



# Laser induced plasma channels by nanosecond to femtosecond pulses

Danilo Giulietti Physics Department of the University & INFN Pisa, Italy

## SUMMARY

- NANOSECOND LASER-MATTER INTERACTION AT HIGH INTENSITIES
- **FEMTOSECOND** LASERS-MATTER INTERACTION AT RELATIVISTIC INTENSITIES
- SELF-PHASE MODULATION OF LASER-PULSE
- RELATIVISTIC SELF-FOCUSING
- PLASMA TRANSPARENCY AND CHANNELING
- LASER PLASMA ACCELERATION
- BETATRON RADIATION
- CONCLUSIONS AND PERSPECTIVES

Nanosecond laser pulse on solid target @ 10<sup>14</sup> W/cm<sup>2</sup>



### Spatial growth rate of the filamentation instability

$$K = \frac{k_{\perp}}{2\sqrt{\varepsilon}} \left[ 2\frac{n_e}{n_c} \left( \gamma_p + \gamma_T \frac{\kappa_{_{SH}}}{\kappa_{_{FP}}} \frac{k_L^2}{k_{\perp}^2} \right) - \frac{k_{\perp}^2}{k_L^2} \right]^{1/2}$$

$\gamma_p = (1/4)(Z/(Z+1))(v_q^2/v_{th}^2)$	ponderomotive effects
$\gamma_{T} = c^{2} S / \omega^{2} \kappa_{SH} k_{B} T_{e}$	thermal effects
$-\frac{k_{\perp}^2}{k_L^2}$	diffraction effects
$\varepsilon = 1 - n_e / n_c$	plasma dielectric function
$\kappa_{\rm SH}$ and $\kappa_{\rm FP}$	Spitzer-Härm and effective Fokker-Planck conductivity
$k_{\perp}$	wave-number of the sinusoidal spatial modulation
$v_q$ and $v_{th}$	electron quiver and thermal velocity
Ζ	charge state of the plasma
S and $T_e$	background inverse bremsstrahlung heating rate and electron temperature

D. GIULIETTI et al. INTENSE DIFFRACTION OF A LASER-BEAM DUE TO SELF-FOCUSING IN UNDERDENSE PLASMA. JOURNAL OF APPLIED PHYSICS, vol. 58, p. 2916-2921, 1985.

D. GIULIETTI, REFRACTION EFFECTS IN LASER PLASMA INTERACTION. OPTICS COMMUNICATIONS, vol. 68, p. 399-403, 1988.

## PONDEROMOTIVE HOLE-BORING

$$\begin{array}{l} Ponderomotive \ force\\ non \ relativistic \ \left\langle U_{q}\right\rangle =\frac{e^{2}E^{2}}{4m\omega^{2}} \Rightarrow F_{p}=-\nabla\left\langle U_{q}\right\rangle =-\frac{2\pi e^{2}}{mc\omega^{2}}\nabla\left\langle I\right\rangle\\ relativistic \ \left\langle U_{q}\right\rangle =mc^{2}(\gamma-1) \Rightarrow F_{p}=-mc^{2}\nabla\gamma\approx-mc^{2}\nabla a=-\frac{e\sqrt{8\pi c}}{\omega}\nabla\left\langle I\right\rangle^{\frac{1}{2}}\end{array}$$

### PRE-FORMED CHANNEL (1)



The laser pulse propagates in a plasma channel acting as a focusing lens that counter-balances the diffraction effects. For the optimal channel shape, laser pulses can be guided over distances exceeding several  $Z_R$ .

### PRE-FORMED CHANNEL (2)

A nanosecond pre-pulse (ASE of the Ti:Sapphire LASER) ionizes a gas-jet (He, Ar...) in the focal region. The pre-pulse self-focusing produces in the plasma a channel extending for several mm.



PRE-FORMED CHANNEL (3)



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#### Target: subsonic jet of He, 3mm x 0.3mm rectangular slit Pressure in the reservoir: 5 to 8 bar

A.Gamucci, Experimental study of stable propagation and efficient electron acceleration in plasmas with ultra-short laser pulses, PhD Thesis at Pisa University, Supervisor Prof. D. Giulietti, 2009





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## **Relativistic Intensities (1)**

$$I = uv_g = \varepsilon_0 E^2 c \cdot n$$
  
for  $n \approx 1$   $E_{V/cm} \approx 27.5 I_{W \cdot cm^{-2}}^{\frac{1}{2}}$   
 $n = \left(1 - \frac{\omega_p^2}{\omega^2}\right)^{\frac{1}{2}}$   $\omega_{pe} = \left(\frac{n_e e^2}{\varepsilon_0 m\gamma}\right)^{\frac{1}{2}}$   
 $\gamma = \left(1 - \beta^2\right)^{-\frac{1}{2}}$   $\beta = \frac{v}{c}$   
 $\gamma = \left(1 + \frac{\alpha a^2}{2}\right)^{\frac{1}{2}} \alpha = 1 (lin. p.); 2 (circ. pol.)$   
 $a = \frac{eE}{m\omega c} \approx 8.5 \cdot 10^{-10} \cdot I_{W \cdot cm^{-2}}^{\frac{1}{2}} \cdot \lambda_{\mu m}$ 

## **Relativistic Intensities (2)**

for 6J, 20 fs @  $\lambda \approx 0.815 \mu m$  laser pulse  $\pi \approx 10^{21} W \cdot cm^{-2} \longrightarrow a \approx 22$   $E \approx 10^{12} V/cm \gg E_{at} \approx 5 \cdot 10^9 V/cm$  $B \approx 10 GGauss$ 

$$P = \frac{I}{c} \approx 6.6 \cdot 10^{16} \, N/m^2 \approx 660 \, GBar$$
$$a \approx 22 \Rightarrow \gamma \approx 15.5 \Rightarrow E_{cin} = mc^2(\gamma - 1) \approx 7 MeV$$

## Femtosecond laser-solid thick target interactions

The characteristic time of the hydrodynamic expansion of laser produced plasmas, i.e. the time taken by the plasma to expand by a length comparable with the laser wavelength  $\lambda$ , is of the order of a few picoseconds. Therefore, the use of femtosecond laser pulses enables to study (in principle!) the interaction of intense optical radiation with plasmas characterised by solid density (5 × 10<sup>23</sup> el / cm<sup>3</sup>) and ultra-steep gradients.

- $L = c_s \Delta t$  plasma density scale length perpendicular to the target surface
- *c*<sub>s</sub> sound speed
- $\Delta t$  laser pulse duration

for  $\Delta t \approx 100$  fs and  $c_s = 10^7$  cm / sec  $\rightarrow L \approx 100$  Å  $\ll \lambda$ 

### Femtosecond laser-solid thin target interactions

A smart use of the ASE radiation accompaining the main ultra-short, super-intense laser pulse is possible: 1) The ASE produces an exploding-foil plasma with the demanded characteristics

### 2) The main pulse interact with the pre-formed plasma

D. Giulietti et al., High-energy electron beam production by femtosecond laser interactions with exploding-foil plasmas, Phys, Rev. E, Rapid. Comm., **64**, 015402(R), 2001.

D. Giulietti et al., Production of ultracollimated bunches of multi-MeV electrons produced by 35fs laser pulses propagating in exploding foil plasmas, Physics of Plasmas, **9**, 3655, 2002.





## ELECTRON DENSITY PROFILE



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## **SELF-PHASE MODULATION OF LASER-PULSES**

$$\phi = kz - \omega_0 t \quad \omega = -\frac{\partial \phi}{\partial t} = \omega_0 - k_0 z \frac{\partial n}{\partial t}$$

$$plasma \ refraction \ index \ n = \left(1 - \frac{n_e}{n_c}\right)^{\frac{1}{2}} \approx 1 - \frac{1}{2} \frac{n_e}{n_c} \implies \frac{\omega - \omega_0}{\omega_0} = \frac{z}{2cn_c} \frac{\partial n_e}{\partial t}$$

*ionization* 
$$\frac{\partial n_e}{\partial t} \rangle 0 \Rightarrow blue shift$$
  
*channel formation*  $\frac{\partial n_e}{\partial t} \langle 0 \Rightarrow red shift$ 

Example: 
$$n_c = 1.7 \times 10^{21} cm^{-3}$$
;  
 $z = 0.5 cm$ ;  
 $\tau = 40 fs$ ;  $\Rightarrow \frac{\omega - \omega_0}{\omega_0} \approx 6$ !!!  
 $\Delta n_e = 5 \times 10^{17} cm^{-3}$ 

AFSHARRAD T, COE S, GIULIETTI A, GIULIETTI D, WILLI O (1991). THE EFFECT OF SELF-PHASE MODULATION ON STIMULATED BRILLOUIN-SCATTERING IN FILAMENTARY LASER PLASMAS. EUROPHYSICS LETTERS, vol. 15, p. 745-751, 1991.

GIULIETTI D, BIANCALANA V, BORGHESI M, CHESSA P, GIULIETTI A, SCHIFANO E., SPECTRALLY MODULATED 2ND-HARMONIC EMISSION FROM LASER-PLASMA FILAMENTS. OPTICS COMMUNICATIONS, vol. 106, p. 52-58, 1994.

## **Relativistic self-focusing**

$$P_{cr} = \frac{mc^5\omega^2}{e^2\omega_{pe}^2} \approx 17 \left(\frac{n_c}{n_e}\right) GW$$

Example: for  $\lambda_0 = 0.815 \mu m$  and  $n_2 = 10^{18} cm^{-3} \implies P_{cr} \approx 29 TW$ 

The laser pulse can be self-focused over distances much larger than the Rayleigh length

$$Z = \frac{\pi w_0^2}{\lambda_0}$$

where  $w_0$  is the laser pulse waist at the focus.

## Relativistic trasparency



*Example* :  $\lambda_0 = 0.815 \mu m$ ;  $I = 10^{21} W cm^{-2} \implies n_e < 2.6 \times 10^{22} cm^{-3}$ 

## Magnetically Induced Optical Transparency

Laser light can propagate through an overdense magnetized plasma as an extraordinary mode provided that:

 $n_e < n_c \left(1 - \frac{\Omega}{\omega}\right)$  where  $\Omega = \frac{eB_0}{mc}$  is the cyclotron frequency and  $B_0$  is a static magnetic field perpendicular to the wavevector and parallel to the oscillating magnetic field

Example: 
$$\lambda_0 = 0.815 \mu m; \frac{n_e}{n_c} \approx 50 \implies B_0 \ge 1GGauss$$

Giulietti D. et al., Observation of solid-density laminar plasma transparency to intense 30 femtosecond laser pulses. PHYSICAL REVIEW LETTERS, vol. 79, p. 3194-3197, 1997. Teychenne D. et al., Magnetically induced optical transparency of overdense plasmas due to ultrafast ionization. PHYSICAL REVIEW E, vol. 58, 1998.

### LASER PLASMA ACCELERATION (1)



## LASER PLASMA ACCELERATION (2)



for 
$$\gamma_p \approx \frac{\omega}{\omega_{pe}} >> 1 \implies \Delta W_{\text{max}} = 4\gamma_p^2 \frac{\delta n_e}{n_e} mc^2$$

energy gain along 
$$L_{deph} \approx \gamma_p^2 \lambda_p$$
,  $\lambda_p \approx \frac{2\pi \alpha}{\omega_{pe}}$ 

$$\Delta W_{\max} \approx e E_{\max} \cdot L_{deph} \propto n_e^{\frac{1}{2}} \cdot \frac{1}{n_e} \cdot n_e^{-\frac{1}{2}} = \frac{1}{n_e}$$

## introduction

Joint experiment Phys. Depart. Pisa Univ., Italy ILIL (IPCF-CNR, Italy) PHI (CEA/Saclay, France) LULI (Ecole Politechnique, France) ITU (Karlsruhe, Germany) @ SLIC laser facility of CEA/Saclay



UHI10 Ti:Sa laser system: 10 TW peak power, 65 fs, up to 0.7 J at  $\lambda$ =800 nm

- ➡ focusing: f/5 OAP
- $\Rightarrow a_0 \leq 2$
- i ⇒ w<sub>0</sub> = 13 μm
- I = 8.5x10<sup>18</sup> W/cm<sup>2</sup>
- He supersonic gas-jet target

 systematic study of electron acceleration
 investigation of several different conditions in laser & target parameter space

A.Gamucci, Experimental study of stable propagation and efficient electron acceleration in plasmas with ultra-short laser pulses, PhD Thesis at Pisa University, Supervisor Prof. D. Giulietti, 2009

### set-up



### propagation @ CEA/Saclay



Two regimes of gas density have been experimentally investigated:

Above ASE ionization threshold

## beam profile monitor

#### $\varnothing$ = 1 mm, P = 6-10 bar (1)(3)200 mrad 200 mrad (10)300 mrad 200 mrad 200 mrad

Single bunch ⊘ = 1 mm, P = 6-10 bar

- ✓ 10 consecutive shots, fairly good collimation
- high reproducibility (even over several days)
- Iow backing pressure
- ✓ mean divergence:
- ~35 mrad for # 1,2,3,6,10
- ~48 mrad for # 4,5,7,8,9 (halo)

### Multi-bunches



- ✓ multiple bunches simultaneously present
- ✓ high backing pressure
- ✓ fairly good collimation of single bunches
- ✓ low reproducibility

## magnetic spectrometer

5.0e+04

#### Quasi-monoenergetic spectra



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#### Major benefits

✓ Gives simultaneously the angular divergence, the spectrum and the absolute number of impinging e<sup>-</sup> beam

✓ Robust and compact set-up

✓ First-sight idea of the beam features





M. Galimberti, Electron trapping and acceleration by relativistic laser interactions with underdense plasmas, PhD Thesis, Supervisor Prof. D. Giulietti, Pisa University 2003.



## Complete raw set of 19 RCFs after exposure to **10 consecutive shots**



#### Notable features (qualitative)

- 1. Every layer is impressed
- 2. Only the central component survives up to the 19<sup>th</sup> layer
- 3. That is the region in which the most energetic electrons are
- 4. The low-energy halo disappears with depth in the device
- Up to 10<sup>th</sup> layer some radial structures ...comparison with BPM (single shot):



 $\varnothing$  = 4 mm, P = 25 bar

## SHEEBA



## Betatron radiation from LASERproduced plasmas

## **Bubble regime 1/3**

- Relativistic parameter  $a_0 \ge 3$
- LASER intensity I₀ ≥ 10<sup>18</sup> W/cm<sup>2</sup>
   Ponderomotive forces → Bubble

• Radius of the bubble 
$$R \approx \sqrt{2}a_0 \frac{c}{\omega_p}$$

Non linear wakefield

• Velocity of the wake 
$$v_{\varphi} \approx \left(1 - \frac{3\omega_p^2}{2\omega_0^2}\right) = v_g$$

## **Bubble regime 2/3**



Lu, W., Tzoufras, M. & Joshi, C.Generating multi-GeV electron bunches using single stage laser wakefield acceleration in a 3D nonlinear regime. Phys. Rev. 10, 061301 (2007).

## **Acceleration parameters**

Dephasing length

$$L_{deph} \approx \frac{2\omega_0^2}{3\omega_p^2}R$$



## **Betatron oscillations**



## Analogy with a wiggler



$$\lambda_w = \frac{L}{2\gamma_0^2} \left(1 + \frac{K_w}{2} + \gamma_0^2 \theta^2\right)$$
$$K_w = 0.934 * B[T] * L[cm]$$
$$\lambda_\beta = \sqrt{2}\lambda_p \gamma_0^{-3/2} \left(1 + \frac{K}{2} + \gamma_0^2 \theta^2\right)$$
$$K = \gamma_0 \lambda_b \tau_b$$

## **Pulse duration**



$$T_p = L_{deph} \frac{c - v_{\varphi}}{c^2}$$



A. Curcio, *High brilliance X- ray sources based on LASER-matter interaction at high intensities*. Master degree Thesis, Supervisor Prof. D. Giulietti, Pisa University, 2014.

## A more realistic model 1/2

Electrons emit during the acceleration



$$r(t) = \frac{r_0}{P_v(-\varepsilon)} P_v(\varepsilon t/t_{deph} - \varepsilon)$$

$$\gamma_{max}(1-\varepsilon) = \gamma_{min}$$



## A more realistic model 2/2

 $\gamma_0 \approx 400, \quad n_e = 10^{18}/cm^3, \ Q_B \approx 100 \ pC, \quad r_b \approx 3 \ \mu m, \ K \approx 40$ 



A. Curcio, *High brilliance X- ray sources based on LASER-matter interaction at high intensities*. Master degree Thesis, Supervisor Prof. D. Giulietti, Pisa University, 2014.

## Diagnostics of plasma- accelerated electron bunches 1/2



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## Diagnostics of plasma- accelerated electron bunches



 $r_x \approx r_y$  $p_x \approx p_y$ 

#### Radiation collected at 1 meter

A. Curcio, *High brilliance X- ray sources based on LASER-matter interaction at high intensities*. Master degree Thesis, Supervisor Prof. D. Giulietti, Pisa University, 2014.



The propagation of super-intense and ultra-short laser pulses in plasmas is a main concern in several applications of the laser-plasma interactions, from ICF to HEP.

During the propagation in the plasma the light beam deeply changes its parameters, inducing at the same time the relativistic regime of the electron quivering motion.

These extreme conditions are suitable for the electron acceleration in high field gradients, opening to the realization of compact secondary sources of radiation (X-gamma rays ) and particles (ions,  $e^+$ , ....)

D Giulietti, The particle laser-plasma acceleration in Italy. JOURNAL OF PHYSICS. CONFERENCE SERIES, vol. 508, 2014

M. Ferrario et al., Interdisciplinary research infrastructure based on dual electron linacs and lasers. NIM A, vol. 740, p. 138-146, 2014.



### **ROUND TABLE**

# Propagation of ultra-intense laser pulses in plasma channels and related phenomena

Danilo Giulietti Physics Department of the University & INFN Pisa, Italy

Research Institute for Nuclear Problems	Minsk
Pisa University	Pisa
LNF-INFN	Frascati
Alikhanian National Laboratory	Yerevan
Laboratoire Optique Appliquée	Palaiseau
Tomsk Polytechnic University	Tomsk
Akhiezer Institute for Theoretical Physics	Kharkon
Kiev National Shevchenko University	Kiev
Lebedev Physical Institute	Moscow
	Research Institutefor Nuclear Problems Pisa University LNF-INFN Alikhanian National Laboratory Laboratoire Optique Appliquée Tomsk Polytechnic University Akhiezer Institute for Theoretical Physics Kiev National Shevchenko University Lebedev Physical Institute

The propagation of super-intense and ultra-short laser pulses in plasmas is a main concern in several applications of the laser-plasma interactions, from ICF to HEP. During the propagation in the plasma the light beam deeply changes its parameters, inducing at the same time the relativistic regime of the electron quivering motion. These extreme conditions are suitable for the electron acceleration in high field gradient, opening to the realization of compact secondary sources of X-gamma rays. Colleagues from the major laser infrastructures and research centers participating to the Round Table will consider present and future links between the different applications of such physical phenomena.