

# On the “ $\Delta A_{CP}$ saga”

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## About the Title

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The question arose because LHCb collaboration, at the end of 2011, measured LHCb Coll. PRL 108, 111602 (2012)

$$\Delta A_{CP} = a_{CP}(K^+ K^-) - a_{CP}(\pi^+ \pi^-)$$

$$\Delta A_{CP} = (-0.82 \pm 0.21 \pm 0.11)\%$$

$$\Delta A_{CP} \approx -1\%$$

Is this value compatible with the Standard Model?  
Is this a signal of New Physics?

## $\Delta A_{CP}$ Measurements and HFAG world average

- CDF [arXiv:1207.2158 \[hep-ex\]](#)  $\Delta A_{CP} = (-0.62 \pm 0.21 \pm 0.10)\%$
- Belle [arXiv:1212.1975 \[hep-ex\]](#)  $\Delta A_{CP} = (-0.87 \pm 0.41 \pm 0.06)\%$
- LHCb [LHCb-CONF-2013-003](#)  $\Delta A_{CP} = (-0.34 \pm 0.15 \pm 0.10)\%$
- LHCb [arXiv:1405.2797 \[hep-ex\]](#)  $\Delta A_{CP} = (+0.14 \pm 0.16 \pm 0.08)\%$

Including also Babar and Belle individual measurements HFAG (in **May 2014**) obtained ([J. Brod @ FPCP 2014](#))

$$\Delta A_{CP} = (-0.253 \pm 0.104)\%$$

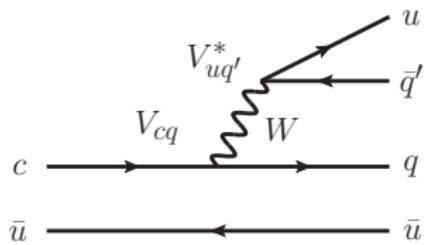
Last HFAG (11 June 2014) uses only latest LHCb results  
(by putting together the individual measurements):

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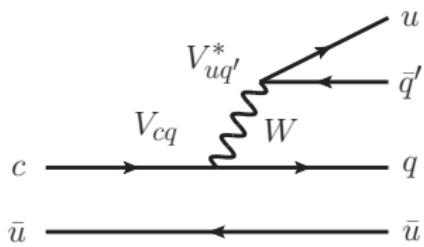
## Outline

- Non-leptonic Decays of D Mesons
- CP Violation and  $\Delta A_{CP}$
- A Model for Cabibbo Suppressed Decays
- Conclusions

# Hadronic two-body Decays of D Meson

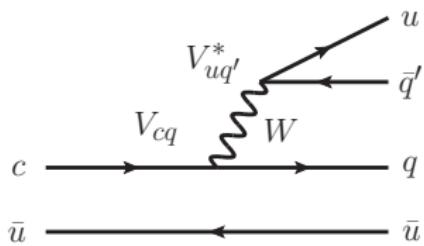


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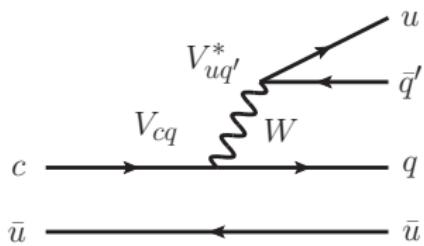


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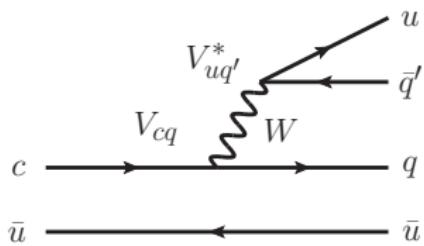
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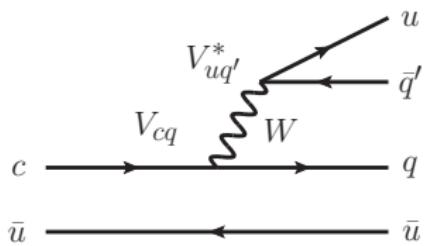
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**DCS** Double Cabibbo Suppressed:  $|V_{cd} V_{us}^*| \approx \lambda^2$  ( $D^0 \rightarrow K^+ \pi^-$ )

# Weak Effective Hamiltonian

The effective field theory formalism allows to separate the **short** and **long** distances and it is easy to include **perturbative QCD corrections**.

$$\begin{aligned} H_w^{\text{SCS}} &= \frac{G_F}{\sqrt{2}} V_{ud} V_{cd}^* [C_1 O_1^d + C_2 O_2^d] + \frac{G_F}{\sqrt{2}} V_{us} V_{cs}^* [C_1 O_1^s + C_2 O_2^s] \\ &- \frac{G_F}{\sqrt{2}} V_{ub} V_{cb}^* \sum_{i=3}^6 C_i O_i + h.c. \end{aligned}$$

## Current-Current Operators

$$O_2 = [\bar{q}^\alpha \gamma^\mu (1 - \gamma_5) c_\alpha] [\bar{u}^\beta \gamma_\mu (1 - \gamma_5) q'_\beta]$$

$$O_1 = [\bar{u}^\alpha \gamma^\mu (1 - \gamma_5) c_\beta] [\bar{q}^\beta \gamma_\mu (1 - \gamma_5) q'_\alpha]$$

$q = q' \in \{d, s\}$  for SCS

## Penguin Operators

$$O_3 = [\bar{u}^\alpha \gamma^\mu (1 - \gamma_5) c_\alpha] \sum_{p=u,d,s} [\bar{p}^\beta \gamma_\mu (1 - \gamma_5) p_\beta]$$

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$$O_6 = [\bar{u}^\alpha \gamma^\mu (1 - \gamma_5) c_\beta] \sum_{p=u,d,s} [\bar{p}^\beta \gamma^\mu (1 + \gamma_5) p_\alpha]$$

# Hadronic Matrix Elements

We have to evaluate

$$\langle f | H_w | D \rangle = \frac{G_F}{\sqrt{2}} VV^* \textcolor{red}{C}_j \langle f | \textcolor{blue}{O}_j | D \rangle + \dots$$

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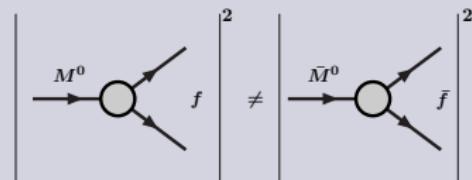
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- Models of calculations can be useful to estimate order of magnitudes
  - Factorization & Final state Interactions
  - Flavour symmetries ( $SU(3)_F$ , Isospin, U-spin, etc. )

## CP Violation in the Decays: The Direct CPV

This occurs when the decay amplitudes for CP conjugate processes into final states  $f$  and  $\bar{f}$  are different in modulus

$$|\mathcal{A}(M^0 \rightarrow f)| \neq |\mathcal{A}(\bar{M}^0 \rightarrow \bar{f})|$$

in our case  $f = \bar{f}$

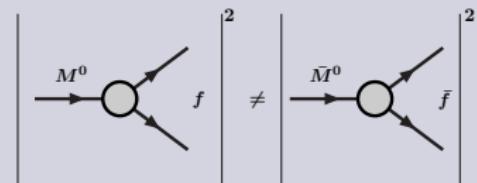


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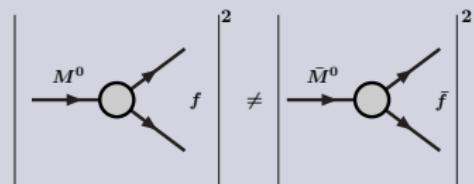
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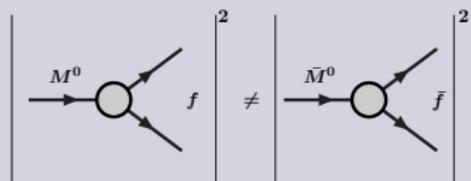
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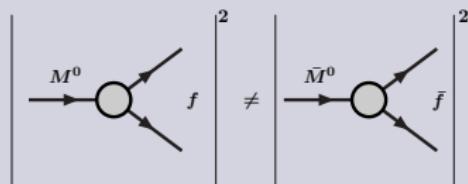
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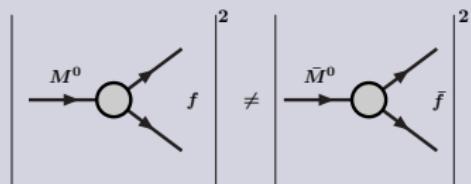
$$a_{CP} = \frac{|\mathcal{A}|^2 - |\bar{\mathcal{A}}|^2}{|\mathcal{A}|^2 + |\bar{\mathcal{A}}|^2} = \frac{2 \Im(T^* P) \sin(\delta_T - \delta_P)}{|T|^2 + |P|^2 + 2 \Re(T^* P) \cos(\delta_T - \delta_P)}$$

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Obviously, New Physics could be responsible of a  $|P/T|$  enhancement

see, for example, talk by Buras

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HFAG

June 2014

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$$\begin{aligned} H_{\Delta U=1} &= \frac{G_F}{2\sqrt{2}} (V_{us} V_{cs}^* - V_{ud} V_{cd}^*) [\textcolor{red}{C}_1 (\textcolor{blue}{O}_1^s - \textcolor{blue}{O}_1^d) + \textcolor{red}{C}_2 (\textcolor{blue}{O}_2^s - \textcolor{blue}{O}_2^d)] \\ &\simeq \frac{G_F}{\sqrt{2}} \sin \theta_C \cos \theta_C [\textcolor{red}{C}_1 (\textcolor{blue}{O}_1^s - \textcolor{blue}{O}_1^d) + \textcolor{red}{C}_2 (\textcolor{blue}{O}_2^s - \textcolor{blue}{O}_2^d)]. \end{aligned}$$

## A Simple Model to Evaluate SCS D Decays (1)

There are only two independent combinations of *S*-wave states having  $U=1$

$$H_{\Delta U=1} |D^0\rangle = \textcolor{red}{a}|v_1\rangle + \textcolor{red}{b}|v_2\rangle$$

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where

$$|\nu_1\rangle = \frac{1}{2} \left\{ |K^+ K^- \rangle + |K^- K^+ \rangle - |\pi^+ \pi^- \rangle - |\pi^- \pi^+ \rangle \right\}$$

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$$A(D^0 \rightarrow \pi^+ \pi^-) = \langle \pi^+ \pi^- | H_{\Delta U=1} | D^0 \rangle = \textcolor{red}{a} \langle \pi^+ \pi^- | \nu_1 \rangle + \textcolor{red}{b} \langle \pi^+ \pi^- | \nu_2 \rangle$$

## A Simple Model to Evaluate SCS D Decays (2)

More interestingly the two independent combinations of  $S$ -wave states having  $U=1$  can be written in terms of two representations of  $SU(3)$

$$|8, U=1\rangle = \frac{\sqrt{3}}{2\sqrt{5}} \left\{ \begin{array}{l} |K^+K^-> + |K^-K^+> - |\pi^+\pi^-> - |\pi^-\pi^+> \\ - \left[ |\pi^0\pi^0> - |\eta_8\eta_8> - \frac{1}{\sqrt{3}}(|\pi^0\eta_8> + |\eta_8\pi^0>) \right] \end{array} \right\},$$
$$|27, U=1\rangle = \frac{1}{\sqrt{10}} \left\{ \begin{array}{l} |K^+K^-> + |K^-K^+> - |\pi^+\pi^-> - |\pi^-\pi^+> \\ + \frac{3}{2} \left[ |\pi^0\pi^0> - |\eta_8\eta_8> - \frac{1}{\sqrt{3}}(|\pi^0\eta_8> + |\eta_8\pi^0>) \right] \end{array} \right\}.$$

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$$\begin{aligned} \langle 8, U=1 | H_{\Delta U=1} | D^0 \rangle &\propto T - \frac{2}{3} C \\ \langle 27, U=1 | H_{\Delta U=1} | D^0 \rangle &\propto T + C \end{aligned}$$



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$$\begin{aligned} A(D^0 \rightarrow K^+K^-) &= \alpha \left( T - \frac{2}{3}C \right) + \beta (T + C) \\ A(D^0 \rightarrow \pi^+\pi^-) &= \gamma \left( T - \frac{2}{3}C \right) + \delta (T + C) \end{aligned}$$

# Final State Interactions in SCS D Decays

The necessary SU(3) breaking is determined by the final state interactions, described as the effect of resonances in the scattering of the final particles.

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In other words, strong phases are generated by the resonances responsible for rescattering of final states.

The possible resonances have SU(3) and isospin quantum numbers  $(8, I = 1)$ ,  $(8, I = 0)$  and  $(1, I = 0)$ . Moreover, the two states with  $I = 0$  can be mixed, yielding two resonances:

$$|f_0\rangle = \sin\phi |8, I=0\rangle + \cos\phi |1, I=0\rangle$$
$$|f'_0\rangle = -\cos\phi |8, I=0\rangle + \sin\phi |1, I=0\rangle$$

The mixing angle  $\phi$  and the strong phases  $\delta_0$ ,  $\delta'_0$  and  $\delta_1$  are our model parameters, together with the two independent weak decay amplitudes

# Final State Interactions in SCS D Decays (1)

$$A(D^0 \rightarrow \pi^+ \pi^-) = \left( \tau - \frac{2}{3} c \right) \left\{ -\frac{3}{10} \left( e^{i\delta_0} + e^{i\delta'_0} \right) + \left( -\frac{3}{10} \cos(2\phi) + \frac{3}{4\sqrt{10}} \sin(2\phi) \right) \left( e^{i\delta'_0} - e^{i\delta_0} \right) \right\}$$
$$- \left( \tau + c \right) \frac{2}{5},$$
$$A(D^0 \rightarrow K^+ K^-) = \left( \tau - \frac{2}{3} c \right) \left\{ \frac{3}{20} \left( e^{i\delta_0} + e^{i\delta'_0} \right) + \left( \frac{3}{20} \cos(2\phi) + \frac{3}{4\sqrt{10}} \sin(2\phi) \right) \left( e^{i\delta'_0} - e^{i\delta_0} \right) \right.$$
$$\left. + \frac{3}{10} e^{i\delta_1} \right\}$$
$$+ \left( \tau + c \right) \frac{2}{5}.$$

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## Parameters

$$\begin{aligned} C/T &= -0.53 \\ \phi &= 22^\circ \\ \delta_0 &= 148^\circ \\ \delta'_0 &= 53^\circ \\ \delta_1 &= 83^\circ \end{aligned}$$

## Results

$$\frac{\Gamma(D^0 \rightarrow K_S K_S)}{\Gamma(D^0 \rightarrow K^+ K^-)} = 0.0429 \text{ (0.043 ± 0.010)}$$
$$\frac{\Gamma(D^0 \rightarrow \pi^+ \pi^-)}{\Gamma(D^0 \rightarrow K^+ K^-)} = 0.354 \text{ (0.354 ± 0.010)}$$
$$\frac{\Gamma(D^0 \rightarrow \pi^0 \pi^0)}{\Gamma(D^0 \rightarrow K^+ K^-)} = 0.202 \text{ (0.202 ± 0.013)}$$
$$\left| \frac{A_2(D^0 \rightarrow \pi^+ \pi^-)}{A_0(D^0 \rightarrow \pi^+ \pi^-)} \right| = 0.40 \text{ (0.41 ± 0.01)}$$

# Direct CPV in SCS D Decays (1)

The second amplitude  $P$  is provided by

$$\langle f | H_{\Delta U=0} | D^0 \rangle$$

where

$$H_{\Delta U=0} = -\frac{G_F}{\sqrt{2}} V_{ub} V_{cb}^* \left\{ \underbrace{\sum_{i=3}^6 C_i O_i}_{\text{Penguins}} + \underbrace{\frac{1}{2} [C_1(O_1^s + O_1^d) + C_2(O_2^s + O_2^d)]}_{\text{Tree } (T', C') \text{ Penguin Contraction}} \right\}$$

Note that

$$|T'/T| = |C'/C| = \left| \frac{V_{ub} V_{cb}^*}{\sin \theta_C \cos \theta_C} \right| \simeq 10^{-4}$$

## Direct CPV in SCS D Decays (2)

$$\mathcal{A}(K^+ K^-) \simeq \textcolor{blue}{T} f_T(\delta_i, \phi, C/T) + \textcolor{blue}{P} f_P(\delta_i, \phi)$$

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thus

$$a_{CP}(K^+ K^-) \simeq \frac{2 T \Im(P) \Im(f_T f_P^*)}{T^2 |f_T|^2} + \dots = +1.5 \frac{\Im(\textcolor{blue}{P})}{T}$$
$$a_{CP}(\pi^+ \pi^-) = -3.4 \frac{\Im(\textcolor{blue}{P})}{T}$$

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$$\frac{\Im(P)}{T} = \frac{|V_{ub} V_{cb}|}{\sin \theta_C \cos \theta_C} \sin \gamma \frac{\langle K^+ K^- | \sum_{i=3}^6 C_i Q_i + \frac{1}{2} [C_1 \{Q_1^s + Q_1^d\} + C_2 \{Q_2^s + Q_2^d\}] |D^0 \rangle}{\langle K^+ K^- | C_1 (Q_1^s - Q_1^d) + C_2 (Q_2^s - Q_2^d) |D^0 \rangle} = 6.3 \cdot 10^{-4} \frac{\hat{P}}{\hat{T}}$$

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$$\Delta A_{CP} = 3.03 \cdot 10^{-3} \frac{\hat{P}}{\hat{T}}$$

With

$$\left| \frac{\hat{P}}{\hat{T}} \right| \approx 1$$

we obtain the central value of the world average result

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## Conclusions

We analyzed the Singly-Cabibbo-Suppressed decays of the neutral  $D$  mesons in the framework of a model that ascribes all of the large SU(3) violations to final state interactions.

The values of the strong phases are in principle suitable to predict consistent CP violations in the decay amplitudes.

We were able to give a good description of decay branching ratios

The experimental situation regarding the CP violating asymmetries seems to be rather clear: there is no significant CP violation in the SCS decays at the level of  $10^{-3}$ .

Nevertheless, we think interesting to have shown that large asymmetries can be obtained, considering the uncertainties of long distance contributions, even without invoking New Physics.

# Backup Slides

# HFAG World Averages

| Year | Experiment | CP Asymmetry in the decay mode D0 to $\pi^+\pi^-$                                       | $[\Gamma(D0)-\Gamma(D0\bar{b}ar)]/[\Gamma(D0)+\Gamma(D0\bar{b}ar)]$ |
|------|------------|---|---|
| 2014 | LHCb       | <a href="#">R. Aaij et al. (LHCb Collab.), arXiv:1405.2797 (2014)</a> ,                 | -0.0020 $\pm$ 0.0019 $\pm$ 0.0010                                   |
| 2012 | BELLE      | <a href="#">B.R. Ko et al. (BELLE Collab.), arXiv:1212.1975 (2012)</a> .                | +0.0055 $\pm$ 0.0036 $\pm$ 0.0009                                   |
| 2012 | CDF        | <a href="#">T. Aaltonen et al. (CDF Collab.), Phys. Rev. D 85, 012009 (2012)</a> .      | +0.0022 $\pm$ 0.0024 $\pm$ 0.0011                                   |
| 2008 | BABAR      | <a href="#">B. Aubert et al. (BABAR Collab.), Phys. Rev. Lett. 100, 061803 (2008)</a> . | -0.0024 $\pm$ 0.0052 $\pm$ 0.0022                                   |
| 2002 | CLEO       | <a href="#">S.E. Csorna et al. (CLEO Collab.), Phys. Rev. D 65, 092001 (2002)</a> .     | +0.019 $\pm$ 0.032 $\pm$ 0.008                                      |
| 2000 | FOCUS      | <a href="#">J.M. Link et al. (FOCUS Collab.), Phys. Lett. B 491, 232 (2000)</a> .       | +0.048 $\pm$ 0.039 $\pm$ 0.025                                      |
| 1998 | E791       | <a href="#">E.M. Aitala et al. (E791 Collab.), Phys. Lett. B 421, 405 (1998)</a> .      | -0.049 $\pm$ 0.078 $\pm$ 0.030                                      |
| .    | .          | COMBOS average  | +0.0005 $\pm$ 0.0015  |

| Year | Experiment | CP Asymmetry in the decay mode D0 to $K^+K^-$   | $[\Gamma(D0)-\Gamma(D0\bar{b}ar)]/[\Gamma(D0)+\Gamma(D0\bar{b}ar)]$ |
|------|------------|---|---|
| 2014 | LHCb       | <a href="#">R. Aaij et al. (LHCb Collab.), arXiv:1405.2797 (2014)</a> ,                 | -0.0006 $\pm$ 0.0015 $\pm$ 0.0010                                   |
| 2012 | BELLE      | <a href="#">B.R. Ko et al. (BELLE Collab.), arXiv:1212.1975 (2012)</a> .                | -0.0032 $\pm$ 0.0021 $\pm$ 0.0009                                   |
| 2012 | CDF        | <a href="#">T. Aaltonen et al. (CDF Collab.), Phys. Rev. D 85, 012009 (2012)</a> .      | -0.0024 $\pm$ 0.0022 $\pm$ 0.0009                                   |
| 2008 | BABAR      | <a href="#">B. Aubert et al. (BABAR Collab.), Phys. Rev. Lett. 100, 061803 (2008)</a> . | +0.0000 $\pm$ 0.0034 $\pm$ 0.0013                                   |
| 2002 | CLEO       | <a href="#">S.E. Csorna et al. (CLEO Collab.), Phys. Rev. D 65, 092001 (2002)</a> .     | +0.000 $\pm$ 0.022 $\pm$ 0.008                                      |
| 2000 | FOCUS      | <a href="#">J.M. Link et al. (FOCUS Collab.), Phys. Lett. B 491, 232 (2000)</a> .       | -0.001 $\pm$ 0.022 $\pm$ 0.015                                      |
| 1998 | E791       | <a href="#">E.M. Aitala et al. (E791 Collab.), Phys. Lett. B 421, 405 (1998)</a> .      | -0.010 $\pm$ 0.049 $\pm$ 0.012                                      |
| 1994 | E687       | <a href="#">P.L. Frabetti et al. (E687 Collab.), Phys. Rev. D 50, 2953 (1994)</a> .     | +0.024 $\pm$ 0.084  |
| .    | .          | COMBOS average  | -0.0016 $\pm$ 0.0012  |

## $H_{\Delta U=0}$

In this case, there are three independent symmetric states of two pseudoscalar mesons:

$$\frac{1}{2} \left\{ |K^+ K^-> + |K^- K^+> + |\pi^+ \pi^-> + |\pi^- \pi^+> \right\};$$

$$\frac{1}{4} \left\{ 3|\pi^0 \pi^0> + |\eta_8 \eta_8> + \sqrt{3}(|\pi^0 \eta_8> + |\eta_8 \pi^0>) \right\};$$

$$\frac{1}{\sqrt{3}} \left\{ \frac{1}{4} |\pi^0 \pi^0> + \frac{3}{4} |\eta_8 \eta_8> - \frac{\sqrt{3}}{4} (|\pi^0 \eta_8> + |\eta_8 \pi^0>) + |K^0 \bar{K}^0> + |\bar{K}^0 K^0> \right\}$$

that give rise to three amplitudes transforming as 27, 8 and 1 under SU(3) (for the  $Q_{1(2)}$  part) and to two amplitudes transforming as 8 and 1 (for the penguin part)