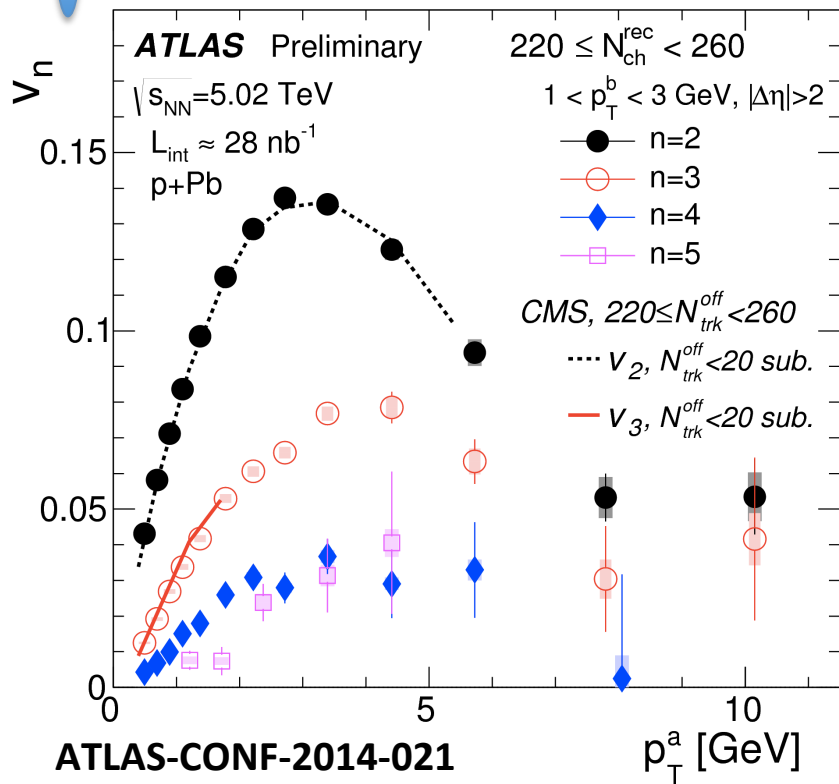
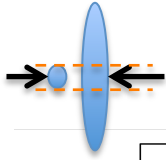


Peripheral Subtraction

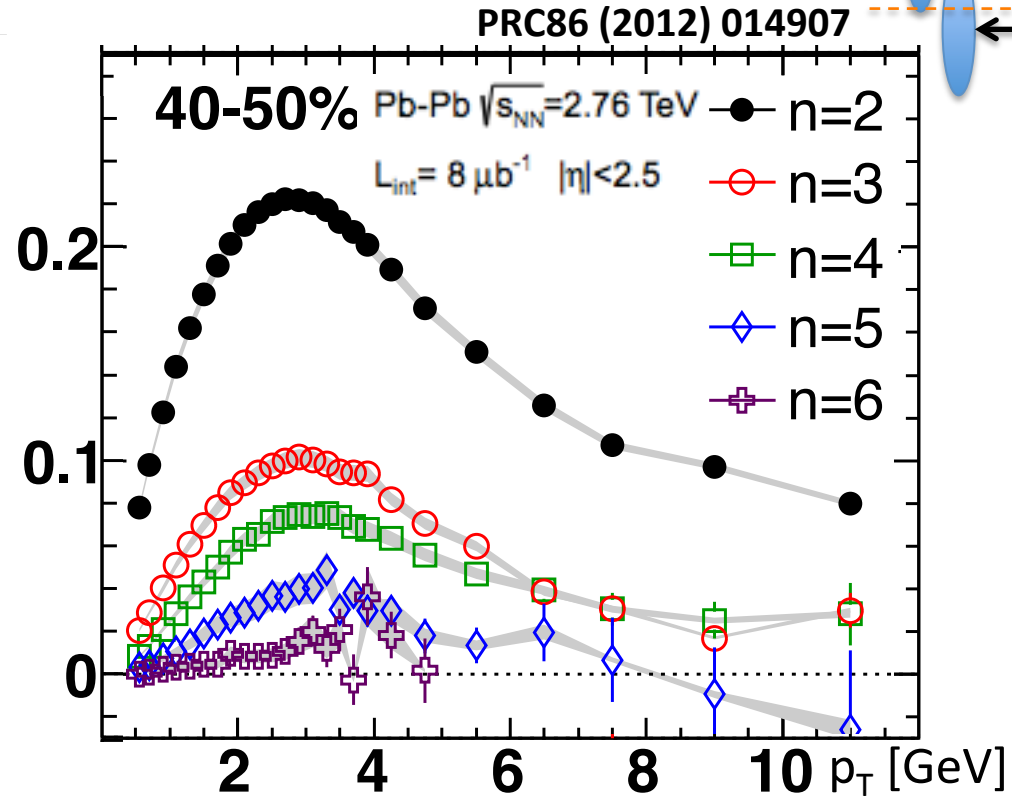
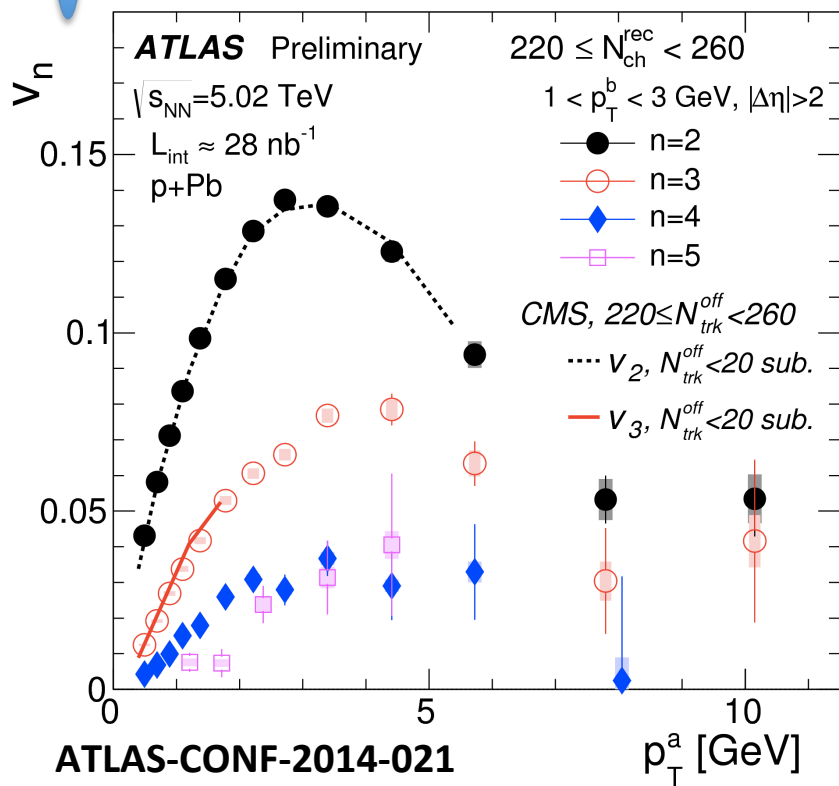
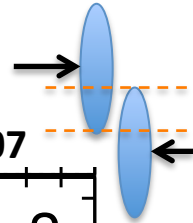
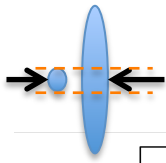


- Ridge in Au direction, but not in d direction
- η dependence of ridge?

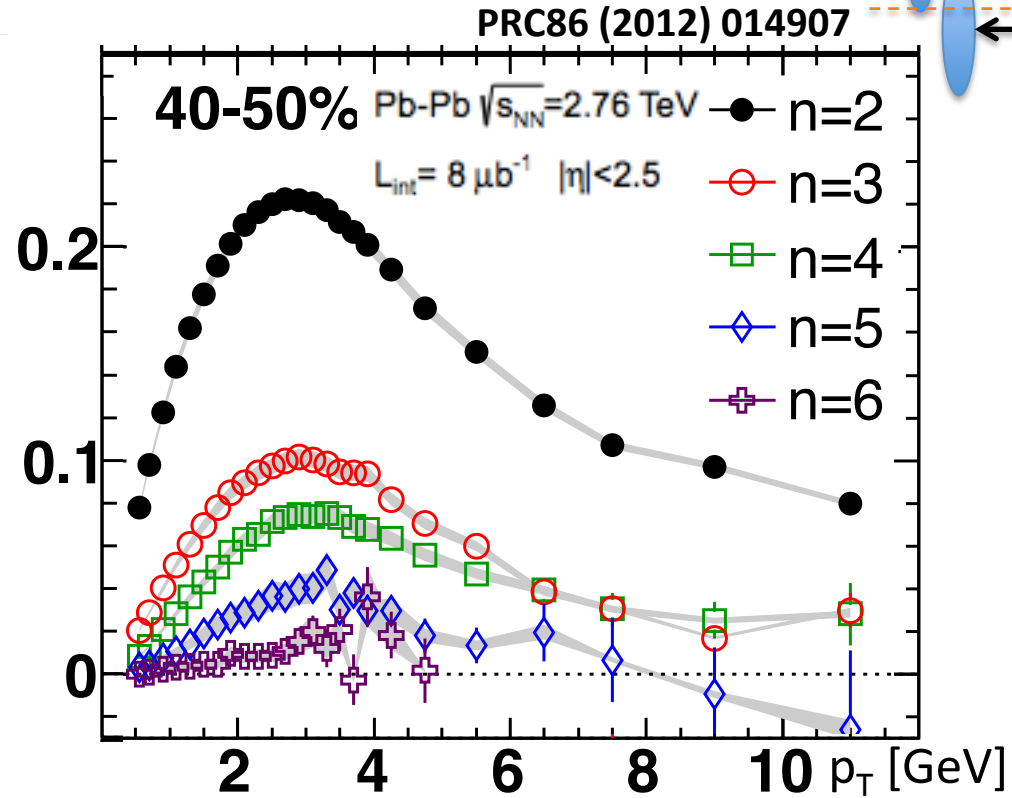
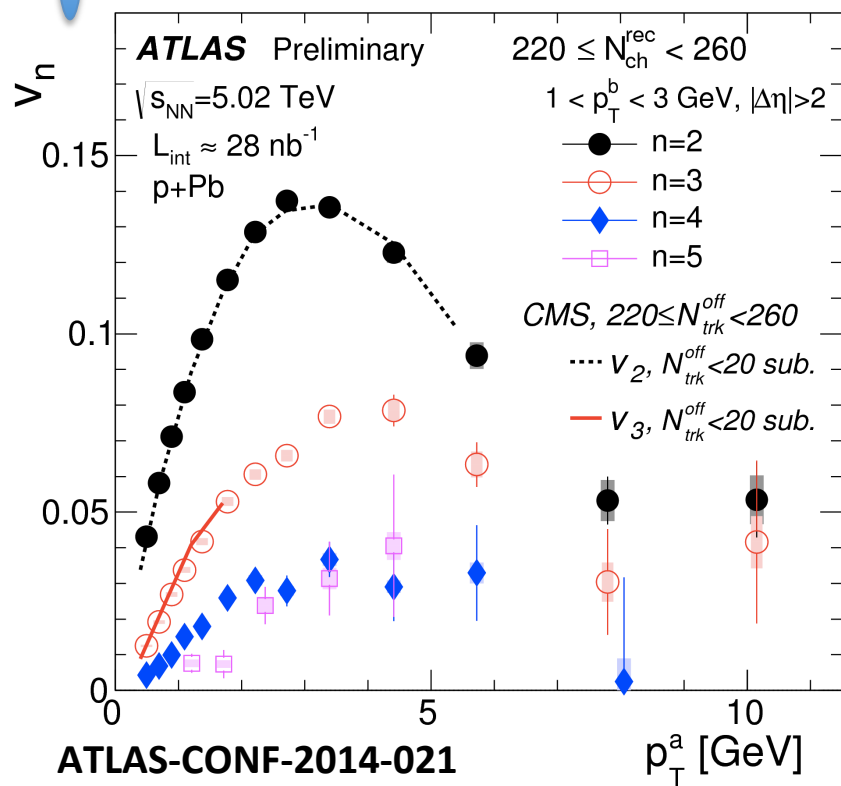
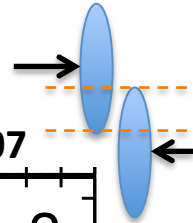
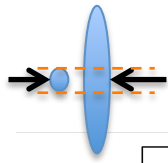
Flow coefficient $v_n(p_T)$



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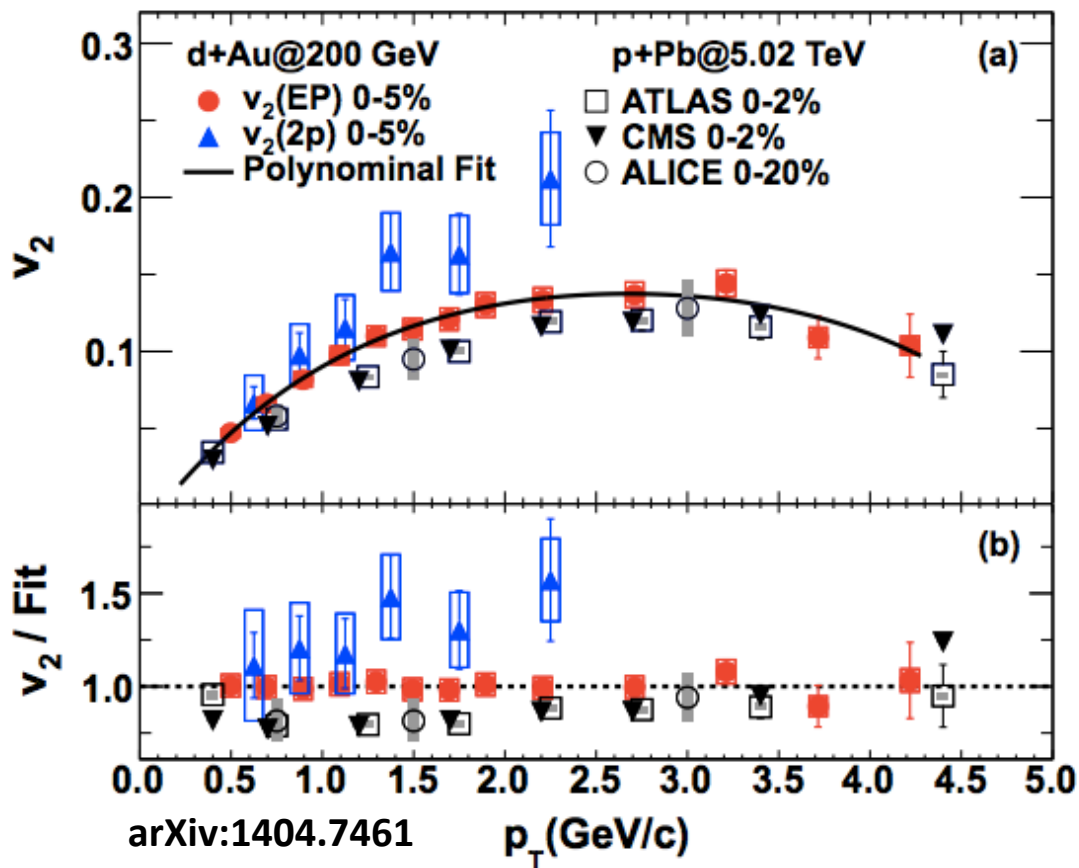


Flow coefficient $v_n(p_T)$

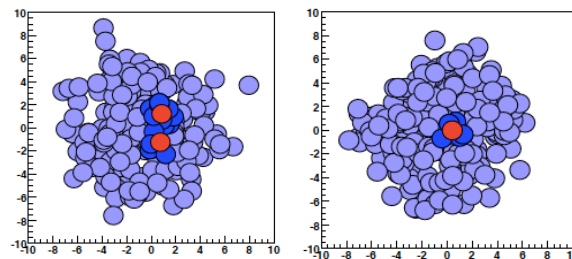


- Striking similar behavior at similar multiplicity
- Same origin?

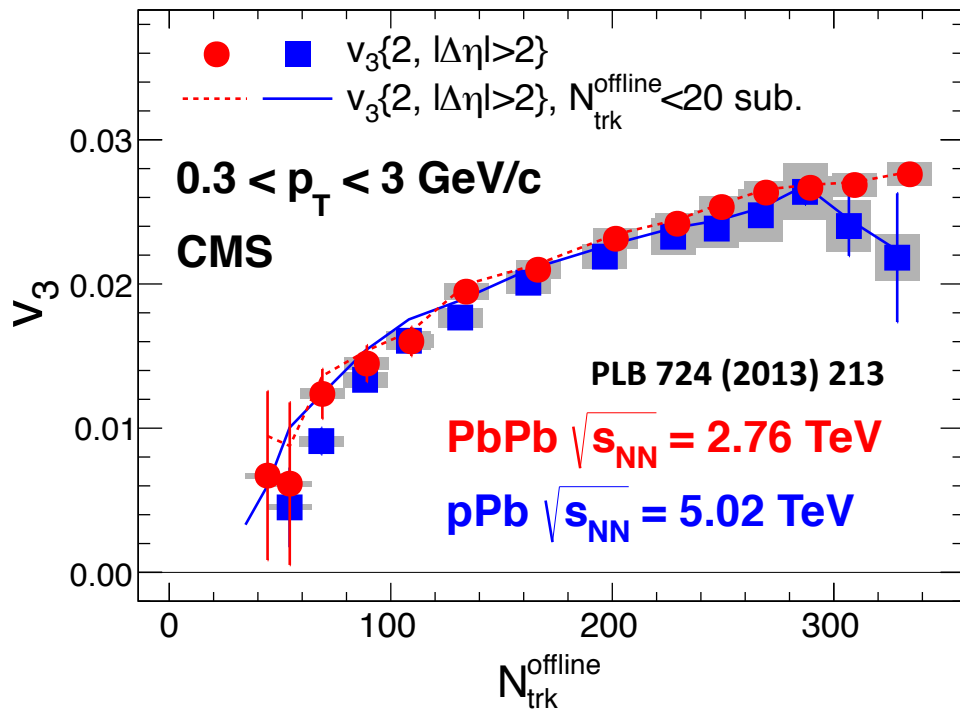
Flow coefficient $v_n(p_T)$



- Very close v_2 results from RHIC and LHC
- Initial conditions are very different

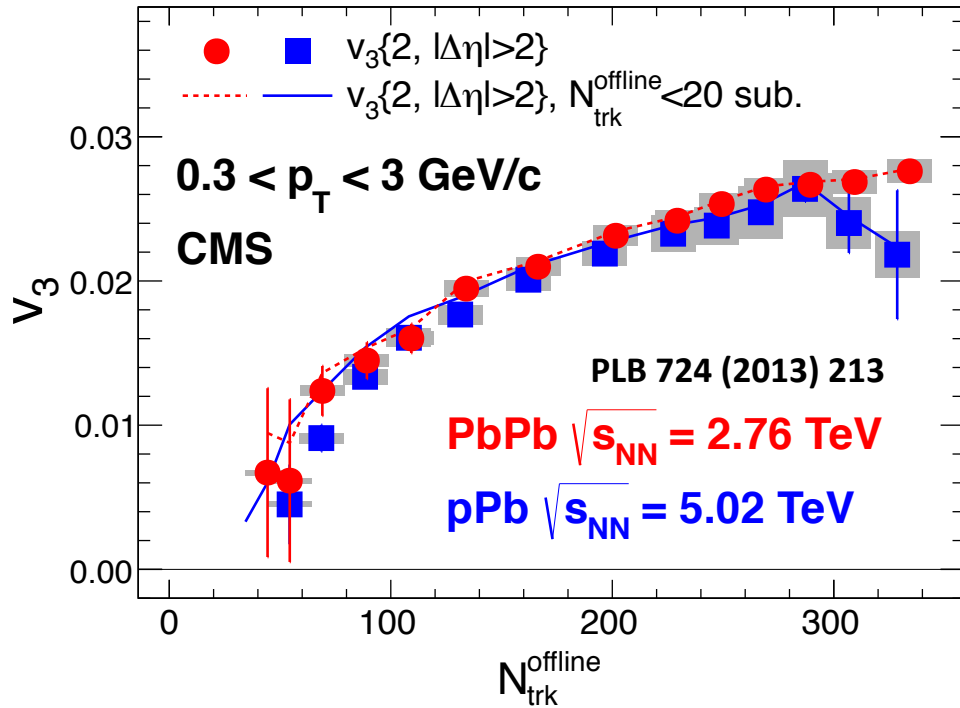


Flow coefficient $v_n(p_T)$

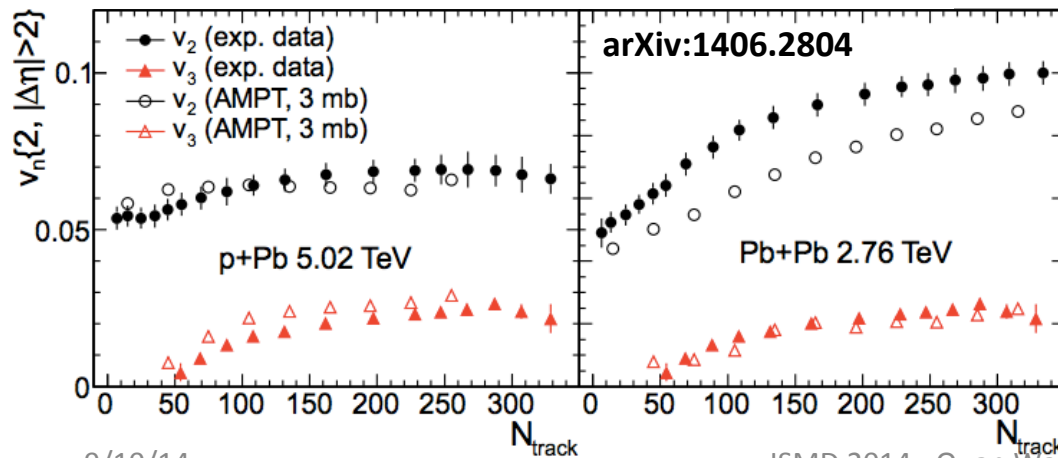


- Intriguing similarity in v_3
- v_3 purely from fluctuation
- System size independent?

Flow coefficient $v_n(p_T)$

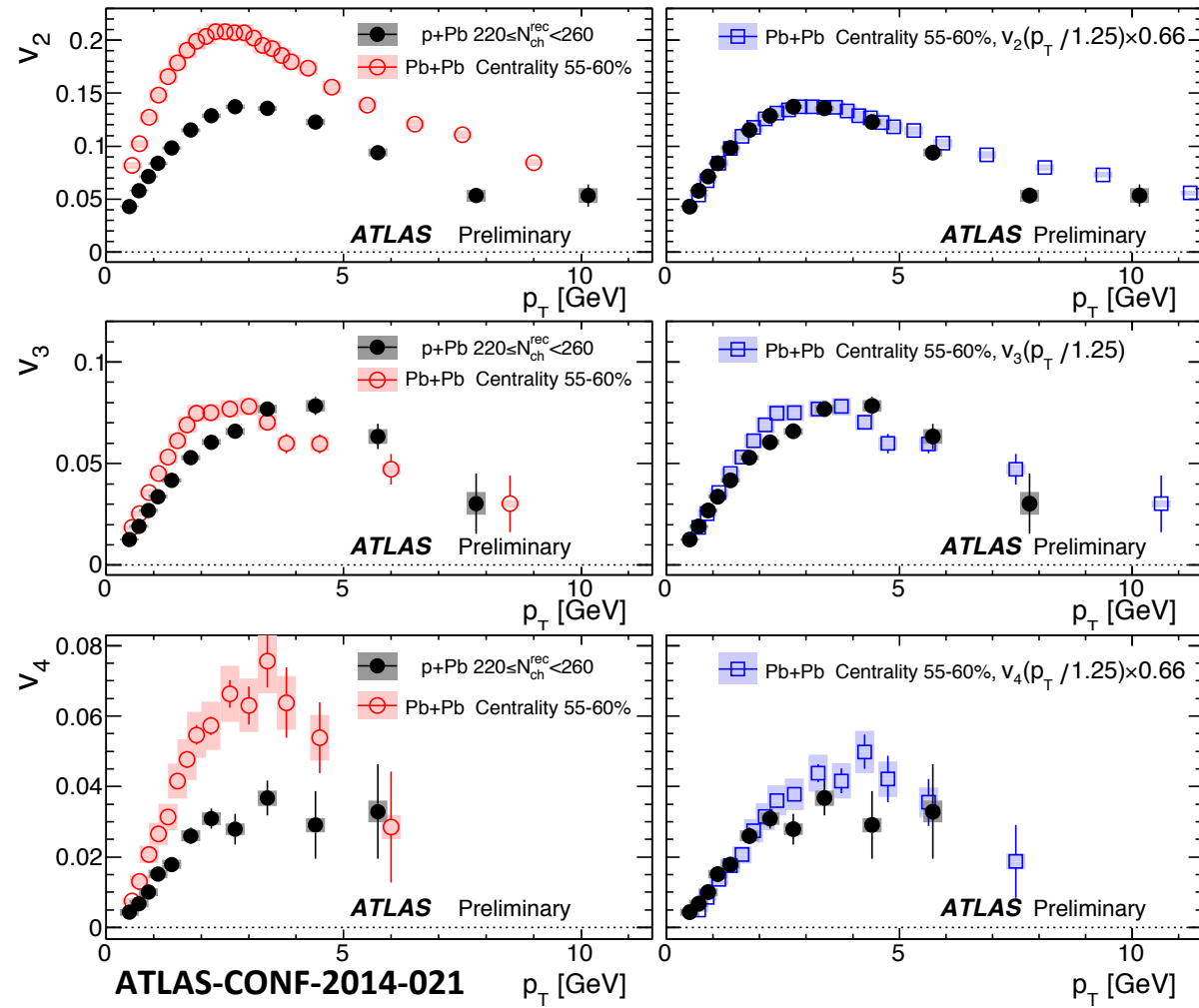


- Intriguing similarity in v_3
- v_3 purely from fluctuation
- System size independent?

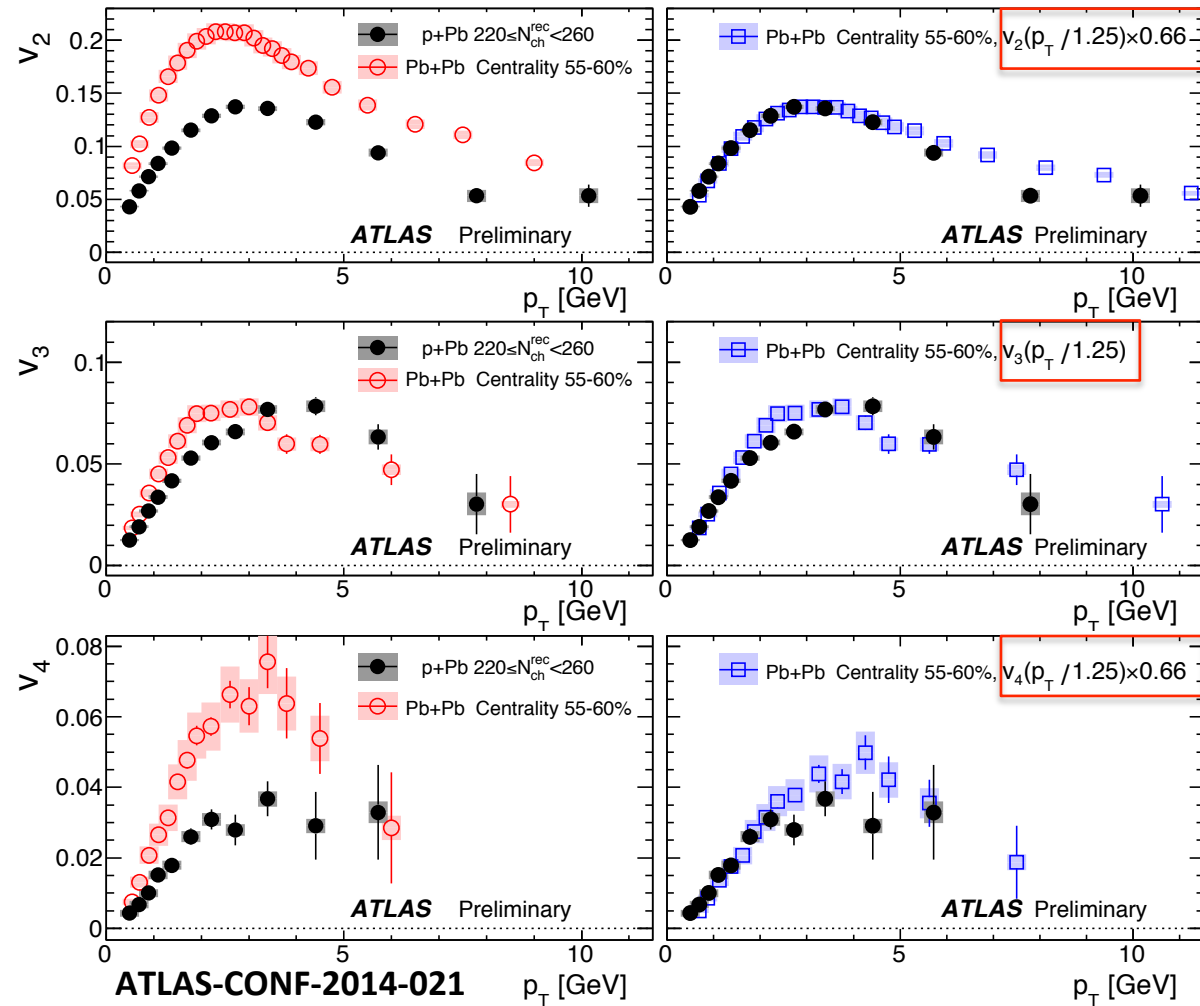


- AMPT with string melting
- Transport model

Flow coefficient $v_n(p_T)$

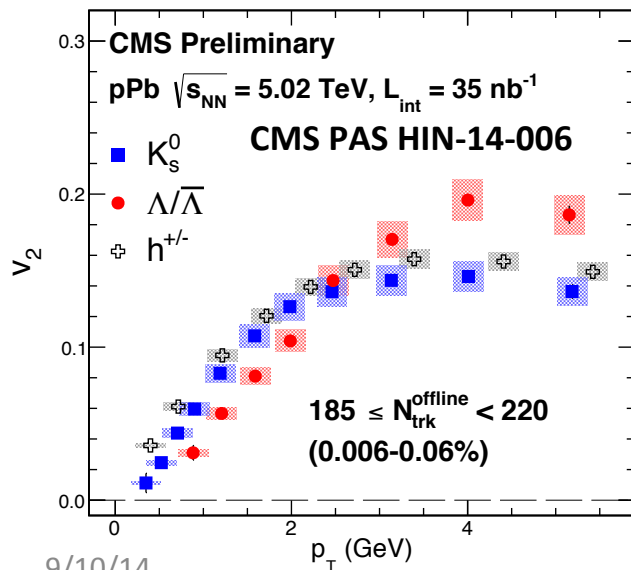
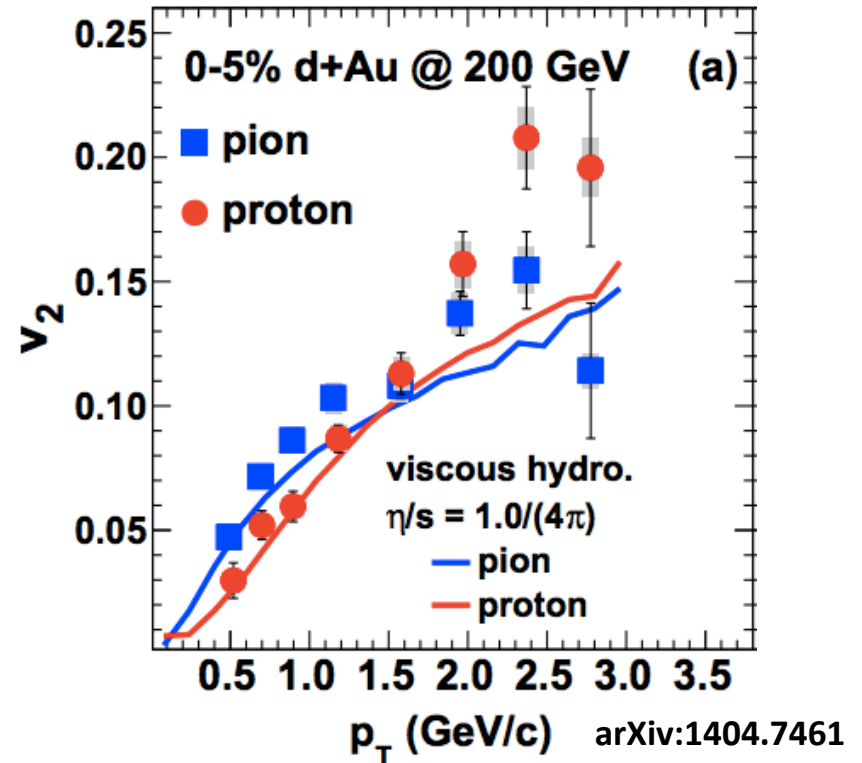
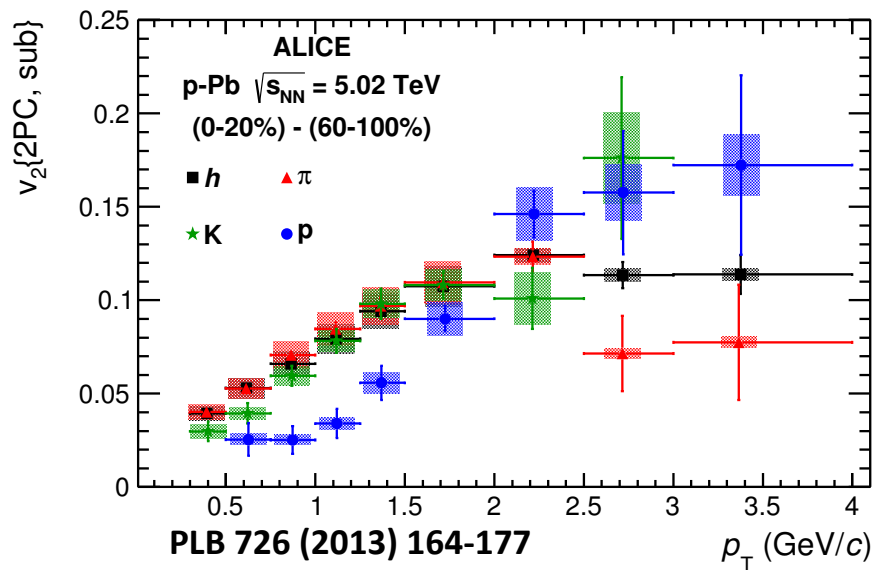


Flow coefficient $v_n(p_T)$



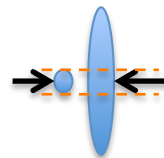
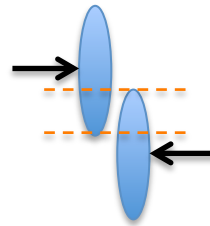
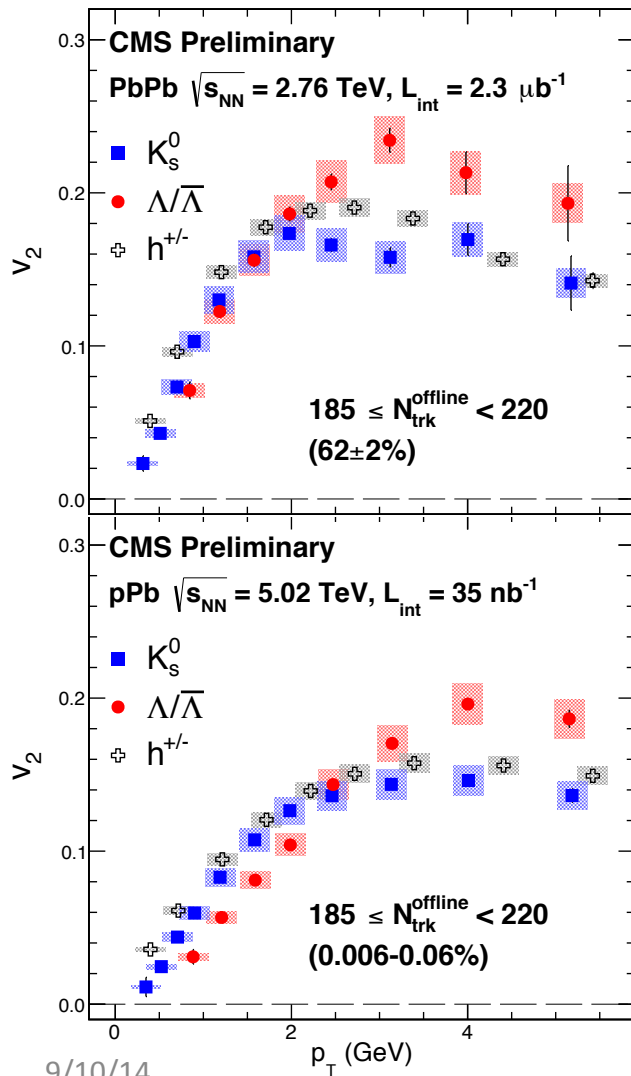
- Rescaling property (arXiv:1312.6770)
- Rescale account for averaged p_T difference of 1.25x

Mass Ordering in Small System



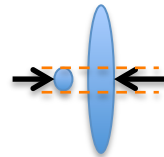
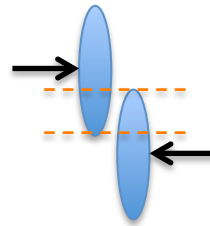
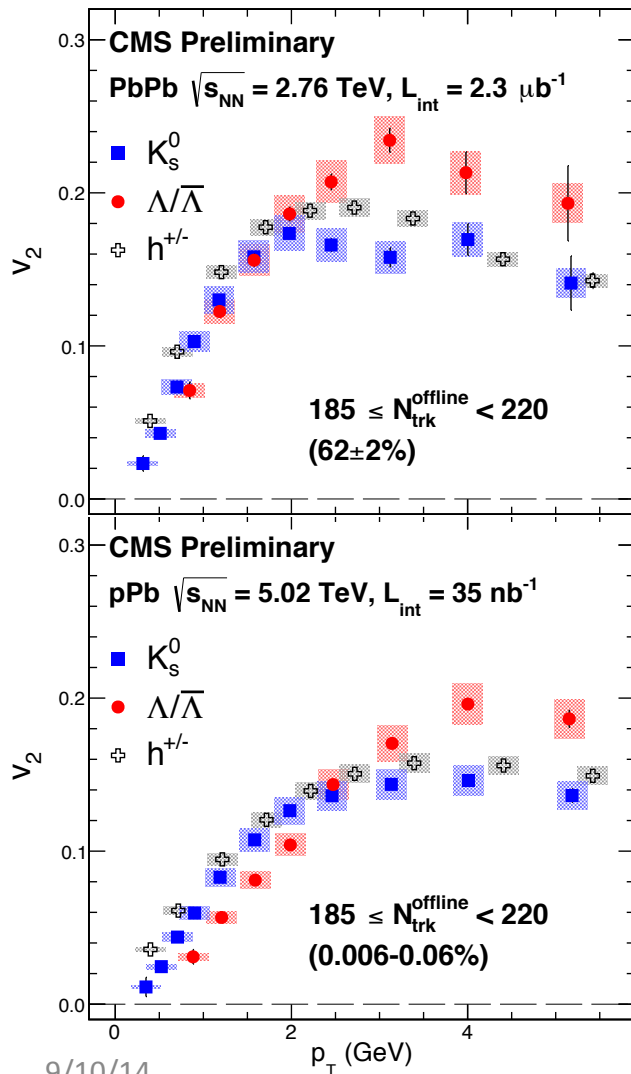
- Mass ordering persists in small system
- Low p_T , light particles have large v_2
- High p_T , $v_2\{\text{baryon}\} > v_2\{\text{meson}\}$
- Cross over around $p_T = 2$ GeV/c

Mass Ordering in Small System

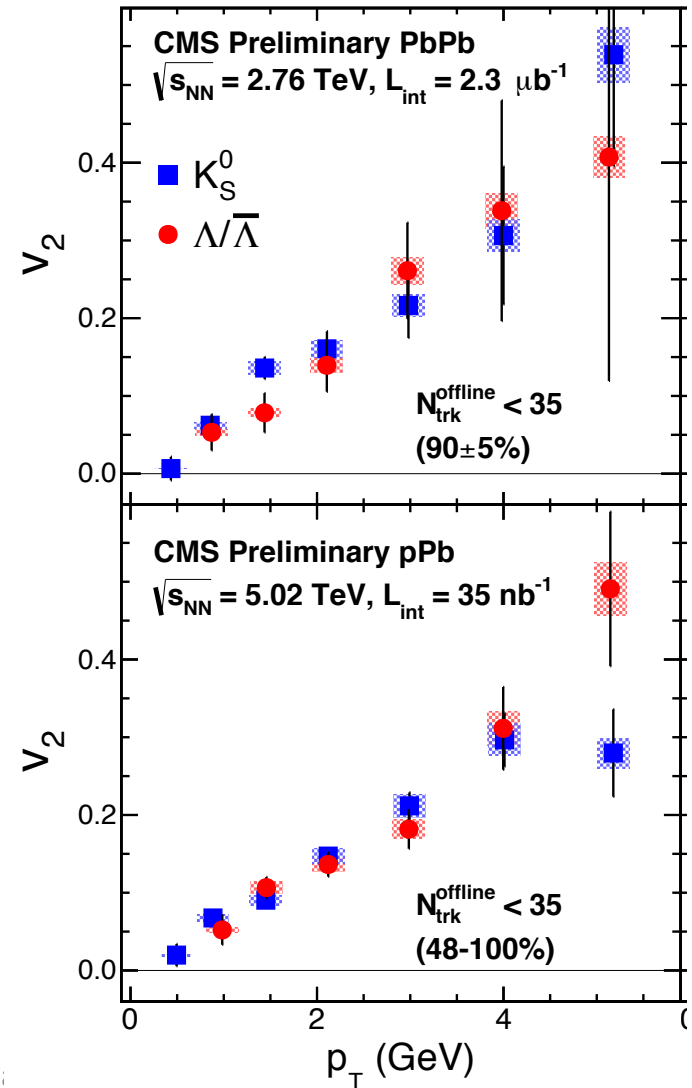


CMS PAS HIN-14-006

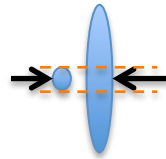
Mass Ordering in Small System



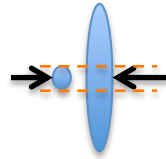
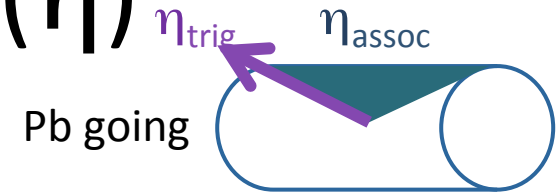
CMS PAS HIN-14-006



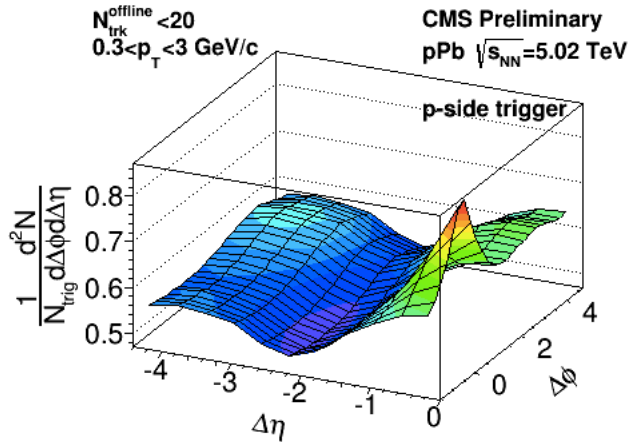
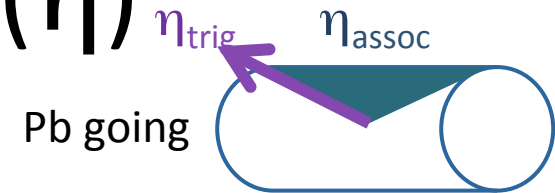
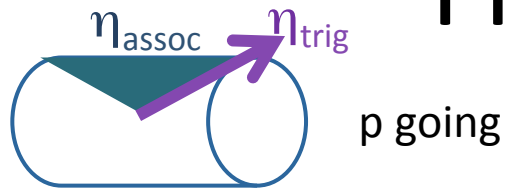
Flow coefficient $v_n(\eta)$



Flow coefficient $v_n(\eta)$

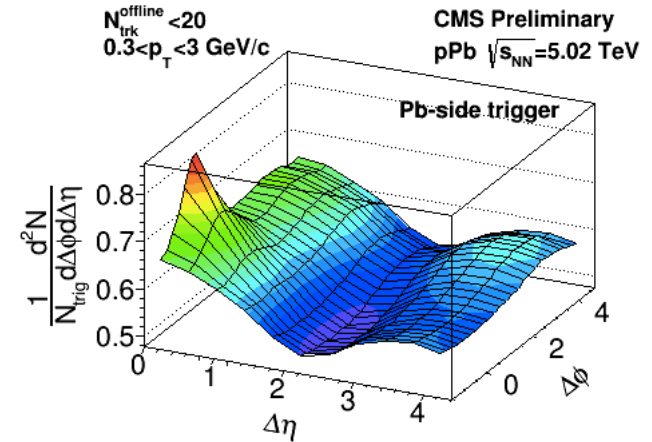
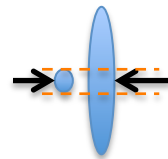


Flow coefficient $v_n(\eta)$



CMS PAS HIN-14-008

Low Multiplicity



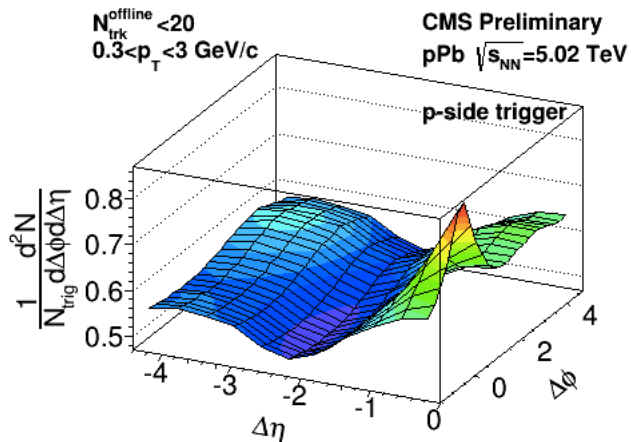
Flow coefficient $v_n(\eta)$



p going

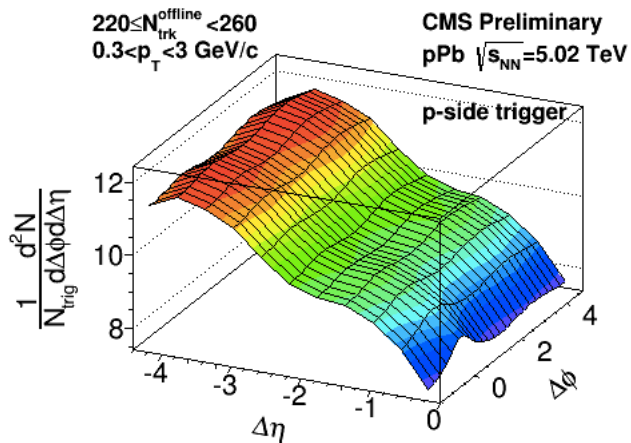
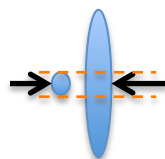
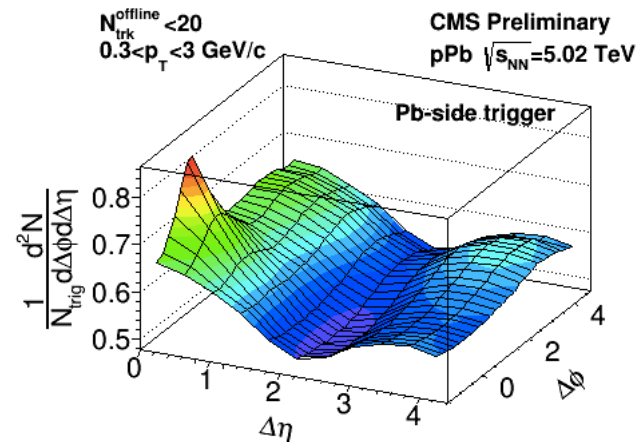


Pb going

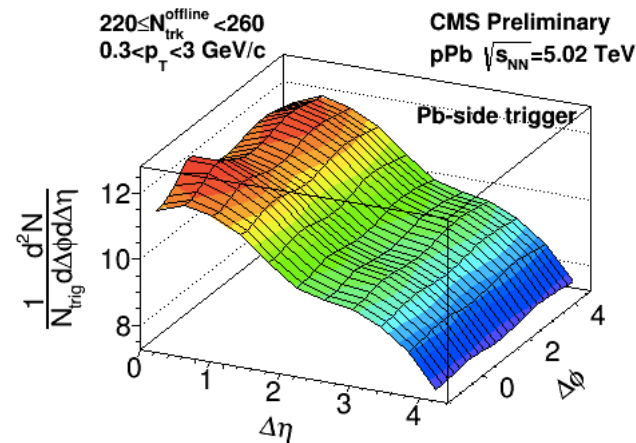


CMS PAS HIN-14-008

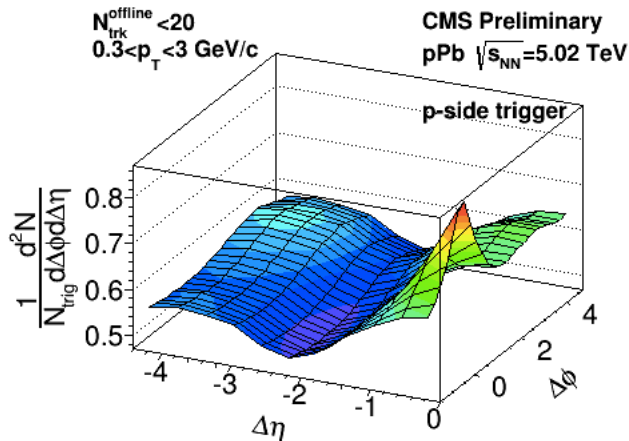
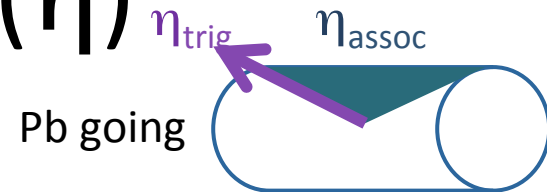
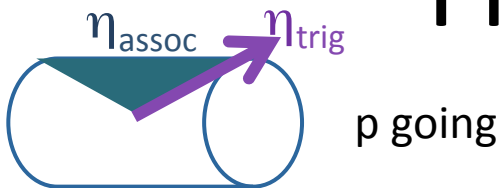
Low Multiplicity



High Multiplicity

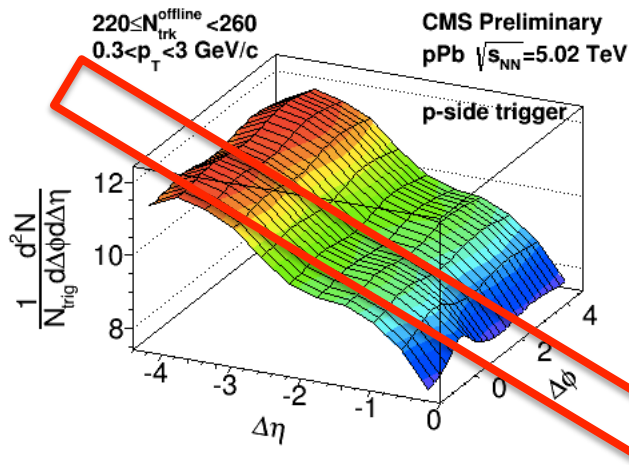
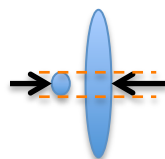
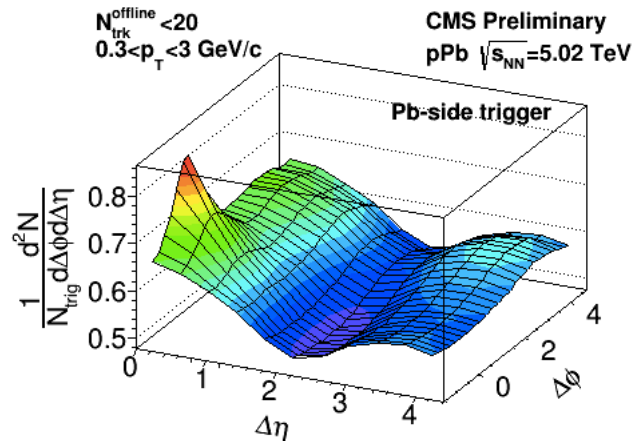


Flow coefficient $v_n(\eta)$

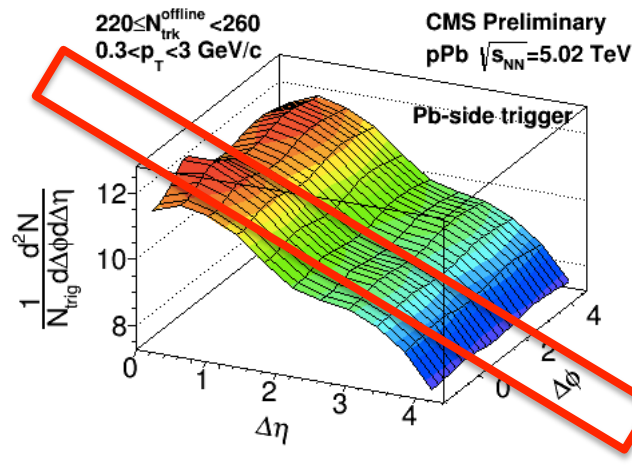


CMS PAS HIN-14-008

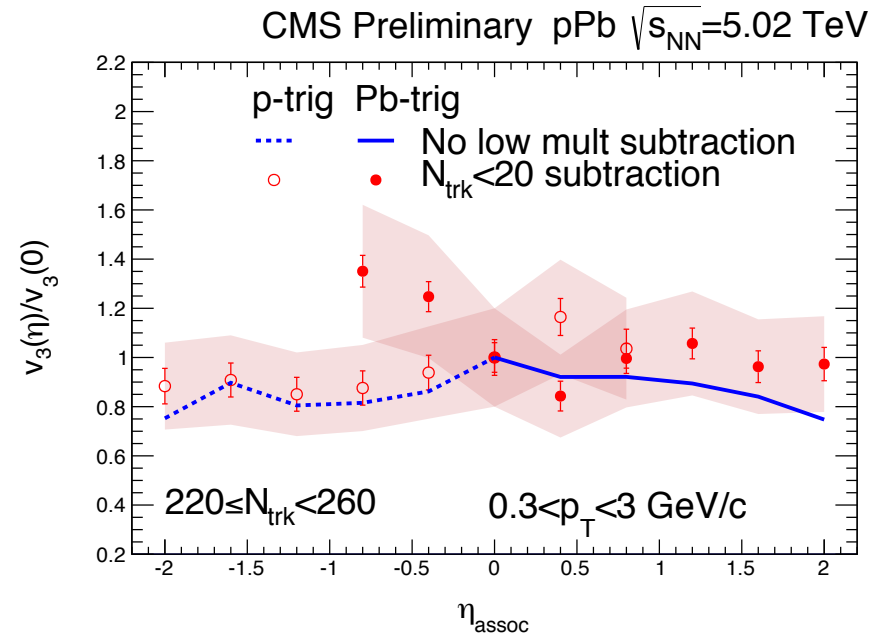
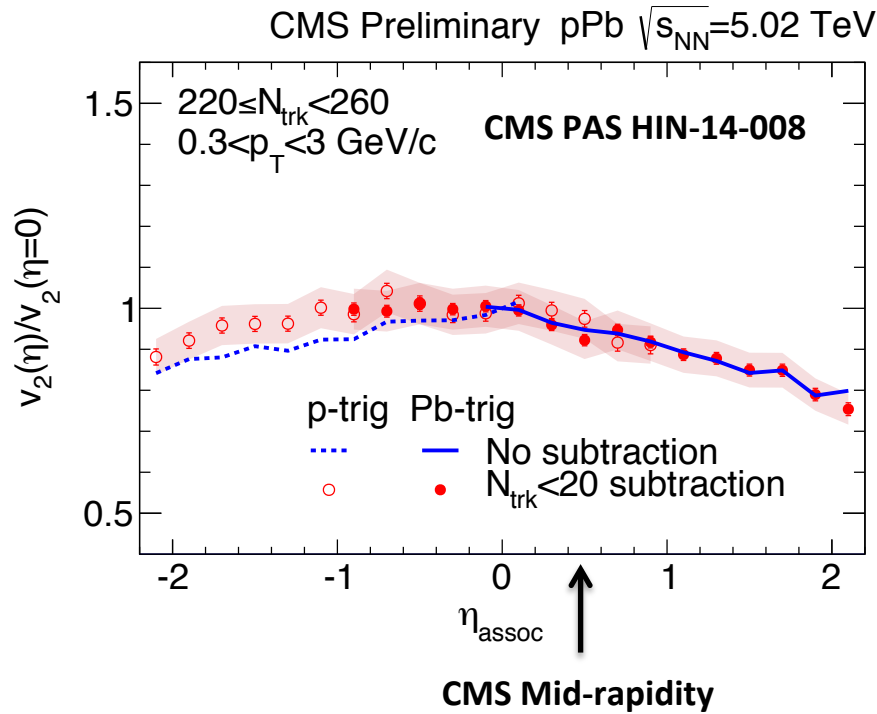
Low Multiplicity



High Multiplicity



Flow coefficient $v_n(\eta)$



- Significant η dependence observed for v_2

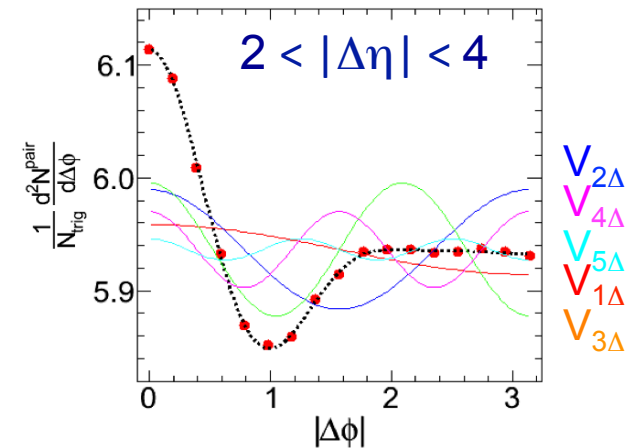
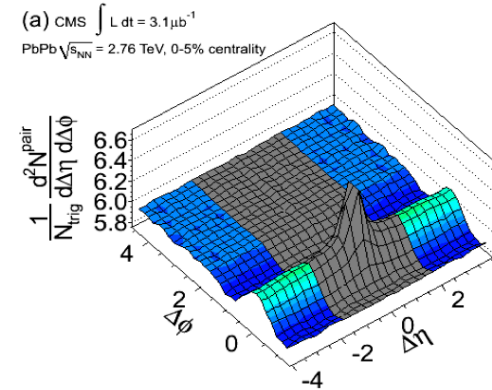
Flow Factorization

Two particle correlation

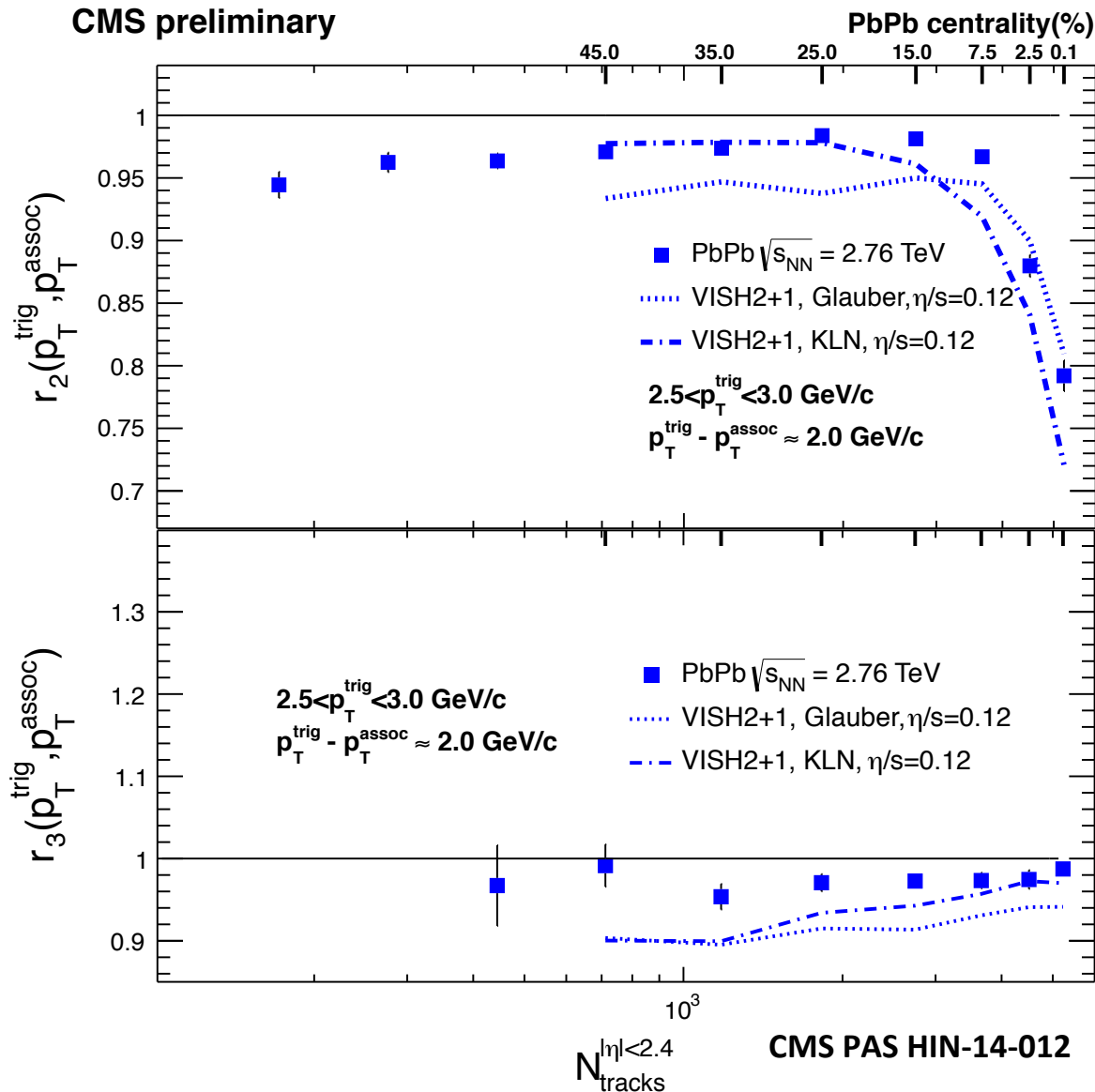
$$\frac{dN}{d\Delta\phi} \sim 1 + 2V_{2\Delta} \cos 2\Delta\phi + 2V_{3\Delta} \cos 3\Delta\phi$$

$$V_{n\Delta}(p_{T1}, p_{T2}) = \langle v_n(p_{T1}) v_n(p_{T2}) \cos[n(\Psi_n(p_{T1}) - \Psi_n(p_{T2}))] \rangle$$

$$r_n = \frac{V_{n\Delta}(p_{T1}, p_{T2})}{\sqrt{V_{n\Delta}(p_{T1}, p_{T1}) V_{n\Delta}(p_{T2}, p_{T2})}}$$

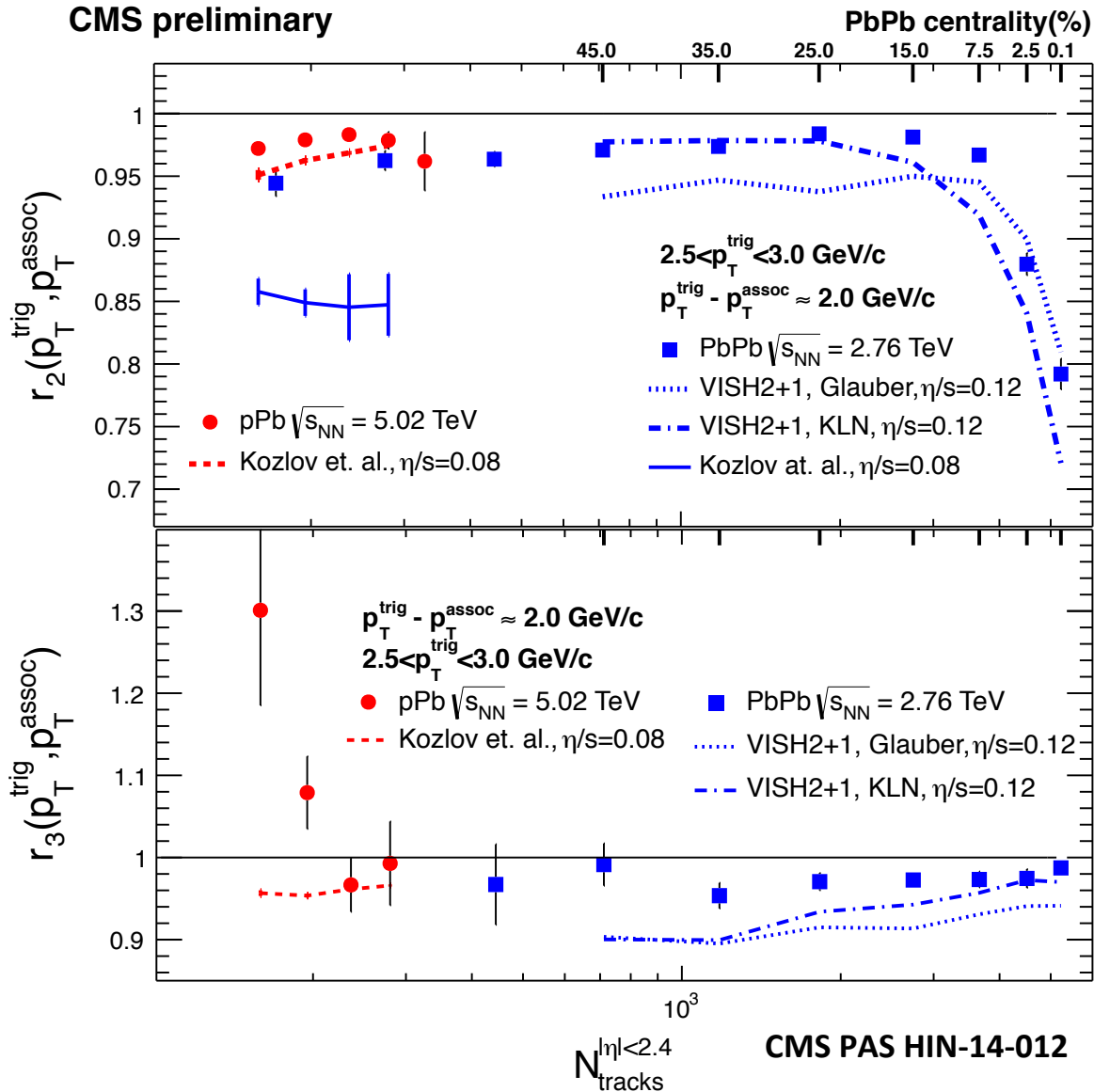


Flow Factorization



- Hydrodynamics Qualitatively consistent with PbPb

Flow Factorization



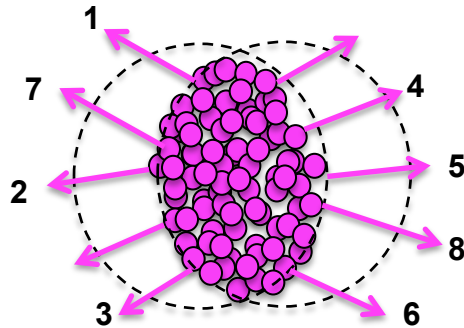
- Hydrodynamics Qualitatively consistent with PbPb and pPb

True Collectivity in pPb?

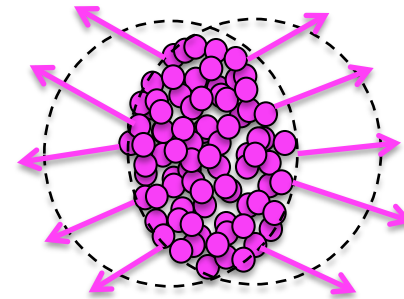
- So far, analysis are on two-particle correlations
- Question: are the correlations **only** amongst particle **pairs**?
- In hydrodynamics, correlations are expected between all particles

True Collectivity in pPb?

4-, 6- and 8-particle cumulant



Lee-Yang Zeros



- Genuine 4-, 6- and 8-particle correlations
- Insensitive to non-flow contributions from $< 4, 6$ and 8 particles
- Q-Cumulant suppress higher order interference

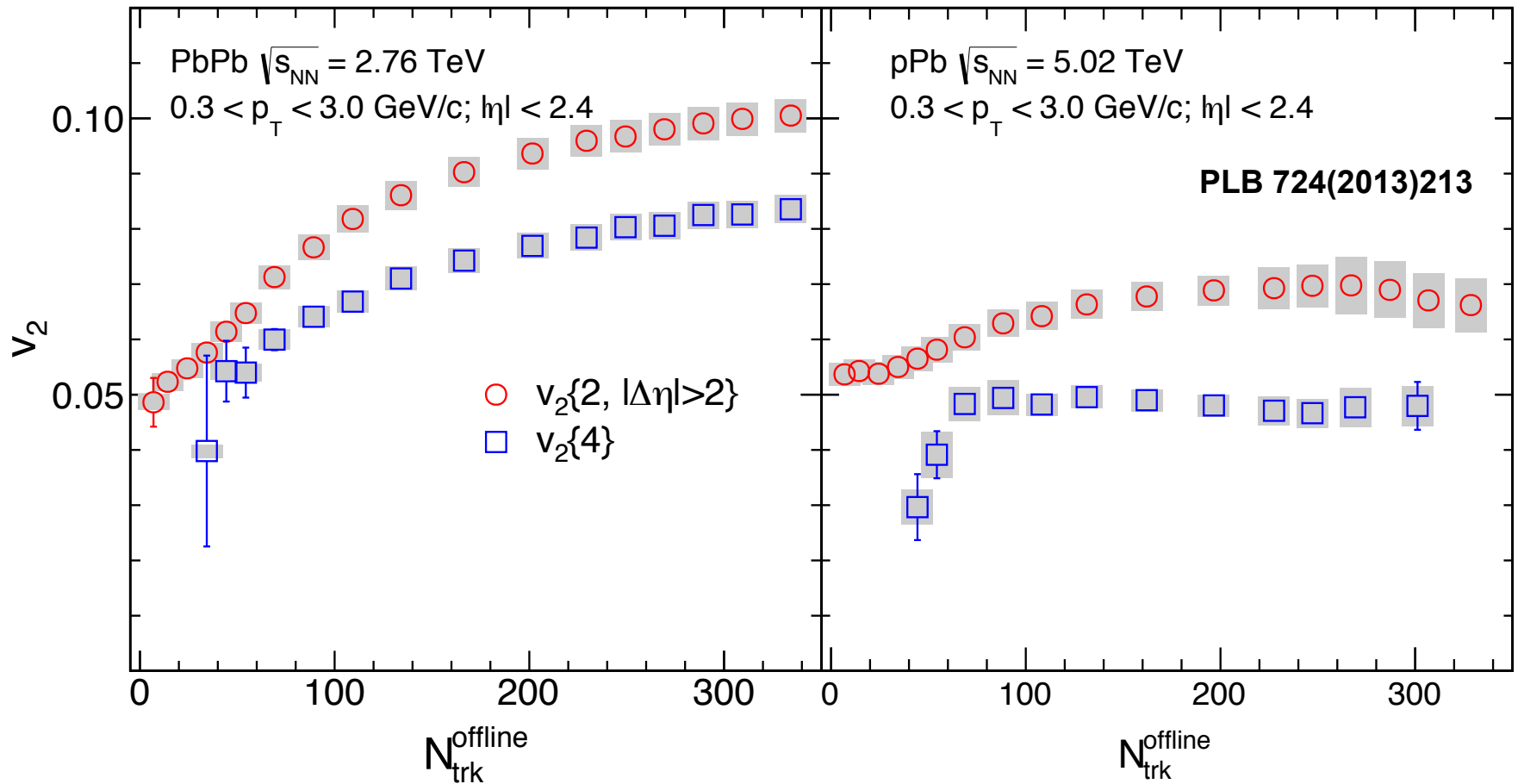
- Genuine all-particle correlation
- Built-in correction for non-uniform distribution

Hydrodynamics:

$$v_2\{2\} > v_2\{4\} \approx v_2\{6\} \approx v_2\{8\} \approx v_2\{\text{LYZ}\}$$

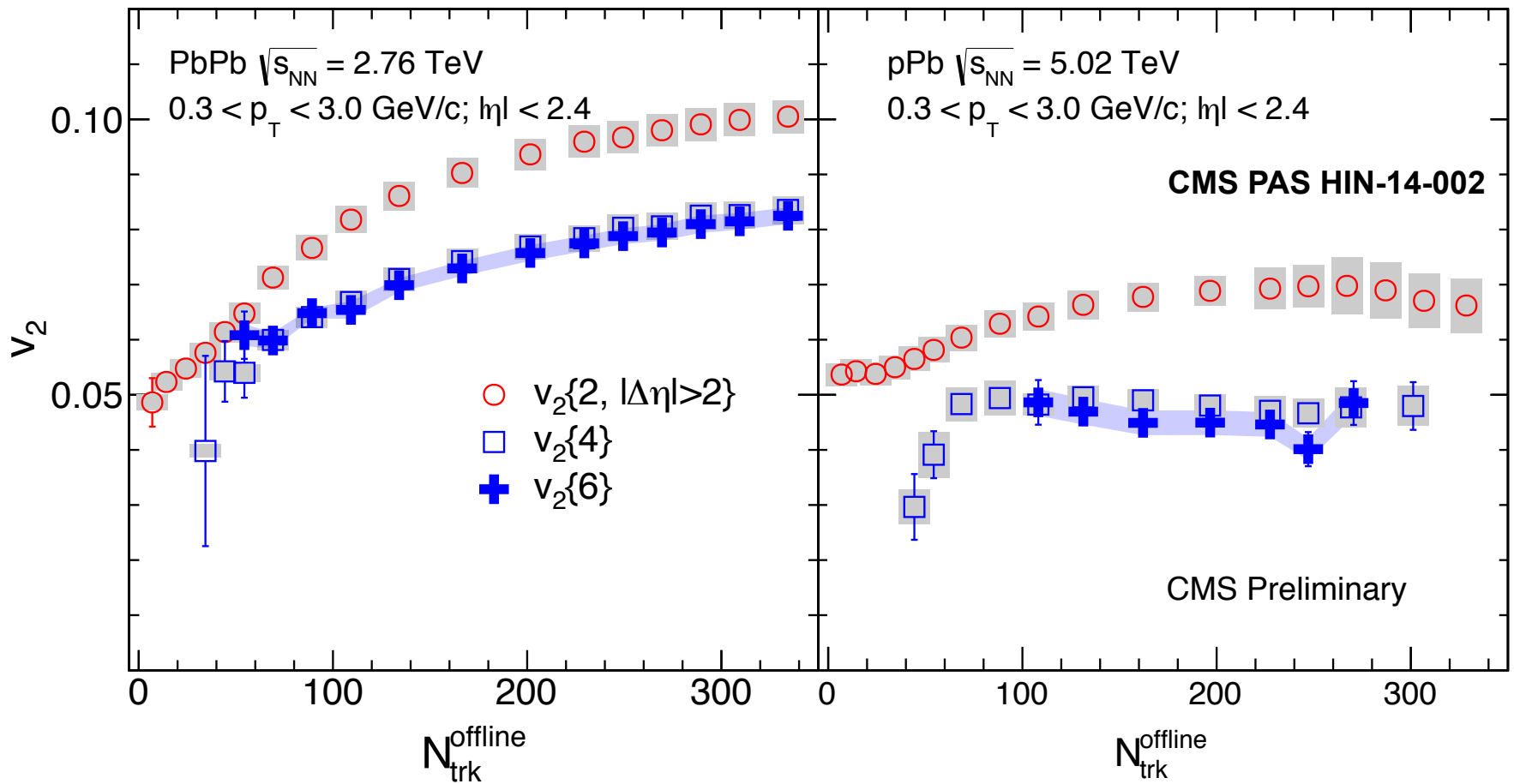
True Collectivity in pPb?

$$v_2\{2\} > v_2\{4\}$$



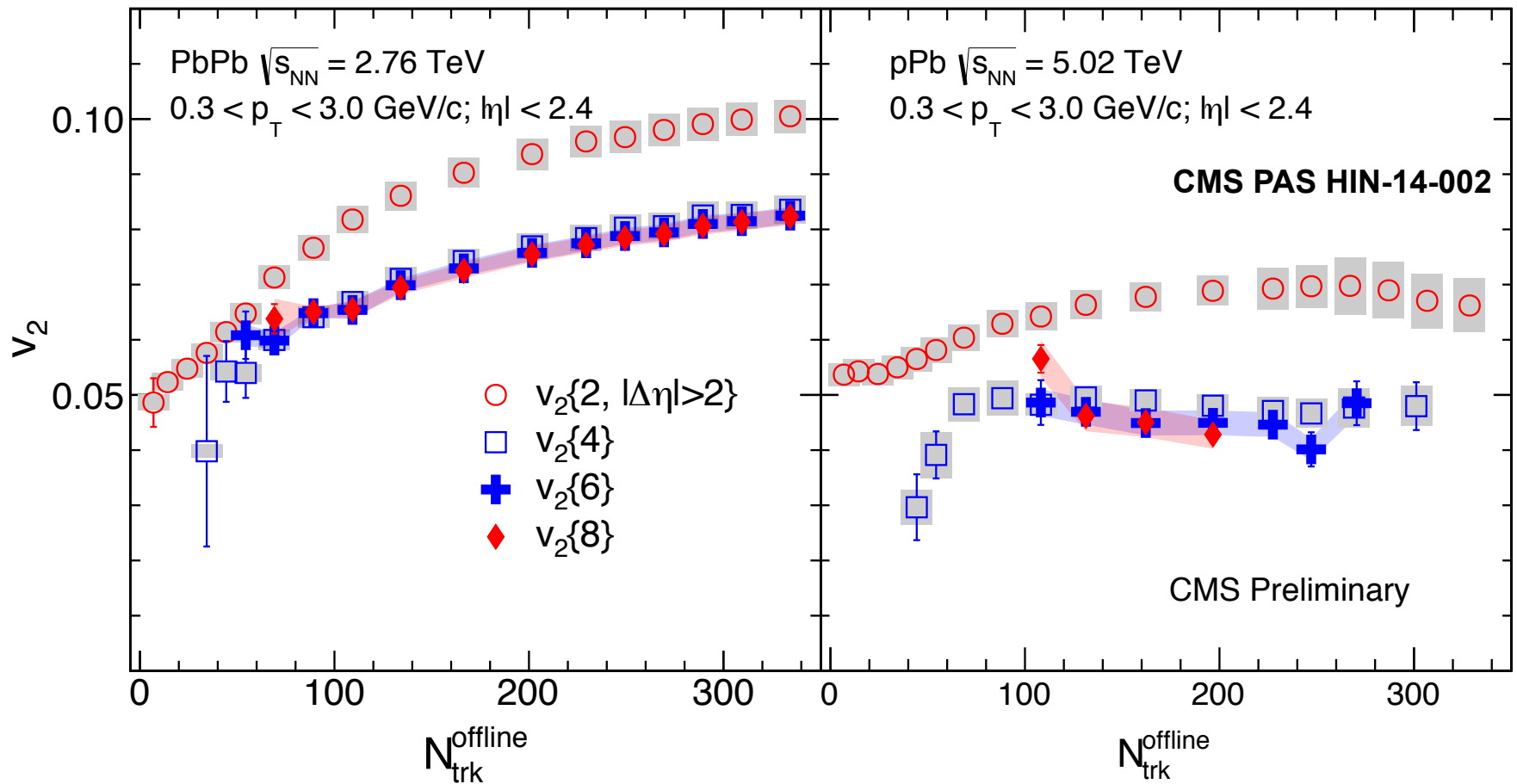
True Collectivity in pPb?

$$v_2\{2\} > v_2\{4\} \approx v_2\{6\}$$



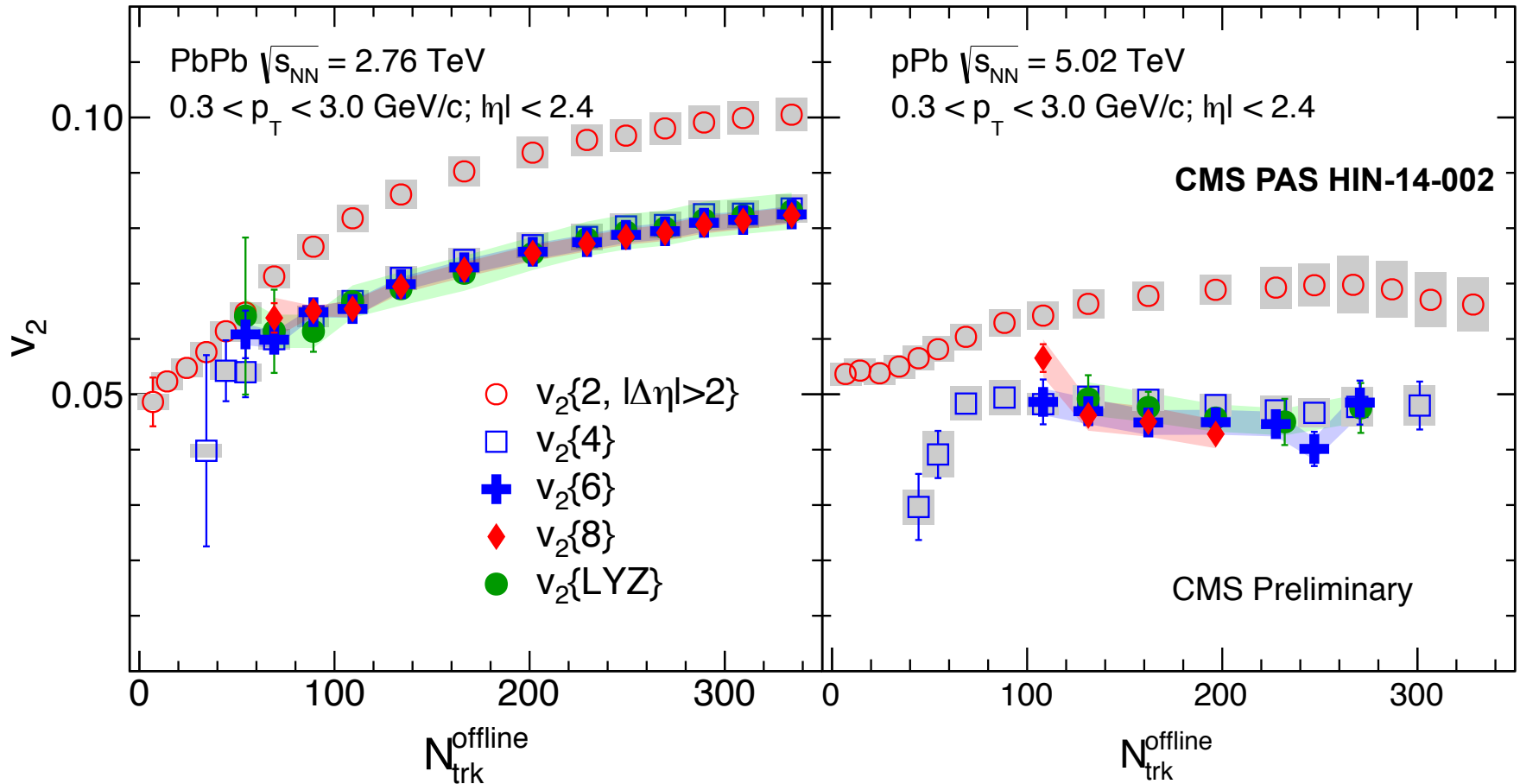
True Collectivity in pPb?

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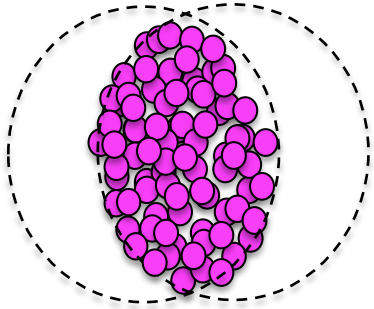
True Collectivity in pPb?

$$v_2\{2\} > v_2\{4\} \approx v_2\{6\} \approx v_2\{8\} \approx v_2\{\text{LYZ}\}$$



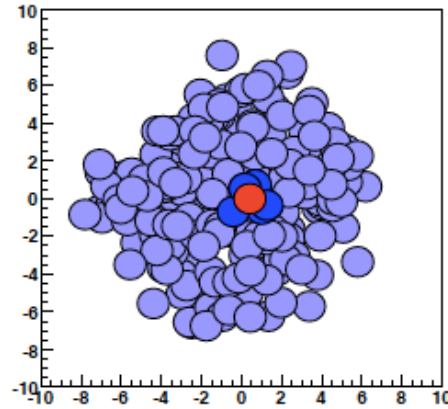
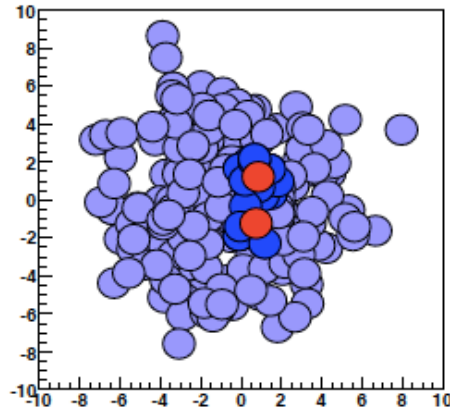
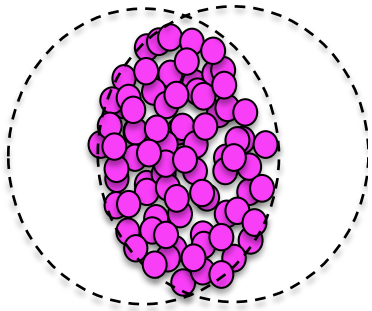
Direct evidence of strong collectivity in pPb!

Full Picture



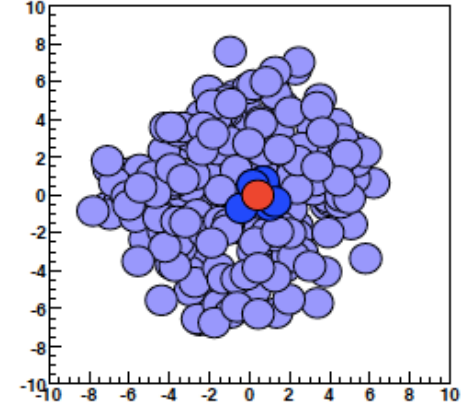
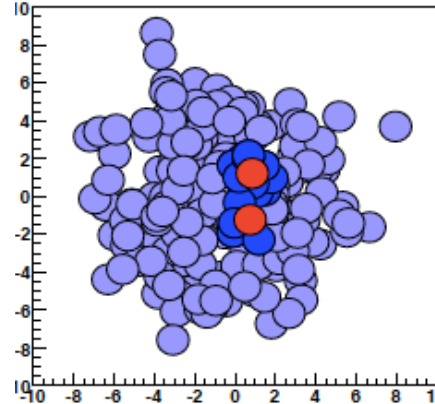
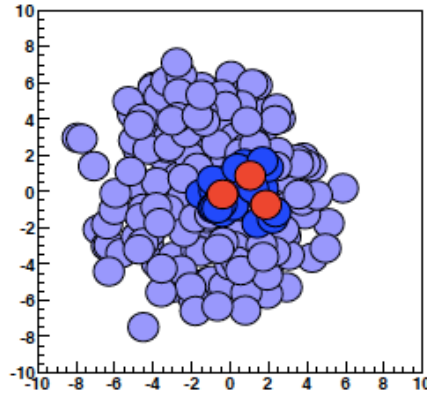
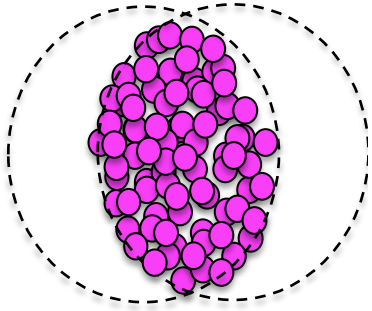
- Hydrodynamics regime in AA

Full Picture



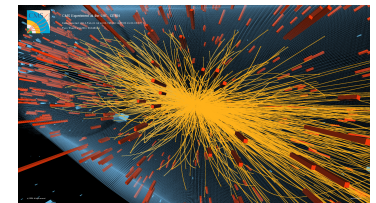
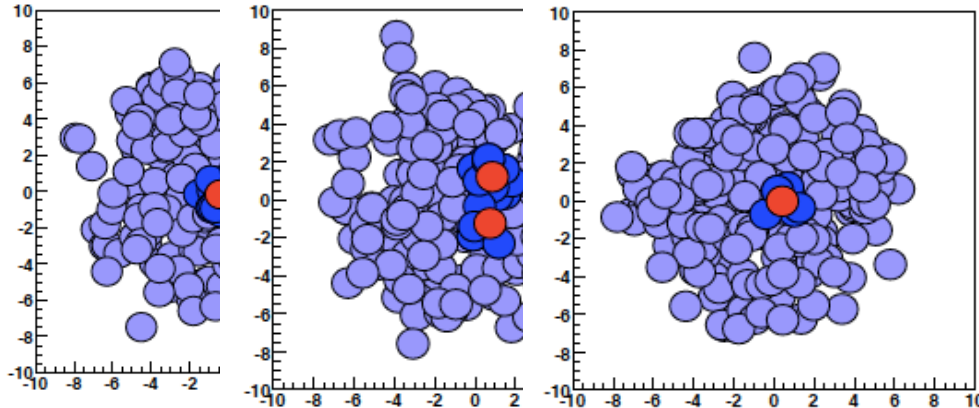
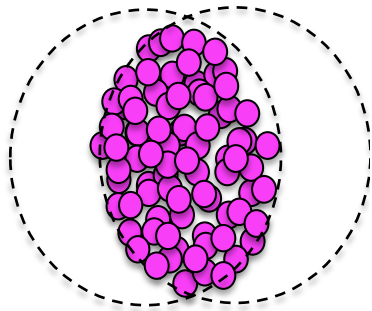
- Hydrodynamics regime in AA
- Hydrodynamics works in p(d)A, although not quite justified.
CGC [PRD 87 (2013) 094034], Non-abelian beam jet [arXiv:1405.7825],
Transport model [arXiv:1406.2804]

Look Forward



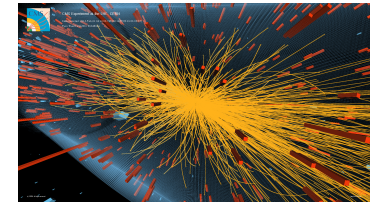
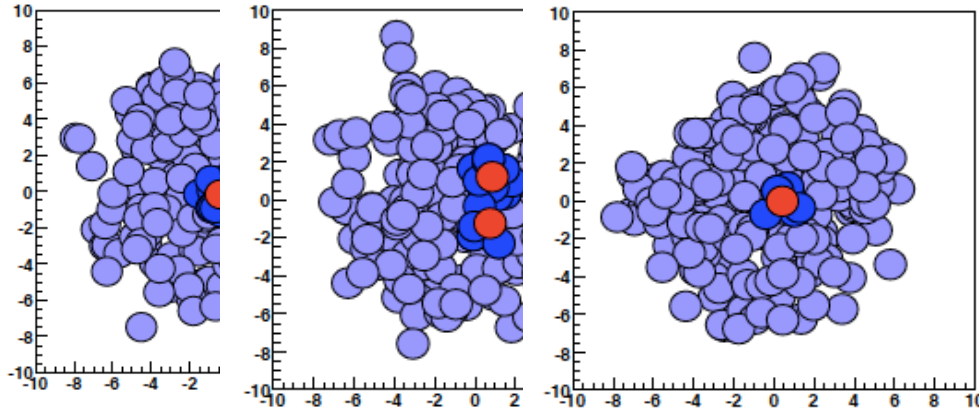
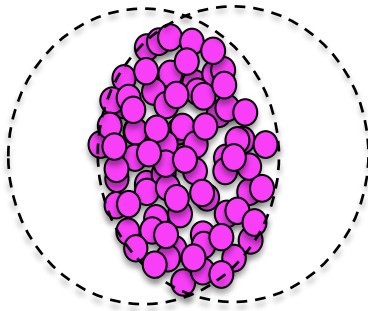
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- He³+Au at RHIC 2015 → Triangularity

Look Forward



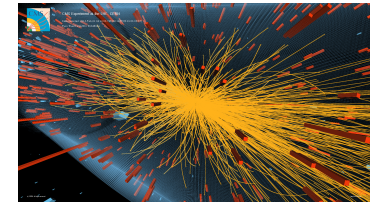
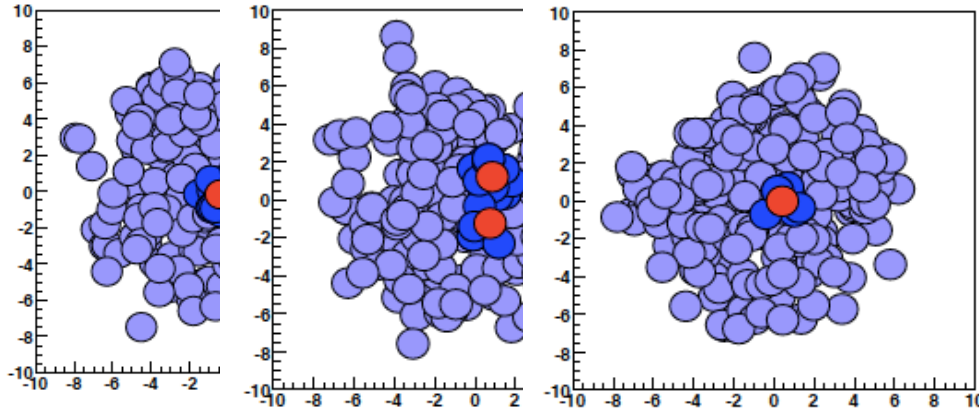
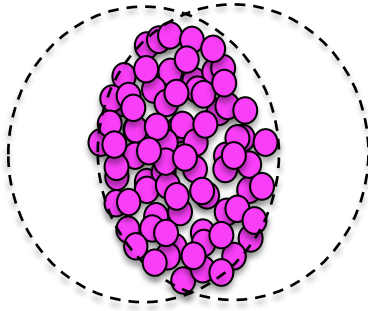
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CGC [PRD 87 (2013) 094034], Non-abelian beam jet [arXiv:1405.7825],
Transport model [arXiv:1406.2804]
- He³+Au at RHIC 2015 → Triangularity
- pp at 14 TeV at LHC 2015, energy doubled
could high multiplicity pp events flow?

Look Forward



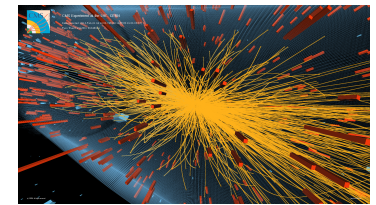
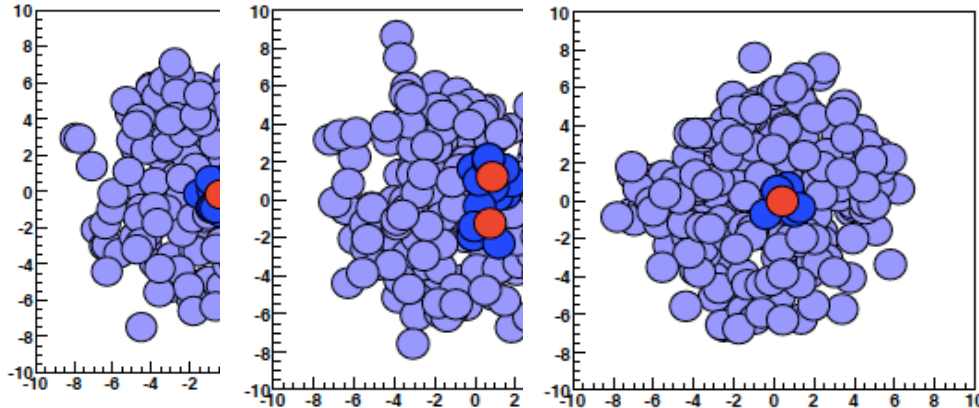
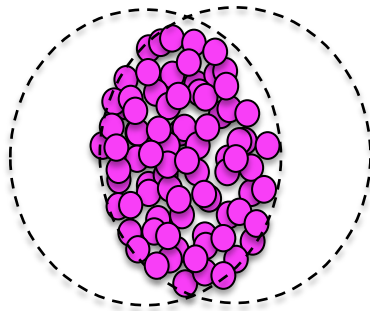
- What do we know about initial state?

Look Forward



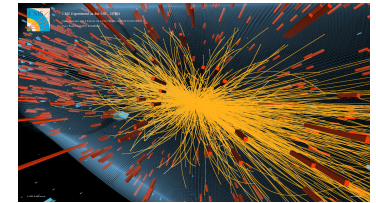
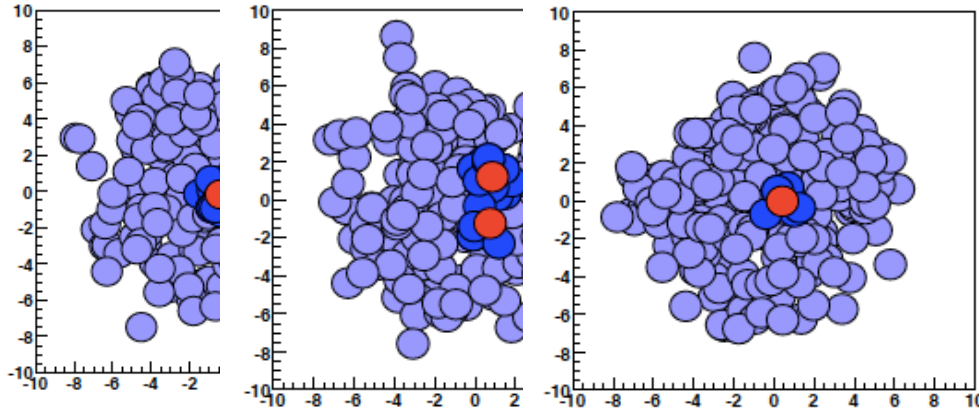
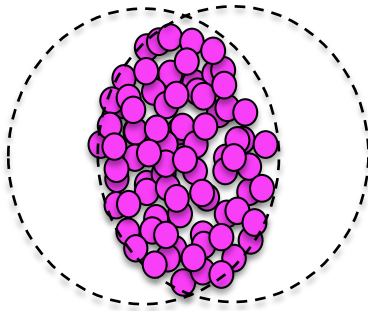
- What do we know about initial state?
- Can the initial condition for the hydrodynamics be determined?

Look Forward



- What do we know about initial state?
- Can the initial condition for the hydrodynamics be determined?
- What is the smallest collision system that behaves collectively, if collectivity is so general?

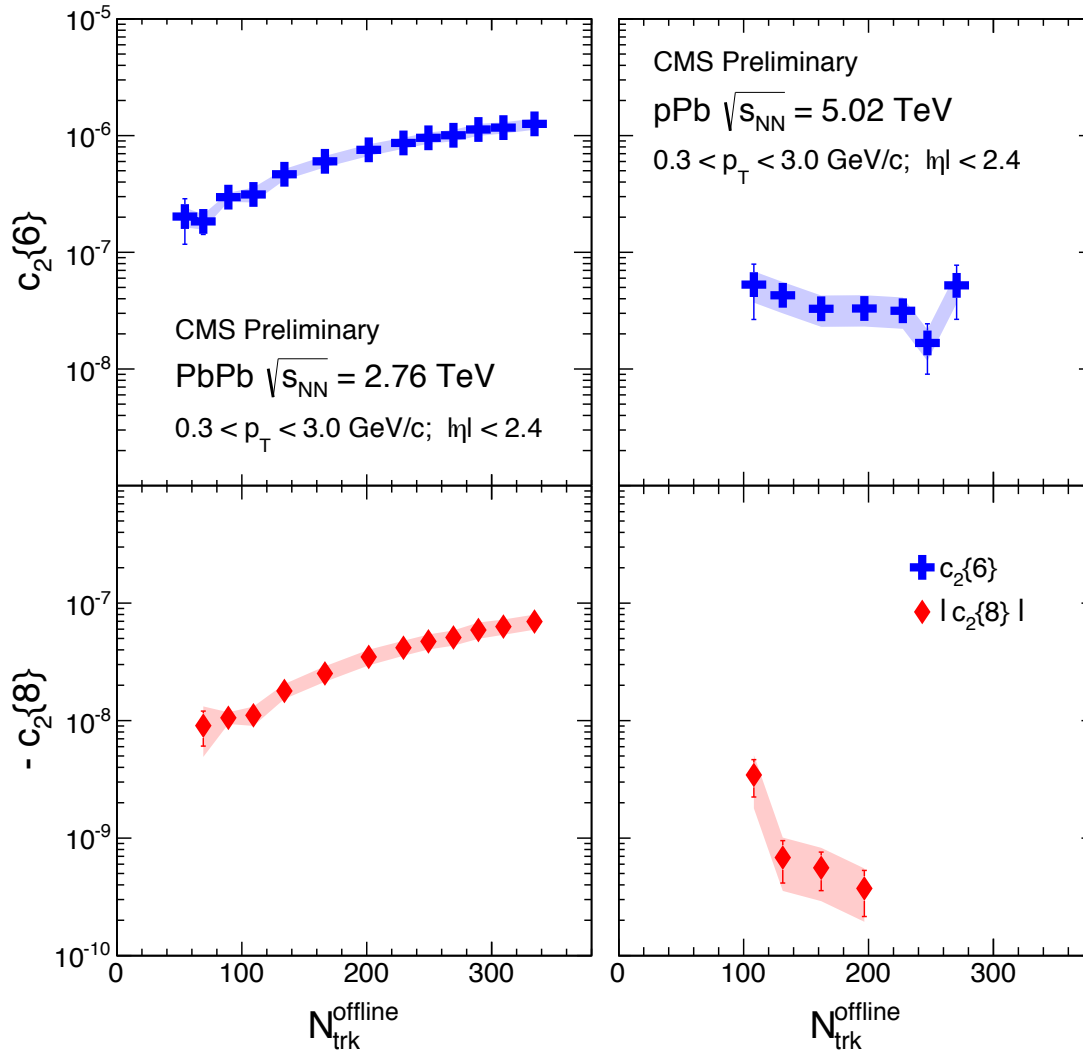
Look Forward



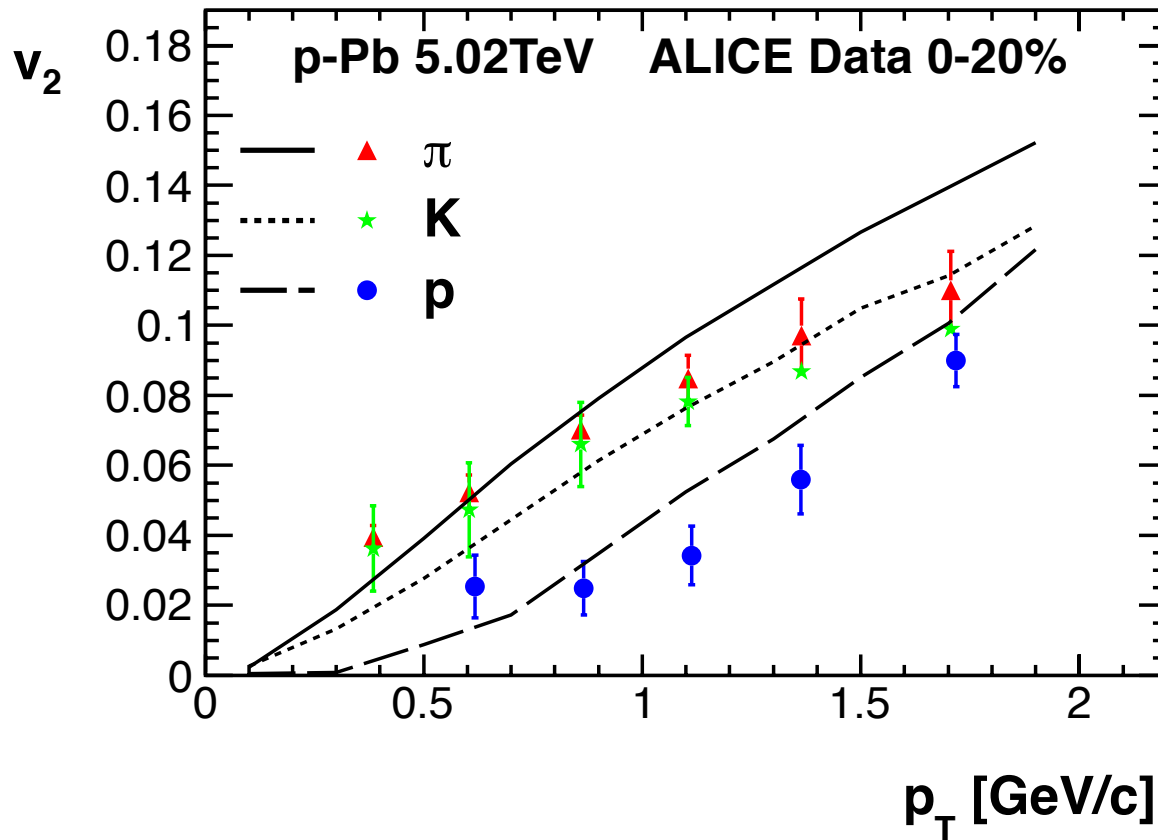
- What do we know about initial state?
- Can the initial condition for the hydrodynamics be determined?
- What is the smallest collision system that behaves collectively, if collectivity is so general?
- I am feeling lucky to be an experimentalist!

Backup

Backup



Backup



PRL 111, (2013) 172303

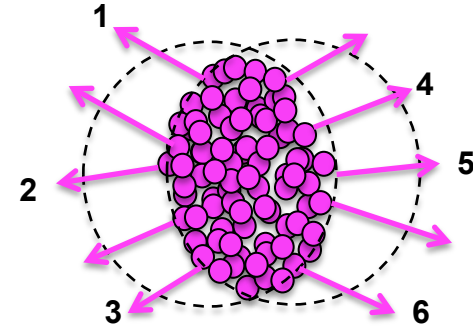
Multi-particle Cumulant

- 6-particle correlator, per event

$$\langle\langle 6 \rangle\rangle \equiv \left\langle e^{in(\phi_1+\phi_2+\phi_3-\phi_4-\phi_5-\phi_6)} \right\rangle$$

$$\equiv \frac{1}{P_{M,6}} \sum_{\substack{i \neq j \neq k \\ \neq l \neq m \neq n}}^M e^{in(\phi_i+\phi_j+\phi_k-\phi_l-\phi_m-\phi_n)}$$

Distinctive 6-particle combinations



- 6-particle cumulant, all events

$$c_n\{6\} = \langle\langle 6 \rangle\rangle - 9 \cdot \langle\langle 4 \rangle\rangle \langle\langle 2 \rangle\rangle + 12 \cdot \langle\langle 2 \rangle\rangle^3$$

- Q-Cumulant: decompose \rightarrow flow vector $Q_n \equiv \sum_{i=1}^M w_i e^{in\phi_i}$

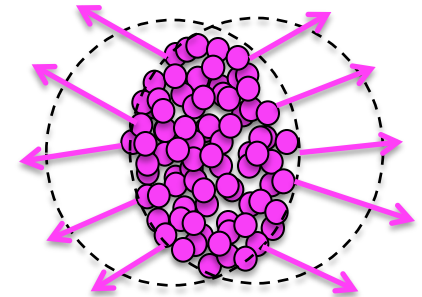
- Cumulant $v_n \rightarrow$

$$v_n\{4\} = \sqrt[4]{-c_n\{4\}}, v_n\{6\} = \sqrt[6]{\frac{1}{4}c_n\{6\}}, v_n\{8\} = \sqrt[8]{-\frac{1}{33}c_n\{8\}}$$

Lee-Yang Zeros

- All-particle correlation, per event

$$g(ir) \equiv \prod_{j=1}^M \left[1 + i \cdot r \cdot w_j \cos(n(\phi_j - \theta)) \right]$$



- Generating function, all events

$$G(ir) = \langle g(ir) \rangle = \frac{1}{N_{evt}} \sum_{events} g(ir)$$

Decompose



Flow vector:

$$Q_n = (Q_{nx}, Q_{ny})$$

$$Q_{nx} = \sum_{j=1}^M w_j \cos(n\phi_j)$$

$$Q_{ny} = \sum_{j=1}^M w_j \sin(n\phi_j)$$

- Integrated $v_{nj}\{LYZ\}$

$$V_2\{LYZ\} = \frac{v_{j_01}}{r_0}$$

$j_{01} = 2.40483$
 r_0 is the first zero of $|G(ir)|$

