

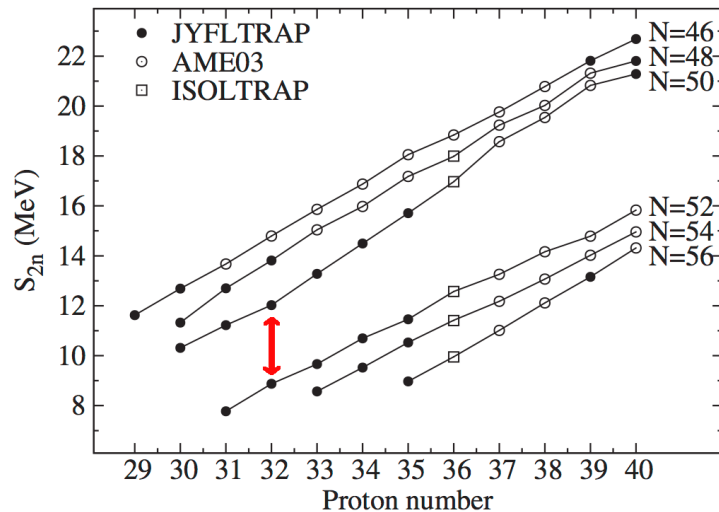
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# Exploring the Z=32 triaxiality corridor towards N=50 via safe Coulomb excitation at SPES

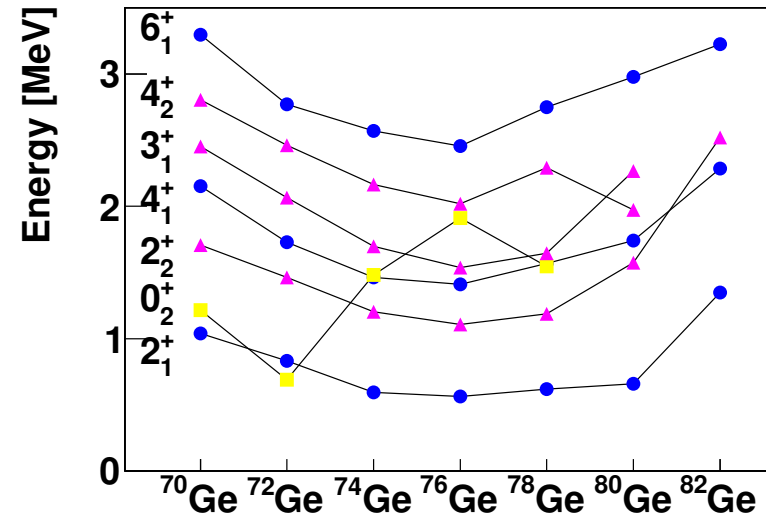
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# Motivation: triaxiality in Ge isotopes

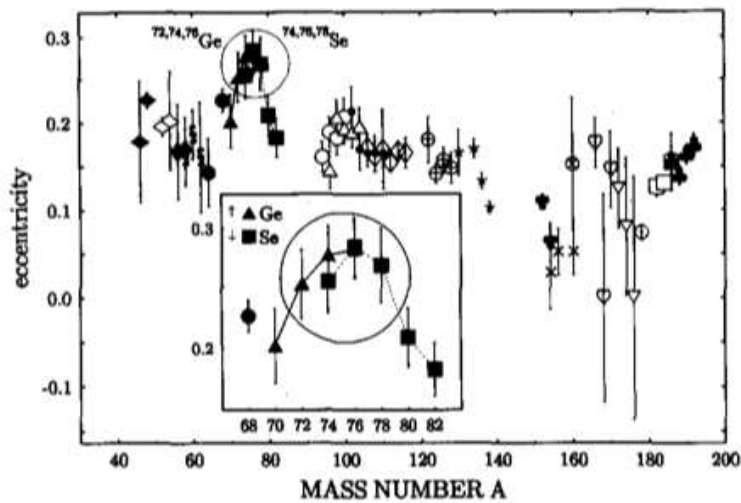


J. Hakala *et al*, PRL 101 (2008) 052502

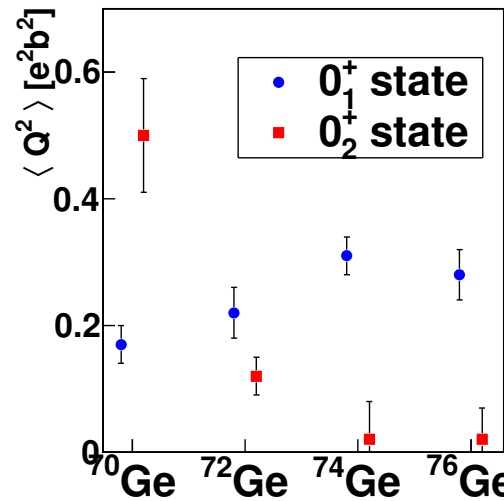


- Local minimum of the effective N=50 gap at Z=32, associated to a maximum of collectivity
- Substantial evidence for triaxiality in Ge isotopes:
  - observation of quasi-gamma bands ( $2_2^+$ ,  $3_1^+$ ,  $4_2^+$ )
  - odd-even staggering in the gamma band in  $^{76}\text{Ge}$  interpreted as rigid triaxiality (Y. Toh *et al*, PRC 87 (2013) 041304)
  - analysis of  $^{80}\text{Ga} \rightarrow ^{80}\text{Ge}$  beta decay: coexistence of collective gamma-soft and spherical  $qp$  structures in  $^{80}\text{Ge}$  (D. Verney *et al*, PRC 87 (2013) 054307)

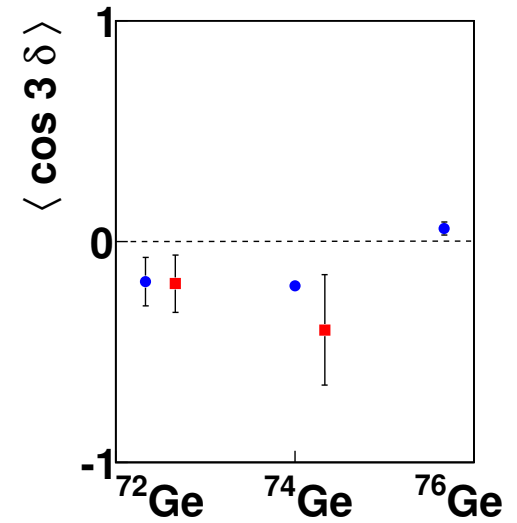
# Motivation: triaxiality in Ge isotopes



A. Andrejtscheff *et al*, Phys. Lett. B 329 (1994) 1



M. Sugawara *et al*, EPJ A 16 (2003) 409

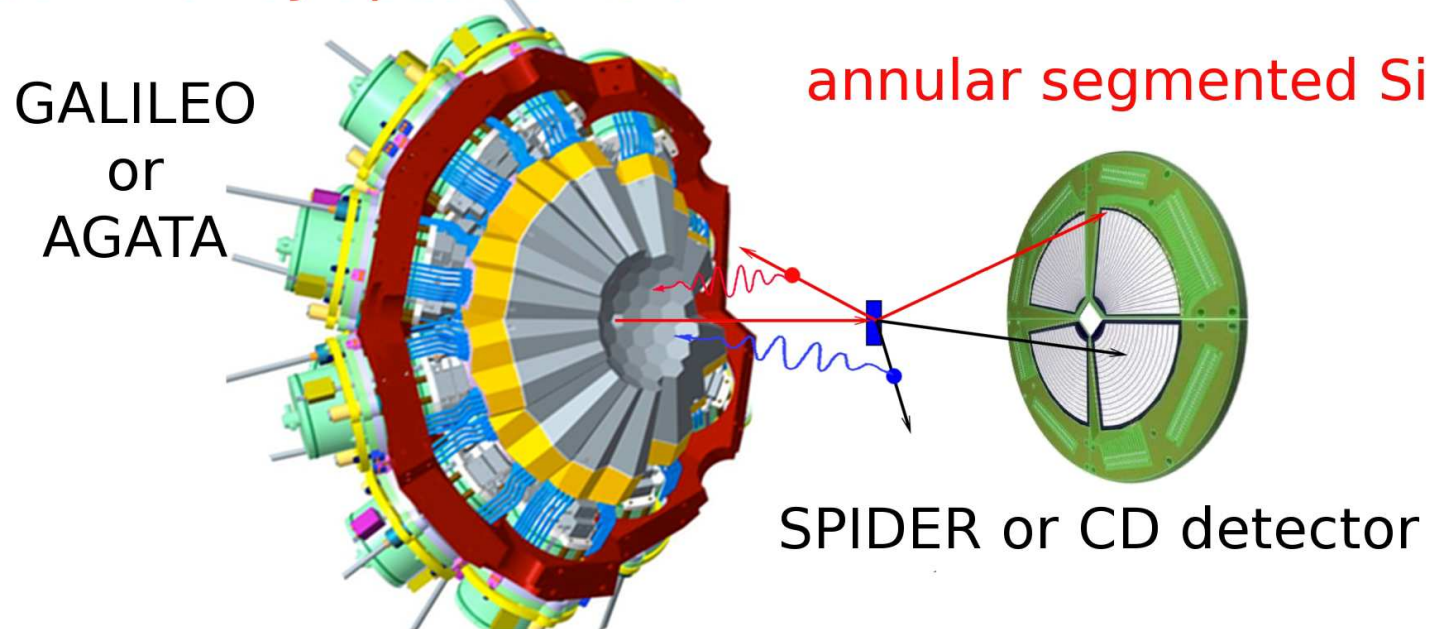


- Triaxiality in stable Ge isotopes confirmed by measured transition probabilities
  - Full quadrupole sum rules approach or approximate evaluation consistent
- Transition probabilities and quadrupole moments in neutron-rich Ge isotopes crucial to understand evolution of triaxiality towards  $N=50$
- Expected high intensities of Ge beams from SPES make a low-energy Coulex experiment feasible in a short measuring time

## Experimental setup

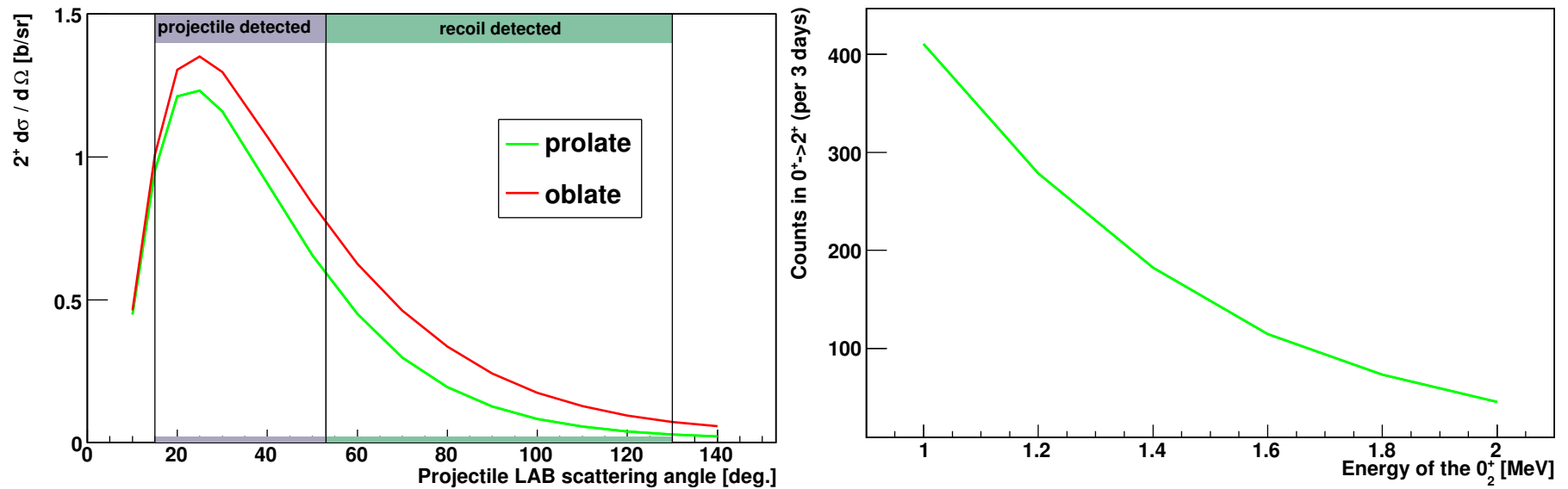
- standard Coulex setup with annular DSSSD detector placed at forward angles; detection of recoils and scattered projectiles

### Gamma-ray spectrometer



- intense SPES beams ( $^{78,80}\text{Ge}$ :  $10^6$  pps,  $^{82}\text{Ge}$ :  $10^5$  pps)
- heavy targets (Pb, Pt) to maximise Coulex cross section
- GOSIA calculations for 2 mg/cm<sup>2</sup> Pb target

# What can we obtain with SPES beams?



- quadrupole moments of  $2_1^+$  states in  $^{78,80,82}\text{Ge}$ : rough estimate in one day of beamtime at  $10^5$  pps, precise measurement (20-30% accuracy) possible at  $10^6$  pps
- quadrupole moments of  $2_2^+$  states in  $^{78,80}\text{Ge}$  measurable at  $10^6$  pps
- lifetimes of higher lying states – few days at  $10^5$  pps enough to get lifetimes of  $4_1^+$  and  $2_2^+$  states in  $N=50$   $^{82}\text{Ge}$
- possibility to identify the (unknown but predicted)  $0_2^+$  state in  $^{80}\text{Ge}$  in a few days measurement at  $10^6$  pps
- detailed information on transition probabilities and static moments for  $^{78,80,82}\text{Ge}$ , possibility to extract triaxiality parameters for  $^{78,80}\text{Ge}$  via quadrupole sum rules approach

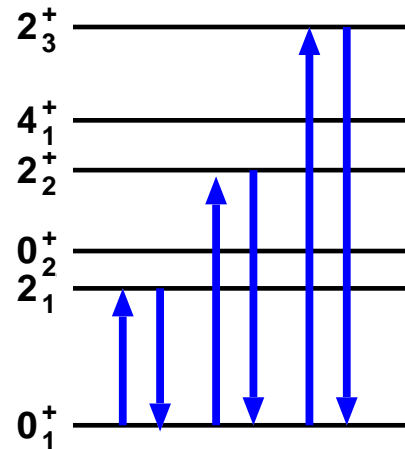
# Quadrupole sum rules

D. Cline, Ann. Rev. Nucl. Part. Sci. 36 (1986)

K. Kumar, PRL 28 (1972)

- electromagnetic multipole operators are spherical tensors → products of such operators coupled to angular momentum 0 are rotationally invariant
- operator products may be expressed using the intermediate state expansion formula

$$\frac{\langle Q^2 \rangle}{\sqrt{5}} = \langle i | [E2 \times E2]^0 | i \rangle = \frac{1}{\sqrt{(2I_i + 1)}} \sum_t \langle i || E2 || t \rangle \langle t || E2 || i \rangle \left\{ \begin{matrix} 2 & 2 & 0 \\ I_i & I_i & I_t \end{matrix} \right\}$$



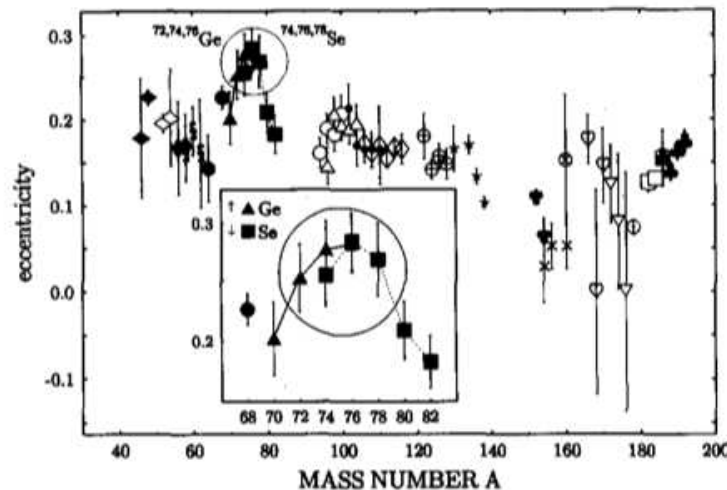
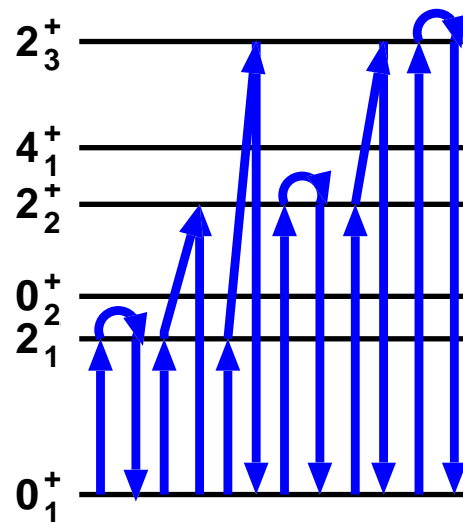
$\langle Q^2 \rangle$ : overall deformation parameter

# Quadrupole sum rules: triaxiality

D. Cline, Ann. Rev. Nucl. Part. Sci. 36 (1986)

K. Kumar, PRL 28 (1972)

$$\begin{aligned} \sqrt{\frac{2}{35}} \langle Q^3 \cos 3\delta \rangle &= \langle i | \{ [E2 \times E2]^2 \times E2 \}^0 | i \rangle \\ &= \frac{1}{(2I_i + 1)} \sum_{t,u} \langle i || E2 || u \rangle \langle u || E2 || t \rangle \langle t || E2 || i \rangle \left\{ \begin{array}{ccc} 2 & 2 & 2 \\ I_i & I_t & I_u \end{array} \right\} \end{aligned}$$



A. Andrejtscheff *et al*, Phys. Lett. B 329 (1994) 1

$\langle \cos 3\delta \rangle$ : triaxiality parameter