



# New results on transverse spin asymmetries from COMPASS: Part I

UNIVERSITÀ  
DEGLI STUDI  
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TAURINENSIS



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on behalf of the COMPASS Collaboration



4th International Workshop on  
Transverse Polarisation Phenomena in  
Hard Processes (Transversity 2014)

Chia, Cagliari, Italy

June 9 - 13, 2014



# Outline

- **Introduction**
  - Brief review of COMPASS results with TSAs
- **COMPASS – “SIDIS-DY bridge”**
- **New results!**
  - Asymmetries
  - Re-evaluation of  $A_{LT}^{\cos\varphi_S}$  and  $A_{LT}^{\cos(\varphi_h - \varphi_s)}$ : from the  $l p$  to  $\gamma * p$  cross-section
  - $A_{LT}^{\cos(\varphi_h - \varphi_s)}$ : Comparison with predictions
  - Multi-D map of kinematical distributions
- **Conclusions**

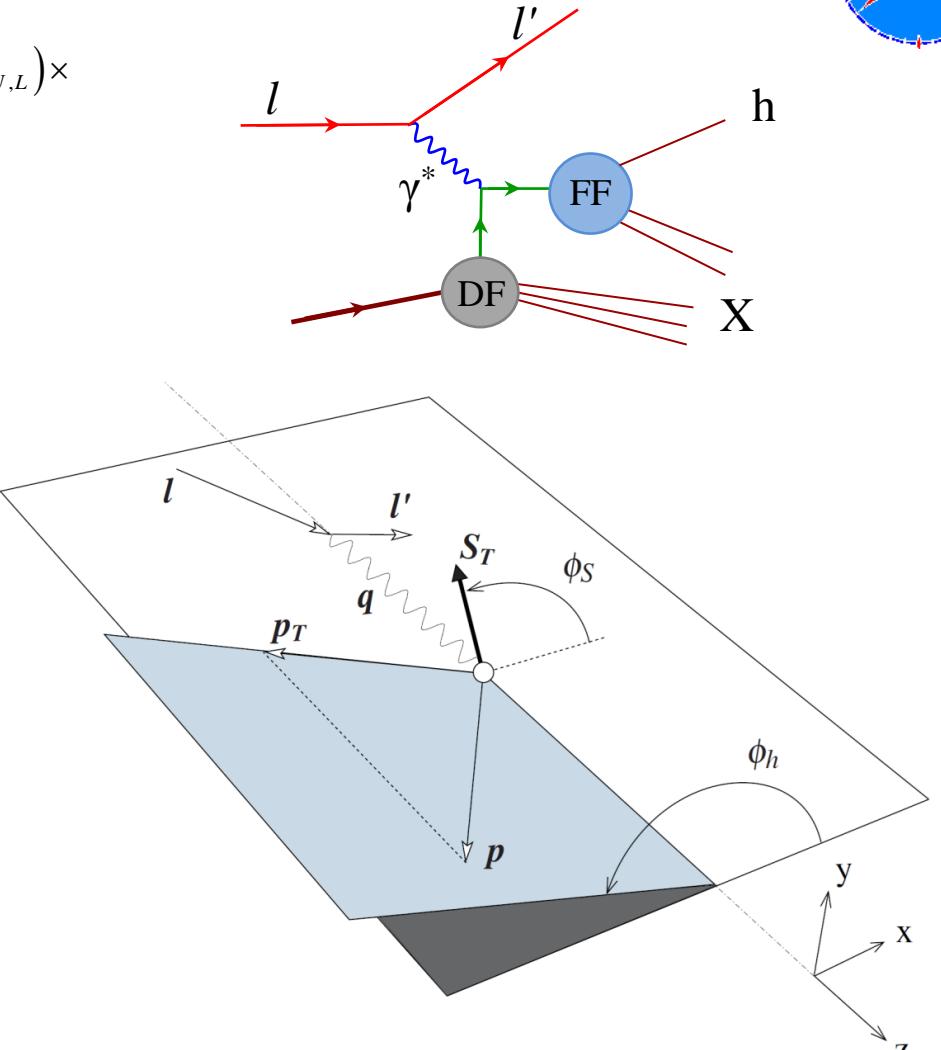
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# SIDIS x-section

$$\frac{d\sigma}{dxdydzdP_{hT}^2d\phi_h d\psi} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] \times (F_{UU,T} + \varepsilon F_{UU,L}) \times$$

$$\left\{ \begin{array}{l} 1 + \cos \varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\varphi_h)} + \\ \lambda \sin \varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \varphi_h} + \\ S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin \varphi_h A_{UL}^{\sin \varphi_h} + \varepsilon \sin(2\varphi_h) A_{UL}^{\sin(2\varphi_h)} \right] + \\ S_L \lambda \left[ \sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \varphi_h A_{LL}^{\cos \varphi_h} \right] + \\ \left[ \begin{array}{l} \sin(\varphi_h - \varphi_s) \times (A_{UT}^{\sin(\varphi_h - \varphi_s)}) + \\ \sin(\varphi_h + \varphi_s) \times (\varepsilon A_{UT}^{\sin(\varphi_h + \varphi_s)}) + \\ \sin(3\varphi_h - \varphi_s) \times (\varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_s)}) + \\ \sin \varphi_s \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \varphi_s}) + \\ \sin(2\varphi_h - \varphi_s) \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_s)}) + \\ \cos(\varphi_h - \varphi_s) \times (\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_s)}) + \\ \cos \varphi_s \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_s}) + \\ \cos(2\varphi_h - \varphi_s) \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_s)}) \end{array} \right] + \\ S_T \lambda \left[ \begin{array}{l} \cos(\varphi_h - \varphi_s) \times (\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_s)}) + \\ \cos \varphi_s \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_s}) + \\ \cos(2\varphi_h - \varphi_s) \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_s)}) \end{array} \right] \end{array} \right\}$$



$$A_{U(L),T}^{w(\varphi_h, \varphi_s)} = \frac{F_{U(L),T}^{w(\varphi_h, \varphi_s)}}{F_{UU,T} + \varepsilon F_{UU,L}};$$

$$\varepsilon = \frac{1 - y - \frac{1}{4}\gamma^2 y^2}{1 - y + \frac{1}{2}y^2 + \frac{1}{4}\gamma^2 y^2}, \quad \gamma = \frac{2Mx}{Q}$$

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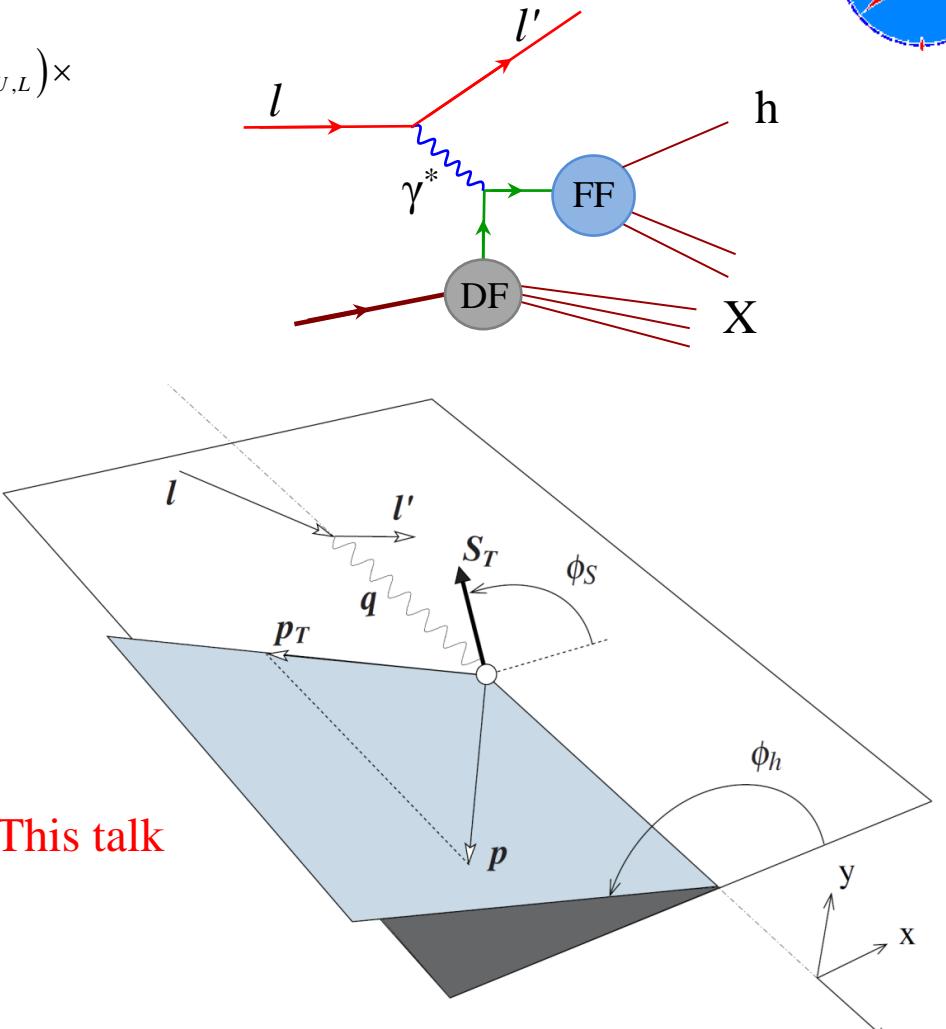
$$\left\{ 1 + \cos \varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\varphi_h)} + \right.$$

$$\lambda \sin \varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \varphi_h} +$$

$$S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin \varphi_h A_{UL}^{\sin \varphi_h} + \varepsilon \sin(2\varphi_h) A_{UL}^{\sin(2\varphi_h)} \right] +$$

$$S_L \lambda \left[ \sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \varphi_h A_{LL}^{\cos \varphi_h} \right] +$$

$$\left. \left[ \begin{array}{l} \sin(\varphi_h - \varphi_s) \times (A_{UT}^{\sin(\varphi_h - \varphi_s)}) \\ \sin(\varphi_h + \varphi_s) \times (\varepsilon A_{UT}^{\sin(\varphi_h + \varphi_s)}) \\ \sin(3\varphi_h - \varphi_s) \times (\varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_s)}) \\ \sin \varphi_s \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \varphi_s}) \\ \sin(2\varphi_h - \varphi_s) \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_s)}) \end{array} \right] + \right. \left. \left[ \begin{array}{l} \cos(\varphi_h - \varphi_s) \times (\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_s)}) \\ \cos \varphi_s \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_s}) \\ \cos(2\varphi_h - \varphi_s) \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_s)}) \end{array} \right] \right]$$



$$A_{U(L),T}^{w(\varphi_h, \varphi_s)} = \frac{F_{U(L),T}^{w(\varphi_h, \varphi_s)}}{F_{UU,T} + \varepsilon F_{UU,L}};$$

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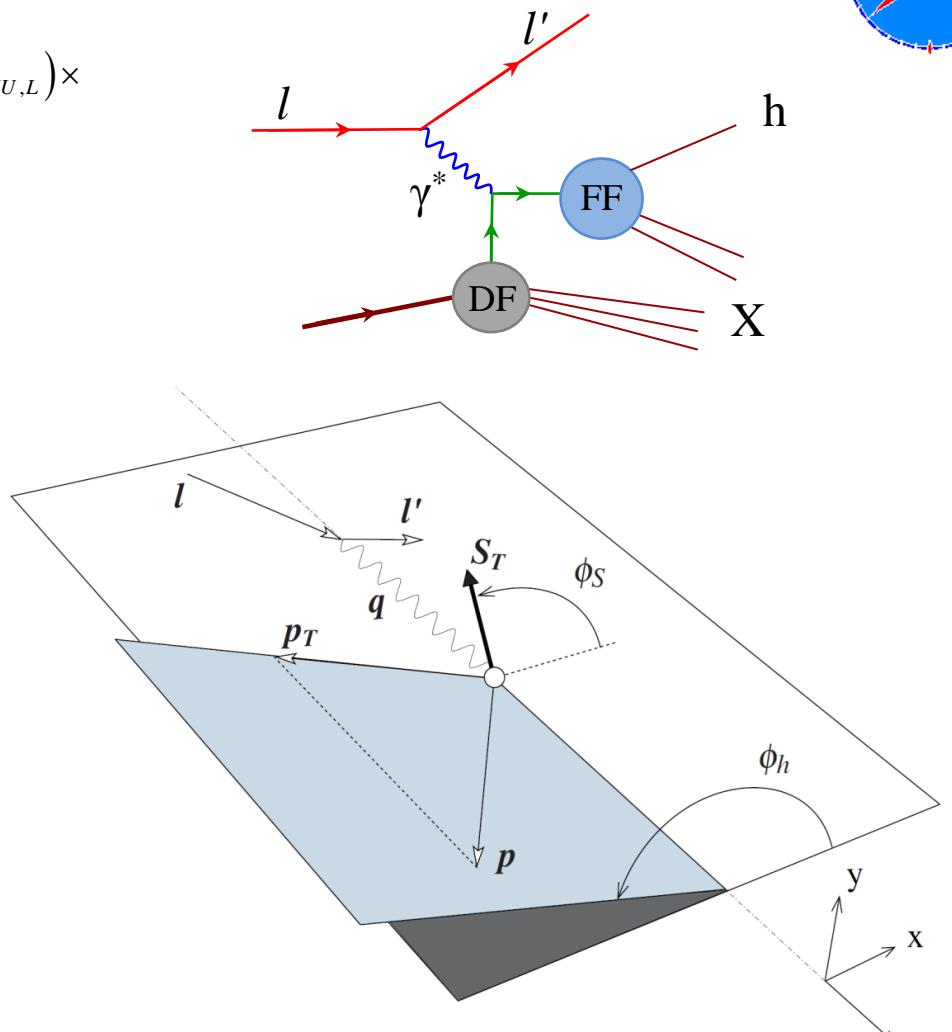
$$\left\{ 1 + \cos \varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\varphi_h)} + \right. \\ \lambda \sin \varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \varphi_h} + \\ S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin \varphi_h A_{UL}^{\sin \varphi_h} + \varepsilon \sin(2\varphi_h) A_{UL}^{\sin(2\varphi_h)} \right] + \\ S_L \lambda \left[ \sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \varphi_h A_{LL}^{\cos \varphi_h} \right] +$$

$$\left. \begin{array}{l} \sin(\varphi_h - \varphi_s) \times (A_{UT}^{\sin(\varphi_h - \varphi_s)}) + \\ \sin(\varphi_h + \varphi_s) \times (\varepsilon A_{UT}^{\sin(\varphi_h + \varphi_s)}) + \\ \sin(3\varphi_h - \varphi_s) \times (\varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_s)}) + \\ \sin \varphi_s \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \varphi_s}) + \\ \sin(2\varphi_h - \varphi_s) \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_s)}) + \end{array} \right] +$$

SSA 

$$\left. \begin{array}{l} \cos(\varphi_h - \varphi_s) \times (\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_s)}) + \\ \cos \varphi_s \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_s}) + \\ \cos(2\varphi_h - \varphi_s) \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_s)}) \end{array} \right]$$

DSA 



$$A_{U(L),T}^{w(\varphi_h, \varphi_s)} = \frac{F_{U(L),T}^{w(\varphi_h, \varphi_s)}}{F_{UU,T} + \varepsilon F_{UU,L}};$$

$$\varepsilon = \frac{1 - y - \frac{1}{4}\gamma^2 y^2}{1 - y + \frac{1}{2}y^2 + \frac{1}{4}\gamma^2 y^2}, \quad \gamma = \frac{2Mx}{Q}$$

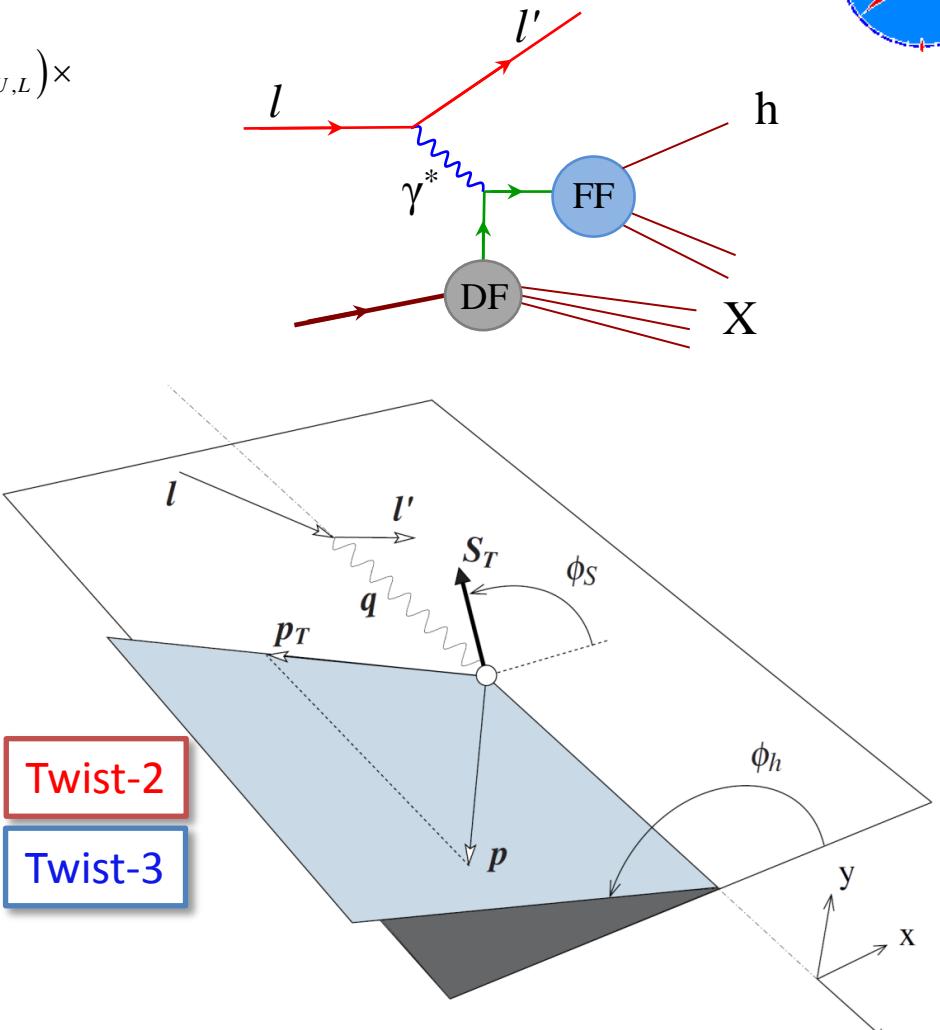
# SIDIS x-section

$$\frac{d\sigma}{dxdydzdP_{hT}^2 d\phi_h d\psi} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] \times (F_{UU,T} + \varepsilon F_{UU,L}) \times$$

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$$\left. \begin{aligned} & \left[ \begin{aligned} & \sin(\varphi_h - \varphi_S) \times (A_{UT}^{\sin(\varphi_h - \varphi_S)}) \\ & \sin(\varphi_h + \varphi_S) \times (\varepsilon A_{UT}^{\sin(\varphi_h + \varphi_S)}) \\ & \sin(3\varphi_h - \varphi_S) \times (\varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_S)}) \\ & \sin \varphi_S \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \varphi_S}) \\ & \sin(2\varphi_h - \varphi_S) \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_S)}) \end{aligned} \right] + \\ & S_T \left[ \begin{aligned} & \cos(\varphi_h - \varphi_S) \times (\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_S)}) \\ & \cos \varphi_S \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_S}) \\ & \cos(2\varphi_h - \varphi_S) \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_S)}) \end{aligned} \right] \end{aligned} \right]$$

+ SSA DSA



$$A_{U(L),T}^{w(\varphi_h, \varphi_s)} = \frac{F_{U(L),T}^{w(\varphi_h, \varphi_s)}}{F_{UU,T} + \varepsilon F_{UU,L}};$$

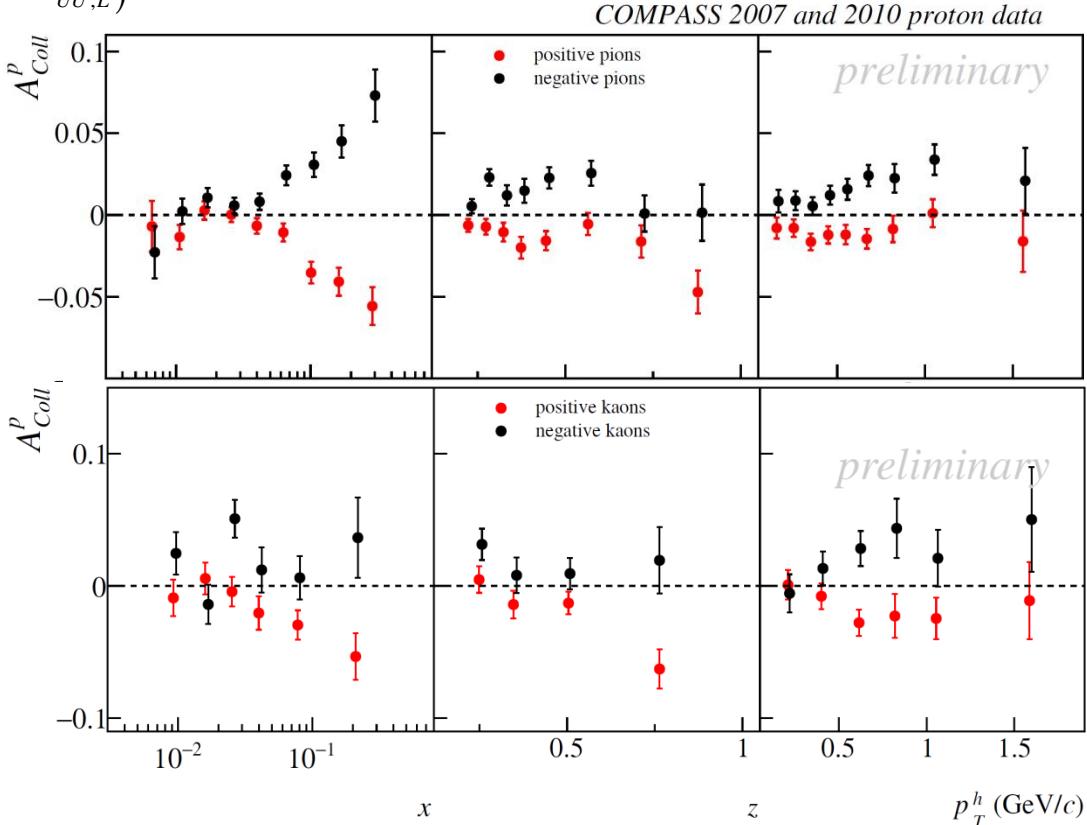
$$\varepsilon = \frac{1 - y - \frac{1}{4}\gamma^2 y^2}{1 - y + \frac{1}{2}y^2 + \frac{1}{4}\gamma^2 y^2}, \quad \gamma = \frac{2Mx}{Q}$$

# SIDIS x-section

$$A_{UT}^{\sin(\phi_h + \phi_s)} \propto h_1^q \otimes H_{1q}^{\perp h} \quad \text{SSA [twist-2]}$$



$$\frac{d\sigma}{dxdydzdP_{hT}^2 d\phi_h d\psi} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] \times \left( F_{UU,T} + \varepsilon F_{UU,L} \right) \times \\ \left\{ 1 + \cos \phi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \phi_h} + \cos(2\phi_h) \times \varepsilon A_{UU}^{\cos(2\phi_h)} + \right. \\ \lambda \sin \phi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \phi_h} + \\ S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_h A_{UL}^{\sin \phi_h} + \varepsilon \sin(2\phi_h) A_{UL}^{\sin(2\phi_h)} \right] + \\ S_L \lambda \left[ \sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_h A_{LL}^{\cos \phi_h} \right] + \\ \left. \left[ \sin(\phi_h - \phi_s) \times \left( A_{UT}^{\sin(\phi_h - \phi_s)} \right) + \right. \right. \\ \boxed{\sin(\phi_h + \phi_s) \times \left( \varepsilon A_{UT}^{\sin(\phi_h + \phi_s)} \right)} + \\ S_T \sin(3\phi_h - \phi_s) \times \left( \varepsilon A_{UT}^{\sin(3\phi_h - \phi_s)} \right) + \\ \sin \phi_s \times \left( \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \phi_s} \right) + \\ \sin(2\phi_h - \phi_s) \times \left( \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\phi_h - \phi_s)} \right) + \\ \left. \left[ \cos(\phi_h - \phi_s) \times \left( \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h - \phi_s)} \right) + \right. \right. \\ S_T \lambda \cos \phi_s \times \left( \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \phi_s} \right) + \\ \left. \left. \cos(2\phi_h - \phi_s) \times \left( \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\phi_h - \phi_s)} \right) \right] \right\}$$

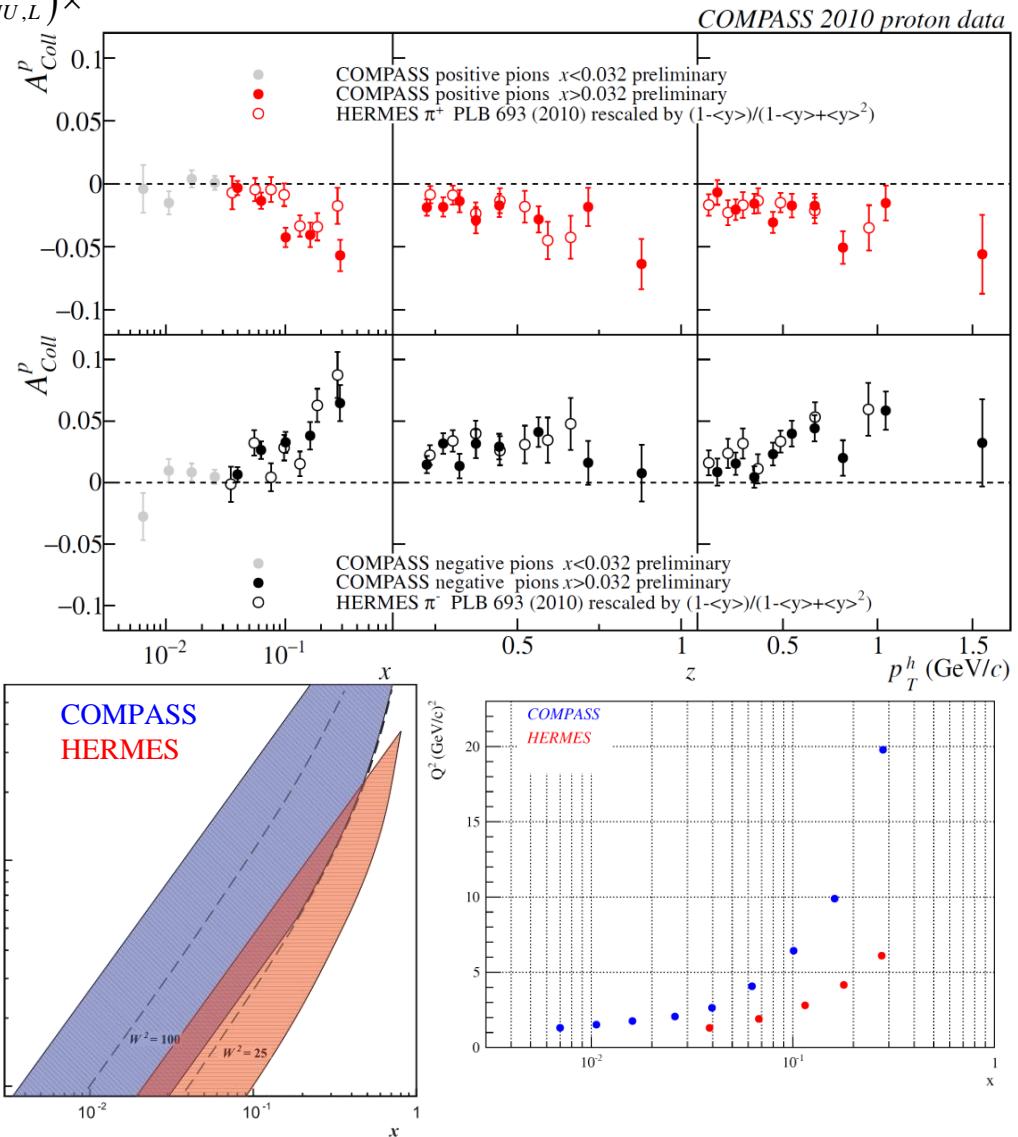


- Asymmetries are compatible with zero at small  $x$
- Strong signal in the valence region of opposite sign for  $\pi^+$  and  $\pi^-$
- Opposite sign also for  $K^+/K^-$  negative trend in the valence region
- Compatible with zero on deuteron

# SIDIS x-section

$$A_{UT}^{\sin(\phi_h + \phi_s)} \propto h_1^q \otimes H_{1q}^{\perp h} \quad \text{SSA [twist-2]}$$

$$\frac{d\sigma}{dxdydzdP_{hT}^2 d\phi_h d\psi} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] \times \left( F_{UU,T} + \varepsilon F_{UU,L} \right) \times \left\{ \begin{array}{l} 1 + \cos \varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\varphi_h)} + \\ \lambda \sin \varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \varphi_h} + \\ S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin \varphi_h A_{UL}^{\sin \varphi_h} + \varepsilon \sin(2\varphi_h) A_{UL}^{\sin(2\varphi_h)} \right] + \\ S_L \lambda \left[ \sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \varphi_h A_{LL}^{\cos \varphi_h} \right] + \\ \left[ \sin(\varphi_h - \varphi_s) \times \left( A_{UT}^{\sin(\varphi_h - \varphi_s)} \right) + \right. \\ \boxed{\sin(\varphi_h + \varphi_s) \times \left( \varepsilon A_{UT}^{\sin(\varphi_h + \varphi_s)} \right)} + \\ \sin(3\varphi_h - \varphi_s) \times \left( \varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_s)} \right) + \\ \sin \varphi_s \times \left( \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \varphi_s} \right) + \\ \sin(2\varphi_h - \varphi_s) \times \left( \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_s)} \right) + \\ \left. \cos(\varphi_h - \varphi_s) \times \left( \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_s)} \right) + \right. \\ S_T \lambda \left[ \cos \varphi_s \times \left( \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_s} \right) + \right. \\ \left. \left. \cos(2\varphi_h - \varphi_s) \times \left( \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_s)} \right) \right] \right\}$$



- COMPASS and HERMES results are compatible - intriguing result! ( $Q^2$  is different by a factor of ~2-3)

# SIDIS x-section

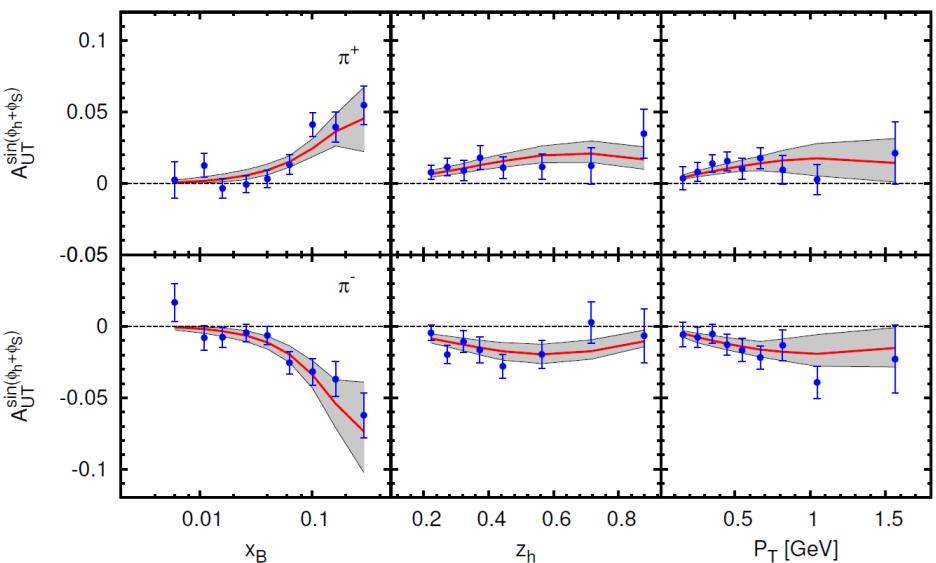
$$A_{UT}^{\sin(\phi_h + \phi_s)} \propto h_1^q \otimes H_{1q}^{\perp h} \quad \text{SSA [twist-2]}$$



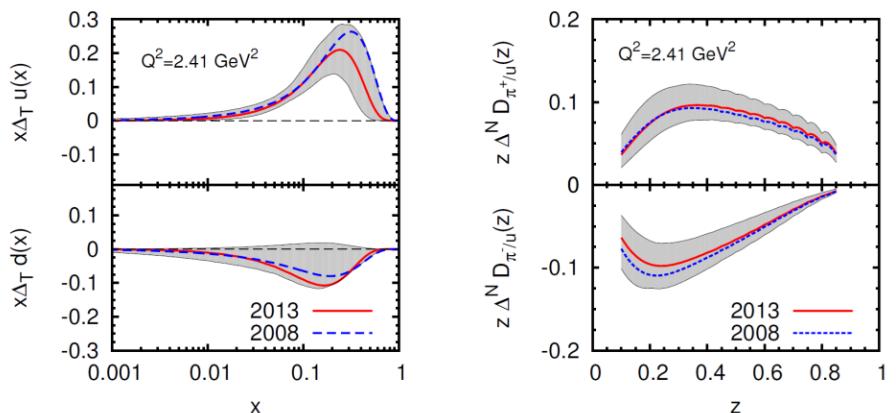
$$\frac{d\sigma}{dxdydzdP_{hT}^2 d\varphi_h d\psi} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] \times \left( F_{UU,T} + \varepsilon F_{UU,L} \right) \times \left\{ \begin{array}{l} 1 + \cos \varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\varphi_h)} + \\ \lambda \sin \varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \varphi_h} + \\ S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin \varphi_h A_{UL}^{\sin \varphi_h} + \varepsilon \sin(2\varphi_h) A_{UL}^{\sin(2\varphi_h)} \right] + \\ S_L \lambda \left[ \sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \varphi_h A_{LL}^{\cos \varphi_h} \right] + \\ \left[ \sin(\varphi_h - \varphi_s) \times \left( A_{UT}^{\sin(\varphi_h - \varphi_s)} \right) + \right. \\ \boxed{\sin(\varphi_h + \varphi_s) \times \left( \varepsilon A_{UT}^{\sin(\varphi_h + \varphi_s)} \right)} + \\ \sin(3\varphi_h - \varphi_s) \times \left( \varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_s)} \right) + \\ \sin \varphi_s \times \left( \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \varphi_s} \right) + \\ \sin(2\varphi_h - \varphi_s) \times \left( \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_s)} \right) + \\ \left. \cos(\varphi_h - \varphi_s) \times \left( \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_s)} \right) + \right. \\ S_T \lambda \left[ \cos \varphi_s \times \left( \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_s} \right) + \right. \\ \left. \cos(2\varphi_h - \varphi_s) \times \left( \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_s)} \right) \right] \end{array} \right\}$$

Phys.Rev. D87 (2013) 094019

COMPASS PROTON



- Global fit of HERMES-COMPASS-BELLE data



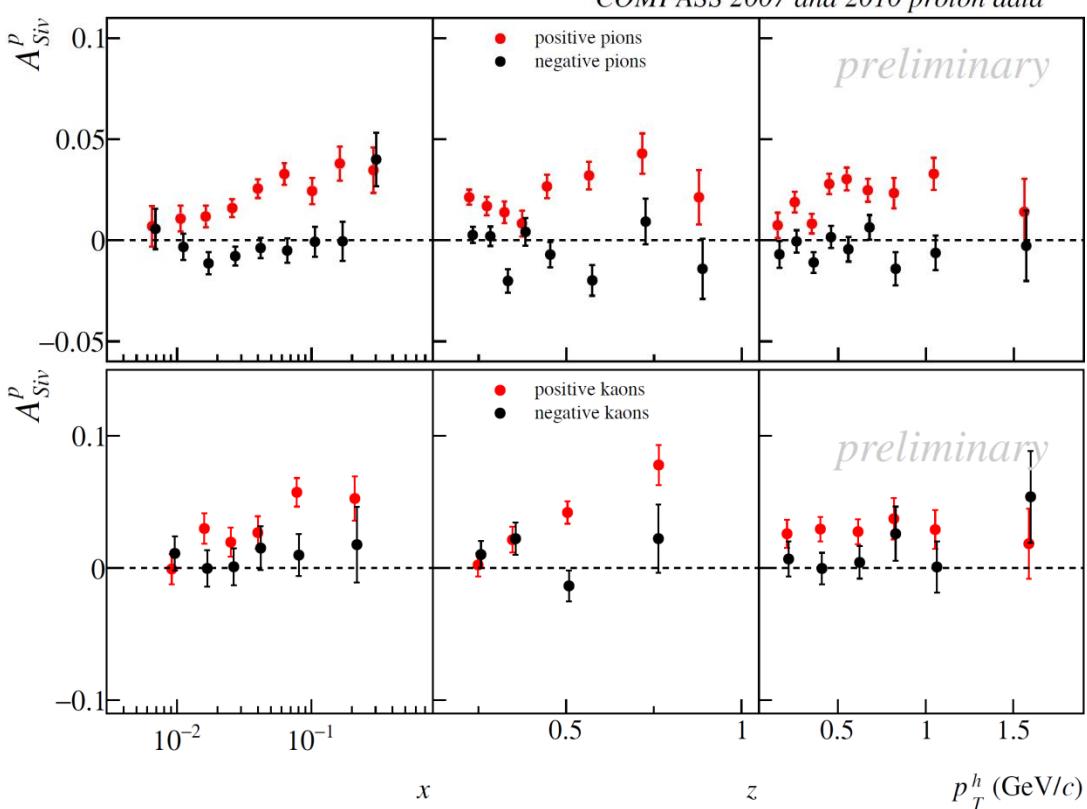
- Transversity PDF + Collins FF

# SIDIS x-section

$$A_{UT}^{\sin(\phi_h - \phi_s)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h \quad \text{SSA [twist-2]}$$



$$\frac{d\sigma}{dxdydzdP_{hT}^2 d\phi_h d\psi} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] \times \left( F_{UU,T} + \varepsilon F_{UU,L} \right) \times \\ \left\{ 1 + \cos \phi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \phi_h} + \cos(2\phi_h) \times \varepsilon A_{UU}^{\cos(2\phi_h)} + \right. \\ \lambda \sin \phi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \phi_h} + \\ S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_h A_{UL}^{\sin \phi_h} + \varepsilon \sin(2\phi_h) A_{UL}^{\sin(2\phi_h)} \right] + \\ S_L \lambda \left[ \sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_h A_{LL}^{\cos \phi_h} \right] + \\ \left. \left[ \begin{array}{l} \sin(\phi_h - \phi_s) \times \left( A_{UT}^{\sin(\phi_h - \phi_s)} \right) + \\ \sin(\phi_h + \phi_s) \times \left( \varepsilon A_{UT}^{\sin(\phi_h + \phi_s)} \right) + \\ \sin(3\phi_h - \phi_s) \times \left( \varepsilon A_{UT}^{\sin(3\phi_h - \phi_s)} \right) + \\ \sin \phi_s \times \left( \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \phi_s} \right) + \\ \sin(2\phi_h - \phi_s) \times \left( \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\phi_h - \phi_s)} \right) + \\ \cos(\phi_h - \phi_s) \times \left( \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h - \phi_s)} \right) + \\ S_T \lambda \left[ \cos \phi_s \times \left( \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \phi_s} \right) + \right. \\ \left. \cos(2\phi_h - \phi_s) \times \left( \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\phi_h - \phi_s)} \right) \right] \end{array} \right]$$



- Significantly large amplitude for  $\pi^+$  and  $K^+$  in whole range of  $x$
- Compatible with zero for  $\pi^-$  and  $K^-$ 
  - (maybe except the last bin of  $x$  for  $\pi^-$ ).
- Compatible with zero on deuteron

# SIDIS x-section

$$A_{UT}^{\sin(\phi_h - \phi_s)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h \quad \text{SSA [twist-2]}$$

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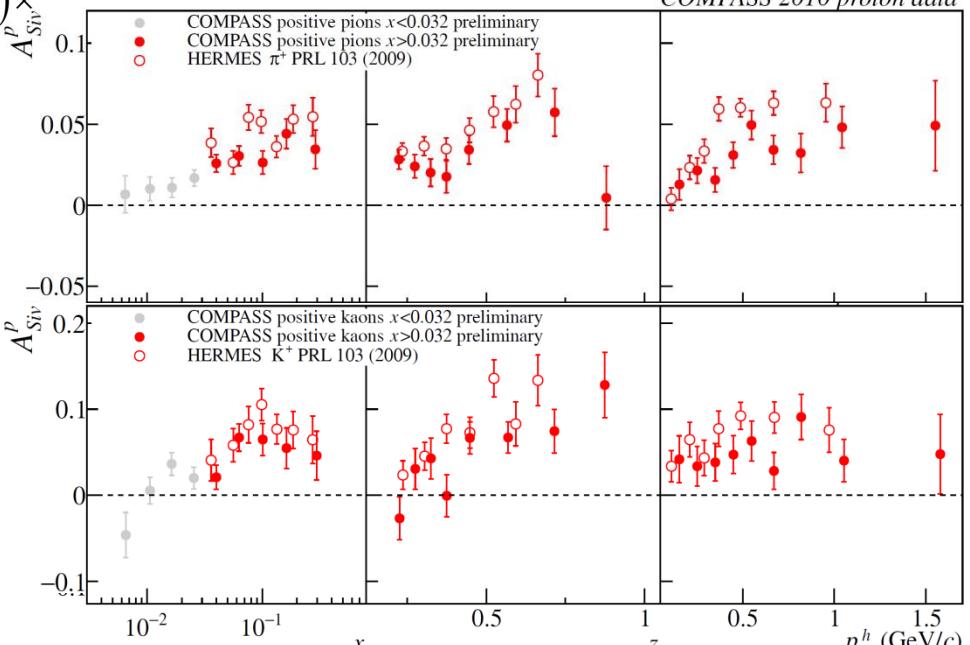
$$\left\{ 1 + \cos \varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\varphi_h)} + \right.$$

$$\lambda \sin \varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \varphi_h} +$$

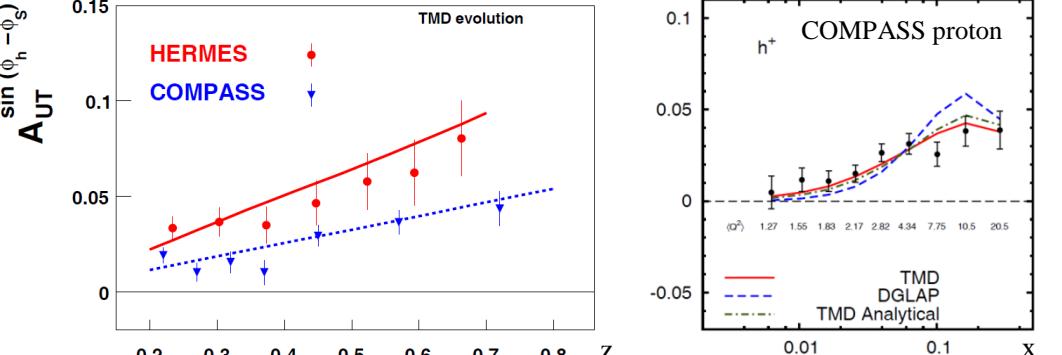
$$S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin \varphi_h A_{UL}^{\sin \varphi_h} + \varepsilon \sin(2\varphi_h) A_{UL}^{\sin(2\varphi_h)} \right] +$$

$$S_L \lambda \left[ \sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \varphi_h A_{LL}^{\cos \varphi_h} \right] +$$

$$\left. \begin{aligned} & \boxed{\sin(\varphi_h - \varphi_s) \times (A_{UT}^{\sin(\varphi_h - \varphi_s)})} + \\ & \sin(\varphi_h + \varphi_s) \times (\varepsilon A_{UT}^{\sin(\varphi_h + \varphi_s)}) + \\ S_T & \sin(3\varphi_h - \varphi_s) \times (\varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_s)}) + \\ & \sin \varphi_s \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \varphi_s}) + \\ & \sin(2\varphi_h - \varphi_s) \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_s)}) + \\ & \cos(\varphi_h - \varphi_s) \times (\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_s)}) + \\ S_T \lambda & \cos \varphi_s \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_s}) + \\ & \cos(2\varphi_h - \varphi_s) \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_s)}) \end{aligned} \right]$$



- Sivers effect at COMPASS is slightly smaller w.r.t HERMES results... Q<sup>2</sup>-evolution?



S. M. Aybat, A. Prokudin, T. C. Rogers **PRL 108 (2012) 242003**

M. Anselmino, M. Boglione, S. Melis **PRD 86 (2012) 014028**

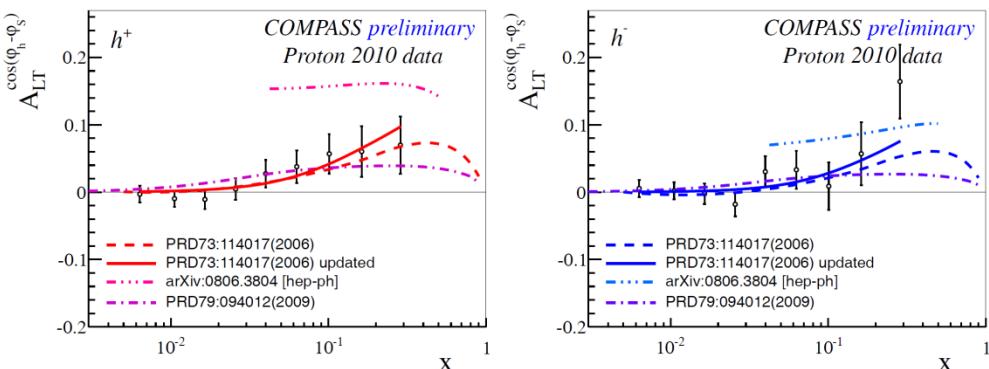
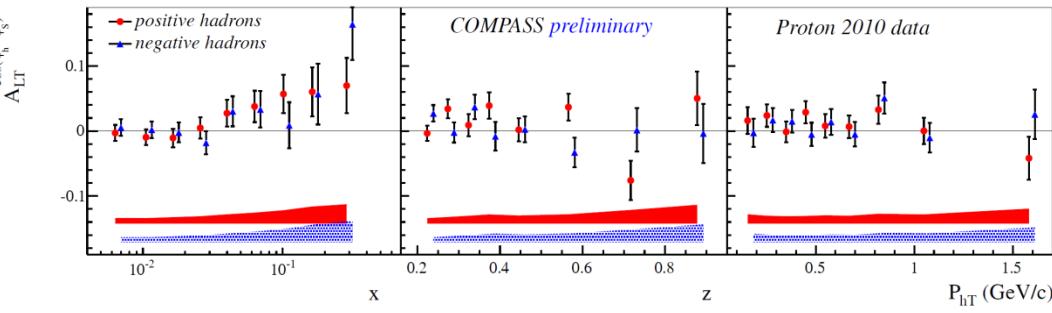
Bakur Parsamyan

# SIDIS x-section

$$A_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h \quad \text{DSA [twist-2]}$$

$$\frac{d\sigma}{dxdydzdP_{hT}^2 d\phi_h d\psi} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] \times (F_{UU,T} + \varepsilon F_{UU,L}) \times$$

$$\begin{aligned} & 1 + \cos \varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\varphi_h)} + \\ & \lambda \sin \varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \varphi_h} + \\ & S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin \varphi_h A_{UL}^{\sin \varphi_h} + \varepsilon \sin(2\varphi_h) A_{UL}^{\sin(2\varphi_h)} \right] + \\ & S_L \lambda \left[ \sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \varphi_h A_{LL}^{\cos \varphi_h} \right] + \\ & \left. \left[ \begin{aligned} & \sin(\varphi_h - \varphi_s) \times (A_{UT}^{\sin(\varphi_h - \varphi_s)}) + \\ & \sin(\varphi_h + \varphi_s) \times (\varepsilon A_{UT}^{\sin(\varphi_h + \varphi_s)}) + \\ & \sin(3\varphi_h - \varphi_s) \times (\varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_s)}) + \\ & \sin \varphi_s \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \varphi_s}) + \\ & \sin(2\varphi_h - \varphi_s) \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_s)}) + \\ & \cos(\varphi_h - \varphi_s) \times (\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_s)}) + \\ & \cos \varphi_s \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_s}) + \\ & \cos(2\varphi_h - \varphi_s) \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_s)}) \end{aligned} \right] \right]$$

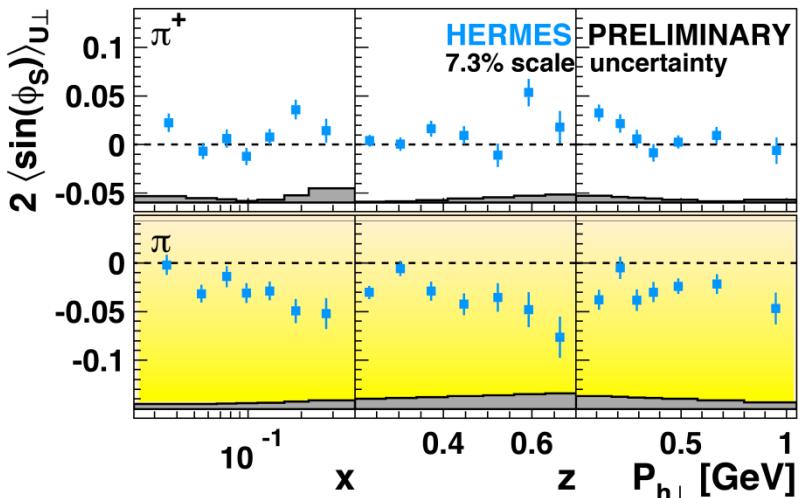
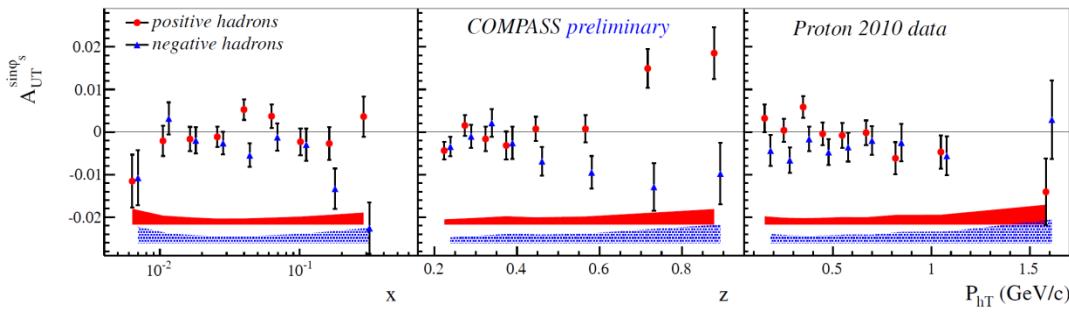


- Gives access to  $g_{1T}$  “twist-2” PDF (worm-gear-T)
- Visible signal for  $h^+$  (*preliminary* confirmation also by HERMES)
- In agreement with several model predictions
- Compatible with zero on deuteron

$$A_{UT}^{\sin(\phi_s)} \stackrel{WW}{\propto} Q^{-1} \left( h_q^q \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right) \quad \text{SSA [higher-twist]}$$

$$\frac{d\sigma}{dx dy dz dP_{hT}^2 d\phi_h d\psi} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] \times (F_{UU,T} + \varepsilon F_{UU,L}) \times$$

$$\begin{aligned}
& 1 + \cos \varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\varphi_h)} + \\
& \lambda \sin \varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \varphi_h} + \\
& S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin \varphi_h A_{UL}^{\sin \varphi_h} + \varepsilon \sin(2\varphi_h) A_{UL}^{\sin(2\varphi_h)} \right] + \\
& S_L \lambda \left[ \sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \varphi_h A_{LL}^{\cos \varphi_h} \right] + \\
& \left. \left[ \begin{aligned} & \sin(\varphi_h - \varphi_S) \times (A_{UT}^{\sin(\varphi_h - \varphi_S)}) + \\
& \sin(\varphi_h + \varphi_S) \times (\varepsilon A_{UT}^{\sin(\varphi_h + \varphi_S)}) + \\
& \sin(3\varphi_h - \varphi_S) \times (\varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_S)}) + \\
& \sin \varphi_S \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \varphi_S}) + \\
& \sin(2\varphi_h - \varphi_S) \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_S)}) + \end{aligned} \right] \right\} + \\
& S_T \lambda \left[ \begin{aligned} & \cos(\varphi_h - \varphi_S) \times (\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_S)}) + \\
& \cos \varphi_S \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_S}) + \\
& \cos(2\varphi_h - \varphi_S) \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_S)}) \end{aligned} \right]
\end{aligned}$$



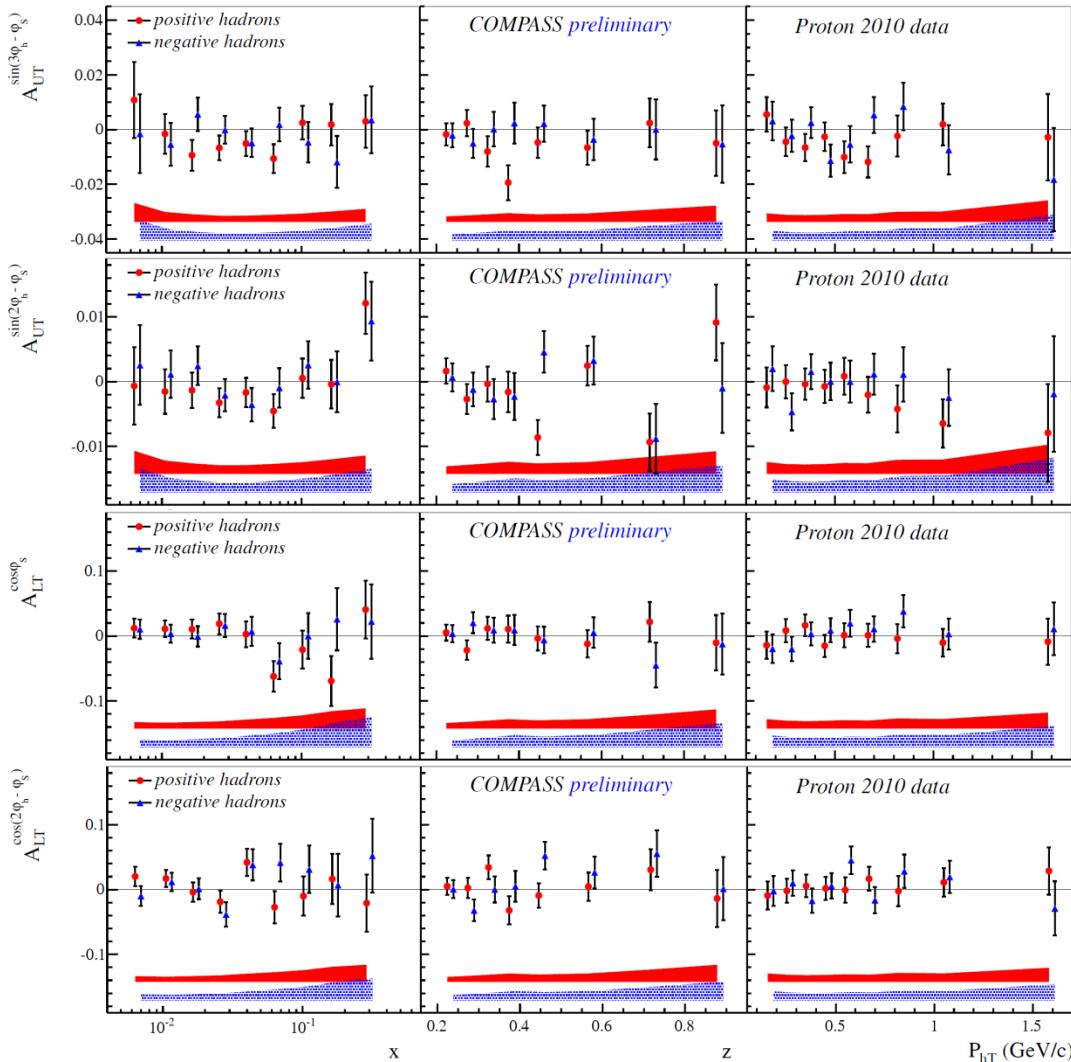
- Higher twist effect..
- In WW-approximation is related to Sivers and Collins
- Non-zero trend for negative hadrons both in COMPASS and HERMES
- Compatible with zero on deuteron

$$A_{UT}^{\sin(3\phi_h - \phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h} \text{ SSA [twist-2]; } A_{UT}^{\sin(2\phi_h - \phi_s)} \overset{\text{WW}}{\propto} Q^{-1} \left( h_{1T}^{\perp q} \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right) \text{ SSA [higher-twist]}$$

$$A_{LT}^{\cos(\phi_s)} \overset{\text{WW}}{\propto} Q^{-1} \left( g_{1T}^q \otimes D_{1q}^h + \dots \right) \text{ DSA [higher-twist]; } A_{LT}^{\cos(2\phi_h - \phi_s)} \overset{\text{WW}}{\propto} Q^{-1} \left( g_{1T}^q \otimes D_{1q}^h + \dots \right) \text{ DSA [higher-twist]}$$

$$\frac{d\sigma}{dx dy dz dP_{hT}^2 d\phi_h d\psi} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] \times (F_{UU,T} + \varepsilon F_{UU,L}) \times$$

$$\left. \begin{aligned} & 1 + \cos \varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\phi_h)} + \\ & \lambda \sin \varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \varphi_h} + \\ & S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin \varphi_h A_{UL}^{\sin \varphi_h} + \varepsilon \sin(2\varphi_h) A_{UL}^{\sin(2\phi_h)} \right] + \\ & S_L \lambda \left[ \sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \varphi_h A_{LL}^{\cos \varphi_h} \right] + \\ & \left. \begin{aligned} & \sin(\varphi_h - \varphi_s) \times (A_{UT}^{\sin(\varphi_h - \varphi_s)}) + \\ & \sin(\varphi_h + \varphi_s) \times (\varepsilon A_{UT}^{\sin(\varphi_h + \varphi_s)}) + \\ & S_T \left[ \sin(3\varphi_h - \varphi_s) \times (\varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_s)}) + \right. \\ & \left. \sin \varphi_s \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \varphi_s}) + \right. \\ & \left. \left. \sin(2\varphi_h - \varphi_s) \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_s)}) \right] + \right. \\ & \left. \begin{aligned} & \cos(\varphi_h - \varphi_s) \times (\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_s)}) + \\ & \cos \varphi_s \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_s}) + \\ & S_T \lambda \left[ \cos(2\varphi_h - \varphi_s) \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_s)}) \right] \right] \end{aligned} \right]$$



- All compatible with zero within uncertainties (P/D)

# Outline

- Introduction
  - Brief review of COMPASS results with TSAs
- **COMPASS – “SIDIS-DY bridge”**
- New results!
  - Asymmetries
  - Re-evaluation of  $A_{LT}^{\cos\varphi_S}$  and  $A_{LT}^{\cos(\varphi_h - \varphi_S)}$ :  
from the  $l p$  to  $\gamma * p$  cross-section
  - $A_{LT}^{\cos(\varphi_h - \varphi_S)}$ : Comparison with predictions
  - Multi-D map of kinematical distributions
- Conclusions

# SIDIS x-section

$$\frac{d\sigma}{dxdydzdP_{ht}^2 d\varphi_h dy} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] \times (F_{UU,T} + \varepsilon F_{UU,L}) \times$$

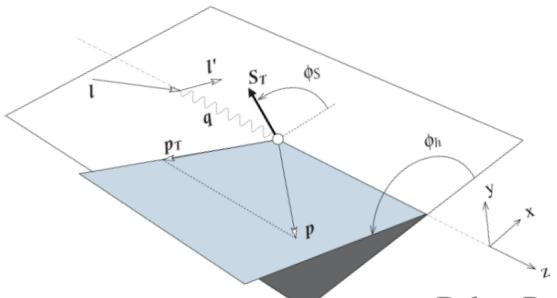
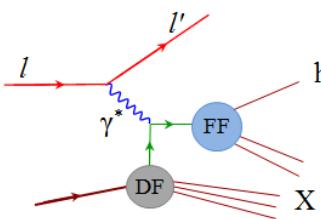
$$1 + \cos \varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\varphi_h)} +$$

$$\lambda \sin \varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \varphi_h} +$$

$$S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_h A_{UL}^{\sin \phi_h} + \varepsilon \sin(2\phi_h) A_{UL}^{\sin(2\phi_h)} \right] +$$

$$S_L \lambda \left[ \sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_h A_{LL}^{\cos \phi_h} \right] +$$

$$S_T \left[ \begin{array}{l} \sin(\varphi_h - \varphi_s) \times (A_{UT}^{\sin(\varphi_h - \varphi_s)}) + \\ \sin(\varphi_h + \varphi_s) \times (\varepsilon A_{UT}^{\sin(\varphi_h + \varphi_s)}) + \\ \sin(3\varphi_h - \varphi_s) \times (\varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_s)}) + \\ \sin \varphi_s \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \varphi_s}) + \\ \sin(2\varphi_h - \varphi_s) \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_s)}) + \\ \cos(\varphi_h - \varphi_s) \times (\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_s)}) + \\ \cos \varphi_s \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_s}) + \\ \cos(2\varphi_h - \varphi_s) \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_s)}) \end{array} \right]$$

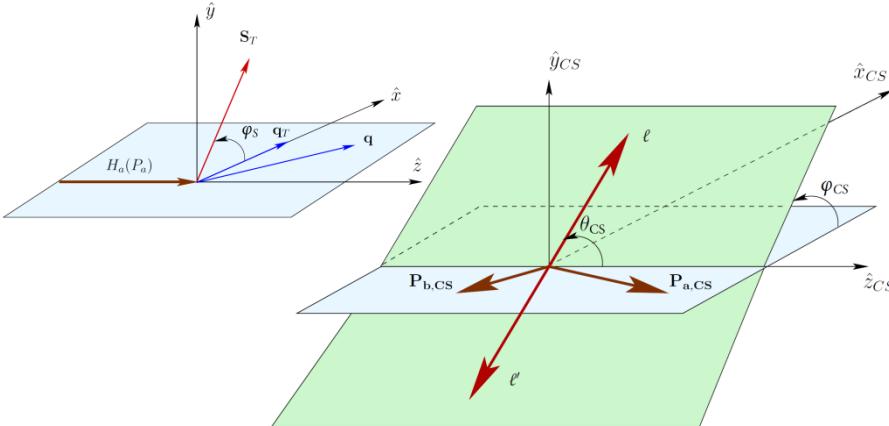
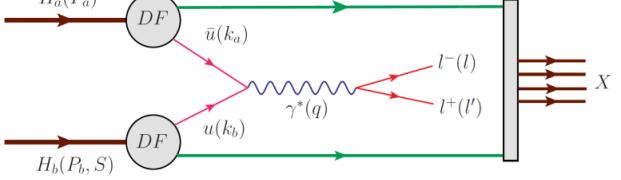


# DY x-section

## LO single polarized

$$\frac{d\sigma^{LO}}{d\Omega} = \frac{\alpha_{em}^2}{Fq^2} F_U^1 \times$$

$$\left. \begin{aligned} & 1 + \cos^2 \theta + \sin^2 \theta A_U^{\cos 2\varphi} \cos 2\varphi \\ & + S_L \sin^2 \theta A_L^{\sin 2\varphi} \sin 2\varphi \\ & \pm \left| \vec{S}_T \right| \left[ \begin{array}{l} (1 + \cos^2 \theta) A_T^{\sin \varphi_S} \sin \varphi_S + \\ \sin^2 \theta \left( A_T^{\sin(2\varphi_{CS} + \varphi_S)} \sin(2\varphi + \varphi_S) + A_T^{\sin(2\varphi_{CS} - \varphi_S)} \sin(2\varphi - \varphi_S) \right) \end{array} \right] \end{aligned} \right\}$$





# TMDs accessed in SIDIS and DY

SIDIS

$$A_{UU}^{\cos\phi_h} \propto Q^{-1} \left( f_1^q \otimes D_{1q}^h - h_1^{\perp q} \otimes H_{1q}^{\perp h} + \dots \right)$$

$$A_{UU}^{\cos 2\phi_h} \propto h_1^{\perp q} \otimes H_{1q}^{\perp h} + Q^{-1} \left( f_1^q \otimes D_{1q}^h + \dots \right)$$

$$A_{UT}^{\sin(\phi_h - \phi_s)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h$$

$$A_{UT}^{\sin(\phi_h + \phi_s)} \propto h_1^q \otimes H_{1q}^{\perp h}$$

$$A_{UT}^{\sin(3\phi_h - \phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$$

$$A_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h$$

$$A_{UT}^{\sin(\phi_s)} \propto Q^{-1} \left( h_1^q \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right)$$

$$A_{UT}^{\sin(2\phi_h - \phi_s)} \propto Q^{-1} \left( h_{1T}^{\perp q} \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right)$$

$$A_{LT}^{\cos(\phi_s)} \propto Q^{-1} \left( g_{1T}^q \otimes D_{1q}^h + \dots \right)$$

$$A_{LT}^{\cos(2\phi_h - \phi_s)} \propto Q^{-1} \left( g_{1T}^q \otimes D_{1q}^h + \dots \right)$$

Single polarized DY (LO)

$$A_U^{\cos 2\phi_{CS}} \propto h_{1,\pi}^{\perp q} \otimes h_{1,p}^{\perp q}$$

$$A_T^{\sin \varphi_S} \propto f_{1,\pi}^q \otimes f_{1T,p}^{\perp q}$$

$$A_T^{\sin(2\phi_{CS} - \varphi_S)} \propto h_{1,\pi}^{\perp q} \otimes h_{1,p}^q$$

$$A_T^{\sin(2\phi_{CS} + \varphi_S)} \propto h_{1,\pi}^{\perp q} \otimes h_{1T,p}^{\perp q}$$

# Nucleon TMD PDFs accessed in SIDIS and DY

SIDIS

$$A_{UU}^{\cos\phi_h} \propto Q^{-1} \left( f_1^q \otimes D_{1q}^h - h_1^{\perp q} \otimes H_{1q}^{\perp h} + \dots \right)$$

$$A_{UU}^{\cos 2\phi_h} \propto h_1^{\perp q} \otimes H_{1q}^{\perp h} + Q^{-1} \left( f_1^q \otimes D_{1q}^h + \dots \right)$$

$$A_{UT}^{\sin(\phi_h - \phi_s)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h$$

$$A_{UT}^{\sin(\phi_h + \phi_s)} \propto h_1^q \otimes H_{1q}^{\perp h}$$

$$A_{UT}^{\sin(3\phi_h - \phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$$

$$A_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h$$

$$A_{UT}^{\sin(\phi_s)} \propto Q^{-1} \left( h_1^q \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right)$$

$$A_{UT}^{\sin(2\phi_h - \phi_s)} \propto Q^{-1} \left( h_{1T}^{\perp q} \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right)$$

$$A_{LT}^{\cos(\phi_s)} \propto Q^{-1} \left( g_{1T}^q \otimes D_{1q}^h + \dots \right)$$

$$A_{LT}^{\cos(2\phi_h - \phi_s)} \propto Q^{-1} \left( g_{1T}^q \otimes D_{1q}^h + \dots \right)$$

Single polarized DY (LO)

$$A_U^{\cos 2\phi_{CS}} \propto h_{1,\pi}^{\perp q} \otimes h_{1,p}^{\perp q}$$

$$A_T^{\sin \varphi_S} \propto f_{1,\pi}^q \otimes f_{1T,p}^{\perp q}$$

$$A_T^{\sin(2\phi_{CS} - \varphi_S)} \propto h_{1,\pi}^{\perp q} \otimes h_{1,p}^q$$

$$A_T^{\sin(2\phi_{CS} + \varphi_S)} \propto h_{1,\pi}^{\perp q} \otimes h_{1T,p}^{\perp q}$$

# Nucleon TMD PDFs accessed in SIDIS and DY

SIDIS

$$A_{UU}^{\cos\phi_h} \propto Q^{-1} \left( f_1^q \otimes D_{1q}^h - h_1^{\perp q} \otimes H_{1q}^{\perp h} + \dots \right)$$

$$A_{UU}^{\cos 2\phi_h} \propto h_1^{\perp q} \otimes H_{1q}^{\perp h} + Q^{-1} \left( f_1^q \otimes D_{1q}^h + \dots \right)$$

$$A_{UT}^{\sin(\phi_h - \phi_s)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h$$

$$A_{UT}^{\sin(\phi_h + \phi_s)} \propto h_1^q \otimes H_{1q}^{\perp h}$$

$$A_{UT}^{\sin(3\phi_h - \phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$$

$$A_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h$$

$$A_{UT}^{\sin(\phi_s)} \propto Q^{-1} \left( h_1^q \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right)$$

$$A_{UT}^{\sin(2\phi_h - \phi_s)} \propto Q^{-1} \left( h_{1T}^{\perp q} \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right)$$

$$A_{LT}^{\cos(\phi_s)} \propto Q^{-1} \left( g_{1T}^q \otimes D_{1q}^h + \dots \right)$$

$$A_{LT}^{\cos(2\phi_h - \phi_s)} \propto Q^{-1} \left( g_{1T}^q \otimes D_{1q}^h + \dots \right)$$

Single polarized DY (LO)

$$A_U^{\cos 2\phi_{CS}} \propto h_{1,\pi}^{\perp q} \otimes h_{1,p}^{\perp q}$$

$$A_T^{\sin \varphi_S} \propto f_{1,\pi}^q \otimes f_{1T,p}^{\perp q}$$

$$A_T^{\sin(2\phi_{CS} - \varphi_S)} \propto h_{1,\pi}^{\perp q} \otimes h_{1,p}^q$$

$$A_T^{\sin(2\phi_{CS} + \varphi_S)} \propto h_{1,\pi}^{\perp q} \otimes h_{1T,p}^{\perp q}$$

# Nucleon TMD PDFs accessed in SIDIS and DY



SIDIS

## Single polarized DY (LO)

The diagram illustrates the relationships between various amplitudes, likely representing different contributions to a total amplitude. The nodes are labeled with mathematical expressions involving  $Q$ ,  $Q^{-1}$ , and tensor products of fields  $f$ ,  $h$ , and  $H$ .

- $A_{UU}^{\cos \phi_h} \propto Q^{-1} \left( f_1^q \otimes D_{1q}^h \rightarrow h_1^{\perp q} \otimes H_{1q}^{\perp h} + \dots \right)$
- $A_{UU}^{\cos 2\phi_h} \propto h_1^{\perp q} \otimes H_{1q}^{\perp h} + Q^{-1} \left( f_1^q \otimes D_{1q}^h + \dots \right)$
- $A_{UU}^{\sin(\phi_h - \phi_s)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h$
- $A_{UT}^{\sin(\phi_h + \phi_s)} \propto h_1^q \otimes H_{1q}^{\perp h}$
- $A_{UT}^{\sin(3\phi_h - \phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1T}^{\perp h}$
- $A_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h$
- $A_{UT}^{\sin(\phi_s)} \propto Q^{-1} \left( h_1^q \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right)$
- $A_{UT}^{\sin(2\phi_h - \phi_s)} \propto Q^{-1} \left( h_{1T}^{\perp q} \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right)$
- $A_{LT}^{\cos(\phi_s)} \propto Q^{-1} \left( g_{1T}^q \otimes D_{1q}^h + \dots \right)$
- $A_{LT}^{\cos(2\phi_h - \phi_s)} \propto Q^{-1} \left( g_{1T}^q \otimes D_{1q}^h + \dots \right)$
- $A_U^{\cos 2\phi_{CS}} \propto h_{1,\pi}^{\perp q} \otimes h_{1,p}^{\perp q}$
- $A_T^{\sin \varphi_s} \propto f_{1,\pi}^q \otimes f_{1T,p}^{\perp q}$
- $A_T^{\sin(2\phi_{CS} - \varphi_s)} \propto h_{1,\pi}^{\perp q} \otimes h_{1,p}^q$
- $A_T^{\sin(2\phi_{CS} + \varphi_s)} \propto h_{1,\pi}^{\perp q} \otimes h_{1T,p}^{\perp q}$

# Nucleon TMD PDFs accessed in SIDIS and DY

SIDIS

$$\begin{aligned}
 A_{UU}^{\cos\phi_h} &\propto Q^{-1} \left( f_1^q \otimes D_{1q}^h \rightarrow h_1^{\perp q} \otimes H_{1q}^{\perp h} + \dots \right) \\
 A_{UU}^{\cos 2\phi_h} &\propto h_1^{\perp q} \otimes H_{1q}^{\perp h} + Q^{-1} \left( f_1^q \otimes D_{1q}^h + \dots \right) \\
 A_{UT}^{\sin(\phi_h - \phi_s)} &\propto f_{1T}^{\perp q} \otimes D_{1q}^h \\
 A_{UT}^{\sin(\phi_h + \phi_s)} &\propto h_1^q \otimes H_{1q}^{\perp h} \\
 A_{UT}^{\sin(3\phi_h - \phi_s)} &\propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h} \\
 A_{LT}^{\cos(\phi_h - \phi_s)} &\propto g_{1T}^q \otimes D_{1q}^h \\
 A_{UT}^{\sin(\phi_s)} &\propto Q^{-1} \left( h_1^q \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right) \\
 A_{UT}^{\sin(2\phi_h - \phi_s)} &\propto Q^{-1} \left( h_{1T}^{\perp q} \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right) \\
 A_{LT}^{\cos(\phi_s)} &\propto Q^{-1} \left( g_{1T}^q \otimes D_{1q}^h + \dots \right) \\
 A_{LT}^{\cos(2\phi_h - \phi_s)} &\propto Q^{-1} \left( g_{1T}^q \otimes D_{1q}^h + \dots \right)
 \end{aligned}$$

Single polarized DY (LO)

$$\begin{aligned}
 A_U^{\cos 2\phi_{CS}} &\propto h_{1,\pi}^{\perp q} \otimes h_{1,p}^{\perp q} \\
 A_T^{\sin \phi_S} &\propto f_{1,\pi}^q \otimes f_{1T,p}^{\perp q} \\
 A_T^{\sin(2\phi_{CS} - \phi_S)} &\propto h_{1,\pi}^{\perp q} \otimes h_{1,p}^q \\
 A_T^{\sin(2\phi_{CS} + \phi_S)} &\propto h_{1,\pi}^{\perp q} \otimes h_{1T,p}^{\perp q}
 \end{aligned}$$

All the answers are encoded in the data...  
In few years many new asymmetries  
measured by different experiments in  
different reactions, at different energies  
and kinematical ranges will wait for a  
“global analysis”...



# Nucleon TMD PDFs accessed in SIDIS and DY

SIDIS $\ell \rightarrow N^\uparrow$	Nucleon TMD PDF	Drell-Yan $\pi N^\uparrow$ (LO)
$A_{UU}^{\cos 2\phi_h}$ , $A_{UU}^{\cos \phi_h}$	$h_1^{\perp q}$ - “Boer-Mulders”	$A_U^{\cos 2\varphi_{CS}}$
$A_{UT}^{\sin(\phi_h - \phi_s)}$ , $A_{UT}^{\sin \phi_s}$ , $A_{UT}^{\sin(2\phi_h - \phi_s)}$	$f_{1T}^{\perp q}$ - ”Sivers”	$A_T^{\sin \varphi_S}$
$A_{UT}^{\sin(\phi_h + \phi_s - \pi)}$ , $A_{UT}^{\sin \phi_s}$	$h_1^q$ - “Transversity”	$A_T^{\sin(2\varphi_{CS} - \varphi_s)}$
$A_{UT}^{\sin(3\phi_h - \phi_s)}$ , $A_{UT}^{\sin(2\phi_h - \phi_s)}$	$h_{1T}^{\perp q}$ - “Pretzelosity”	$A_T^{\sin(2\varphi_{CS} + \varphi_s)}$
$A_{LT}^{\cos(\phi_h - \phi_s)}$ , $A_{LT}^{\cos \phi_s}$ , $A_{LT}^{\cos(2\phi_h - \phi_s)}$	$g_{1T}^q$ - “Worm-Gear” (T)	<b>Double-polarized DY</b> to be accessed by NICA see talk by O. Teryaev on 13.06

DY measurements at COMPASS are complementary to the previous COMPASS SIDIS results. Unique opportunity to access TMD PDFs via two mechanisms and test their universality and key features.

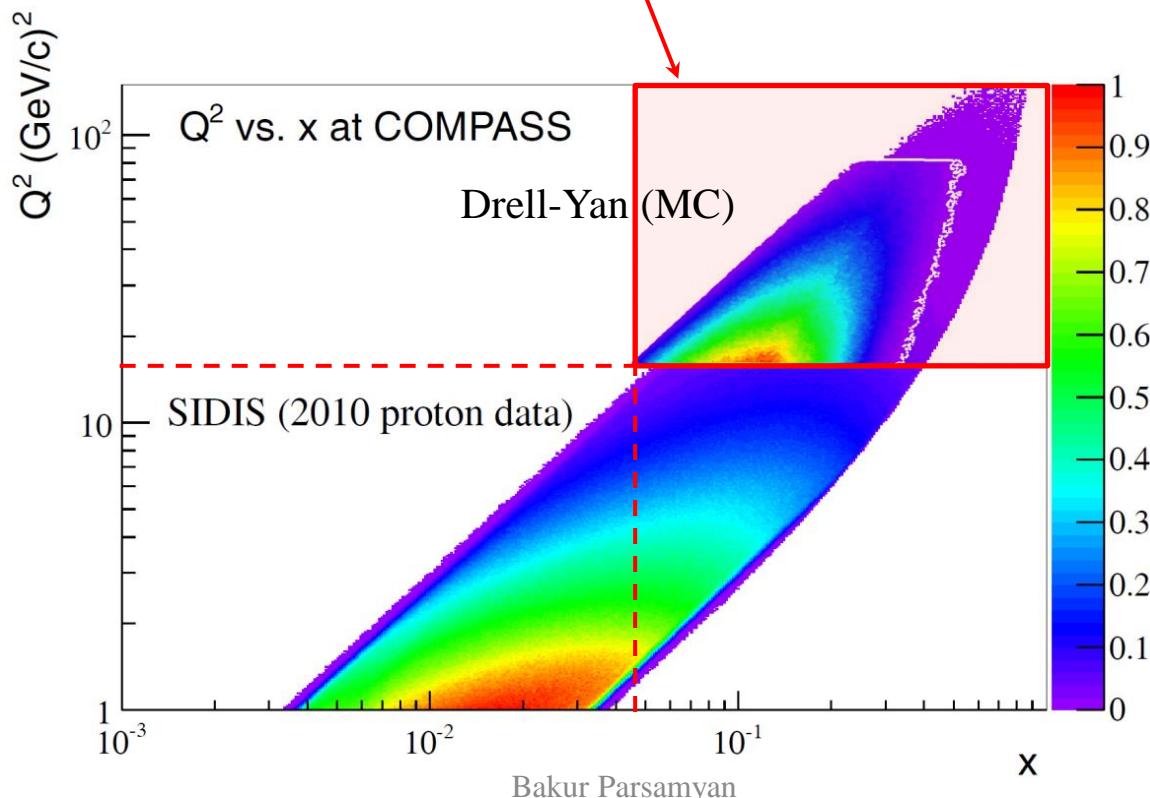
red - “twist-2”, blue - “twist-3”

# COMPASS Drell-Yan program: $Q^2$ ranges

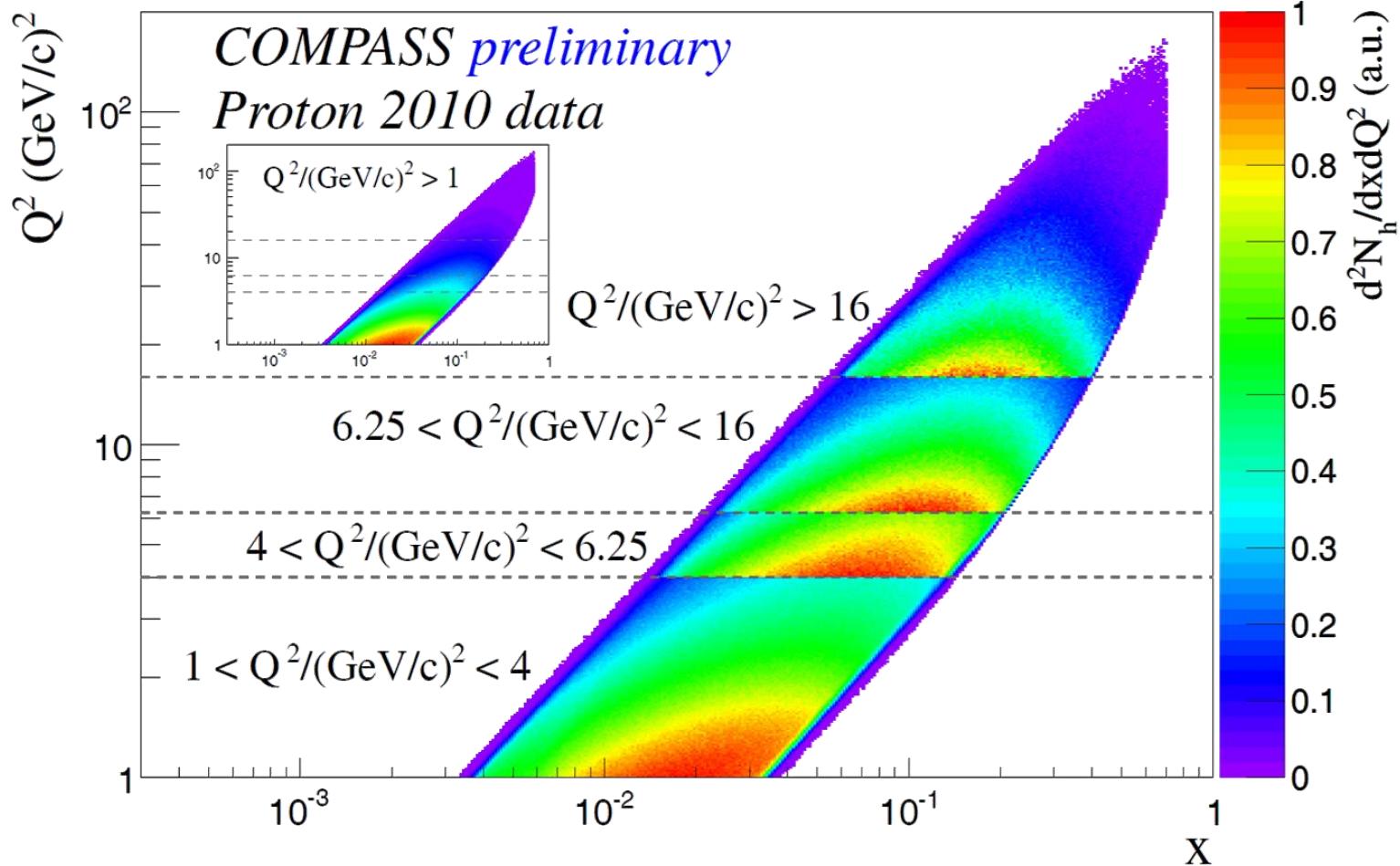
## Four $Q^2$ -ranges:

See talk by M. Chiosso on 13.06

- $1 < Q^2 / (\text{GeV}/c)^2 < 4$  “Low”
- $4 < Q^2 / (\text{GeV}/c)^2 < 6.25$  “Intermediate”
- $6.25 < Q^2 / (\text{GeV}/c)^2 < 16$  “ $J/\psi$ ”
- $Q^2 / (\text{GeV}/c)^2 > 16$  “High mass”



# COMPASS phase-space x:Q<sup>2</sup> (“DY” Q<sup>2</sup>-ranges)



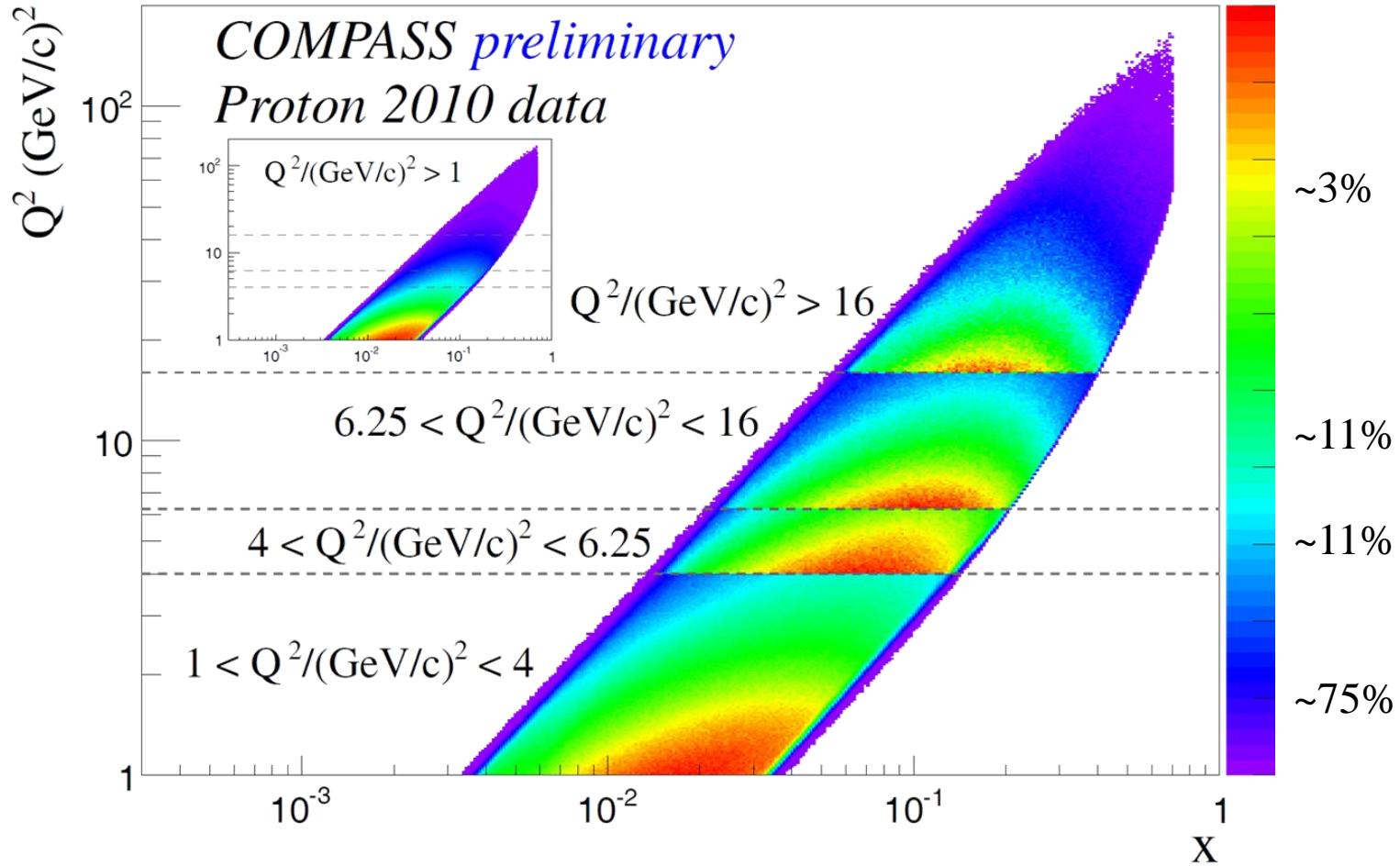
Proton 2010 data-sample ( $Q^2 > 1 \text{ (GeV}/c)^2; 0.1 < y < 0.9; W > 5 \text{ GeV}, z > 0.1, p_T > 0.1 \text{ GeV}/c$ )

Four  $Q^2$ -bins:  $1 < Q^2/(\text{GeV}/c)^2 < 4, 4 < Q^2/(\text{GeV}/c)^2 < 6.25, 6.25 < Q^2/(\text{GeV}/c)^2 < 16, Q^2/(\text{GeV}/c)^2 > 16$

For each  $Q^2$ -bin → two different z-ranges:

- $z \in [0.2; 1.0]$  – “standard” selection
- $z \in [0.1; 1.0]$  – “extended” region: Low  $z$  ( $z \in [0.1; 0.2]$ ) + “standard” selection

# COMPASS phase-space x:Q<sup>2</sup> (“DY” Q<sup>2</sup>-ranges)



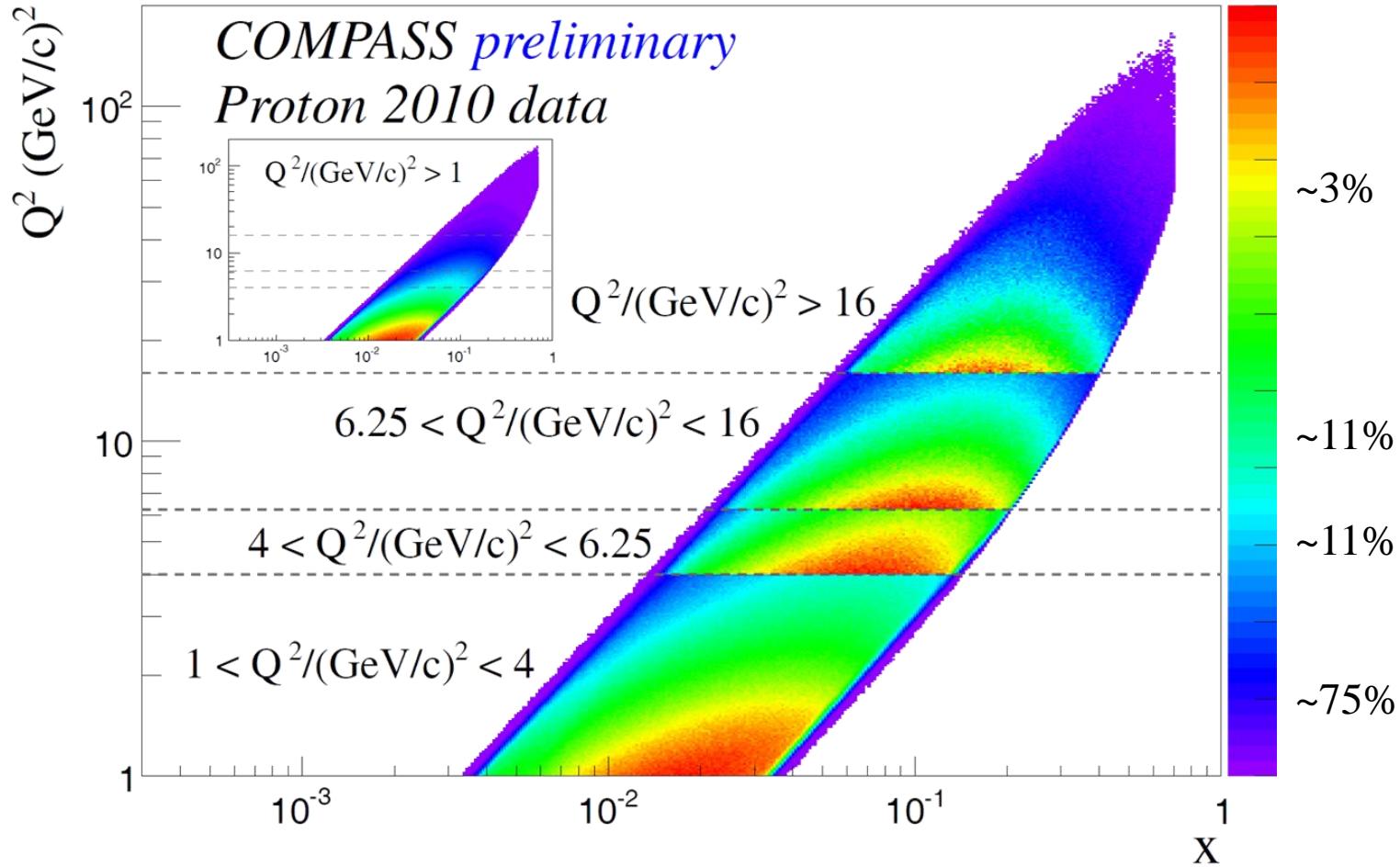
Proton 2010 data-sample ( $Q^2 > 1 \text{ (GeV}/c)^2; 0.1 < y < 0.9; W > 5 \text{ GeV}, z > 0.1, p_T > 0.1 \text{ GeV}/c$ )

Four  $Q^2$ -bins:  $1 < Q^2/(\text{GeV}/c)^2 < 4$ ,  $4 < Q^2/(\text{GeV}/c)^2 < 6.25$ ,  $6.25 < Q^2/(\text{GeV}/c)^2 < 16$ ,  $Q^2/(\text{GeV}/c)^2 > 16$

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# COMPASS phase-space x:Q<sup>2</sup> (“DY” Q<sup>2</sup>-ranges)



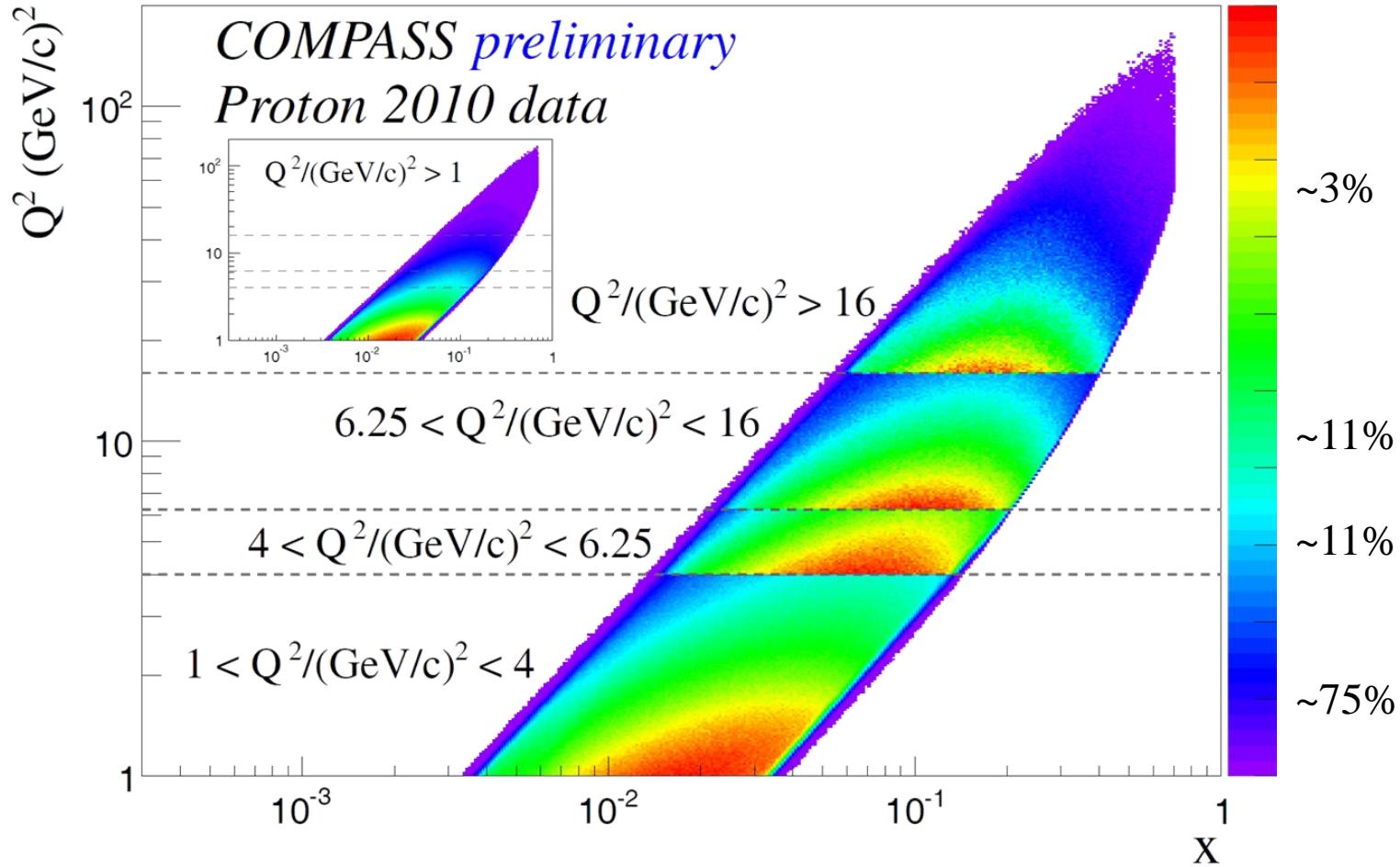
Proton 2010 data-sample ( $Q^2 > 1 \text{ (GeV}/c)^2; 0.1 < y < 0.9; W > 5 \text{ GeV}, z > 0.1, p_T > 0.1 \text{ GeV}/c$ )

Four  $Q^2$ -bins:  $1 < Q^2/(\text{GeV}/c)^2 < 4$ ,  $4 < Q^2/(\text{GeV}/c)^2 < 6.25$ ,  $6.25 < Q^2/(\text{GeV}/c)^2 < 16$ ,  $Q^2/(\text{GeV}/c)^2 > 16$

For each  $Q^2$ -bin → two different  $z$ -ranges:

- $z \in [0.2; 1.0]$  – “standard” selection
- $z \in [0.1; 1.0]$  – “extended” region: Low  $z$  ( $z \in [0.1; 0.2]$ ) + “standard” selection

# COMPASS phase-space x:Q<sup>2</sup> (“DY” Q<sup>2</sup>-ranges)



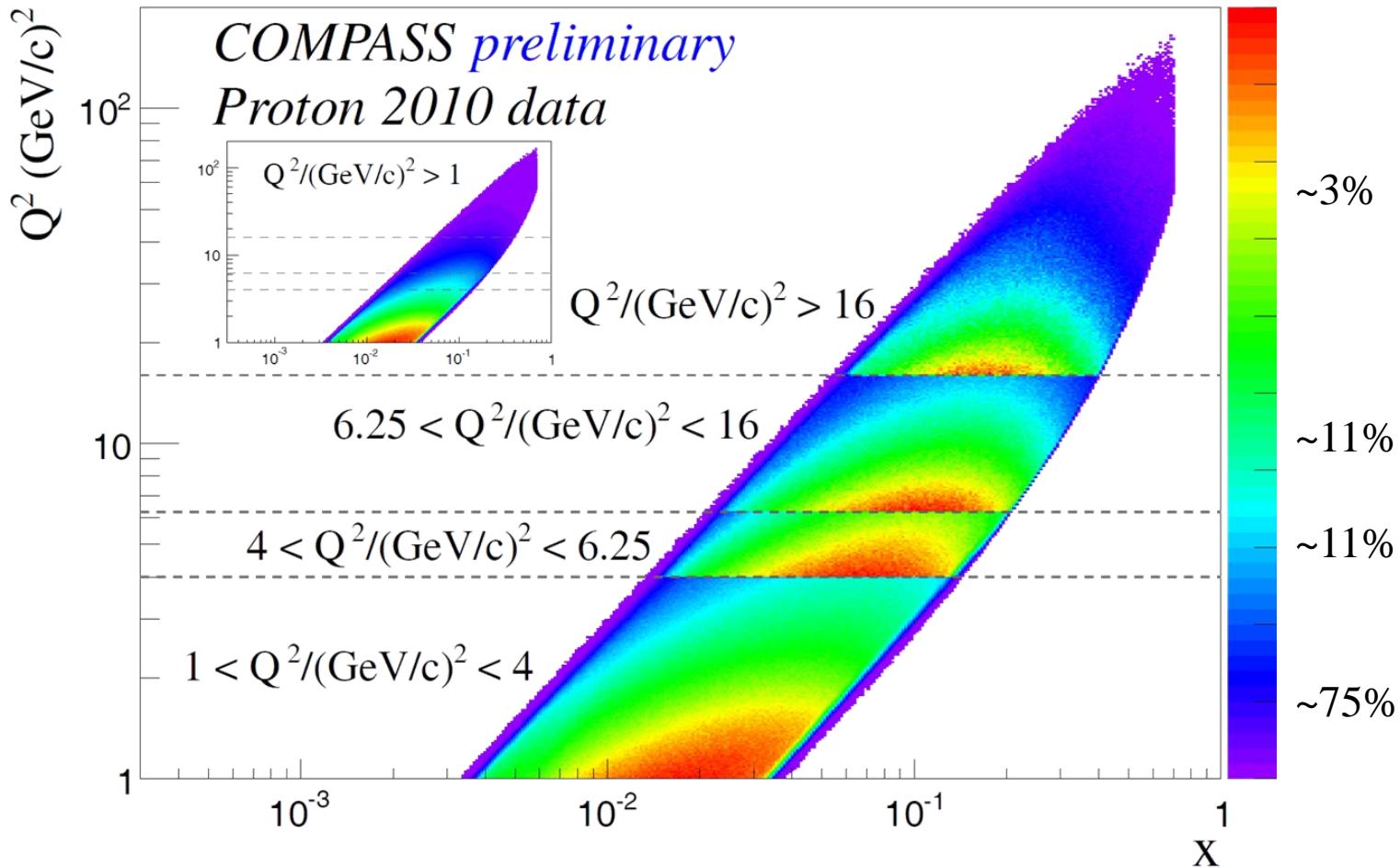
On a way towards multi-dimensional analysis..! More news soon!

Four Q<sup>2</sup>-bins:  $1 < Q^2/(\text{GeV}/c)^2 < 4$ ,  $4 < Q^2/(\text{GeV}/c)^2 < 6.25$ ,  $6.25 < Q^2/(\text{GeV}/c)^2 < 16$ ,  $Q^2/(\text{GeV}/c)^2 > 16$

For each Q<sup>2</sup>-bin → two different z-ranges:

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# COMPASS phase-space x:Q<sup>2</sup> (“DY” Q<sup>2</sup>-ranges)



- In SIDIS with  $z>0.2$  and  $Q^2>16 \text{ (GeV/c)}^2$ :  $\delta A_{UT}^{\sin(\phi_h-\phi_s)} \approx 0.01$  (for  $h^+$ ) and  $\approx 0.012$  (for  $h^-$ )
  - $\delta A_T^{\sin\phi_s}$  in DY “high mass” range with  $2.85 \cdot 10^5$  events (140 days)  $\approx 0.013$  ↗
- See talk by M. Chiosso on 13.06

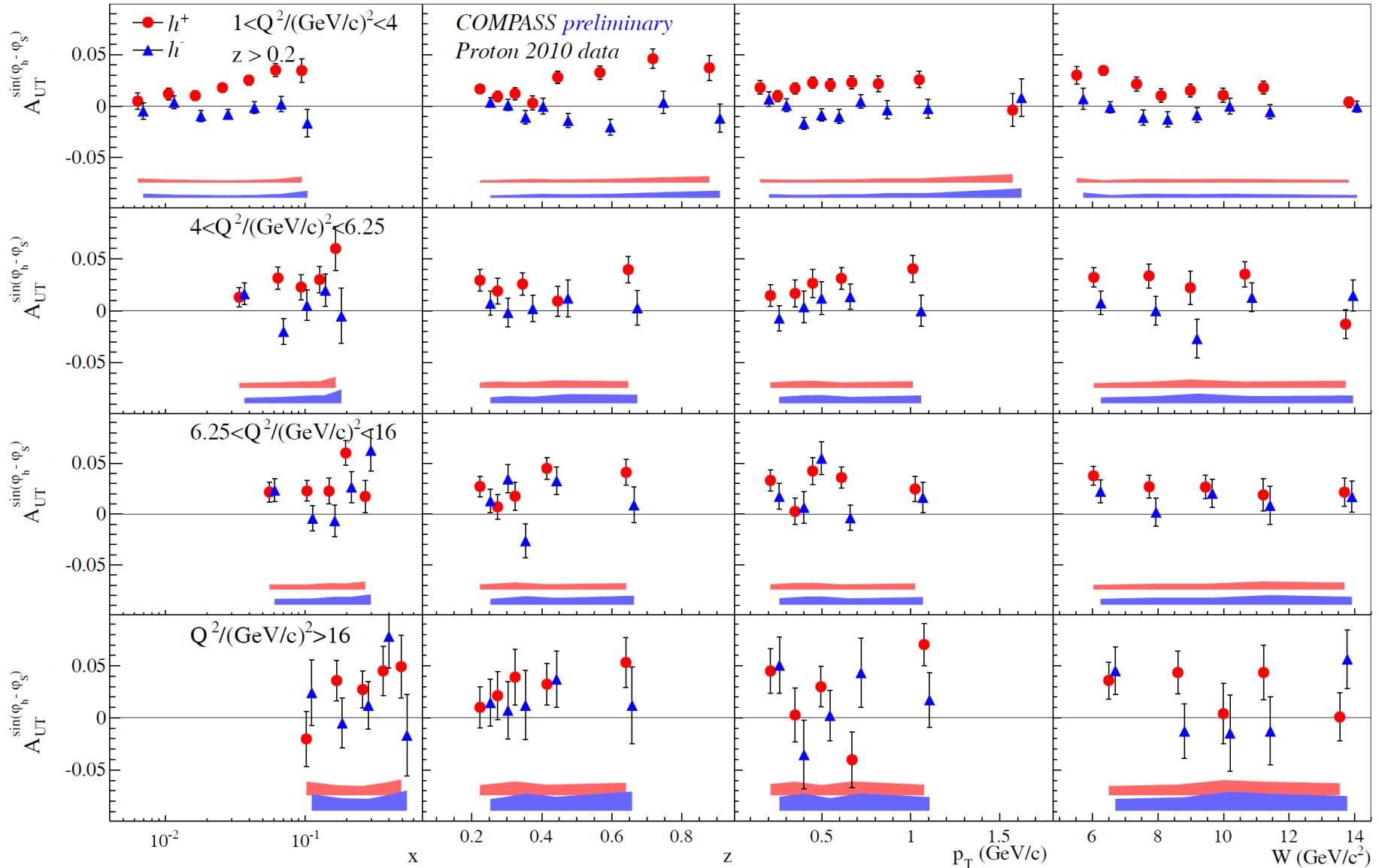
# Outline

- Introduction
  - Brief review of COMPASS results with TSAs
- COMPASS – “SIDIS-DY bridge”
- **New results!**
  - **Asymmetries**
  - Re-evaluation of  $A_{LT}^{\cos\varphi_S}$  and  $A_{LT}^{\cos(\varphi_h - \varphi_S)}$ :  
from the  $l p$  to  $\gamma * p$  cross-section
  - $A_{LT}^{\cos(\varphi_h - \varphi_S)}$ : Comparison with predictions
  - Multi-D map of kinematical distributions
- Conclusions



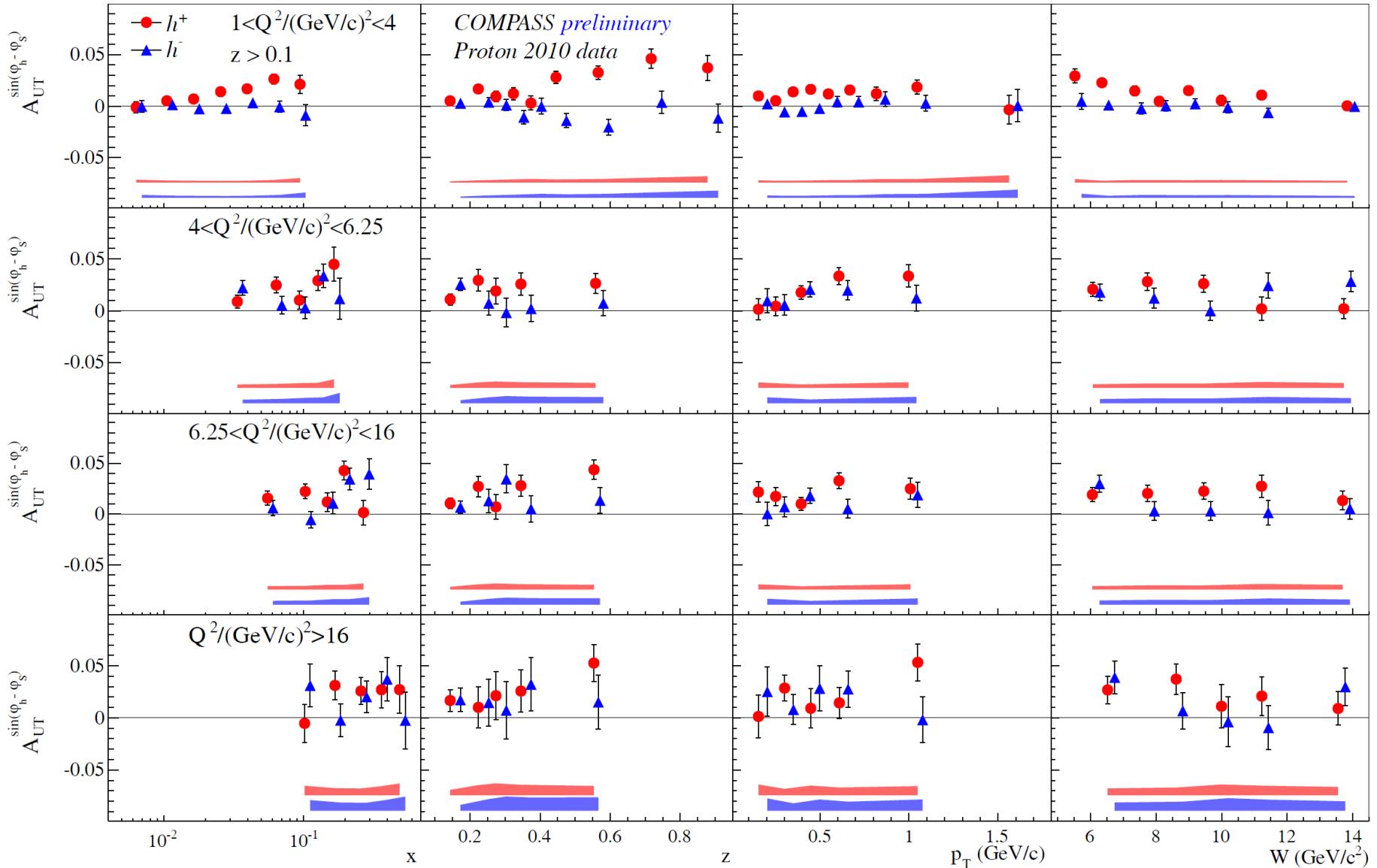
# Sivers in DY Q<sup>2</sup>-bins: z > 0.2

**NEW!** These results are being shown for the first time



# Sivers in DY Q<sup>2</sup>-bins: z > 0.1

**NEW!** These results are being shown for the first time

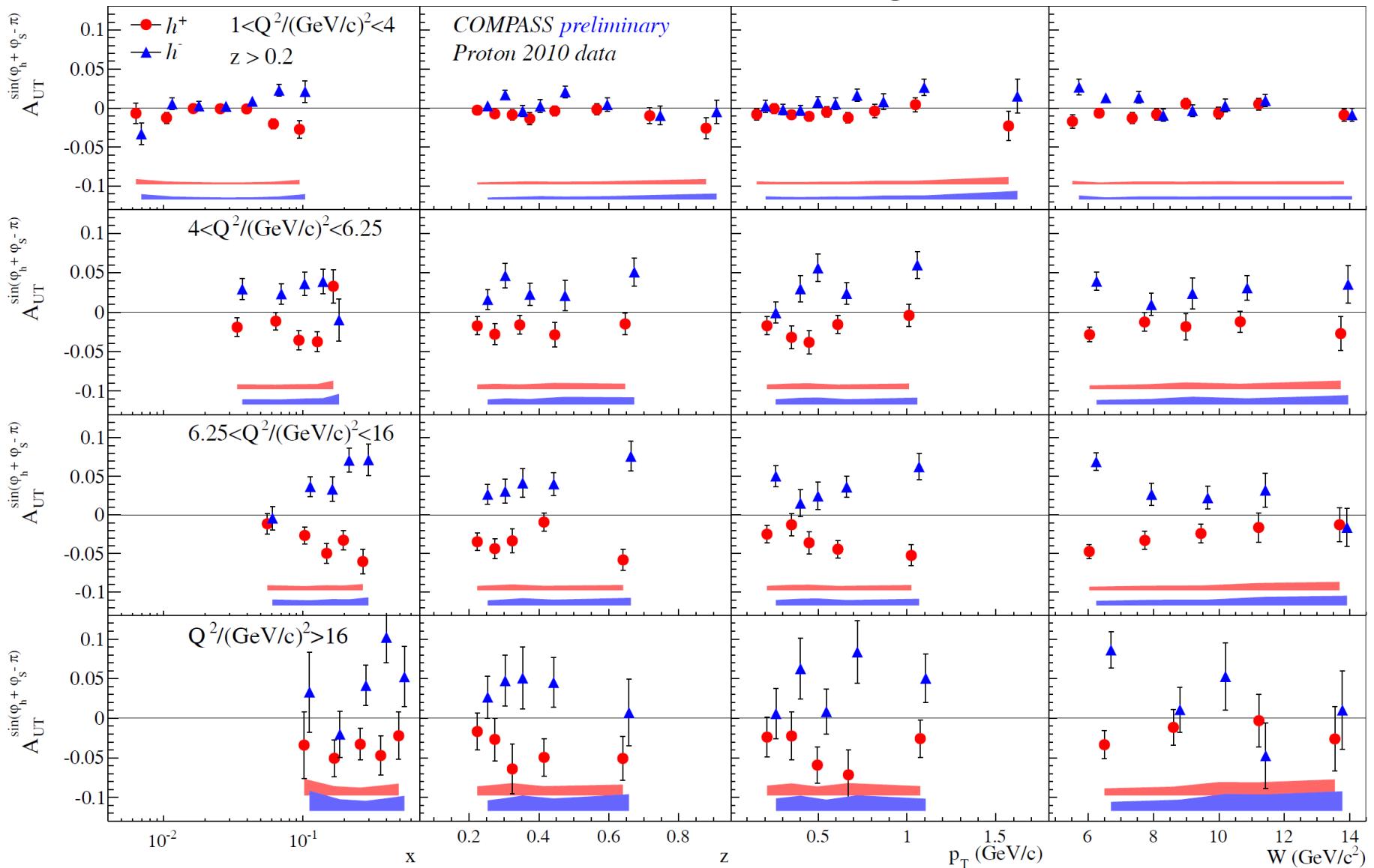


# Collins in DY Q<sup>2</sup>-bins: z > 0.2

Input for “Q<sup>2</sup>-evolution”-related studies



**NEW!** These results are being shown for the first time

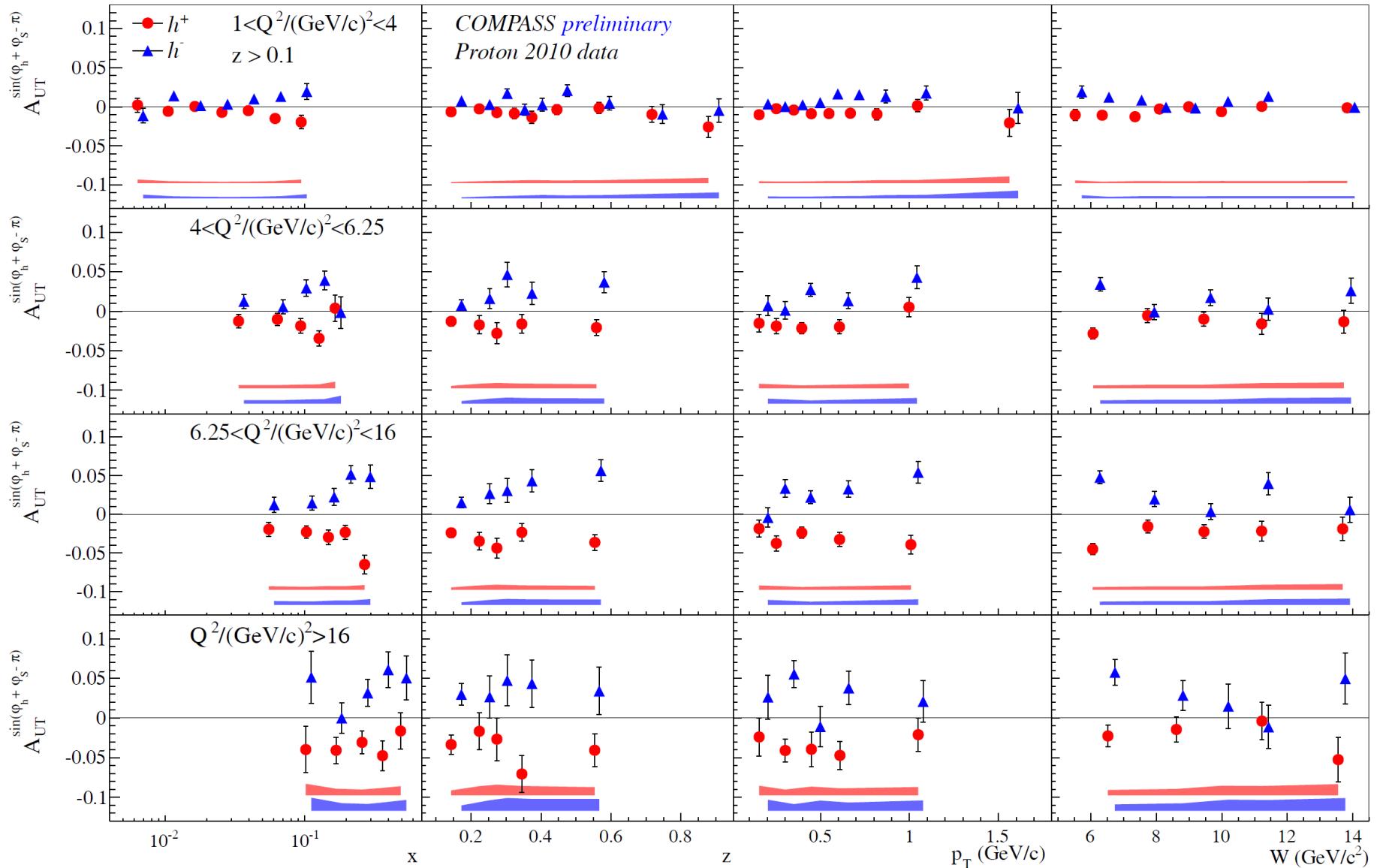


# Collins in DY Q<sup>2</sup>-bins: z > 0.1

Input for “Q<sup>2</sup>-evolution”-related studies



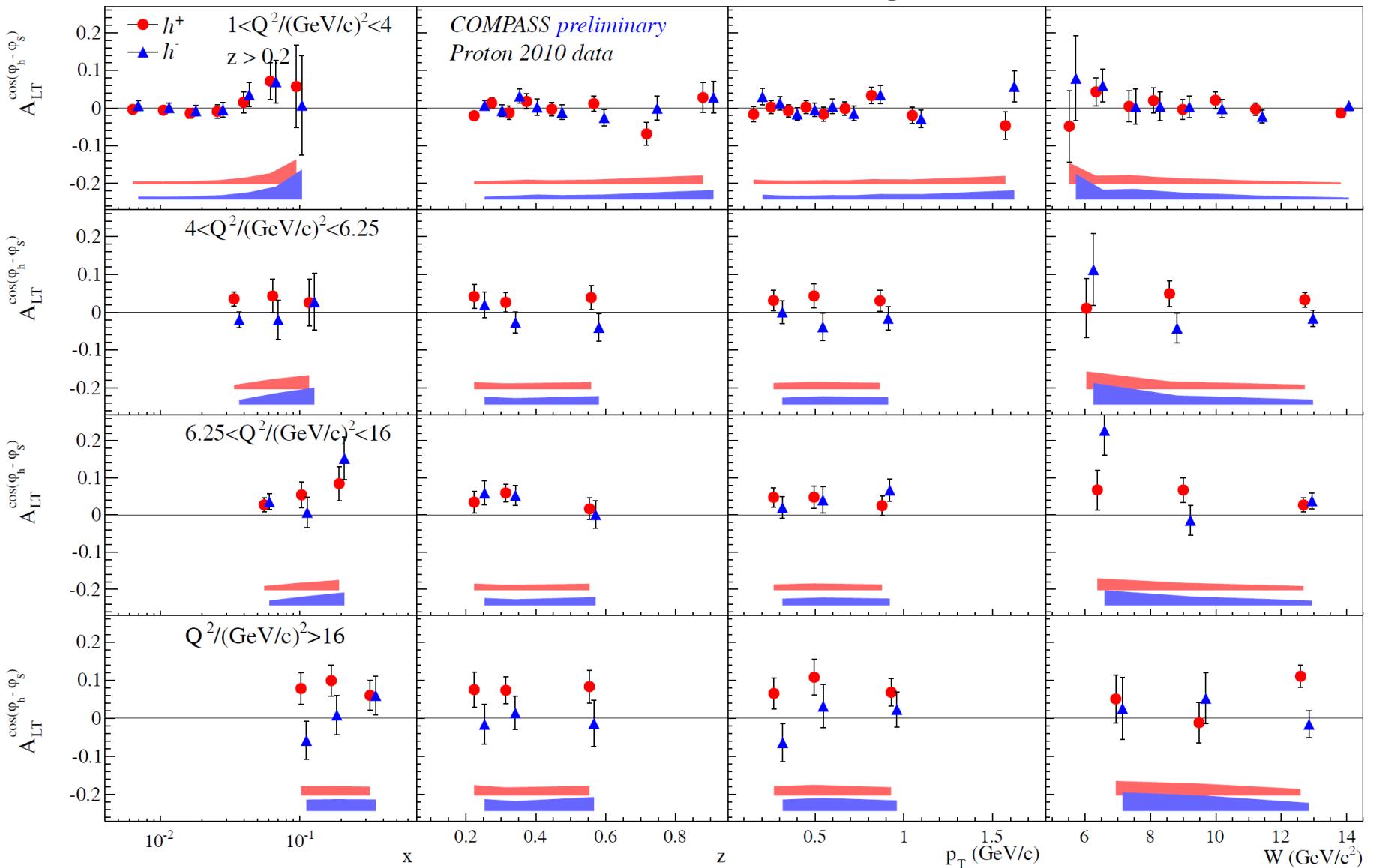
**NEW!** These results are being shown for the first time





# $A_{LT} \cos(\phi_h - \phi_s)$ in DY Q<sup>2</sup>-bins: z > 0.2

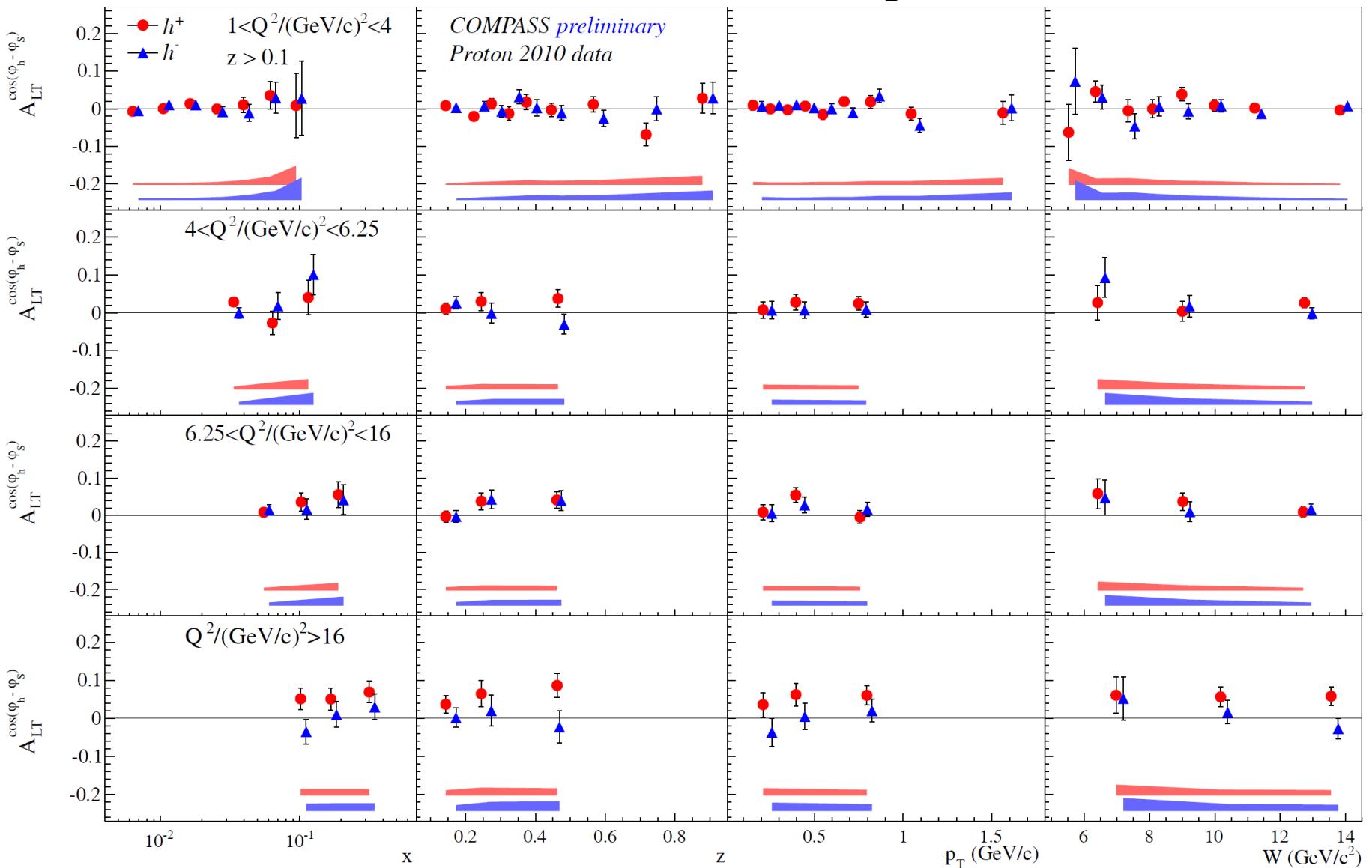
**NEW!** These results are being shown for the first time





# $A_{LT} \cos(\phi_h - \phi_s)$ in DY Q<sup>2</sup>-bins: z > 0.1

**NEW!** These results are being shown for the first time

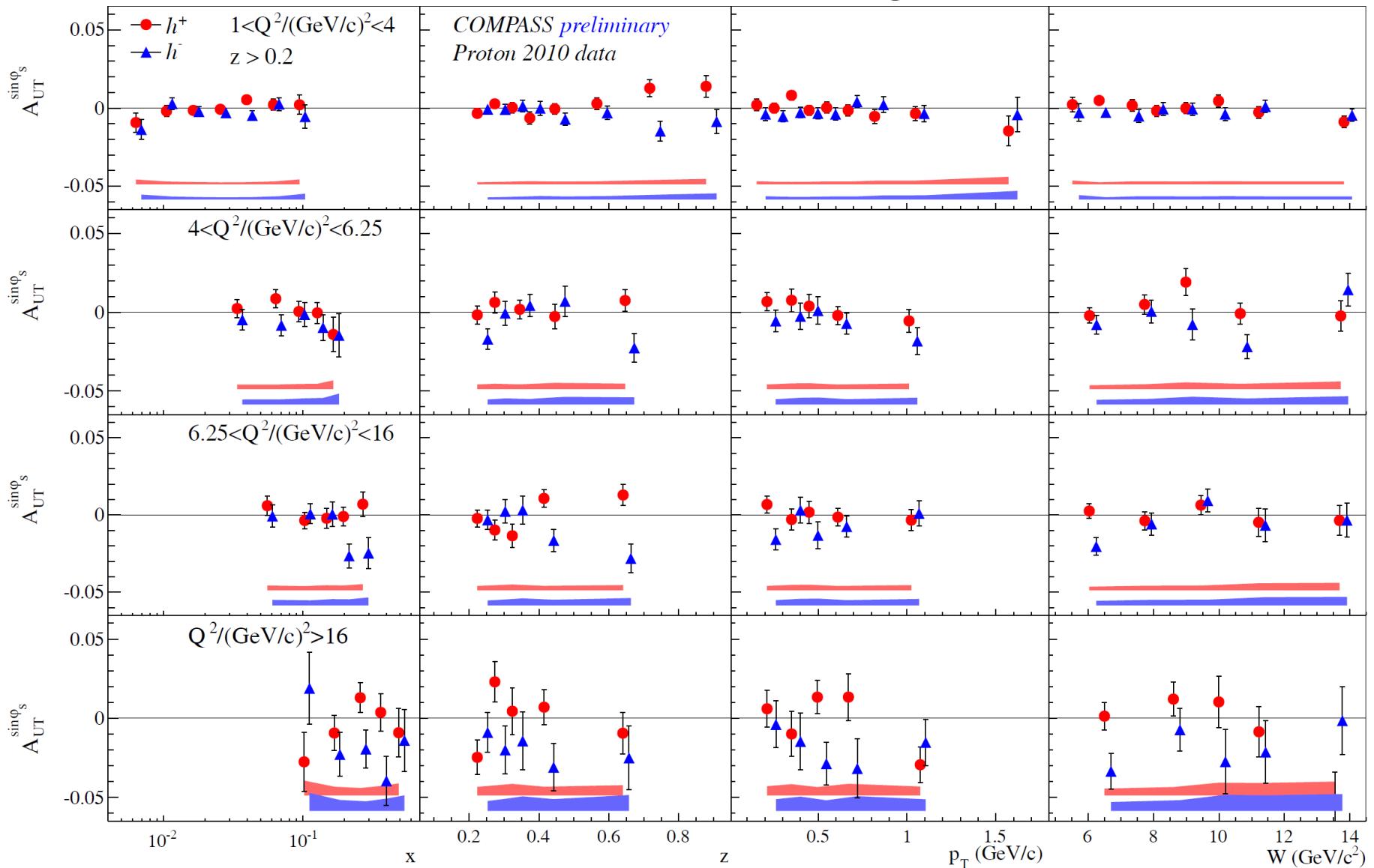


# $A_{UT} \sin\varphi_s$ in DY Q<sup>2</sup>-bins: z > 0.2

Input for “Q<sup>2</sup>-evolution”-related studies



NEW! These results are being shown for the first time

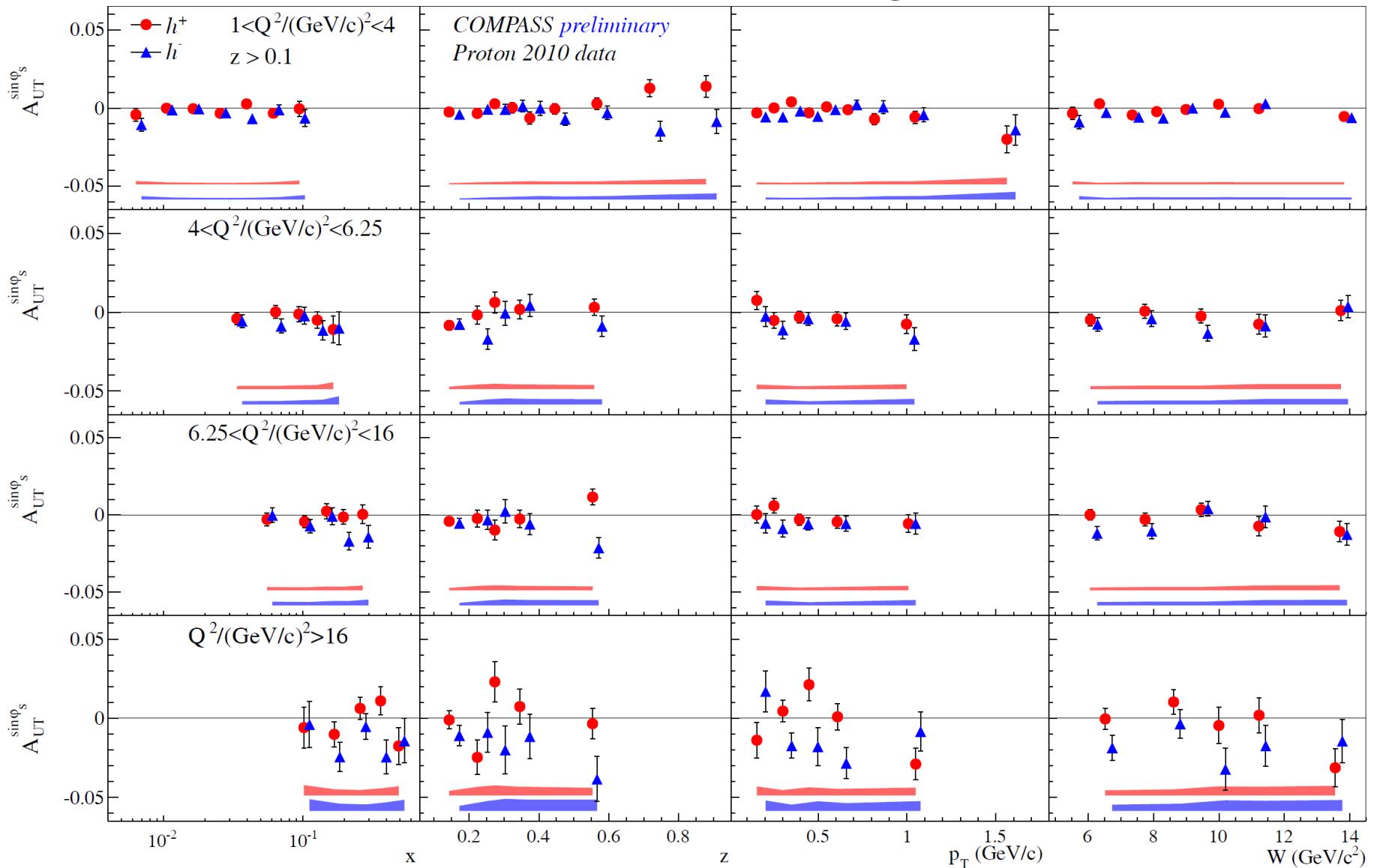


# $A_{UT} \sin\varphi_s$ in DY Q<sup>2</sup>-bins: z > 0.1

Input for “Q<sup>2</sup>-evolution”-related studies COMPASS

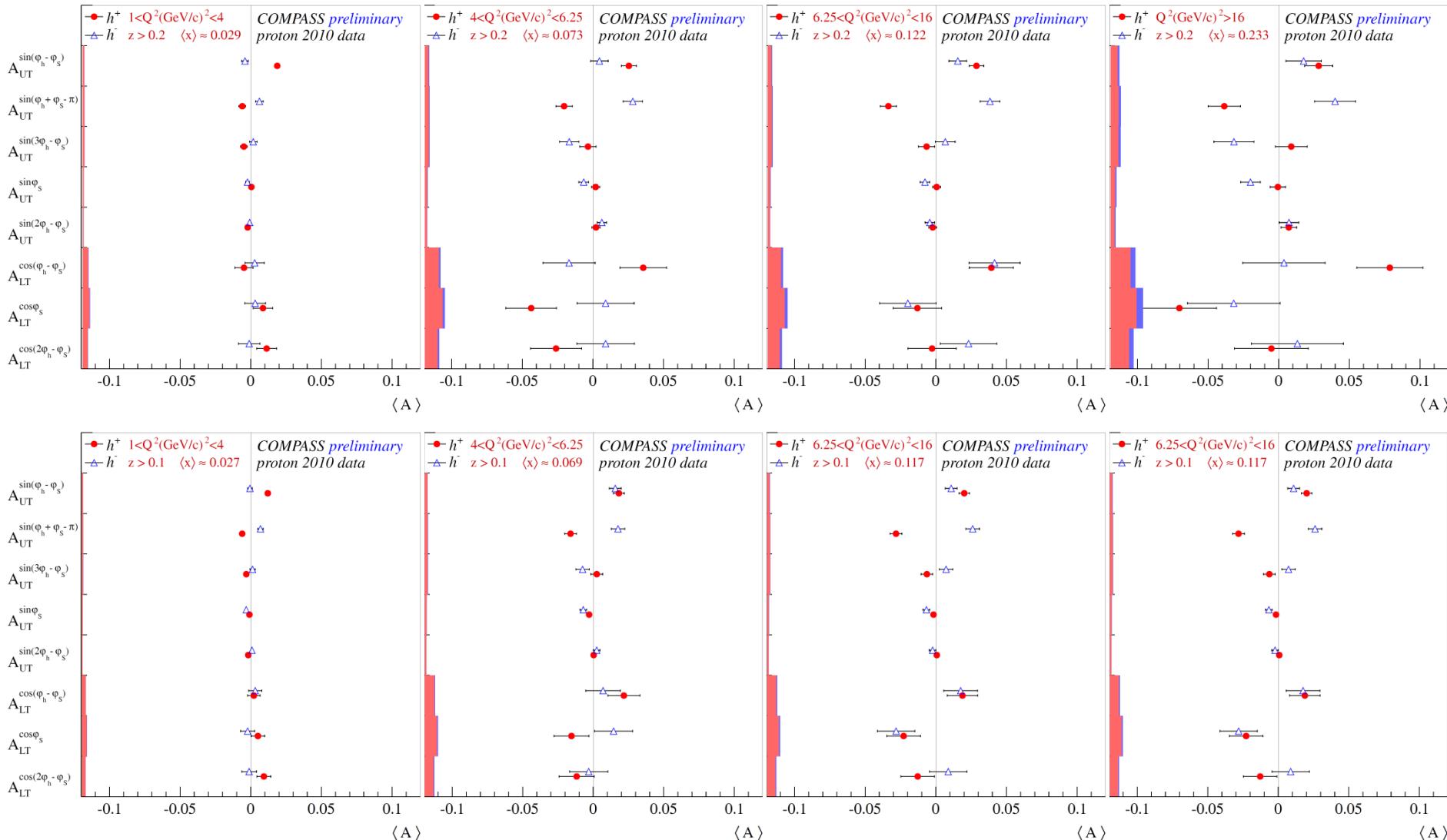


NEW! These results are being shown for the first time



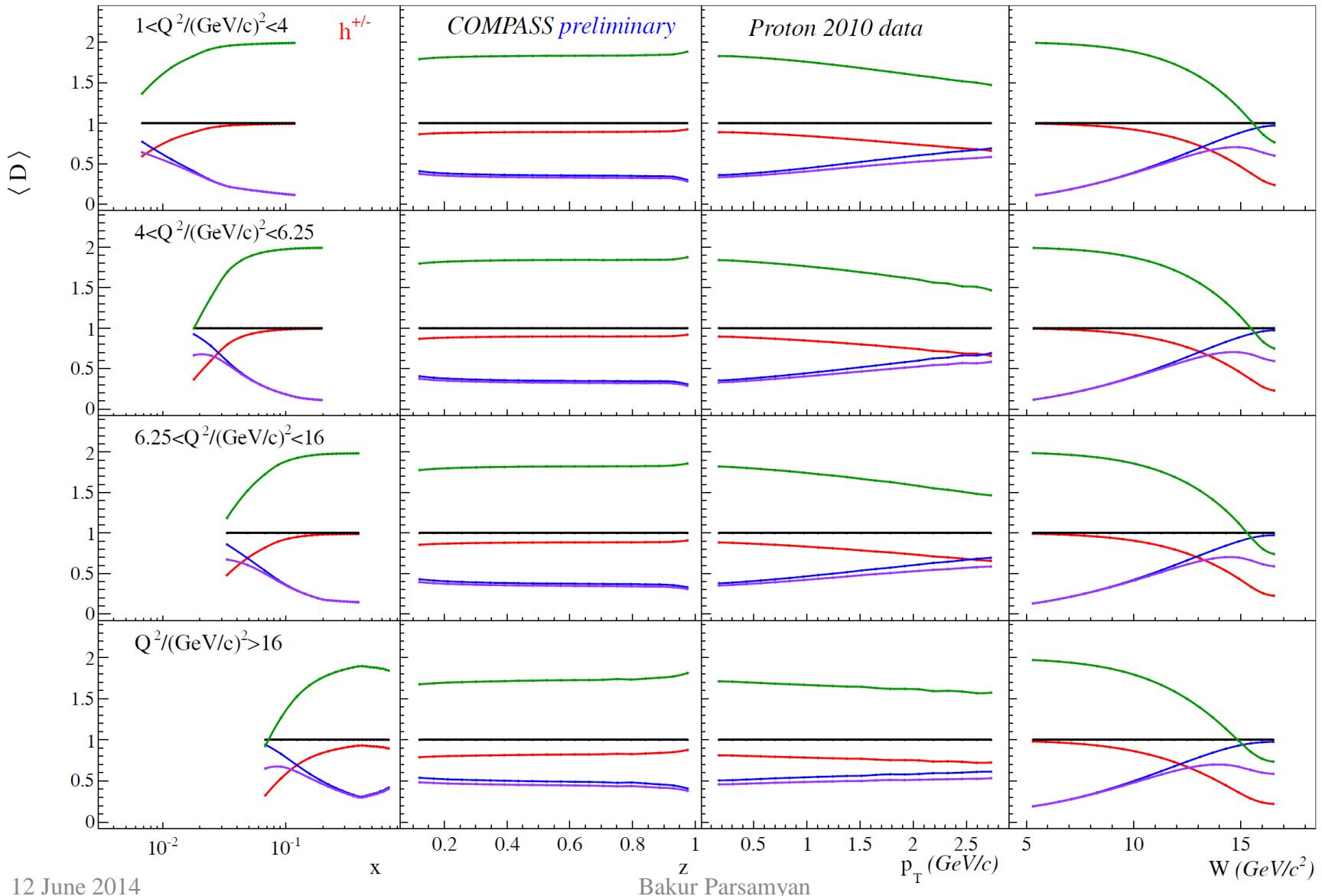
# Mean asymmetries in DY-ranges

**NEW!** These results are being shown for the first time



# Depolarization factors

$$\begin{aligned}
 -D & \sin(\varphi_h - \varphi_s) \\
 D & \sin(\varphi_h + \varphi_s - \pi), \sin(3\varphi_h - \varphi_s) \\
 D & \cos(\varphi_h - \varphi_s) \\
 D & \sin\varphi_s, \sin(2\varphi_h - \varphi_s) \\
 D & \cos\varphi_s, \cos(2\varphi_h - \varphi_s)
 \end{aligned}$$



# Outline

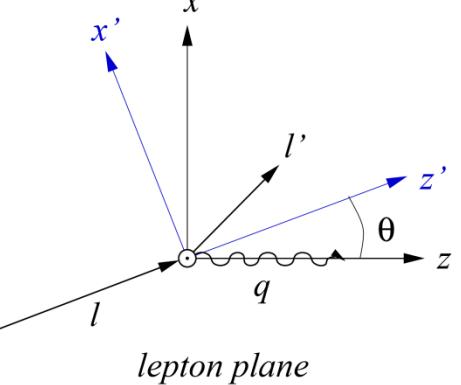
- Introduction
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# SIDIS x-section: from $lp$ to $\gamma*p$ ( $P_L=0$ )

$$\frac{d\sigma}{dx dy dz dP_{hT}^2 d\varphi_h d\varphi_s} = \left[ \frac{\cos \theta}{1 - \sin^2 \theta \sin^2 \varphi_s} \right] \times \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] \times (F_{UU,T} + \varepsilon F_{UU,L}) \times$$

$$\left[ 1 + \cos \varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\varphi_h)} + \lambda \sin \varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \varphi_h} + \right. \\ \left. \sin \varphi_s \times (\cos \theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \varphi_s}) + \right. \\ \left. \sin(\varphi_h - \varphi_s) \times \left( \cos \theta A_{UT}^{\sin(\varphi_h - \varphi_s)} + \frac{1}{2} \sin \theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin \varphi_h} \right) + \right. \\ \left. \sin(\varphi_h + \varphi_s) \times \left( \cos \theta \varepsilon A_{UT}^{\sin(\varphi_h + \varphi_s)} + \frac{1}{2} \sin \theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin \varphi_h} \right) + \right. \\ \left. \sin(2\varphi_h - \varphi_s) \times \left( \cos \theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_s)} + \frac{1}{2} \sin \theta \varepsilon A_{UL}^{\sin 2\varphi_h} \right) + \right. \\ \left. \sin(3\varphi_h - \varphi_s) \times (\cos \theta \varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_s)}) + \right. \\ \left. \sin(2\varphi_h + \varphi_s) \times \left( \frac{1}{2} \sin \theta \varepsilon A_{UL}^{\sin 2\varphi_h} \right) \right]$$

$$\frac{P_T}{\sqrt{1 - \sin^2 \theta \sin^2 \varphi_s}} \left[ \cos \varphi_s \times \left( \cos \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_s} + \sin \theta \sqrt{(1-\varepsilon^2)} A_{LL} \right) + \right. \\ \left. \cos(\varphi_h - \varphi_s) \times \left( \cos \theta \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_s)} + \frac{1}{2} \sin \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos \varphi_h} \right) + \right. \\ \left. \cos(2\varphi_h - \varphi_s) \times (\cos \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_s)}) + \right. \\ \left. \cos(\varphi_h + \varphi_s) \times \left( \frac{1}{2} \sin \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos \varphi_h} \right) \right]$$



$$\sin \theta = \gamma \sqrt{\frac{1 - y - \frac{1}{4} \gamma^2 y^2}{1 + \gamma^2}}, \quad \gamma = \frac{2Mx}{Q};$$

$$\theta \xrightarrow{\text{Bjorken limit}} 0 \Rightarrow S_T \simeq P_T, \quad S_L \simeq P_L$$

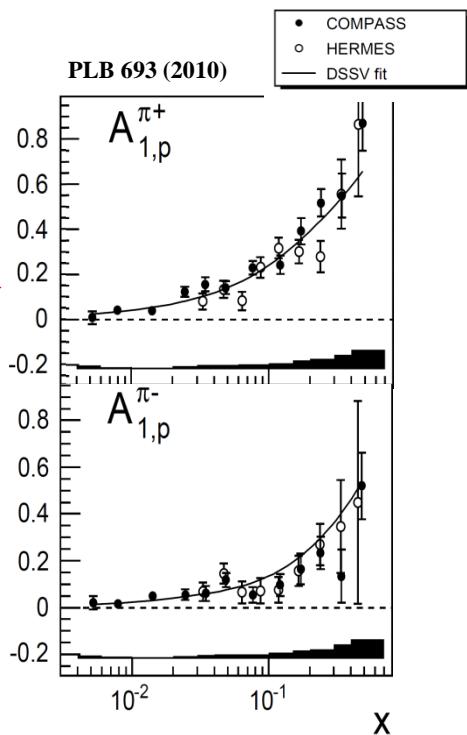
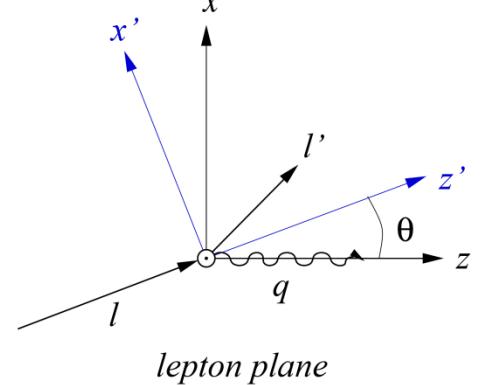
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$$\frac{d\sigma}{dx dy dz dP_{hT}^2 d\varphi_h d\varphi_s} = \left[ \frac{\cos \theta}{1 - \sin^2 \theta \sin^2 \varphi_s} \right] \times \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] \times (F_{UU,T} + \varepsilon F_{UU,L}) \times$$

$$1 + \cos \varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\varphi_h)} + \lambda \sin \varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \varphi_h} +$$

$$\begin{aligned} & \left[ \sin \varphi_s \times \left( \cos \theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \varphi_s} \right) + \right. \\ & \sin(\varphi_h - \varphi_s) \times \left( \cos \theta A_{UT}^{\sin(\varphi_h - \varphi_s)} + \frac{1}{2} \sin \theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin \varphi_h} \right) + \\ & \sin(\varphi_h + \varphi_s) \times \left( \cos \theta \varepsilon A_{UT}^{\sin(\varphi_h + \varphi_s)} + \frac{1}{2} \sin \theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin \varphi_h} \right) + \\ & \sin(2\varphi_h - \varphi_s) \times \left( \cos \theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_s)} + \frac{1}{2} \sin \theta \varepsilon A_{UL}^{\sin 2\varphi_h} \right) + \\ & \sin(3\varphi_h - \varphi_s) \times \left( \cos \theta \varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_s)} \right) + \\ & \left. \sin(2\varphi_h + \varphi_s) \times \left( \frac{1}{2} \sin \theta \varepsilon A_{UL}^{\sin 2\varphi_h} \right) \right] + \end{aligned}$$

$$\begin{aligned} & \left[ \cos \varphi_s \times \left( \cos \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_s} + \sin \theta \sqrt{(1-\varepsilon^2)} A_{LL} \right) + \right. \\ & \cos(\varphi_h - \varphi_s) \times \left( \cos \theta \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_s)} + \frac{1}{2} \sin \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos \varphi_h} \right) + \\ & \cos(2\varphi_h - \varphi_s) \times \left( \cos \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_s)} \right) + \\ & \left. \cos(\varphi_h + \varphi_s) \times \left( \frac{1}{2} \sin \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos \varphi_h} \right) \right] \end{aligned}$$



# Mixing of the "T" and "L" amplitudes

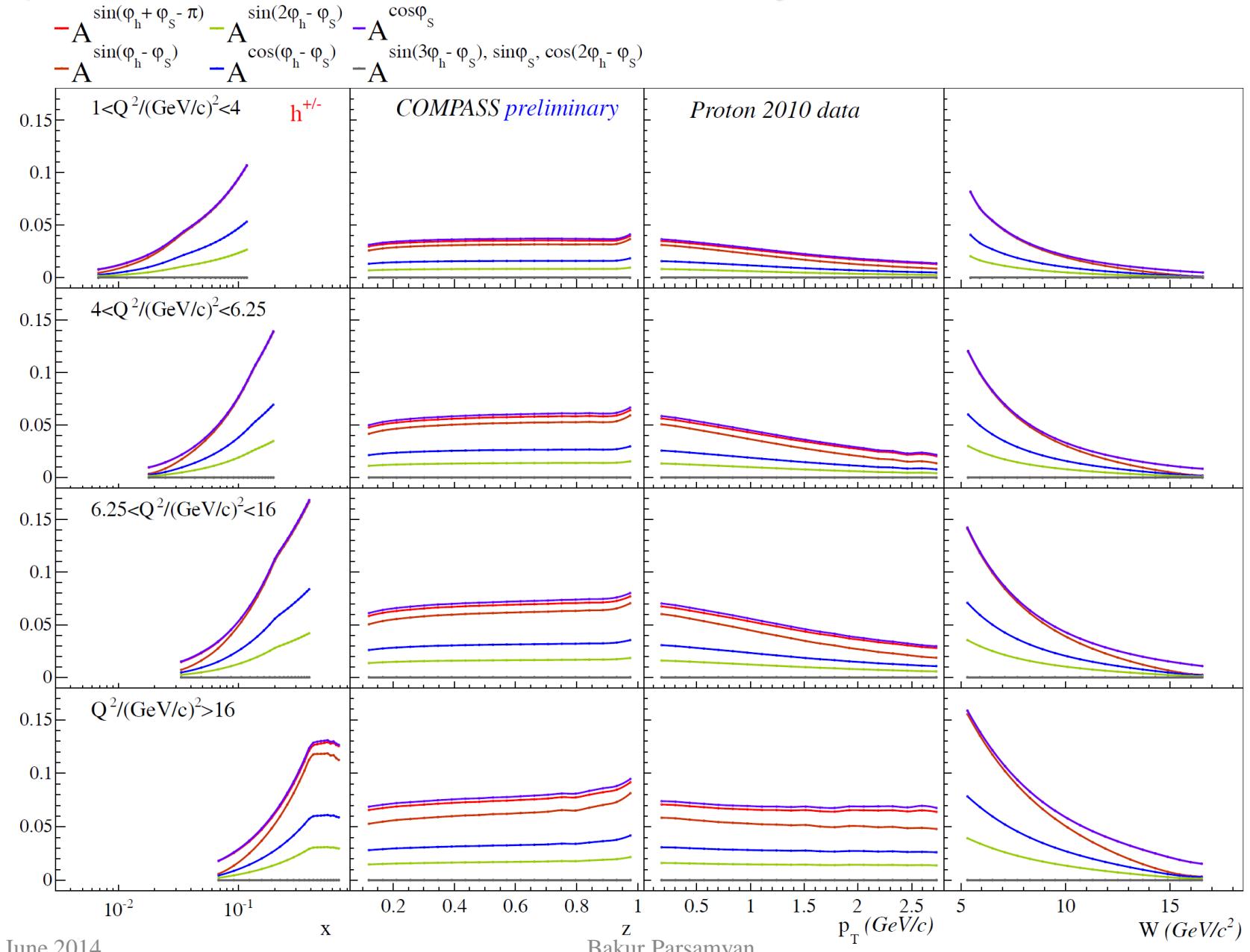
$$\text{TSA}_{\text{fit}} = \cos\theta \cdot \text{TSA}_{\text{real}} + C(\varepsilon, \theta) \cdot \text{LSA}$$

TSA	$C(\varepsilon, \theta)$ - factor	Contributing LSA
$A_{UT}^{\sin(\phi_h - \phi_s)}$	$\sin\theta \frac{\sqrt{2\varepsilon(1 + \varepsilon)}}{2}$	$A_{UL}^{\sin\phi_h}$
$A_{UT}^{\sin(\phi_h + \phi_s)}$	$\sin\theta \frac{\sqrt{2\varepsilon(1 + \varepsilon)}}{2\varepsilon}$	$A_{UL}^{\sin\phi_h}$
$A_{UT}^{\sin(2\phi_h - \phi_s)}$	$\sin\theta \frac{\varepsilon}{2\sqrt{2\varepsilon(1 + \varepsilon)}}$	$A_{UL}^{\sin 2\phi_h}$
$A_{LT}^{\cos(\phi_h - \phi_s)}$	$\sin\theta \frac{\sqrt{2\varepsilon(1 - \varepsilon)}}{2\sqrt{(1 - \varepsilon^2)}}$	$A_{LL}^{\cos\phi_h}$
$A_{LT}^{\cos\phi_s}$	$\sin\theta \frac{\sqrt{(1 - \varepsilon^2)}}{\sqrt{2\varepsilon(1 - \varepsilon)}}$	$A_{LL}$
$A_{UT}^{\sin(3\phi_h - \phi_s)}, A_{UT}^{\sin\phi_s}, A_{LT}^{\cos(2\phi_h - \phi_s)}$	—	—

The  $\sin\theta$  is small at COMPASS kinematics.

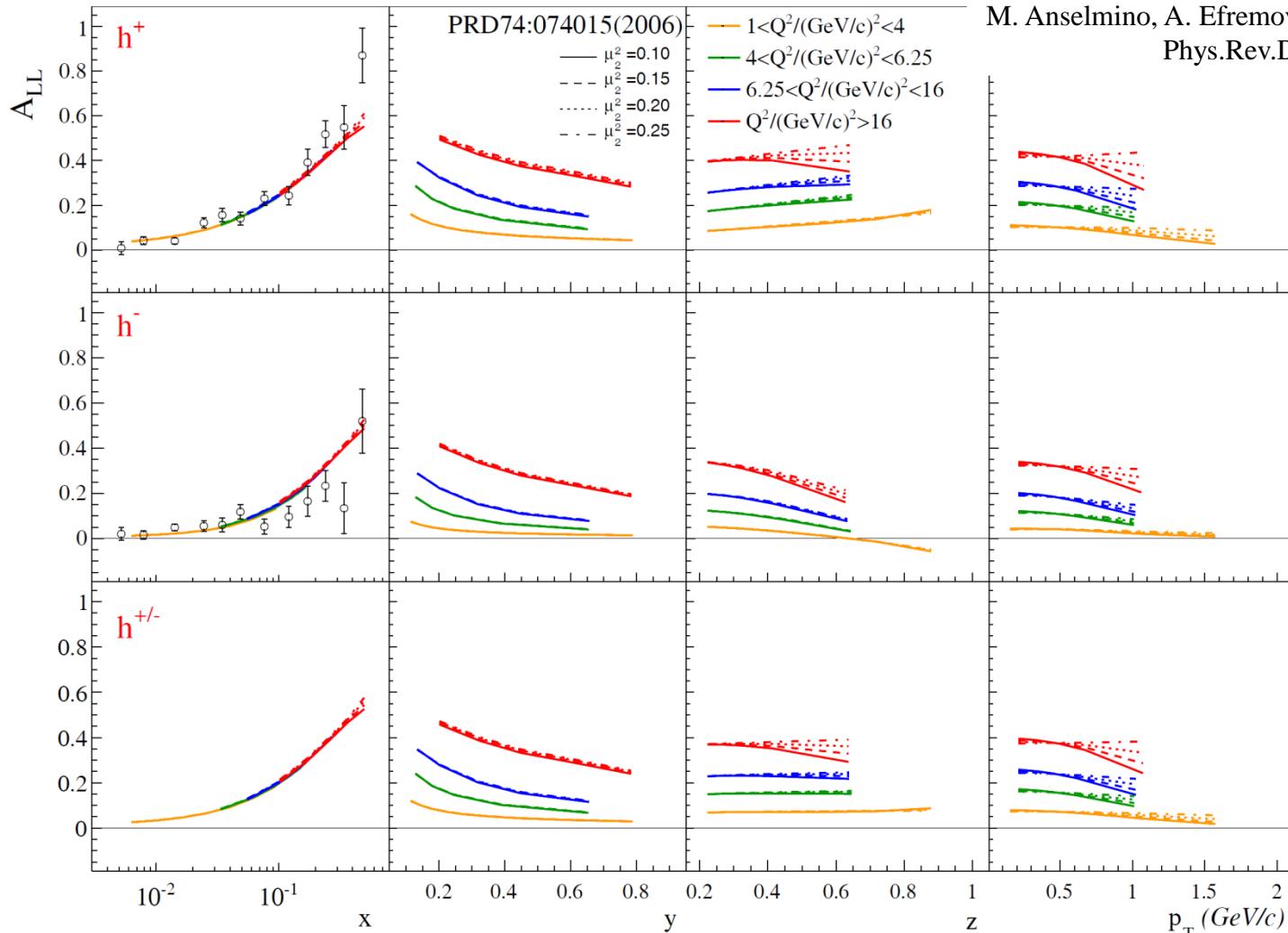
The maximum reached value is  $\sim 0.18$  and the mean is around 0.05 ( $\cos\theta > 0.98$ ).

# $C(\varepsilon, \theta)$ - factors for different asymmetries



# A<sub>LL</sub> evaluated according to the PRD 74, 074015 (2006)

COMPASS Proton 2007 (PLB 693(2010))



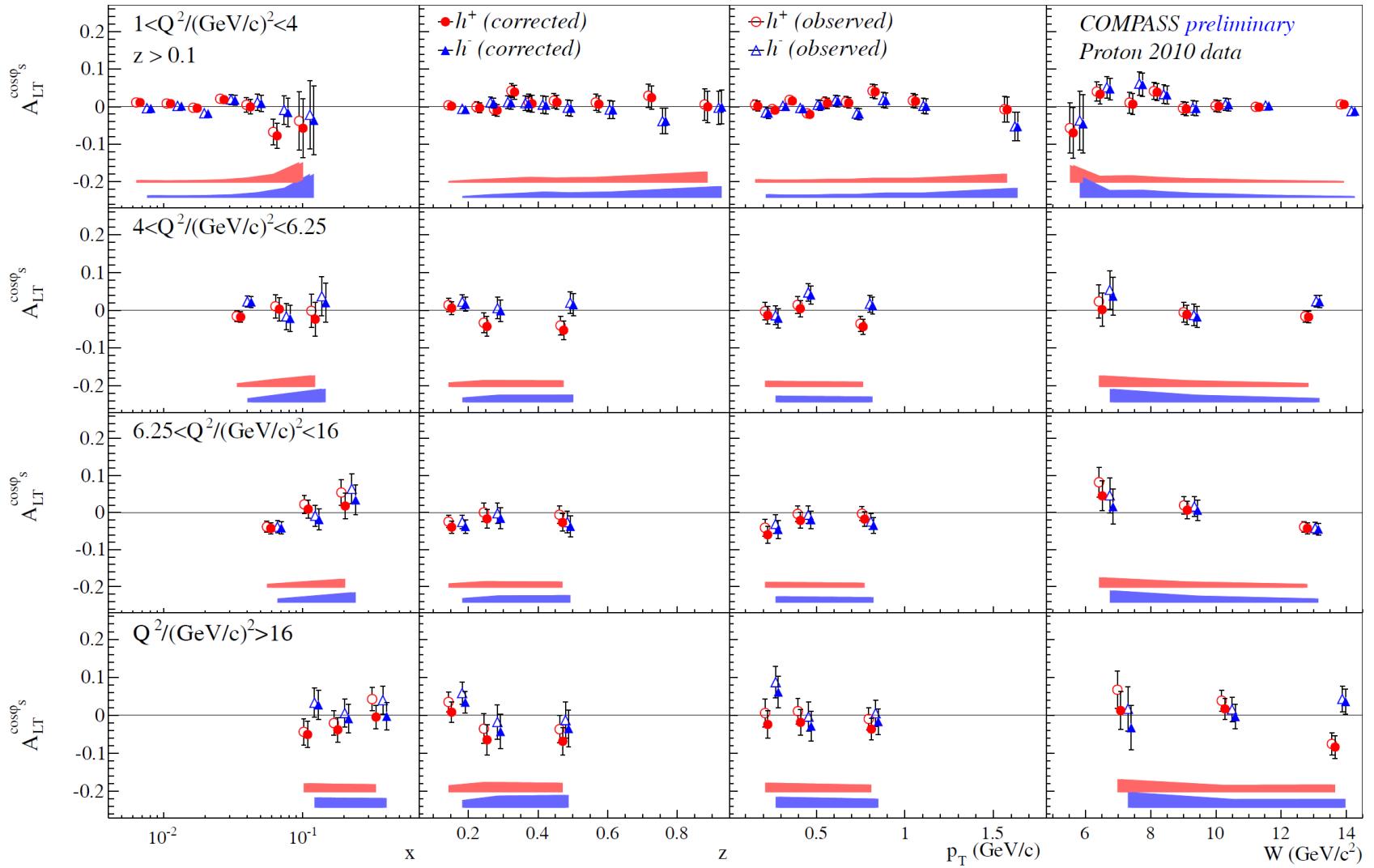
M. Anselmino, A. Efremov, A. Kotzinian, and B. Parsamyan  
Phys.Rev.D74:074015 (2006)

Asymmetry is evaluated in COMPASS specific mean kinematic points extracted from the data.  
Good level of agreement, which allows us to use the predicted  $x$ -,  $z$ - and  $p_T$ -dependencies for the  $A_{LT}^{\cos(\varphi_S)}$ -correction.

# $A_{LT}^{\cos\varphi_S}$ corrected for $A_{LL}$ -contribution

using  $A_{LL}$  from PRD 74, 074015(2006)

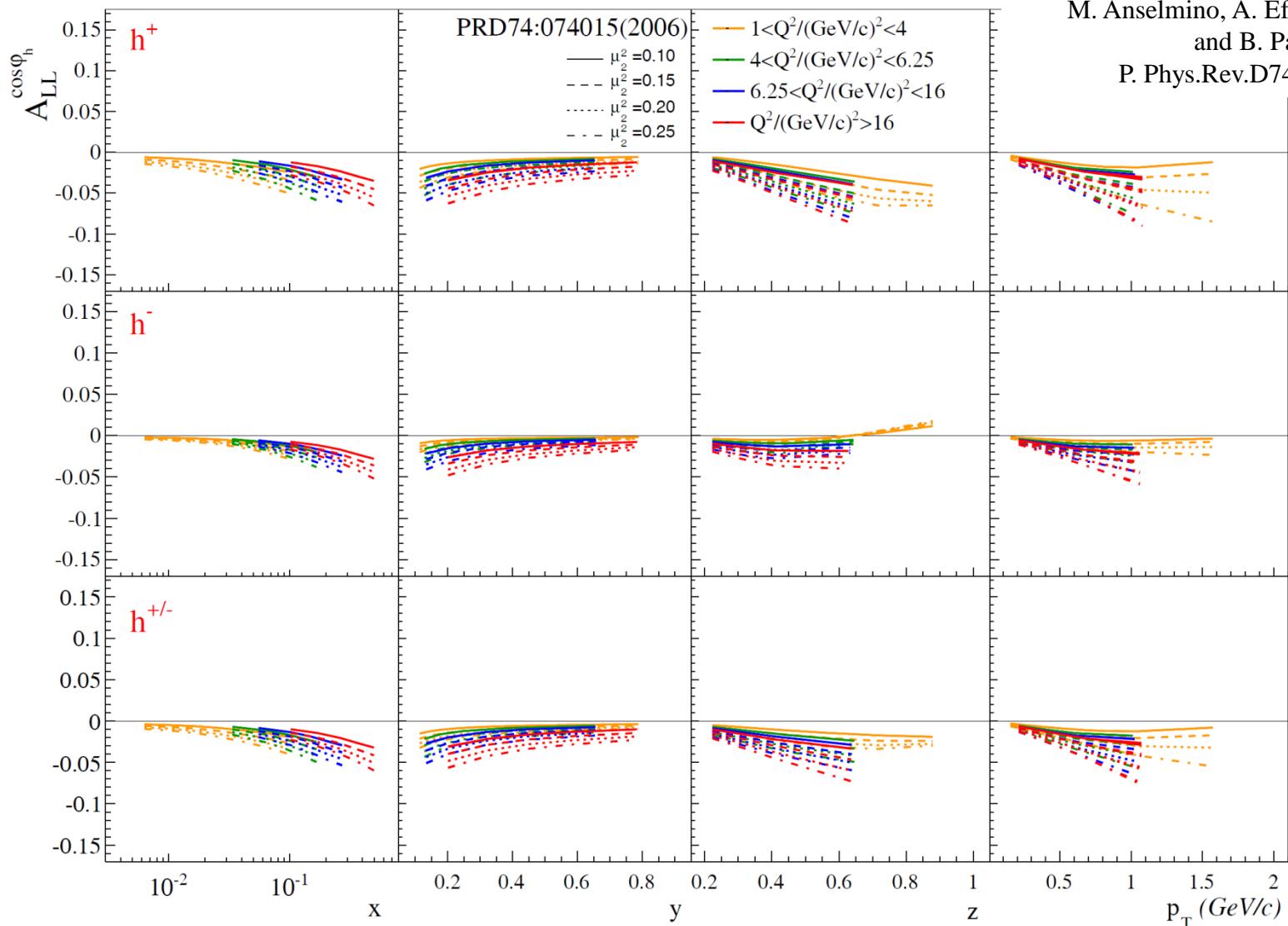
$$A_{LT, \text{observed}}^{\cos\varphi_S} \approx \left( \cos\theta A_{LT}^{\cos\varphi_S} + \sin\theta \frac{\sqrt{(1-\varepsilon^2)}}{\sqrt{2\varepsilon(1-\varepsilon)}} A_{LL} \right)$$



As expected, at large  $x$  the corrections become sizable.

# $A_{LL} \cos\varphi_h$ evaluated according to the PRD 74, 074015 (2006)

COMPASS Proton

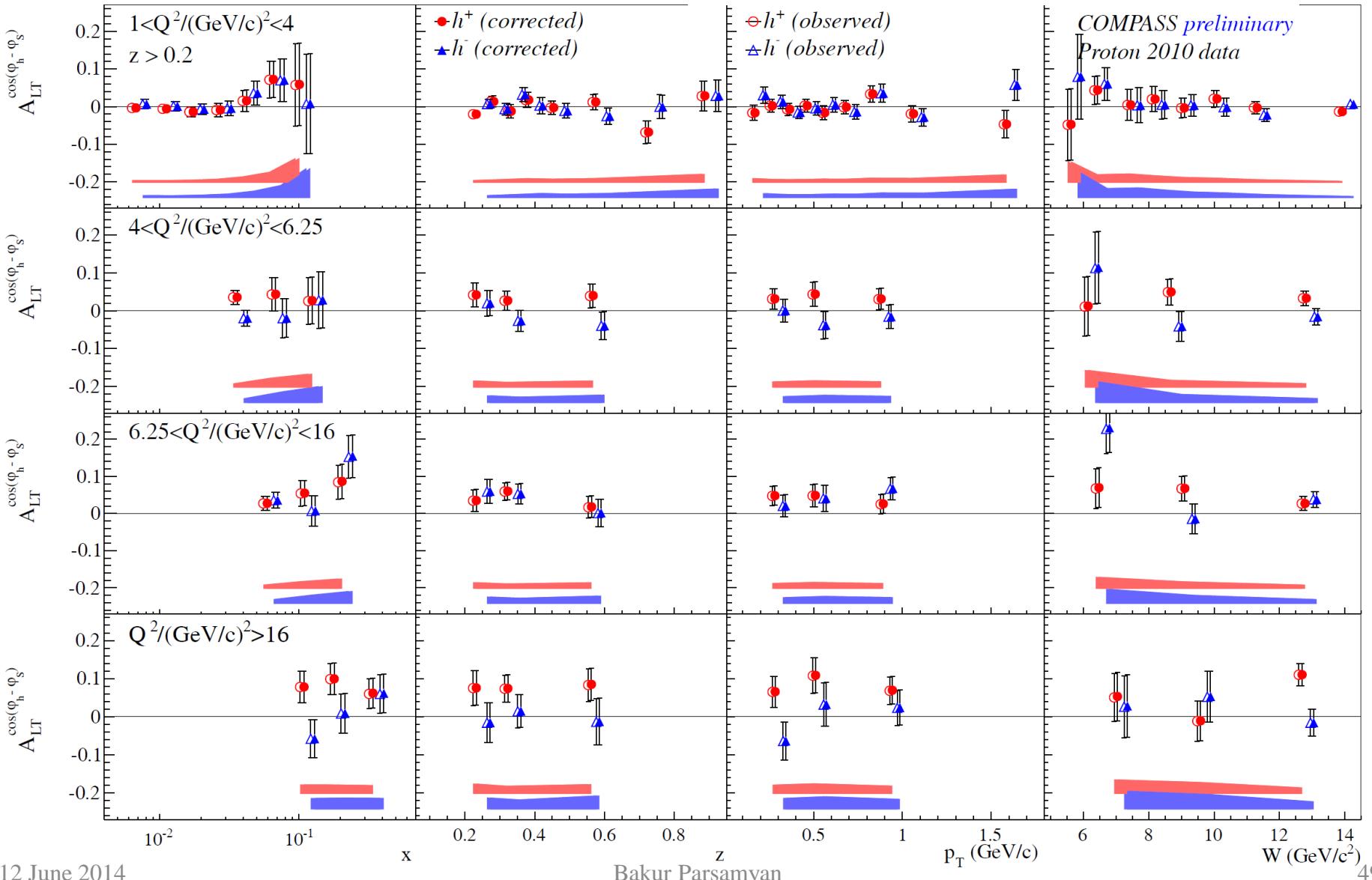


M. Anselmino, A. Efremov, A. Kotzinian,  
and B. Parsamyan  
P. Phys.Rev.D74:074015 (2006)

Asymmetry is evaluated in COMPASS specific mean kinematic points extracted from the proton data.

# $A_{LT} \cos(\phi_h - \phi_s)$ corrected for $A_{LL} \cos\phi_h$ -contribution

M. Anselmino, A. Efremov, A. Kotzinian, and B. Parsamyan  
 Phys.Rev.D74:074015 (2006)



# Outline

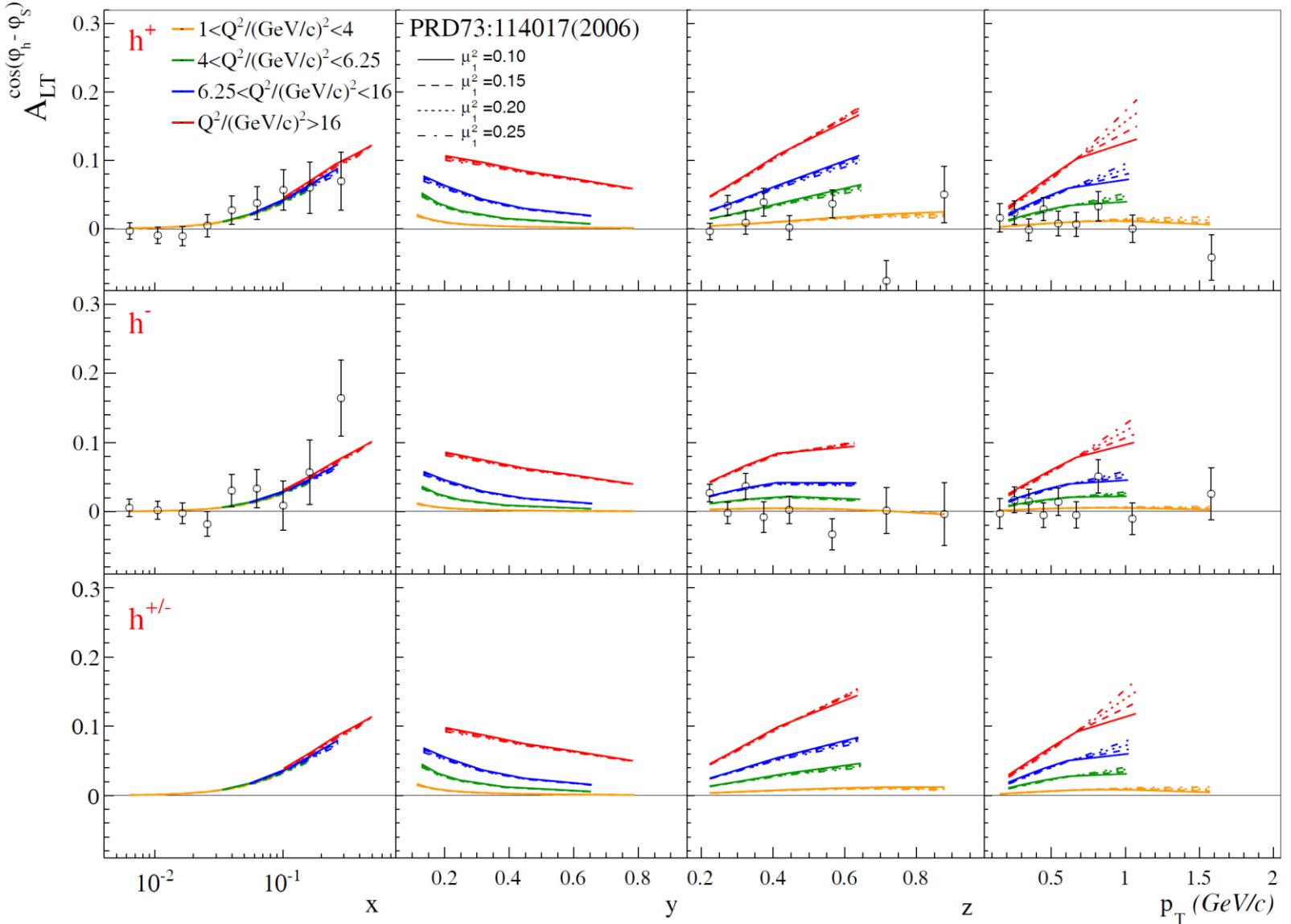
- Introduction
  - Brief review of COMPASS results with TSAs
- COMPASS – “SIDIS-DY bridge”
- **New results!**
  - Asymmetries
  - Re-evaluation of  $A_{LT}^{\cos\varphi_S}$  and  $A_{LT}^{\cos(\varphi_h - \varphi_s)}$ :  
from the  $l p$  to  $\gamma * p$  cross-section
  - $A_{LT}^{\cos(\varphi_h - \varphi_s)}$ : Comparison with predictions
  - Multi-D map of kinematical distributions
- Conclusions

# $A_{LT} \cos(\varphi_h - \varphi_s)$ in DY Q<sup>2</sup>-bins: PRD 73, 114017(2006)



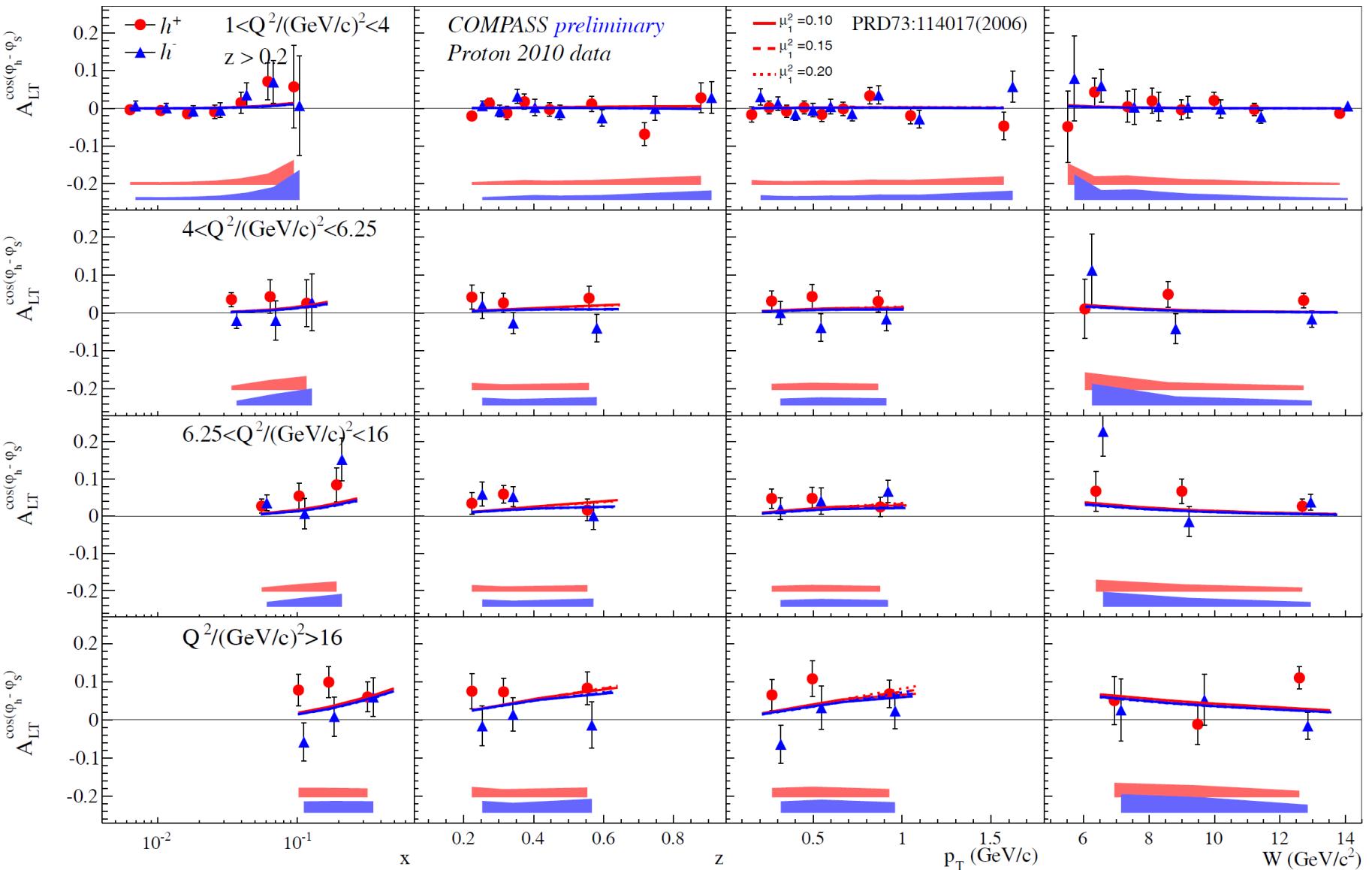
A. Kotzinian, B. Parsamyan, A. Prokudin  
Phys.Rev.D73:114017 (2006)

COMPASS Proton 2010 preliminary



# $A_{LT} \cos(\phi_h - \phi_s)$ in DY Q<sup>2</sup>-bins:

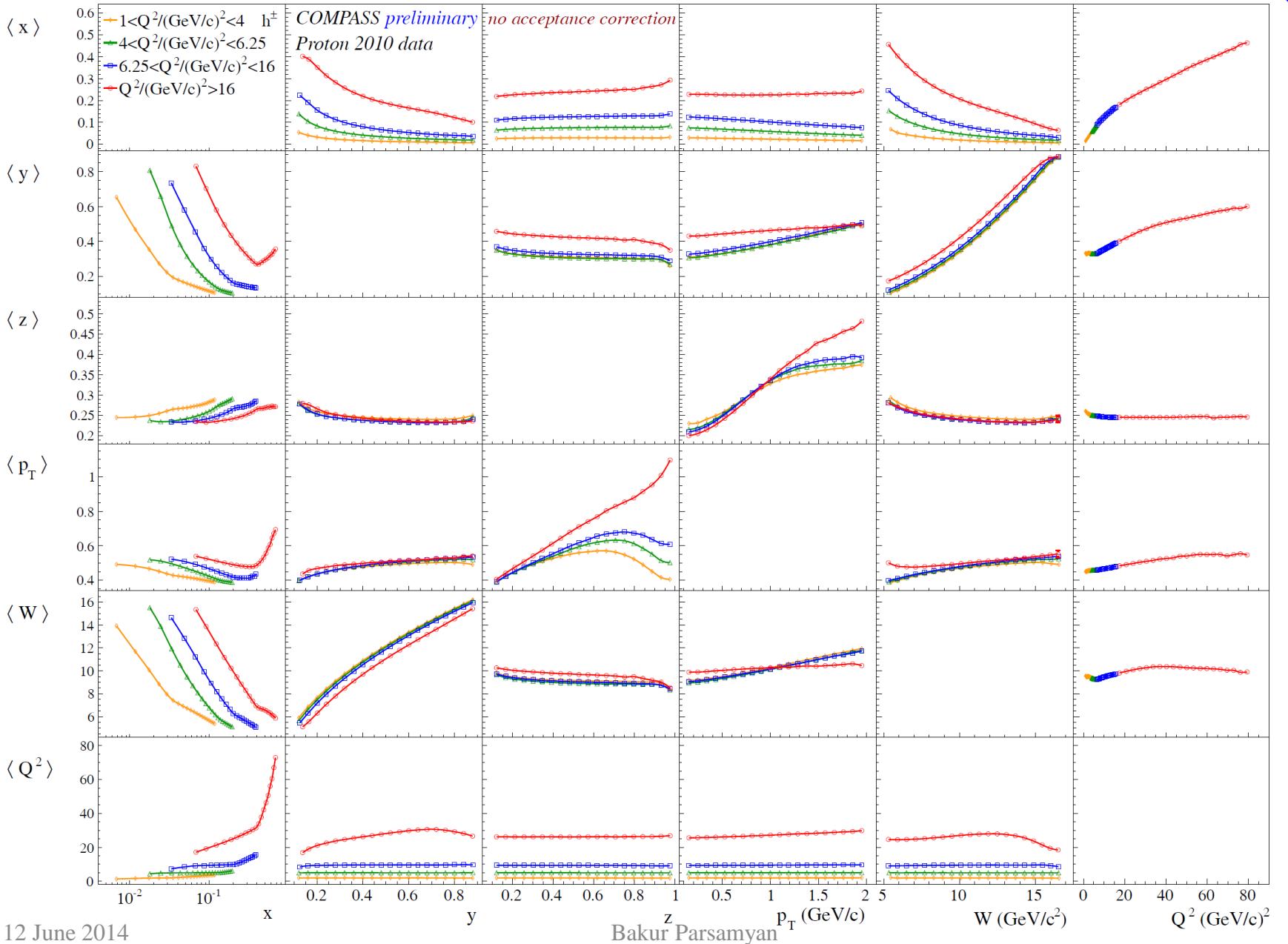
predictions i.a.w. PRD 73, 114017(2006)



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  - **Multi-D map of kinematical distributions**
- Conclusions

# Multi-D map of kinematical distributions



# Outline

- Introduction
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- New results!
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from the  $l p$  to  $\gamma * p$  cross-section
  - $A_{LT}^{\cos(\varphi_h - \varphi_S)}$ : Comparison with predictions
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# Conclusions

- First input for the future global SIDIS-DY studies is provided
  - All eight SIDIS TSAs were extracted from COMPASS proton-2010 data in four “Drell-Yan”  $Q^2$ -bins.
- Several asymmetries show a non-zero trend in different kinematical regions
  - i.e. Sivers, Collins,  $A_{LT}^{\cos(\varphi_h-\varphi_S)}$ ,  $A_{UT}^{\sin\varphi_S}$
  - Predictions for the  $A_{LT}^{\cos(\varphi_h-\varphi_S)}$  are in good agreement with the experimental results within the given statistical accuracy
- Interesting input to the “ $Q^2$ -evolution” related studies
  - Essentially, no strong  $Q^2$ - dependence observed within given statistical accuracy
- More refined multi-dimensional analysis is ongoing..! More news soon!

Thank you!

Sorry Christopher.. I did my best..!

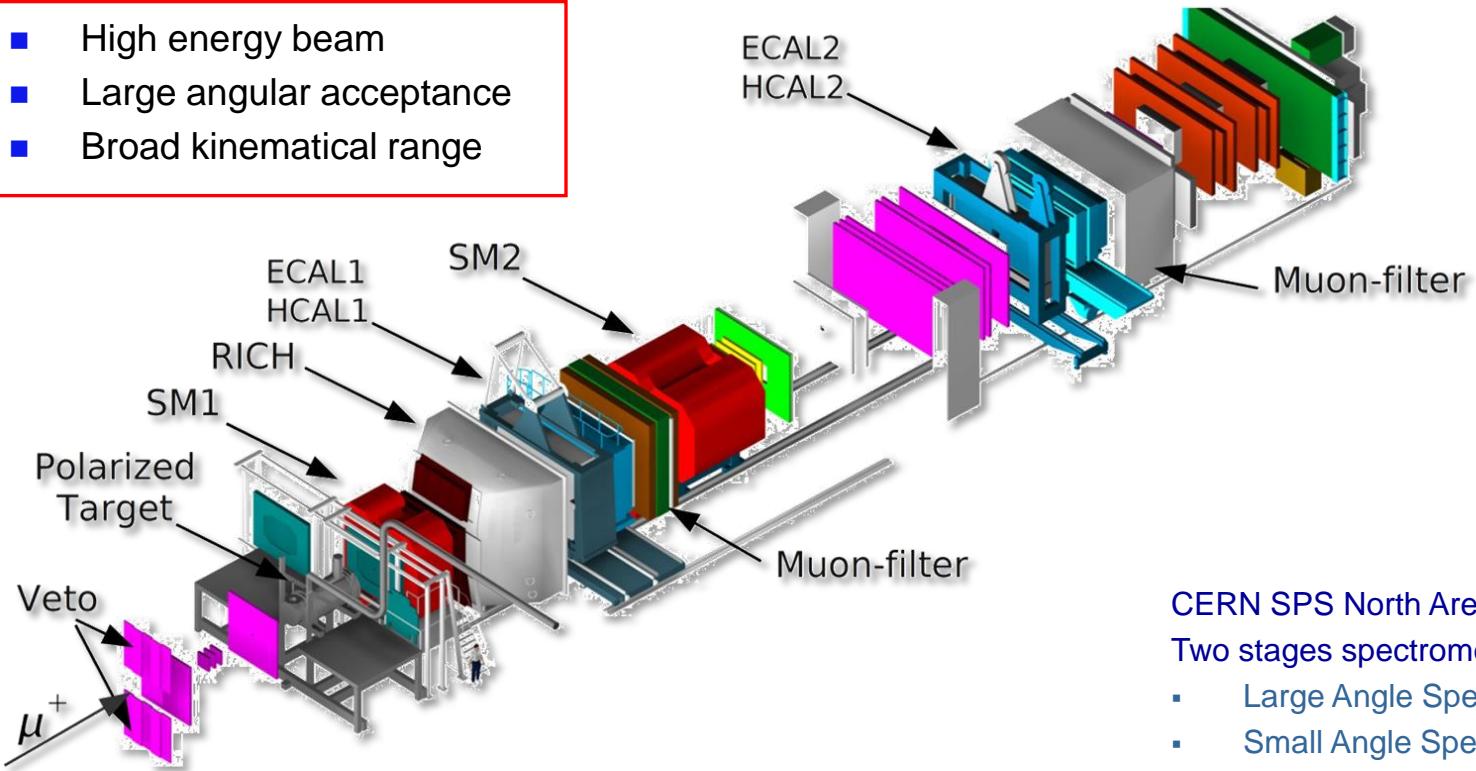


# Spare slides

# COMPASS experimental setup

## COmmon Muon Proton Apparatus for Structure and Spectroscopy

- High energy beam
- Large angular acceptance
- Broad kinematical range



**Longitudinally polarized  $\mu^+$  beam (160 GeV/c).**

**Longitudinally or Transversely polarized  ${}^6\text{LiD}$  or  $\text{NH}_3$  target**

**Momentum, tracking and calorimetric measurements, PID**

CERN SPS North Area.

Two stages spectrometer

- Large Angle Spectrometer (SM1)
- Small Angle Spectrometer (SM2)

**Hadron & Muon high energy beams.**

Beam rates:  $10^8$  muons/s,  $5 \cdot 10^7$  hadrons/s.

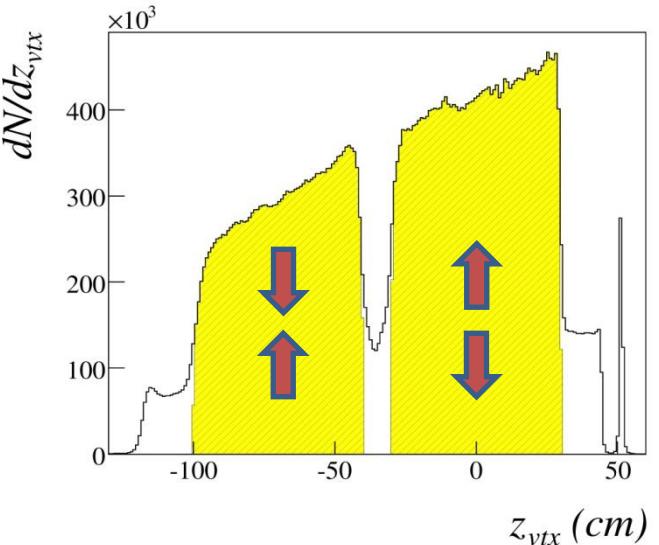
# COMPASS Polarized target system

## solid state target operated in frozen spin mode

Years 2002-2004

Deuteron -  ${}^6\text{LiD}$ :

- Two 60 cm long  ${}^6\text{LiD}$  cells with opposite polarization
- Polar angle acceptance – 70 mrad
- Target Polarization  $\pm 50\%$
- dilution factor  $f = 0.38$

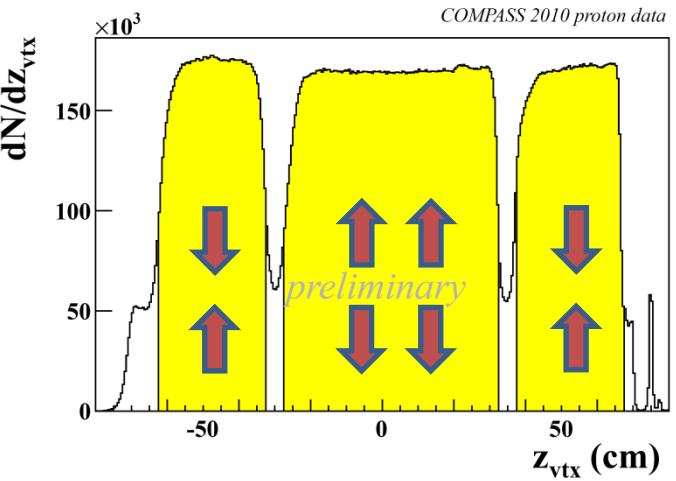


Data is collected simultaneously for the two target spin orientations  
Polarization reversal after each ~4-5 days

Years 2007 and 2010

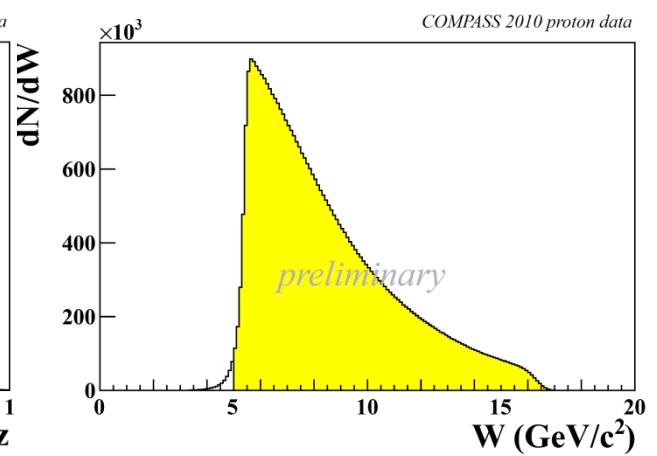
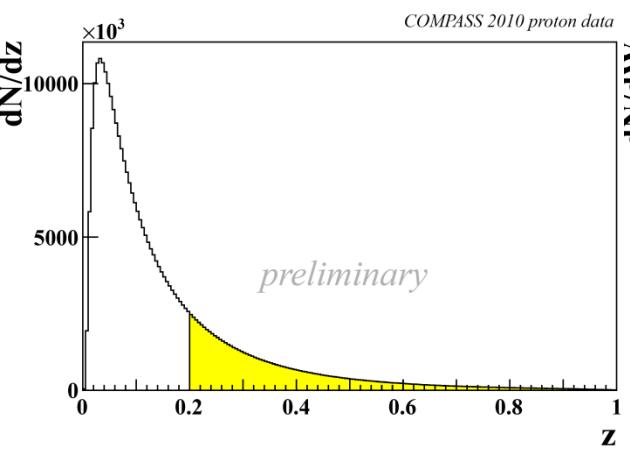
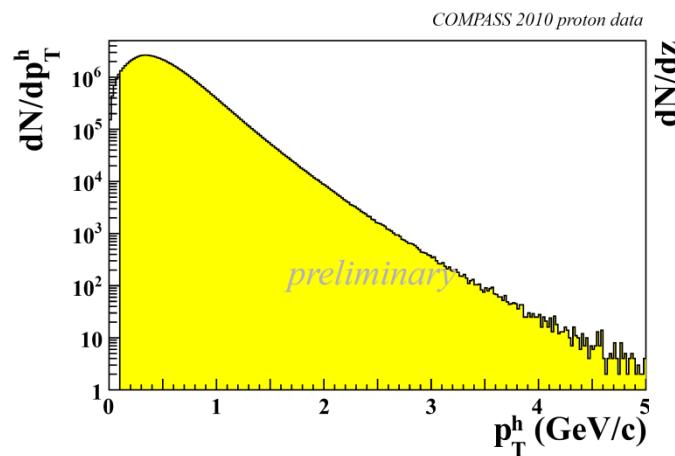
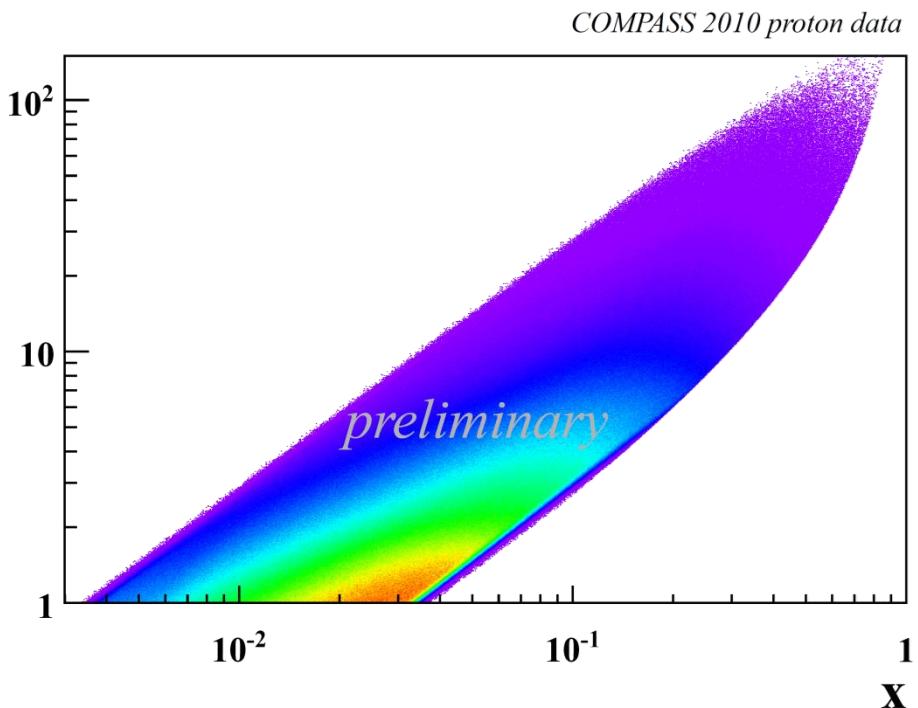
Proton -  $\text{NH}_3$ :

- Three cells system (30 cm, 60cm, 30cm)
- Polar angle acceptance – 180 mrad ( new magnet in 2006)
- Target Polarization  $\pm 90\%$
- dilution factor  $f = 0.14$



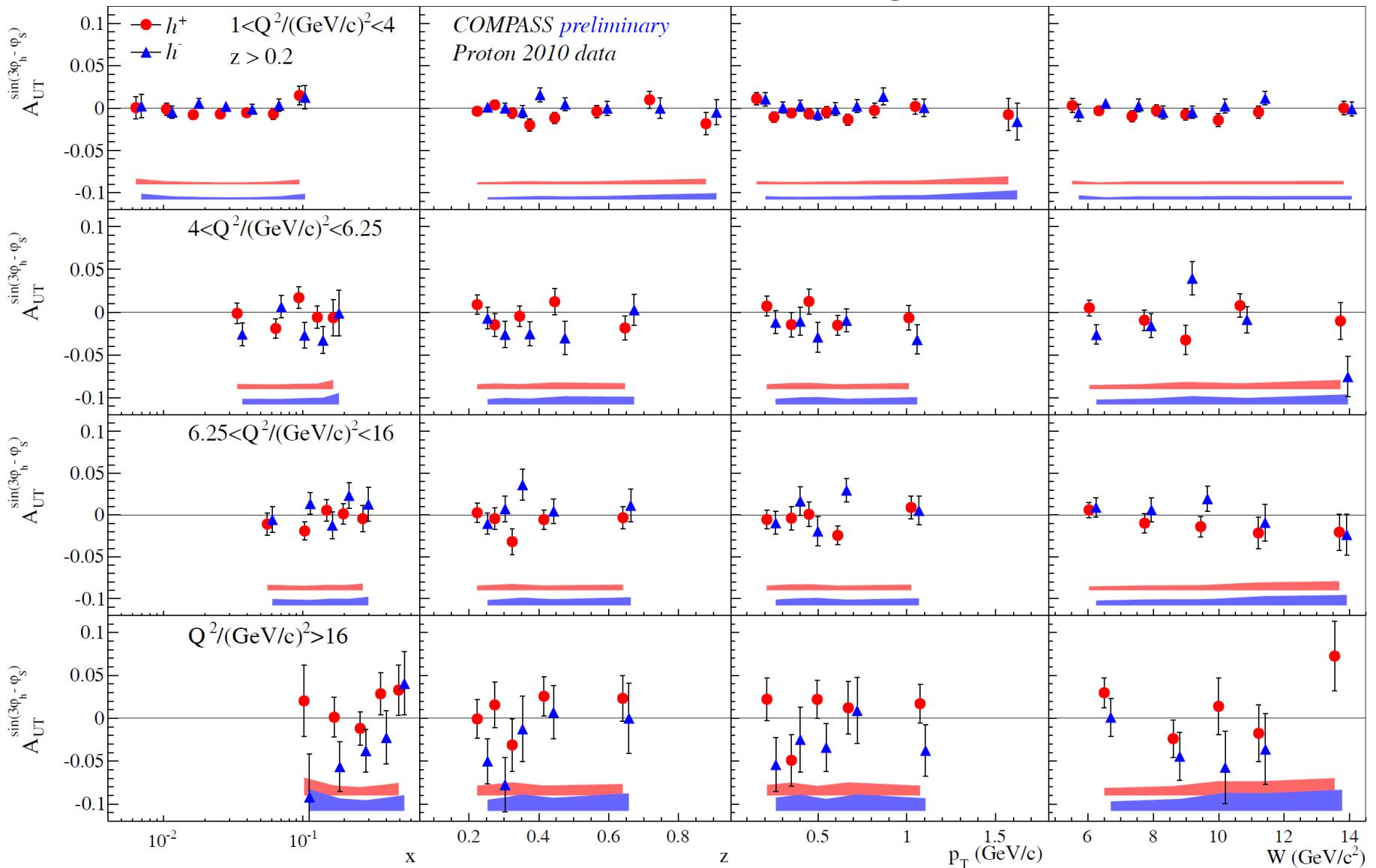
# Data selection

- DIS cuts :
  - $Q^2 > 1 \text{ GeV}^2$
  - $0.1 < y < 0.9$
  - $W > 5 \text{ GeV}$
  
- Hadron cuts :
  - $z > 0.2$
  - $P_{hT} > 0.1 \text{ GeV}/c$



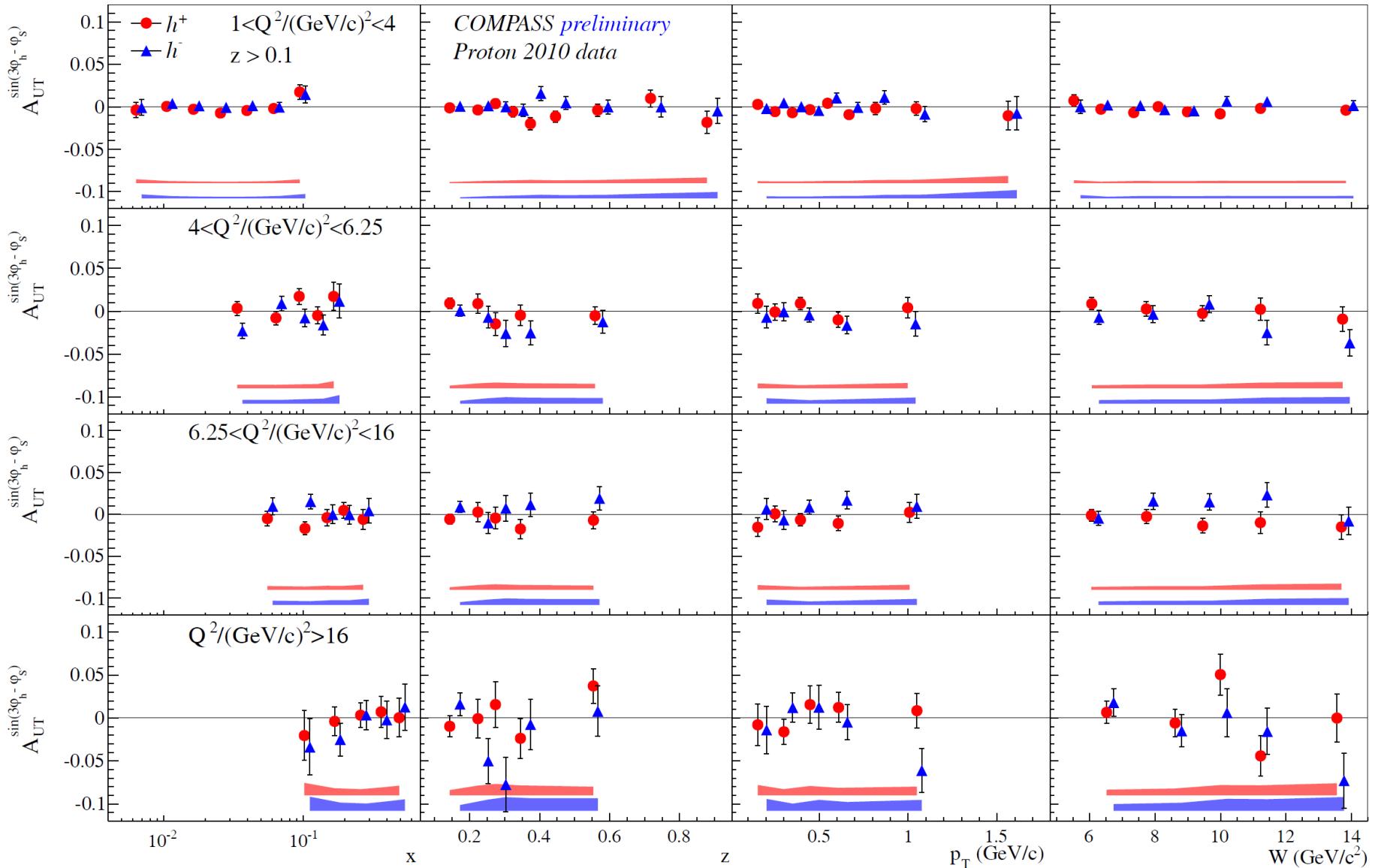
# $A_{UT} \sin(3\phi_h - \phi_s)$ in DY-ranges: $z > 0.2$

**NEW!** These results are being shown for the first time



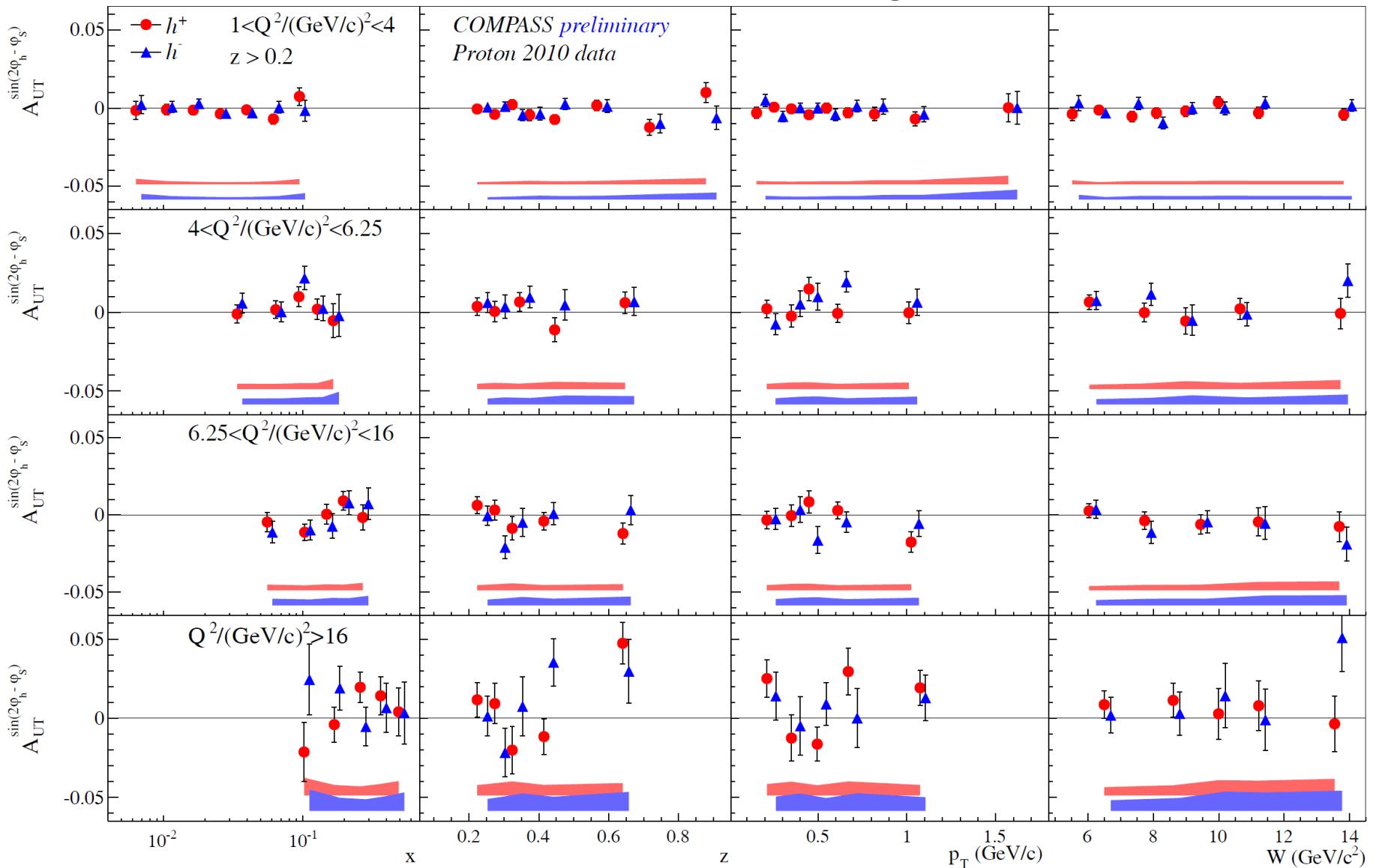
# $A_{UT} \sin(3\phi_h - \phi_s)$ in DY-ranges: $z > 0.1$

**NEW!** These results are being shown for the first time



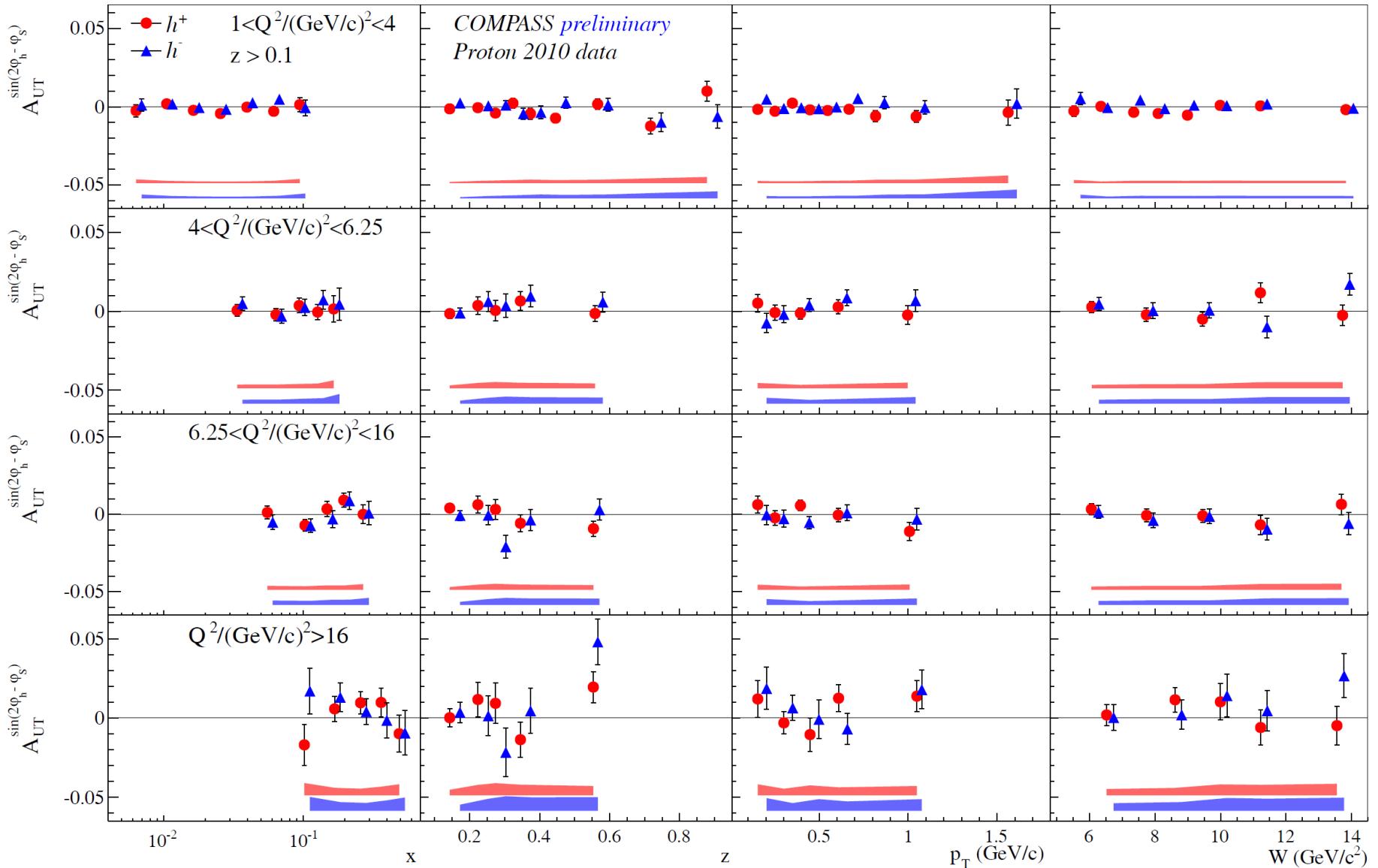
# $A_{UT} \sin(2\phi_h - \phi_s)$ in DY-ranges: $z > 0.2$

**NEW!** These results are being shown for the first time



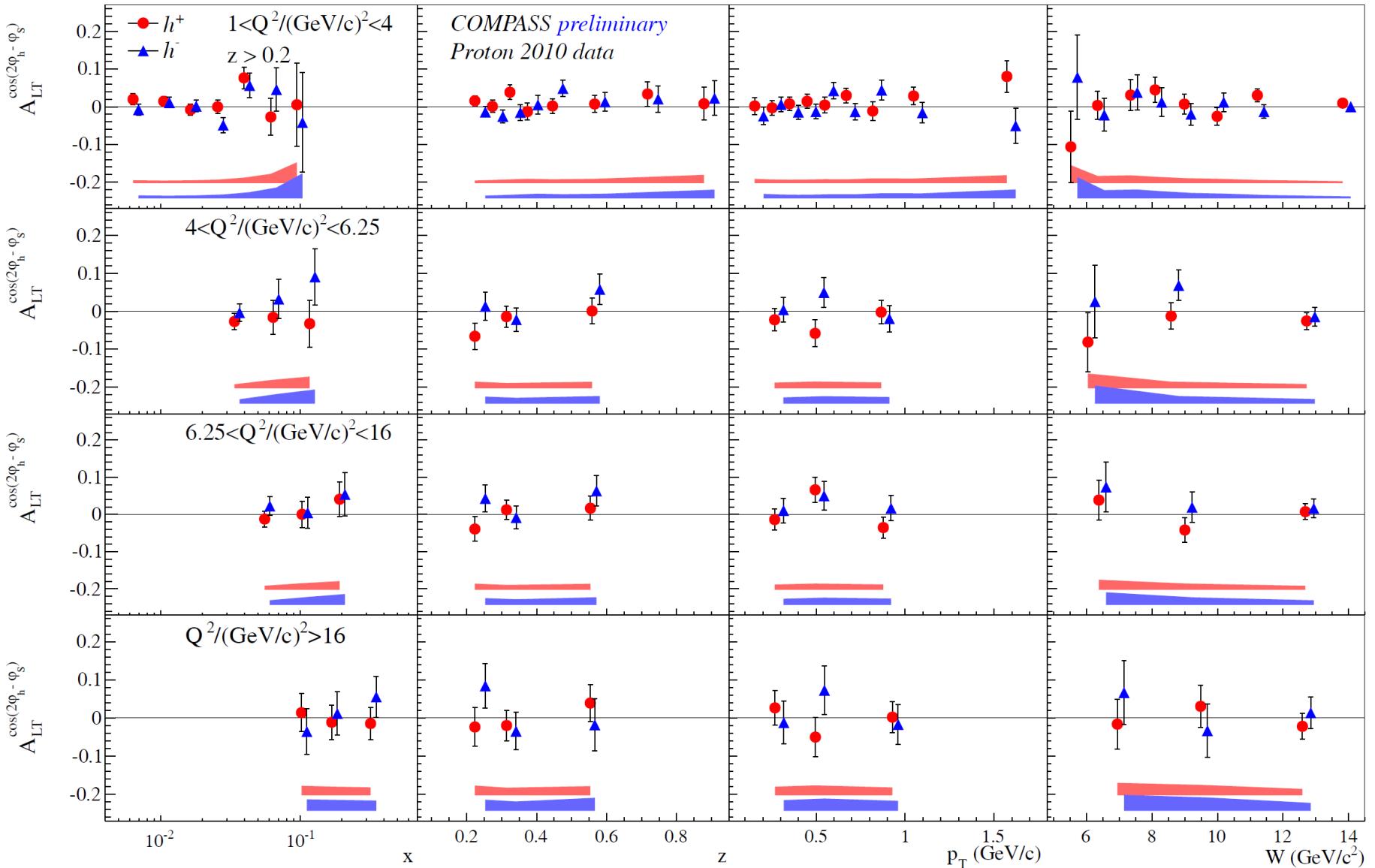
# $A_{UT} \sin(2\phi_h - \phi_s)$ in DY-ranges: $z > 0.1$

**NEW!** These results are being shown for the first time



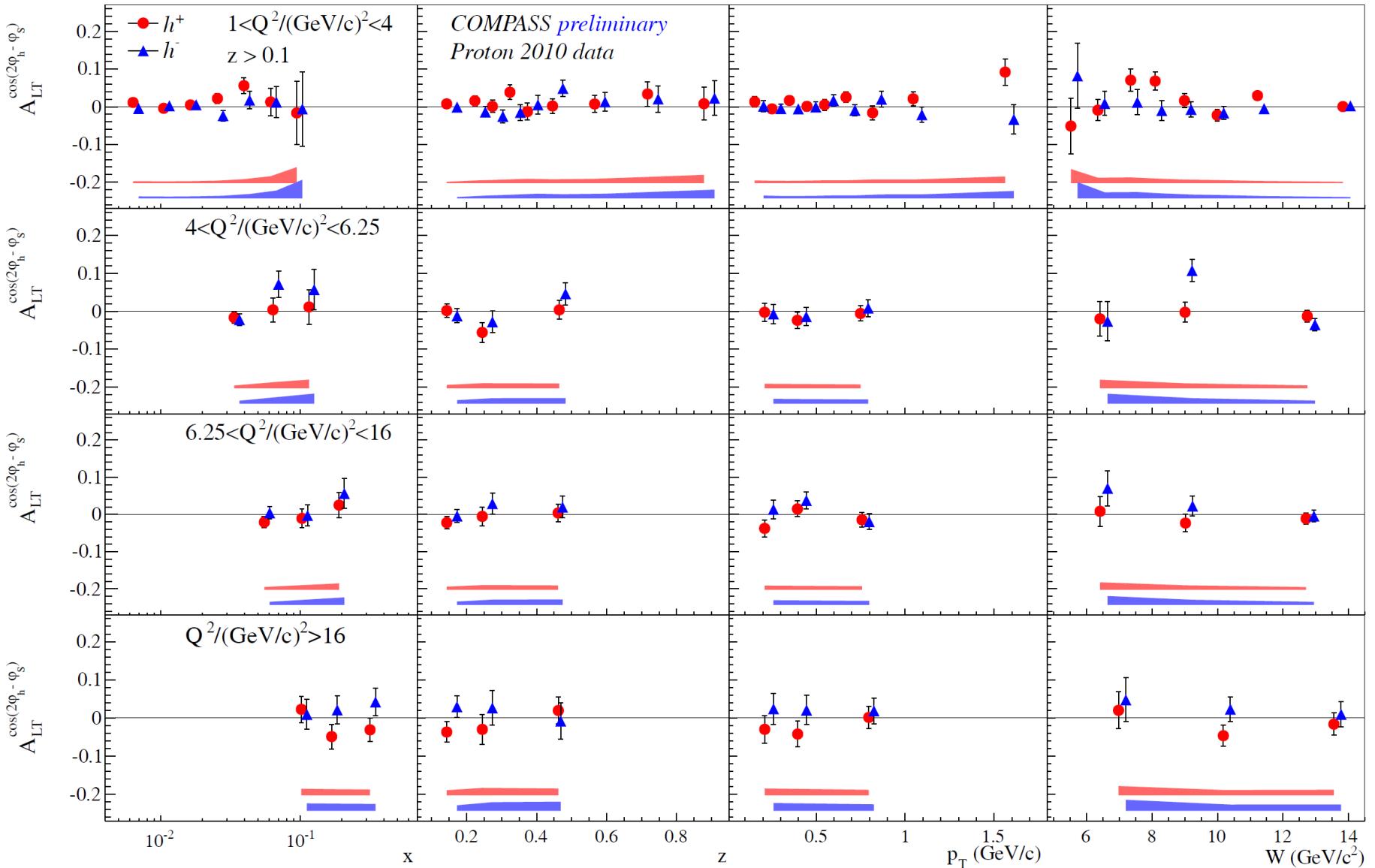
# $A_{LT} \cos(2\phi_h - \phi_s)$ in DY-ranges: $z > 0.2$

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# $A_{LT} \cos(2\phi_h - \phi_s)$ in DY-ranges: $z > 0.1$

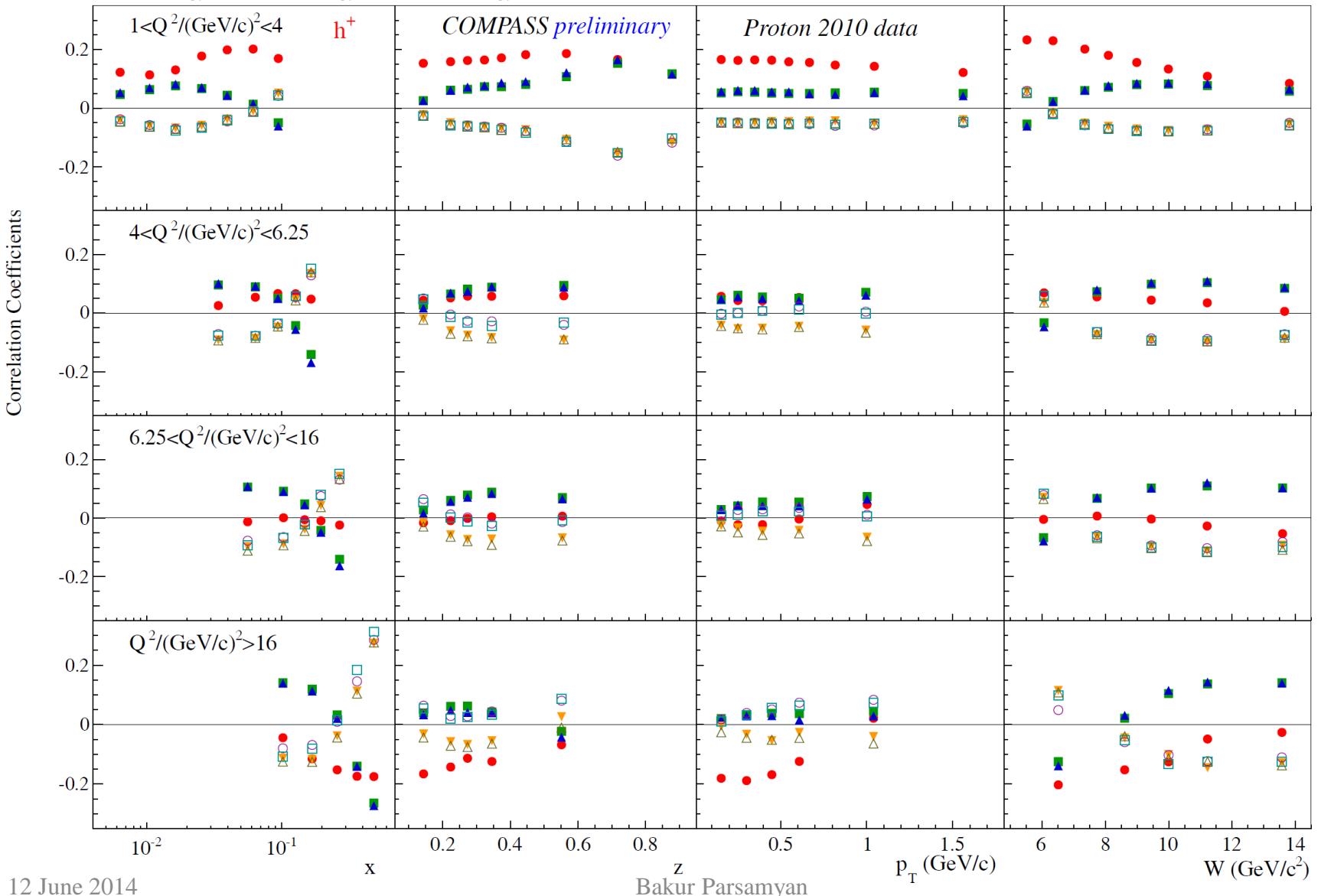
**NEW!** These results are being shown for the first time



# Correlation Coefficients

Legend:

- $\textcolor{red}{\bullet} A_{\text{UT}}^{\sin(\phi_h + \phi_s - \pi)}, A_{\text{UT}}^{\sin(\phi_h - \phi_s)}$
- $\textcolor{blue}{\triangle} A_{\text{UT}}^{\sin(\phi_h - \phi_s)}, A_{\text{UT}}^{\sin\phi_s}$
- $\textcolor{violet}{\circ} A_{\text{UT}}^{\cos(\phi_h - \phi_s)}, A_{\text{UT}}^{\cos\phi_s}$
- $\textcolor{brown}{\triangle} A_{\text{UT}}^{\sin(3\phi_h - \phi_s)}, A_{\text{UT}}^{\sin(2\phi_h - \phi_s)}$
- $\textcolor{green}{\blacksquare} A_{\text{UT}}^{\sin(\phi_h + \phi_s - \pi)}, A_{\text{UT}}^{\sin\phi_s}$
- $\textcolor{orange}{\triangledown} A_{\text{UT}}^{\sin(\phi_h - \phi_s)}, A_{\text{UT}}^{\sin(2\phi_h - \phi_s)}$
- $\textcolor{teal}{\square} A_{\text{UT}}^{\cos(\phi_h - \phi_s)}, A_{\text{UT}}^{\cos(2\phi_h - \phi_s)}$



# SIDIS x-section: from $lp$ to $\gamma * p$ ( $P_L=0$ )

$$\frac{d\sigma}{dx dy dz dP_{hT}^2 d\varphi_h d\varphi_s} = \left[ \frac{\cos \theta}{1 - \sin^2 \theta \sin^2 \varphi_s} \right] \times \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] \times (F_{UU,T} + \varepsilon F_{UU,L}) \times$$

$$1 + \cos \varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\varphi_h)} + \lambda \sin \varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \varphi_h} +$$

$$\sin \varphi_s \times (\cos \theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \varphi_s}) +$$

$$\sin(\varphi_h - \varphi_s) \times \left( \cos \theta A_{UT}^{\sin(\varphi_h - \varphi_s)} + \frac{1}{2} \sin \theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin \varphi_h} \right) +$$

$$\sin(\varphi_h + \varphi_s) \times \left( \cos \theta \varepsilon A_{UT}^{\sin(\varphi_h + \varphi_s)} + \frac{1}{2} \sin \theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin \varphi_h} \right) +$$

$$\sin(2\varphi_h - \varphi_s) \times \left( \cos \theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_s)} + \frac{1}{2} \sin \theta \varepsilon A_{UL}^{\sin 2\varphi_h} \right) +$$

$$\sin(3\varphi_h - \varphi_s) \times (\cos \theta \varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_s)}) +$$

$$\sin(2\varphi_h + \varphi_s) \times \left( \frac{1}{2} \sin \theta \varepsilon A_{UL}^{\sin 2\varphi_h} \right)$$

$$\cos \varphi_s \times \left( \cos \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_s} + \sin \theta \sqrt{(1-\varepsilon^2)} A_{LL} \right) +$$

$$\cos(\varphi_h - \varphi_s) \times \left( \cos \theta \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_s)} + \frac{1}{2} \sin \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos \varphi_h} \right) +$$

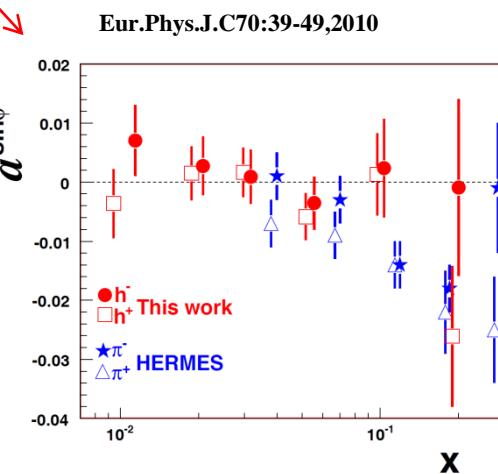
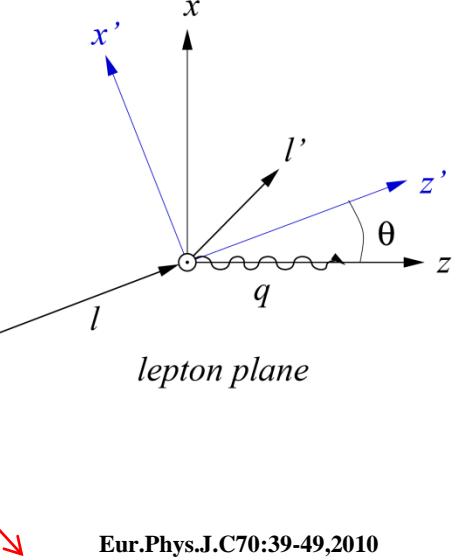
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Kotzinian et al.

hep-ph/9808368 (1998)

hep-ph/9908466 (1999)

**M. Diehl and S. Sapeta,**  
**Eur. Phys. J. C 41 (2005) 515**


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$$\sin(2\varphi_h - \varphi_s) \times \left( \cos \theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_s)} + \frac{1}{2} \sin \theta \varepsilon A_{UL}^{\sin 2\varphi_h} \right) +$$

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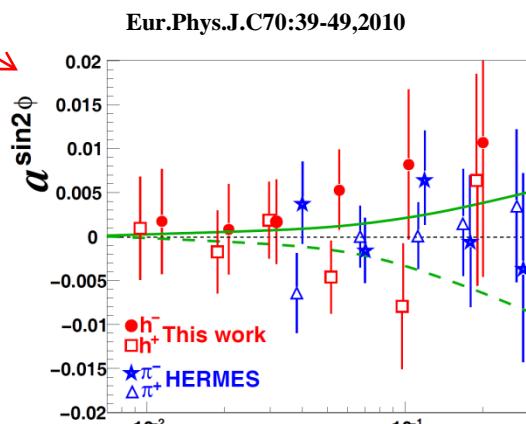
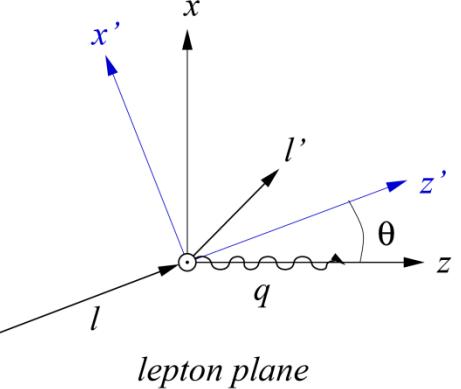
$$\cos \varphi_s \times \left( \cos \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_s} + \sin \theta \sqrt{(1-\varepsilon^2)} A_{LL} \right) +$$

$$\cos(\varphi_h - \varphi_s) \times \left( \cos \theta \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_s)} + \frac{1}{2} \sin \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos \varphi_h} \right) +$$

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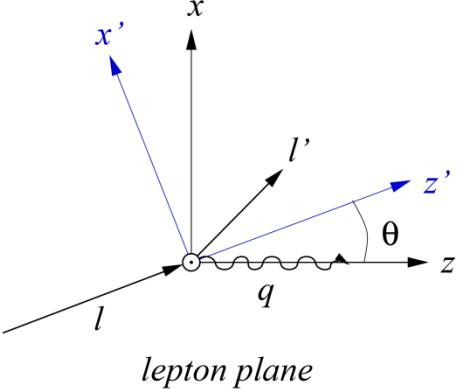


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$$\left[ \cos \varphi_s \times \left( \cos \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_s} + \sin \theta \sqrt{(1-\varepsilon^2)} A_{LL} \right) + \right. \\ \left. \cos(\varphi_h - \varphi_s) \times \left( \cos \theta \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_s)} + \frac{1}{2} \sin \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos \varphi_h} \right) + \right. \\ \left. \cos(2\varphi_h - \varphi_s) \times \left( \cos \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_s)} \right) + \right. \\ \left. \cos(\varphi_h + \varphi_s) \times \left( \frac{1}{2} \sin \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos \varphi_h} \right) \right]$$



Eur.Phys.J.C70:39-49,2010

