



Experimental results on the atmospheric muon charge ratio



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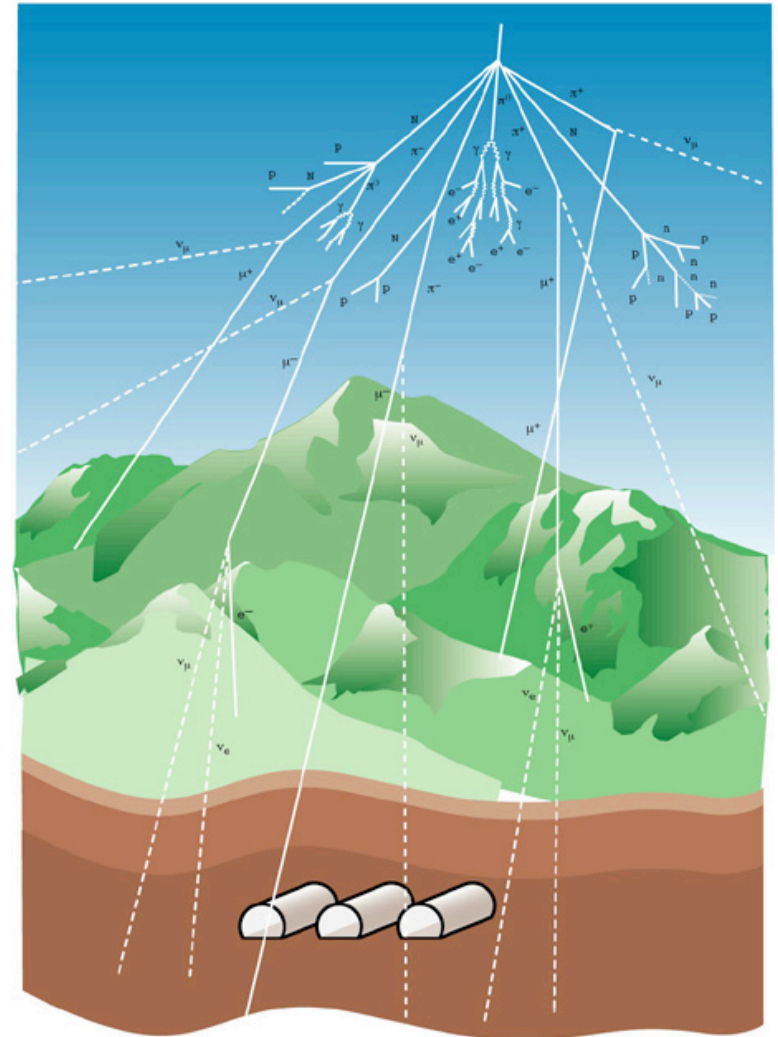
Università di Bologna and INFN Sezione di Bologna



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Noto, September 30th, 2014

The atmospheric muon charge ratio

- The atmospheric muon charge ratio $R_\mu \equiv N_{\mu^+}/N_{\mu^-}$ is being studied and measured since many decades
 - Depends on the **chemical composition** and energy spectrum of the primary cosmic rays
 - Depends on the **hadronic interaction features**
 - At high energy, depends on the **prompt component**
- It provides the possibility to check HE hadronic interaction models ($E > 1 \text{ TeV}$) in the **fragmentation region**, in a phase space complementary to the collider's one
- Since atmospheric muons are kinematically related to atmospheric neutrinos (same sources), R_μ provides a benchmark for **atmospheric ν flux computations** (e.g. background for neutrino telescopes)



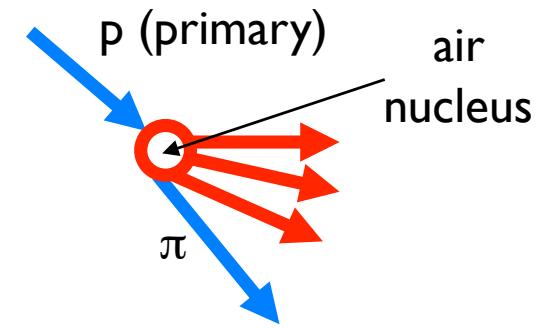
Key features of R_μ

Naïf prediction (Gaisser, Cambridge University Press)

- Assume only primary protons with a spectrum $dN/dE = N_0 E^{-(1+\gamma)}$
- Assume only pions and neglect muon decays (HE limit)
- Consider the inclusive cross-section for pions

$$f_{p\pi}^\pm(E_\pi, E_p) \equiv \frac{E_\pi}{\sigma_{pp}^{inel}} \frac{d\sigma_{p \rightarrow \pi}^\pm}{dE_\pi} \xrightarrow{E \rightarrow \infty} \tilde{f}_{p\pi}^\pm(x)$$

**Feynman
scaling**



Assuming Feynman scaling, the muon charge ratio prediction:

$$R_\mu = \frac{\mu^+(E_\mu)}{\mu^-(E_\mu)} = \frac{\pi^+(E_\pi)}{\pi^-(E_\pi)} = \frac{Z_{p\pi^+}}{Z_{p\pi^-}}$$

where Z_{ij} :

$$Z_{p\pi^\pm} \equiv \int_0^1 \tilde{f}_{p\pi}^\pm(x) x^{\gamma-1} dx$$

**Spectrum weighted moments
(SWM)**

Key features of R_μ (cont'd)

Elaborating the minimal model:

- Introducing the neutron component in the primary flux (in heavy nuclei) and considering the isospin symmetries: $Z_{p\pi^+} = Z_{n\pi^-}$, $Z_{p\pi^-} = Z_{n\pi^+}$

$$R_\mu = \frac{1 + \delta_0 AB}{1 - \delta_0 AB}$$

where:

$$A = (Z_{p\pi^+} - Z_{p\pi^-}) / (Z_{p\pi^+} + Z_{p\pi^-})$$

$$B = (1 - Z_{pp} - Z_{pn}) / (Z_{pp} + Z_{pn})$$

$$\delta_0 = (p_0 - n_0) / (p_0 + n_0) \quad \text{primary proton excess}$$

Interpretation of the prominent features:

- The result is valid only in the fragmentation region, enhanced in the SWM
- But the steeply falling primary spectrum ($\gamma \sim 1.7$) in the SWM suppresses the contribution of the central region \rightarrow scaling holds

Each pion is likely to have an energy close to the one of the projectile (primary CR proton) and comes from its fragmentation (valence quarks)

\rightarrow positive charge ($R_\mu > 1$)

Feynman
scaling
validity 

- R_μ does not depend on E_μ (or E_π) nor on the target nature
- R_μ depends on the primary composition through δ_0

Kaon contribution

- At higher energy (>100 GeV) the contribution of K becomes important
- In general, the contribution of each component to the muon flux $N_{\text{par}} = (\pi, K, \text{charmed, etc.})$ depends on the relative contribution of decays and interaction probabilities:

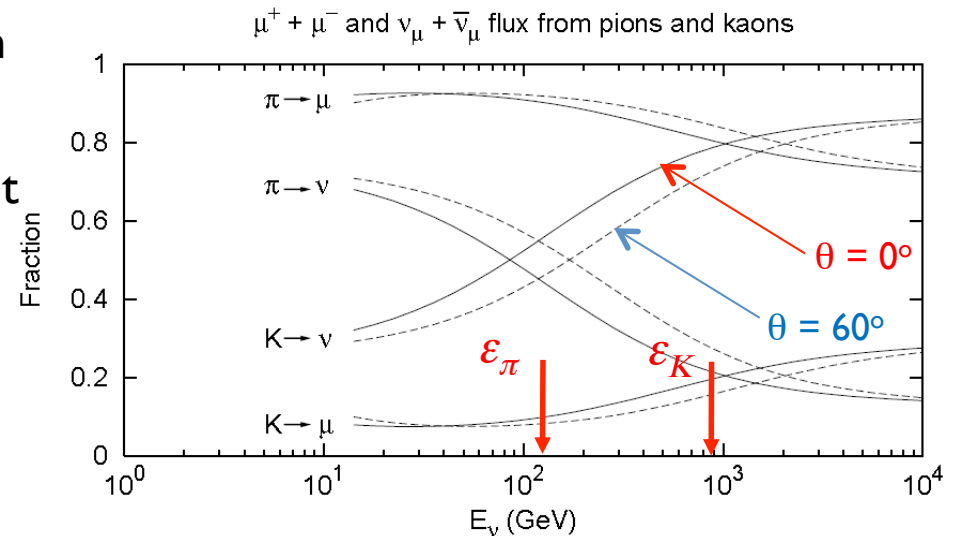
$$\Phi_{\mu} = \frac{\Phi_N(\mathbf{E}_{\mu})}{1 - Z_{NN}} \sum_{i=1}^{N_{\text{par}}} \frac{a_i Z_{Ni}}{1 + b_i \mathbf{E}_{\mu} / \varepsilon_i(\theta)}$$

- For kaons:

$$Z_{pK^+} \gg Z_{nK^-} \approx Z_{pK^-}$$

because the reaction

$p \text{ Air} \rightarrow K^+ \Lambda N + \text{anything}$
is favoured (**associated production**)



$\varepsilon_i = \varepsilon_i(\theta)$ critical energy
energy above which interactions
dominate over decays. Along the
vertical ($\theta = 0^\circ$):

$$\varepsilon_{\pi} = 115 \text{ GeV}$$

$$\varepsilon_K = 850 \text{ GeV}$$

$$\varepsilon_X > 10^7 \text{ GeV}$$

→ This leads to a larger R_{μ} ratio
at high energy

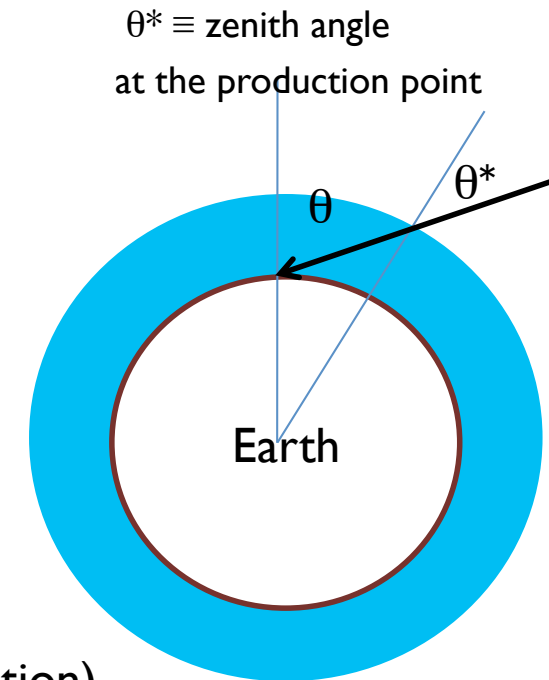
Parameterization of the charge ratio

- Considering the general form for the muon flux

$$\Phi_{\mu^\pm} = \frac{\Phi_N(\mathbf{E}_\mu)}{1 - Z_{NN}} \sum_{i=1}^{N_{par}} \frac{a_i Z_{Ni}^\pm}{1 + b_i \mathbf{E}_\mu \cos \theta^* / \varepsilon_i(0)}$$

where we have made explicit the $\varepsilon_i(\theta)$ dependence on θ

$$\varepsilon_i(\theta) = \varepsilon_i(0) / \cos \theta^*$$



- The correct variable to describe the evolution of R_μ is therefore $\mathbf{E}_\mu \cos \theta^*$ (assuming a constant primary composition)
- The R_μ evolution as a function of $\mathbf{E}_\mu \cos \theta^*$ spans over the different sources

$$R_\mu = w_\pi R_\mu^\pi + w_K R_\mu^K + w_{charm} R_\mu^{charm} + \dots$$
➡ POWERFUL HANDLE TO DISCRIMINATE MODELS

Analysis of experimental results in terms of $\mathbf{E}_\mu \cos \theta^*$

R_μ measurements with $E_\mu \cos\theta^* \sim 1 \text{ TeV}$

Experiments with magnetic field:

- Utah:
G. K. Ashley et al., Phys. Rev. D12 (1975) 20
– Underground at Utah University, flat surface above ~ 1400 m.w.e., magnetic spectrometer (1.63 T) + spark chambers, six bins with $46^\circ < \theta < 78^\circ$
- CMS: (shallow depth)
CMS Collaboration, Phys. Lett. B692 (2010) 83
- MINOS:
P. Adamson et al., Phys. Rev. D76 (2007) 052003 + Phys. Rev. D83 (2011) 032011
- OPERA:
N. Agafonova et al., Eur. Phys. J. C67 (2010) 25 + Eur. Phys. J. C74 (2014) 2933

Experiments without magnetic field:

- Kamiokande-II
M. Yamada et al., Phys. Rev. D44 (1991) 617
– Underground Cherenkov detector at Kamioka ~ 2700 m.w.e., delayed events on stopping muons, one bin with $0^\circ < \theta < 90^\circ$
- LVD:
N. Agafonova et al., Proc. 31th ICRC, ŁÓDŹ 2009 + arXiv:1311.6995
– Underground at LNGS, average overburden ~ 3800 m.w.e., scintillators, delayed events on stopping muons, one bin with $\theta < 15^\circ$

R_μ measurements with $E_\mu \cos\theta^* \sim 1 \text{ TeV}$

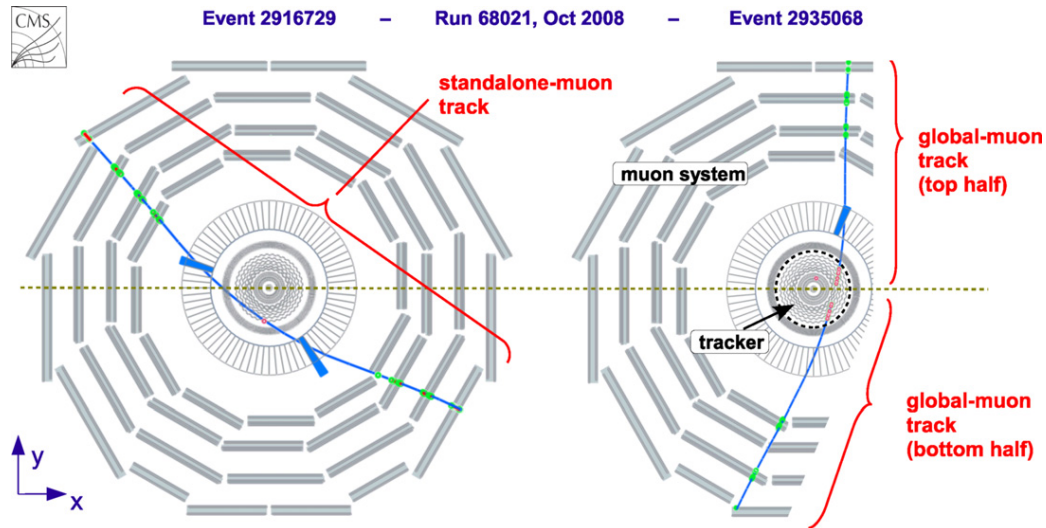
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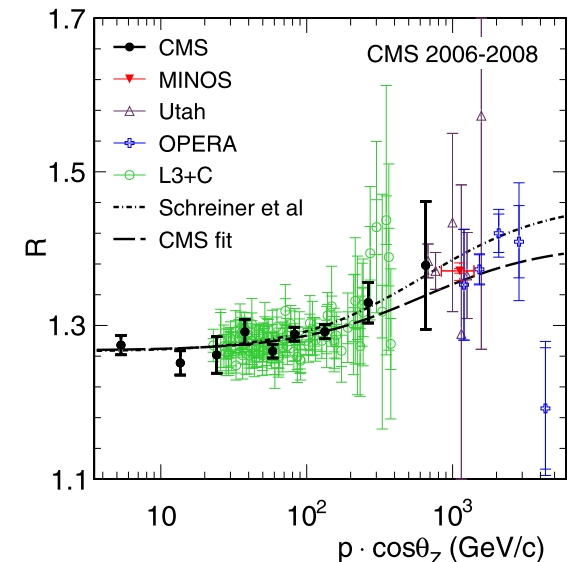
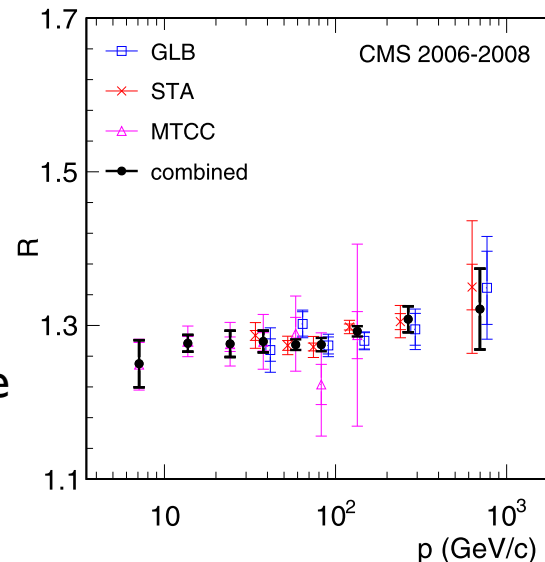
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CMS results



- Average vertical overburden ~ 100 m.w.e.
- Superconducting solenoid (3.8 T)
- Muon tracking with **inner** silicon trackers + **outer** muon chambers (DT + RPC)
- Zenith window $0^\circ < \theta < 80^\circ$

CMS provides the measurement of R_μ in the **[5 GeV/c - 1 TeV/c]** momentum range: rise in R_μ
 → Measurement in the transition region between the pion dominated charge ratio ($p < 100$ GeV/c) and the pion+kaon charge ratio

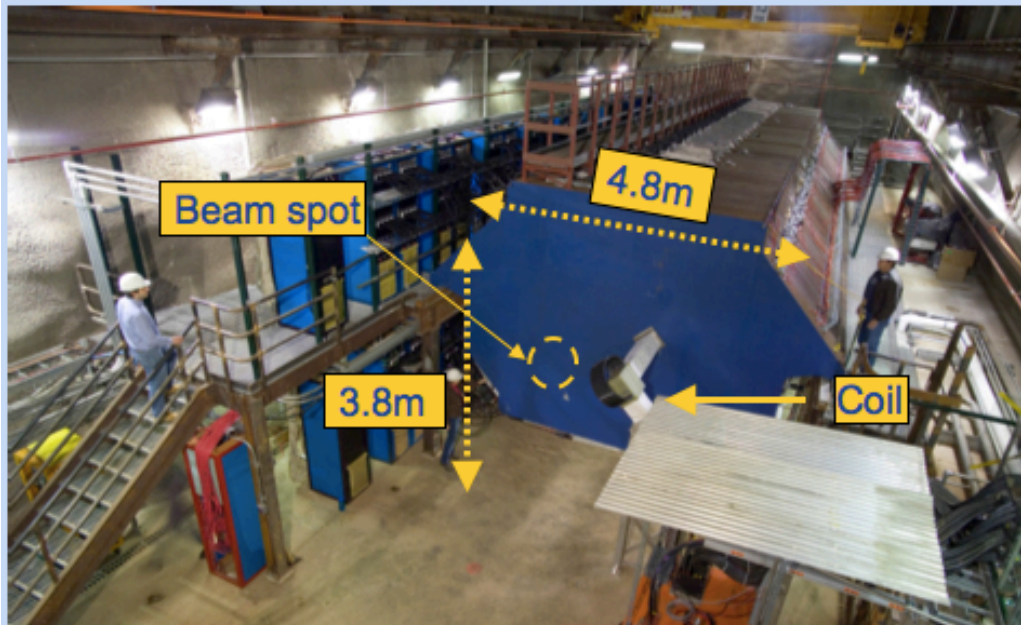


MINOS Near and Far detectors

Identical detectors: magnetized steel (toroidal magnetic field, average ~ 1.3 T) + scintillators
At FD in Soudan flat overburden profile ~ 2000 m.w.e., detector angular window $0^\circ < \theta < 90^\circ$

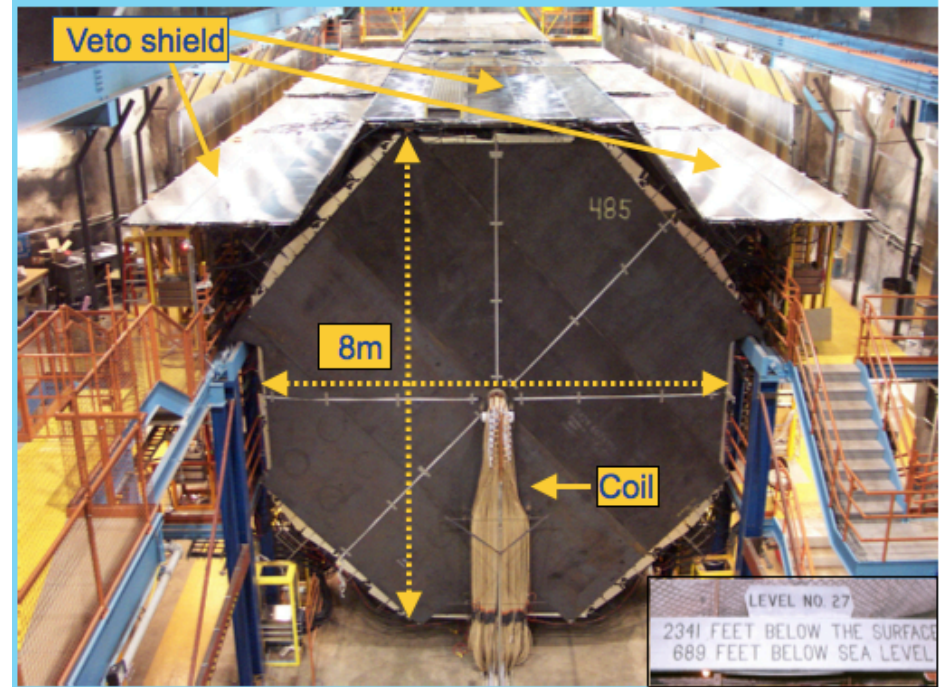
Near Detector

- 980 ton total mass
- Located 1 km downstream of the target at Fermilab
- 100 m depth



Far Detector

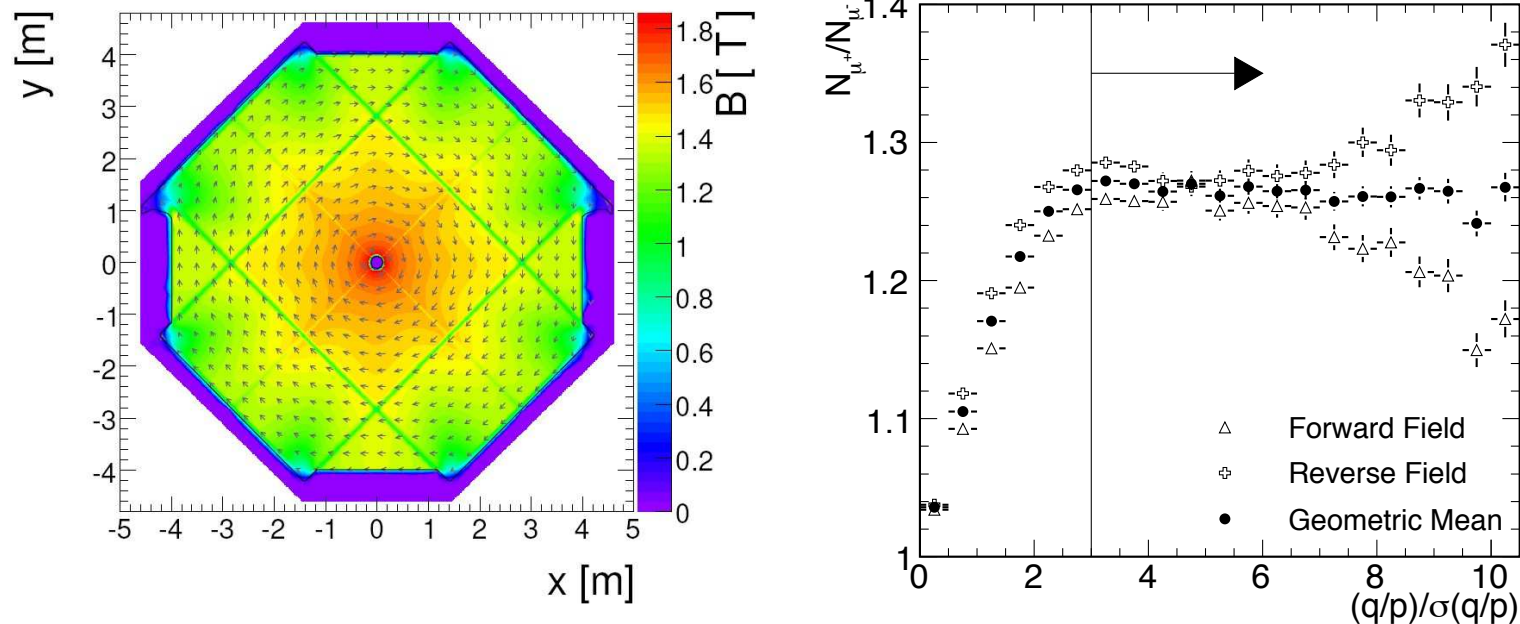
- 5.4 kton, 2 supermodules
- Located 735 km away in Soudan mine, MN
- 714 m depth
- Veto shield enables atmospheric neutrino studies



MINOS results

Measurements by two functionally identical detectors, one at shallow depth, one deep underground

- Toroidal magnetic field: different acceptance for μ^+ and μ^-
 - Combination of data sets with opposite magnetic field orientations to minimize systematic errors



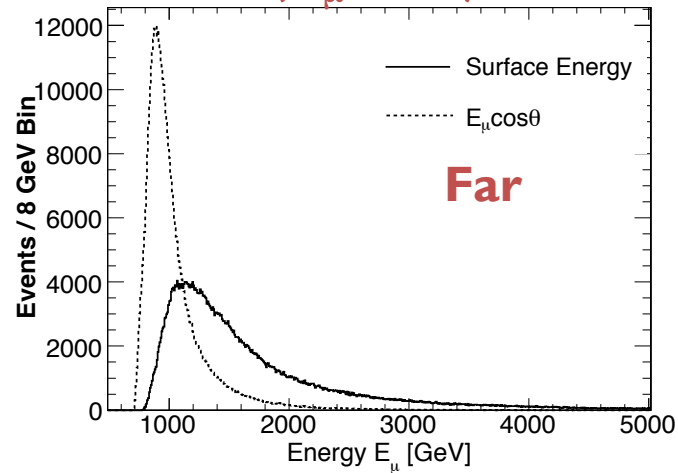
Near $\left[R_\mu (\text{single } \mu) = 1.266 \pm 0.001 (\text{stat.})^{+0.015}_{-0.014} (\text{syst.}) \right]$

Far $\left[R_\mu (\text{single } \mu) = 1.374 \pm 0.004 (\text{stat.})^{+0.012}_{-0.010} (\text{syst.}) \right]$

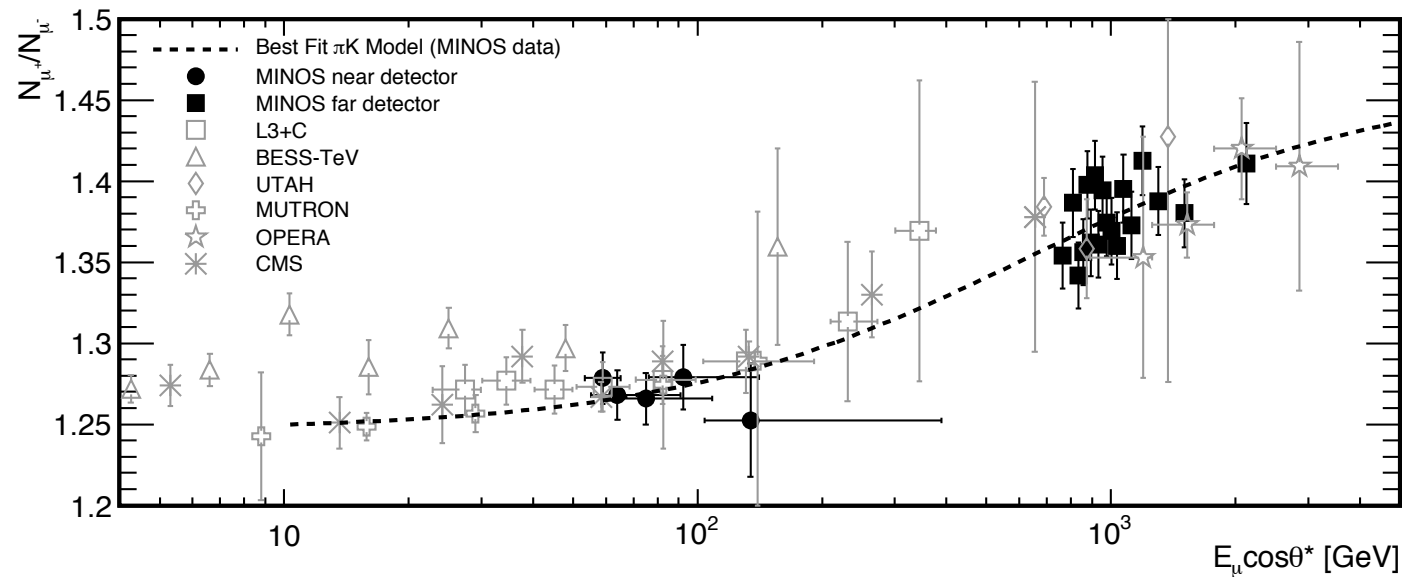
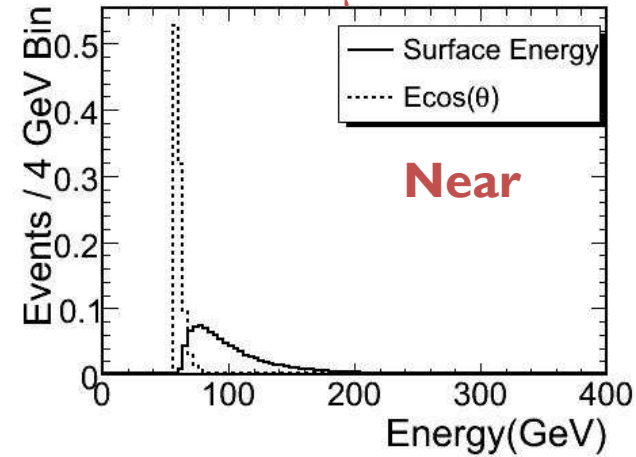
$R_\mu (\text{multiple } \mu) = 1.080 \pm 0.004 (\text{stat.})$ (C. Castromonte et al., Proc. 33rd ICRC, 2013)

MINOS results

MINOS Far $\langle E_\mu \cos\theta^* \rangle \approx 1 \text{ TeV}$

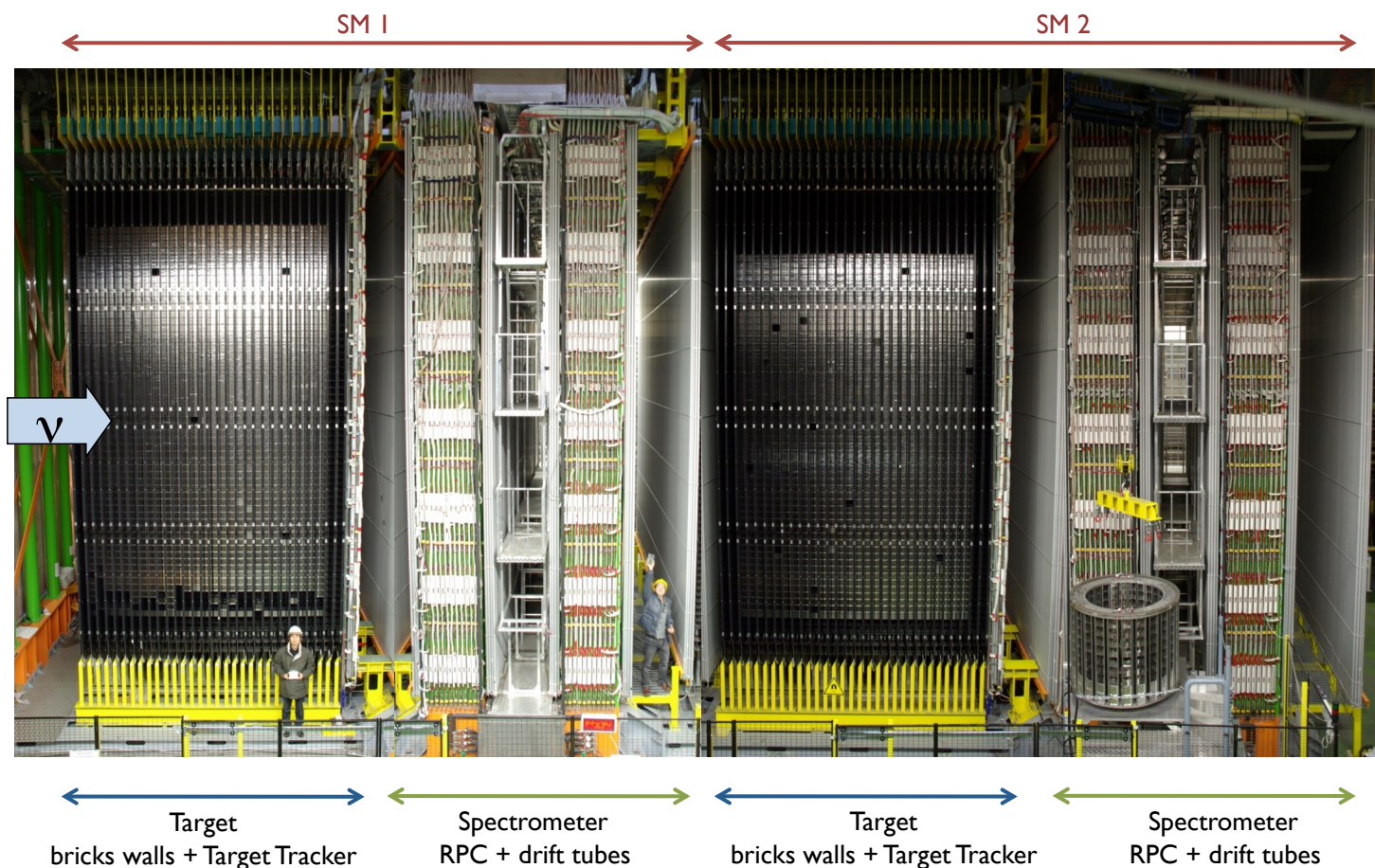


MINOS Near $\langle E_\mu \cos\theta^* \rangle \sim O(100) \text{ GeV}$



OPERA detector

Target + magnetic spectrometer (1.53 T) at LNGS, average overburden ~ 3800 m.w.e., drift tubes + RPC + scintillators, detector angular window $0^\circ < \theta < 90^\circ$

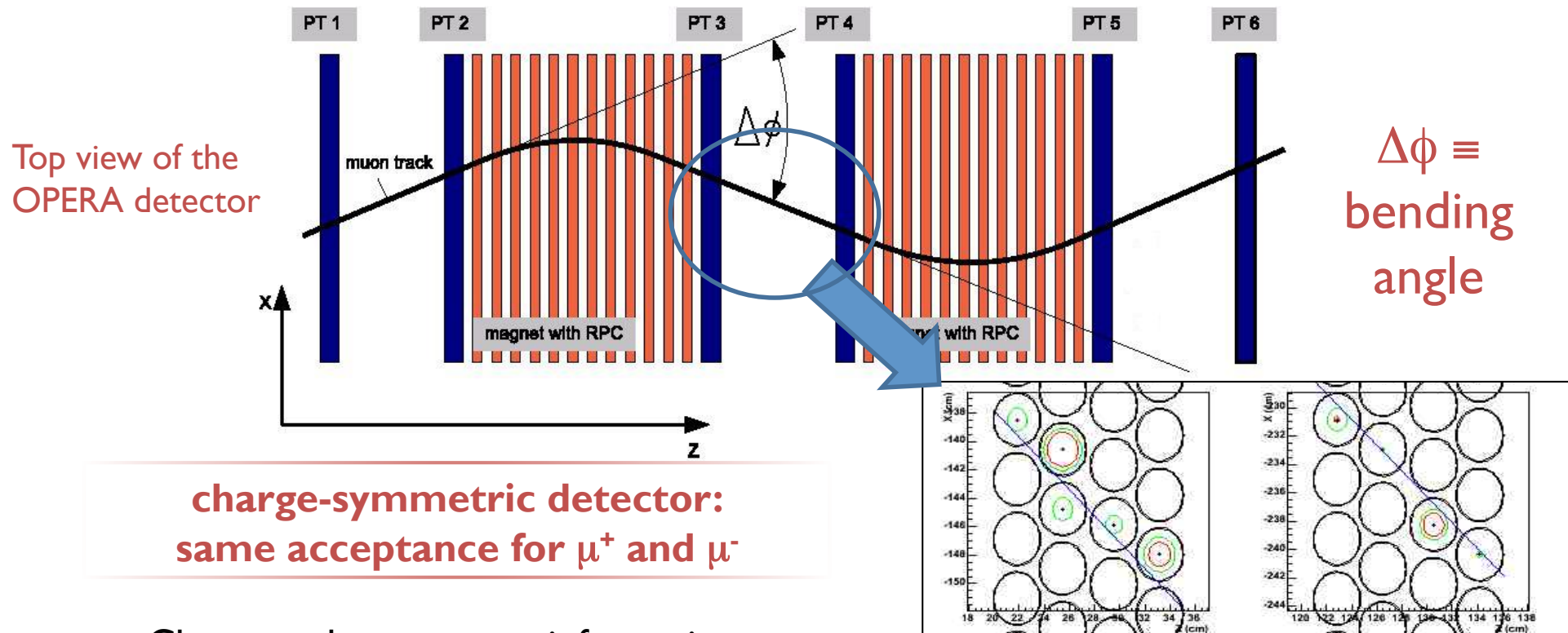


OPERA: $\langle E_\mu \cos \theta^* \rangle \approx 2$ TeV



The (magnetized) experiment with the largest $E_\mu \cos \theta^*$

Charge and momentum reconstruction



- Charge and momentum information provided by the bending angle $\Delta\phi_k = \phi_i - \phi_j$ ($k=1, \dots, 4$, for the 4 arms)

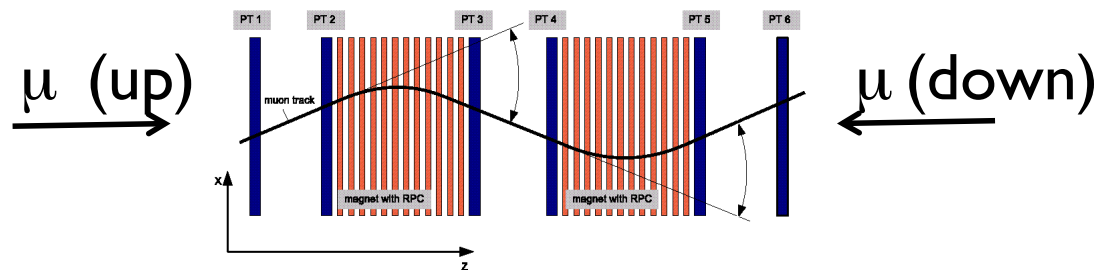
➤ 0.15 mrad angular resolution for $\phi = 0$ (improve for $\phi > 0$)

➤ Combination of the two data sets with opposite magnet polarities
→ disposing of the misalignment systematics (~ 0.1 mrad)

Systematic uncertainty on R_μ

Two main sources of systematic uncertainties:

- Misalignment: combination procedure
 - Estimate of the residual systematic uncertainty related to the combination procedure: difference between the charge ratio R_μ for muons coming from opposite directions: $\delta R_\mu = |R_\mu(\text{up}) - R_\mu(\text{down})|$
- Charge misidentification η from **experimental data**
 - Estimate $\delta\eta = \eta_{\text{data}} - \eta_{\text{MC}}$ for a subsample of events crossing both arms of a spectrometer: computation of the probability p of reconstructing opposite charges



Total systematic uncertainty for single μ : $\delta R_\mu^{\text{unf}}(\text{syst}) = +0.007, -0.001$

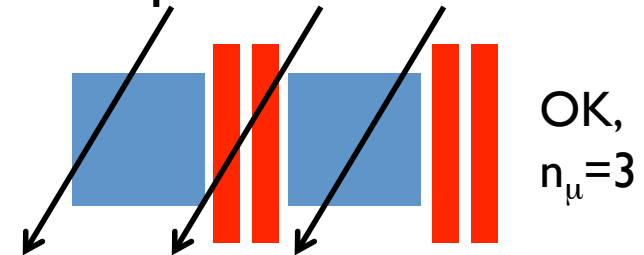
Total systematic uncertainty for multiple μ : $\delta R_\mu^{\text{unf}}(\text{syst}) = +0.015, -0.013$

Results: underground muon charge ratio

Full OPERA data set (2008-2012): combining data taken with opposite magnet polarities

R_μ computed separately for single and multiple muon events

- Multiple muons: compute R_μ when the 3D multiplicity is > 1 , independently on the number of measured charges in the event



primary features extracted from a full MC

Full OPERA data
(5-year statistics)

N_μ	$\langle A \rangle$	$\langle E/A \rangle_{\text{primary}}$ [TeV]	H fraction	N_p/N_n	R_μ^{unf}
$= 1$	3.35 ± 0.09	19.4 ± 0.1	0.667 ± 0.007	4.99 ± 0.05	1.377 ± 0.006
> 1	8.5 ± 0.3	77 ± 1	0.352 ± 0.012	2.09 ± 0.07	1.098 ± 0.023

“dilution” of R_μ for multiple muon events

convolution of two effects:

larger n/p ratio in the all-nucleon spectrum \otimes different x_F region

Charge ratio of multiple muon events

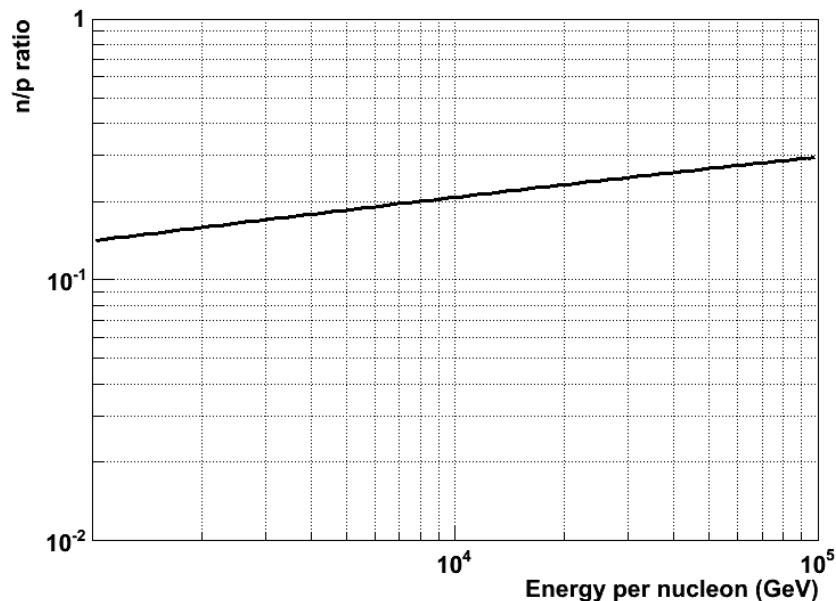
- The smaller value of the charge ratio of multiple muons is due to the convolution of two effects:

larger n/p ratio in the all-nucleon spectrum \otimes different x_F region

Multiple muon sample:
higher E/nucleon, higher average A



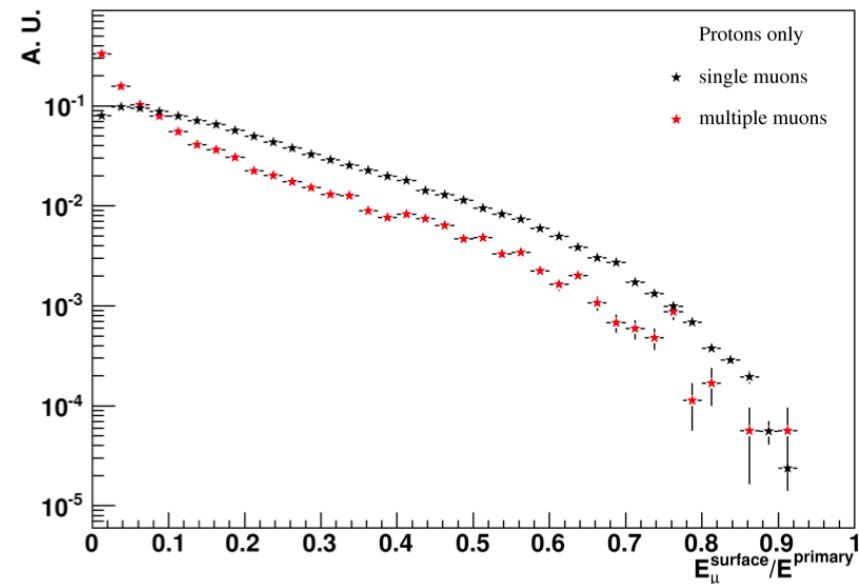
n/p ratio in primary cosmic rays



Multiple muon sample:
smaller x_F , towards the central region

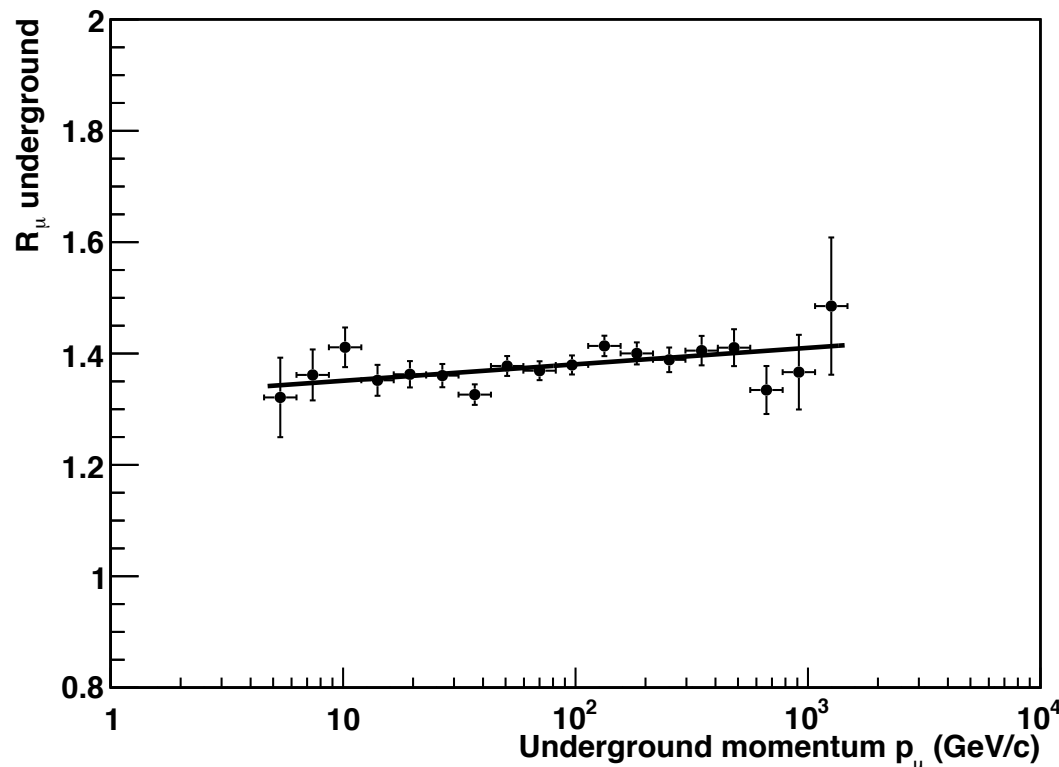
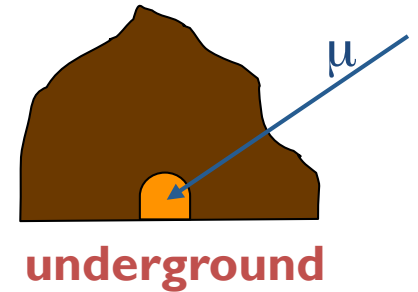


Feynman x: $x_F \cong E_{\text{secondary}}/E_{\text{primary}}$



R_μ as a function of p_μ

- R_μ (**single muons**)
- Evolution with p_μ is compatible both with a constant and with a logarithmic energy increase, with a 2.4σ preference for the latter



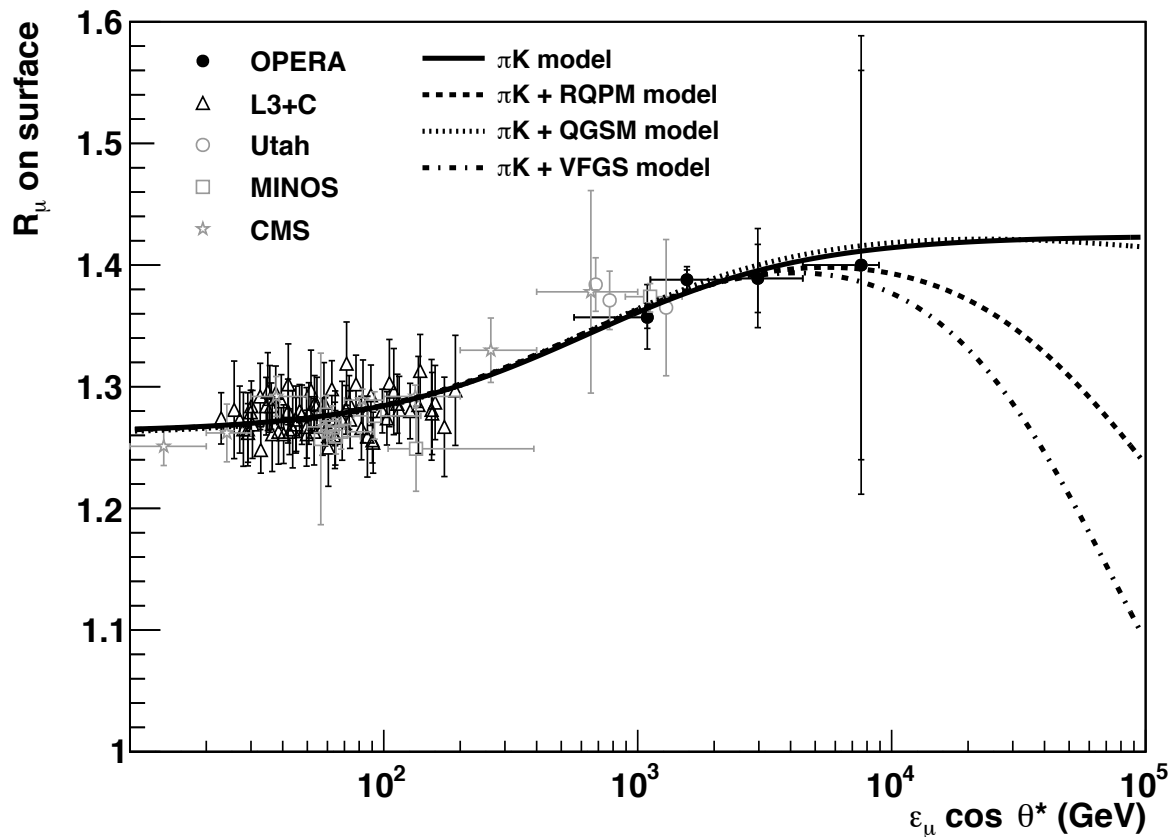
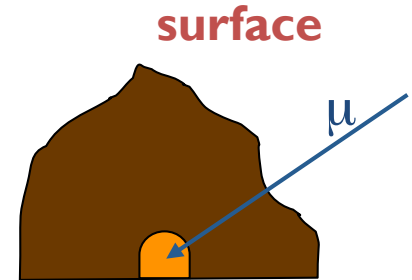
$$R_\mu = a_0 + a_1 \log_{10} p_\mu$$
$$\rightarrow a_0 = 1.322 \pm 0.023$$
$$\rightarrow a_1 = 0.030 \pm 0.012$$
$$(\chi^2/\text{dof} = 14.99/16)$$

$$R_\mu = c_0$$
$$\rightarrow c_0 = 1.377 \pm 0.006$$
$$(\chi^2/\text{dof} = 20.86/17)$$

$$\Delta\chi^2/\text{dof} = 5.87/1 \text{ } (\sim 2.4 \text{ sigma})$$

R_μ as a function of $E_\mu \cos \theta^*$

Bin	$\mathcal{E}_\mu \cos \theta^*$ (GeV)	$(\mathcal{E}_\mu \cos \theta^*)_{MPV}$ (GeV)	$\langle \theta \rangle$ (deg)	R_μ	$\delta R_\mu(stat.)$	$\delta R_\mu(syst.)$ %
1	562 - 1122	1091	47.5	1.357	0.009	1.8
2	1122 - 2239	1563	42.8	1.388	0.008	0.1
3	2239 - 4467	2972	46.9	1.389	0.028	2.1
4	4467 - 8913	7586	60.0	1.40	0.16	7.1



only single muons

□ Fit with the function

$$\phi_{\mu^\pm} \propto \frac{a_\pi f_{\pi^\pm}}{1 + b_\pi \mathcal{E}_\mu \cos \theta / \epsilon_\pi} + R_{K\pi} \frac{a_K f_{K^\pm}}{1 + b_K \mathcal{E}_\mu \cos \theta / \epsilon_K}$$

Fixing $R_{K\pi} = 0.127$ (weighted average of experimental values, Grashorn et al.):

$$f_{\pi^+} = 0.5512 \pm 0.0014$$

$$f_{K^+} = 0.705 \pm 0.014$$

R_μ as a function of $E_\mu \cos \theta^*$ and δ_0

Taking into account an explicit dependence on $\delta_0 = (p - n)/(p + n)$:

(Gaisser, Astropart. Phys. 35 (2012) 801)

$$R_\mu = \left[\frac{f_{\pi^+}}{1 + B_\pi \mathcal{E}_\mu \cos \theta^* / \varepsilon_\pi} + \frac{\frac{1}{2}(1 + \alpha_K \beta \delta_0) A_K / A_\pi}{1 + B_K^+ \mathcal{E}_\mu \cos \theta^* / \varepsilon_K} \right] \times \left[\frac{1 - f_{\pi^+}}{1 + B_\pi \mathcal{E}_\mu \cos \theta^* / \varepsilon_\pi} + \frac{(Z_{NK^-} / Z_{NK}) A_K / A_\pi}{1 + B_K \mathcal{E}_\mu \cos \theta^* / \varepsilon_K} \right]^{-1}$$

δ_0 depends on $E_{\text{primary}}/\text{nucleon} \approx 10 E_\mu$ (not on $E_\mu \cos \theta^*$!)

→ Different dependencies:

fit in 2-dimensions ($E_\mu, \cos \theta^*$)

20 bins: 5 energy bins \times 4 angular bins

Fixed parameters (see table)



Inferred parameters: Z_{pK^+} and δ_0

Parameter	Value	Ref.
Parameters depending on hadronic interactions		
$Z_{p\pi^+}$	0.046	[2]
$Z_{p\pi^-}$	0.033	[2]
Z_{pK^-}	0.0028	[2]
β	0.909	[22]
Parameters depending on primary spectral index		
A_π	$0.675 Z_{N\pi}$	[7]
A_K	$0.246 Z_{NK}$	[7]
B_π	1.061	[7]
B_K	1.126	[7]
Parameters depending on primary composition		
b	-0.035	[2]
Critical energies		
ε_π	115 GeV	[22]
ε_K	850 GeV	[22]

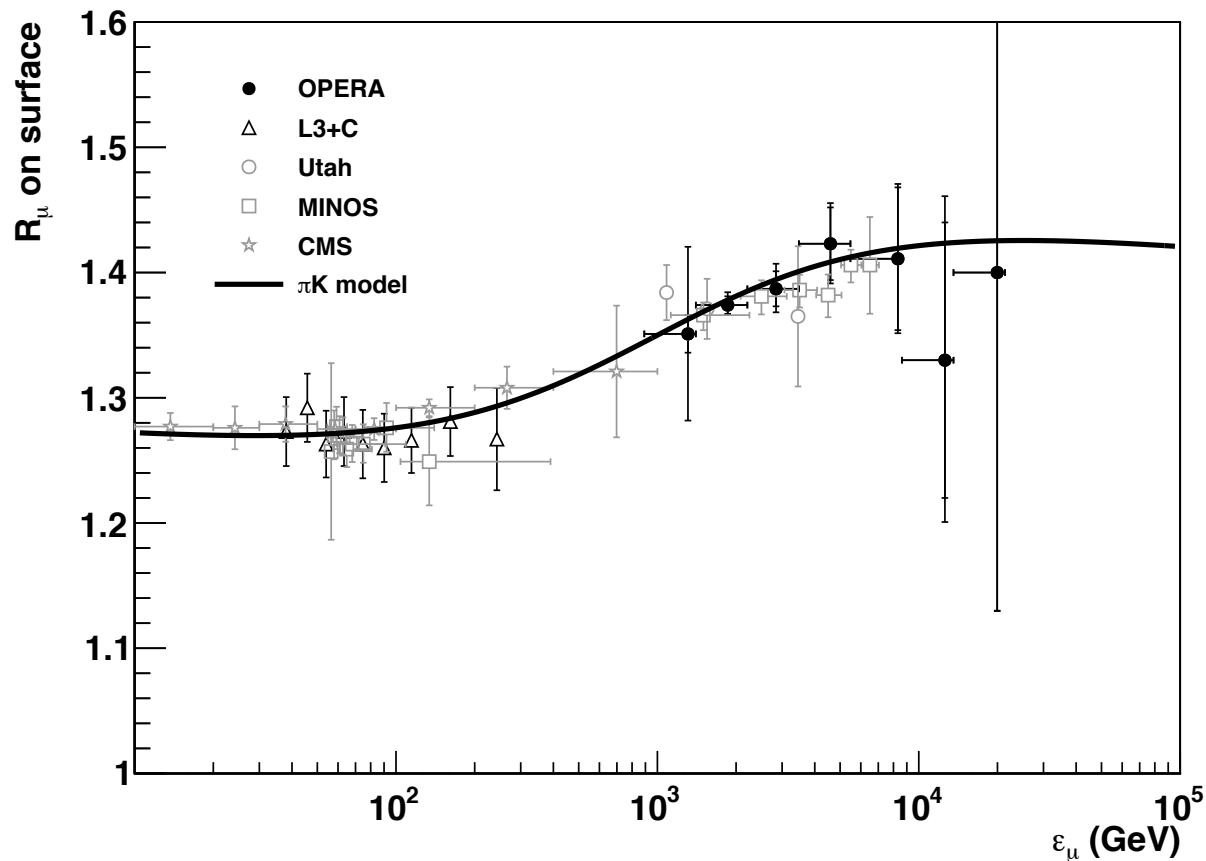
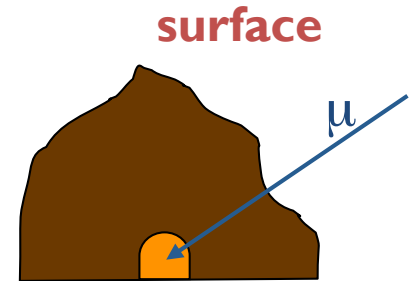
R_μ as a function of E_μ

Fit result:

$$\delta_0 (E_N \approx 20 \text{ TeV/n}) = 0.61 \pm 0.02$$
$$Z_{pK^+} = 0.0086 \pm 0.0004$$

Projecting the fit result on the average OPERA zenith $\langle \cos \theta^* \rangle \cong 0.7$:

R_μ as a function of the surface muon energy



only single muons

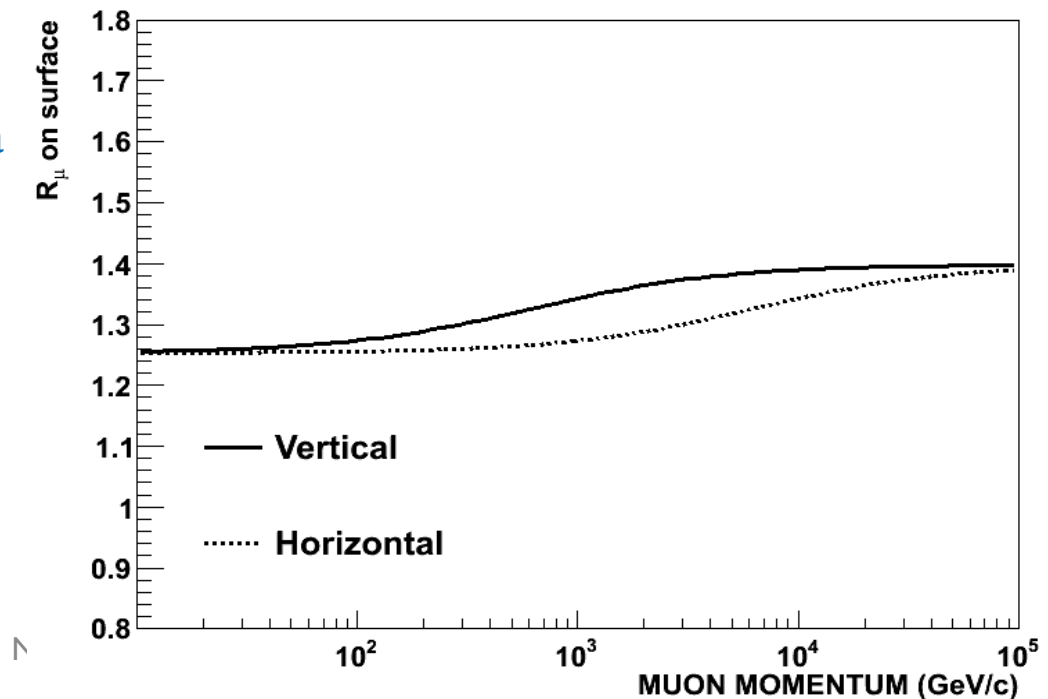
Conclusions

- The measurement of the atmospheric muon charge ratio R_μ provides relevant information for both particle- and astrophysics
- R_μ was measured in a wide energy range, from $O(1 \text{ GeV})$ up to $O(10 \text{ TeV})$
- The results of CMS, MINOS and OPERA show a rise of R_μ vs $E_\mu \cos \theta^*$
→ increasing kaon contribution
- The OPERA measurement in the highest energy region:
 - Found a strong reduction of the charge ratio for multiple muon events
 - R_μ for single muons compatible with the expectation from a **simple π -K model**
 - **No significant contribution of the prompt component** up to $E_\mu \cos \theta^* \sim 10 \text{ TeV}$
 - Extracted relevant parameters on the primary composition (δ_0) and the associated kaon production in the forward fragmentation region (Z_{pK+} moment)
 - **Validity of Feynman scaling** in the **fragmentation region** up to $E_\mu \sim 20 \text{ TeV}$, corresponding to primary energy/nucleon $E_N \sim 200 \text{ TeV}$

Spares

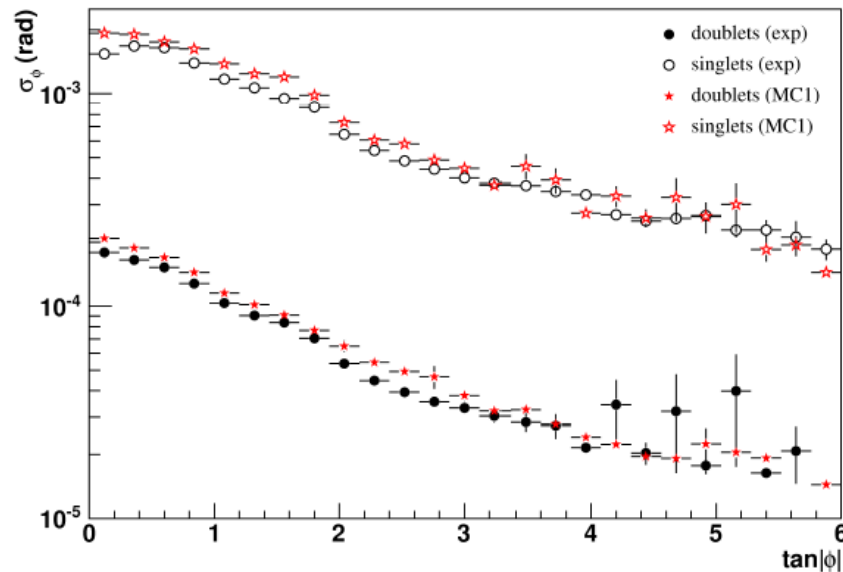
Dependencies of R_μ

- R_μ exhibits a zenith dependence if:
 - a) Muon contributions from different sources with different R_μ
 - b) At least one source has a zenith dependence (e.g. π and K due their relatively long lifetimes)
- In the past several authors applied corrections to convert inclined to vertical R_μ measurements
- This procedure has a limit: it assumes no other sources apart from π and K and it assumes $Z_{p\pi}$ and Z_{pK} are known
- The projection on the vertical via $E_\mu \cos\theta$ is safer → capability to explore new (isotropic) components and to derive $Z_{p\pi}$ and Z_{pK} from data



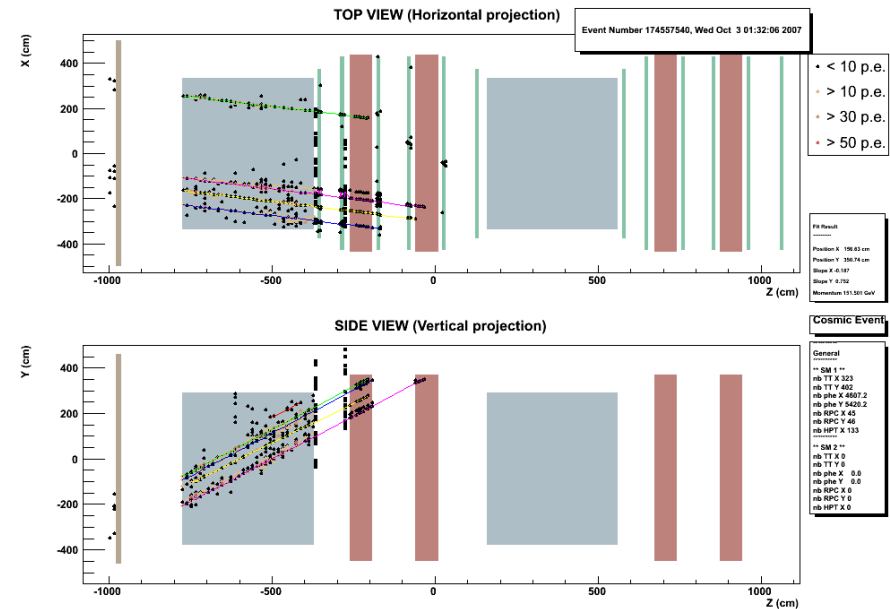
Cosmic event reconstruction in OPERA

➤ Multiple muon events well reconstructed

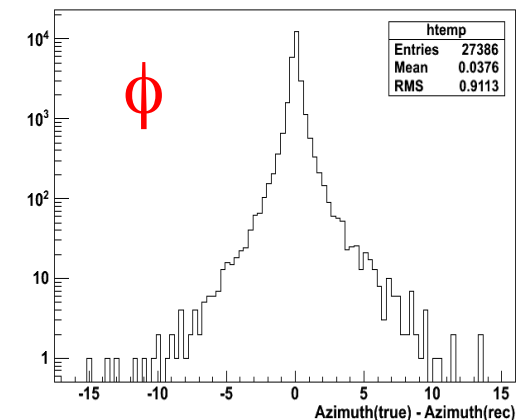
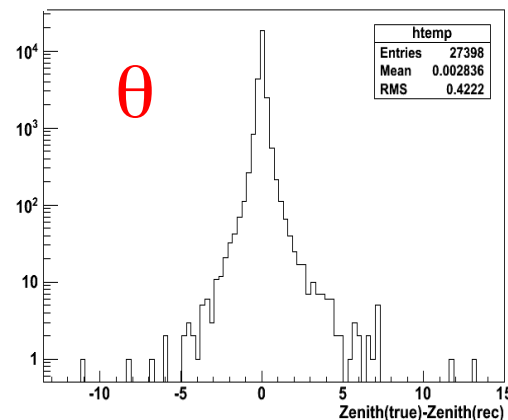


➤ Good overall angular resolution
“resolutions” < 1 deg both for zenith
and azimuth direction reconstruction

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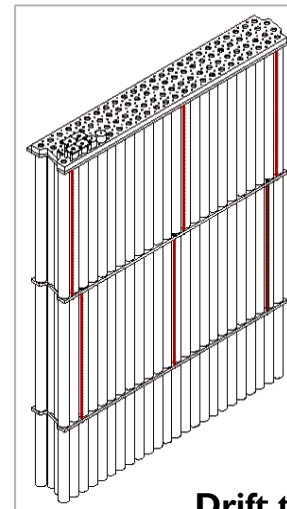


➤ High angular resolution in the PT system

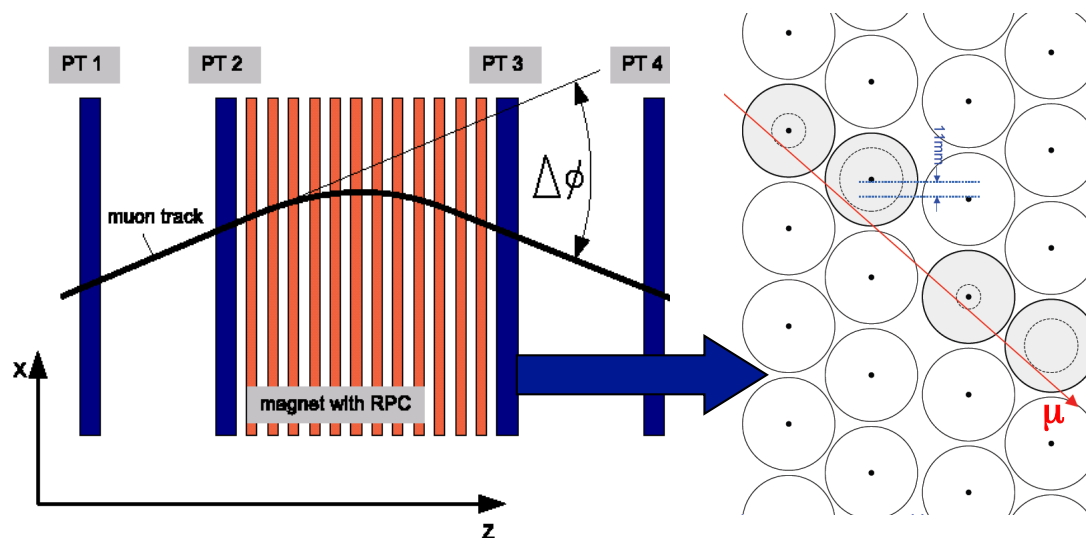
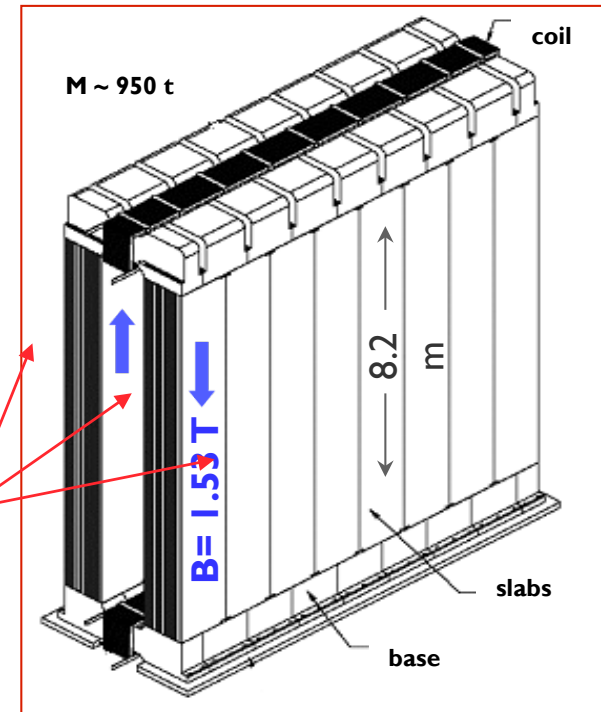


PT system in the spectrometer

6 PT stations for each spectrometer:
2 upstream of the first magnet arm, 2
in the middle, 2 downstream of the
second magnet arm



Drift tube
stations



Top view of the
OPERA spectrometer