

# Probing the nuclear symmetry energy with heavy ion collisions

W. Lynch

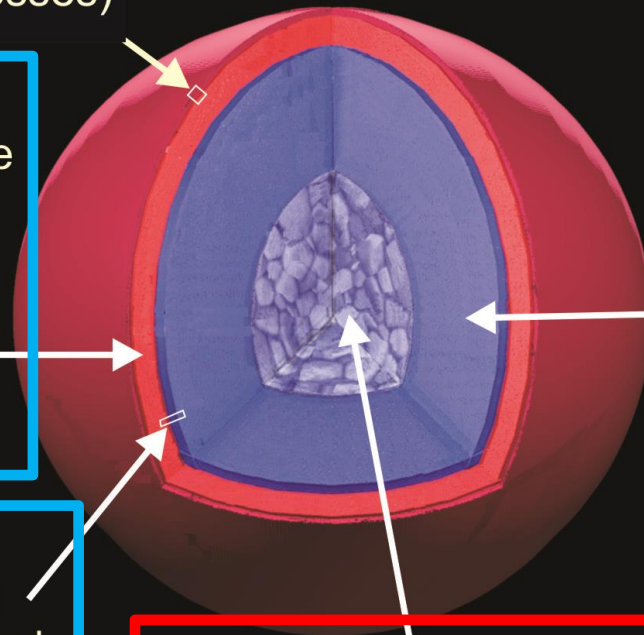
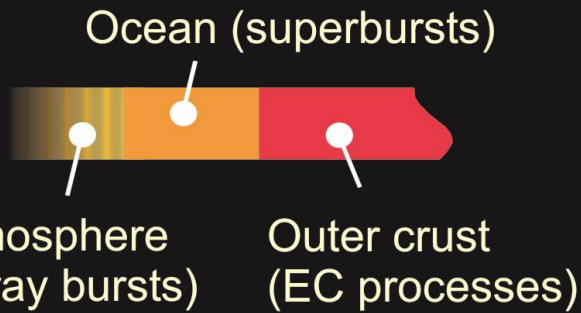
NSCL and Department of Physics and Astronomy

Michigan State University

- Relevance to neutron stars
- Improving constraints at sub-saturation densities
- Improving constraints at supra-saturation densities
- Issues of momentum dependence
- Outlook and perspectives

To progress, you need the relevant Equations of State for matter in the star

# Anatomy of a neutron star



EoS at  $\rho > \rho_0$

Outer core: Composed of neutron-rich nuclear matter. Governs stellar radii, and moments of inertia.

Inner crust: Neutron gas in coexistence with "Coulomb lattice" of nuclei. Thickness governs observed frequencies in star quakes.  
EoS at  $\rho < \rho_0$

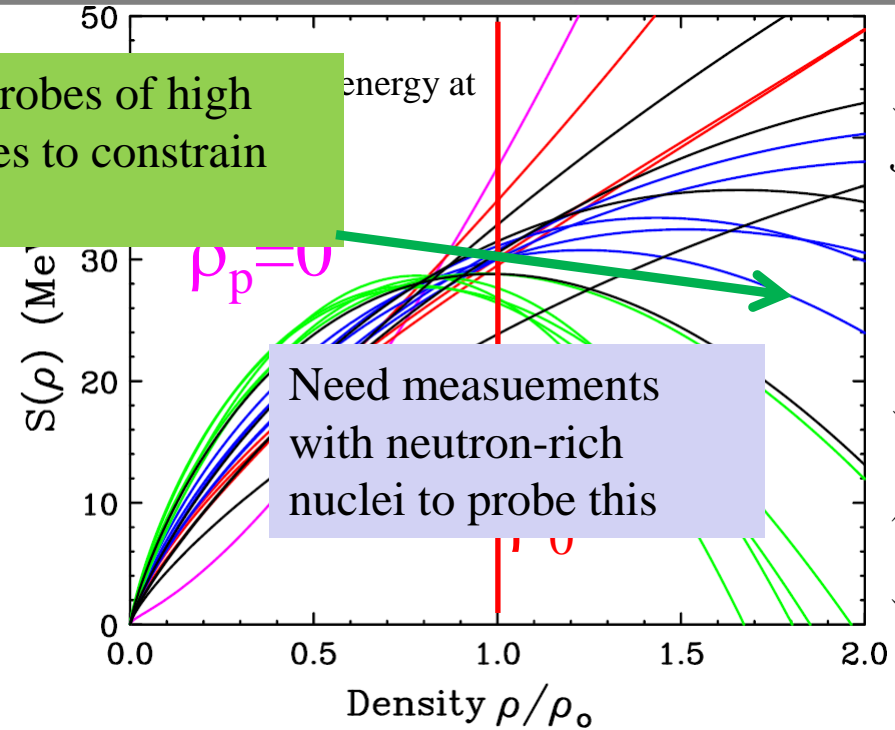
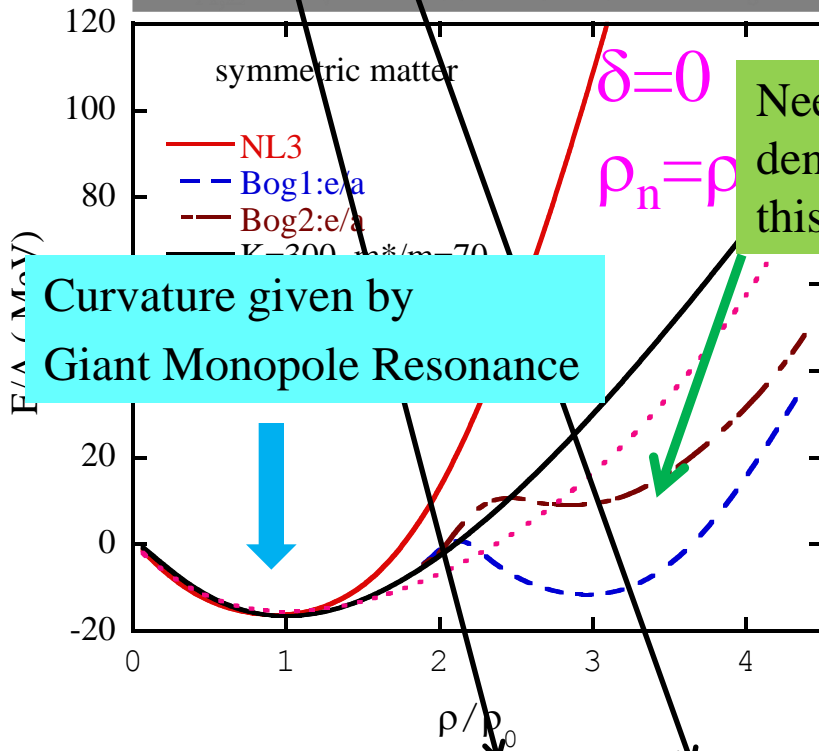
Inner boundary of inner crust: Transition to uniform "neutron matter". Cylindrical and plate-like nuclear "pasta"  
EoS at  $\rho < \rho_0$

Inner core: Composition? Strange or quark matter? Key to understanding maximum N-star mass cooling of proto-neutron star.  
momentum dependence

# For N-stars $T \approx 0 \Rightarrow$ Can use energy/nucleon as EoS

nuclear binding energy

$$B_{A,Z} = a_v [1 - b_1 ((N-Z)/A)^2] A - a_s [1 - b_2 ((N-Z)/A)^2] A^{2/3} - a_c Z^2/A^{1/3} + \delta_{A,Z} A^{-1/2} + C_d Z^2/A,$$



Brown, Phys. Rev. Lett. 85, 5296 (2001)

$$\varepsilon(\rho, \delta) = (E/A(\rho, \delta) - E/A(\rho, 0)) + \delta^2 S(\rho)$$

• Symmetry energy calculated from the EoS at  $\rho < \rho_0$ .

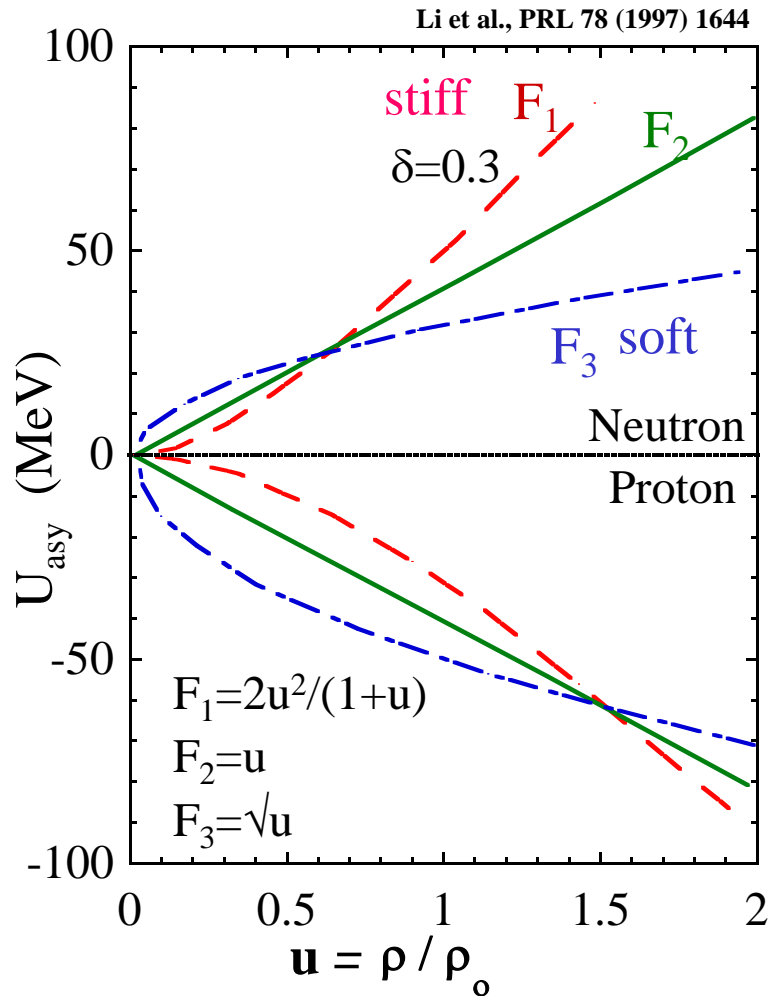
$\delta$  This was the situation in 2001  $\Leftrightarrow$  EoS is now much more constrained

$\partial \rho \big|_{s/a}$

EoS at  $\rho < \rho_0$ .

f S( $\rho$ ) of the

# Improvement $\Leftrightarrow$ Improved constraints on the potential energy contributions to $S(\rho)$ which provide the largest uncertainties



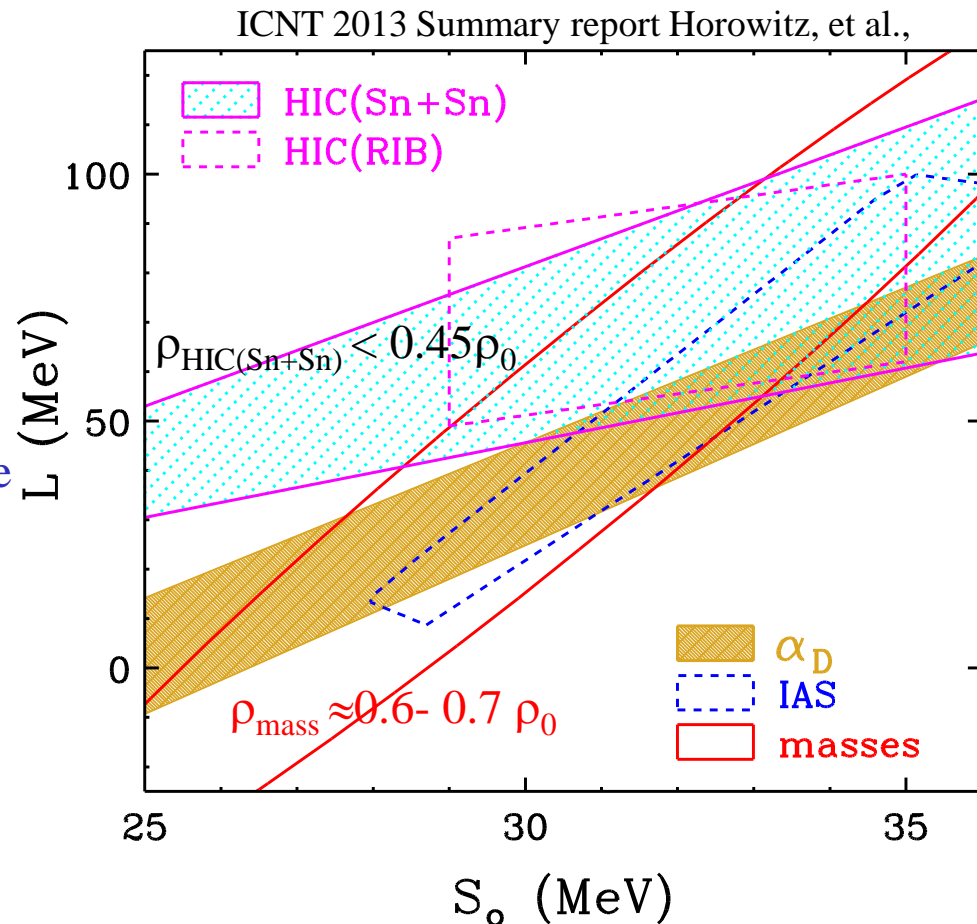
- In a neutron-rich system, the symmetry energy attracts protons and repels neutrons
- Observables that can probe sub-saturation densities:
  - Isospin diffusion:
  - Neutron-proton spectra and flows.
  - Difference between neutron and proton matter radii.
  - Giant and pygmy dipole resonances
  - El dipole polarizability  $\alpha_D$
  - Nuclear binding energies and isobaric analog resonance energies.

# Laboratory constraints on Symmetry energy at $\rho < \rho_0$

- Taylor expand about  $\rho_0$
- Experimental observables are mainly sensitive to  $S_0 = S(\rho_0)$  and  $L$ .
- Some sensitive observables:
  - masses
  - Isobaric Analog States (IAS)
  - Electric dipole polarizability ( $\alpha_D$ )
  - Diffusion of neutrons and protons between nuclei of different  $N/Z$  in peripheral collisions **HIC (Sn+Sn)**
  - Transverse flow **HIC (RIB)**
- Slope of constraint indicates the sensitive density
 
$$\rho_{\text{sens.}} = \rho_0 (1 - 3/M); M \text{ is slope}$$
- Neutron skin  $R_{\text{np}} = \langle r_n^2 \rangle^{1/2} - \langle r_p^2 \rangle^{1/2}$  is only sensitive to  $L$ .
- Realistic theoretical “Error bars” are key to combining constraints.

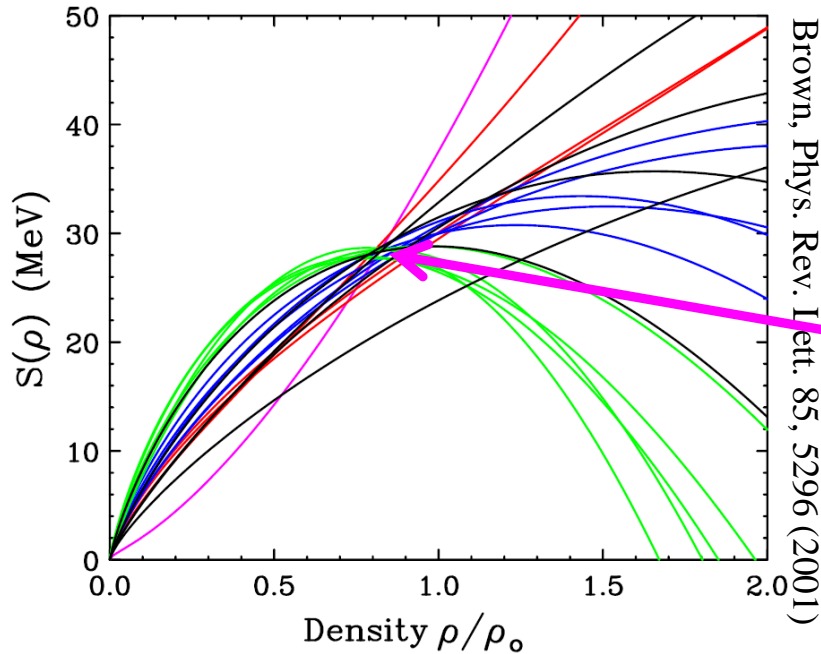
$$S(\rho) = S_0 + \frac{L}{3} \left( \frac{\rho_B - \rho_0}{\rho_0} \right) + \frac{K_{\text{sym}}}{18} \left( \frac{\rho_B - \rho_0}{\rho_0} \right)^2 + \dots$$

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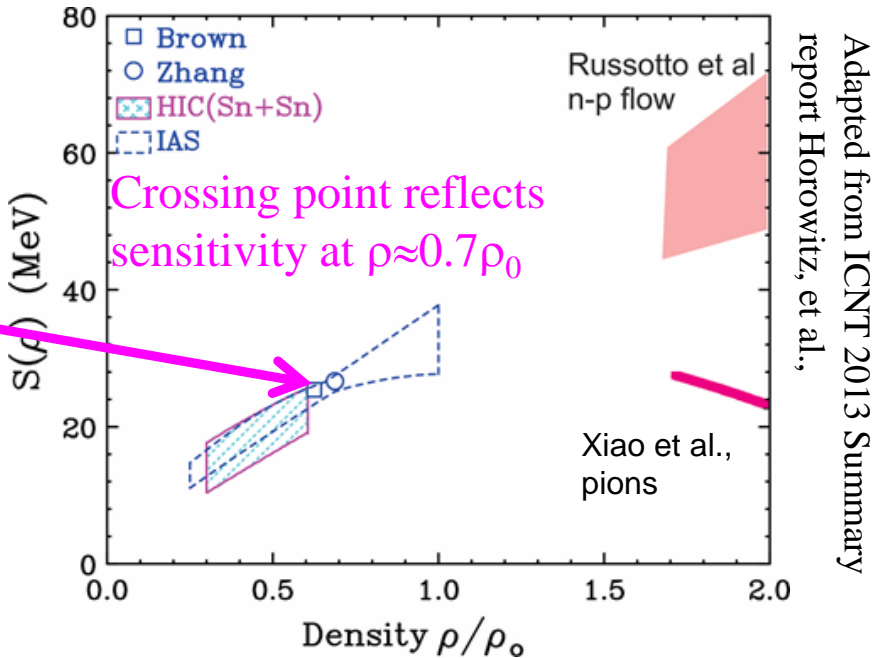


# Past vs. Present status of $S(\rho)$

Brown 2001 obtained by fitting Sn masses



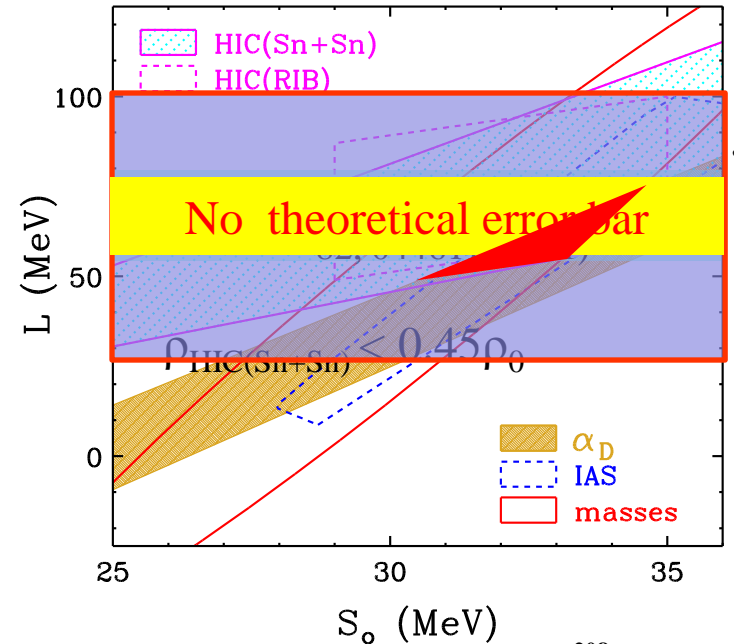
Constraints 2014 showing sensitive densities



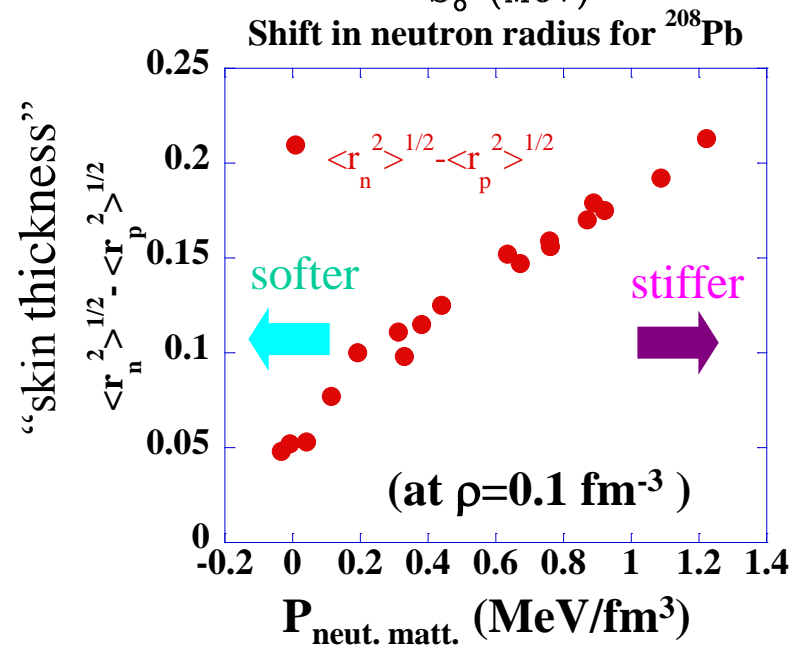
- Have initial constraints at sub and supra-saturation densities:
  - Contours reflect assessment of theoretical and experimental uncertainties
- Relevant questions:
  - How do we improve the constraints at  $\rho < \rho_0$ ?
  - How do we improve the constraints at supra-saturation densities?
  - How do we deal with momentum dependencies of mean fields?
    - Important for non-zero temperatures and non-equilibrium systems

# Improving constraints on Symmetry energy at $\rho < \rho_0$

- ❖ Sensitive observables that are or will be more extensively explored :
  - masses:
    - Penning traps, TOF
  - Isobaric Analog States (IAS)
    - Reaccelerated RIB's ReA3 and CARABU: AT-TPC collab.
  - Isospin diffusion between nuclei of different N/Z in peripheral HIC
    - Sn+Sn NSCL: new results soon
  - Neutron skins:
    - PREX, CREX at JLAB
  - Isoscalar GMR
    - RCNP-ND, MAYA, AT-TPC collaborations
  - Neutron and proton transverse and elliptical flow
  - Fragmentation of hot nuclei:
    - TAMU



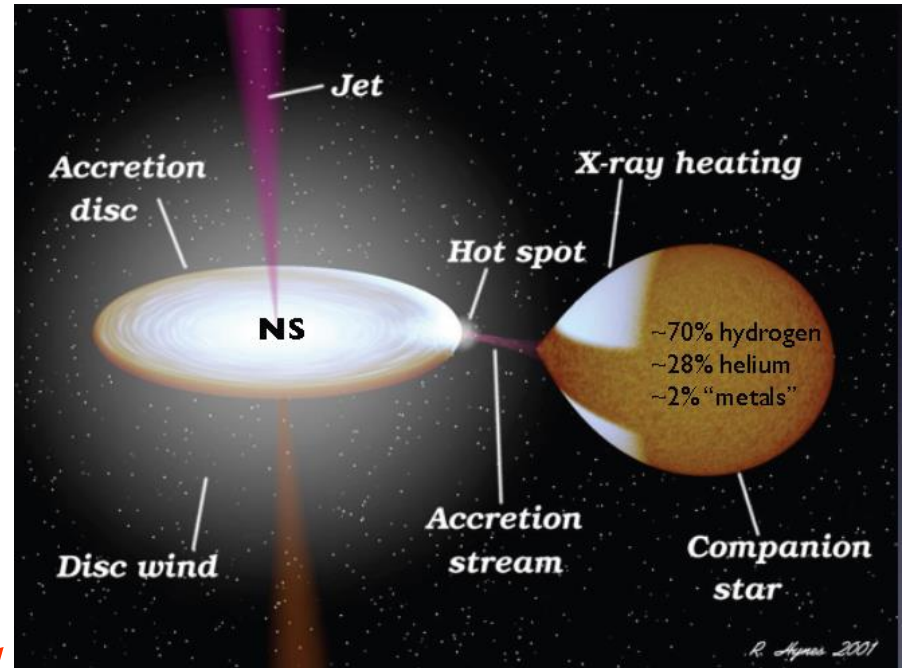
Horowitz, et al., J. Phys. G: Nucl. Part. Phys. 41 (2014) 093001



Brown, Phys. Rev. Lett. 85, 5296 (2001)

# New challenge: probing supra-saturation densities $\rho \approx 2\rho_0$

- EoS & Symmetry energy influence:
  - Neutron star stability against gravitational collapse
  - Stellar density profile
  - Internal structure: occurrence of various phases.
- Observational consequences:
  - Cooling rates of proto-neutron stars: [D. Yakovlev et al, Phys.Rep 354, 1 \(2001\)](#)
  - Correlation between stellar masses and radii—two sites:
    - X-ray bursters
    - Quiescent x-ray binary systems

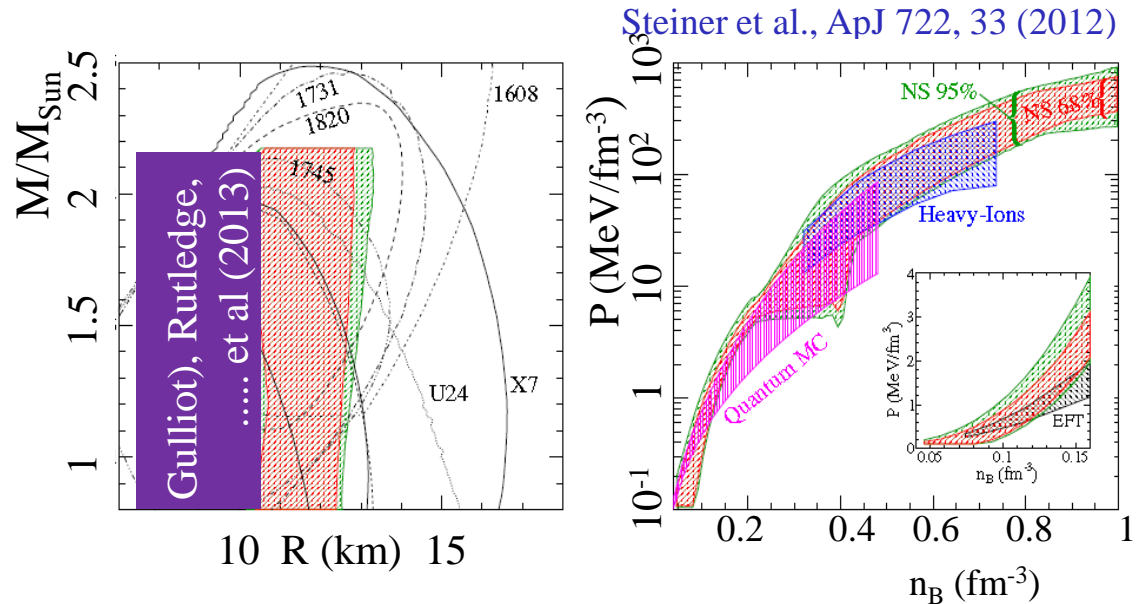


- Steiner et al., ApJ 722, 33 extract  $R=12.5 \pm 1.5$  km from both x-ray bursters and quiescent x-ray binaries consistent with a soft neutron matter EoS.



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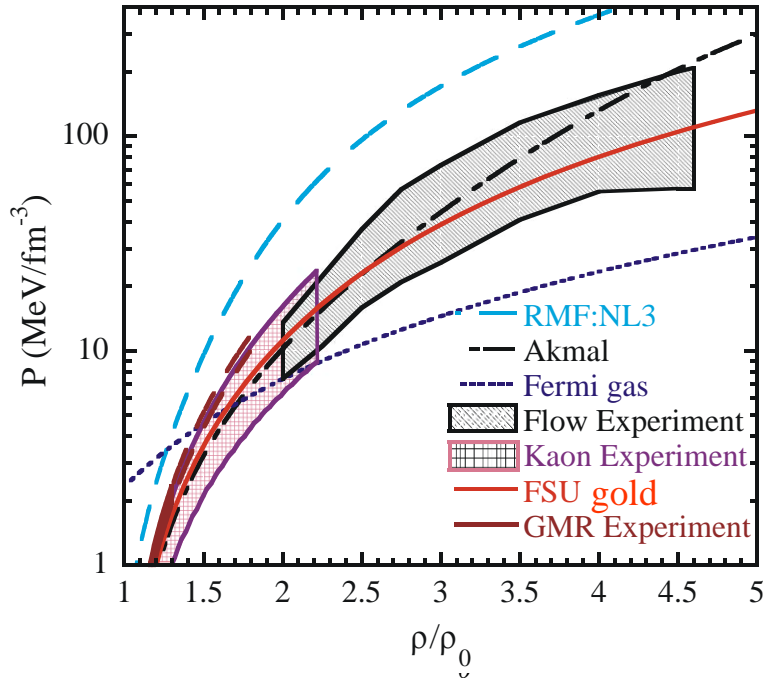


- Steiner et al., ApJ 722, 33 extract  $R=12.5 \pm 1.5$  km, larger than Ozel ( $R=10 \pm 2$  km) arXiv:1210.0916v1.
- Sensitive to modeling of radiation transport – see Suleimanov et al, ApJ 742, 122 who extract  $\sim 2$  km larger radii.
- Rutledge studied quiescent only x-ray binary systems and extracts  $\sim 3$  km smaller radii.
- $\Rightarrow$  It is important to obtain laboratory constraints. For high densities, one needs heavy-ion collisions.

# Laboratory Constraints on symmetric matter EOS at $\rho > 2 \rho_0$ .

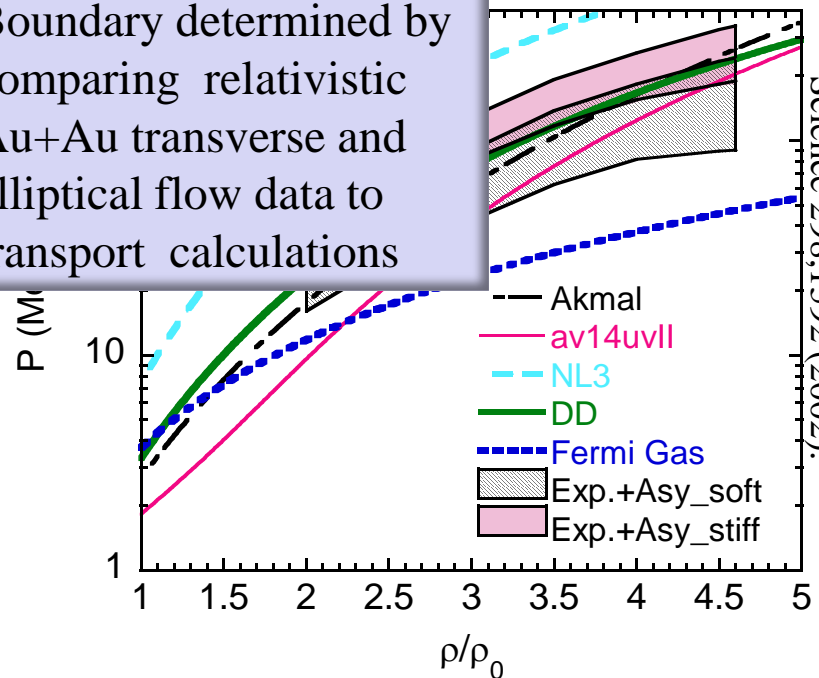
$$E/A(\rho, \delta) = E/A(\rho, 0) + \delta^2 \cdot S(\rho)$$

$$\delta = (\rho_n - \rho_p) / (\rho_n + \rho_p) = (N - Z) / A \approx 1$$



Lynch Prog. Part. Nucl.

Boundary determined by comparing relativistic Au+Au transverse and elliptical flow data to transport calculations



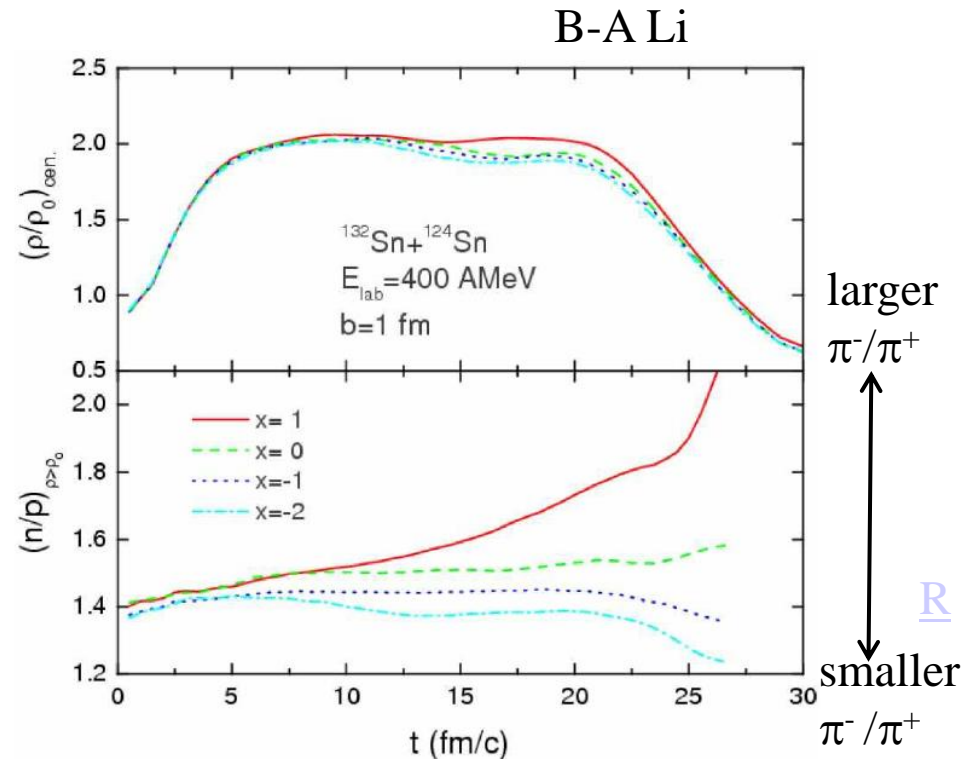
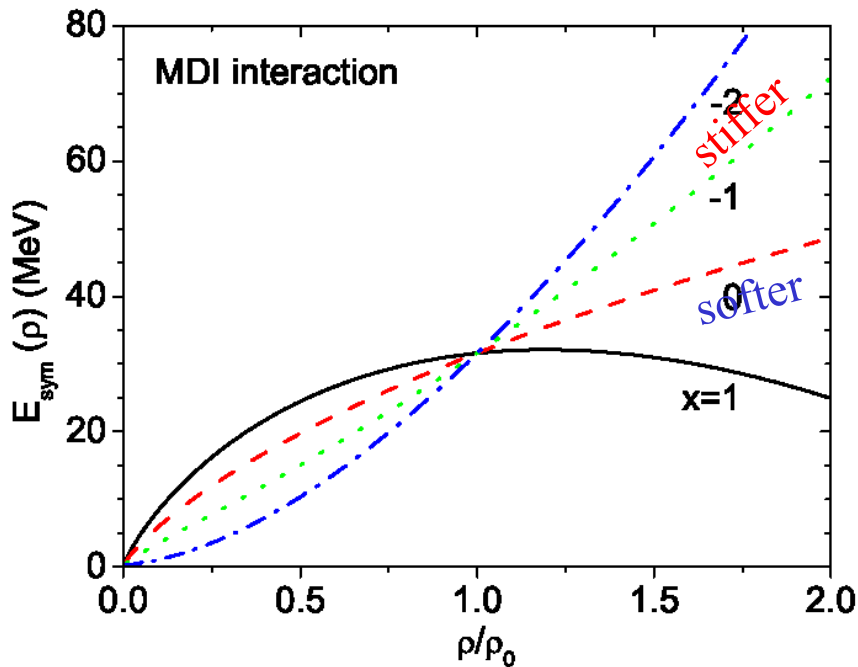
Danielewicz et al.,

- Flow confirms the softening of the EOS at high density.
- Constraints from kaon production are consistent with the flow constraints and bridge gap to GMR constraints.
- Note: analysis requires additional constraints on  $m^*$  and  $\sigma_{NN}$ .

- The symmetry energy dominates the uncertainty in the n-matter EOS.
- Improved laboratory constraints on the density dependence of the symmetry energy are needed to tighten the constraints.

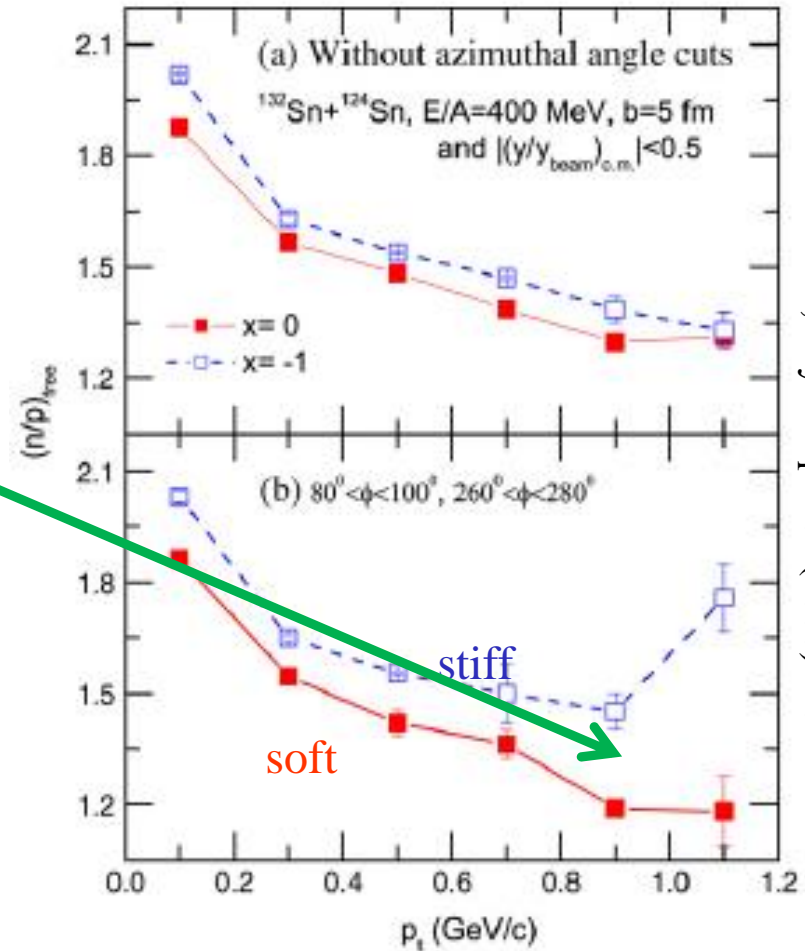
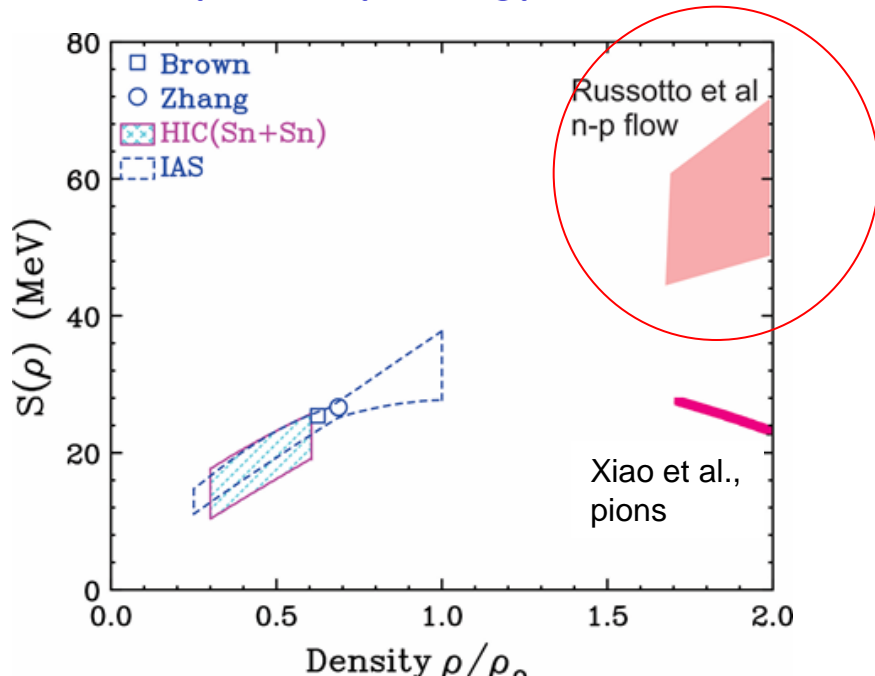
# Symmetry energy studies at $\rho \approx 2\rho_0$

- Densities of  $\rho \approx 2\rho_0$  can be achieved at  $E/A \approx 400$  MeV.
  - Provides information relevant to the mass-radius relation of neutron stars and possibly about direct URCA cooling in proto-neutron stars.
  - Stronger (stiffer) density dependence of symmetry energy expels more neutrons from densest region. Since  $\pi^-$  originates from n-n collisions and  $\pi^+$  originates from p-p collisions, this reduces the  $\pi^-/\pi^+$  spectral ratio



# Comparisons of neutron and proton observables :

- Most models predict the differences between neutron and proton flows and  $t$  and  $^3\text{He}$  flows to be sensitive to the symmetry energy and the  $n$  and  $p$  effective mass difference.
- At this energy, the ratio of neutron over proton spectra out of the reaction plane displays a significant sensitivity to the symmetry energy.



B.-A. Li et al., Phys. Rep. 464 (2008) 113.

- A new experiment was performed at GSI and new results may be expected:
  - Asyeos exp.

# Probing $\rho > \rho_0$ via pion production

- Larger values for  $\rho_n / \rho_p$  at high density for the soft asymmetry term ( $x=0$ ) causes stronger emission of negative pions for the soft asymmetry term ( $x=0$ ) than for the stiff one ( $x=-1$ ).

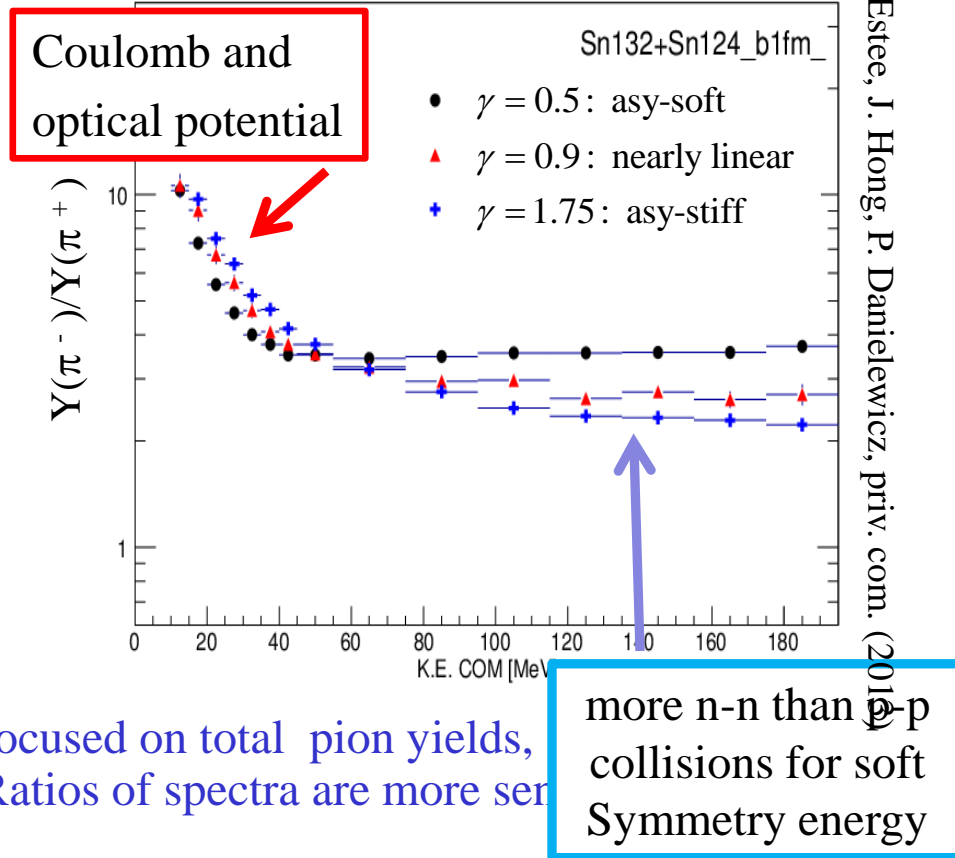
- Expectations for  $Y(\pi^-) / Y(\pi^+)$

- In delta resonance model,  
 $Y(\pi^-) / Y(\pi^+) \approx (\rho_n / \rho_p)^2$
- In equilibrium,  
 $\mu(\pi^+) - \mu(\pi^-) = 2(\mu_p - \mu_n)$

- Most calculations and measurements have focused on total pion yields, effect – difficult to measure and calculate. Ratios of spectra are more sensitive than integrated yields.

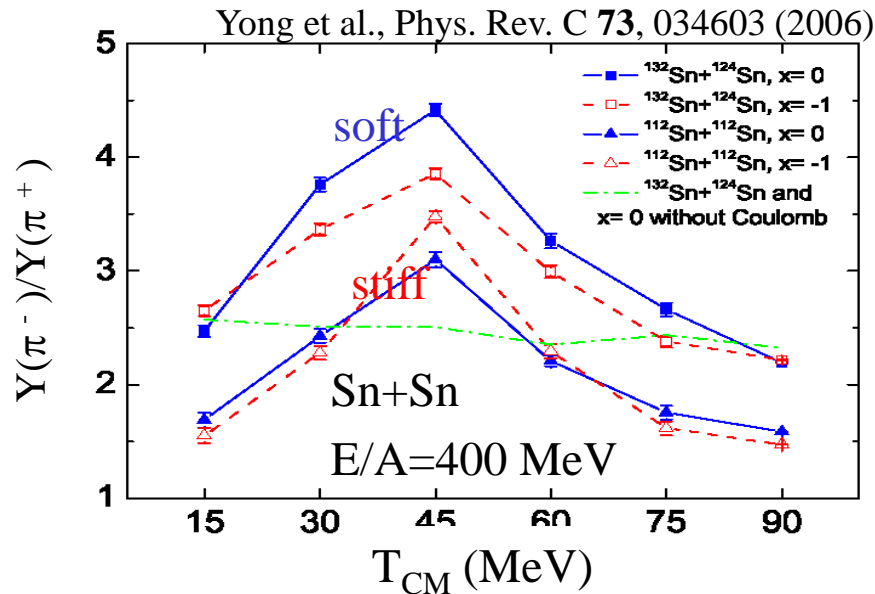
- Most clear sensitivity is for early pion emission at higher energies.
- The integrated yields are difficult to measure because they require measuring the full pion spectrum down to very low energies in the CM. system.
- Low energy pions strongly reflect pion charge exchange, and pion optical potentials.

$E/A = 300 \text{ MeV}$

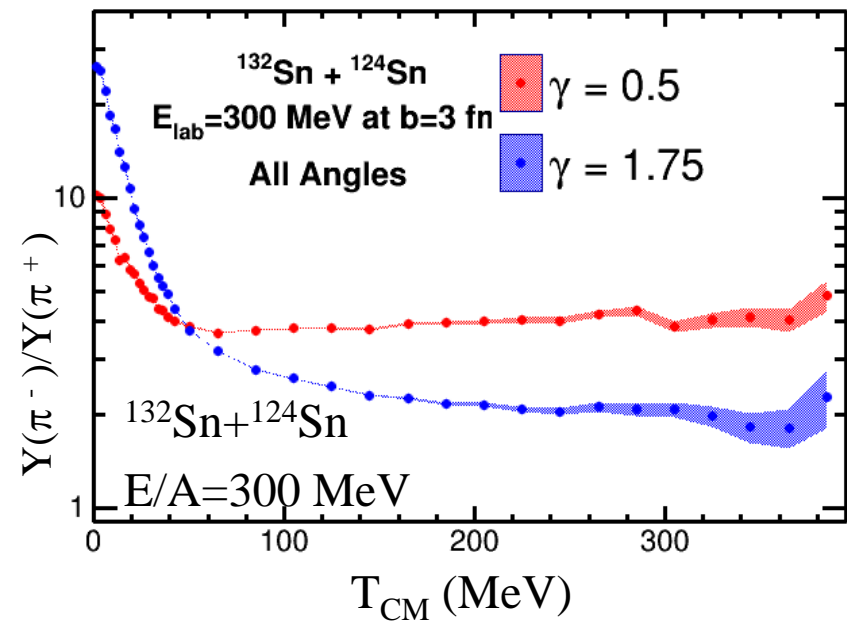
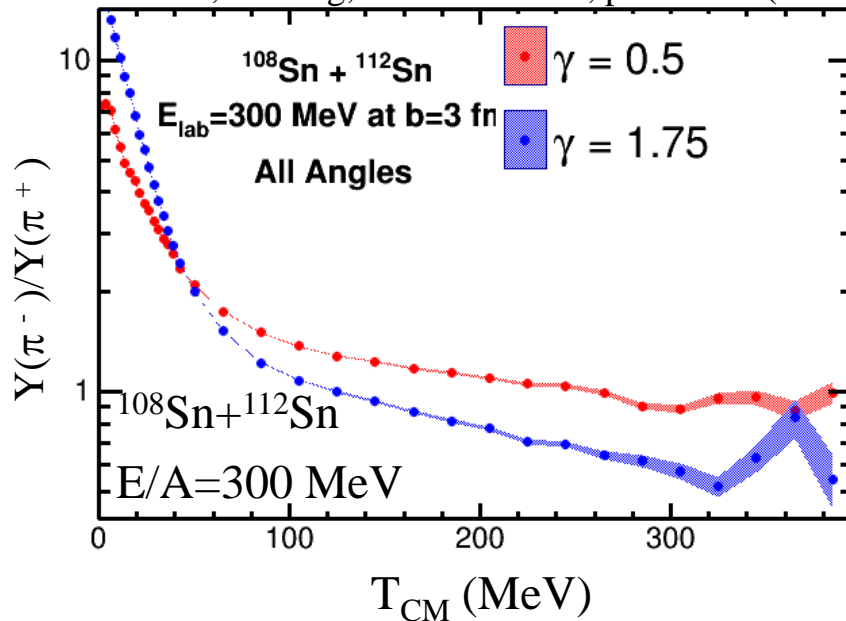


# Comparison to other calculated pion spectra

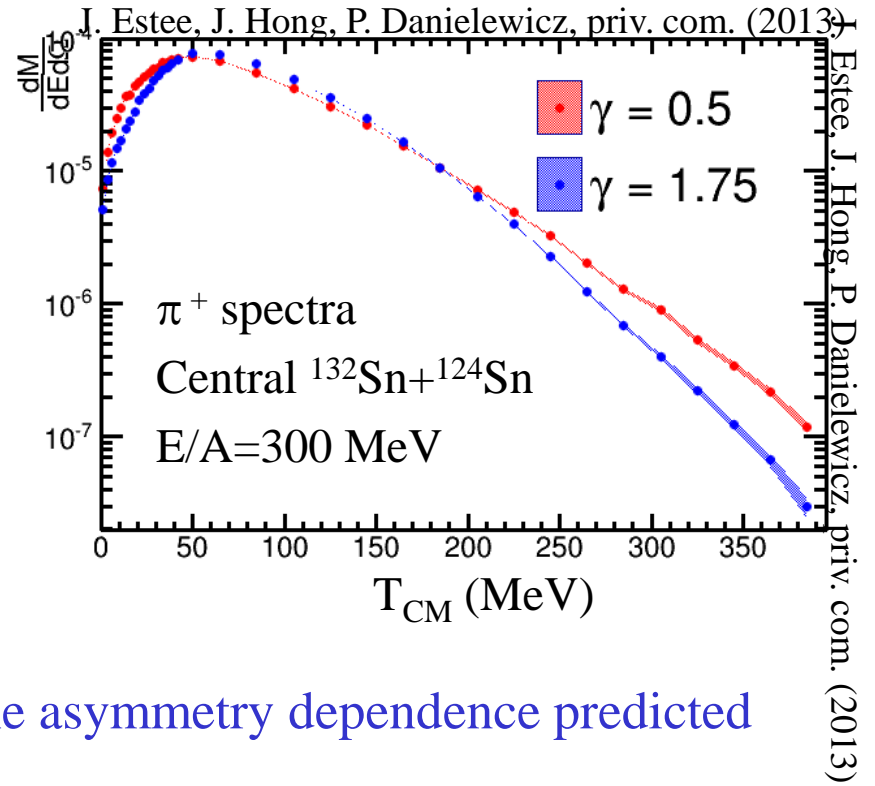
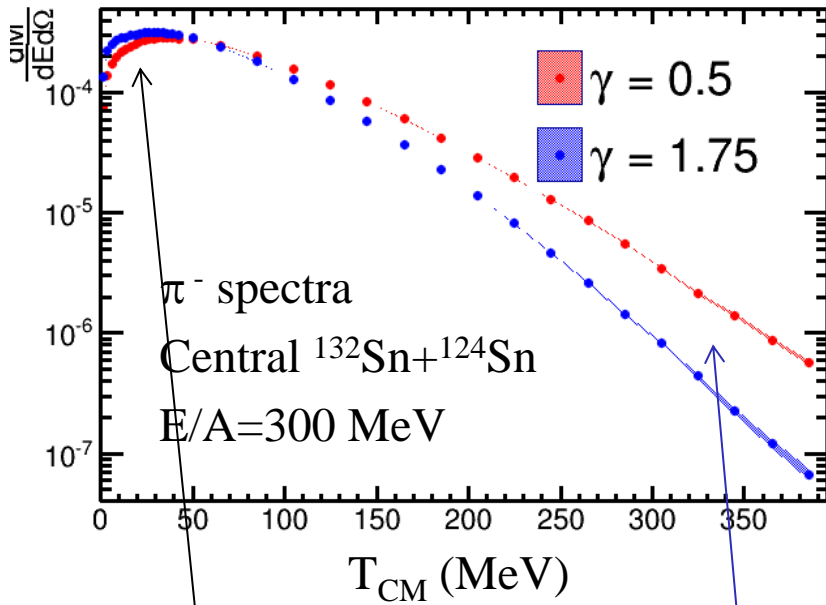
- Calculations of  $^{132}\text{Sn}+^{124}\text{Sn}$  and  $^{112}\text{S}+^{112}\text{Sn}$  spectral ratios were performed by Yong et al.,
- Behavior at low  $T_{\text{CM}}$  are very different. (no pion optical potential)
- Why does the latest calc. increase at low  $T_{\text{CM}}$ ?



J. Estee, J. Hong, P. Danielewicz, priv. com. (2013)



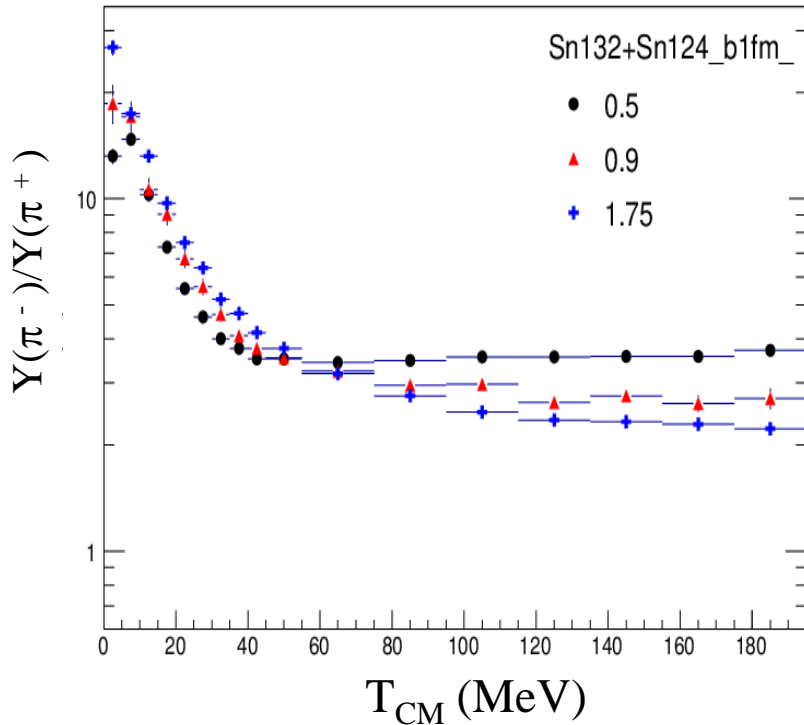
# How spectra influence these ratios



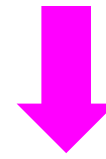
- Higher energy emissions reflect the asymmetry dependence predicted by the delta resonance model.
  - $Y(\pi^-)/Y(\pi^+) \approx (\rho_n/\rho_p)^2$
- Low energy emission reflect the combined influence of the Coulomb and optical potentials.

# Difference between $^{132}\text{Sn}+^{124}\text{Sn}$ and $^{108}\text{Sn}+^{112}\text{Sn}$ collisions

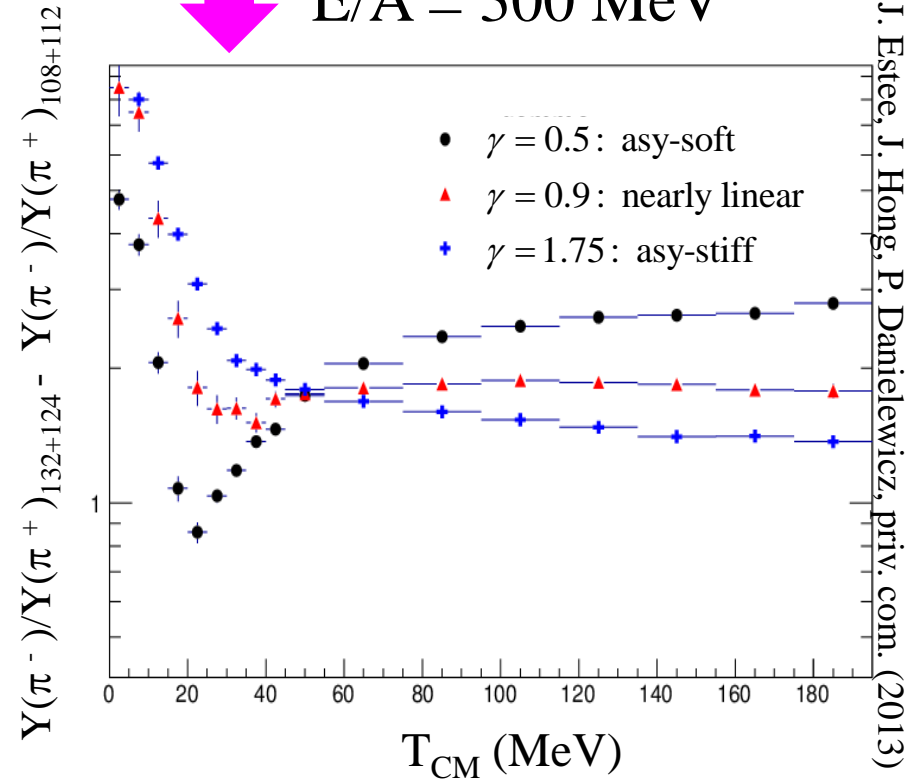
$E/A = 300 \text{ MeV}$



J. Estee, J. Hong, P. Danielewicz, priv. com. (2013)



$E/A = 300 \text{ MeV}$



J. Estee, J. Hong, P. Danielewicz, priv. com. (2013)

- Comparing two systems with different asymmetries enhances the sensitivity to the symmetry energy.
- Experiment has been approved for 13.5 days of running at the RIBF facility at RIKEN.



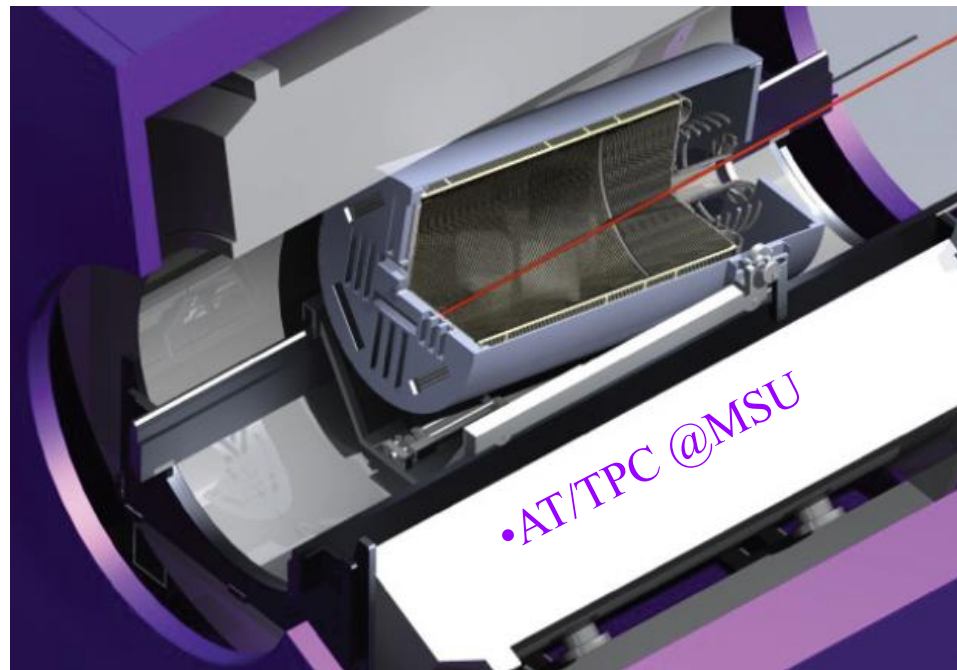
# Devices: SAMURAI TPC and AT-TPC

S $\pi$ RIT TPC



- U.S./Japan collaboration
  - Uses SAMURAI dipole
  - Recently completed (2013)
  - Measure  $\pi^+$ ,  $\pi^-$ ,  $t$ ,  $^3\text{He}$ ,  $n$ ,  $p$  next year, hopefully.

Active Target -TPC



- U.S. Collaboration (NSF MRI)
  - Solenoidal (MRI) magnet
  - Recently completed (2013)
  - Will enable future measurements of  $\pi^+$ ,  $\pi^-$ ,  $t$ ,  $^3\text{He}$ ,  $n$ ,  $p$



MSU, Texas A&M, WMU,  
Kyoto U., Riken, Seoul U.,  
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# Another issue: momentum dependence of mean fields

- Momentum dependence of the mean field (real part of optical potential) is well established for symmetric matter.

- At low energies, it can be described by effective mass,  $m^*$ :

$$p^2 \left( \frac{1}{2m^*} - \frac{1}{2m} \right) = p^2 \frac{\partial U}{\partial p^2} \Big|_{p^2=0}$$

- Momentum dependence increases with  $\rho$ , is maximal at  $p=p_F$  and vanishes as  $p \rightarrow \infty$ .

- Symmetry potential mom. dependence?
- This uncertainty influences  $m_n^*$ , and  $m_p^*$  and has an significant influence on the excitation energy – temperature relationship for neutron stars.  $T^2 \propto E^* / A \left( m_n / m_n^* \right)$
- It also influences the neutrino flux from neutron stars: (Baldo et al PRC 89, 048801 (2014)).

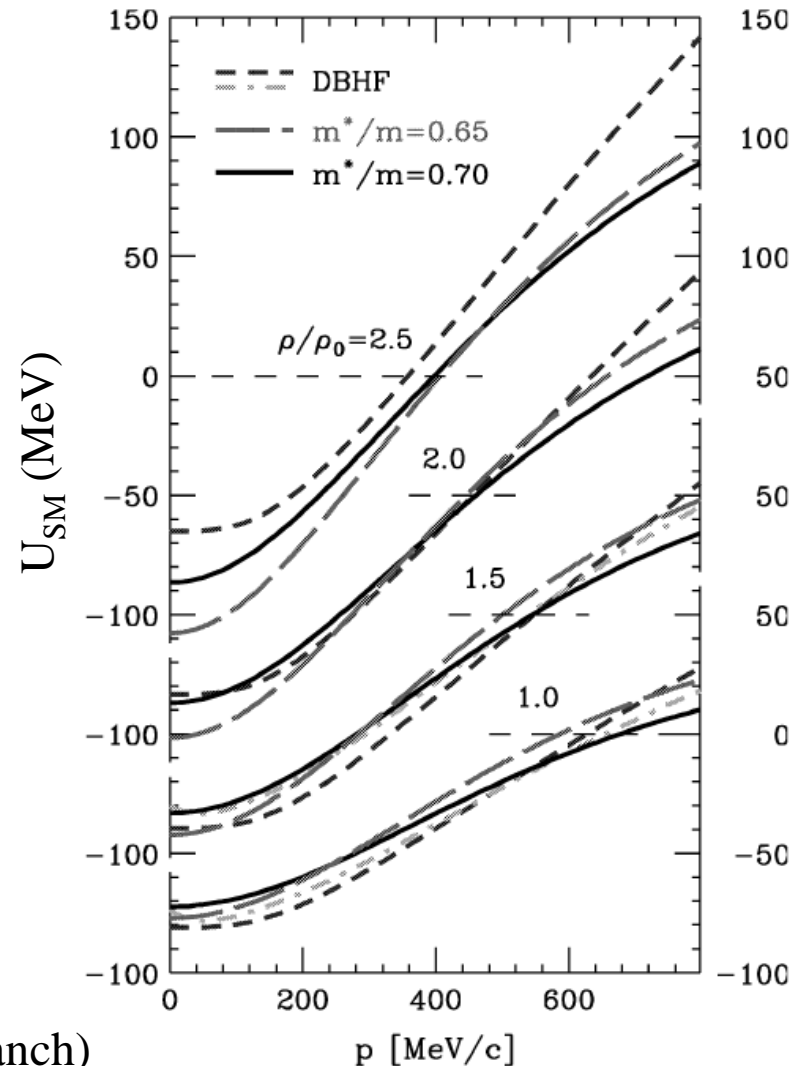
$$Q^{(DU)} \propto \frac{m_n^*}{m_n} \frac{m_p^*}{m_p} T^6$$

direct Urca

$$Q^{(Mn)} \propto \left( \frac{m_n^*}{m_n} \right)^3 \frac{m_p^*}{m_p} T^8$$

modified Urca (neutron branch)

*P. Danielewicz / Nuclear Physics A 673 (2000) 375–410*



# Emission of neutrons and protons from a neutron-rich system

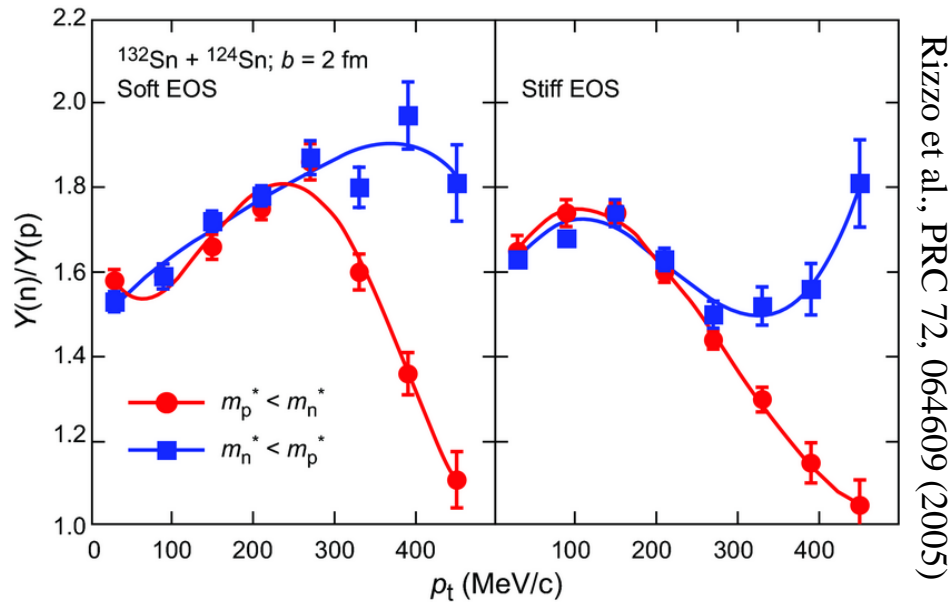
- For an expanding and statistically emitting source, it is easy to show that that the n/p ratio depends on  $\mu_n$  and  $\mu_p$ , at low T (in the effective mass approx. and neglecting  $V_{Coul}$ ).

$$\left. \frac{dN_n(t_n)}{dN_p(t_p)} \right|_{t_n=t_p=t} \propto \exp([\mu_n - \mu_p]/T) \approx \exp\left(\left[ \frac{p_{F,n}^2}{2m_{n,eff}} - \frac{p_{F,p}^2}{2m_{p,eff}} + c2\delta\rho^\gamma \right] / T \right)$$

Kinetic Esym +  
Mom. Dep.

- The effective mass effects dominate at early higher energies, corresponding to early emission times when density is higher.
- Trend is well supported by transport theory and by simple dynamical arguments.

Ratios of center of mass spectra at  $90^\circ$

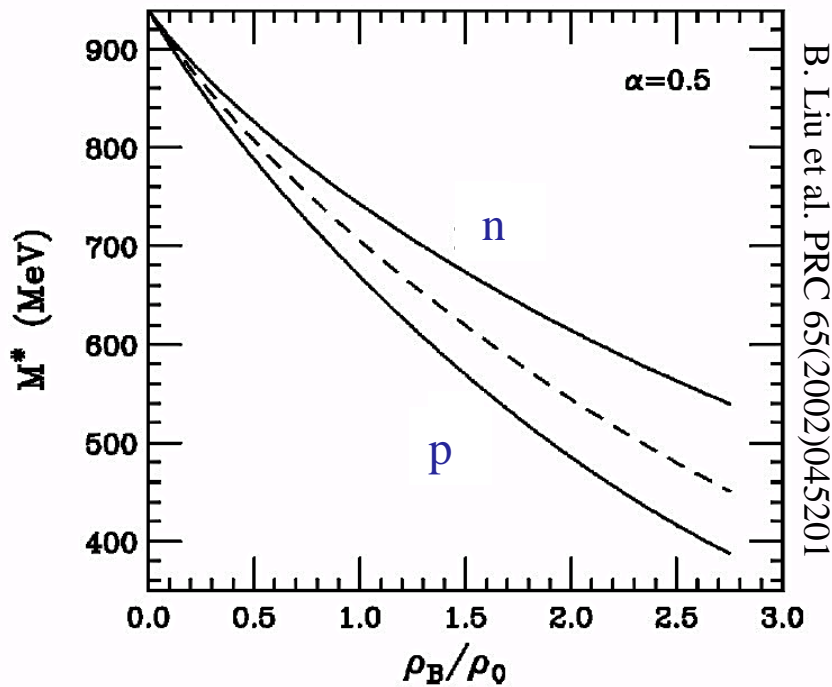


Symmetry potential contribution: neutron expelled and protons attracted by symmetry potential

# From dynamical point of view (e.g. in transport theory)

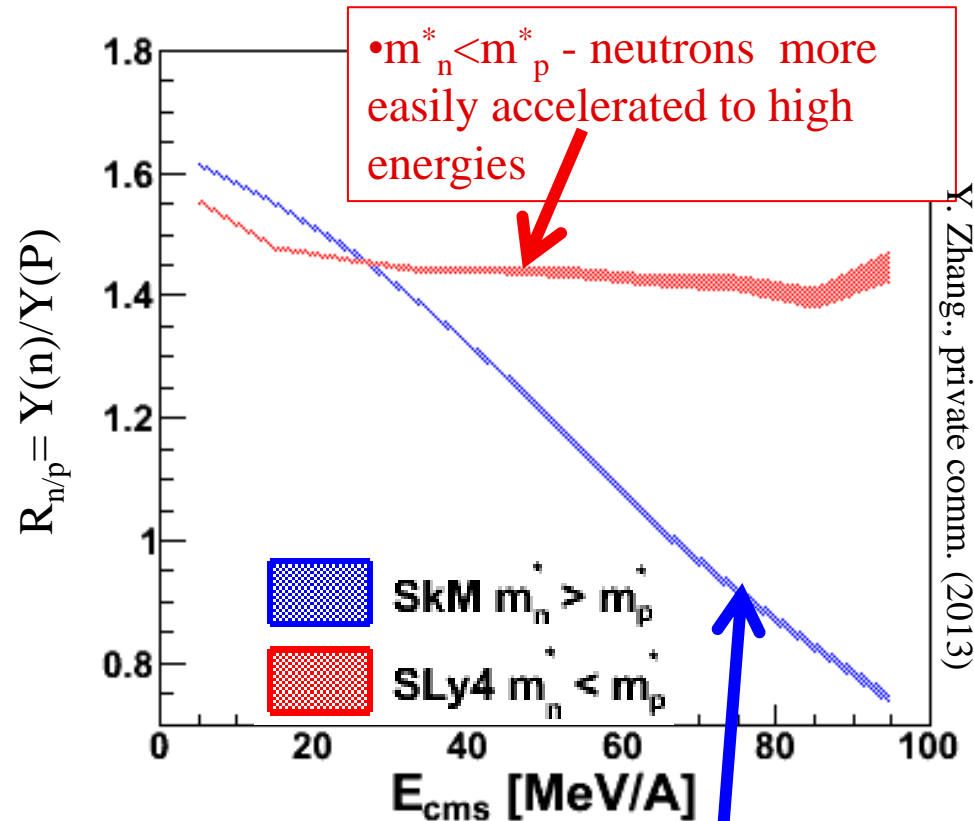
if  $U_{\text{sym}} = U_{\text{sym}}(\rho, p^2)$

$$\text{accel.} = \frac{dv}{dt} = \frac{\nabla U}{m^*}$$



## Central $^{124}\text{Sn}+^{124}\text{Sn}$ Collision

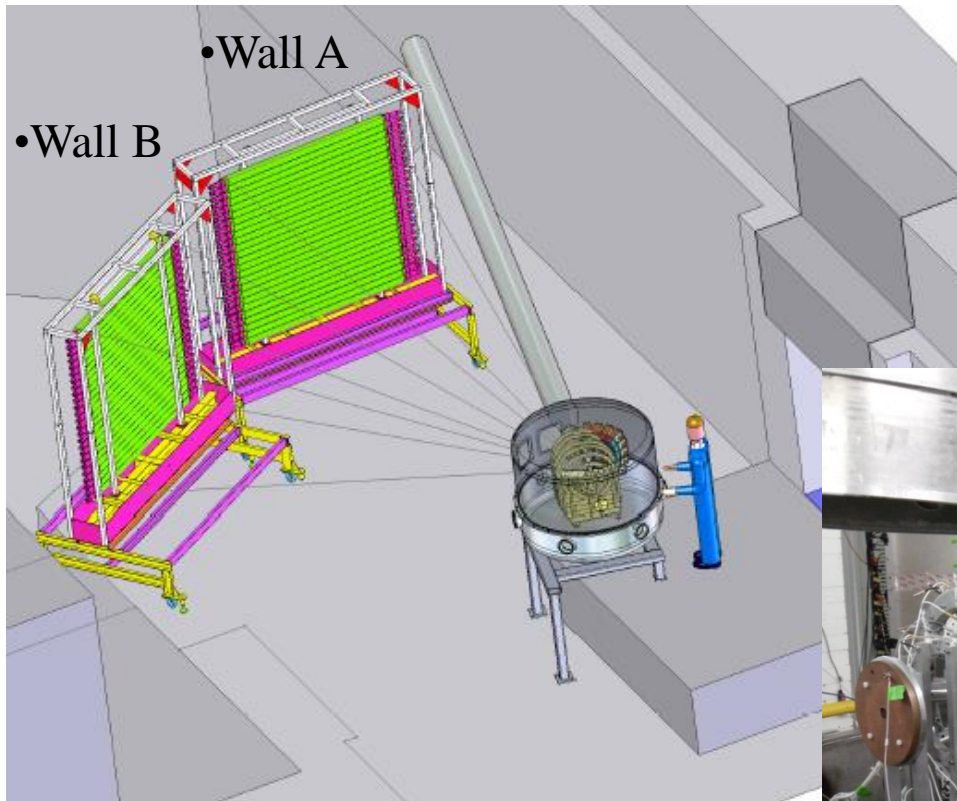
$E/A = 120 \text{ MeV/A}$



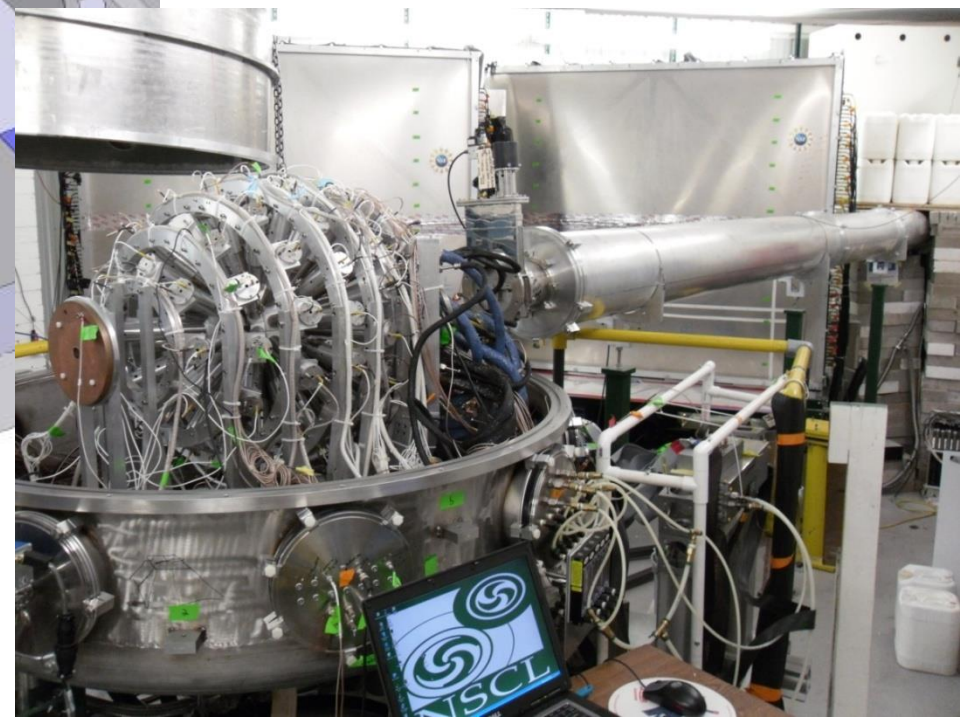
$m_p^* < m_n^*$  - protons more easily accelerated to high energies

# Experimental Layout

PhD theses: Daniel Coupland & Michael Youngs



- LASSA – charged particles
- Miniball – impact parameter

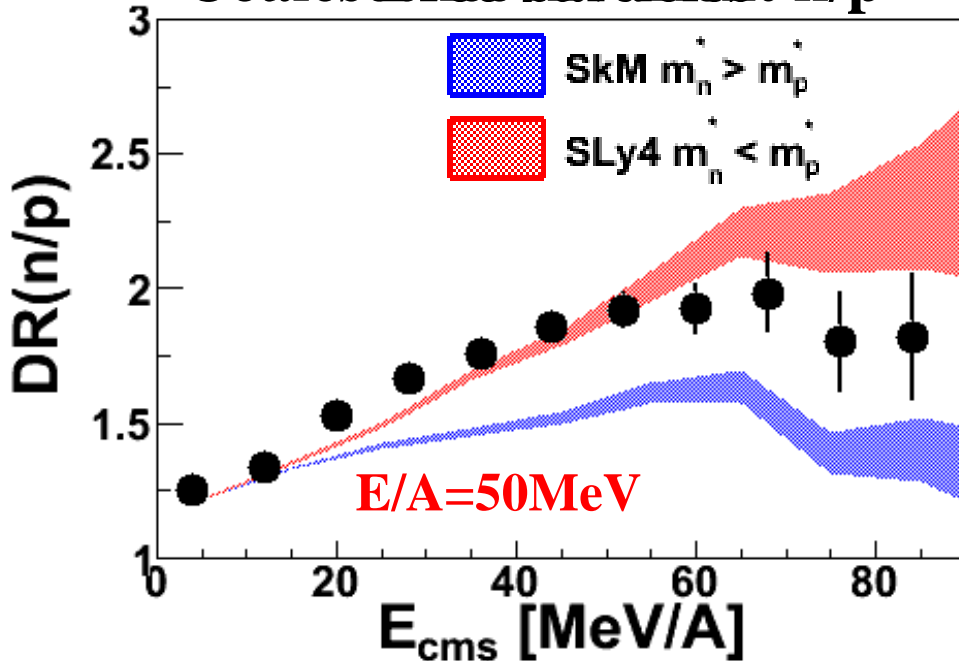


•Courtesy Mike Famiano

- Neutron walls – neutrons
- Forward Array – time start
- Proton Veto scintillators

# Comparisons with transport theory: n,p

## Coalescence invariant n/p



$$DR_{n/p} = \frac{R_{n/p} \left( {}^{124}\text{Sn} + {}^{124}\text{Sn} \right)}{R_{n/p} \left( {}^{112}\text{Sn} + {}^{112}\text{Sn} \right)}$$

ImQMD05\_sky: incorporate Skyrme interactions  
 Y. Zhang (2013) Private Communication  
 Tsang (2013) Private Communication  
 D. Coupland, M. Youngs (2013)

## ImQMD:

- Cluster production does not have the correct binding energies for light fragments  $\Rightarrow$  too few fragments.
- Test semi-classical dynamics by constructing “coalescence invariant” nucleon spectra, which represent flows prior to clusterization.

## Coalescence invariance:

- Coalescence protons or neutrons spectra include both free neutrons and protons and those within clusters. This is done for both experiment data and theoretical calculations.

The data suggest only a weak momentum dependence of the symmetry mean field potential

# Summary and Outlook

- Experiment is beginning to provide constraints on the EoS.
  - Isospin diffusion, n/p spectral ratios, mass, IAS's, GMR, Pigmy and Giant Dipole resonances, E1 polarizabilities and neutron skin thicknesses already provide some constraints at  $\rho \leq \rho_0$ . These constraints should become more stringent.
  - These constraints  $\rho < \rho_0$  may be helpful to understand phenomena occurring in the inner crust of neutrons stars.
  - New results for  $\pi^-$ ,  $\pi^+$ , n, p, t, and  $^3\text{He}$  spectra and flows will provide sensitivity to the symmetry energy at supra-saturation densities of  $\rho \approx 2\rho_0$ .
- Neutron star observations provide complimentary information.
  - Comparisons of laboratory and astronomical constraints on EoS at  $\rho \approx 2\rho_0$  should prove to be very interesting.
- The importance of strange and quark matter in the inner core is an open question.
  - How can laboratory experiments contribute?