

# Bridging two-proton emitters and neutron halos

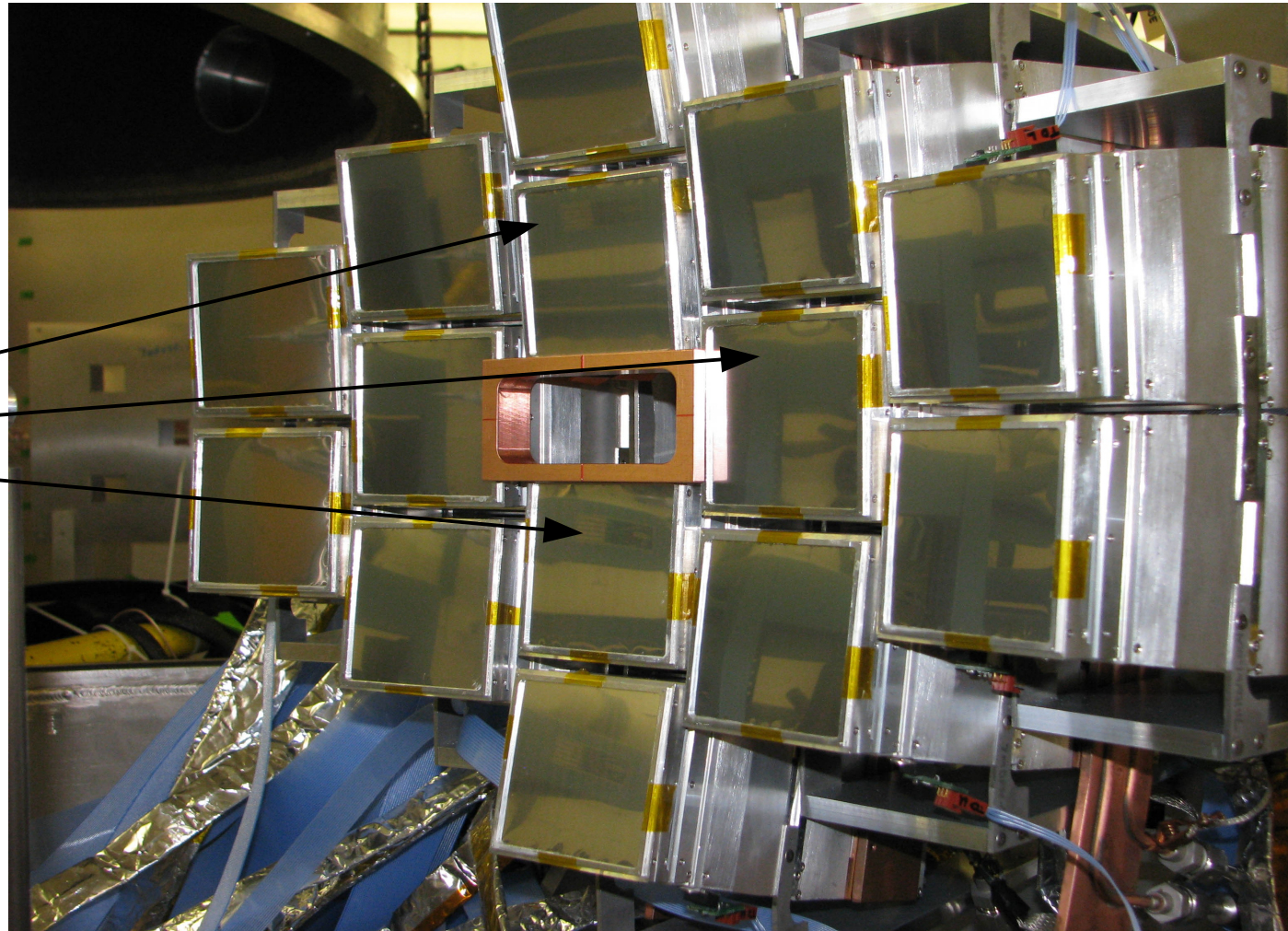
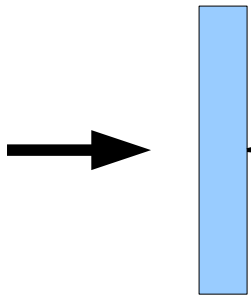
Robert Charity

Washington University in St. Louis



HiRA array  
 Washington University  
 Michigan State,  
 Western Michigan  
 Indiana University  
 Milan

High Resolution Array.



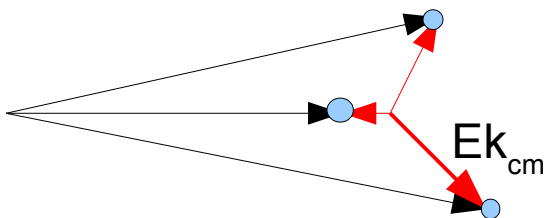
Parent nucleus decays in target.  
 Detect decay products in HiRA.  
 Need high angular resolution  
 (Si Strips)

1.5 mm DSSD has 32x32 strips  
 ~800 Si strips in experiment.

Chip readout.

Multi-hit capability – multiple fragments in a single telescope

Si-CsI E-ΔE telescopes



Invariant Mass Method

$$M_{inv} = \sum_i Ek_{cm}^i + M^i. \quad \text{decay energy } E_T = \sum_i Ek_{cm}^i$$

$$E^* = M_{inv} - M_{g.s.} = E_T - Q_{breakup}$$

An example of we get from an experiment

$E/A=70$  MeV  $^{12}\text{C} + ^9\text{Be}$  reaction with HiRA

Found so far 42 resonances in  $^{5,6,7}\text{Li}$ ,  $^{6,7,8}\text{Be}$ ,  $^{7,8,9}\text{B}$  and  $^{8,9,10}\text{C}$

These consist of

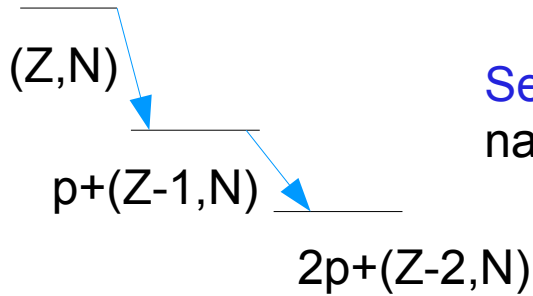
- 21 2-body exit channels
- 13 3-body exit channels (sequential and prompt decays)
- 7 4-body exit channels  $2p+d+\alpha$ ,  $p+\alpha+^3\text{He}$ ,  $2p+2\alpha$ ,
- 1 5-body exit channels  $4p+\alpha$

Most of these were known (can be used to check energy and angular calibration and simulations of detector resolution.)

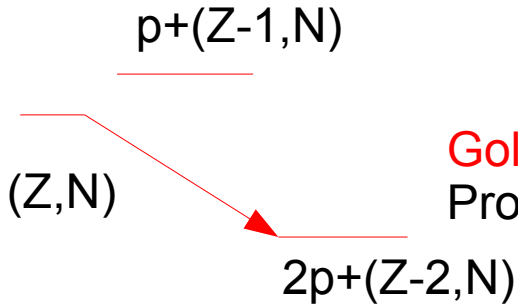
These include 6 previously unknown states and 14 cases where the resonance was previously known but we provided new information. (excitation energy, width, spin, decay path, branching ratios).

# 3, 4, 5-body exits channels: Prompt or Sequential?

## Look at 2p decay for example



**Sequential**,  
narrow intermediate state  $^{10}\text{C}^*$ ,  $^{13}\text{O}^*$ ,  $^{17}\text{Ne}^*$ ,  $^{16}\text{Ne}^*$

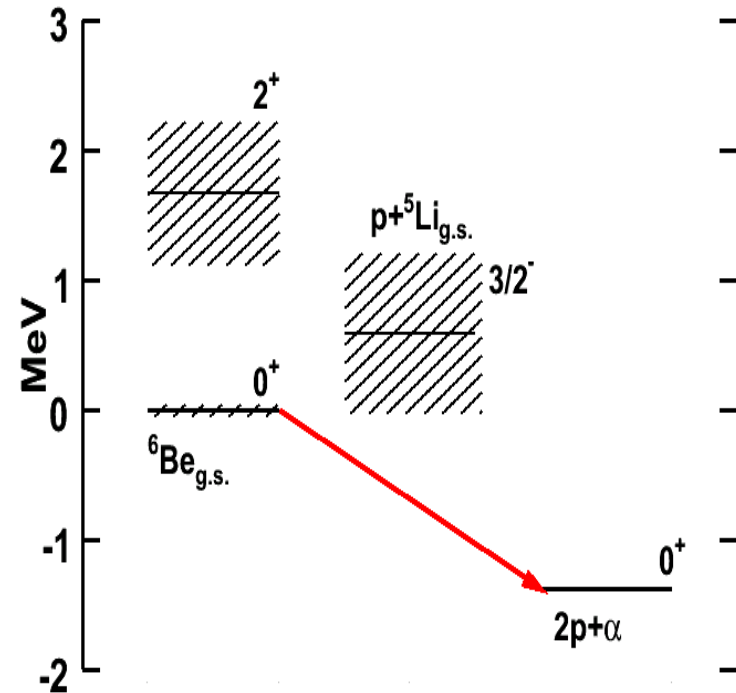


**Goldansky**, even Z (pairing) ( $^{45}\text{Fe}$ ,  $^{48}\text{Ni}$ )  
Prompt 2p decay



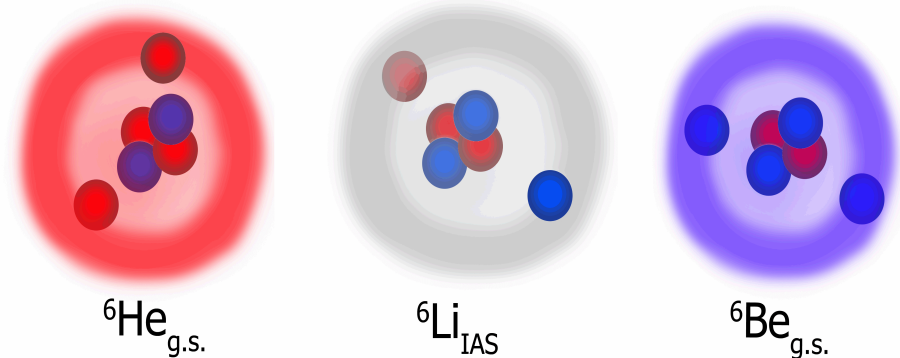
**Democratic**, wide intermediate state  
Lifetime too short and so must  
treat as prompt 2p decay.  
Again pairing can be important (even Z)

2p decay of light ground-state nuclei can be a combination of Goldansky and Democratic e.g.  $^6\text{Be}$



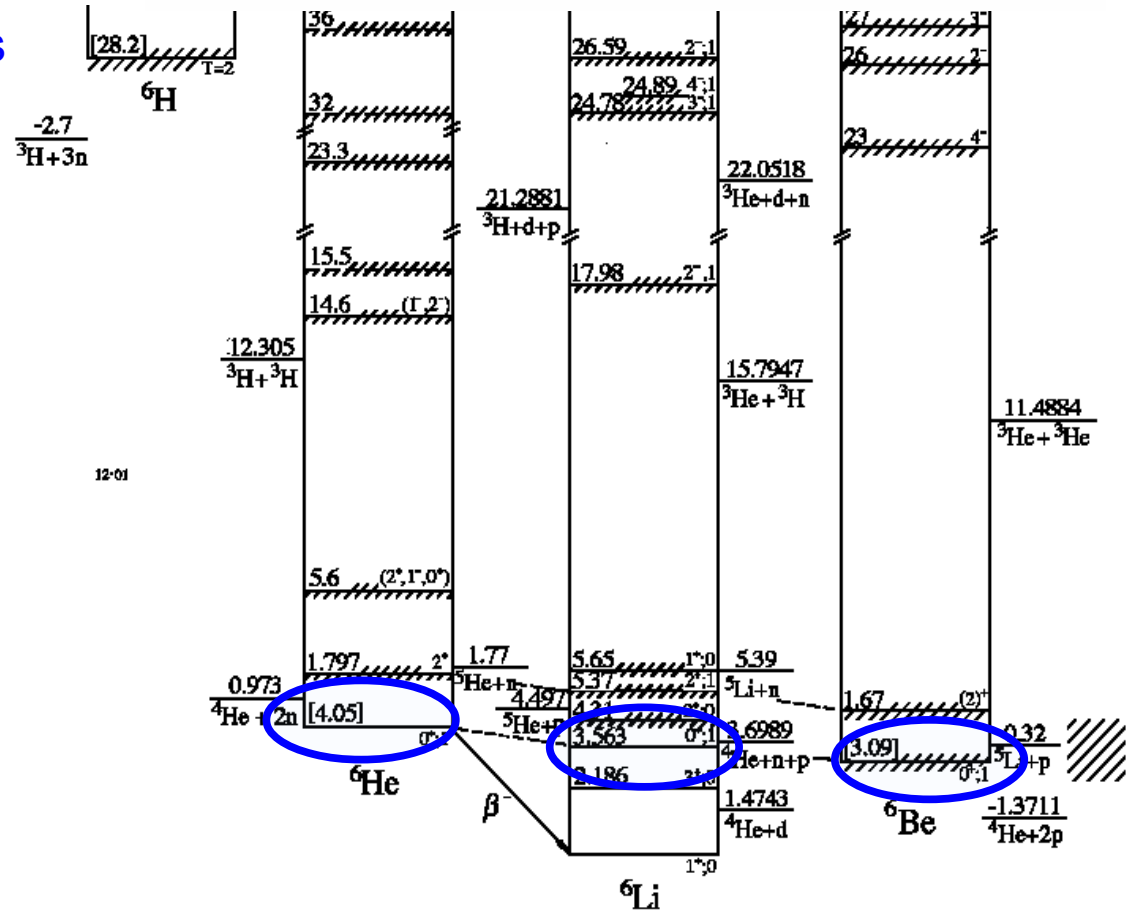
# Relationship between $2p$ decay and $2n$ -halo nuclei

The lightest  $2p$ -decayer  ${}^6\text{Be}_{\text{gs}}$  is the mirror to the  $2n$ -halo system  ${}^6\text{He}$ . Together with  ${}^6\text{Li}$  (IAS) form a isospin triplet with “two-nucleon halo”.



$A=6$   $T=1$  triplet

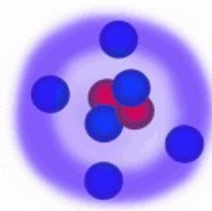
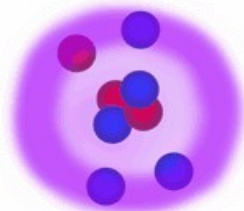
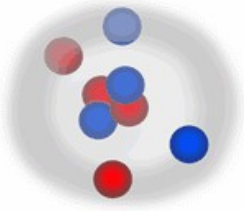
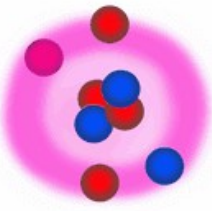
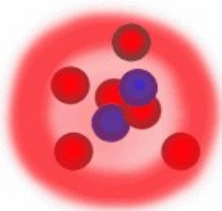
All members have a “halo structure”  
 $n$ - $n$ ,  $n$ - $p_{T=1}$ , and  $p$ - $p$  pairing interactions  
 in halo



4n- halo

mixed 2n+2p halo

Leaky 4p-halo



Halo structure of T=2 quintet  
α core + 4-nucleon halo

$^8\text{He}_{\text{g.s.}}$

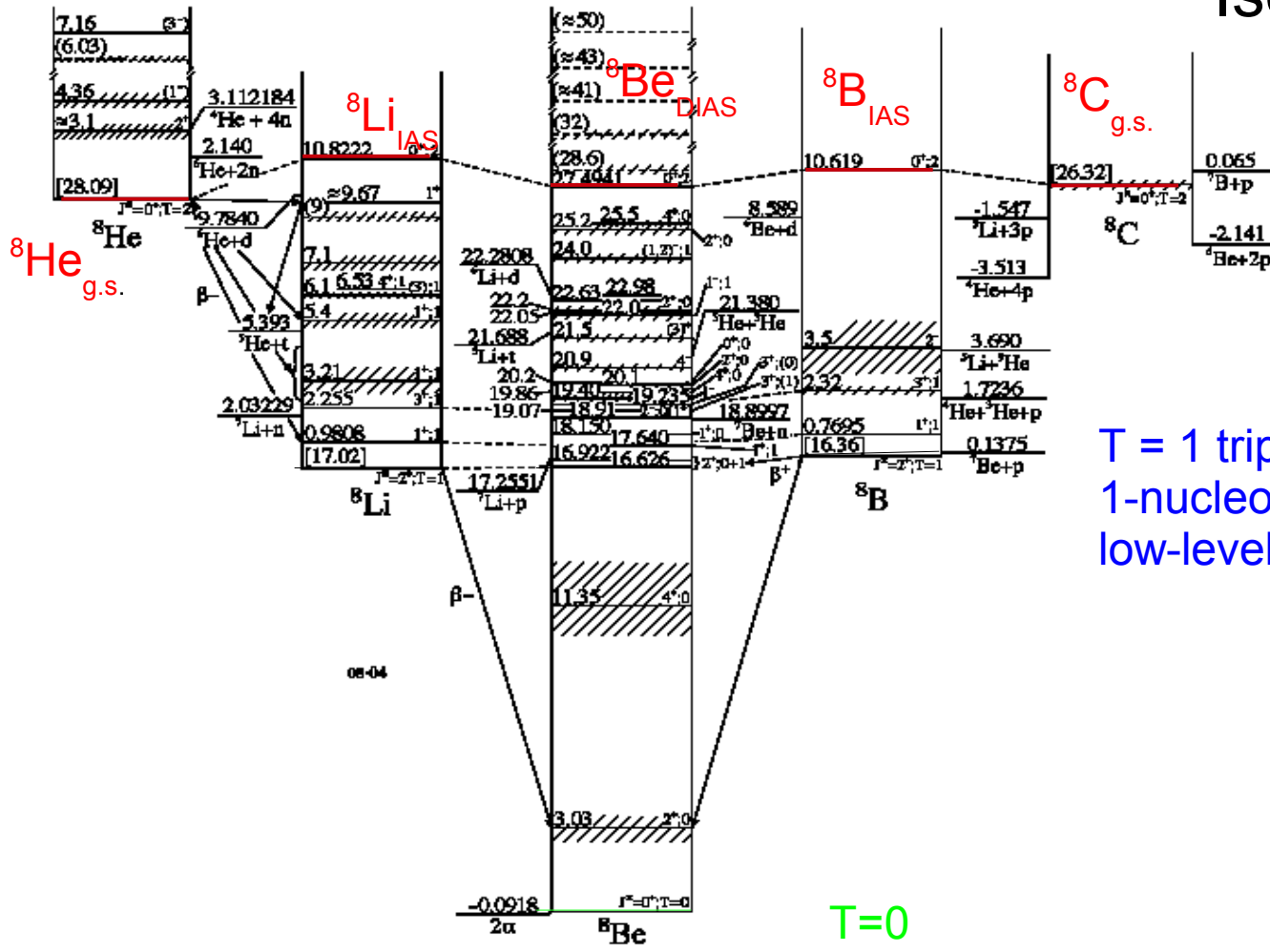
$^8\text{Li}_{\text{IAS}}$

$^8\text{Be}_{\text{DIAS}}$

$^8\text{B}_{\text{IAS}}$

$^8\text{C}_{\text{g.s.}}$

Isobaric multiplets for A=8



T = 2 quintet (2T+1)  
4-nucleon halo  
high-level bridge

T = 1 triplet (2T+1)  
1-nucleon halo  
low-level bridge

T=0

$T_z=2$

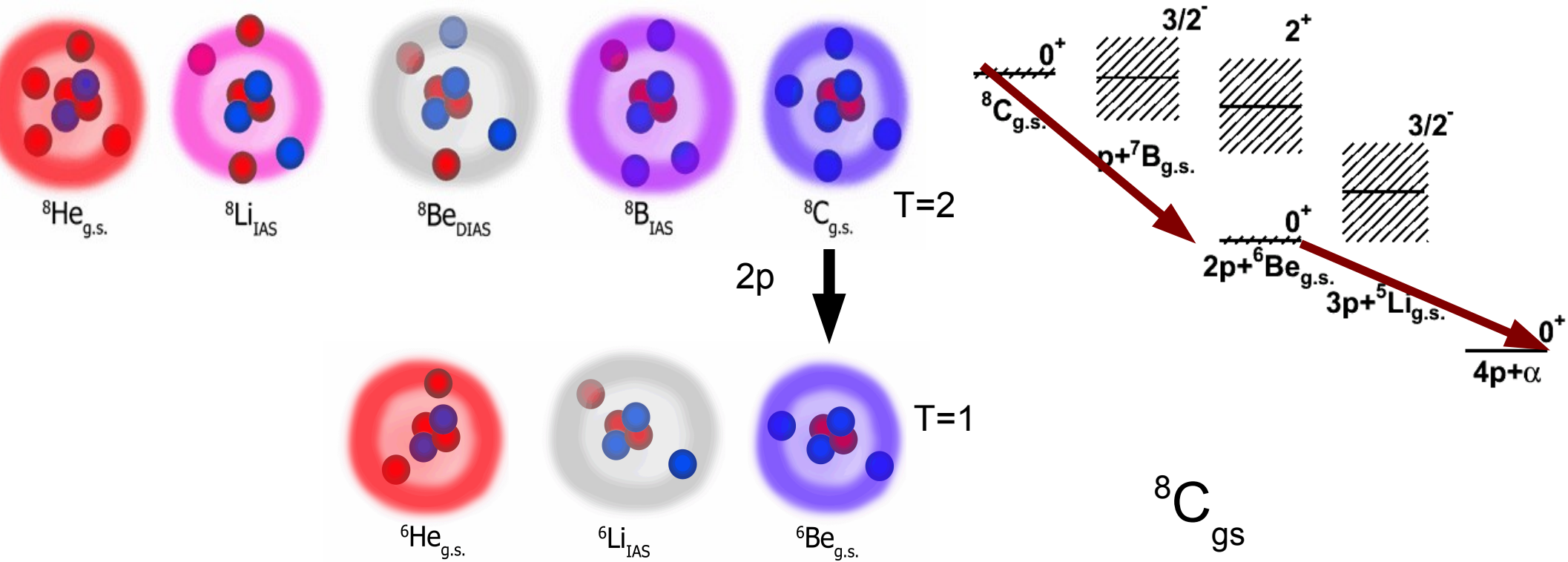
$T_z=1$

$T_z=0$

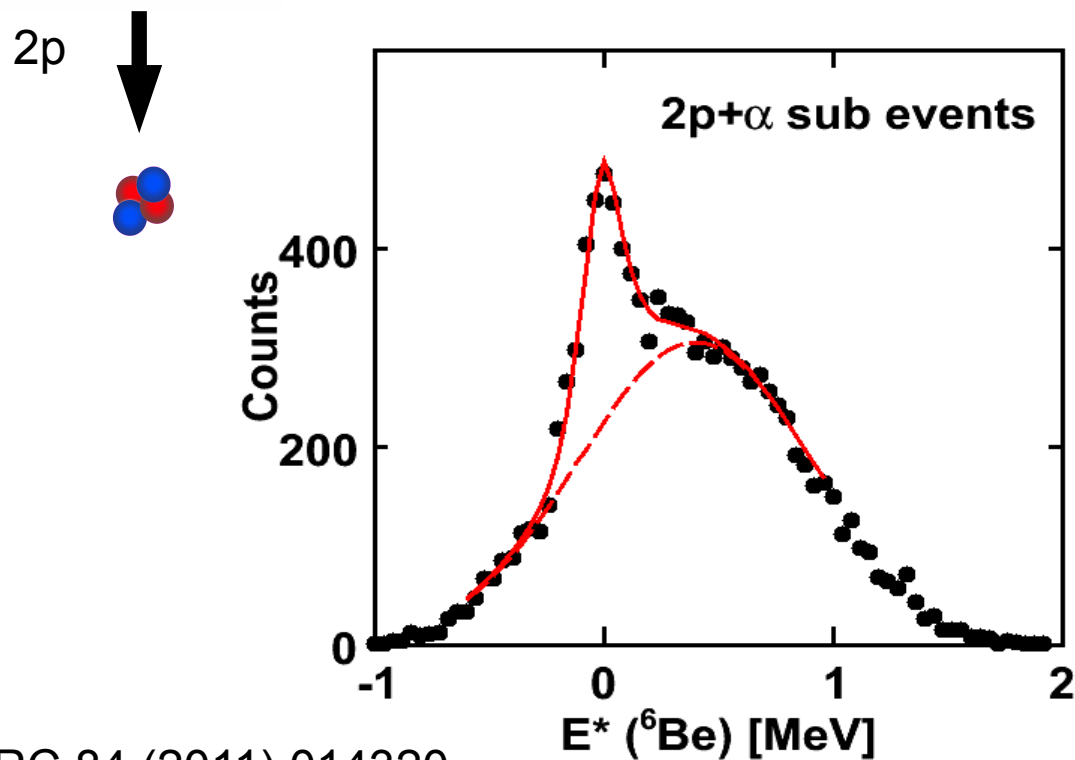
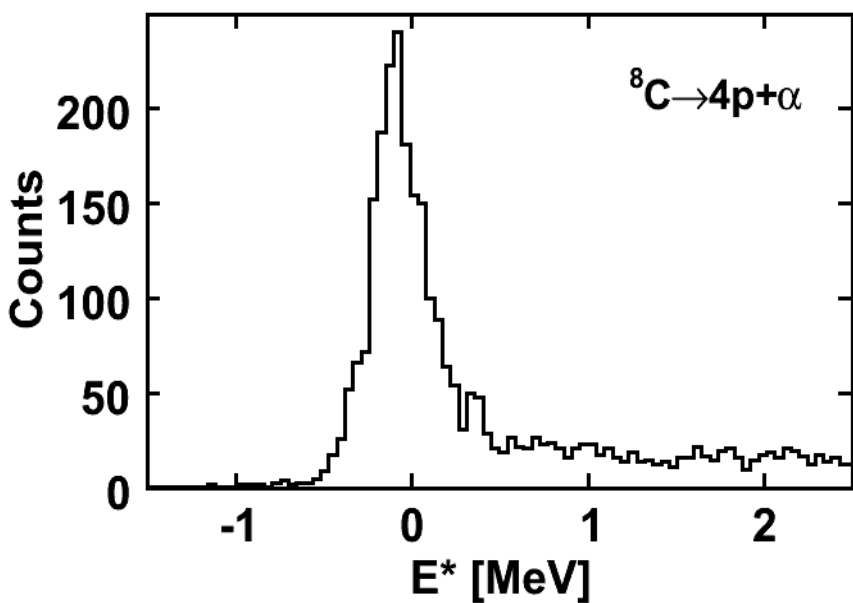
$T_z=-1$

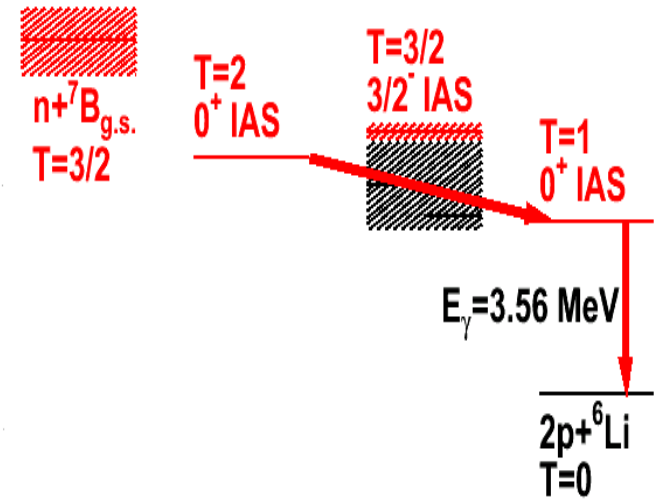
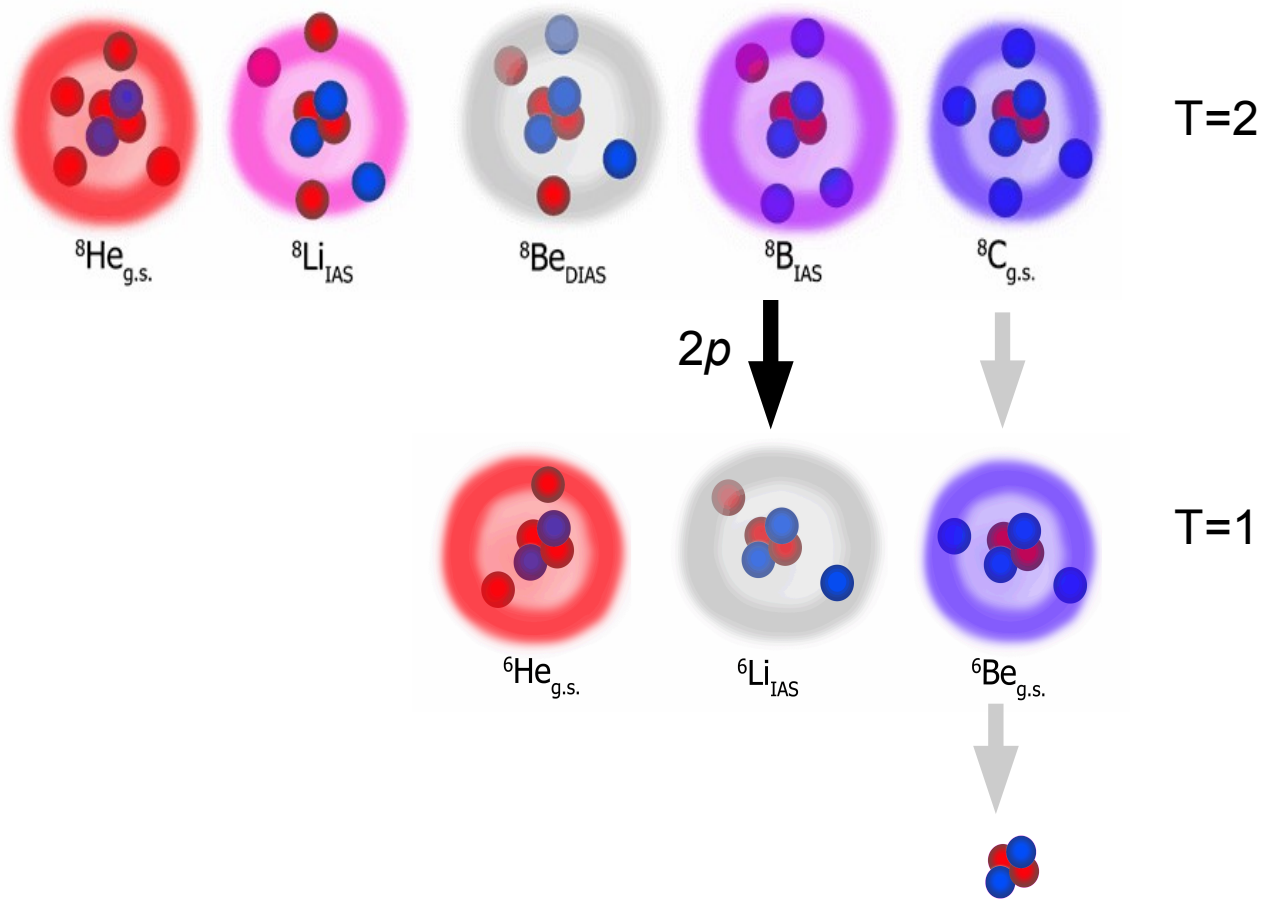
$T_z=-2$





${}^8\text{C}$  formed from a  $n$ -knockout from  ${}^9\text{C}$  beam at MSU.  
 Detect  $4p+\alpha$  decay products in HiRA.



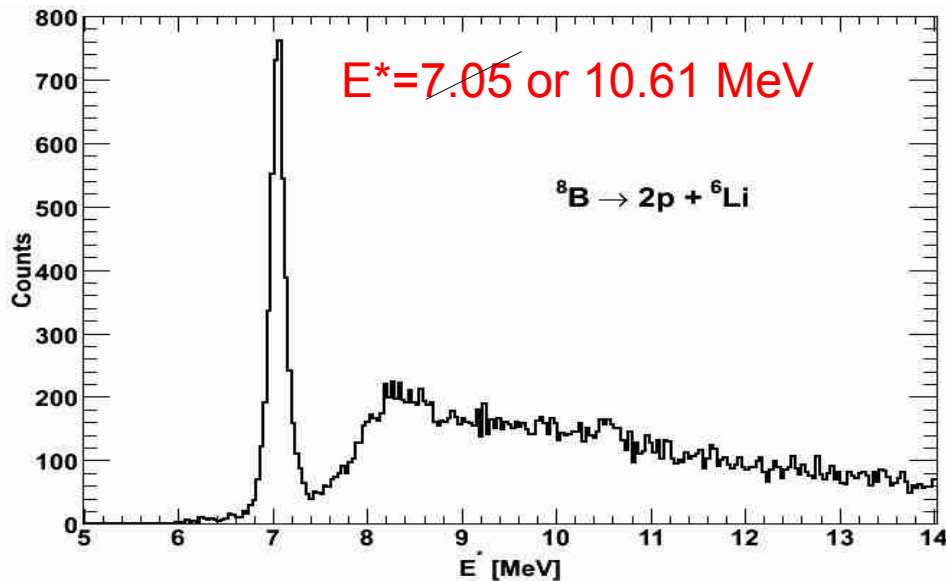


Does the isobaric analog of  ${}^8\text{C}$  undergo prompt  $2p$  decay?  
 An analog decay of  ${}^8\text{C}_{\text{g.s.}}$

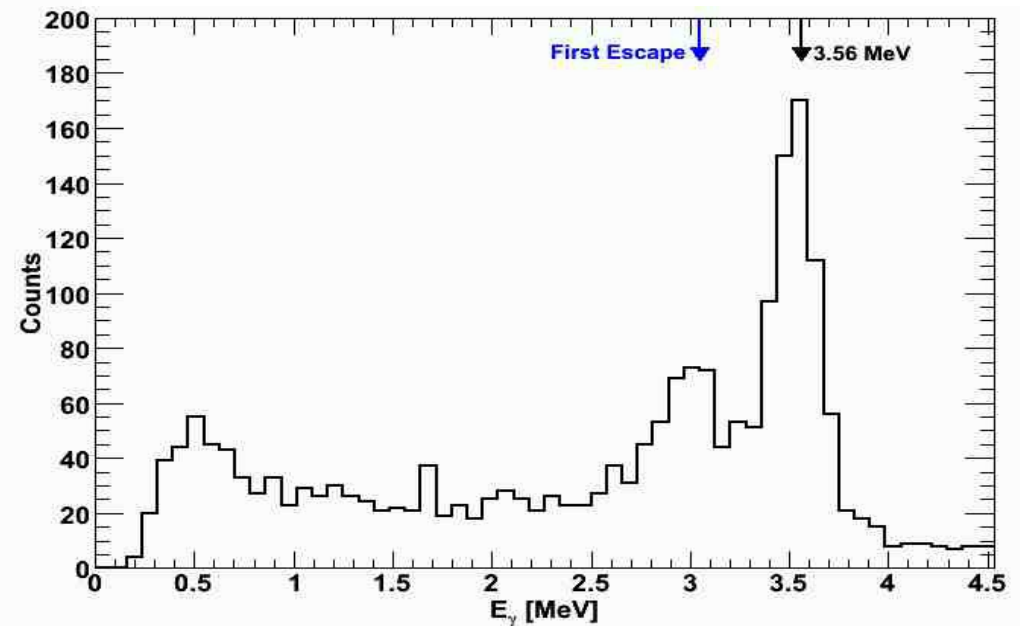
${}^8\text{B}_{\text{g.s.}}$   $T=1$     $p+{}^7\text{Be}$   $T=1/2$

## Experiment with CAESAR + HiRA

$^8\text{B}$  (IAS) formed from a  $p$ -knockout from  $^9\text{C}$  beam at MSU.  
Detect  $2p+^6\text{Li}$  decay products in HiRA.



Doppler-corrected  $\gamma$ -spectra  
gated on  $2p+^6\text{Li}$  peak



New class of  $2p$  emitter. Single proton emission violates isospin conservation. The only isospin allowed decay is a prompt  $2p$  emission. Goldansky-type decay if isospin is conserved

# Isobaric Multiplet Mass Equation

If no Coulomb and isospin is a good quantum Number, then mass of neutron = mass of proton. All members of an isobaric multiplet would have the same mass.

Differences in masses comes mainly from  $n-p$  mass difference and the Coulomb energy. Wigner showed that for a multiplet with isospin  $T$ , the mass is

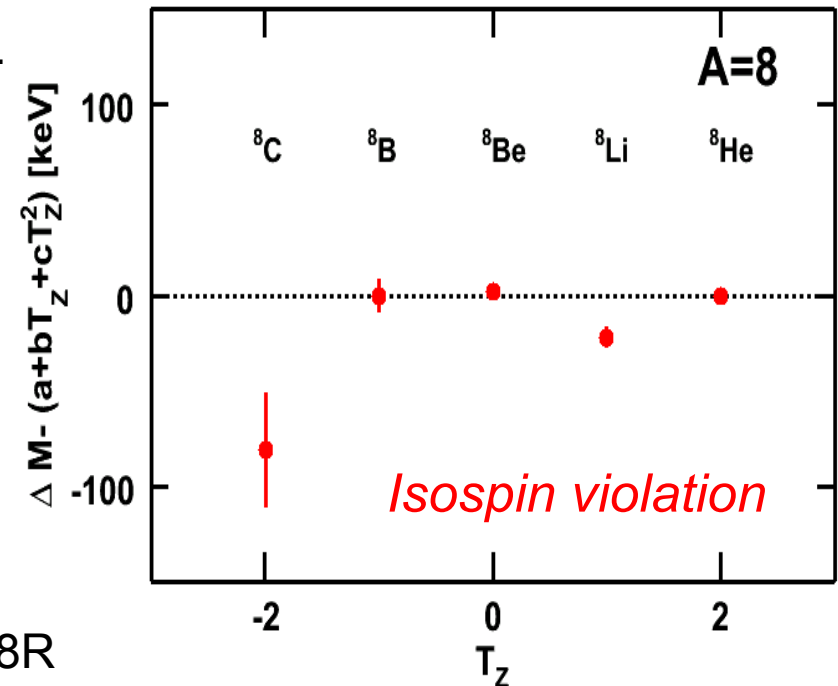
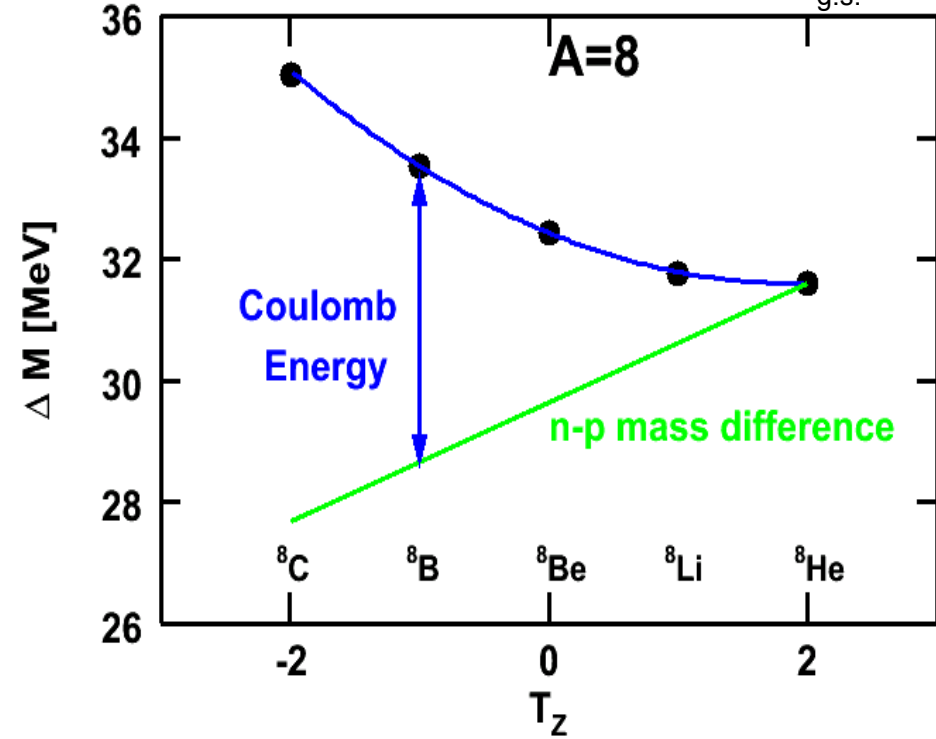
$$M(T, T_z) = a + b T_z + c T_z^2$$

$$T_z = (N-Z)/2 = \text{isospin projection}$$

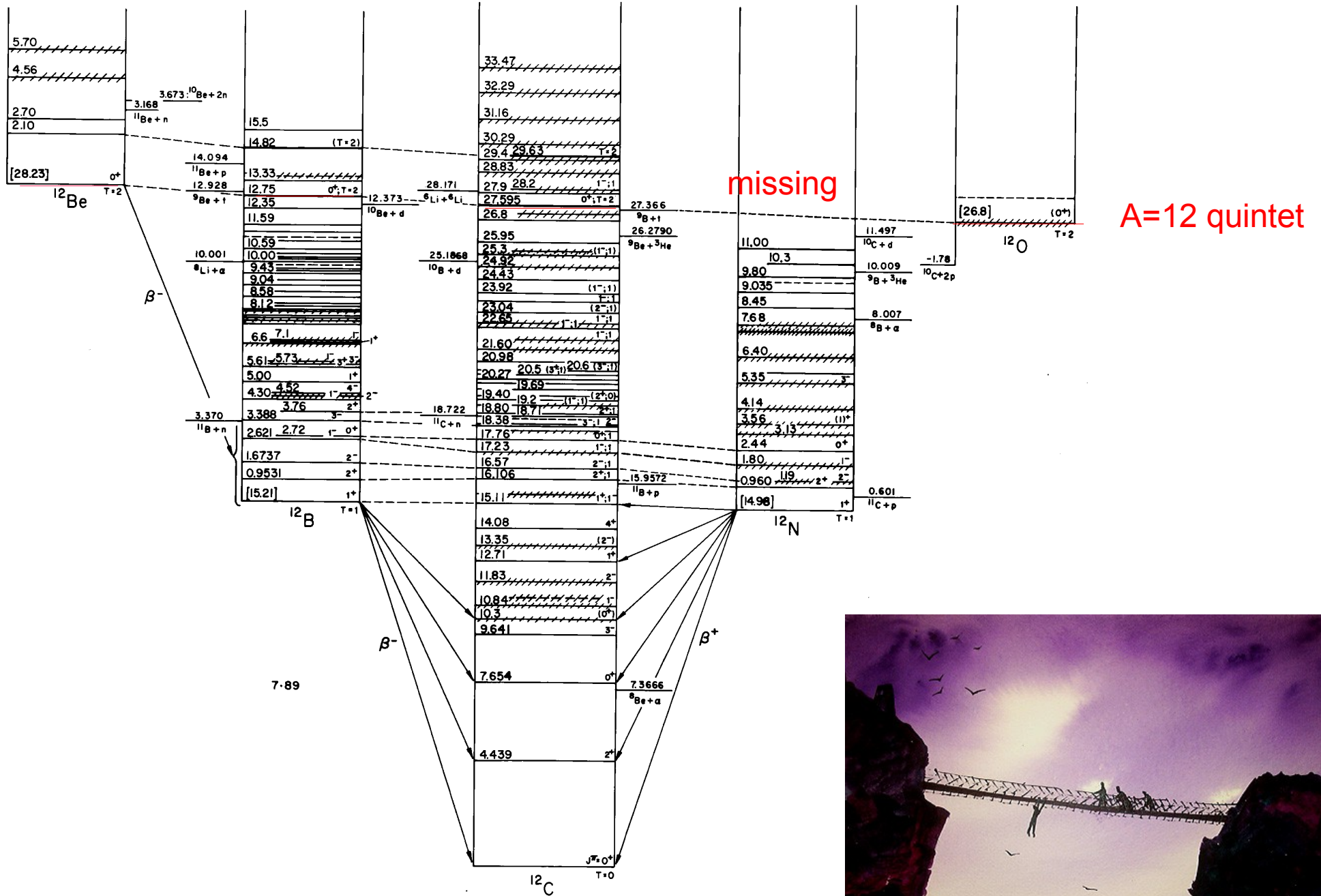
Deviations to this would be related to non-isospin conserving nuclear forces. The IMME works quite well, with only a few exceptions. However,  $A=8$  quintet is the largest deviation known.



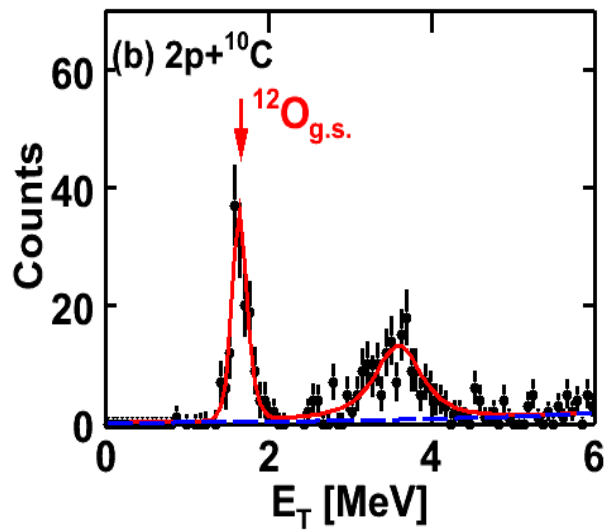
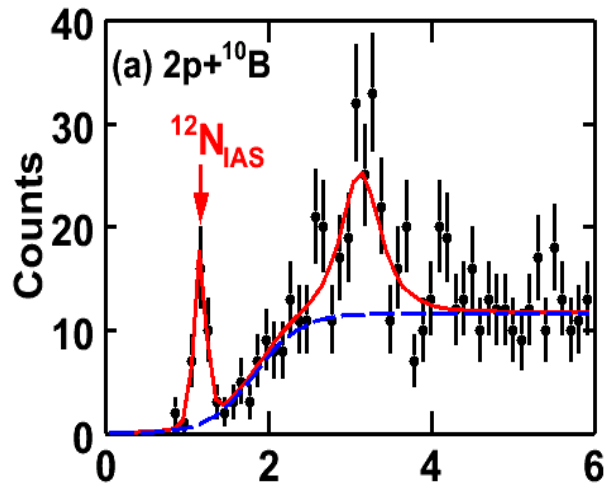
New mass measurement of  ${}^8\text{C}_{\text{g.s.}}$



# Bridges with missing pieces



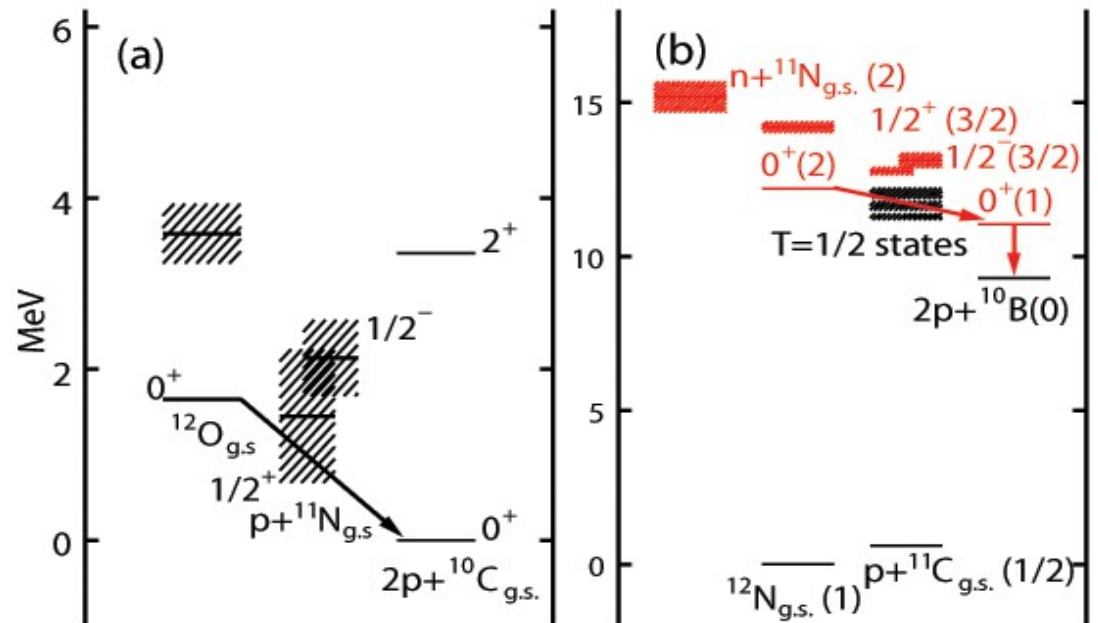
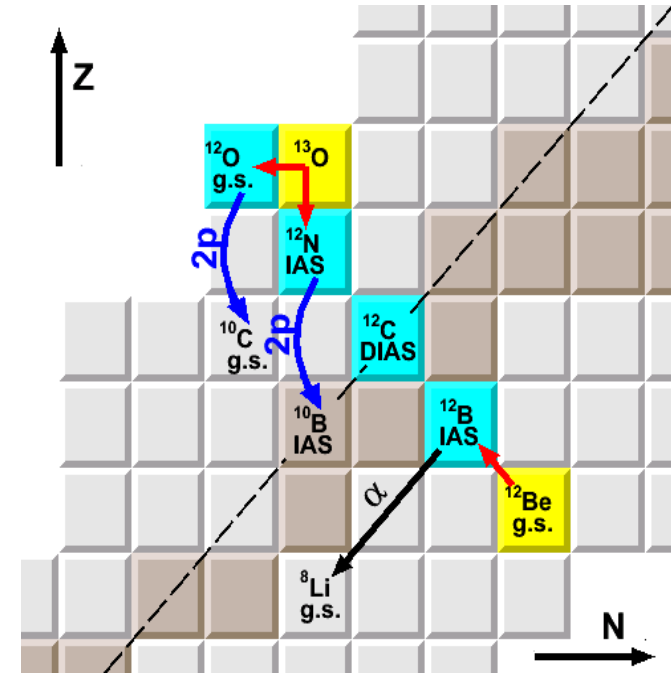
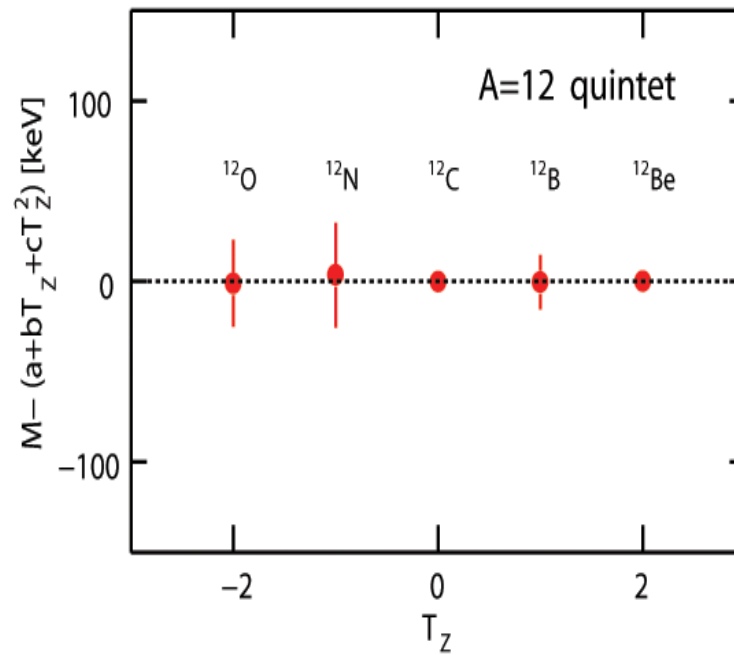
E/A=30 MeV  $^{13}\text{O}$  beam  
 Texas A&M university  
 $^9\text{Be}$  target

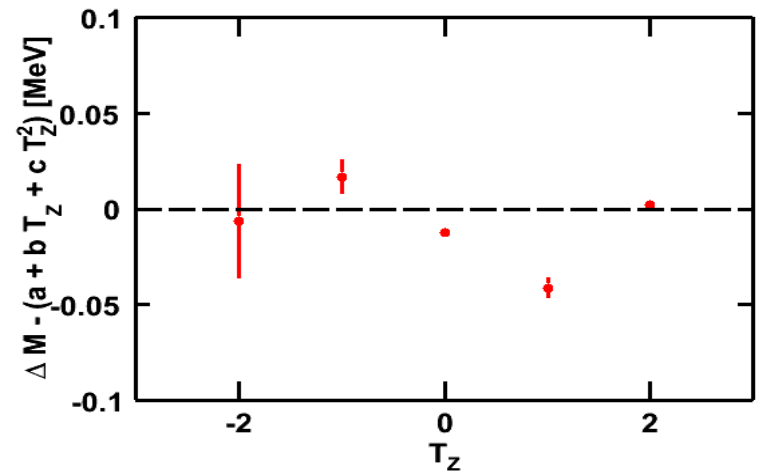
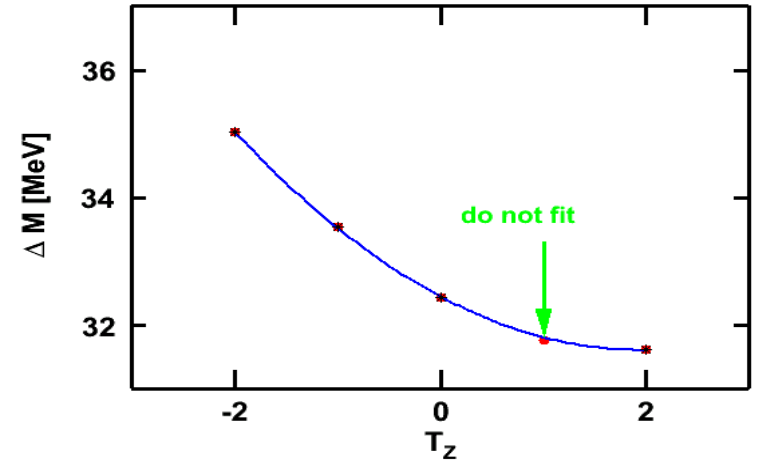
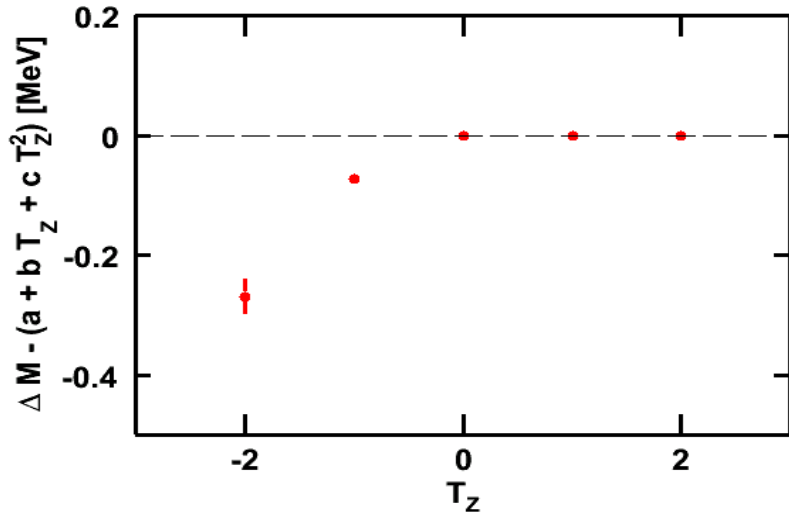
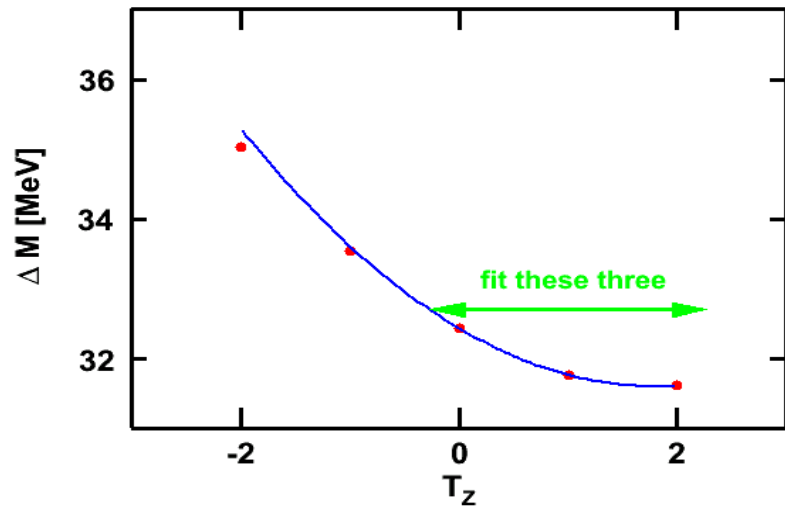


PRC 86 (2012) 011304R

$^{12}\text{O}_{\text{gs}}$  – new width consistent with theory

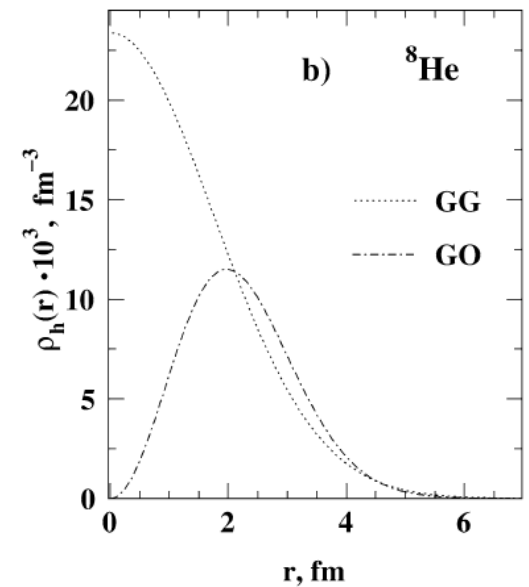
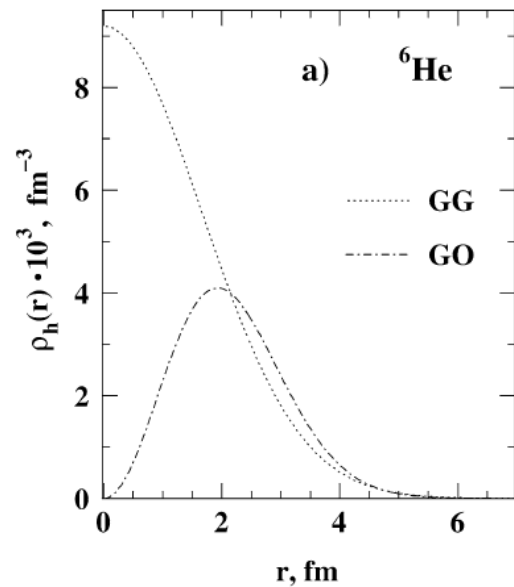
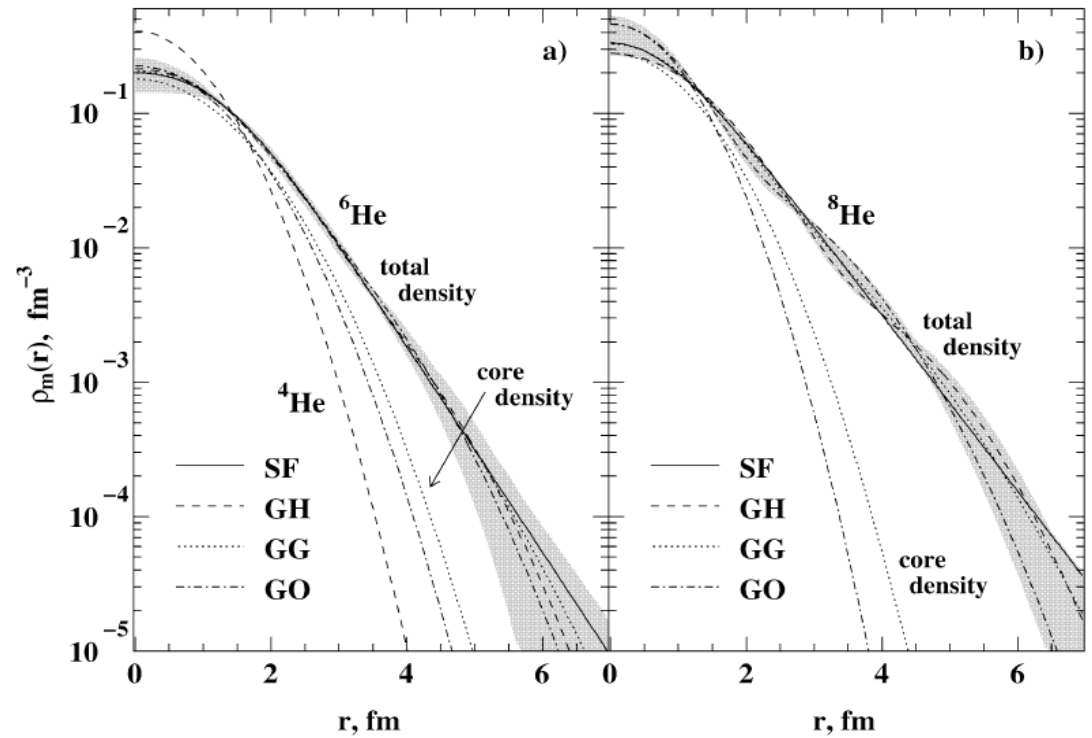
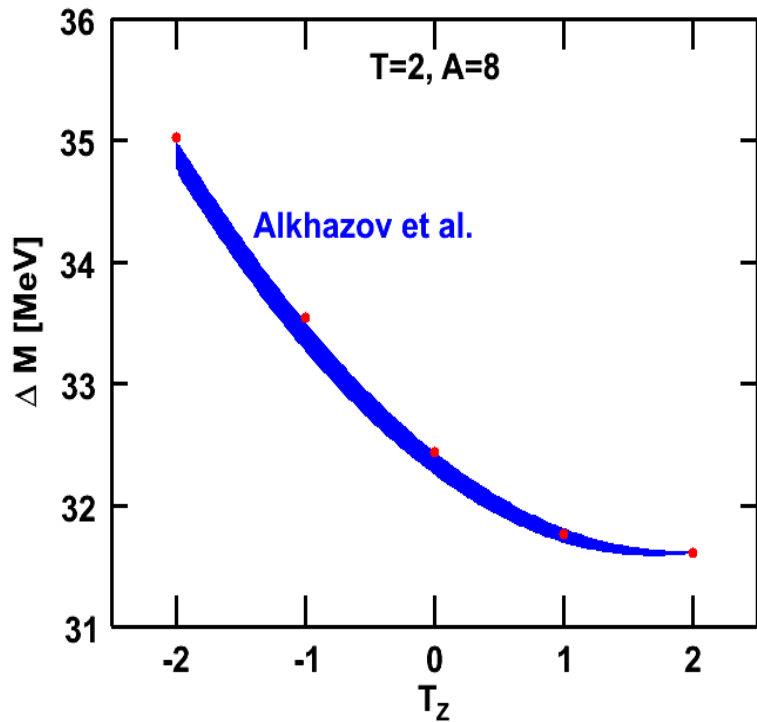
IMME shows no deviation





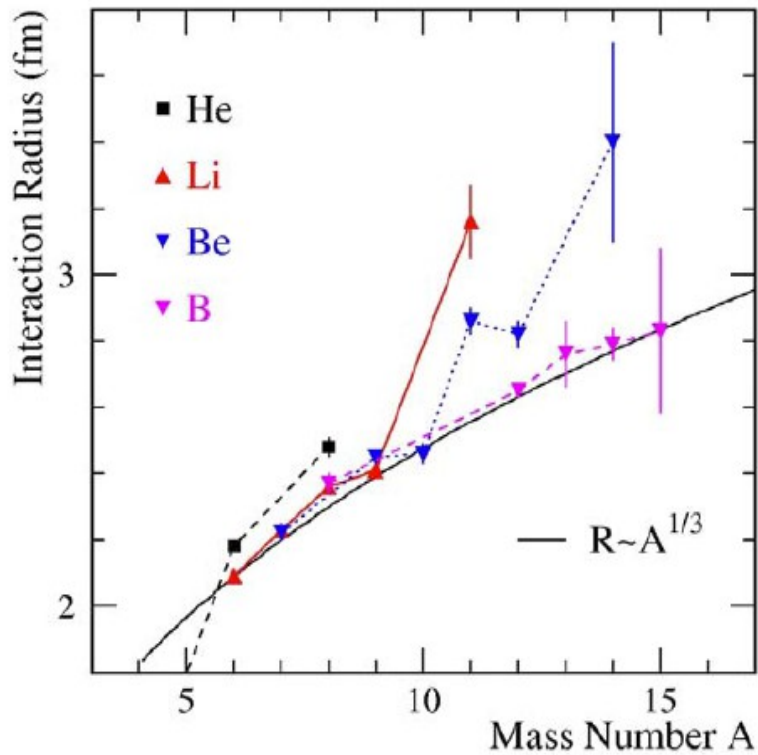
Modification of structure for proton rich Members.

${}^8\text{Li}(\text{IAS})$  energy has only been measured once. Same time as  ${}^8\text{Be}(\text{DIAS})$ .

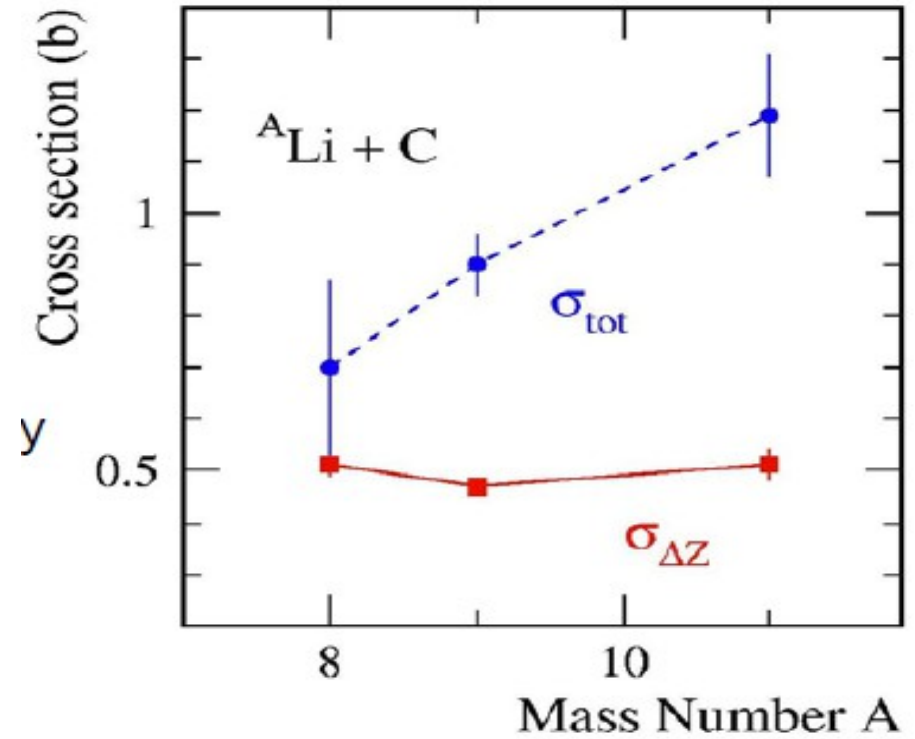


Alkhazov et al  
 NPA 712 (2002) 269

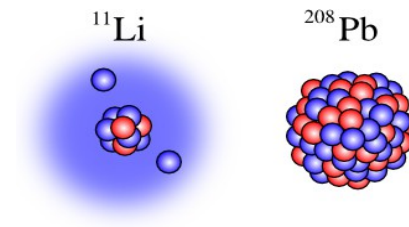
From 0.7 GeV  ${}^{6,8}\text{He} + p$   
 scattering extracted halo  
 distribution. Within level of  
 uncertainty consistent with IMME  
 if halo is frozen.



Tanihata et al,  
 PRL 55(1985) 2676  
 PLB 206 (1988) 592



Blank et al.  
 Z. Phys. A343 (1992) 375



# A=11 sextet

## Core-Halo model

Suzuki and Yabana  
Phys. Lett. B **273**(1991) 173

Core Halo

$$|^{11}\text{Li}\rangle = |^9\text{Li}_{\text{g.s.}}\rangle |nn\rangle$$

$$|^{11}\text{Be}\rangle_{T=5/2} = T_- |^{11}\text{Li}\rangle$$

$^{11}\text{Be}_{\text{IAS}}$  observed in  $n+p+^9\text{Li}$  channel  
by Teranishi et al PLB 407 (1997) 110.

$$= \left\langle \frac{3}{2}, \frac{1}{2}, 1, 1 \left| \frac{5}{2}, \frac{3}{2} \right. \right\rangle |^9\text{Be}\rangle_{T=3/2} |nn\rangle$$

$$+ \left\langle \frac{3}{2}, \frac{3}{2}, 1, 0 \left| \frac{5}{2}, \frac{3}{2} \right. \right\rangle |^9\text{Li}_{\text{g.s.}}\rangle |np\rangle_{T=1}$$

$$= \sqrt{3/5} |^9\text{Be}\rangle_{T=3/2} |nn\rangle \quad 60\% \text{ n-n halo (stable)}$$

$$+ \sqrt{2/5} |^9\text{Li}_{\text{g.s.}}\rangle |np\rangle_{T=1} \quad 40\% \text{ n-p halo}$$

$$|^{11}\text{B}\rangle_{T=5/2} = T_- |^{11}\text{Be}\rangle_{T=5/2}$$

$$= \sqrt{3/10} |^9\text{B}\rangle_{T=3/2} |nn\rangle \quad 30\% \text{ n-n halo (stable)}$$

$$+ \sqrt{6/10} |^9\text{Be}\rangle_{T=3/2} |np\rangle_{T=1} \quad 60\% \text{ n-p halo}$$

$$+ \sqrt{1/10} |^9\text{Li}_{\text{g.s.}}\rangle |pp\rangle \quad 10\% \text{ p-p halo}$$

# T=5/2 Sextet in A=11

Core-halo model of Suzuki +Yabana PLB 272 (173) 1991

$T_z = 5/2$

$^{11}\text{Li}_{\text{gs}}$

$3/2$

$^{11}\text{Be}_{\text{IAS}}$

$1/2$

$^{11}\text{B}_{\text{DIAS}}$

$-1/2$

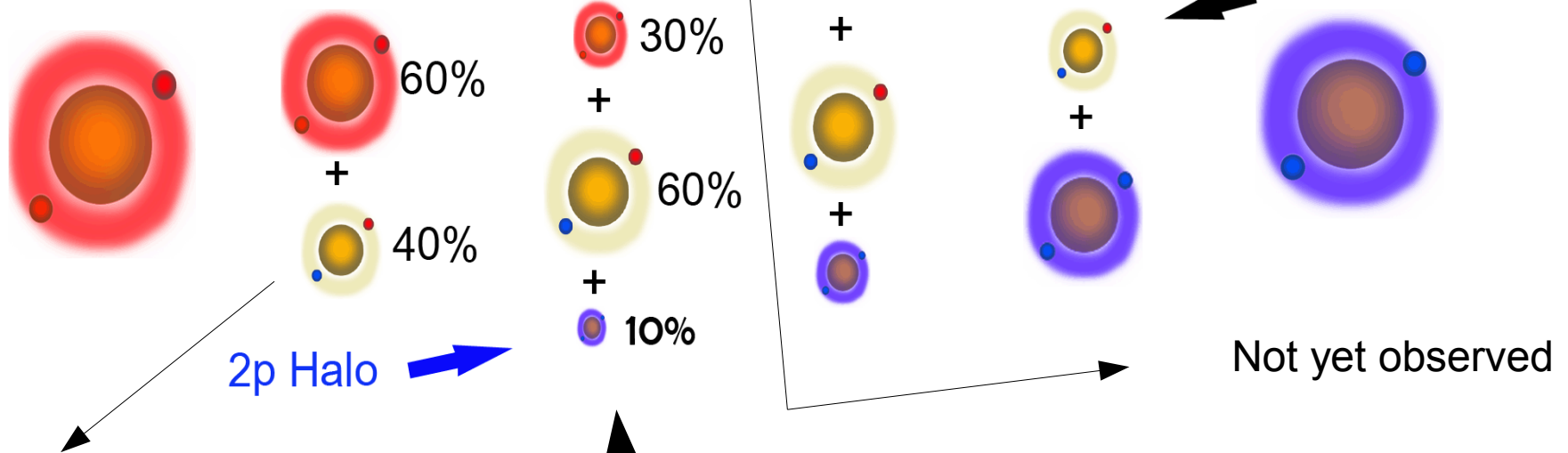
$^{11}\text{C}_{\text{DIAS}}$

$-3/2$

$^{11}\text{N}_{\text{IAS}}$

$-5/2$

$^{11}\text{O}_{\text{gs}}$



Observed at RIKEN in 1997  
in  $p+n+^9\text{Li}$  channel

$E^* = 21.2 \text{ MeV}$ ,  $\Gamma = 490(70) \text{ keV}$   
PLB 407 (1997) 110



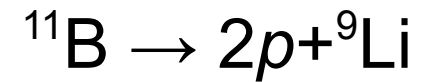
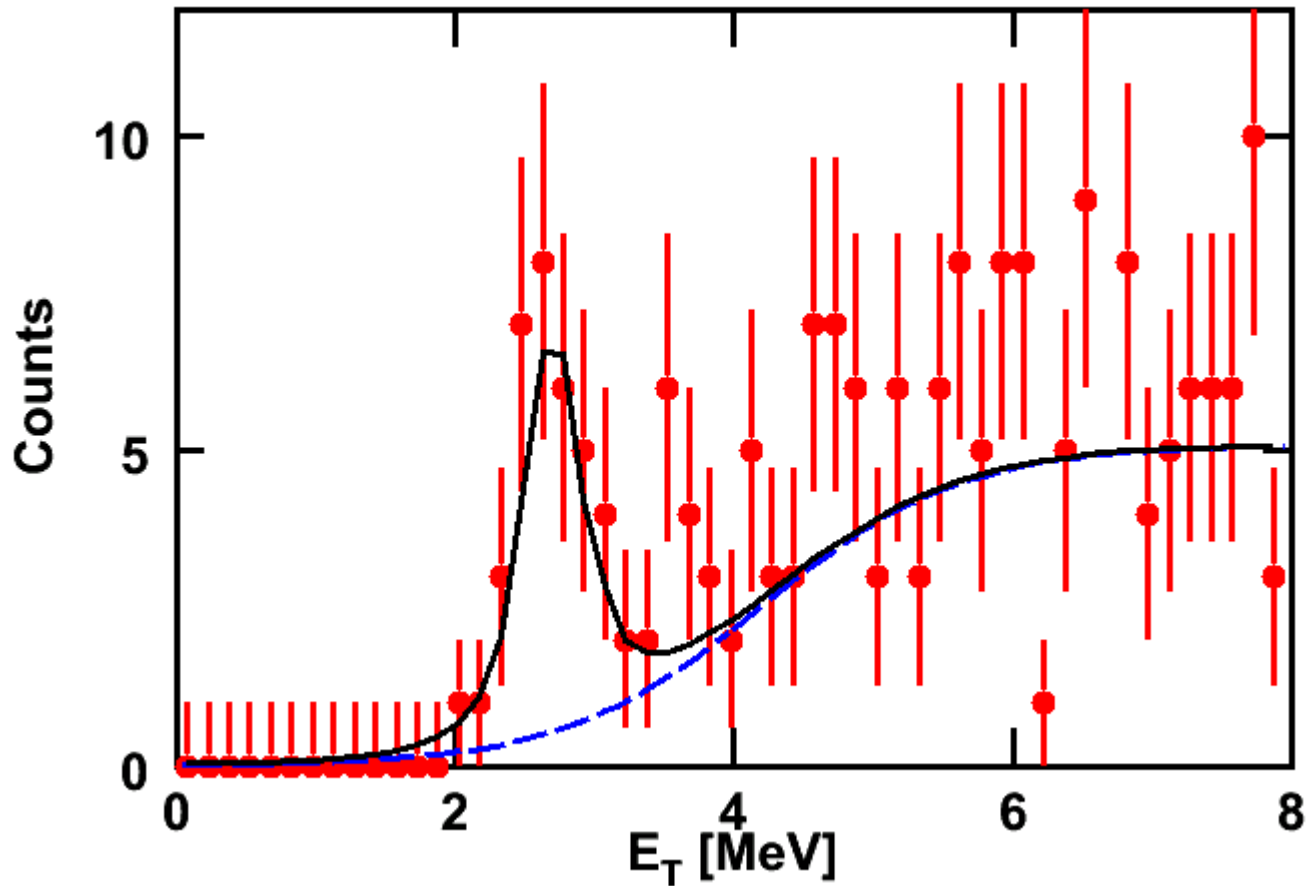
## Double Isobaric analog of $^{11}\text{Li}$ in $^{11}\text{B}$

$^{12}\text{Be}$  beam @  $E/A = 50$  MeV with carbon and polyethylene targets.

See peak with Polyethylene target but not with  $^{12}\text{C}$  target

Reaction  $^{12}\text{Be}(p,2n)^{11}\text{B}$

For  $2p$  decay branch  $\sigma = 72(21)\mu\text{b}$ , should also have a  $n+p$  decay branch



$E^* = 33.6$  MeV

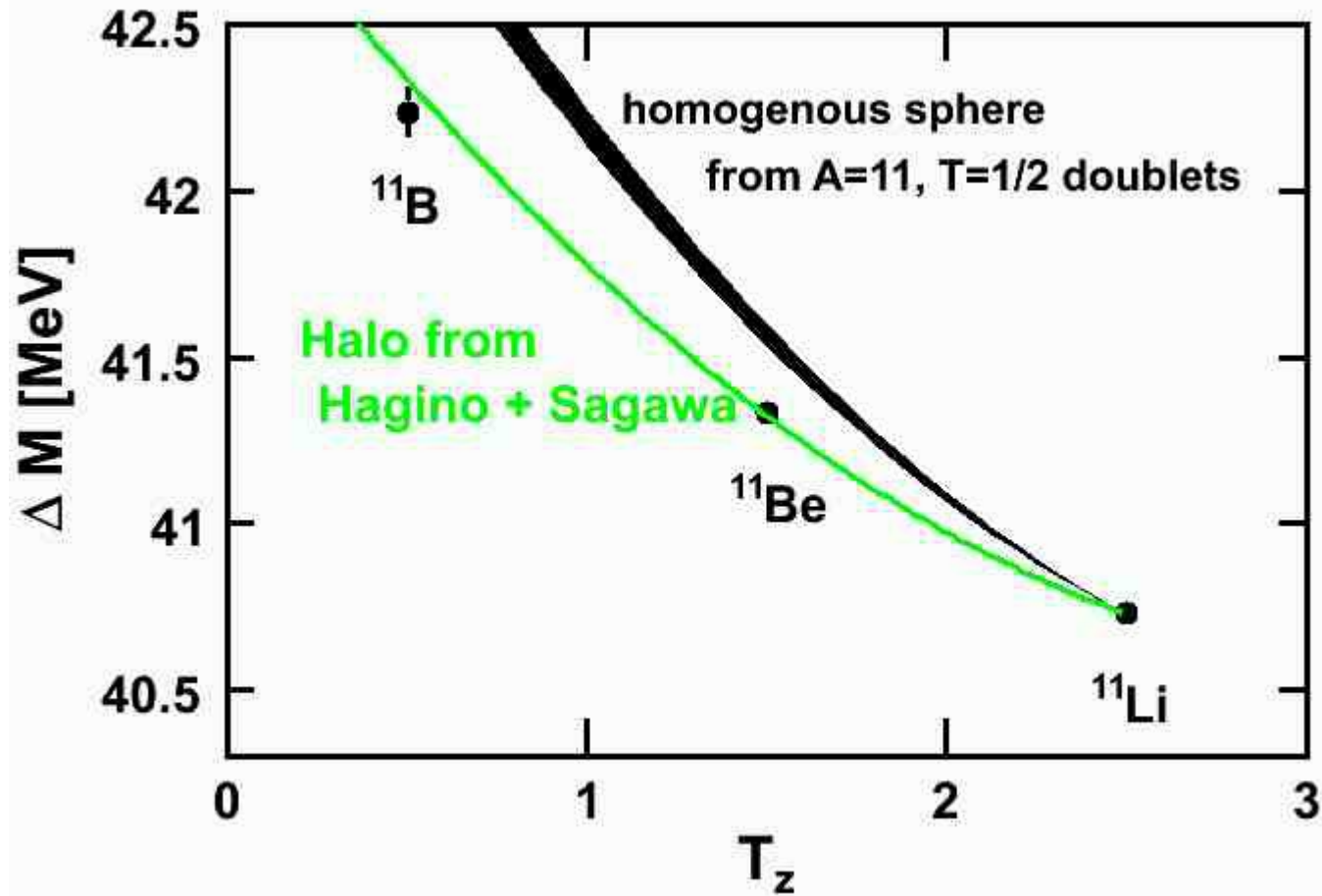
$E_T = 2.70(8)$  MeV

$\Gamma = 306(182)$  keV

Fit include detector resolution

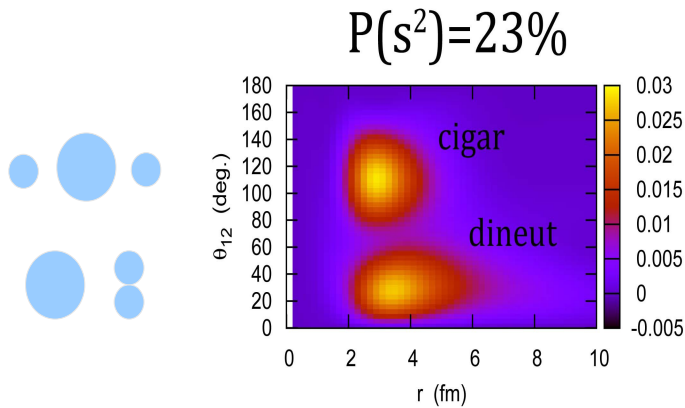
Decay kinetic energy

## Isobaric Multiplet Mass Equation for $A=11$ , $T=5/2$

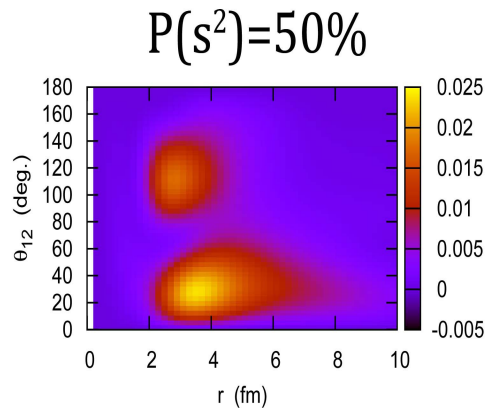


Reduced Coulomb energy compared to expectation from  $A=11$ ,  $T=1/2$  doublets. Confirmation of Halo structure. Consistent with  $^{11}\text{Li}$  Halo wavefunctions calculated by Hagino and Sagawa [ $P(s^2)=0.23$ ] and assuming Halo wavefunctions are frozen along sextet.

How much  $(s_{1/2})^2$  configuration is there in  $^{11}\text{Li}$  in addition to the  $(p_{1/2})^2$

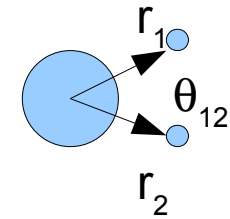


Consistent with  
Measured dipole  
response



Consistent with  
measured charge  
radius

$$r=r_1=r_2$$



From Hagino

The dineutron configuration gives us the halo. The IMME is dependent on the radial extent of the halo (dineutron component fraction) which is dependent on  $P(s^2)$ .

The physics is similar to the Thomas-Ehrman shift.

# Correlations in 3-body decay

Start:

3 fragments each with a momentum vector = 9 degrees of freedom

Remove:

- |  |                      |
|--|----------------------|
| a) center-of-mass motion                       | 3 degrees of freedom |
| b) fixed decay energy<br>(energy conservation) | 1 degree of freedom  |
| c) arbitrary rotation                          | 3 Euler angles       |

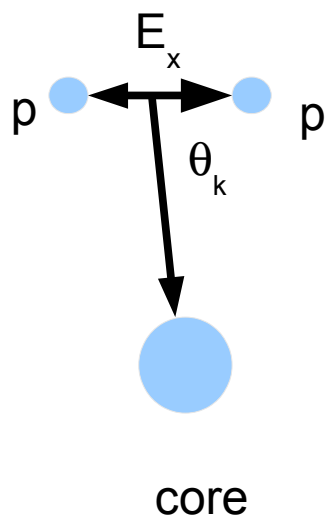
Remainder = 2 degrees of freedom for correlations

The 2-dim distribution can give us nuclear-structure information.

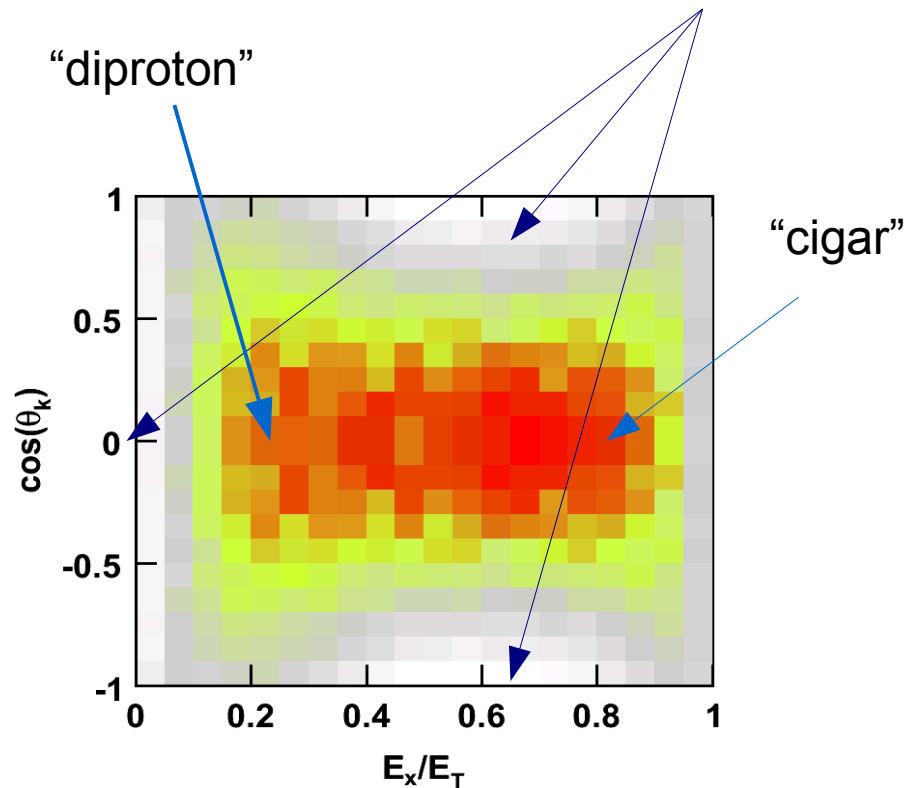
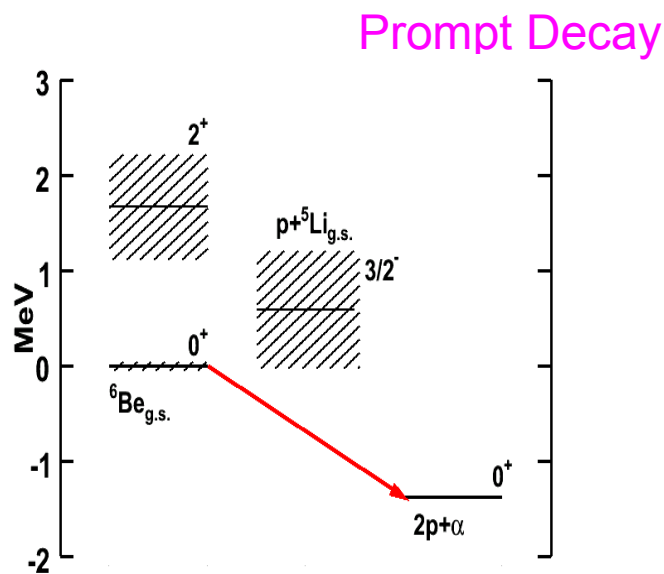
3-body decays can give more information than 2-body decays.

# Jacobi T hyperspherical coordinates

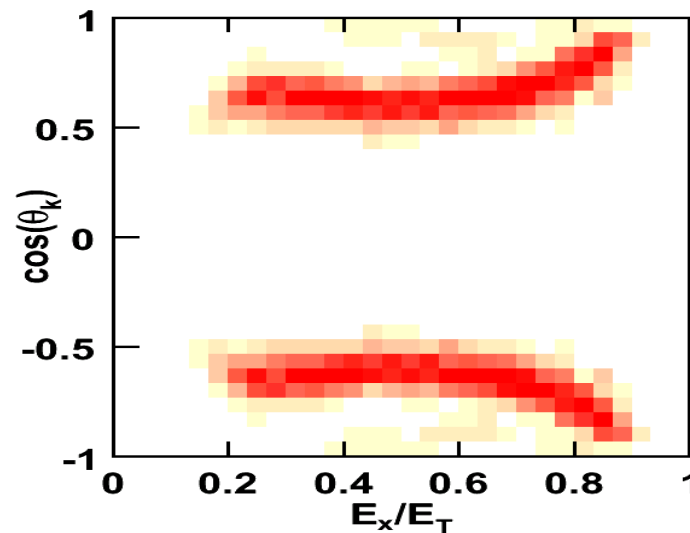
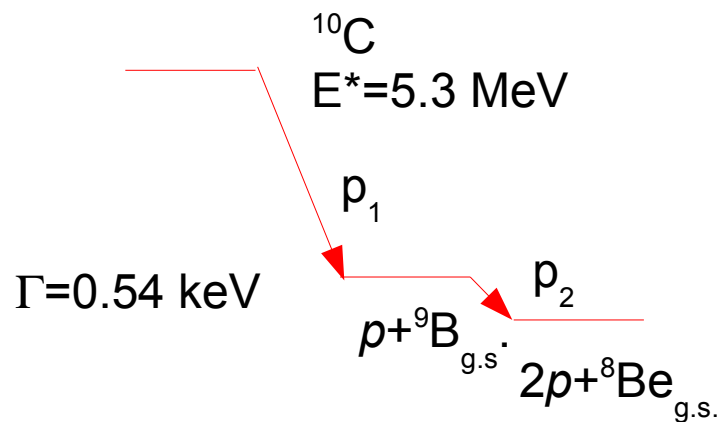
Coulomb  
Suppressions



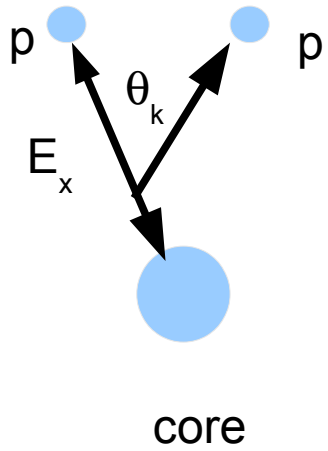
$E_x$  - relative KE between 2 protons  
 $E_T$  - total decay KE.



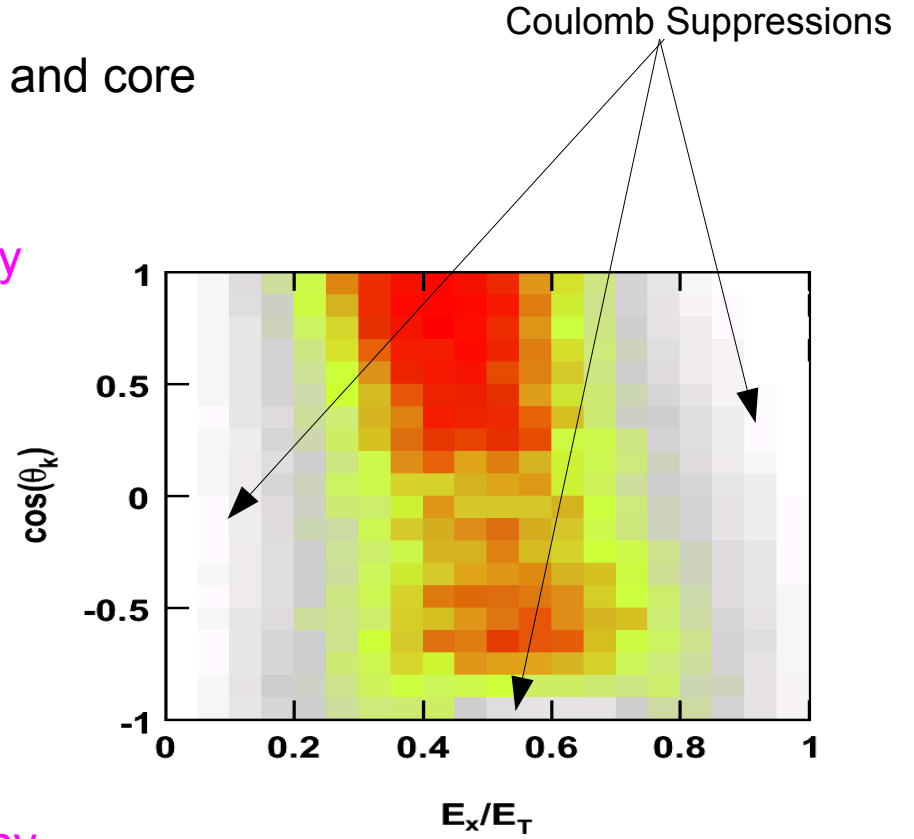
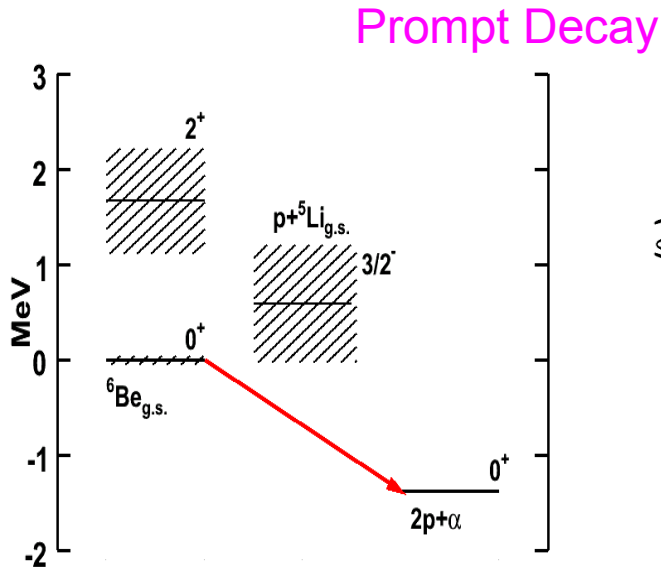
Sequential decay



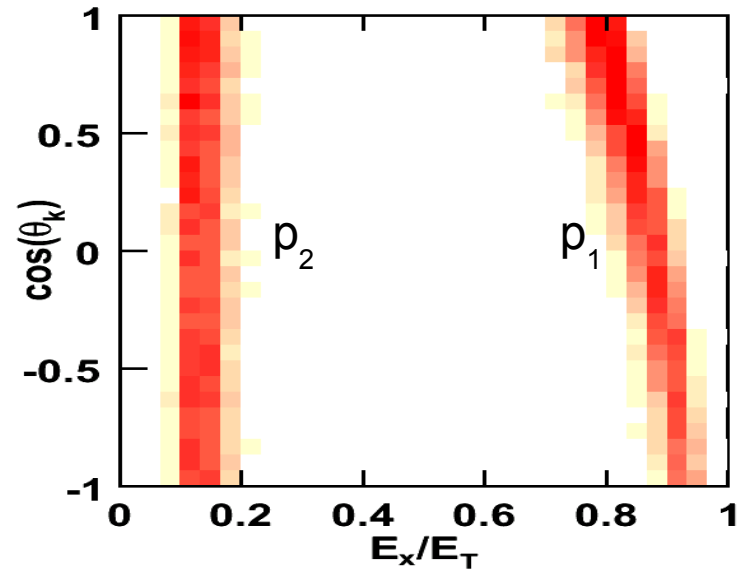
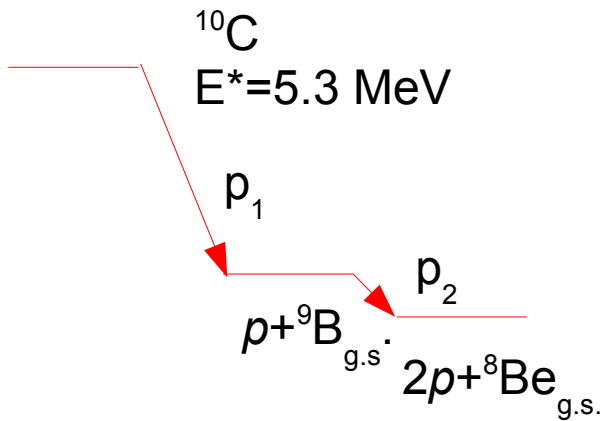
# Jacobi Y hyperspherical coordinates



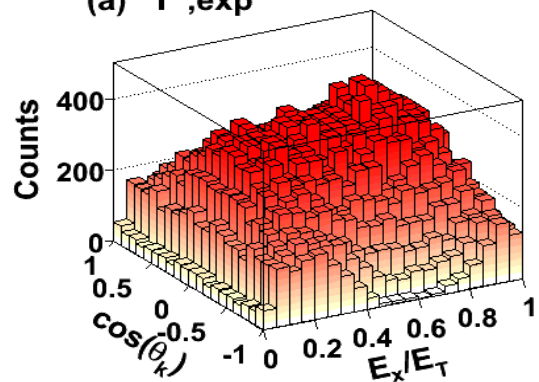
$E_x$  - relative KE between proton and core  
 $E_T$  - total decay KE.



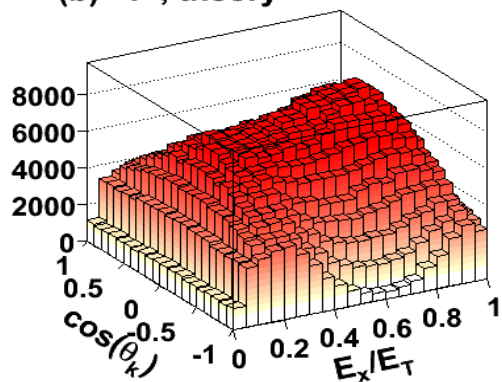
Sequential decay



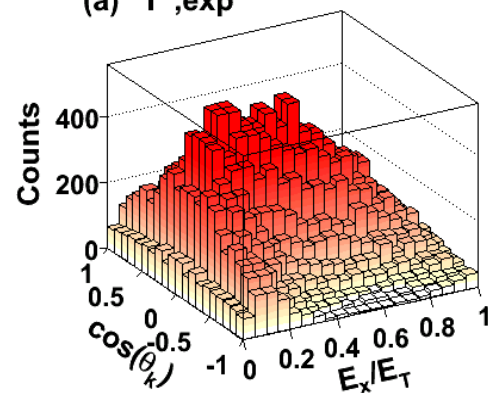
(a) "T", exp



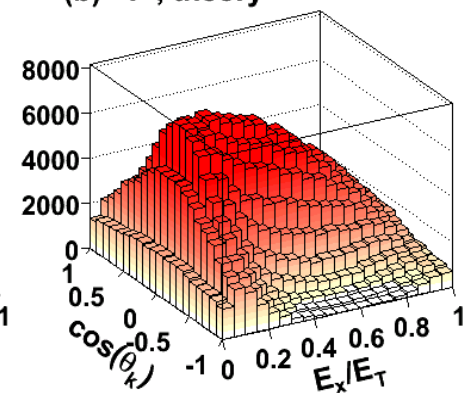
(b) "T", theory



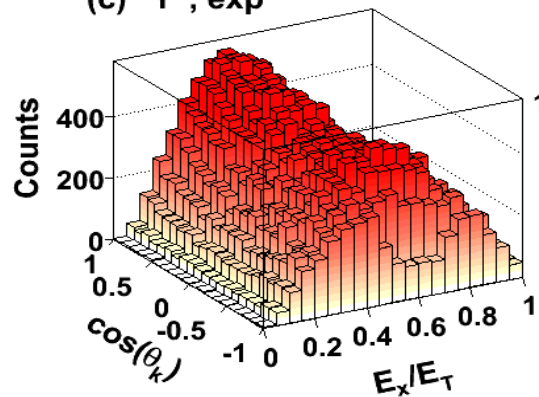
(a) "T", exp



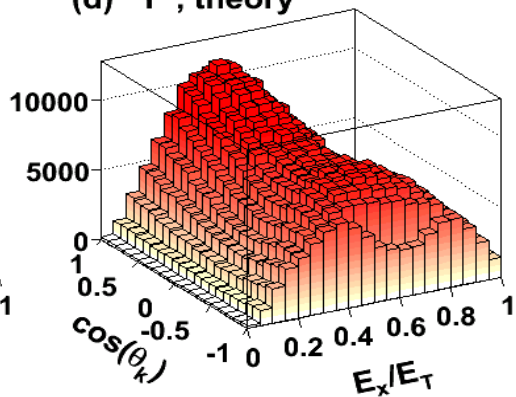
(b) "T", theory



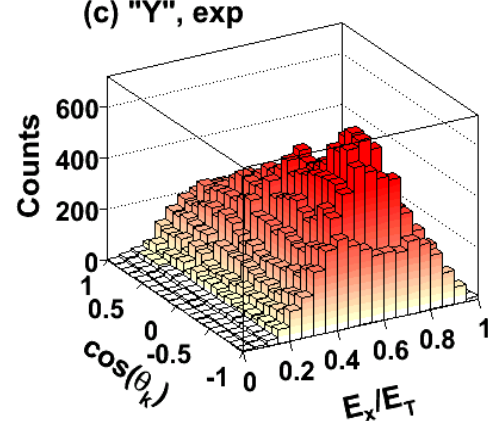
(c) "Y", exp



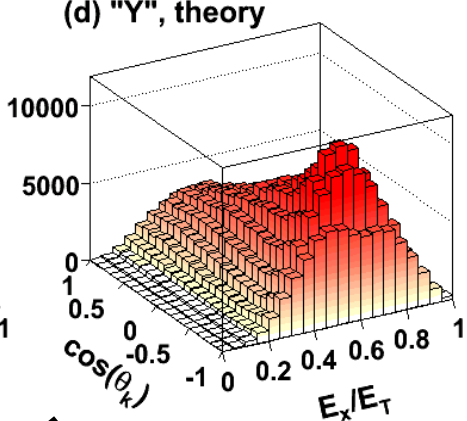
(d) "Y", theory



(c) "Y", exp

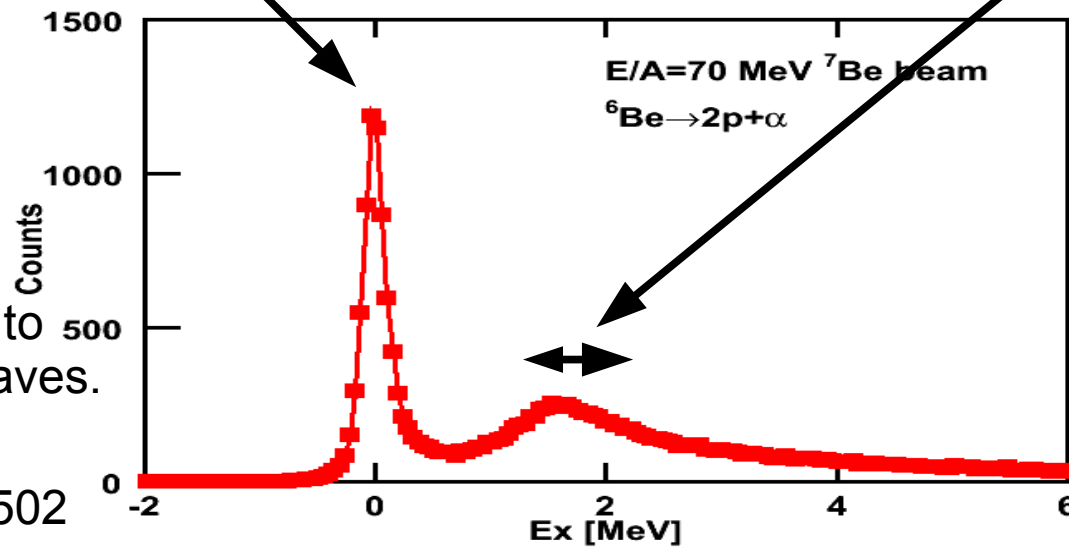


(d) "Y", theory

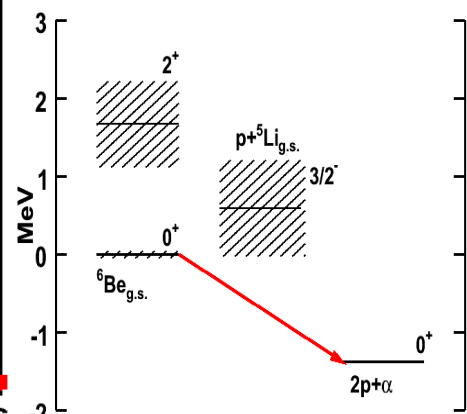


${}^6\text{Be}$  ground-state  $0^+$

Grigorenko's  
3-body cluster model.  
2 and 3-body forces.  
Wavefunctions matched to  
approximate outgoing waves.

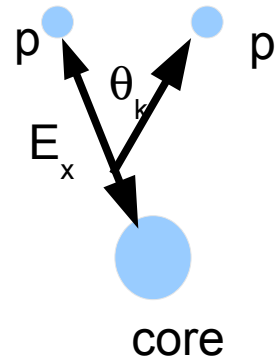


${}^6\text{Be}$  1<sup>st</sup> excited state  
 $2^+$



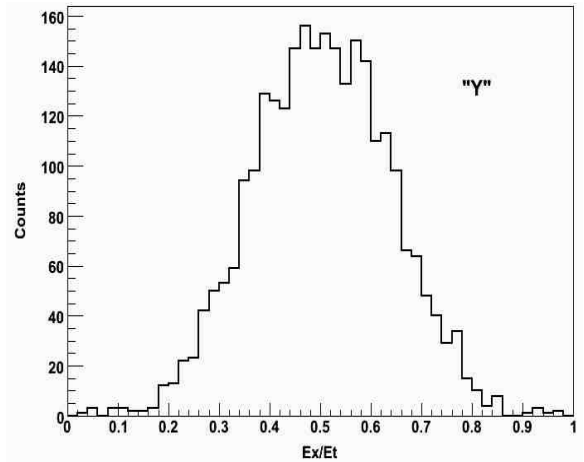
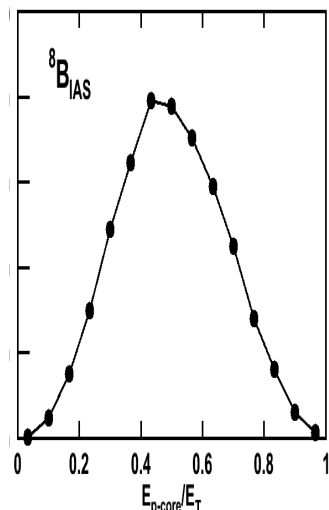
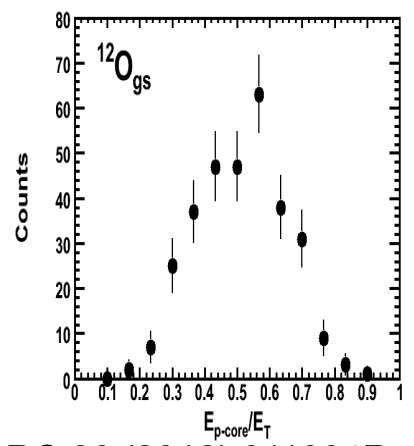
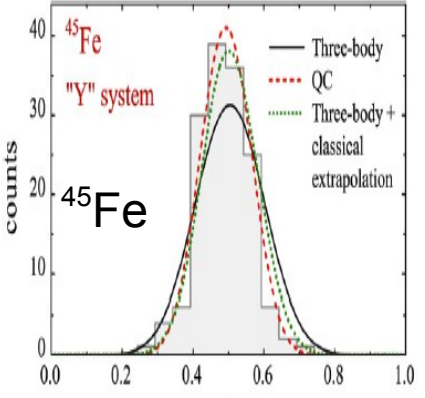
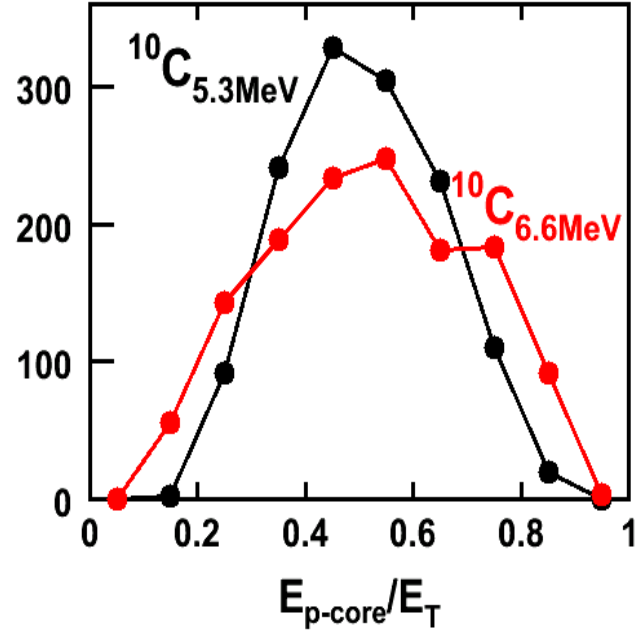
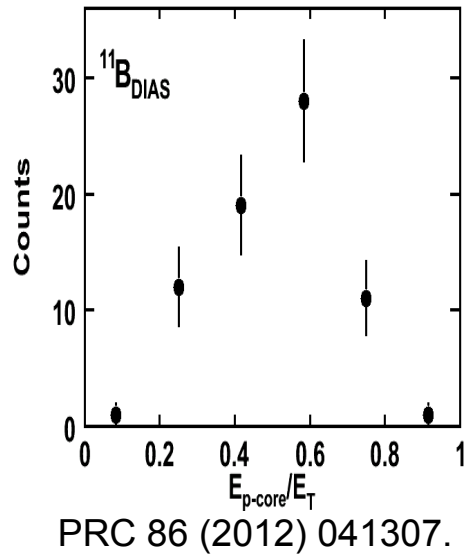
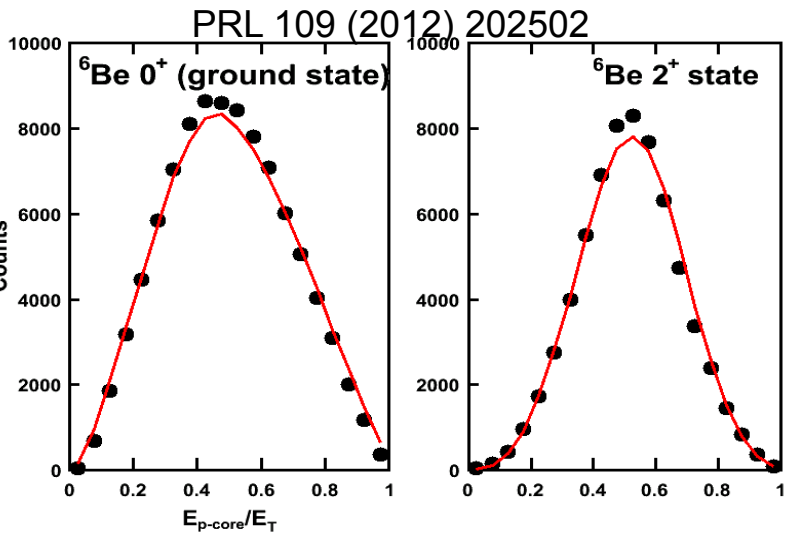
# Systematics of $E_{p\text{-core}} = E_x$ (Jacobi Y)

- a) Less dependent of calculation details
- b) Less dependent on detector bias
- c) Goldansky  $\sim P(E_x)P(E_T - E_x)$



PRC 80 (2009) 024306

Product of 2 penetration factors  
Peaks at  $E_x = E_T/2$

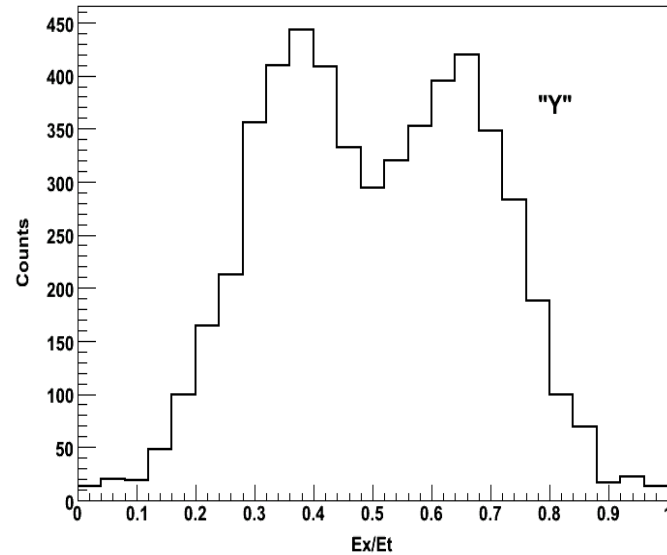
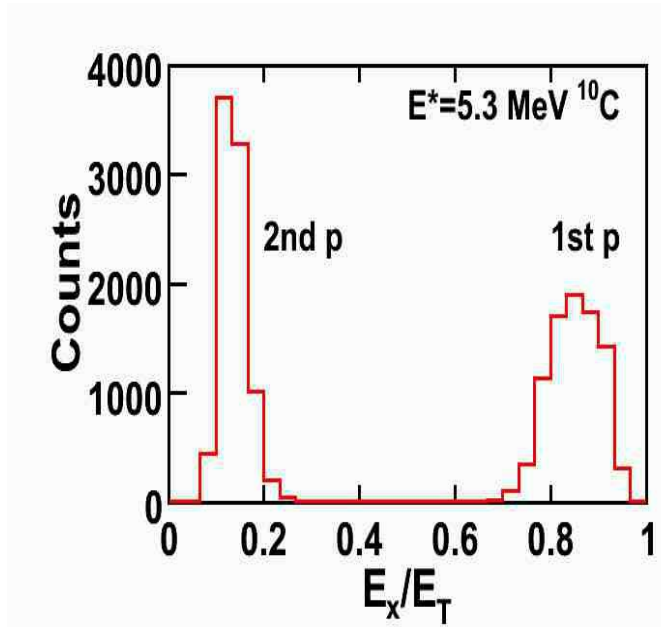
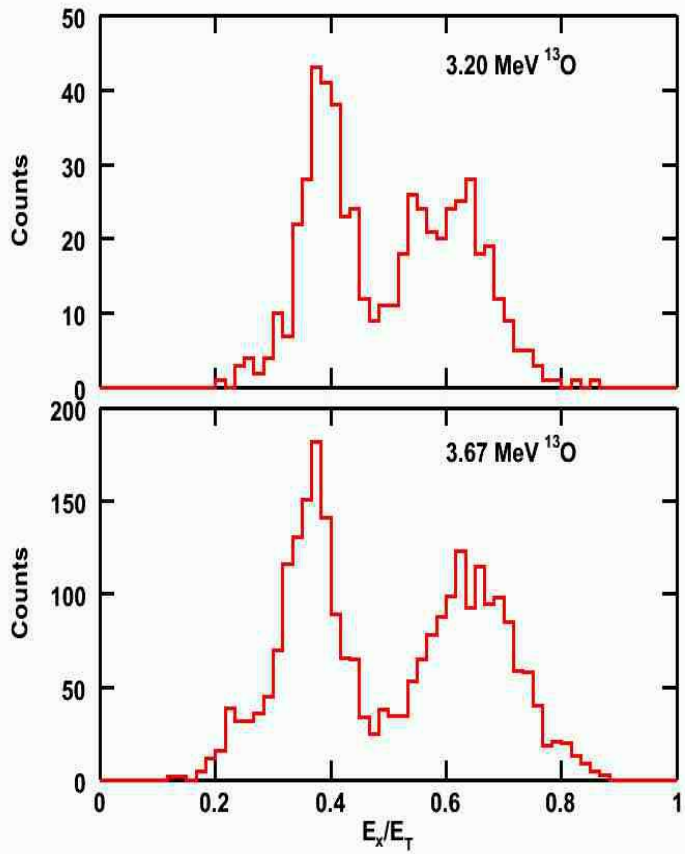


PRL 99 (2007) 192501

PRC 86 (2012) 011304R

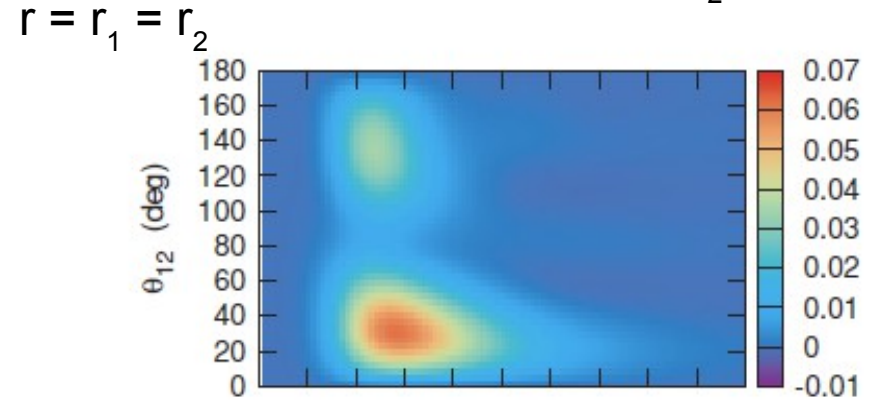
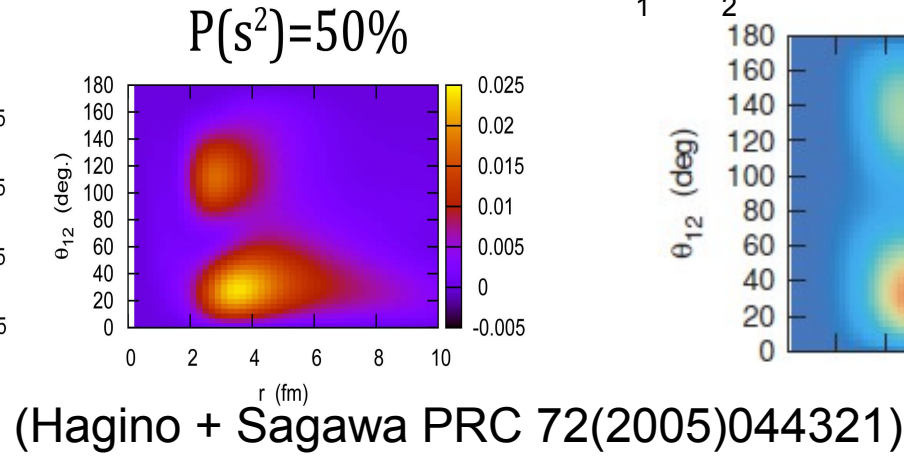
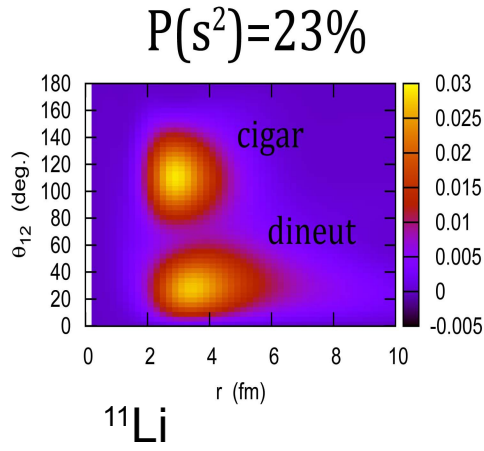
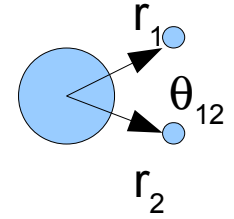
${}^{16}\text{Ne}$  ground state

# $E_{\text{core-p}}$ (Jacobi $\eta$ ) for sequential decay

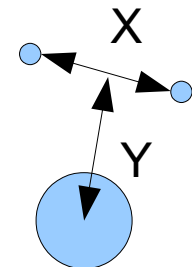
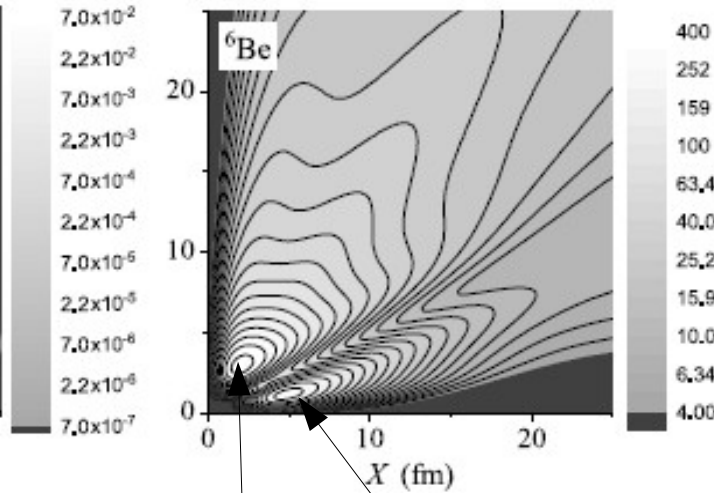
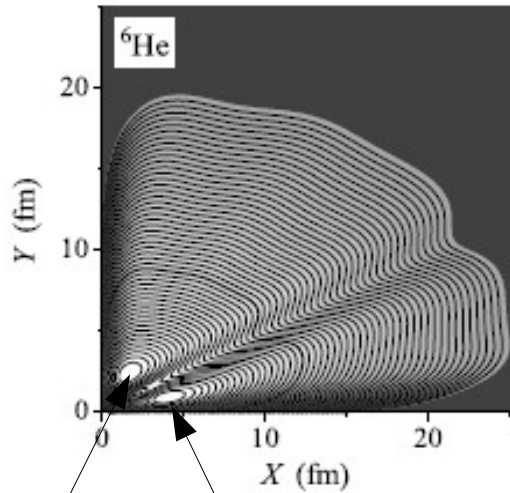


$^{16}\text{Ne}$  first excited state

Can we see the correlations in the halo of the 2p emitters



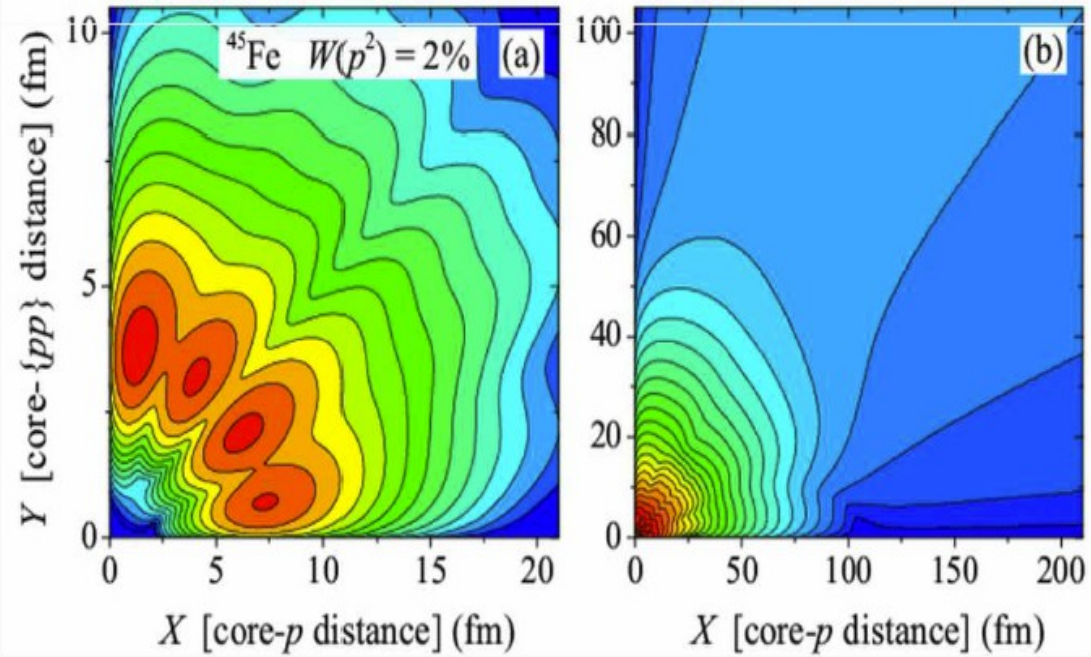
Grigorenko PRC 80 (2009) 034602



dineutron

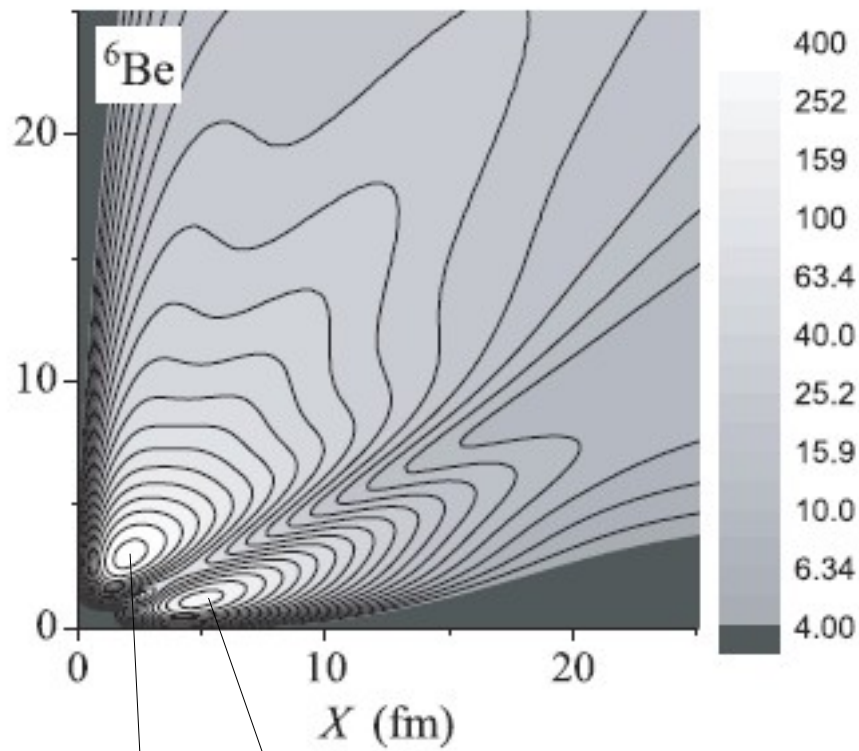
diproton

The  $^{45}\text{Fe}$  wave function density in the T system for the configuration  $98\% f^2 + 2\% p^2$



Grigorenko and Zhukov, PRC 68 (03) 054005

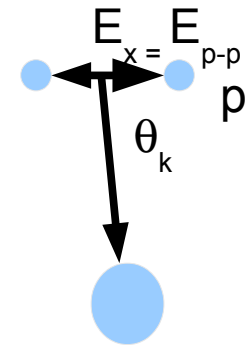
M.P. et al, RMP (2012) 567



ground state of  ${}^6\text{Be}$  has similar amounts of diproton and cigar configurations.

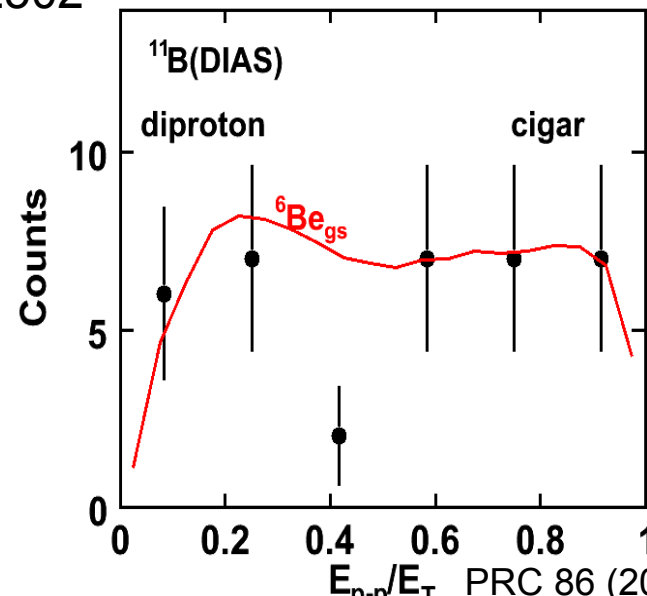
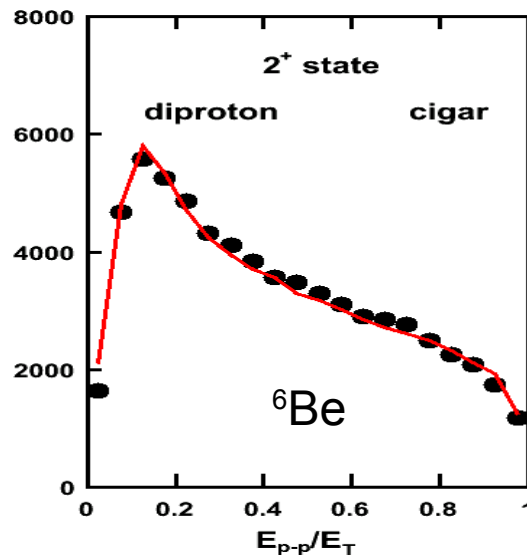
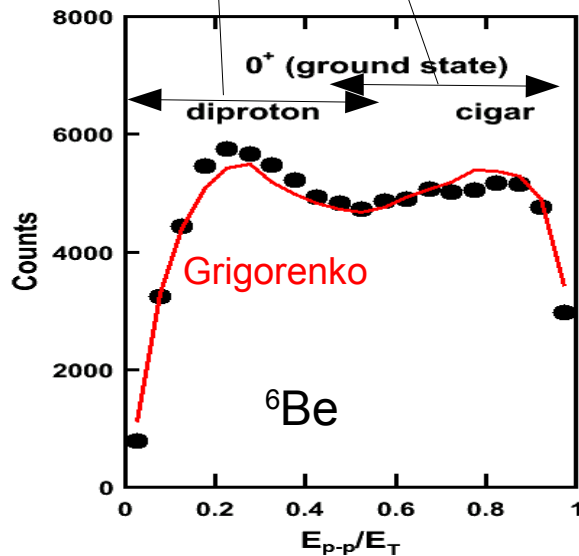
$2^+$  state has more diproton

${}^{11}\text{B}(\text{DIAS})$  is  $\sim$  similar to  ${}^6\text{Be}_{\text{g.s.}}$

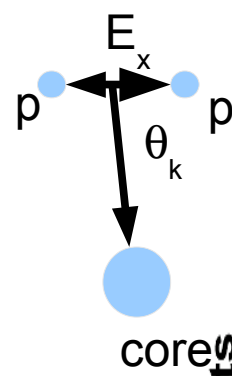


core  
Jacobi T

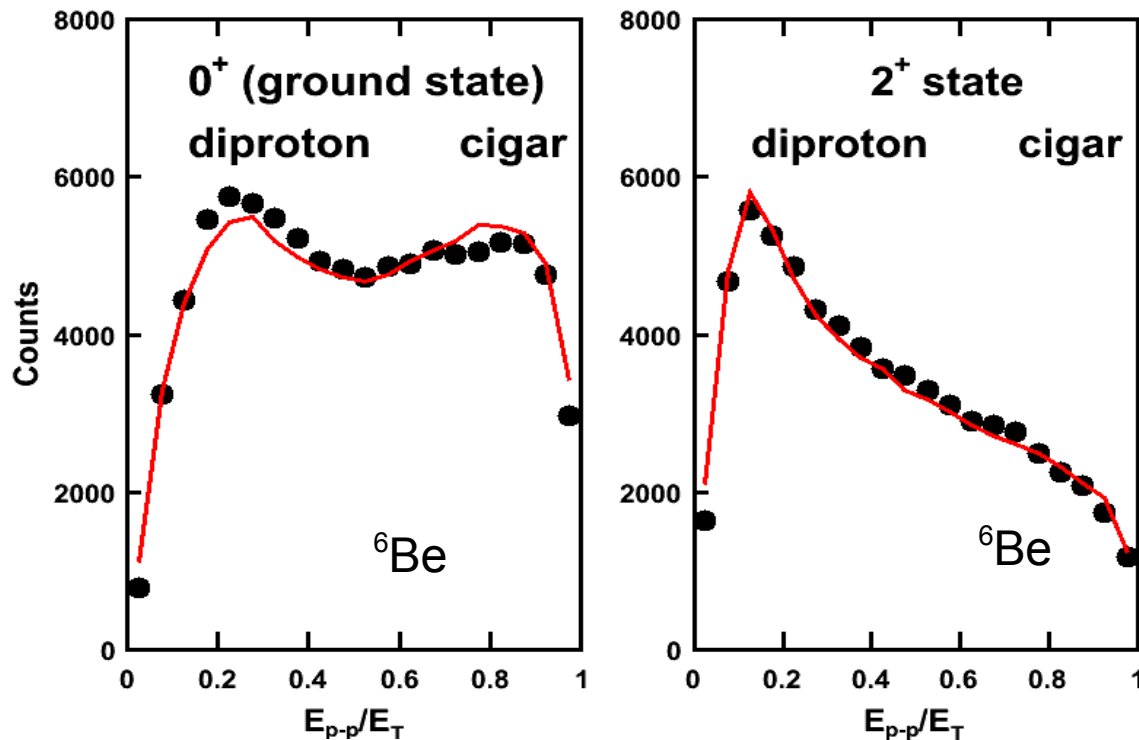
PRL 109 (2012) 202502



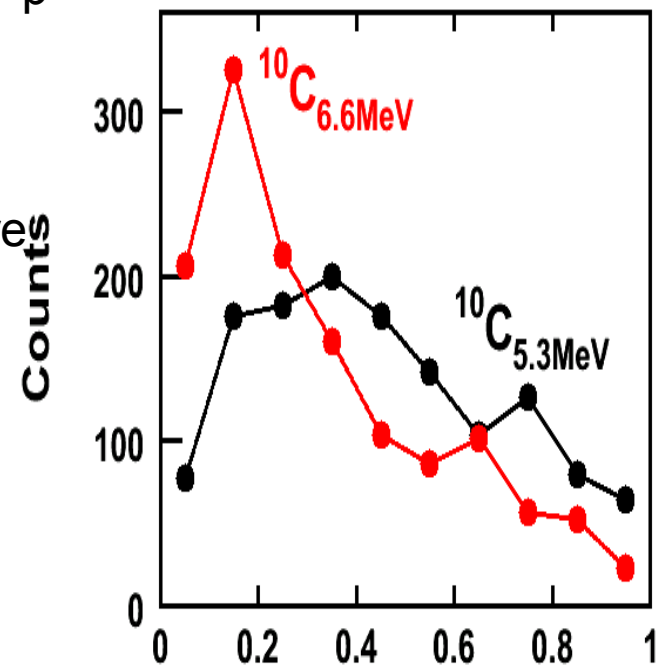
# Systematic of $E_{p-p} = E_x$ Jacobi T



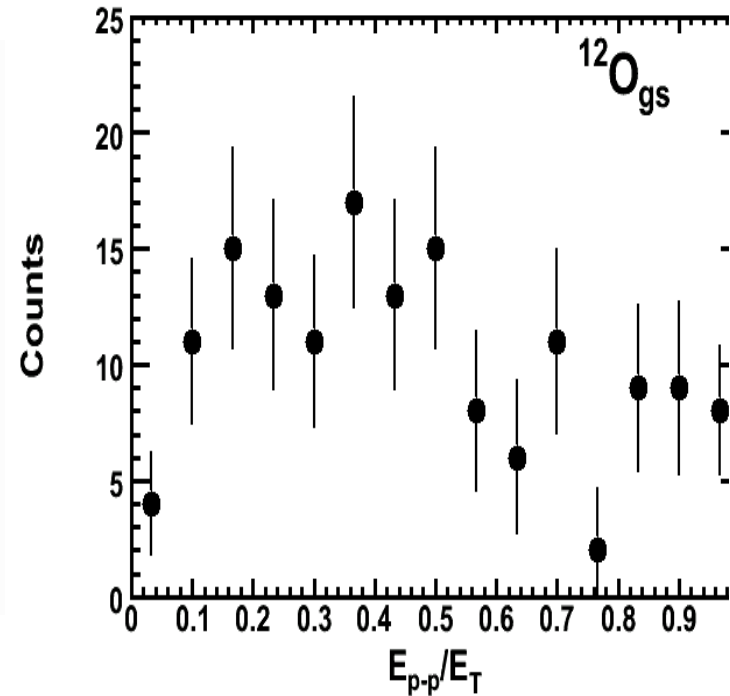
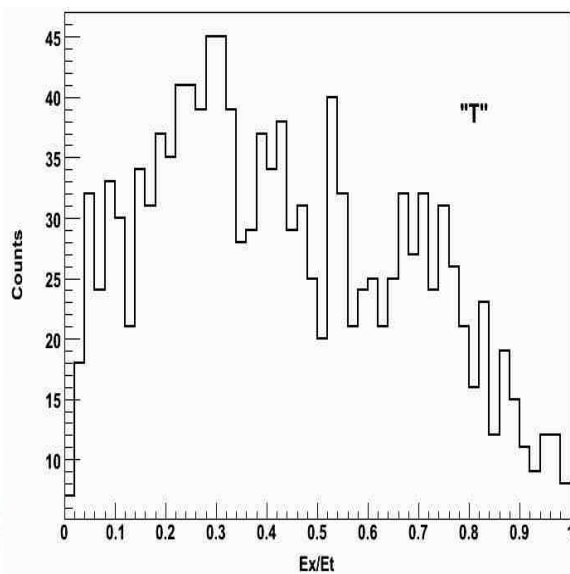
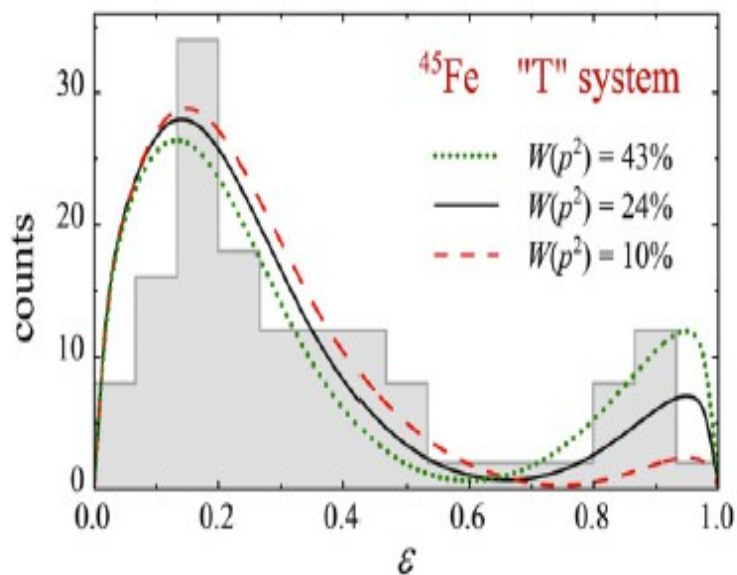
PRL 109 (2012) 202502



PRC 80 (2009) 024306

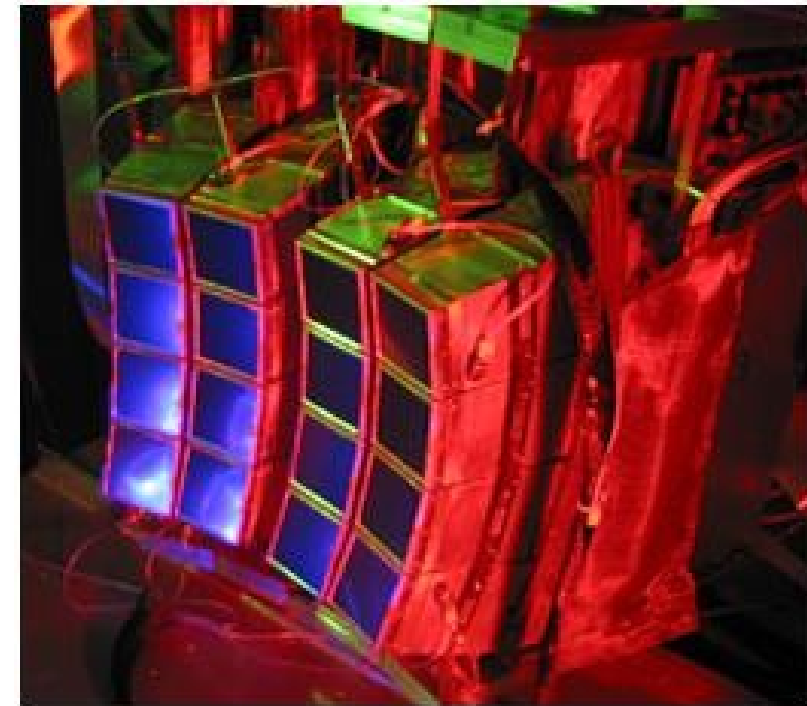


PRC 86 (2012) 011304R



PLB 677 (2009) 30

<sup>16</sup>Ne<sub>gs</sub>



Charity, Komarov, Sobotka, Elson, Manfredi, Shane, Brown, Jager  
Buhro [Washington Univ.](#)  
Egorva, Grigorenko, [Bogolyubov Lab. of Theoretical Phys. Dubna](#)  
Hagino, [Tohoku Univ.](#), Sagawa, [Univ. of Azu](#)  
Clifford, Bazin, Chajeki, Coupland, Gade, Iwasaki, Kilburn, Lee,  
Lukyanov, Lynch, Mocko, Lobastov, Rodgers, Sanetullaev, Tsang,  
Wallace, Winkelbauer, Youngs, Barney, Showalter. [NSCL, Michigan State Univ.](#)  
Hudan, Metelko [Indiana Univ.](#)  
Famiano, Wuosmaa, Marley, Shetty, Bedoor, McNeel, [Western Michigan Univ.](#)  
McCleskey, Pizzone, Roeder, Spiridon, Simmons, Trache. [Texas A&M](#)  
Kurokawa, [RIKON](#)  
Van Goethem [Kernfysisch Versneller Instit.](#)  
Ghosh, [Variable Energy Cyclotron Centre, Kolkata](#) Howard, [Rutgers Univ.](#)  
Zhukov, [Calmers Univ., Sweden](#)

# Summary

HiRA is a powerful tool for invariant mass spectroscopy

Exotic structure in light nuclei is not confined to nuclei near the drip lines (high  $T_z$ ) but more generally to states with high  $T$ .

Strong connection between two-proton decay and two-neutron halo nuclei.

Two-proton decay of proton-rich members of the

$A=6$ ,  $T=1$  triplet  ${}^6\text{Be}$

$A=8$ ,  $T=2$  quintet  ${}^8\text{C}$  and  ${}^8\text{B}_{\text{IAS}}$

$A=11$ ,  $T=5/2$  sextet  ${}^{11}\text{B}_{\text{DIAS}}$

$A=12$ ,  $T=2$  quintet  ${}^{12}\text{O}$  and  ${}^{12}\text{N}_{\text{IAS}}$

$2p$  decay from Isobaric analog states -  
new class of  $2p$  decay

Correlations between the three-body decay fragments tell us if the decay is sequential or prompt. For prompt decay, we are sensitive to the relative diproton and Cigar configurations in the halo

