

Multiple Filamentation of UV Supercritical Laser Beam in Atmospheric Air

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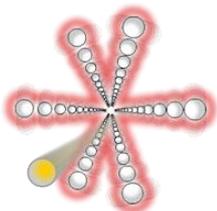
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**The 6th International Conference Channeling 2014 -
Charged & Neutral Particles Channeling Phenomena
Capri (NA), Italy, October 5-10, 2014**

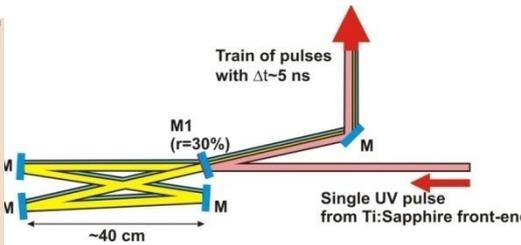
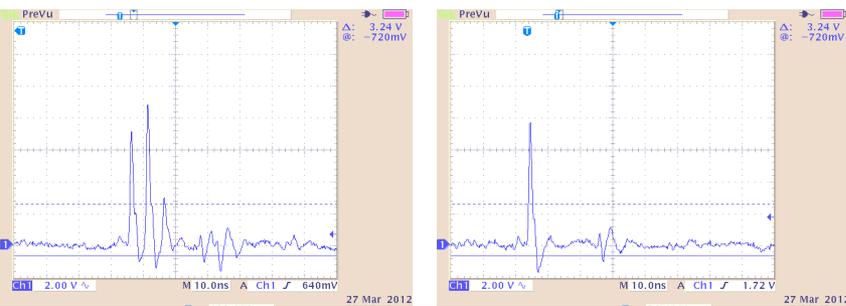
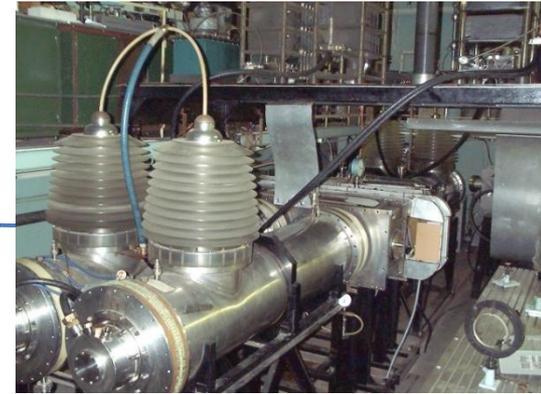
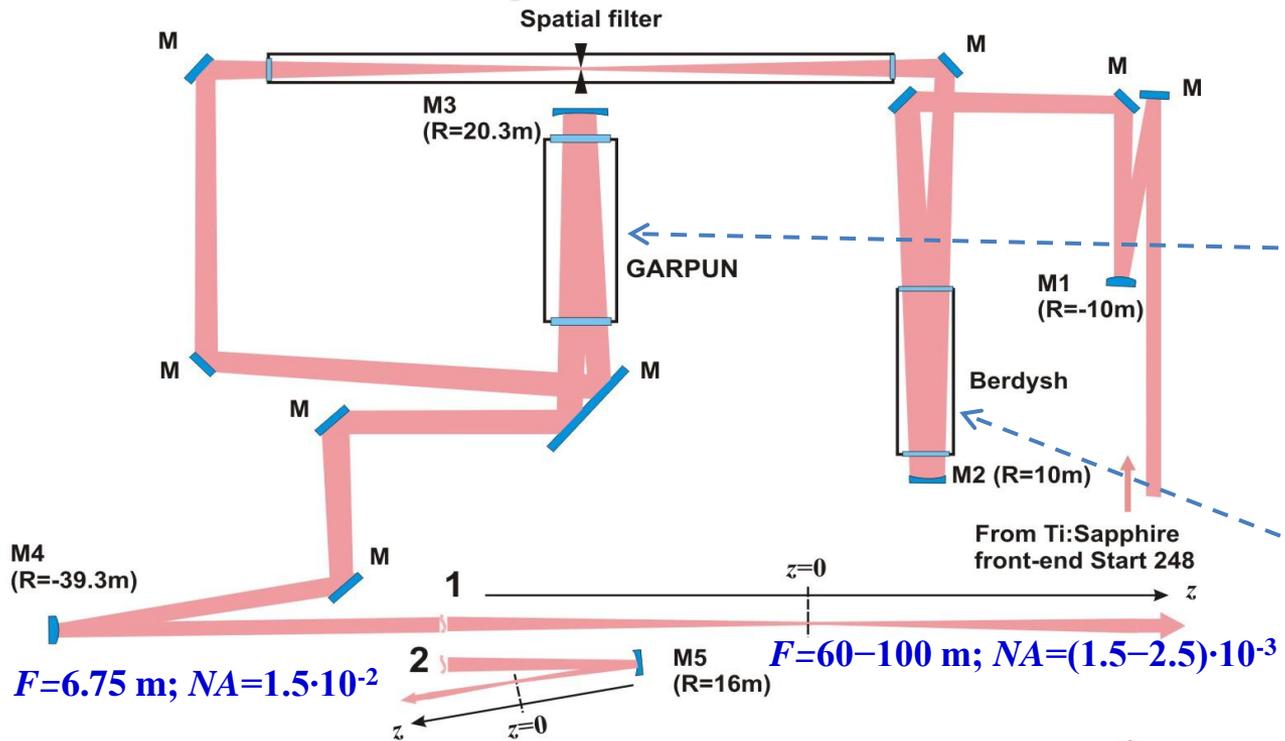
Outline

- **History of laser beam filamentation and motivation for research:**
 - **guiding of HV electric (lightning) discharges**
 - **transport of MW radiation in plasma waveguides**
 - **filament induced breakdown spectroscopy (FIBS)**
 - **backward atmospheric N₂ laser**
- **Ti:Sapphire/KrF GARPUN-MTW laser facility**
- **Filamentation of supercritical UV laser radiation**
- **Conclusions**

Historical notes

- Self-focusing (filamentation) of laser radiation was firstly suggested by Askar'yan (*Sov. Phys. JETP*, 1962, 15, 1088) and observed by Pilipetskii & Rustamov in organic liquids for Q-switched 20 MW, ns laser pulses (*JETP Lett.*, 1965, 2, 55). For theory see Akhmanov et al, *Sov. Phys. Usp.* 1968, 10, 609.
- Commonly observed in liquids and solids, filaments damage solid-state laser amplifiers and put power limit for short pulses (Basov, et al, *Sov. Phys. JETP*, 1966, 23, 16).
- With Ti: Sapphire laser, which generates ultra-short pulses (USP) in fs range at wavelength ~ 800 nm, filamentation was also observed in atmospheric air (Braun et al. *Opt. Lett*, 1995, 20, 73); nowadays it has a big room for applications.
- **KrF laser due to a short radiation wavelength $\lambda=248$ nm, unique possibility to generate pulses of different waveforms and duration from subps to 100 ns can produce extended plasma channels for various applications.**

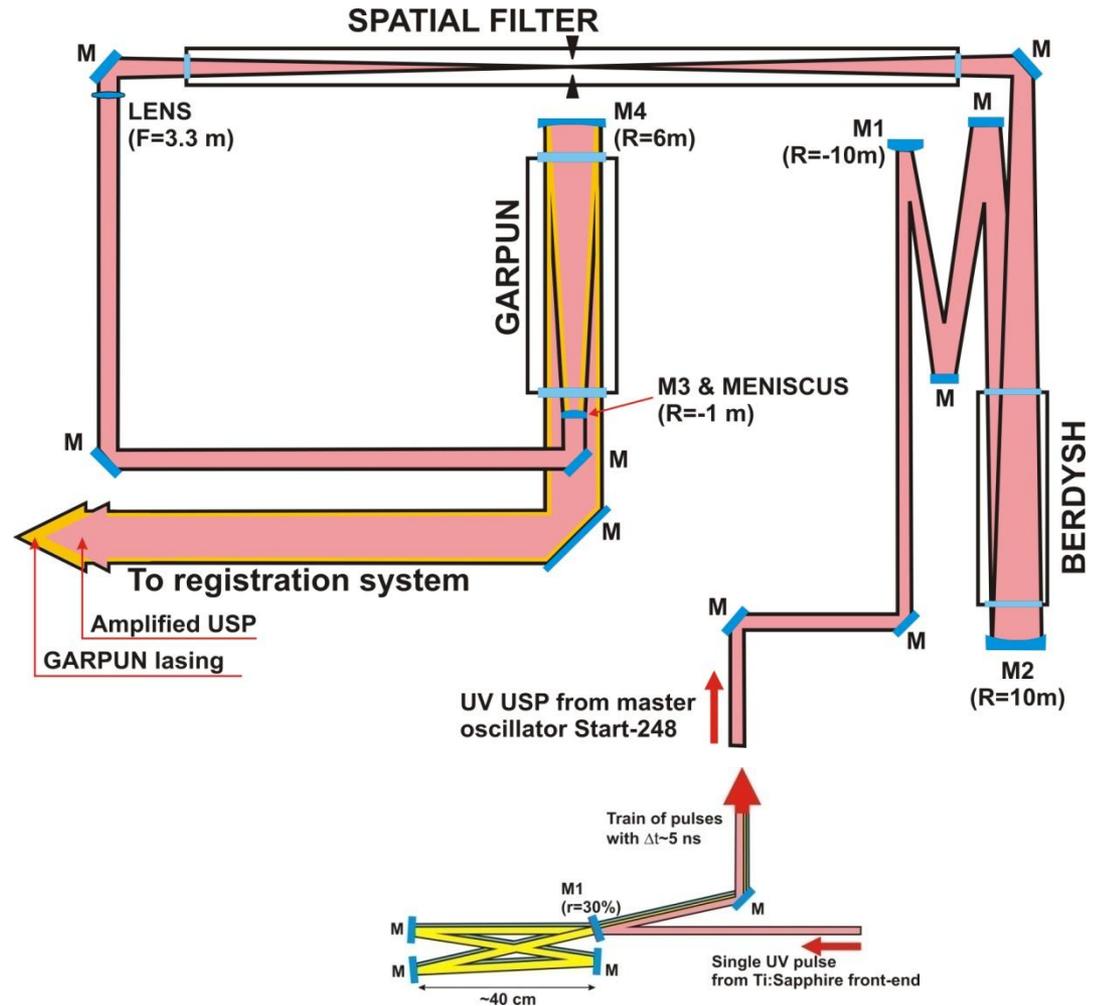
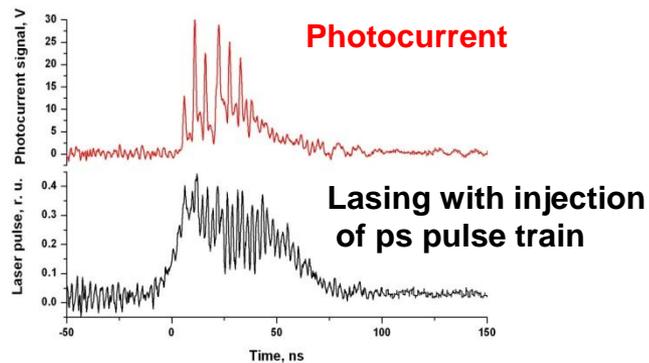
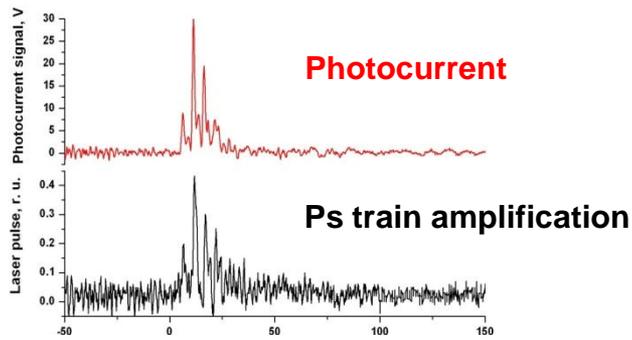
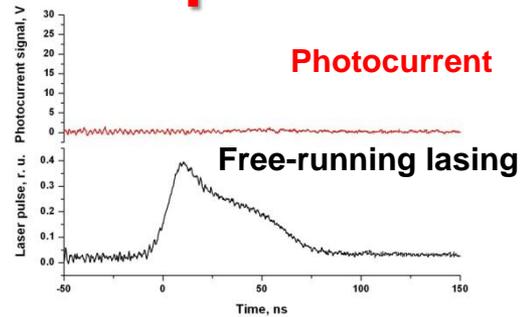
Amplification of a train of ps, sub-TW UV pulses at Ti:Sapphire/KrF GARPUN-MTW Laser



Single USP: $E_1 \leq 1 \text{ J}$; $\tau_p < 1 \text{ ps}$; $P_1 \sim 1 \text{ TW}$; train : $E \leq 2 \text{ J}$;
 $P_1:P_2:P_3\dots=3:5:1.5:0.5\dots$, $\Delta t = 3-5 \text{ ns}$

Zvorykin et al, *Quantum electron*. 2014, **44**, 431.

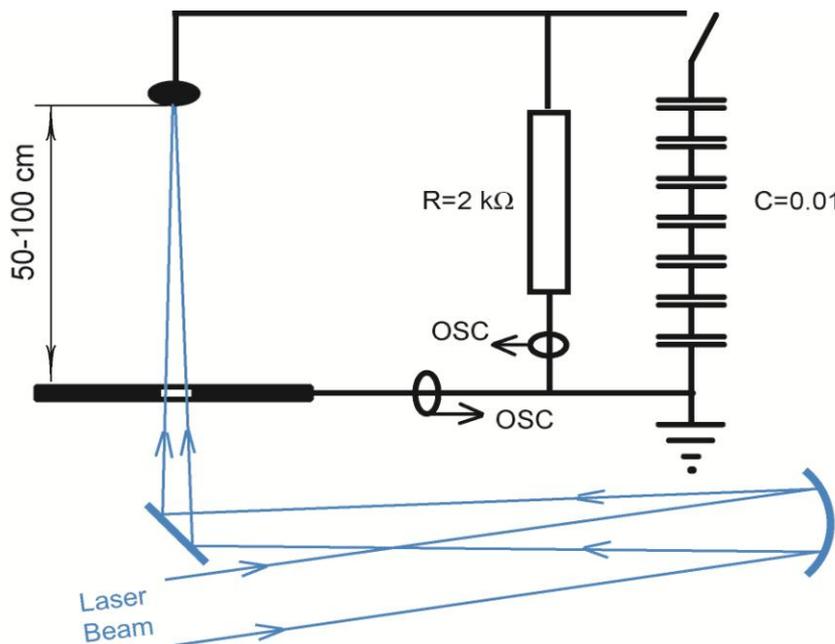
Simultaneous amplification of ps pulse train and 100-ns UV pulses at Ti:Sapphire/KrF GARPUN-MTW laser



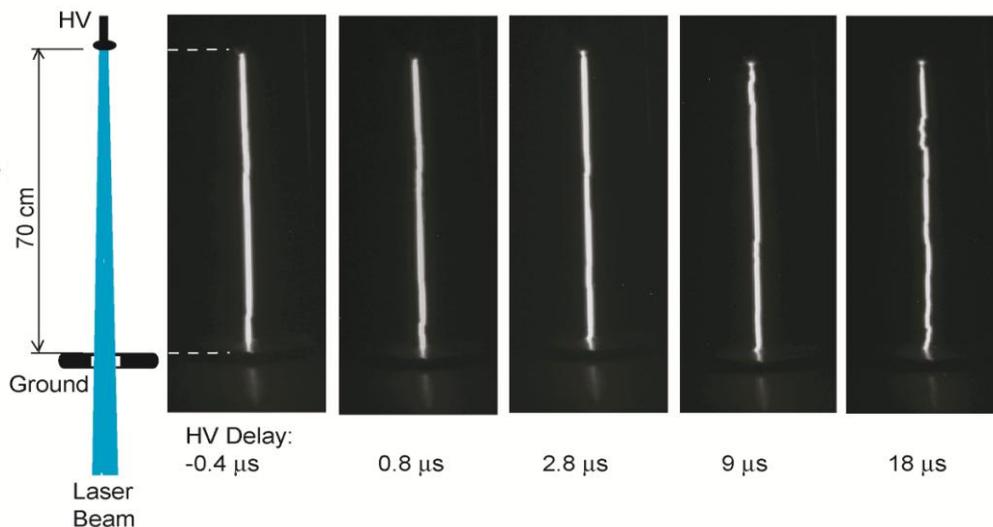
Combination of the USP train and 100-ns lasing pulse is an effective tool for air ionization and maintenance electron density in a plasma channel for a long time, while spatial matching of both radiations is an issue.

Guiding of HV discharge by combined UV radiation

Layout of experiments



Images of discharges initiated by combined laser pulse ($E_L=6.3\text{ J}$) for different delays of applied voltage ($U=420\text{ kV}$).



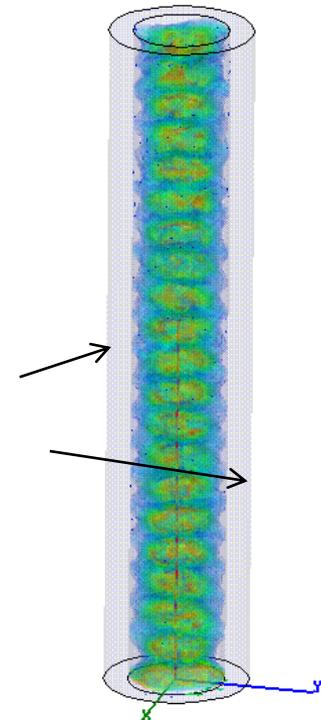
A combined laser pulse produces long ionization trace in air which initiates HV discharge and guides it along 70-cm gap.

A sliding-mode hollow-core plasma waveguide for directed transfer of MW radiation

- Firstly proposed by Askar'yan (*Sov. Phys. JETP*, 1969, 28, 732) with a powerful tubular UV laser beam as a source for multi-photon air ionization. It was realized with 1 GW, 100 ns KrF laser (V.D. Zvorykin, *et al*, 2010, *Bull. of Lebedev Phys. Inst*, 37, 60; V.D. Zvorykin, *et al*, 2010, *JETP Lett.* 2010, 91, 226).
- As a refractive index in air plasma is slightly less than in air, for waveguide radius $R_{wg} \gg \lambda_{MW}$ internal reflection at the air-plasma boundary confines radiation in the central core of a waveguide. Physically this sliding-mode regime is similar to light propagation in optical fibers.



Plasma wall



MW source

USP train or combined radiation seems to be the most attractive to produce a sliding-mode waveguide consisting of plasma filaments (Zvorykin *et al.* *Appl. Opt.* 2014, 31).

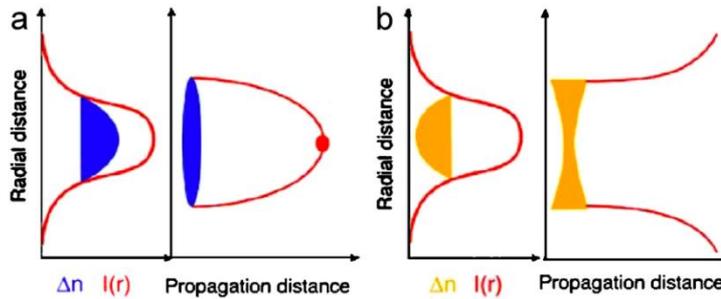
Comparison of filamentation of IR and UV radiation

Kerr focusing

$$n = n_0 + n_2 I(r, t)$$

Critical power

$$P_{cr} = 3.77 \lambda_0^2 / 8\pi n_0 n_2$$



Plasma defocusing

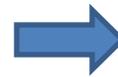
$$n \approx n_0 - \rho(r, t) / 2\rho_c, \quad \rho_c = \epsilon_0 m_e \omega_0^2 / e^2,$$

$$\rho = \sigma_K I^K \rho_{at} \tau_p$$

$$\sigma_{Br} = \frac{e^2}{\epsilon_0 m_e c n_0} \frac{\tau_c}{(1 + \omega^2 \tau_c^2)} \approx \frac{e^2}{\epsilon_0 m_e c n_0 \tau_c \omega^2}$$

The collapse is stopped when plasma defocusing balances Kerr focusing

$$n_2 I = \frac{\rho(I)}{2\rho_c} + \frac{(1.22\lambda_0)^2}{8\pi n_0 w_0^2}; \quad \rho(I) = \sigma_K I^K \rho_{at} \tau_p$$



Scaling for filament parameters :

$$I \sim \left(\frac{0.76 n_2 \rho_c}{\sigma_K \rho_{at} \tau_p} \right)^{\frac{1}{K-1}}; \quad \rho(I) \propto \left[\frac{(0.76 n_2 \rho_c)^K}{\sigma_K \rho_{at} \tau_p} \right]^{\frac{1}{K-1}};$$

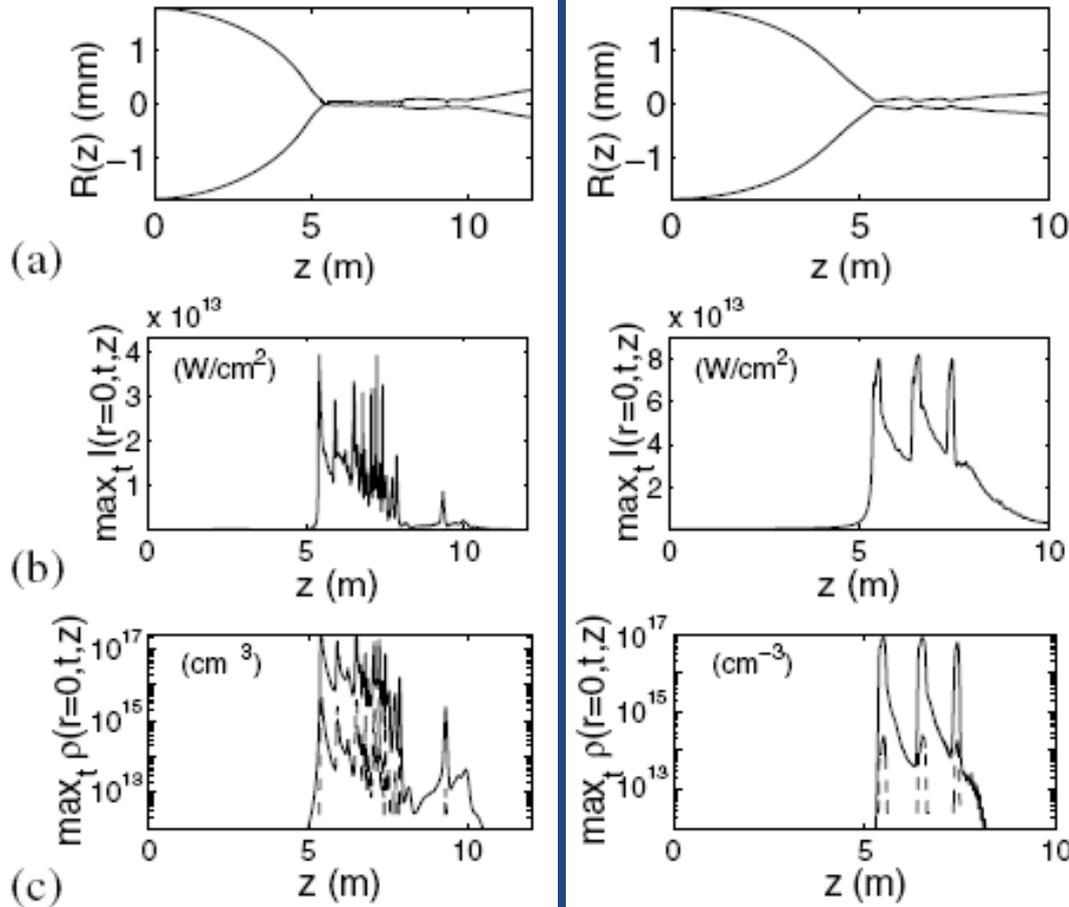
$$w_0 \propto \left(\frac{2P_{cr}}{\pi} \right)^{1/2} \left(\frac{0.76 n_2 \rho_c}{\sigma_K \rho_{at} \tau_p} \right)^{-\frac{1}{2(K-1)}}$$

Wavelength λ , nm	800	248
n_2 , cm ² ·W ⁻¹	(2.8–3.0)·10 ⁻¹⁹	(8–10)·10 ⁻¹⁹
P_{cr} , GW	3.4–3.6	0.1–0.12
O ₂ ($W_i=12.06$ eV): K ; σ_K , s ⁻¹ ·(cm ² ·W ⁻¹) ^K	8; 2.8·10 ⁻⁹⁶	3; 1.4·10 ⁻²⁸
N ₂ ($W_i=15.58$ eV): K ; σ_K , s ⁻¹ ·(cm ² ·W ⁻¹) ^K	11; 6.3·10 ⁻¹⁴⁰	4; 3.2·10 ⁻⁴⁴

Parameters of single filaments for the IR and UV radiation (according to Couairon & Berge calculations)

UV light ($\lambda = 248$ nm)

IR light ($\lambda = 800$ nm)

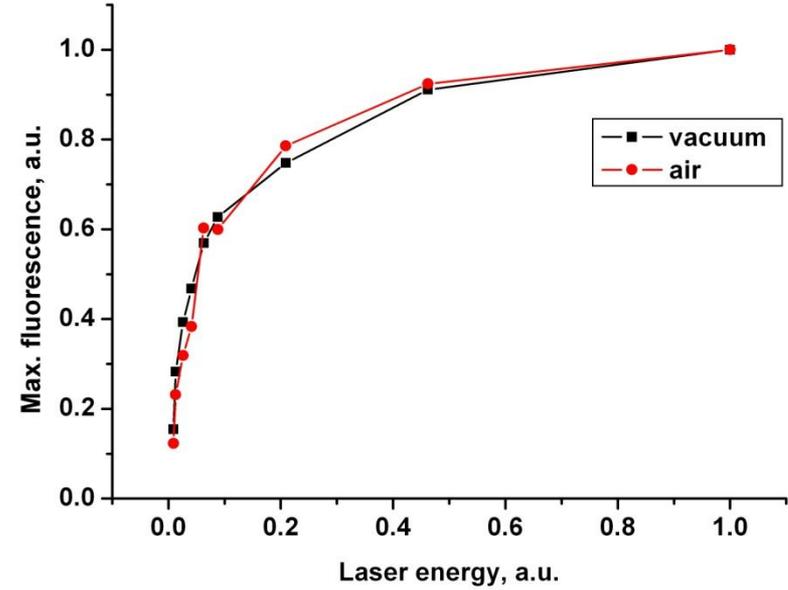
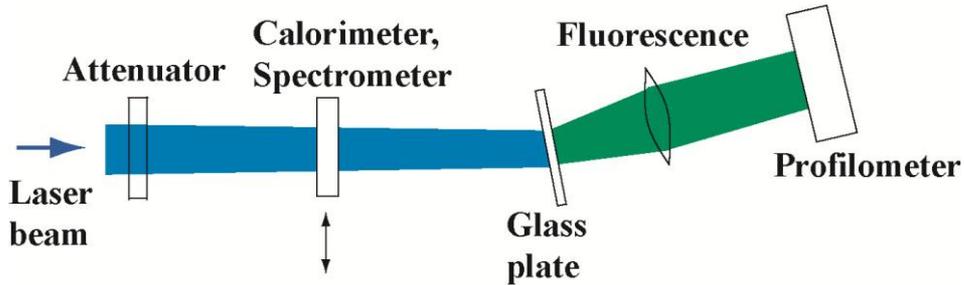


- According to scaling formulas and numerical simulations (PRL, 88, 135003 (2002)) peak intensities in single filaments $I \sim 10^{13}$ W/cm², electron densities $\rho \sim 10^{16} \div 10^{17}$ cm⁻³, and filament size $w_0 \sim 100$ μ m are approximately equal for both UV and IR wavelengths.

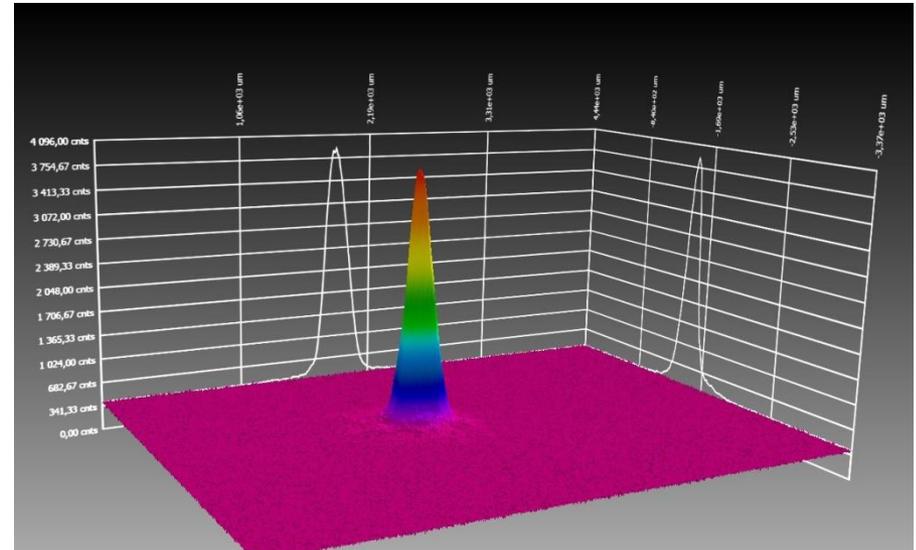
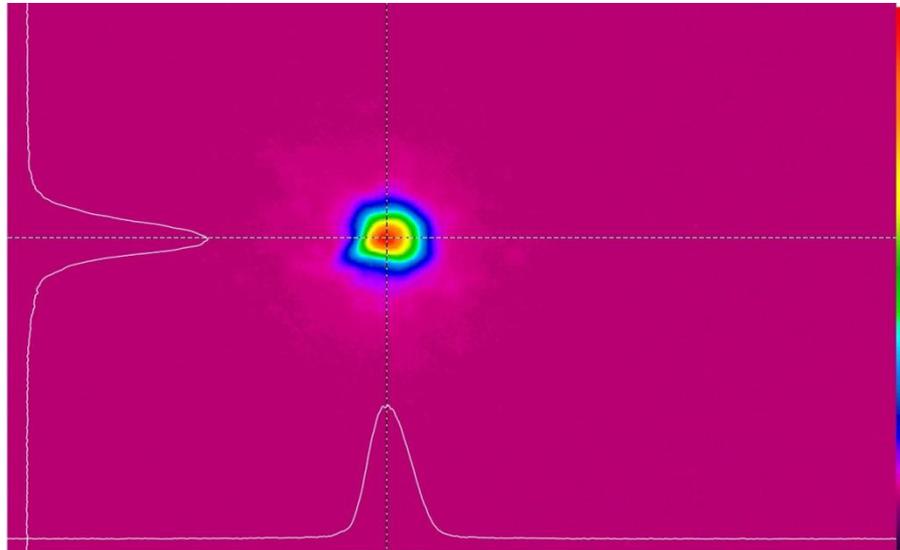
- **A big room for experimental values for UV radiation still exists. Present experiments were performed at frequency-tripled Ti:Sapphire front-end ($\tau_{1/2} \sim 100$ fs) of GARPUN-MTW laser facility to find critical power and diameter of filaments.**

FIG. 2. (a) Beam radius, (b) peak intensity, and (c) electron density as functions of z for a UV pulse (left column) and an IR pulse (right column) propagating in air.

Filaments registration

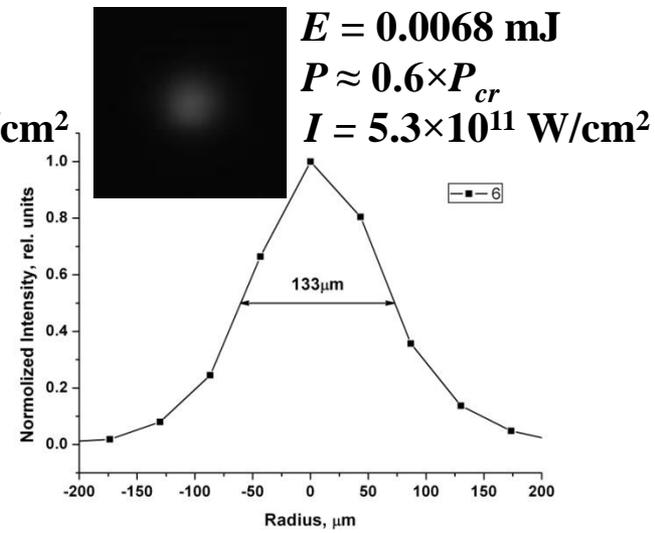
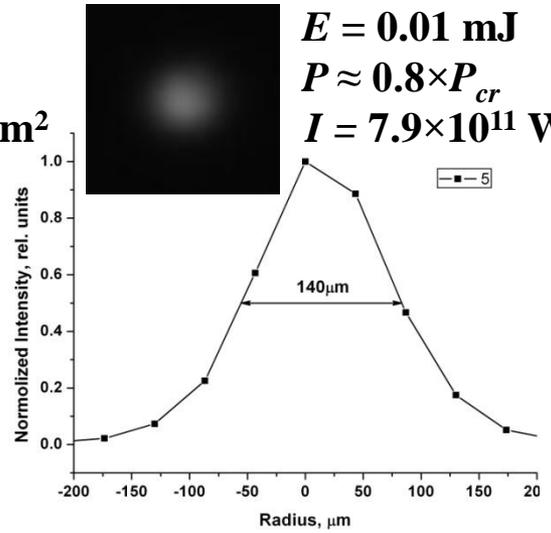
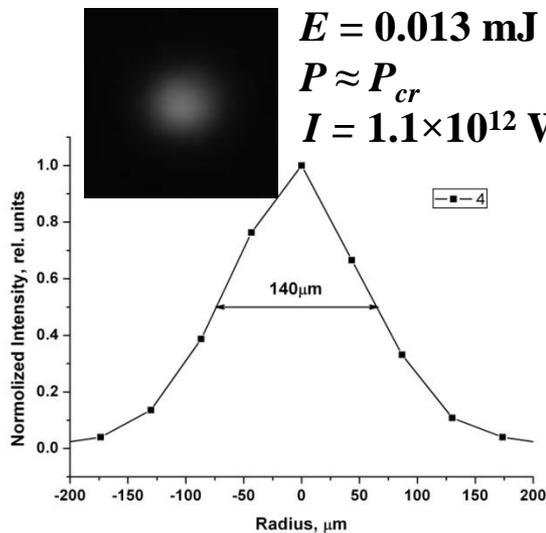
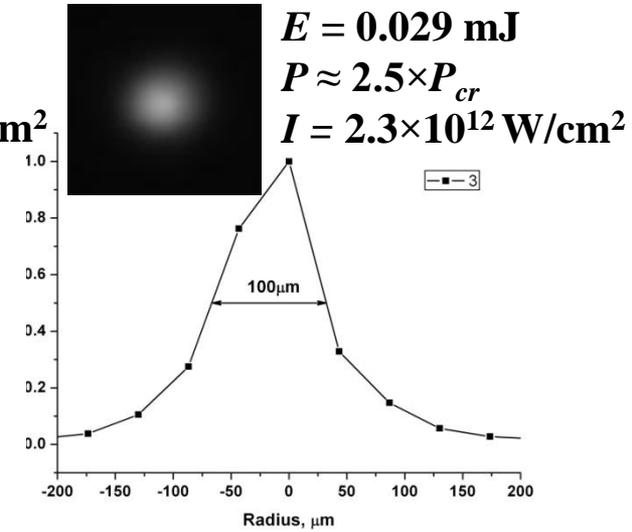
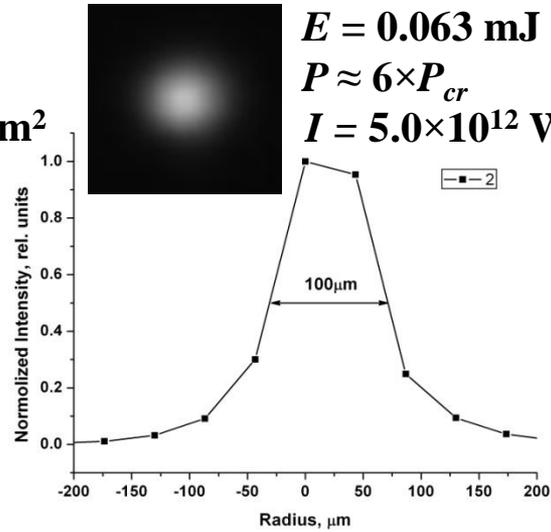
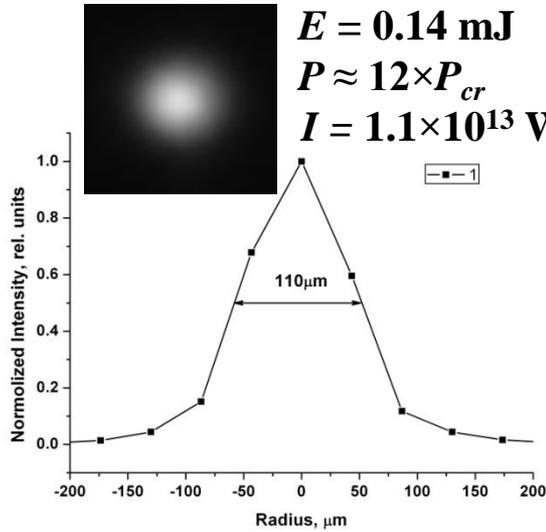


Glass fluorescence under UV irradiation was measured with Ti: Sapphire front-end. A single filament produced by 0.2 mJ, 100-fs USP has 20 cm length which is much more than diffraction (Reyleigh) length of focused beam.



Single filaments of 100-fs UV laser pulse

For higher peak powers of 100-fs UV USP $10 \cdot P_{cr} \geq P \geq P_{cr}$ a single filament of $d_{0.5} \approx 100 \mu\text{m}$ diameter was observed



For lower powers $P \leq P_{cr}$ filaments were not observed while $d_{0.5} \approx 130 \mu\text{m}$

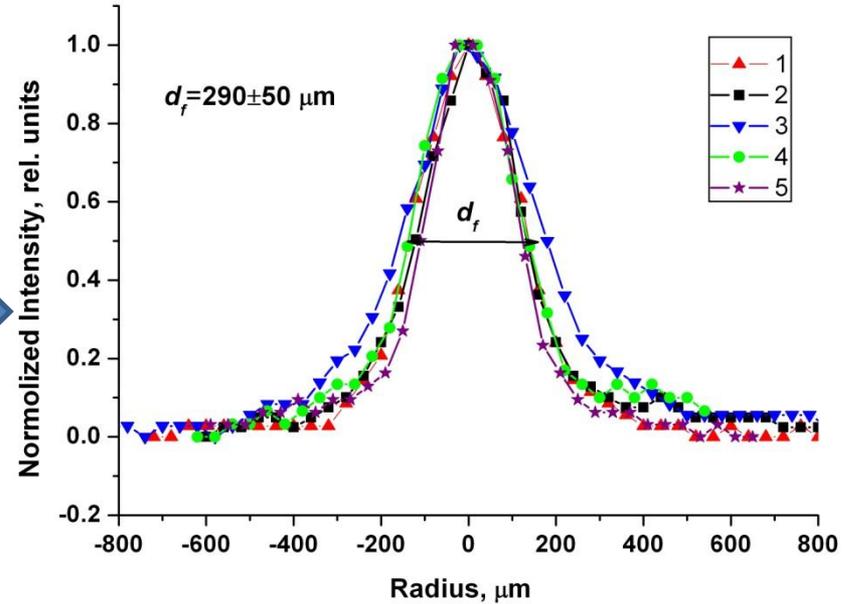
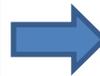
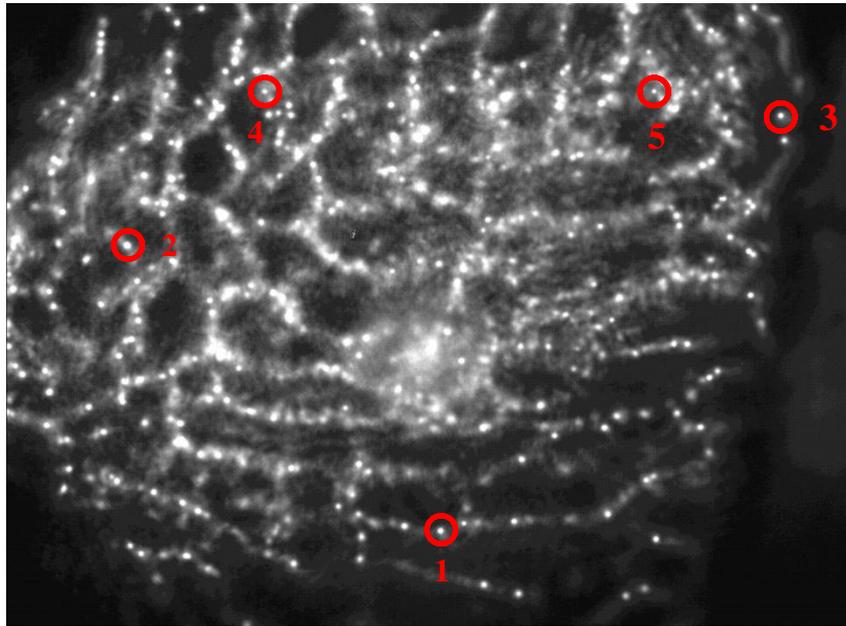
Multiple filamentation of a supercritical UV laser beam

- For $P \gg P_{cr}$ modulation instability breaks the beam to multiple filaments (Campillo et al., *Appl. Phys. Lett.*, 1973, 23, 628).
- Theory of the linear power partitioning (Roskey et al, *Appl. Phys. B*, 2007, 86, 249) predicts that a number of filaments is $N \sim P / P_{cr}$, while experiments with very high 100 TW peak power at $\lambda \sim 800$ nm evidence about saturation of filaments density due to their mutual interaction (Henin et al, *Appl. Phys. B*, 2010, 100, 77).
- For UV laser beam at $\lambda=248$ nm wavelength filamentation is 30 times easier to achieve that enables us to investigate multifilamentation dynamics at TW power level available at GARPUN-MTW laser facility.
- Filamentation of a single USP of ~ 1 ps pulse duration and sub-TW peak power ($P / P_{cr} > 1000$) is compared with filamentation of a USP train when they both propagate along 100-m distance in various focusing geometries.

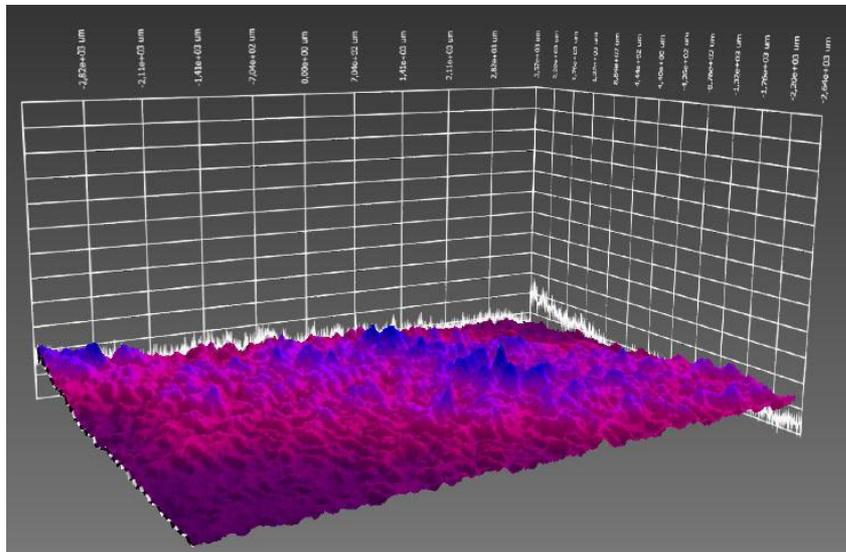
Multiple filamentation of 1-ps UV USP beam

80 mm

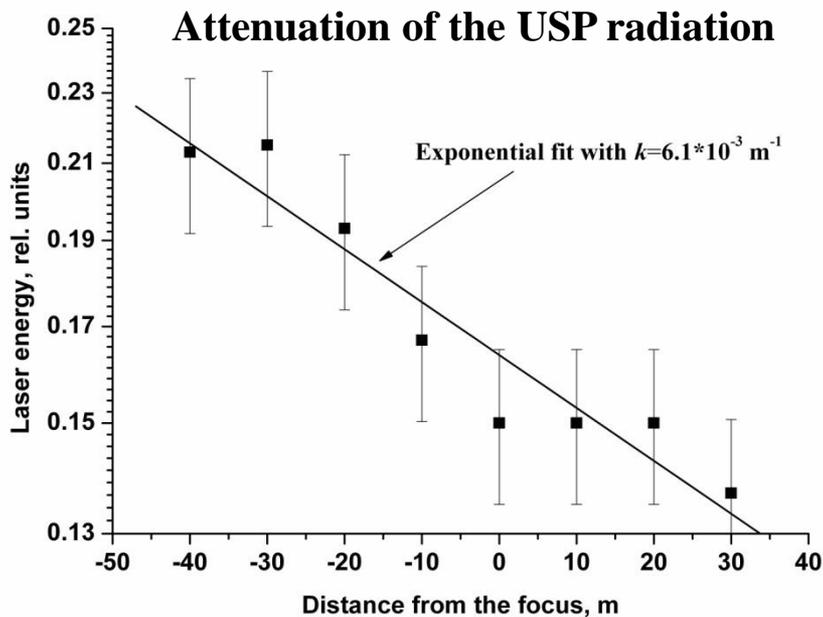
$$E_1 = 0.23 \text{ J}; P_1 \approx 2000 \times P_{cr}; z = -75 \text{ m}$$



About 500 filaments contain 30% of the total pulse energy while the rest is in the background radiation. Filaments are grouped along the boundaries of CaF_2 window blocks, which introduce phase aberrations into the beam. Diameter of filaments is in the range 240–340 μm .



Parameters of multiple filaments of UV USP beam



- **Filaments for 1-ps UV USP are quite different of those for 100-fs pulse: their diameter is 3 times bigger, while intensity and electron density are lower in 10^2 and 10^3 times.**
- **Diffraction balances Kerr self-focusing instead of plasma defocusing.**
- **Resonance processes (REMPI instead of direct MPI and SRS) supposedly give additional input into nonlinear matter polarization.**

Absorbed laser energy:

$$\frac{dE}{dz} = \kappa E = 1.2 \cdot 10^{-5} \text{ J/cm (for } E = 0.2 \text{ J)}$$

Number of electrons per beam length:

$$\frac{dN_e}{dz} = \frac{1}{3h\nu} \frac{dE}{dz} = 5 \cdot 10^{12} \text{ cm}^{-1} \text{ (for } h\nu = 5 \text{ eV)}$$

Number of filaments: $N_f \approx 500$

Number of electrons per filament length:

$$\frac{dN_{ef}}{dz} = \frac{1}{N_f} \frac{dN_e}{dz} = 10^{10} \text{ cm}^{-1}$$

Electron density in filaments:

$$\rho = \frac{1}{S_f} \frac{dN_{ef}}{dz} = (1.5 \pm 0.5) \cdot 10^{13} \text{ cm}^{-3},$$

where $S_f = \frac{\pi d_f^2}{4}$; $d_f = (290 \pm 50) \mu\text{m}$

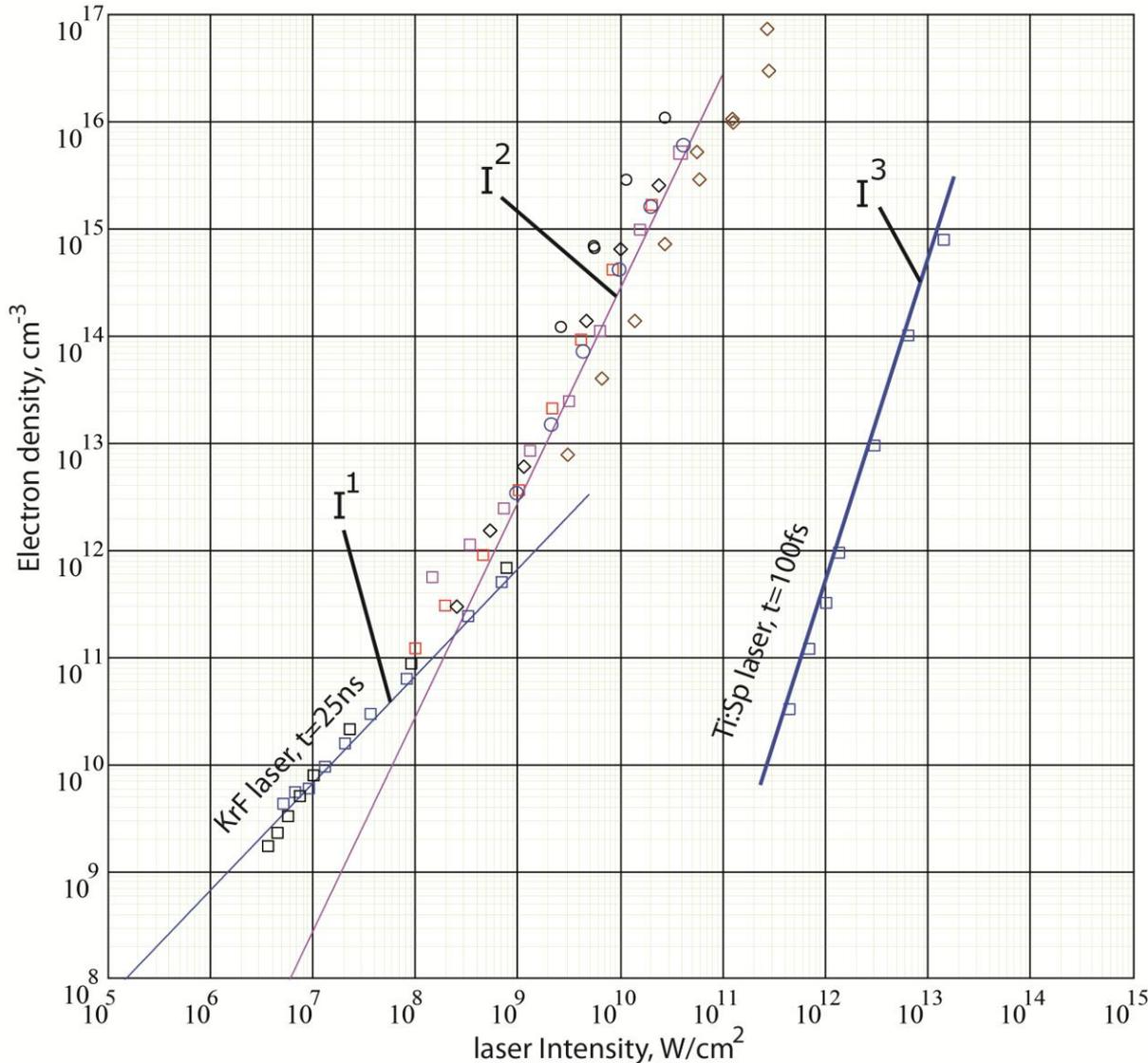
Power in a filament:

$$P_f = 0.3P/N \approx 1.2 \cdot 10^8 \text{ W} \approx P_{cr}$$

Intensity in filaments:

$$I = P_f/S_f = (1.8 \pm 0.6) \cdot 10^{11} \text{ W/cm}^2$$

Air ionization by UV radiation



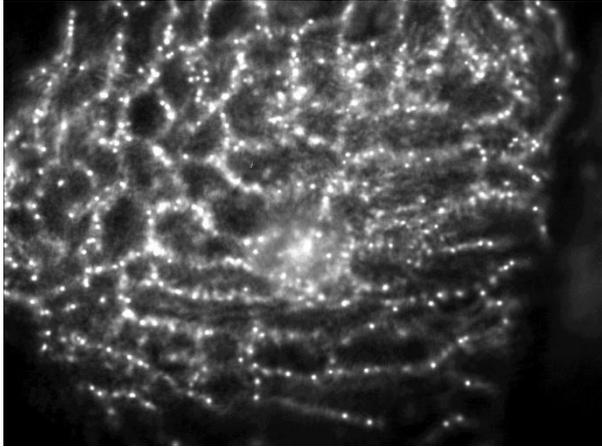
Electron density vs. laser intensity

- For USP ($\tau \sim 100$ fs),
 $I = 3 \cdot 10^{11} \div 1.5 \cdot 10^{13}$ W/cm²
 $\rho \sim I^3 \cdot \tau$ – 3-photon O₂ ionization (MPI).
- For long pulses ($\tau \sim 25$ ns),
 $I = 10^8 \div 10^{11}$ W/cm² $\rho \sim I^2 \cdot \tau$
 – (2+1) resonance enhanced multiphoton O₂ ionization (REMPI).
- For $I = 5 \cdot 10^6 \div 5 \cdot 10^8$ W/cm² $\rho \sim I \cdot \tau$ – photoionization of impurities or photoemission of aerosol particles.

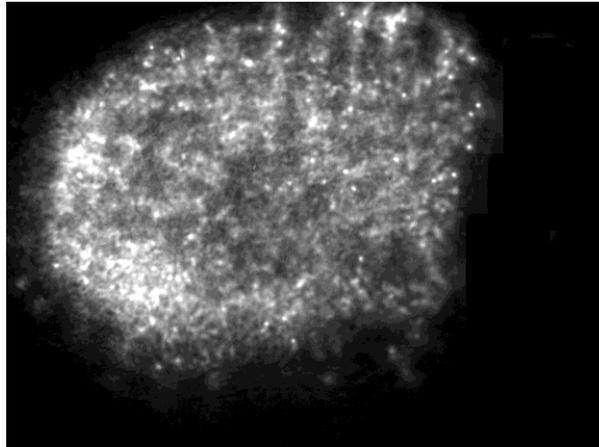
Focusing of a multiply-filamented USP beam ($F = 100$ m)

$$E_1 = 0.23 \text{ J}; P_1 \approx 2000 \times P_{cr}$$

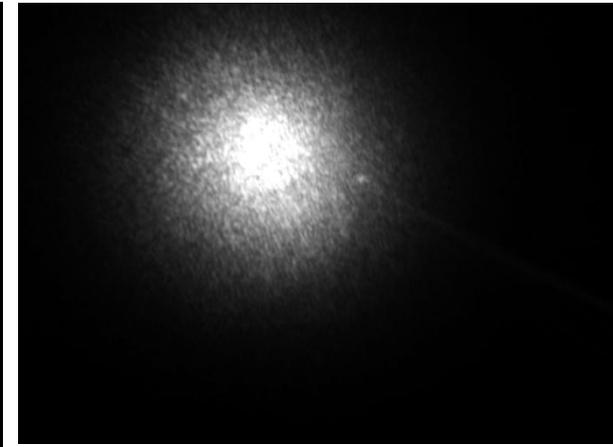
$z = -75$ m



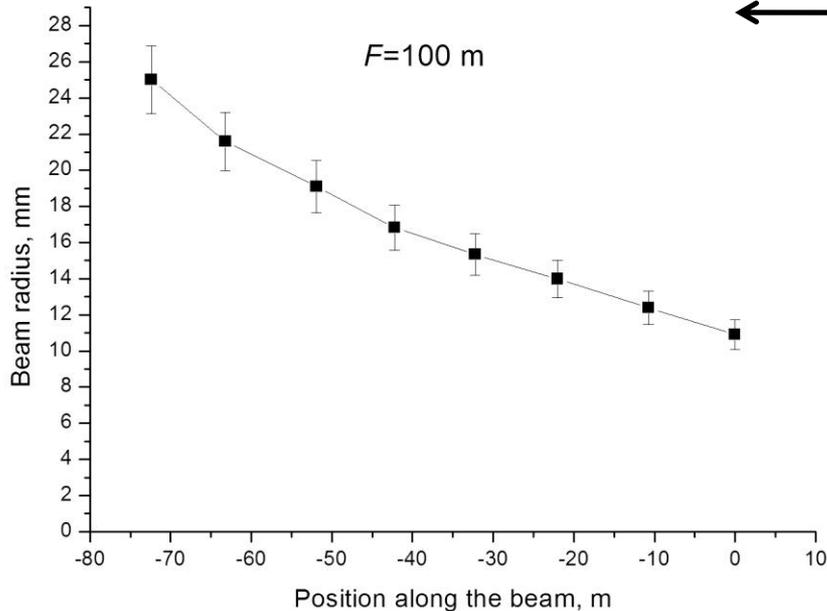
$z = -50$ m



$z = 0$

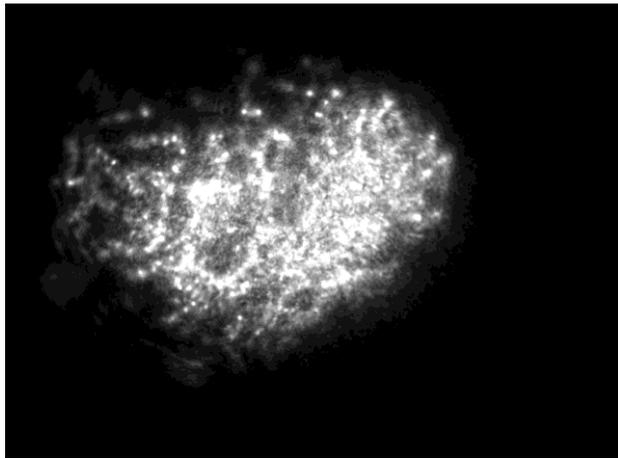


40 mm

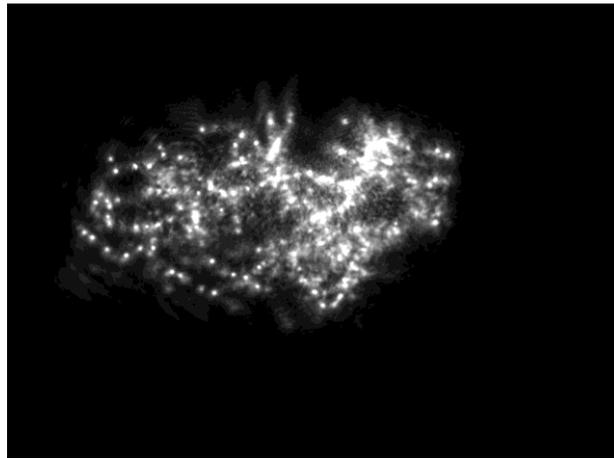


Linear focusing was observed for multiply-filamented UV USP beam which allows us to combine it with low-intensity 100-ns lasing pulse.

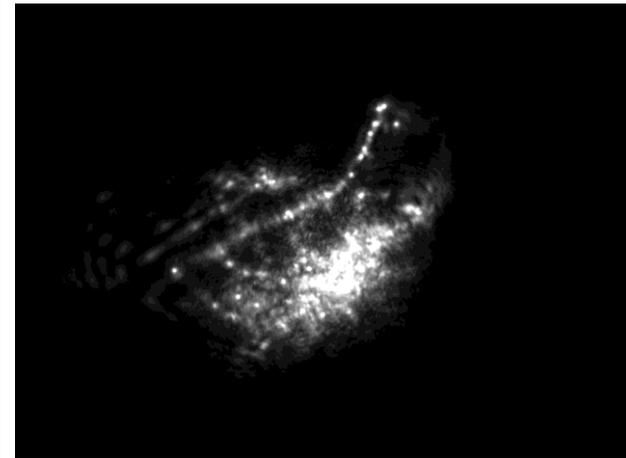
Multiple filamentation of USP beam in dependence on power ($F = 60$ m; $z = -22.5$ m)



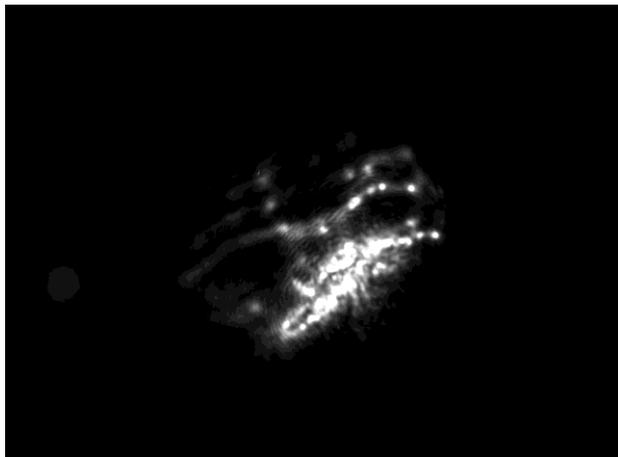
$$E_1 = 0.16 \text{ J}; P_1 = 1330 \times P_{cr}$$



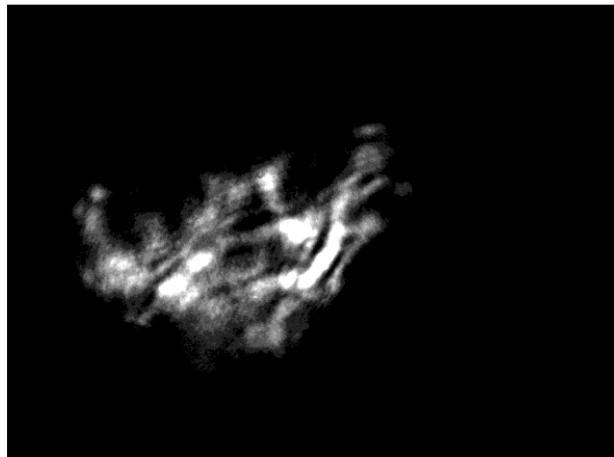
$$E_1 = 0.084 \text{ J}; P_1 = 700 \times P_{cr}$$



$$E_1 = 0.048 \text{ J}; P_1 = 400 \times P_{cr}$$



$$E_1 = 0.016 \text{ J}; P_1 = 133 \times P_{cr}$$



$$E_1 = 0.004 \text{ J}; P_1 = 33 \times P_{cr}$$

30 mm



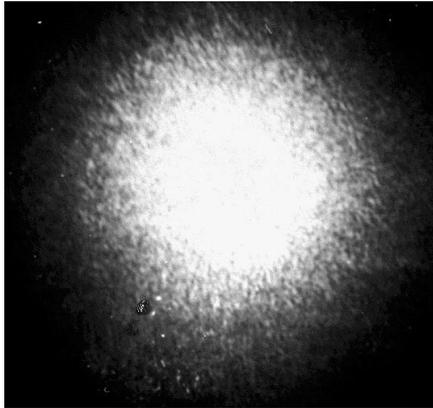
- In front of the linear focus a number of filaments decreases for lower USP energy.
- At $E_1 = 0.004$ J ($P_1 = 0.004$ TW = $33P_{cr}$) individual filaments coalesce into hot spots of bigger size ~ 1 mm.

Filamentation of a single USP behind the focus ($F = 60$ m)

$z = 0$

$$E_1 = 0.2 \text{ J};$$

$$P_1 = 1660 \times P_{cr}$$

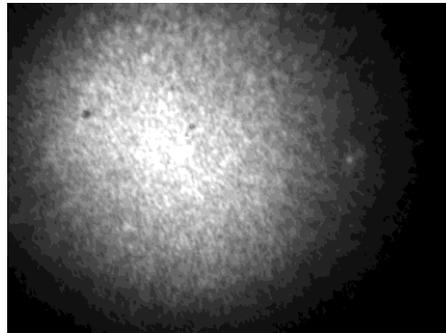


10 mm

$z = 37.5$ m

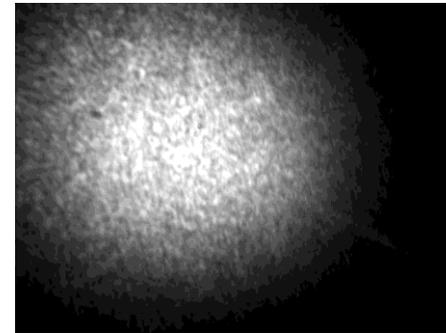
$$E_1 = 0.12 \text{ J};$$

$$P_1 = 1000 \times P_{cr}$$



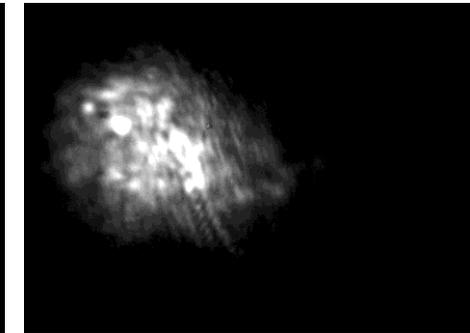
$$E_1 = 0.09 \text{ J};$$

$$P_1 = 750 \times P_{cr}$$

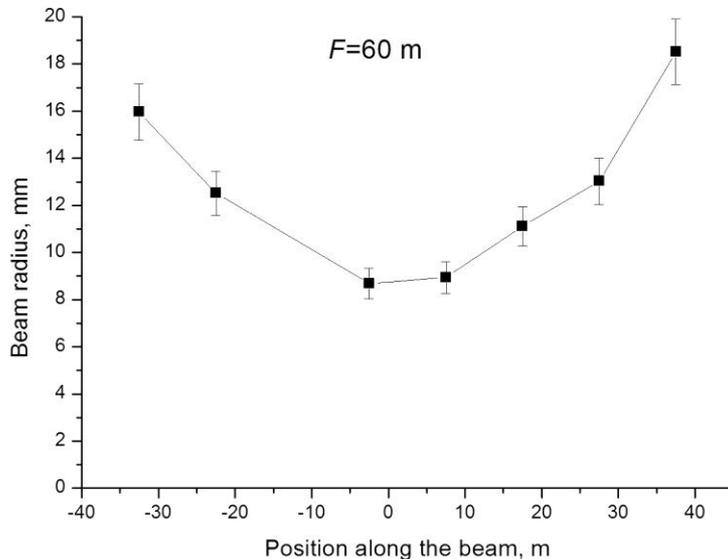


$$E_1 = 0.02 \text{ J};$$

$$P_1 = 166 \times P_{cr}$$

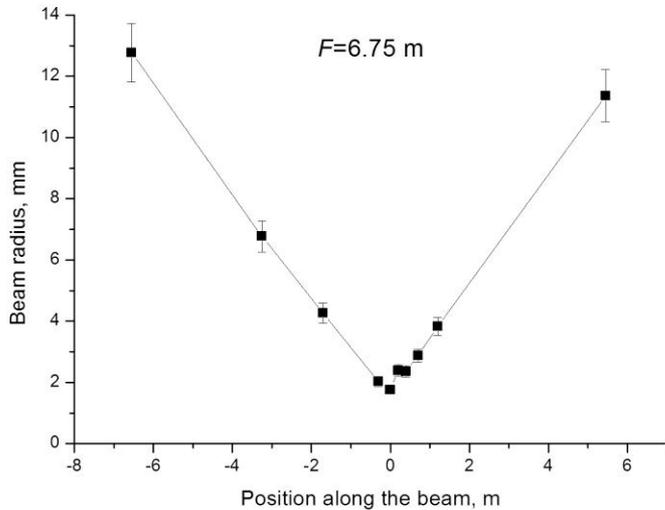


30 mm



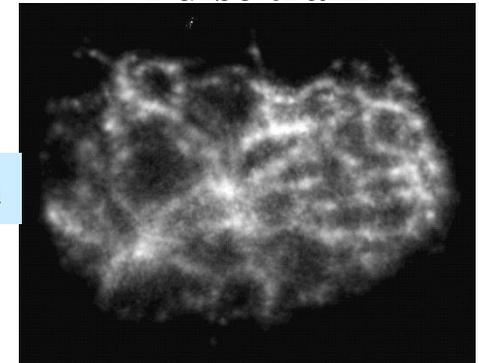
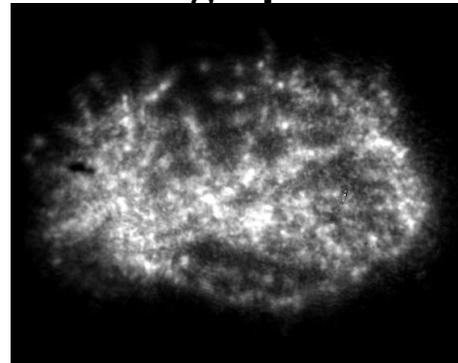
- The mean radius of the USP beam obeys a linear focusing with the caustic waist radius ~ 9 mm corresponding to the beam divergence $\sim 1.5 \times 10^{-4}$ rad;
- In the focal plane the maximal density of filaments is achieved and they are overlapped;
- In the expanding beam behind the focus filamentous structure reappears;
- Beam diameter and amount of filaments decrease at lower USP energy; filaments coalesce into hot spots of bigger size ~ 1 mm.

Multiple filamentation of USP train ($F = 6.75$ m)



Single pulse

Pulse train

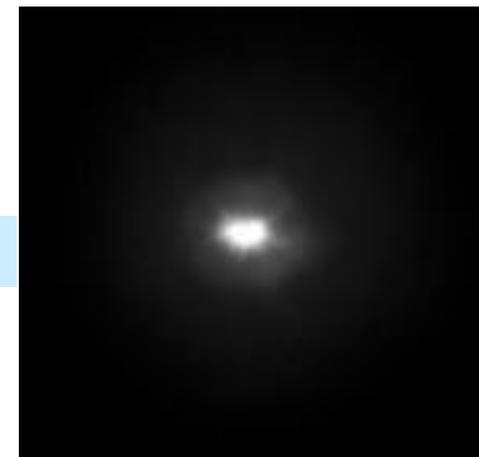
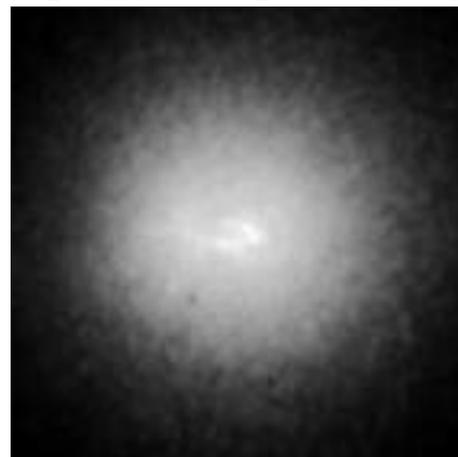


$z = -3.45$ m

20 mm

$E_1 = 0.19$ J; $P_1 = 1600 \times P_{cr}$

$E = 0.43$ J

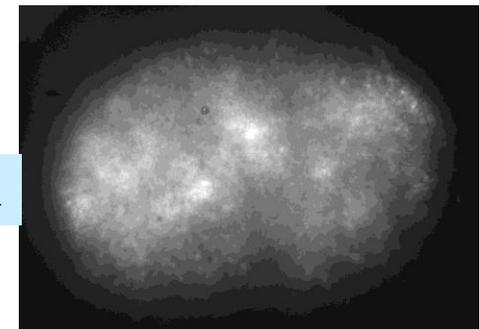
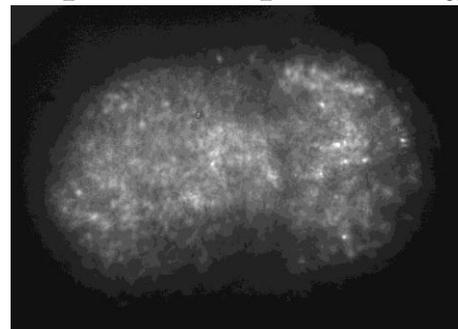


$z = 0$

2 mm

$E_1 = 0.15$ J; $P_1 = 1250 \times P_{cr}$

$E = 0.3$ J



$z = 5.25$ m

20 mm

$E_1 = 0.16$ J; $P_1 = 1330 \times P_{cr}$

$E_1 = 0.28$ J

- Linear beam focusing was observed for a single USP;
- For the USP train individual small-size filaments tend to coalesce into hot spots of bigger size ~ 1 mm;
- This effect is the most pronounced nearby the focus;
- Behind the focus multi-filamentous structure reappears with the same tendency towards coalescence of individual filaments for the USP train.

CONCLUSIONS

- A train of UV picoseconds pulses with TW peak power was generated at hybrid Ti:Sapphire/KrF GARPUN-MTW laser facility. It can be combined with 30-J, 100-ns pulse of a free-running lasing.
- Multiple filamentation of a single 1-ps UV pulse, as well as the pulse train with peak powers $P/P_{cr} > 1000$ was investigated in air along 100-m distance. In various focusing geometries ($NA = 1.5 \cdot 10^{-2} - 1.5 \cdot 10^{-3}$) multi-filamentous super-critical single-pulse beam demonstrated linear focusing behavior. For lower power as well as for the pulse train coalescence of individual filaments into 1-mm size hot spots was observed.
- Parameters of filaments for 1-ps pulse are quite different of those for 100-fs pulse. Radiation diffraction balances Kerr self-focusing instead of plasma defocusing. Probably resonance processes (REMPI and SRS) introduce into nonlinear matter polarization.