Pion Production in Heavy-Ion Collisions

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Natl Superconducting Cyclotron Lab, USA

International Workshop on Nuclear Symmetry Energy and Reaction Mechanisms

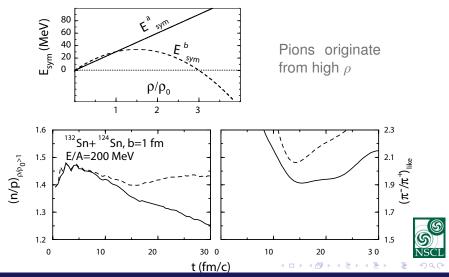
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Interest: π as Probe of High- ρ Symmetry Energy B-A Li PRL88(02)192701: $S(\rho > \rho_0) \Rightarrow n/p_{\rho > \rho_0} \Rightarrow \pi^-/\pi^+$



 π Production

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Simulations of Heavy-Ion Collisions

Separation of time and distance scales:

- Short scales reduced to negligible extent with outcomes of events treated probabilistically
- Long scales treated explicitly and deterministically
- Cut-off scales: $t \sim 1 \text{ fm}/c$, $r \lesssim 1 \text{ fm}$

Primarily binary collision processes

Equation of state: if there is an optical potential affecting a particle, that particle impacts the interaction parts of thermodynamic functions.

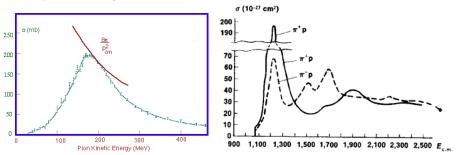
Low-*E* pion production: $N + N \leftrightarrow N + \Delta$, $\Delta \longleftrightarrow N + \pi$



(1)

Δ in π –*N* Interactions

π –*p* scattering cross sections



$$\sigma = \frac{4\pi}{p^2} \frac{2J+1}{2s+1} \frac{\Gamma^2/4}{(E-m_\Delta c^2)^2 + \Gamma^2/4}$$

 $J=3/2,\,m_{\Delta}=1232\,\text{MeV}/c^2,\,\Gamma(p)\propto p^3$

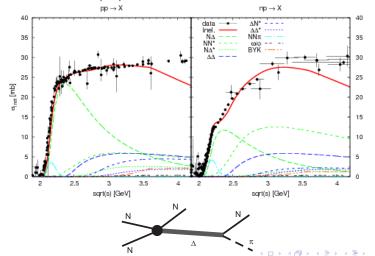


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Inelastic NN Interactions

Decomposition of inelastic *NN* cross section Weil *et al* EPJA48(12)111





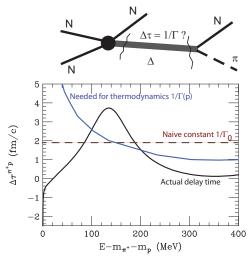
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Charged-*π* Yields, Theory & Expt

Conclusions

Δ in Transport

Ambiguity in deciding on time of π production



PD&Pratt PRC53(96)249

Different perspectives yield different Δ lifetimes

 $\Delta \tau$ consistent with fireball model most often used, but yields unphysically long-lived Δ close to threshold.

 \Rightarrow Need to transition to direct 3-ptcle production?



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$$\Delta \longleftrightarrow N + \pi$$
 $U_{\Delta} \stackrel{?}{=} U_N + U_{\pi}$

'Conservation' of potential consistent with the quark perspective. Also also greatly facilitates calculations of process kinematics as thresholds in kinetic energy stay put.

Ferini *et al* NPA762(05)147: $U_{\pi} = 0 \& U_{\Delta} = U_N$ employed in most models, including IBUU.

However, a strong isospin-dependent potential is needed to explain the existence of pionic atoms!

pBUU: *U* dependent on conserved quantities, density of baryon number and isospin - π end up with potentials that depend on isospin & symmetry energy



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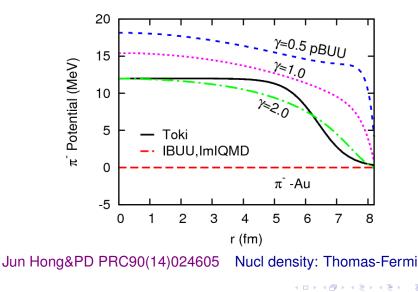
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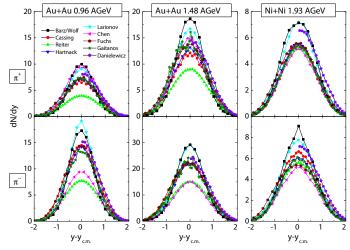
Symmetry-Energy Derived π Potential





 π Production

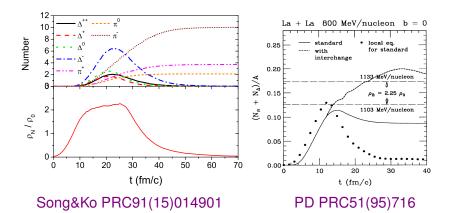
Technical Differences between Calculations



Kolomeitsev et al JPG31(05)S741



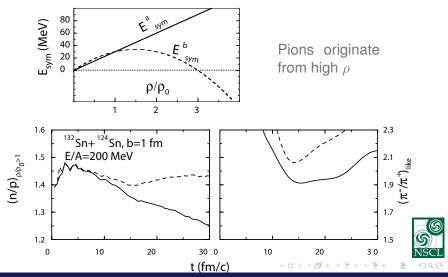
Pions Probe System at High- ρ !



 π test the maximal densities reached and collective motion then



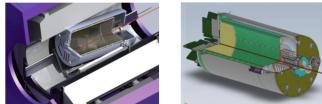
Pions as Probe of High- ρ Symmetry Energy B-A Li PRL88(02)192701: $S(\rho > \rho_0) \Rightarrow n/\rho_{\rho > \rho_0} \Rightarrow \pi^-/\pi^+$



Dedicated Experimental Efforts

SAMURAI-TPC Collaboration (8 countries and 43 researchers): comparisons of near-threshold π^- and π^+ and also *n-p* spectra and flows at RIKEN, Japan. NSCL/MSU, Texas A&M U Western Michigan U, U of Notre Dame GSI, Daresbury Lab, INFN/LNS U of Budapest, SUBATECH, GANIL China IAE, Brazil, RIKEN, Rikkyo U Tohoku U, Kyoto U

AT-TPC Collaboration (US & France)

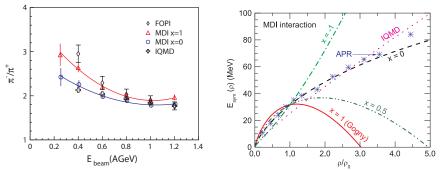




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Interpretation of FOPI Data

Reisdorf et al NPA781(07)459

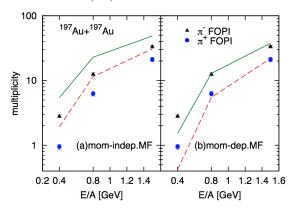


Transport IBUU04 Xiao et al PRL102(09)062502

Symmetry energy dropping with ρ , at $\rho > \rho_0$!?



Net π Yields and $U(\rho, \rho)$ in pBUU Reisdorf *et al* NPA781(07)459

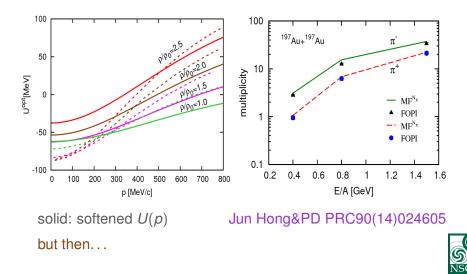


Jun Hong & PD PRC90(14)024605, π^- and π^+

?Imperfect Mom Dependence?? [No sensitivity to π/Δ rates] affects maximal densities reached

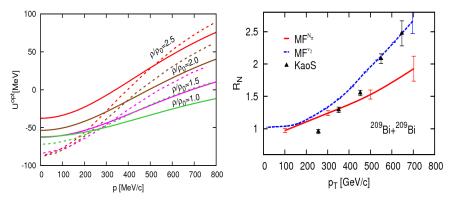


π Yields Reproduced with Softened U(p)



 π Production

Inferior Description of Midrapidity Flow Anisotropy



solid: new U(p), dashed: old U(p)

 $R_N \leftrightarrow \text{elliptic flow}$

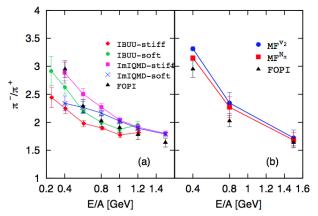
Jun Hong & PD PRC90(14)024605

too weak with new U(p



FOPI π^-/π^+ Reproduced by pBUU

... irrespectively of U(p), right panel

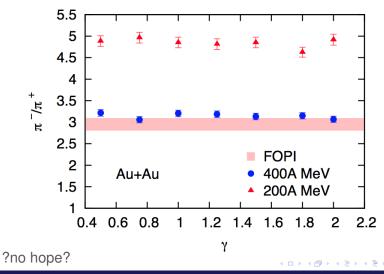


Left panel: discrepancies in the literature - correlation vs anticorrelation of $S(\rho > \rho_0)$ with π^-/π^+ .



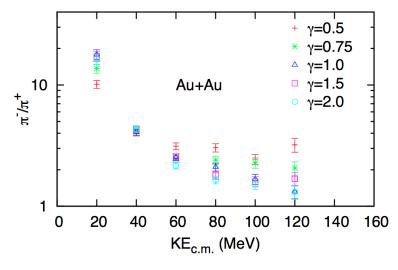
π Production

FOPI π^-/π^+ Reproduced by pBUU ... irrespectively of $S_{int}(\rho) = S_0 (\rho/\rho_0)^{\gamma}$:





Original Idea Still Correct for High- $E \pi$'s



$$S_{\rm int}(
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ight)^{\gamma}$$

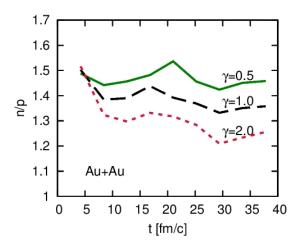


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n/p Ratio in pBUU at $\rho > \rho_0$

changes with the supranormal symmetry energy:



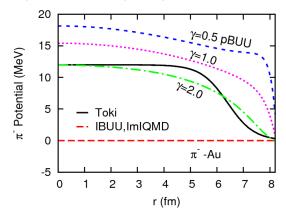
$$S_{\rm int}(\rho) = S_0 \left(\rho / \rho_0 \right)^{\gamma}$$



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Why Differences for Net π Ratios?

In pBUU isospin-driven π^{\pm} optical potential



 π/Δ rate sensitivities claimed in Larionov&Mosel NPA728(03)135; Prassa *et al* NPA789(07)311 and Song&Ko PRC91(15)014901. Virtually none there in pBUU



- Pions probe high-ρ matter, net density, n/p-ratio, collective flow there! ... U(p)
- Uncertainties in the near-threshold π production: Δ lifetime, $\pi \& \Delta$ optical potentials, in-medium rates.
- pBUU reproduces FOPI π^-/π^+ , irrespectively of details in *U* and *S*.
- High-energy π^+/π^- ratio more robust than ratio of net yields. Sensitivity to the dependence of effective masses on isospin?
- Azimuthal dependence of π^+/π^- ratio?

Acknowledgement: US Natl Science Foundation



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