

Iso-Vector Giant Dipole Resonance Mode within the Constrained Molecular Dynamics Approach

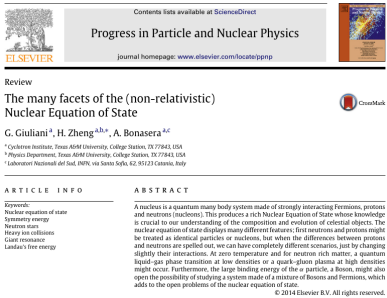
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 - Neutron Skin Thickness (NST)(preliminary)
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- Iso-Vector Giant Dipole Resonance (IVGDR) and Neutron Skin Thickness (NST) calculations within Mean Field (Boltzmann-Nordheim-Vlasov Equation) and Constrained Molecular Dynamics (CoMD) approaches
- Slope and Curvature of the Nuclear Symmetry Energy
- Test Our NEOS



NEOS for Asymmetric Nuclear Matter:

$$\frac{E}{A}(\rho, \alpha) = \left(1 + \frac{5}{9}\alpha^2\right)\tilde{\epsilon}_f\tilde{\rho}^{2/3} + (1 + c_1\alpha^2)\frac{A_1}{2}\tilde{\rho} + (1 + c_2\alpha^2)\frac{B_1}{1 + \sigma}\tilde{\rho}^\sigma$$

$\tilde{\epsilon}_f = \frac{3}{5}T_f$, $\alpha = \frac{\rho_n - \rho_p}{\rho}$ neutron-proton concentration. $A_1, B_1, \sigma \leftarrow$
Equilibrium Conditions for Symmetric Nuclear Matter:

$$\left.\frac{E}{A}\right|_{\rho=\rho_0} = -15\text{MeV}$$

$$\left.P\right|_{\rho=\rho_0} = \rho^2 \left.\frac{\partial(\frac{E}{A})}{\partial\rho}\right|_{\rho=\rho_0} = 0$$

$$\left.K\right|_{\rho=\rho_0} = 9 \left.\frac{\partial P}{\partial\rho}\right|_{\rho=\rho_0}$$

The Symmetry Term:

$$\frac{E}{A}(\rho, \alpha) - \frac{E}{A}(\rho, 0) = \left(\frac{5}{9} \tilde{\epsilon}_f \tilde{\rho}^{2/3} + c_1 \frac{A_1}{2} \tilde{\rho} + c_2 \frac{B_1}{1+\sigma} \tilde{\rho}^\sigma \right) \alpha^2 = S(\rho) \alpha^2$$

Density Dependence, Slope (L) and Curvature K_{sym}

$$S(\rho) = \frac{5}{9} \tilde{\epsilon}_f \tilde{\rho}^{2/3} + c_1 \frac{A_1}{2} \tilde{\rho} + c_2 \frac{B_1}{1+\sigma} \tilde{\rho}^\sigma$$

$$L(\rho) = 3\rho_0 \frac{\partial S(\rho)}{\partial \rho} = 3 \left(\frac{10}{27} \tilde{\epsilon}_f \tilde{\rho}^{-1/3} + c_1 \frac{A_1}{2} + c_2 \frac{B_1 \sigma}{1+\sigma} \tilde{\rho}^{\sigma-1} \right)$$

$$K_{\text{sym}}(\rho) = 9\rho_0^2 \frac{\partial^2 S}{\partial \rho^2} = 9 \left(-\frac{10}{81} \tilde{\epsilon}_f \tilde{\rho}^{-4/3} + c_2 \frac{B_1 \sigma (\sigma - 1)}{1+\sigma} \tilde{\rho}^{\sigma-2} \right)$$

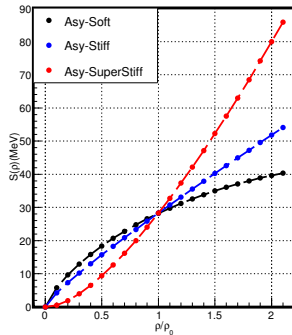
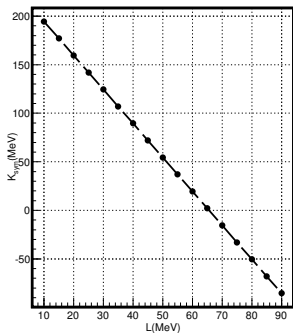
$$S(\rho_0) = S = \frac{5}{27} \tilde{\epsilon}_f - \frac{10}{81} \frac{\tilde{\epsilon}_f}{\sigma} + \frac{L(\rho_0)}{3} - \frac{K_{\text{sym}}(\rho_0)}{9\sigma}$$

 c_1 and c_2 by fixing $S(\rho)$ and $L(\rho)$ values at ρ_0 .*Second order phase transition in a Neutron Star (PPNP paper)*

$$K = 200 \text{ MeV} \implies A_1 = -356 \text{ MeV}, B_1 = 303 \text{ MeV}, \sigma = \frac{7}{6}$$

$$S(\rho_0) = S = 28.3 \text{ MeV}, L = 50 \pm 40 \text{ MeV} \implies K_{\text{sym}} =$$

$$-85.5 \div 194.5 \text{ MeV}$$



$L=14.4 \text{ MeV}$ $c_1 = 0.564, c_2 = 0.832$ - Asy-Soft

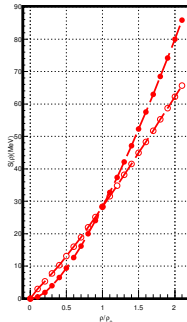
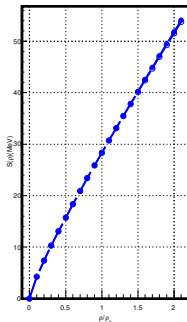
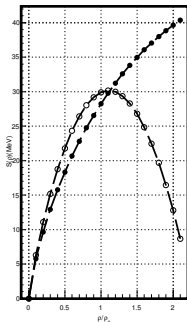
$L=72 \text{ MeV}$ $c_1 = 0.08315, c_2 = 8.581 \cdot 10^{-3}$ - Asy-Stiff

$L=96.6 \text{ MeV}$ $c_1 = -0.359, c_2 = -0.343$ - Asy-SuperStiff

Comparing Symmetry Terms - Form Factors

(B.-A. Li, L-W Chen, C. M. Ko Phys. Rep. 464 (2008) 113-281, V. Baran, M. Colonna, V. Greco, M. Di Toro Phys. Rep. 410 (2005) 335-466, M. Papa and G. Giuliani, Eur. Phys. J. A 39, 117-124 (2009))

- Asy-Soft: $S(\rho) = \frac{5}{9}\tilde{\epsilon}_f\tilde{\rho}^{2/3} + (482 - 1638\rho)\frac{\rho}{2}$ (V. Baran et al Phys. Rev. C 88 044610 (2013))
- Asy-Stiff: $S(\rho) = \frac{5}{9}\tilde{\epsilon}_f\tilde{\rho}^{2/3} + \frac{C}{2}\tilde{\rho}$, $C = 32\text{MeV}$
- Asy-SuperStiff: $S(\rho) = \frac{5}{9}\tilde{\epsilon}_f\tilde{\rho}^{2/3} + \frac{C}{2}\frac{2\tilde{\rho}^2}{1+\tilde{\rho}}$, $C = 32\text{MeV}$



- Same $S_0 = 28.3 \text{ MeV}$ and $L=14.4, 72, 96.6 \text{ MeV}$ values
- Different behaviors as a function of the density (except for the Asy-Stiff case)
- S , L and K_{sym} are differently related - Asy-SuperStiff:

$$S = \frac{5}{27} \tilde{\epsilon}_f - \frac{10}{81} \frac{\tilde{\epsilon}_f}{\sigma} + \frac{L}{3} - \frac{K_{sym}}{9\sigma}$$

$$S = \frac{1}{9}(L + K_{sym})$$

- Different K_{sym} values

| $L(\text{MeV})$ | $K_{sym}^{(1)}(\text{MeV})$ | $K_{sym}^{(2)}(\text{MeV})$ |
|-----------------|-----------------------------|-----------------------------|
| 14.4 | 179.1 | -402 |
| 72 | -22.5 | -24 |
| 96.6 | -109 | 47 |

Hamiltonian in the CoMD Framework

M. Papa Phys. Rev. C 87 014001 (2013) - (Symmetry Potential in the CoMD Model in Nuclear Matter and Nuclei)

$$H = T + V_{2B} + V_{3B} + V_{Sym} + V_{Surf} + V_{Coul}$$

$$V_{2B} = \frac{A_1}{2\rho_0} \bar{S}_V$$

$$V_{3B} = \frac{B_1}{(\sigma + 1)(\rho_0)^\sigma} (\bar{S}_V)^\sigma$$

$$V_{sym} = \frac{T_4}{2\rho_0} F'_k(\bar{S}_V) \tilde{\rho}_A \left[\left(1 + \frac{\alpha_c}{2}\right) \alpha^2 - \frac{\alpha_c}{2} \right]$$

$$V_{sym} = \left[c_1 \frac{A_1}{2\rho_0} \bar{S}_V + c_2 \frac{B_1}{(\sigma + 1)(\rho_0)^\sigma} (\bar{S}_V)^\sigma \right] \left(\frac{\rho_n - \rho_p}{\rho_n + \rho_p} \right)^2$$

\bar{S}_V average overlap integral per nucleon

Constraining the NEOS:

$L, K_{sym} \leftrightarrow E_{GDR} = 31.2A^{-1/3} + 20.6A^{-1/6}$ (M. N. Harakeh A. Van Der Woude, Giant Resonances, first ed. Oxford Science Publications (2001))

- $t=0$ fm/c: protons and neutrons displaced in momentum space

$$\Delta P_z = \frac{E_{GDR}}{A\hbar},$$

$$P_z^n \rightarrow P_z^n - \left(\frac{Z}{A} \Delta P_z\right)$$

$$P_z^p \rightarrow P_z^p - \left(\frac{N}{A} \Delta P_z\right)$$

- Time evolution: dipole momentum in coordinate and momentum spaces

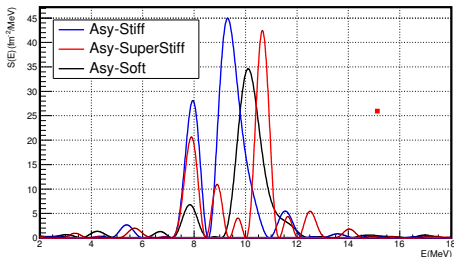
$$D\mathbf{R}(t) = \frac{NZ}{A} (\mathbf{R}_p - \mathbf{R}_n)$$

$$D\mathbf{K}(t) = \frac{NZ}{A} (\mathbf{K}_p - \mathbf{K}_n)$$

- IVGDR strength: $\frac{dP}{dE} \propto |D(E)|^2$

$$^{132}\text{Sn} \longrightarrow E_{GDR} = 15.26 \text{ MeV}$$

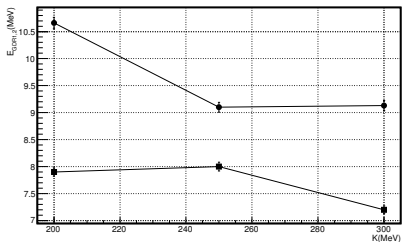
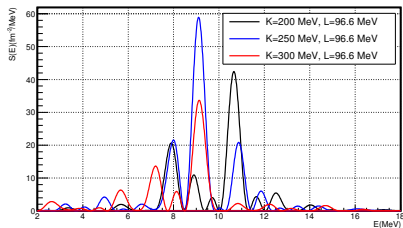
(1): $A_1 = -356 \text{ MeV}$, $B_1 = 303 \text{ MeV}$, $\sigma = \frac{7}{6}$, $K = 200 \text{ MeV}$, $L = 14.4, 72, 96.6 \text{ MeV}$



- No Filtering of the Dipolar Signal (P.-G. Reinhard Phys. Rev. E 73 036709 (2006))
- Peaks Around 8 MeV, Pygmy Dipole Resonance Systematics (PDR) $E_{PDR} = 41A^{-1/3} = 8.05 \text{ MeV}$ (V. Baran et al PRC 88 044610 (2013))

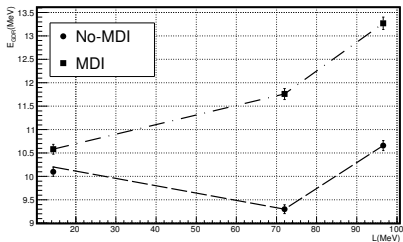
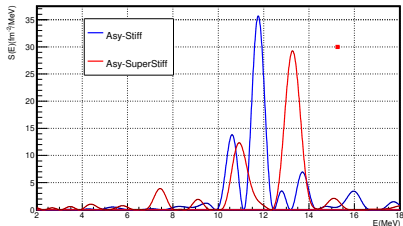
| L(MeV) | $E_{GDR}(\text{MeV})$ |
|--------|-----------------------|
| 14.4 | 10.1 |
| 72 | 9.3 |
| 96.6 | 10.66 |

(2): $L=96.6$ MeV (Asy-SuperStiff), $K=200, 250, 300$ MeV



Iso-Scalar and Iso-Vector parts of the NEOS cannot be completely disentangled

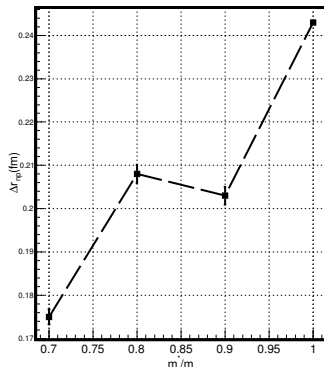
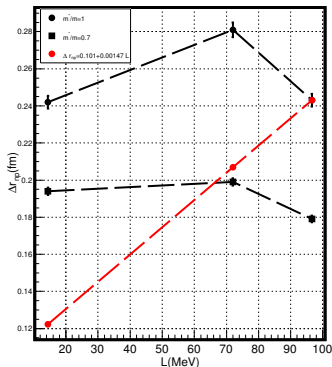
Momentum Dependent Potential $U(\mathbf{p}_{i,j}) = \alpha p_{i,j}^2$
 (3): $K=200$ MeV, $m^*/m = 0.7$ - $L = 14.4, 72, 96.6$ MeV (A_1, B_1, σ)



- Oscillation Energy Distributions Sensitive to the Effective Mass
- Improvement of the Sensitivity to the L parameter
- Increasing as L Increases

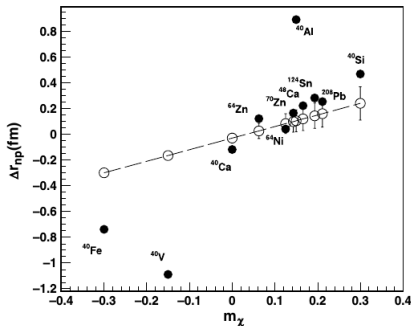
- $\Delta r_{np} = \langle R_n^2 \rangle^{\frac{1}{2}} - \langle R_p^2 \rangle^{\frac{1}{2}}$
- Dependence and connection with collective modes (IVPDR):
 Non-Relativistic and Relativistic mean field calculations

[B. Alex Brown Phys. Rev. Lett. 85 (2000), R. J. Furnstahl Nucl. Phys. A 706 (2002); C. J. Horowitz, J. Piekarewicz Phys. Rev. Lett. 86 (2001), X. Roca-Maza et al, Phys. Rev. Lett. 106 (2011)]

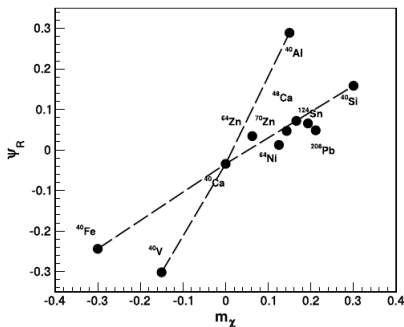


A=40 Isotopes Calculations - Neutron-Proton concentration Dependence

- $\Delta r_{np} = (0.90 \pm 0.15)m_\chi + (-0.03 \pm 0.02)$ fm
- Odd-Even staggering effect $^{40}\text{V}(\text{odd-odd})$, $^{40}\text{Fe}(\text{even-even})$;
 $^{40}\text{Al}(\text{odd-odd})$, $^{40}\text{Si}(\text{even-even})$



Geometrical effects: $\Psi_R = \frac{\langle R_n^2 \rangle - \langle R_p^2 \rangle}{\langle R_n^2 \rangle + \langle R_p^2 \rangle} = \begin{matrix} +1, m_\chi = 1 \\ -1, m_\chi = -1 \end{matrix}$



- Approximately linear relation for systems having the same mass - $A=40$
- Sensitivity on whether the nuclei are odd-odd or even-even
- Fixing A and varying m_χ , $\implies a_a$ coefficient (similar to the IAS method)
- $N=Z$ system:

$$\Delta r_{np}({}^{40}\text{Ca}) \approx -0.12 \text{ fm} \Leftrightarrow$$

$$\Psi_R({}^{40}\text{Ca}) \approx -0.035$$

remove Coulomb effects $\Psi_R({}^{40}\text{Ca}) = \Psi_0$: $\Psi'_R = |\Psi_R - \Psi_0|$

Conclusions:

- A Symmetry Potential Term having a 2+3 body dependence has been suggested. The comparison with other Symmetry Terms shows the dependence of the L and K_{sym} parameters on the details of the NEOS
- The CoMD model is suitable to perform collective modes calculations to constrain the NEOS
- Calculations for the ^{132}Sn nucleus reveal that IVGDR mode and NST constrain the symmetry term, however effective mass plays a role to reproduce experimental results

Outlook:

- Calculations for further S and L values (in progress)
- IVPDR, IVGDR for Tin Isotopes and other nuclei (EWSR, $N - Z/A$ dependence, Surface Effects)
- Comparisons with Dynamical (MD), Transport Models (Landau-Vlasov) and available experimental data