

Transversity 2014

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Transverse Polarization Phenomena in Hard Processes

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Measurement of Collins Asymmetries in inclusive production of pion pairs @ BaBar

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Outline

INTRODUCTION

- Theoretical framework
 - Collins fragmentation functions
 - Reference frames: RF12 and RF0
- PEP-II and the BaBar detector at SLAC

ANALYSIS OVERVIEW

- Analysis method
- Extraction of the asymmetry for light quarks
- Asymmetry corrections and studies of systematic uncertainty

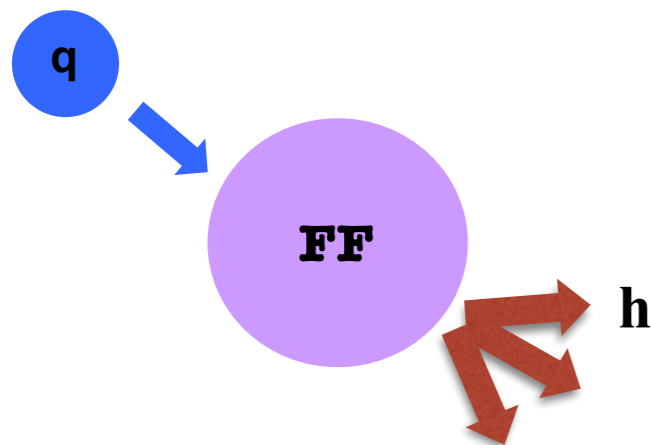
RESULTS

- Asymmetries *vs.* pion fractional energies, pion transverse momentum, analysis axis polar angle, and 4-D results

PLANS and CONCLUSIONS

Collins Fragmentation Function

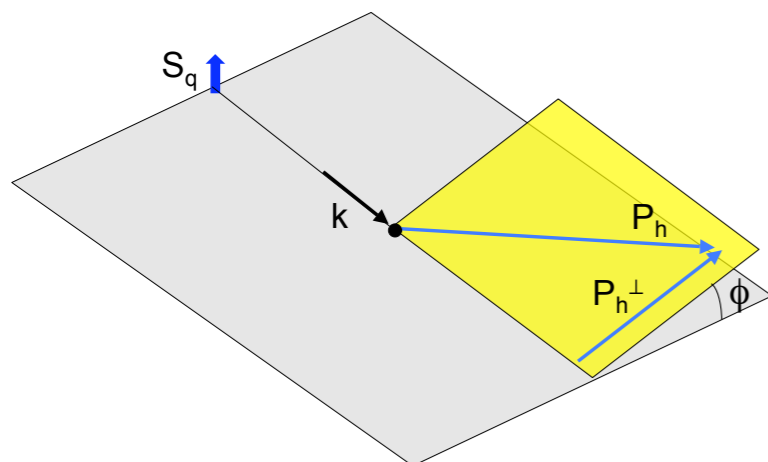
- Fragmentation Functions** (FFs) → dimensionless and universal functions
 → non-perturbative information
 → describe the final state particles in hard processes
 → dependence on $z=2E_h/\sqrt{s}$, P_\perp , and s_q



“Standard” unpolarized FF

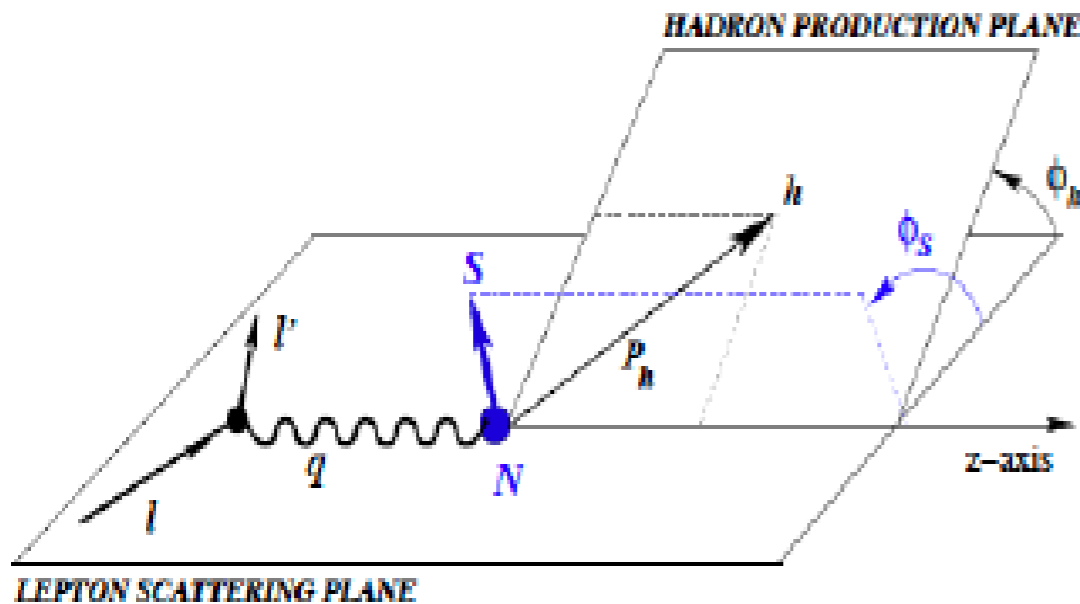
$$D_1^{q\uparrow}(z, \mathbf{P}_\perp; s_q) = D_1^q(z, P_\perp) + \frac{P_\perp}{zM_h} \underbrace{H_1^{\perp q}(z, P_\perp) \mathbf{s}_q \cdot (\mathbf{k}_q \times \mathbf{P}_\perp)}$$

Definition of the azimuthal angle ϕ in the case of a quark of momentum \mathbf{k} and spin \mathbf{s}_q fragments into a spin-0 hadron of momentum \mathbf{P}_h with transverse component P_h^\perp transverse to \mathbf{k}



- could arise from a **spin-orbit** coupling
- leads to an azimuthal modulation of hadrons around the quark momentum $\mathbf{k} \implies$ **Collins asymmetry**
- H_1^\perp is the **polarized** fragmentation function or **Collins FF**
 → it describes the fragmentation of a **transversely polarized quark into a spinless (or unpolarized) hadron h**
- J. C. Collins, Nucl.Phys. **B396**, 161 (1993)

Collins effect



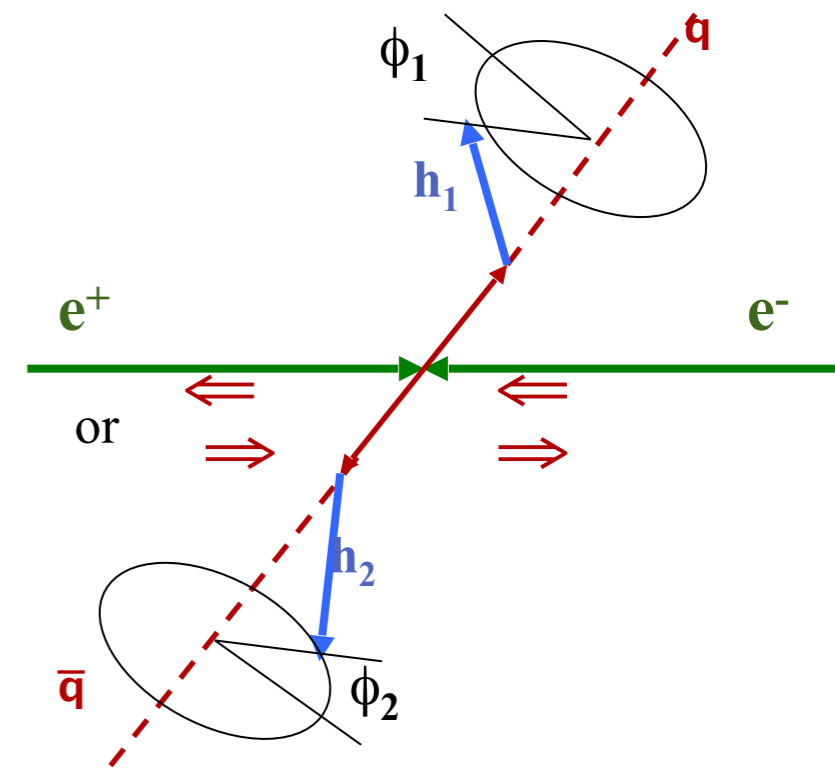
SIDIS

- First observed in Semi-Inclusive DIS (SIDIS)
 - unpolarized lepton beam (l) off transversely polarized target (N) ($lN \rightarrow l'\pi X$)
 - non-zero Collins effect
- $\sigma \propto \sin(\varphi_h + \varphi_s) h_1(x_B) \otimes H_1^\perp(z_1)$
 - two chiral-odd functions
 - azimuthal single spin asymmetry

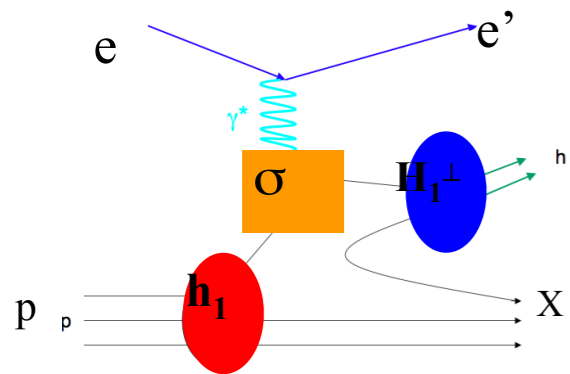
e^+e^- annihilation

- In a given event, the q and \bar{q} spin directions are unknown, but they must be parallel, with a polarization component transverse to the q direction $\propto \sin^2\theta$
- exploit this correlation by using hadrons in opposite jets
- the observed asymmetry is proportional to the product of two Collins functions:

$$e^+e^- \rightarrow q\bar{q} \rightarrow \pi_1\pi_2X \quad (q=u, d, s) \implies \sigma \propto \cos(\phi_i) H_1^\perp(z_1) \otimes H_1^\perp(z_2),$$



Extraction of Collins functions from data



SIDIS
 HERMES: PRL **94**, 012002 (2005)
 COMPASS: NP **B765**, 31 (2007)

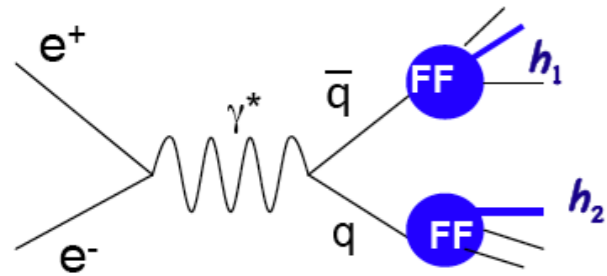
$$A_T \propto h_1(x_B) \otimes H_1^\perp(z)$$

+

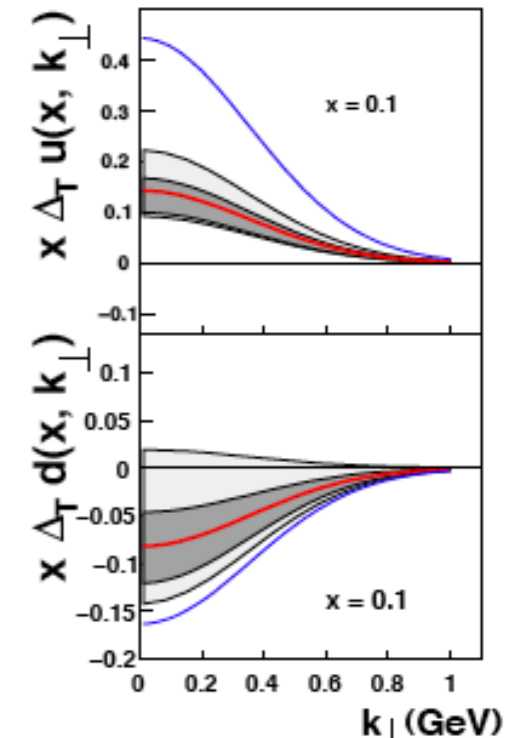
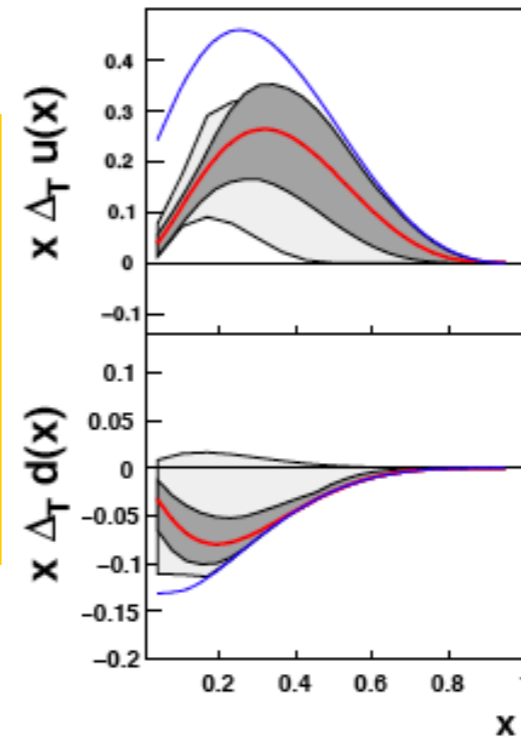
e⁺e⁻ annihilation

BELLE: PRL **96**, 232002, PRD
 78, 03201, PRD 86,039905(E)

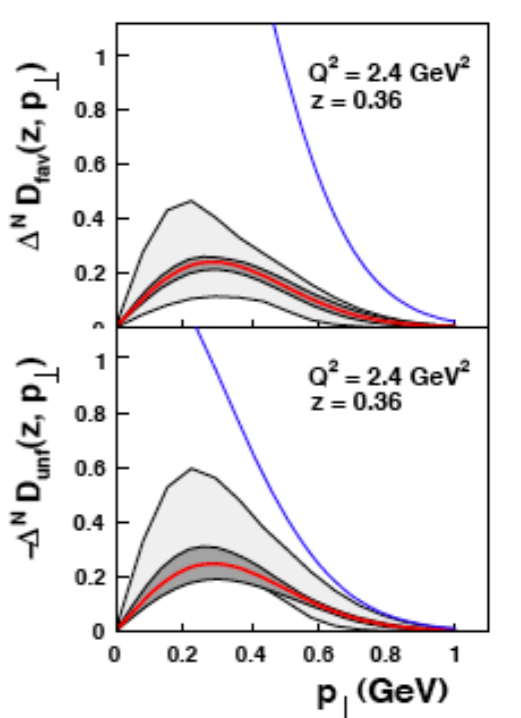
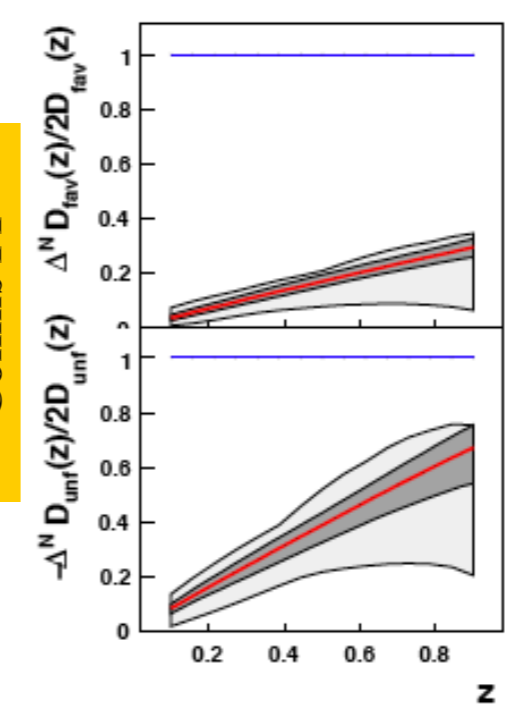
$$A \propto H_1^\perp(z_1) \otimes H_1^\perp(z_2)$$



Transversity PDF



Collins FF



GLOBAL ANALYSIS: simultaneous determination of H_1^\perp and the transversity parton distribution function h_1

Anselmino et al., PRD 75, 054032, NP Proc.Suppl. 191, 98

Improvements from BABAR studies:

- Different number of pion fractional energy intervals
- Asymmetry vs. p_t and 4-D analysis
- Measurement obtained with a different experimental setup
 \implies different systematics

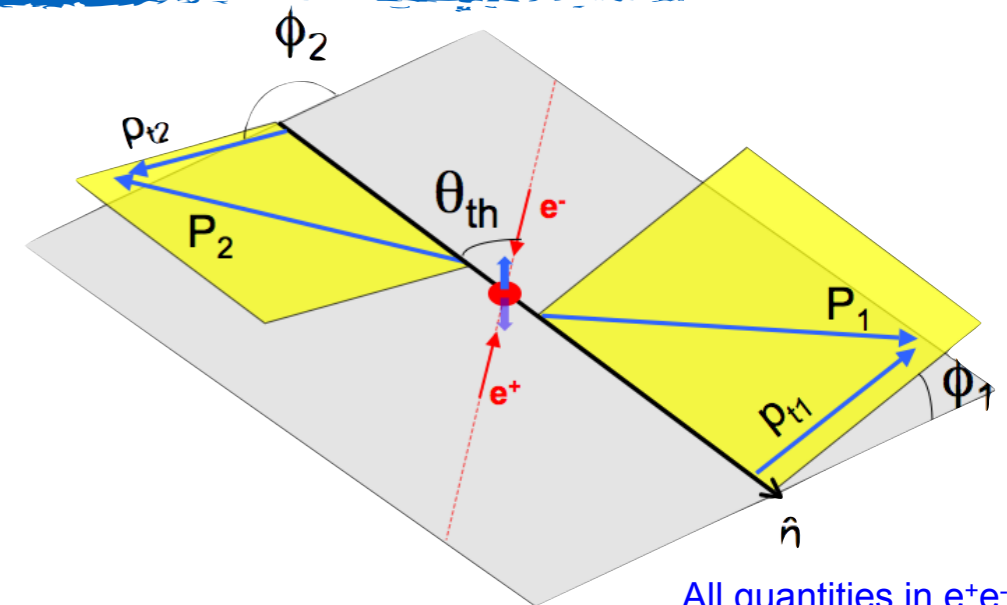
Reference Frames

RF12 or Thrust RF

- **Thrust axis** to estimate the $q\bar{q}$ direction
- $\phi_{1,2}$ defined using thrust-beam plane
- Modulation diluted by gluon radiation, detector acceptance,...

$$\frac{d\sigma(e^+e^- \rightarrow \pi_1\pi_2X)}{dz_1dz_2d\phi_1d\phi_2d\cos\theta_{th}} = \sum_{q,\bar{q}} \frac{3\alpha^2}{s} \frac{e_q^2}{4} z_1^2z_2^2 \times$$

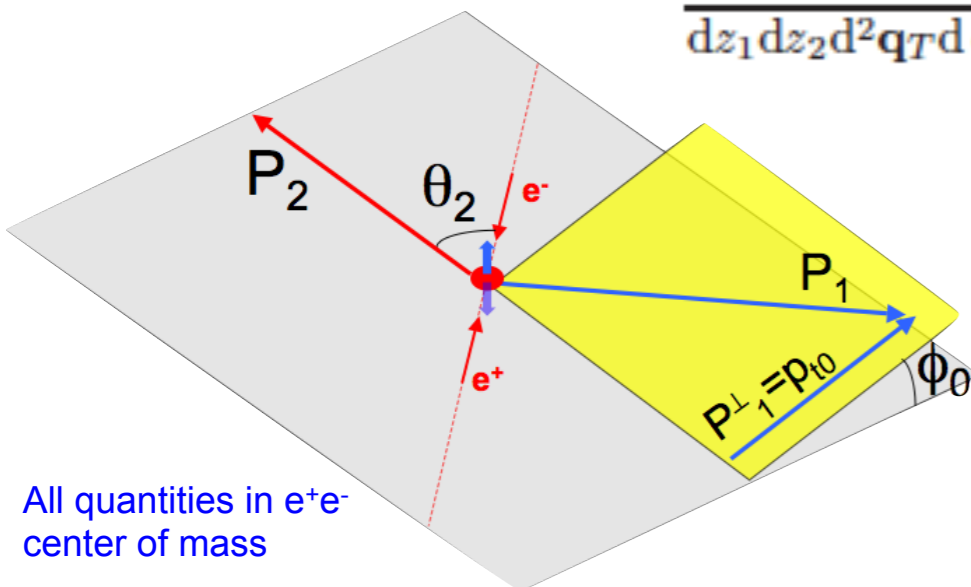
$$\{(1 + \cos^2\theta_{th}) D_1^{q,[0]}(z_1)\bar{D}_1^{q,[0]}(z_2) + \sin^2\theta_{th} \cos(\phi_1 + \phi_2) H_1^{\perp q,[1]}(z_1)\bar{H}_1^{\perp q,[1]}(z_2)\}$$



RF0 or Second hadron frame

$$\frac{d\sigma(e^+e^- \rightarrow \pi_1\pi_2X)}{dz_1dz_2d^2\mathbf{q}_T d\cos(\theta_2)d\phi_0} = \frac{3\alpha^2}{s} \frac{z_1^2z_2^2}{4} \times \left\{ (1 + \cos^2\theta_2) \mathcal{F}(D_1(z_1)\bar{D}_1(z_2)) + \sin^2\theta_2 \cos(2\phi_0) \right.$$

$$\left. \times \mathcal{F} \left[(2\hat{h} \cdot \mathbf{k}_T \hat{h} \cdot \mathbf{p}_T - \mathbf{k}_T \cdot \mathbf{p}_T) \frac{H_1^\perp(z_1)\bar{H}_1^\perp(z_2)}{M_\pi^2} \right] \right\}$$



- Alternatively, just use **one track** in a pair
- Very clean experimentally (no thrust axis), less theoretically
- Gives quark direction for higher pion momentum

[See NPB 806, 23 (2009)]

Collins effect in e^+e^- annihilation

Different combination of charged pions: $e^+e^- \rightarrow q\bar{q} \rightarrow \pi_1^\pm \pi_2^{\pm(\mp)} X$ ($q=u, d, s$)

\Rightarrow sensitivity to **favored** or **unfavored** FFs

- **favored** fragmentation process: i.e. $u \rightarrow \pi^+$, $d \rightarrow \pi^-$, describes the fragmentation of a quark of flavor q into a hadron with a valence quark of the same flavor
- **disfavored** for $d \rightarrow \pi^+$, $u \rightarrow \pi^-$, and $s \rightarrow \pi^\pm$

$$D^{\text{fav}}(z) = D_u^{\pi^+}(z) = D_d^{\pi^-}(z)$$

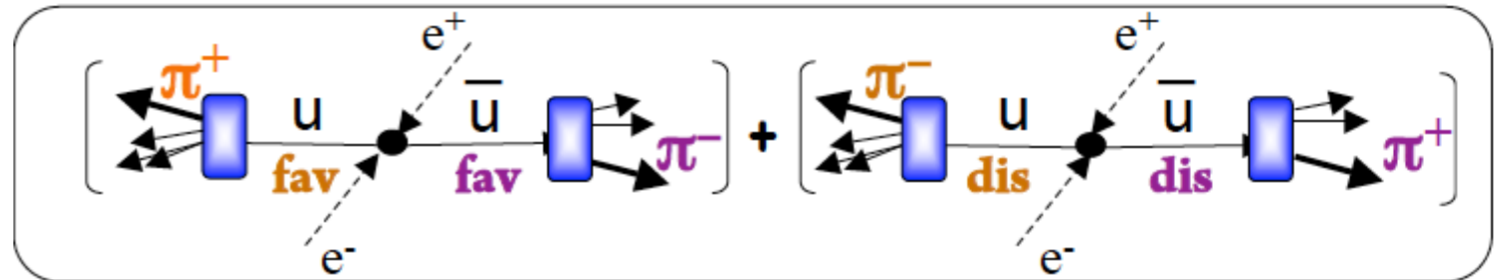
$$\bar{D}^{\text{fav}}(z) = D_{\bar{u}}^{\pi^-}(z) = D_{\bar{d}}^{\pi^+}(z)$$

$$D^{\text{dis}}(z) = D_u^{\pi^-}(z) = D_d^{\pi^+}(z) = D_s^{\pi^\pm}(z)$$

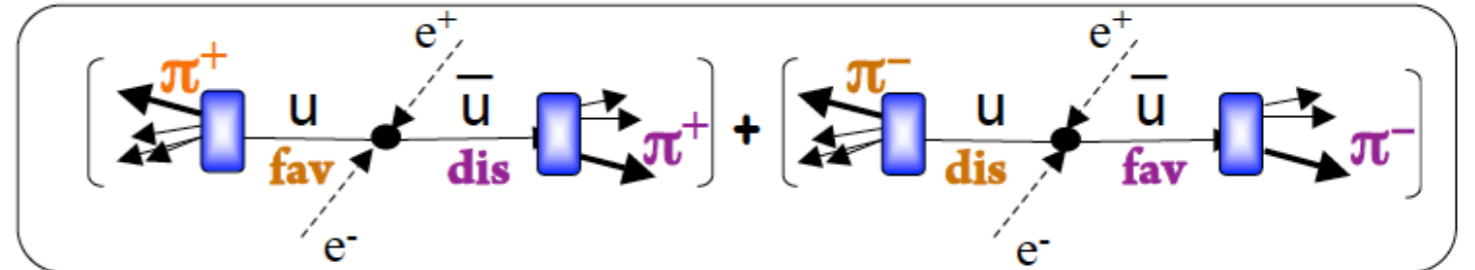
$$\bar{D}^{\text{dis}}(z) = D_{\bar{u}}^{\pi^+}(z) = D_{\bar{d}}^{\pi^-}(z) = D_s^{\pi^\pm}(z)$$

Collins effect in e^+e^- annihilation

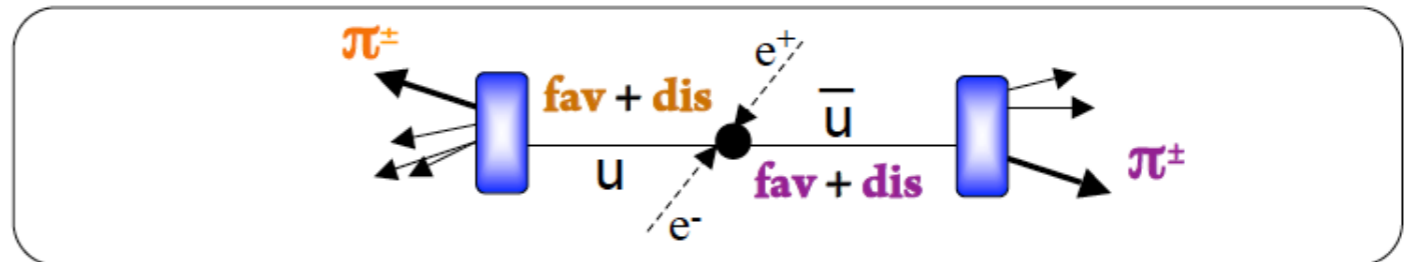
Unlike-sign pion pair = **U**:
 $\pi^+\pi^-$: (**fav** x **fav**)+(**dis** x **dis**)



Like-sign pion pair = **L**:
 $\pi^+\pi^+$: (**fav** x **dis**)+(**dis** x **fav**)



Charged pion pair = **C (U+L)**:
 $\pi\pi$: (**fav** + **dis**)x(**fav** + **dis**)
 $\pi=\pi^\pm$



The cross section can be written in terms of favored and disfavored fragmentation functions:

$$N^U(\phi) = \frac{d\sigma(e^+e^- \rightarrow \pi^\pm\pi^\mp X)}{d\Omega dz_1 dz_2} \propto \frac{5}{9} D^{\text{fav}}(z_1) \bar{D}^{\text{fav}}(z_2) + \frac{7}{9} D^{\text{dis}}(z_1) \bar{D}^{\text{dis}}(z_2)$$

$$N^L(\phi) = \frac{d\sigma(e^+e^- \rightarrow \pi^\pm\pi^\pm X)}{d\Omega dz_1 dz_2} \propto \frac{5}{9} D^{\text{fav}}(z_1) \bar{D}^{\text{dis}}(z_2) + \frac{5}{9} D^{\text{dis}}(z_1) \bar{D}^{\text{fav}}(z_2) + \frac{2}{9} D^{\text{dis}}(z_1) \bar{D}^{\text{dis}}(z_2)$$

$$N^C(\phi) = \frac{d\sigma(e^+e^- \rightarrow \pi\pi X)}{d\Omega dz_1 dz_2} = N^U(\phi) + N^L(\phi) \propto \frac{5}{9} [D^{\text{fav}}(z_1) + D^{\text{dis}}(z_1)] [\bar{D}^{\text{fav}}(z_2) + \bar{D}^{\text{dis}}(z_2)] + \frac{4}{9} D^{\text{dis}}(z_1) \bar{D}^{\text{dis}}(z_2)$$

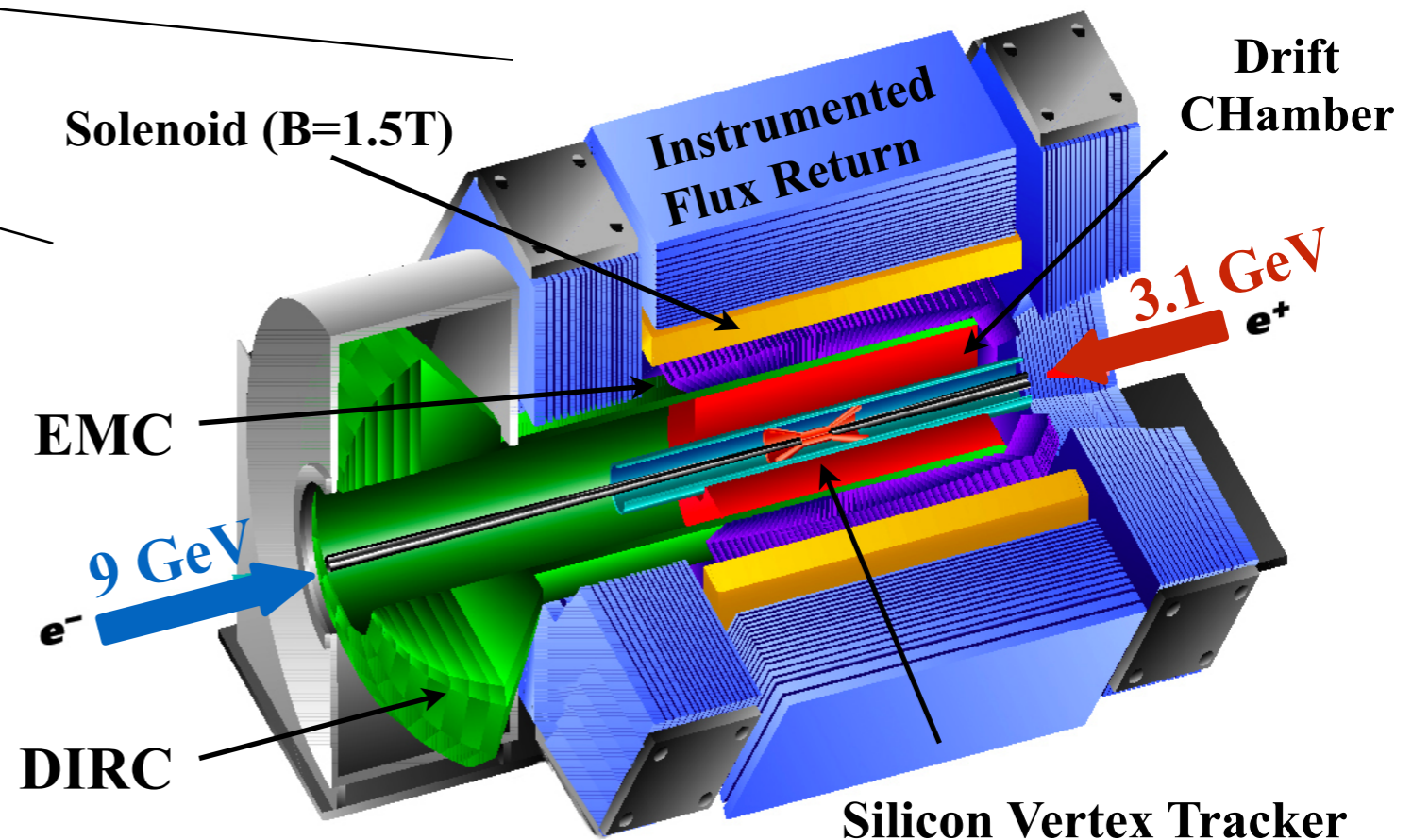
PEP-II and the BaBar Detector at SLAC



- Asymmetric e^+e^- collider operating at the $\Upsilon(4S)$ resonance ($\sqrt{s}=10.58$ GeV)
 - High Energy Ring (**HER**): 9.0 GeV e^-
 - Low Energy Ring (**LER**): 3.1 GeV e^+
 - c.m.-lab boost, $\beta\gamma\approx 0.56$
- High luminosity: $L \sim 468 \text{ fb}^{-1}$ used here

- Asymmetric detector
 - c.m. acceptance $-0.9 < \cos\theta^* < 0.85$ wrt e^- beam
- Excellent performance
 - good tracking, mass resolution
 - good γ , π^0 reconstruction
 - full e , μ , π , K , and p identification

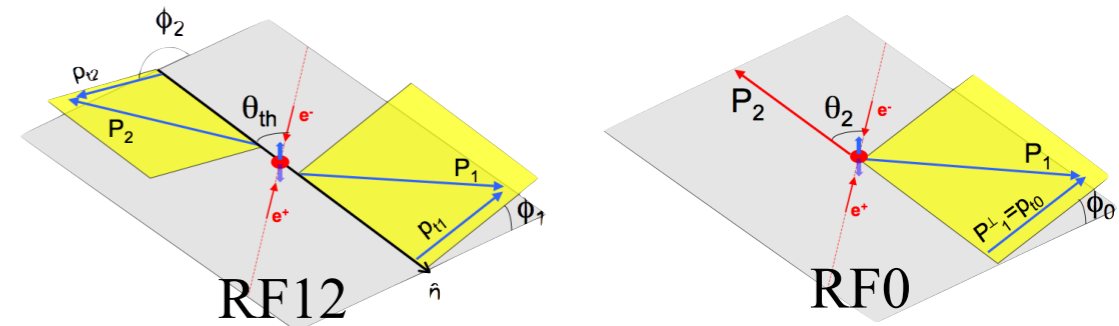
NIM A479,1 (2002),
update: NIM A729, 615 (2013)



Analysis strategy

- 1) The analysis is performed using an integrated luminosity of $\mathcal{L} \sim 470 \text{ fb}^{-1}$ of data collected at the $\Upsilon(4S)$ and off-resonance
- 2) We study the Collins asymmetry in two different reference frames: RF12 and RF0
(Nucl.Phys. B 806, 23 (2009), PRD 78, 032011 (2008))

- Selection of multi-hadronic events
- Selection of pions in opposite jets according to the thrust axis
 - the thrust axis in the $e^+ e^-$ center of mass frame is assumed to be the $q\bar{q}$ direction
 - thrust axis direction chosen at random to avoid forward/backward detector asymmetry effect
- Measurement of the azimuthal angles ϕ_i in both reference frames as a function of:
 - pion fractional energies $(z_1, z_2) \implies (6 \times 6)$ bins
 - pion transverse momenta: $(p_{t1}, p_{t2}) \implies (4 \times 4)$ bins; $p_{t0} \implies 9$ bins
 - $\sin^2 \theta_{(th,2)} / (1 + \cos^2 \theta_{(th,2)}) \implies 15$ bins
 - 4-D analysis $\implies (z_1, z_2) \times (p_{t1}, p_{t2}) \implies (4 \times 4) \times (3 \times 3)$
- Fit to the azimuthal distributions
- Estimation and subtraction of backgrounds
- Study of the systematic effects

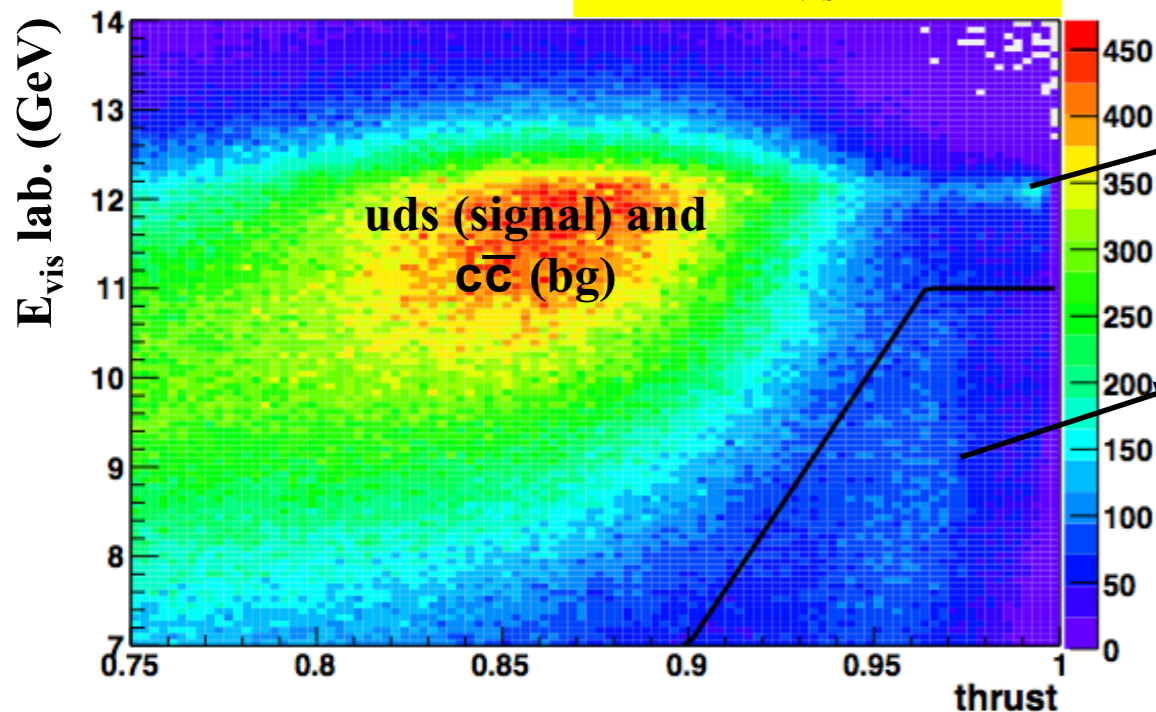


Event and track selection

EVENT SELECTION

- Number of charged tracks > 2
- Visible energy: $E_{\text{vis}} > 7 \text{ GeV}$
- Selection of two-jet topology events requiring **thrust** > 0.8
- Events in the $\tau^+\tau^-$ region removed

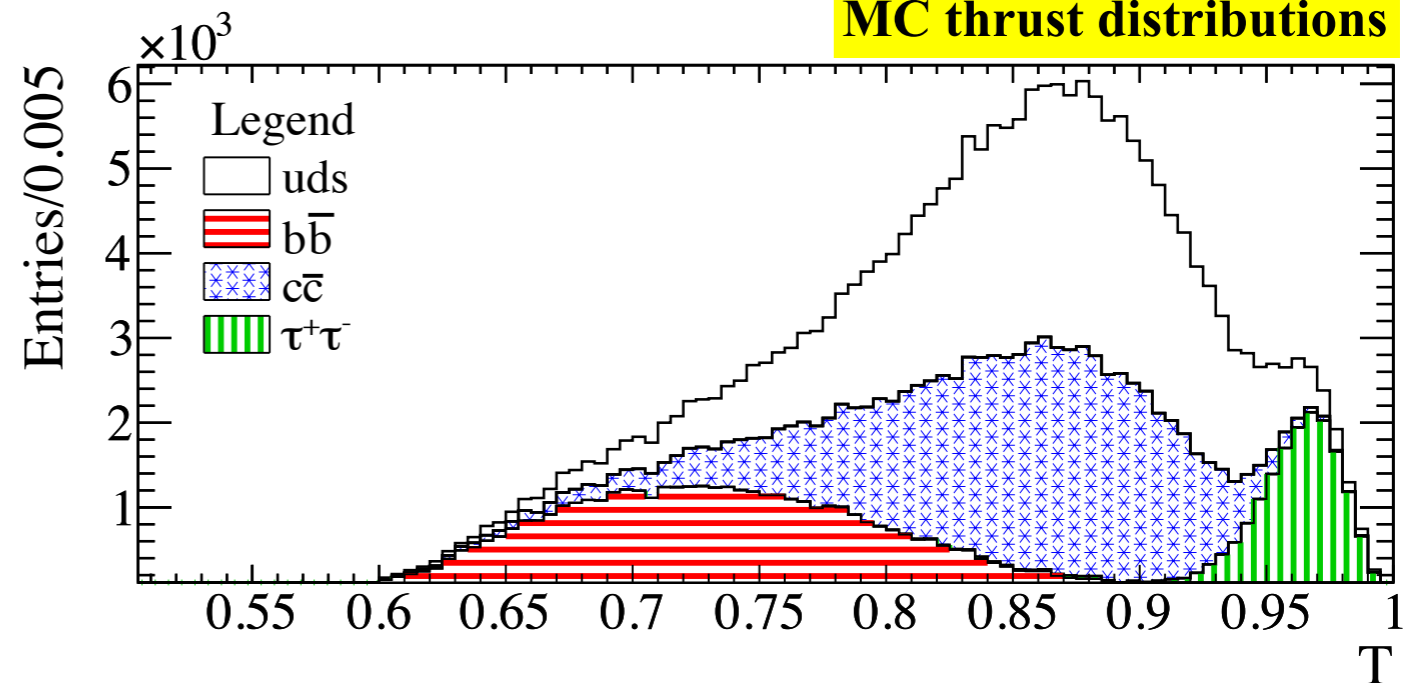
DATA: E_{vis} vs thrust



Bhabha and $\mu^+\mu^-(\gamma)$ events,
with $\gamma \rightarrow e^+e^-$ conversion

$\tau^+\tau^-$
region

MC thrust distributions



TRACK SELECTION

- μ^\pm and e^\pm veto, and pion ID required
- Tracks in the detector acceptance region:
 $0.41 < \theta_{\text{lab}} < 2.54 \text{ rad}$
- **Pion fractional energies:**
 $0.15 < z = 2E_{\pi}/\sqrt{s} < 0.9$

→ Opening angle ($\theta_{\text{pi-thrust}}$) of the pions with respect to the thrust axis $< 45^\circ$

→ $Q_t < 3.5 \text{ GeV}$, where Q_t is the transverse momentum of the virtual photon in the pions c.m.

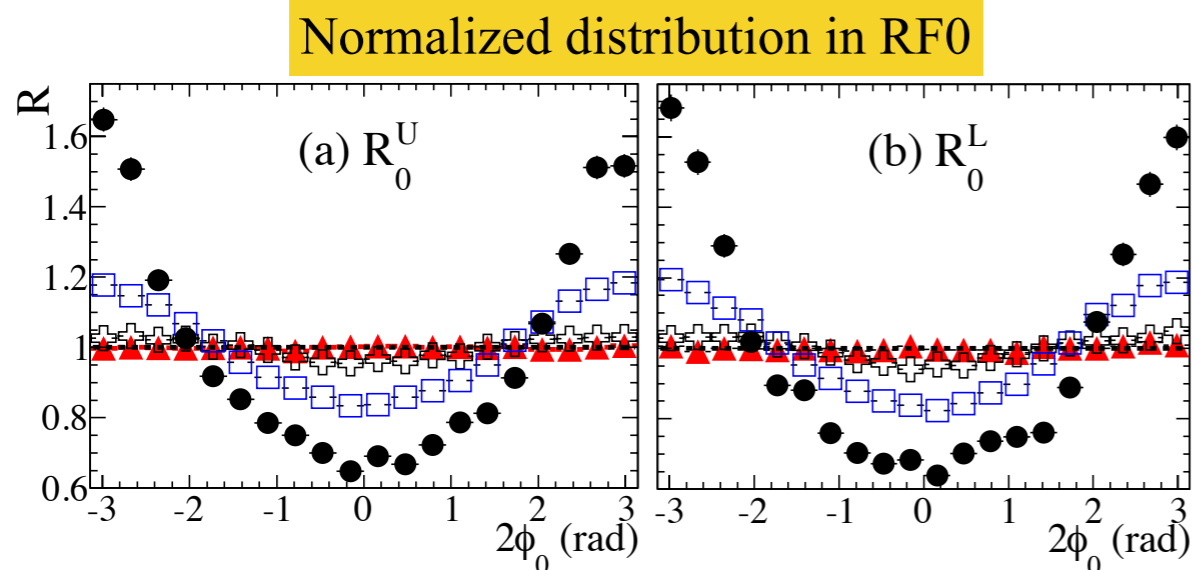
Raw asymmetry

- **Collins asymmetry**

- consider all the **U** and **L** pion pairs
- make the normalized distributions of $\phi_\alpha = \phi_1 + \phi_2$ or $2\phi_0$ ($\alpha=12,0$)

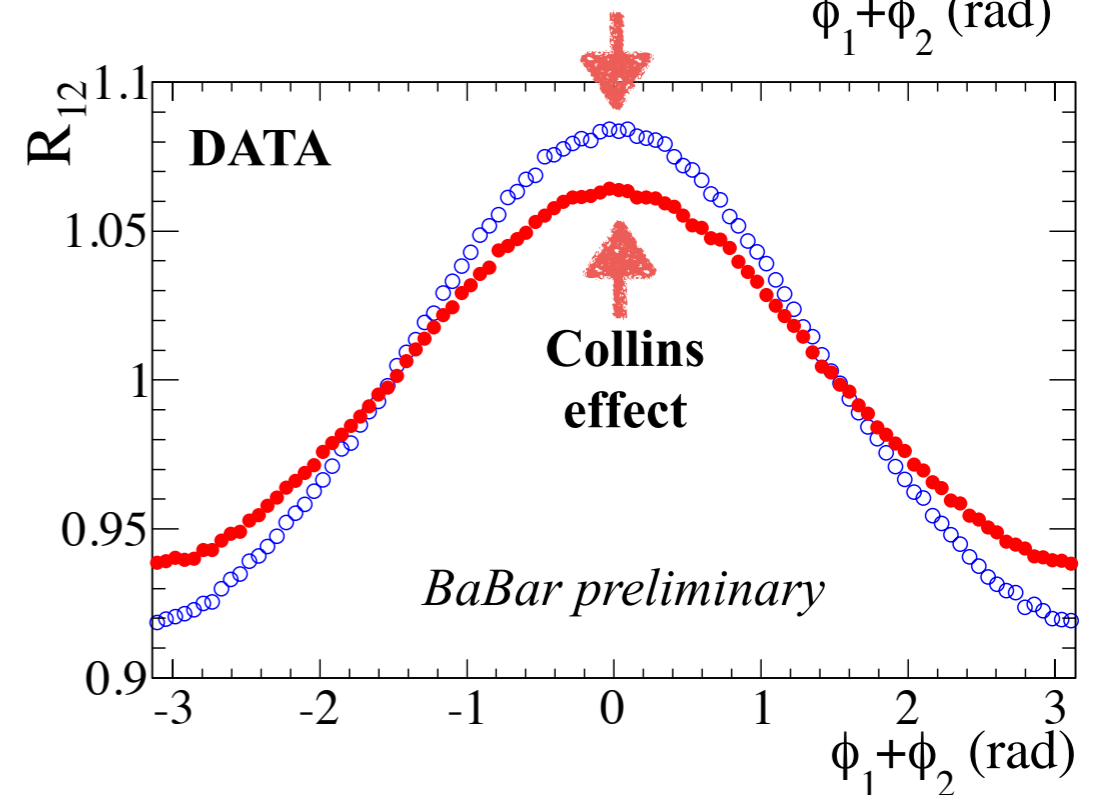
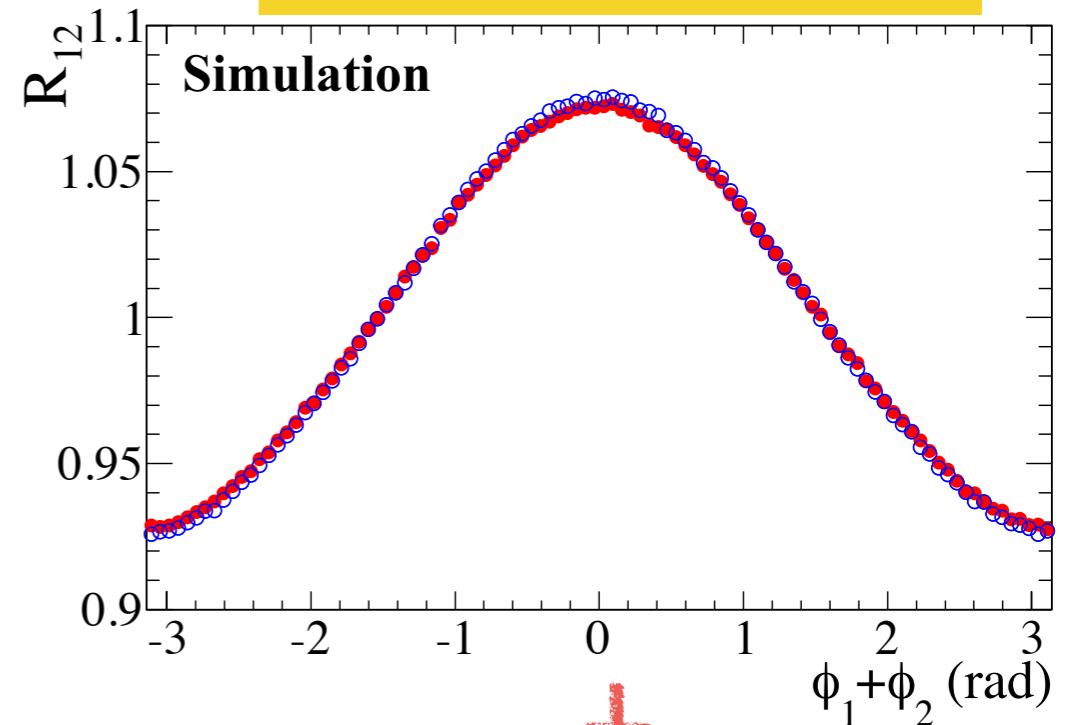
- **The MC generator (JETSET) does not include the Collins effect, but it shows a strong cosine modulation**

- mostly due to acceptance of the detector
- depends strongly on the thrust axis polar angle
- but similar distribution for **U** and **L** pairs



- **Data shows a large difference between U and L distributions, that can be ascribed to the Collins effect**

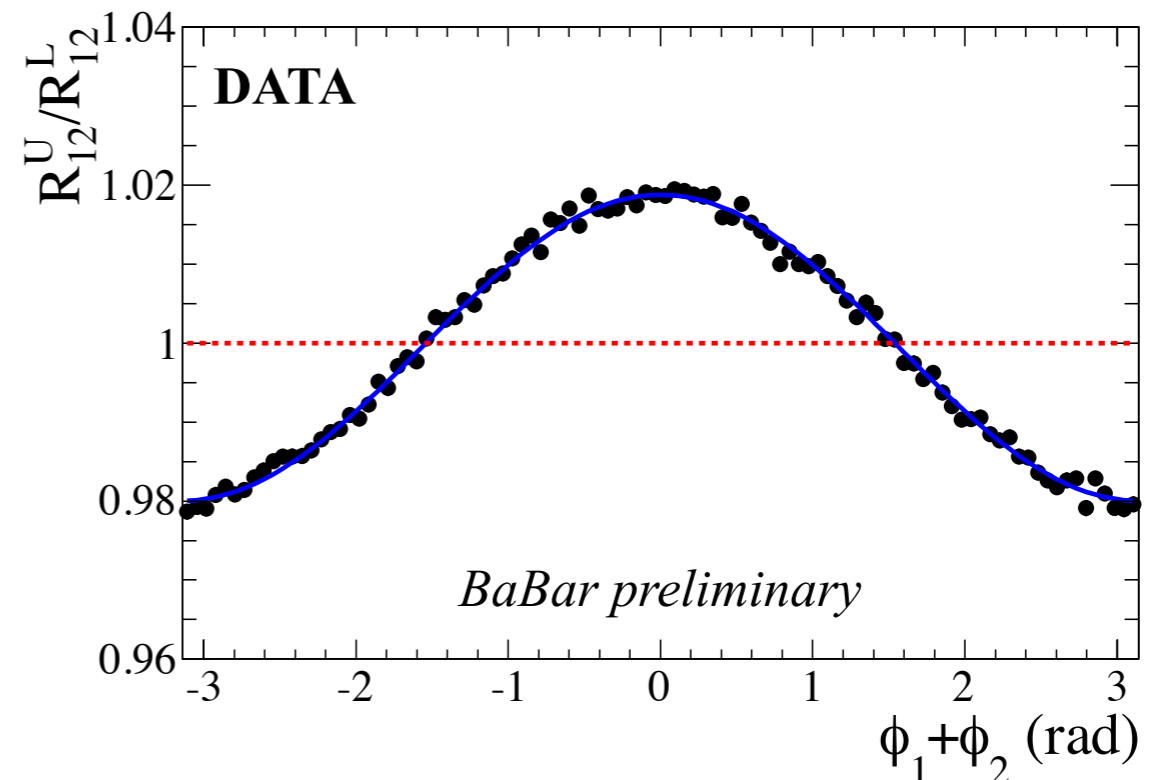
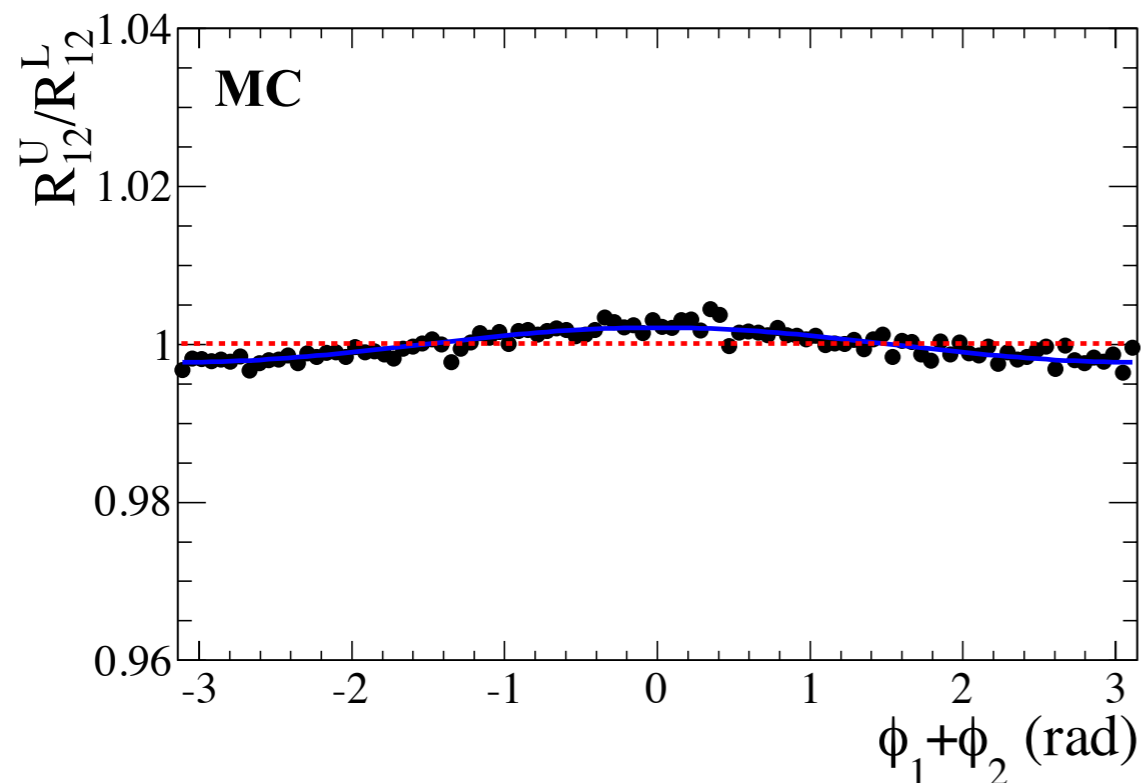
Normalized distribution in RF12



Double Ratio

Acceptance effects can be reduced by performing the ratio of **Unlike/Like** sign pion pairs (or **Unlike/Charged**)

- small deviation from zero still present (\ll asymmetry measured in data sample)



MC: small deviation from a flat distribution

DATA: cosine modulation clearly visible

$$\frac{R_{\alpha}^U}{R_{\alpha}^{L(C)}} = \frac{N^U(\phi_{\alpha}) / \langle N^U(\phi_{\alpha}) \rangle}{N^{L(C)}(\phi_{\alpha}) / \langle N^{L(C)}(\phi_{\alpha}) \rangle} \rightarrow B_{\alpha}^{UL(UC)} + A_{\alpha}^{UL,(UC)} \cdot \cos(\phi_{\alpha})$$

A : contains only the Collins effect and higher order radiative effects

Extraction of uds Collins asymmetry

- In each bin, the data sample includes pairs from
 - signal uds events
 - $B\bar{B}$ events (small, mostly at low z)
 - $c\bar{c}$ events (important at low/medium z)
 - $\tau^+\tau^-$ events (important at high z)

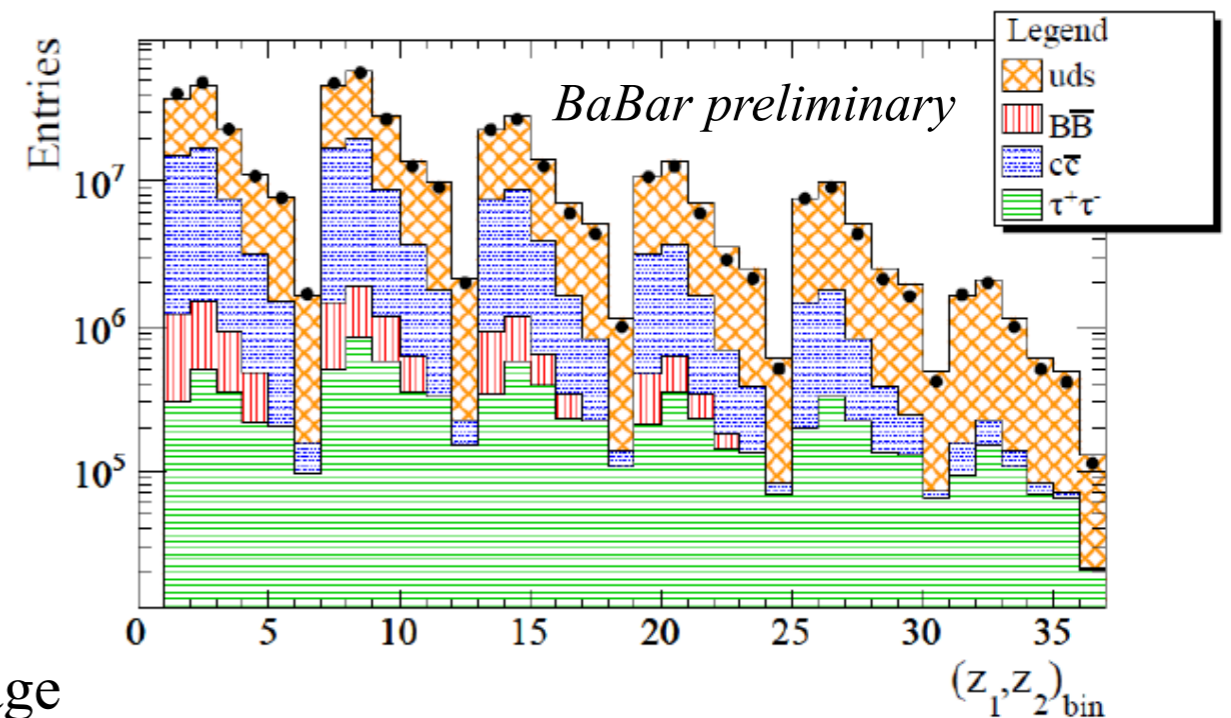


Fraction of $\pi\pi$ due to the i^{th} bkg process

$$A_{\alpha}^{\text{meas}} = \left(1 - \sum_i F_i\right) \cdot A_{\alpha} + \sum_i F_i \cdot A_{\alpha}^i$$

True asymmetry \swarrow
 \uparrow Bkg asymmetry

- We must calculate these quantities:
 - F_i using MC sample; we assign MC-data difference in each bin as systematic error
 - $A^{B\bar{B}}$ must be zero; we set $A^{B\bar{B}} = 0$
 - A^{τ} small in simulation; checked in data; we set $A^{\tau} = 0$

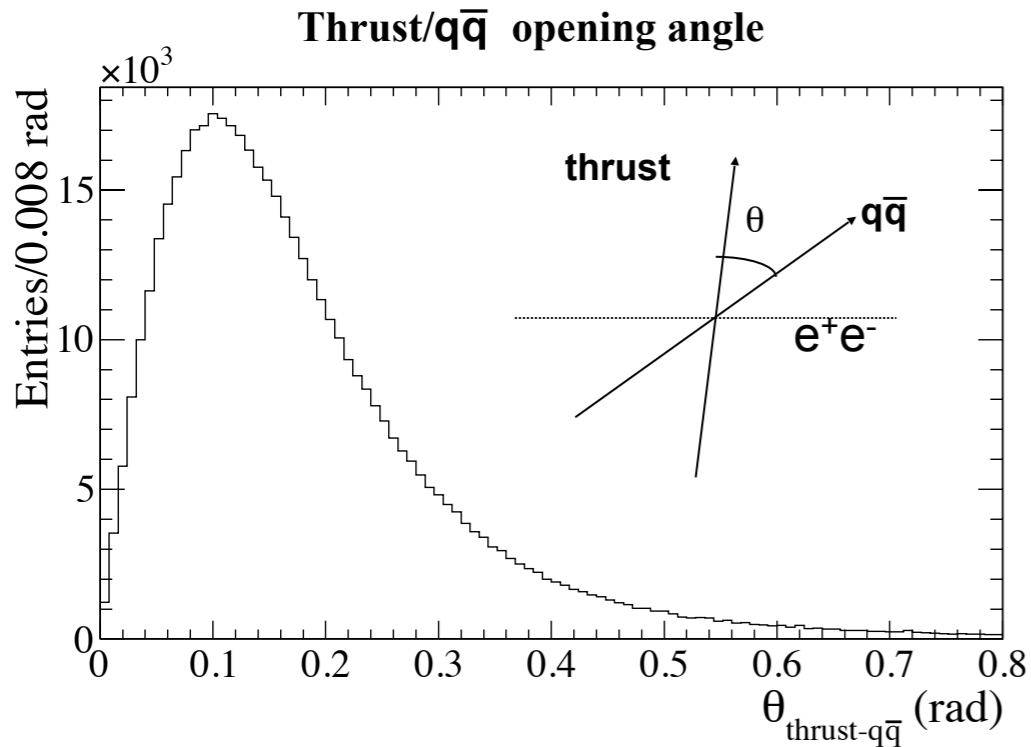


- **Charm** background contribution is about 30% on average
 - Both fragmentation processes and weak decays can introduce azimuthal asymmetries
 - We used a **$D^{*\pm}$ -enhanced control sample** to estimate its effect

$$A_{\alpha}^{\text{meas}} = (1 - F_c - F_B - F_{\tau}) \cdot A_{\alpha} + F_c \cdot A_{\alpha}^c$$

$$A_{\alpha}^{D^*} = (1 - f_c - f_B) \cdot A_{\alpha} + f_c \cdot A_{\alpha}^c$$

Asymmetry dilution



The experimental method assumes the thrust axis as $q\bar{q}$ direction: this is only a rough approximation

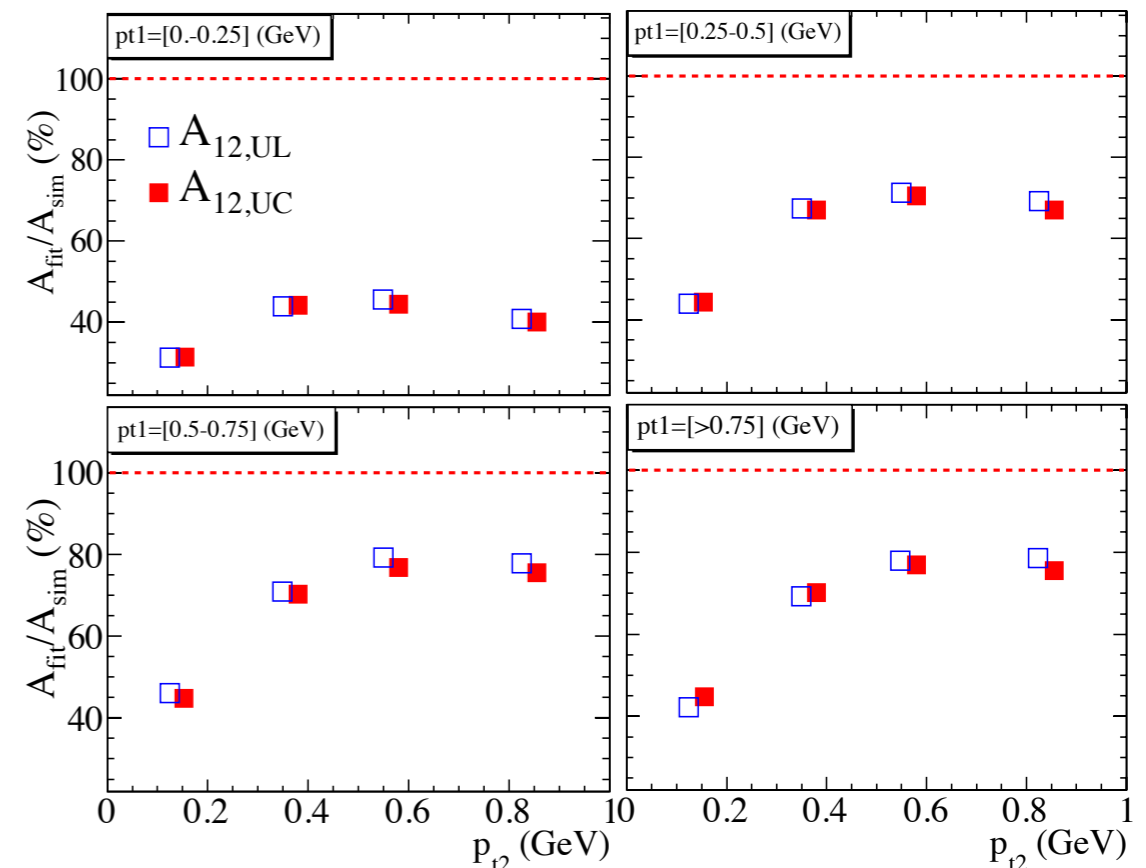
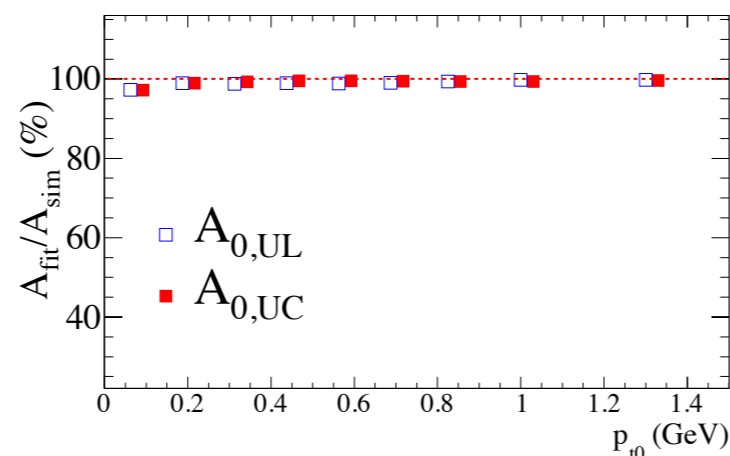
RF12: large smearing since the azimuthal angles ϕ_1 and ϕ_2 are calculated with respect to the thrust axis; additional dilution due to very energetic tracks close to the thrust axis.

RF0: the azimuthal angle ϕ_0 is calculated with respect to the second hadron momenta \rightarrow small smearing due to PID and tracking resolution.

We study the influence of the detector effects by correcting a posteriori the generated angular distribution: weights defined as $w^{UL(UC)} = 1 \pm a \cdot \cos(\phi_{gen12,0})$ are applied to every selected pion pairs.

RF12: correction ranging between (1.3-2.3) as a function of z , and (1.3-3) as a function of p_t .

RF0: no correction needed.



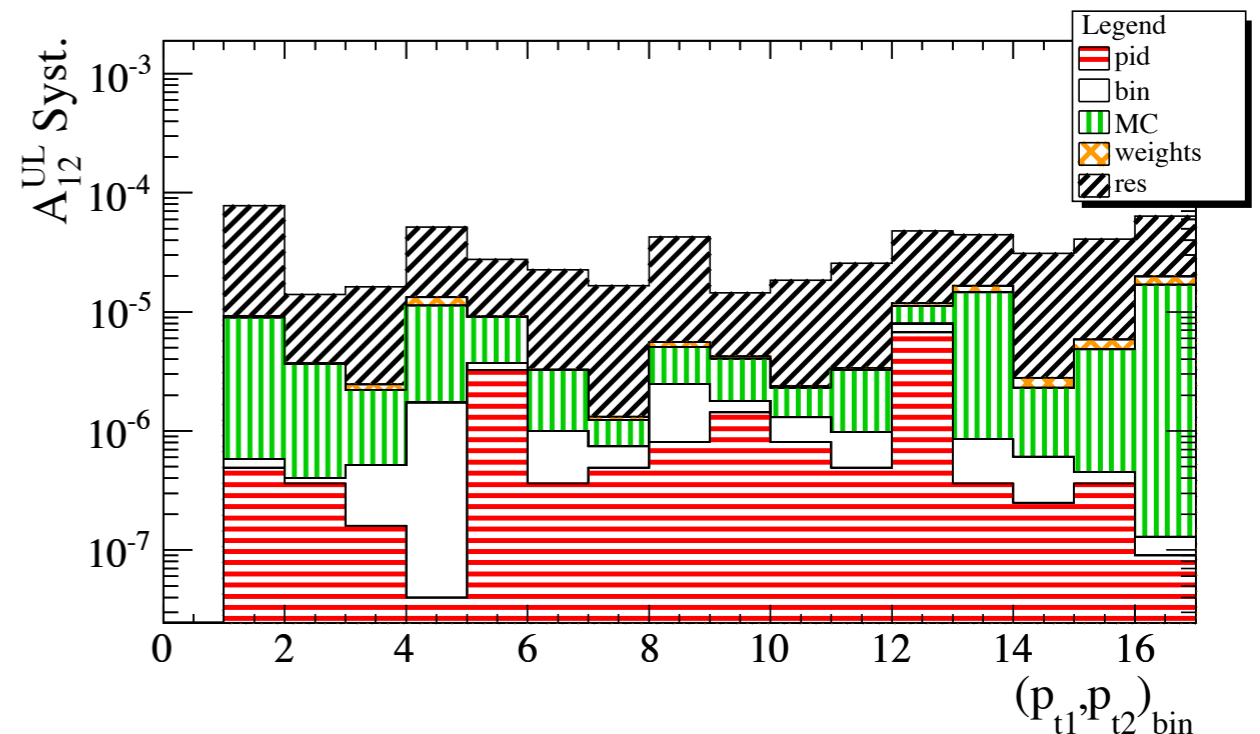
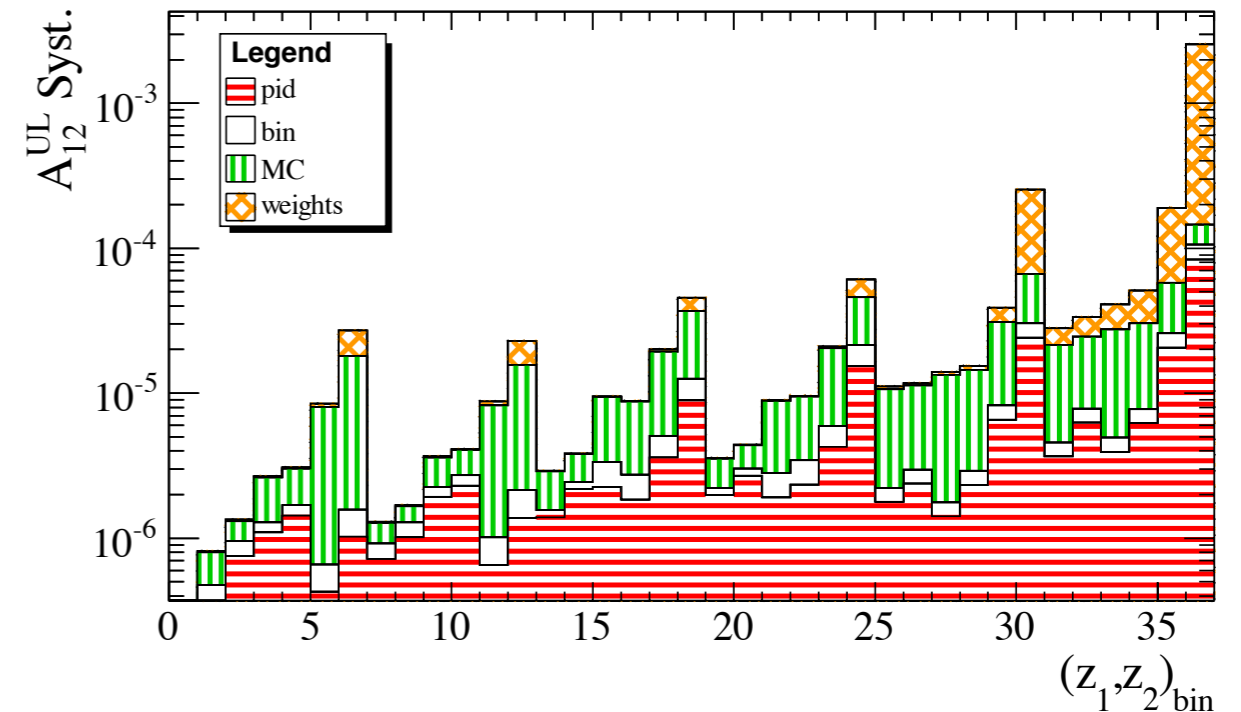
Corrections and Systematics summary

We correct the asymmetries for:

- **Background contributions**
- **MC bias**
- **Dilution effects** (RF12 only)

A large number of systematic checks were done. The main contributions come from:

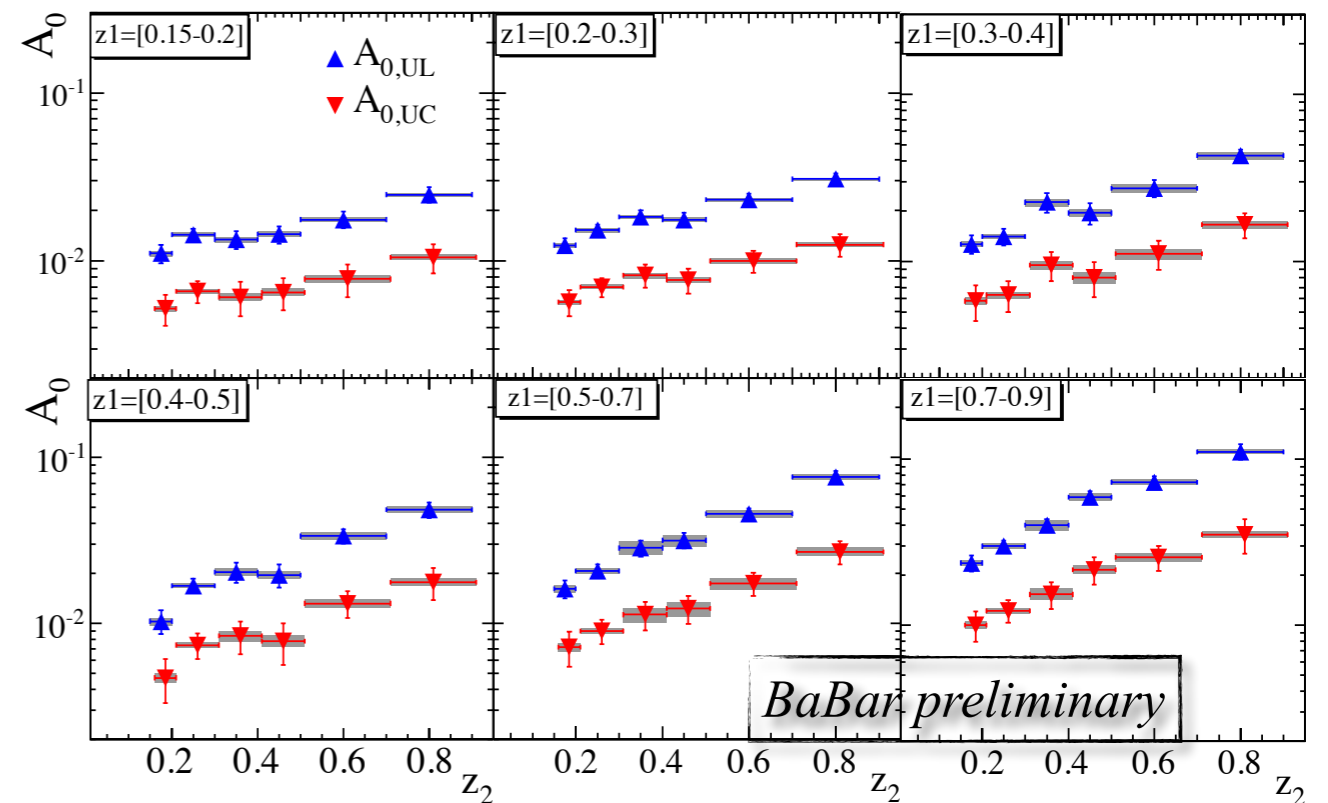
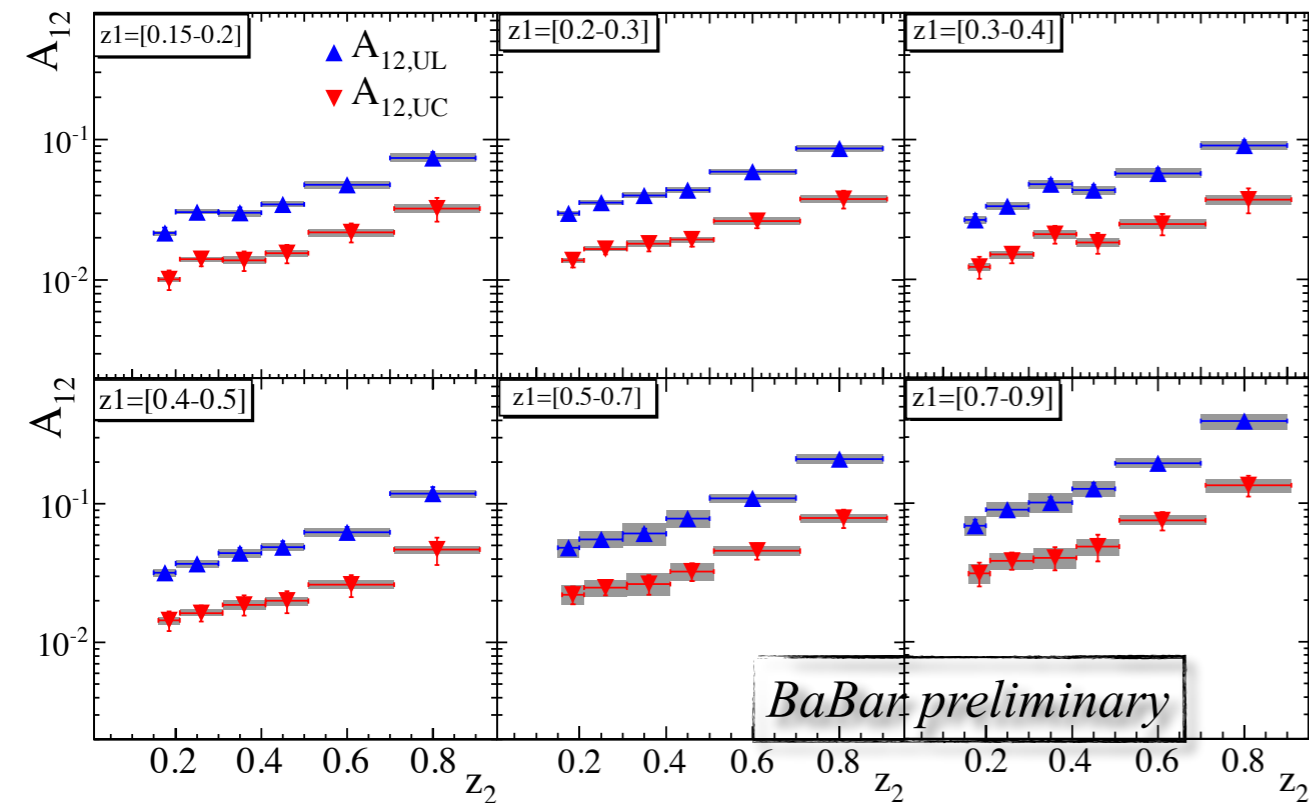
- **Particle identification (PID):** few percent change in the asymmetry by changing the PID cuts
- **Fit procedure:** different angular bin size leads to about 1% of deviation from standard bins
- **MC uncertainties:** we used different track selection requirements
- **Dilution method**
- Pion transverse **momentum resolution** (only for the asymmetry *vs.* (p_{t1}, p_{t2})). The p_t resolution is about 100 MeV on average \implies 10% effect on asymmetries for all bins, except for the lowest energies (30%)



Results I: asymmetry vs. (z_1, z_2)

RF12

RF0



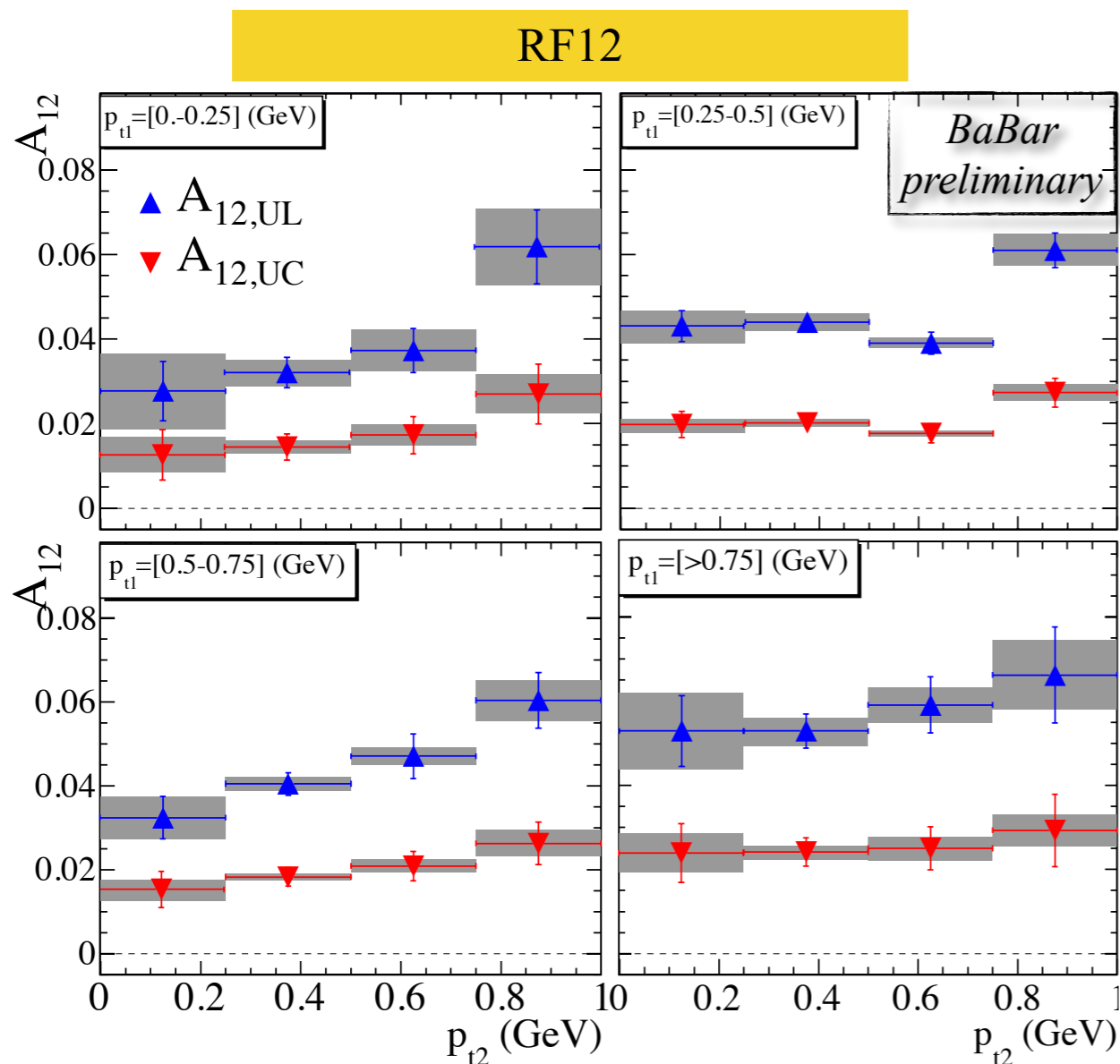
Statistical errors shown as bars; systematic errors shown as bands

Significant nonzero A^{UL} and A^{UC} in all bins

- strong dependence on (z_1, z_2) : 1-39% in RF12 and 1-11% in RF0
- $A^{UC} < A^{UL}$ as expected; complementary information about the favored and disfavored fragmentation processes (PRD 73, 094025 (2006))
- consistent with $z_1 \Leftrightarrow z_2$ symmetry

Results II: asymmetry vs. (p_{t1}, p_{t2})

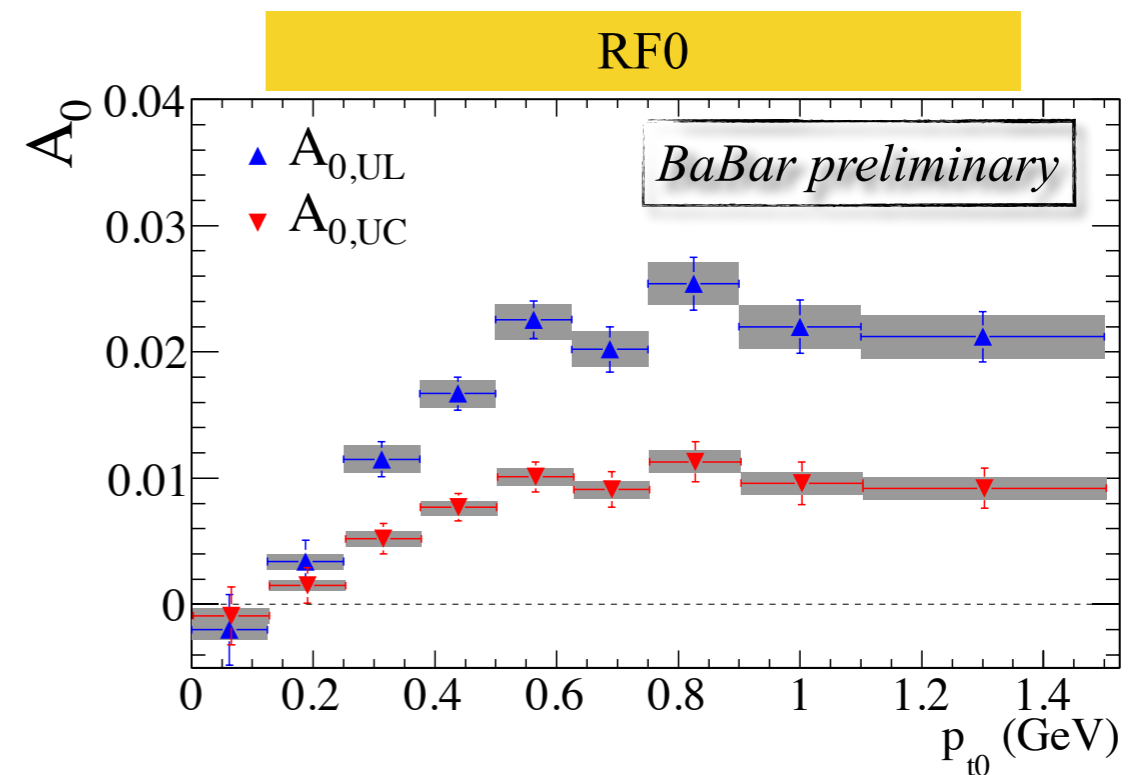
- **FIRST MEASUREMENT** of Collins asymmetries vs. p_t in e^+e^- annihilation at $Q^2 \sim 110$ (GeV/c)² (time-like region)
- **non-zero A^{UL} and A^{UC} asymmetries**



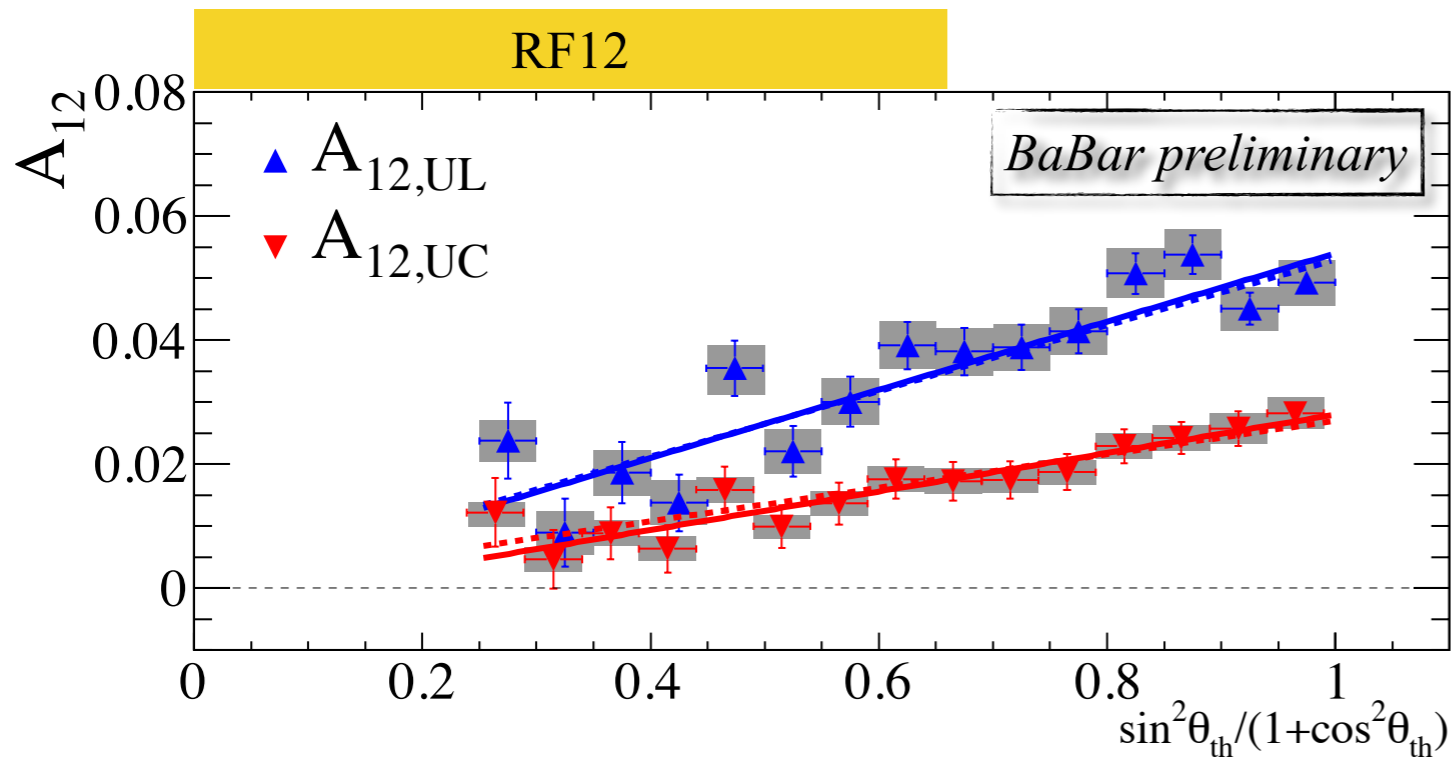
⇒ only modest dependence on (p_{t1}, p_{t2})

⇒ $A_0 < A_{12}$, but interesting structure in p_t

$A^{UC} < A^{UL}$: complementary information on $H_1^{\perp, fav}$ and $H_1^{\perp, dis}$



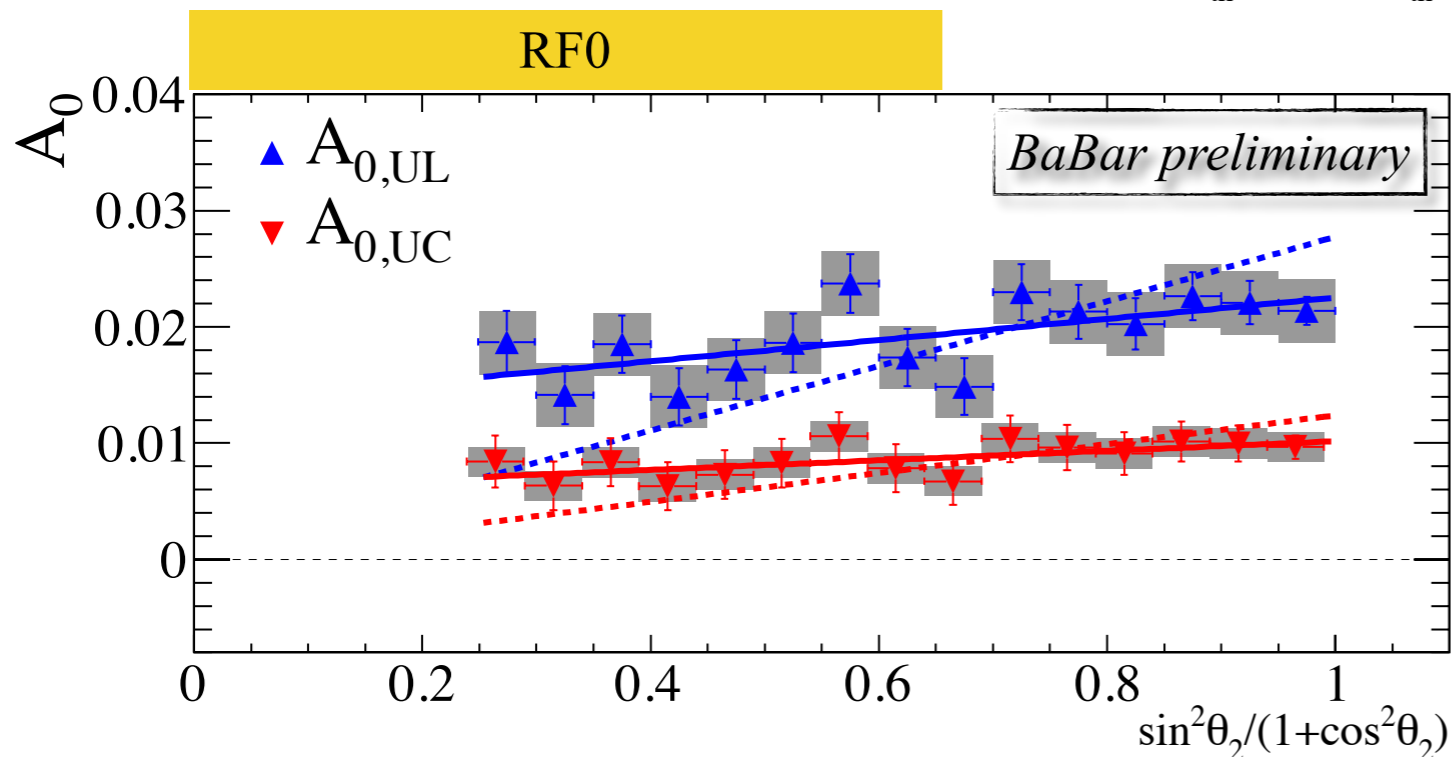
Results III: asymmetry vs. polar angle



We study the angular dependence after integration over fraction energies and transverse momenta

$$A_{12} \propto \frac{\sin^2 \theta_{th}}{1 + \cos^2 \theta_{th}} \cos(\phi_1 + \phi_2) \frac{H_1^\perp(z_1) \bar{H}_1^\perp(z_2)}{D_1(z_1) \bar{D}_1(z_2)}$$

==> Intercept consistent with zero, as expected (consistent with Belle results)

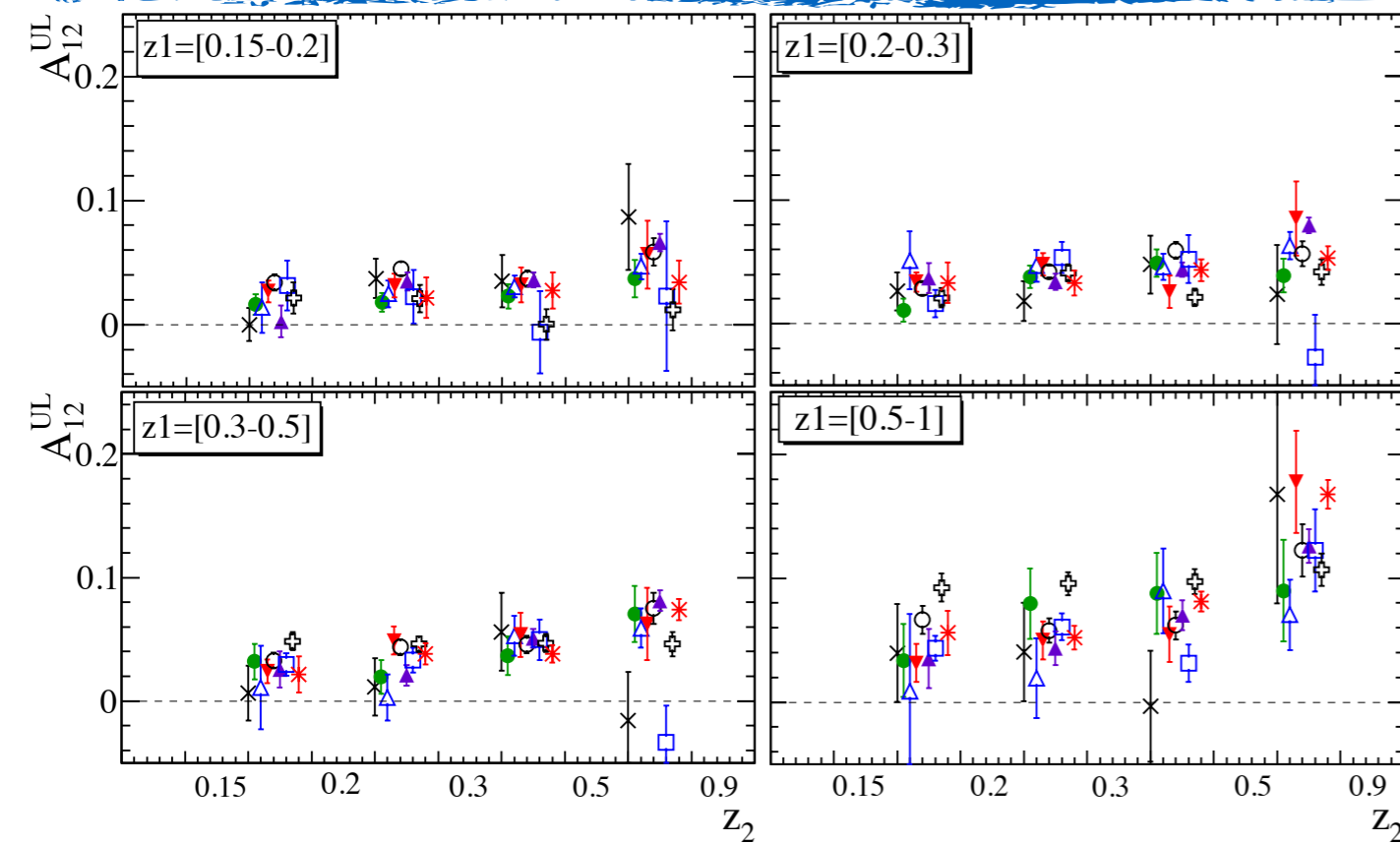


$$A_0 \propto \frac{\sin^2 \theta_2}{1 + \cos^2 \theta_2} \cos(2\phi_0) \mathcal{F} \left[\frac{H_1^\perp(z_1) \bar{H}_1^\perp(z_2)}{D_1(z_1) \bar{D}_1(z_2)} \right]$$

==> The linear fit gives a non-zero constant parameter (consistent with Belle results)

Lines: fit results with a linear functions
Dotted lines: fit results with a linear function crossing the origin

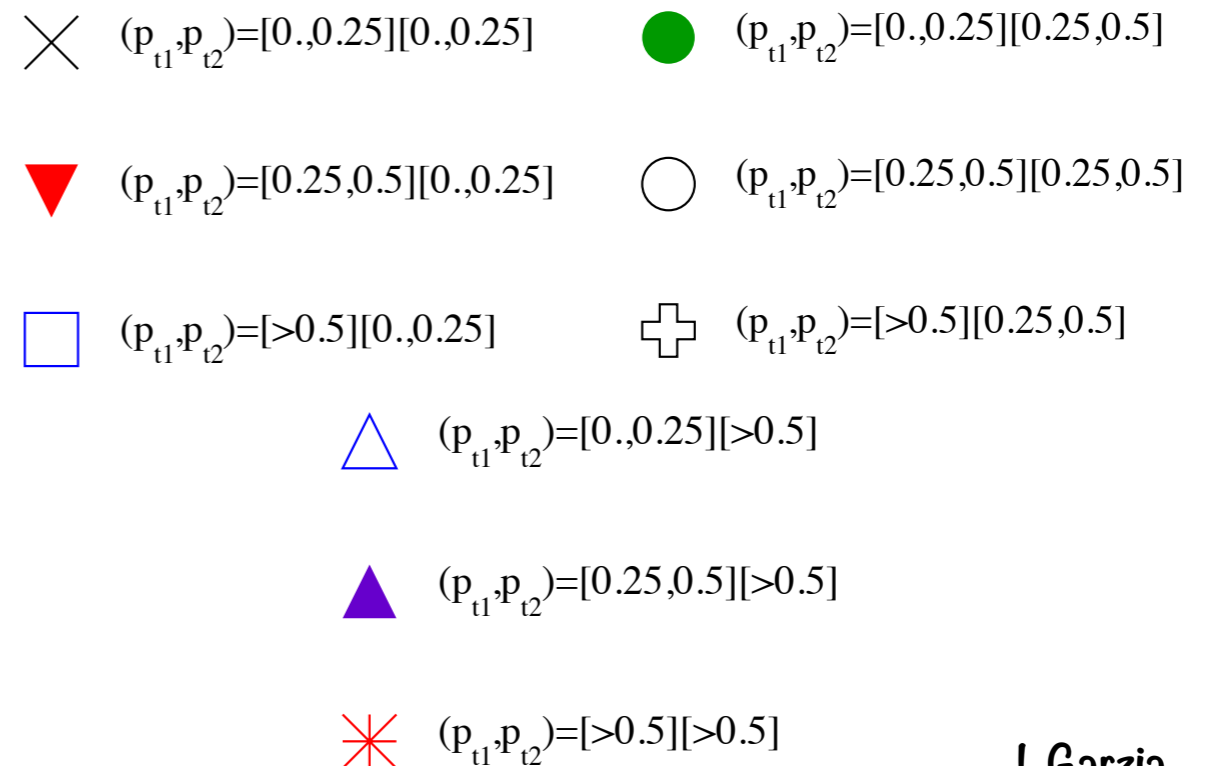
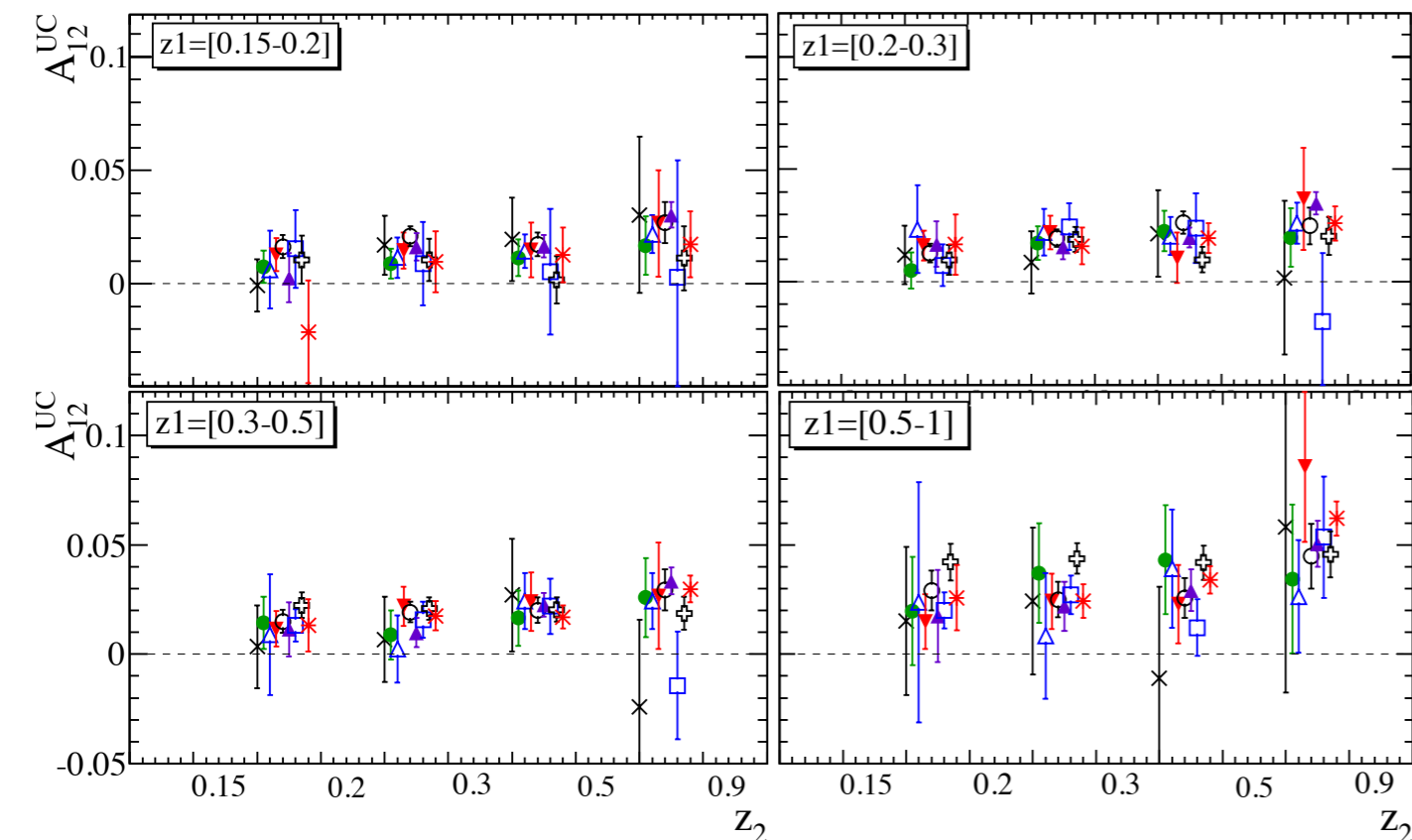
4-D: asymmetry vs. $(z_1, z_2) \times (p_{t1}, p_{t2})$



We study the asymmetries in the RF12 frame in a four-dimensional space:

$$(z_1, z_2, p_{t1}, p_{t2})$$

- We use 4 z_i and 3 p_{t_i} intervals
- Test to probe the factorization of the Collins fragmentation functions
- Powerful tools to access $p_t - z$ correlation



Summary

BABAR has measured the Collins asymmetries for charged pion pairs in $e^+e^- \rightarrow u\bar{u}, d\bar{d}, s\bar{s} \rightarrow \pi^\pm \pi^\pm X$

\Rightarrow in two distinct reference frames	RF12	RF0
\Rightarrow vs. π^\pm fractional energy z	z_1, z_2	z_1, z_2
\Rightarrow vs. π^\pm transverse momentum p_t	p_{t1}, p_{t2}	p_{t0}
\Rightarrow 4-D analysis	z_1, z_2, p_{t1}, p_{t2}	
\Rightarrow polar angle	θ_{th}	θ_2

$\Rightarrow A_{12}$ and A_0 increase with increasing z_1, z_2

- consistent with theoretical expectations
- general agreement with Belle results (PRD 86, 039905(E) (2012))
- effect is stronger for leading particles

$\Rightarrow A_{12}$ (A_0) increases with p_{t1}, p_{t2} (p_{t0}) for p_t between 0 to 1 GeV/c

- first measurement in e^+e^- annihilation at $Q^2 \sim 110$ (GeV/c)²
- important for understanding the evolution of the fragmentation function

$\Rightarrow A_{12}$ (A_0) increases linearly with $\sin^2\theta/(1+\cos^2\theta)$

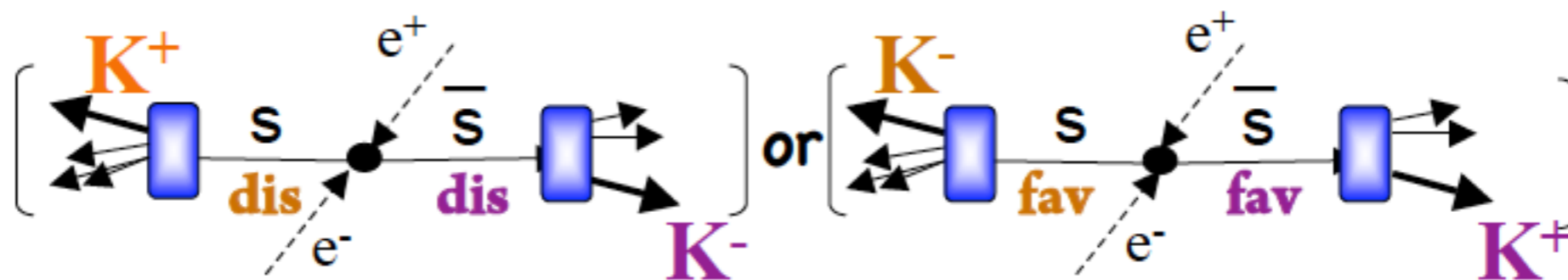
- as (might be) expected

Paper submitted to PRD

PLANS

work in progress

WHAT NEXT? Collins effect for kaon pairs
Why kaon pairs? \Rightarrow Strange contribution to the Collins effect



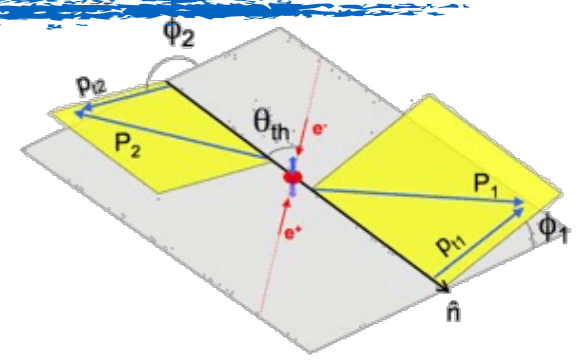
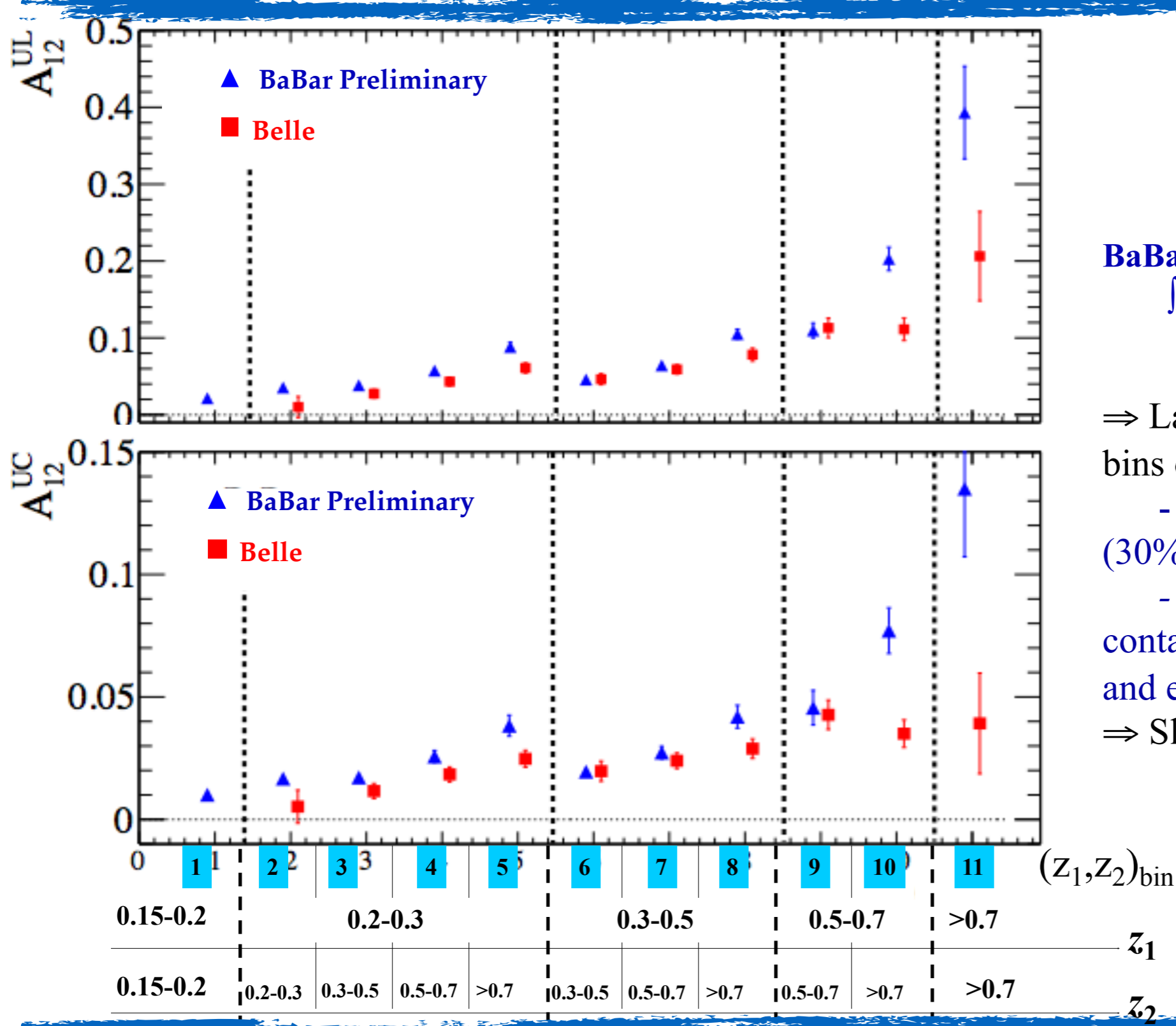
Results expected soon

Thanks for your attention



BK SLIDES

RF12: BaBar/Belle comparisons



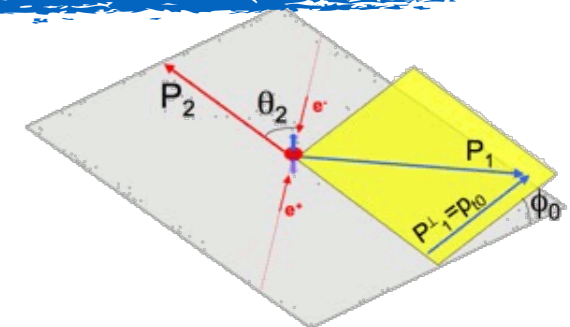
BaBar ($0.15 < z < 0.9$) $\int \mathcal{L} \sim 468 \text{ fb}^{-1}$
Belle ($0.2 < z < 1$) $\int \mathcal{L} \sim 547 \text{ fb}^{-1}$
 PRD 86, 039905(E) (2012)

\Rightarrow Large discrepancy in the last two bins of z :

- bin-by-bin correction factors (30%)
- $z < 0.9$ to remove the contamination from $\mu\mu\gamma$ background and exclusive events

\Rightarrow Slightly higher at lower z

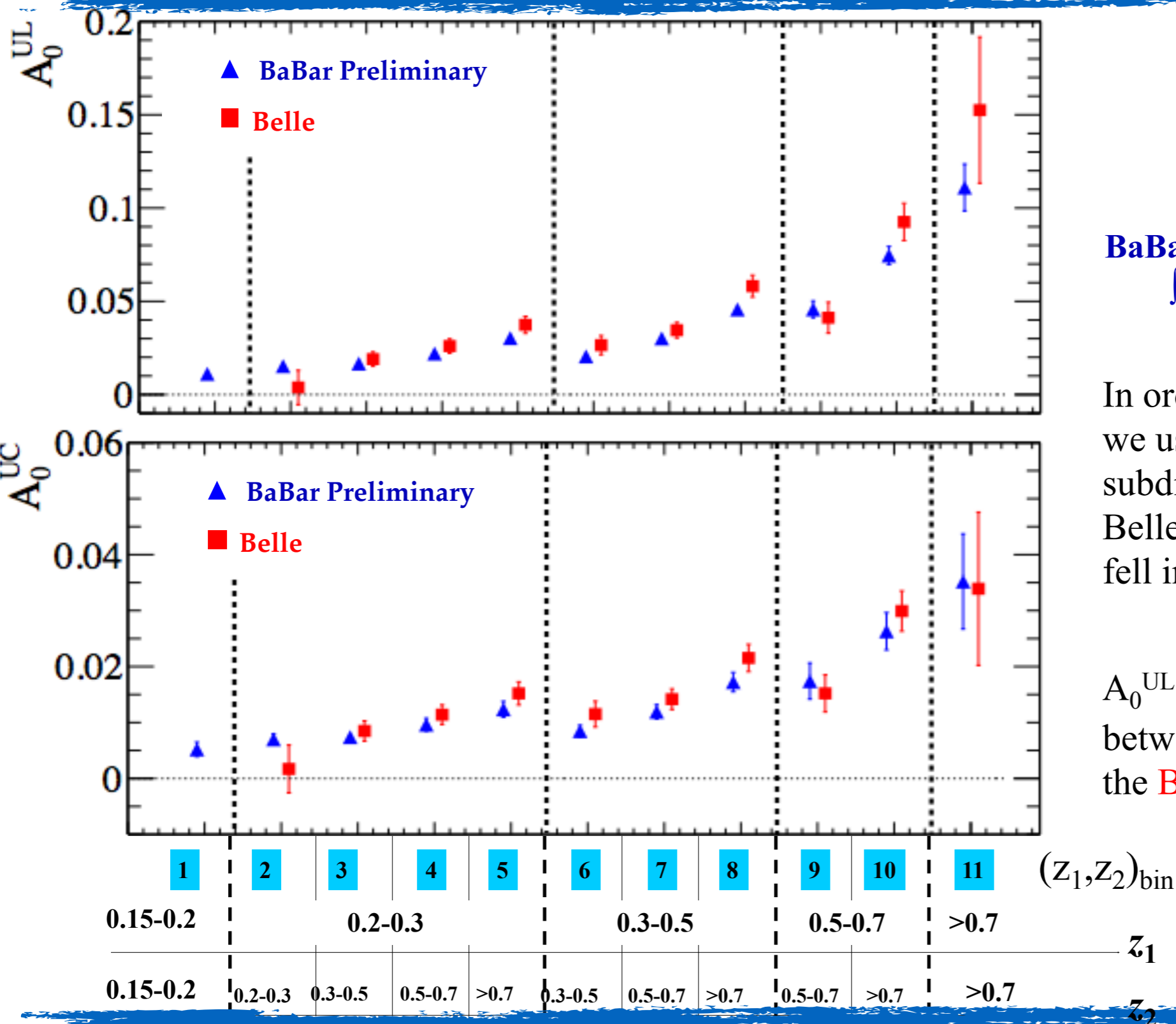
RF0: BaBar/Belle comparisons



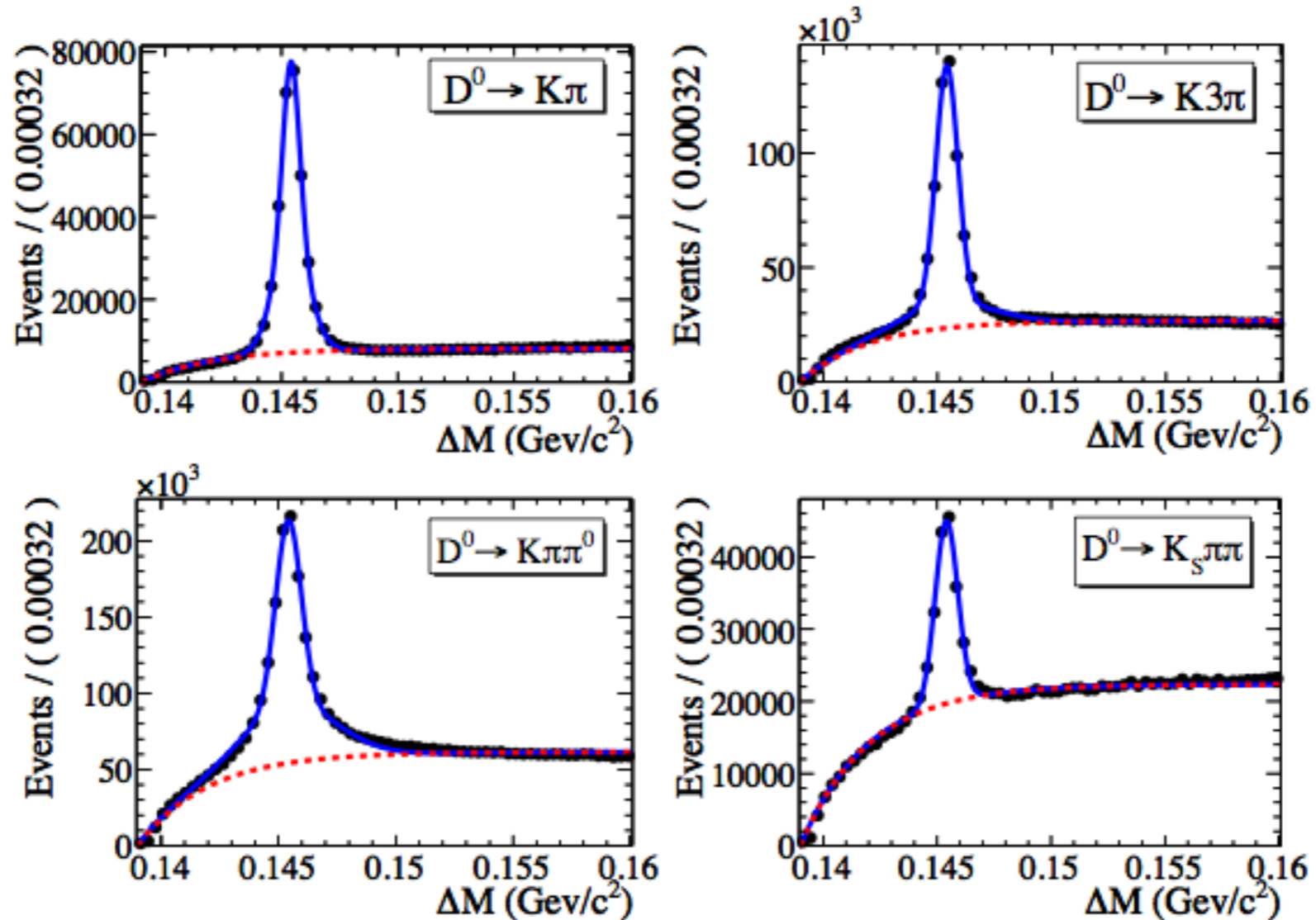
BaBar ($0.15 < z < 0.9$) **Belle ($0.2 < z < 1$)**
 $\int \mathcal{L} \sim 468 \text{ fb}^{-1}$ $\int \mathcal{L} \sim 547 \text{ fb}^{-1}$
 PRD 86, 039905(E) (2012)

In order to perform this comparison, we used 10 (+1) symmetrized z -bin subdivisions, averaging the measured Belle and BaBar asymmetries which fell in the same symmetric bins

A_0^{UL} and A_0^{UC} : good agreement between the **BaBar asymmetries** and the **Belle results**.



D*-enhanced control sample



$D^{*\pm} \rightarrow D^0\pi^\pm$, $D^0 \rightarrow K\pi$ (mode 1)
 $D^0 \rightarrow K3\pi$ (mode 2)
 $D^0 \rightarrow K\pi\pi^0$ (mode 3)
 $D^0 \rightarrow K_S\pi\pi$ (mode 4)

$1.835 < M_{D^0} < 1.895 \text{ GeV}/c^2$
 $0.1425 < \Delta M < 0.149 \text{ GeV}/c^2$
 $(\Delta M = M_{D^{*\pm}} - M_{D^0})$