

# Tool to compare different methods: The $L$ function

(JCC & Rogers, in preparation)

- Shape change of transverse momentum distribution comes only from  $b_T$ -dependence of  $\tilde{K}$

- Write cross section as

$$\frac{d\sigma}{d^4q} = \text{norm.} \times \int e^{i\mathbf{q}_T \cdot \mathbf{b}_T} \tilde{W}(b_T, s, x_A, x_B) d^2\mathbf{b}_T$$

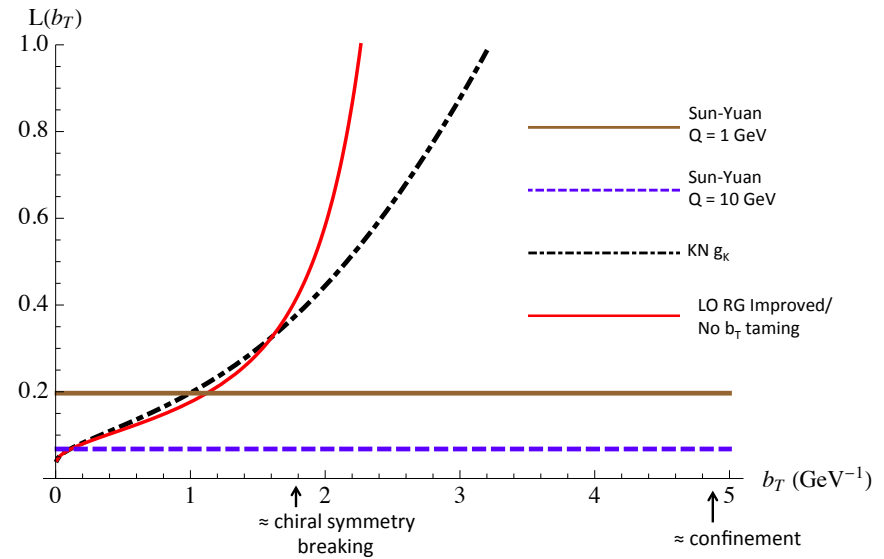
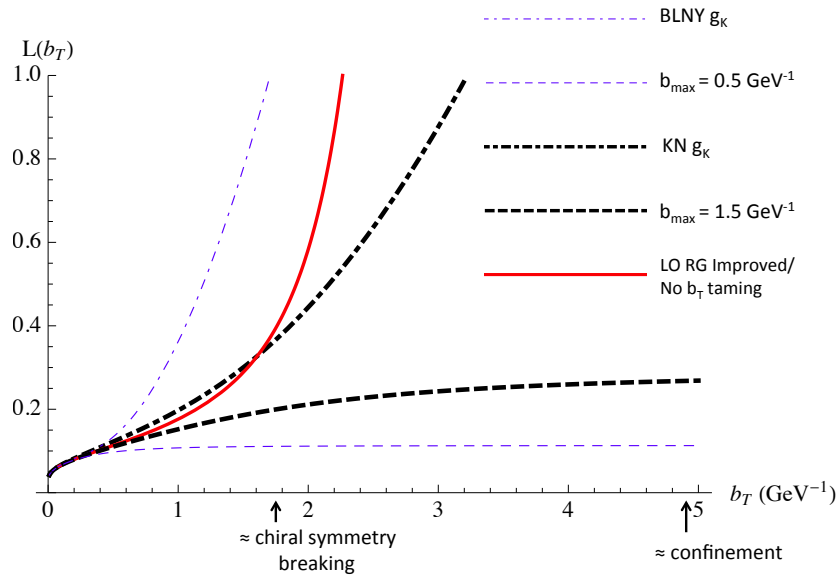
- So define scheme independent

$$L(b_T) = -\frac{\partial}{\partial \ln b_T^2} \frac{\partial}{\partial \ln Q^2} \ln \tilde{W}(b_T, Q, x_A, x_B) \stackrel{\text{CSS}}{=} -\frac{\partial}{\partial \ln b_T^2} \tilde{K}(b_T, \mu)$$

- QCD predicts it is
  - independent of  $Q, x_A, x_B$
  - independent of light-quark flavor
  - RG invariant
  - perturbatively calculable at small  $b_T$
  - non-perturbative at large  $b_T$

# Comparing different results using the $L$ function

(Preliminary)



$Q$	Typical $b_T$
2 GeV	3 GeV $^{-1}$
10 GeV	1.2 GeV $^{-1}$
$m_Z$	0.5 GeV $^{-1}$

SY = Sun & Yuan (PRD 88, 114012 (2013)):

$$L_{SY} = C_F \frac{\alpha_s(Q)}{\pi}$$

Depends on  $Q$ : contrary to QCD