

# Polycapillary Optics for Advanced X-ray Instrumentations

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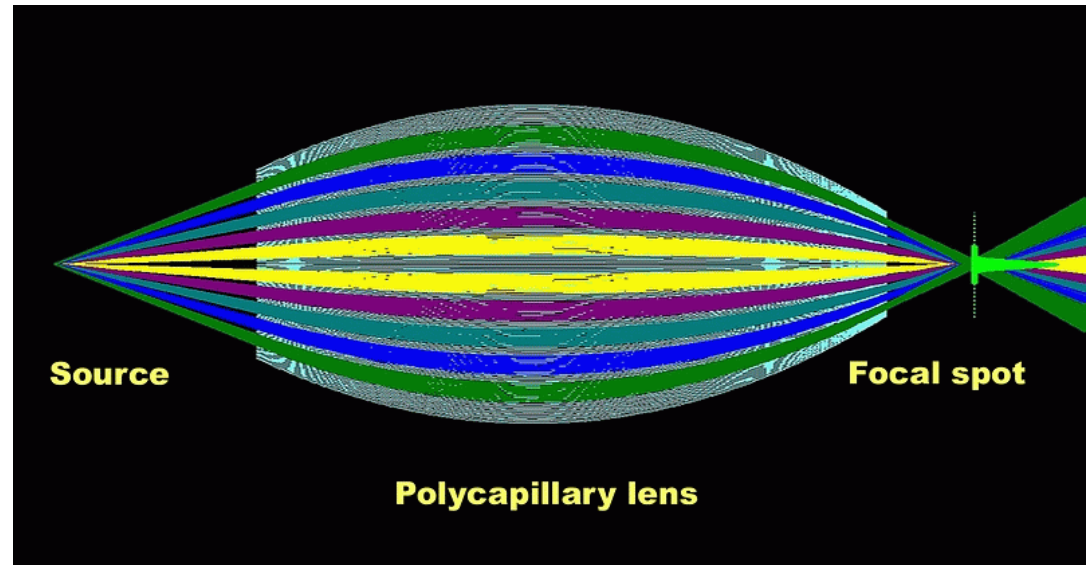


Prof. Kumakhov was Founder and Director  
Of the Institute of Roentgen Optics  
150 scientific publications and a lot of Patents

M.A.Kumakhov, Radiation of Channeled  
Particles(Energoatomizdat,Moscow,1986).

Sad news  
Prof. Kumakhov  
passed away on June 23,2014

He contributed immensely to  
Science and to the  
Channeling Conferences

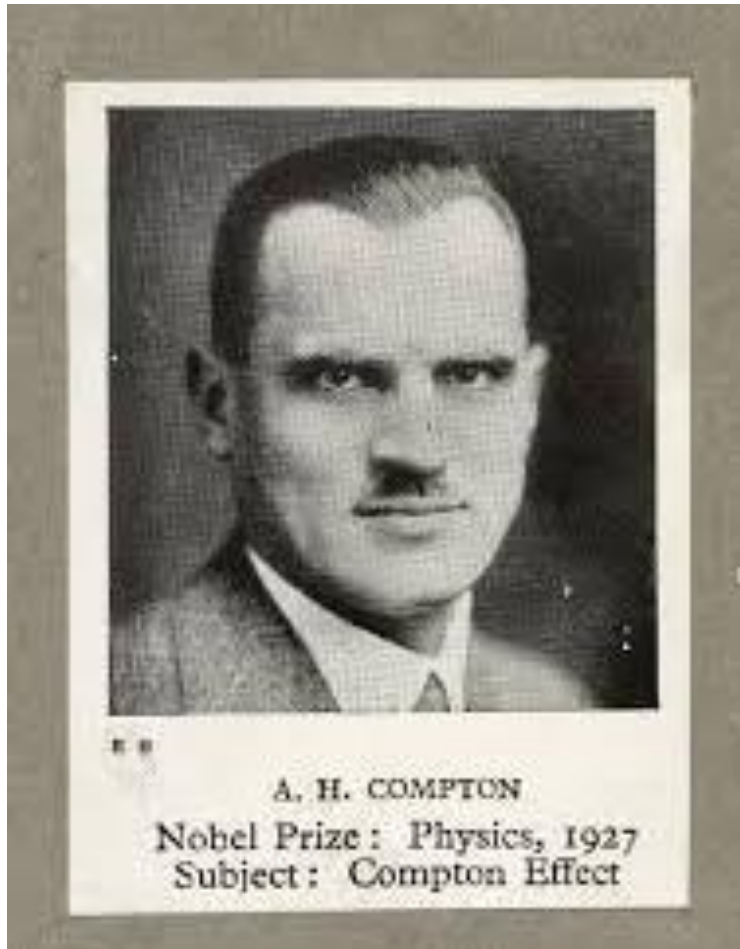




Discovered X-rays Nov. 8 1895 made  
A large number of experiments with the  
new kind of radiation:

Some conclusions were correct as  
absorption phenomena and ionizing  
effects

- X-rays cannot be refracted
- X-rays cannot be reflected
- X-rays propagate straight



## Experimental evidence of Total reflection of X-rays

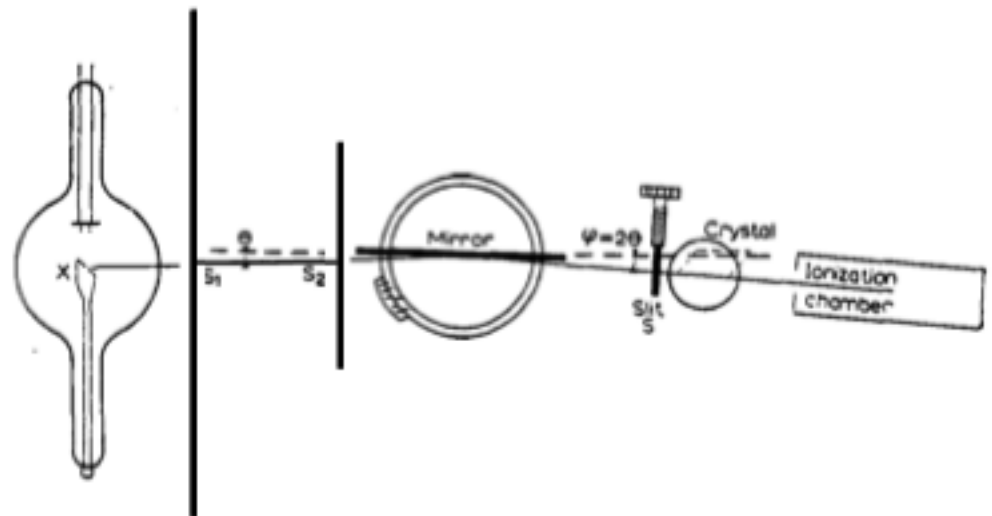


Fig. 1. Apparatus for studying the total reflection of X-rays.

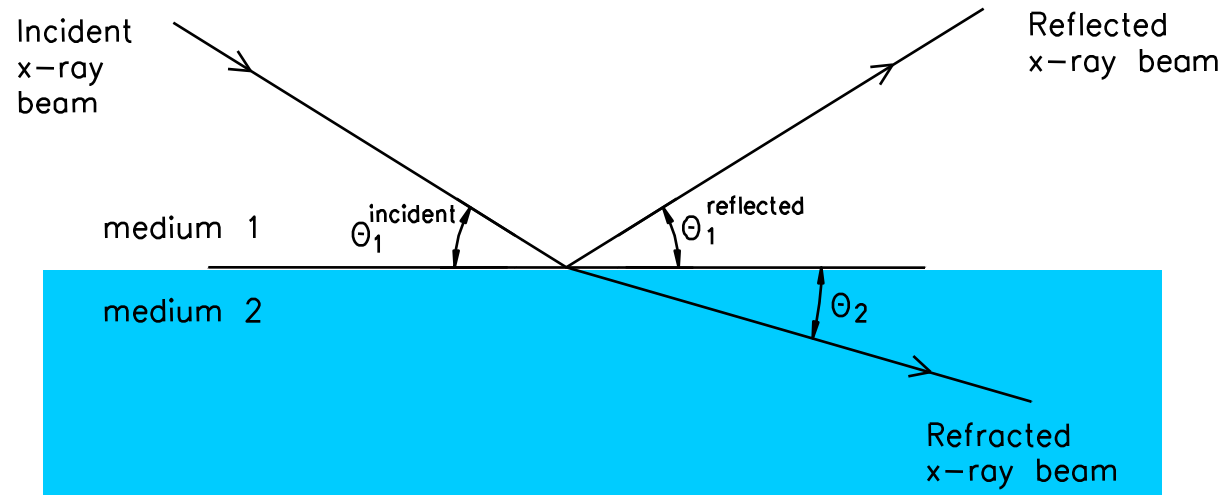
## *The refraction and reflection of X-rays*

We should consider the phenomena of refraction and reflection as one problem, since it is a well-known law of optics that reflection can occur only from a boundary surface between two media of different indices of refraction. If one is found, the other must be present.

In his original examination of the properties of X-rays, Röntgen<sup>1</sup> tried unsuccessfully to obtain refraction by means of prisms of a variety of materials such as ebonite, aluminum, and water. Perhaps the experiment of this type most favorable for detecting refraction was one by Barkla<sup>2</sup>. In this work X-rays of a wavelength which excited strongly the characteristic K-radiation from bromine were passed through a crystal of potassium bromide. The precision of his experiment was such that he was able to conclude that the refractive index for a wavelength of  $0.5 \text{ \AA}$  probably differed from unity by less than five parts in a million.

Although these direct tests for refraction of X-rays were unsuccessful, Stenström observed<sup>3</sup> that for X-rays whose wavelengths are greater than about  $3 \text{ \AA}$ , reflected from crystals of sugar and gypsum, Bragg's law,  $n\lambda = 2D \sin \theta$ , does not give accurately the angles of reflection. He interpreted the difference as due to an appreciable refraction of the X-rays as they enter the crystal. Measurements by Duane and Siegbahn and their collaborators<sup>4</sup> showed that discrepancies of the same type occur, though they are very small indeed, when ordinary X-rays are reflected from calcite.

The direction of the deviations in Stenström's experiments indicated that the index of refraction of the crystals employed was less than unity. If this is the case also, for other substances, total reflection should occur when X-rays in air strike a polished surface at a sufficiently sharp glancing angle, just as light in a glass prism is totally reflected from a surface between the glass and air if the light strikes the surface at a sufficiently sharp angle. From a measurement of this critical angle for total reflection it should be possible to determine the index of refraction of the X-rays.



$$n \text{ (x-ray range) } = 1 - \delta - i\beta$$

$$\delta \sim 10^{-6} \quad \text{decrement } \delta \propto f_1(Z)$$

$$\beta \sim 10^{-8} \quad \text{absorption part}$$

$$\varphi_{\text{critical}} \approx \sqrt{2\delta} \propto \sqrt{\rho}/E$$

$$\varphi_{\text{critical}}$$

$$(\text{Si}, 17.5 \text{ keV}) \approx 0.1^\circ \approx 1.75 \text{ mrad}$$

$$(\text{Si}, 500 \text{ eV}) \approx 3.7^\circ \approx 64.6 \text{ mrad}$$

$f_1$  represents the scattering coefficient  
thus electronic structure of the atom

## Surface Studies of Solids by Total Reflection of X-Rays\*

L. G. PARRATT

*Cornell University, Ithaca, New York*

(Received March 22, 1954)

The critical angle and the shape of the observed curve are determined essentially by the electron density and are otherwise independent of the amorphous or crystalline structure, or of the orientation of crystallites on (or in) the surface. If the mirror interface is a sharply defined boundary between two uniform homogeneous media, the dispersion theory predicts the reflection curve. The predicted curve for air and glass is shown

of surfaces) improved experimental techniques in the production and control of the surfaces.

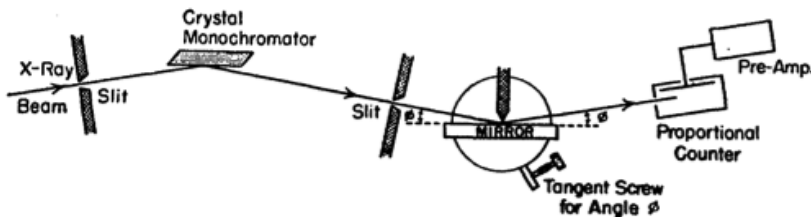


FIG. 1. Experimental arrangement for the x-ray total reflection method of studying smooth solid surfaces.

\* This research was supported by the United States Air Force through the Office of Scientific Research of the Air Research and Development Command.

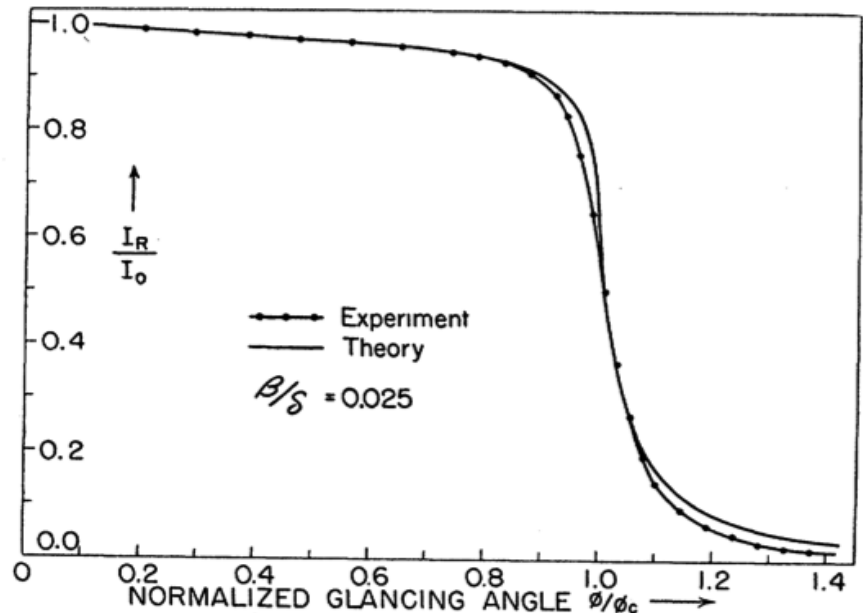


FIG. 2. Intensity reflected from polished glass at small angles of incidence. The angle  $\phi_c$  is the critical angle for total reflection.



## II. DISPERSION THEORY

### Two Homogeneous Media

For any glancing angle, the expressions for the electric vector of the incident beam  $E_1(z_1)$ , of the reflected beam  $E_1^R(z_1)$ , and of the refracted beam  $E_2(z_2)$  at a perpendicular distance  $z$  from the surface, are

$$\left. \begin{aligned} E_1(z_1) &= E_1(0) \exp\{i[\omega t - (k_{1,x}x_1 + k_{1,z}z_1)]\} \\ E_1^R(z_1) &= E_1^R(0) \exp\{i[\omega t - (k_{1,x}x_1 - k_{1,z}z_1)]\} \\ E_2(z_2) &= E_2(0) \exp\{i[\omega t - (k_{2,x}x_2 + k_{2,z}z_2)]\} \end{aligned} \right\}, \quad (1)$$

where  $k_1$  and  $k_2$  are the propagation vectors (of magnitudes  $2\pi/\lambda_1$  and  $2\pi/\lambda_2$ ) outside and inside the mirror, respectively,  $z$  is taken as positive into the mirror,  $x, z$  is the plane of incidence, refraction, and reflection of the beam, and the athwart direction  $y$  is parallel to the mirror surface. For x-rays, the glancing angle  $\phi_1$  (written hereafter without the subscript) is always very small, and we write

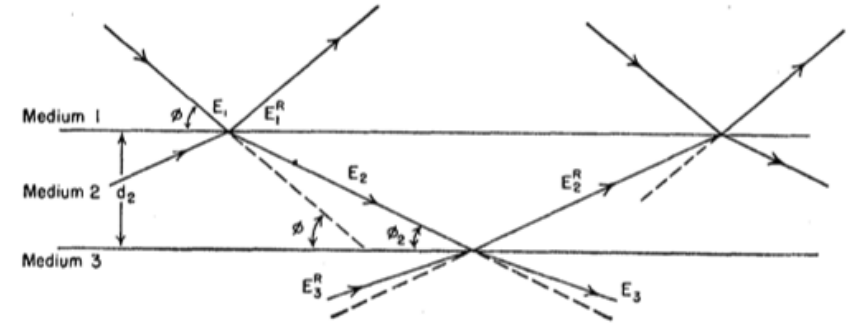


FIG. 4. Sketch of reflection and refraction for stratified homogeneous media.

### Shape of the Reflection Curve: Two Media

The Fresnel<sup>1</sup> coefficient for reflection,  $F_{1,2}$ , can be written

$$F_{1,2} = \frac{E_1^R}{E_1} = \frac{\sin\phi - r_2 \sin\phi_2}{\sin\phi + r_2 \sin\phi_2} \doteq \frac{\phi - f_2}{\phi + f_2} = \frac{f_1 - f_2}{f_1 + f_2}, \quad (3)$$

where

$$f_1 = (\phi^2 - 2\delta_1 - 2i\beta_1)^{\frac{1}{2}} = \phi.$$

The interaction of X-rays with atomic electrons in a substance is described by the complex dielectric constant:  $\epsilon = 1 - 2d - 2ib$  which yields the complex index of refraction:

$$n = \sqrt{\epsilon} = 1 - d - ib$$

The small quantities  $d$  and  $b$  are related to dispersive and absorptive natures of the material and given at X-ray wavelengths far from the absorption edges by:

$$d = ne^2 / 2pmc^2 \quad b = \mu / 4p$$

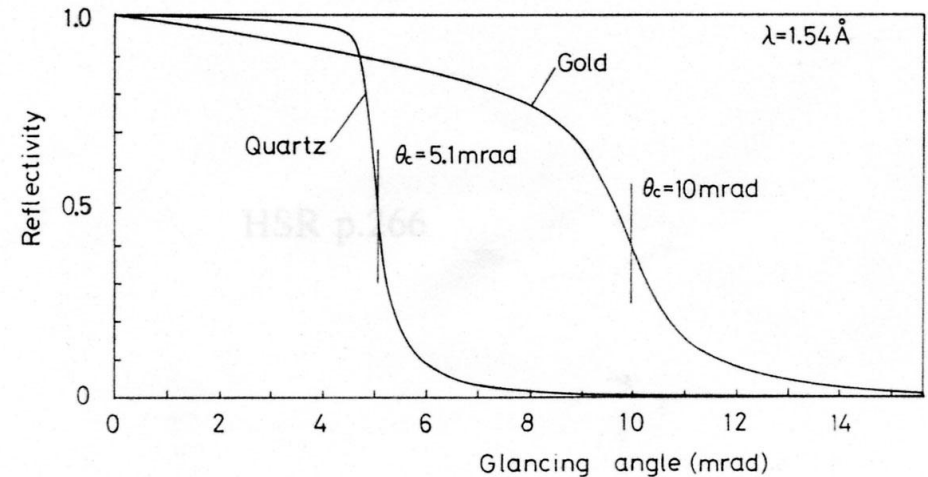
$n$  ...total number of dispersive electrons per unit volume of the material

$\mu$  ...linear absorption coefficient.

As the refractive index is less than unity, X-rays incident on a material are totally reflected if the glancing angle  $Q$  is less than the critical angle  $Q_c$ :

$$Q_c = \sqrt{2d} = 28.8 \times \frac{1}{E} \times \sqrt{\frac{Zr}{A}}$$

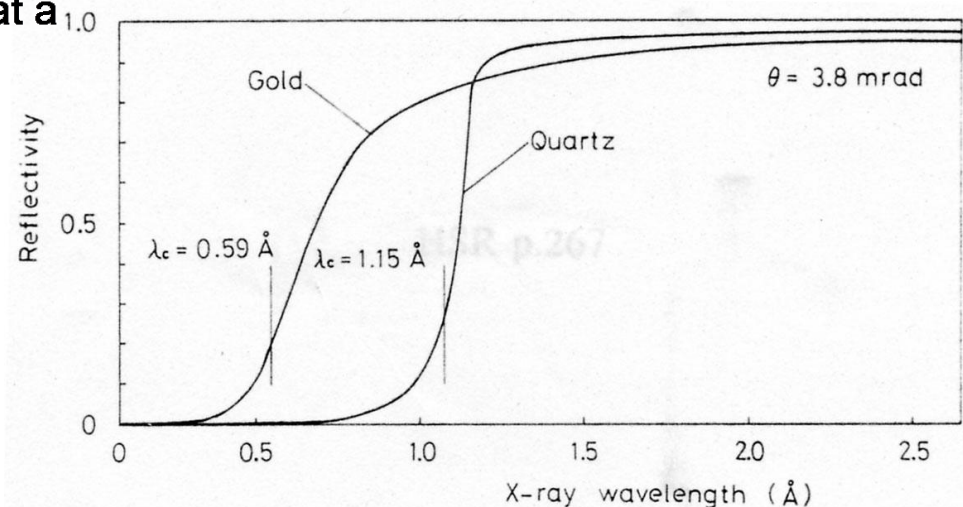
reflectivity curves for uncoated and gold coated quartz mirrors for 1.5 Å (8.04 keV).  
**→ heavy metals**, deposited on the mirror surface, **degrade the sharpness** of the **cut-off** as well as the **reflectivity near the critical angle**.

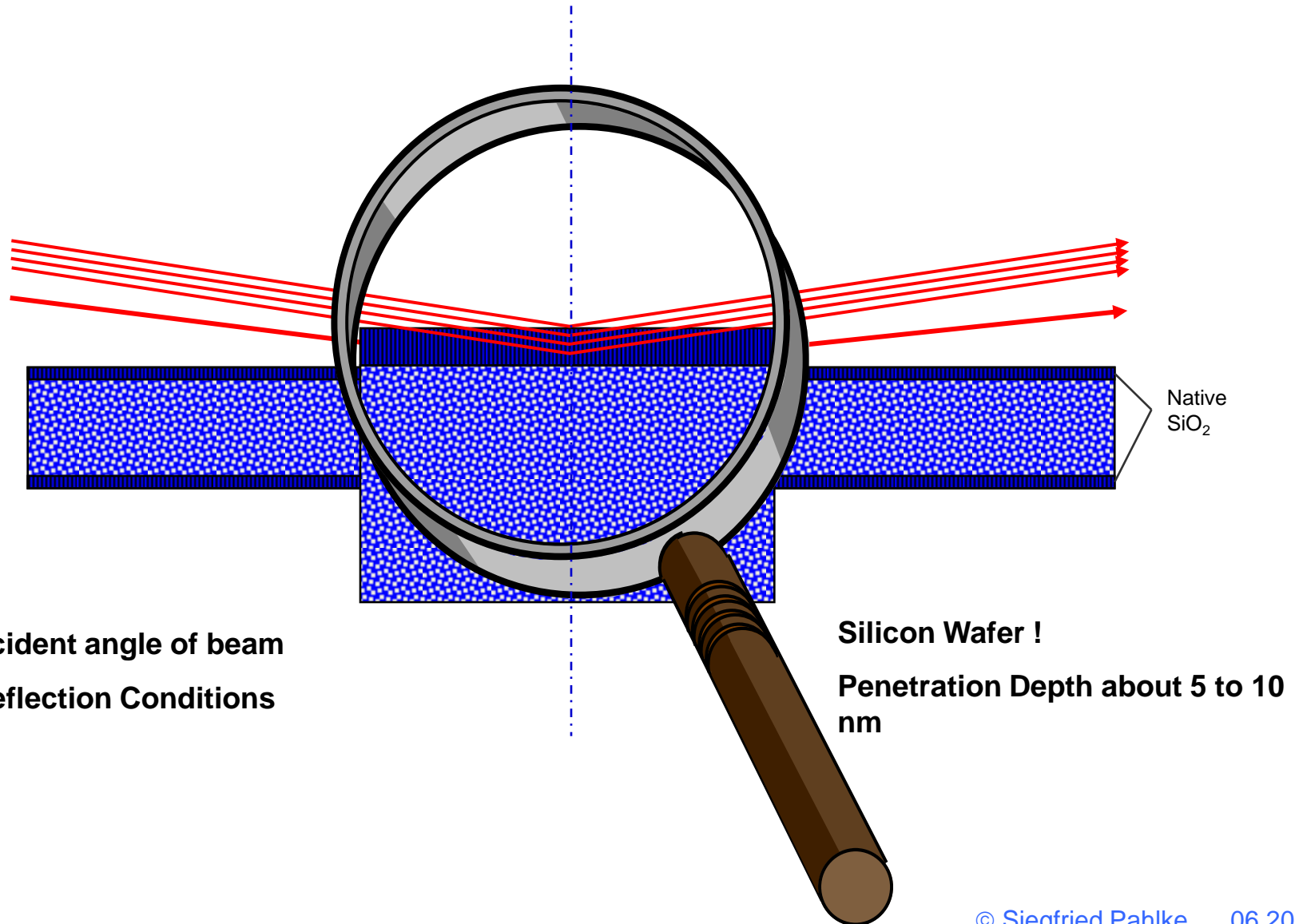


As  $\Theta_c$  is proportional to  $\lambda$ , a mirror set at a glancing angle  $\Theta$  does not reflect wavelength shorter than

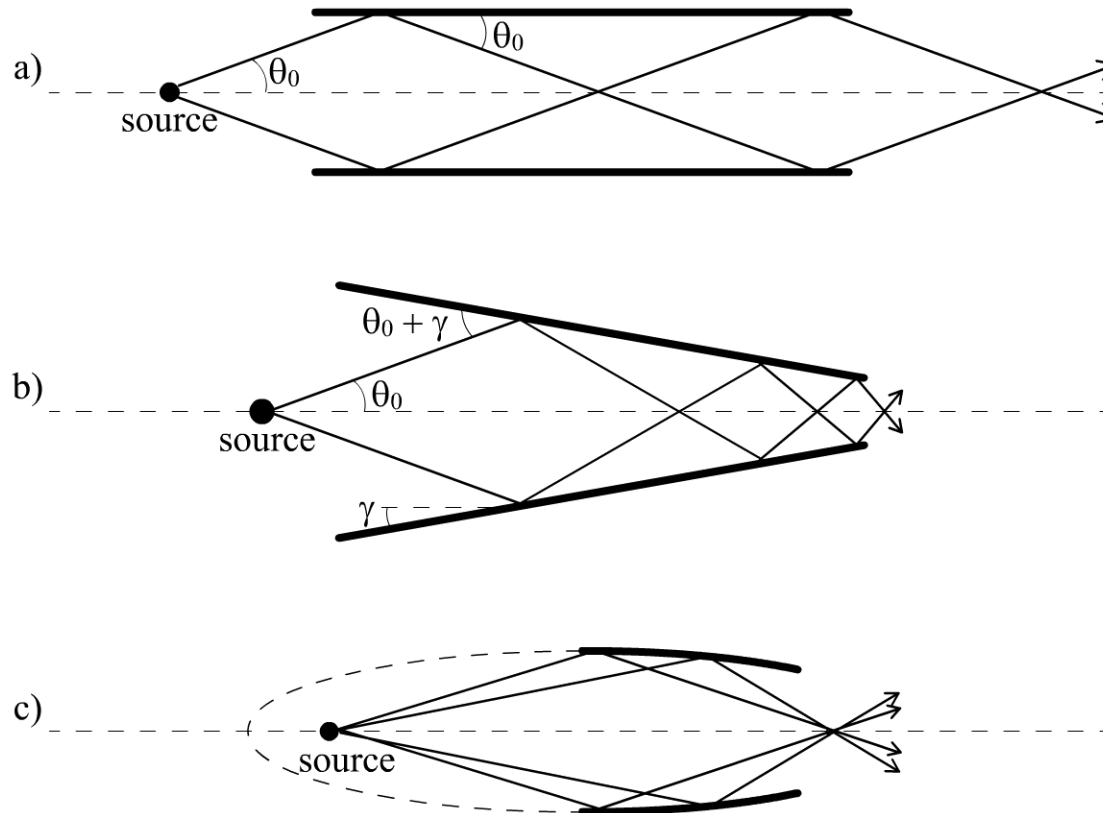
$$\lambda_c = \Theta \sqrt{\frac{\pi m c^2}{n e^2}} \quad E_c (\text{keV}) = \frac{32.2}{\Theta_c^{\text{Si}} (\text{mrad})}$$

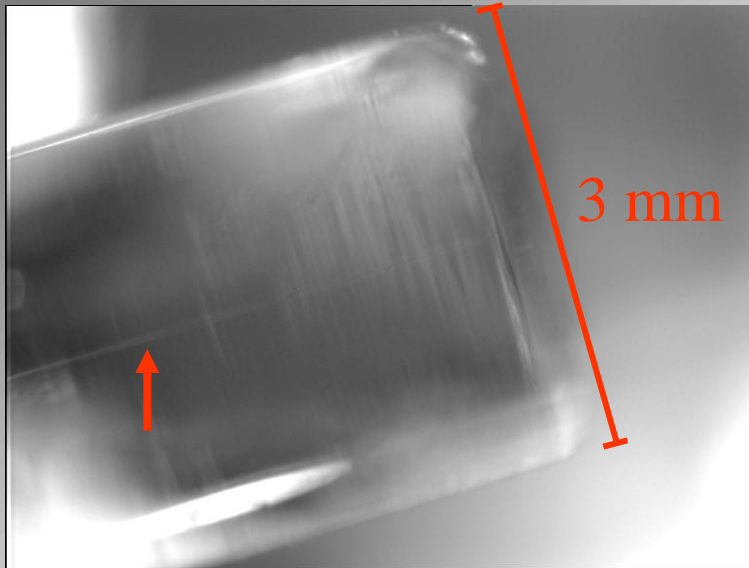
present in the incident beam.





## Monocapillaries





## tapered borosilicate capillary

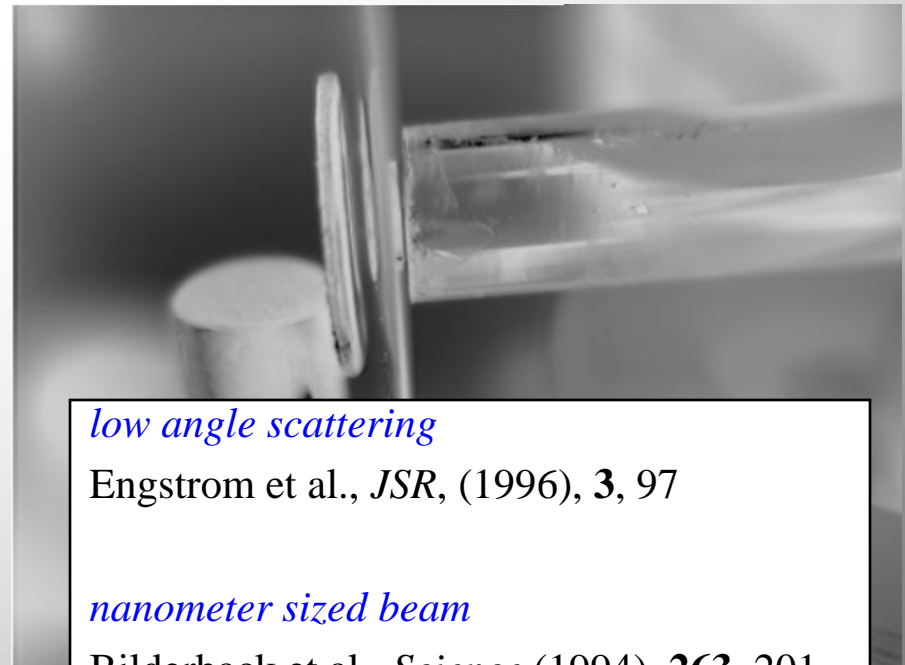
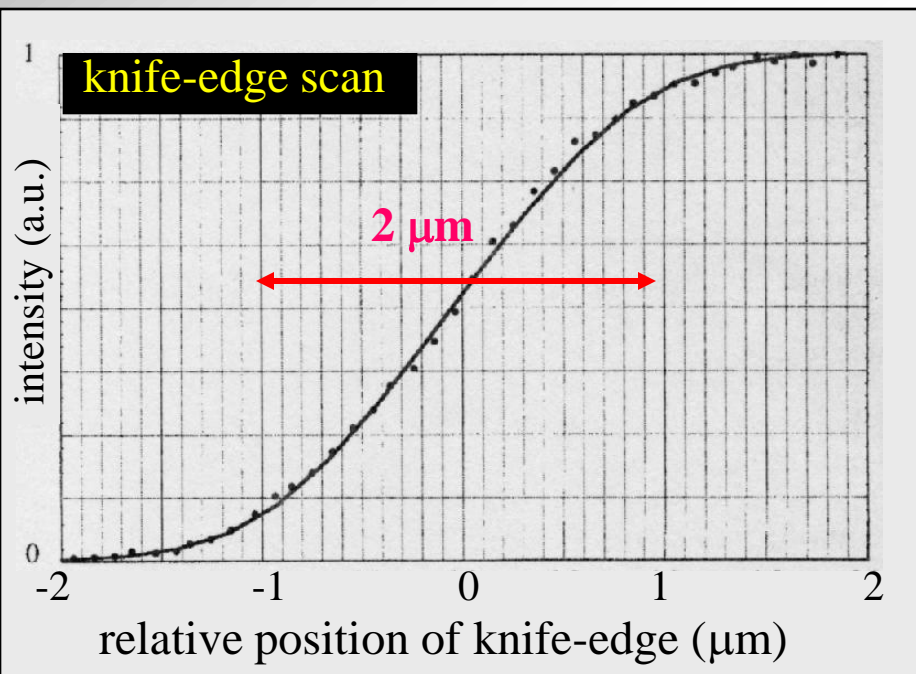
length about 100 mm

2  $\mu\text{m}$  diameter full width at base

2.3 mrad divergence @ 13 keV

flux  $\leq 3 \cdot 10^{10}$  ph/s/100mA

flux density  $\leq 1 \cdot 10^{10}$  ph/s/ $\mu\text{m}^2$ /100mA



## low angle scattering

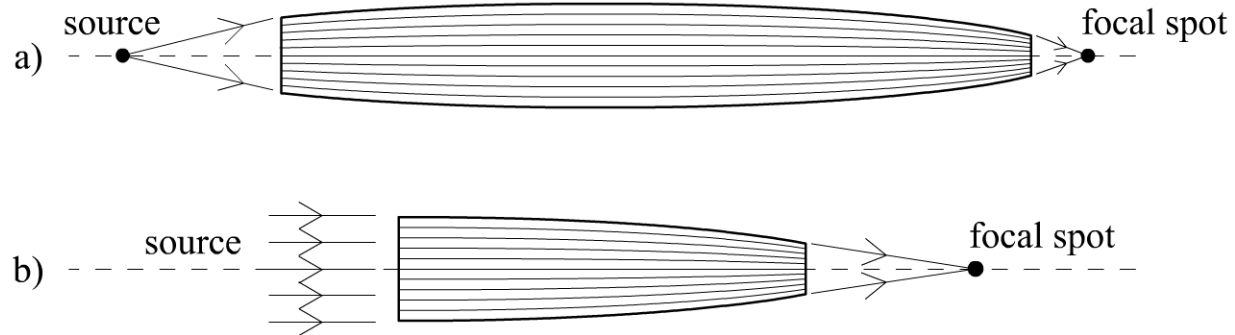
Engstrom et al., *JSR*, (1996), **3**, 97

## nanometer sized beam

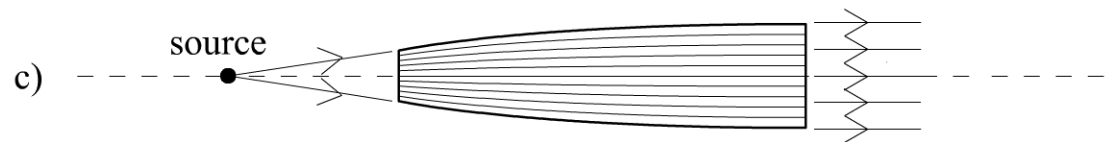
Bilderback et al., *Science* (1994), **263**, 201

## Polycapillaries

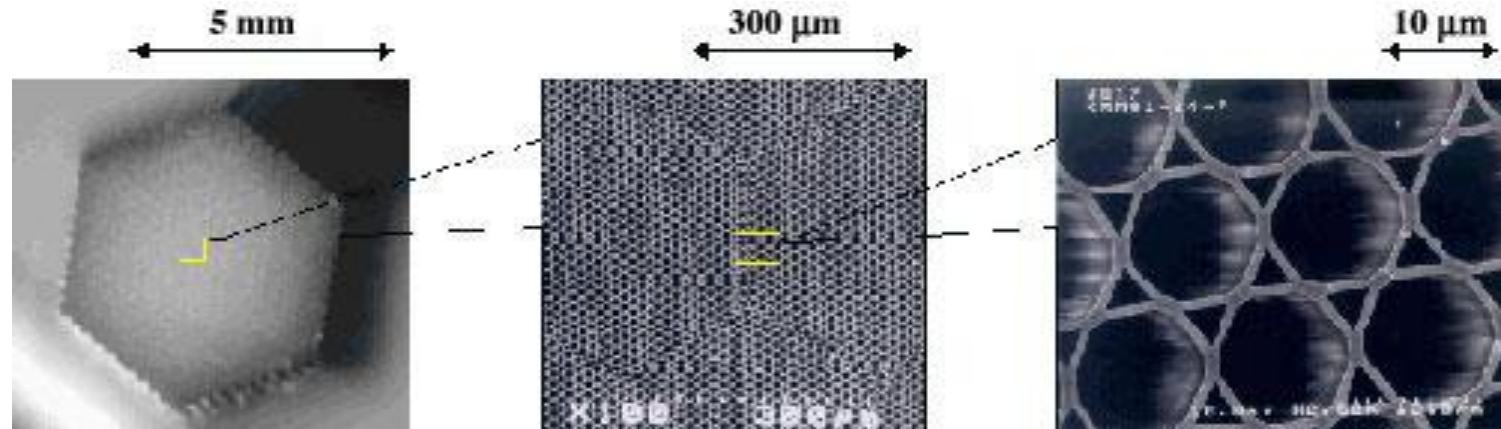
### Focusing optics



### Collimating optics

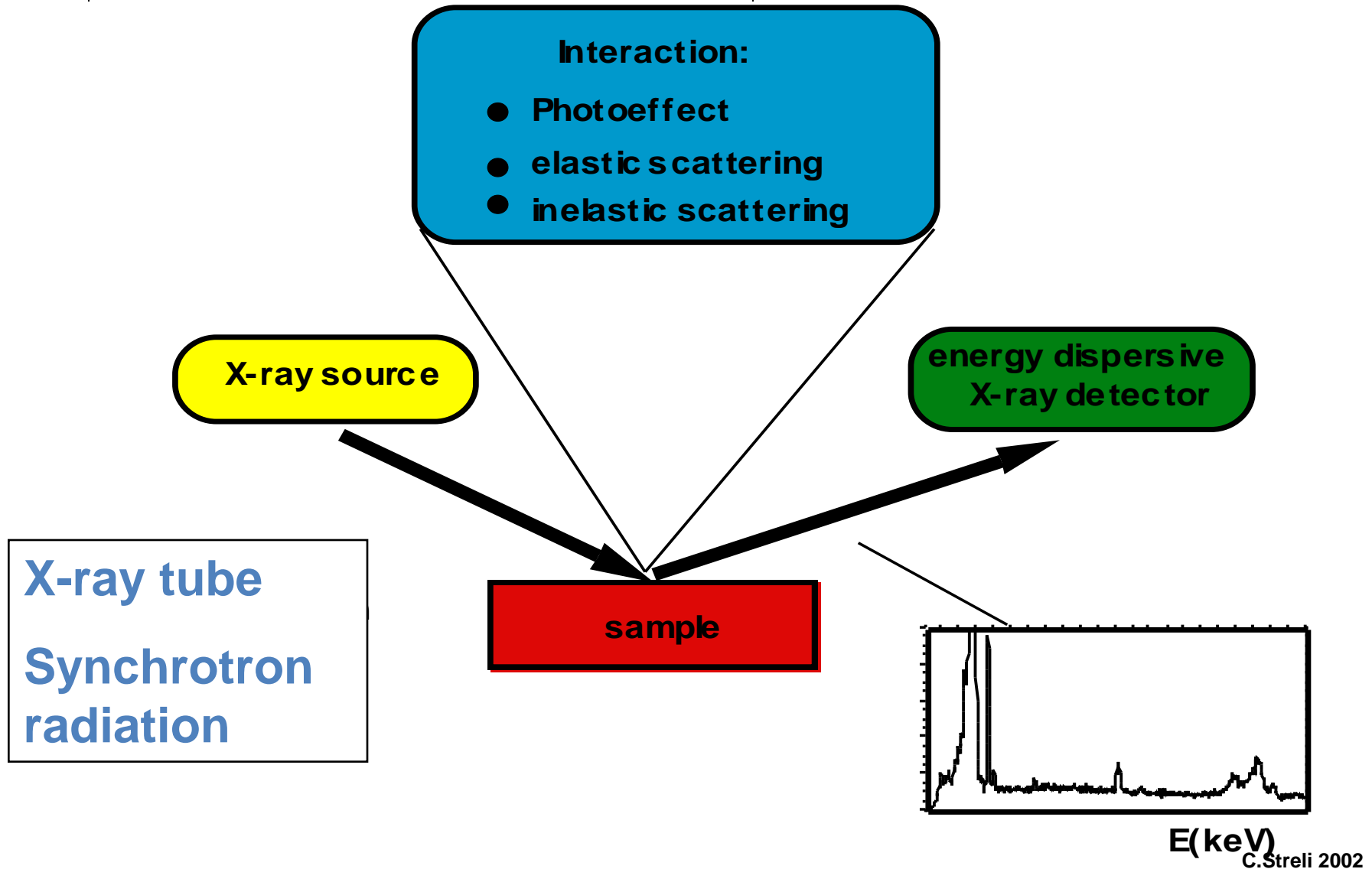


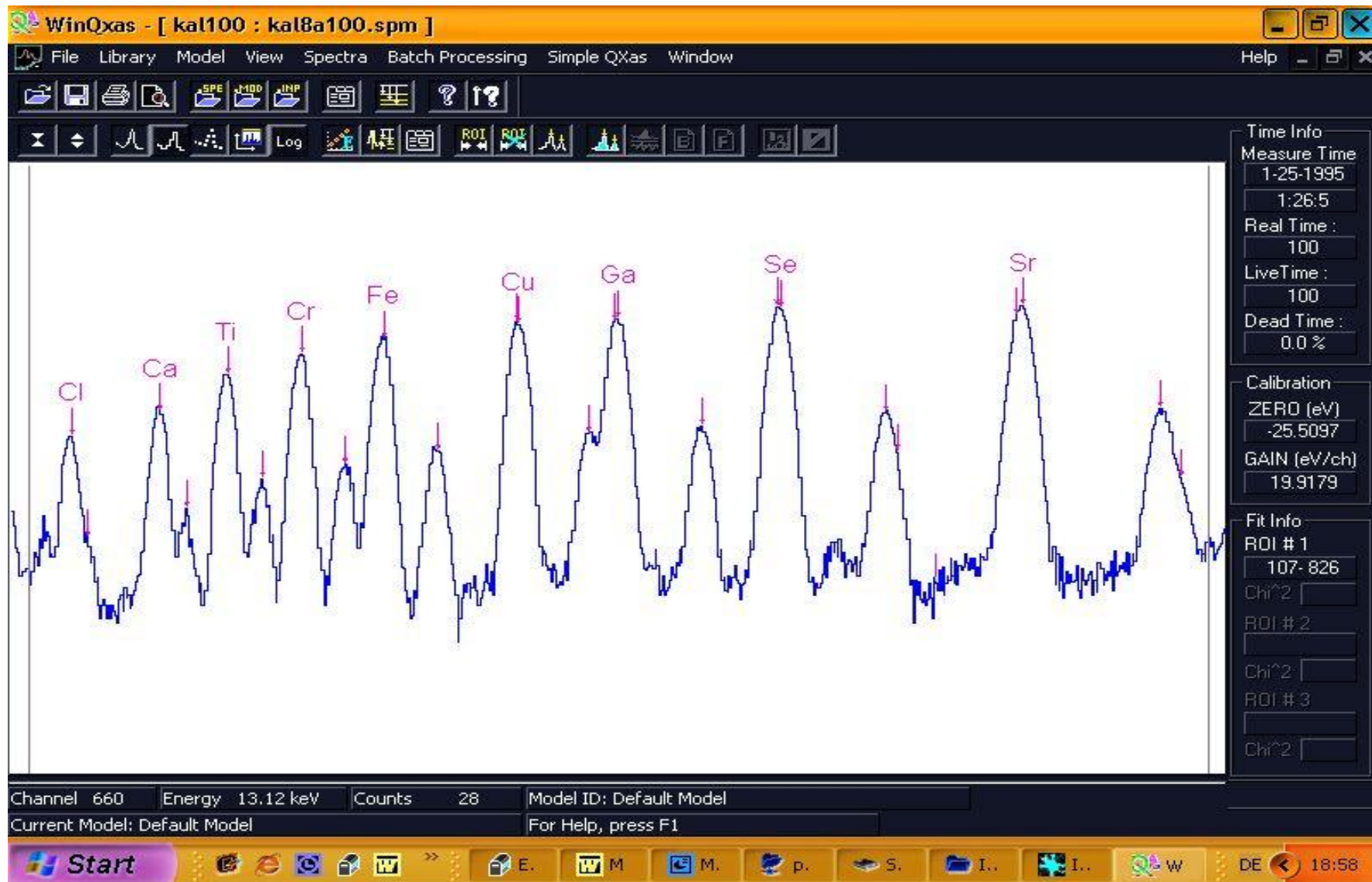


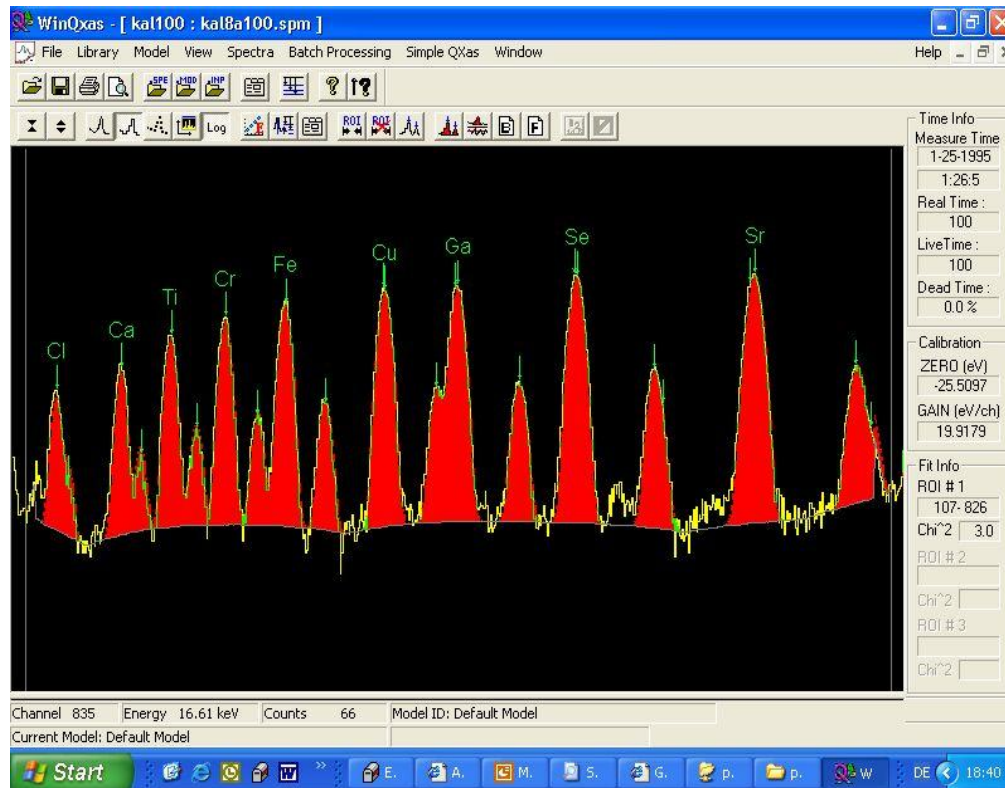


Capillary X-ray optics use hollow capillaries for controlling incident X-rays in many, varied X-ray applications. These optics are formed from a single capillary (monocapillary), or up to several million hollow glass capillaries (polycapillary) that have been fused together and tapered to desired profiles. The principle behind their operation is multiple total external reflection of X-rays along the smooth inner walls of the capillary channels. Reflection of X-ray photons occurs at the boundary between media with different refractive indices. When an X-ray strikes the reflecting surface of a capillary at a grazing angle smaller than the critical angle of the material, it undergoes total external reflection. X-rays satisfying the total reflection condition can be effectively transported through the capillary channels, and therefore formed into a desired wavefront pattern defined by the shaped profile of the optic.









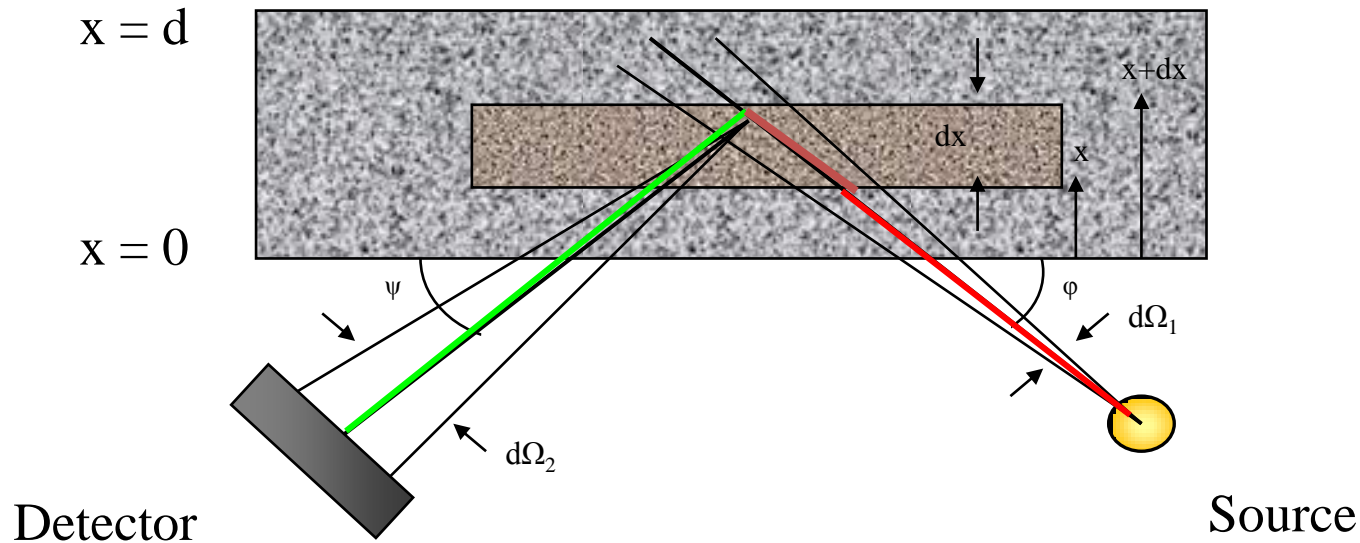
WinQXAS version 1.30, Aug.2001

Feb, 19 2003 06:46:45

Document filename: kal100  
Spectrum ID: kal8a100.spm  
Model ID: Default Model

Fitting Region: channels 107 - 826, Chisquare = 3.0

Line	E(KeV)	Peak area	st. dev	Chi-sq
Cl - KA1	2.622	2741	± 55	3.8
Cl - KB1	2.816	582	± 21	7.2
Ca - KA1	3.691	4934	± 71	3.5
Ca - KB1	4.013	935	± 23	12.3
Ti - KA1	4.509	10079	± 99	2.0
Ti - KB1	4.932	1662	± 26	8.5
Cr - KA1	5.412	15181	± 121	2.1
Cr - KB1	5.947	2254	± 28	3.0
Fe - KA1	6.399	21380	± 141	2.1
Fe - KB1	7.059	3140	± 29	2.0
Cu - KA1	8.048	19514	± 111	1.6
Cu - KA2	8.028	10005	± 60	1.5
Cu - KB1	8.905	4137	± 33	0.9
Ga - KA1	9.252	21789	± 117	2.2
Ga - KA2	9.225	11201	± 64	2.1
Ga - KB1	10.263	4769	± 34	0.7
Se - KA1	11.222	28584	± 131	1.7
Se - KA2	11.181	14733	± 71	1.6
Se - KB1	12.494	6574	± 38	0.8
Se - KB2	12.652	361	± 23	1.6
Sr - KA1	14.165	31734	± 138	1.3
Sr - KA2	14.098	16510	± 75	1.3
Sr - KB1	15.832	7690	± 44	0.9
Sr - KB2	16.085	986	± 38	14.4



$$I(E_{K\alpha}^i) = \int_{E=E_{abs}^i}^{E=E_{max}} \int_{x=0}^{x=d} I_0(E) \cdot G_1 \cdot \frac{\rho}{\sin \varphi} \cdot \frac{\tau_K^i(E)}{\rho} \cdot \omega_K^i \cdot p_{\alpha}^i \cdot c^i \cdot V^i(E) \cdot e^{-\left(\frac{\mu(E)}{\rho \cdot \sin \varphi} + \frac{\mu(E_{K\alpha}^i)}{\rho \cdot \sin \psi}\right) \cdot \rho \cdot x} \cdot G_2 \cdot f(E_{K\alpha}^i) \cdot \varepsilon(E_{K\alpha}^i) \cdot dx \cdot dE$$

Gain in intensity in focus

Change of energy distribution by high energy cut off

High energy photons pass through central channels

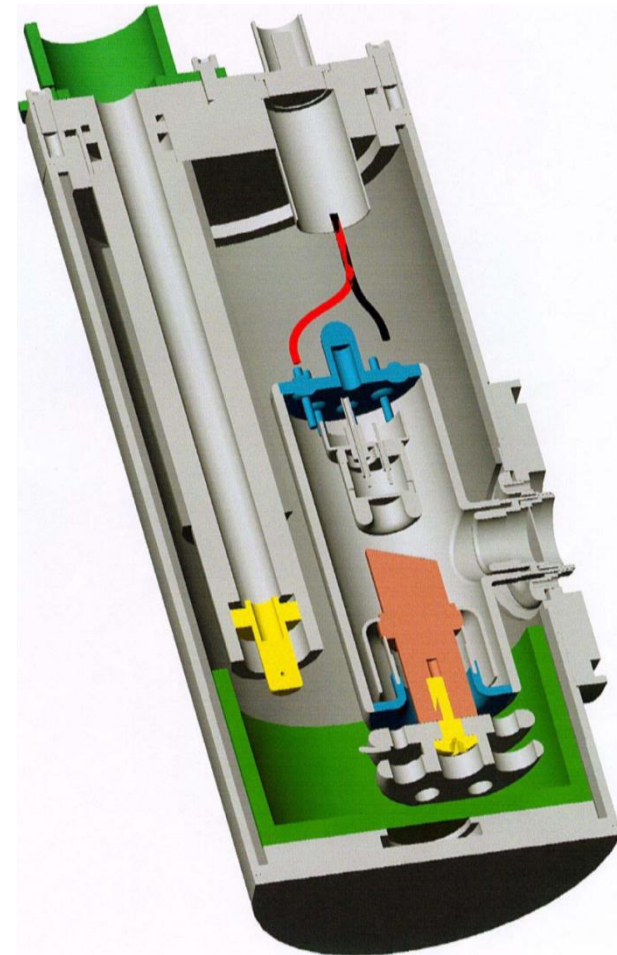
Radial energy distribution due to changes according angle and energy relation

- LIGHT ELEMENTS Be B C N O F Ne Na Mg Al Si
- Extreme challenge for EDXRS
- Experiments must be performed in vacuum
- Excitation source with energies close to light element absorption edges and high intensities requested
- Detector window Ultra thin polymer to have efficiency in the low energy region
- Low fluorescence yield



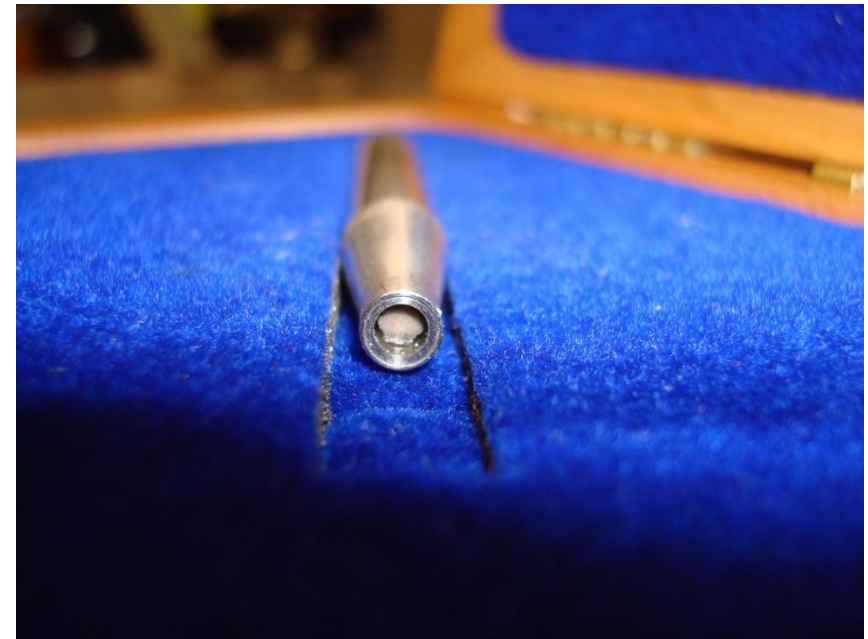
# ATI $\mu$ XRF Spectrometer components

- 50kV/1mA/50W X-ray tube Oxford „Apogee“
  - Mo Anode on HV
  - Cathode grounded
  - Microfocus (35  $\mu$ m)
  - Thin exit window (125  $\mu$ m  $\rightarrow$  Mo-L, 2,3 keV)
  - Air cooled

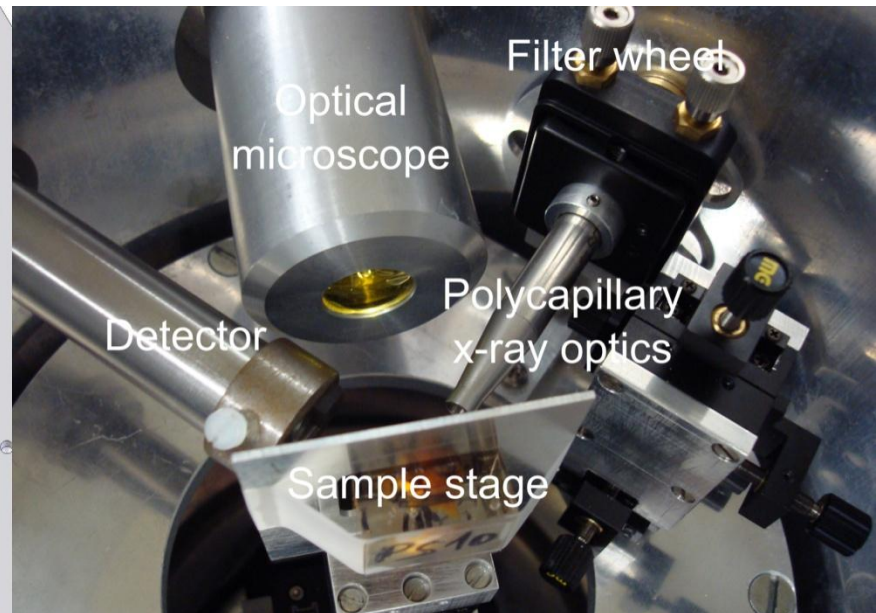
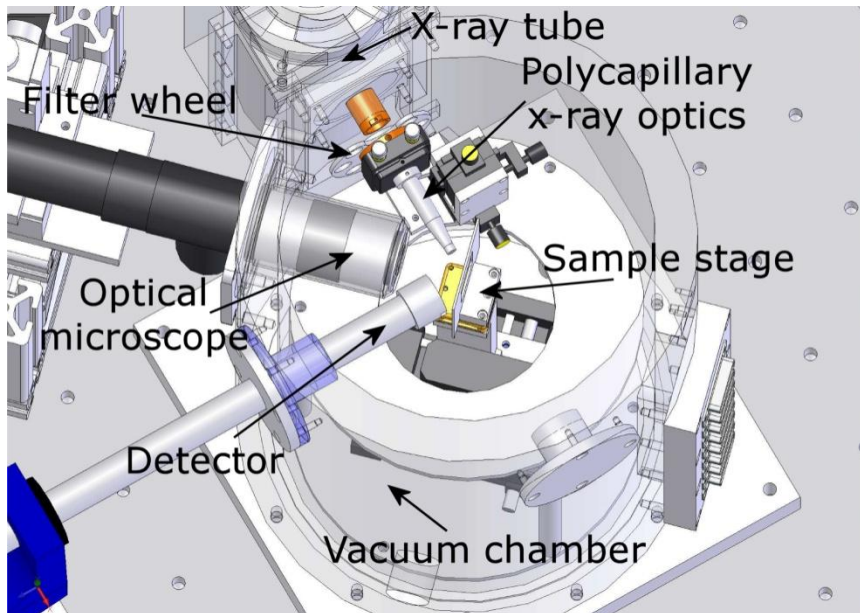


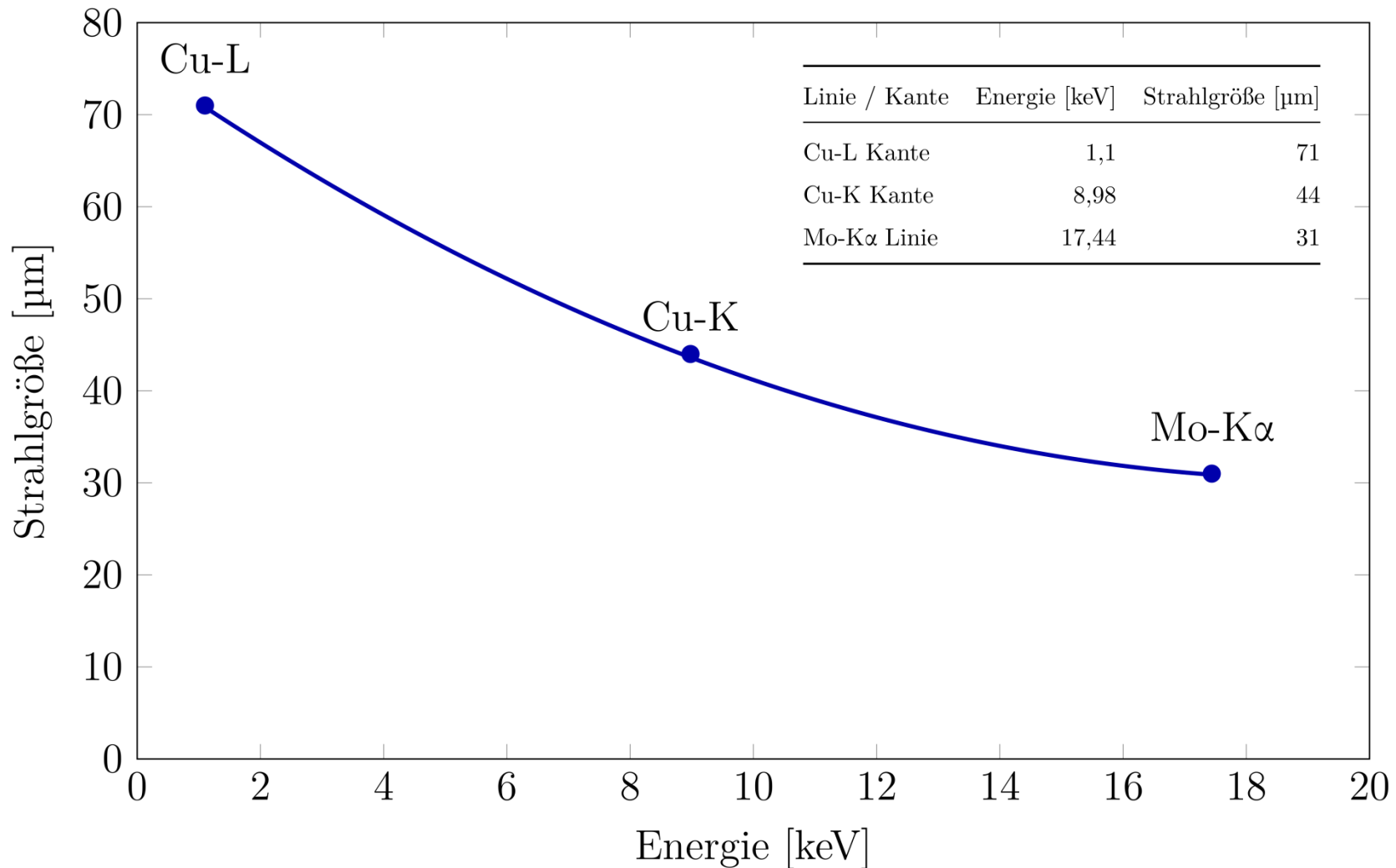
# ATI $\mu$ XRF Spectrometer components

- Polycapillary X-ray optics produced (XOS)
  - Spotsize  $32\mu\text{m}$  @ Mo-K $\alpha$  (17,44 keV)
  - Intensity gain 39-times (compared to pinhole of  $50\mu\text{m}$  )
  - 5-Axis adjustable



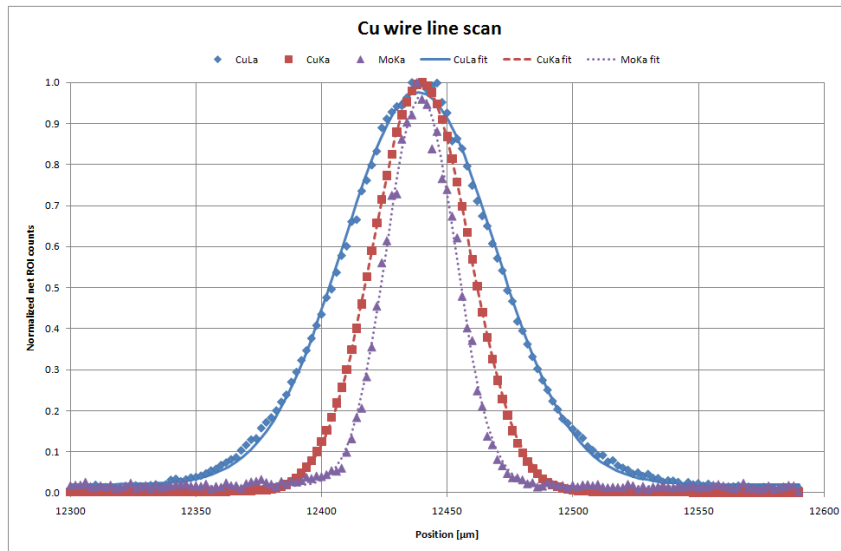






# ATI $\mu$ XRF Spectrometer

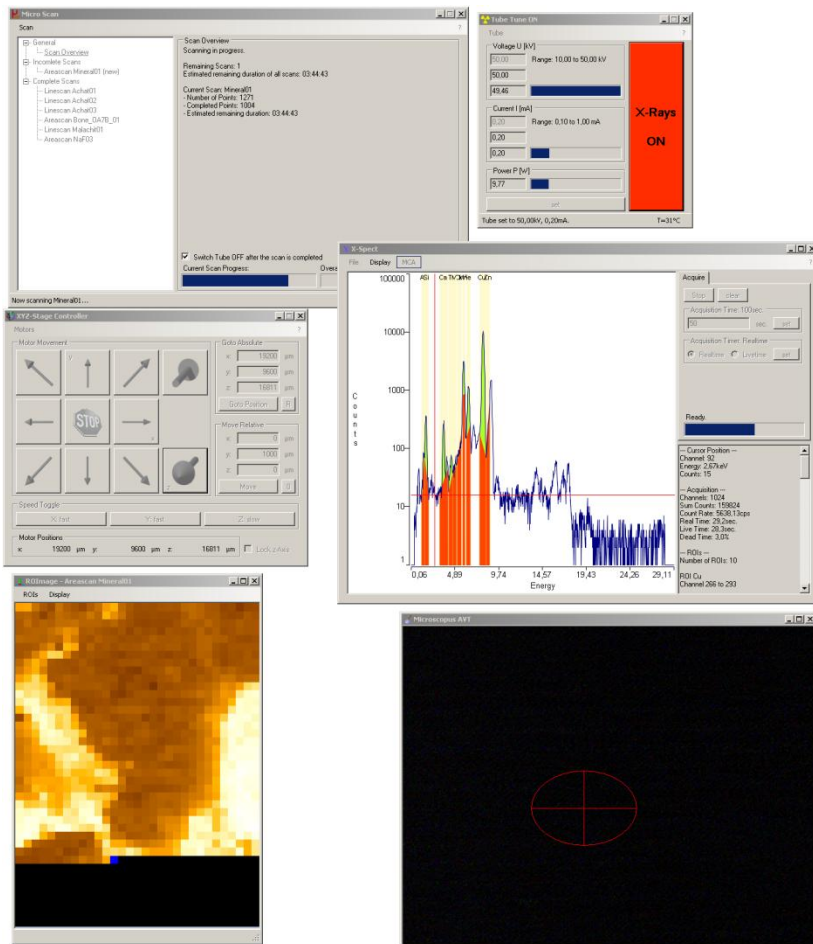
## Resolution



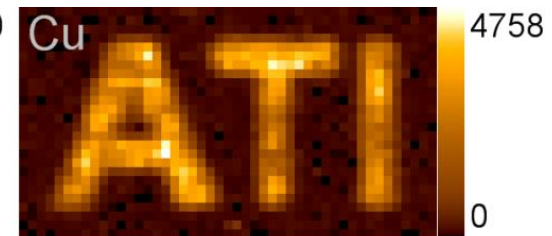
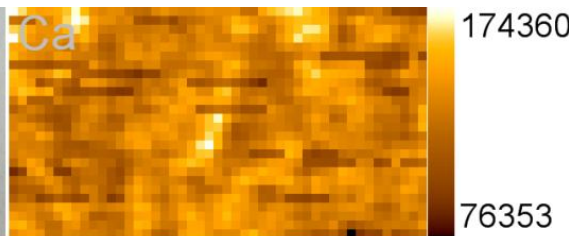
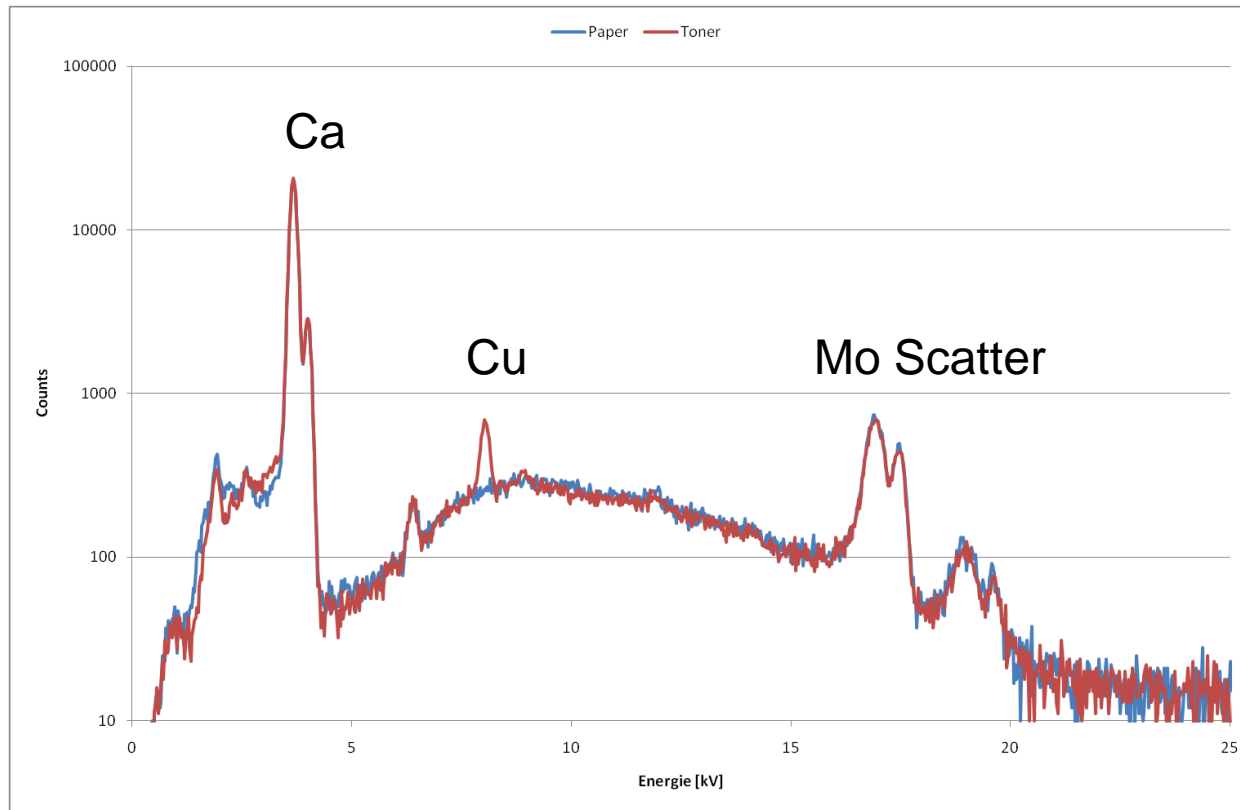
$$FWHM_{beam} \approx \sqrt{FWHM_{profile}^2 - d_{wire}^2}$$

- Determination of minimum beam diameter with a 10μm Cu wire:
  - @ Mo-K $\alpha$  (17,44 keV): 31 μm
  - @ Cu-K (8,98 keV): 44 μm effektiv
  - @ Cu-L (1,1 keV): 71 μm effektiv

# ATI $\mu$ XRF Spectrometer Software



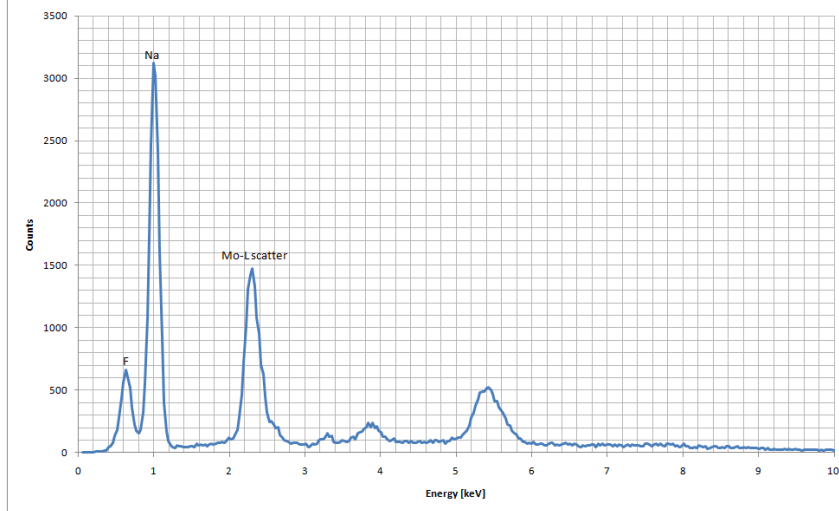
- Software for automatic Mapping of a sample
- Automatic Region of Interest (ROI) Spectrum evaluation with live-preview
- All Spectra stored for later evaluation with software packages as (AXIL,...)



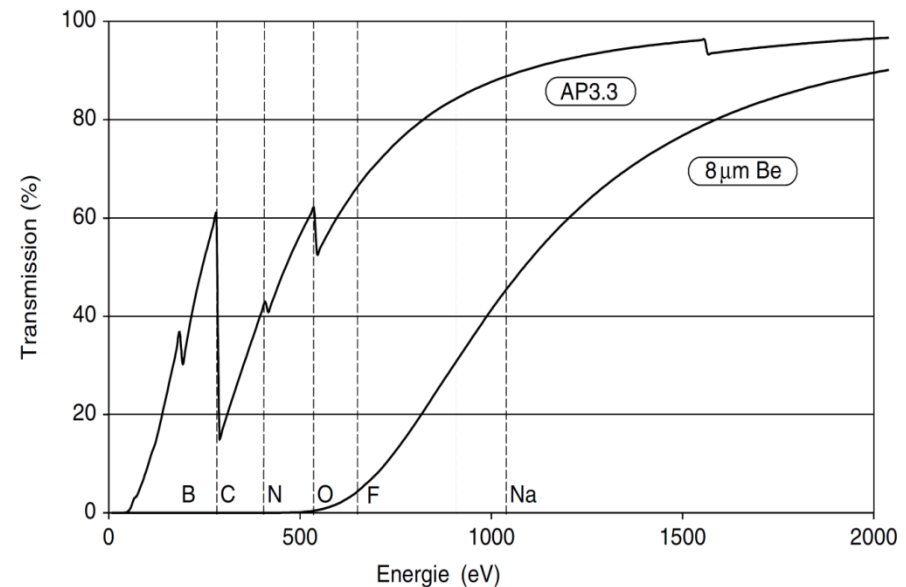
Name: ATl  
Scan size: 47x26 pixel  
Resolution: 40 $\mu$ m per pixel.  
Counting time: 150sec. per pixel  
Tube parameters: 50kV, 1mA



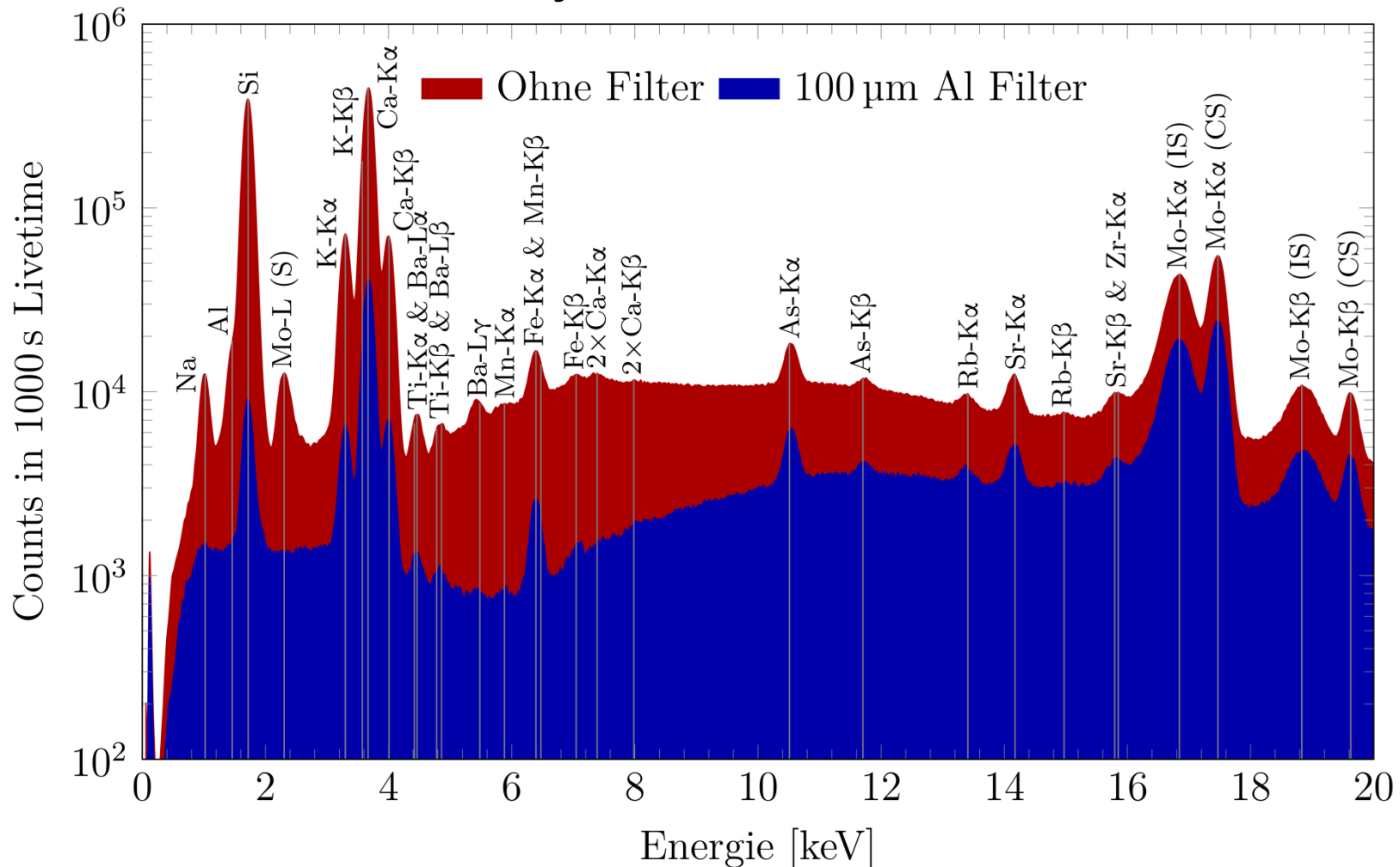
NaF spectrum at position (2/7)



- Analysis of elements with low Z :
  - Mo-L excitation
  - Vacuum
  - UTW Detektor



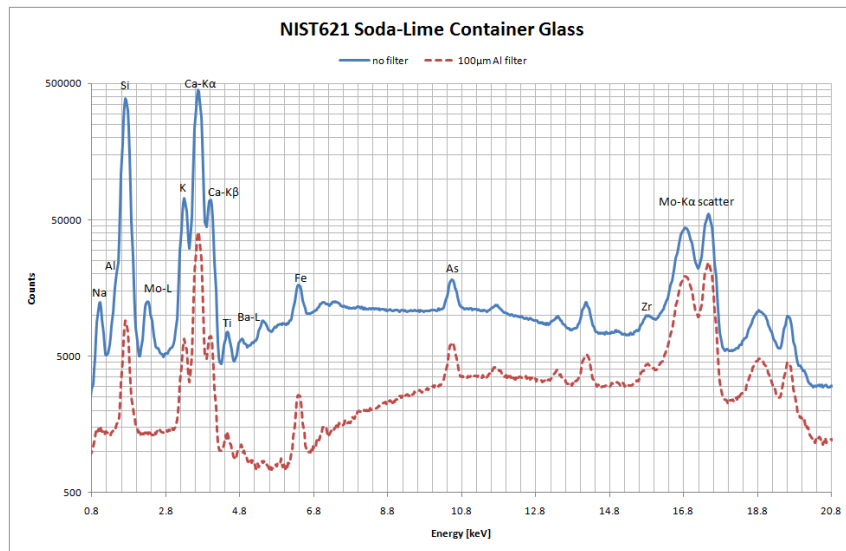
- 50 kV / 1 mA
- 10x10 Punkte, je 10 s LT → 1000 s





Determination of (LLD) using Standard Reference Material NIST621 Soda-Lime Container Glass:

## LLD



Element	LLD [ppm]	LLD (100µm Al filter) [ppm]
Na	878	36409
Al	115	4898
Si	95	2513
K	22	148
Ca	15	81
Ti	8	17
Fe	5	6
As	4	5
Zr	2	4
Ba	54	145

S. Smolek, C. Strelj, N. Zoeger, P. Wobrauschek, Improved Micro-XRF Spectrometer for Light Element Analysis, REVIEW OF SCIENTIFIC INSTRUMENTS **81**, 053707 2010

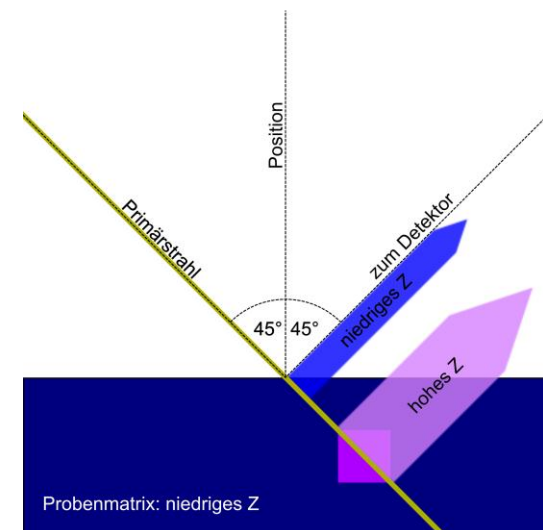
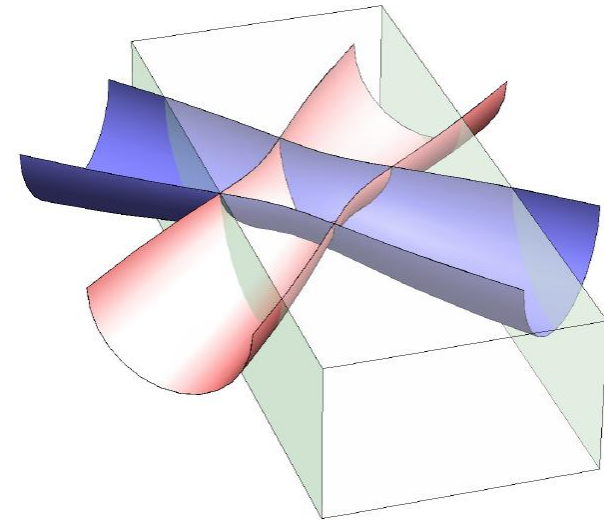
Project supported by "Innovative Projekte" of TU Wien

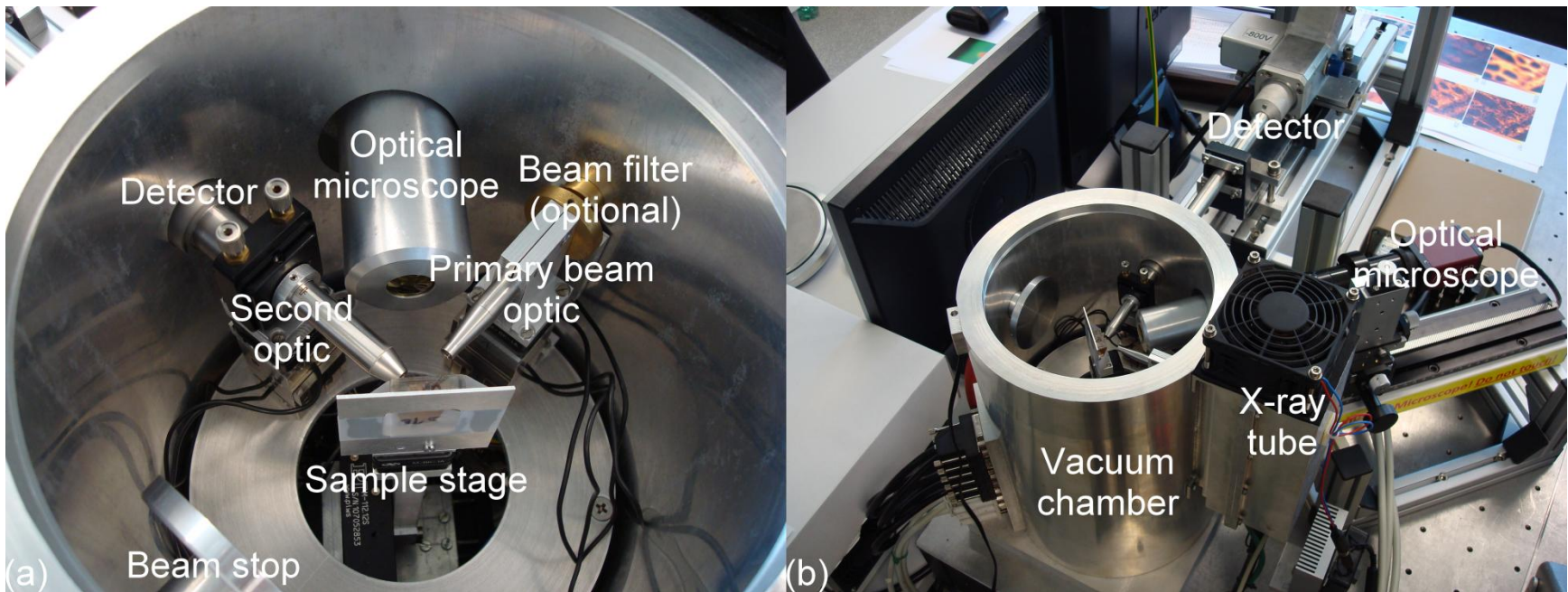
$$LLD = m \frac{3\sqrt{N_E}}{N_N}$$



- confocale Extension of the Spectrometer
- Determination of the effective Spotsizes (Volume) for different Elements
- Determination of the Transmission function of Polycapillaries
- Quantification models
- Measurement of various samples open projects (ANNA, ...)

- Measuring in a defined Micro volume
- 3D Analysis
- Information depth for thick samples solved as the actual depth is known





- **Improved micro x-ray fluorescence spectrometer for light element analysis.**

*Smolek S., Strelí C., Zoeger N., Wobrauschek P.*

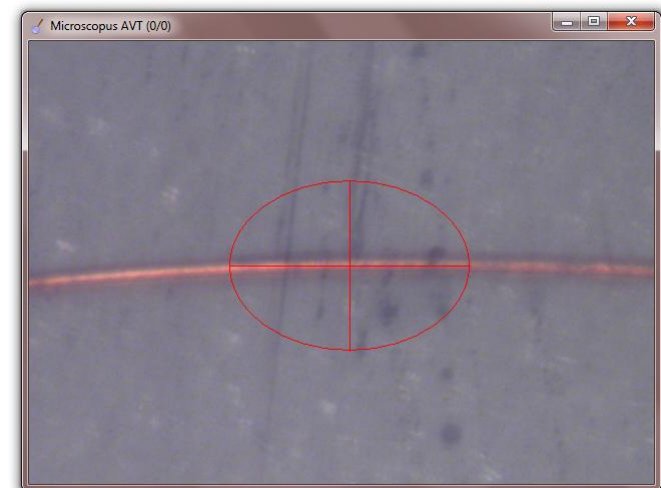
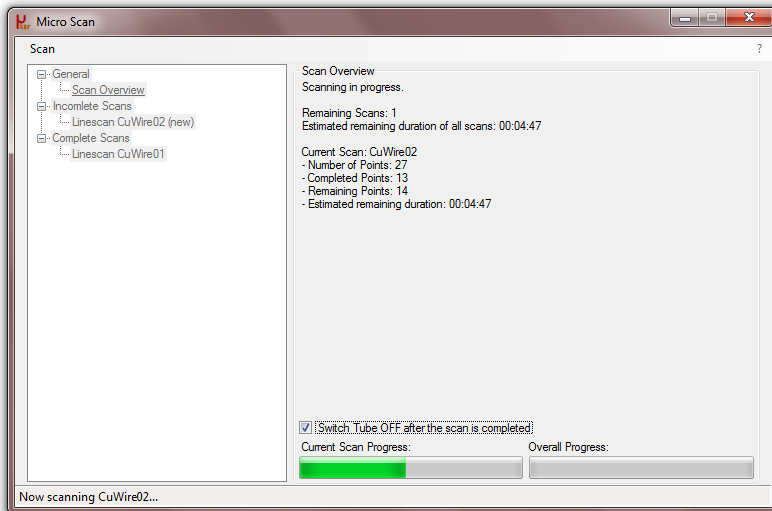
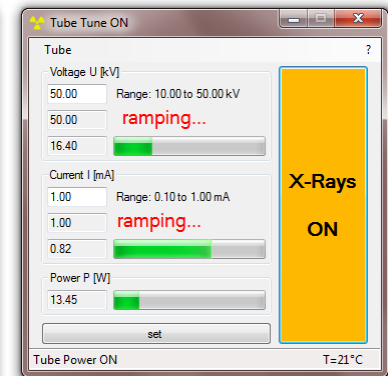
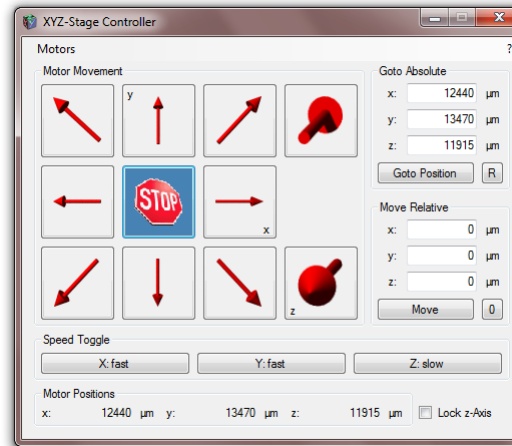
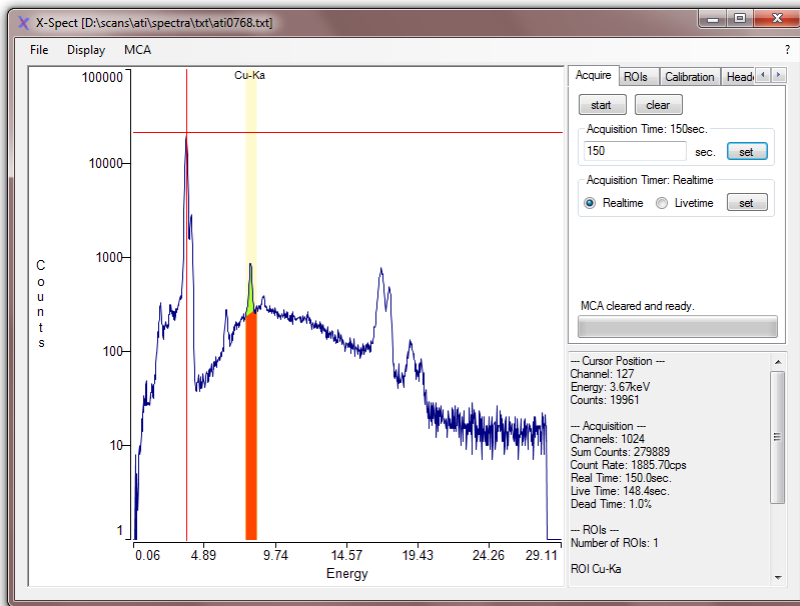
*Rev Sci Instrum.* 2010 May;81(5):053707.

- **Confocal micro-x-ray fluorescence spectrometer for light element analysis.**

*Smolek S., Pemmer B., Fölser M., Strelí C., Wobrauschek P.*

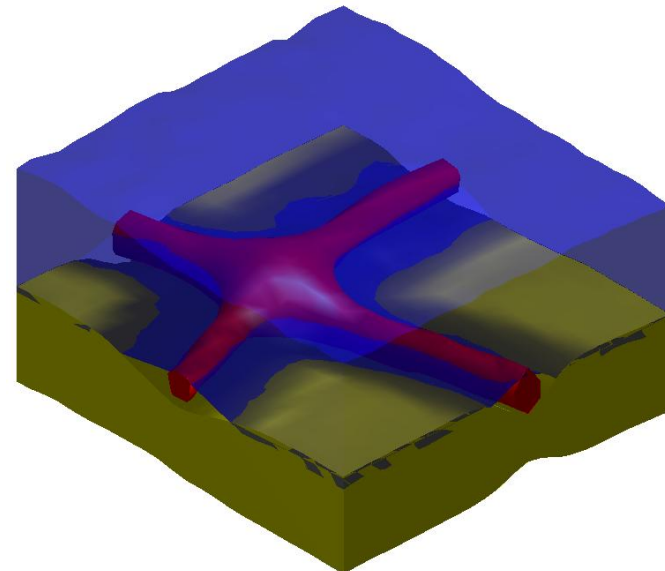
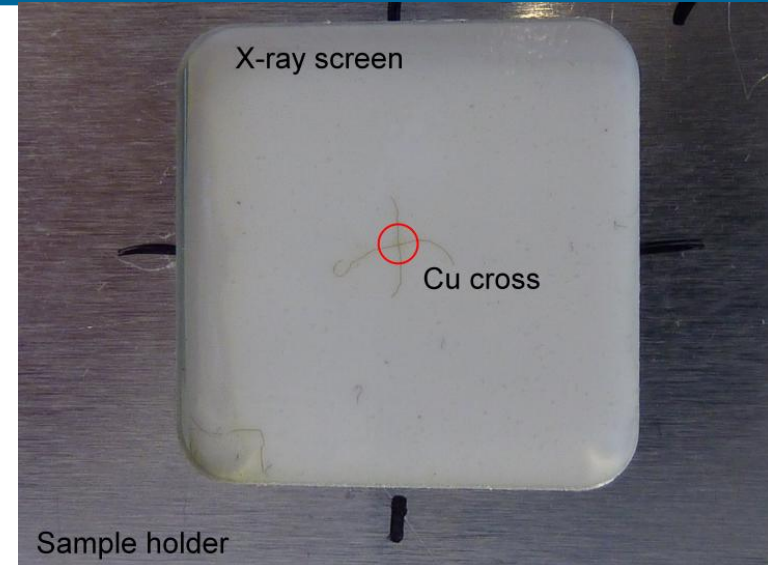
*Rev Sci Instrum.* 2012 Aug;83(8):083703.

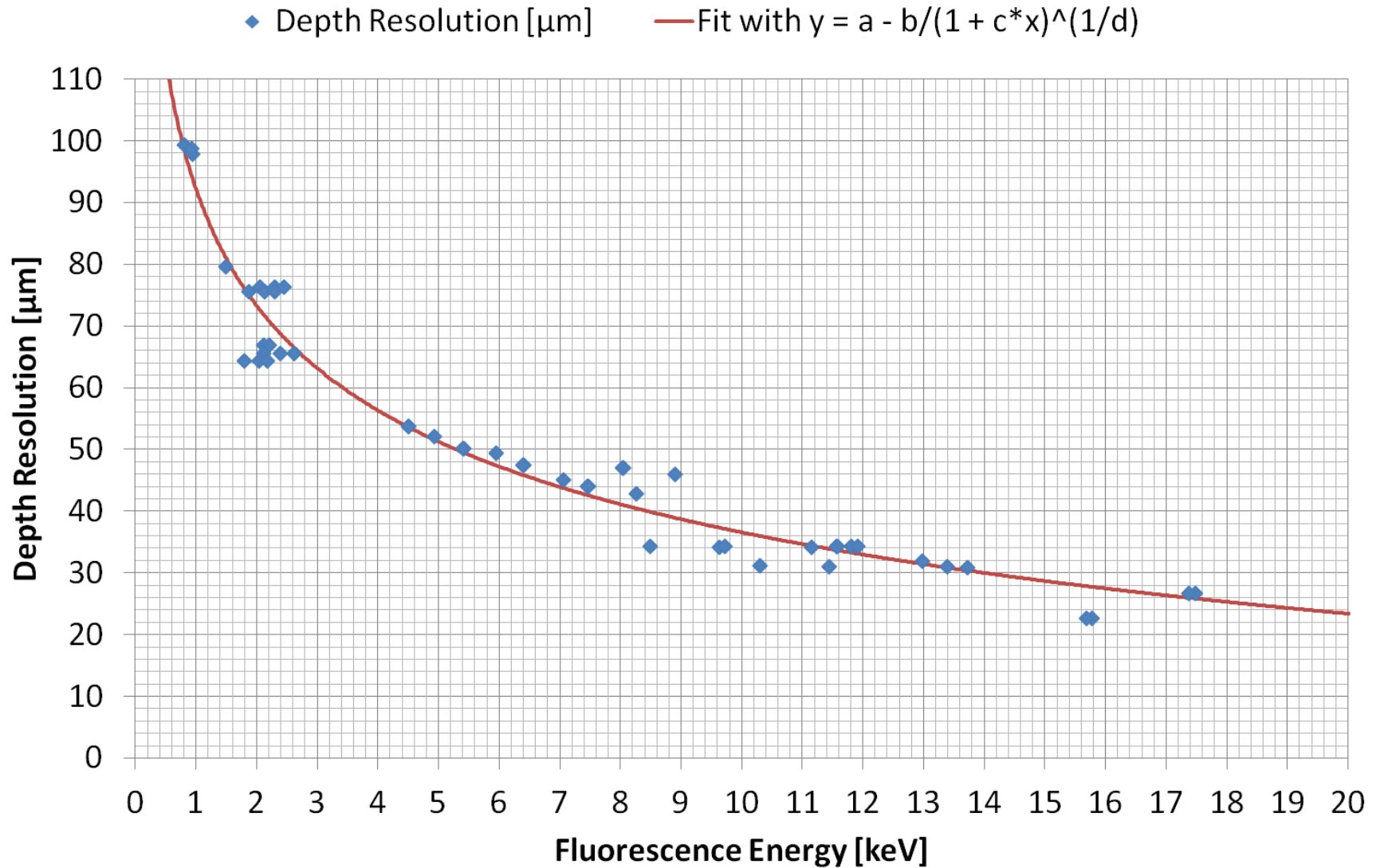
- Air cooled low power microfocus X-ray tubes (Oxford “Apogee”)
  - 35  $\mu\text{m}$  spot size
  - 50 W Mo anode, 50 kV, 1 mA
  - 20 W Rh anode, 50 kV, 1 mA
  - Thin window (125  $\mu\text{m}$ , Mo-L & Rh-L)
- Polycapillary X-ray optics (XOS)
  - Spot size: 32  $\mu\text{m}$  @ Mo-K $\alpha$  (17.44 keV)
- Optics x/y/z adjustment with attocube ANPx/z101 piezo positioners
  - 5 mm travel range





- Scan parameters & data treat.:
  - 24x24x24 voxels
  - 10  $\mu\text{m}$  steps
  - 5 s realtime acquisition
  - Mo X-ray tube at 50kV / 1mA
  - Gross ROI counts used
  - 3D data smoothed
- Red: 10 $\mu\text{m}$  Cu wire cross (Cu-K $\alpha$ )
- Yellow: Gd x-ray screen (Gd-L $\alpha$ )
- Blue: sticky tape (Mo-L scatter)

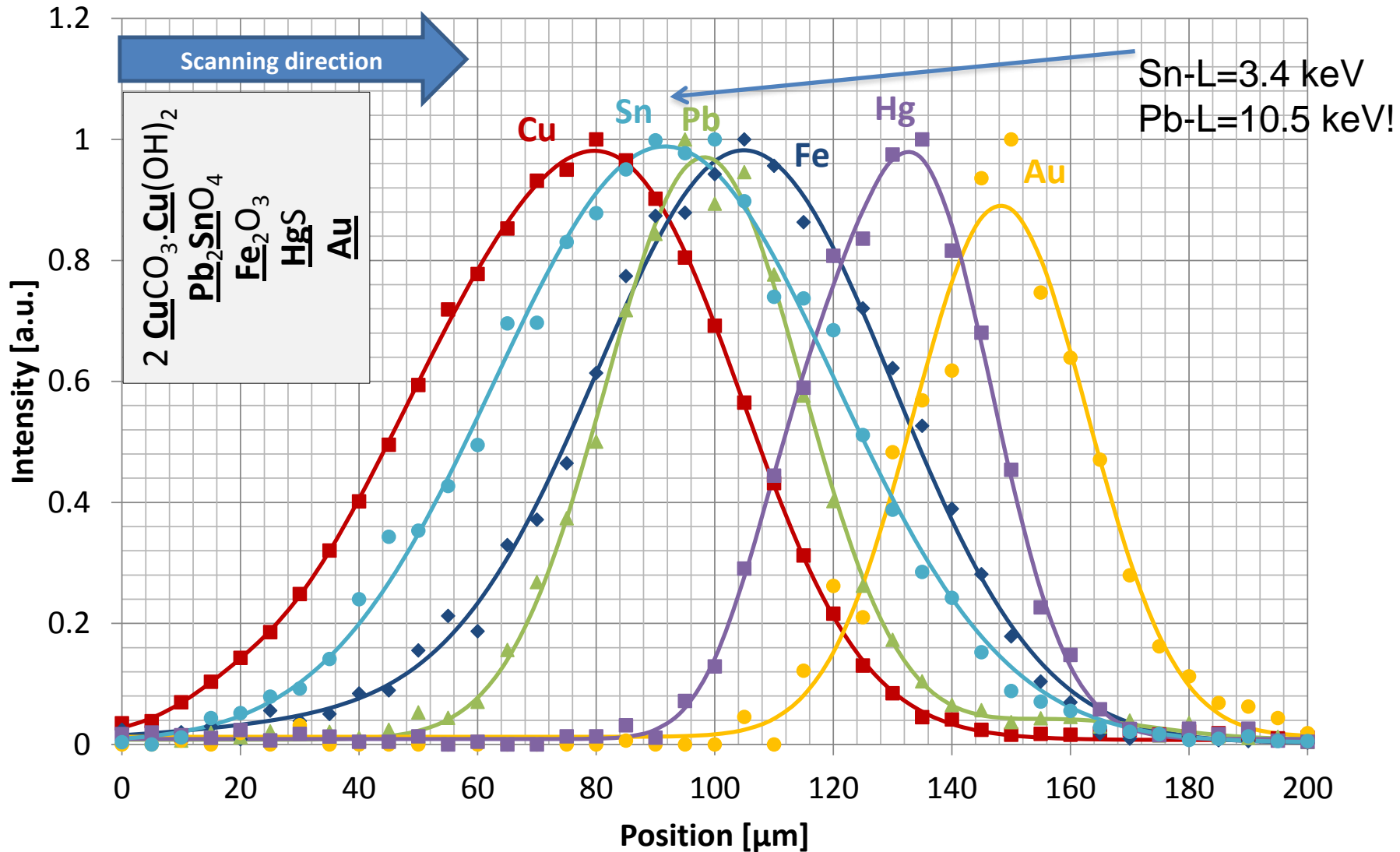




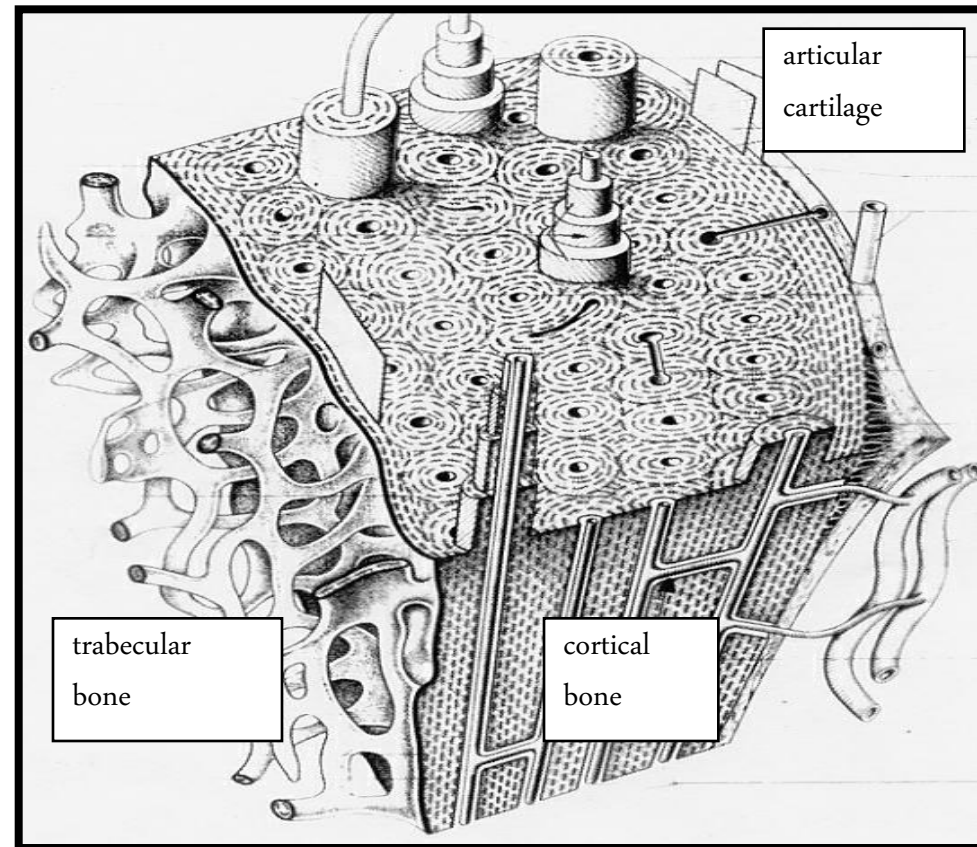
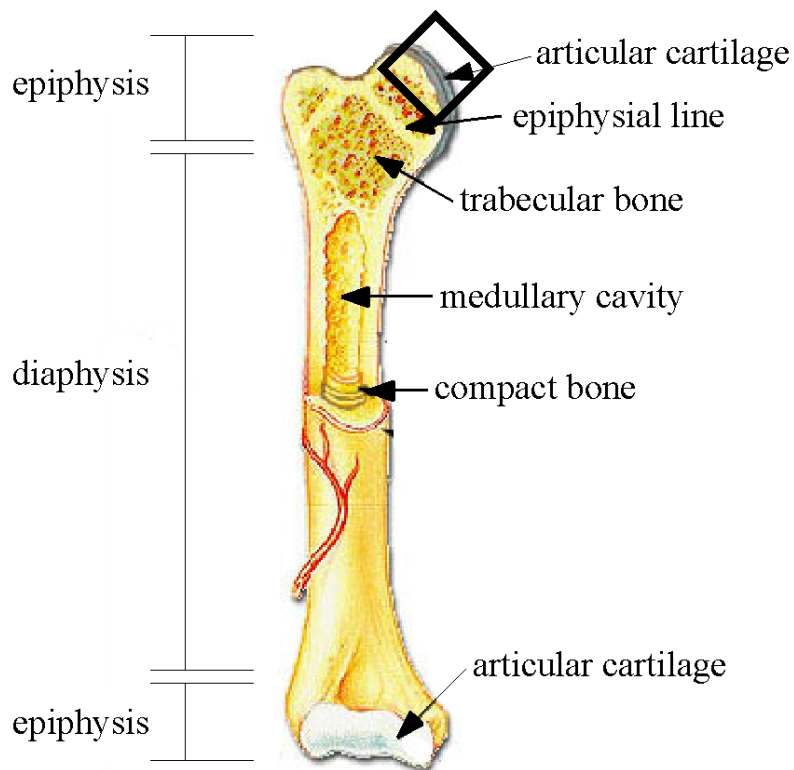
- Base: **Cu**
- Base coat:  
**Pb**CO<sub>3</sub>·2Pb(OH)<sub>2</sub>
- Metal overlay: **Au**
- Paint: **HgS**
- Paint: **Fe**<sub>2</sub>O<sub>3</sub>
- Paint: **Pb**<sub>2</sub>**Sn**O<sub>4</sub>
- Paint: 2  
**Cu**CO<sub>3</sub>·Cu(OH)<sub>2</sub>



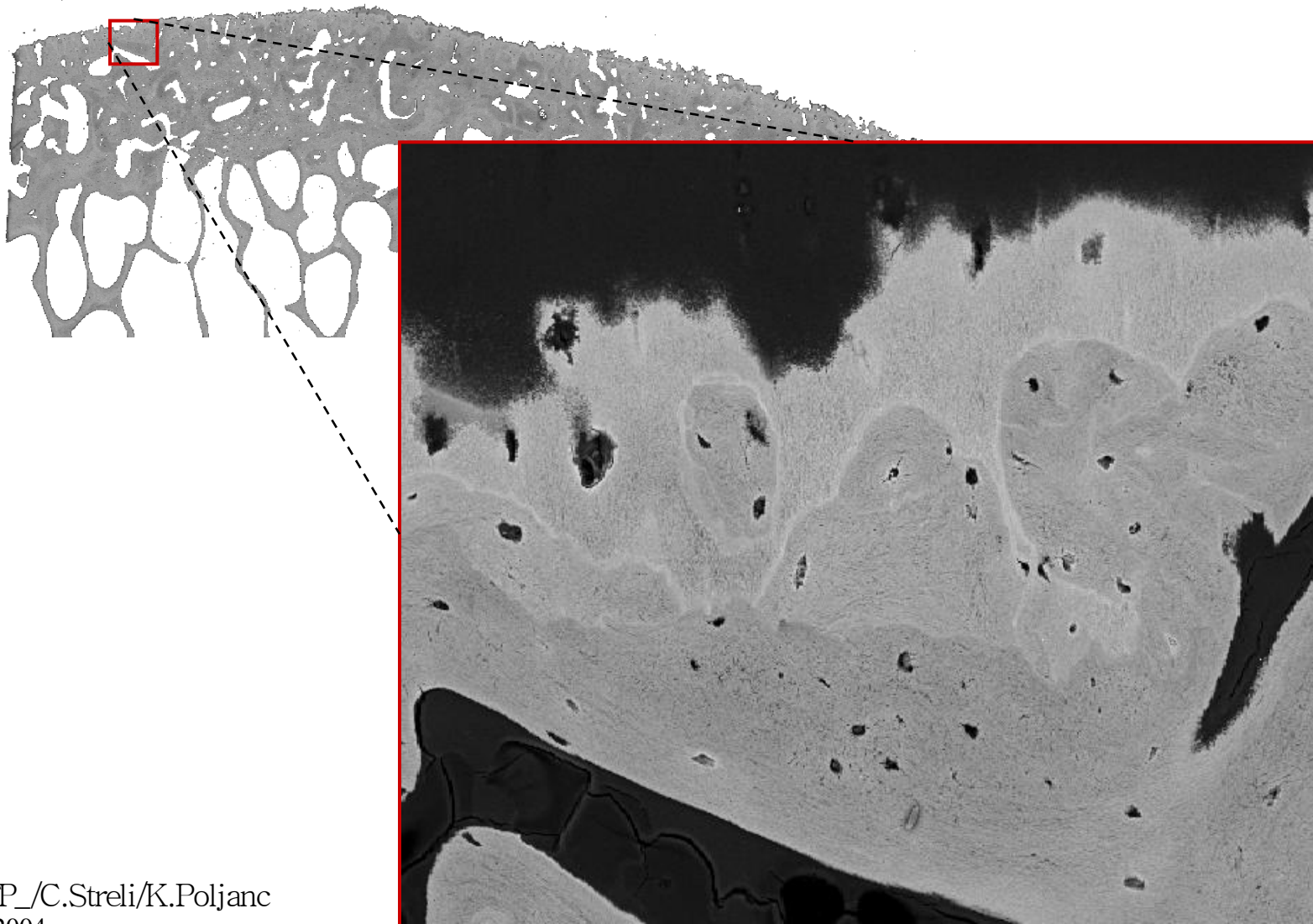


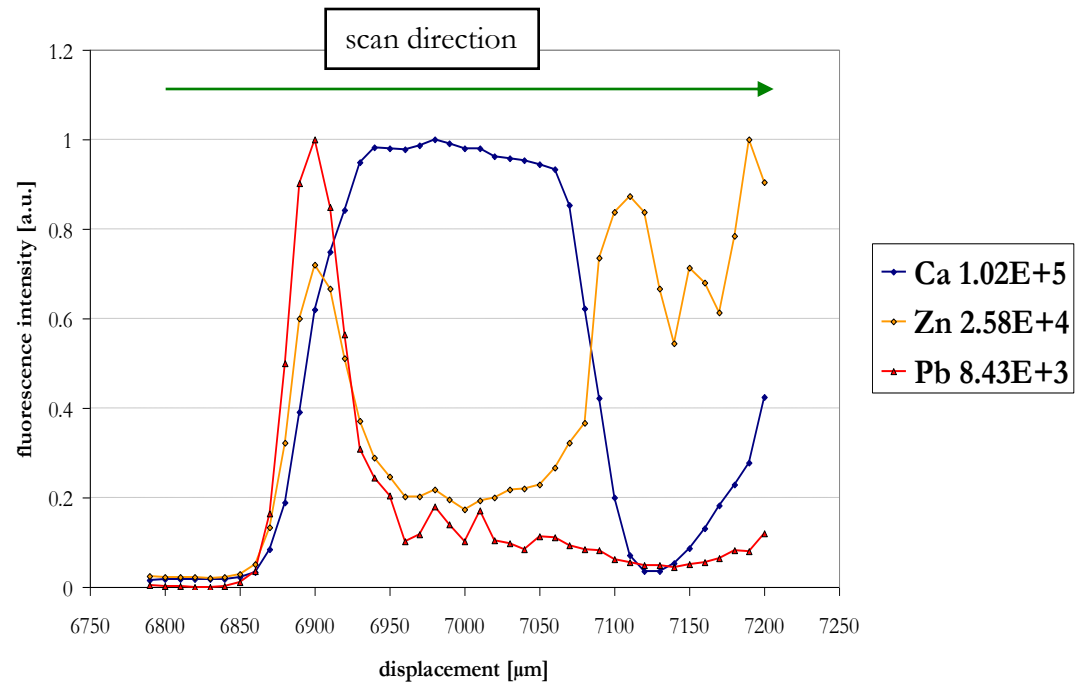
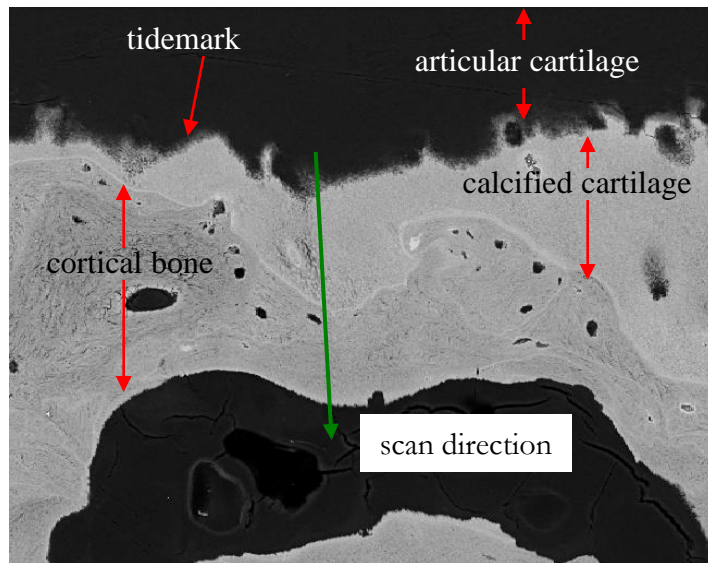


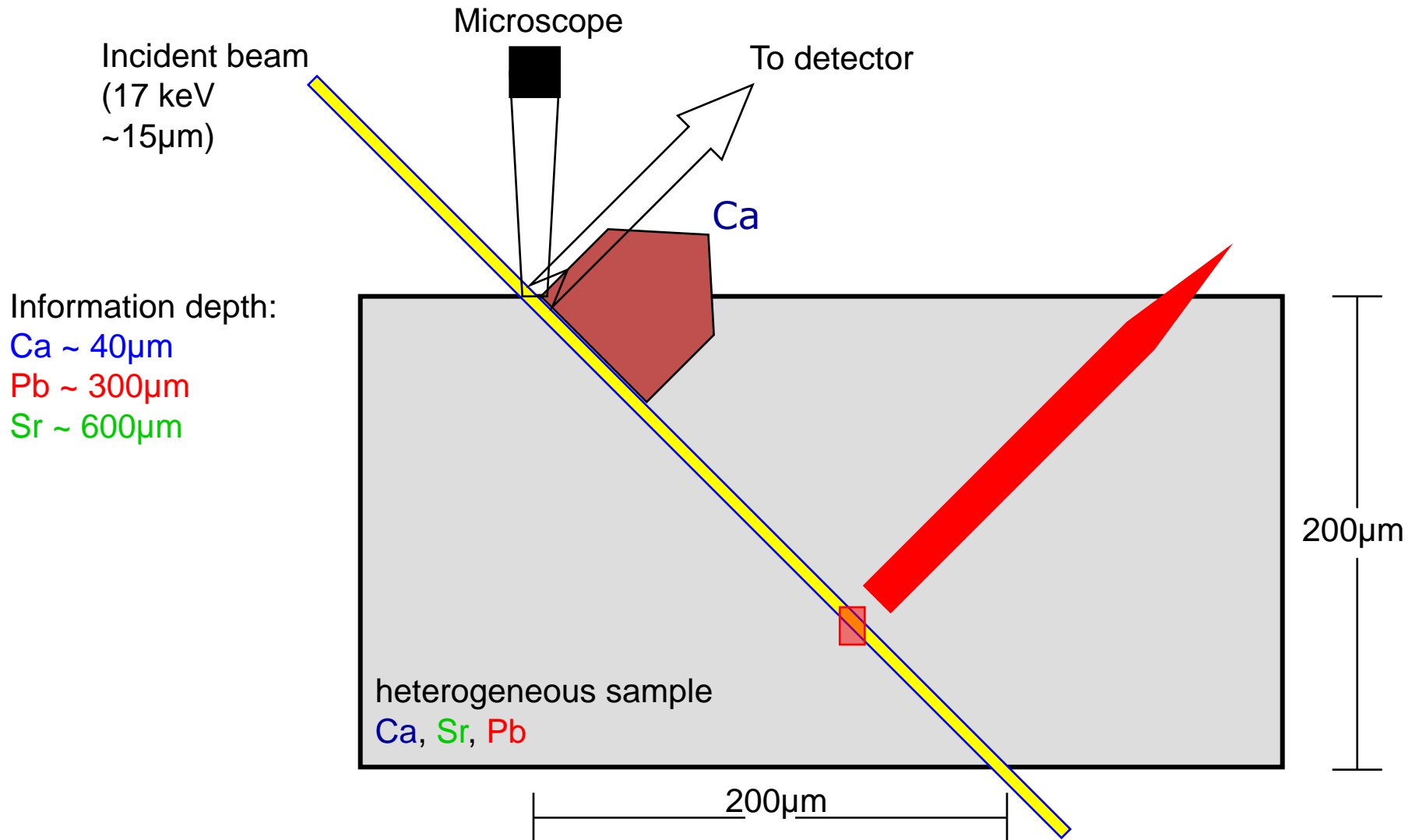
## Bone Structure



# Patella - line scan

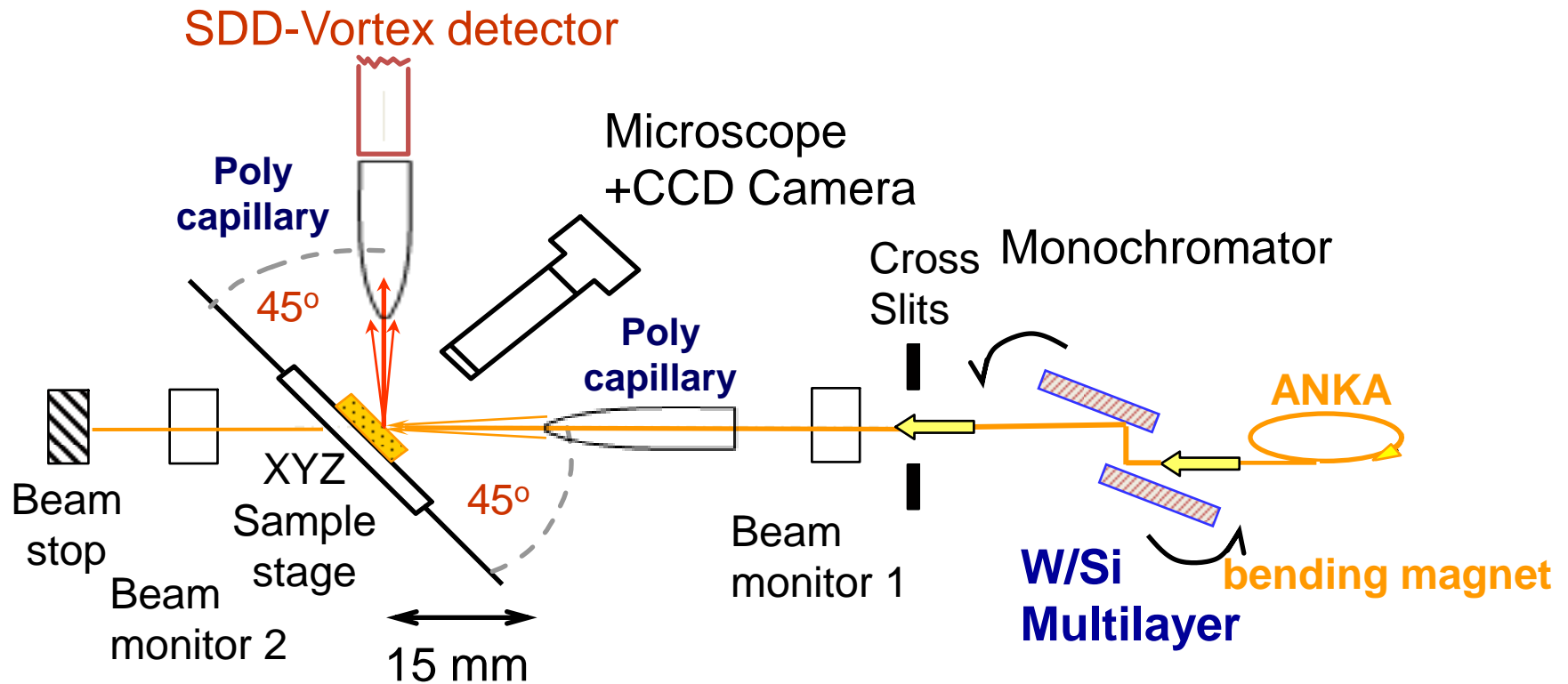






Applet to show this effect

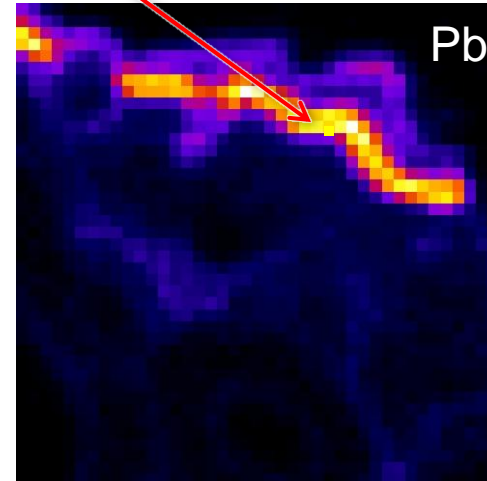
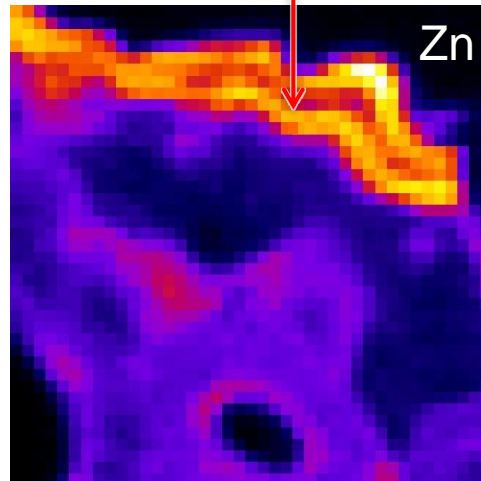
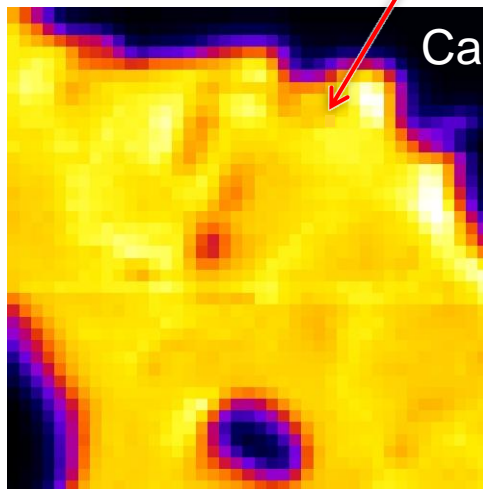
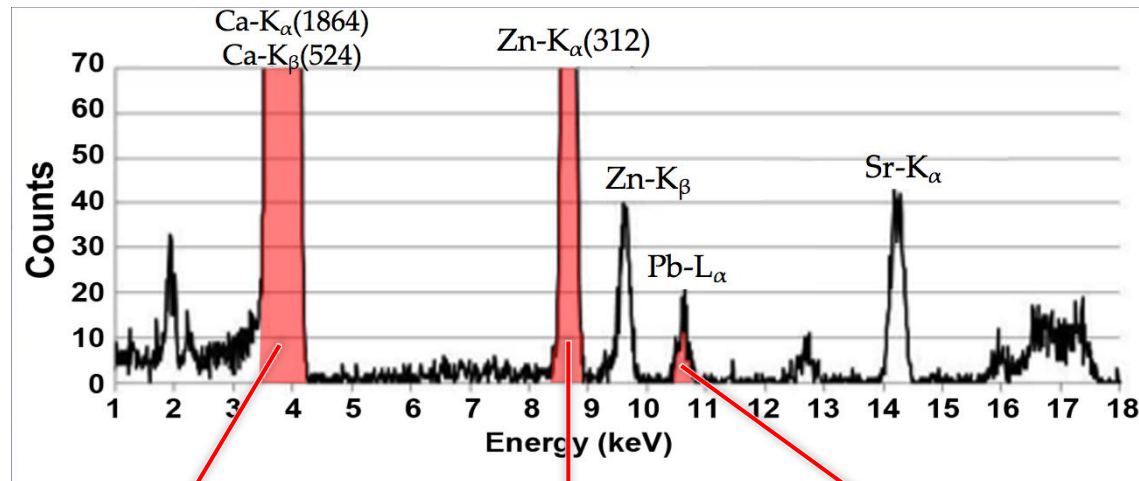
## Setup at ANKA Fluo Beamline:



Focal size: ~10-20  $\mu\text{m}$   
Depth resolution: ~15-20  $\mu\text{m}$

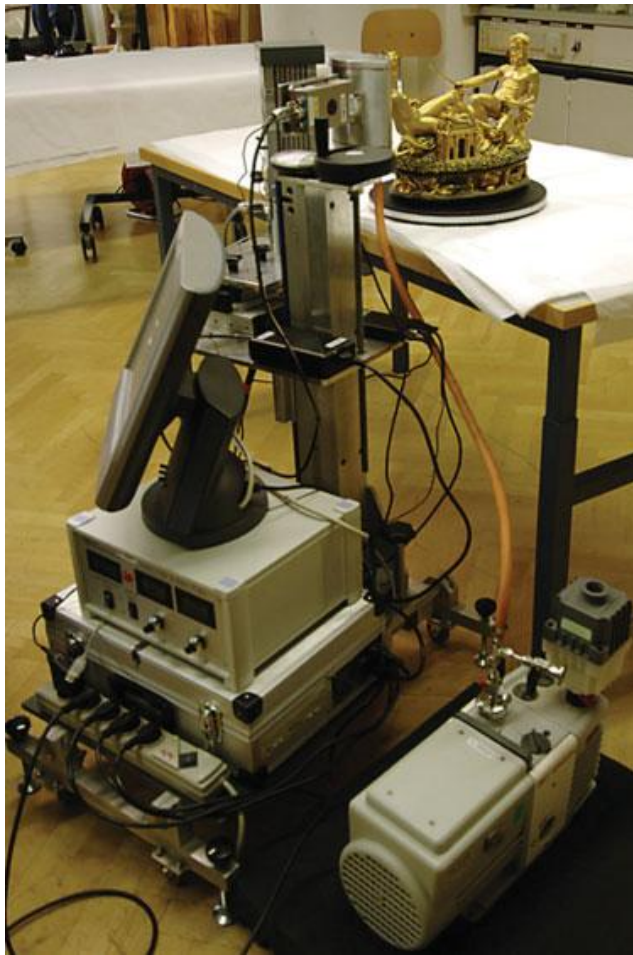


## Generation of the Elemental Maps:

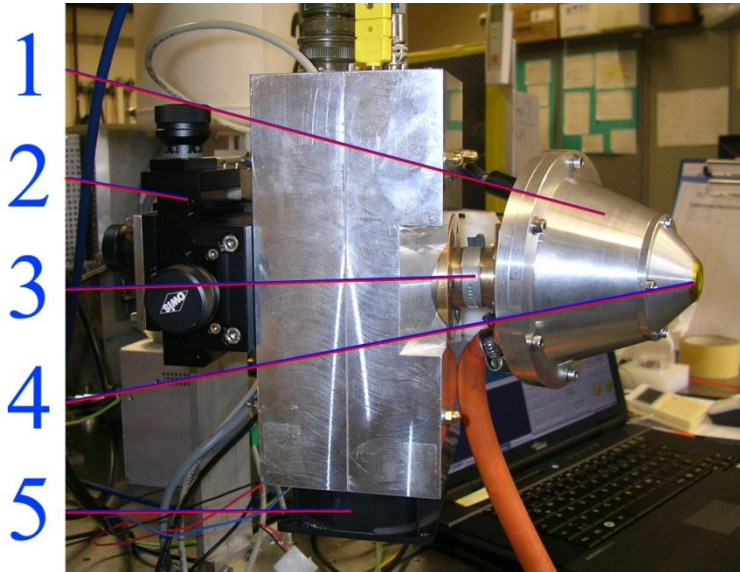




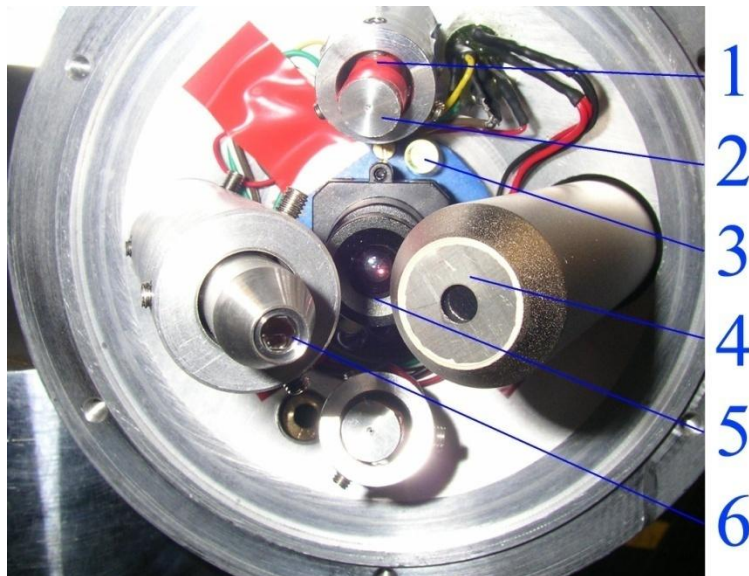
# Portable ART analyzer (PART I & II)



In cooperation with Art History Museum Wien and IAEA



- Exchangeable x-ray tube (Mo /Cr) 50W
- Polycapillary x-ray optic (XOS), 145 $\mu$ m for Cr-K $\alpha$  (5.41 keV)



- Ketek SDD, 20mm<sup>2</sup>, 8 $\mu$ m Be
- Vacuumchamber

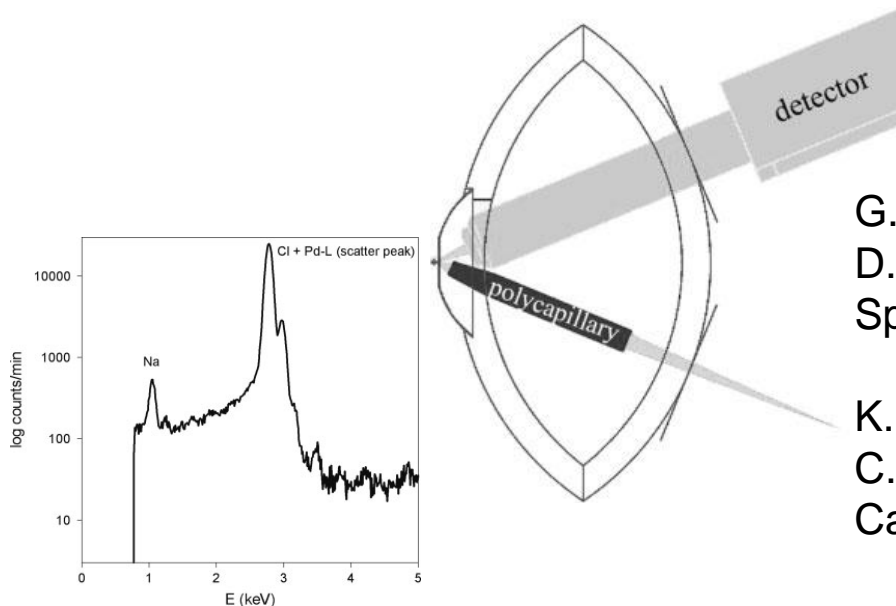
G. Buzanich, P. Wobrauschek, C. Streli, A. Markowicz, D. Wegrzynek, E. Chinea-Cano, M. Griesser and K. Uhler, X-Ray Spectrom. 2009; 39: 98-102



Saliera B. Cellini 1540-43 produced



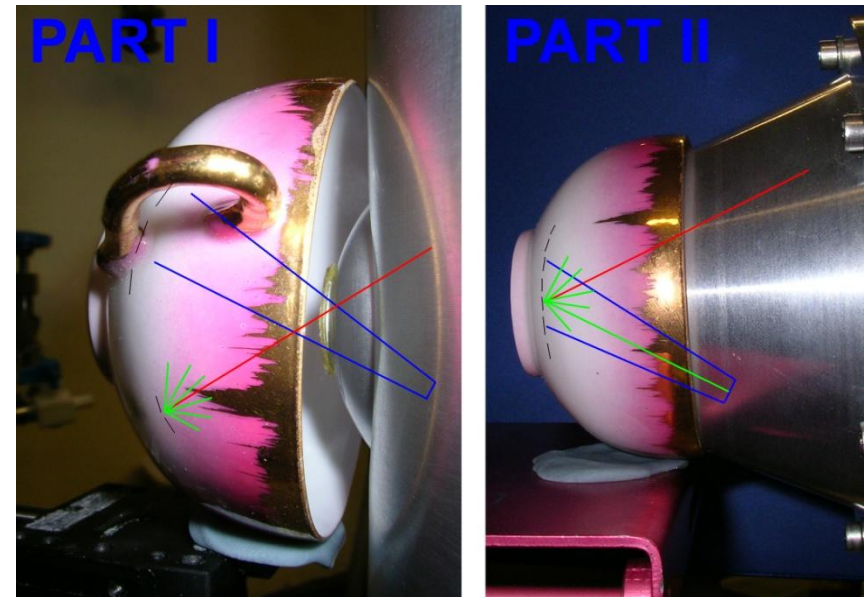
- 50kV/1mA Pd x-ray tube
- Polycapillary x-ray optic (160 $\mu$ m) or collimator (1mm)
- Ketek SDD, 10mm<sup>2</sup>, 8 $\mu$ m Be
- Vacuum chamber



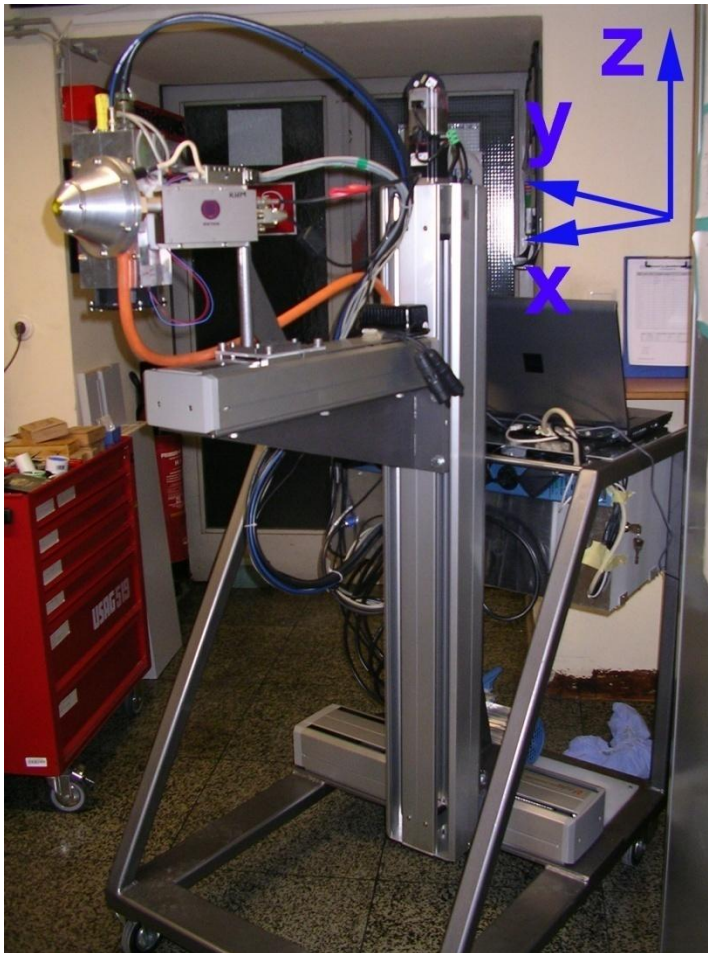
G. Buzanich, P. Wobrauschek, C. Streli, A. Markowicz, D. Wegrzynek, E. Chinea-Cano, S. Bamford, *Spectrochimica Acta Part B* 62 (2007) 1252 –1256

K. Uhler, M. Griesser, G. Buzanich, P. Wobrauschek, C. Streli, D. Wegrzynek, A. Markowicz, E. Chinea-Cano, *X-Ray Spectrom.* 2008; 37: 450–457

- Too large shaped Vacuum chamber – not all interesting point on the object could be reached.
- Problems measuring paintings due to base holder of the chamber.
- Kapton™ window is bending towards inside and increases air gap, light elements as Na absorption in air.
- Laserspots were too large for 150  $\mu\text{m}$  optic undefined position.

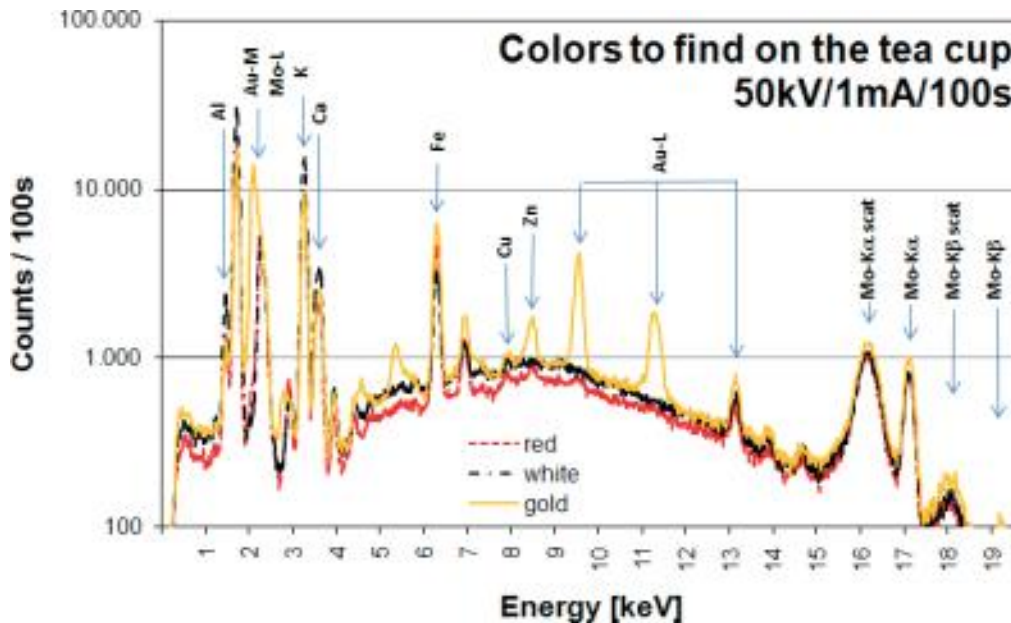


➤ solution: New design PART II



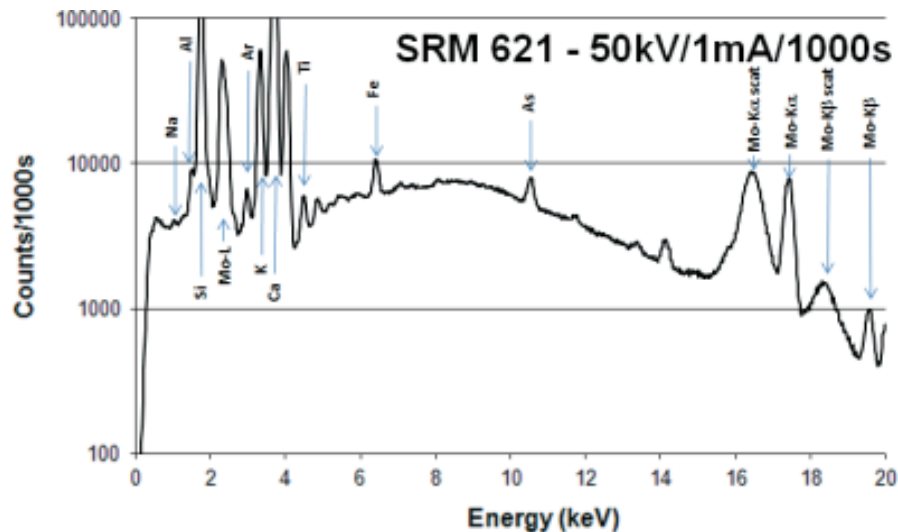
- Spectrometer motorized positioning (200 mm / 300 mm / 1000 mm depth x width x Height)
- Stable design of stand
- User friendly control

- Elemental composition of various colors of the tea cup:
  - White: base material
  - Red: Higher Fe Gehalt, probably red Ockre. Small amounts of Zn point to a cup of the last century.
  - yellow: Gold





Determination of detection limits (LLD)  
with NIST621 Soda-Lime Container  
Glass:



Element	LLD [ppm]
Na	7,69%
Al	452
Si	205
K	39
Ca	28
Ti	4
Fe	6
As	6

$$LLD = m \frac{3\sqrt{N_B}}{N_N}$$

Official radiation protection !!

THANKS FOR YOUR

ATTENTION

