

Dark Matter: Galaxy Formation, Small Scale Crisis, and WDM

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Outline

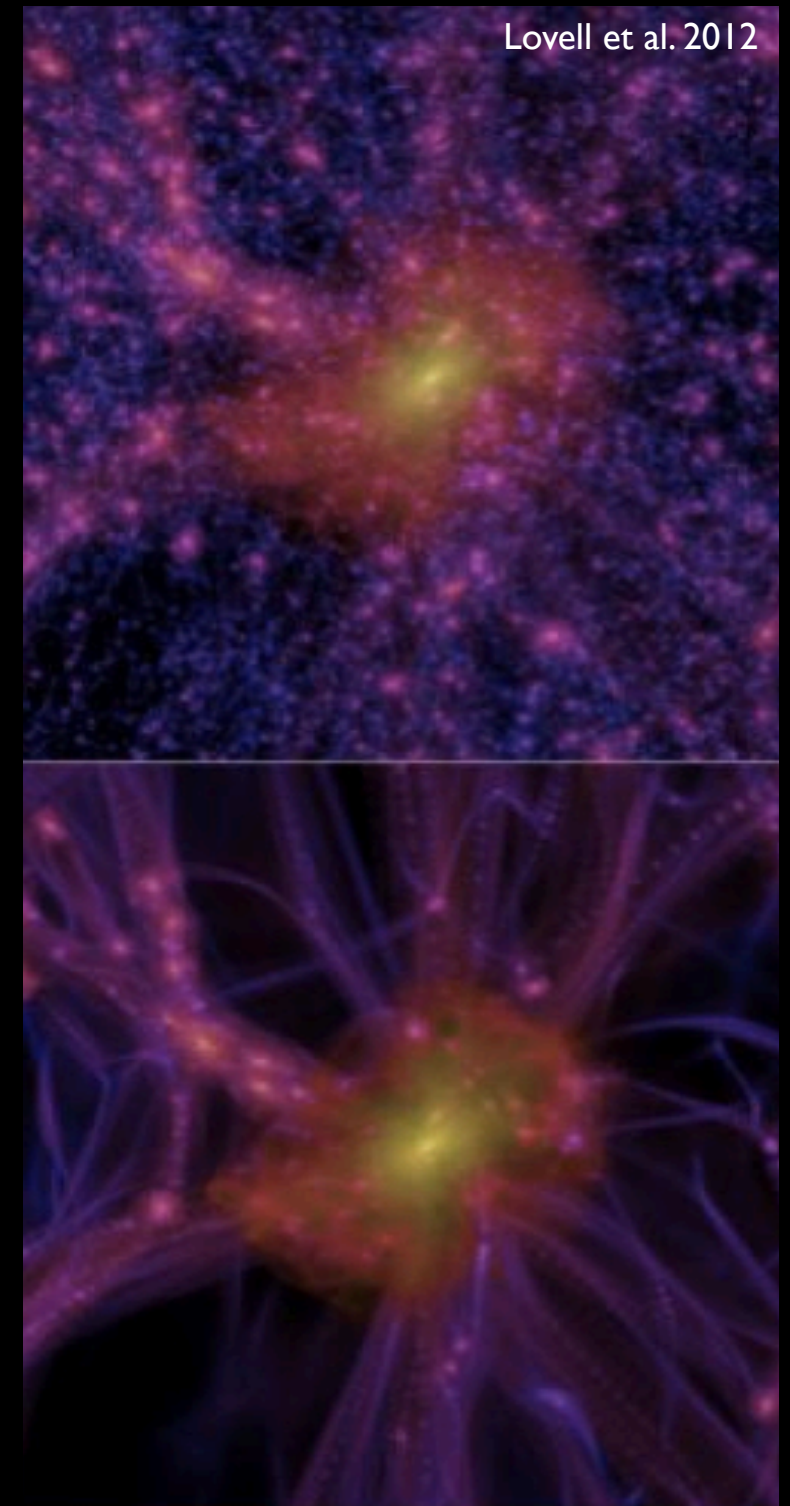
Evidences for DM

- rotation curves
- galaxy clusters
- growth of perturbations from CMB
- concordance cosmology

The Impact of the mass DM particles on the formation of cosmic structures

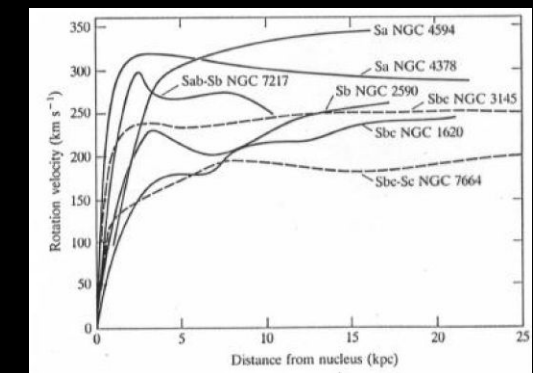
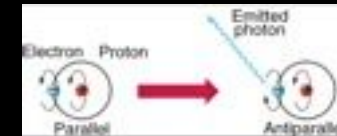
Galaxy Formation in Cold Dark Matter:
The small-scale crisis

Galaxy Formation in Warm Dark Matter scenarios



Galaxy rotation curves

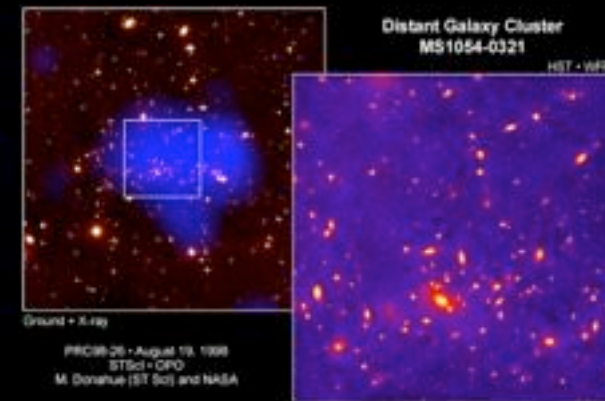
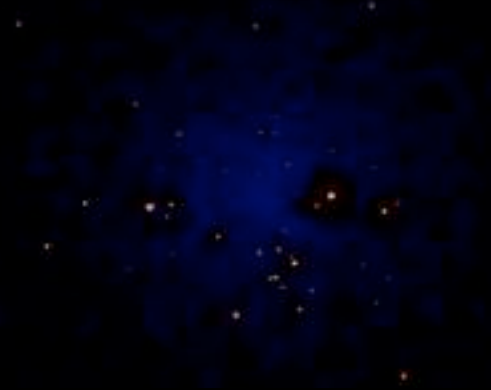
$$M/L \approx 10-50$$



Galaxy clusters:

velocity dispersions
X-ray temperature
Gravitational lensing

$$M/L \sim 100$$



$$\langle v^2 \rangle = \frac{GM}{R}$$

$$KT = \frac{GM}{R} / \mu m_p$$

Cosmology

Ordinary matter (baryons) can only grow after recombination ($z \sim 1000$).
Since $\delta \sim (1+z)^{-1}$, they can grow at most a factor 1000.

$\delta \sim 10^{-5}$ observed at recombination implies that they cannot grow non-linear ($\delta \sim 1$) at the present time

Dark Matter: starts to grow earlier. At recombination baryons fall into potential wells which are already in place



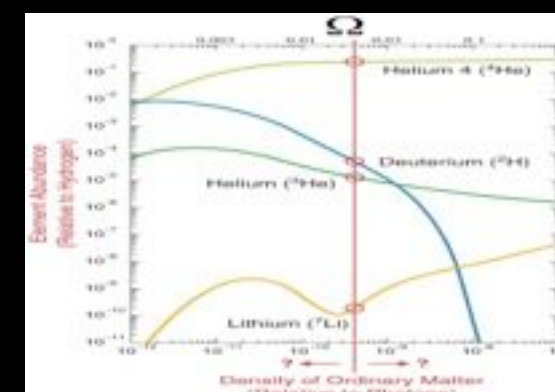
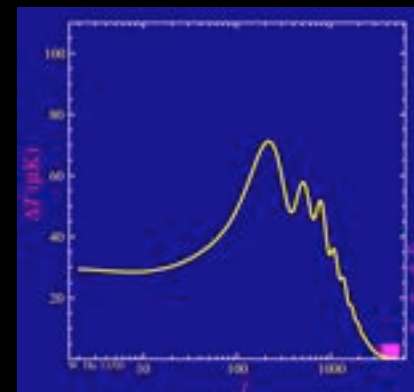
$$\delta(t_{rec}) \sim 10^{-5}$$

$$\delta(t) \sim t^{2/3} \sim (1+z)$$

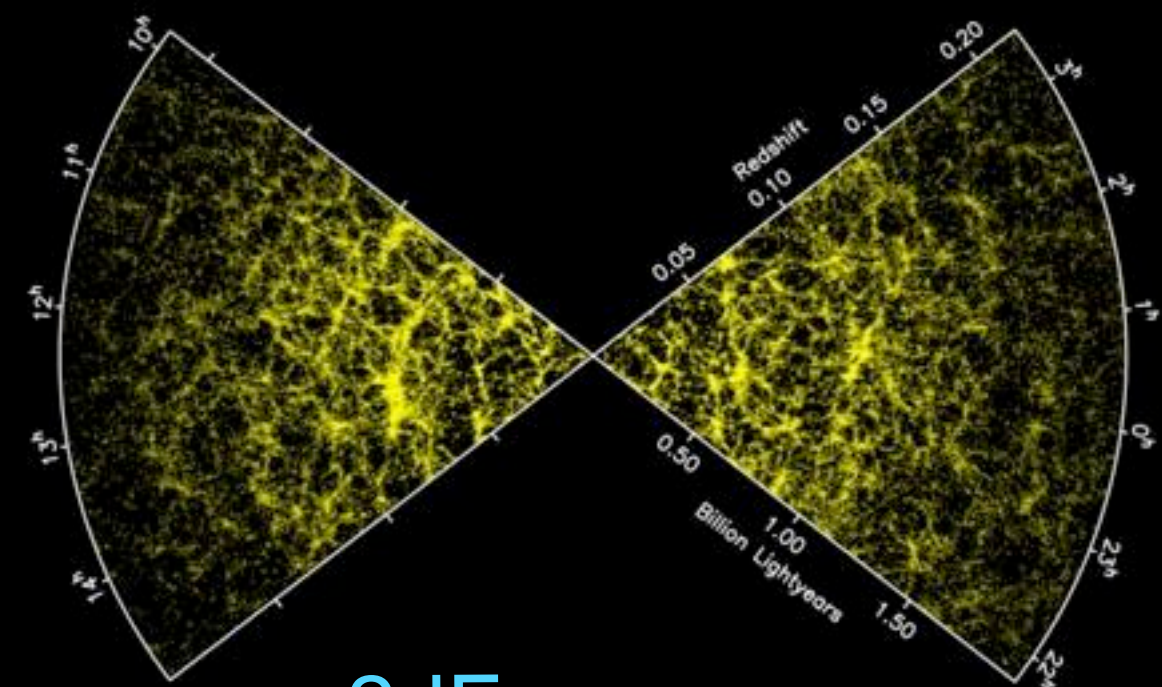
CMB+Baryon Nucleosynthesis

$$\Omega_b \approx 0.04$$

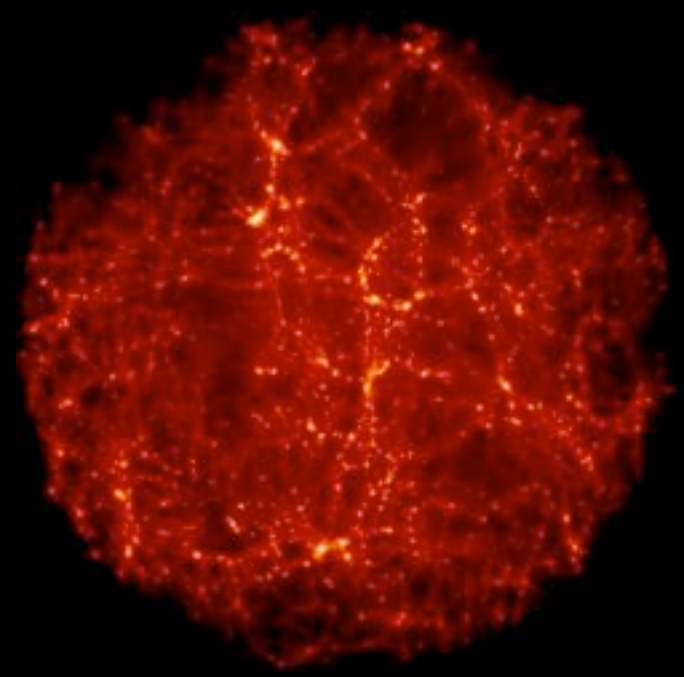
$$\Omega_M \approx 0.25$$



Galaxies are the tip of the iceberg (underlying DM distribution)



2dF survey

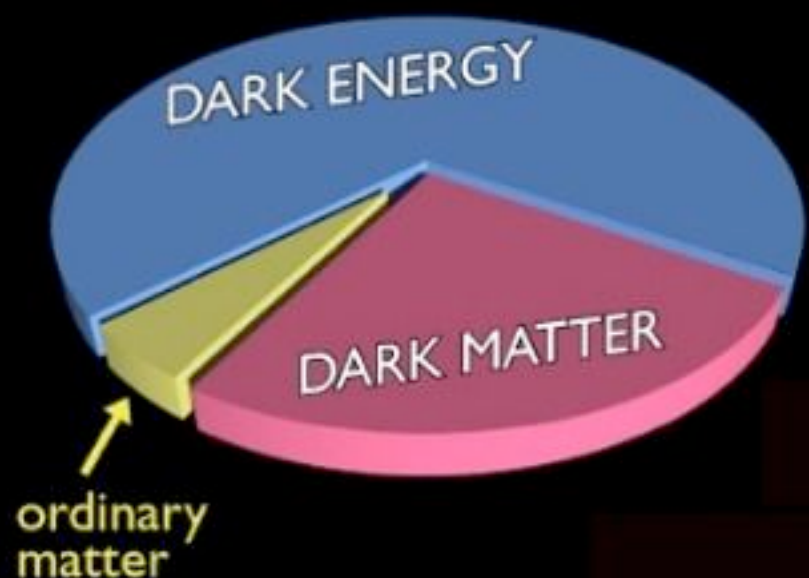
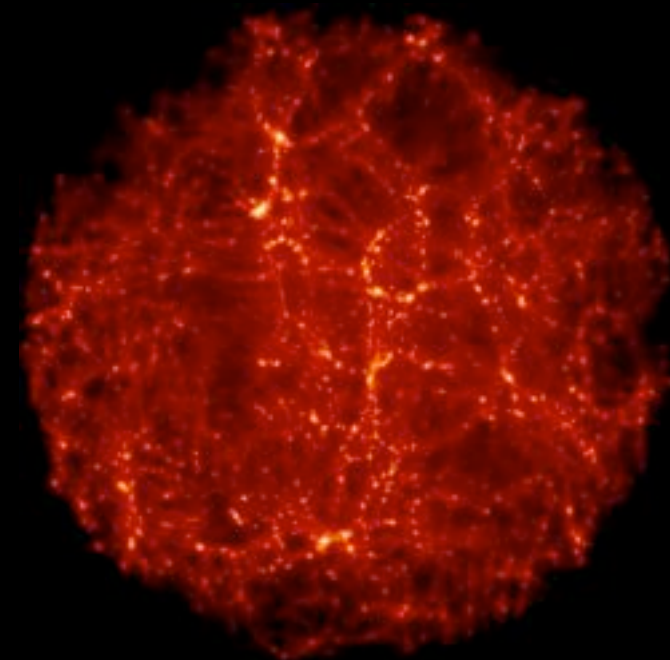


Galaxies are the tip of the iceberg (underlying DM distribution)

Galaxy Formation Theory

Describe the collapse and evolution of the DM clumps dominating the gravitational dynamics

Connect properties of ordinary matter (gas physics, star formation, astrophysical processes) to the potential wells of DM condensations

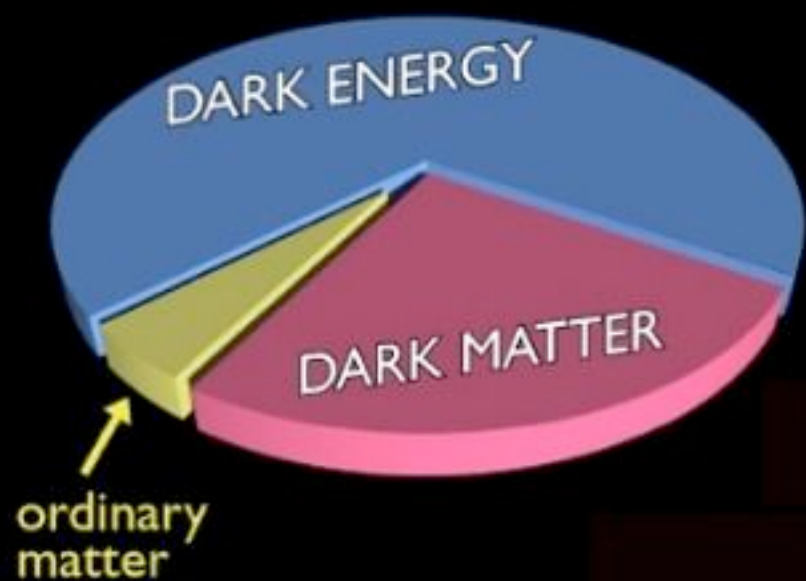


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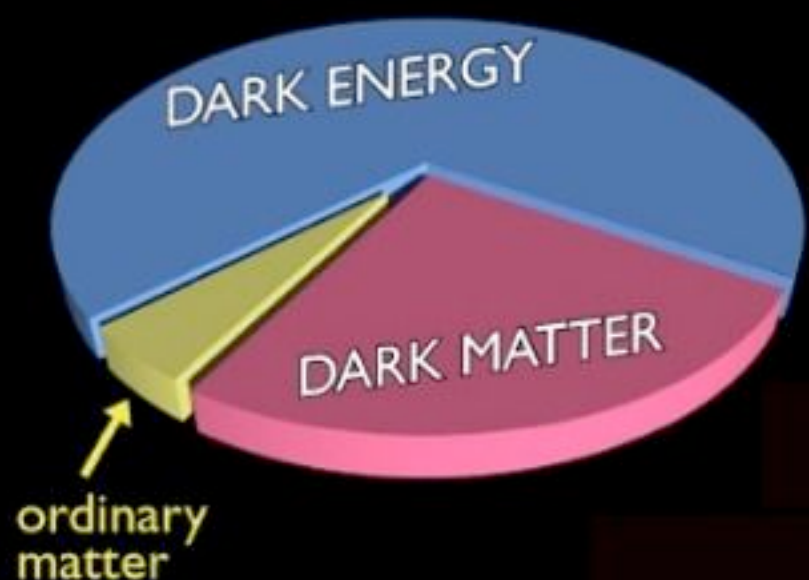
Galaxies are the tip of the iceberg (underlying DM distribution)

Diemand et al. 2008

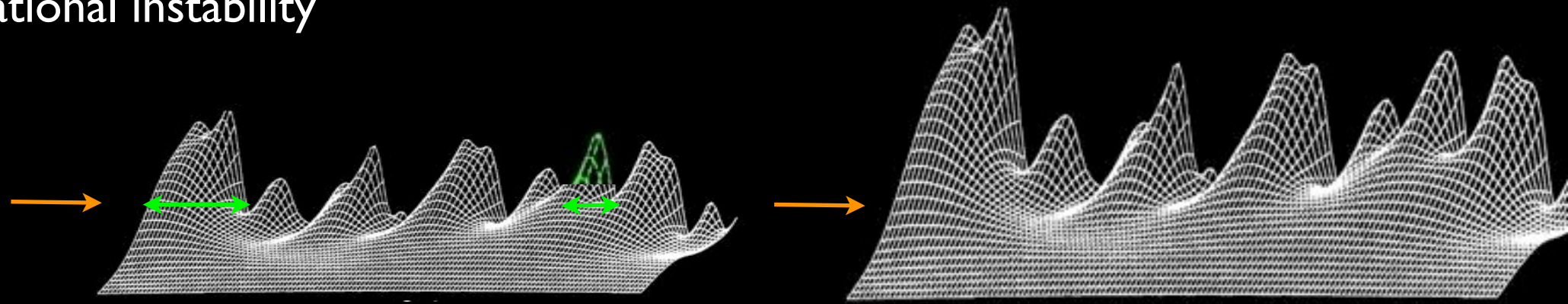
Galaxy Formation Theory

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Cosmic Structures form from the collapse of overdense regions in the DM primordial density field, and grow by gravitational instability



Gaussian Random field

$$\delta = \frac{\delta\rho}{\rho}$$

$$p(\delta_k) = \frac{1}{\sqrt{2\pi} \sigma_k} e^{-\frac{\delta_k^2}{2\sigma_k^2}}$$

$$R=2\pi/k$$

$$M = \frac{4\pi}{3} \rho R^3$$

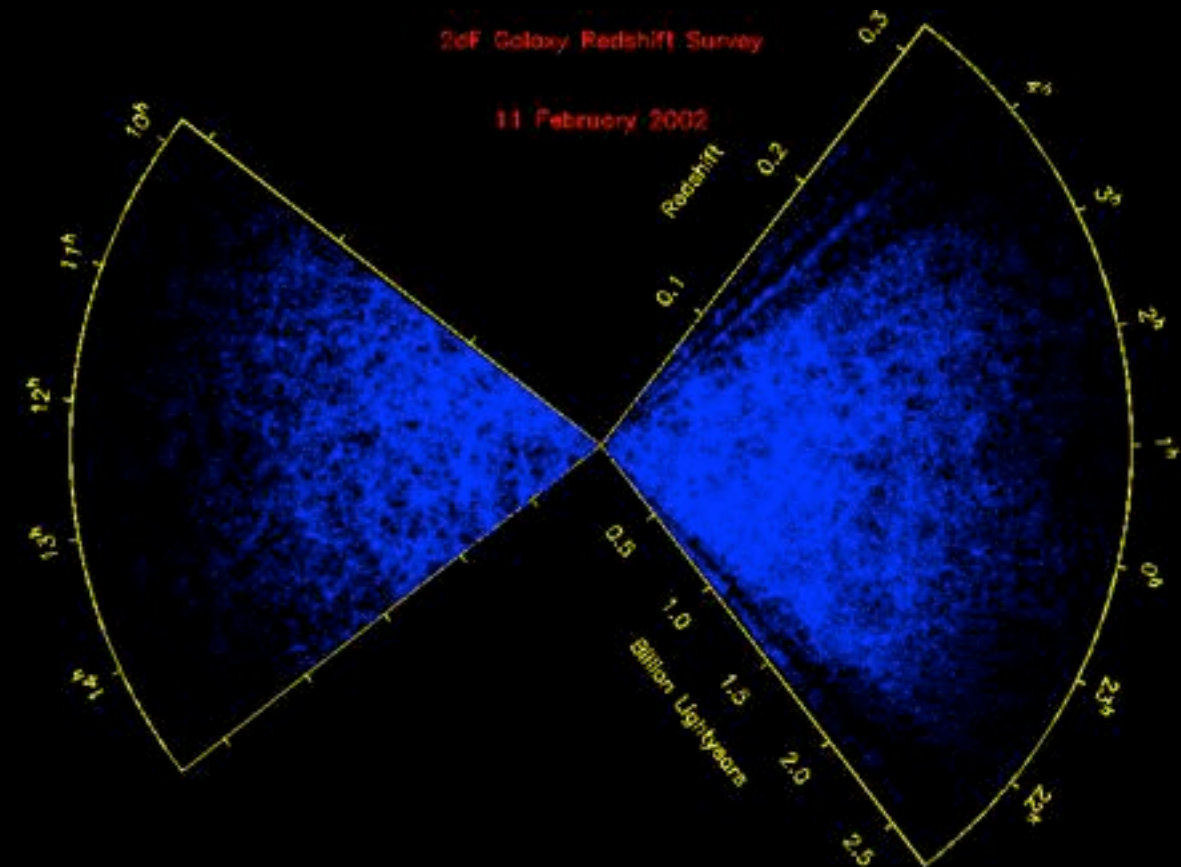
$$\langle \delta_M^2 \rangle = \sigma^2(M) g(t)$$

Mean (square) value of perturbations of size $R(\sim 1/k)$ enclosing a mass M

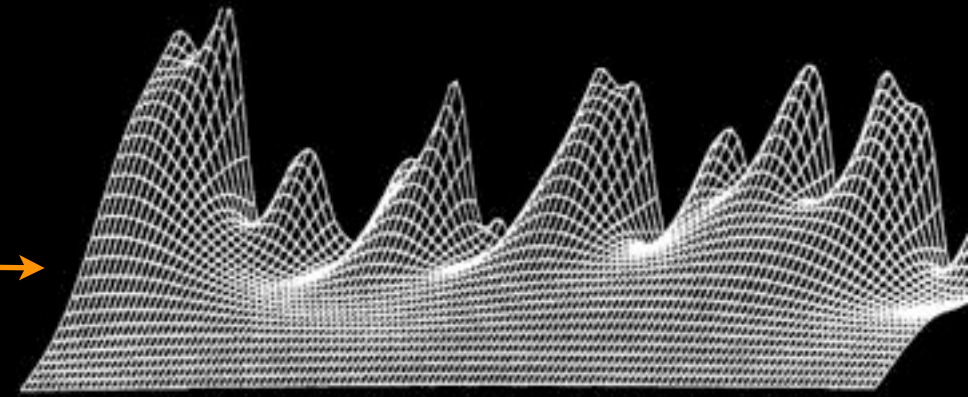
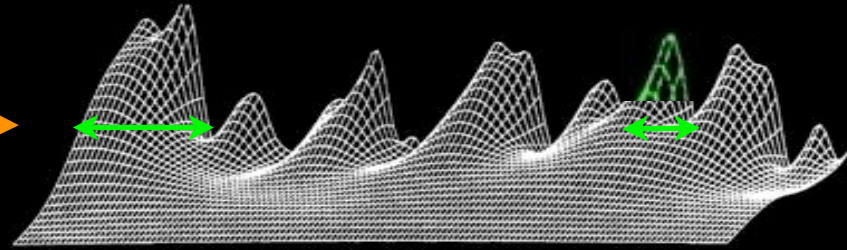
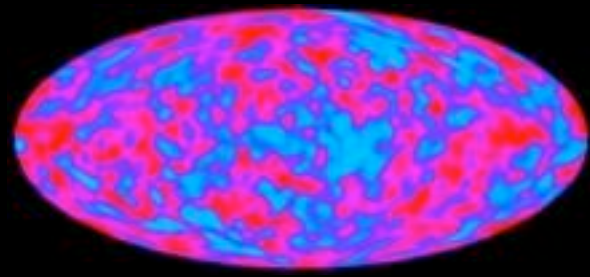
$$P(k) = \frac{1}{V} \langle |\delta_k|^2 \rangle$$

$$\sigma_M^2 = \frac{1}{(2\pi)^3 V} \int^{M \leftrightarrow k} dk k^2 P(k)$$

$$\sigma_M^2 \leftrightarrow P(k)$$



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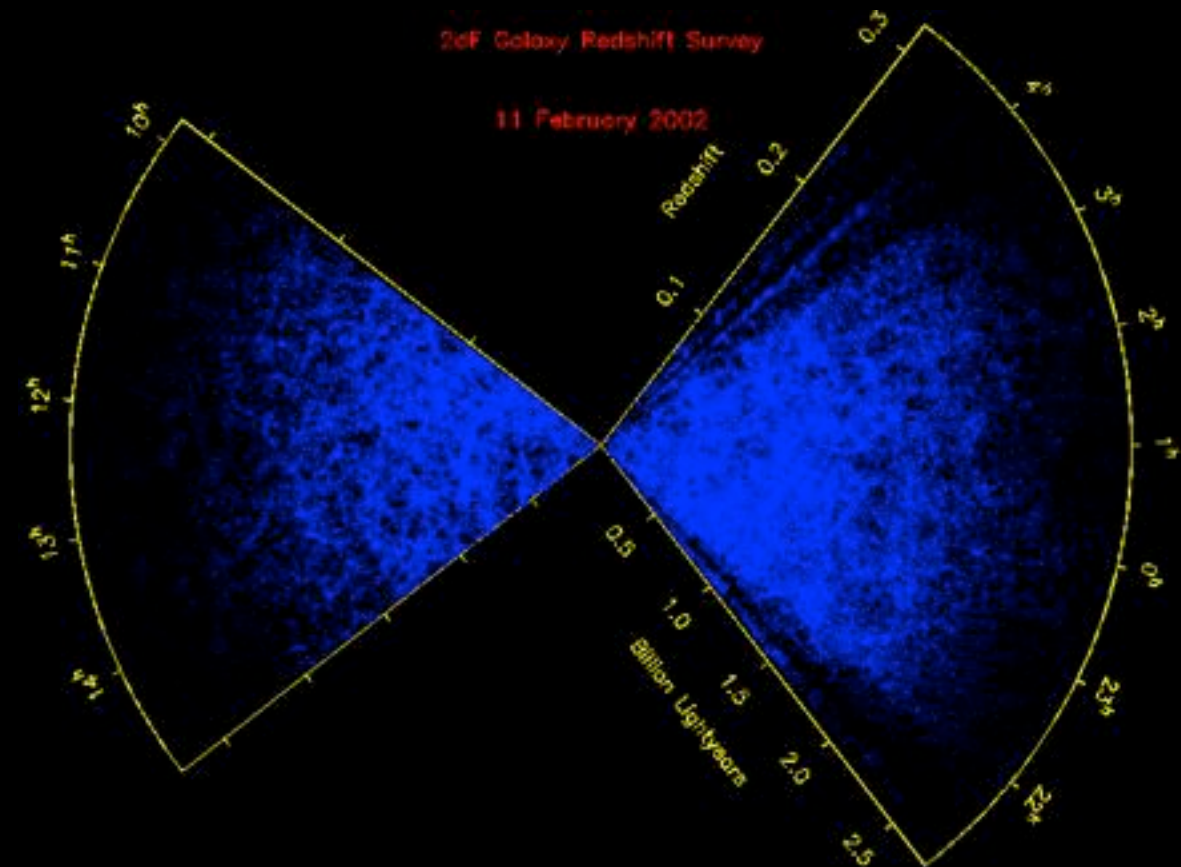


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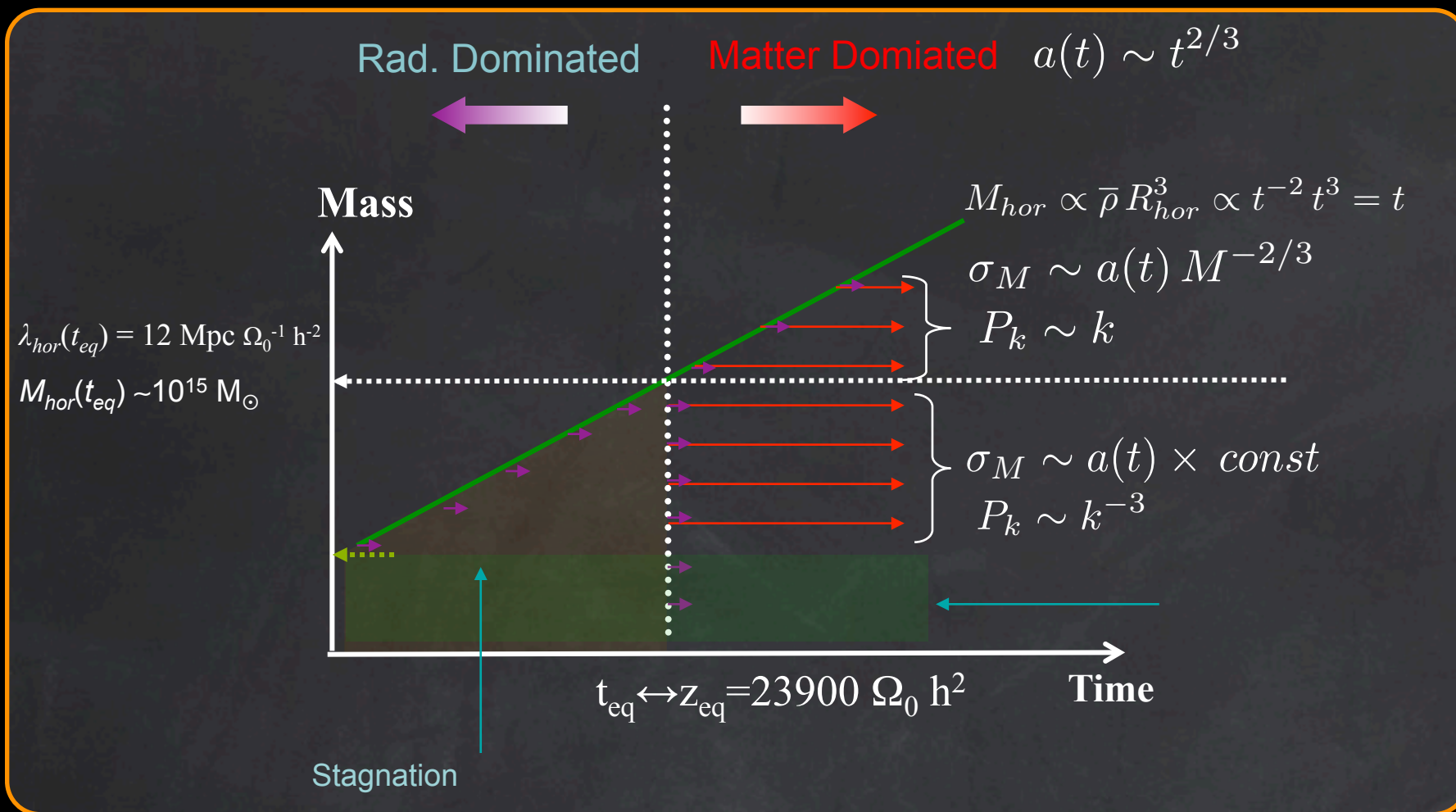
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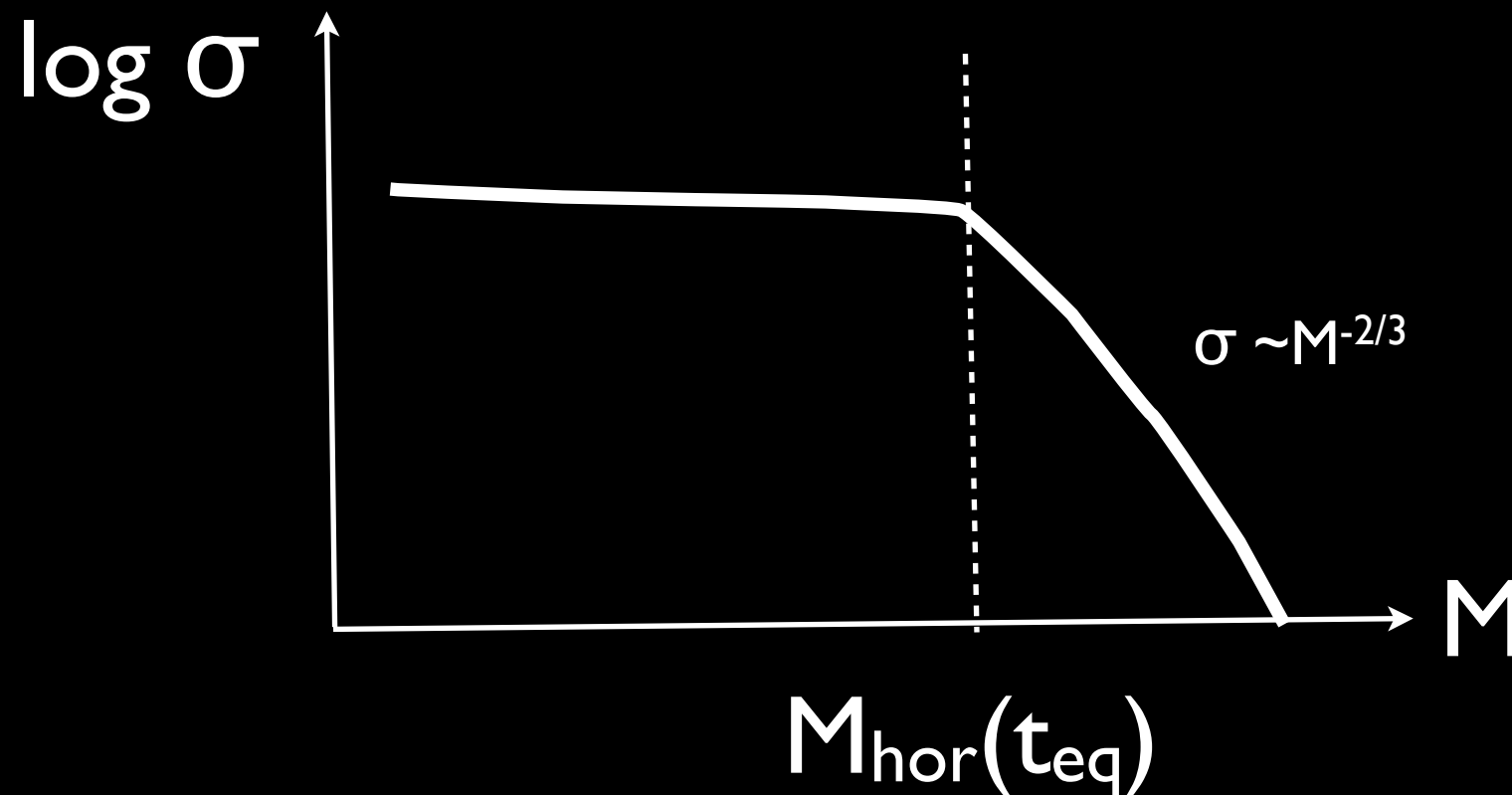
The Variance of the perturbation field



Perturbations involving scales larger than that of the horizon at the equivalence start to grow later

$$R_{hor} = 2c t_{hor} = 13 h^{-2} \text{ Mpc}$$

$$= 110 \text{ Mpc for } \sigma_0 = 0.3 \text{ } h = 0.7$$



The Variance of the perturbation field

Perturbations involving scales larger than that of the horizon at the equivalence start to grow later



The Variance of the perturbation field

On average, perturbations on large scales (large masses) have a lower amplitude

$$\sigma \sim \text{const for } M < M_{\text{hor}}(t_{\text{eq}})$$

$$\sigma \sim M^{-2/3} \text{ for } M > M_{\text{hor}}(t_{\text{eq}})$$

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In terms of wavenumber $k \rightarrow$ Power Spectrum

$$\sigma_M^2 = \frac{1}{(2\pi)^3 V} \int^{M \leftrightarrow k} dk k^2 P(k)$$

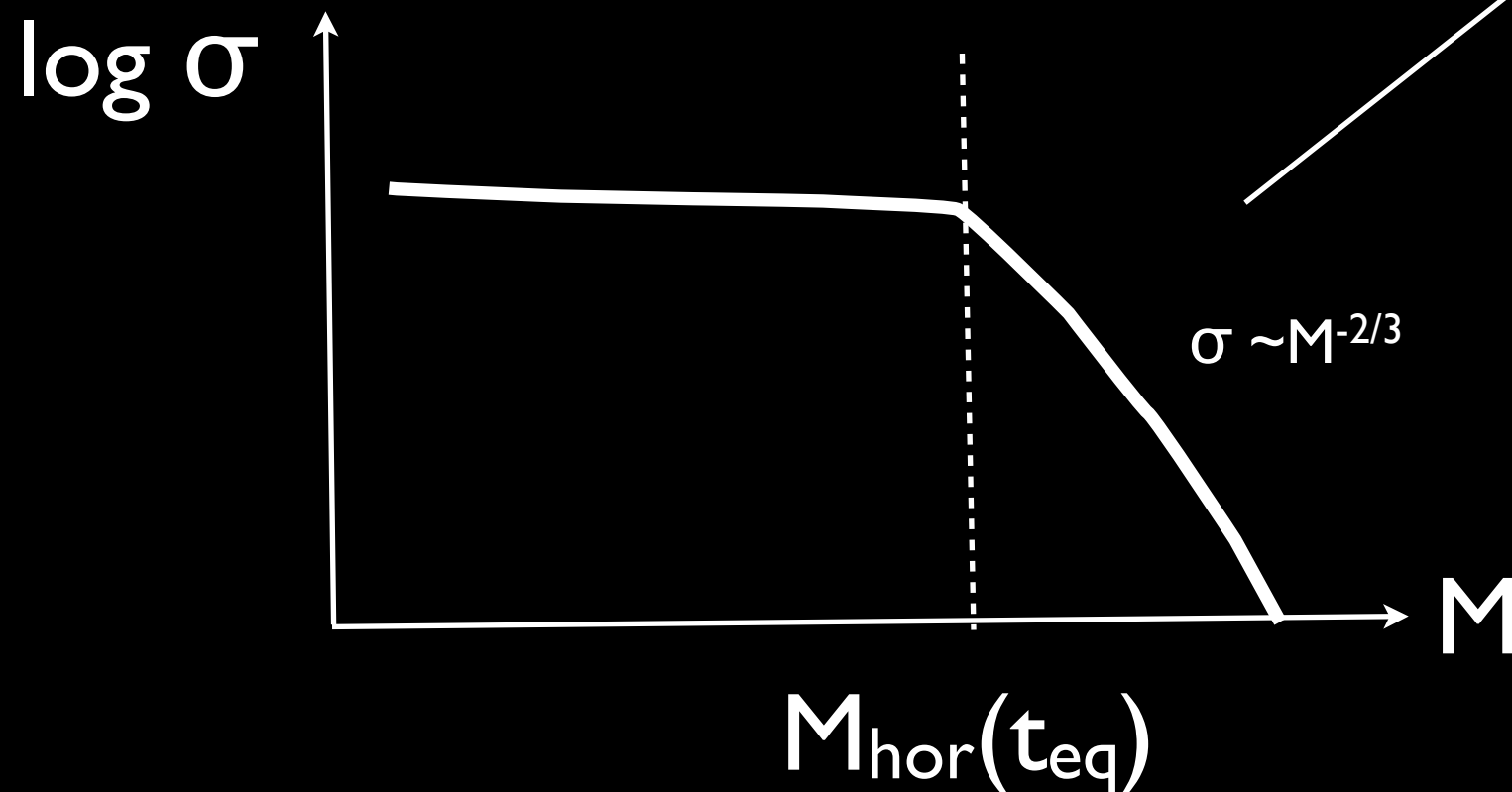
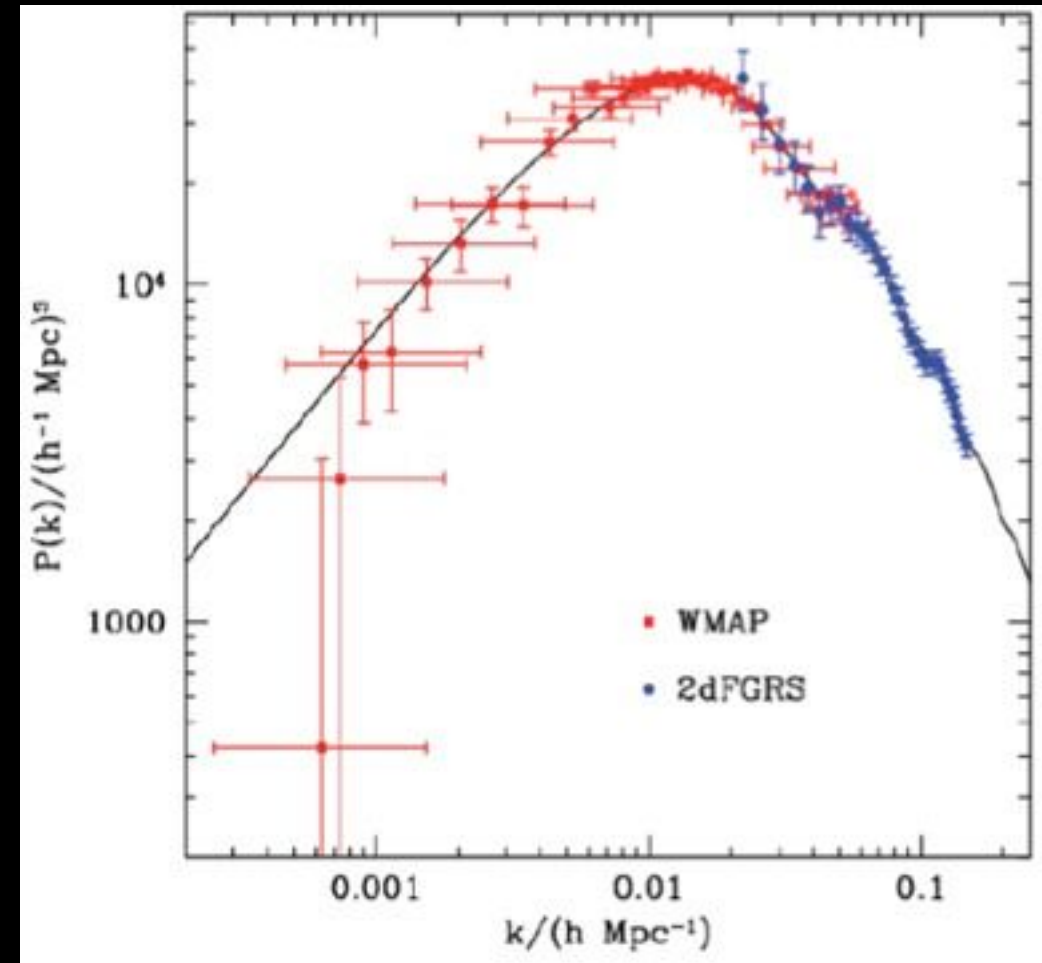
$$\langle |\delta_k^2| \rangle = P(k) \propto k^2$$

$$\sigma_M \propto M^{-2/3}$$

$$P(k) \propto k$$

$$\sigma_M = \text{const}$$

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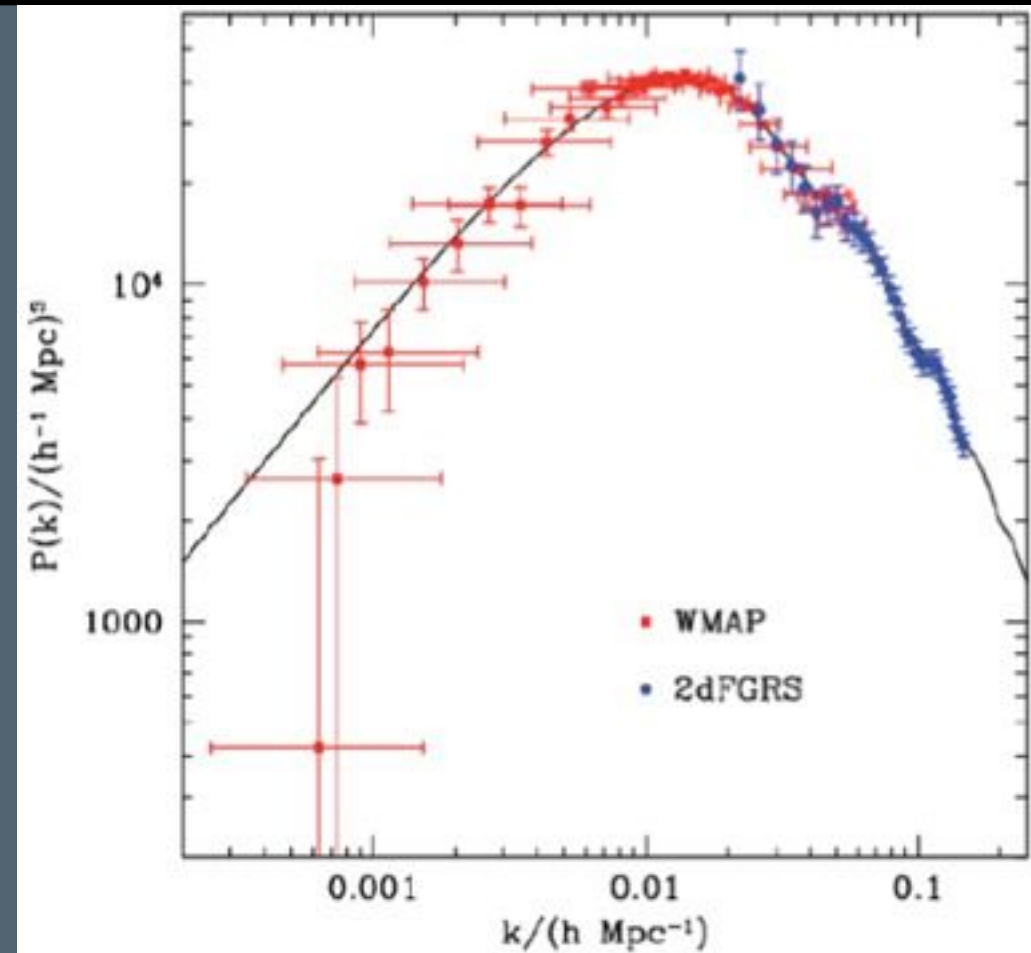
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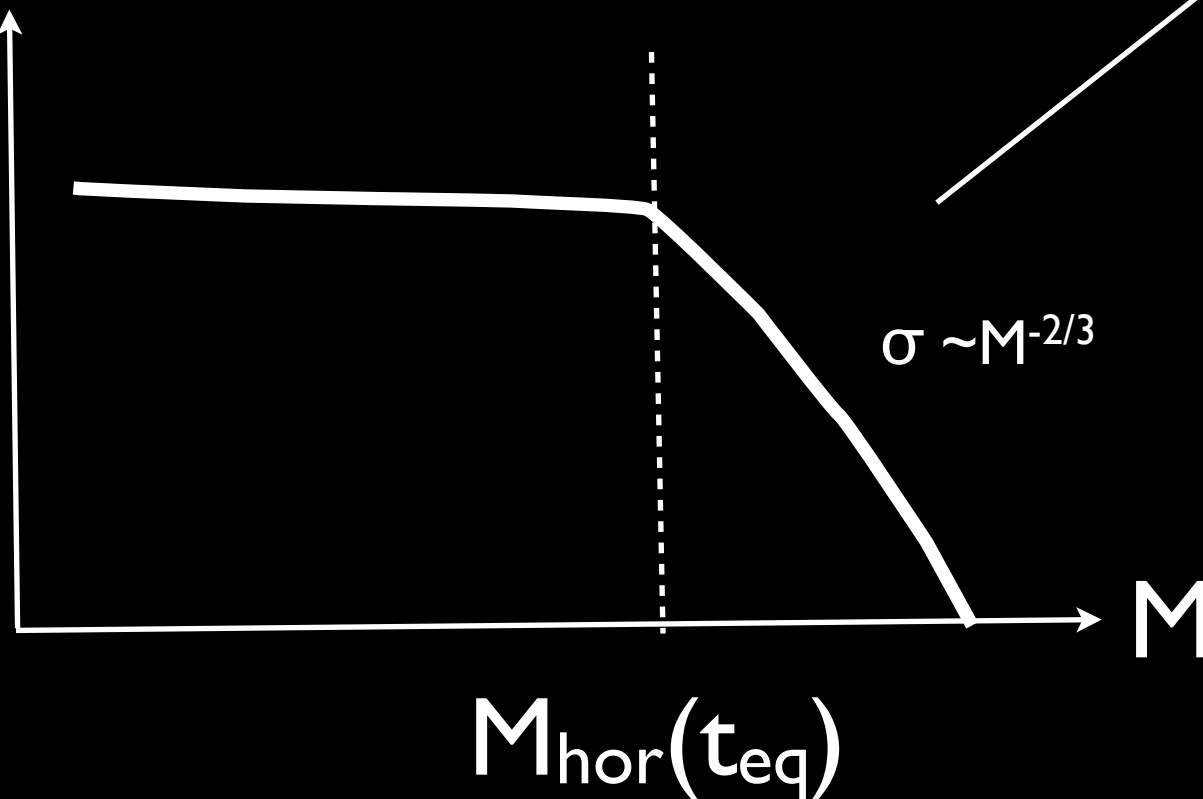
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$\log \sigma$

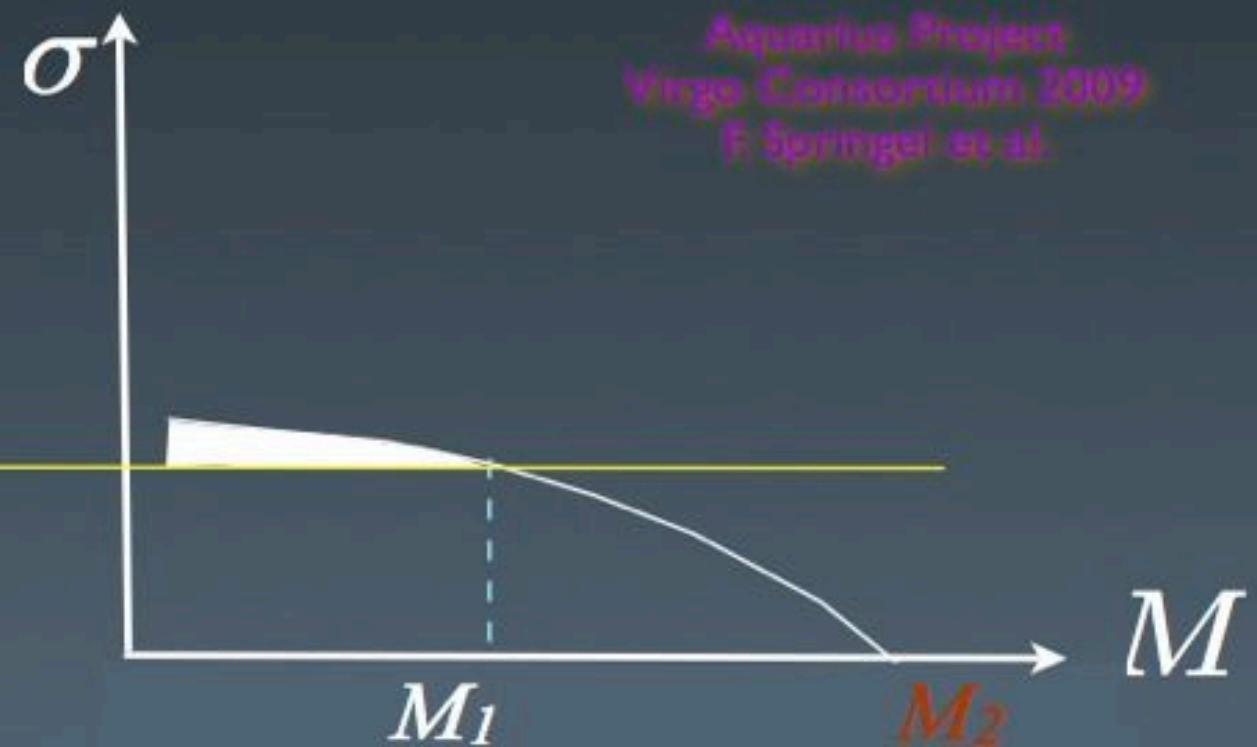
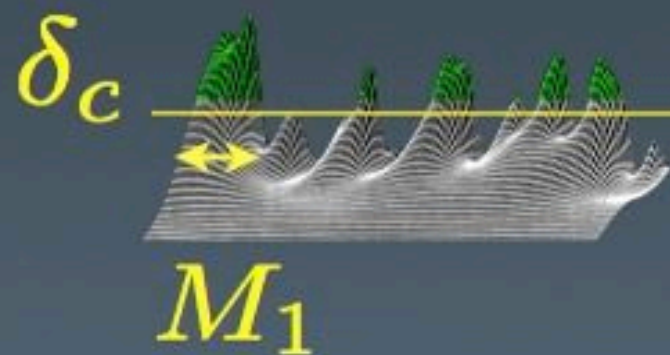


The evolution of DM perturbation

Initial density perturbations constitute a random Gaussian field.

Measurements of the CMB show that its variance is inversely related to their mass scale.

This implies that small scales collapse - on average - at earlier times

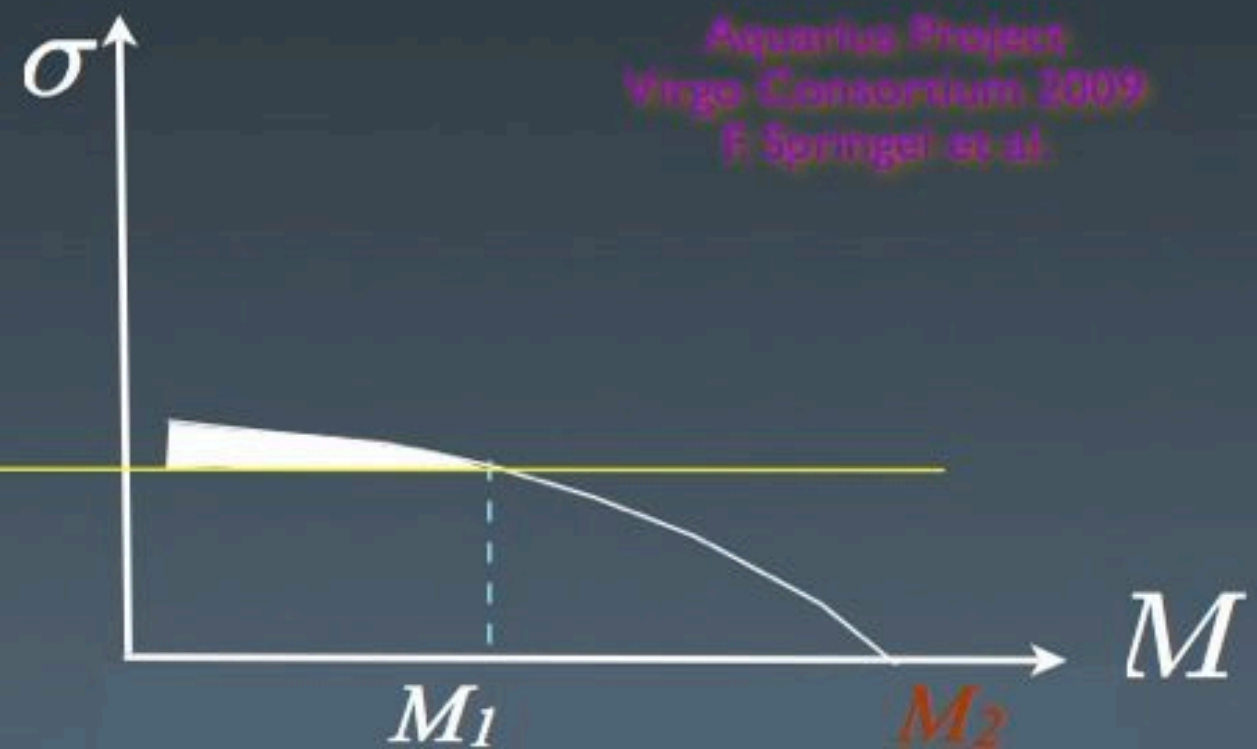
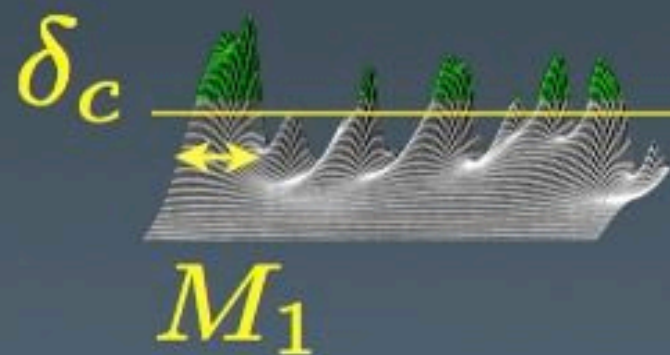


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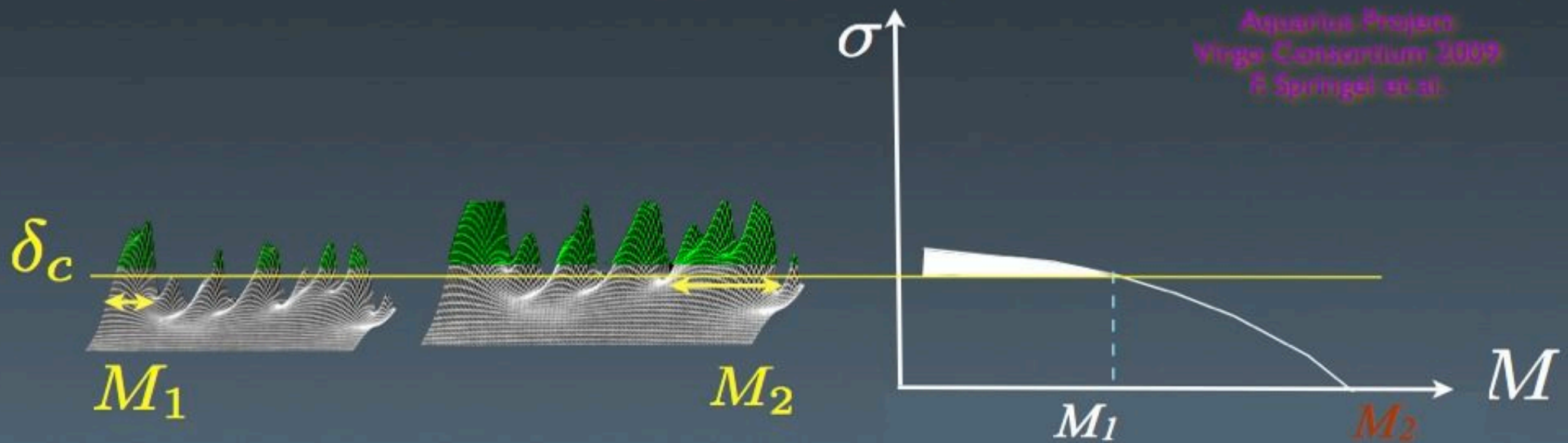


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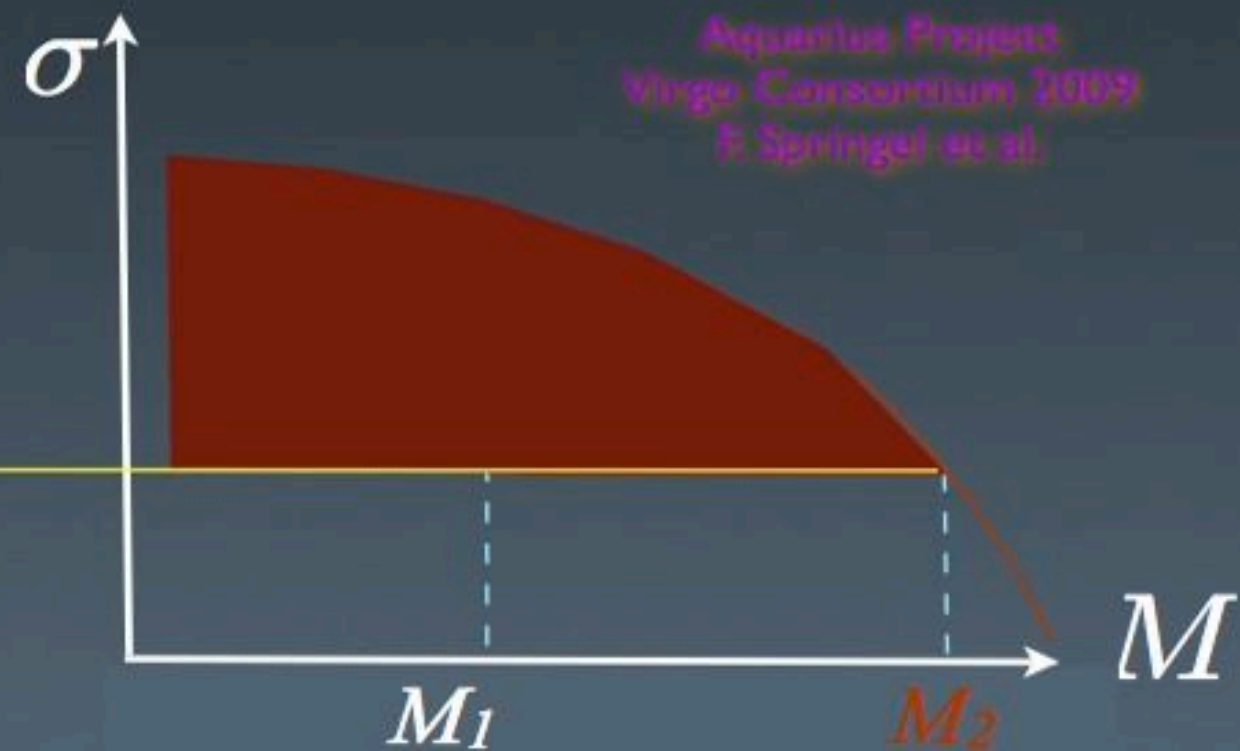
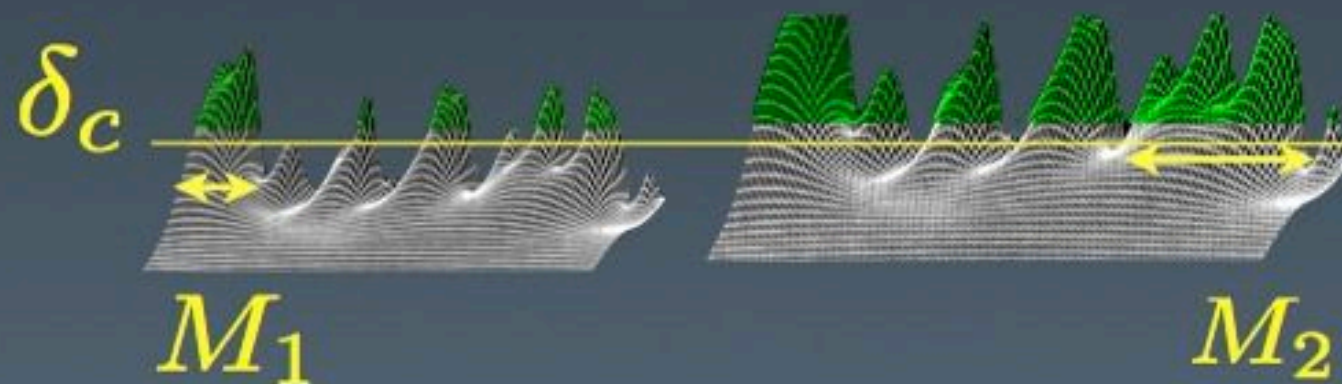


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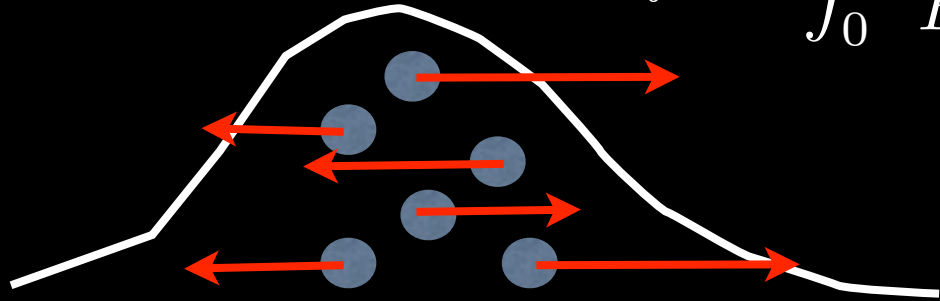
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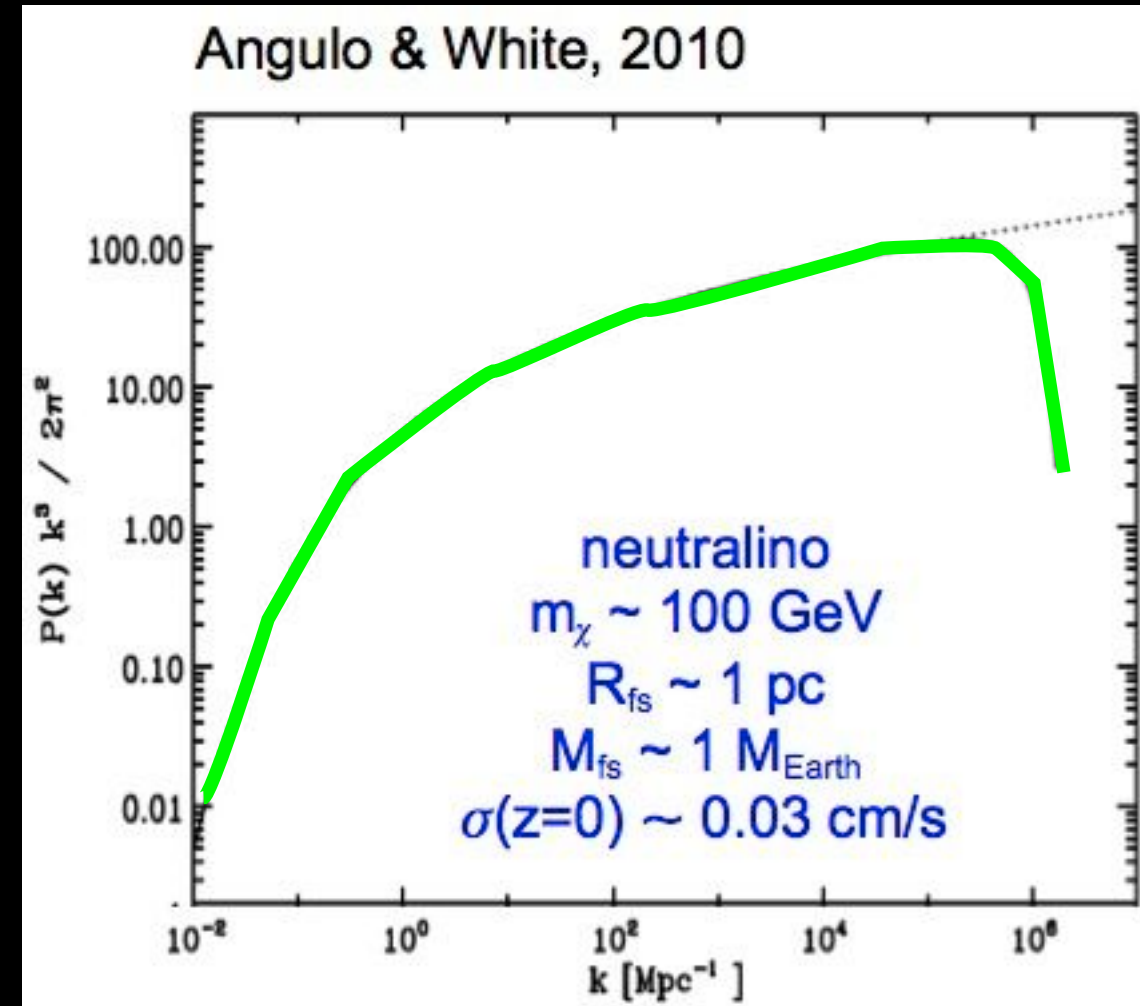
Dissipation, free-streaming scale

$$r_{fs} = \int_0^t \frac{v(t)}{R(t)} dt$$

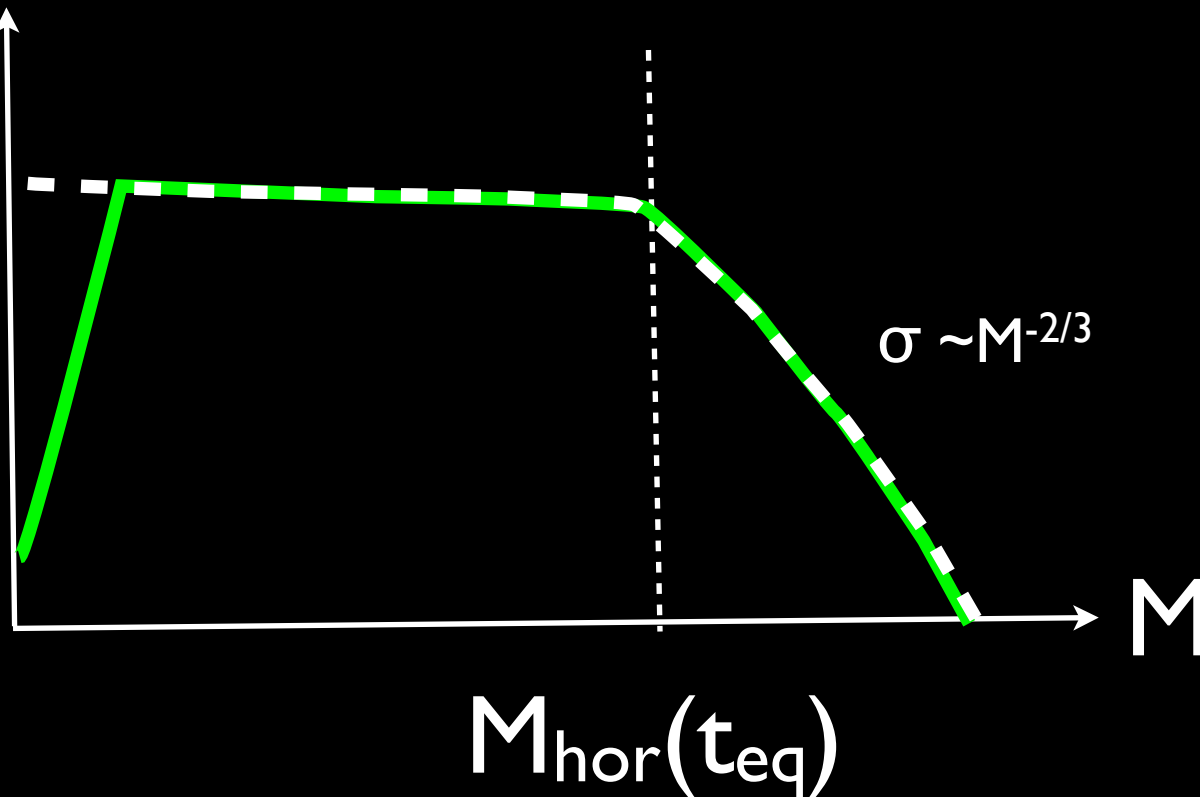


$$\sigma_\chi \propto a^{-1} m_\chi^{-1/2}$$

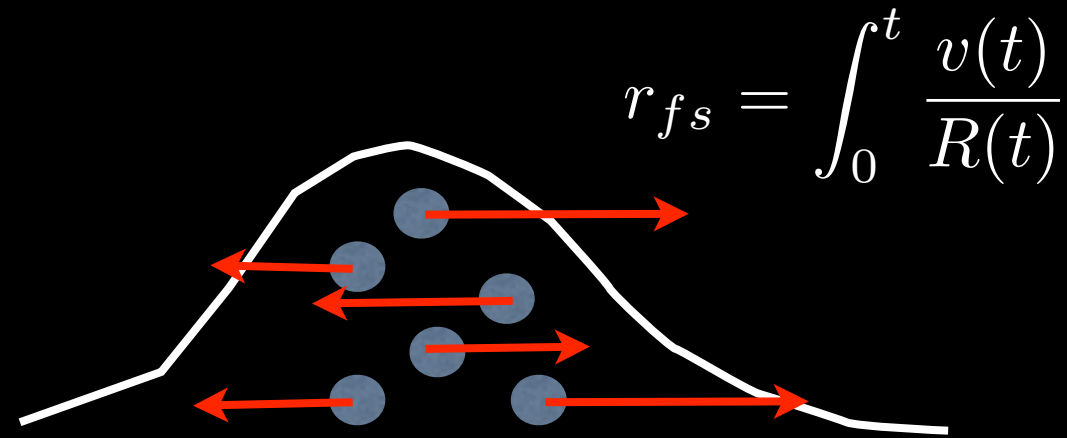
$$M_{fs} = 4 \times 10^{15} \left(\frac{m_\nu}{30 \text{ eV}} \right)^{-2} M_\odot$$



$\log \sigma$

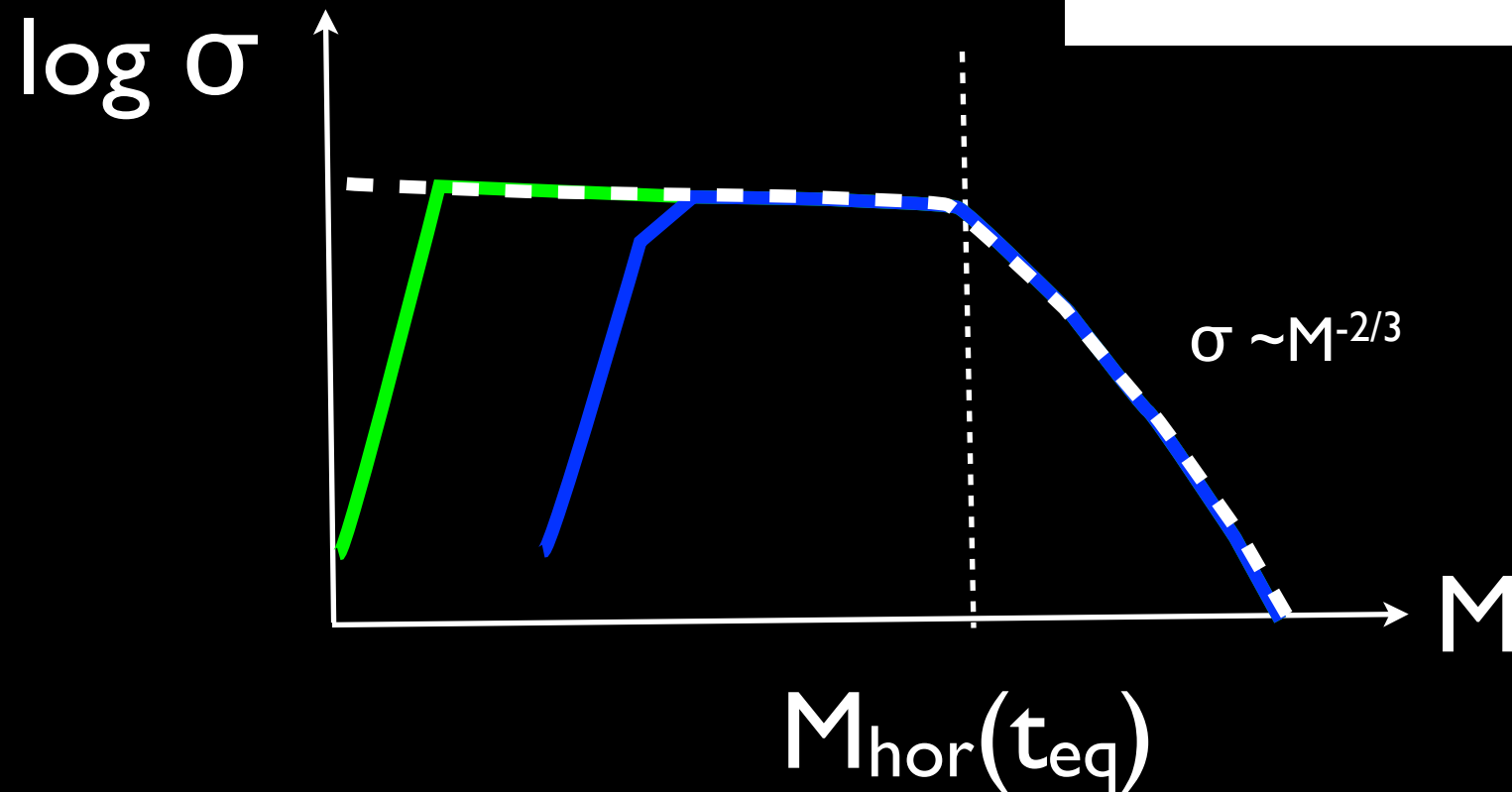
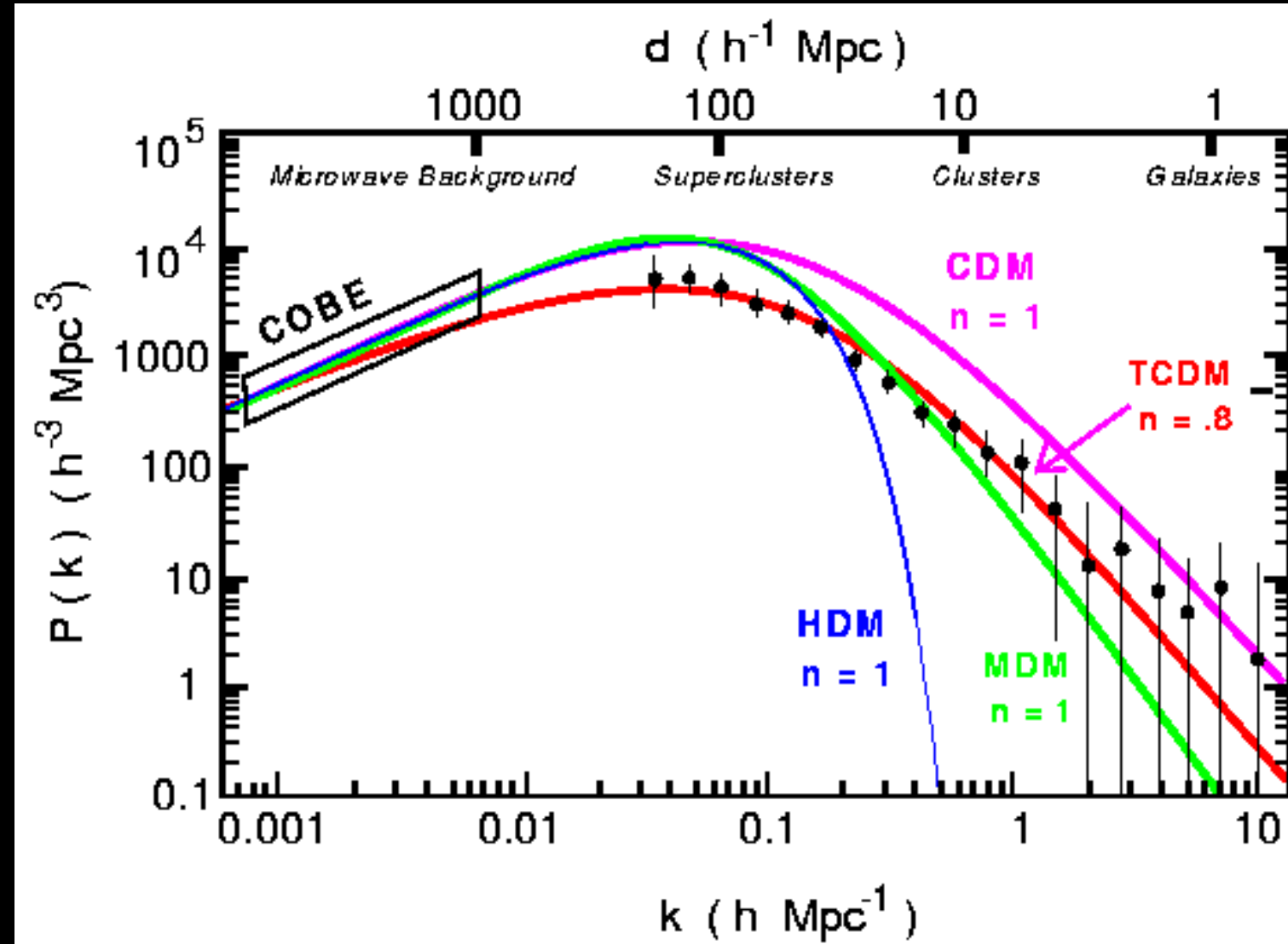


Dissipation, free-streaming scale

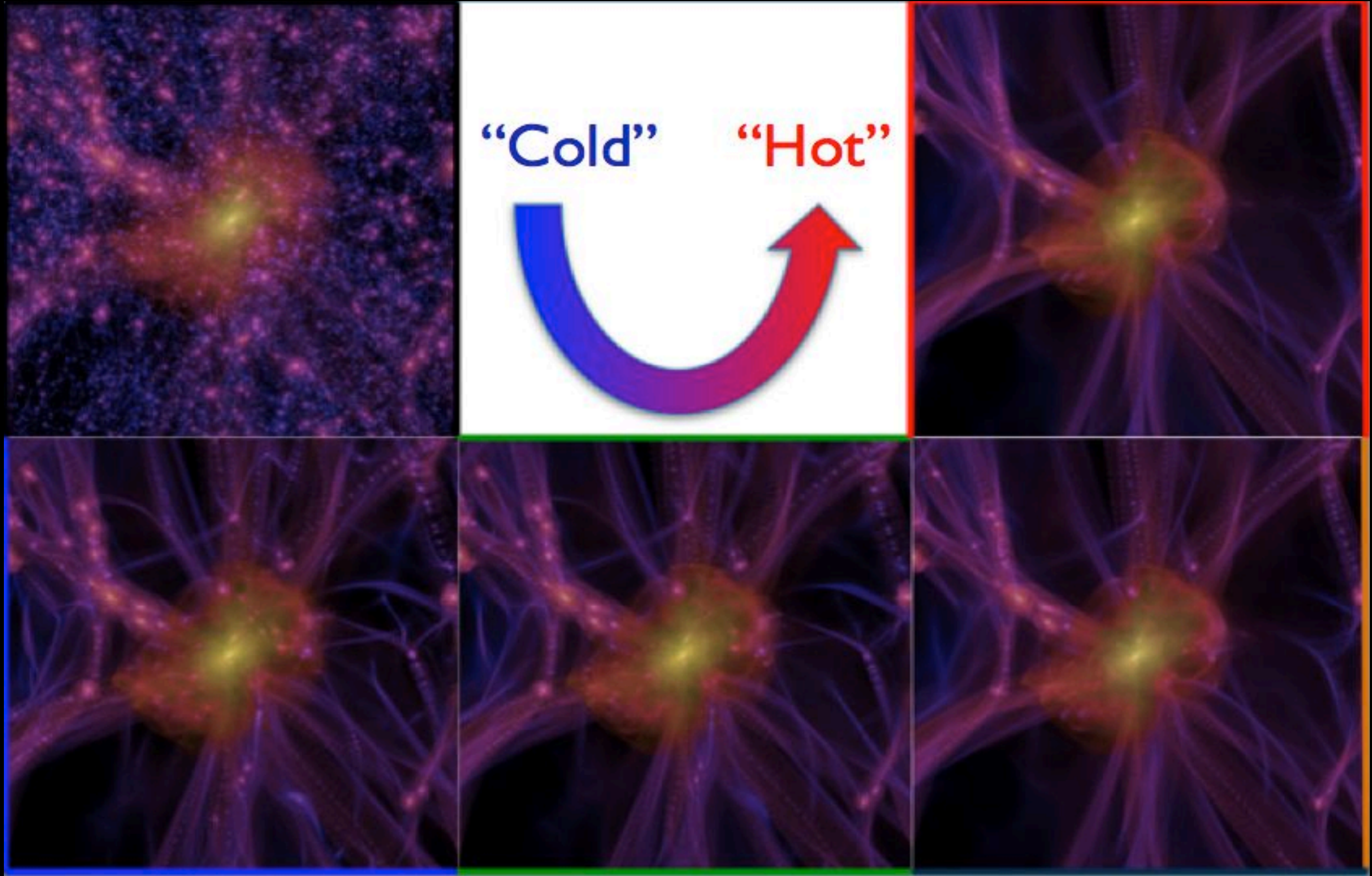


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Varying the particle mass



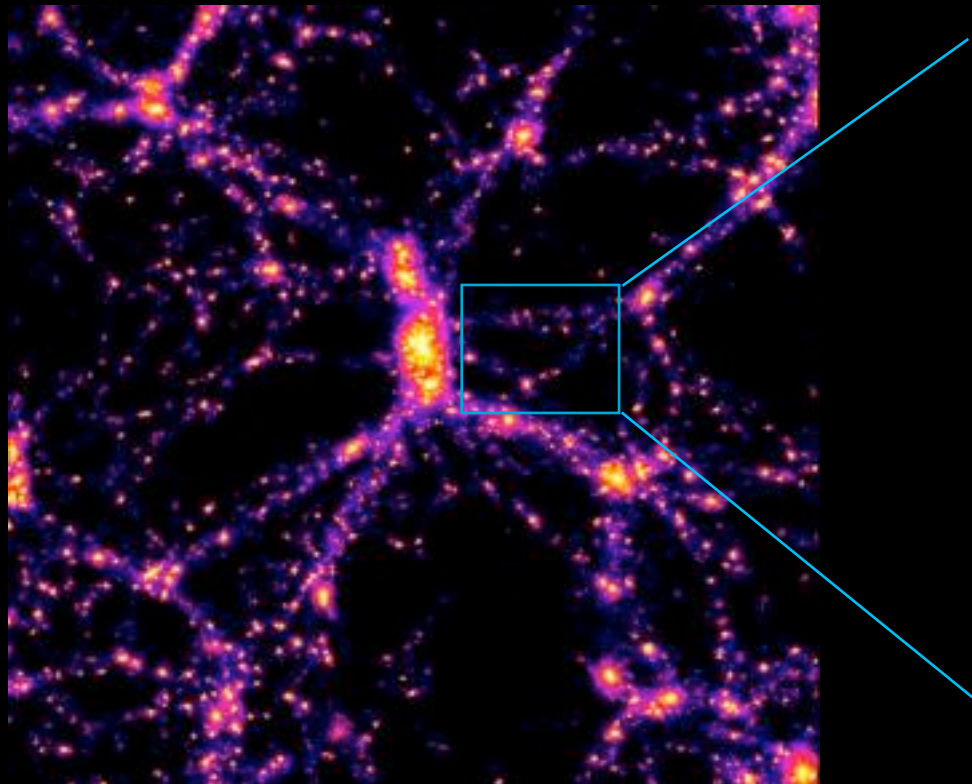
What' so cold about CDM

For “thermal relics” such as neutrinos, it is relatively straightforward to compute their present day abundance.
Neutrinos relativistic at decoupling → large velocity dispersion.

Candidates for “Hot Dark Matter” -- ruled out by observation.

CDM: Velocity dispersion assumed to be vanishingly small

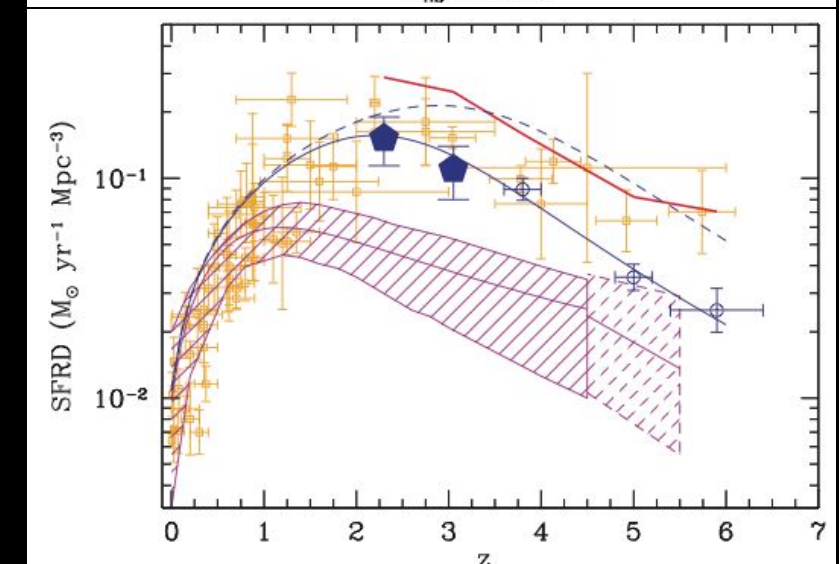
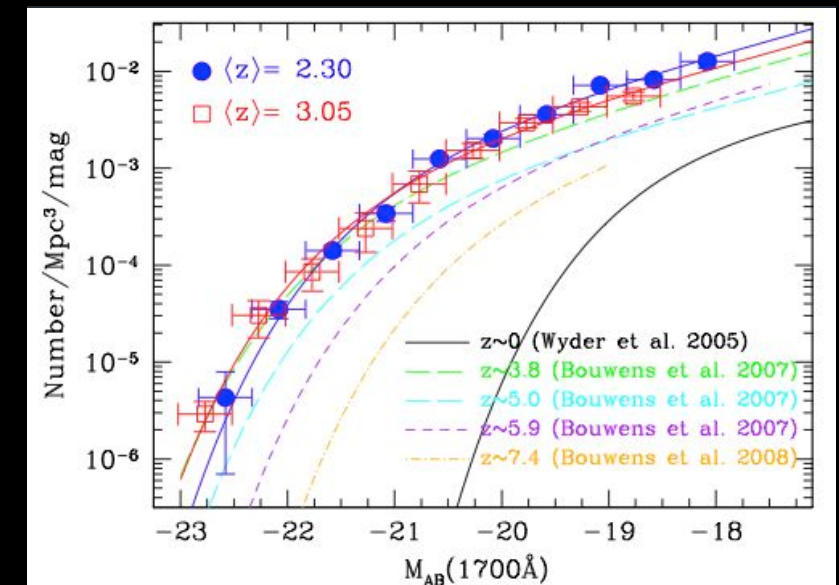
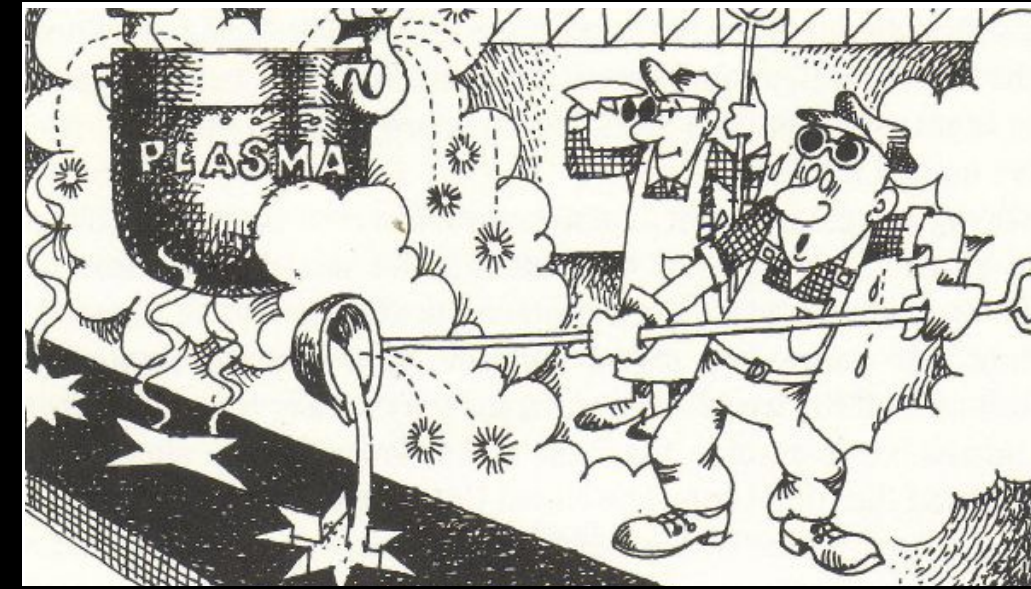
limit $M_{fs} \ll$ Masses of Cosmological Relevance



Testing the COLD DARK MATTER scenario against observations: the evolution of galaxies

Requires modelling of baryon physics inside evolving DM potential wells

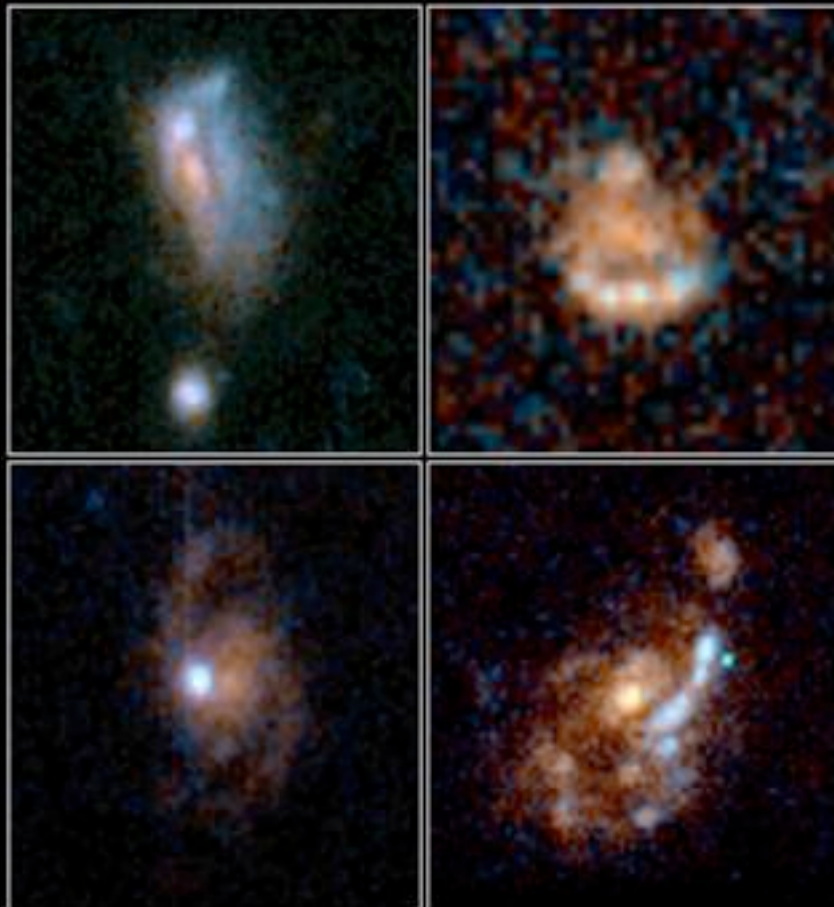
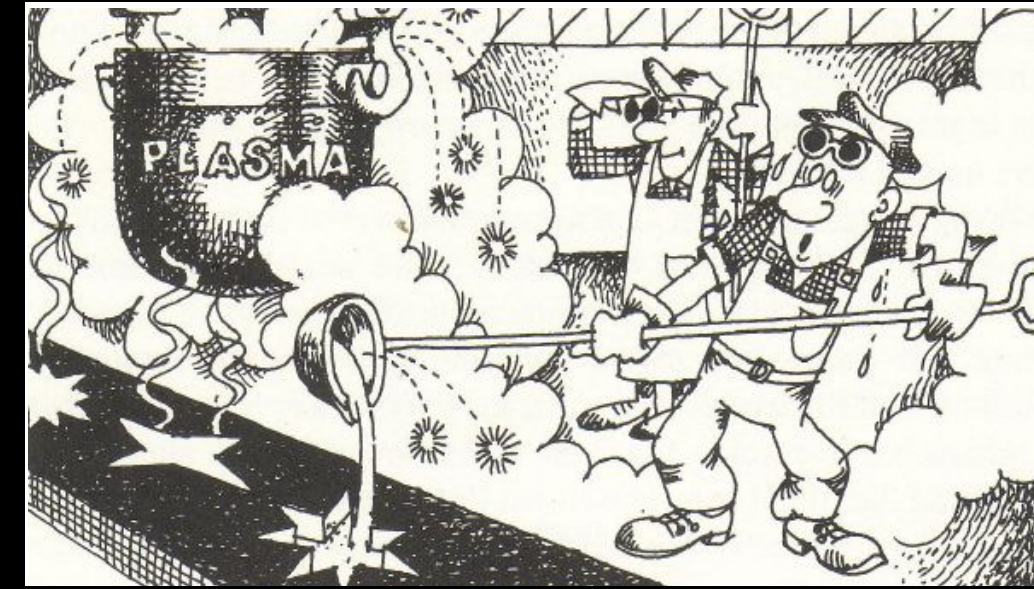
- gas physics (cooling, heating)
- disk formation
- star formation
- evolution of the stellar population
- injection of energy into the gas from SNe



Testing the COLD DARK MATTER scenario against observations: the evolution of galaxies

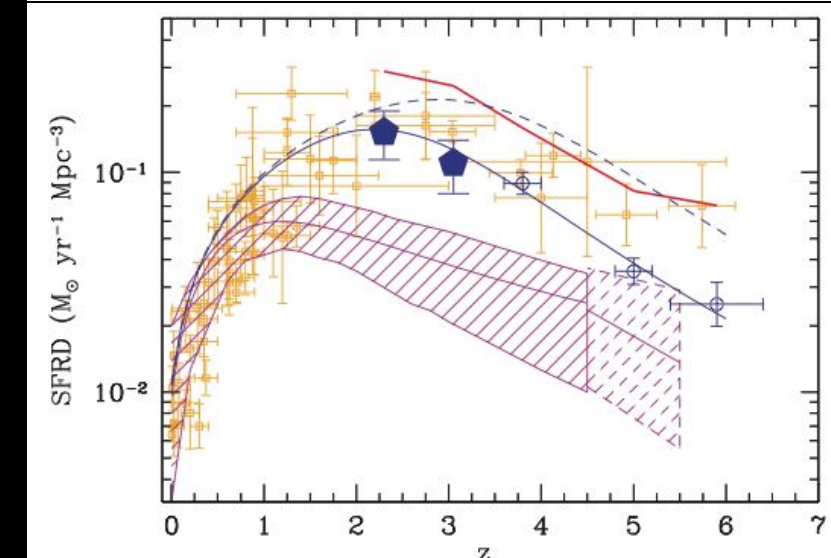
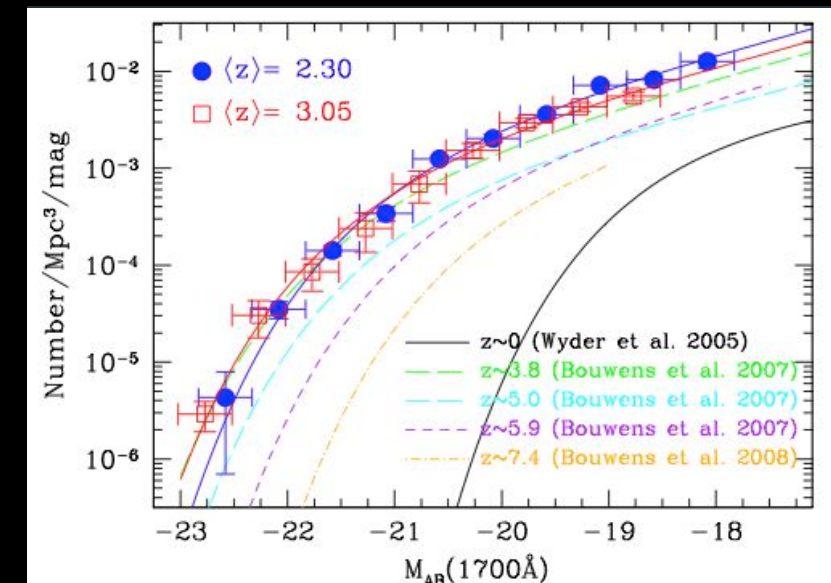
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Medium Deep Survey

HST · WFPC2



Galaxy Formation in a Cosmological Context

Hydrodynamical N-body simulations

Pros

include hydrodynamics of gas
contain spatial information

Cons

numerically expensive
(limited exploration of parameter space)
requires sub-grid physics

Semi-Analytic Models Monte-Carlo realization of collapse and merging histories

Pros

Physics of baryons linked to DM halos
through scaling laws, allows a fast spanning
of parameter space

Cons

Simplified description of gas physics
Do not contain spatial informations

Galaxy Formation in a Cosmological Context

Semi-Analytic Models Monte-Carlo realization of collapse and merging histories

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Sub-Halo dynamics:
dynamical friction, binary aggregation

Halo Properties
Density Profiles
Virial Temperature

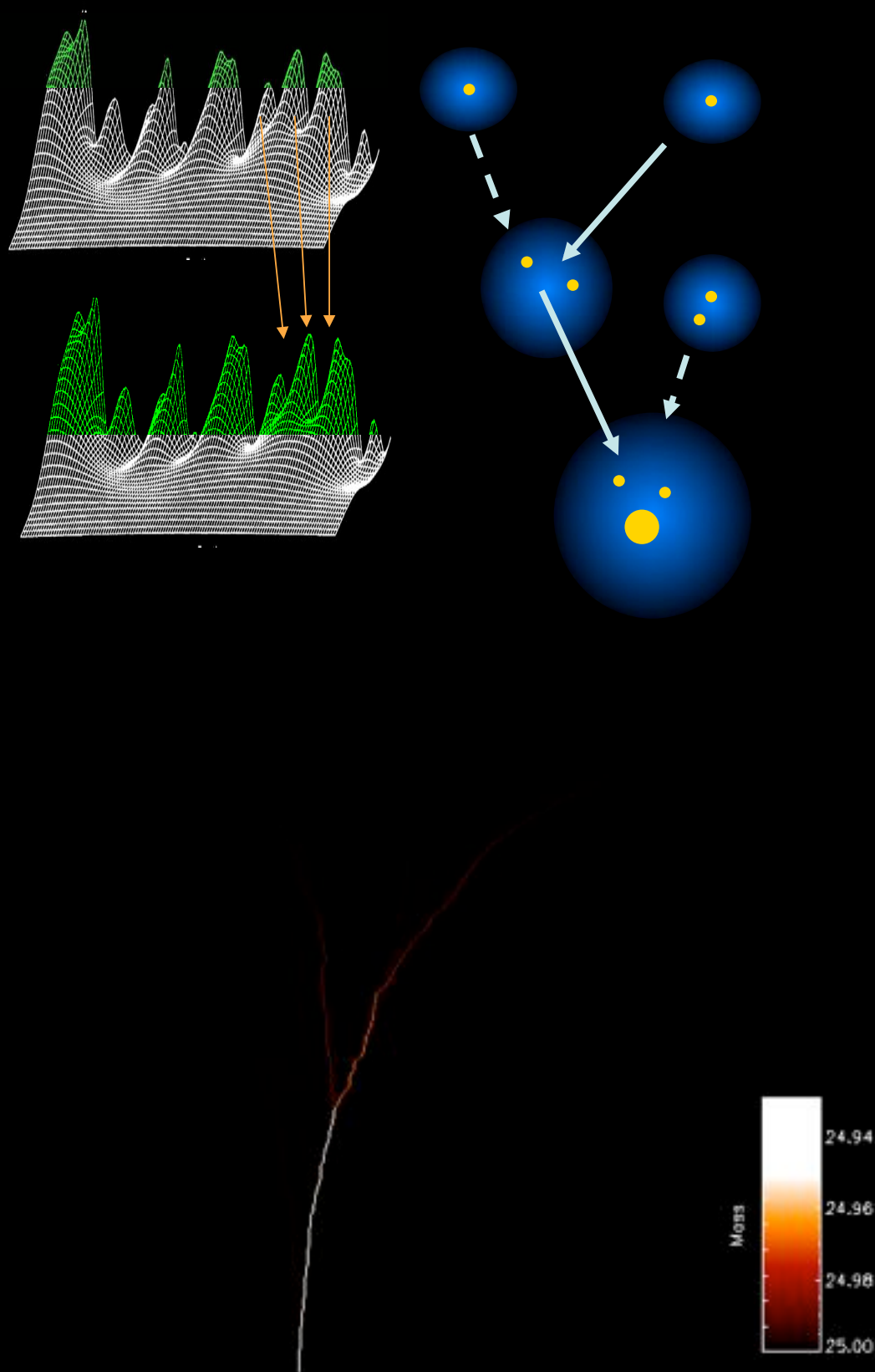
Gas Properties
Profiles
Cooling - Heating Processes
Collapse, disk formation

Star Formation Rate

Gas Heating (feedback)
SNe
UV background

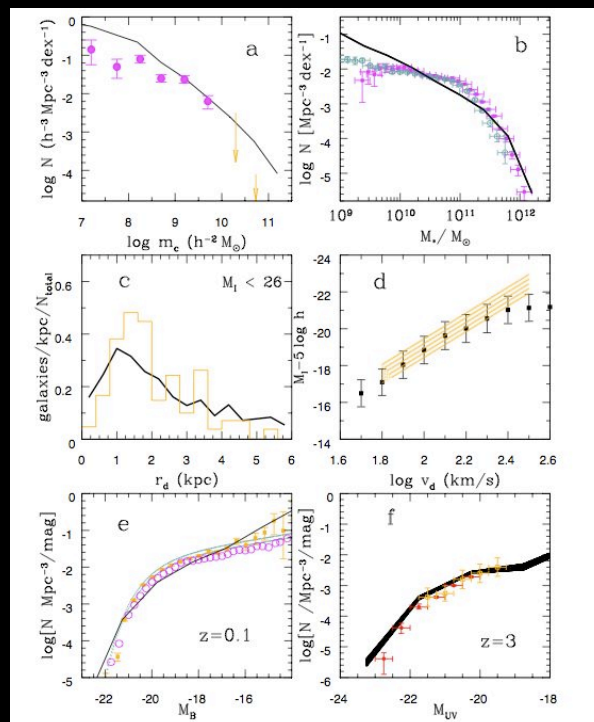
Evolution of stellar populations

Growth of Supermassive BHs
Evolution of AGNs



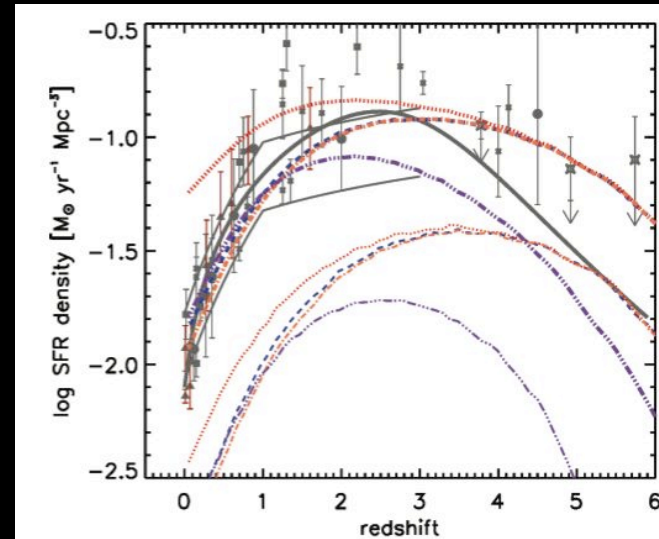
Galaxy Formation models in CDM scenario

Local properties:
 gas content
 luminosity distribution
 disk sizes
 distribution of the stellar
 mass content

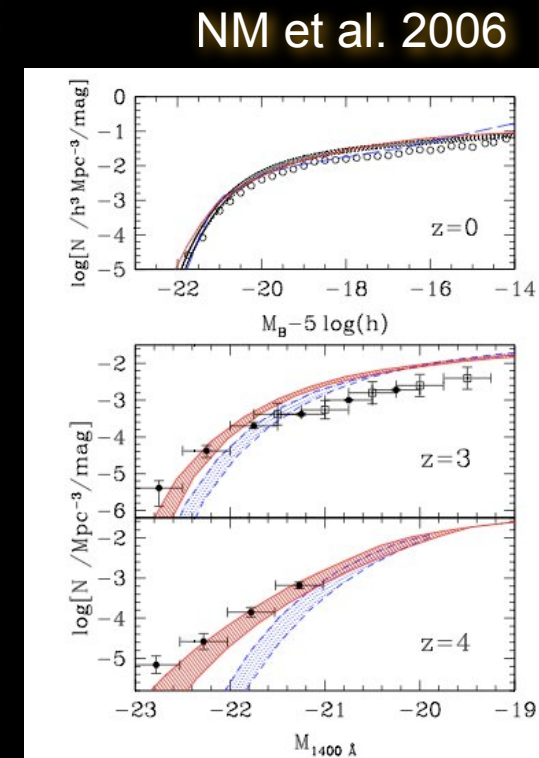


NM et al. 2006

properties of distant galaxies:
 luminosity distribution
 evolution of the star formation rate

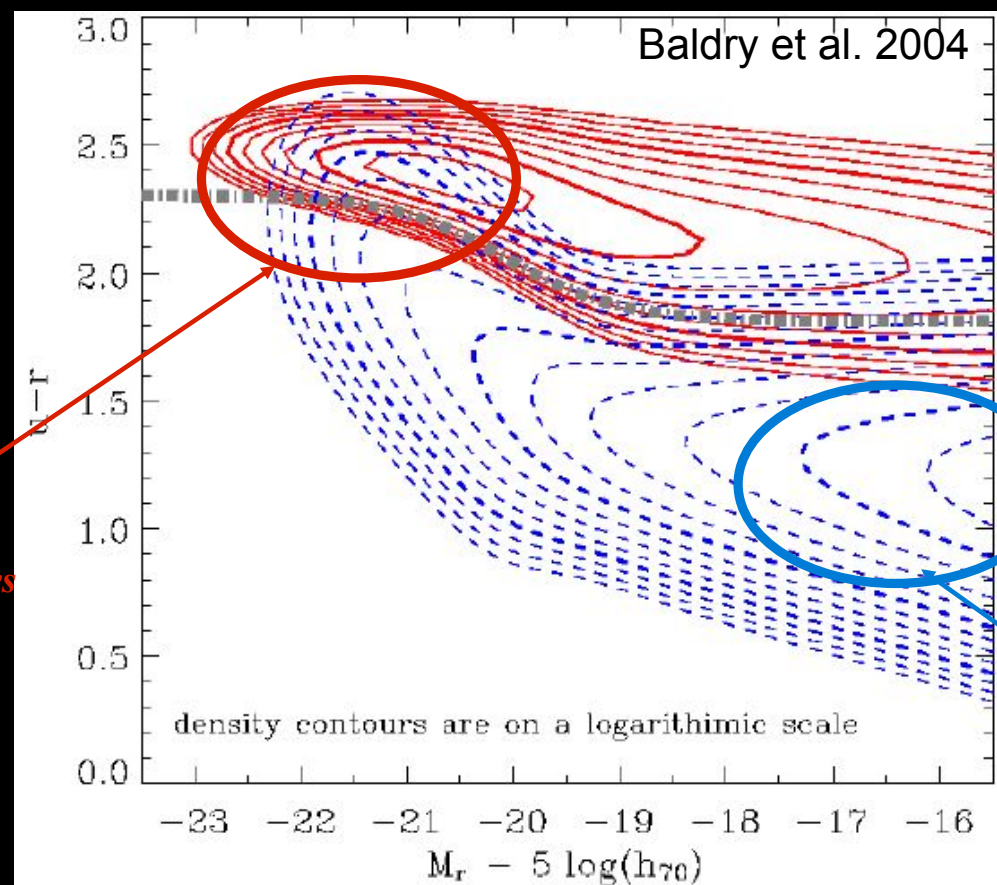


Somerville et al. 2010

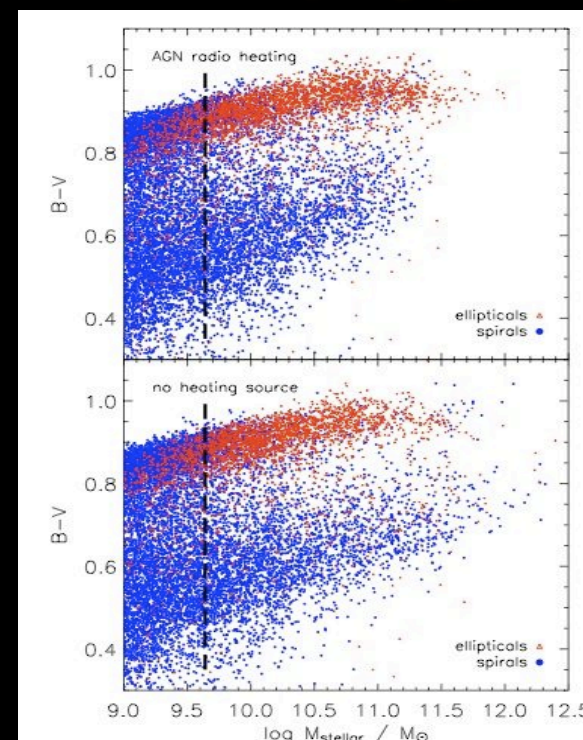


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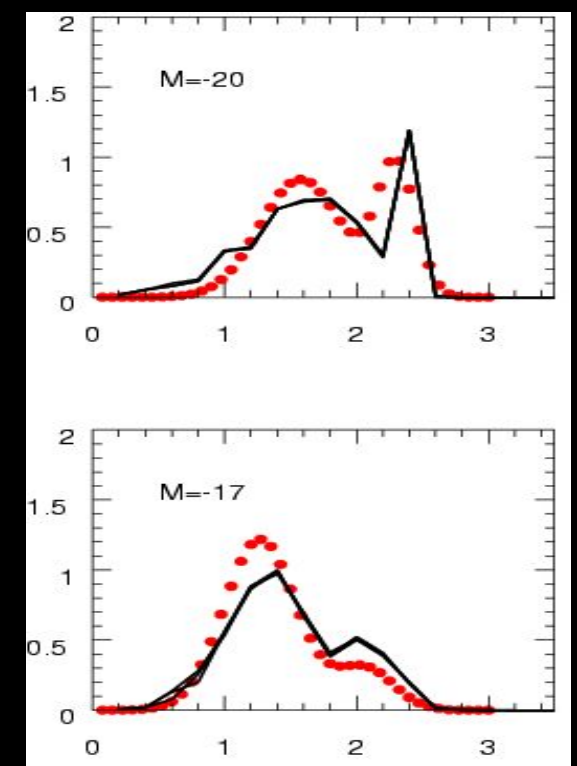
Color Distributions: bimodal
 distribution (early type vs late type)



Baldry et al. 2004



Croton et al. 2006



NM et al. 2008

Critical Issues

Overabundance of low-mass objects

- i) satellite DM haloes
- ii) density profiles
- iii) abundance of faint galaxies
- iv) abundance of faint AGN

Critical Issues

i) satellite DM haloes

Via Lactea simulation of a Milky Way - like galaxy
Diemand et al. 2008



CDM Substructure in simulated cluster and galaxy haloes look similar.

Expected number of satellites in Milky Way- like galaxies in CDM largely exceeds the observed abundance.



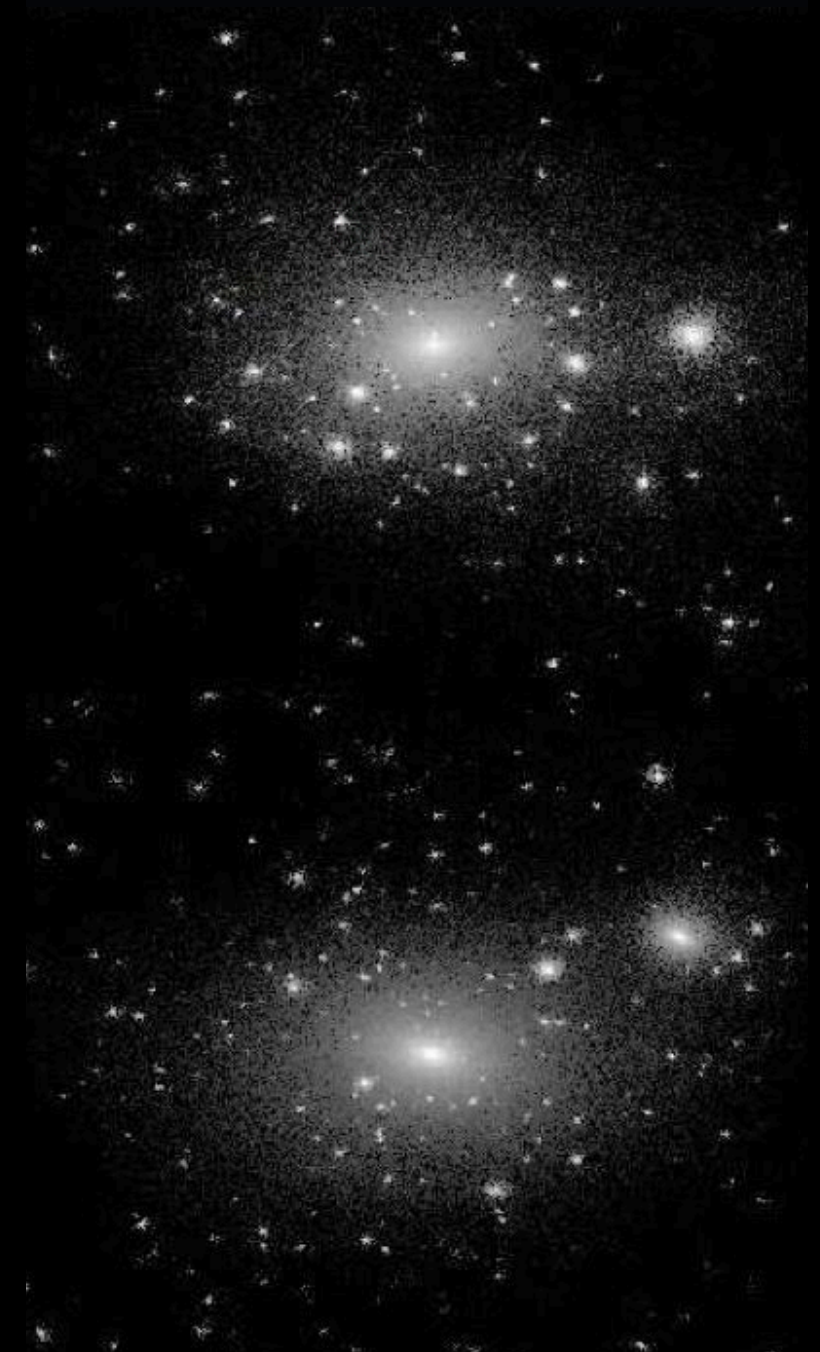
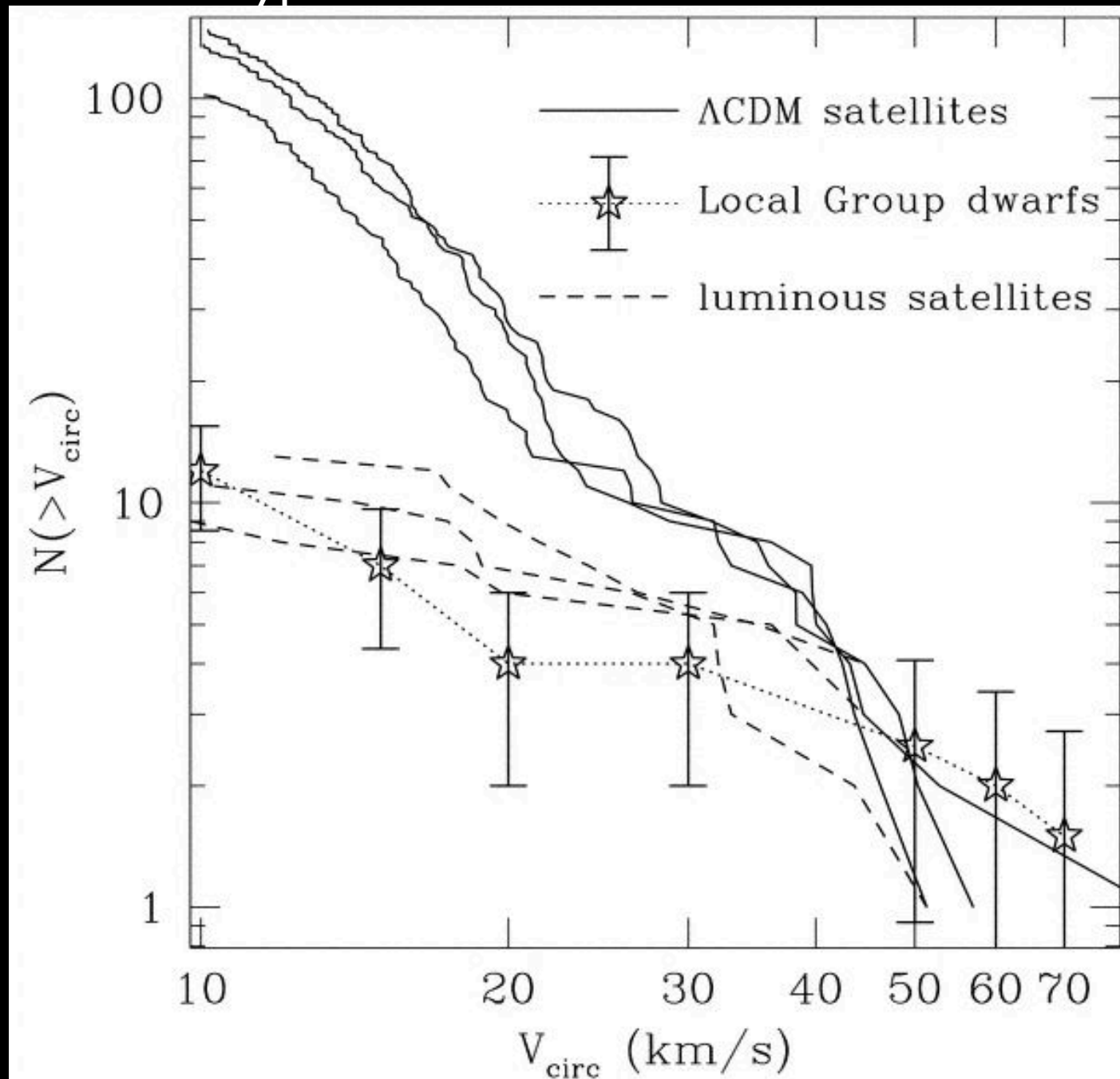
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Kravtsov, Klypin, Gnedin 2004

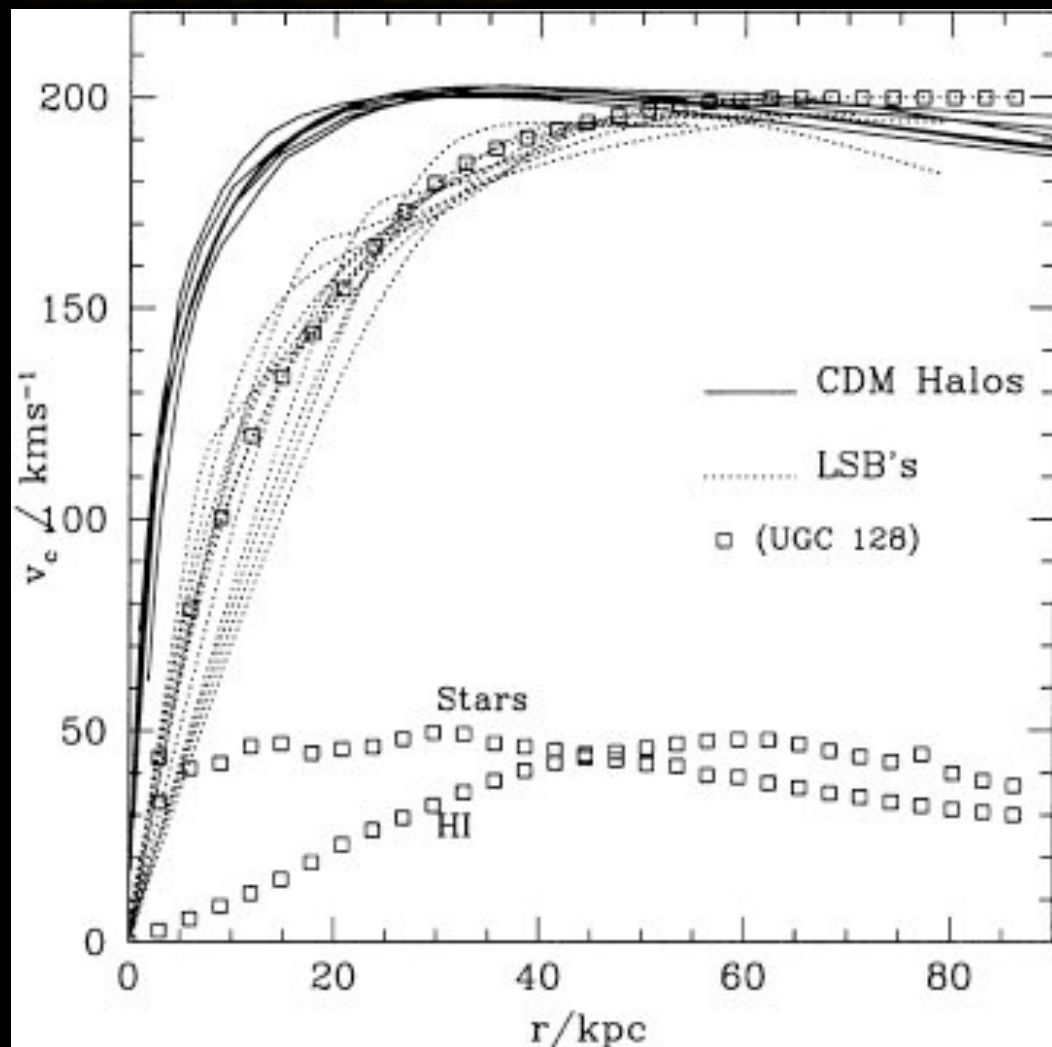


Critical Issues

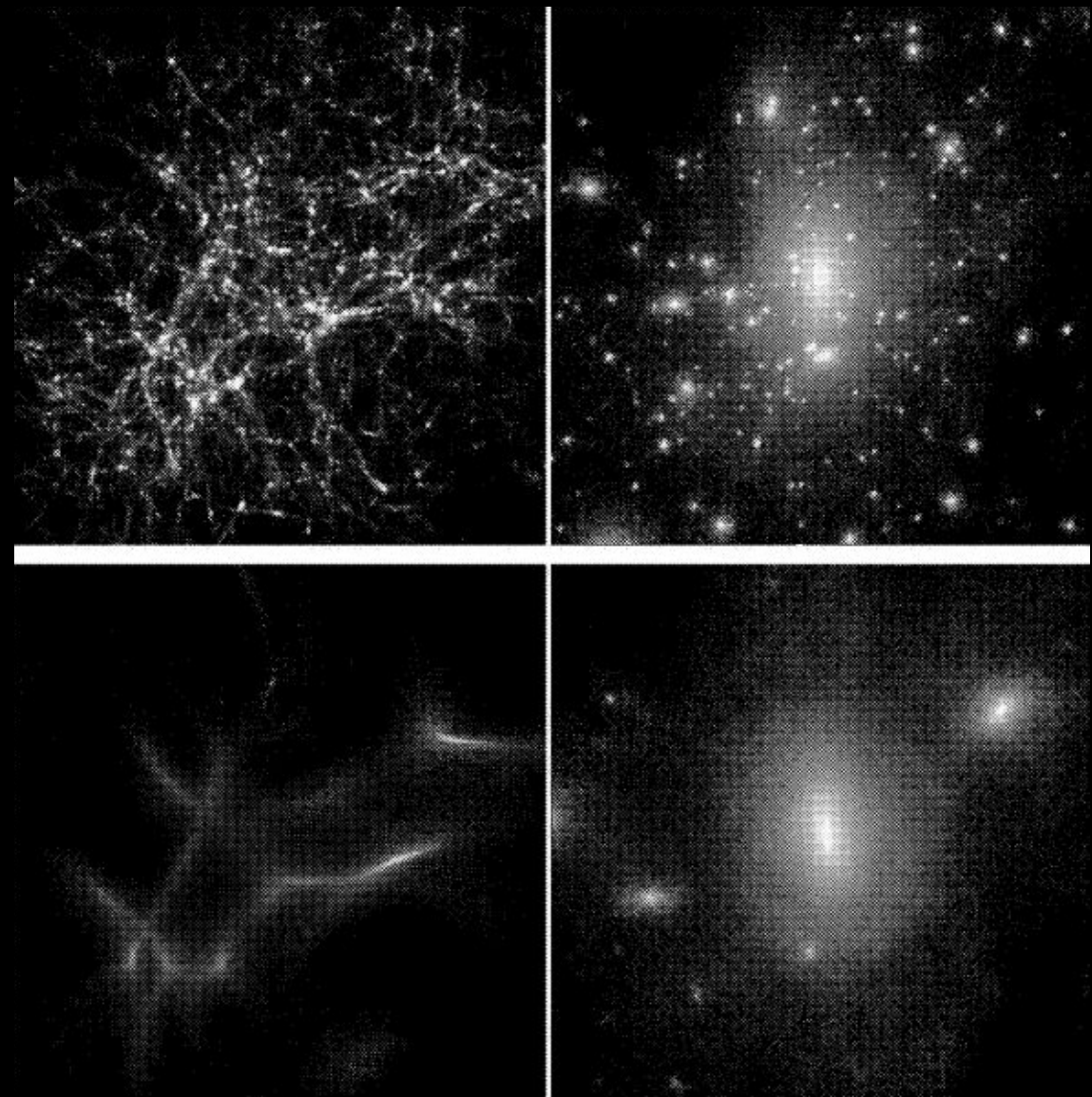
ii) density profiles

Most observed dwarf galaxies consist of a rotating stellar disk embedded in a massive dark-matter halo with a near-constant-density core. Models based on the dominance of CDM, however, invariably form galaxies with dense spheroidal stellar bulges and steep central dark-matter profiles, because low-angular-momentum baryons and dark matter sink to the centres of galaxies through accretion and repeated mergers.

Moore et al. 2002

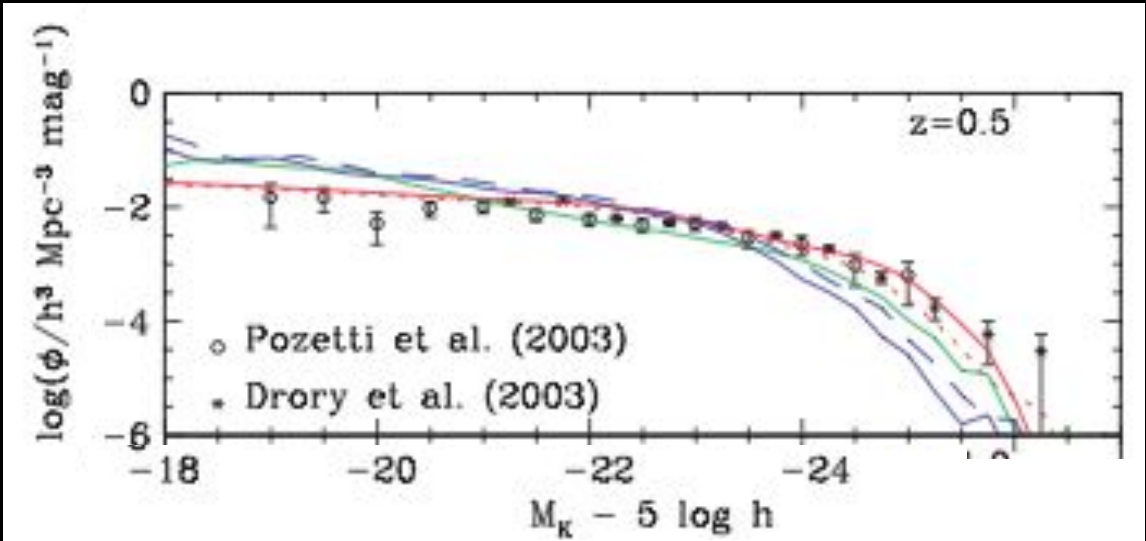


The effect of adopting a cutoff
in the power spectrum for $r < 8$ Mpc

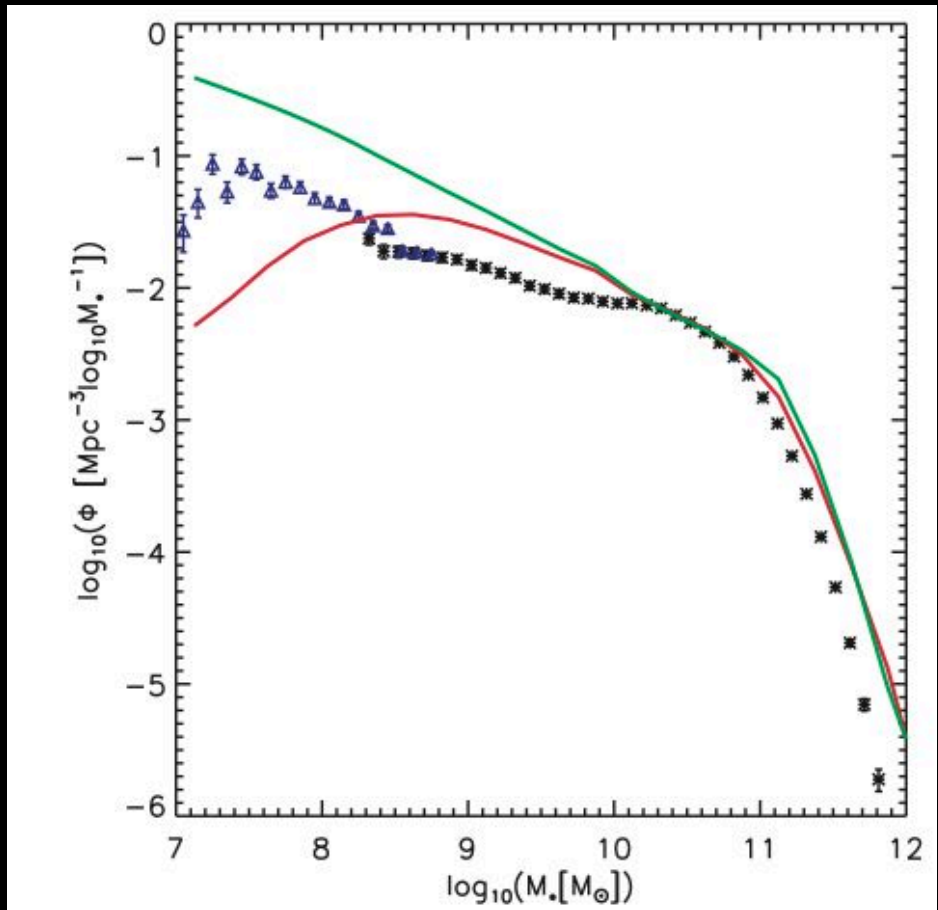


Critical Issues

iii) over-prediction of faint galaxies



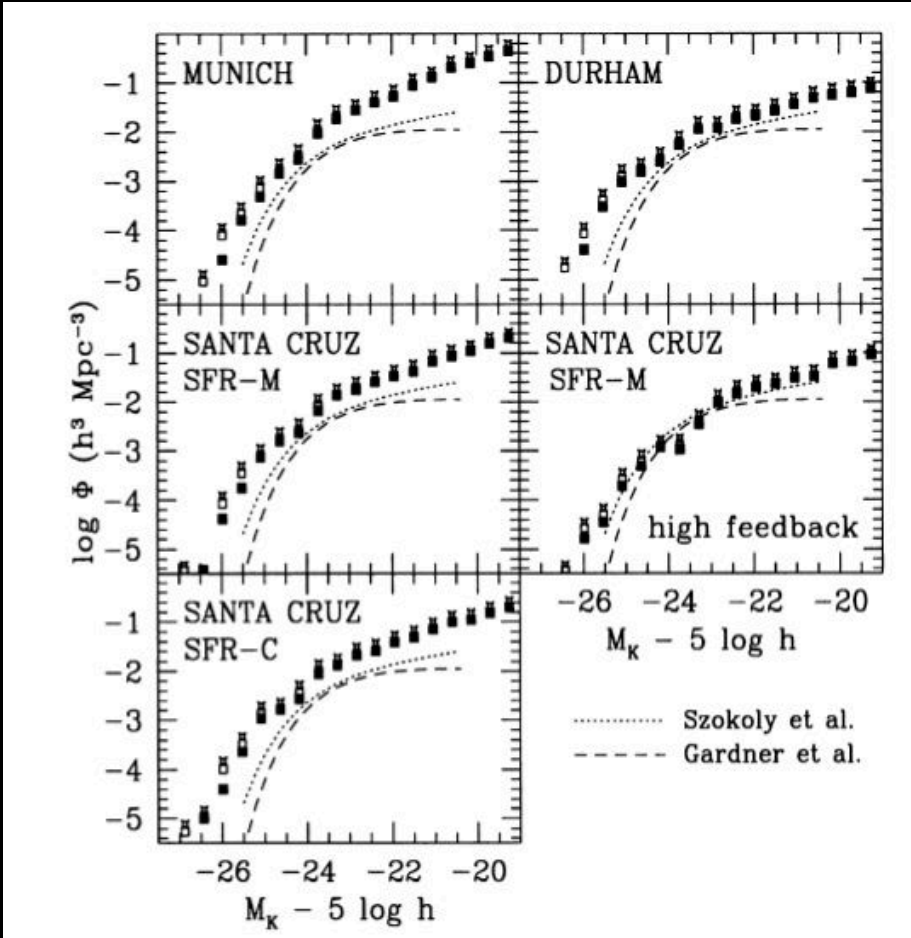
Bower et al. 2006



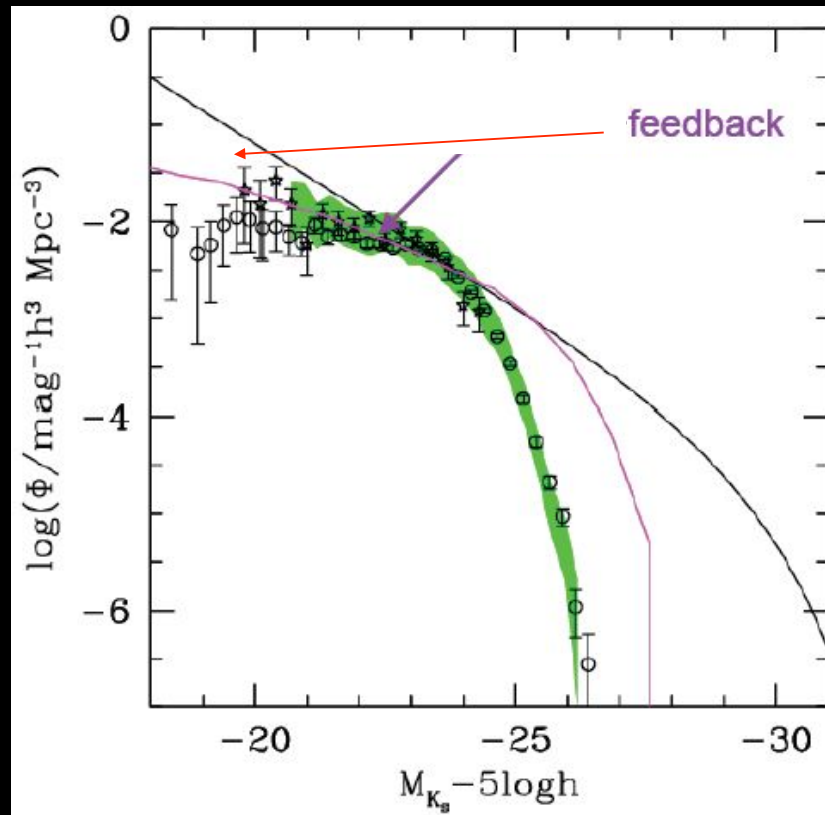
The Stellar Mass Function in the De Lucia et al. SAM based on Millenium merger trees

In all first-generation SAM the number density of faint (low-mass) galaxies was over-predicted

The K-Band Luminosity Function in the Somerville et al. SAM



A first-order solution: feedback and UV background



The origin of the problem:

The DM halo Mass function has a steep log slope $N \sim M^{-1.8}$
While the Observed Galaxy Luminosity Function has a much flatter slope $N \sim L^{-1.2}$

A Possible Solution:

Suppress luminosity (star formation) in low-mass haloes
Heat - Expell Gas from shallow potential wells

- Enhanced SN feedback
- UV background

$$E_{SN} \approx 10^{51} \eta_0 \eta_{IMF} \Delta M_* \text{ erg/s}$$

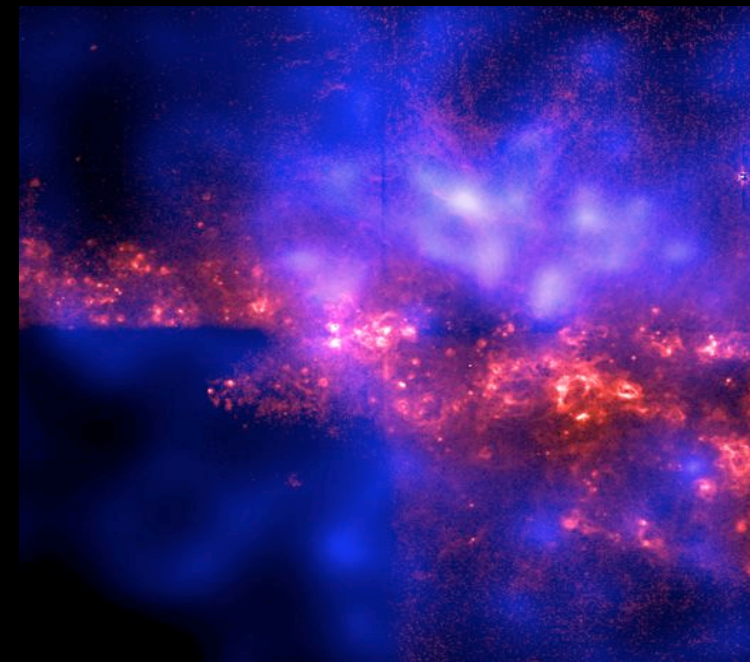
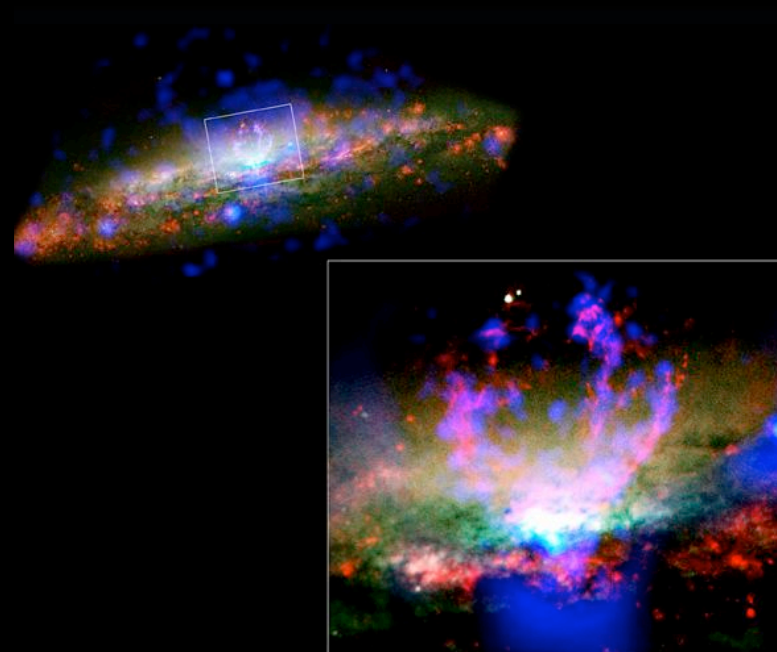
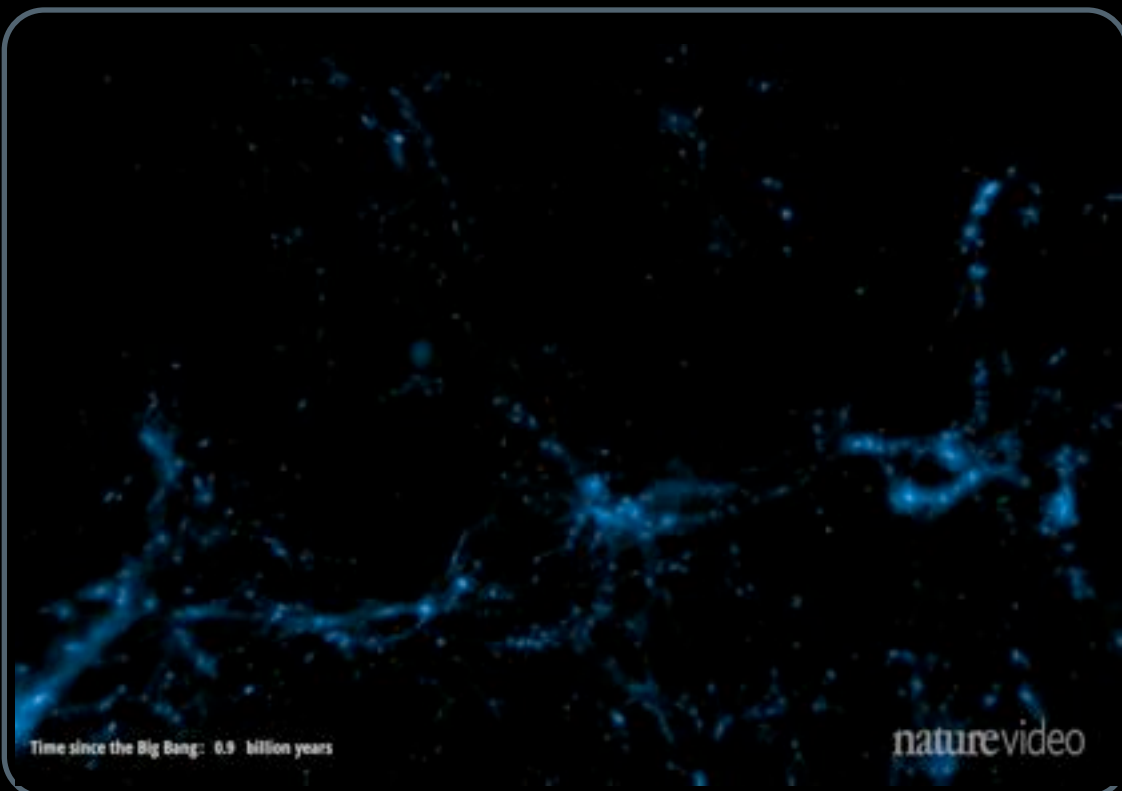
Mass scale at which
SN can effectively expell gas from
DM potential wells

$$v_{esc} = \sqrt{E_{SN}/M_{gas}} \approx 100 \text{ km/s}$$

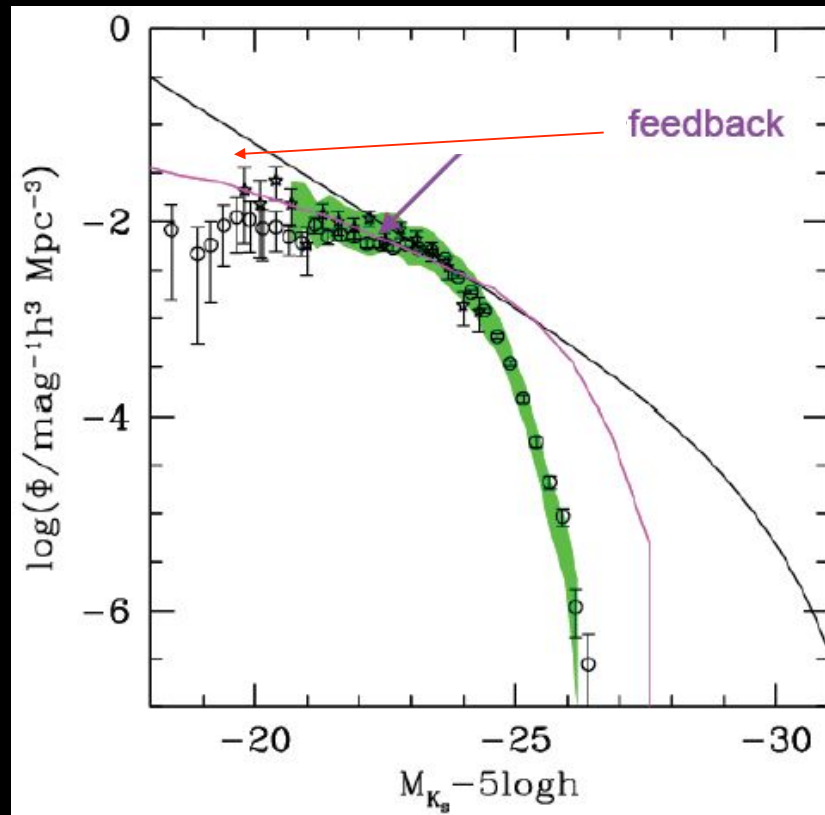
$$M_{SN} \sim 10^{10} M_{\odot}$$

at low z, att higher redshift the
density is higher an M_{SN} increases

Vogelsberger et al. 2014



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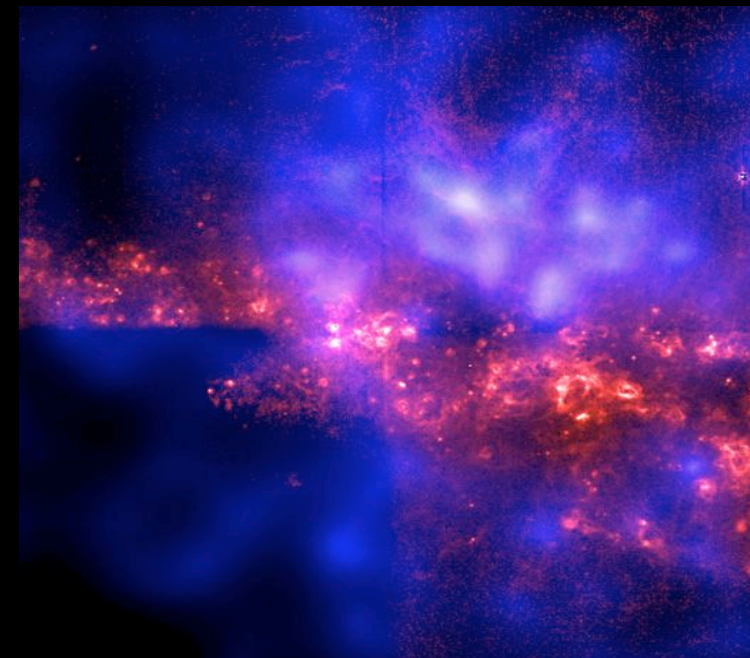
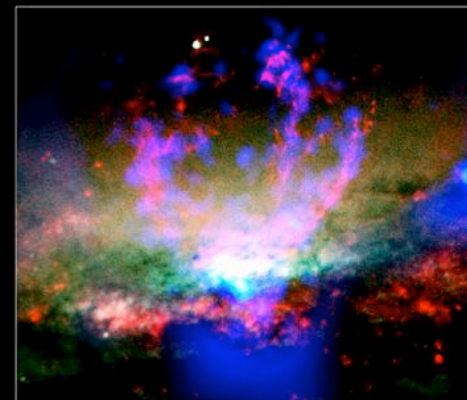
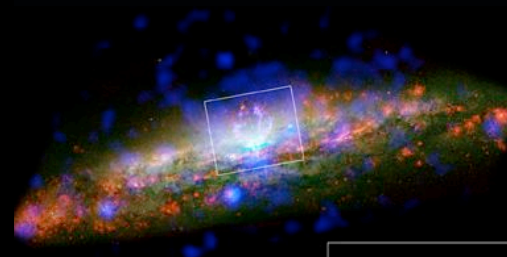
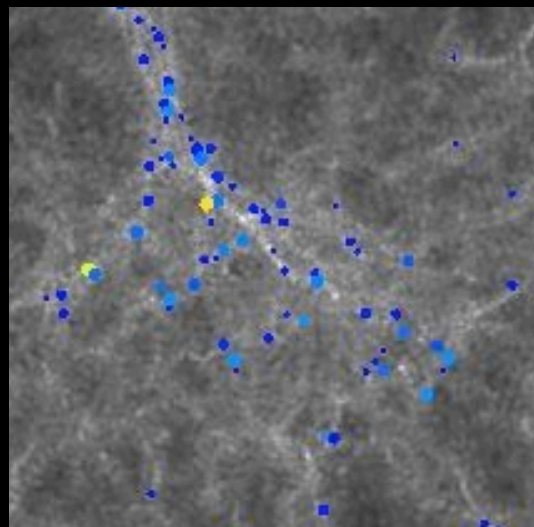
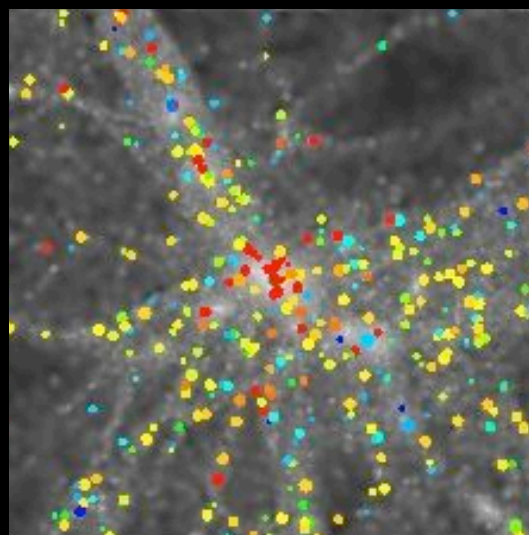
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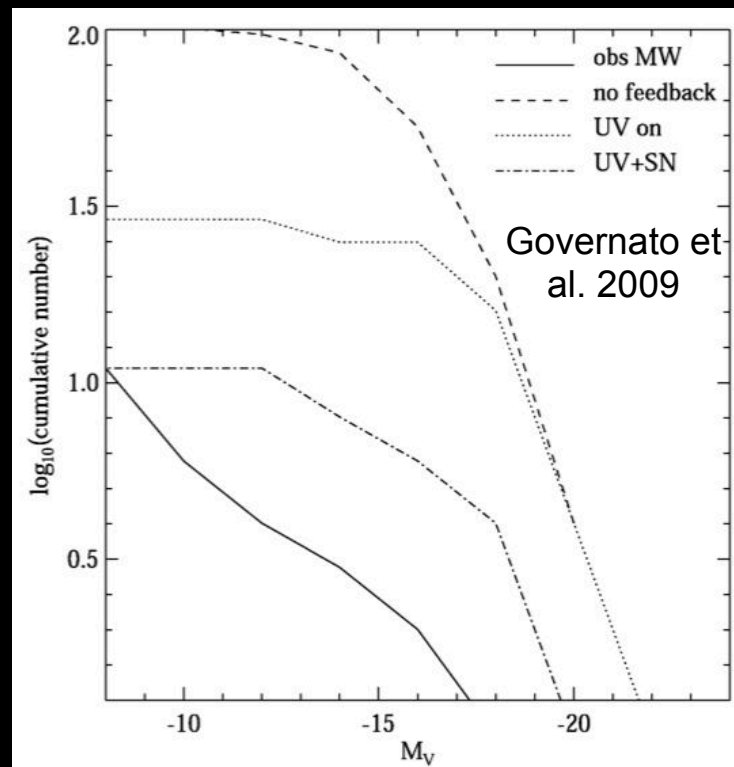
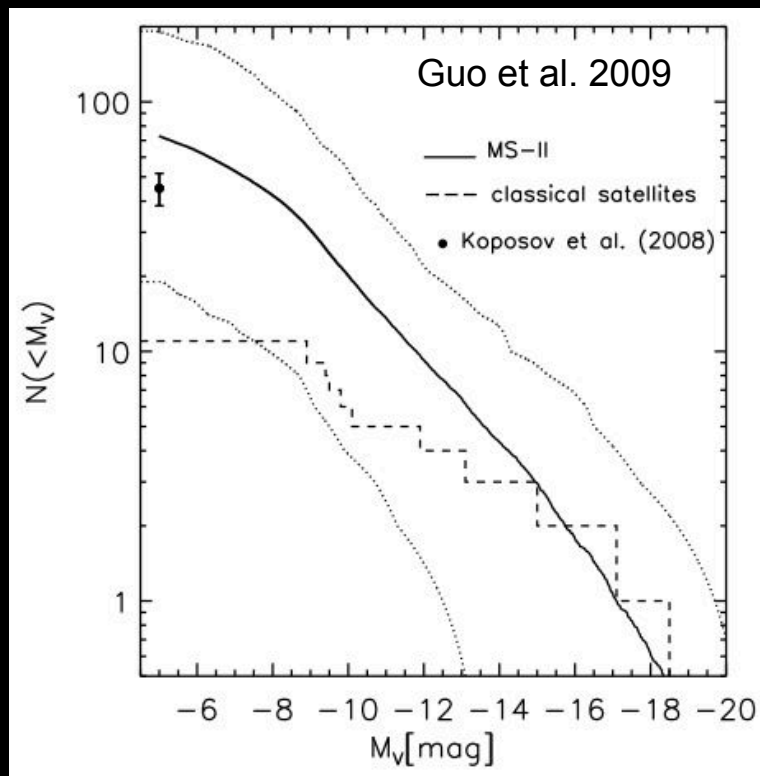
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Vogelsberger et al. 2014

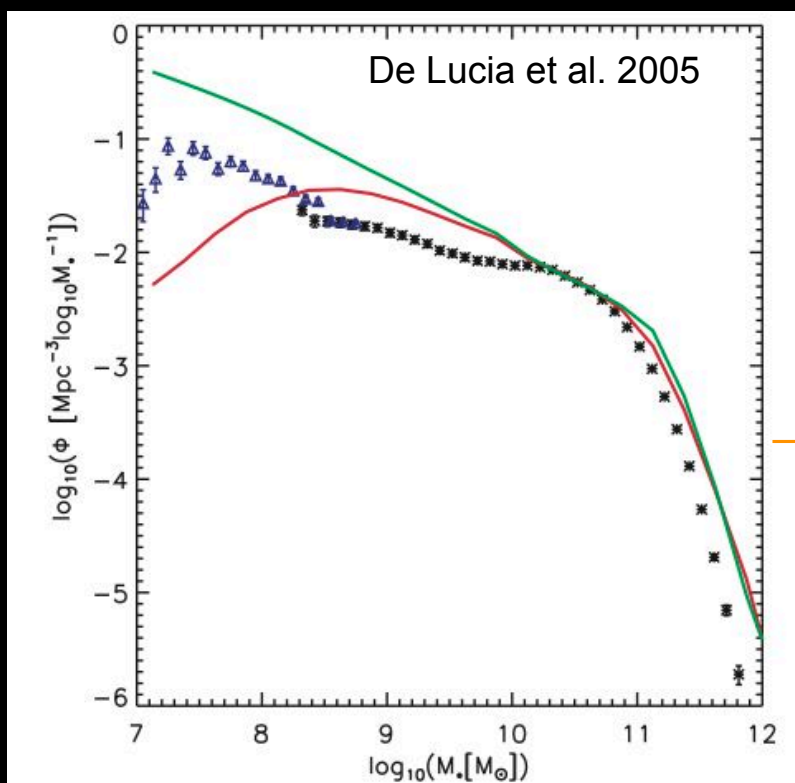


The effect of feedback

i) the abundance of satellites

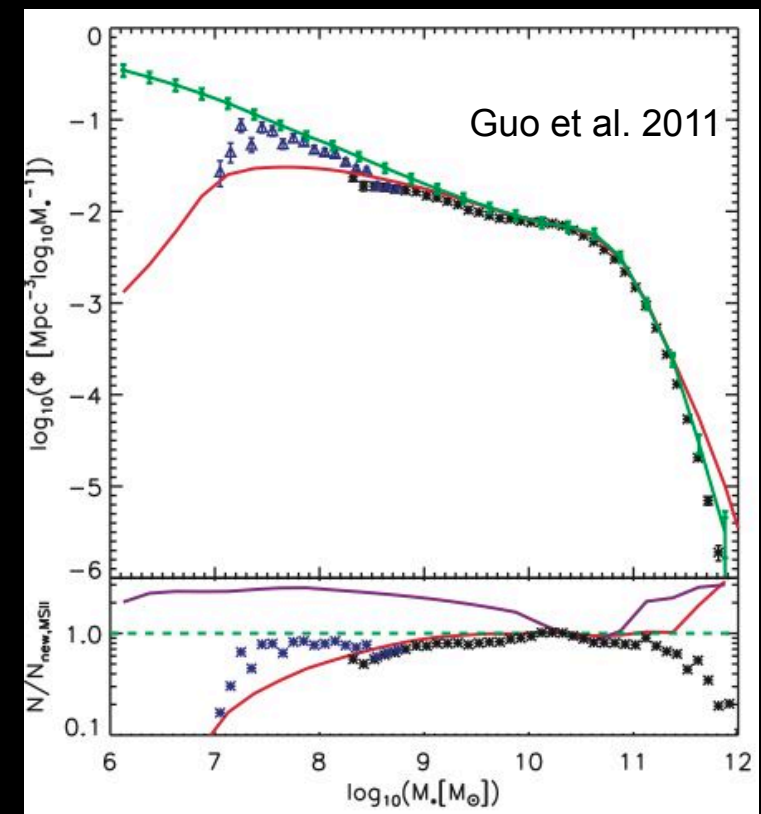


ii) the abundance of faint galaxies

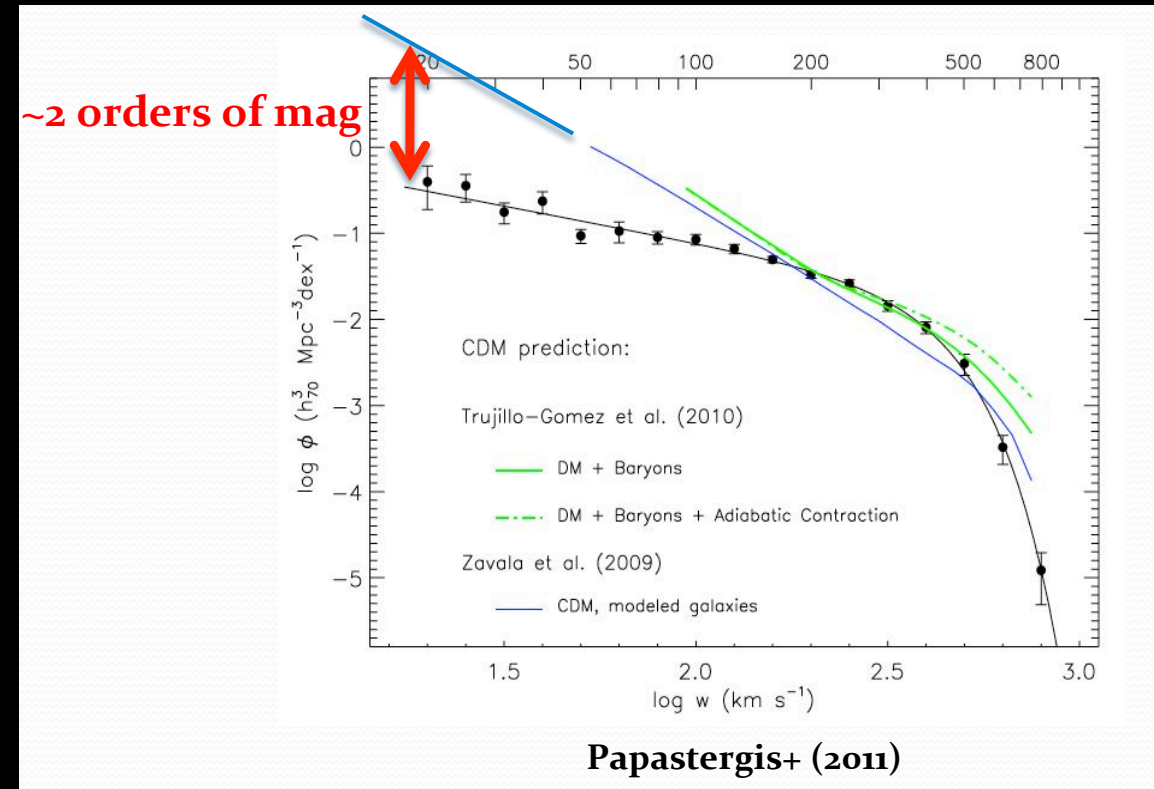


Refined treatment of Gas and Stellar Stripping

Enhanced (tuned) feedback dependence on the circular velocity of the DM halo



Abundance of galaxies as a function of their velocity width (gas rotation velocity)

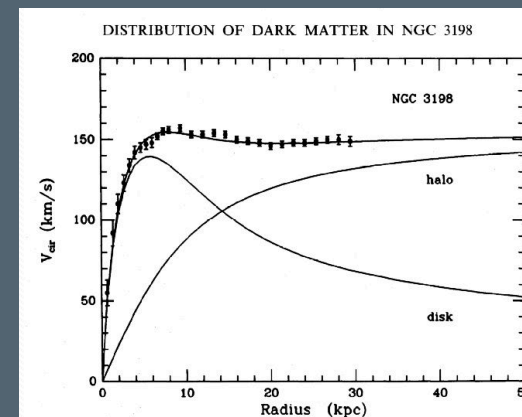


21-cm survey done with Arecibo Telescope: 3000 deg²; 11000 detections
 measures: redshift, velocity width, integrated flux
 No spatial resolution (size, inclination, shape)

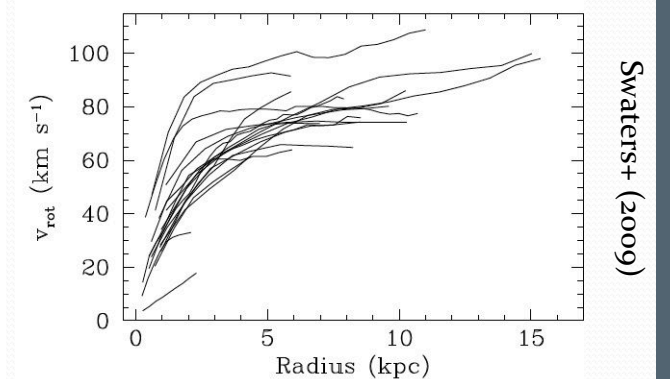
Directly measures
 the depth of the potential well:
 less prone to physics of gas (feedback)

Solutions within CDM scenario ?

- large fraction of galaxies with low gas content (below the sensitivity)
- large fraction of galaxies with rising rotation curve



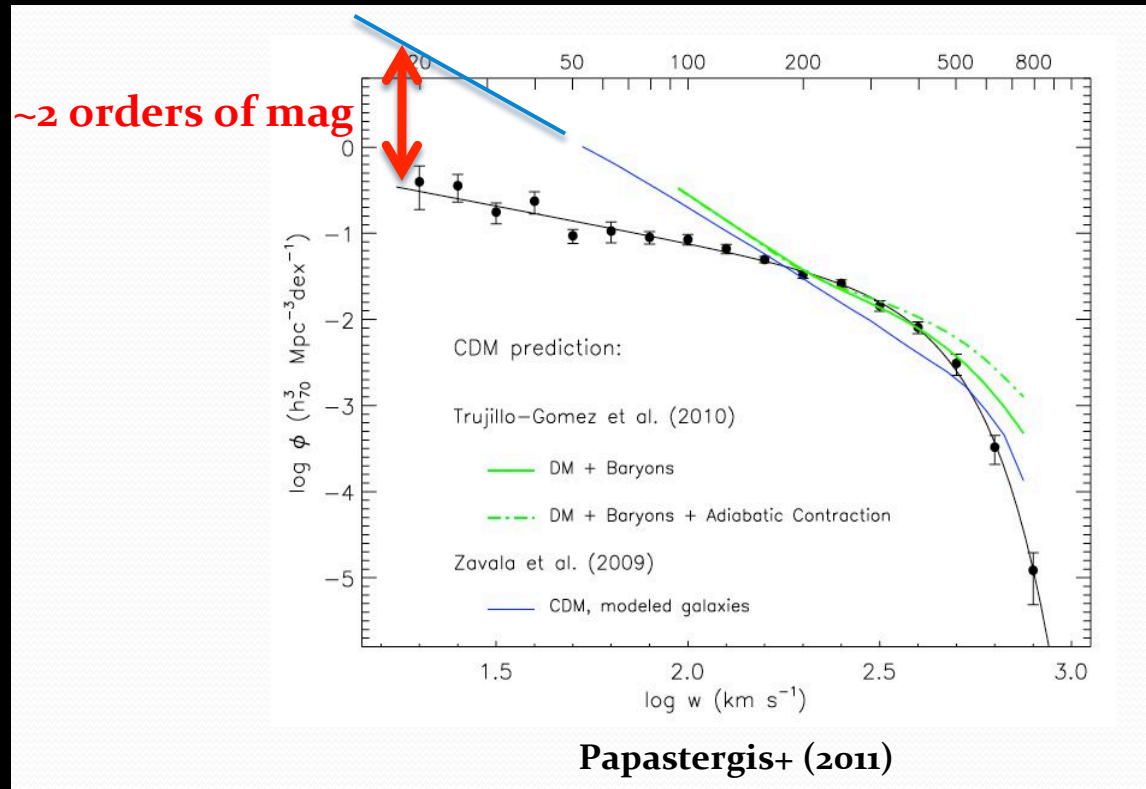
'flat' rotation curve



'rising' rotation curves

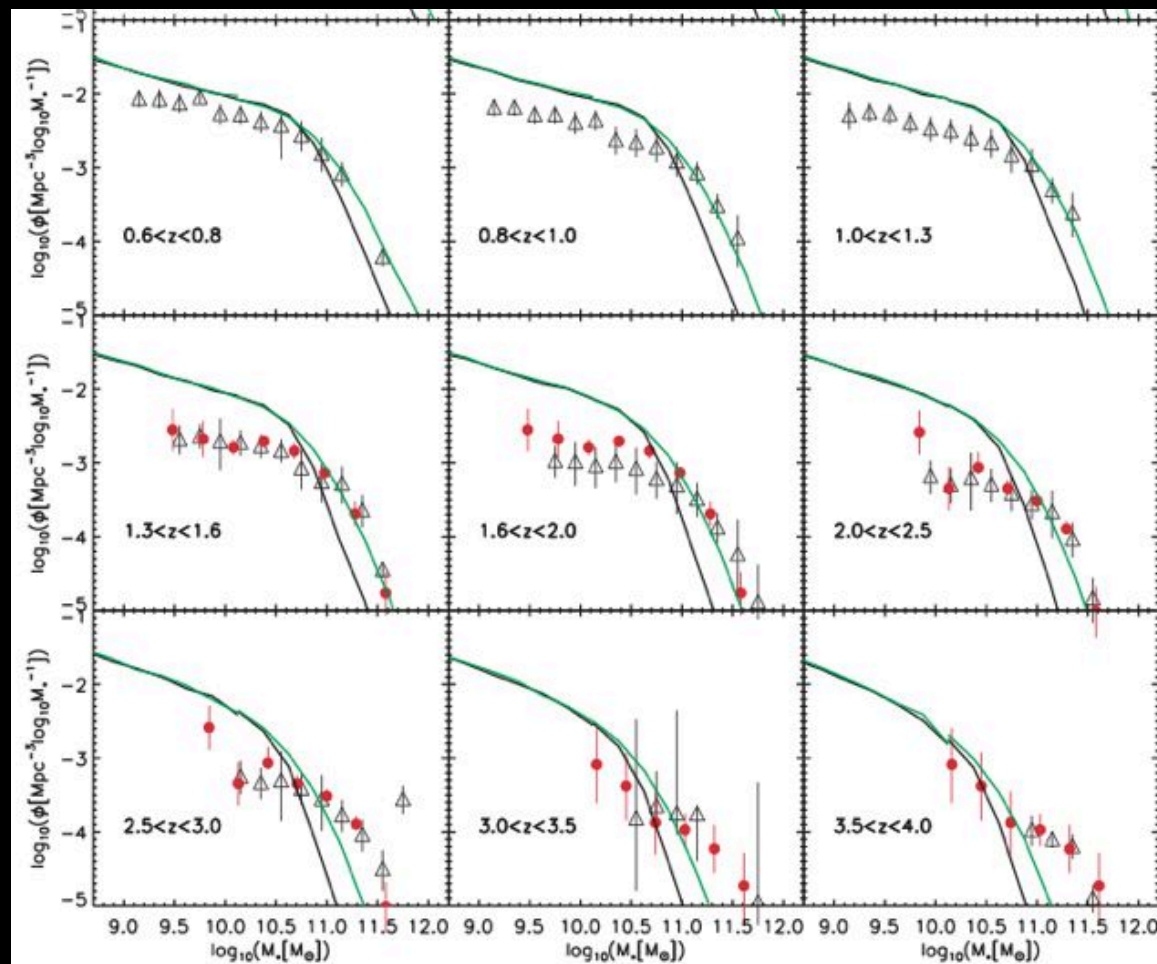
Swaters+ (2009)

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At high redshift, galaxies are denser

Difficult to expel gas from such compact objects

Even with maximized feedback, current models still over estimate the number of small mass galaxies

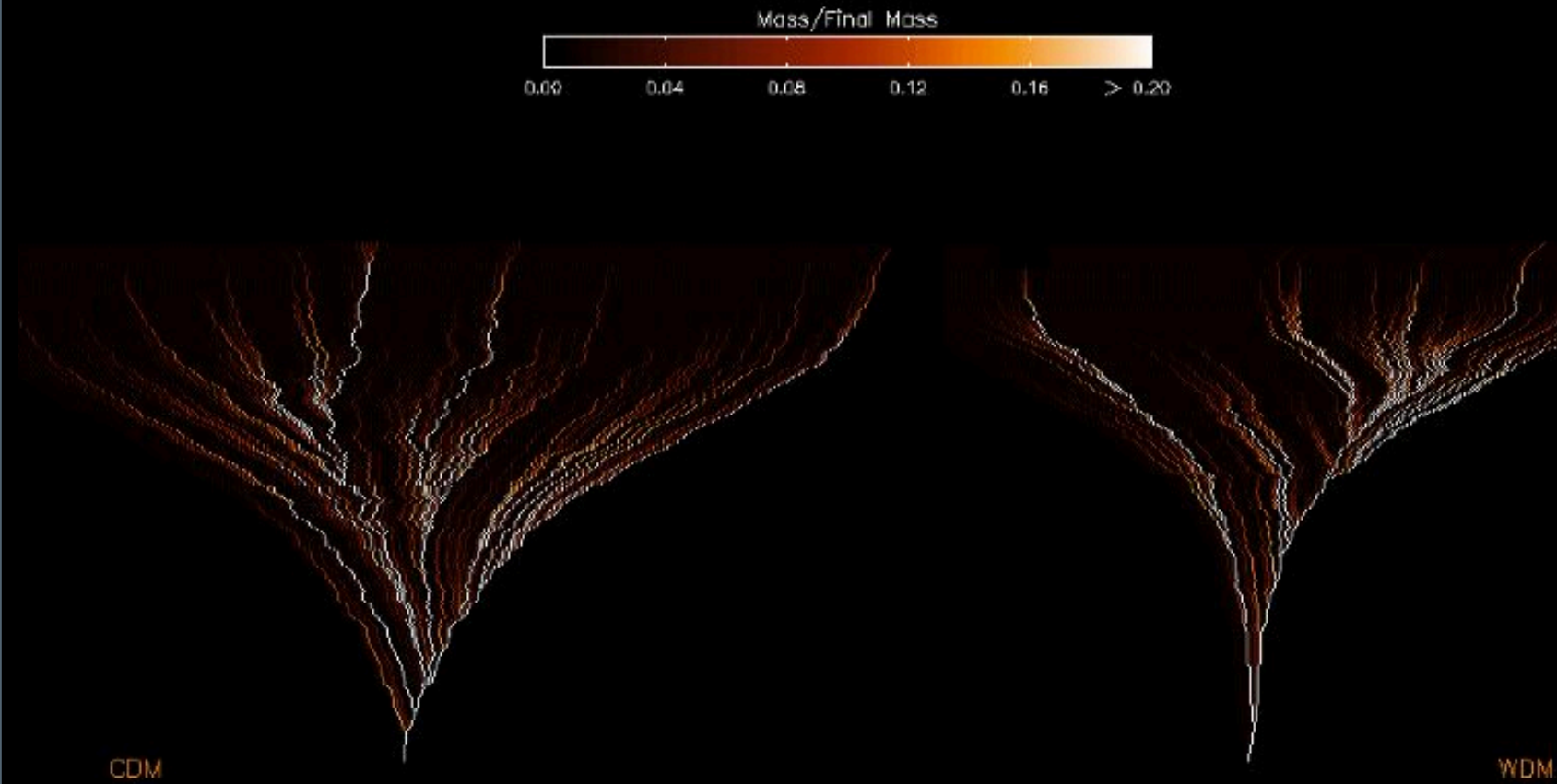
Galaxy formation in WDM Cosmology

Problem Persists at
high redshifts

Too many low-mass
structures

Need to suppress
Power Spectrum
at small scales ?

can WDM solve all
problems
simultaneously ?



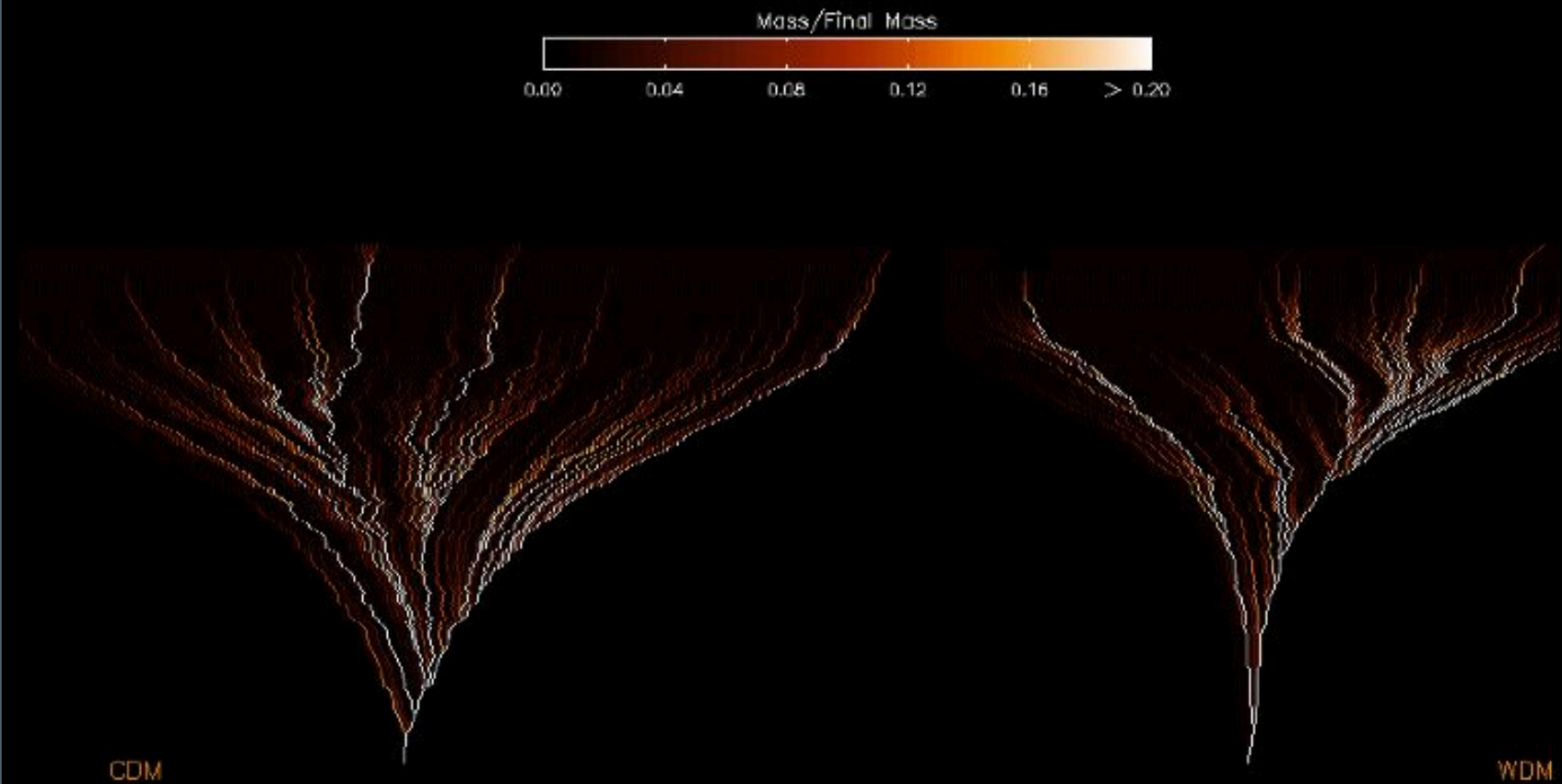
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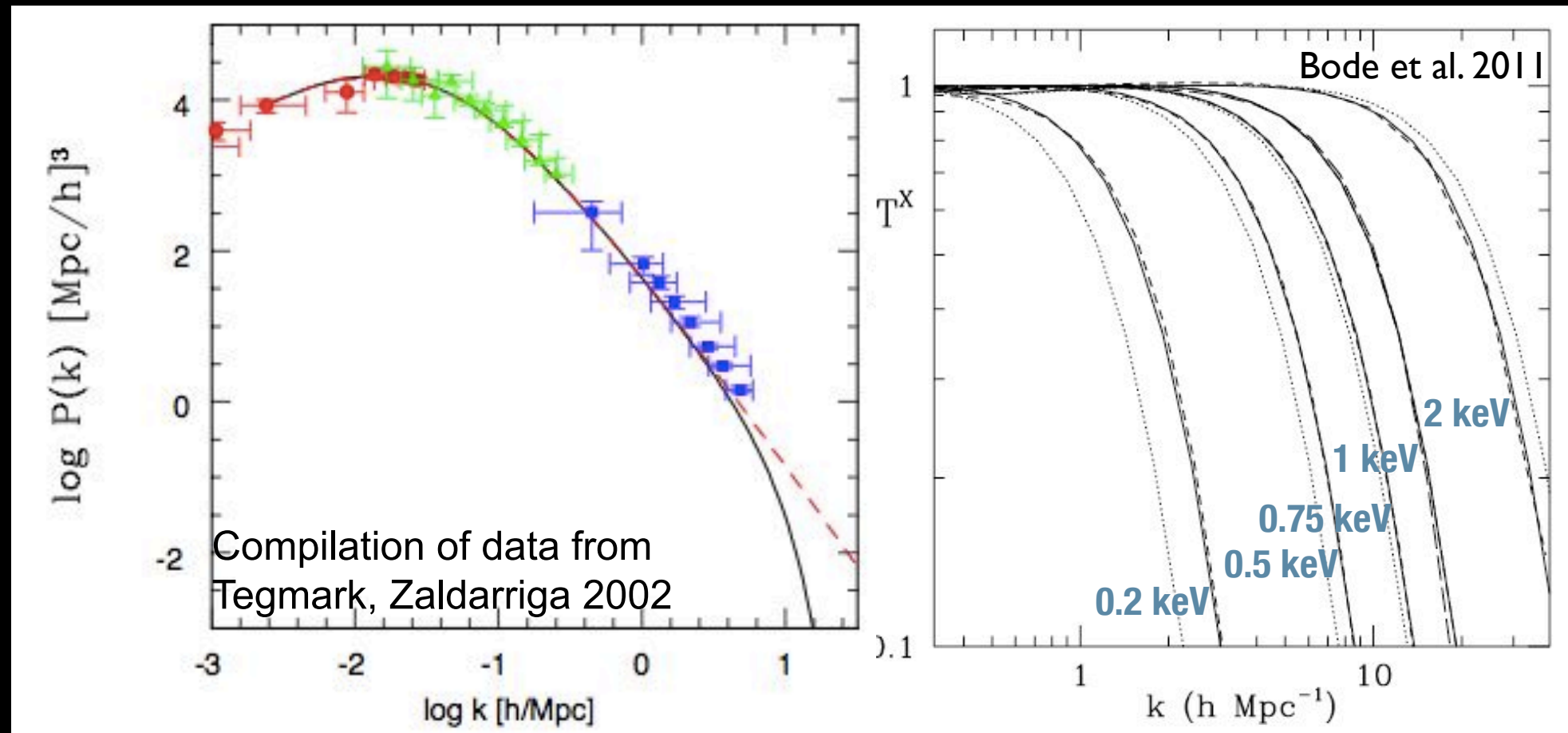
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simultaneously ?



Rome PANDA
model

NM, A. Lamstra

Implementing WDM power spectrum in the galaxy formation model



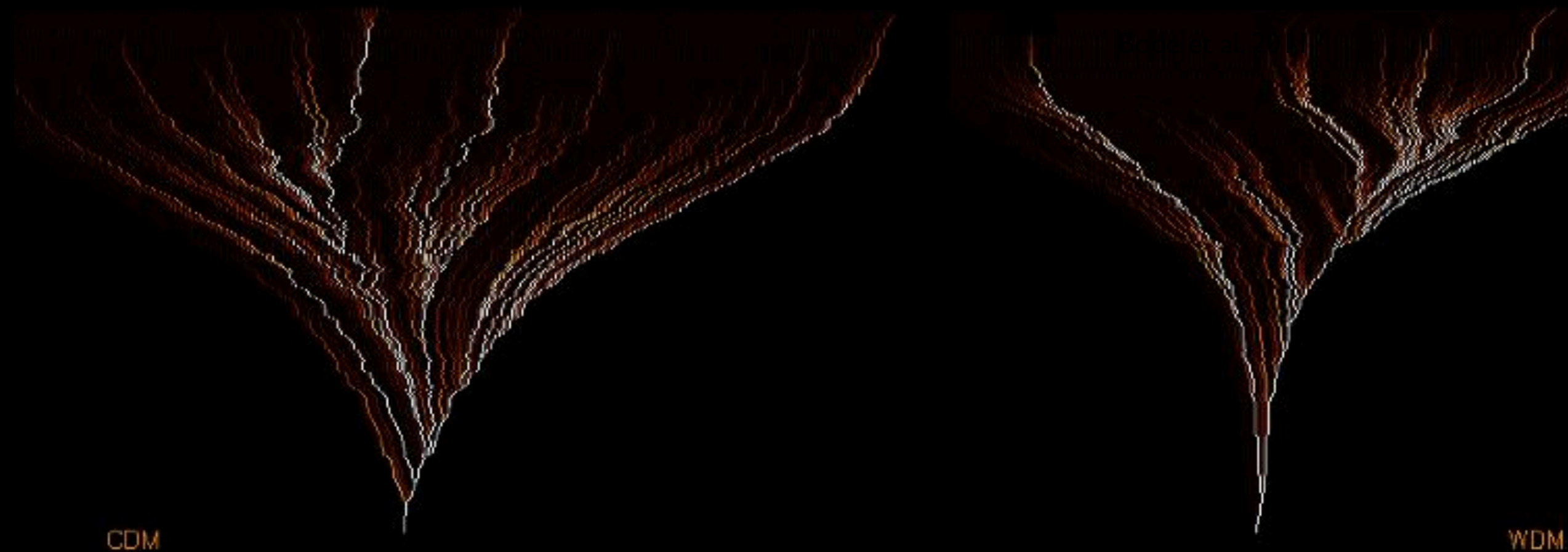
To explore the maximal effect of a power-spectrum cutoff on galaxy formation, we consider a cutoff at scales just below 0.2 Mpc, where data from Lyman- α systems (compared to N-body simulations) yields stringer upper limits on power suppression. This corresponds to mass scales $M_{fs} \sim 5 \cdot 10^8 M_{\odot}$

$$r_{fs} \approx 0.2 \left[\frac{\Omega_X h^2}{0.15} \right]^{1/3} \left[\frac{m_X}{rmkeV} \right]^{-4/3} \text{ Mpc} \quad \frac{P_{WDM}(k)}{P_{CDM}(k)} = \left[1 + (\alpha k)^{2\mu} \right]^{-5\mu}$$

$$\alpha = 0.049 \left[\frac{\Omega_X}{0.25} \right]^{0.11} \left[\frac{m_X}{keV} \right]^{-1.11} \left[\frac{h}{0.7} \right]^{1.22} h^{-1} \text{ Mpc}$$

WDM
particle mass
1 keV

Implementing WDM power spectrum in the galaxy formation model



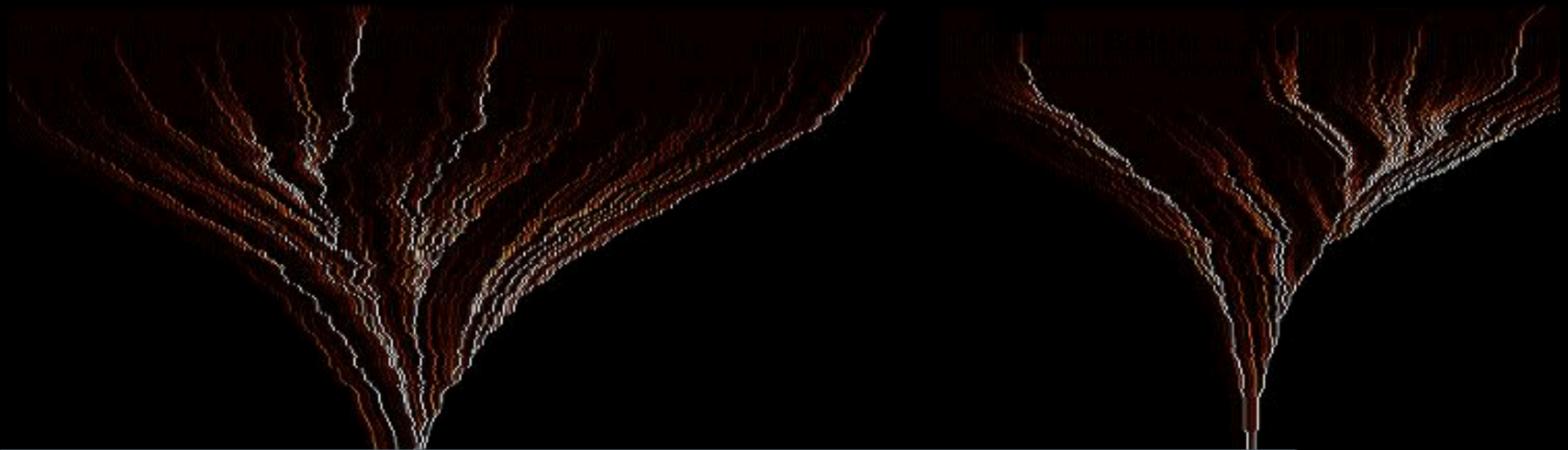
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Implementing WDM power spectrum in the galaxy formation model



Halo Properties
Density Profiles
Virial Temperature

Gas Properties
Profiles
Cooling - Heating
Collapse
Disk formation

Star Formation

Gas Heating (feedback)
SNe
UV background

Evolution of stellar
populations

WDM

Galaxy formation in WDM implies computing how modifications of the power spectrum propagate to the above processes

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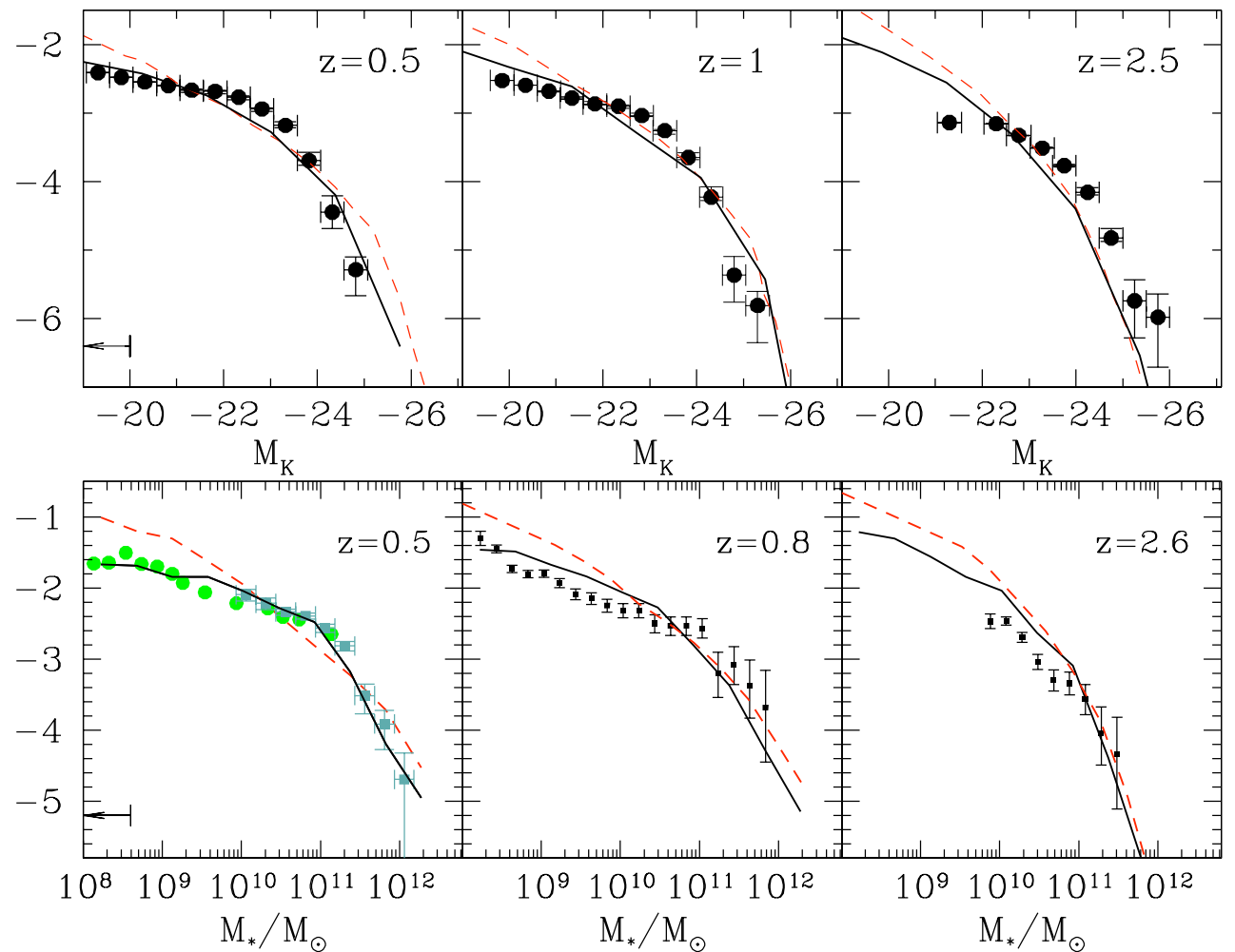
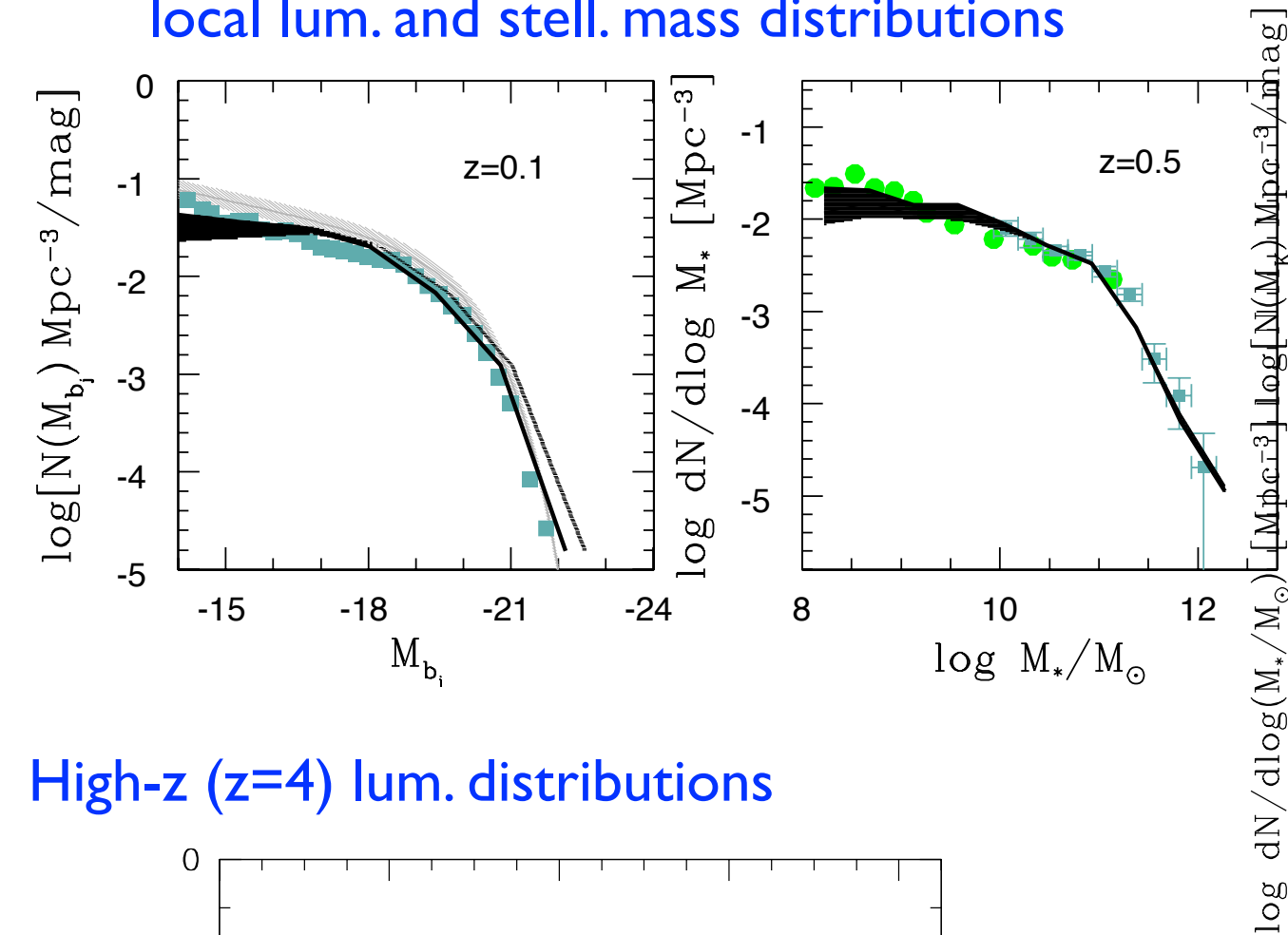
WDM
particle mass
1 keV

Galaxy Formation in WDM cosmology ($m_{\text{WDM}}=1$ keV)

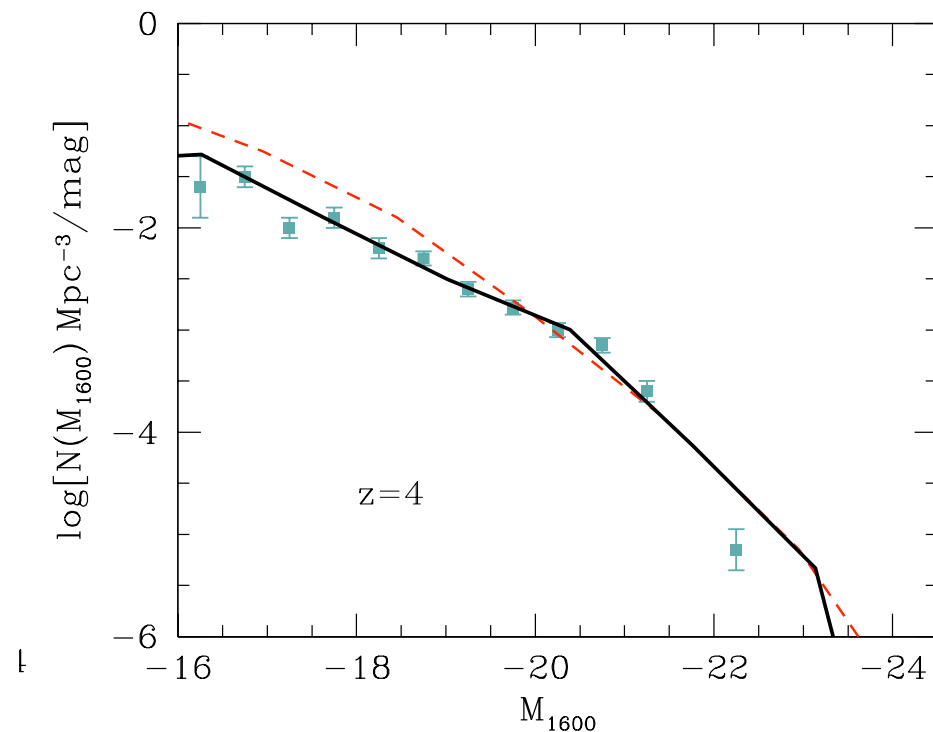
NM et al. 2012-2013

Evolution

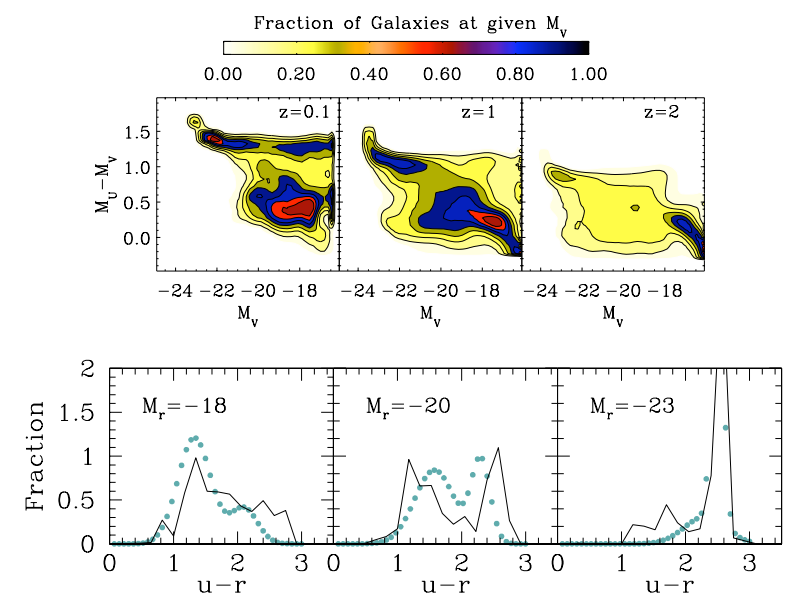
local lum. and stell. mass distributions



High-z ($z=4$) lum. distributions

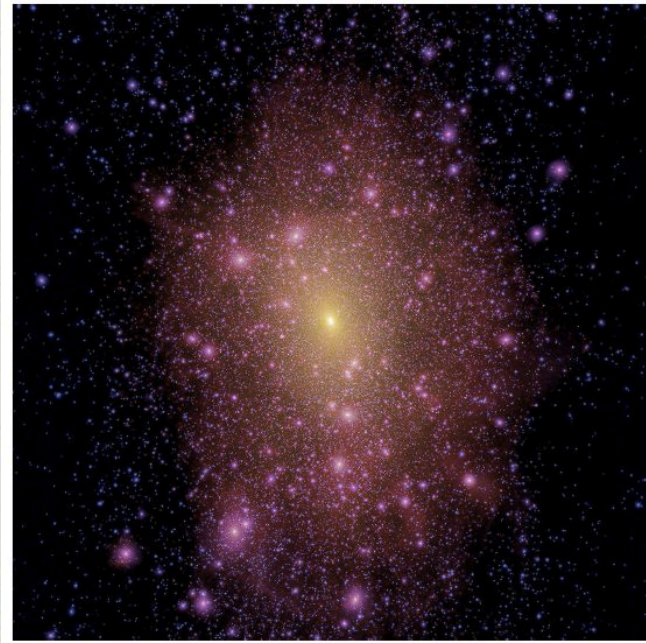


color distributions

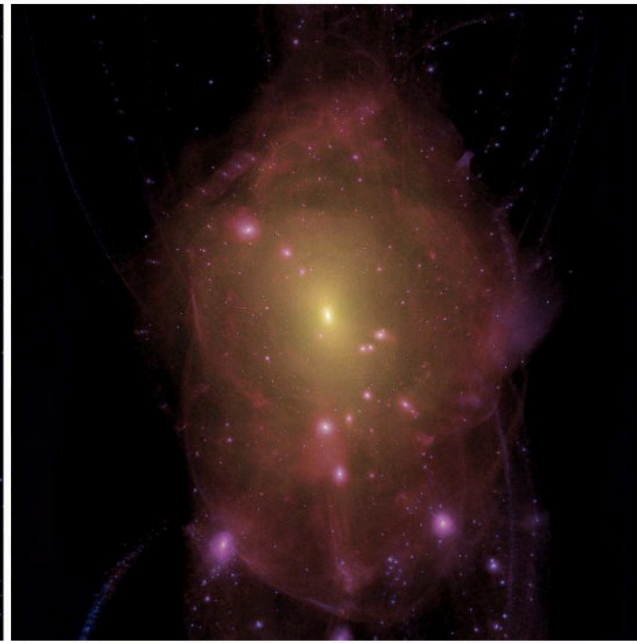


Substructure Predictions

CDM

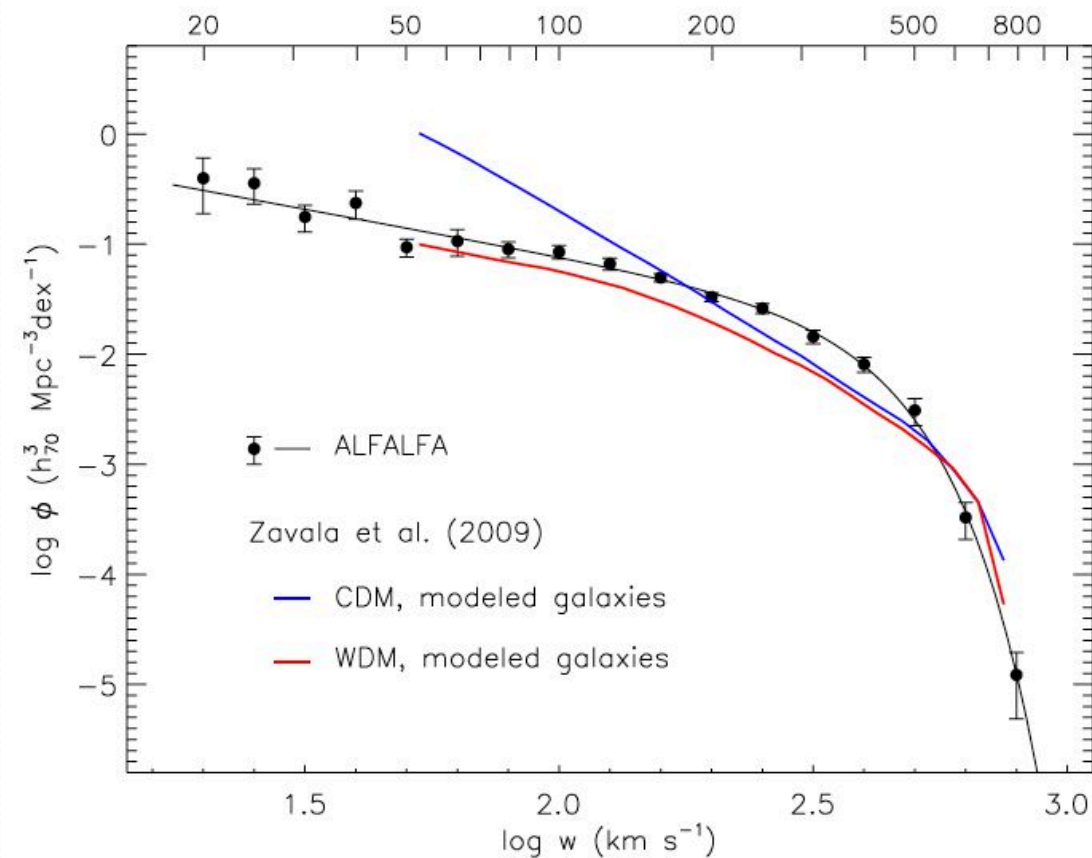


WDM



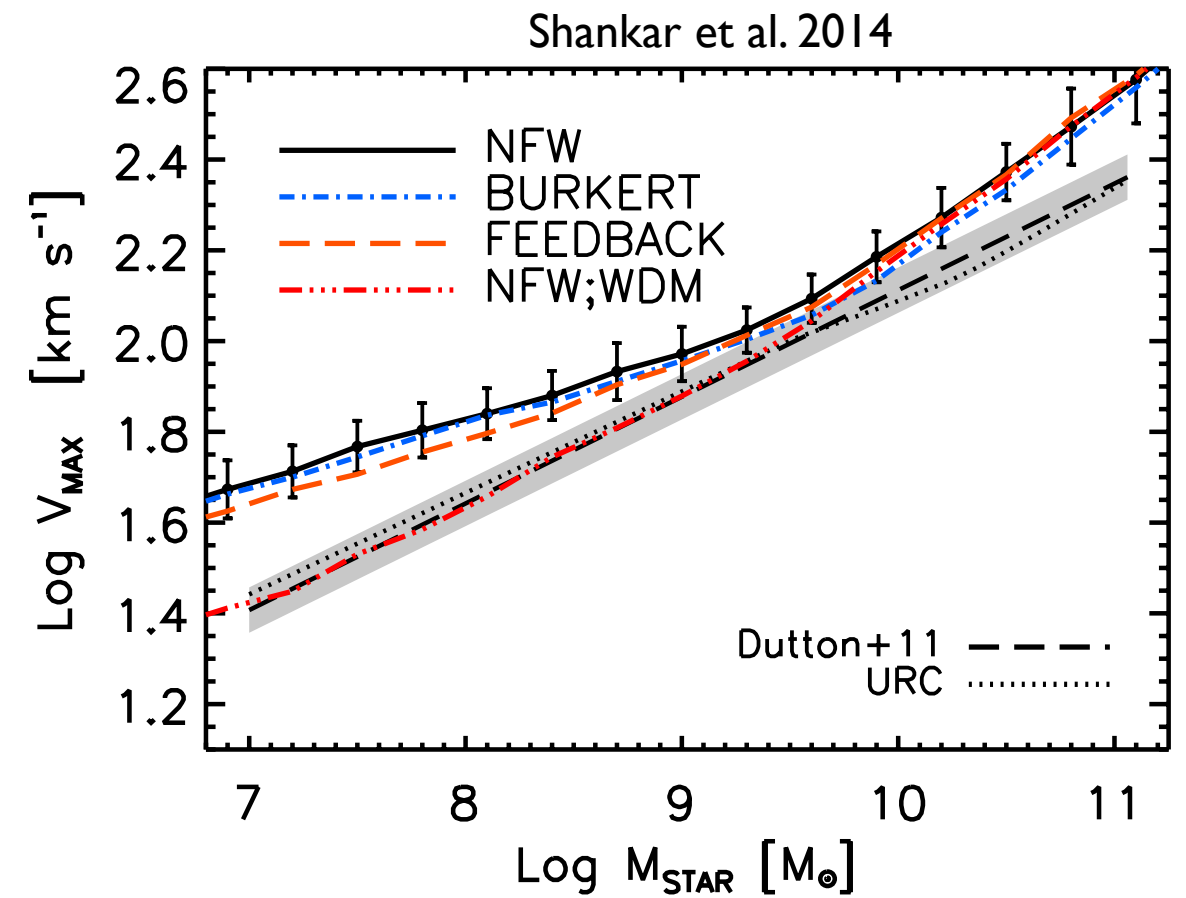
$m_{\text{wdm}} = 1 \text{ keV}$

LOVELL ET AL. 2013



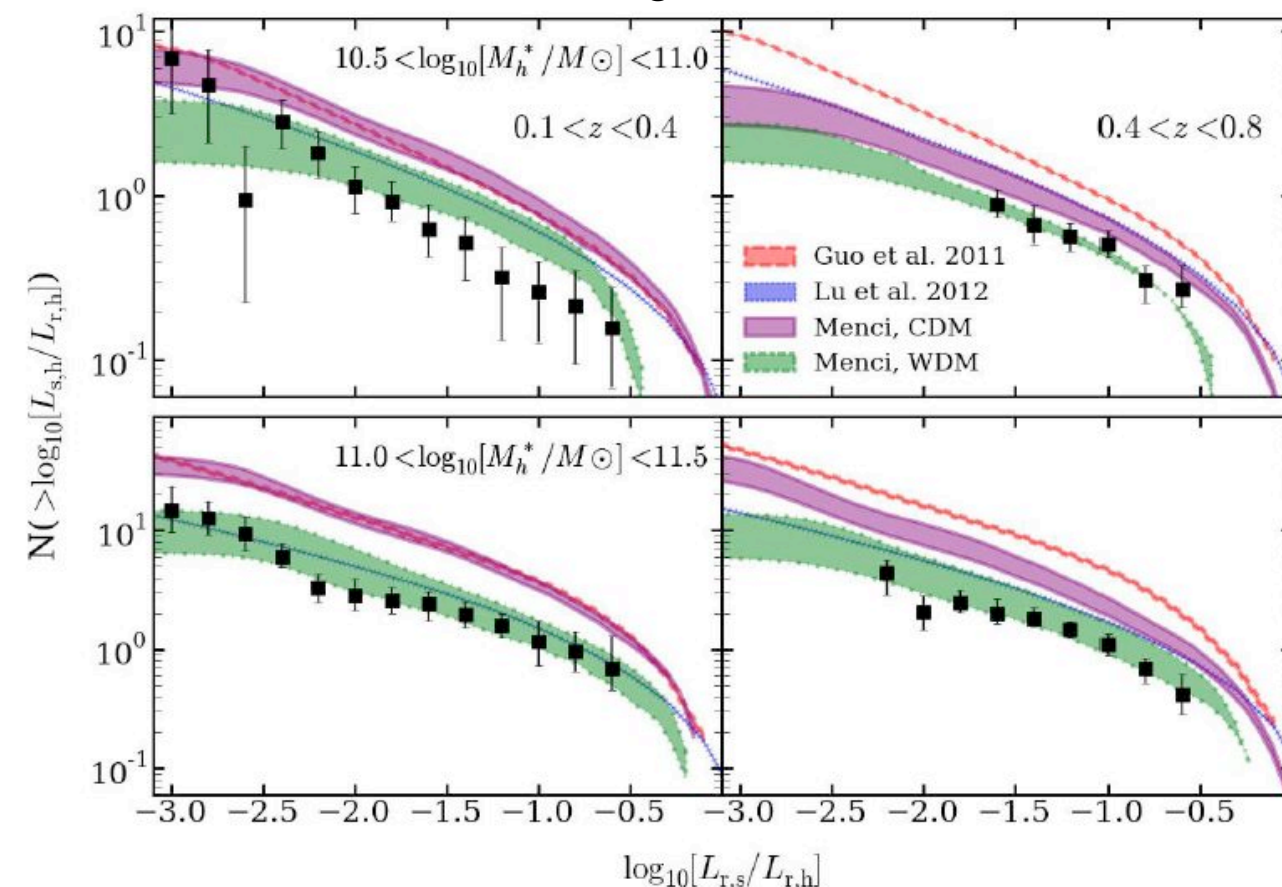
modeling: Zavala+ (2009)

Papastergis+ (2011)



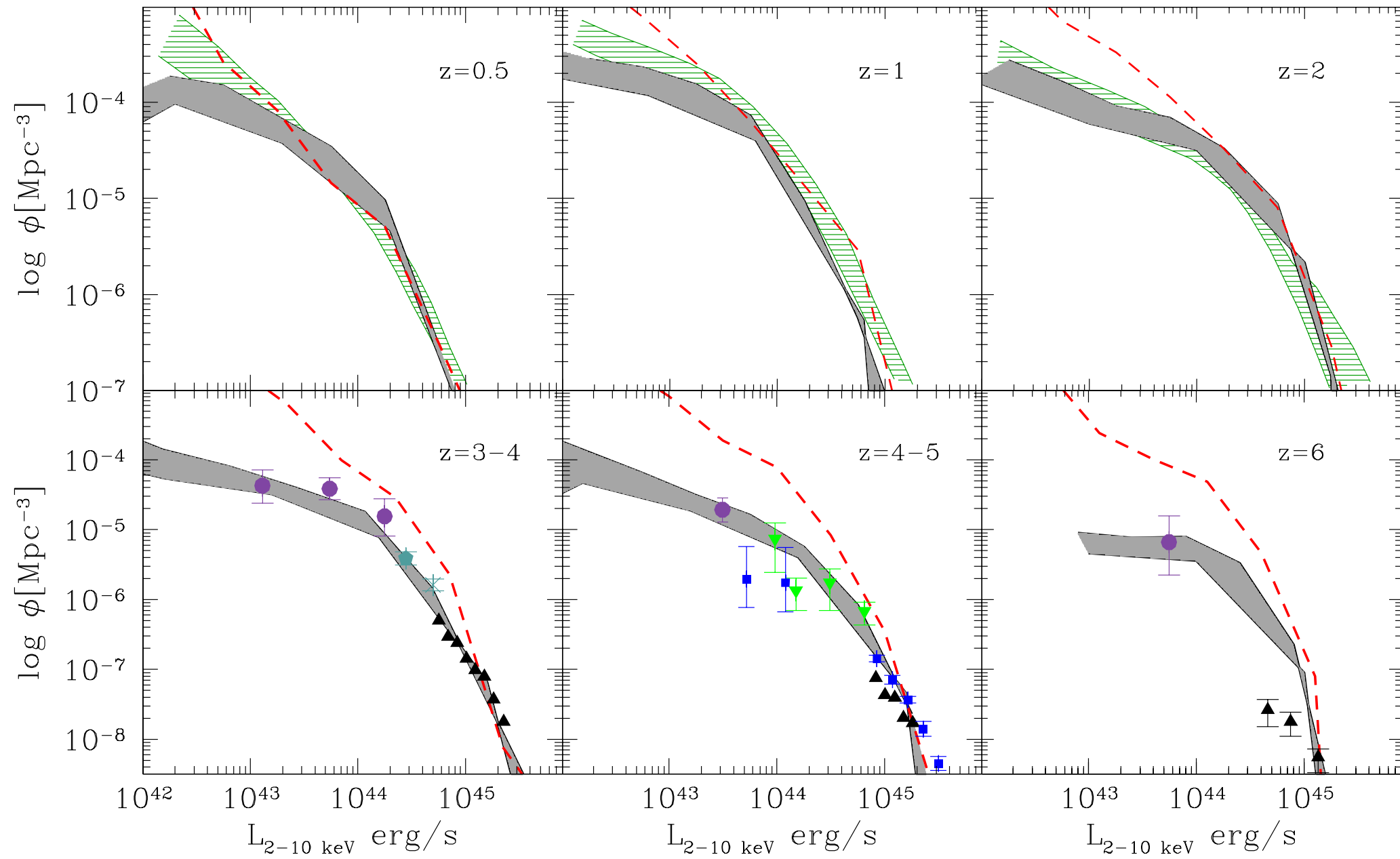
Shankar et al. 2014

The luminosity distribution of Satellite Galaxies
Nierenberg, Treu, NM 2013



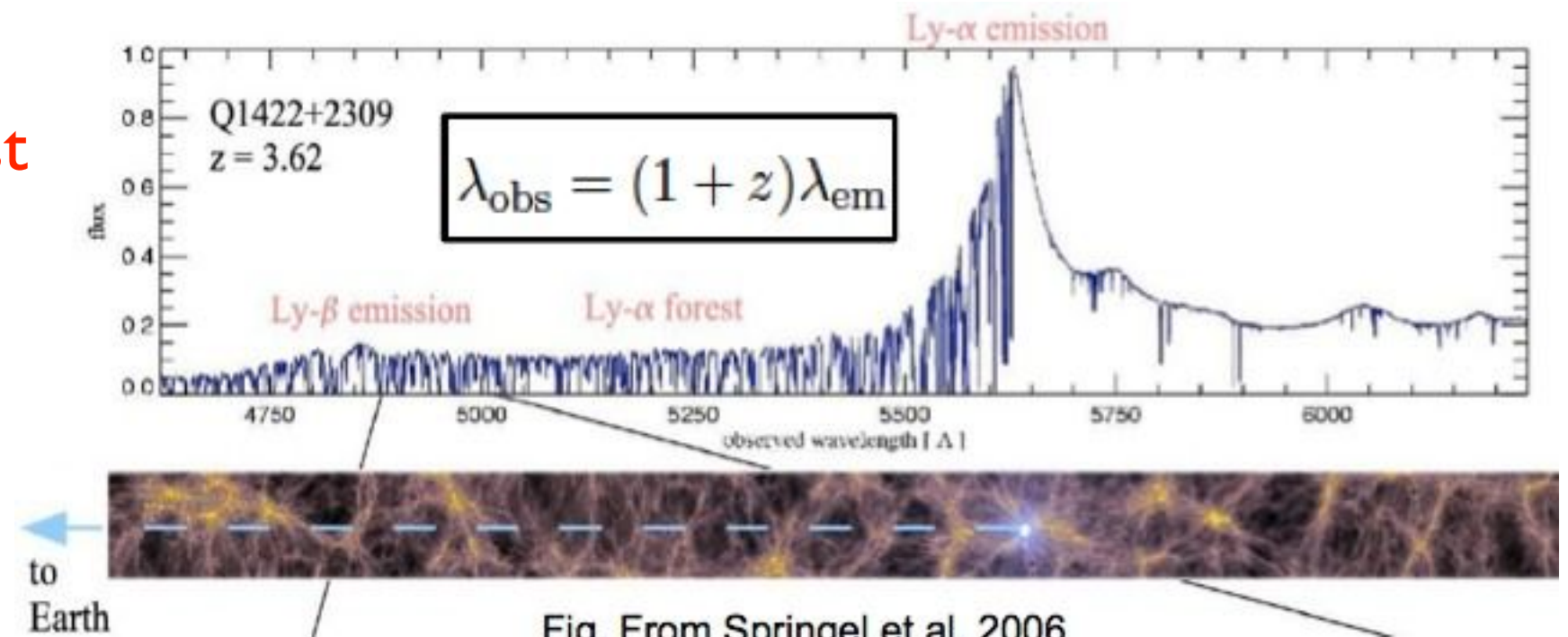
observations of satellites between $0.1 < z < 0.8$ based on Hubble Space Telescope images

The AGN luminosity Functions



WDM particle mass: limits from the Ly- α forest

Viel et al. 2005-2013



$m_{\text{WDM}} > 1 \text{ keV}$

Thermal
relics WDM

$m_{\nu} > 4 \text{ keV}$

Sterile ν
WDM (DW)
Dodelson-Widrow

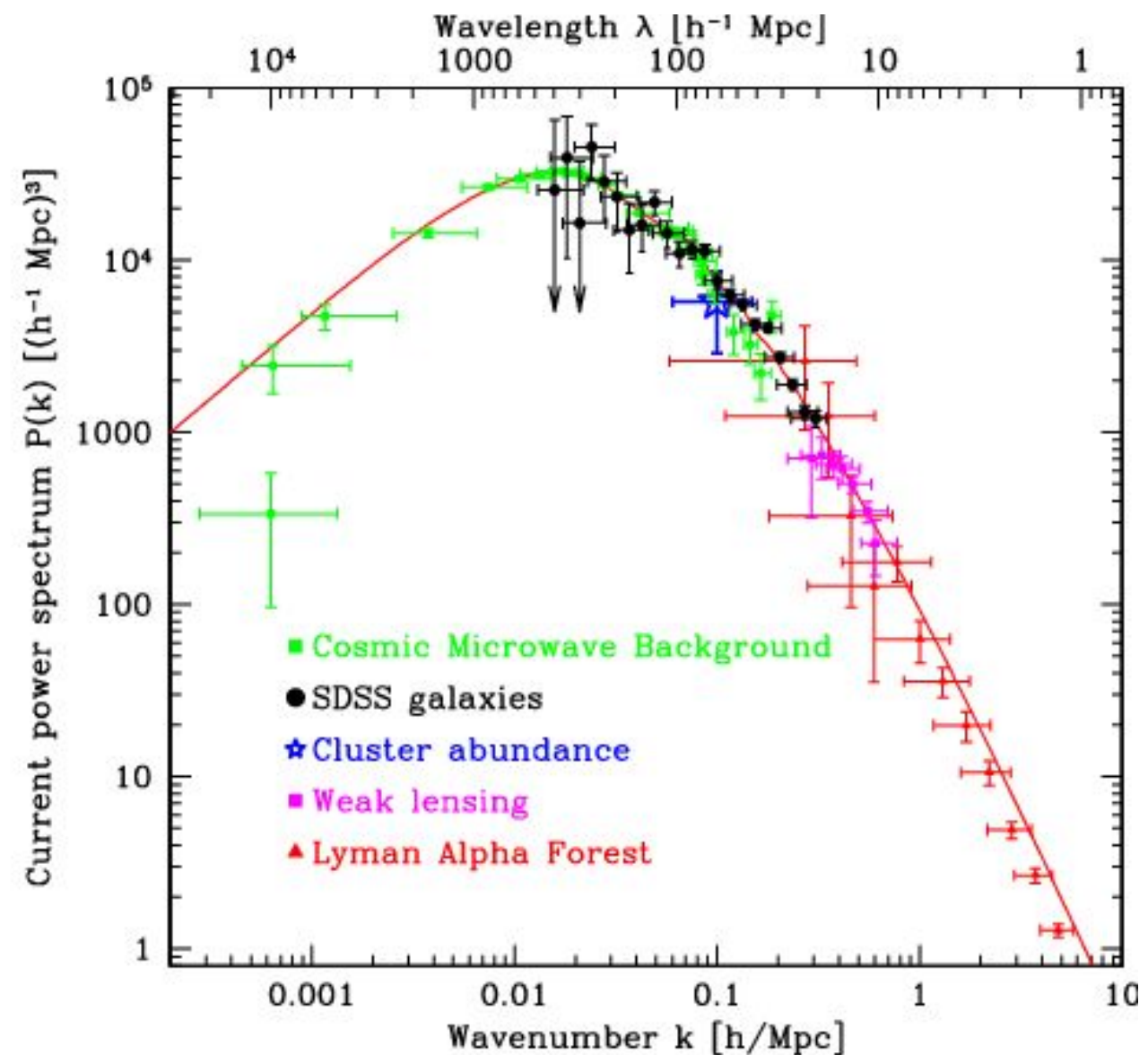


$m_{\text{WDM}} > 4 \text{ keV}$

Thermal
relics WDM

$m_{\nu} > 12 \text{ keV}$

Sterile ν
WDM (DW)
Dodelson-Widrow



Constraints from X-ray emission from clusters and galaxies

if $m_s > m_\alpha$ the radiative decay $\nu_s \rightarrow \nu_\alpha + \gamma$ becomes allowed

$$E_\gamma = \frac{1}{2}m_s \left(1 - \frac{m_\alpha^2}{m_s^2} \right).$$

Emission lines in X-rays from DM concentrations:

- clusters (large signal but also large background)
- galaxies

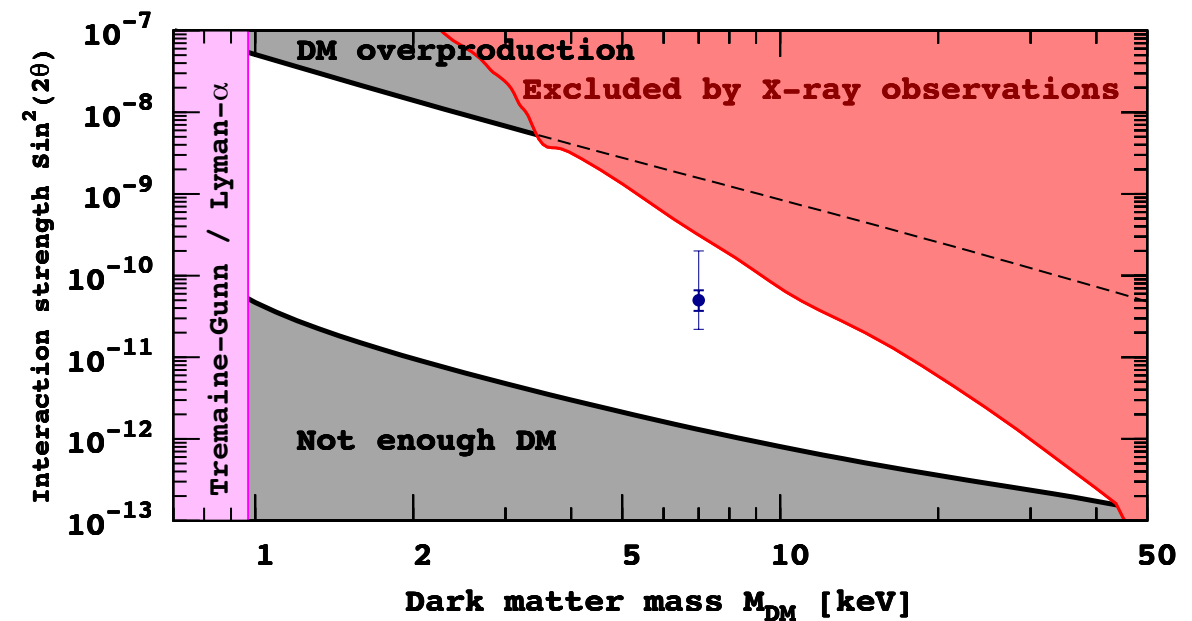


FIG. 4: Constraints on sterile neutrino DM within ν MSM [4]. The blue point would corresponds to the best-fit value from M31 if the line comes from DM decay. Thick errorbars are $\pm 1\sigma$ limits on the flux. Thin errorbars correspond to the uncertainty in the DM distribution in the center of M31.

Boyarsky et al. 2014



Summary

The mass of DM particles has a major impact on structure formation (suppression of small-scale perturbations due to free-streaming)
CDM is the limit of $M_{fs} \ll$ masses of cosmological interest

CDM problems on small scales:

- cusps

- number of satellite galaxies

- abundance of low-mass (faint) galaxies at low and high redshifts

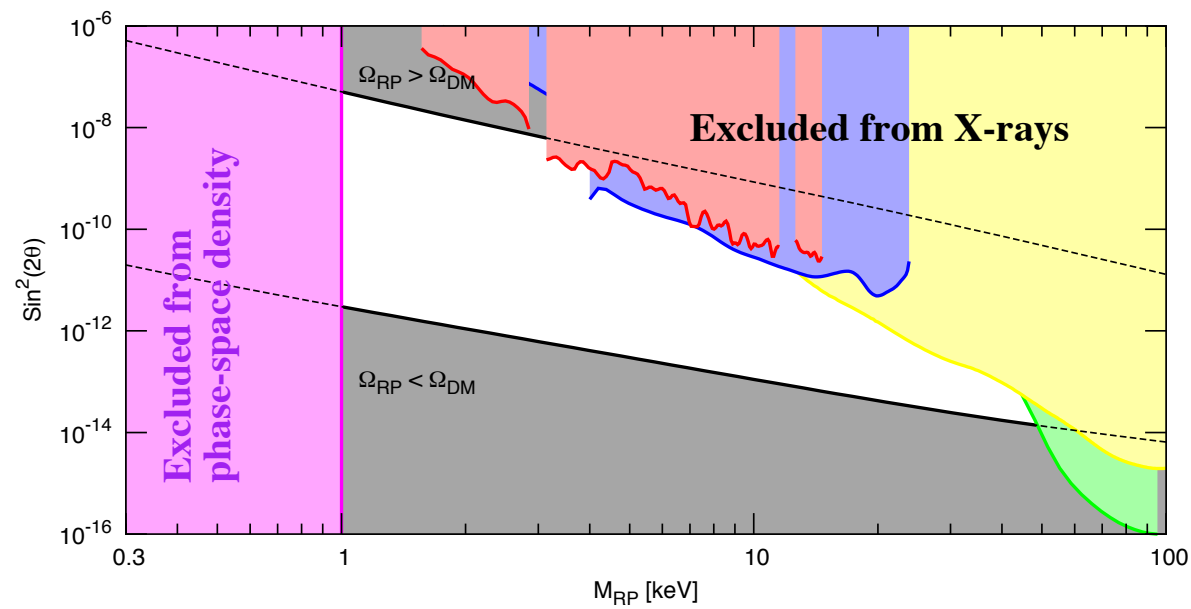
Baryonic physics can hardly solve the problems

Galaxy formation in WDM cosmology is a viable solution

There is a tension:

- current limits from high- z structure (Lyman- α forest)

- suggest $m > 10$ keV, but to solve the galactic small-scale crisis $m < 2$ keV is needed



Window corresponds to resonant production
 Upper boundary - zero lepton asymmetry
 Lower boundary - maximal lepton asymmetry

Boyarsky et al 2009

6 – Sterile neutrino resonant production

In presence of a large lepton asymmetry, $\mathcal{L} \equiv (n_\nu - n_{\bar{\nu}})/n_\gamma$, matter effects become important and the mixing angle can be resonantly enhanced. [Shi,

Fuller, 1998; Abazajian et al., 2001

$$\sin^2 2\theta_m = \frac{\Delta^2(p) \sin^2 2\theta}{\Delta^2(p) \sin^2 2\theta + D^2 + (\Delta(p) \cos 2\theta - \frac{2\sqrt{2}\zeta(3)}{\pi^2} G_F T^3 \mathcal{L} + |V_T|)^2}$$

The mixing angle is maximal $\sin^2 2\theta_m = 1$ when the **resonant condition** is satisfied (with $\Delta(p) \equiv m_4^2/(2p)$)

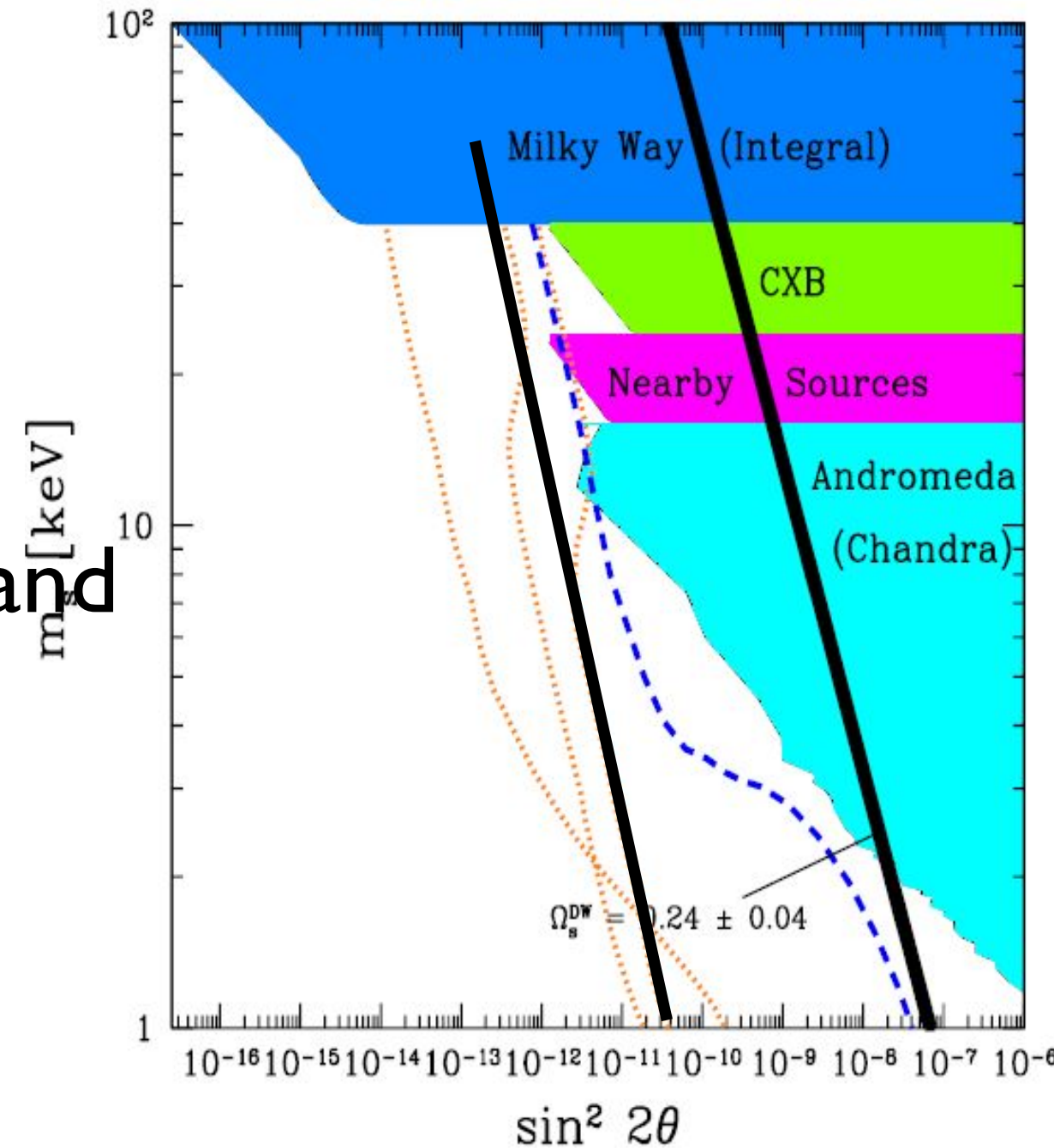
$$\Delta(p) \cos 2\theta - \frac{2\sqrt{2}\zeta(3)}{\pi^2} G_F T^3 \mathcal{L} + |V_T| = 0$$

$$\left(\frac{m_4}{1\text{keV}}\right)^2 \simeq 0.08 \frac{p}{T} \frac{\mathcal{L}}{10^{-4}} \left(\frac{T}{100\text{MeV}}\right)^4 + 2 \left(\frac{p}{T}\right)^2 \frac{B}{\text{keV}} \left(\frac{T}{100\text{MeV}}\right)^6$$

Sterile neutrinos are produced in primordial plasma through

- off-resonance oscillations. [Dodelson, Widrow; Abazajian, Fuller; Dolgov, Hansen; Asaka, Laine, Shaposhnikov et al.]
- oscillations on resonance, if the lepton asymmetry is non-negligible [Fuller, Shi]
- production mechanisms which do not involve oscillations
 - inflaton decays directly into sterile neutrinos [Shaposhnikov, Tkachev] – Higgs physics: both mass and production [AK, Petraki]

Limits from the X-ray emission from clusters and galaxies



Very small mixing ($\sin^2 2\theta \lesssim 10^{-7}$) **between**

mass $|\nu_{1,2}\rangle$ **&**

flavor $|\nu_{\alpha,s}\rangle$ **states:**

$$\begin{aligned} |\nu_\alpha\rangle &= \cos\theta|\nu_1\rangle + \sin\theta|\nu_2\rangle \\ |\nu_s\rangle &= -\sin\theta|\nu_1\rangle + \cos\theta|\nu_2\rangle \end{aligned}$$

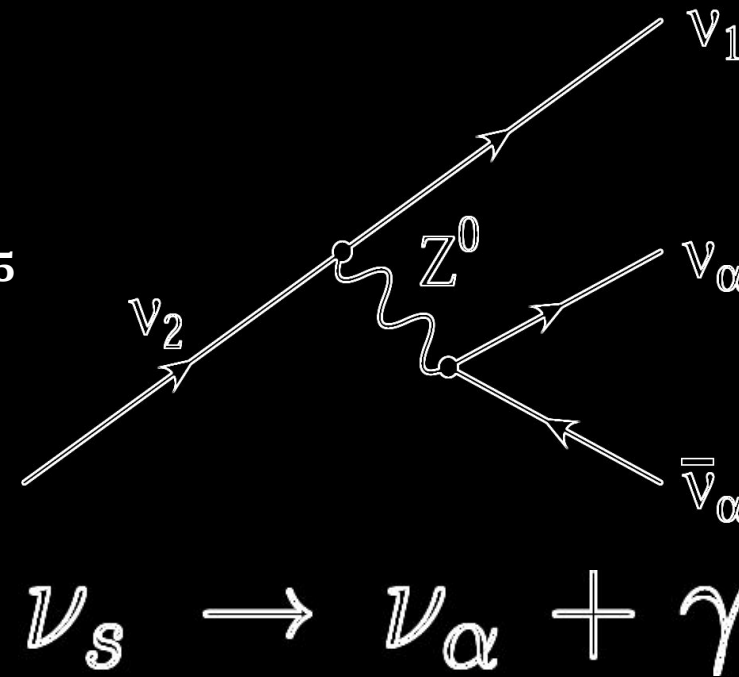
For $m_s < m_e$,

3ν Decay Mode Dominates:

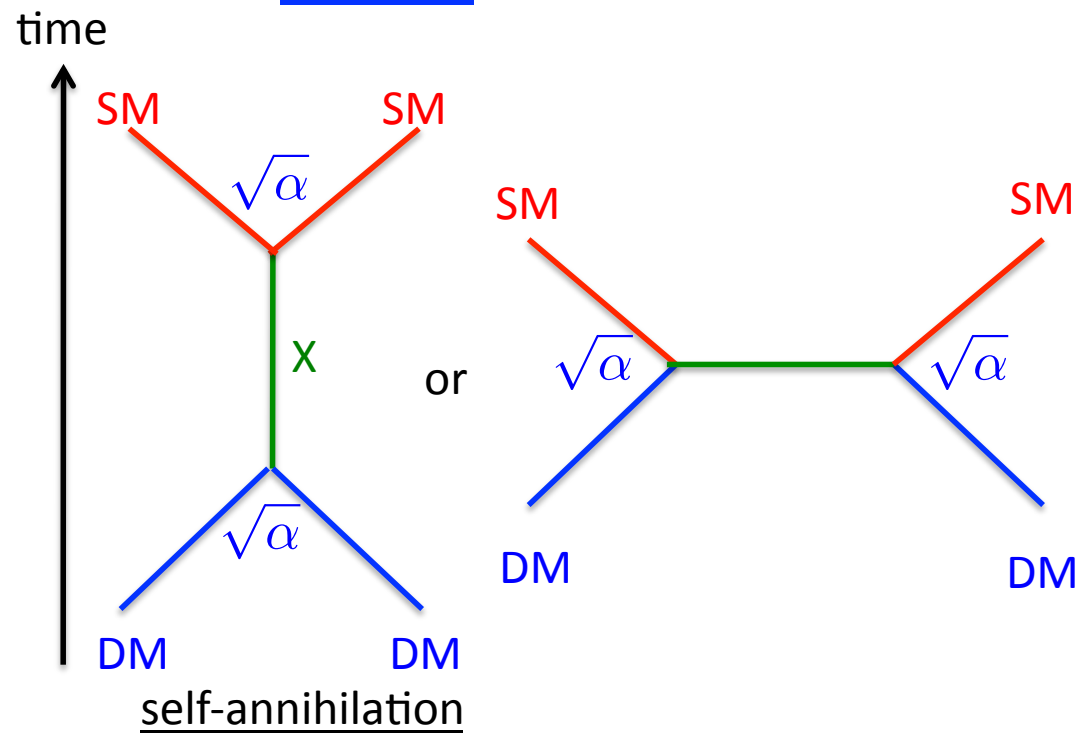
$$\Gamma_{3\nu} \simeq 1.74 \times 10^{-30} s^{-1} \left(\frac{\sin^2 2\theta}{10^{-10}} \right) \left(\frac{m_s}{\text{keV}} \right)^5$$

Radiative Decay Rate is:

$$\Gamma_s \simeq 1.36 \times 10^{-32} s^{-1} \left(\frac{\sin^2 2\theta}{10^{-10}} \right) \left(\frac{m_s}{\text{keV}} \right)^5$$

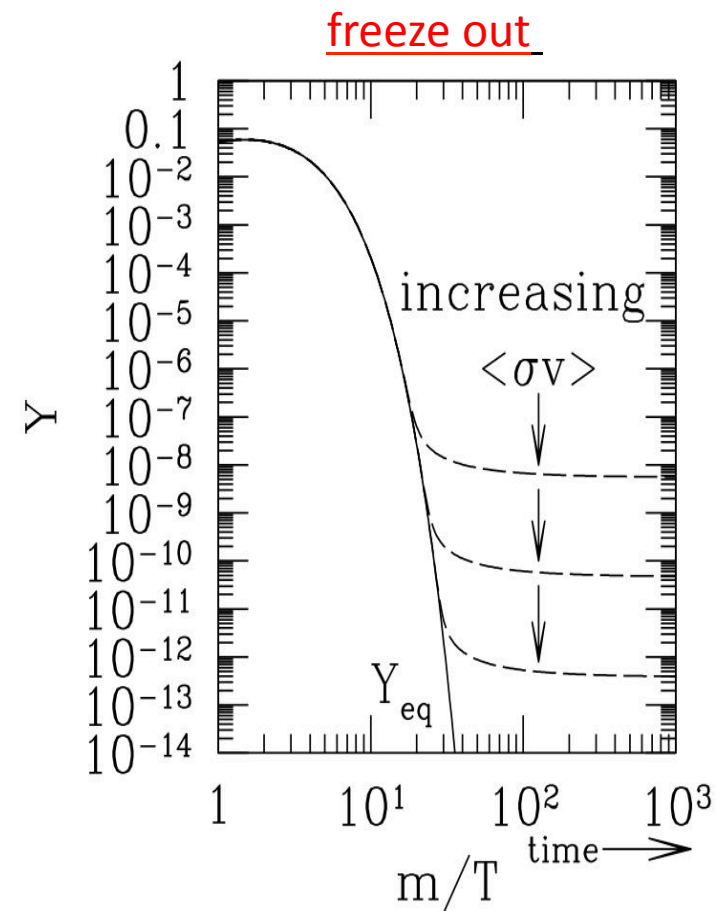


WIMP



$$\Omega h^2 \approx \frac{3 \times 10^{-27} \text{ cm}^3/\text{s}}{\langle \sigma_{\text{ann}} v \rangle}.$$

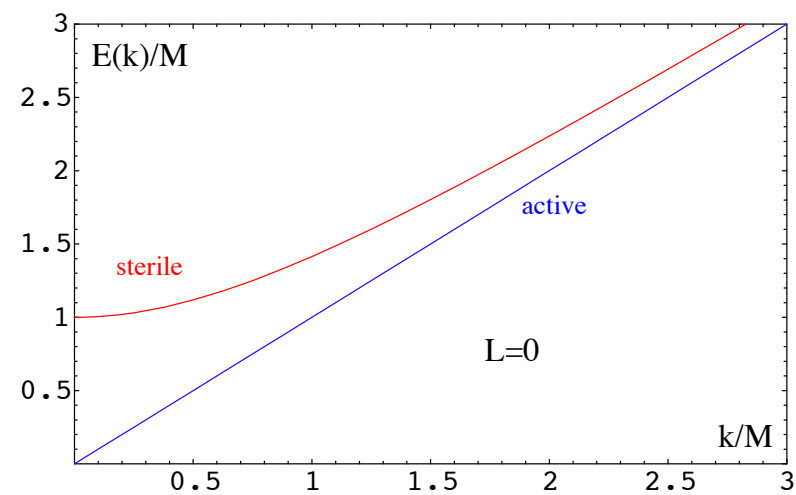
$$\langle \sigma_{\text{ann}} v \rangle \sim 10^{-25} \text{ cm}^3 \text{ s}^{-1} \left(\frac{\alpha}{10^{-2}} \right)^2 \left(\frac{100 \text{ GeV}}{m_X} \right)^2$$



Electro Weak Scale ($\sim 100 \text{ GeV}$) WIMP naturally explains the relic abundance.

TeV scale SUSY & neutralino dark matter

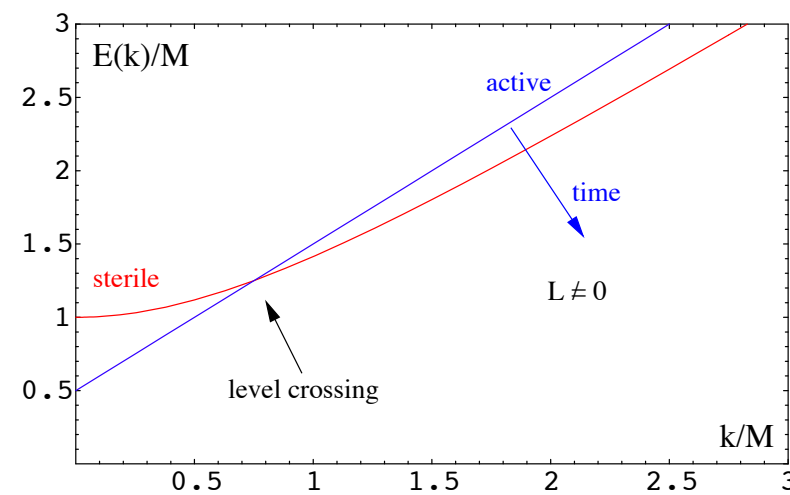
Dispersional relations for active and sterile neutrinos (from real part)



Transitions $\nu \rightarrow N_1$

Dodelson-Widrow

Zero lepton asymmetry



Resonant transitions

Shi-Fuller

Lepton asymmetry
created in $N_{2,3}$ decays

Dark matter and the Lyman- α forest.

The bounds depend on the production mechanism.

$$\lambda_{FS} \approx 1 \text{ Mpc} \left(\frac{\text{keV}}{m_s} \right) \left(\frac{\langle p_s \rangle}{3.15 T} \right)_{T \approx 1 \text{ keV}}$$

The ratio

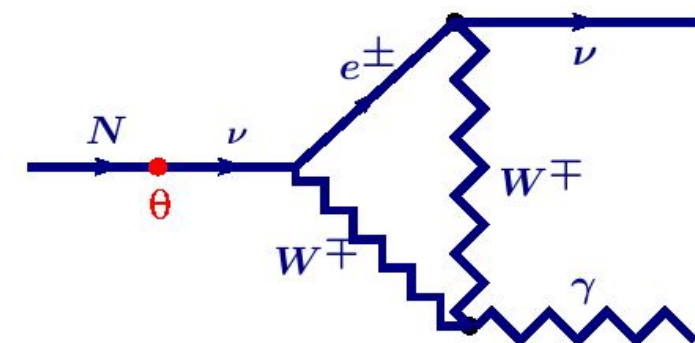
$$\left(\frac{\langle p_s \rangle}{3.15 T} \right)_{T \approx 1 \text{ keV}} = \begin{cases} 0.9 & \text{for production off — resonance} \\ 0.6 & \text{for MSW resonance (depends on } L) \\ 0.2 & \text{for production at } T > 100 \text{ GeV} \end{cases}$$

- Photon energy:

$$E_\gamma = \frac{M_1}{2}$$

- Radiative decay width

$$\Gamma = \frac{9\alpha_{\text{EM}} G_F^2}{256\pi^4} \theta^2 M_1^5$$



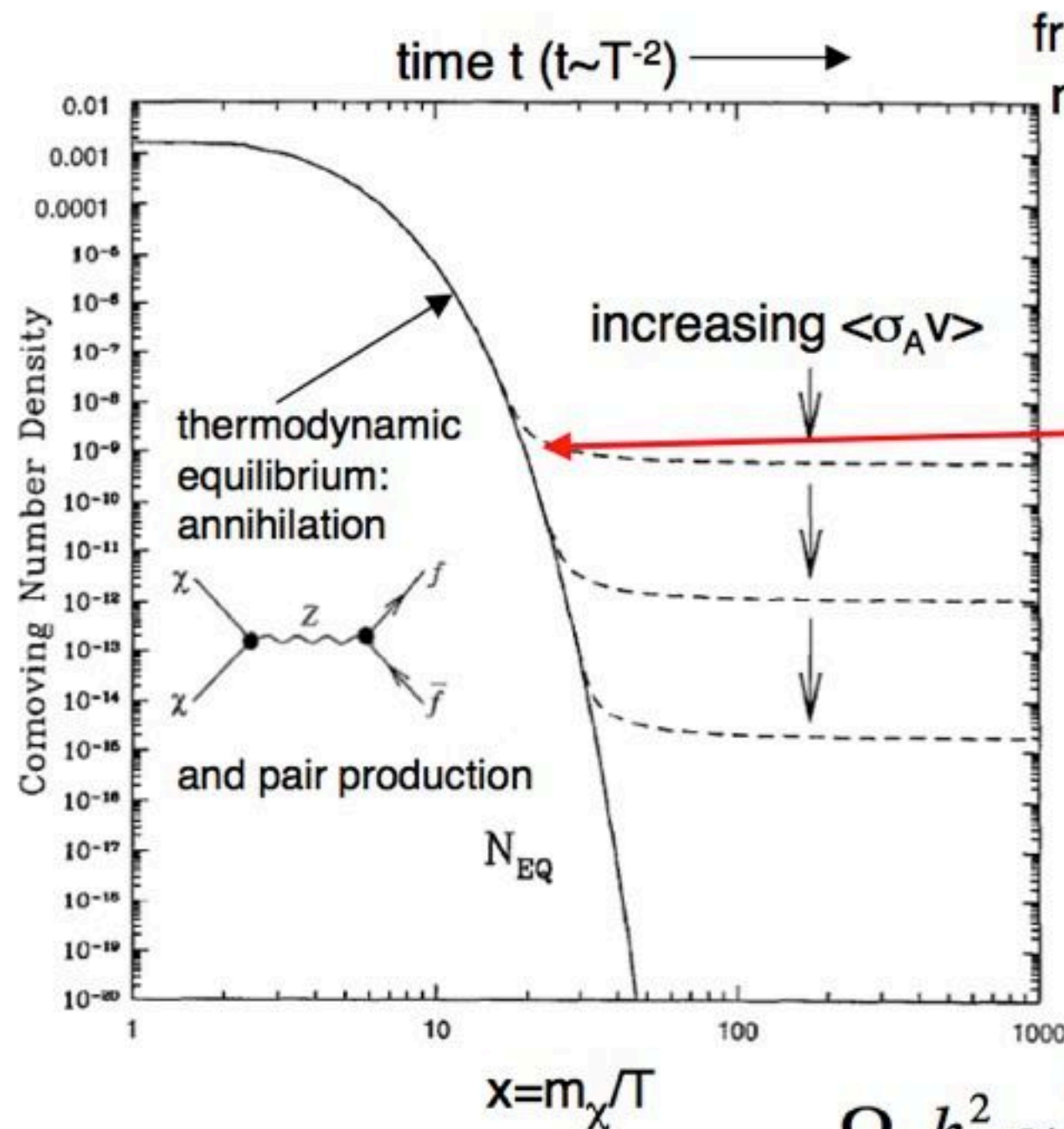
Dark matter made of sterile neutrino is not completely dark

Where to look for DM decay line?

- | | |
|---|---|
| ■ Extragalactic diffuse X-ray background (XRB) | Dolgov & Hansen, 2000; Abazajian et al., 2001
Mapelli & Ferrara, 2005; Boyarsky et al. 2005 |
| ■ Clusters of galaxies | Abazajian et al., 2001
Boyarsky et al. astro-ph/0603368 |
| ■ DM halo of the Milky Way.
Signal increases as we increase FoV! | Boyarsky et al. astro-ph/0603660
Riemer-Sørense et al. astro-ph/0603661
Boyarsky, Nevalainen, O.R. (in preparation) |
| ■ Local Group galaxies | Boyarsky et al. astro-ph/0603660
Watson et al. astro-ph/0605424 |
| ■ “Bullet” cluster 1E 0657-56 | Boyarsky, Markevitch, O.R. (in preparation) |
| ■ Cold nearby clusters | Boyarsky, Vikhlinin, O.R. (in preparation) |
| ■ Soft XRB | Boyarsky, Neronov, O.R. (in preparation) |

Need to find the best ratio between the DM decay *signal* and object's X-ray emission

CDM as particle Dark Matter



freeze-out of a weakly interacting massive particle (WIMP χ) when reaction rate drops below expansion rate

Cold Dark Matter:
 \triangleright non-relativistic

“survival of the weakest”
 At or below the weak scale

$$\Omega_\chi h^2 \approx \frac{m_\chi n_\chi}{\rho_c} \approx \frac{3 \times 10^{-27} \text{ cm}^3 / \text{sec}}{\langle \sigma_A v \rangle}$$