

# Higgs Physics beyond the Standard Model

## Footprints of a Warped Extra Dimension ?



Matthias Neubert

Mainz Institute for Theoretical Physics  
Johannes Gutenberg University

*Les Rencontres de Physique de  
La Vallée d'Aoste*  
La Thuile, 23 February - 1 March 2014



**ERC Advanced Grant (EFT4LHC)**  
An Effective Field Theory Assault on the  
Zeptometer Scale: Exploring the Origins of  
Flavor and Electroweak Symmetry Breaking



# Higgs and flavor physics as indirect BSM probes

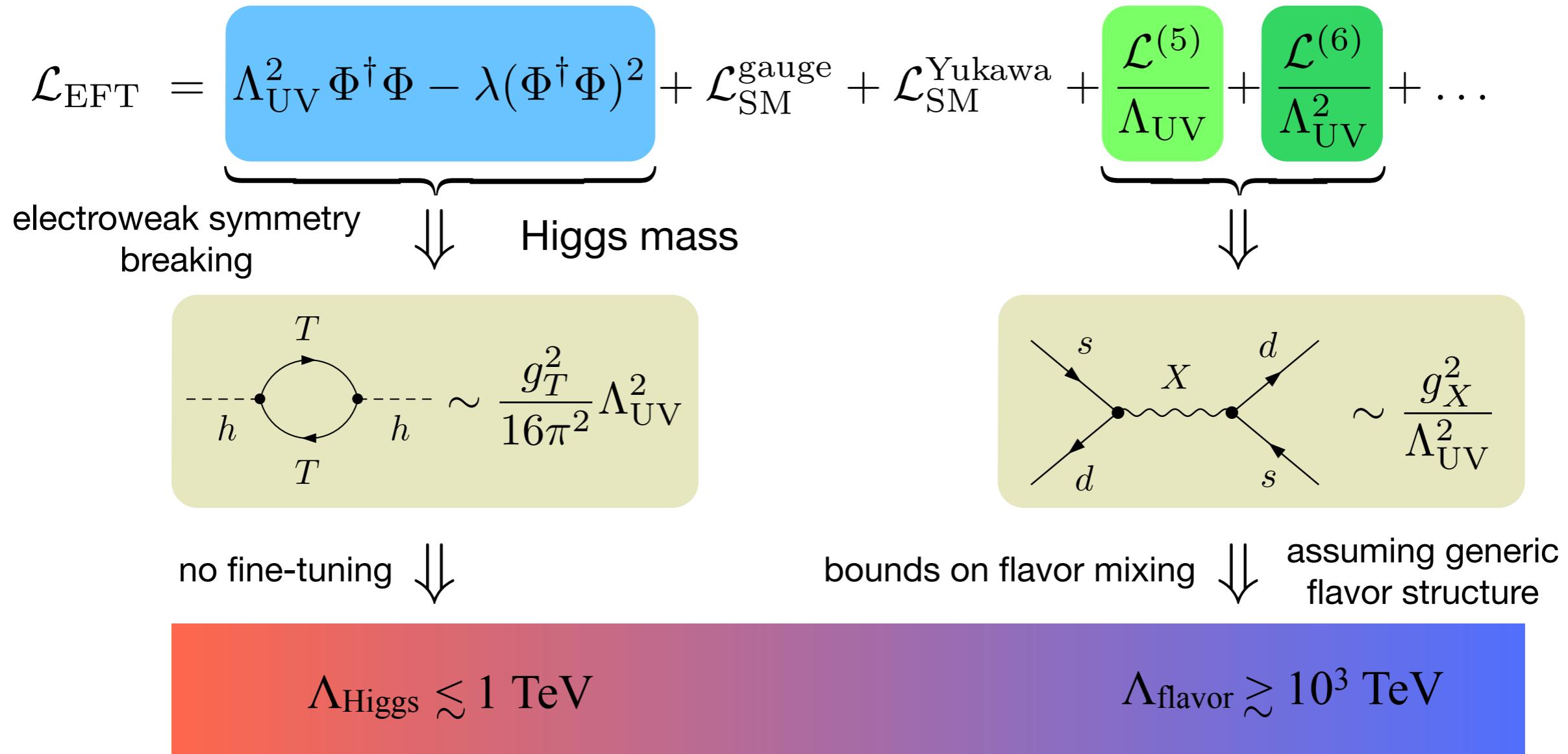
---

The **hierarchy problem** and the **origin of flavor** are two major, unsolved mysteries of fundamental physics

- connected to deep questions such as the **origin of mass**, the **stability of the electroweak scale**, the **matter-antimatter asymmetry**, the **origin of fermion generations**, and the reason for the **hierarchies** observed in the fermion sector
- we **do not understand the SM** until we understand these puzzles (both rooted in Higgs Yukawa interactions)

Higgs and flavor physics provide unique opportunities to probe the **structure of electroweak interactions at the quantum level**, thereby offering sensitive probes of physics beyond the SM

# Higgs and flavor physics as indirect BSM probes



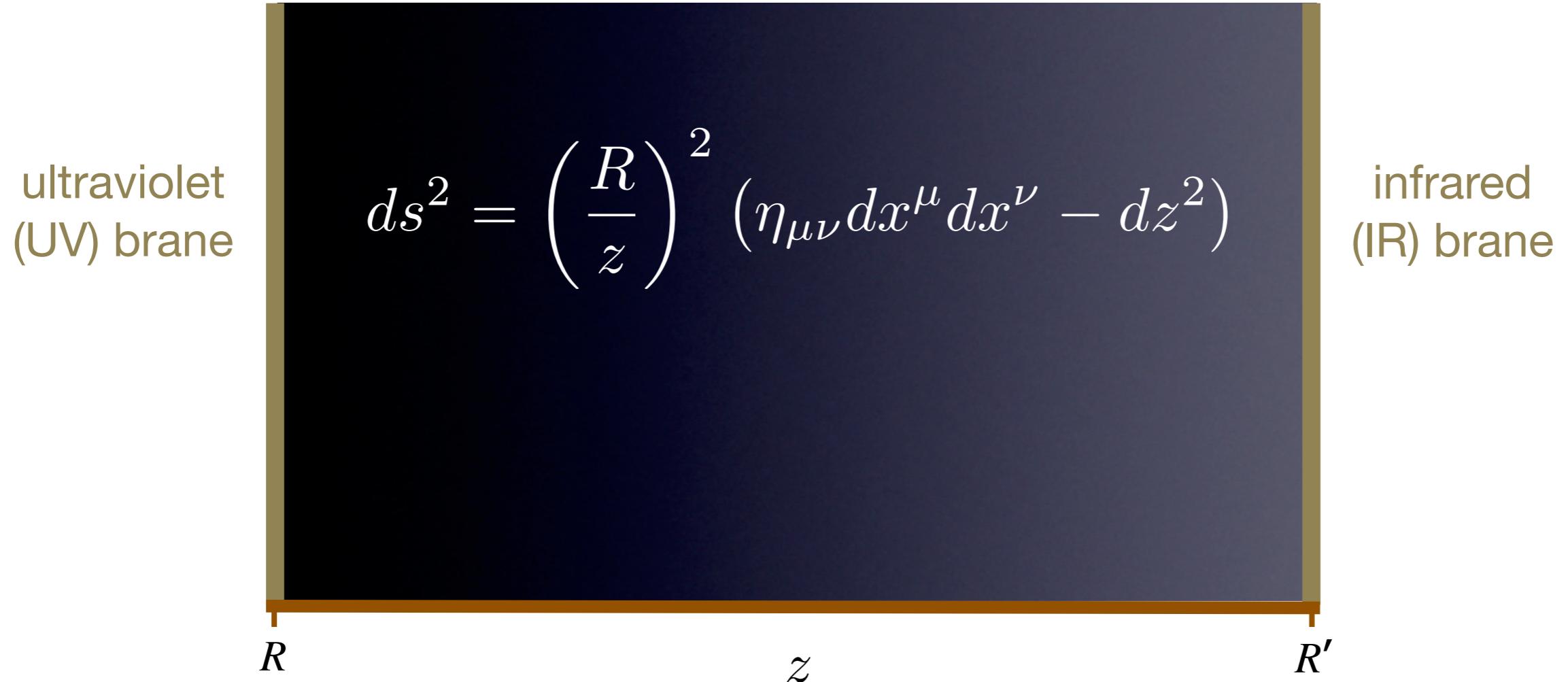
Possible solutions to flavor problem explaining  $\Lambda_{\text{Higgs}} \ll \Lambda_{\text{flavor}}$ :

- (i)  $\Lambda_{\text{UV}} \gg 1 \text{ TeV}$ : **Higgs fine tuned**, new particles too heavy for LHC
- (ii)  $\Lambda_{\text{UV}} \approx 1 \text{ TeV}$ : quark flavor-mixing protected by a **flavor symmetry**



# Hierarchies from geometry

# Flavor structure in RS models

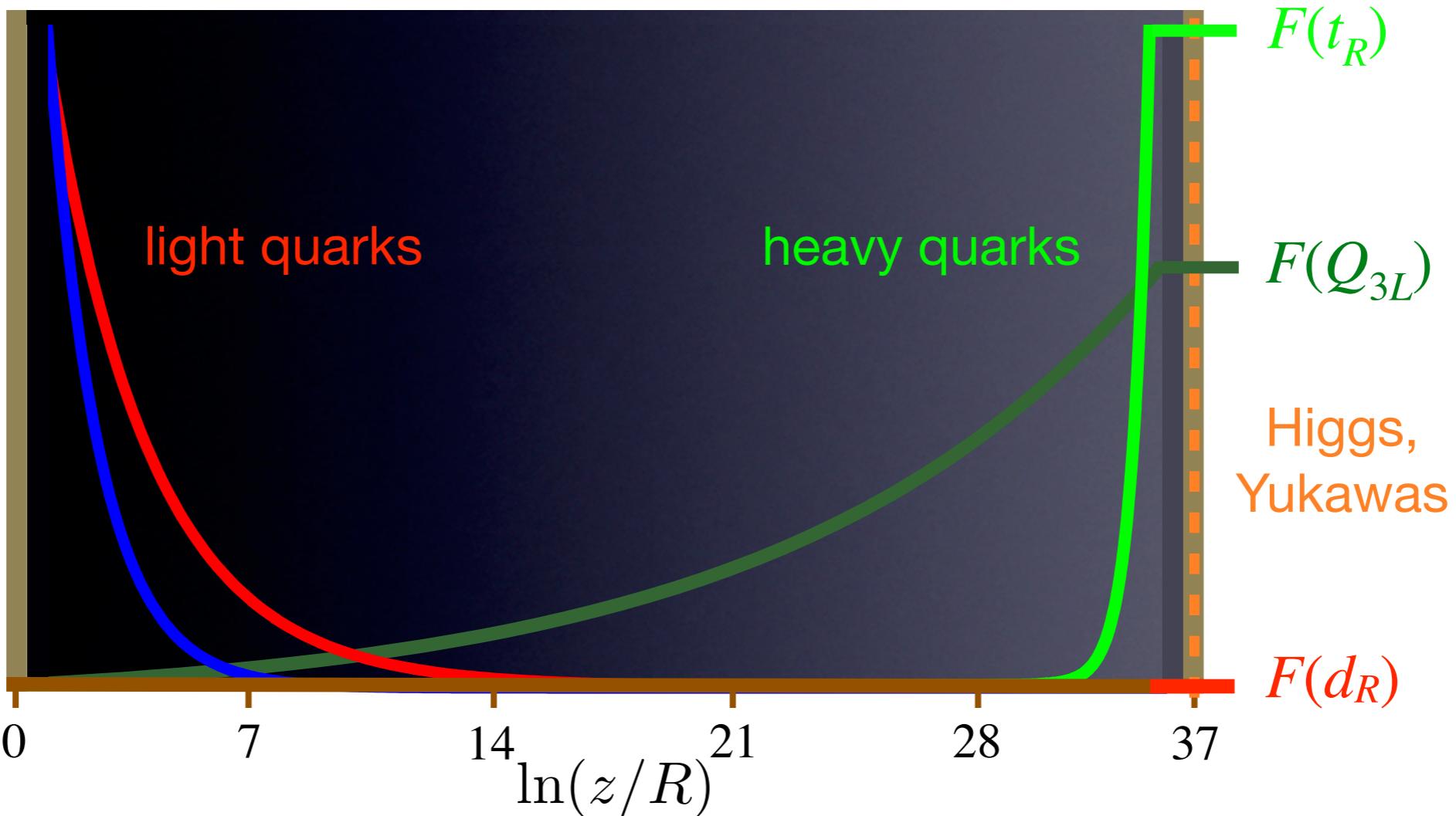


Randall-Sundrum (RS) models with a warped extra dimension address, at the same time, the **hierarchy problem** and the **flavor puzzle** (hierarchies seen in the spectrum of quark masses and mixing angles)

# Flavor structure in RS models

UV brane

IR brane



Localization of fermions in extra dimension depends exponentially on O(1) parameters related to the **5D bulk masses**. Overlap integrals  $F(Q_L)$ ,  $F(q_R)$  with Higgs profile are **exponentially small** for light quarks, while O(1) for top quark

# Flavor structure in RS models

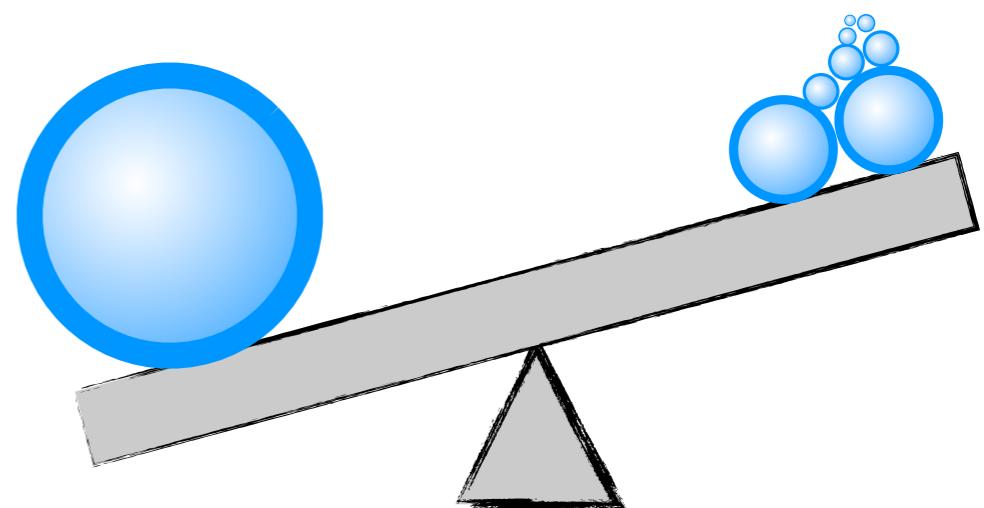
SM mass matrices can be written as: Huber (2003)

$$\mathbf{m}_q^{\text{SM}} = \frac{v}{\sqrt{2}} \text{diag} [F(Q_i)] \mathbf{Y}_q \text{diag} [F(q_i)]$$

$$\begin{pmatrix} \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot \end{pmatrix}$$

where  $\mathbf{Y}_q$  with  $q = u, d$  are structureless, complex Yukawa matrices with  $O(1)$  entries, and  $F(Q_i) \ll F(Q_j), F(q_i) \ll F(q_j)$  for  $i < j$

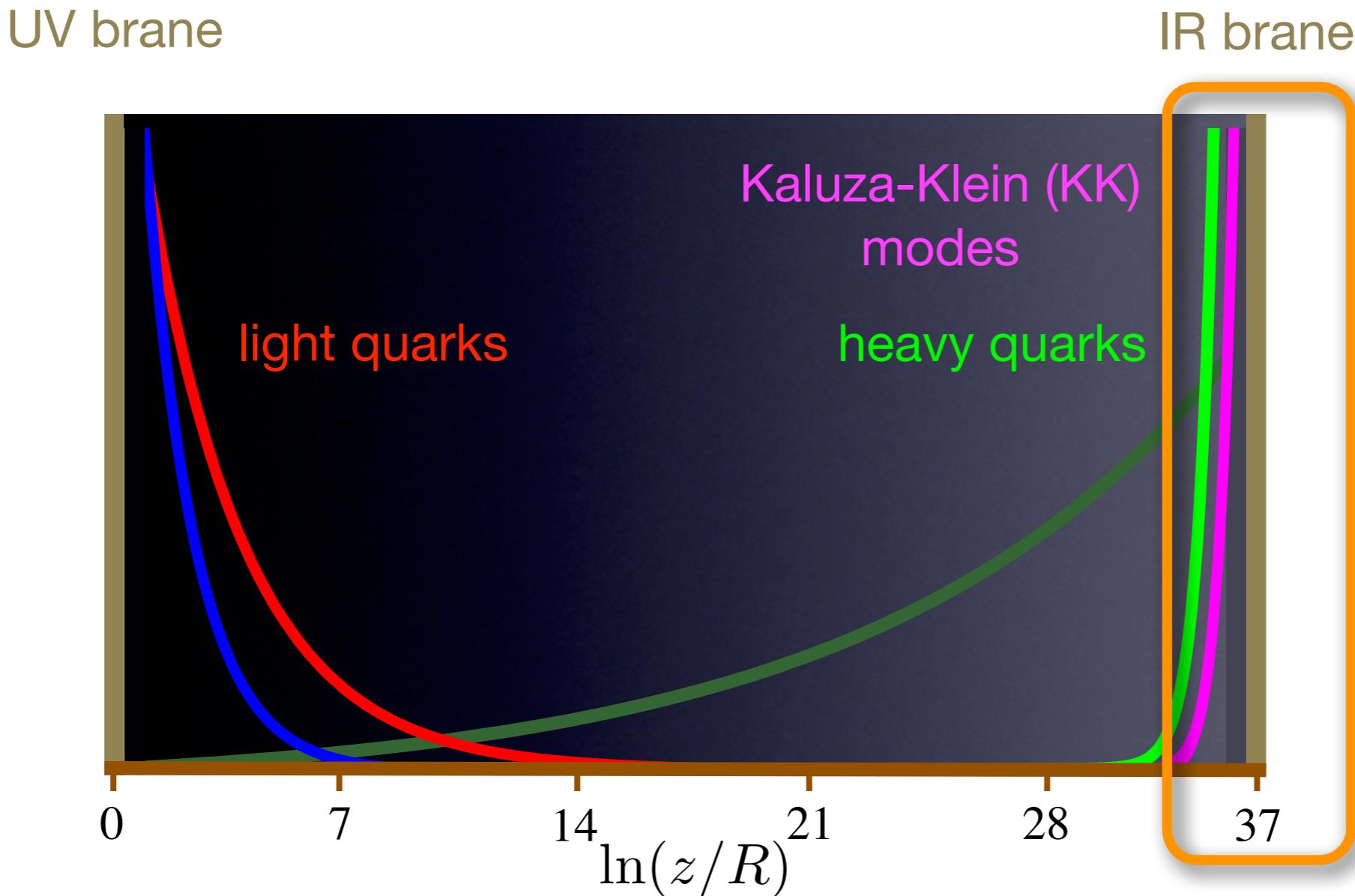
- in analogy to seesaw mechanism, matrices of this form give rise to hierarchical mass eigenvalues and mixing matrices
- hierarchies can be adjusted by  $O(1)$  variations of bulk mass parameters
- yet the CKM phase is predicted to be  $O(1)$



**Warped-space Froggatt-Nielsen mechanism!**

Casagrande et al. (2008); Blanke et al. (2008)

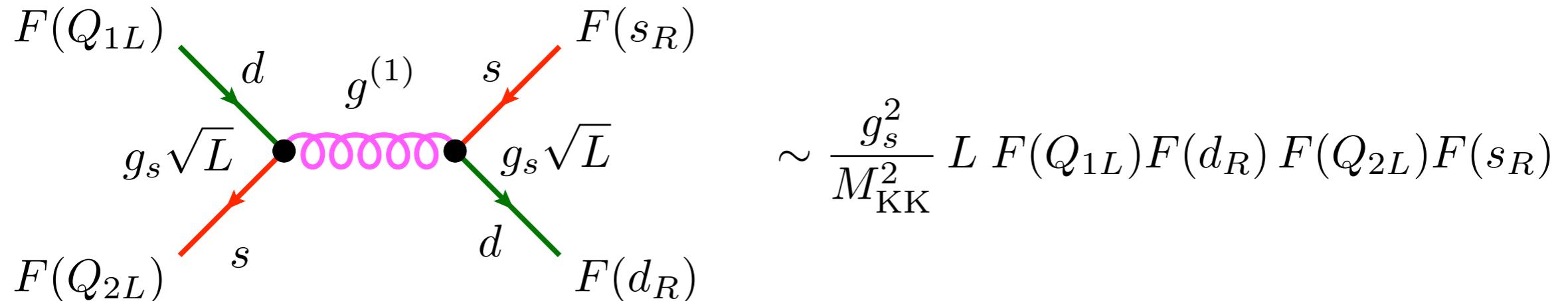
# Flavor structure in RS models



Kaluza-Klein (KK) excitations of SM particles live close to the IR brane

Davoudiasl, Hewett, Rizzo (1999); Pomarol (1999)

# RS-GIM protection of FCNCs

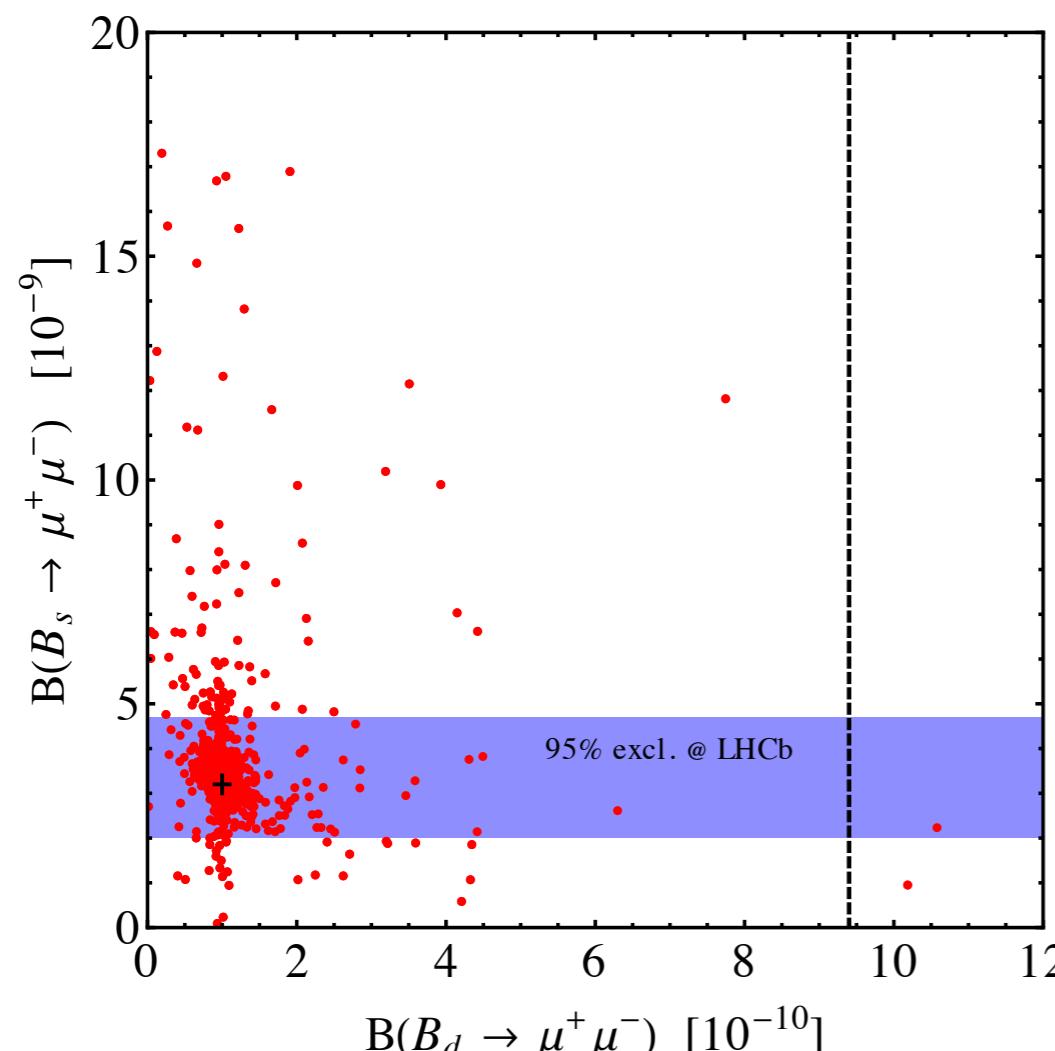


- Tree-level quark FCNCs induced by **virtual exchange of Kaluza-Klein (KK) gauge bosons** (including gluons!) Huber (2003); Burdman (2003); Agashe et al. (2004); Casagrande et al. (2008)
- Resulting FCNC couplings depend on same exponentially small overlap integrals  $F(Q_L)$ ,  $F(q_R)$  that generate fermion masses
- FCNCs involving light quarks are strongly suppressed: **RS-GIM mechanism** Agashe et al. (2004)

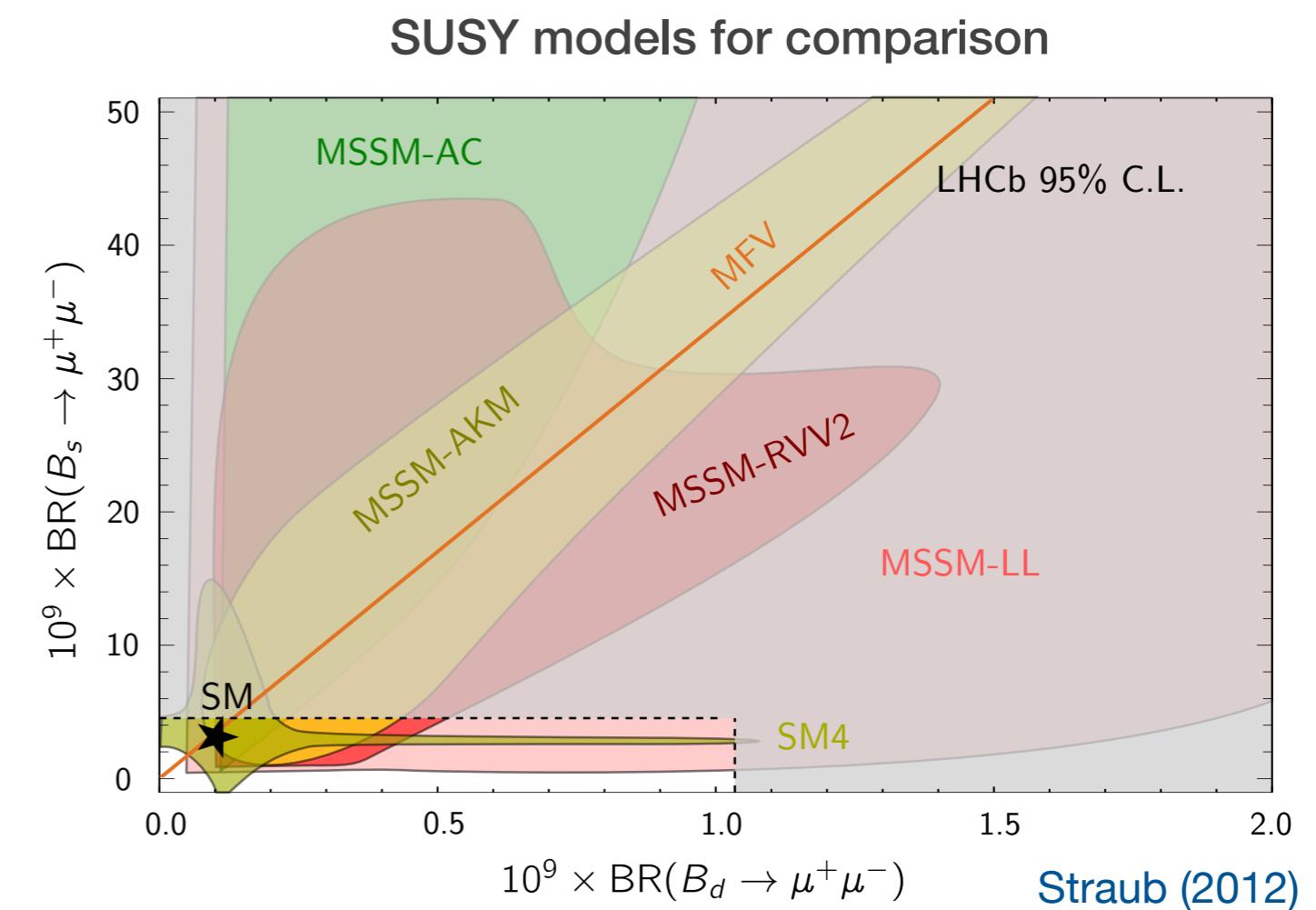
**This mechanism suffices to suppress most of the dangerous FCNC couplings!**

# Example: Rare leptonic $B_{s/d} \rightarrow \mu^+ \mu^-$ decays

Rare decays  $B_{d,s} \rightarrow \mu^+ \mu^-$  could be significantly affected, but RS-GIM protection is sufficient to prevent too large deviations from SM:



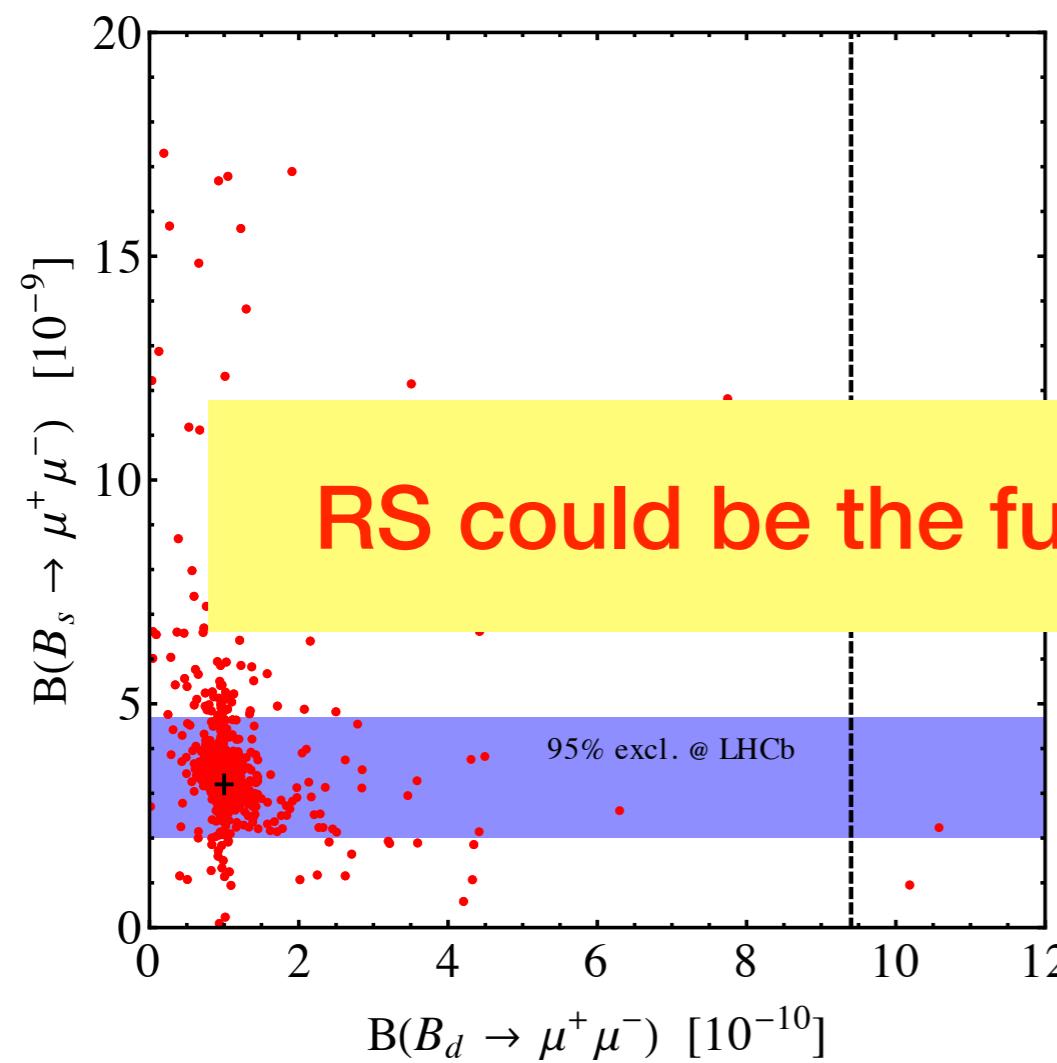
Bauer, Casagrande, Haisch, MN (2009)  
see also: Blanke et al. (2008)



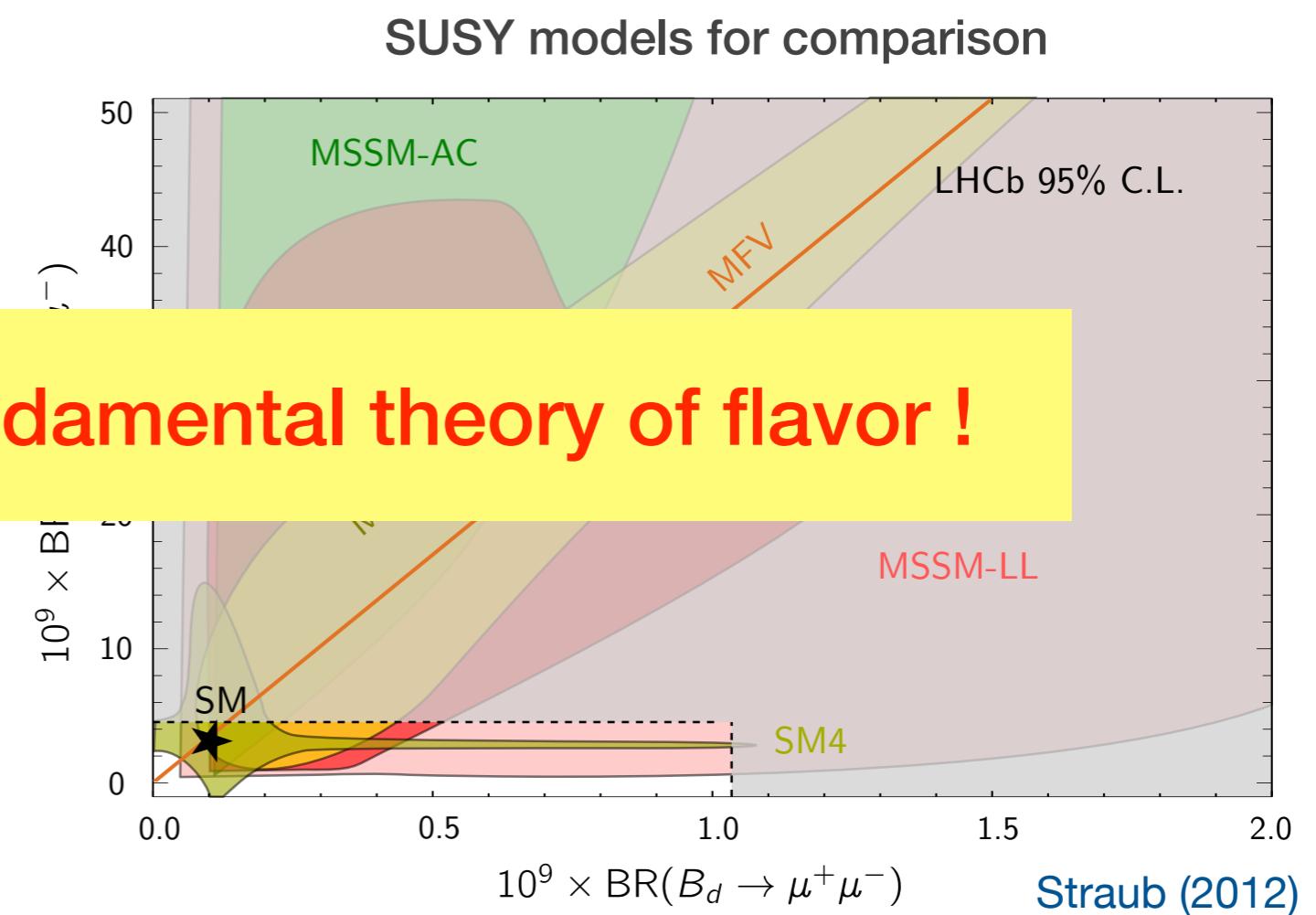
Recent LHC(b) results on  $B_s \rightarrow \mu^+ \mu^-$  begin cutting into the interesting parameter space!

# Example: Rare leptonic $B_{s/d} \rightarrow \mu^+ \mu^-$ decays

Rare decays  $B_{d,s} \rightarrow \mu^+ \mu^-$  could be significantly affected, but RS-GIM protection is sufficient to prevent too large deviations from SM:

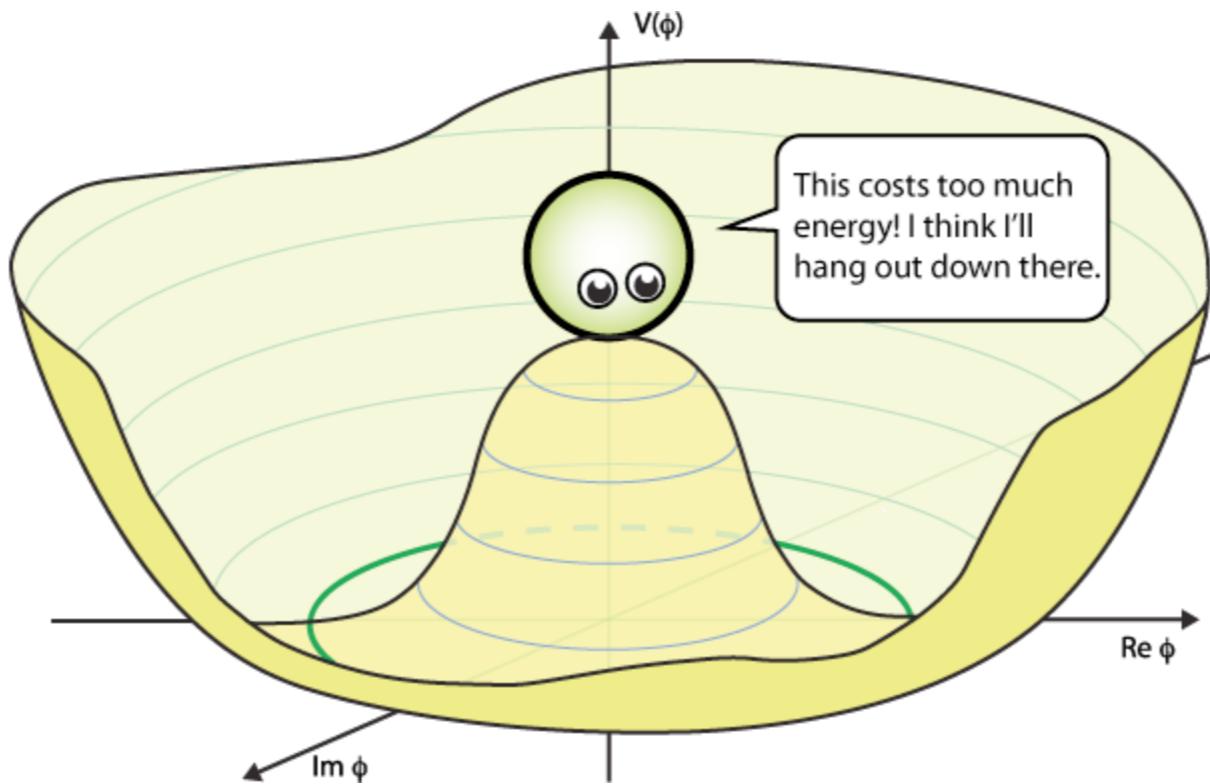


Bauer, Casagrande, Haisch, MN (2009)  
see also: Blanke et al. (2008)



Recent LHC(b) results on  $B_s \rightarrow \mu^+ \mu^-$  begin cutting into the interesting parameter space!

# Higgs Properties as an Indirect Probe for New Physics



Goertz, Haisch, MN: arXiv:1112.5099 (PLB)

Carena, Casagrande, Goertz, Haisch, MN: arXiv:1204.0008 (JHEP)

Malm, MN, Novotny, Schmell: arXiv:1303.5702 (JHEP)

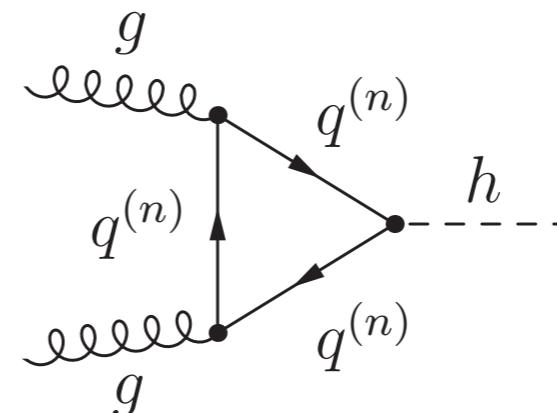
Hahn, Hörner, Malm, MN, Novotny, Schmell: arXiv:1312.5731

# Higgs physics as an indirect BSM probe

Higgs discovery marks the birth of the **hierarchy problem**:

- one of the main motivations for physics beyond the SM
- detailed study of **Higgs properties** (mass, width, cross section, branching fractions) will help to probe whether the Higgs sector is as simple as predicted by the SM
- **Higgs couplings to photons and gluons** are loop-suppressed in the SM and hence are **particularly sensitive** to the presence of new particles

In RS models, **large number of bulk fermionic fields** in 5D theory gives rise to large loop effects, which change the effective  $hgg$  and  $h\gamma\gamma$  couplings



Casagrande, Goertz, Haisch,  
MN, Pfoh (2010);  
Azatov, Toharia, Zhu (2010)

- KK towers of light quarks contribute as much as those of heavy quarks
- effect even more pronounced in models with custodial protection

**Much like flavor physics, precision Higgs physics probes quantum effects of new particles!**

# Higgs physics as an indirect BSM probe

---

RS model is an effective theory defined with a **physical, 5D position-dependent cutoff** - the warped Planck scale:

$$\Lambda_{\text{UV}}(z) \sim M_{\text{Pl}} \frac{R}{z} = \Lambda_{\text{TeV}} \frac{R'}{z}$$

- for loop graphs including a Higgs boson as an external particle, the warped Planck scale is in the **several TeV range** (since  $z \approx R'$ )
- two **physically different** variants of the RS model can be defined, depending on whether the structure of the Higgs boson as a 5D bulk field can be resolved by the high-momentum modes of the theory, i.e., whether the **inverse 5D Higgs width**  $v/\eta$  (with  $\eta \ll 1$ ) is larger or smaller than the cutoff scale:

$$\frac{v}{\eta} \gg \Lambda_{\text{TeV}}$$

(brane-localized Higgs)

$$M_{\text{KK}} \ll \frac{v}{\eta} \ll \Lambda_{\text{TeV}}$$

(narrow bulk Higgs)

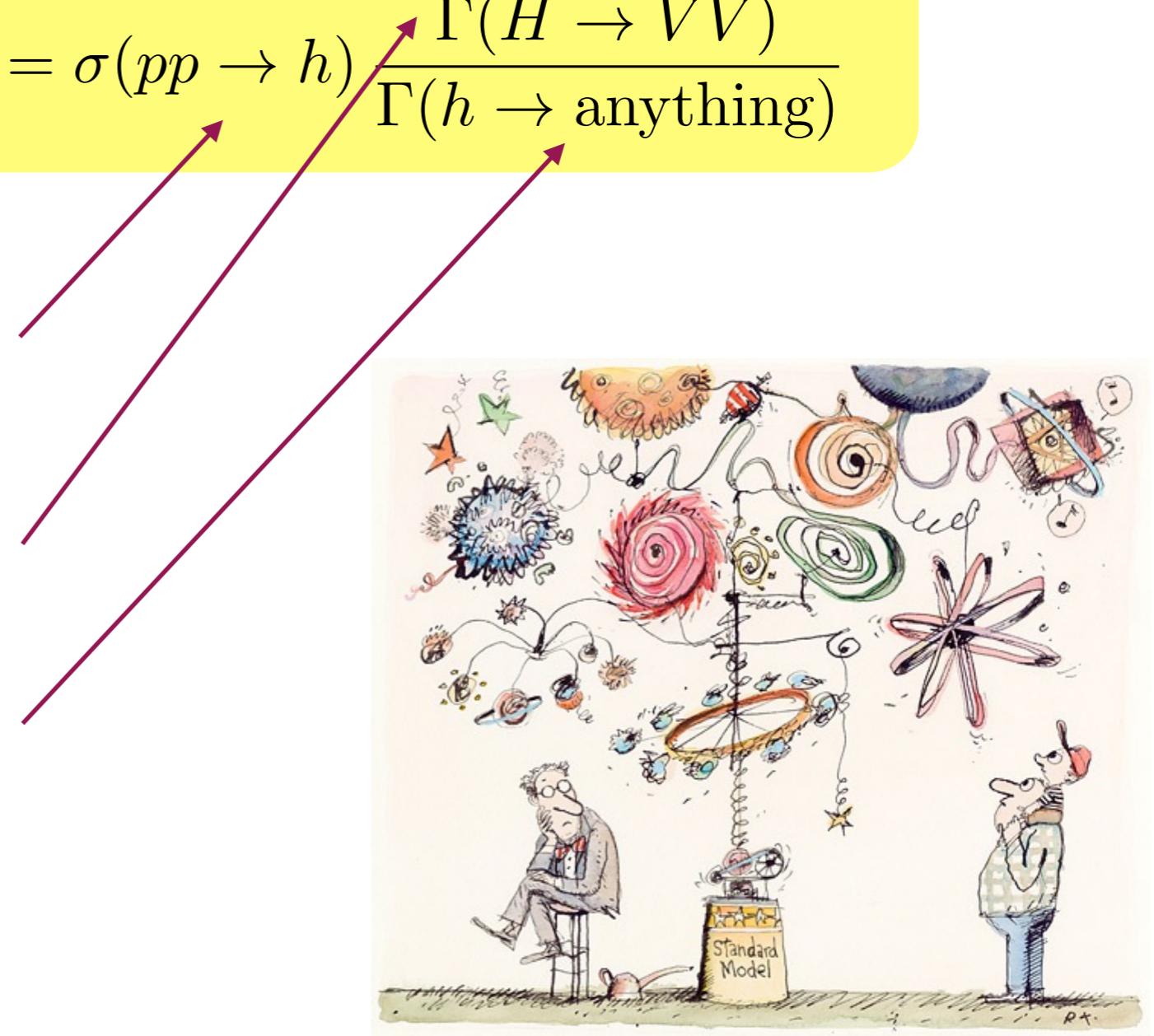
Carena, Casagrande, Goertz, Haisch, MN (2012)  
Delaunay, Kamenik, Perez, Randall (2012)  
Malm, MN, Novotny, Schmell: arXiv:1303.5702

# New physics in Higgs decays: 3 portals

In any extension of the Standard Model, new-physics contributions can affect the measured rates for Higgs production and decay in three ways:

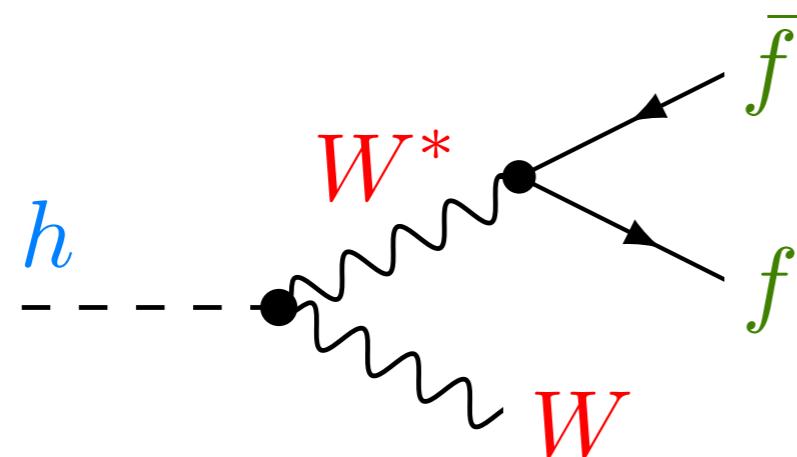
$$(\sigma \cdot \text{BR})(pp \rightarrow h \rightarrow VV) = \sigma(pp \rightarrow h) \frac{\Gamma(H \rightarrow VV)}{\Gamma(h \rightarrow \text{anything})}$$

- Higgs **production cross section** (~90% gluon fusion, <10% vector-boson fusion, ~few % VH prod.)
- Higgs **decay rate** to the observed final state (here  $VV$ )
- **total Higgs width** (sensitive to  $h \rightarrow b\bar{b}$ ,  $h \rightarrow WW$ , also  $h \rightarrow \text{invisible}$ )



# Higgs decay rates to $WW^*$ and $ZZ^*$

Four different sources of effects from new physics:



- modification of Higgs vev:  $\kappa_v$
- modification of Higgs coupling to gauge-boson pairs:  $\kappa_W$
- modification of  $W$ - and  $Z$ -boson couplings to fermions:  $\kappa_\Gamma$
- contribution of heavy KK bosons

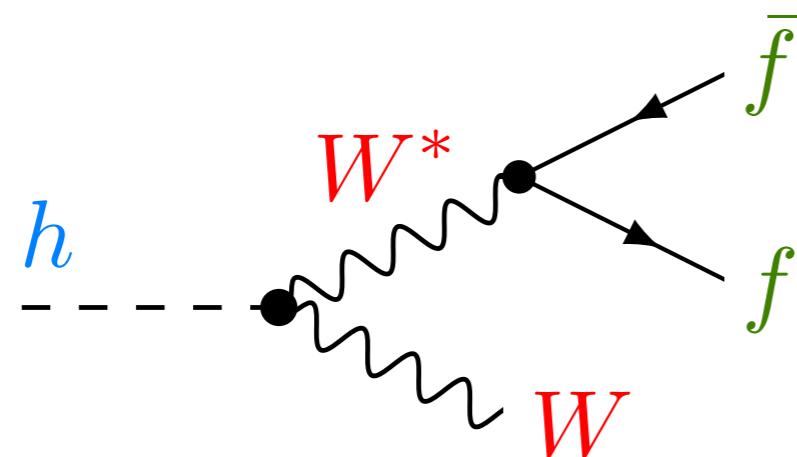
Expression for the decay rate:

$$\Gamma(h \rightarrow WW^*) = \frac{m_H^3}{16\pi\kappa_v^2 v_{\text{SM}}^2} \frac{\kappa_\Gamma \Gamma_W}{\pi m_W} \left\{ \kappa_W g\left(\frac{m_W^2}{m_H^2}\right) - \frac{m_H^2}{2M_{\text{KK}}^2} \left(1 - \frac{1}{L}\right) h\left(\frac{m_W^2}{m_H^2}\right) \right\}$$

Malm, MN, Schmell: in preparation

# Higgs decay rates to $WW^*$ and $ZZ^*$

Four different sources of effects from new physics:



- modification of Higgs vev:  $\kappa_v$
- modification of Higgs coupling to gauge-boson pairs:  $\kappa_W$
- modification of  $W$ - and  $Z$ -boson couplings to fermions:  $\kappa_\Gamma$
- contribution of heavy KK bosons

Expression for the decay rate:

$$\Gamma(h \rightarrow WW^*) = \frac{m_H^3}{16\pi \kappa_v^2 v_{\text{SM}}^2} \frac{\kappa_\Gamma \Gamma_W}{\pi m_W} \left\{ \kappa_W g\left(\frac{m_W^2}{m_H^2}\right) - \frac{m_H^2}{2M_{\text{KK}}^2} \left(1 - \frac{1}{L}\right) h\left(\frac{m_W^2}{m_H^2}\right) \right\}$$

Malm, MN, Schmell: in preparation

Correction factors:

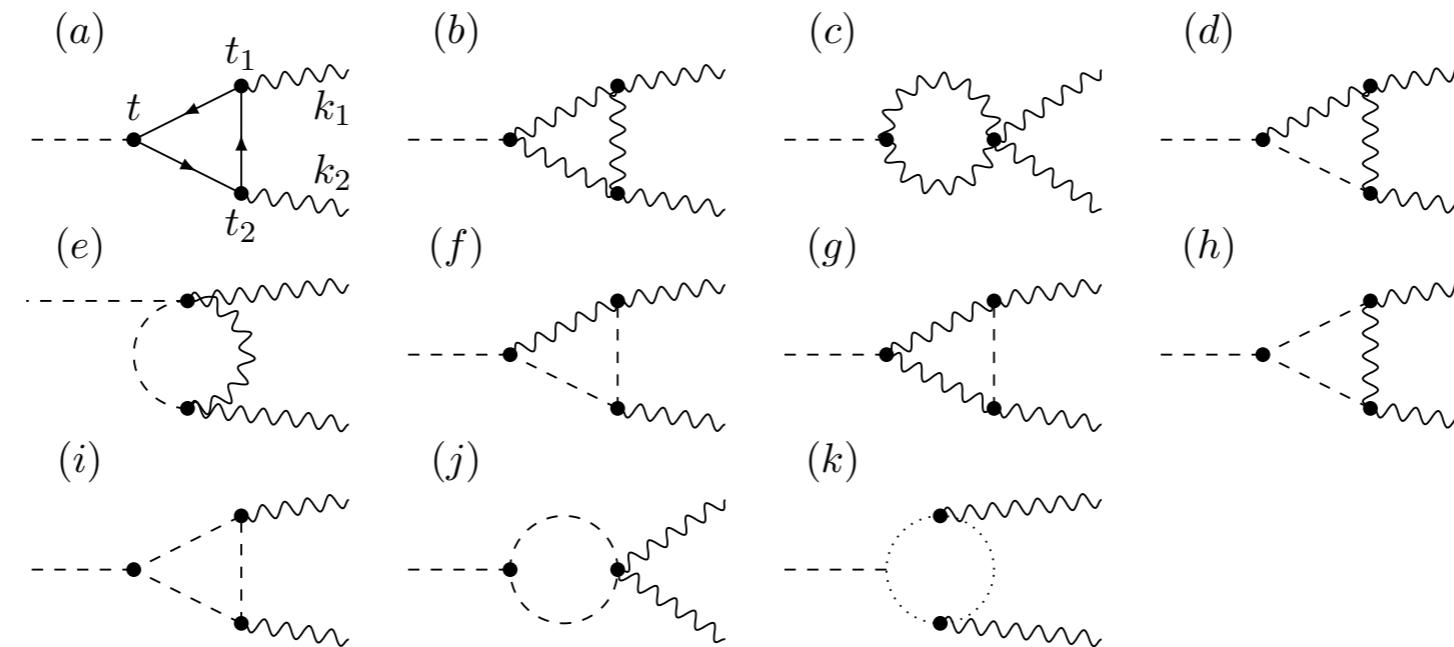
$$\kappa_v = 1 + \frac{L m_W^2}{4 M_{\text{KK}}^2}, \quad \kappa_\Gamma = 1 - \frac{m_W^2}{4 L M_{\text{KK}}^2}, \quad \kappa_W = 1 - \frac{m_W^2}{2 M_{\text{KK}}^2} \left(L - 1 + \frac{1}{2L}\right)$$

(with:  $L = \ln(M_{\text{Pl}}/\Lambda_{\text{TeV}}) \approx 34$ )

# $h \rightarrow \gamma\gamma$ decay rate (details of the calculation)

---

Decay  $h \rightarrow \gamma\gamma$  mediated by loops of gauge bosons (+ KK modes) and fermions (+ KK modes):

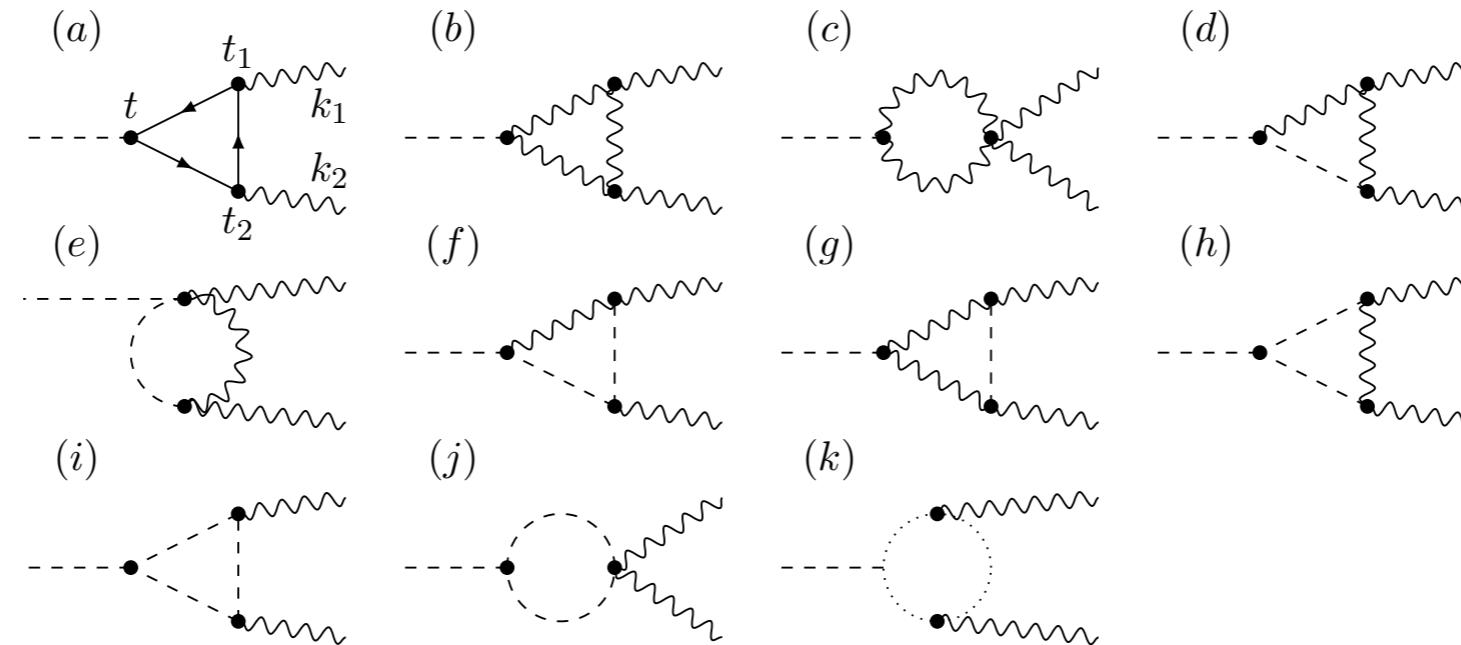


Bosonic contribution expressed in terms of 5D gauge-boson propagators:

$$\begin{aligned}
 i\mathcal{A}(h \rightarrow \gamma\gamma) = & -\frac{2\tilde{m}_W^2}{v} 2\pi e^2 \epsilon_\mu^*(k_1) \epsilon_\nu^*(k_2) \eta^{\alpha\beta} \int \frac{d^d p}{(2\pi)^d} \int_{\epsilon}^1 dt \delta^\eta(t-1) \frac{2\pi}{L} \int_{\epsilon}^1 \frac{dt_1}{t_1} \\
 & \times \left[ \frac{2\pi}{L} \int_{\epsilon}^1 \frac{dt_2}{t_2} 2V^{\gamma\mu\lambda\rho\nu\delta} D_{W,\alpha\gamma}^{\xi \rightarrow \infty}(t, t_1, p + k_1) D_{W,\lambda\rho}^{\xi \rightarrow \infty}(t_1, t_2, p) D_{W,\delta\beta}^{\xi \rightarrow \infty}(t_2, t, p - k_2) \right. \\
 & \left. + (2\eta^{\gamma\delta}\eta^{\mu\nu} - \eta^{\delta\nu}\eta^{\gamma\mu} - \eta^{\nu\gamma}\eta^{\mu\delta}) D_{W,\alpha\gamma}^{\xi \rightarrow \infty}(t, t_1, p + k_1) D_{W,\beta\delta}^{\xi \rightarrow \infty}(t_1, t, p - k_2) \right]
 \end{aligned}$$

# $h \rightarrow \gamma\gamma$ decay rate (details of the calculation)

Decay  $h \rightarrow \gamma\gamma$  mediated by loops of gauge bosons (+ KK modes) and fermions (+ KK modes):



Parameterization of the decay amplitude:

$$\mathcal{A}(h \rightarrow \gamma\gamma) = C_{1\gamma} \frac{\alpha_e}{6\pi v} \langle \gamma\gamma | F_{\mu\nu} F^{\mu\nu} | 0 \rangle - C_{5\gamma} \frac{\alpha_e}{4\pi v} \langle \gamma\gamma | F_{\mu\nu} \tilde{F}^{\mu\nu} | 0 \rangle$$

# $h \rightarrow \gamma\gamma$ decay rate (details of the calculation)

Exact result for  $C_{1\gamma}^W$  expressed in terms of a **single 5D propagator**:

$$C_{1\gamma}^W = -3\pi\tilde{m}_W^2 \left[ T_W(0) + 6 \int_0^1 dx \int_0^{1-x} dy (1 - 2xy) T_W(-xym_h^2) \right]$$

Hahn, Hörner, Malm, MN, Novotny, Schmell:  
arXiv:1312.5731

with:

$$T_W(-p^2) = \int_{\epsilon}^1 dt \delta^{\eta}(t-1) B_W(t, t; -p^2 - i0) = B_W(1, 1; -p^2 - i0) + \mathcal{O}(\eta)$$

$$D_{W,\mu\nu}^{\xi}(t, t'; p) = B_W(t, t'; -p^2 - i0) \left( \eta_{\mu\nu} - \frac{p_{\mu}p_{\nu}}{p^2} \right) + B_W(t, t'; -p^2/\xi - i0) \frac{p_{\mu}p_{\nu}}{p^2}$$

Results for bosonic contributions:

$$C_{1\gamma}^W = -\frac{21}{4} [\kappa_W A_W(\tau_W) + \nu_W] + \mathcal{O}\left(\frac{v^4}{M_{KK}^4}\right), \quad C_{5\gamma}^W = 0$$

$$\kappa_W = 1 - \frac{m_W^2}{2M_{KK}^2} \left( L - 1 + \frac{1}{2L} \right), \quad \nu_W = \frac{m_W^2}{2M_{KK}^2} \left( L - 1 + \frac{1}{2L} \right)$$

# Higgs production in gluon fusion

---

Results for fermionic contributions (quarks and charged leptons):

$$C_{1\gamma}^q \approx \left[ 1 - \frac{v^2}{3M_{KK}^2} \operatorname{Re} \frac{(\mathbf{Y}_u \mathbf{Y}_u^\dagger \mathbf{Y}_u)_{33}}{(\mathbf{Y}_u)_{33}} \right] N_c Q_u^2 A_q(\tau_t) + N_c Q_d^2 A_q(\tau_b) + \sum_{q=u,d} N_c Q_q^2 \operatorname{Re} \operatorname{Tr} g(\mathbf{X}_q)$$

$$C_{5\gamma}^q \approx -\frac{v^2}{3M_{KK}^2} \operatorname{Im} \left[ \frac{(\mathbf{Y}_u \mathbf{Y}_u^\dagger \mathbf{Y}_u)_{33}}{(\mathbf{Y}_u)_{33}} \right] N_c Q_u^2 B_q(\tau_t) + \sum_{q=u,d} N_c Q_q^2 \operatorname{Im} \operatorname{Tr} g(\mathbf{X}_q)$$

$$C_{1\gamma}^l + iC_{5\gamma}^l \approx Q_e^2 \operatorname{Tr} g(\mathbf{X}_e)$$

$$\mathbf{X}_q = \frac{v}{\sqrt{2}M_{KK}} \sqrt{\mathbf{Y}_q \mathbf{Y}_q^\dagger}$$

$$0 \leq |(\mathbf{Y}_f)_{ij}| \leq y_\star$$

with:

Hahn, Hörner, Malm, MN, Novotny, Schmell:  
arXiv:1312.5731

$$g(\mathbf{X}_q)|_{\text{brane Higgs}} = \mathbf{X}_q \tanh \mathbf{X}_q - \mathbf{X}_q \tanh 2\mathbf{X}_q$$

$$g(\mathbf{X}_q)|_{\text{narrow bulk Higgs}} = \mathbf{X}_q \tanh \mathbf{X}_q$$

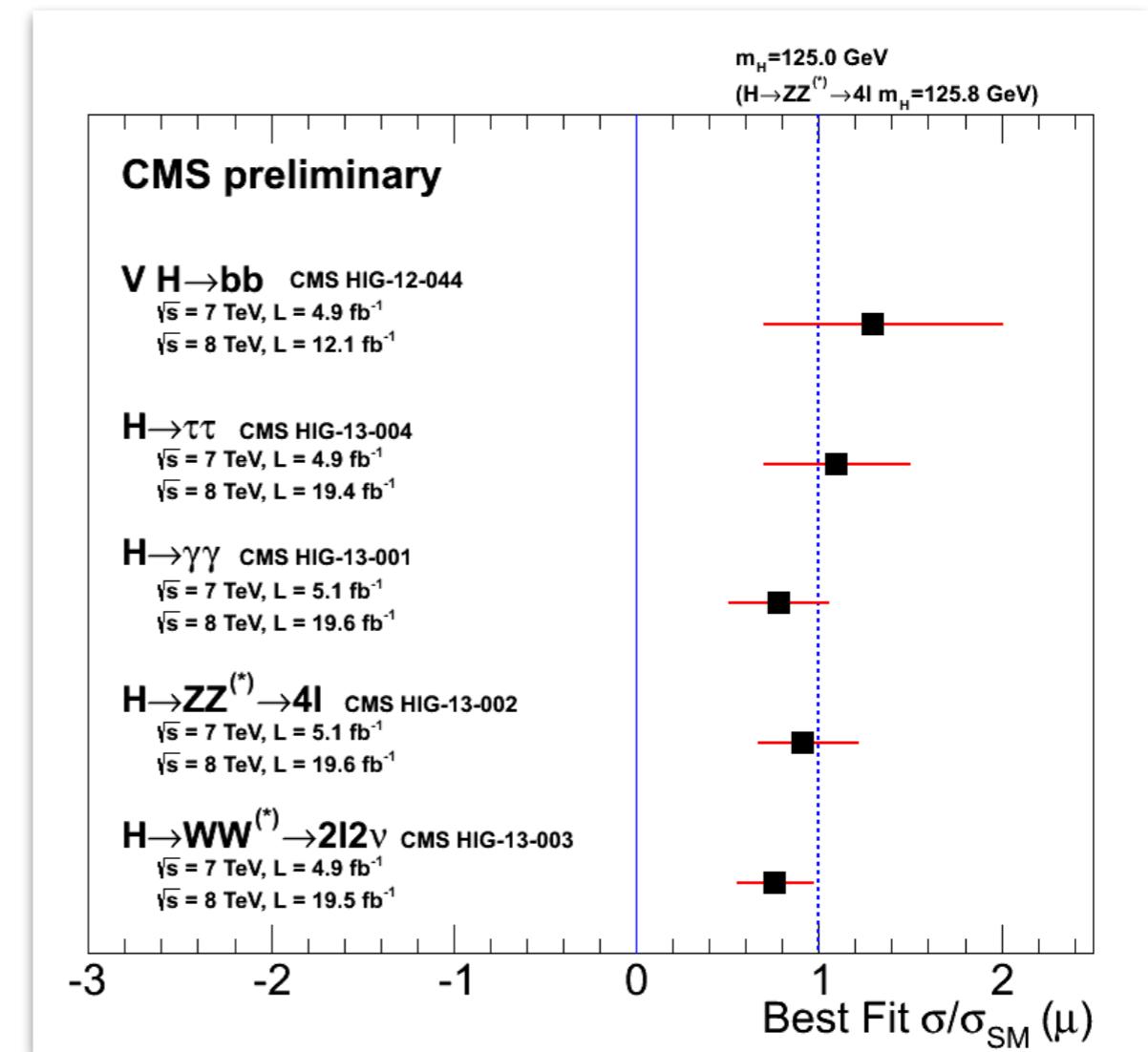
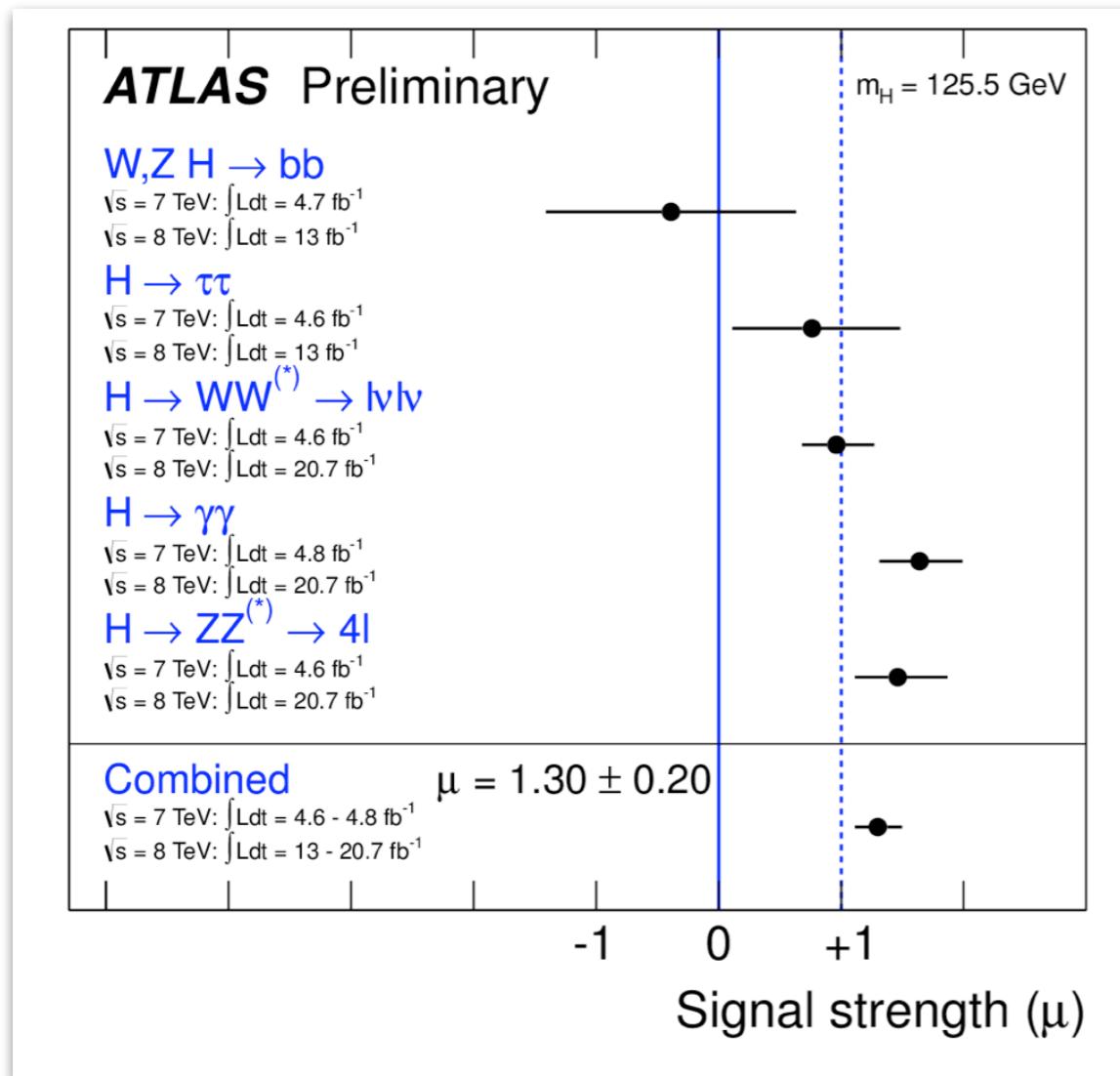
difference due to “resonant” contribution from  
high-mass KK modes ( $\sim 1/\eta$ ) near the cutoff

Results depend on very few parameters only:

$$M_{KK}, \quad L, \quad \left\langle \operatorname{Tr} \mathbf{Y}_f \mathbf{Y}_f^\dagger \right\rangle = N_g^2 \frac{y_\star^2}{2}, \quad \left\langle \frac{(\mathbf{Y}_u \mathbf{Y}_u^\dagger \mathbf{Y}_u)_{33}}{(\mathbf{Y}_u)_{33}} \right\rangle = (2N_g - 1) \frac{y_\star^2}{2}$$

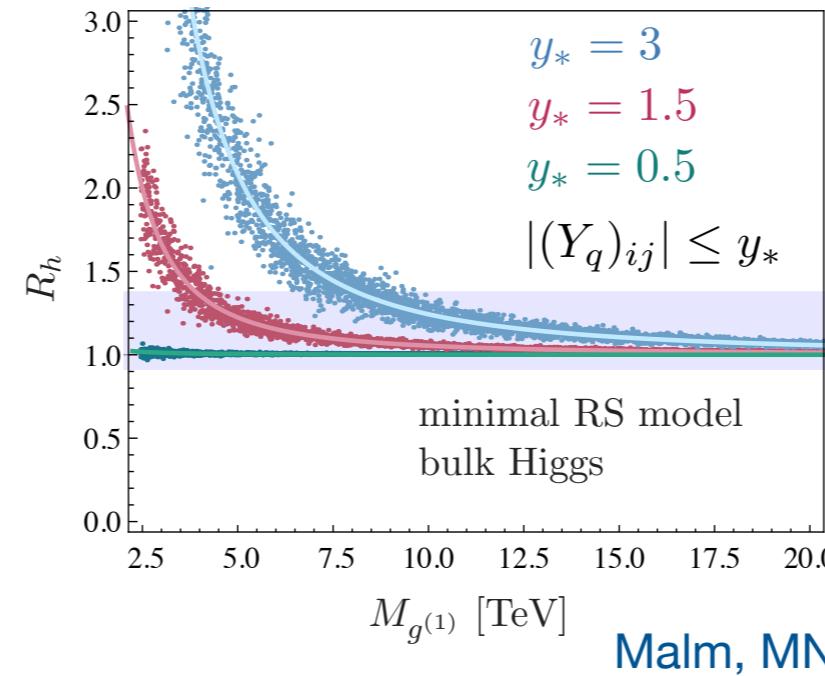
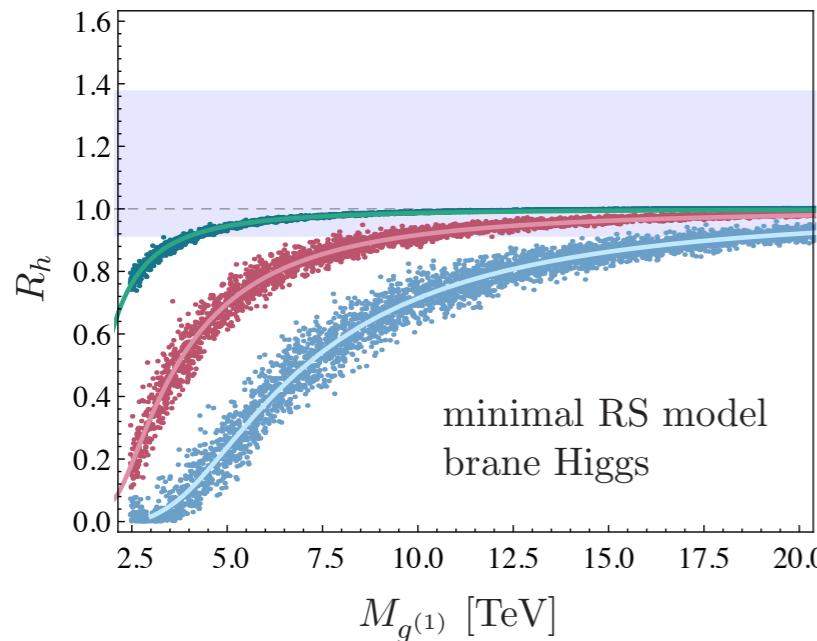
# Phenomenological predictions and LHC data

Use Run-I date sets from ATLAS and CMS:



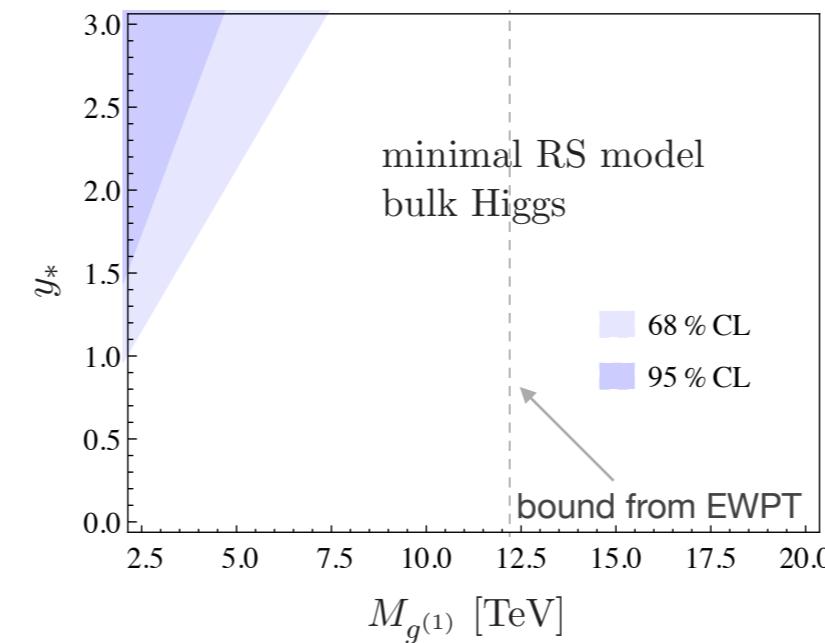
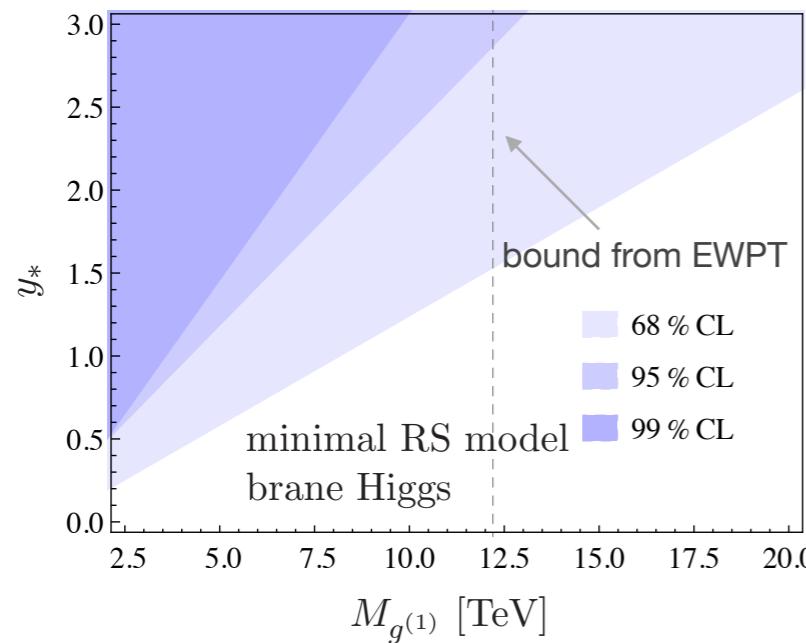
# Phenomenological predictions and LHC data

Ratio  $R_h = \frac{\sigma(gg \rightarrow h)_{\text{RS}}}{\sigma(gg \rightarrow h)_{\text{SM}}}$  compared with data from ATLAS and CMS:



experimental data  
extracted from  
 $pp \rightarrow h \rightarrow ZZ^{(*)} \rightarrow 4\ell$

[Malm, MN, Novotny, Schmell: arXiv:1303.5702](#)



# Phenomenological predictions and LHC data

---

Extended RS model with **custodial symmetry** protecting the  $T$  parameter, the left-handed  $Zb\bar{b}$  couplings and flavor-violating  $Z$ -boson couplings

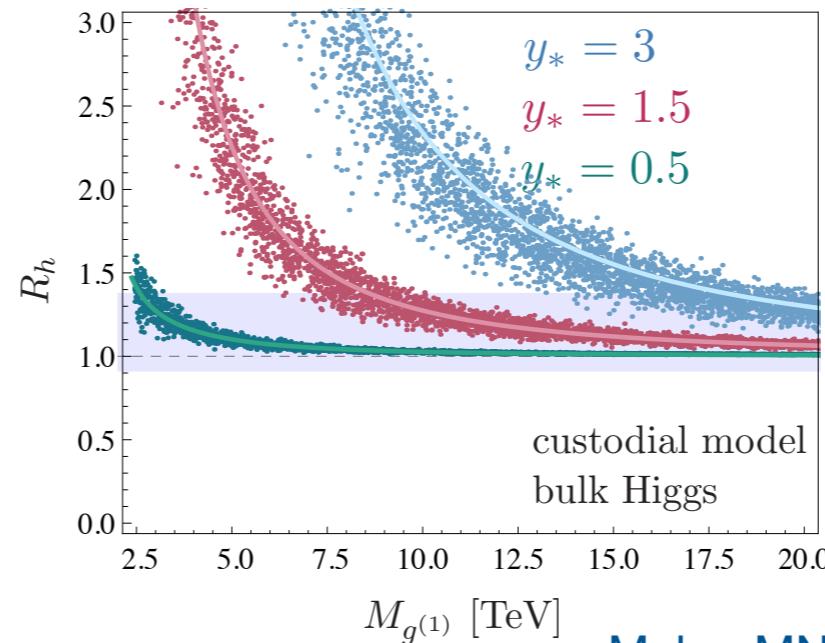
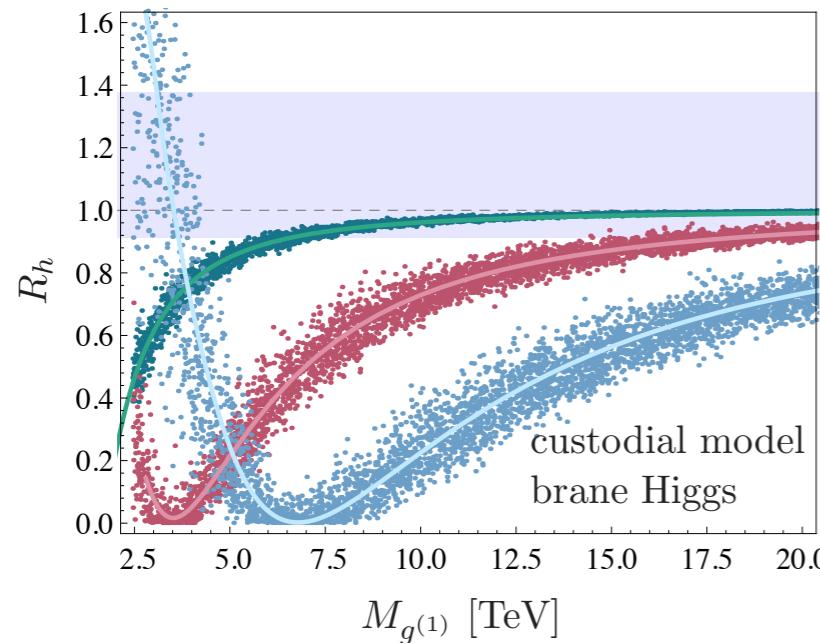
Bulk symmetry group:  $SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_X \times P_{LR}$

Representations of quark multiplets:

$$Q_L = \begin{pmatrix} u_L^{(+)} & \lambda_L^{(-)} \\ d_L^{(+)} & u_L'^{-(-)} \end{pmatrix}_{\frac{2}{3}}, \quad u_R^c = \left(u_R^{c(+)}\right)_{\frac{2}{3}}$$
$$\mathcal{T}_R = \mathcal{T}_{1R} \oplus \mathcal{T}_{2R} = \begin{pmatrix} \Lambda_R'^{-(-)} \\ U_R'^{-(-)} \\ D_R'^{-(-)} \end{pmatrix}_{\frac{2}{3}} \oplus \left(D_R^{(+)} & U_R^{(-)} & \Lambda_R^{(-)}\right)_{\frac{2}{3}}$$

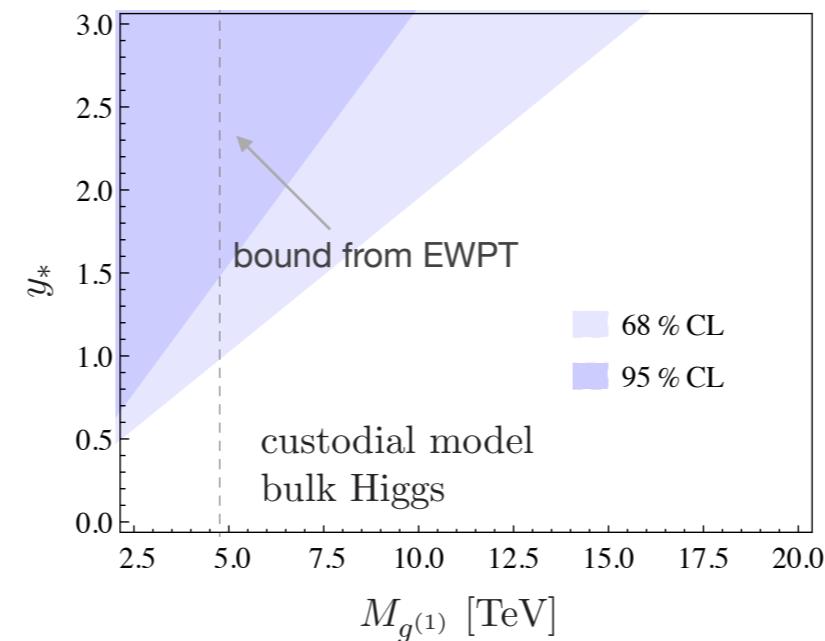
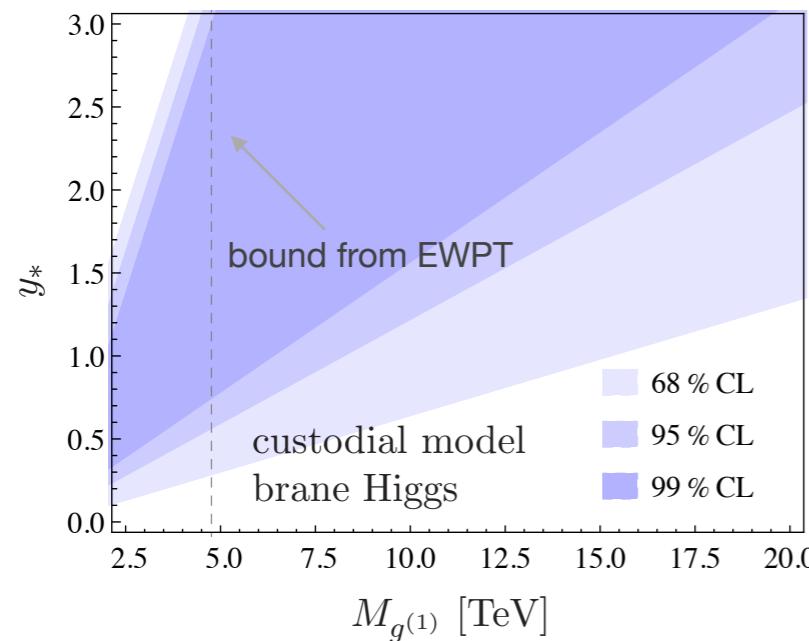
# Phenomenological predictions and LHC data

Ratio  $R_h = \frac{\sigma(gg \rightarrow h)_{\text{RS}}}{\sigma(gg \rightarrow h)_{\text{SM}}}$  in RS model with **custodial symmetry**:



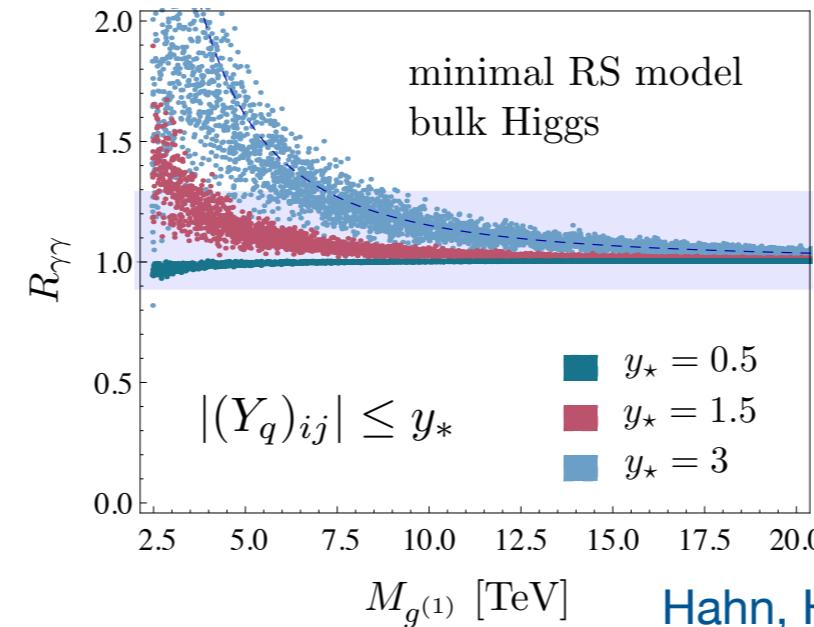
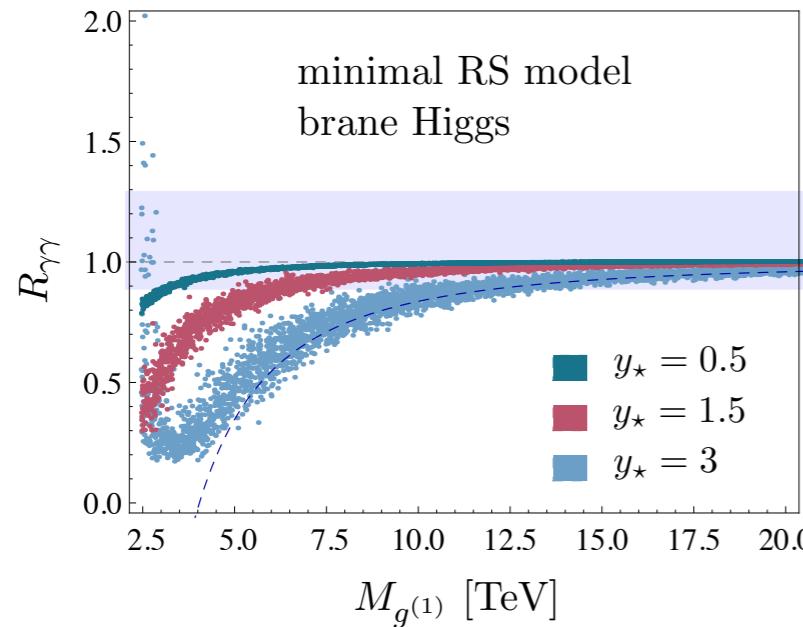
experimental data  
extracted from  
 $pp \rightarrow h \rightarrow ZZ^{(*)} \rightarrow 4\ell$

Malm, MN, Novotny, Schmell: arXiv:1303.5702



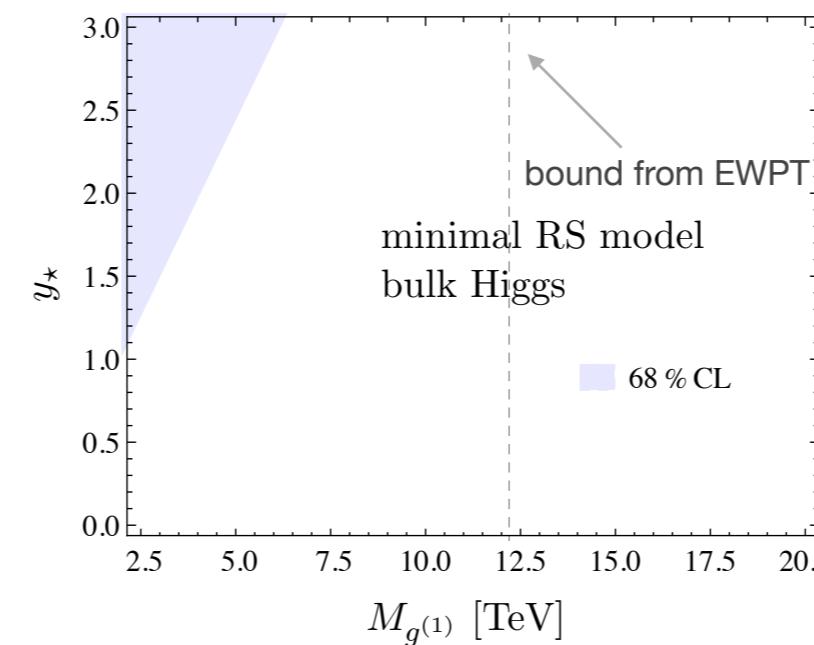
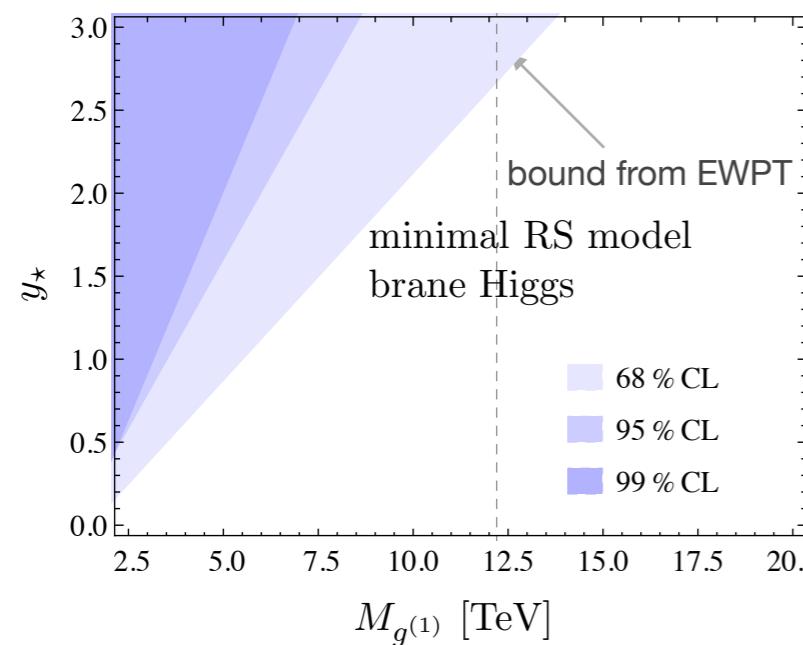
# Phenomenological predictions and LHC data

Ratio  $R_{\gamma\gamma} \equiv \frac{(\sigma \cdot \text{BR})(pp \rightarrow h \rightarrow \gamma\gamma)_{\text{RS}}}{(\sigma \cdot \text{BR})(pp \rightarrow h \rightarrow \gamma\gamma)_{\text{SM}}}$  compared with data from ATLAS and CMS:



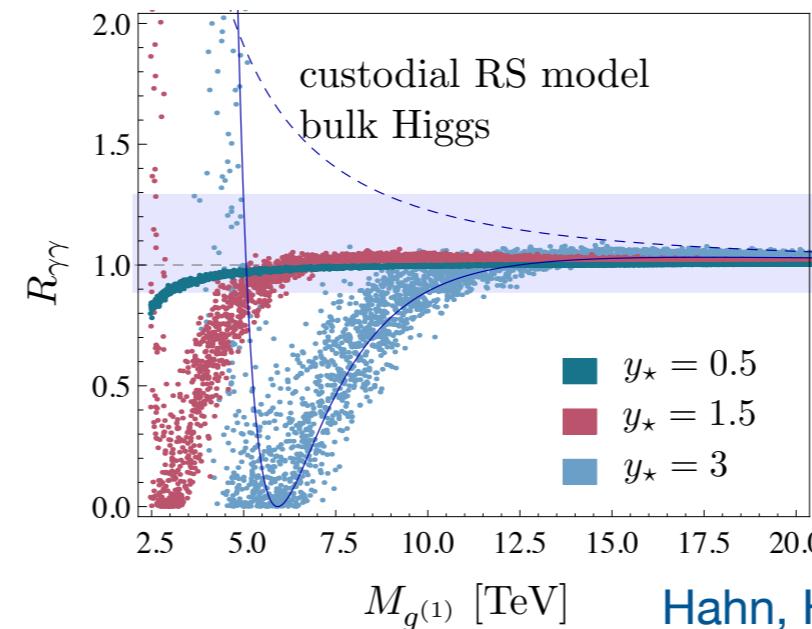
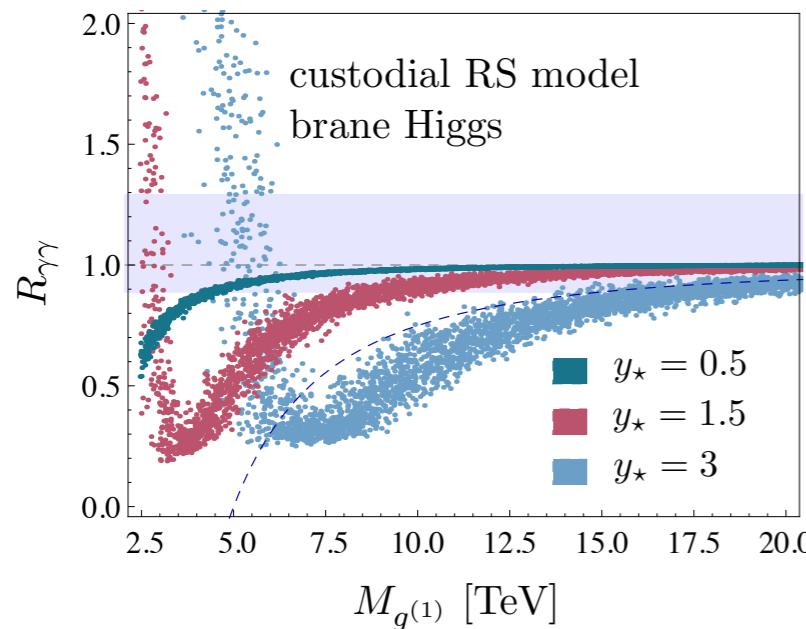
experimental data  
from ATLAS/CMS  
(combined)

Hahn, Hörner, Malm, MN, Novotny, Schmell:  
[arXiv:1312.5731](https://arxiv.org/abs/1312.5731)



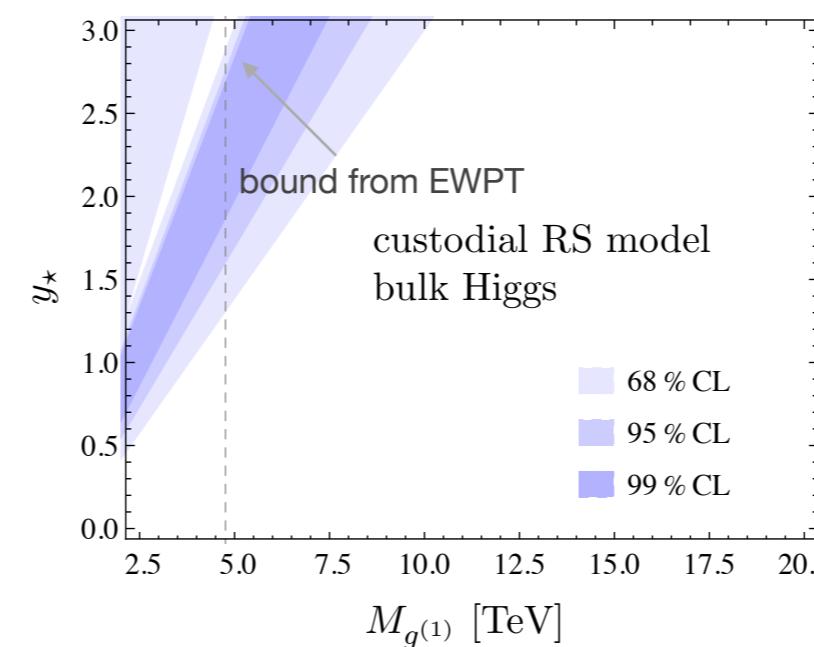
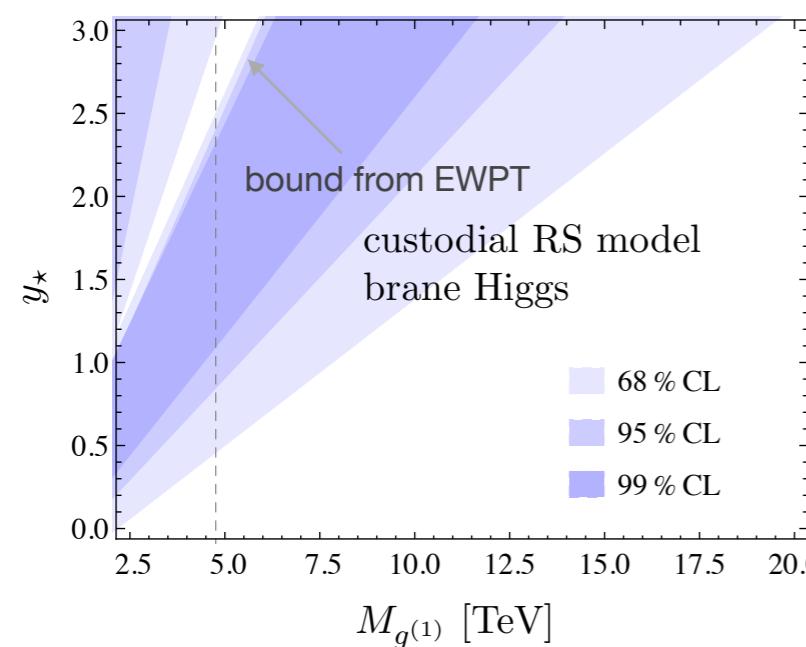
# Phenomenological predictions and LHC data

Ratio  $R_{\gamma\gamma} \equiv \frac{(\sigma \cdot \text{BR})(pp \rightarrow h \rightarrow \gamma\gamma)_{\text{RS}}}{(\sigma \cdot \text{BR})(pp \rightarrow h \rightarrow \gamma\gamma)_{\text{SM}}}$  in RS model with **custodial symmetry**:



experimental data  
from ATLAS/CMS  
(combined)

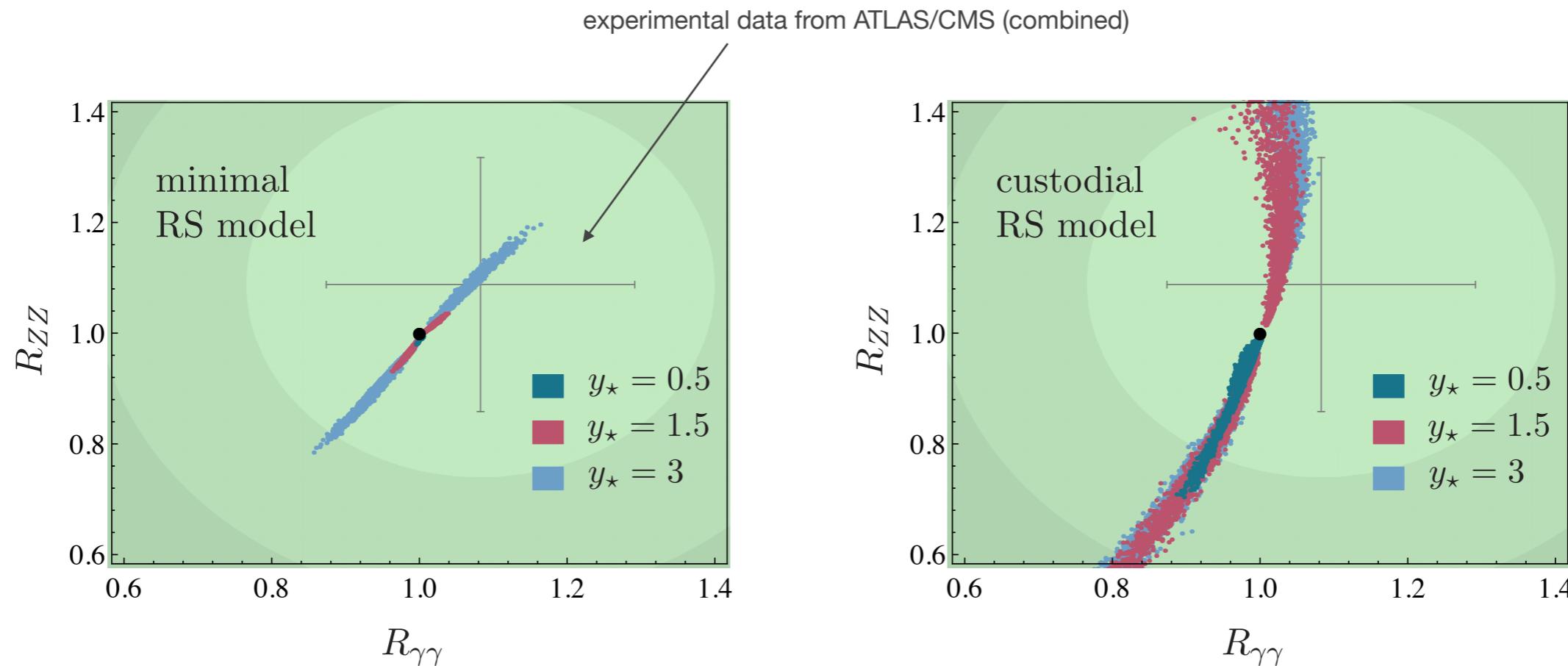
Hahn, Hörner, Malm, MN, Novotny, Schmell:  
[arXiv:1312.5731](https://arxiv.org/abs/1312.5731)



# Strong correlation between $R_{\gamma\gamma}$ and $R_{ZZ}$

**Strong correlation** of the predictions for  $R_{\gamma\gamma}$  and  $R_{ZZ}$  is observed!

Parameter scan of model points satisfying the bounds from electroweak precision tests:



Malm, MN, Schmell: in preparation

More precise measurements at LHC and ILC will allow one to differentiate between different variants of RS models

# Conclusions

---

- Higgs **phenomenology** provides a **superb laboratory for probing new physics** in the EWSB sector at the quantum level
- Much like rare FCNC processes, Higgs production in gluon fusion and Higgs decays into two photons are **loop-suppressed processes**, which are sensitive to new heavy particles
- **Warped extra-dimension models** provide an appealing framework for addressing the **hierarchy problem** and the **flavor puzzle** within the same geometrical approach
- Find that the contribution of the Kaluza-Klein towers of SM quarks and gauge bosons are universal and given entirely in terms of fundamental **5D Yukawa matrices** and **KK mass scale**
- Effects are enhanced by the **large multiplicity** of 5D fermion states and probe regions of parameter space **not accessible to direct searches**



# **BACKUP SLIDES**

# Representations of lepton multiplets

---

Extended RS model with **custodial symmetry** protecting the  $T$  parameter, the left-handed  $Z b\bar{b}$  couplings and flavor-violating  $Z$ -boson couplings

Bulk symmetry group:  $SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_X \times P_{LR}$

Representations of lepton multiplets: **minimal model**

$$L_L = \begin{pmatrix} \nu_L^{(+)} & 0 \\ e_L^{(+)} & -1 \end{pmatrix}_{-\frac{1}{2}}, \quad L_R^c = \begin{pmatrix} e_R^{c(+)} & -1 \\ N_R^{(-)} & 0 \end{pmatrix}_{-\frac{1}{2}}$$

→ used as default

# Representations of lepton multiplets

---

Extended RS model with **custodial symmetry** protecting the  $T$  parameter, the left-handed  $Zb\bar{b}$  couplings and flavor-violating  $Z$ -boson couplings

Bulk symmetry group:  $SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_X \times P_{LR}$

Representations of lepton multiplets: **extended model**

$$\xi_{1L} = \begin{pmatrix} \nu_L^{(+)} & \psi_L^{(-)} \\ e_L^{(+)} & \nu_L'^{-(-)} \end{pmatrix}_0, \quad \xi_{2R} = \left( \nu_R^{c(+)} \right)_0$$

$$\xi_{3R} = \mathcal{T}_{3R} \oplus \mathcal{T}_{4R} = \begin{pmatrix} \Psi_R'^{-(-)} \\ N_R'^{-(-)} \\ E_R'^{-(-)} \end{pmatrix}_0 \oplus \begin{pmatrix} E_R^{(+)} & N_R^{(-)} & \Psi_R^{(-)} \end{pmatrix}_0$$

$$L_L = \begin{pmatrix} \nu_L^{(+)} \\ e_L^{(+)} \end{pmatrix}_{-\frac{1}{2}}, \quad L_R^c = \begin{pmatrix} e_R^{c(+)} \\ N_R^{(-)} \end{pmatrix}_{-\frac{1}{2}}$$

# gg $\rightarrow$ h production (details of the calculation)

---

Definition of the gg $\rightarrow$ h amplitude:

$$\mathcal{A}(gg \rightarrow h) = C_1 \frac{\alpha_s}{12\pi v} \langle 0 | G_{\mu\nu}^a G^{\mu\nu,a} | gg \rangle - C_5 \frac{\alpha_s}{8\pi v} \langle 0 | G_{\mu\nu}^a \tilde{G}^{\mu\nu,a} | gg \rangle$$

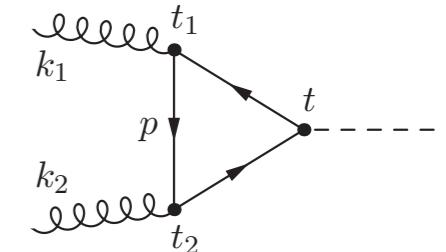
Expression in terms of 5D propagators:

$$\begin{aligned} \mathcal{A}(gg \rightarrow h) &= ig_s^2 \delta^{ab} \sum_{q=u,d} \int \frac{d^d p}{(2\pi)^d} \int_{\epsilon}^1 dt_1 \int_{\epsilon}^1 dt_2 \int_{\epsilon}^1 dt \delta_h^\eta(t-1) \\ &\quad \times \text{Tr} \left[ \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & \mathbf{Y}_q \\ \mathbf{Y}_q^\dagger & 0 \end{pmatrix} \mathbf{S}^q(t, t_2; p - k_2) \not{k}(k_2) \mathbf{S}^q(t_2, t_1; p) \not{k}(k_1) \mathbf{S}^q(t_1, t; p + k_1) \right] \end{aligned}$$

with:

$$\begin{aligned} i\mathbf{S}^q(t, t'; p) &= \int d^4 x e^{ip \cdot x} \langle 0 | T(\mathcal{Q}_L(t, x) + \mathcal{Q}_R(t, x)) (\bar{\mathcal{Q}}_L(t', 0) + \bar{\mathcal{Q}}_R(t', 0)) | 0 \rangle \\ &= [\Delta_{LL}^q(t, t'; -p^2) \not{p} + \Delta_{RL}^q(t, t'; -p^2)] P_R + (L \leftrightarrow R) \end{aligned}$$

Malm, MN, Novotny, Schmell: arXiv:1303.5702



# gg $\rightarrow$ h production (details of the calculation)

---

**Exact analytic results** for Wilson coefficients in terms of an integral over a single 5D propagator function:

$$C_{1\gamma}^q = 3N_c \sum_{f=u,d} Q_q^2 \int_0^1 dx \int_0^{1-x} dy (1 - 4xy) [T_+^q(-xym_h^2) - T_+^q(\Lambda_{\text{TeV}}^2)]$$

$$C_{5\gamma}^q = 2N_c \sum_{f=u,d} Q_q^2 \int_0^1 dx \int_0^{1-x} dy [T_-^q(-xym_h^2) - T_-^q(\Lambda_{\text{TeV}}^2)]$$

where:

$$T_+(p_E^2) = - \sum_{q=u,d} \frac{v}{\sqrt{2}} \int_{\epsilon}^1 dt \delta_h^\eta(t-1) \text{Tr} \left[ \begin{pmatrix} 0 & \mathbf{Y}_q \\ \mathbf{Y}_q^\dagger & 0 \end{pmatrix} \frac{\Delta_{RL}^q(t,t;p_E^2) + \Delta_{LR}^q(t,t;p_E^2)}{2} \right]$$

$$T_-(p_E^2) = - \sum_{q=u,d} \frac{v}{\sqrt{2}} \int_{\epsilon}^1 dt \delta_h^\eta(t-1) \text{Tr} \left[ \begin{pmatrix} 0 & \mathbf{Y}_q \\ \mathbf{Y}_q^\dagger & 0 \end{pmatrix} \frac{\Delta_{RL}^q(t,t;p_E^2) - \Delta_{LR}^q(t,t;p_E^2)}{2i} \right]$$

Contributions at large momenta (near cutoff) vanish if the Higgs is a bulk field, but not if it lives on the IR brane!

# Impact of higher-dimensional hgg operators

---

Consider a dimension-6 operator localized on the IR brane, which can mediate  $gg \rightarrow h$  at tree level with effective strength  $c_{\text{eff}}$  (could be  $O(1)$  for strong coupling):

$$S_{\text{eff}} = \int d^4x \int_{-r\pi}^{r\pi} dx_5 c_{\text{eff}} \delta(|x_5| - r\pi) \frac{\Phi^\dagger \Phi}{\Lambda_{\text{TeV}}^2} \frac{g_{s,5}^2}{4} G_{\mu\nu}^a G^{\mu\nu,a} + \dots$$

Resulting effective Lagrangian:

$$\mathcal{L}_{\text{eff}} = \frac{c_{\text{eff}}}{\Lambda_{\text{TeV}}^2} \mathcal{O}_{\text{eff}} \quad \text{with} \quad \mathcal{O}_{\text{eff}} = \Phi^\dagger \Phi \frac{g_s^2}{4} G_{\mu\nu}^a G^{\mu\nu,a} \ni \frac{g_s^2 v^2}{8} \left(1 + \frac{h(x)}{v}\right)^2 G_{\mu\nu}^a G^{\mu\nu,a}$$

Resulting contribution to Wilson coefficient  $C_1$ :

$$\Delta C_1 = \frac{3c_{\text{eff}}}{4} \left(\frac{4\pi v}{\Lambda_{\text{TeV}}}\right)^2 \approx c_{\text{eff}} \left(\frac{2.7 \text{ TeV}}{\Lambda_{\text{TeV}}}\right)^2$$

for  $\Lambda_{\text{TeV}} \sim 20\text{-}50 \text{ TeV}$ , as is appropriate for KK masses  
in 5-15 TeV range, this effect is very small !