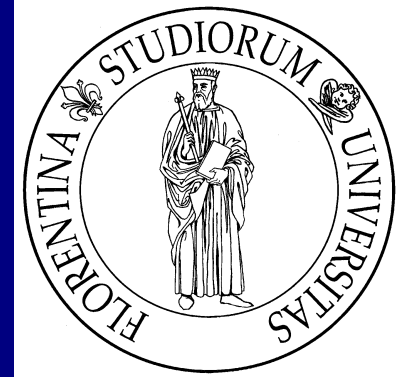


# Quark-Gluon Plasma and Relativistic Heavy Ion Collisions in the LCH era



F. Becattini (University of Florence  
and INFN)

## OUTLINE

- QCD thermodynamics
- Hadronic thermometers
- The hydrodynamical model
- Outlook

# Strong interaction thermodynamics

- Hagedorn (1965): density of hadronic states  $dN/dm$  grows exponentially

$$\rho(m) = C m^\alpha e^{m/T_0}$$

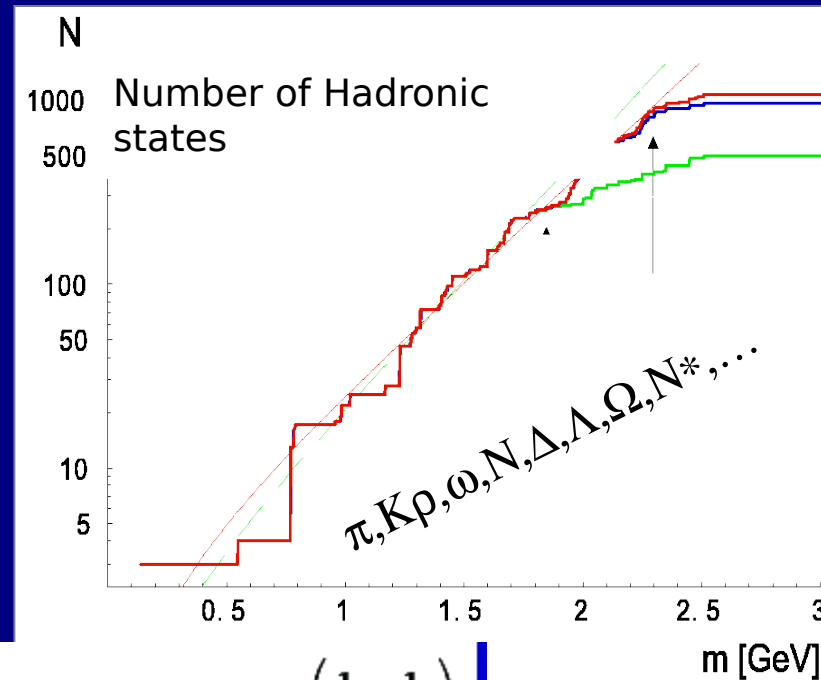
$T_0$  estimated to be 160 MeV

$T_0$  is called Hagedorn *limiting temperature for an hadronic system*

Partition function for a gas of hadrons, with  $m \gg T$

$$\log Z(T, V) \propto \int_{m_0}^{\infty} dm m^{3/2} \rho(m) e^{-\frac{m}{T}} \propto \int_{m_0}^{\infty} dm m^{\alpha+3/2} e^{-m \left( \frac{1}{T} - \frac{1}{T_0} \right)}$$

Integral diverges for  $T \rightarrow T_0$ :  
hadronic matter cannot have a  $T > T_0$

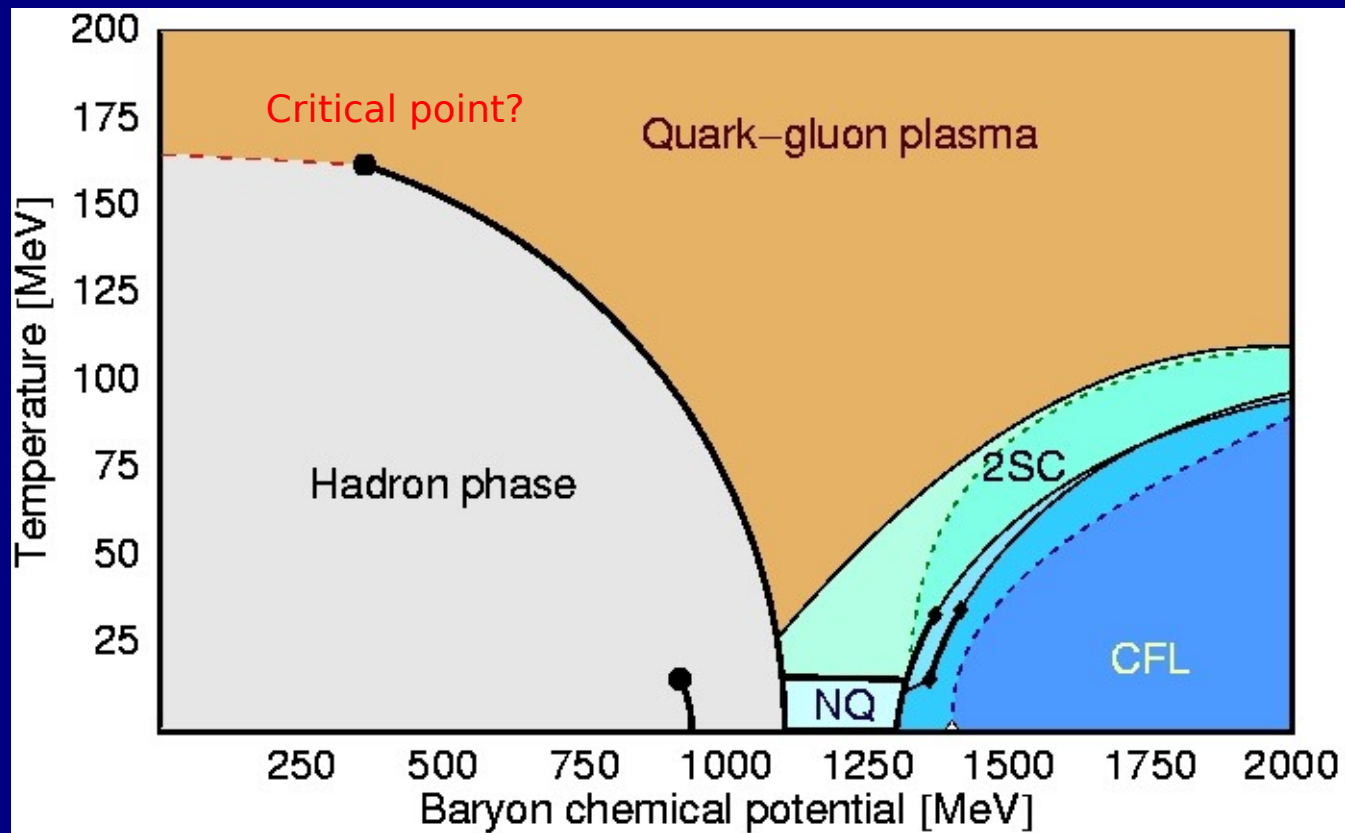


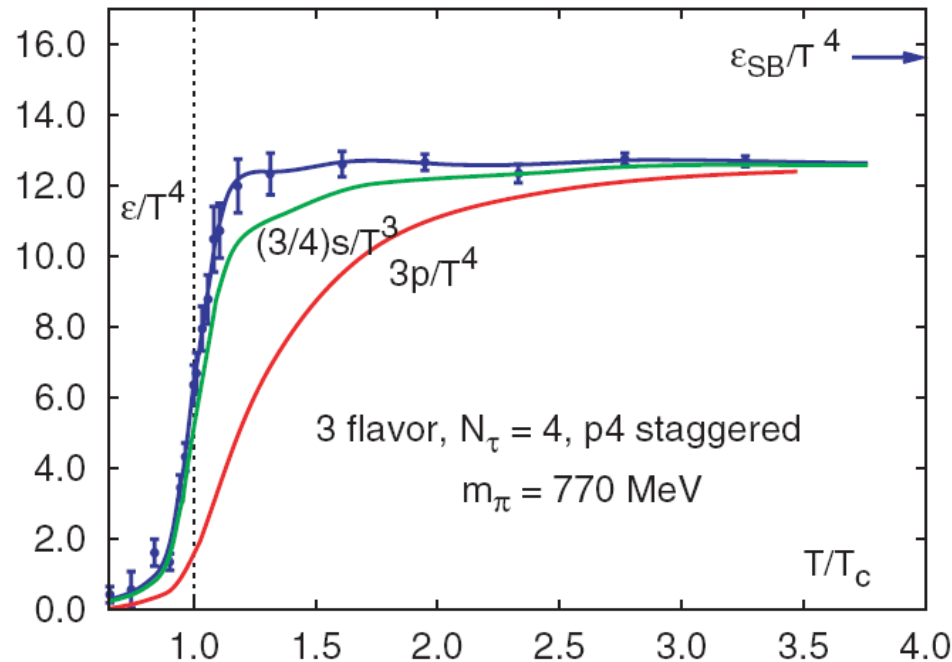
Cabibbo-Parisi (1975) – one year after Gross –Wilczek paper:

Divergency of the partition function has to be associated with  
**a phase transition of hadronic matter to quark-gluon matter**

+ asymptotic freedom at large  $T \rightarrow$  weakly quark gluon gas

# QCD phase diagram



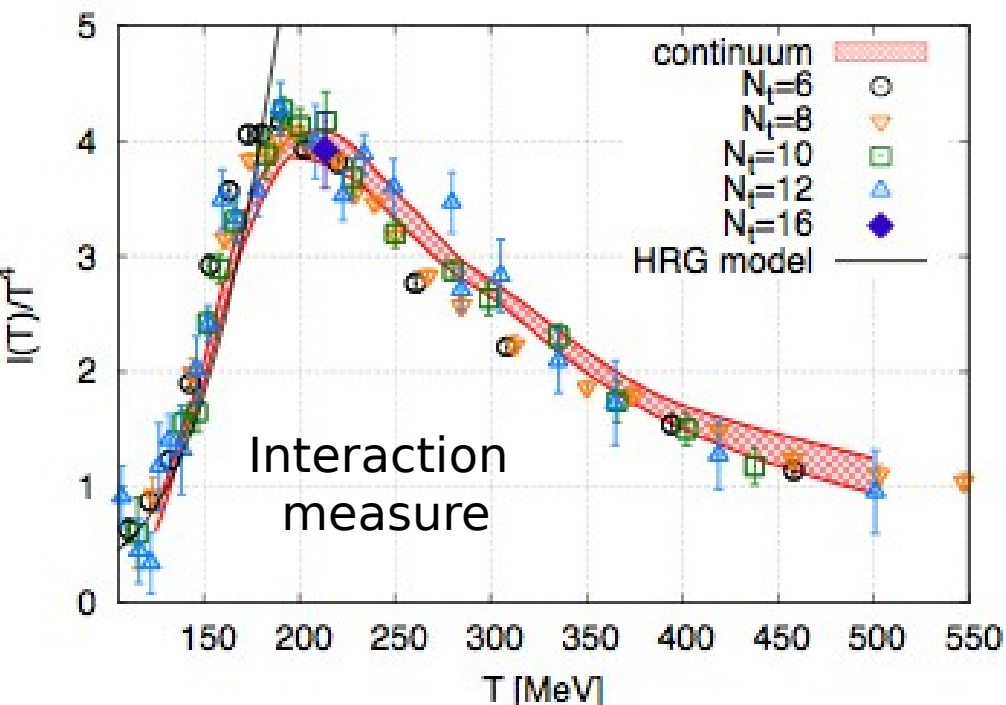


Reference: a gas of non-interacting massless Particle (Stefan-Boltzmann law)

$$\frac{\mathcal{E}_{SB}}{T^4} = \frac{\pi^2}{30} \left[ \frac{7}{8} d_{q+\bar{q}} + d_g \right]$$

$$\mathcal{E}_c \approx 0.7 \text{ GeV} / \text{fm}^3$$

$$T_c \cong 160 \text{ MeV}$$



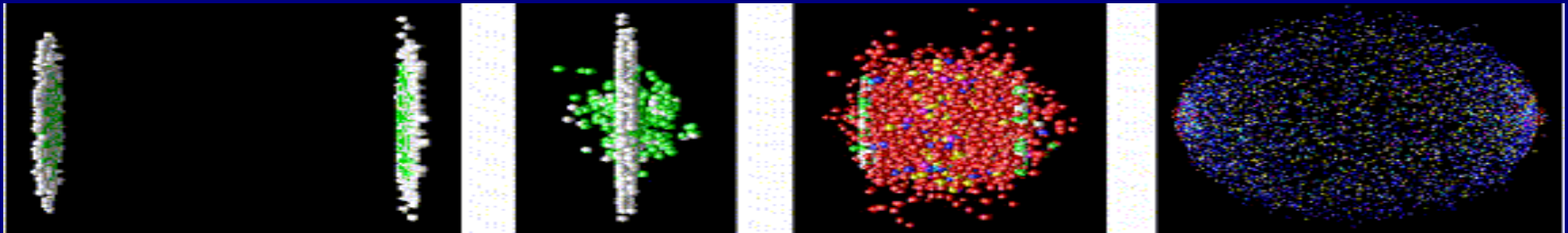
No interaction means (for a massless gas)

$$I = T^\mu_\mu = \rho - 3p = 0$$

but in fact  $I = O(\rho)$  !

$T > T_c$  ceases to be a hadron gas  
 but it is not a gas of weakly interacting  
 quarks and gluons up to very high  $T$

How to produce a matter  
with  $\rho \gg 1 \text{ GeV/fm}^3$   
lasting for  $t > 1 \text{ fm/c}$   
in a volume much larger than a hadron?



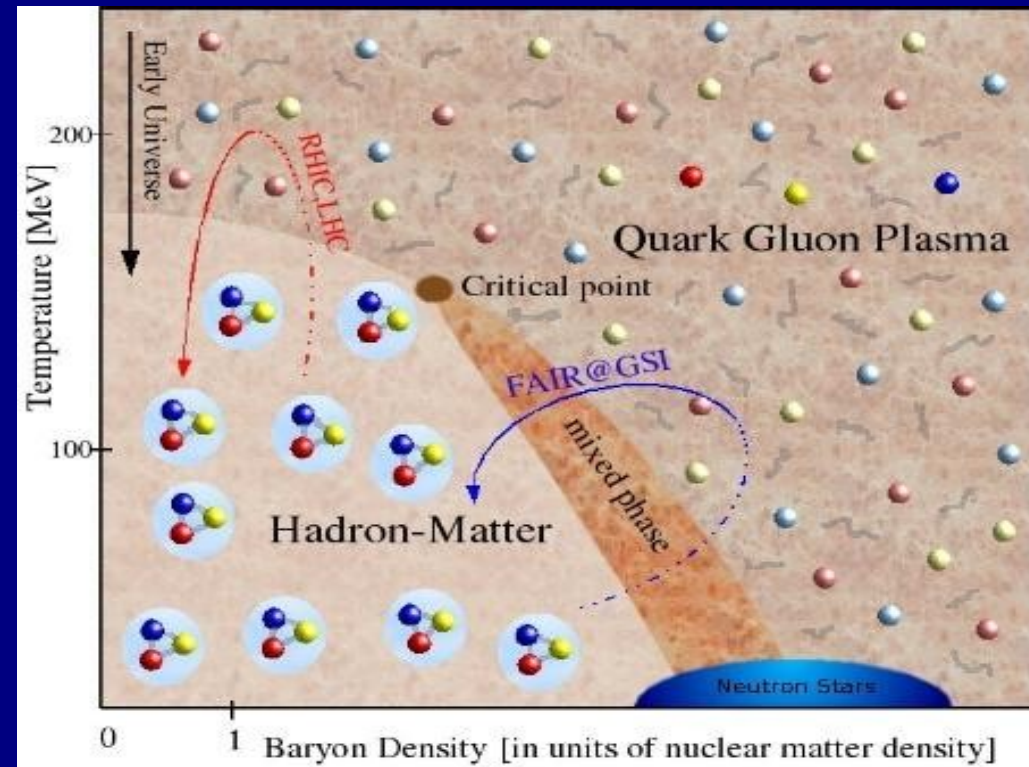
Accelerator	Lab	$\sqrt{s}_{\text{NN}}$	Nuclei
SPS (90's)	CERN	6-18	Pb-Pb
RHIC (00-..)	RHIC	7.7-200	Au-Au
LHC (09-..)	CERN	2750	Pb-Pb

# Probing the Quark Gluon Plasma

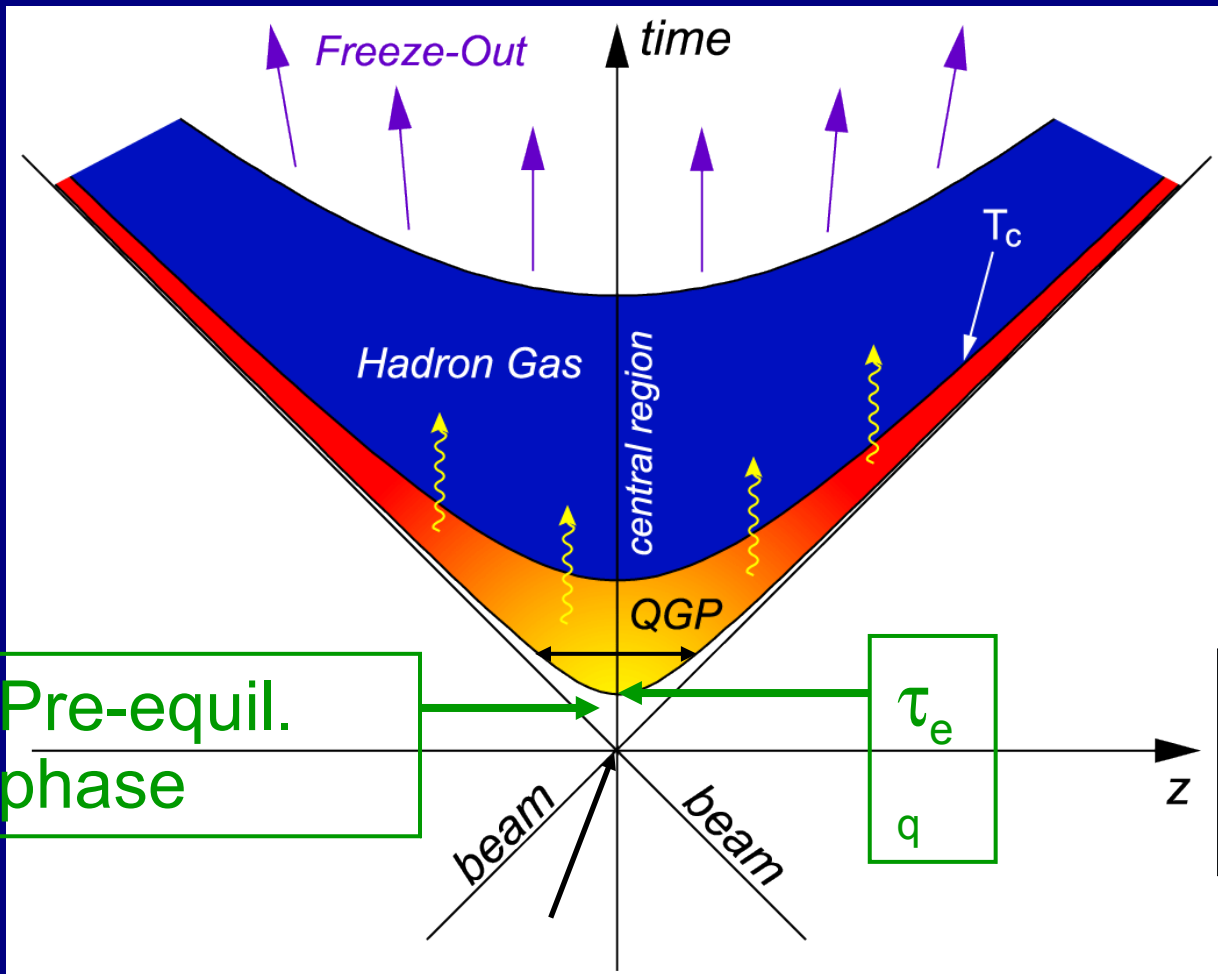
The plasma is a transient and rapidly decays. This situation is dramatically different from the idealized (steady) situation of lattice QCD calculations.

Several possible probes at our disposal, that can be clustered in three groups

- Hadron radiation
  - Electromagnetic radiation
  - Hard probes: heavy quarks and quarkonia, jets, hard photons etc.
- Common feature: early production, “calculable” in perturbative QCD, easily comparable to pp and pA



# Relativistic hydrodynamical model



$$\begin{cases} \partial_{\mu} T^{\mu\nu}(x) = 0 \\ \partial_{\mu} j_B^{\mu}(x) = 0 \end{cases}$$

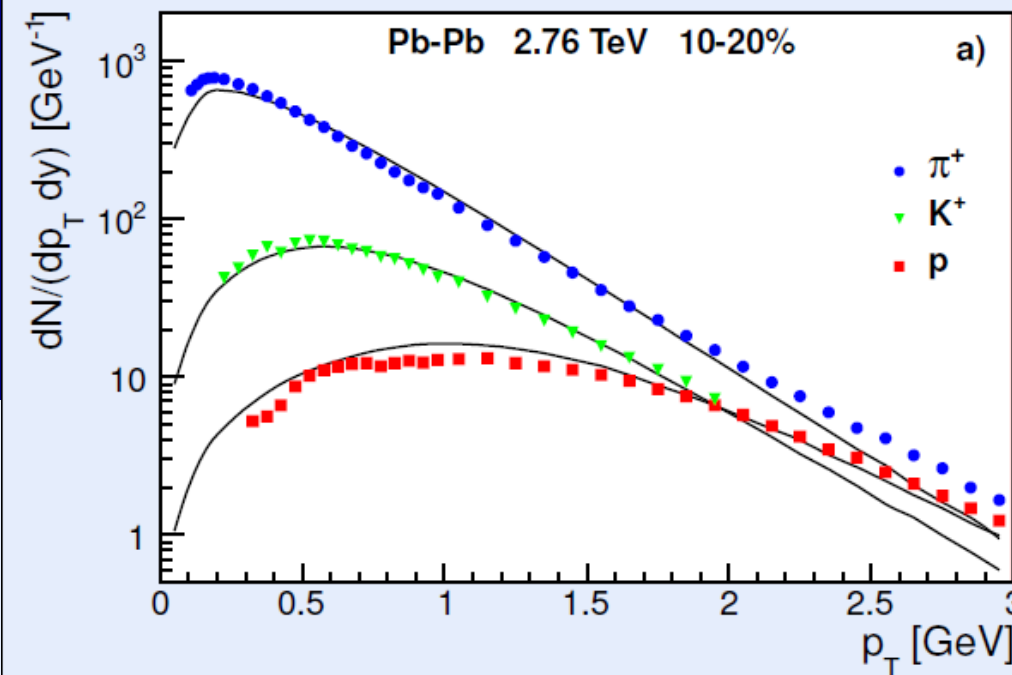
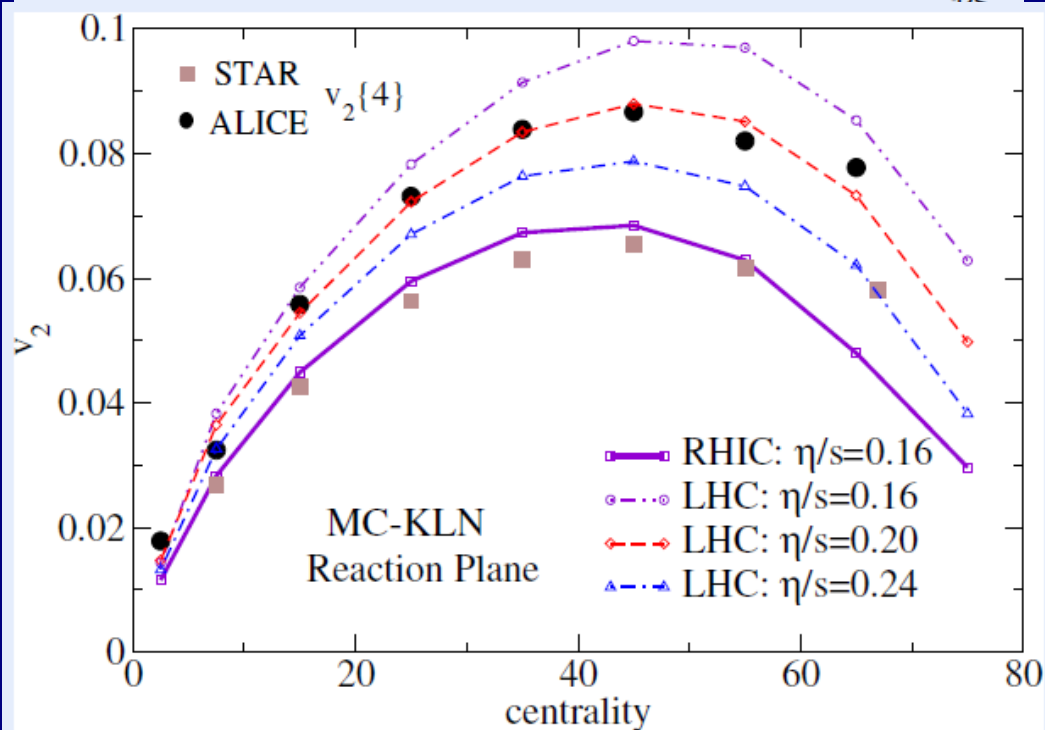
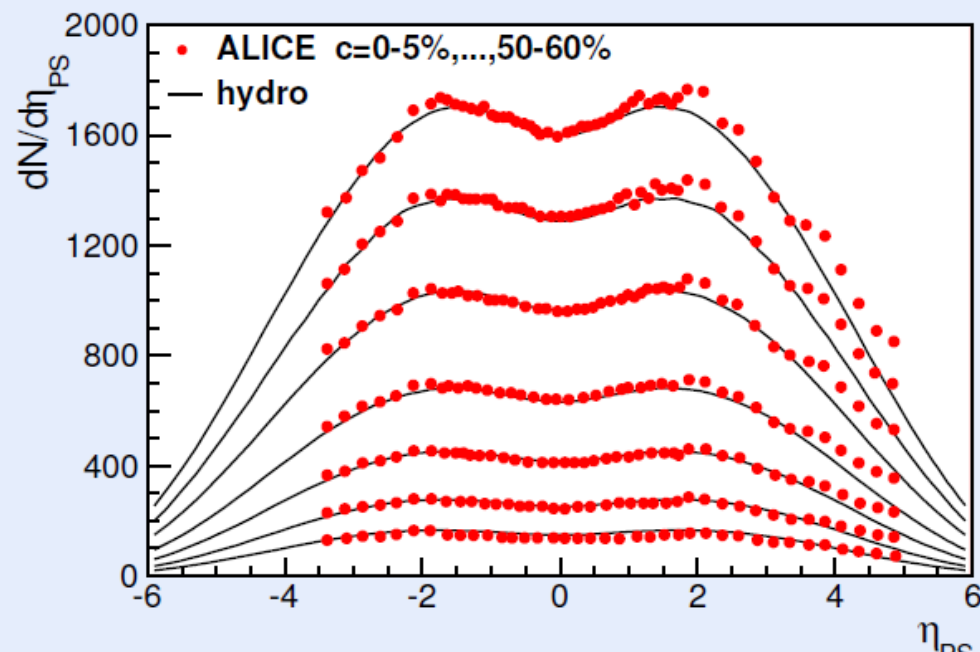
Generate particles with:

$$\varepsilon \frac{dn}{d^3p} = \int d\Sigma_{\mu} p^{\mu} \frac{1}{e^{\beta \cdot p} \pm 1}$$

Hydrodynamics requires *local thermodynamical equilibrium*. This implies a formidable reduction of the degrees of freedom in the dynamical problem: from the full problem of interacting quantum fields to the evolution of few functions:  $u(x)$ ,  $T(x)$ ,  $\mu(x)$



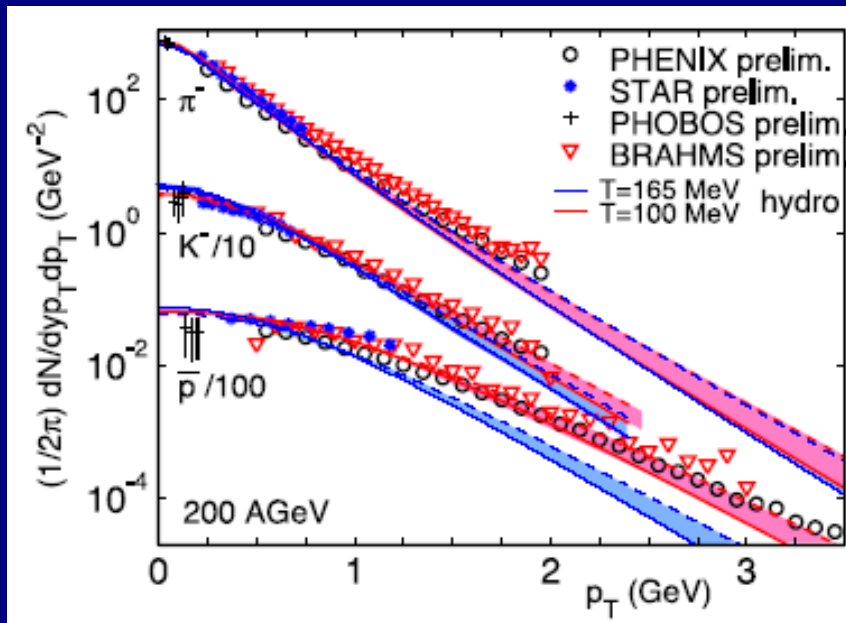
# Hydrodynamical model is very successful





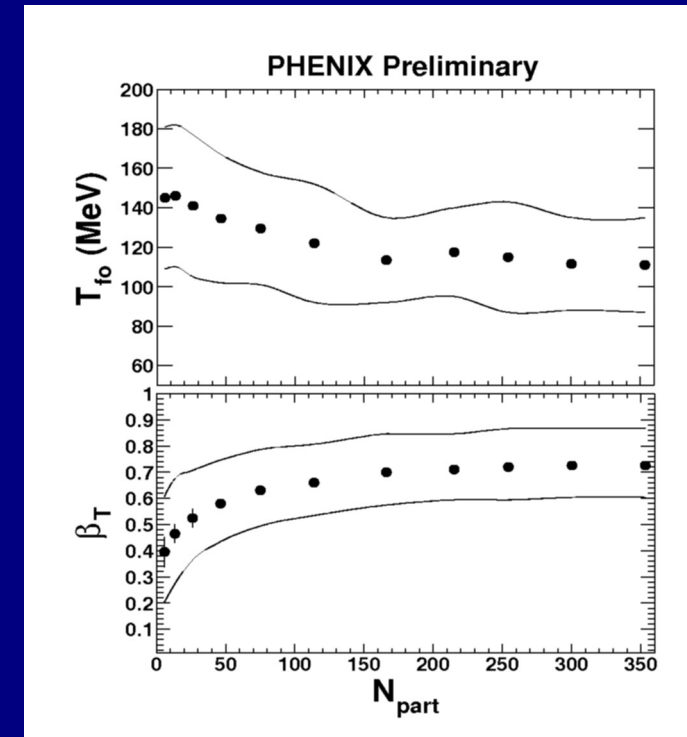
# “Measuring” the initial temperature of the plasma with hydrodynamical model

The idea is to determine the initial conditions  
from the observed final spectra (in the transverse plane)



$$\frac{dN}{dp_T} \approx e^{-m_T/T_{eff}}$$

$$T_{eff} \approx T_{dec} + \frac{1}{2}m\langle u_T^2 \rangle$$

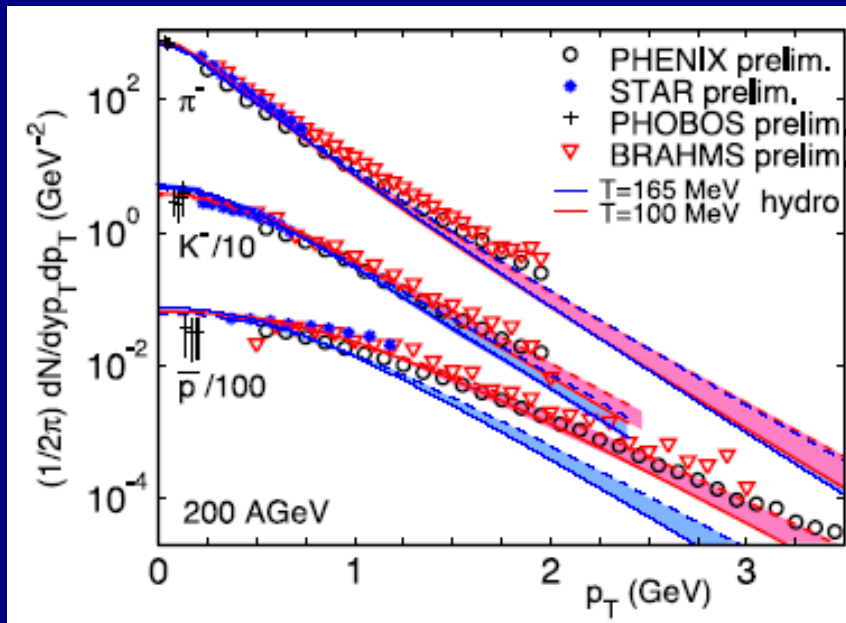


$\sqrt{s_{NN}}$ (GeV)	SPS	RHIC 1	RHIC 2
$s_{eq}$ (fm <sup>-3</sup> )	43	95	110
$T_{eq}$ (MeV)	257	340	360
$\tau_{eq}$ (fm/c)	0.8	0.6	0.6

← Fitted parameters (U Heinz et al.).  
The initial T is correlated  
to the initial equilibration time.

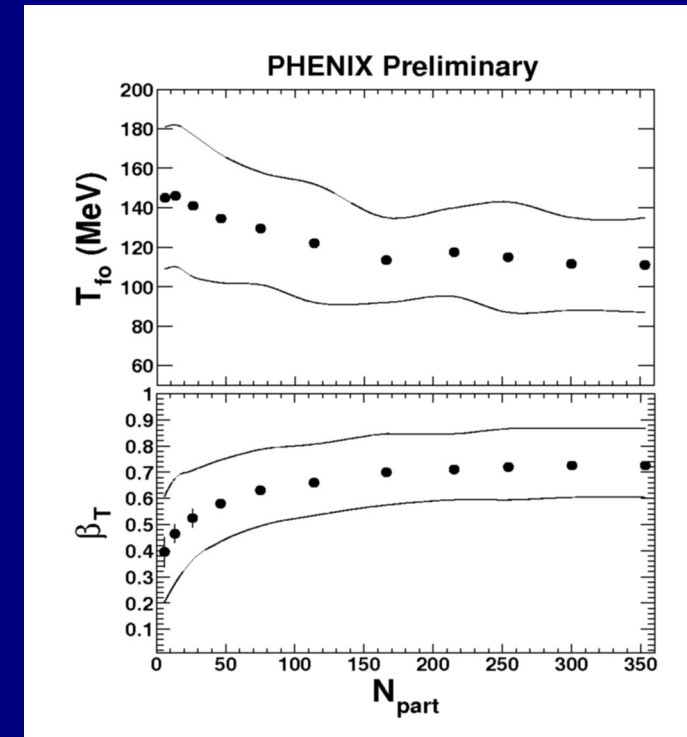
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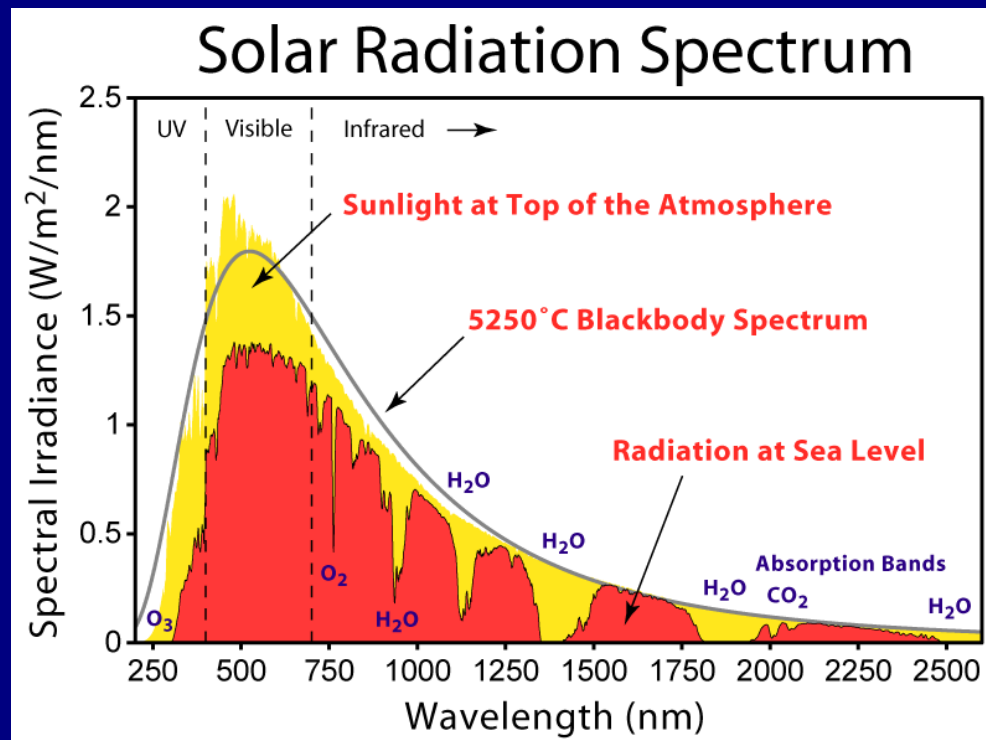


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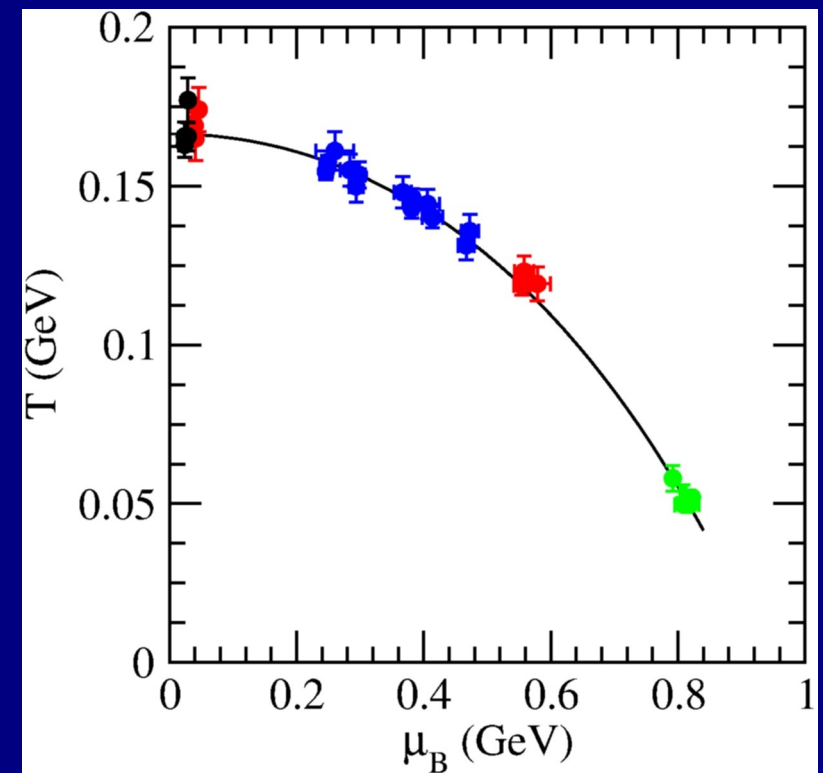
← Fitted parameters (U Heinz et al.).  
The initial T is correlated  
to the initial equilibration time.

With hadronic multiplicities one can determine the thermodynamical state at the stage when hadrons cease inelastic interactions and decouple (chemical freeze-out)

$$\langle n_j \rangle = \frac{(2S_j + 1)V}{2\pi^2} m_j^2 T \gamma_S^{n_{sj}} K_2(m/T) e^{\sum_i \mu_i q_j^i / T}$$



J. Cleymans et al. Phys.Rev. C73 (2006) 034905

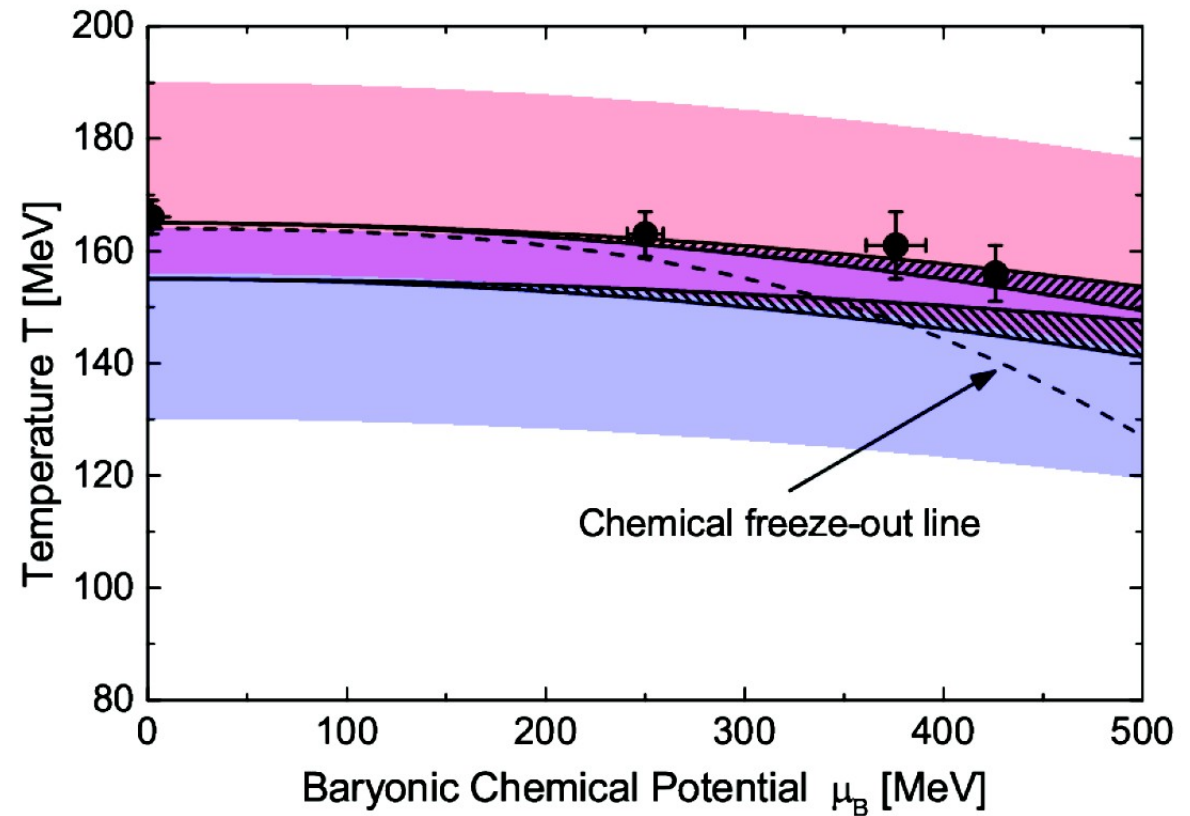


*The temperature at the chemical freeze-out at RHIC is that of a hadronic black-body and it is the largest ever measured on Earth ( $\sim 2 \cdot 10^{12}$  K)*

# Reconstruction of the hadronization point and comparison with lattice QCD

F.B., M. Bleicher, J. Steinheimer, R. Stock, Phys. Rev. Lett. 111, 082302 (2013)

Rescattering corrections imply an upward shift of the c.f.o. temperature



Lattice calculations from

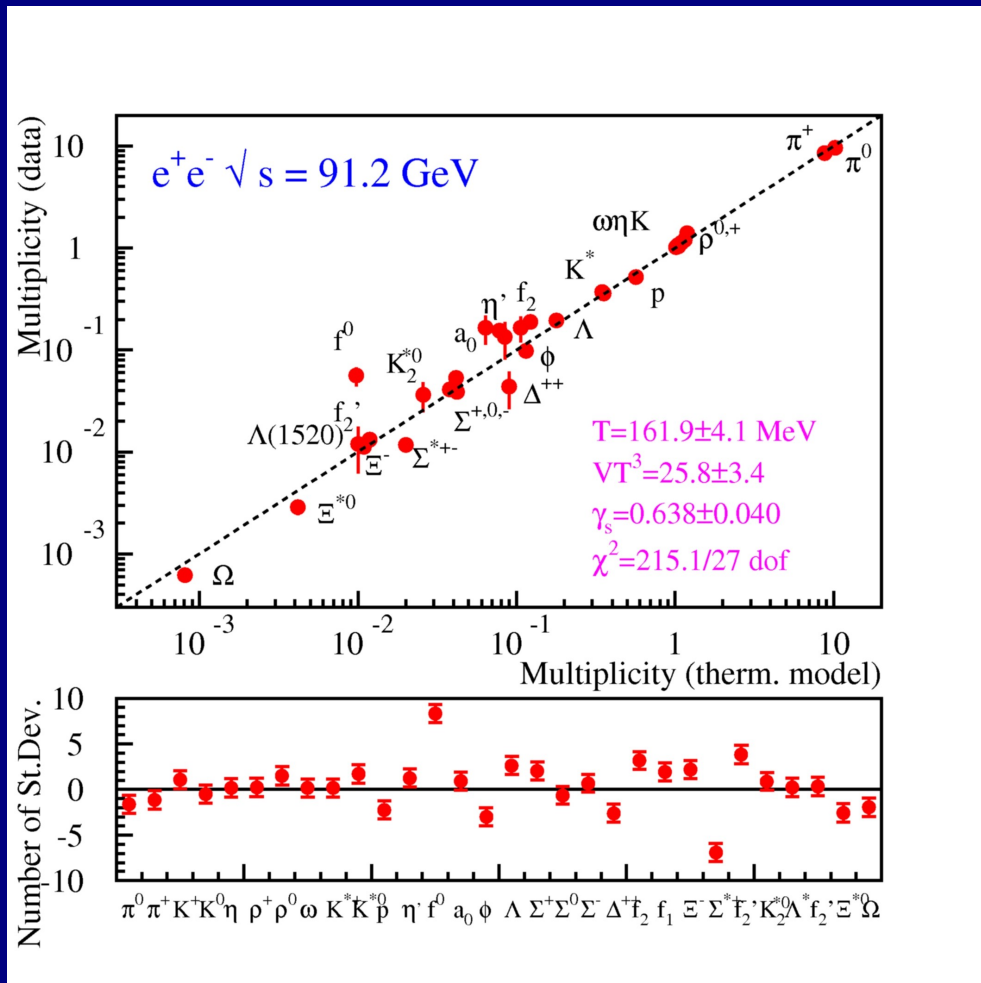
F. Karsch, J. Phys. G 38, 124098 (2011); S. Borsanyi et al., ibidem 124101

G. Endrodi, Z. Fodor, S. D. Katz and K. K. Szabo, JHEP 1104, 001 (2011)

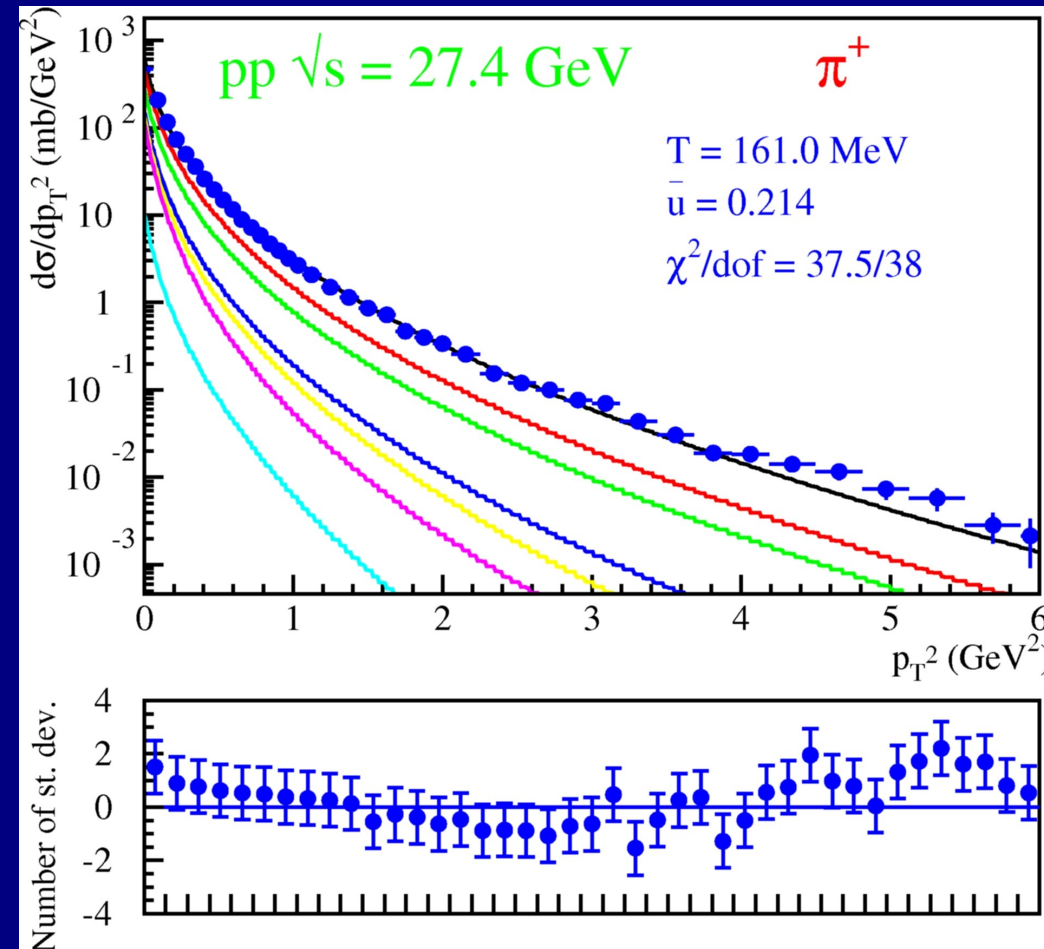
P. Cea, L. Cosmai, M. D'Elia, A. Papa, F. Sanfilippo, Phys.Rev. D85 (2012) 094512

Thermal distributions are ubiquitous in relativistic heavy ion collisions and in strong interactions (in the soft regime) in general.  
It seems to be a feature of QCD in the non-perturbative regime. Why?

F. B., P. Castorina, J. Manninen, H. Satz, Eur. Phys. J. C 56 (2008) 493



F. B., G. Passaleva, Eur. Phys. J. C 23 (2002) 551





# Quark Gluon Plasma as a quasi-ideal fluid

Contacts: [Karen McNulty Walsh](#), (631) 344-8350 or [Mona S. Rowe](#), (631) 344-5056

 [Print-friendly](#)  [E-mail Article](#)

## RHIC Scientists Serve Up "Perfect" Liquid

**New state of matter more remarkable than predicted -- raising many new questions**

April 18, 2005

TAMPA, FL -- The four detector groups conducting research at the [Relativistic Heavy Ion Collider](#) (RHIC) -- a giant atom "smasher" located at the U.S. Department of Energy's Brookhaven National Laboratory -- say they've created a new state of hot, dense matter out of the quarks and gluons that are the basic particles of atomic nuclei, but it is a state quite different and even more remarkable than had been predicted. In [peer-reviewed papers](#) summarizing the first three years of RHIC findings, the scientists say that instead of behaving like a gas of free quarks and gluons, as was expected, the matter created in RHIC's heavy ion collisions appears to be more like a *liquid*.

"Once again, the physics research sponsored by the Department of Energy is producing historic results," said Secretary of Energy Samuel Bodman, a trained chemical engineer. "The DOE is the principal federal funder of basic research in the physical sciences, including nuclear and high-energy physics. With today's announcement we see that investment paying off."

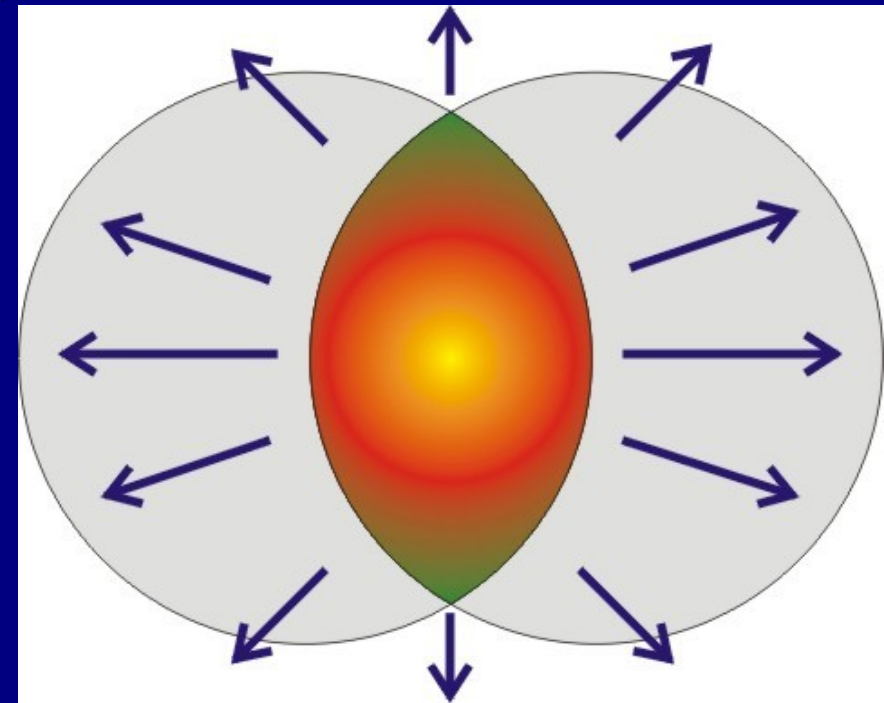
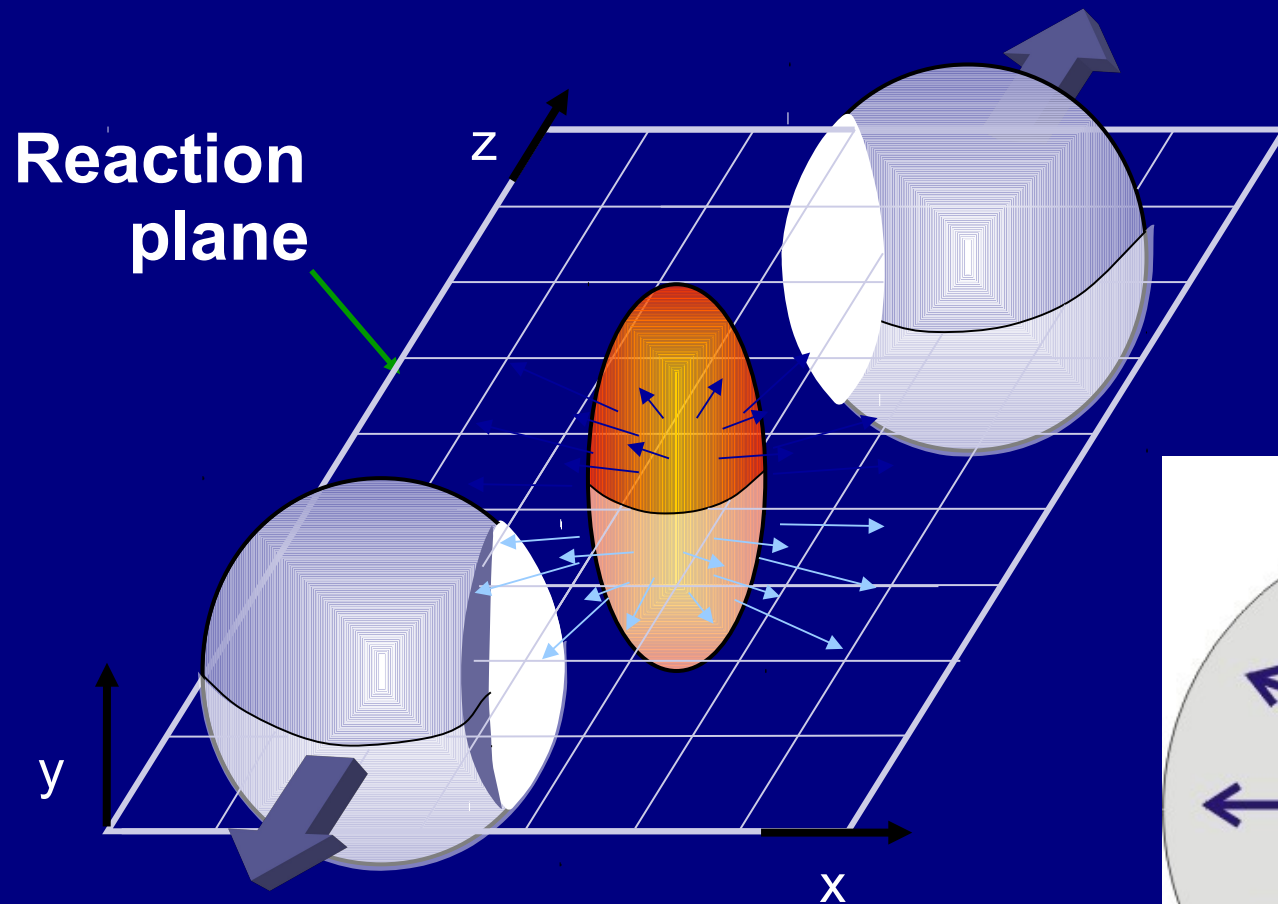
"The truly stunning finding at RHIC that the new state of matter created in the collisions of gold ions is more like a liquid than a gas gives us a profound insight into the earliest moments of the universe," said Dr. Raymond L. Orbach, Director of the DOE Office of Science.

Also of great interest to many following progress at RHIC is the emerging connection between the collider's results and calculations using the methods of string theory, an approach that attempts to explain fundamental properties of the universe using 10 dimensions instead of the usual three spatial dimensions plus time.



Secretary of Energy  
Samuel Bodman

# Elliptic flow in peripheral collisions



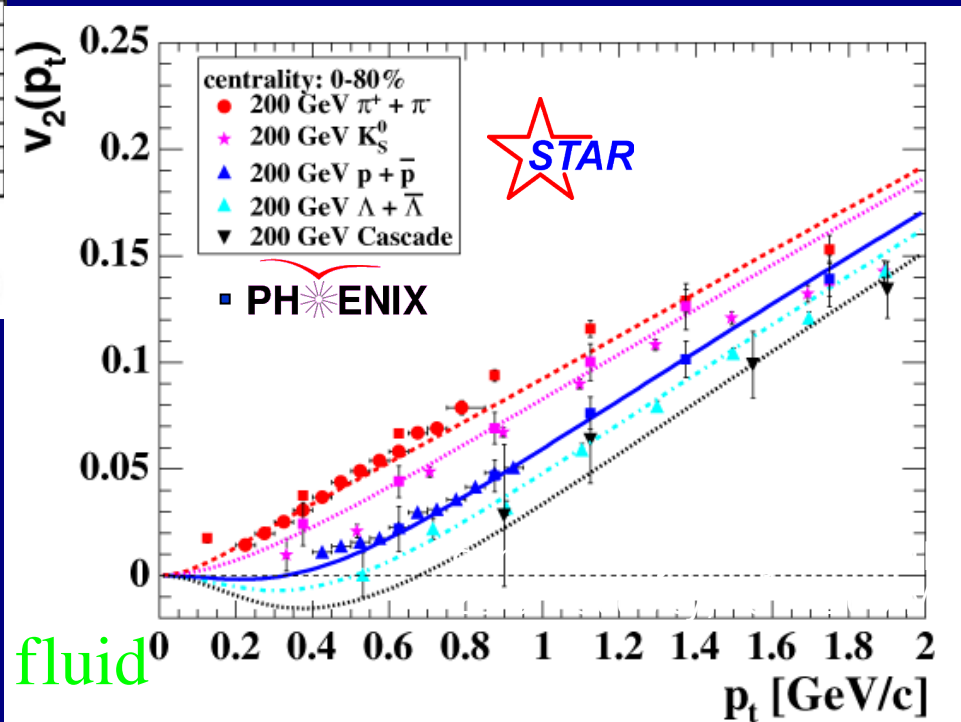
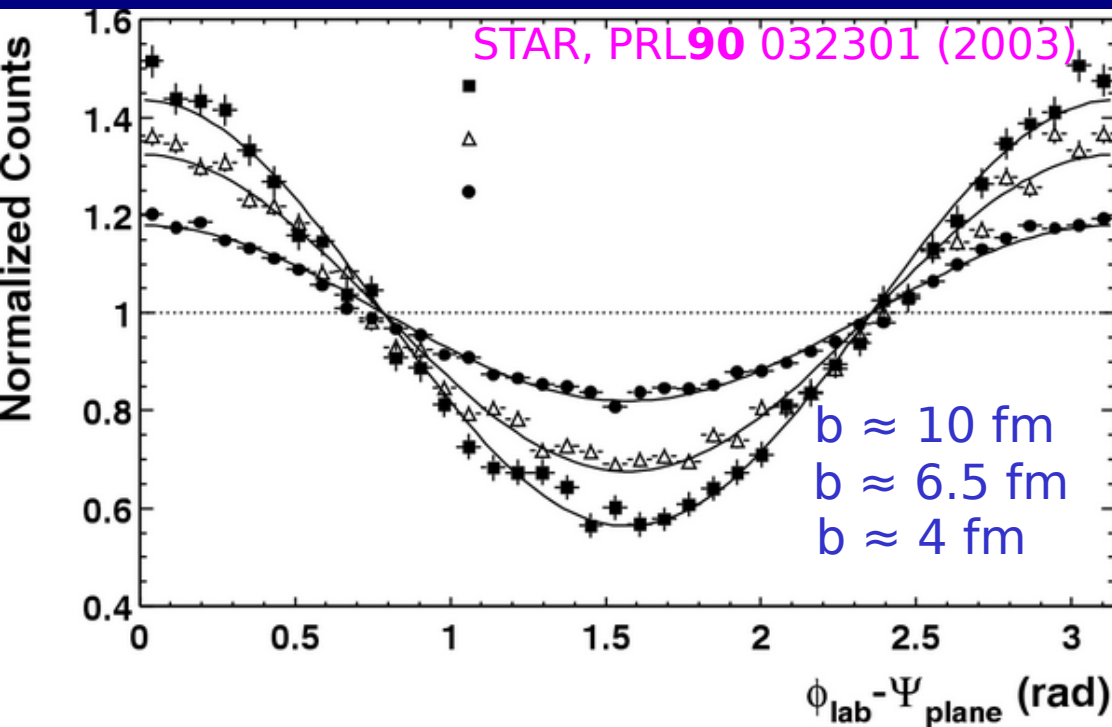
Anisotropic pressure gradient: if there is collective flow, particles get a larger momentum on the reaction plane!

$$\frac{dN_i}{dy p_{\perp} dp_{\perp} d\varphi_p}(b) = \frac{1}{2\pi} \frac{dN_i}{dy p_{\perp} dp_{\perp}}(b) \left( 1 + 2 v_2^i(p_{\perp}, b) \cos(2\varphi_p) + \dots \right).$$



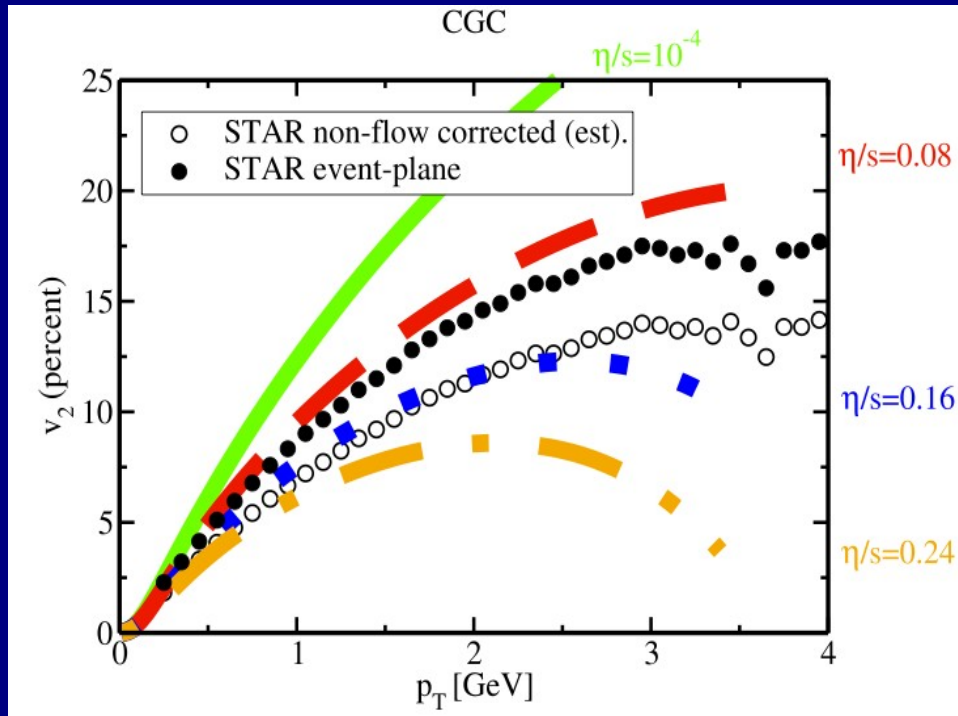
# Elliptic flow coefficient $v_2$

$$\frac{dN_i}{dy p_\perp dp_\perp d\varphi_p}(b) = \frac{1}{2\pi} \frac{dN_i}{dy p_\perp dp_\perp}(b) \left( 1 + 2 v_2^i(p_\perp, b) \cos(2\varphi_p) + \dots \right).$$



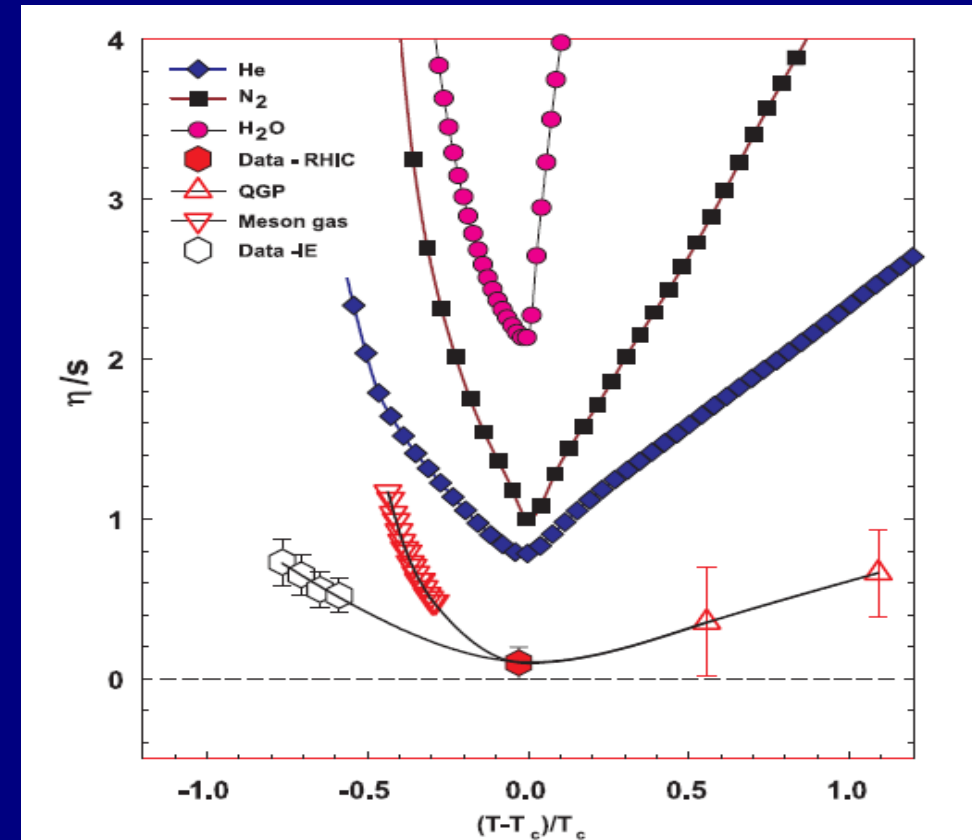
$v_2$  in good agreement with quasi-ideal fluid

# Elliptic flow is sensitive to the viscosity of the QGP



P. Romatschke

Very low values of viscosity, or  
better:  $\eta/s$  ratio



Summary of viscosity “measurements” at RHIC and LHC (U. Heinz, RANP 2013)

$$(\eta/s)_{\text{QGP}}(T_c < T < 2T_c) = \frac{2}{4\pi} \pm 50\%$$

# What does low viscosity mean?

From kinetic theory:

$$\eta = \frac{1}{3}\rho v_T \lambda = \frac{1}{3}m n v_T \lambda = \frac{1}{3}n p_T \lambda$$

In relativistic fluid:

$$n \sim s \qquad \frac{\eta}{s} \sim p_T \lambda$$

Low values of  $\eta/s$  imply that the thermal wavelength is comparable to the mean free path: a particulate description of this fluid is inconsistent

Gas at STP:

$$n = 2.7 \times 10^{25} m^{-3} \qquad \sigma \approx 10^{-19} m^2$$
$$\rightarrow \lambda \approx 400 nm \gg d = (1/n)^{1/3} = 3 nm \gg \lambda_T \approx 5 pm$$

Water:

$$n = 3.4 \times 10^{28} m^{-3} \qquad \sigma \approx 10^{-19} m^2$$
$$\rightarrow \lambda \approx 0.3 nm \approx d = (1/n)^{1/3} = 0.31 nm \gg \lambda_T \approx 5 pm$$

QGP is so strongly interacting near  $T_c$  that a particle cannot travel a wavelength without colliding!

# Beyond Quasiparticles

- QGP at RHIC & LHC, unitary Fermi “gas”, gauge theory plasmas with holographic descriptions are all strongly coupled fluids with no apparent quasiparticles.
- In QGP, with  $\eta/s$  as small as it is, there can be no ‘transport peak’, meaning no self-consistent description in terms of quark- and gluon-quasiparticles. [Q.p. description self consistent if  $\tau_{qp} \sim (5\eta/s)(1/T) \gg 1/T$ .]
- Other “fluids” with no quasiparticle description include: the “strange metals” (including high- $T_c$  superconductors above  $T_c$ ); quantum spin liquids; matter at quantum critical points;...

K. Rajagopal

QGP near  $T_c$  is not a kinetic system, it is a system of strongly interacting quantum fields, still it is a fluid.

Microscopic scale  $\ll$  macroscopic size:  $\lambda \ll L$ .

# Hydrodynamics without kinetic theory

$$T^{\mu\nu}(x) = \text{tr}(\hat{\rho} \hat{T}^{\mu\nu}(x))$$

$$\partial_\mu T^{\mu\nu} = 0$$

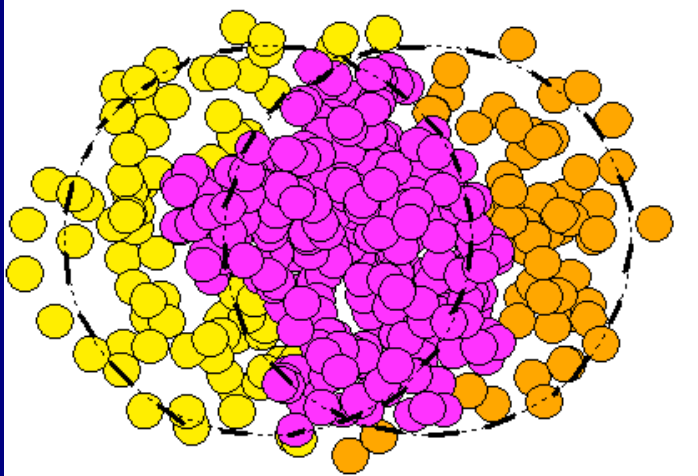
Zubarev non-equilibrium stationary density operator (for close-to-local equilibrium evolution):

$$\hat{\rho} = \frac{1}{Z} \exp \left[ - \lim_{\varepsilon \rightarrow 0} \varepsilon \int_{-\infty}^{t'} dt e^{\varepsilon(t-t')} \int d^3x (\hat{T}^{0,\nu}(x) \beta_\nu(x) - j^0(x) \xi(x)) \right]$$

$$\beta = \frac{1}{T} u \quad \xi = \mu/T$$

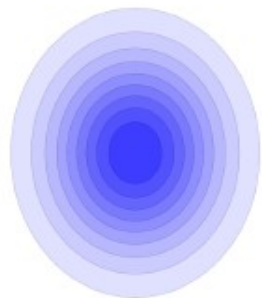
It contains a microscopic length, which is not properly a mean free path, rather a correlation distance for quantum fields, particularly of stress-energy tensor components.

# Recent developments from LHC experiments: from averages to event-by-event hydrodynamics

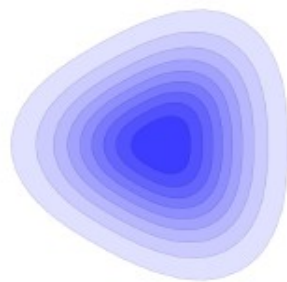


Higher harmonics in the azimuthal spectrum of  
Particles in the transverse plane

When including fluctuations, all moments appear:



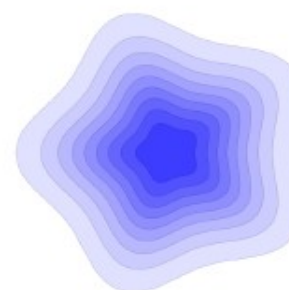
$n = 2$



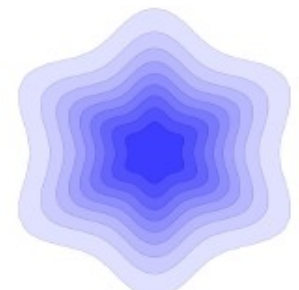
$n = 3$



$n = 4$



$n = 5$



$n = 6$

also  $v_1$  and  $n > 6$

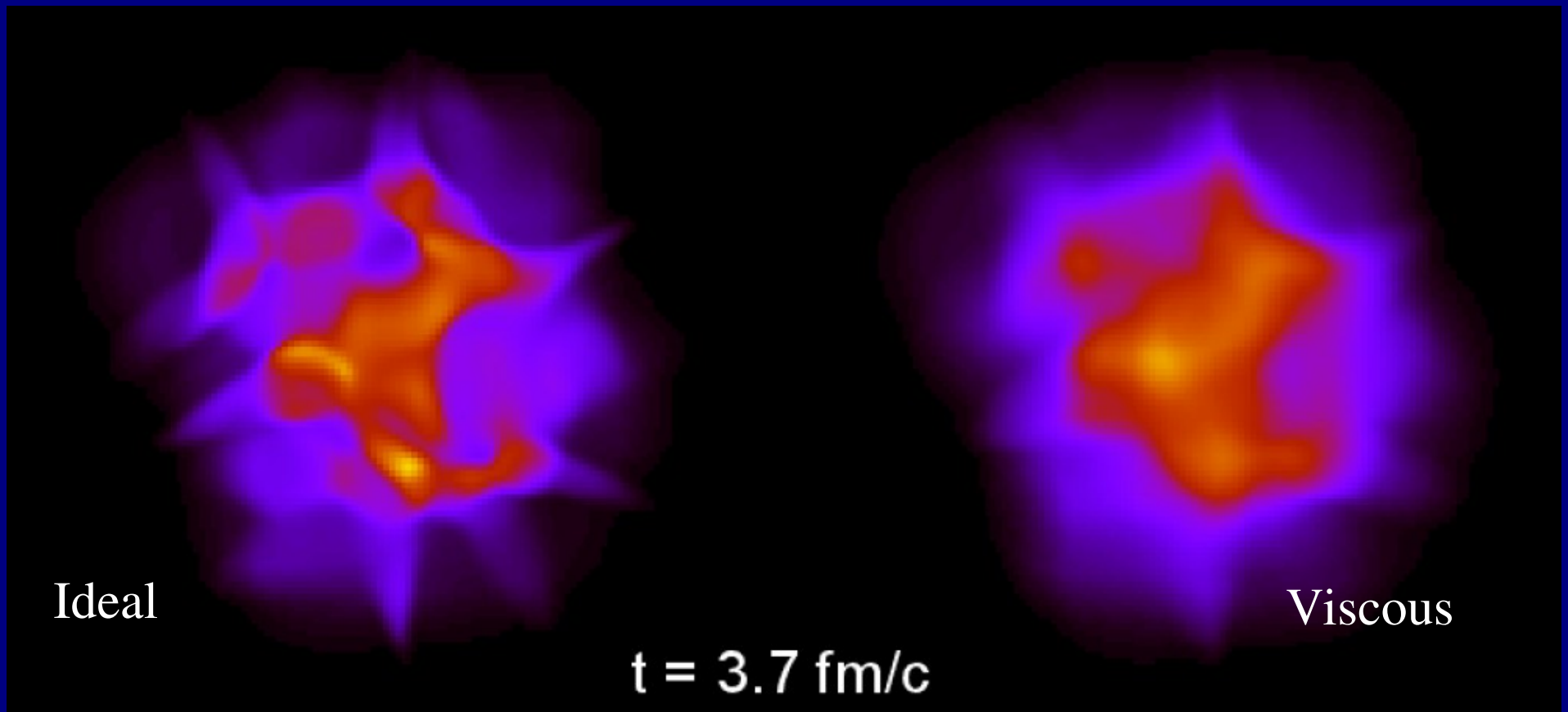
Compute  $v_n = \langle \cos[n(\phi - \psi_n)] \rangle$

# Viscosity smoothens fluctuations and affect more higher harmonics

$$(\eta/s)_{\text{QGP}}(T_c < T < 2T_c) = \frac{2}{4\pi} \pm 50\%$$

Numerical codes are getting more important and more performing.

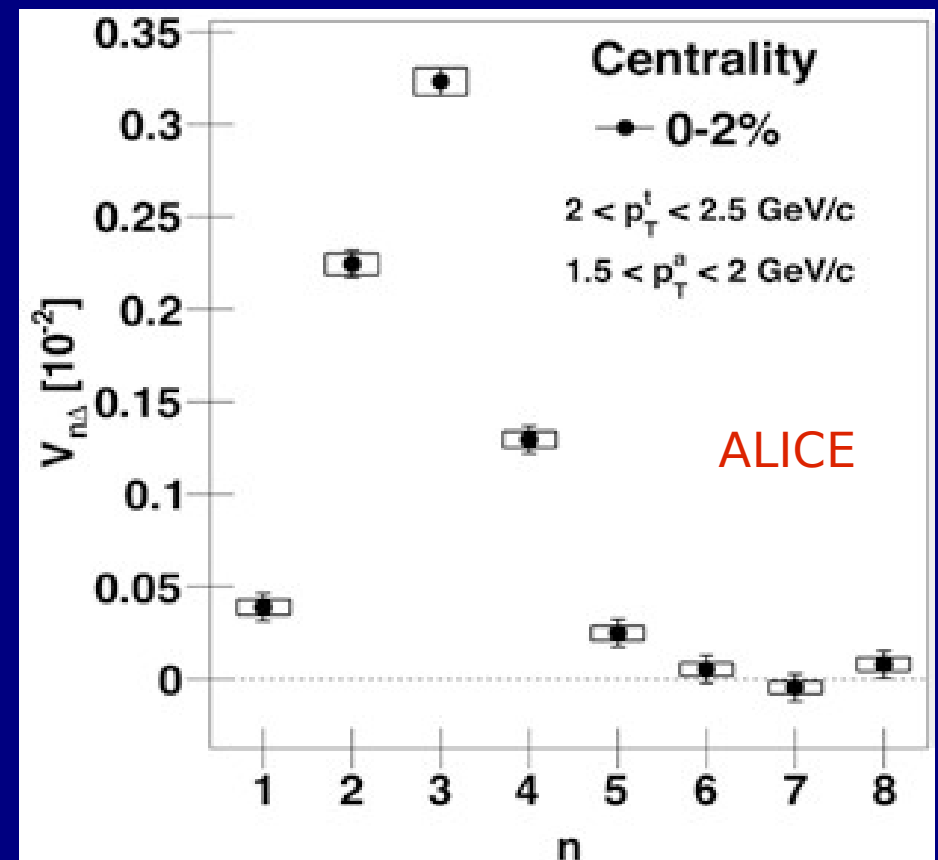
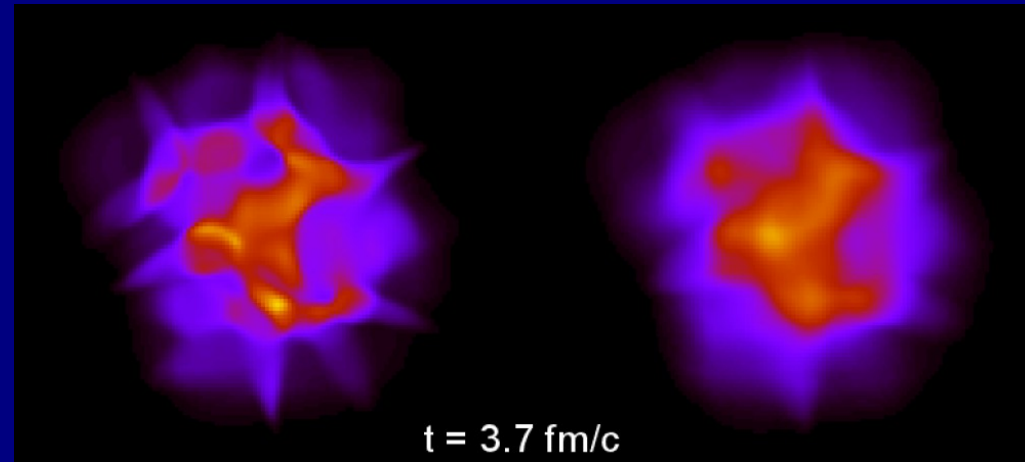
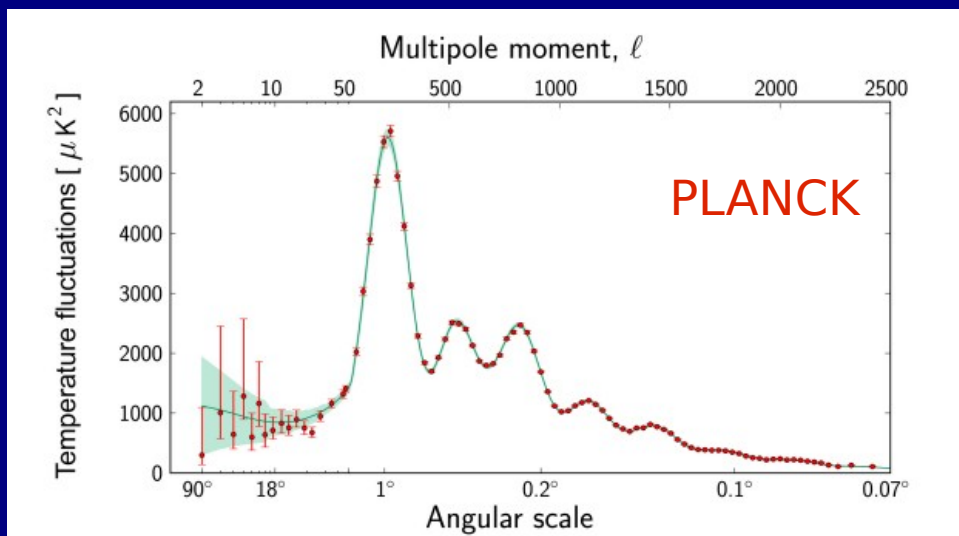
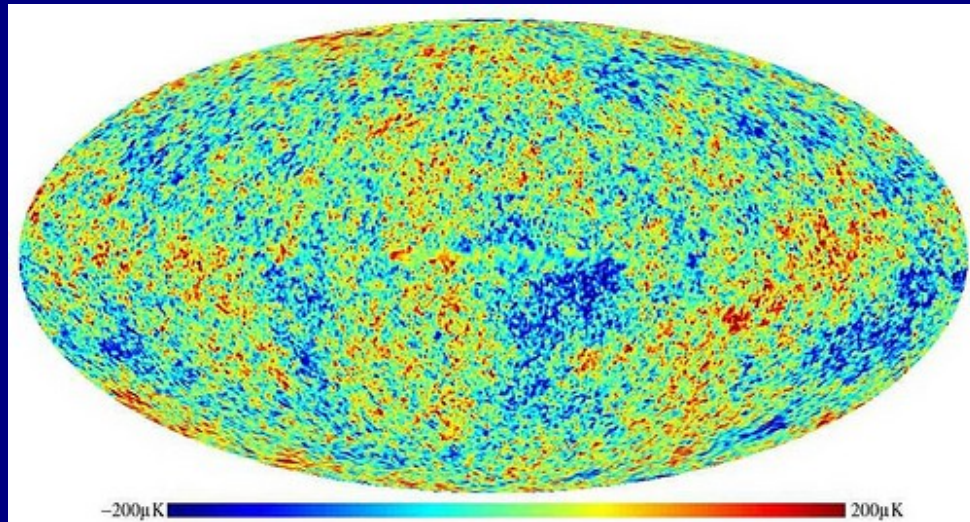
State of the art: 3+1 D with viscous corrections in the Israel-Stewart framework plus initial state fluctuations (among others: ECHO-QGP, Firenze-Ferrara-Torino collaboration).





# Anisotropies in the azimuthal plane in relativistic heavy ion collisions: extraction of the QCD transport coefficients

Analogous to CMB anisotropies



# Outlook

- There is little doubt that QGP has been produced in relativistic heavy ion collisions. The study of its properties is ongoing at the LHC.
- The dynamical QGP evolution can be described in terms of relativistic thermodynamics and hydrodynamics. This allows to test specific predictions of QCD thermodynamics, such as equation of state, transport coefficients etc.
- Why are the thermal distributions observed at all in strong interactions in high energy collisions?
- Search of more features of QCD phase diagram at lower energy: critical point ?
- Relativistic heavy ion collisions have been a very effective laboratory for many physics subjects: not only QCD, but also relativistic statistical mechanics, relativistic hydrodynamics and kinetics

# ECHO-QGP: codice di idrodinamica relativistica dissipativa della comunità italiana

Collaborazione Firenze-Ferrara-Torino entro RM31-SIM e PRIN2009(2011)

Eur. Phys. J. C (2013) 73:2524  
DOI 10.1140/epjc/s10052-013-2524-5

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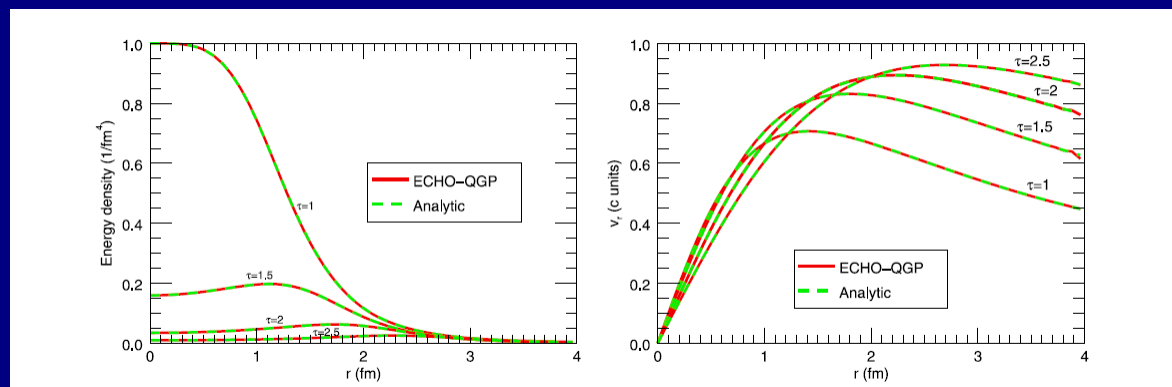
Regular Article - Theoretical Physics

## Relativistic viscous hydrodynamics for heavy-ion collisions with ECHO-QGP

L. Del Zanna<sup>1,2,3,a</sup>, V. Chandra<sup>2</sup>, G. Inghirami<sup>1,2</sup>, V. Rolando<sup>4,5</sup>, A. Beraudo<sup>6</sup>, A. De Pace<sup>7</sup>, G. Pagliara<sup>4,5</sup>, A. Drago<sup>4,5</sup>, F. Becattini<sup>1,2,8</sup>

Evoluzione di ECHO codice numerico 3+1 D ideale GR per plasmi astrofisici (L. Del Zanna et al.)

Include 3+1D Israel-Stewart con fluttuazioni di stato iniziale e produzione di particelle (vedi talk di Valentina Rolando)



# Shear viscosity in strongly interacting conformal quantum field theory (from AdS/CFT correspondence)

Kovtun, Son, Starinets PRL 94, 111601 (2005)

$$\frac{\eta}{s} = \frac{\hbar}{4\pi}$$

Conjecture: it is a universal quantum bound which is reached for the maximal coupling

$$\eta \sim \rho v \ell, \quad s \sim n = \frac{\rho}{m}$$

$$\frac{\eta}{s} \sim m v \ell \sim \hbar \frac{\text{mean free path}}{\text{de Broglie wavelength}}$$

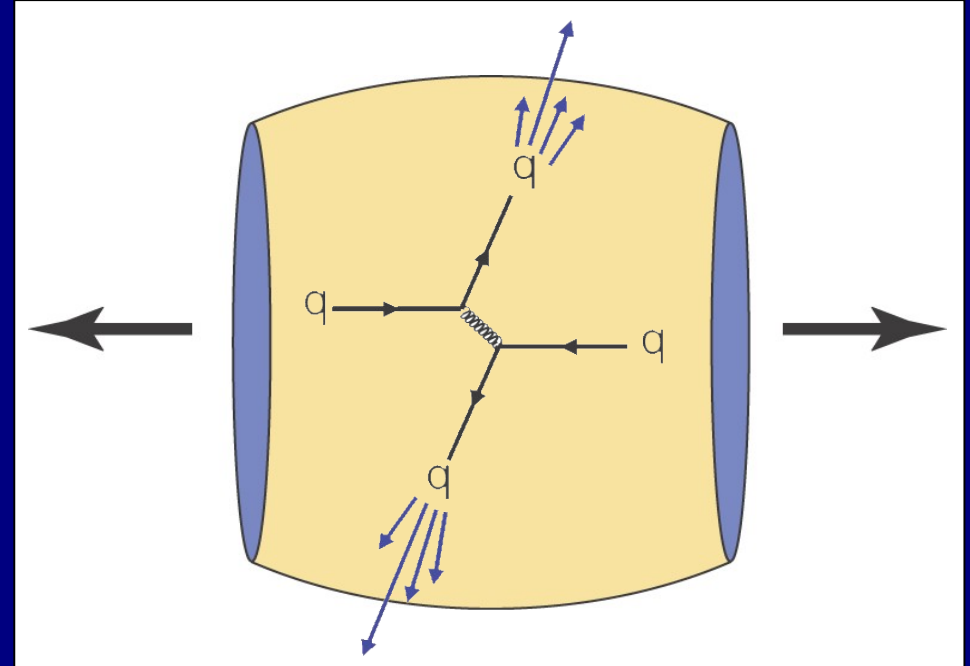
Quasiparticles: de Broglie wavelength  $\lesssim$  mean free path

Therefore  $\eta/s \gtrsim \hbar$

# Jets as a probe of the plasma

## Nucleus-nucleus collisions

- hard initial scattering
  - scattered partons probe traversed hot and dense medium
  - ‘jet tomography’
- Initial parton-parton scattering with large momentum transfer
    - Unlike in vacuum, quarks and gluons lose energy (brehmsstrahlung and collisions) before hadronizing

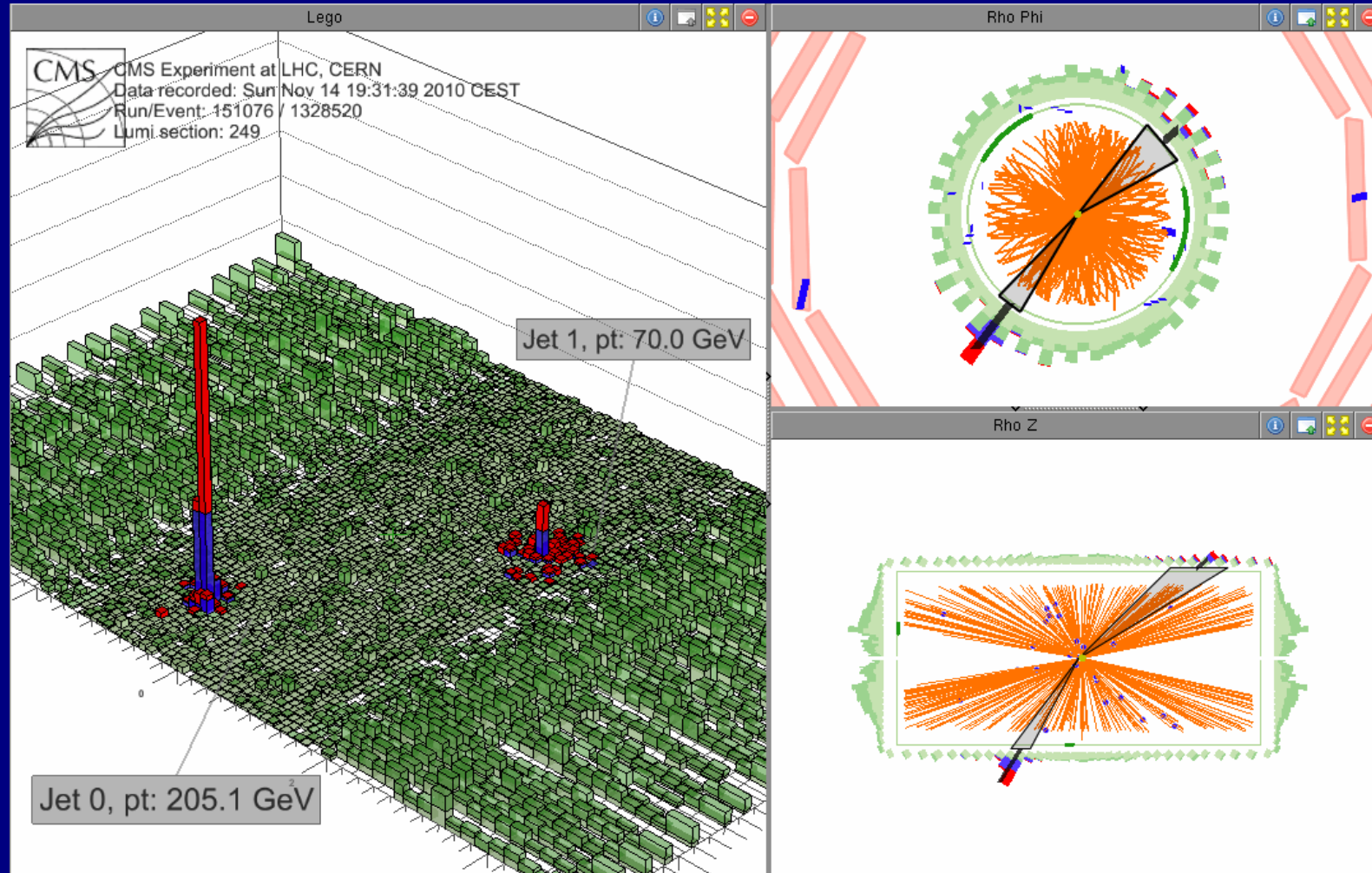


Theoretical task: to calculate energy distribution of hard partons traversing a length  $L$  within the medium



# Di-jet imbalance

- Pb-Pb events with large di-jet imbalance observed at the LHC

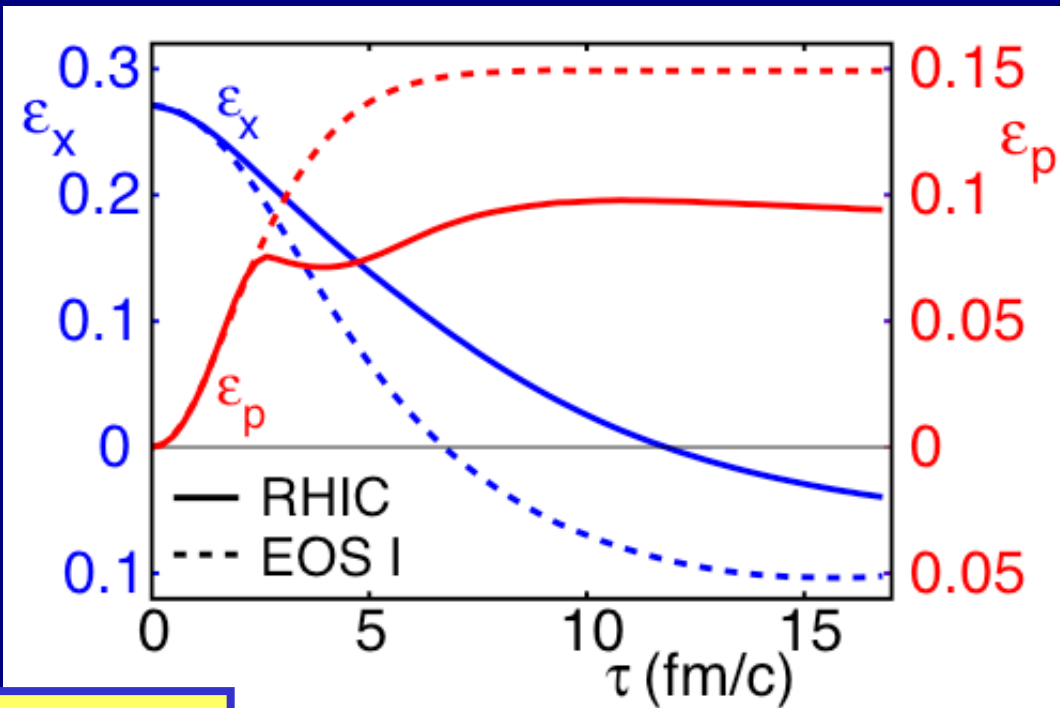
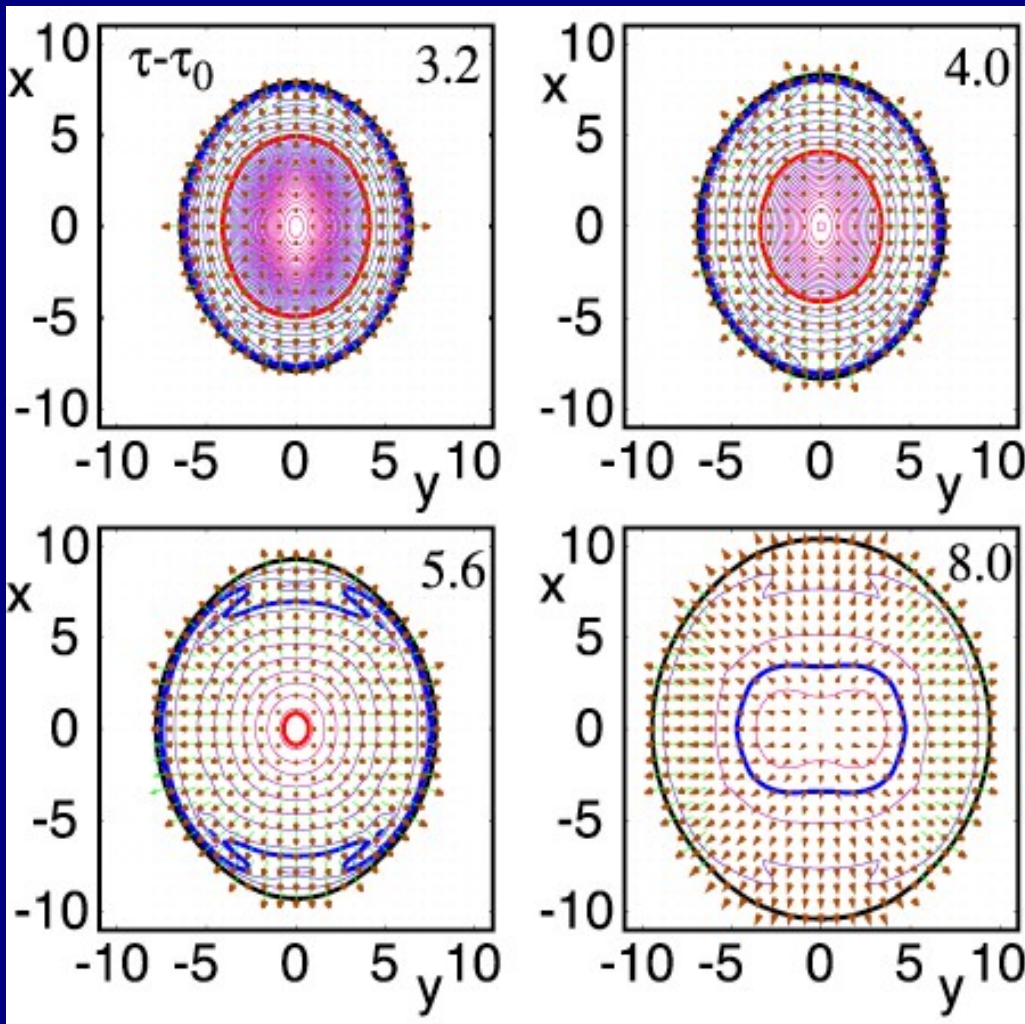


→ recoiling jet strongly quenched!

CMS: arXiv:1102.1957

## Anisotropia di impulso

$$\epsilon_p = \frac{\langle T^{xx} - T^{yy} \rangle}{\langle T^{xx} + T^{yy} \rangle}$$



Spatial anisotropy gets converted into momentum anisotropy provided that:

- Thermalization occurs while the system is still almond-shaped
- This requires short times ( $\sim 1$  fm/c) when the system is still in the QGP phase



# Soft and Hard probes

**SOFT** ( $p_T \sim \Lambda_{\text{QCD}}, T$ )

driven by **non perturbative QCD**

hadron yields, collective modes of the bulk,  
strangeness enhancement, fluctuations,  
thermal radiation, dilepton enhancement

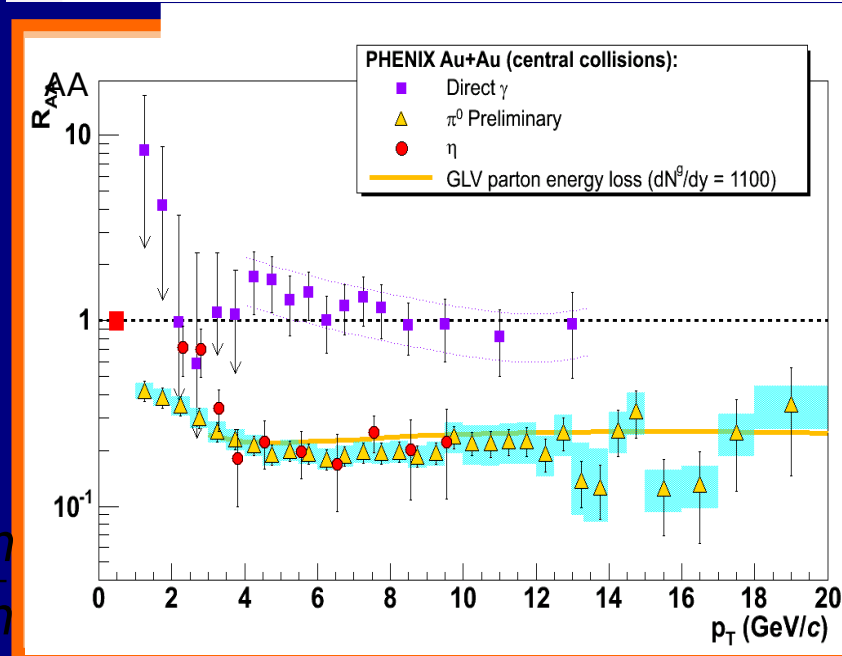
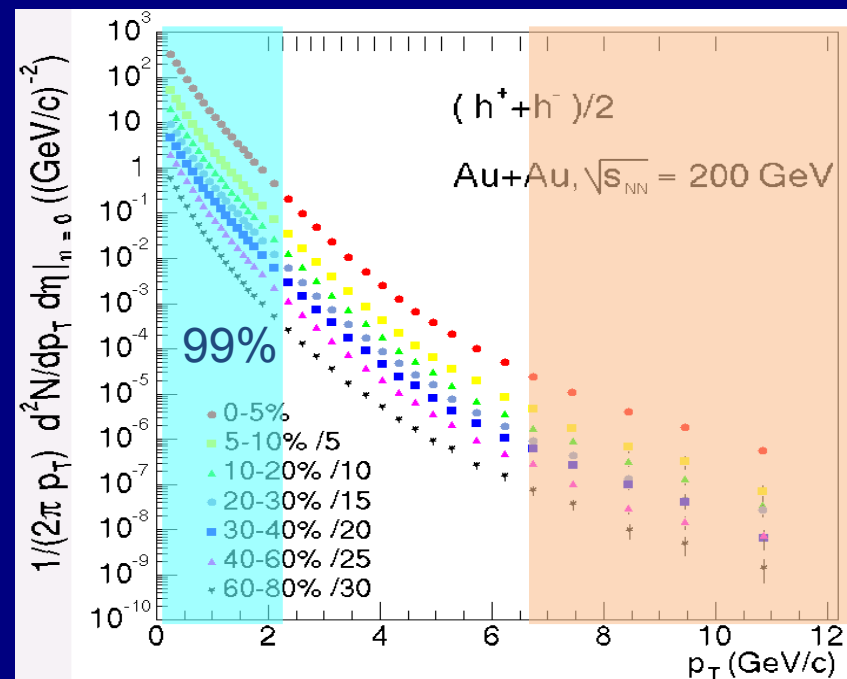
**HARD** ( $p_T \gg \Lambda_{\text{QCD}}$ )

Early production, pQCD applicable,  
Baseline pp, pA

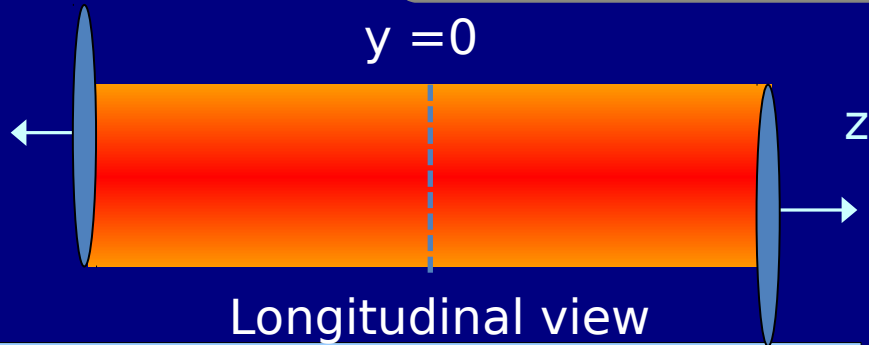
jet quenching, heavy quarks, quarkonia,  
hard photons (W,Z)

Nuclear modification factor

$$R_{AA}(p_T) = \frac{d^2 N^{AA} / dp_T}{N_{\text{coll}} d^2 N^{NN} / dp_T} = \frac{\text{medium}}{\text{vacuum}}$$

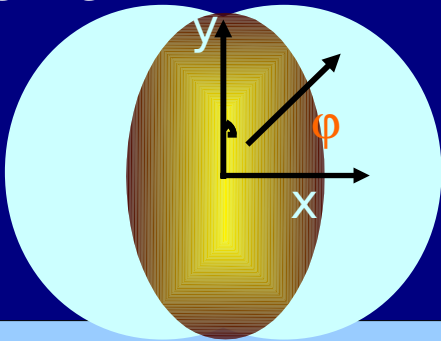


# Some typical definitions



$$y_z = \tanh^{-1} \beta = \frac{1}{2} \ln \frac{E + p_z}{E - p_z} \approx v_z$$

Transverse view

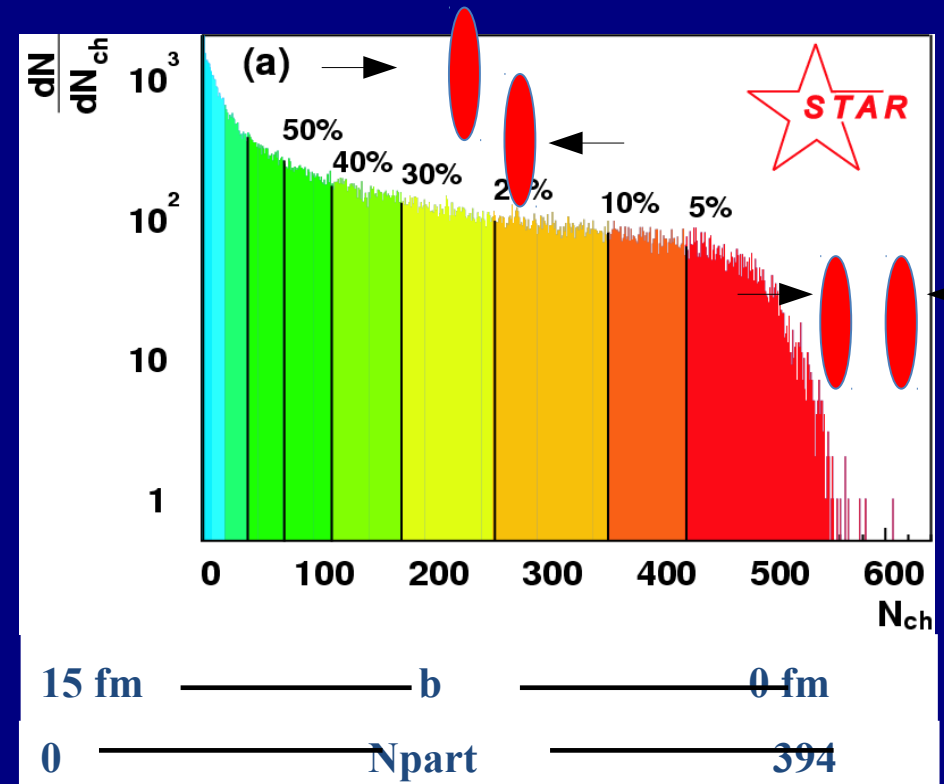


$$p^\mu = (E, p_x, p_y, p_z)$$

In terms of  $p_T$  and  $y$

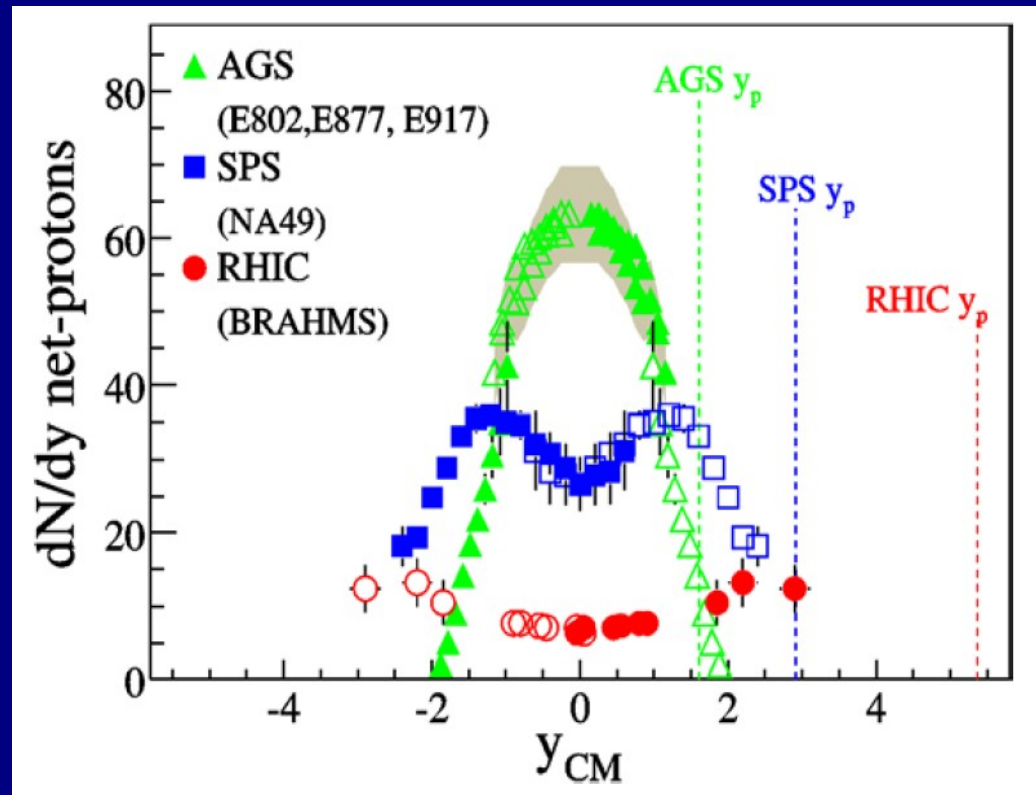
$$p^\mu = (m_T \cosh y, p_T, m_T \sinh y)$$

Centrality of the collisions

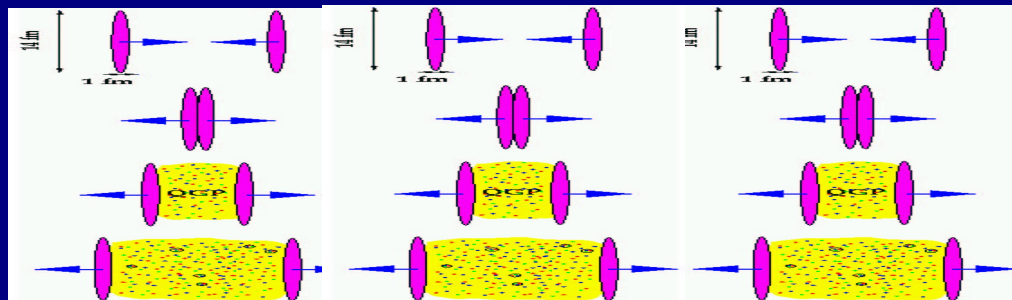


$$m_T = \sqrt{p_T^2 + m^2}$$

# Increasing the energy...

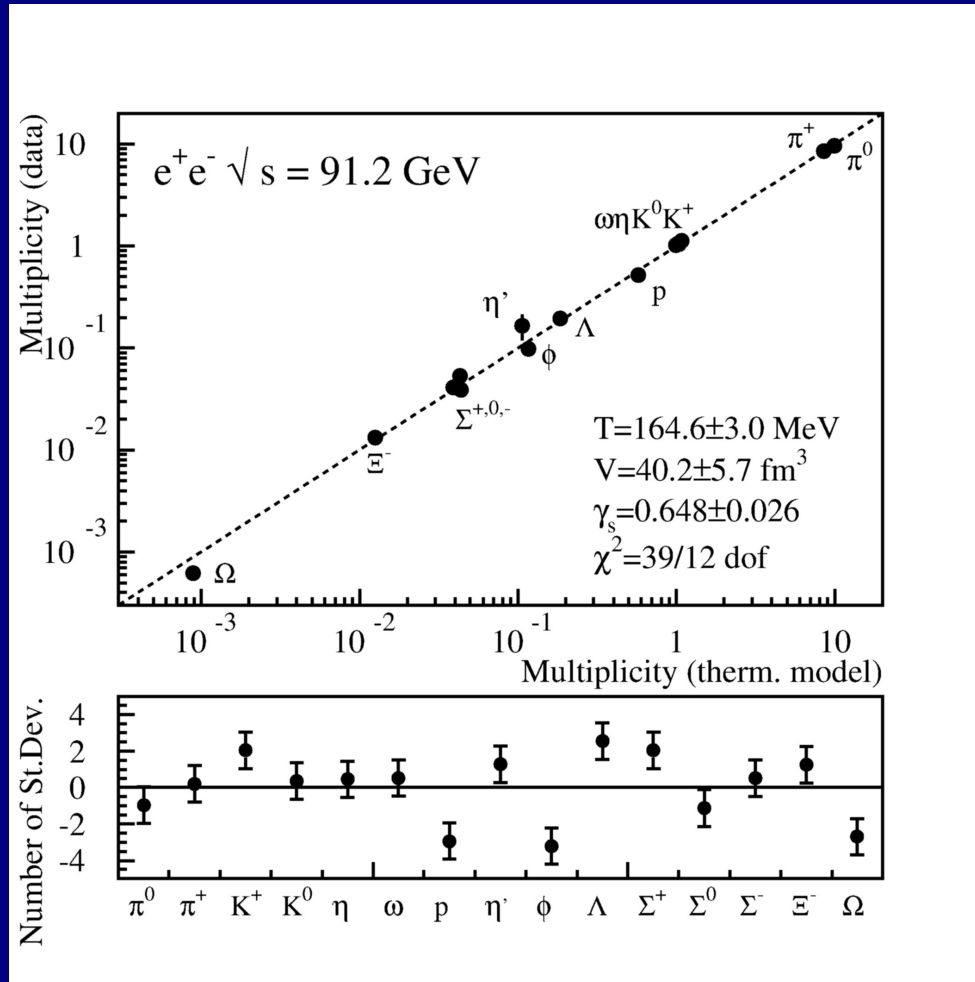


Baryon stopping decreases, but a larger energy density is achieved (hotter, denser, longer)



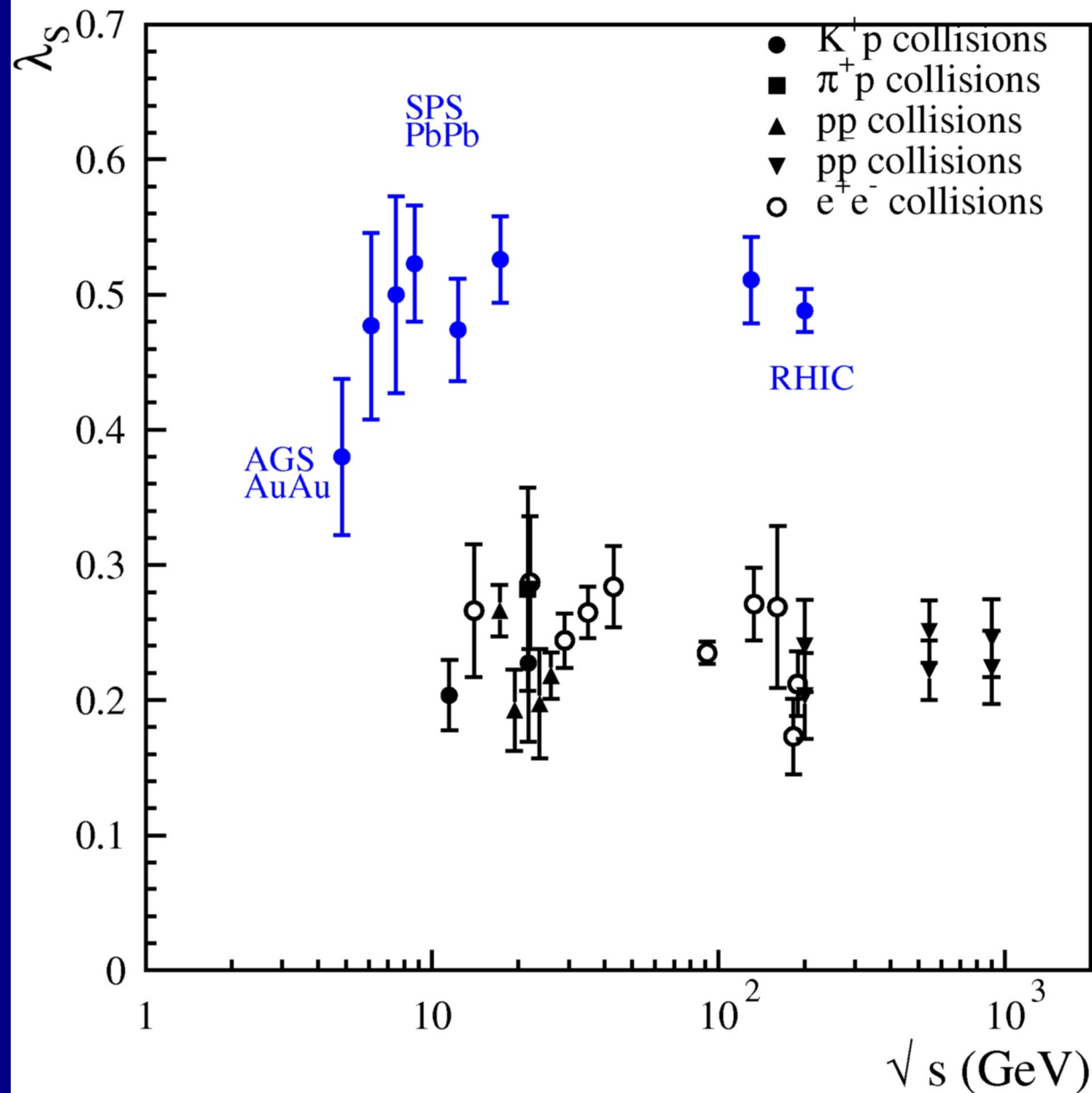
# Have we overcome the critical T?

Same observation as in elementary collisions. Statistical equilibrium as an Intrinsic feature of QCD at the soft scale, i.e. hadronization (F.B., U. Heinz, R. Stock, H. Satz et al)



In order to show that  $T_c$  has been overcome, i.e. that a QGP has been produced, we need to go to other observables

# Strangeness enhancement: Wroblewski ratio

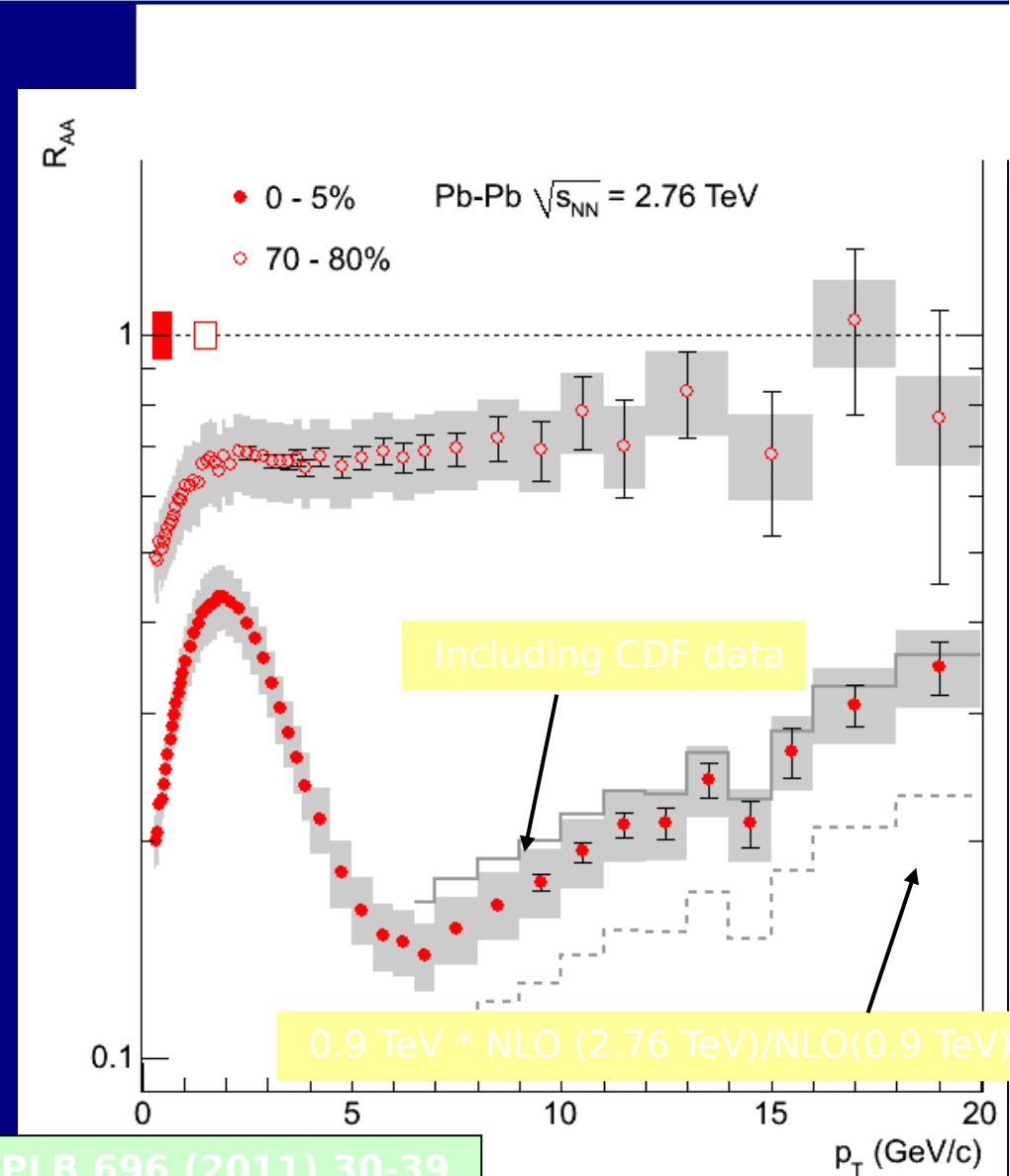


$$\lambda_S = 2 \frac{\langle s\bar{s} \rangle}{\langle u\bar{u} + d\bar{d} \rangle}$$

# Suppression of high- $p_T$ hadrons (not so for $\gamma$ )

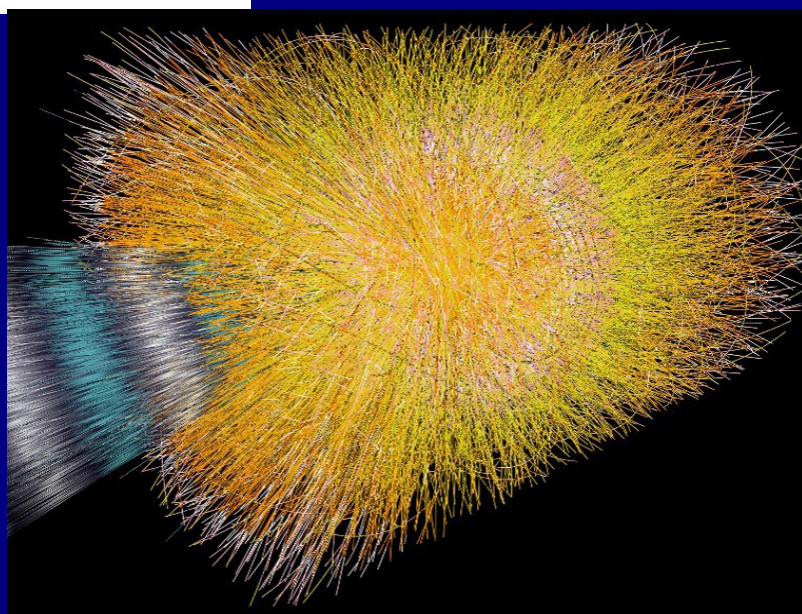
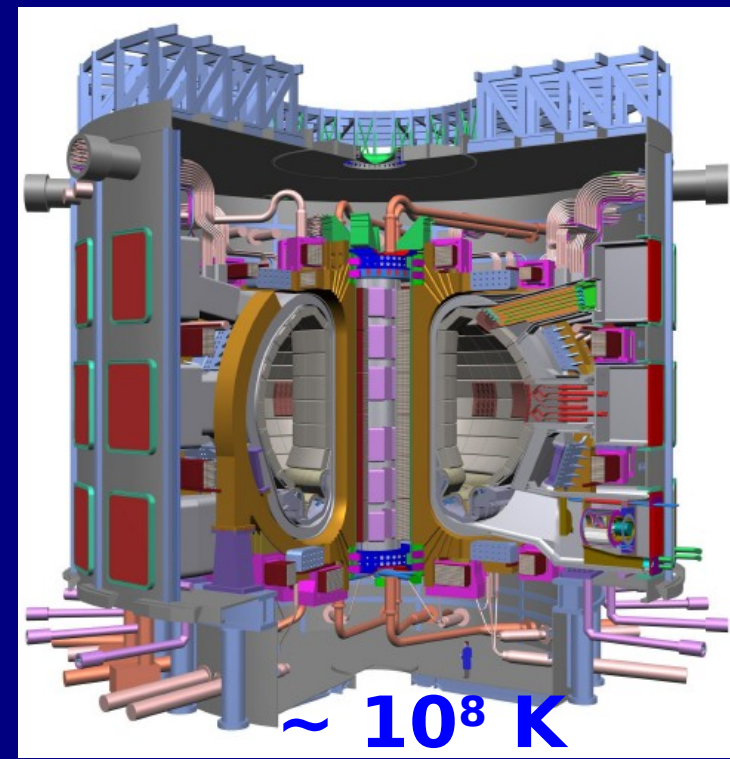
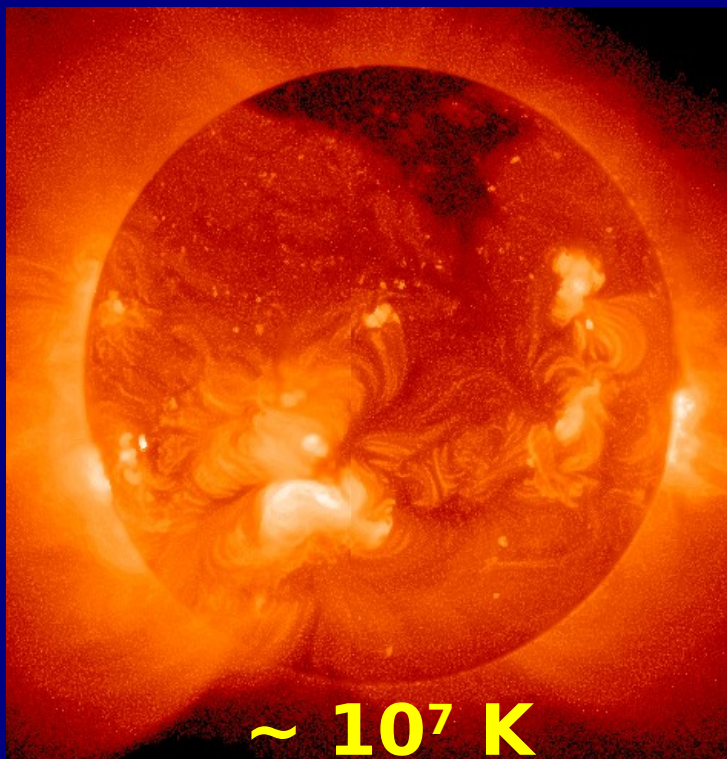
- Due to energy loss of partons, there is a strong suppression of high  $p_T$  hadrons
- Even larger at LHC than @ RHIC
- Nuclear modification factor  $R_{AA}(p_T)$  for charged particles produced in 0-5% centrality range
  - minimum ( $\sim 0.14$ ) for  $p_T \sim 6-7$  GeV/c
  - then slow increase at high  $p_T$

$$R_{AA}(p_T) = \frac{\text{Yield}_{AA}(p_T)}{\langle N_{bin} \rangle_{AA} \text{Yield}_{pp}(p_T)}$$





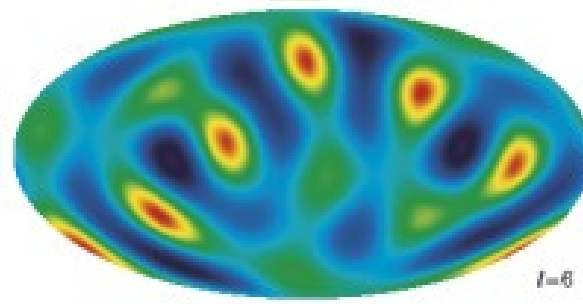
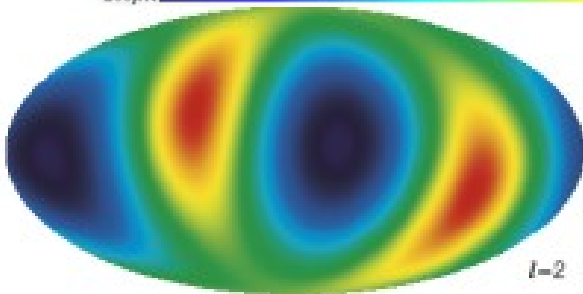
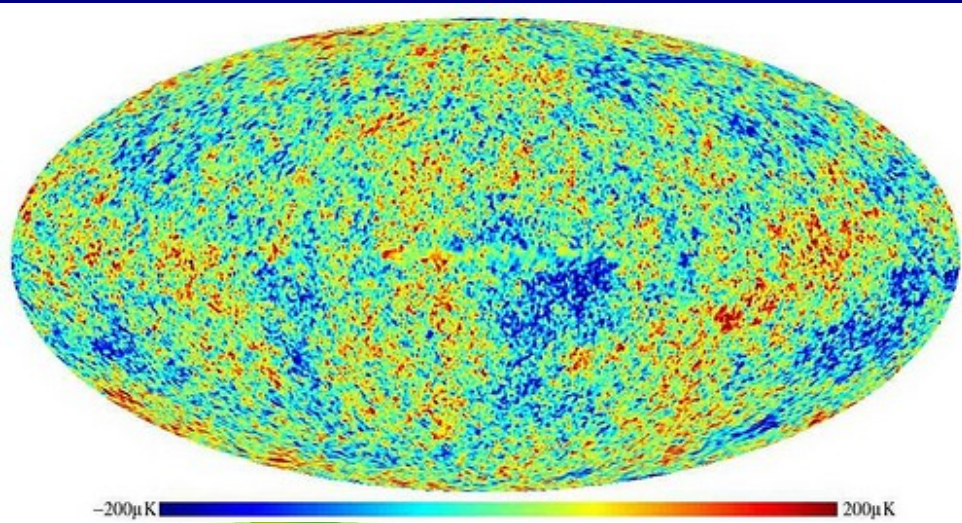
# The largest temperature ever achieved on Earth ( $> 2 \times 10^{12}$ K)



$\sim 5 \cdot 10^{12}$  K !



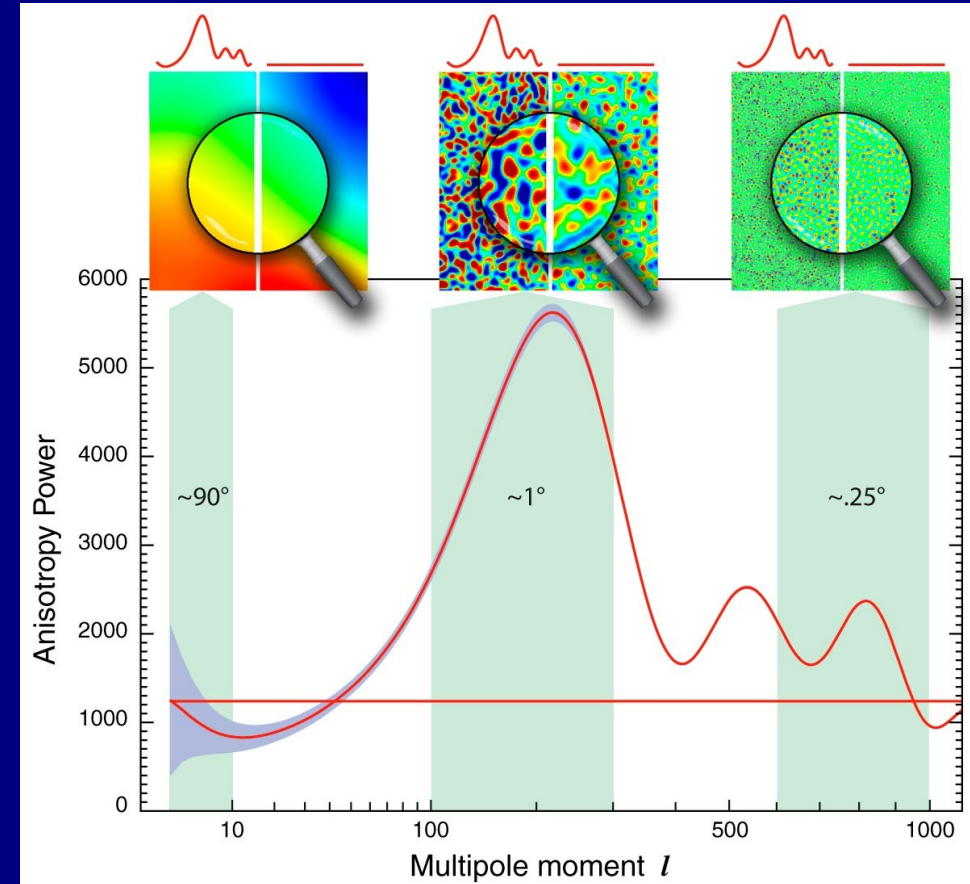
# High harmonics fluctuations reminds the CMB fluctuations...



$$\frac{\Delta T}{T} \sim 10^{-5}$$

$$l_{\text{maximum}} \approx 210$$

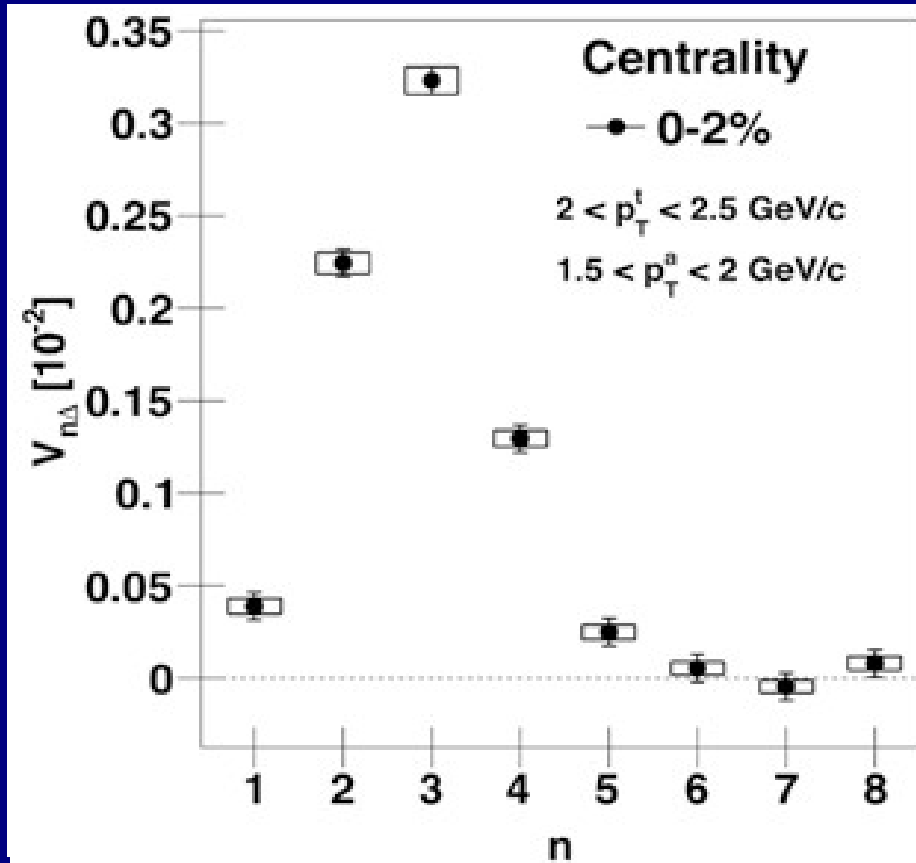
$$\delta\phi \sim 2\pi/l_{\text{maximum}} \sim 1^\circ$$



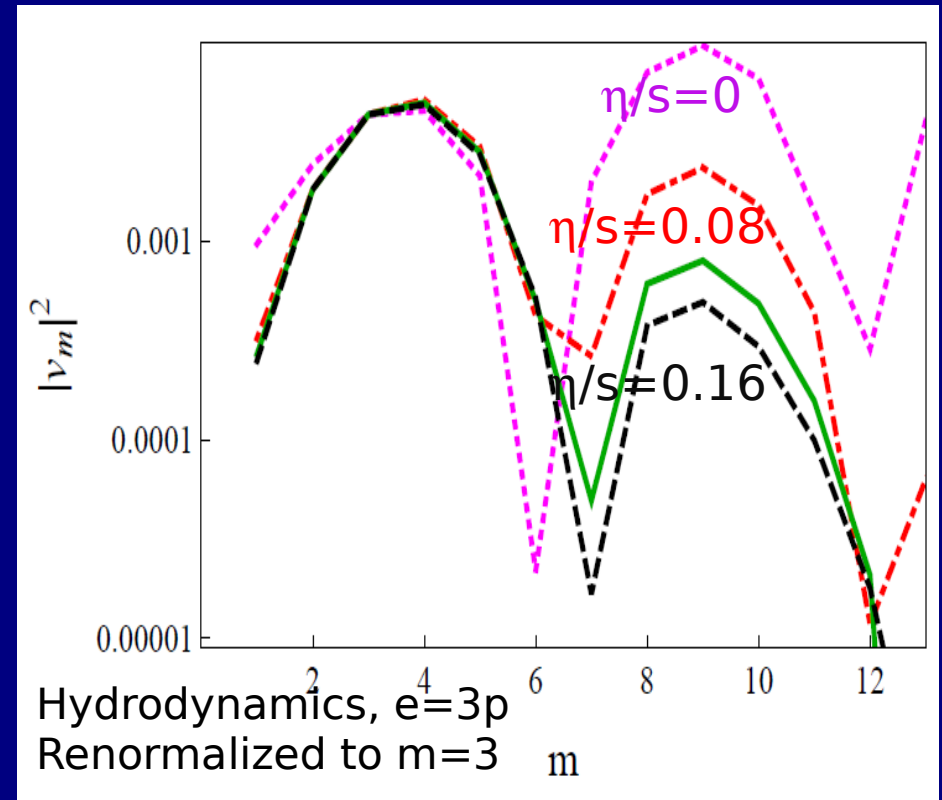
Freeze-out  $\tau \sim 380.000 \text{ y's}$  (QGP  $\sim 10^{-22} \text{ s}$ )  
 Sound horizon  $R \sim \text{Mps}$  (QGP  $\sim 6 \text{ fm}$ )

Of course  $n=200$  is not possible to be seen for a hadron system  
 with  $R \sim 10 \text{ fm}$

# A recent ALICE measurement



## A first schematic calculation



Staig & Shuryak, PRC (2011)

None of the models reproduce the correct shapes:

- No peak at  $n=3$
- Too large for  $n > 6$

A promising new challenge -> new findings and knowledge