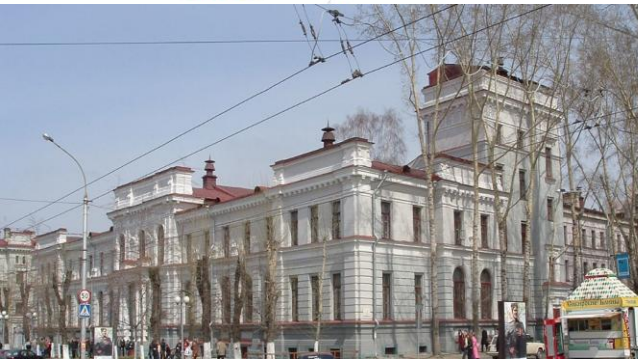




# Combined Effect in the Coherent Bremsstrahlung



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## Coherent Bremsstrahlung

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## Channeling Radiation

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## Combined Effect

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Yu.P.Kunashenko, Coherent Bremsstrahlung from planar channeled positrons//  
Journal of Physics: Conference Series **517** (2014) 012029 P.1-6.

# Photon scattering by channeled electron

(in reference frame moving with longitudinal channeled electron velocity)

$$d\sigma_{fi} = \frac{2\pi}{\hbar} |M_{fi}|^2 \delta(E_i - E_f - \hbar\omega) \frac{1}{J} d^3\mathbf{p}_{\parallel f} d\rho, \quad d\rho = \frac{d^3\mathbf{k}}{(2\pi)^3};$$

$$M_{fi} = \sum_n \left\{ \frac{(\mathbf{e}_2 \mathbf{R}_{fn})(\mathbf{e}_1 \mathbf{A}_{ni})}{(E_i + \hbar\omega_1) - E_n} + \frac{(\mathbf{e}_1 \mathbf{A}_{fn})(\mathbf{e}_2 \mathbf{R}_{ni})}{E_i - E_n - \hbar\omega} \right\}$$

$$\Psi_{ph}(\mathbf{r}) = \sqrt{\frac{2\pi\hbar c}{\hbar\omega}} \exp[-i\mathbf{k}\mathbf{r}]$$

Photon wave function

$$\mathbf{R}_{kl} = -\frac{e}{mc} \int \Psi_k^*(\mathbf{r}) \hat{\mathbf{p}} \sqrt{\frac{2\pi\hbar c}{\hbar\omega_2}} \exp[-i\mathbf{k}_2\mathbf{r}] \Psi_l(\mathbf{r}) d\mathbf{r}$$

$$\mathbf{A}_{kl} = -\frac{e}{mc} \int \Psi_k^*(\mathbf{r}) \hat{\mathbf{p}} \sqrt{\frac{2\pi\hbar c}{\hbar\omega_1}} \exp[+i\mathbf{k}_1\mathbf{r}] \Psi_l(\mathbf{r}) d\mathbf{r}$$

$\mathbf{k}_1$     $\mathbf{e}_1$     $\omega_1$    wave vector, polarization vector and frequency of the incident photon while

$\mathbf{k}_2$ ,  $\mathbf{e}_2$     $\omega_2$    wave vector, polarization vector and frequency of the scattered photon

$\hat{\mathbf{p}}$    momentum operator    $\Psi_l(\mathbf{r})$    channeled electron wave function.

$$\Psi_{i(f)}(\mathbf{r}) = \varphi_{i(f)}(\boldsymbol{\rho}) \exp(i\mathbf{k}_{|i(f)\parallel} \mathbf{r}_{\parallel}) \quad \text{Channeled electron wave function}$$

$$V(\rho) = -\frac{V_0}{\rho} \quad \text{- axis continuous potential}$$

$$\varphi_{i(f)}(\boldsymbol{\rho}) = e^{im\varphi} U_{nm}(\rho) \quad \text{transverse wave function}$$

$$U_{nm}(\rho) = \sqrt{\rho} \frac{1}{\Gamma(2m+1)} \left( \frac{\Gamma\left(n+m+\frac{1}{2}\right)}{\Gamma\left(n-m+\frac{1}{2}\right) 2m} \right)^{1/2} (2\alpha_n)^{3/2} e^{-\alpha_n \rho} (2\alpha_n \rho)^{m-1/2} F\left(-n+m+\frac{1}{2}; 2m; \alpha_n \rho\right);$$

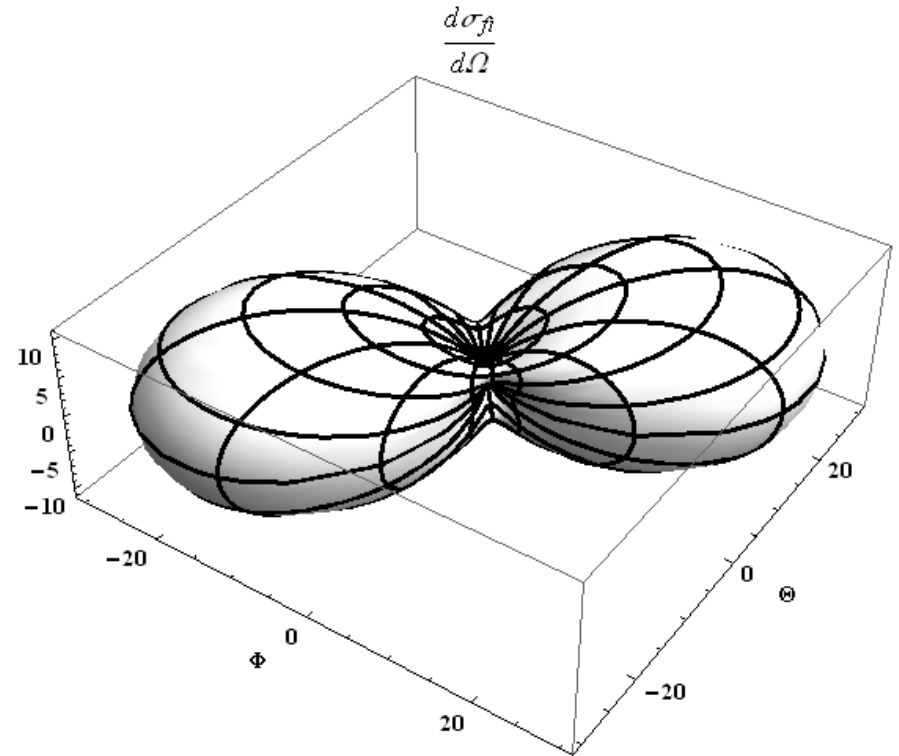
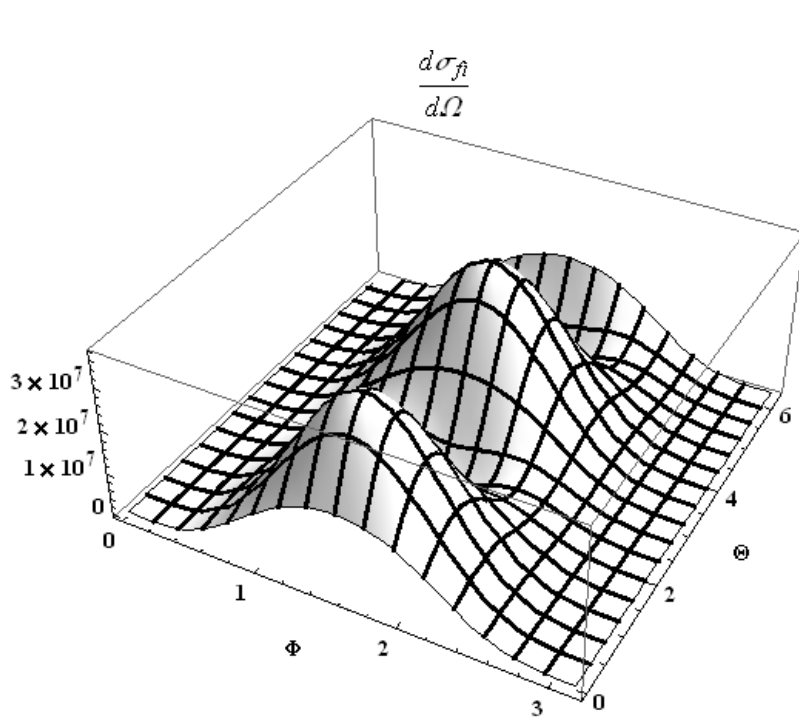
$$\alpha_n = \sqrt{-2\varepsilon_n E} / (\hbar c)^2;$$

$$\varepsilon_n = -\frac{V^2 E}{2\left(n+m+\frac{1}{2}\right)}. \quad \text{- transverse energy}$$

$$F\left(-n+m+\frac{1}{2}; 2m; \alpha_n \rho\right); \quad \text{confluent hypergeometric function (Kummer function)}$$

# Photon scattering by channeled electron

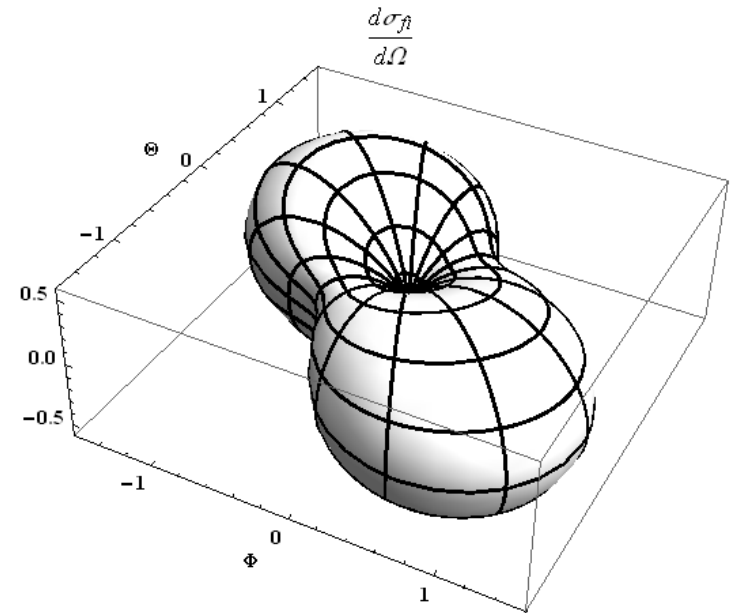
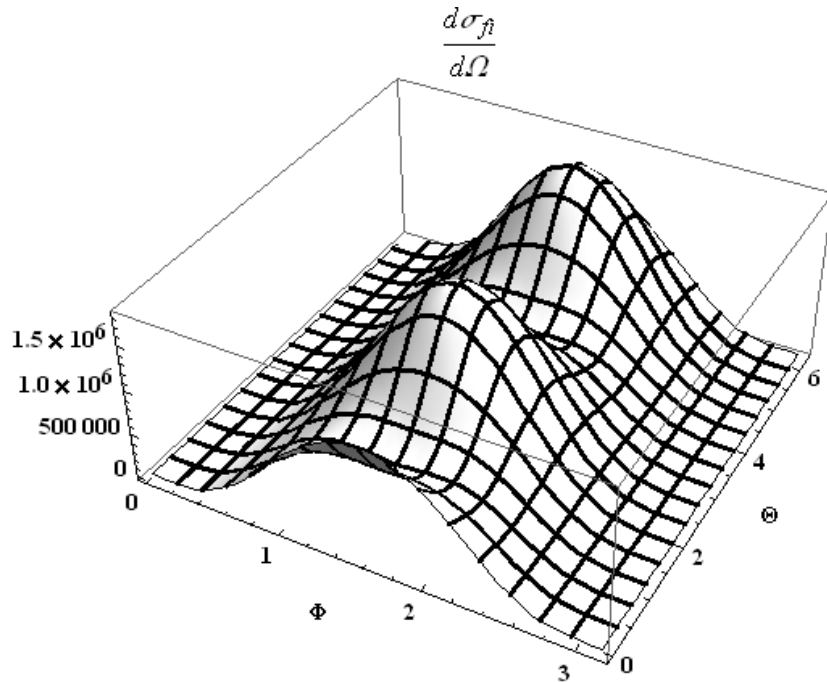
Crystal  $W\langle 100 \rangle$ , electron relativistic factor  $\gamma=10$ , transition  $(n=1, m=1) \rightarrow (n=0, m=0)$



Angular distribution of scattered photon in reference frame moving with longitudinal channeled electron velocity

# Photon scattering by channeled electron

Crystal  $W\langle 100 \rangle$ , electron relativistic factor  $\gamma=10$ , transition  $(n=3, m=2) \rightarrow (n=0, m=0)$



Angular distribution of scattered photon in reference frame moving with longitudinal channeled electron velocity

## The cross section of coherent bremsstrahlung

$$V(\vec{r}) = \sum_{i=1}^N V_1(|\vec{r} - \vec{r}_i|), \quad V_1(r) = \frac{Ze}{r} \exp\left(-\frac{r}{R}\right). \quad \text{electrostatic potential of the crystal axis}$$

Here  $V_1$  is the potential of a single atom,  $R$  is the screening radius,  $N$  is the number of atoms in the axis,  $Z$  is atomic number.

### The spectrum of virtual photons of crystal axis

$$n(\omega)d\omega = \frac{Z^2 e^2}{\pi^2} N \times \left\{ \left[ L - B \exp\left[-\left(\frac{\hbar\omega}{\gamma\hbar c} \bar{u}\right)^2\right] \right] + \frac{2\pi}{d} \sum_{g_n} B \exp\left[-\left(\frac{\hbar\omega}{\gamma\hbar c} \bar{u}\right)^2\right] \delta(k_1 - g_n) |S|^2 \right\} \frac{d\omega}{\omega}$$

$$L = \pi \ln \left[ \frac{a\lambda^{-2}}{(\hbar\omega/\gamma\hbar c)^2 + R^{-2}} \right], \quad a \approx 1$$

$d$  - the lattice constant,  $\omega$  - the frequency of virtual photon,  $\lambda$  - Compton wave length of electron

$\bar{u}^2$  - mean-square displacement of the crystal atom from equilibrium position

$Ei(-x)$  - exponential integral function

$g_n = 2\pi n/d$  - 1D reciprocal lattice vector

$|S|$  - structure factor of a crystal axis

$\gamma$  - electron relativistic factor

**Channeling 2014**

In accordance with the virtual photons method, the cross-section of CB by channeled positron is:

$$\frac{\sigma^{CR}(\omega_r)}{d\omega_r} = \int_{\omega_{MIN}}^{\omega_{MAX}} \frac{\sigma(\omega_r, \omega)}{d\omega_r d\omega} n(\omega) d\omega$$

$\hbar\omega_r = \gamma \hbar\omega'(1 - \beta \cos \Theta')$  the Lorentz transformation  
for the photon energy (the Dopp

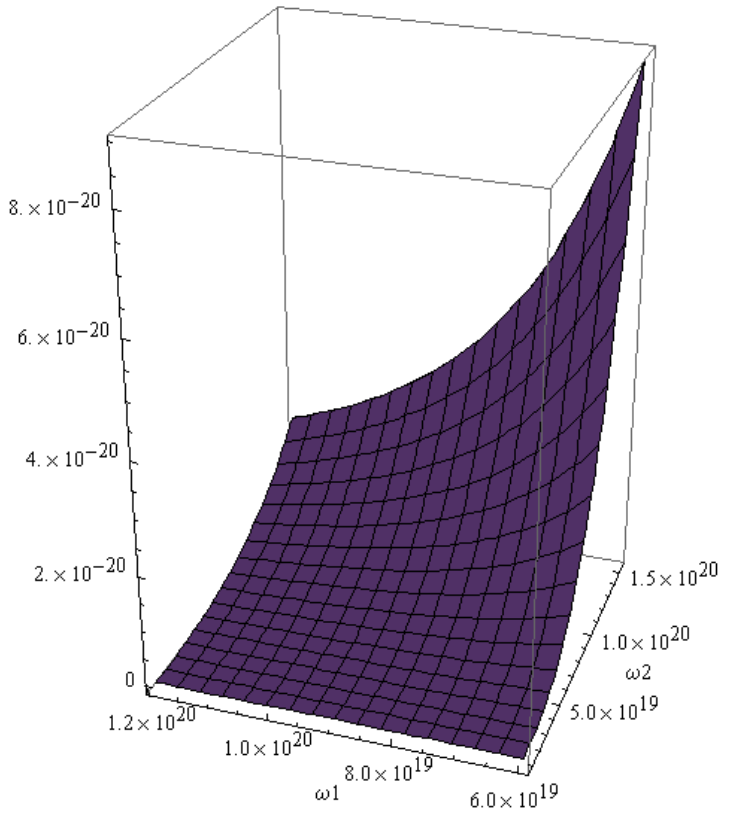
$\beta = v/c$   $v$  the longitudinal velocity of  
channeled electron in the laboratory coordinate system

The limits of integration are determined by the condition

$$\left. \begin{aligned} (\mathbf{k}_{\perp i} + \mathbf{k}_{\parallel}) &= (\mathbf{k}_{\perp f} + \mathbf{k}_{\parallel}) \\ (E_i + \hbar\omega_1) &= (E_f + \hbar\omega_2) \end{aligned} \right\}$$

$$\omega_{MIN} = \frac{\hbar\omega + \gamma(1 + \beta)(\epsilon_{\perp f} - \epsilon_{\perp i})}{\gamma(1 + \beta)\hbar}$$

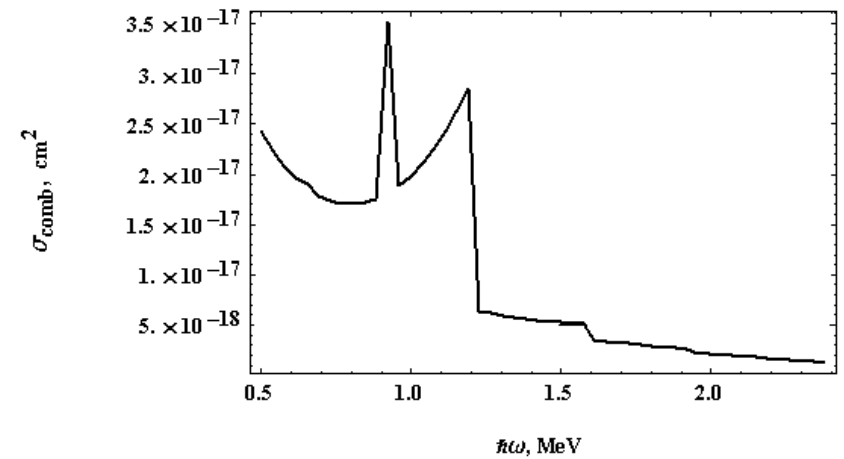
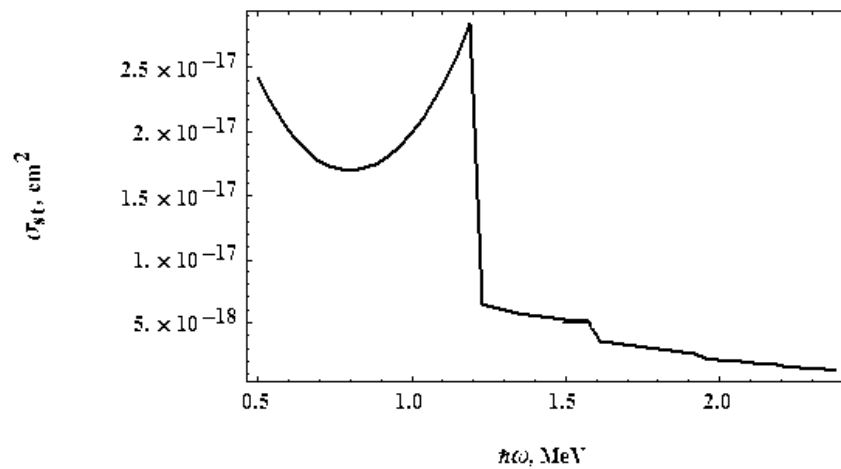
$$\omega_{MAX} = \frac{\hbar\omega + \gamma(1 - \beta)(\epsilon_{\perp f} - \epsilon_{\perp i})}{\gamma(1 - \beta)\hbar}$$





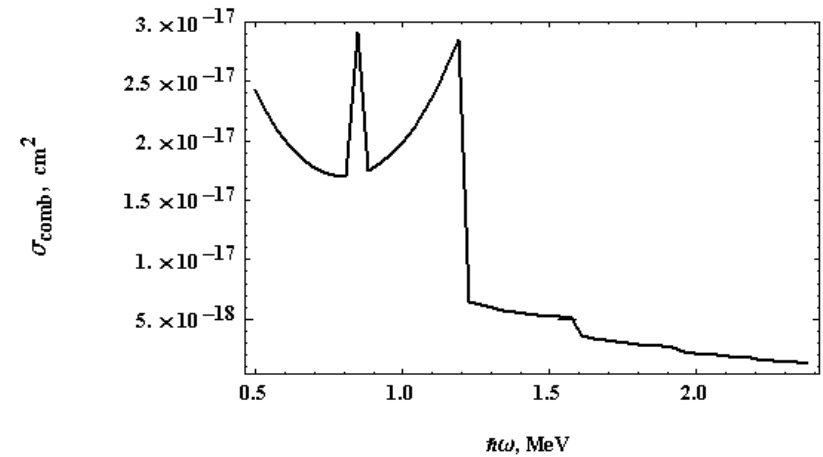
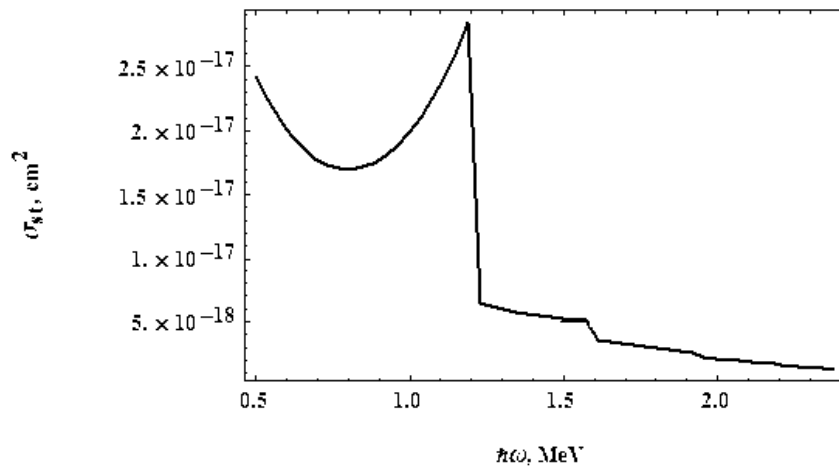
## Result of calculation

Crystal W<100>, electron relativistic factor  $\gamma=10$ , transition  $(n=2, m=1) \rightarrow (n=0, m=0)$



## Result of calculation

Crystal W<100>, electron relativistic factor  $\gamma=10$ , transition  $(n=3, m=1) \rightarrow (n=0, m=0)$



We obtain that combined effect result in appearance of additional sharp peak in coherent bremsstrahlung cross-section. This result is not agree with the experiment. The reason is as follows:

1. It was used very simple approximation for continuous crystal potential.
2. It was used one string approximation.
3. It is necessary to take into account the resolution of detector.

**Tank you for your attention**