

# Transverse Spin Effects in MC Generators

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- **Sivers and Cahn effects in MC generators**
  - mLEPTO
  - mPYTHIA
- Collins effect in fragmentation

# Initial quark $k_T$ in MC generators PYTHIA and LEPTO

- Generate virtual photon – quark scattering in collinear configuration:

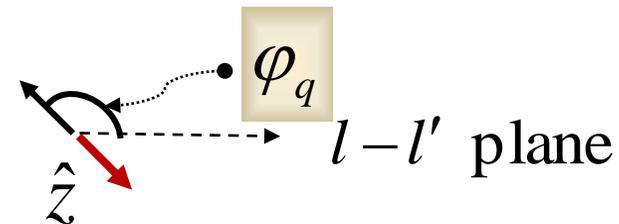


- Generate intrinsic transverse momentum of quark (Gaussian  $k_T$ )



- Generate **uniform** azimuthal distribution of quark

- Rotate around virtual photon



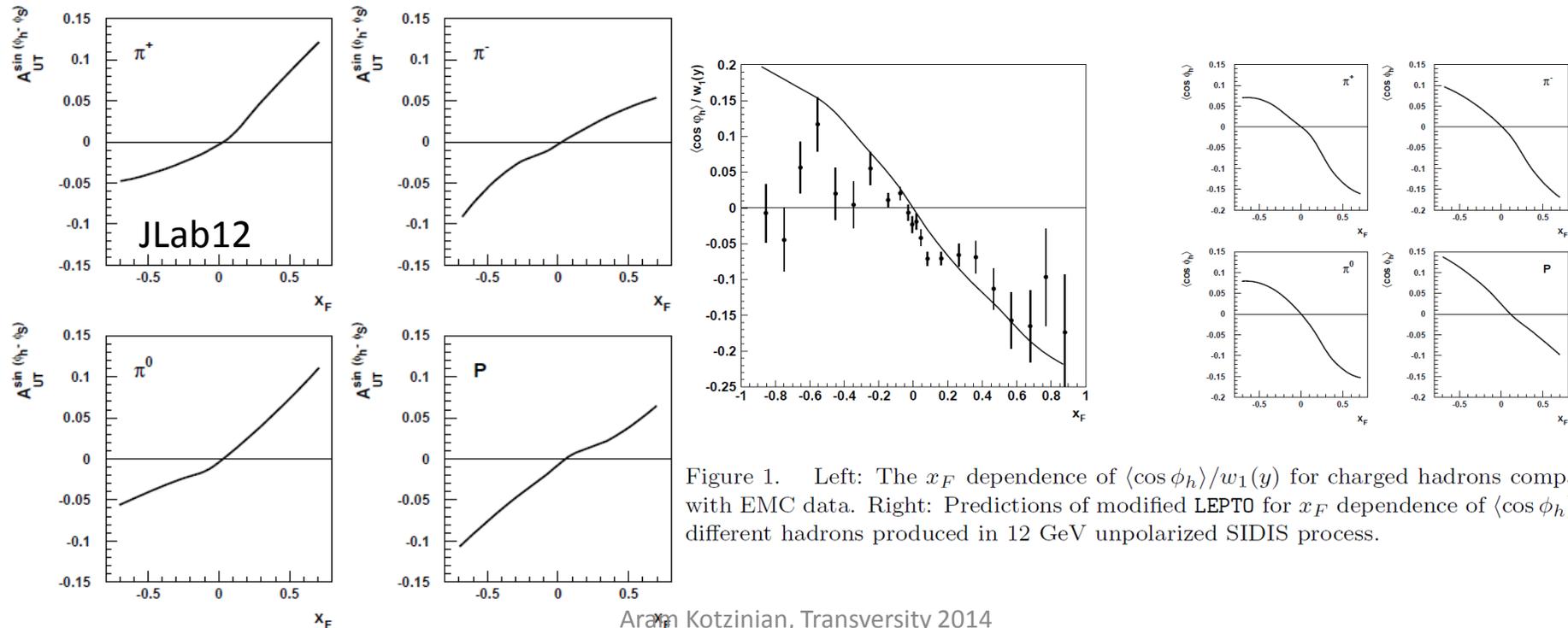
mLEPTO – modified LEPTO, includes Sivers modulation of the quark intrinsic transverse momentum in the transversely polarized nucleon

A.K. hep-ph/0504081, 0510359

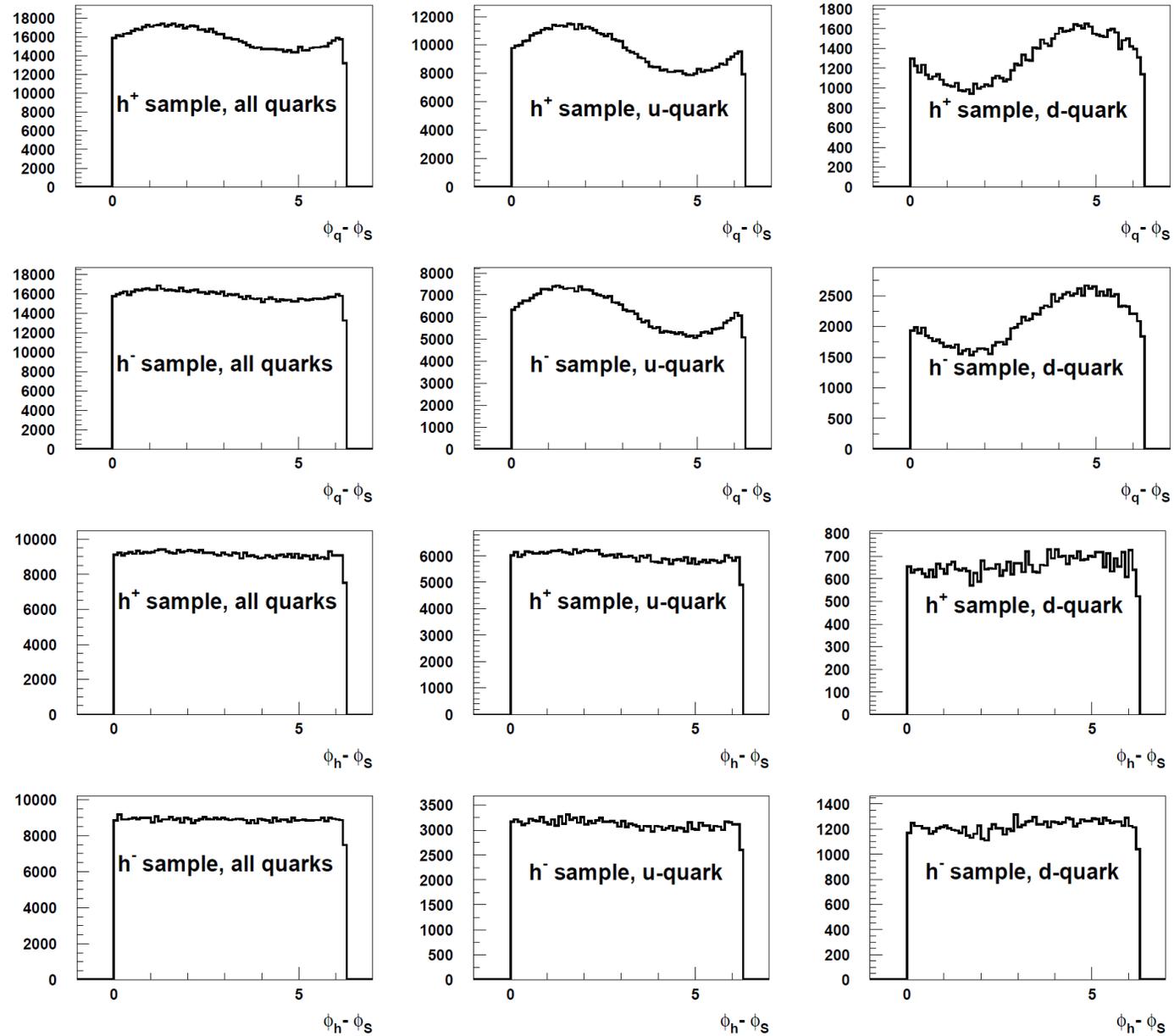
## Generate initial quark azimuth according

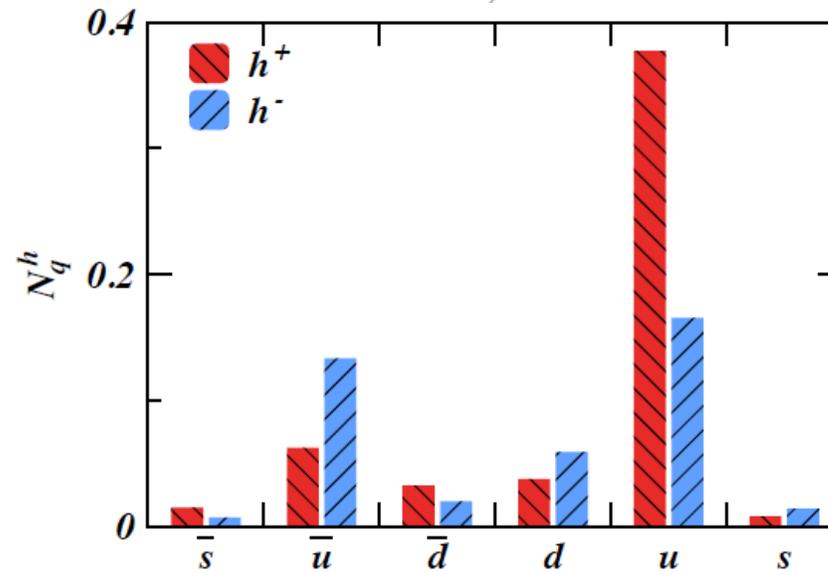
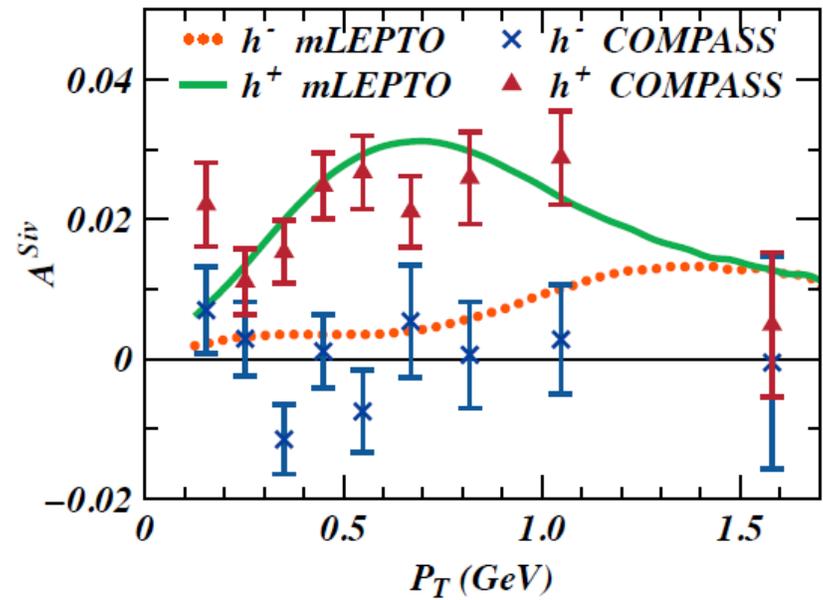
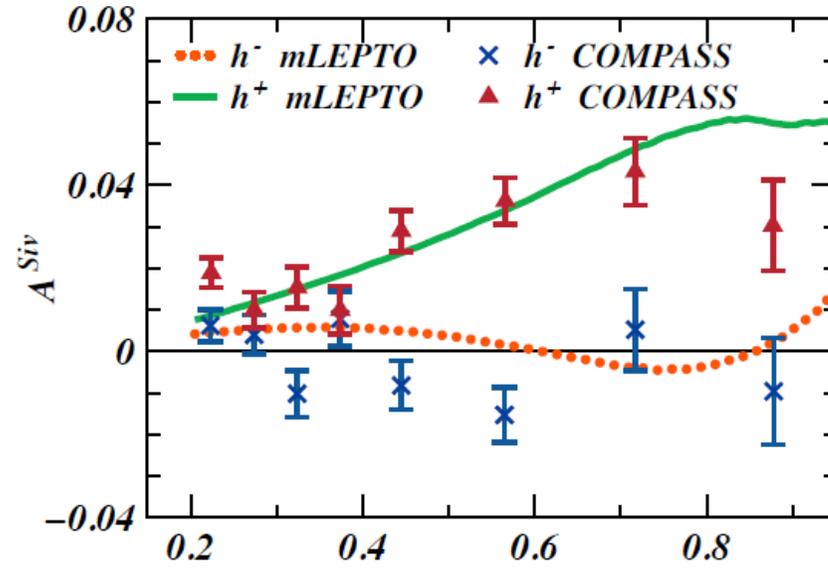
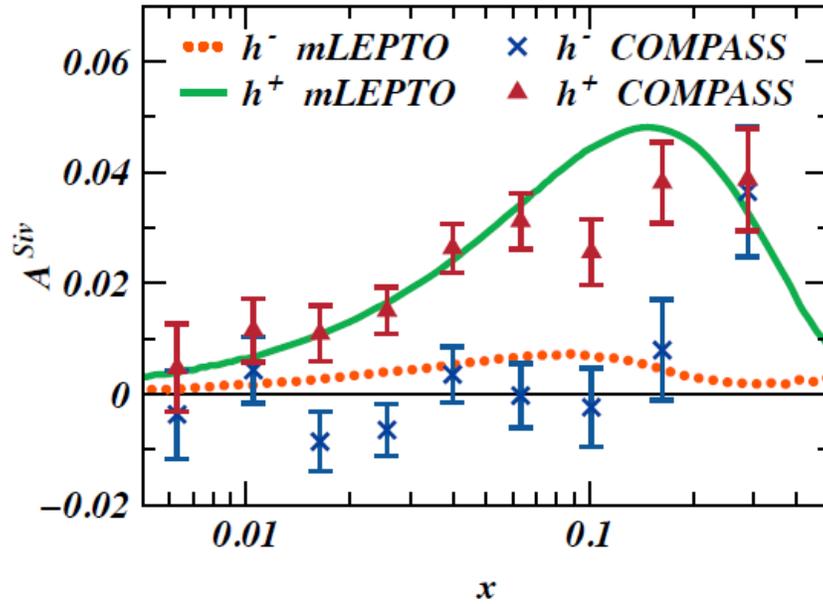
$$1 + |S_T| \frac{f_{1T}^\perp(x, k_T)}{f_1(x, k_T)} \frac{k_T}{M} \sin(\phi_q - \phi_S)$$

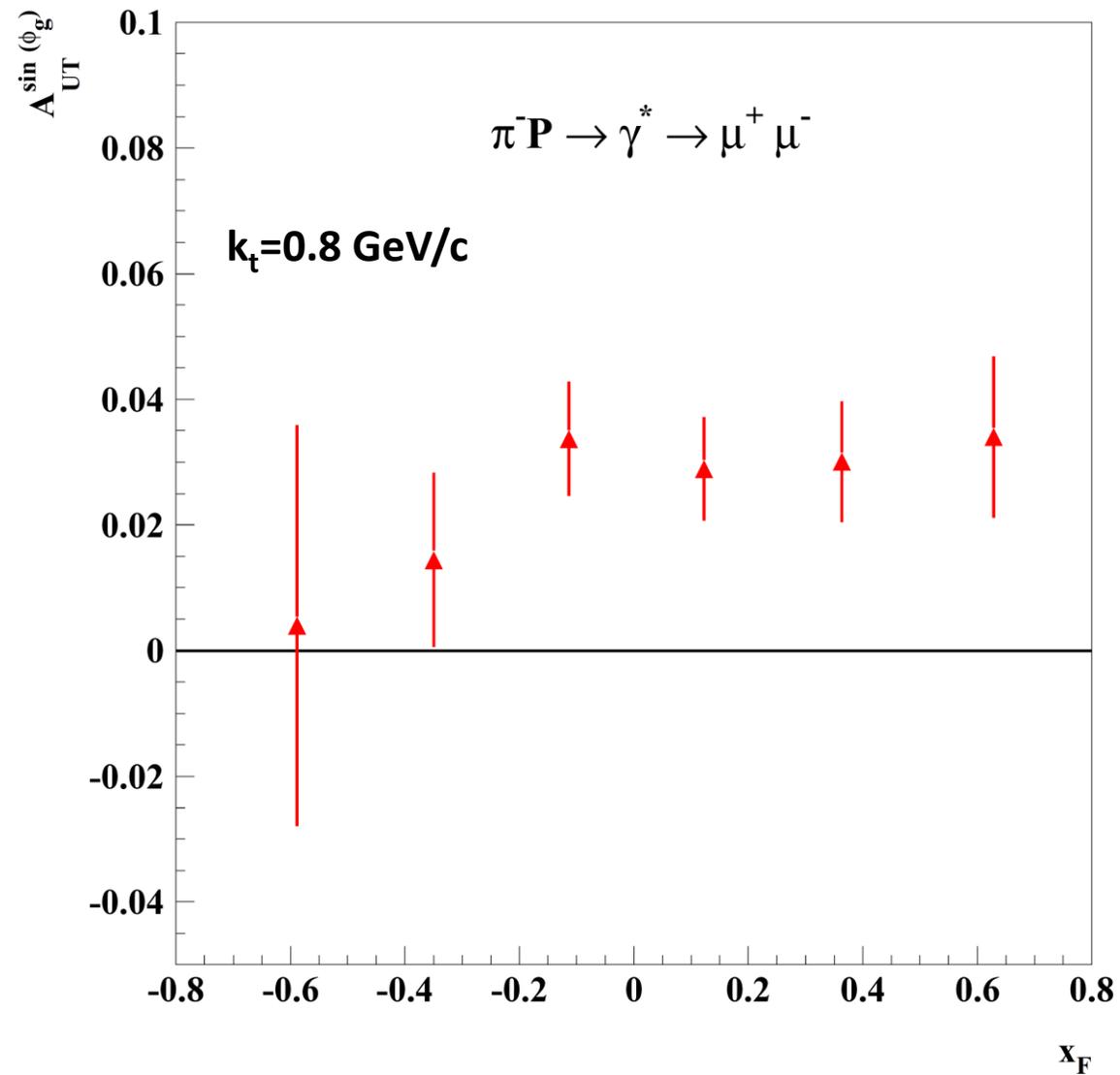
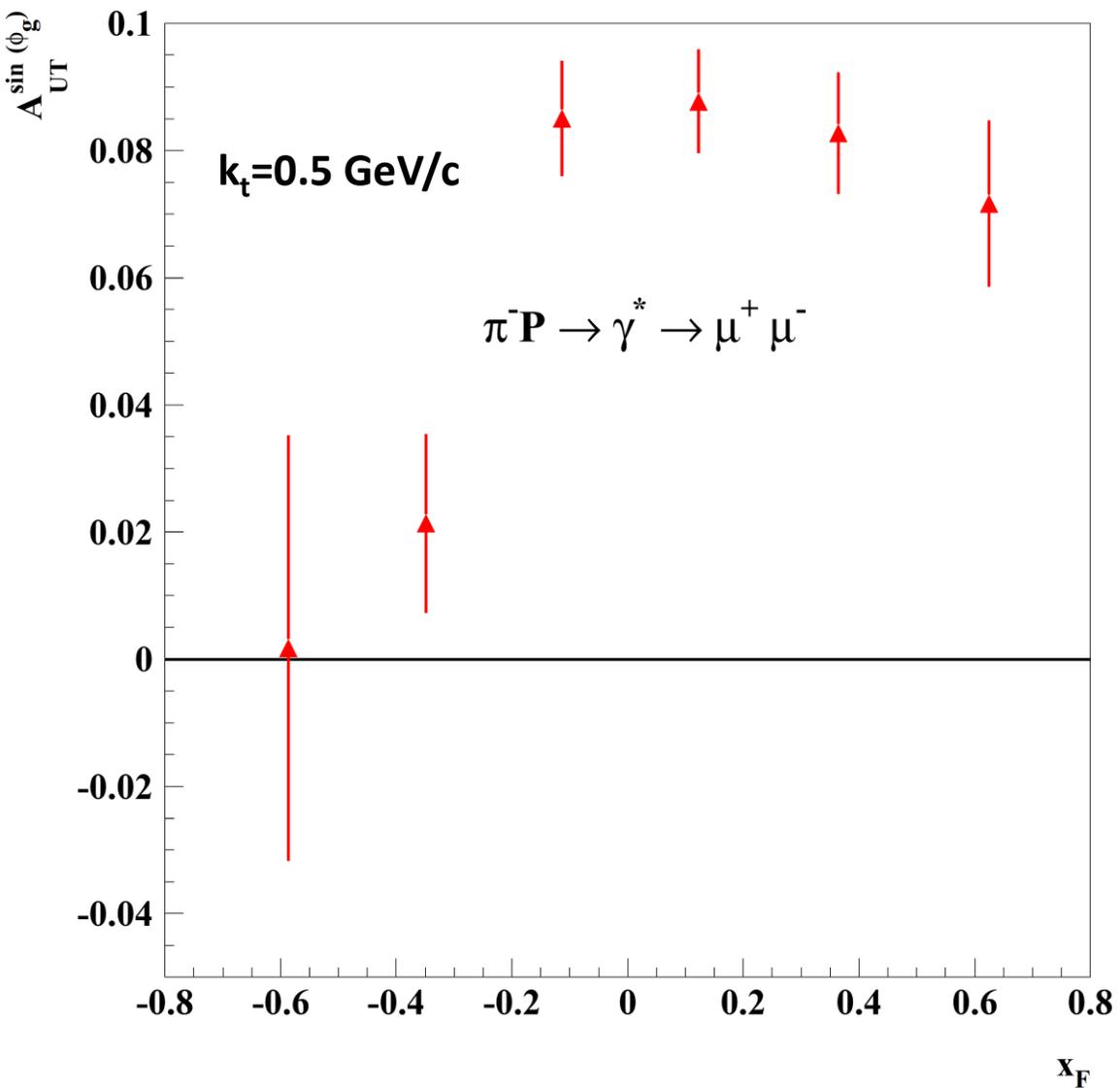
No 1/Q suppression for Sivers effect



# Quark Sivers angle distribution







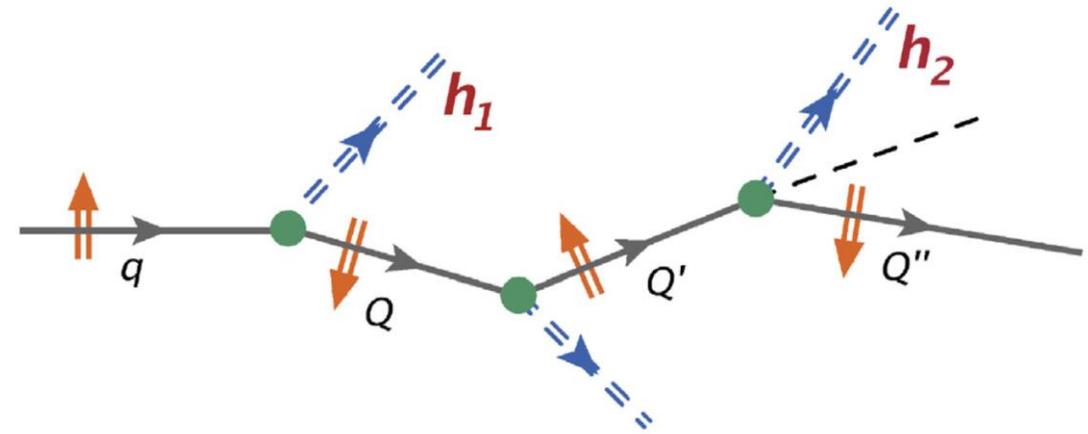
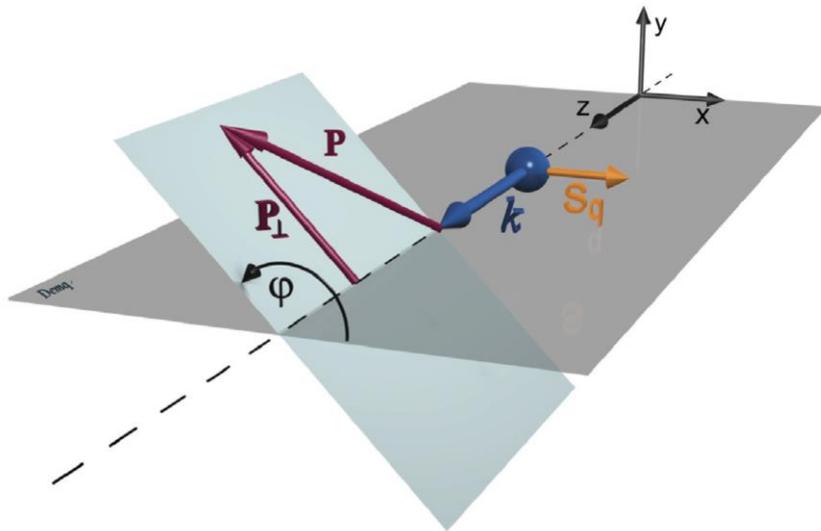
# Transversely polarized quark fragmentation (Collins effect)

H.H. Matevosyan, A.W. Thomas, W. Bentz,

Collins fragmentation function within NJL-jet model, PRD86 (2012) 034025.

H.H. Matevosyan, A.K., A.W. Thomas,

Studies of azimuthal modulations in two hadron fragmentation of a transversely polarized quark, PLB 731 (2014) 208



# Elementary Collins effect in the string fragmentation

H.H. Matevosyan , AK, A.W. Thomas, PLB 731 (2014) 208

$$\begin{aligned}
 &= \hat{D}_1 \otimes \hat{D}_2 \otimes \hat{D}_3 \otimes \hat{D}_4 + \hat{H}_1 \otimes \hat{D}_2 \otimes \hat{D}_3 \otimes \hat{D}_4 + \hat{D}_1 \otimes \hat{H}_2 \otimes \hat{D}_3 \otimes \hat{D}_4 + \\
 &+ \hat{D}_1 \otimes \hat{D}_2 \otimes \hat{H}_3 \otimes \hat{D}_4 + \hat{D}_1 \otimes \hat{D}_2 \otimes \hat{D}_3 \otimes \hat{H}_4
 \end{aligned}$$

$$\begin{aligned}
 d_{h/q\uparrow}(z, p_{\perp}^2, \varphi) &= \\
 &= d_{h/q}(z, p_{\perp}^2) - h_{h/q}(z, p_{\perp}^2) \frac{p_{\perp} s_q}{zm} \sin(\varphi)
 \end{aligned}$$

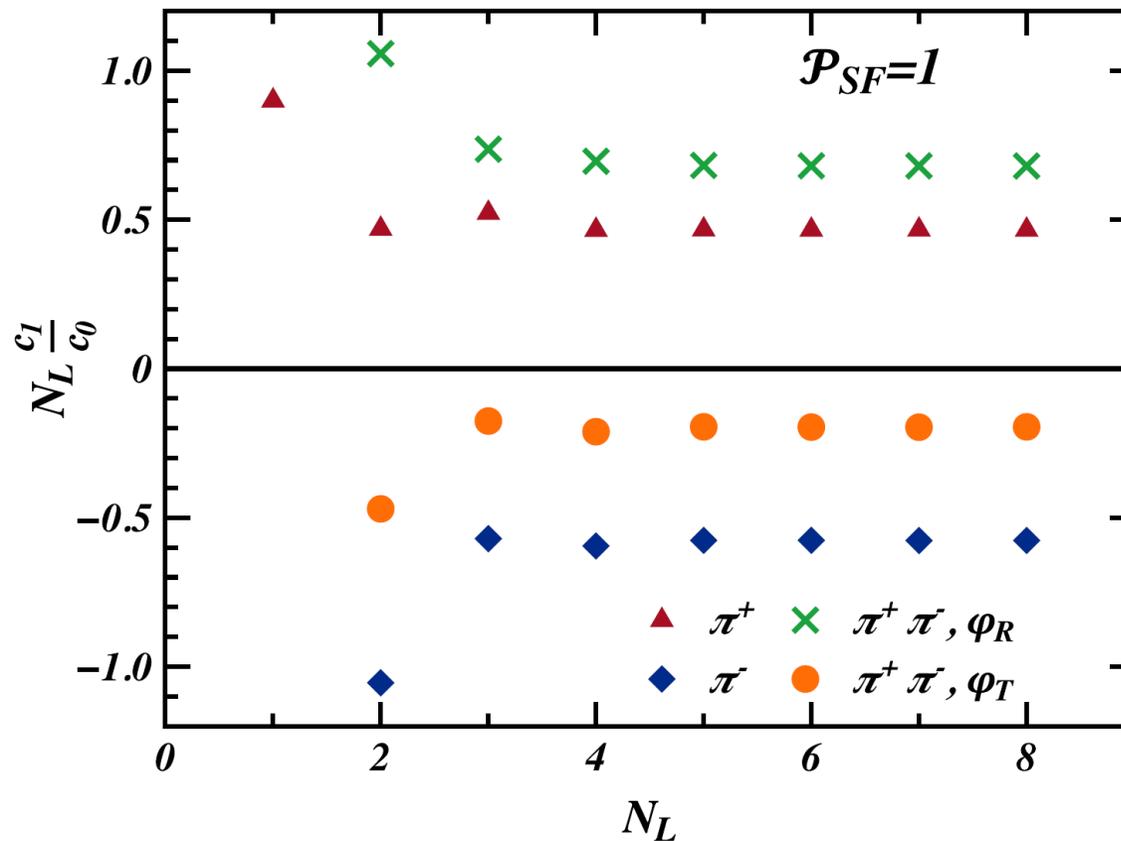
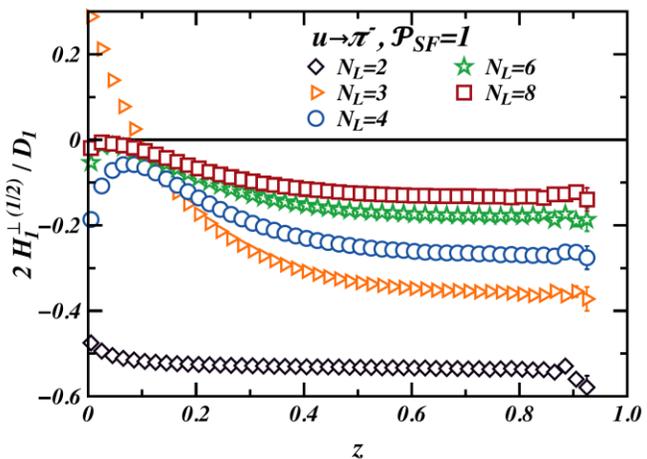
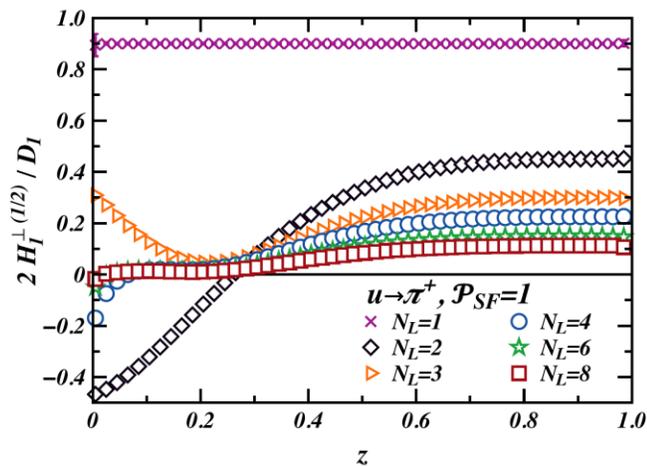
More realistic description of  $h_{h/q}$  a la  
 A. Bacchetta, L. P. Gamberg, G. R. Goldstein, and  
 A. Mukherjee, (PLB659, 234 (2008))  
 Spectator Model gives similar results

# Collins effect in 1h and 2h fragmentation

## Toy model

$$d_{h/q^-}(z, p_\perp^2, \varphi) = d_{h/q}(z, p_\perp^2) (1 - 0.9 \sin(\varphi))$$

$$F(c_0, c_1) \equiv c_0 - c_1 \sin(\varphi).$$



**Fig. 4.** Fitted values of the ratio  $2H_1^{\perp(1/2)}/D_1$  for  $u \rightarrow \pi^+$  (a) and  $u \rightarrow \pi^-$  (b) as a function of  $z$  from MC simulations with several values of  $N_L$ , where  $\mathcal{P}_{SF} = 1$ .