

Search for Majorana neutrinos in $K^{\pm} \rightarrow \pi^{\mp} \mu^{\pm} \mu^{\pm}$ decays Status Report

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NA62 Collaboration Meeting – Ferrara – 04/09/2014

Outline

- Motivations
- Method
- MC samples
- $K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$ Event selection
- Muon reconstruction and Efficiency
- Kaon flux
- Background sources
- Data-MC and Signal-Background study
- Statistical Framework
- Conclusions and Outlook

Motivations

- NA48/2 single event sensitivity for $K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$ decays $\sim 10^{-11}$
- Best UL: $BR(K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm) < 1.1 \times 10^{-9}$ @ 90% CL [Phys.Lett. **B697**, 107 (2011)]
Based on 52 data events observed VS 52.6 ± 19.8 expected ($K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ MC)
- The world strongest constraints to the sterile-active mixing parameter $|U_{\mu 4}|$ for **heavy Majorana neutrinos** with $m_\pi + m_\mu < m_N < m_K - m_\mu$ can be obtained from $K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$ search in the NA48/2 data:

$$\begin{aligned}
 BR(K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm) &\ll 10^{-13} && \text{for } m_N \ll m_K \text{ or } m_N \gg m_K \\
 BR(K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm) &= \tau_K \frac{G_F^4 m_K}{128 \pi^2} f_K^2 f_\pi^2 |V_{us} V_{ud}|^2 \frac{m_N^5}{\Gamma_N} |U_{\mu 4}|^4 \varphi_{\mu\mu} && \text{for } m_\pi + m_\mu < m_N < m_K - m_\mu \\
 &\approx 10^{-19} \text{ GeV} \times \frac{1}{\Gamma_N} |U_{\mu 4}|^4 && [\text{@ } m_N = 300 \text{ MeV}/c^2] \\
 &\approx 10^{-7} \text{ ps}^{-1} \times \tau_N |U_{\mu 4}|^4
 \end{aligned}$$

To reach the same limit on $|U_{\mu 4}|$ for $m_\pi + m_\mu < m_N < m_K - m_\mu$ and same τ_N , the ULs on $BR(h^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm)$ [$h = B, D$ and D_s] must be 10^6 , 10^3 and 10^2 times smaller than the one on $BR(K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm)$

Method

- Blind analysis: $m_{\pi\mu\mu} < 0.48 \text{ GeV}/c^2$ for data [SR: $|m_{\pi\mu\mu} - m_K| < 5 \text{ MeV}/c^2$]
Event selection finalised by studying MC simulations (Signal + Bkg)
- Reconstructed 3-trk vertex: sensitive to neutrino lifetimes $\tau_N \leq 10 \text{ ps}$
lifetime scan $\tau_N = 0 \rightarrow 10 \text{ ps}$: to be done soon
- [Future development: **displaced vertex** studies (to be done soon)]
- Number N_K of kaon decays in the fiducial volume from $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ decays
 - Same trigger used for the $K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$ search
 - Similar kinematics ($m_\mu/m_\pi = 0.76$)
 } First order cancellation of systematic effects due to trigger inefficiency
- Signal acceptance $\varepsilon_{\pi\mu\mu}$ estimated from $K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$ MC
- Upper Limit for the number of signal events $N(K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm)$ in data to be obtained from statistical analysis: observed events VS expected (bkg only)
- Upper Limit for the $\text{BR}(K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm)$ to be estimated using the relation

$$\text{BR}(K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm) = \frac{N(K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm)}{N_K \varepsilon_{\pi\mu\mu}}$$

MC Samples

Signal acceptance $\varepsilon_{\pi\mu\mu}$ study

- Three $K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$ samples, 10M each



1. Resonance [Atre *et al.*, JHEP 0905,030 (2009)]: $K^\pm \rightarrow N\mu^\pm + N \rightarrow \pi^\mp \mu^\pm$
[for this talk: $m_N = 300$ MeV, $\Gamma_N = 1$ MeV; scan in m_N and in Γ_N in progress]

2. “Scalar”: flat phase space



3. “Vector”: $K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$ -like (with form factor $|W(z)| = 1$)
[contacts with J. Kamenik for model-independent treatment]

} for comparison

- Two $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ samples, 10G+12G produced with the FULL (optimised) MC mode (see my talk @ NA48/2 Analysis Meeting, 17/10/2013)

- 1st: used exclusively to finalise the event selection;



- 2nd: used to estimate the number of expected bkg events

- Other bkg sources:



- $K^\pm \rightarrow \pi^\pm \pi^\mp \mu^\pm \nu$ (100M), $K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$ (10M) and $K^\pm \rightarrow \mu^+ \mu^- \mu^\pm \nu$ (10M)

Final $K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$ event selection

- At least one 3-track vertex with
 - total $Q = \pm 1$ and $\chi^2 < 20$
 - all the vertex tracks with $3 \text{ GeV}/c < p < 60 \text{ GeV}/c$ and within DCH, LKr, MUV* acceptances * $\sim 2 \text{ cm}$ MUV shift detected (see my talk 19/12/13)
 - $P_t^2 < 0.0001 \text{ GeV}^2/c^2$, $|\mathbf{P}_{\text{tot}} - 60 \text{ GeV}/c| < 5 \text{ GeV}/c$
 - VtxZ within $(-1800, 8000) \text{ cm}$
 - Max 2-trk Vtx distance $< 5 \text{ m} + \text{max 2-trk CDA} < 3 \text{ cm}$
- π ID: $E/p < 0.95$, $!(\text{MUV1}\&\text{MUV2})^{**}$
- μ ID: $E/p < 0.2$, $\text{MUV1}\&\text{MUV2}^{**}$
- $P_\pi > 15 \text{ GeV}/c$, $P_\mu > 5 \text{ GeV}/c$
- Trk-Trk Dist $> 2 \text{ cm}$ @ DCH, $> 20 \text{ cm}$ @ LKr, $> 20 \text{ cm}$ @ MUV1
- μ - μ dist > 0 (NO muon duplication), Max Trk- μ dist $< 35 \text{ cm}$
- Signal Region: $|\mathbf{m}_{\pi\mu\mu} - m_K| < 5 \text{ MeV}/c^2 (= 2\sigma)$

** MUV search radius multiplier = 2.5



Comparison with $K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$ selection*

* Phys.Lett. **B697**, 107 (2011)

Published UL can be related to **single point $\tau_N = 0$** , no mass dependence

– 3-track vertex:

- $K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$: $\chi^2 < 40$
- New: $\chi^2 < 20 + \max 2\text{-trk Vtx dist} < 5 \text{ m} + \max 2\text{-trk CDA} < 3 \text{ cm}$
 → Acceptance: -1.5% (abs.) or -7% (rel.)

– Total Momentum:

- $K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$: $P_t^2 < 0.0005 \text{ GeV}^2/c^2$, $|P_{\text{tot}} - 60 \text{ GeV}/c| < 6 \text{ GeV}/c$
- New: $P_t^2 < 0.0001 \text{ GeV}^2/c^2$, $|P_{\text{tot}} - 60 \text{ GeV}/c| < 5 \text{ GeV}/c$
 → Acceptance: -2.5% (abs.) or -10% (rel.)

– Track Momentum:

- $K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$: $P_{\text{trk}} > 10 \text{ GeV}/c$
- New: $P_\pi > 15 \text{ GeV}/c$, $P_\mu > 5 \text{ GeV}/c$
 → Acceptance: +6% (abs.) or +42% (rel.)



Comparison with $K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$ selection*

* Phys.Lett. **B697**, 107 (2011)

– Particle ID:

- $K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$: π : $E/p < 0.95$, no associated muon
 μ : $E/p < 0.2$, MUV1&MUV2
- New: π : $E/p < 0.95$, !(MUV1&MUV2)**
 μ : $E/p < 0.2$, MUV1&MUV2** + μ - μ dist > 0
+ Max Trk- μ dist < 35 cm

→ Acceptance: +7% (abs.) or +47% (rel.)

** MUV search radius multiplier = 2.5

– Signal Region:

- $K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$: $|m_{\pi\mu\mu} - m_K| < 8 \text{ MeV}/c^2 (= 3.2\sigma)$
- New: $|m_{\pi\mu\mu} - m_K| < 5 \text{ MeV}/c^2 (= 2\sigma)$

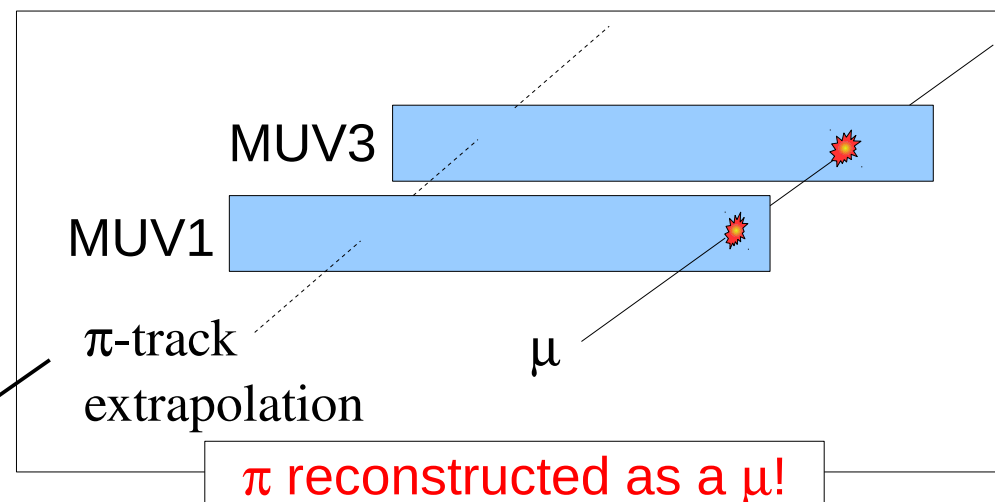
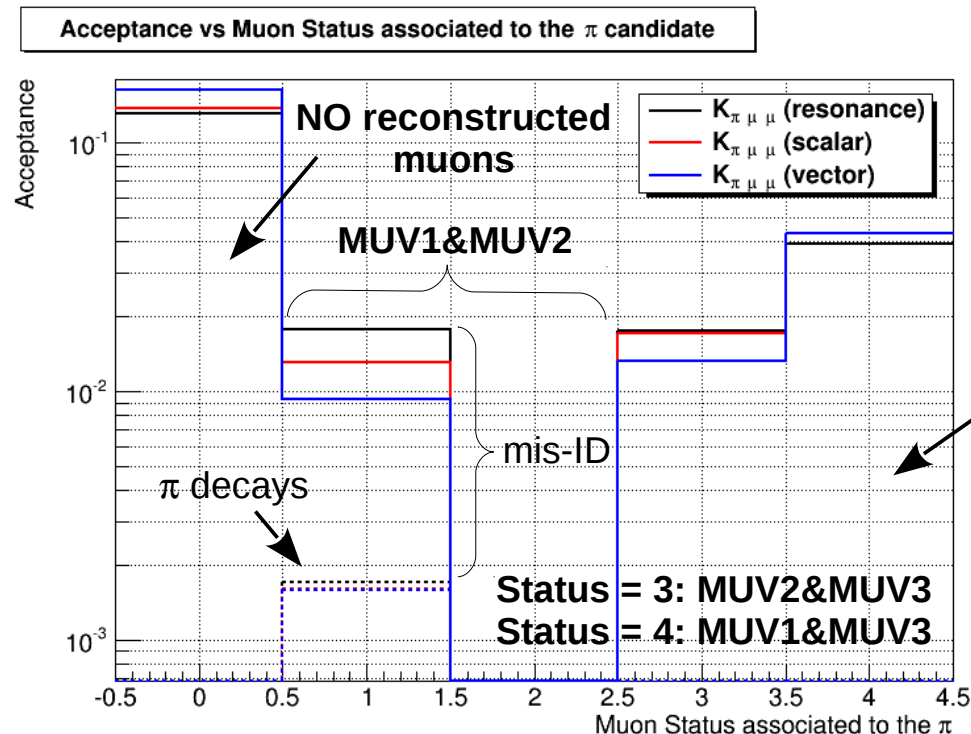
→ Acceptance: -1.2% (abs.) or -5% (rel.)

Published* acceptance:
 $\epsilon(K^\pm \rightarrow \pi^\pm \mu^+ \mu^-) = 16.97\%$

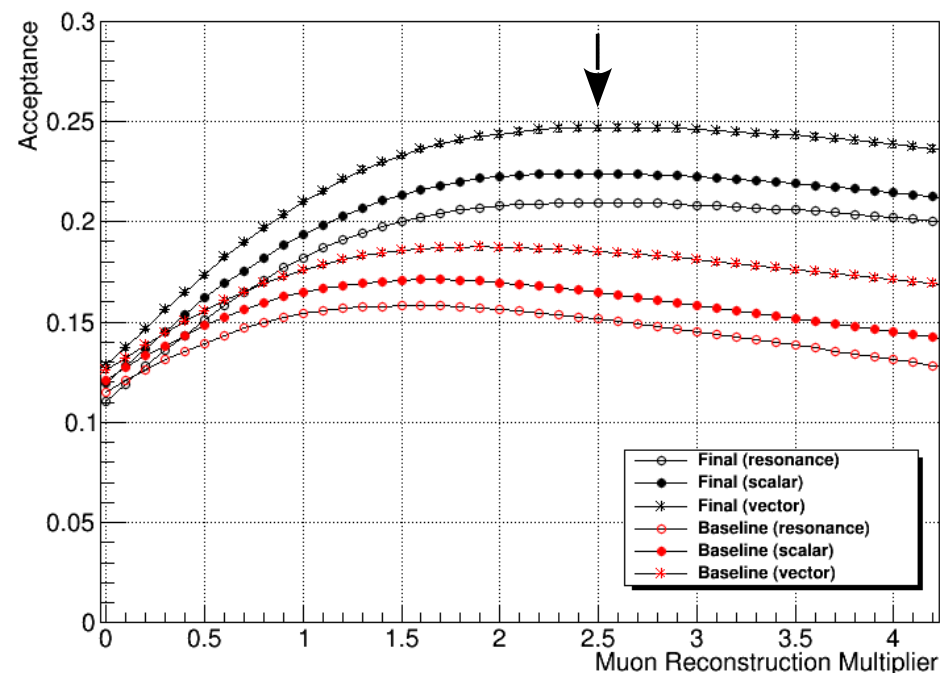
Total Acceptance: +6% (abs.) or +40% (rel.)

- $K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$: $\epsilon_{\pi\mu\mu}^{(r)} = (13.28 \pm 0.01)\%$ $\epsilon_{\pi\mu\mu}^{(s)} = (14.73 \pm 0.01)\%$, $\epsilon_{\pi\mu\mu}^{(v)} = (17.25 \pm 0.01)\%$
- New: $\epsilon_{\pi\mu\mu}^{(r)} = (19.44 \pm 0.01)\%$ $\epsilon_{\pi\mu\mu}^{(s)} = (20.62 \pm 0.01)\%$, $\epsilon_{\pi\mu\mu}^{(v)} = (22.75 \pm 0.01)\%$

Muon Reconstruction



Acceptance VS Muon Reconstruction Multiplier



Pions are allowed to be associated to reconstructed muons with status 3 or 4
→ **Acceptance:** +6% (abs.) or +40% (rel.)

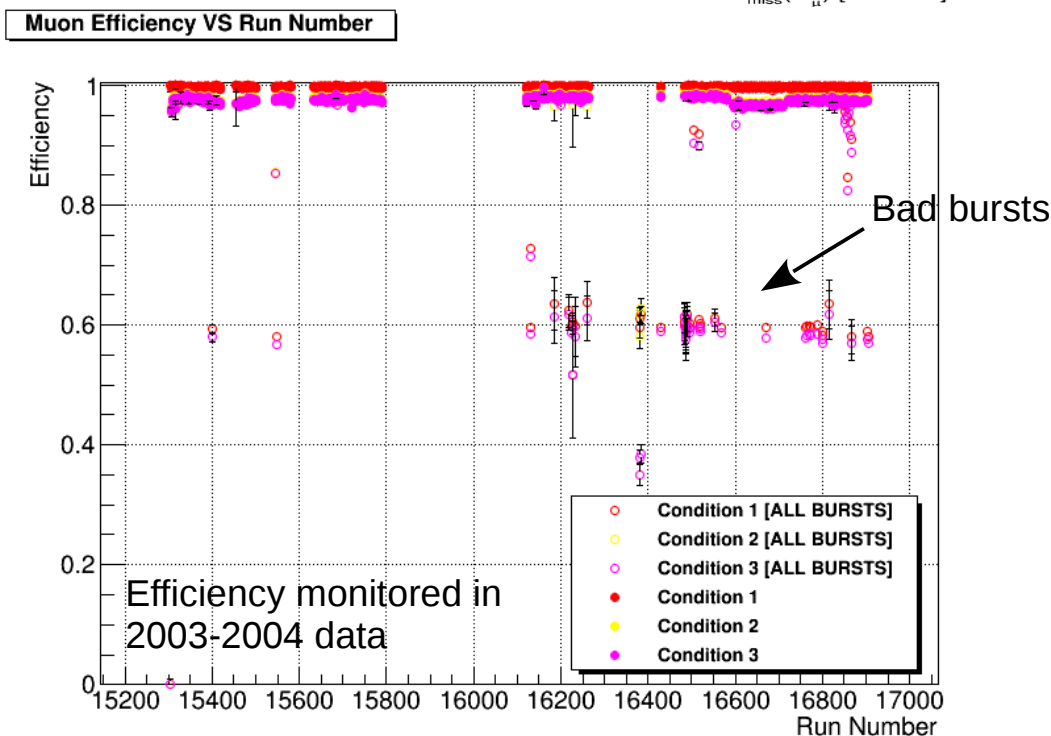
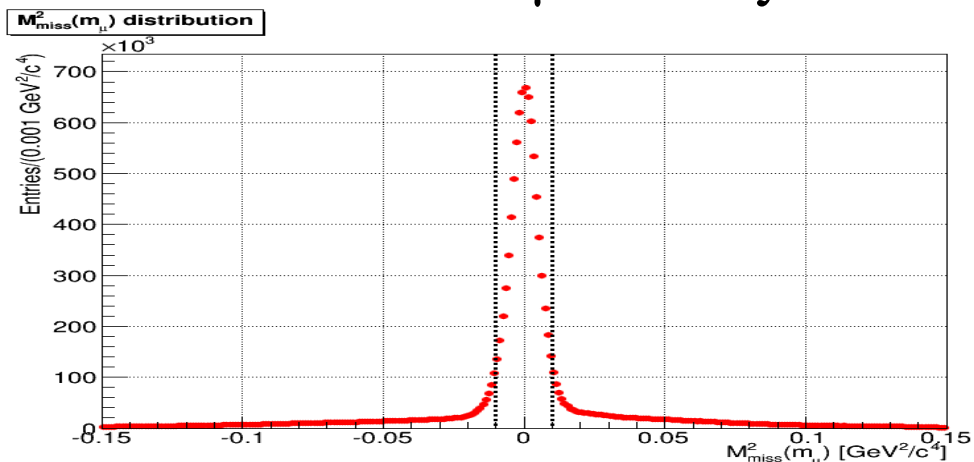
Search Radius Multiplier set to $m=2.5$
→ **Acceptance:** +1% (abs.) or +5% (rel.)

Total μ Reco: +7% (abs.) or +47% (rel.)



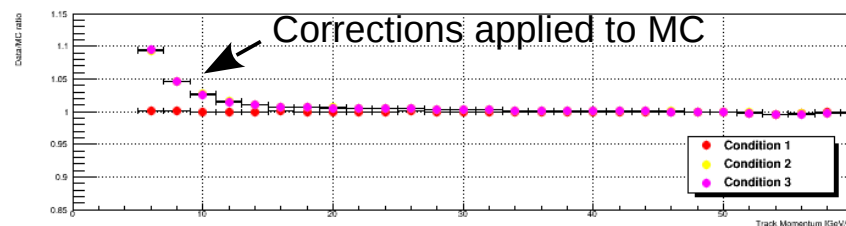
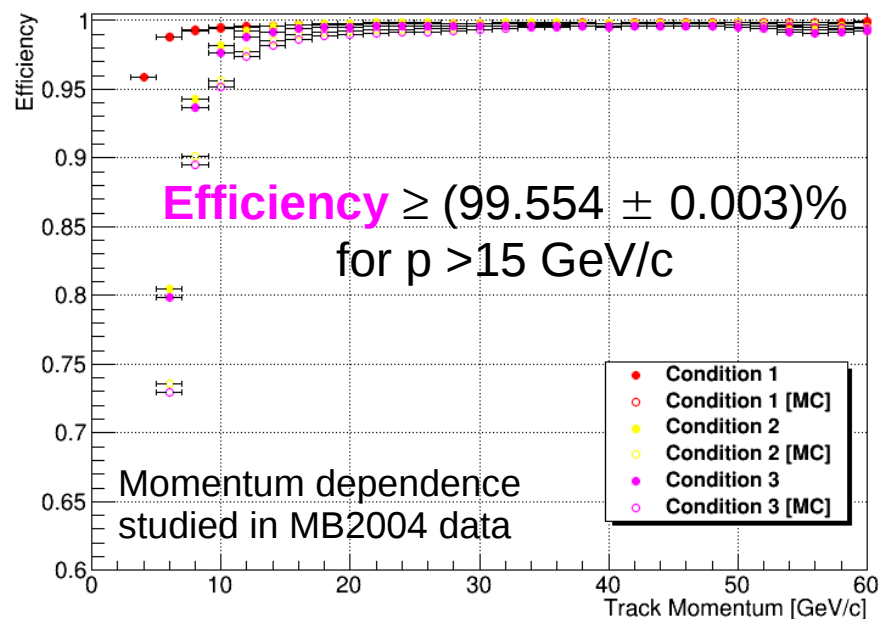
Muon Efficiency

Reconstructed $K^\pm \rightarrow \mu^\pm \nu$ decays with applying NO μ -ID requirements



Condition 1: $E/p < 0.2$
Condition 2: MUV1 & MUV2
Condition 3: Condition 1 & Condition 2

Muon Efficiency VS Track Momentum





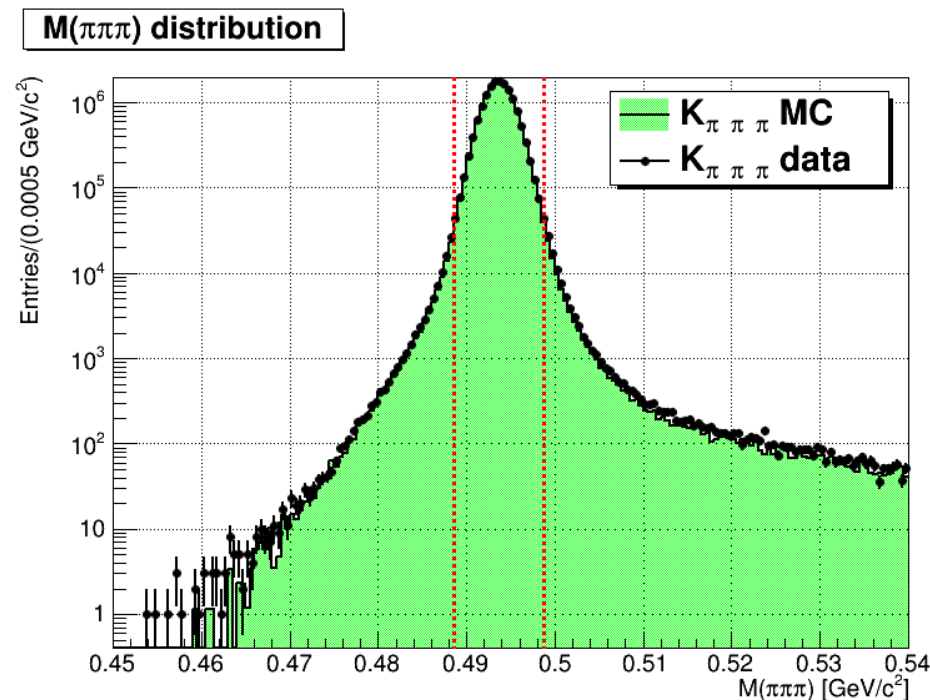
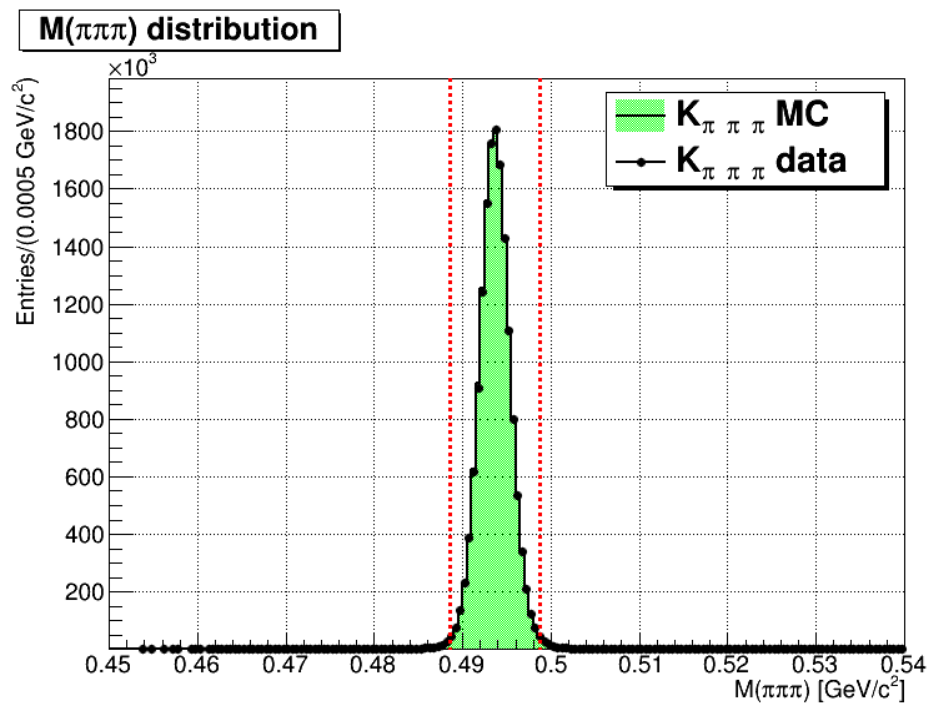
Kaon Flux

Published flux: $N_K^{\text{tot}} = 1.9 \times 10^{11}$

- $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ selection: same requirements as $K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$ except
 - No particle ID for same-sign tracks;
 - Requirement $|m_{\pi\mu\mu} - m_K| < 5 \text{ MeV}/c^2$ replaced by $|m_{\pi\pi\pi} - m_K| < 5 \text{ MeV}/c^2$
- Acceptance $\varepsilon_{\pi\pi\pi} = (14.721 \pm 0.004)\%$

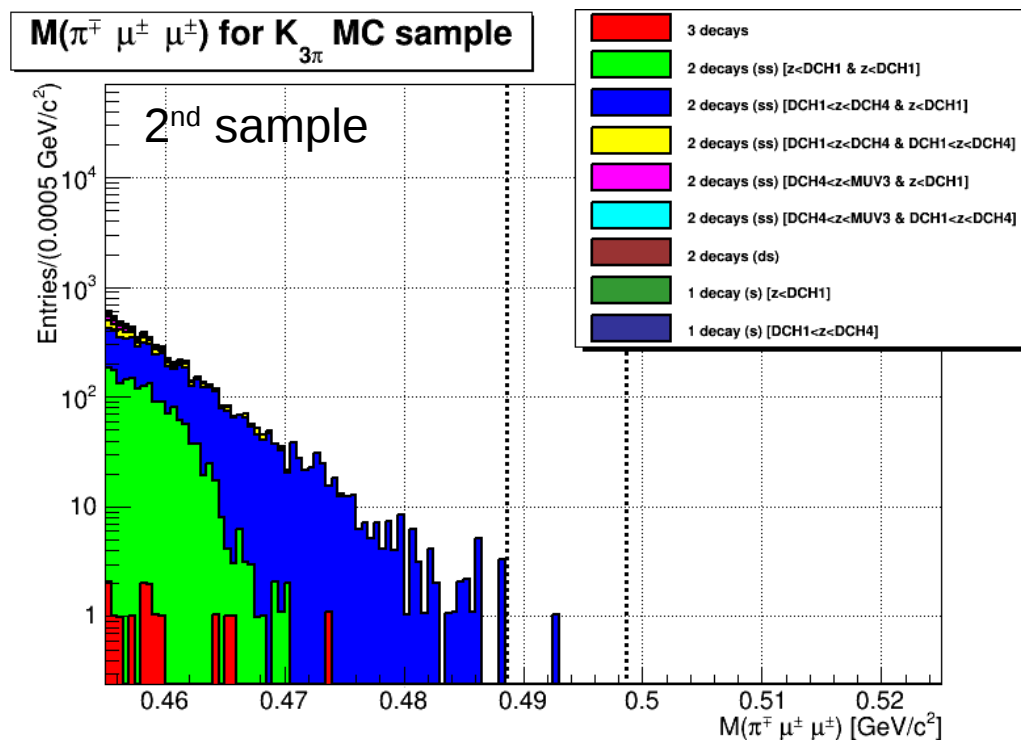
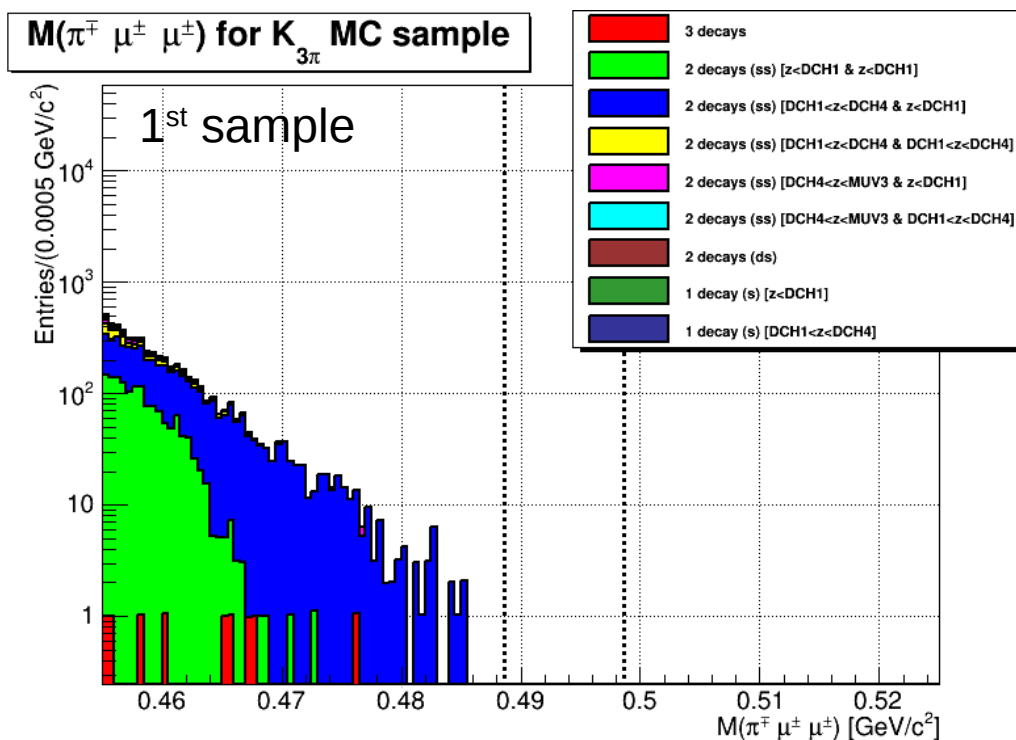
No MUV bad bursts (-3.7%)

$$N_K^{\text{tot}} = (1.901 \pm 0.014) \times 10^{11}, \quad N_K = (1.832 \pm 0.014) \times 10^{11}$$



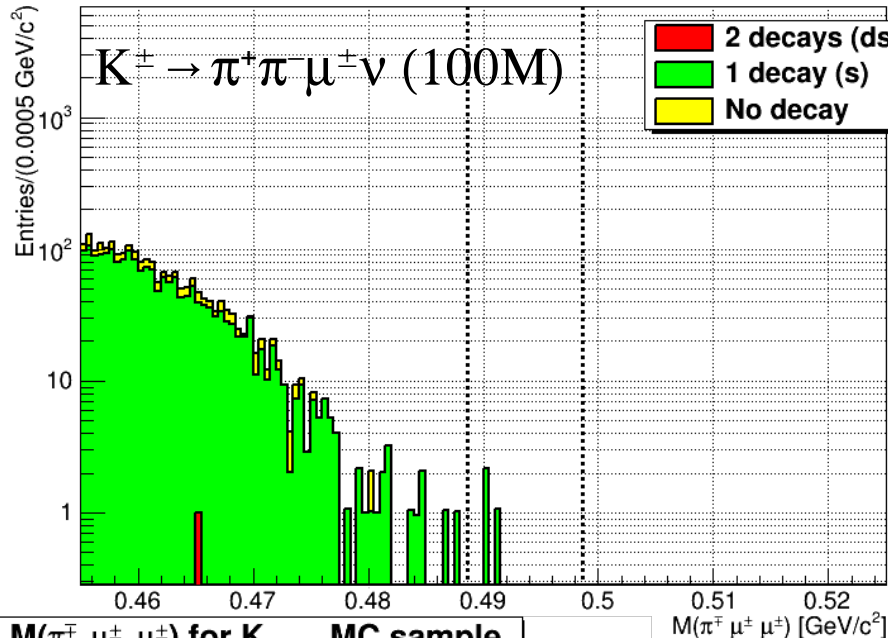
$K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ background

- Two MC samples to avoid bias due to the choice of $K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$ selection
 - 1st sample [10G, used exclusively to finalise the event selection]: 0 events
 -  2nd sample [12G, used to estimate the number of expected bkg events]: 1 event
- $\rightarrow 0.97 \pm 0.97_{\text{stat}} \pm 0.01_{\text{syst}}$ expected $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ events



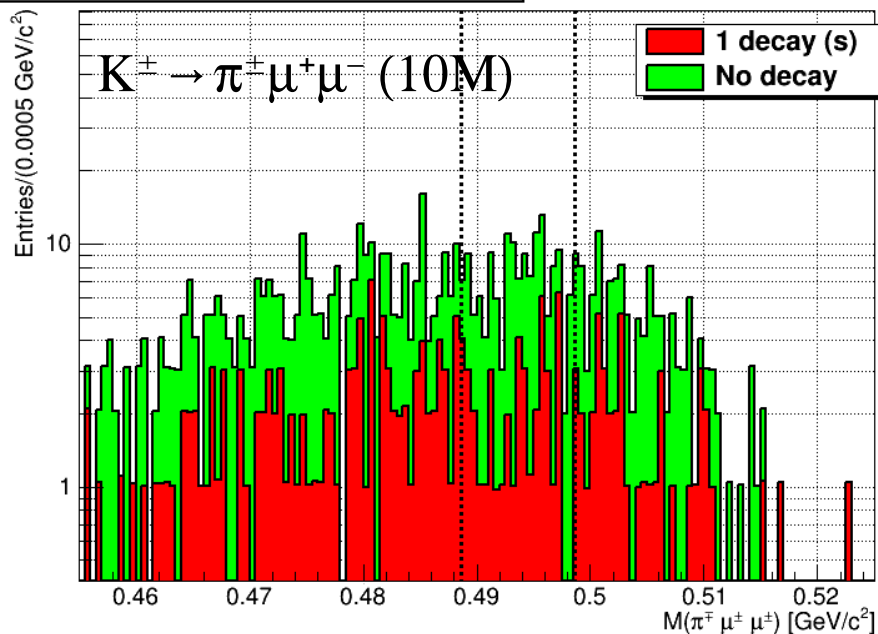
Other backgrounds NEW

$M(\pi^\mp \mu^\pm \mu^\pm)$ for $K_{\mu 4}$ MC sample

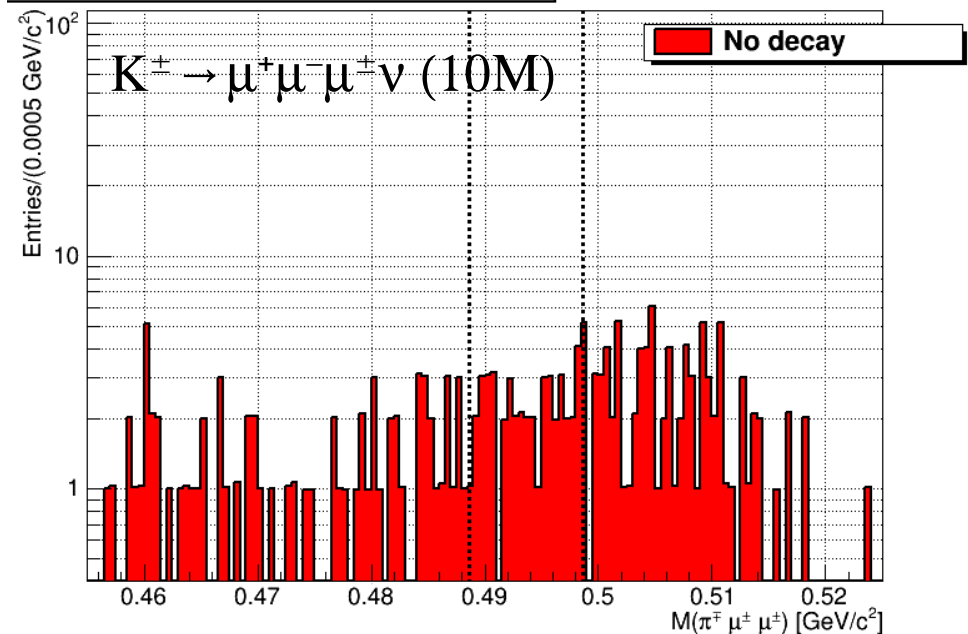


- $K^\pm \rightarrow \pi^\pm \pi^\mp \mu^\pm \nu$ (100M): 3 events
 $\rightarrow 0.09 \pm 0.05_{\text{stat}} \pm 0.06_{\text{syst}}$ expected
- $K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$ (10M): 147 events
 $\rightarrow 0.29 \pm 0.02_{\text{stat}} \pm 0.02_{\text{syst}}$ expected
- $K^\pm \rightarrow \mu^+ \mu^- \mu^\pm \nu$ (10M): 48 events
 $\rightarrow 0.013 \pm 0.001_{\text{stat}} \pm 0.010_{\text{syst}}$ expected

$M(\pi^\mp \mu^\pm \mu^\pm)$ for $K_{\pi^+ \mu^+ \mu^-}$ MC sample



$M(\pi^\mp \mu^\pm \mu^\pm)$ for $K_{\mu^+ \mu^- \mu^\pm \nu}$ MC sample

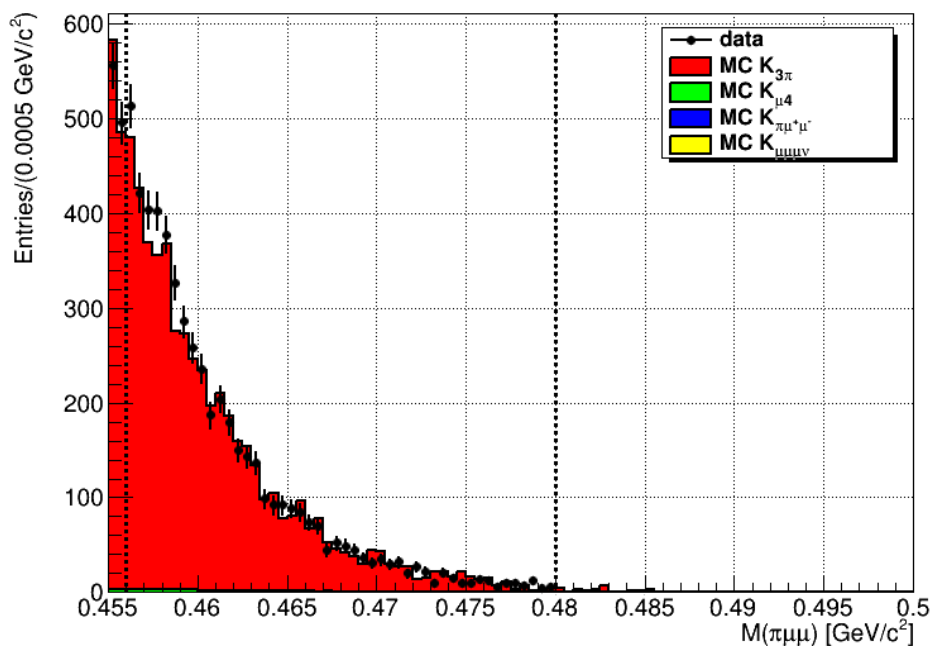


Data-MC comparison in CR

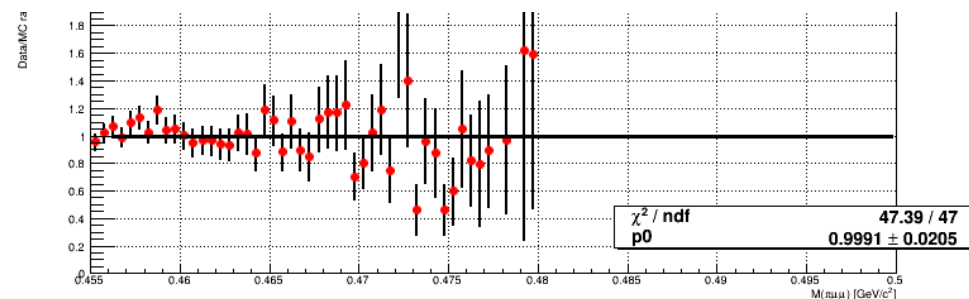
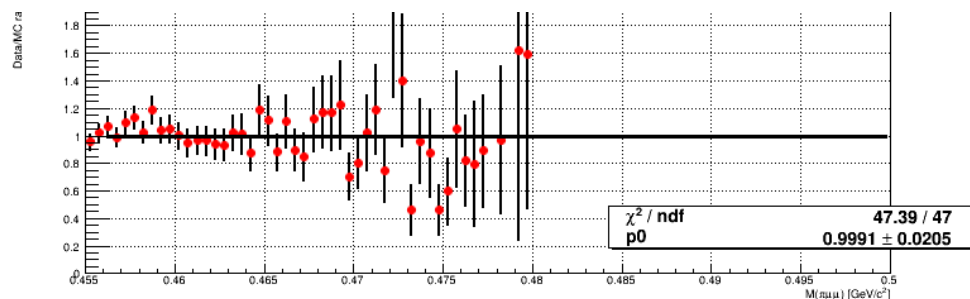
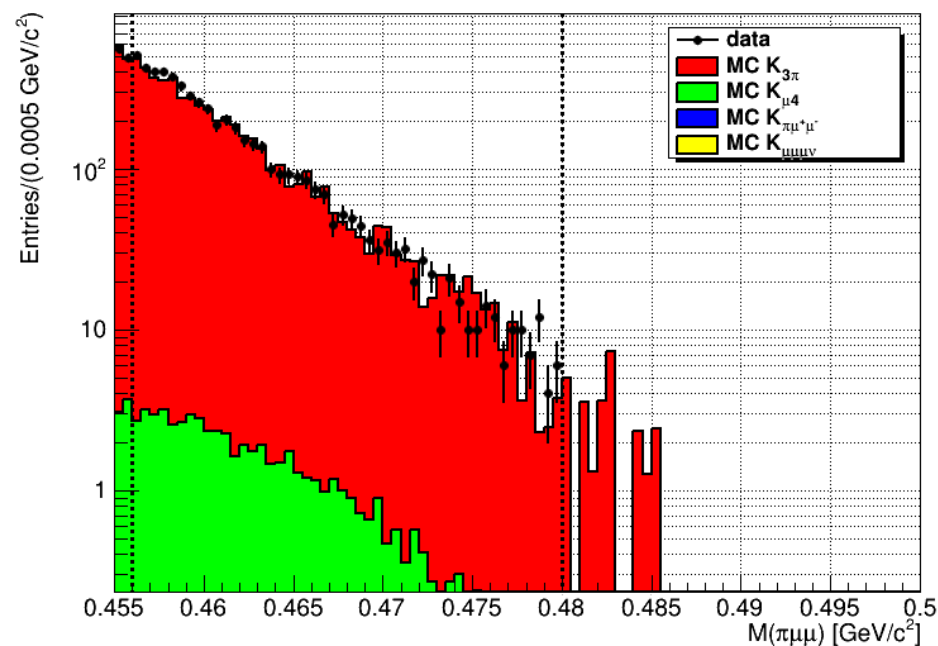
- For each variable, final $K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$ selection except
 - any cut on the variable itself
 - SR requirement changed on purpose to CR requirement

$$\text{CR: } 0.456 \text{ GeV}/c^2 < m_{\pi\mu\mu} < 0.48 \text{ GeV}/c^2$$

$M(\pi\mu\mu)$ distribution

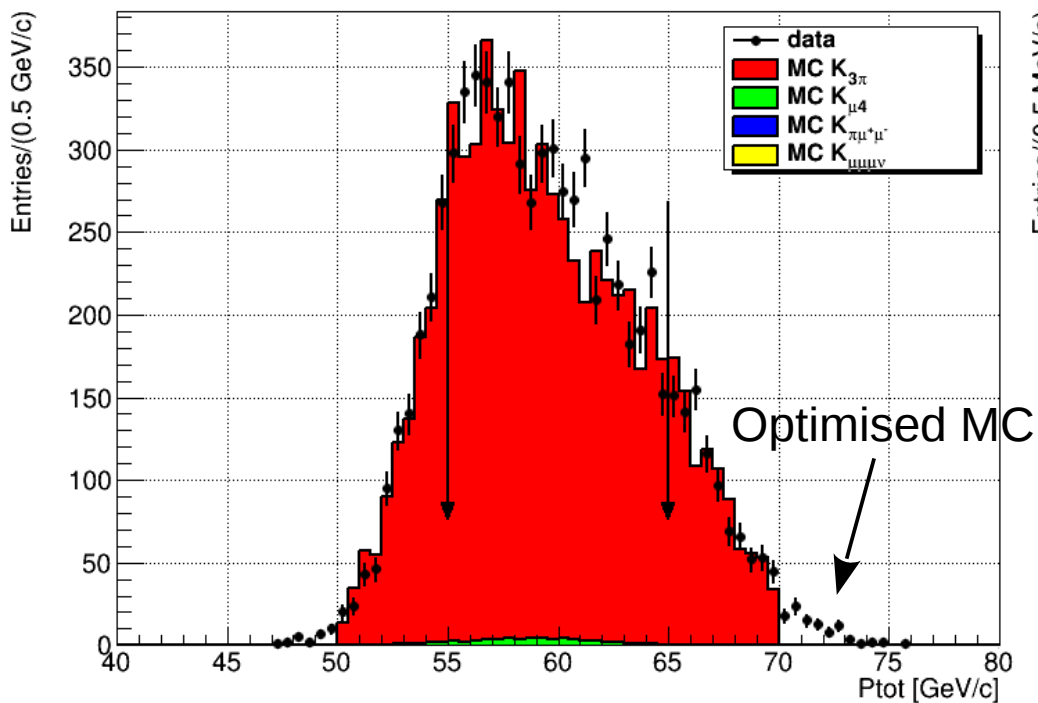


$M(\pi\mu\mu)$ distribution

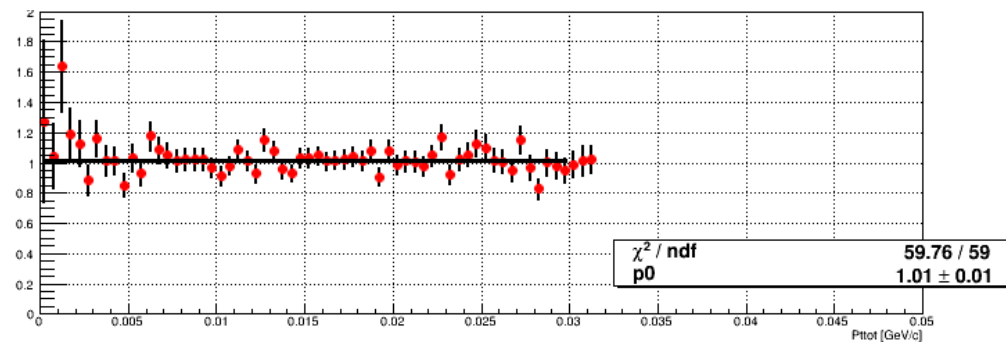
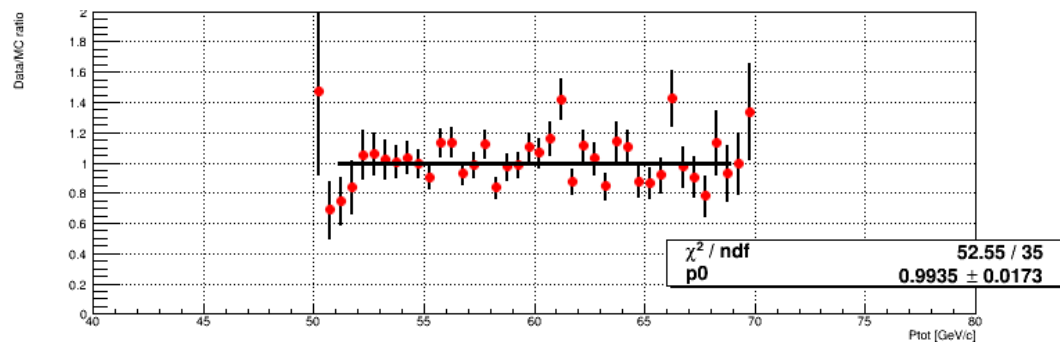
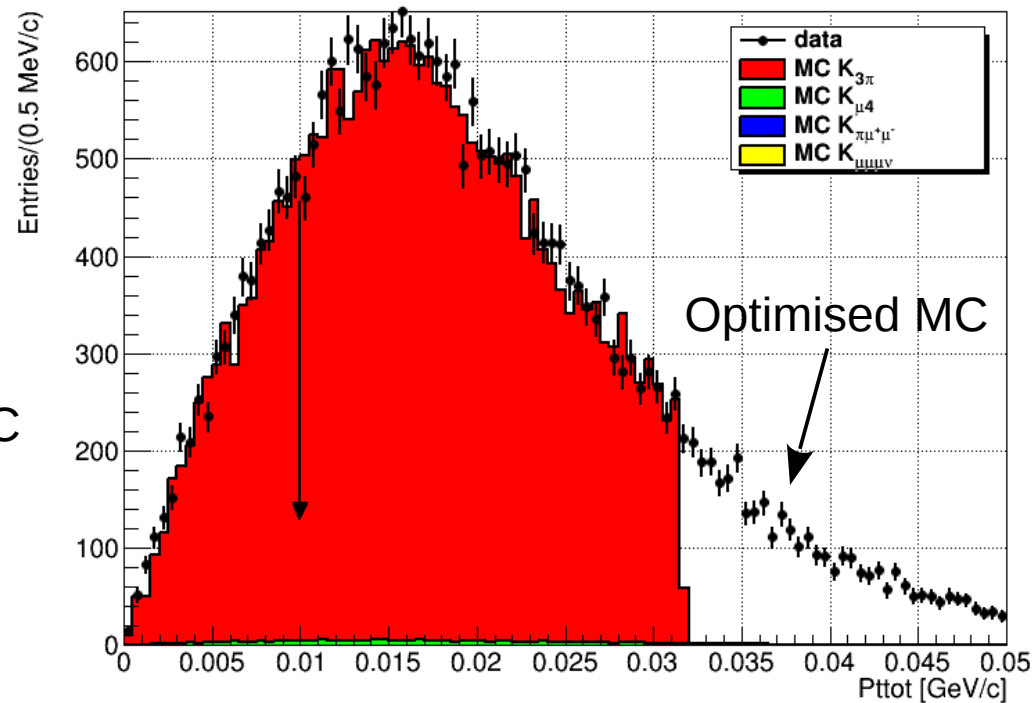


Data-MC comparison in CR

Total Momentum distribution

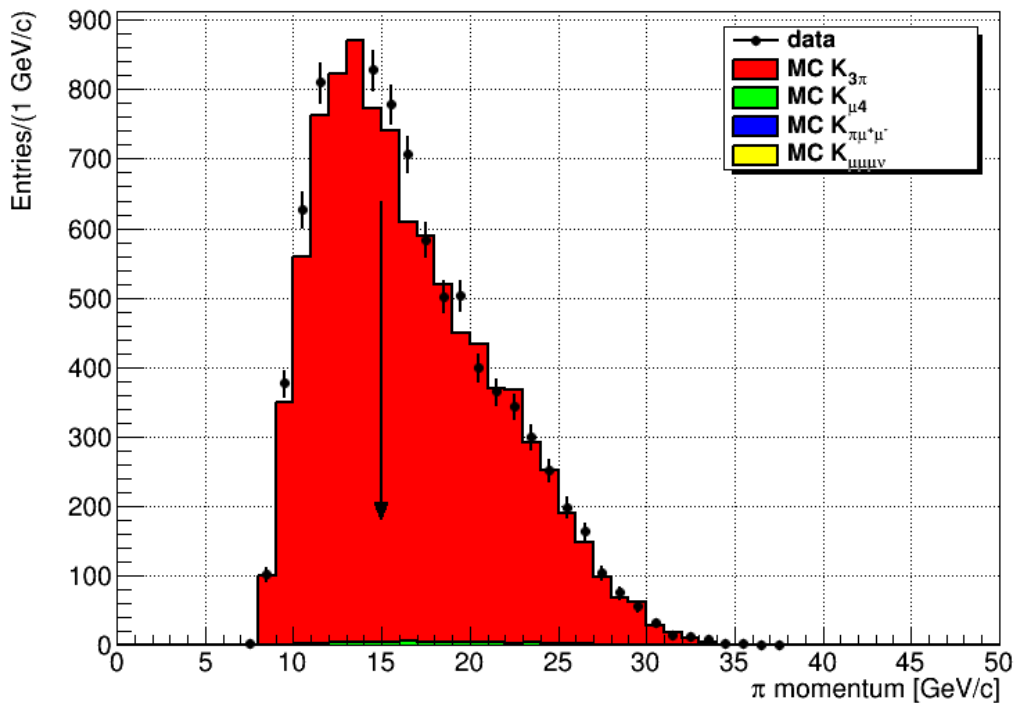


Total Transverse Momentum distribution

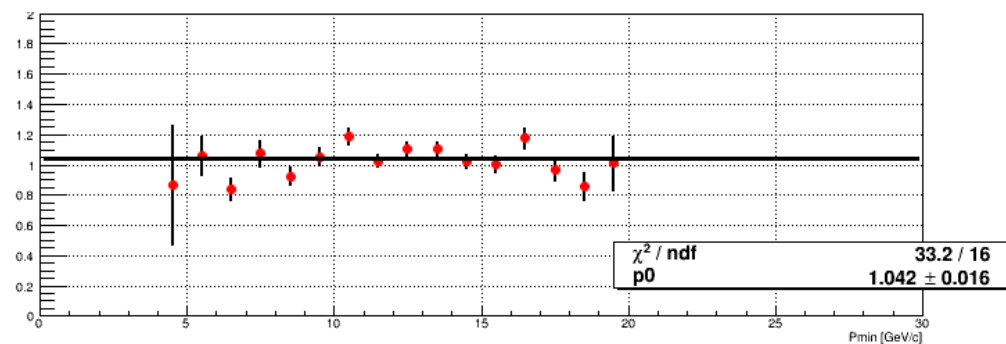
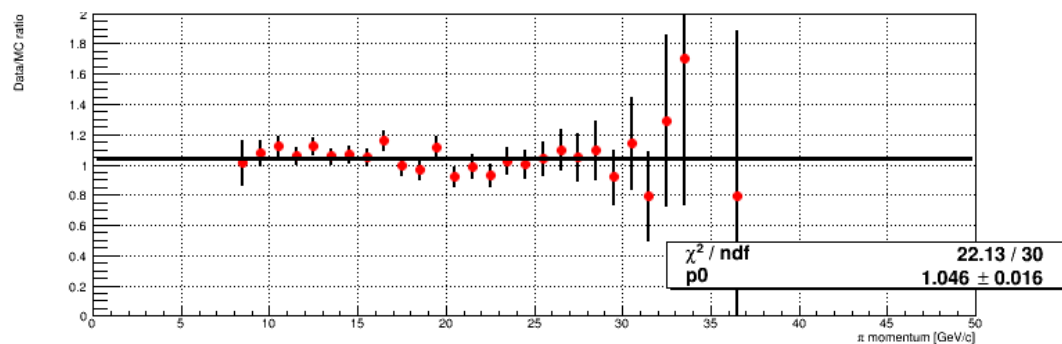
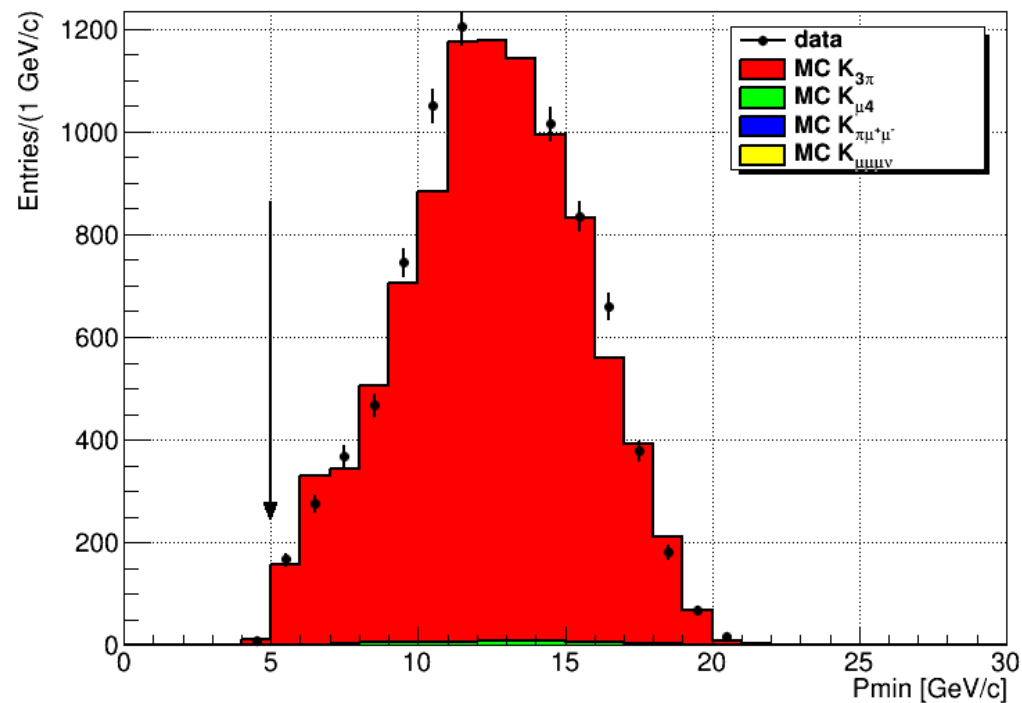


Data-MC comparison in CR

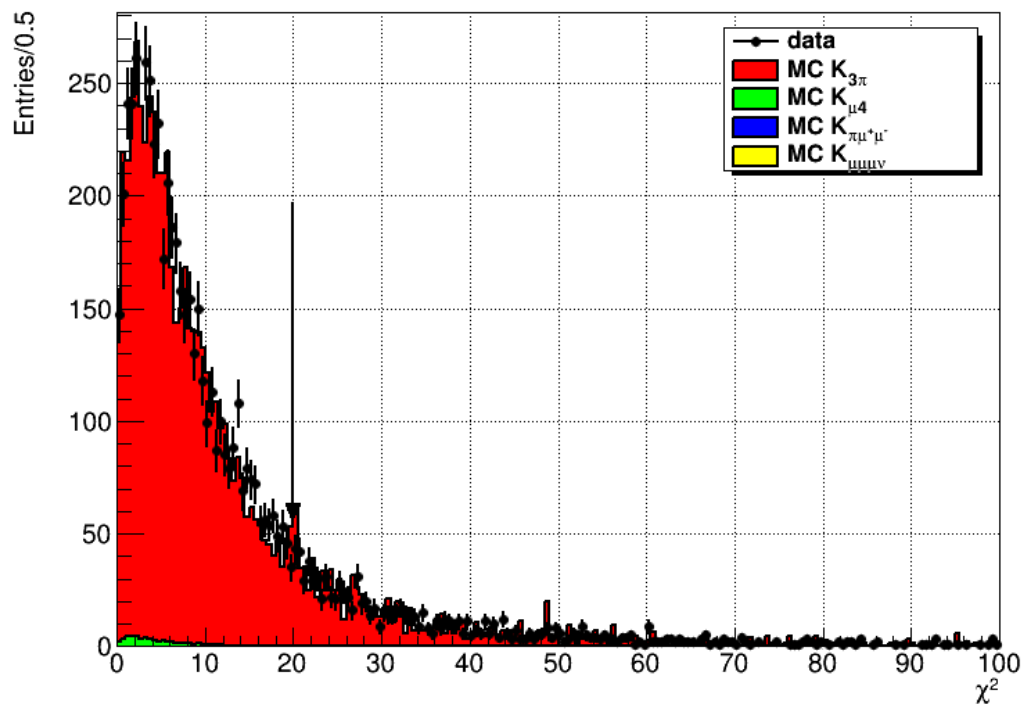
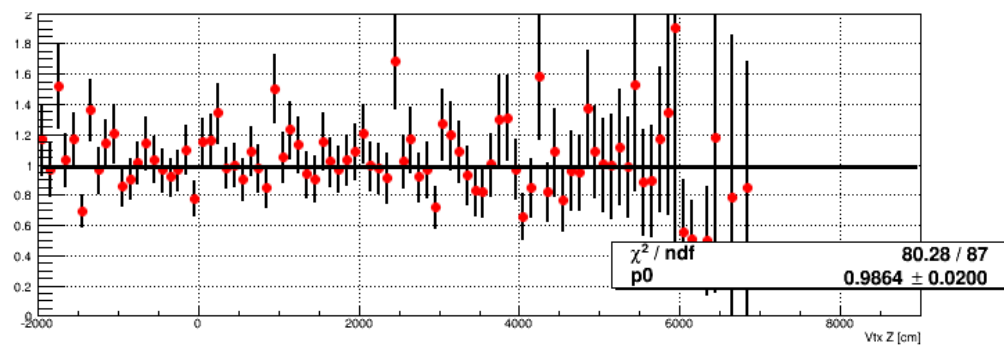
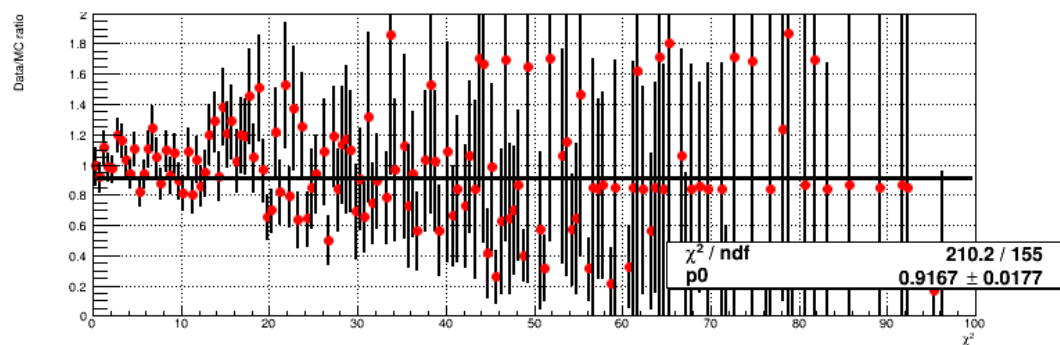
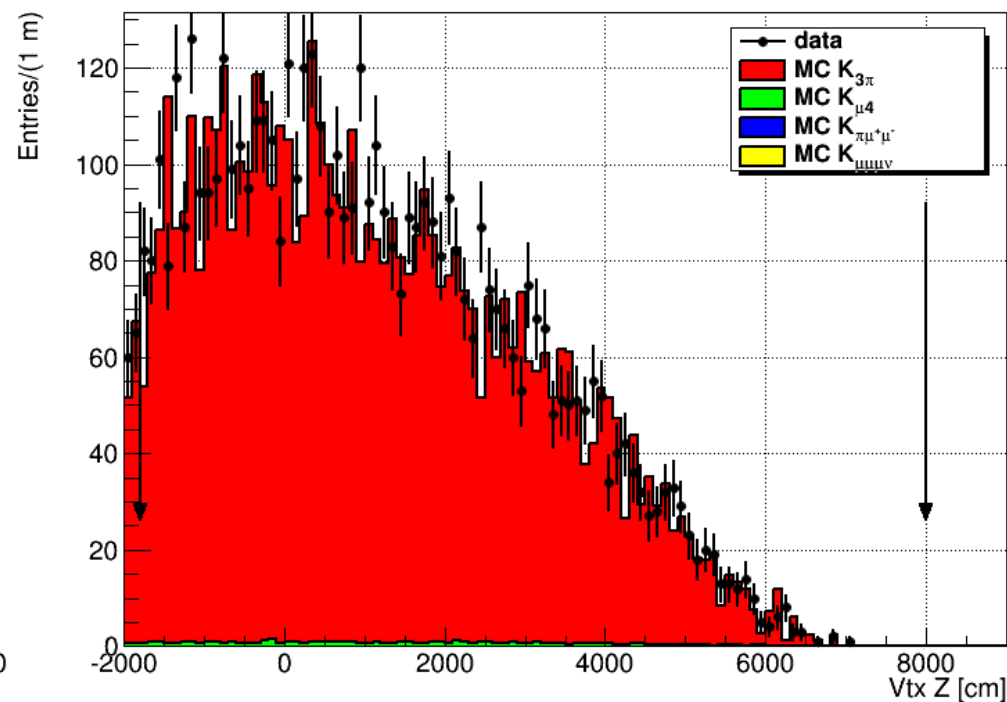
π candidate momentum distribution



Momentum distribution of the lowest momentum track

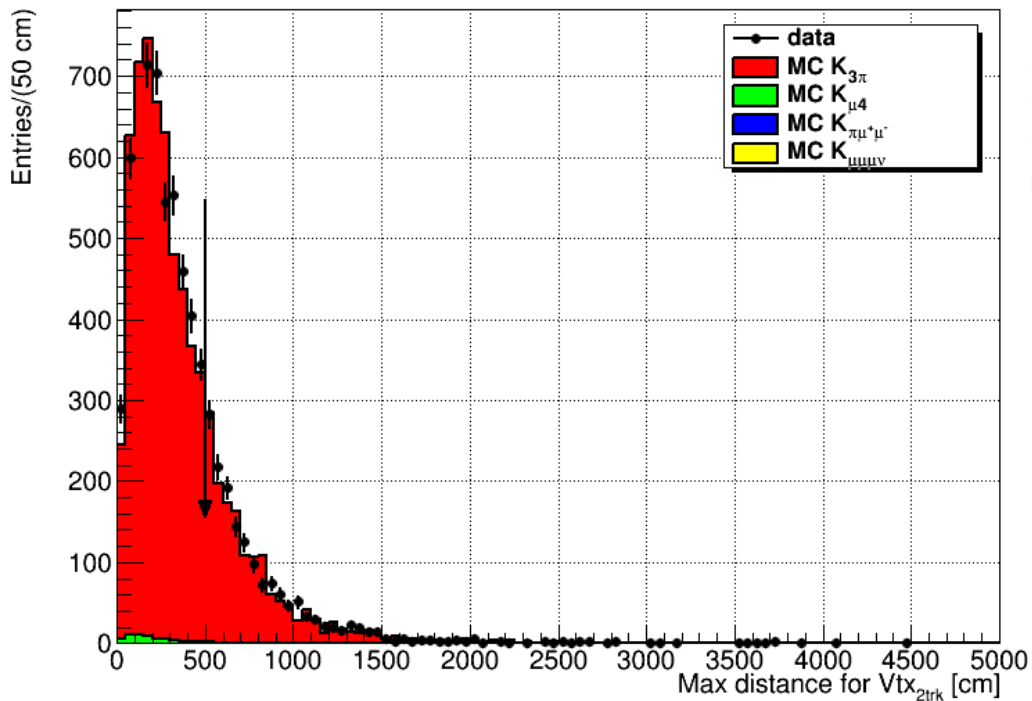


Data-MC comparison in CR

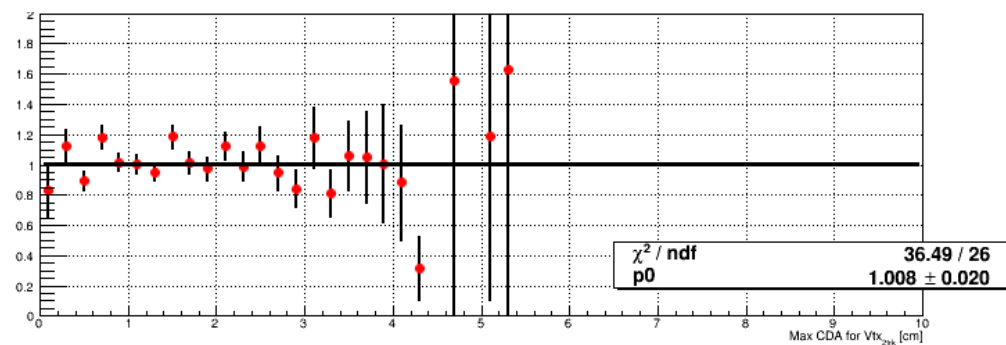
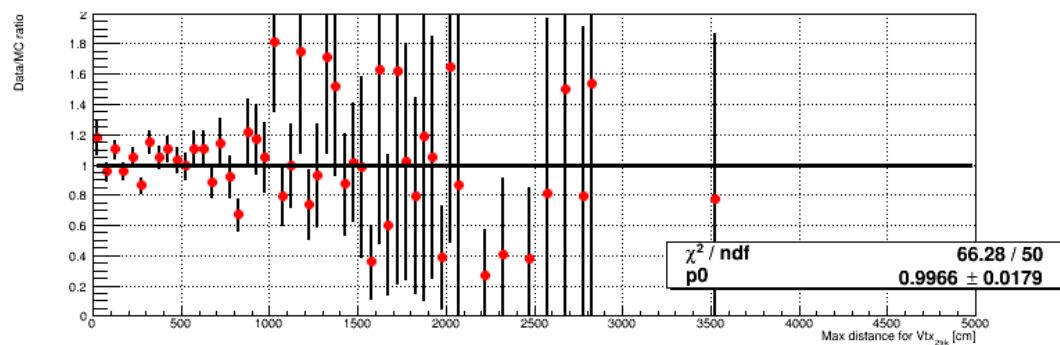
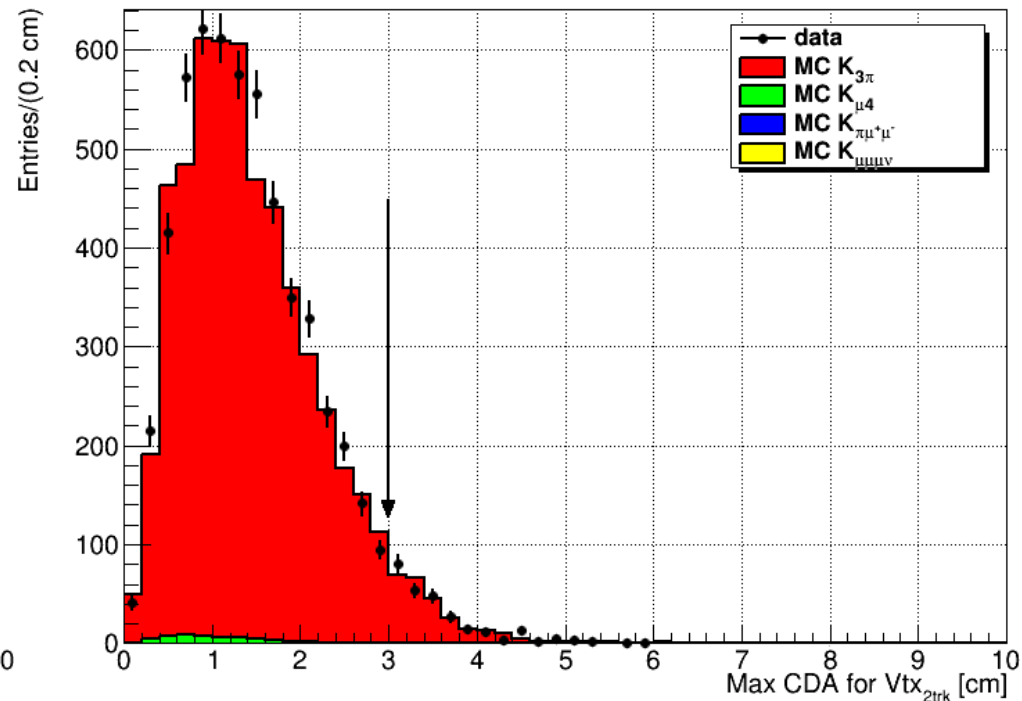
3-track χ^2 distribution

3-track Vertex z distribution


Data-MC comparison in CR

Max Distance for 2trk Vertexes

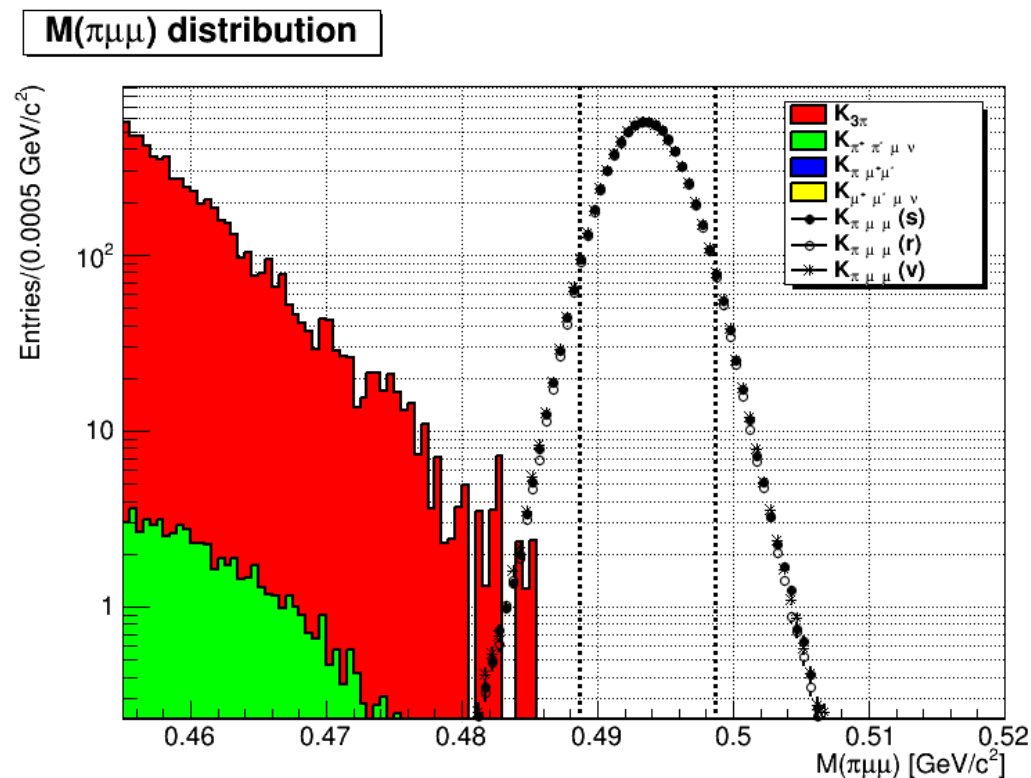
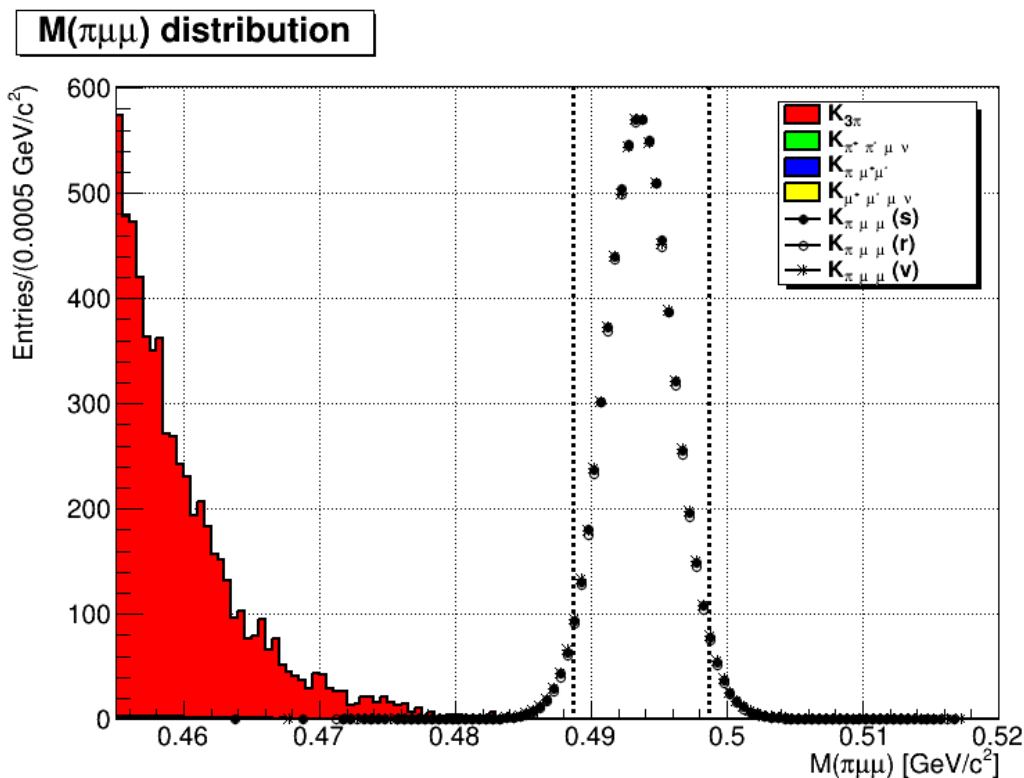


Max CDA for 2trk Vertexes

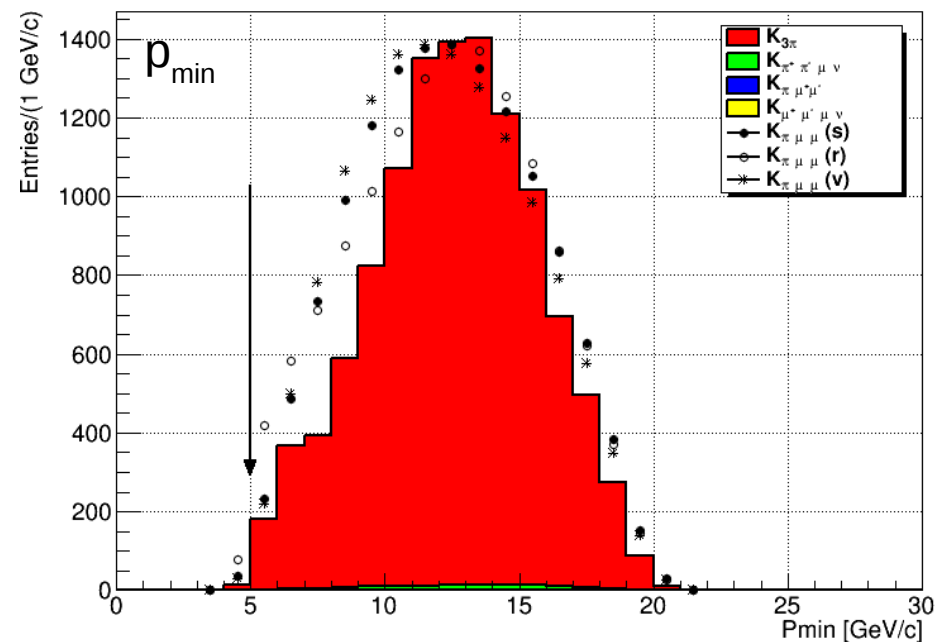
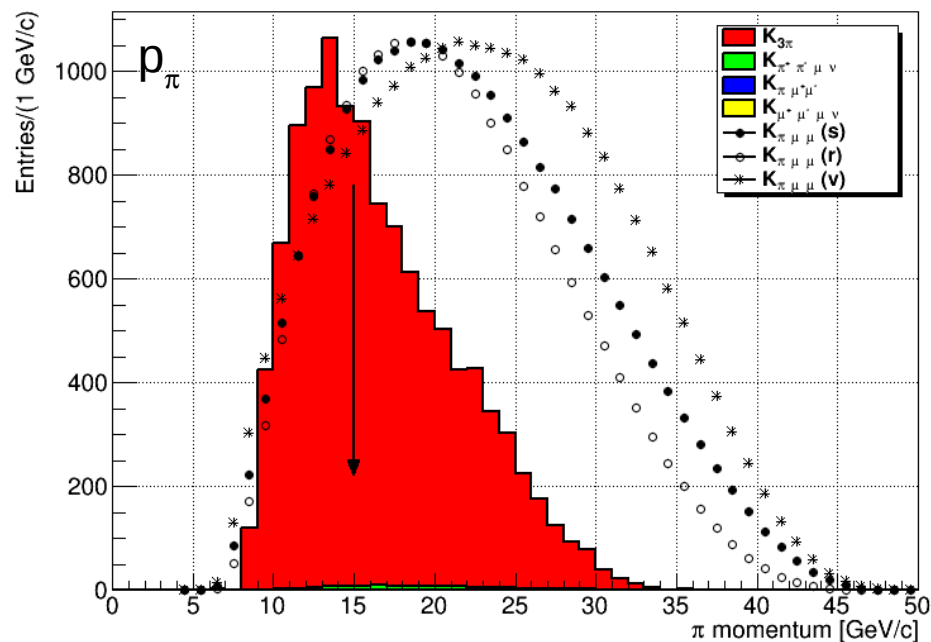
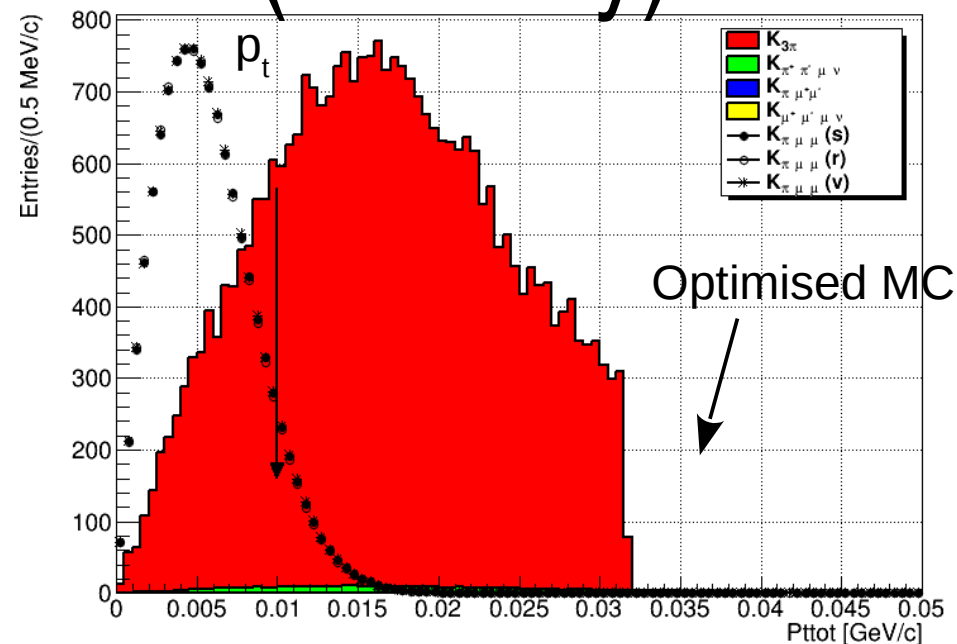
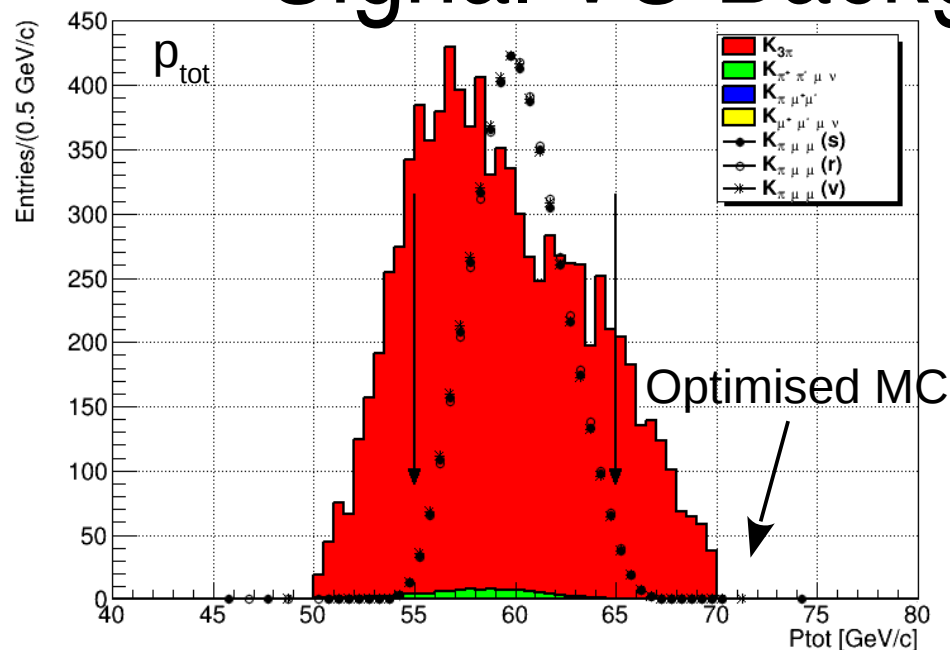


Signal VS Background (MC only)

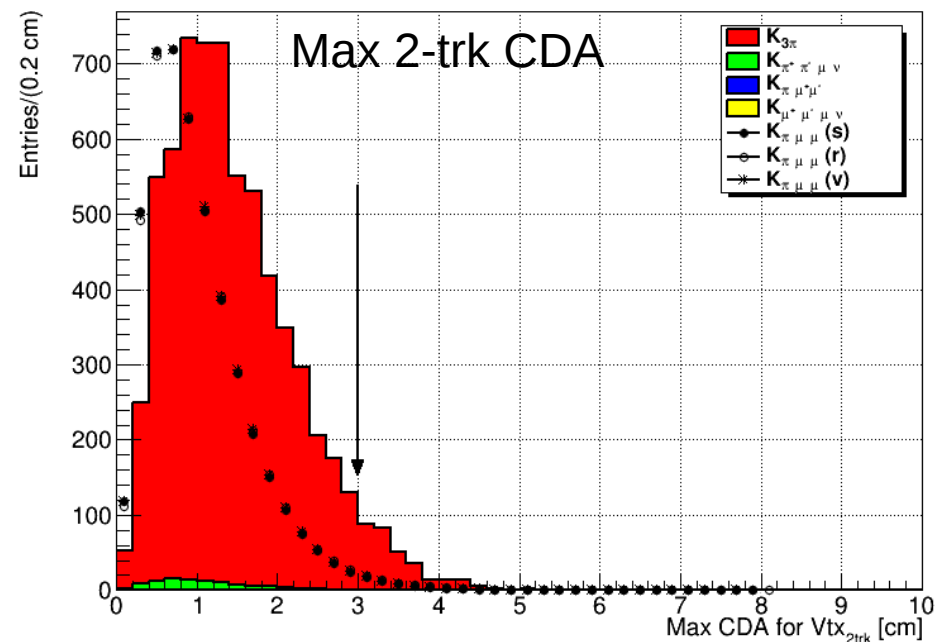
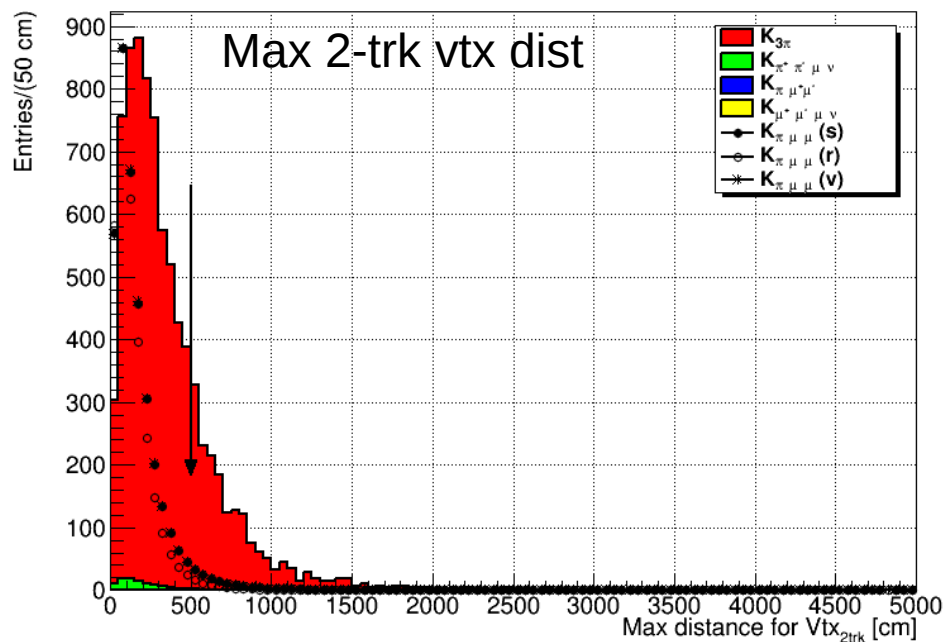
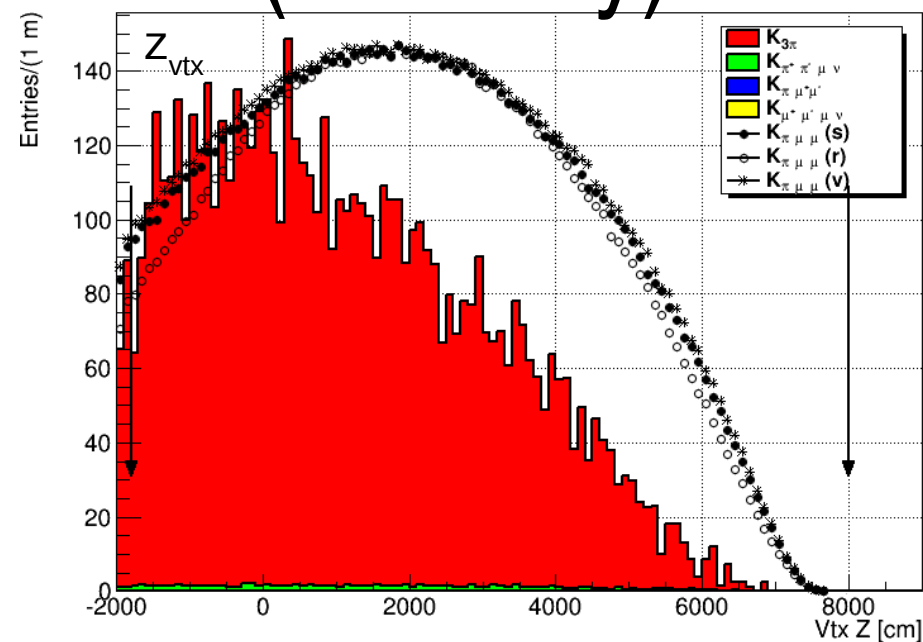
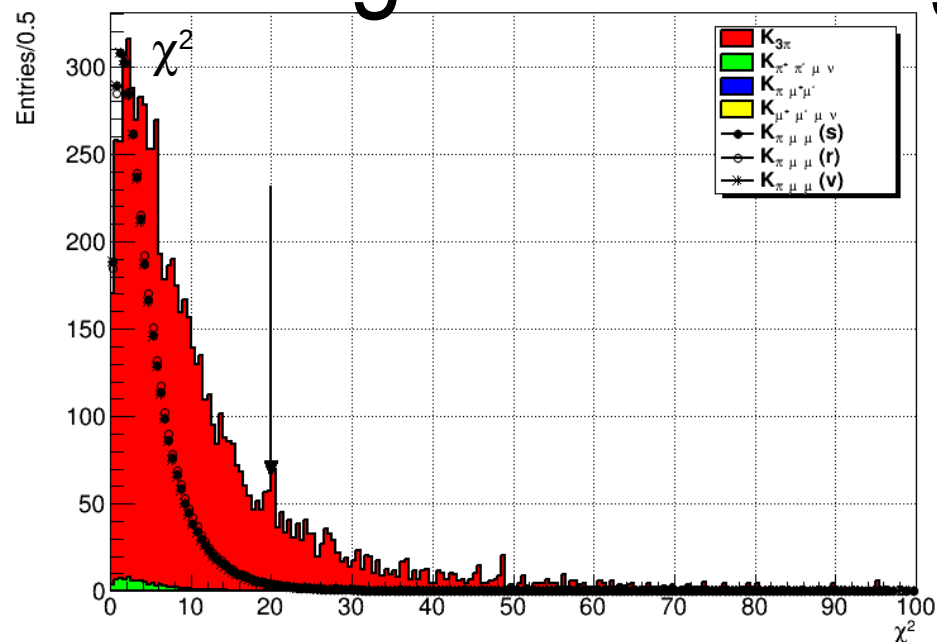
- For each variable, final $K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$ selection except
 - any cut on the variable itself
 - No $m_{\pi\mu\mu}$ cuts, to increase bkg statistics



Signal VS Background (MC only)



Signal VS Background (MC only)



Statistical Analysis

- Feldman-Cousins approach abandoned:
Poisson-distributed signal with Poisson-distributed bkg with *known* mean
→ actually NOT suitable for this analysis!
- $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ background uncertainty dominated by statistics:
Statistics fluctuations MUST be taken into account!
- Rolke-Lopez method [Nucl.Instrum.Meth. **A551**, 493 (2005)]
Poisson-distributed signal with Poisson-distributed bkg with *unknown* mean

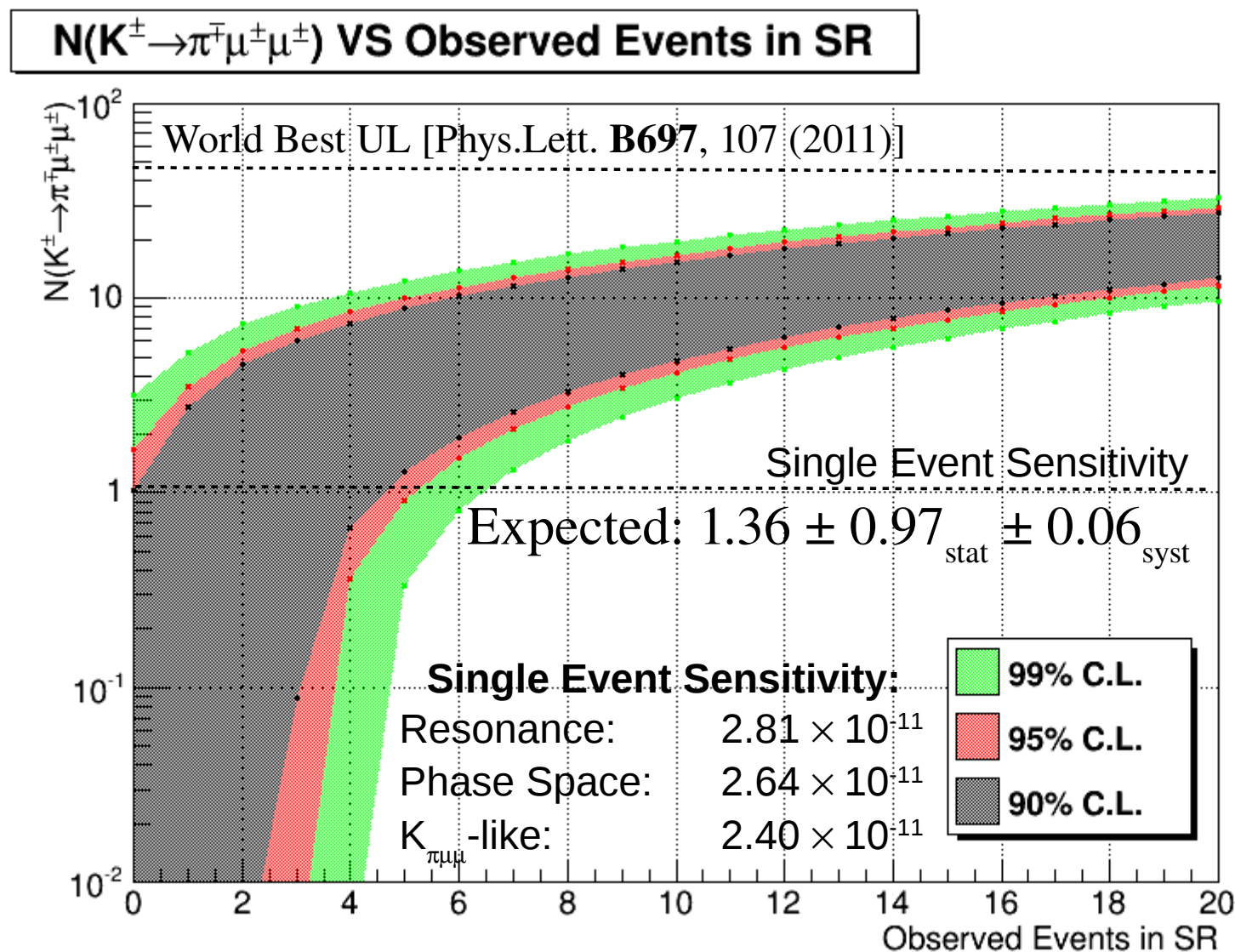


TRolke class not extendable to the case of interest with 4 bkg estimations
New framework “STAT62” developed for numerical evaluation
of Rolke-Lopez confidence intervals
[with improved convergence algorithms with respect to TRolke]
User-friendly and customisable environment ready: to be released soon



Confidence Belt

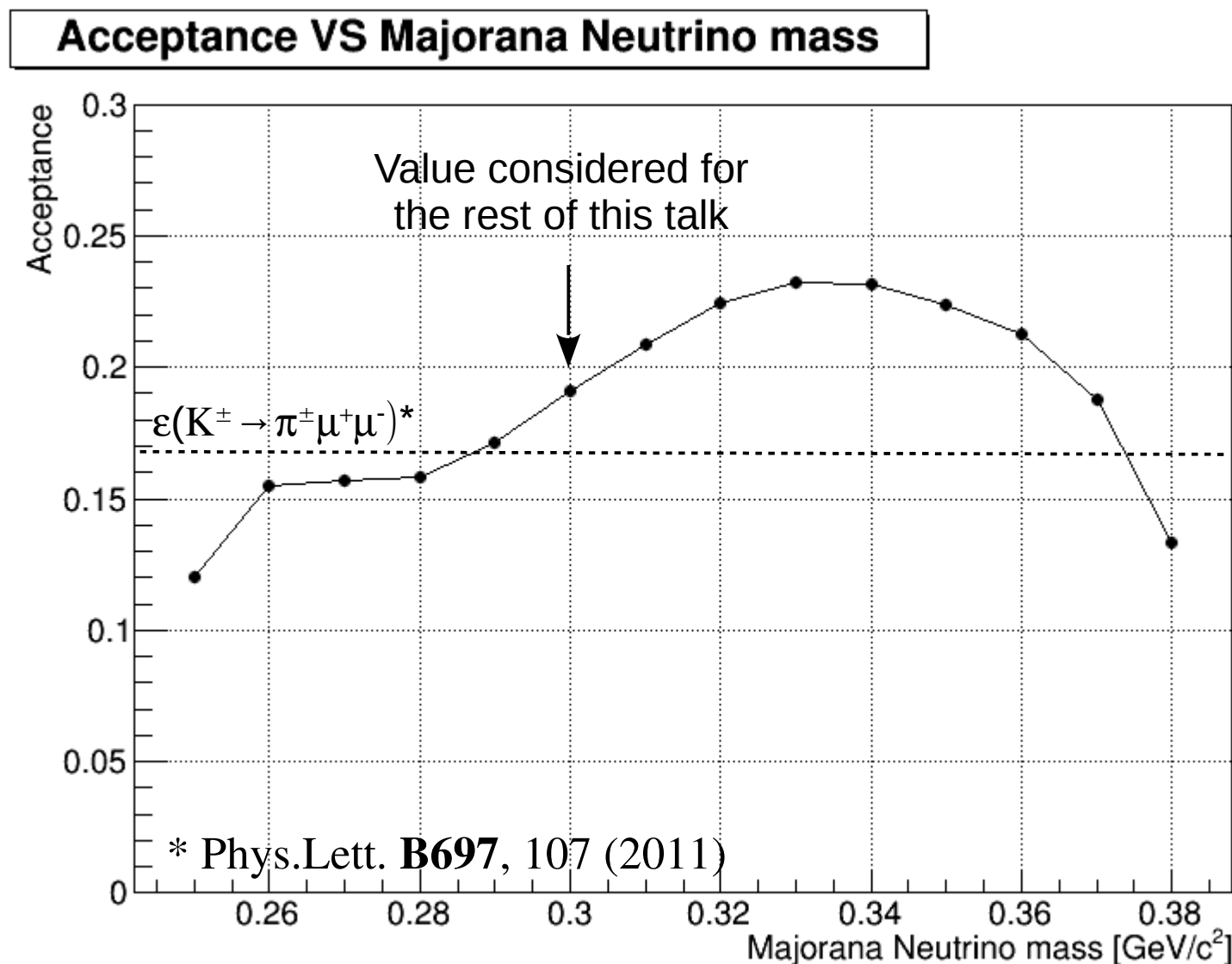
Confidence Belt built using number of expected bkg events





Neutrino mass scan (preliminary)

Signal acceptance $\varepsilon_{\pi\mu\mu}(m_N)$ for resonance model evaluated ($\tau_N \approx 0$)



Conclusions and Outlook

- Fine-tuning of the $K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$ Event Selection completed
- Final Selection: $1.36 \pm 0.97_{\text{stat}} \pm 0.06_{\text{syst}}$ background
- Potential sensitivity $\sim 3 \times 10^{-11}$ @ 90% C.L
- Muon efficiency evaluated (and bad bursts removed)
- Kaon flux evaluated (in agreement with previous results)
- New statistical analysis using the Rolke-Lopez method for a Poisson-distributed bkg with *unknown* mean

Next Steps:

- Scan in m_N and in τ_N to evaluate the signal acceptance $\varepsilon_{\pi\mu\mu}(m_N, \tau_N)$ for resonance model
- Independent “displaced vertex” analysis to cover region $\tau_N > 10$ ps

Conclusions and Outlook

- Standing items will be completed soon (< 1 week)
- **Asking for internal referees to be nominated**
- Internal “living” note describing the analysis about to be released next week, in order to receive feedback from referees
- Subsequently, asking the permission to open the box