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EUROPEAN CENTRE FOR THEORETICAL STUDIES
IN NUCLEAR PHYSICS AND RELATED AREAS
TRENTO, ITALY

Hadronic contribution to the muon anomalous magnetic moment

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**LC13: Exploring QCD from the infrared regime to heavy
flavour scales at B-factories, the LHC and a Linear Collider**

Trento 16-20 September 2013

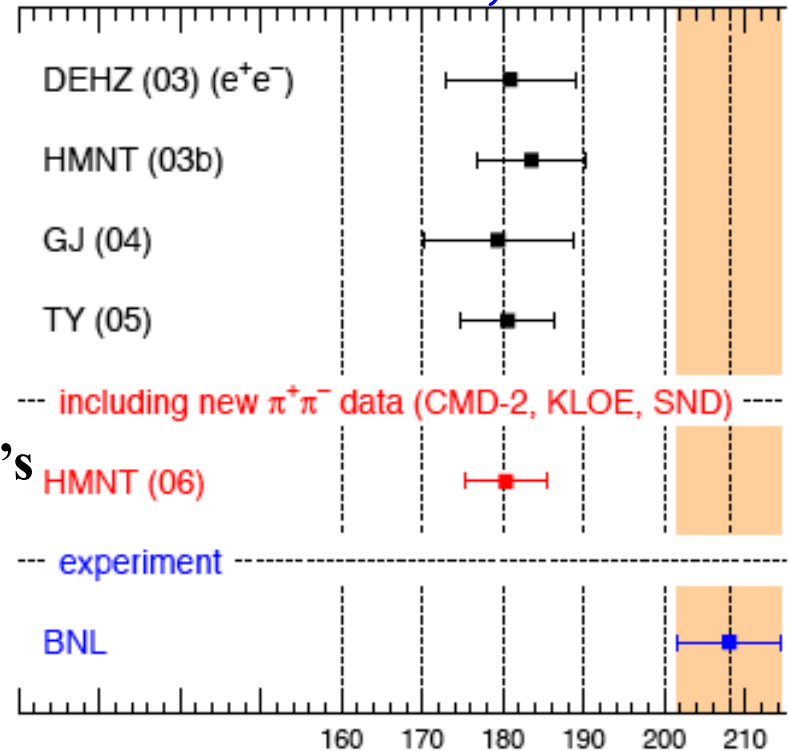
Muon anomaly

$$a_\mu = \frac{(g_\mu - 2)}{2}$$

- Long established discrepancy ($>3\sigma$) between SM prediction and BNL E821 exp.
- Theoretical error δa_μ^{SM} ($\sim 6 \times 10^{-10}$) dominated by HLO VP ($4 \div 5 \times 10^{-10}$) and HLbL ($[2.5 \div 4] \times 10^{-10}$). A **twofold** improvement on δa_μ^{SM} from 2001 (thanks to new e^+e^- measurements)!
- Experimental error $\delta a_\mu^{\text{EXP}} \sim 6 \times 10^{-10}$ (E821). Plan to reduce it to 1.5×10^{-10} by the new g-2 experiments at FNAL and J-PARC.

a_μ^{SM} compared to BNL world av.

T. Teubner, PHIPSI08

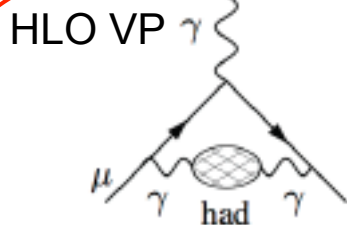


--- including new $\pi^+\pi^-$ data (CMD-2, KLOE, SND) ---

--- experiment ---

$$a_\mu^{\text{SM}} \times 10^{10} - 11659000$$

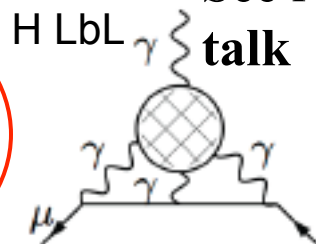
$$a_\mu^{\text{EXP}} - a_\mu^{\text{TH}} = (27.6 \pm 8.1) \cdot 10^{-10}, \sim 3.4\sigma$$



$$a_\mu^{\text{HLO}} = (690.9 \pm 4.4) \cdot 10^{-10}$$

[Eidelman, TAU08]

$$\delta a_\mu^{\text{HLO}} \sim 0.7\%$$



$$a_\mu^{\text{HLbL}} = (10.5 \pm 2.6) \cdot 10^{-10}$$

[Prades, dR&V. 08]
(11 ± 4) $\cdot 10^{-10}$ (Jegerlehner, Nyffler)

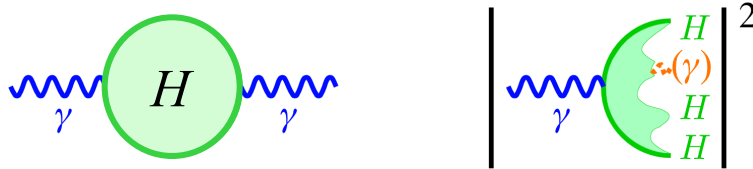
$$\delta a_\mu^{\text{HLbL}} \sim 25-40\%$$

See Nyffler's talk

$$\text{In 2001 } a_\mu^{\text{EXP}} - a_\mu^{\text{TH}} = (23 \pm 16) \cdot 10^{-10}$$

a_μ^{HLO} :

L.O. Hadronic contribution to a_μ can be estimated by means of a dispersion integral:



$$a_\mu^{\text{had}} = \left(\frac{\alpha m_\mu}{3\pi} \right)^2 \int_{4m_\pi^2}^{\infty} ds \frac{R(s) \hat{K}(s)}{s^2}$$

$$R(s) = \frac{\sigma_{\text{tot}}(e^+e^- \rightarrow \gamma^* \rightarrow q\bar{q} \rightarrow \text{hadrons})}{\sigma_{\text{tot}}(e^+e^- \rightarrow \gamma^* \rightarrow \mu^+\mu^-)}$$

$1/s^2$ makes **low energy contributions** especially important:

$$e^+e^- \rightarrow \pi^+\pi^-$$

in the range < 1 GeV contributes to 70% !

- $K(s)$ = analytic kernel-function

- above sufficiently high energy value, typically 2...5 GeV, use *pQCD*

Input:

a) **hadronic electron-positron cross section data** (G.dR 69, E.J.95, A.D.H.'97,....)

b) **hadronic τ - decays**, which can be used with the help of the CVC-theorem and an isospin rotation (plus isospin breaking corrections)

(A., D., H. '97)

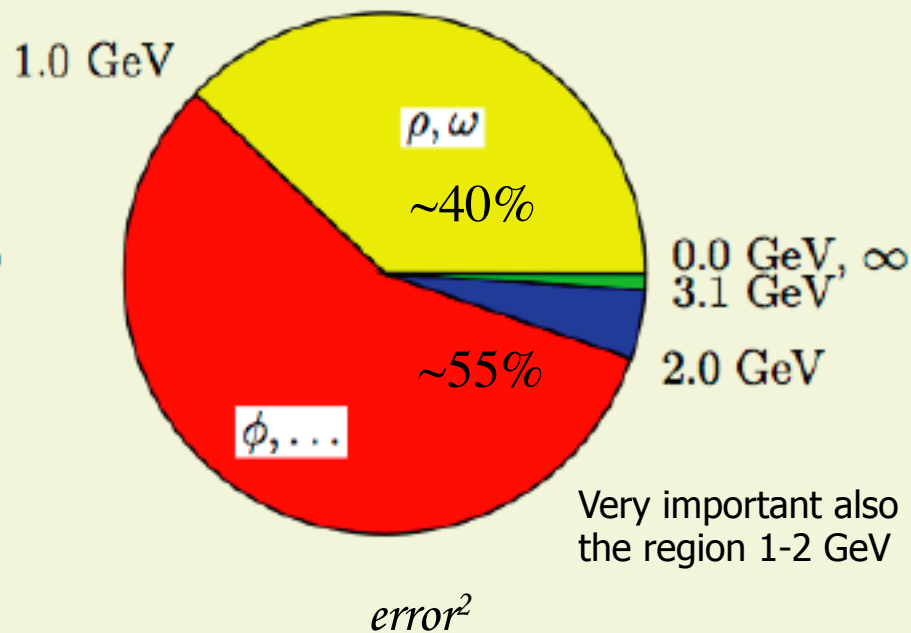
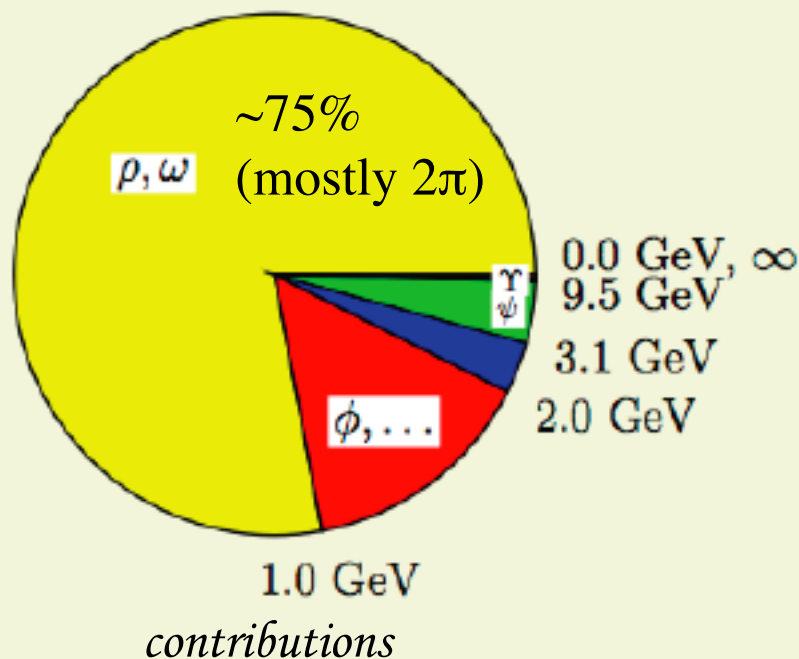
Dispersion Integral:

$$a_{\mu}^{HLO} = \int_{4m_{\pi}^2}^{\infty} \sigma_{had}(s)K(s)ds$$

$$K(s) \sim 1/s$$

Contribution of different energy regions to the dispersion integral and the error to a_{μ}^{HLO}

F. Jegerlehner, Talk at PHIPSI08



Experimental errors on σ^{had} translate into theoretical uncertainty of a_{μ}^{had} !
 → Needs precision measurements!

$$\delta a_{\mu}^{exp} \rightarrow 1.5 \cdot 10^{-10} = 0.2\% \text{ on } a_{\mu}^{HLO}$$

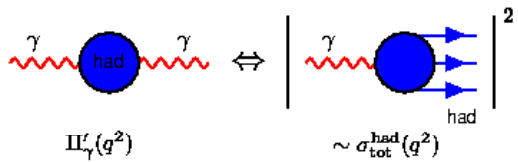
New g-2 exp.

$\alpha_{em}(M_Z)$ and EW fit of the SM (M_{Higgs})

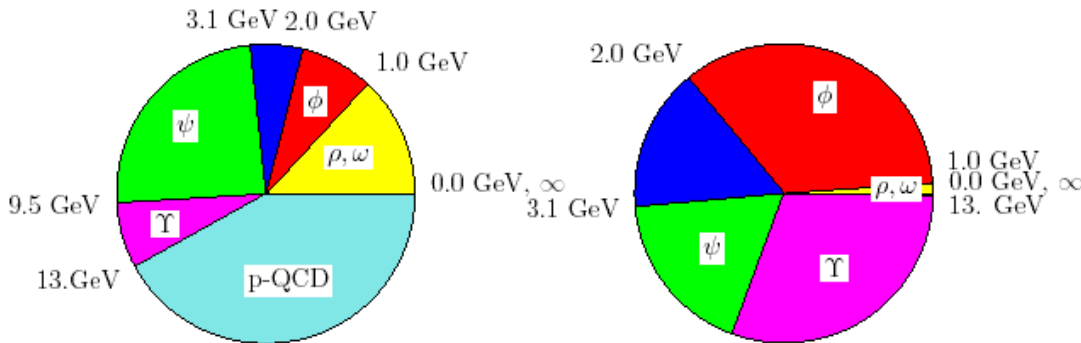
$$\alpha(M_Z) = \frac{\alpha(0)}{1 - \Delta\alpha(M_Z)}$$

$$\Delta\alpha = \Delta\alpha_l + \Delta\alpha_{had}^{(5)} + \Delta\alpha_{top}$$

polarization function $\Pi'_\gamma(q^2)$



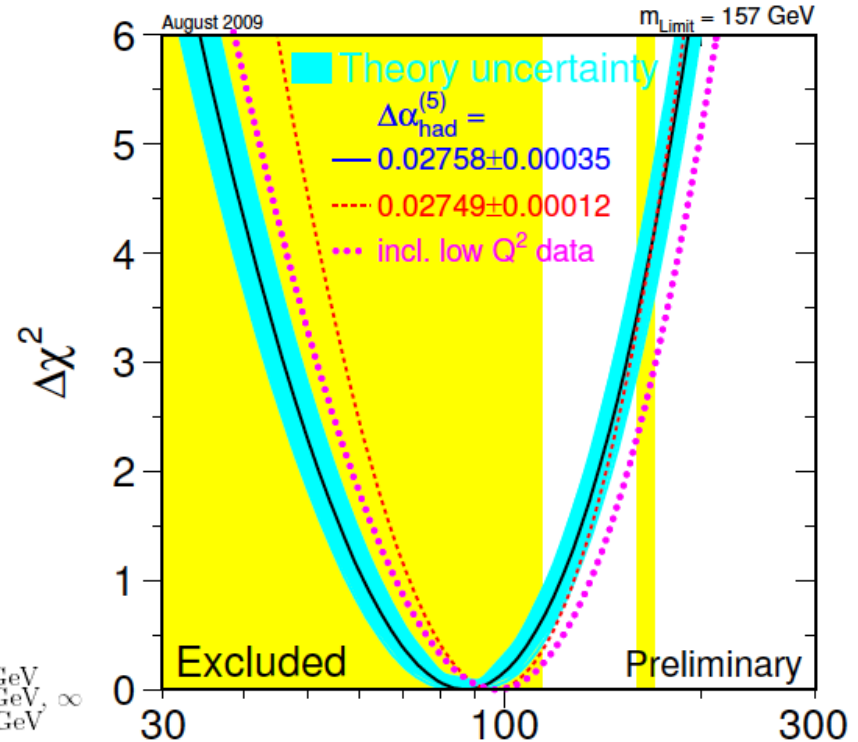
$$\Delta\alpha_{had}^{(5)}(M_Z^2) = -\frac{\alpha M_Z^2}{3\pi} \text{Re} \int_{4m_\pi^2}^{\infty} ds \frac{R(s)}{s(s - M_Z^2 - i\epsilon)}$$



$$\Delta\alpha_{had}^{(5)}(M_Z^2)$$

$$\delta^2 \Delta\alpha_{had}^{(5)}(M_Z^2)$$

$$\delta\alpha(M_Z)/\alpha(M_Z) \sim 2 \times 10^{-4} \rightarrow 5 \times 10^{-5}$$



$$\Delta\alpha_{had}^{(5)}(M_Z^2) = 0.027607 \pm 0.000225$$

$$\alpha^{-1}(M_Z^2) = 128.947 \pm 0.035$$

$$\alpha^{-1}(0) = 137.0359895 \pm 0.0000061$$

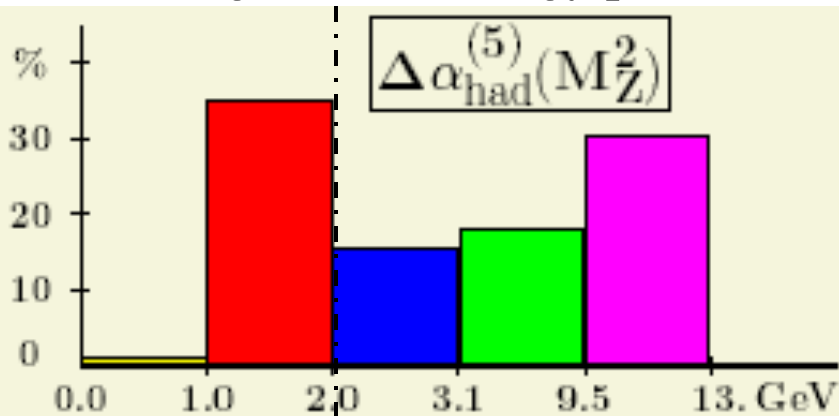
FJ08

Requirement from ILC (6x improvement)

Comparison of error profiles for $\alpha_{em}(M_Z)$

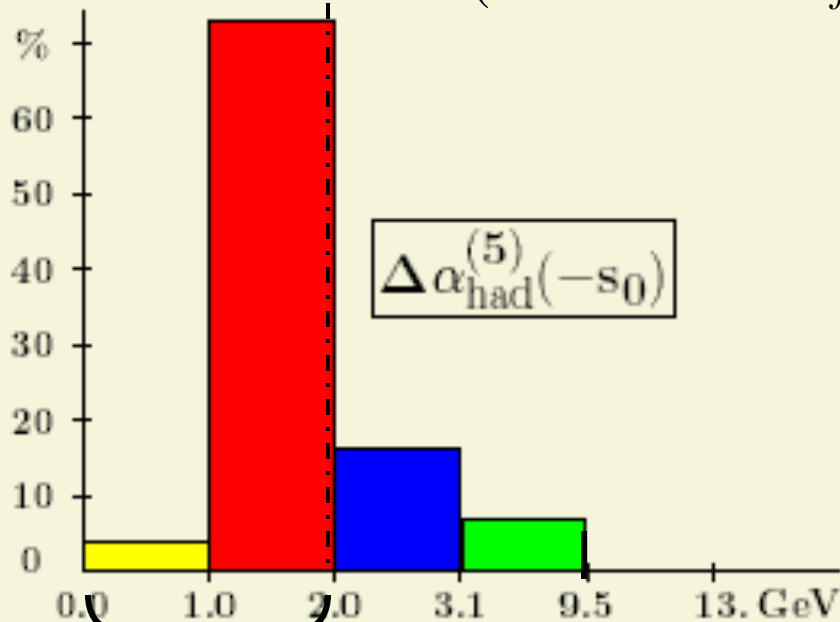
Direct integration of energy points

*F. Jegerlehner, Nucl. Phys. B
181-182 (2008) 135*



→ $\delta\sigma$ at 1% in the region $\sqrt{s} < 10$ GeV
 ⇒ improvement of ~ 3 in $\delta\alpha(M_Z)$

Use of Adler function (It allows to use *safely* pQCD down to 2.5 GeV)



→ 1% in the region $1 < \sqrt{s} < 2.5$ GeV
 ⇒ improvement of ~ 5 on $\delta\alpha(M_Z)$

$2m_\pi < \sqrt{s} < 2$ GeV

Extremely important:

- 80% of $\delta\Delta\alpha_{had}^{(5)}$ (using Adler function)
- 95% of δa_μ

Cross section data:

Two approaches:

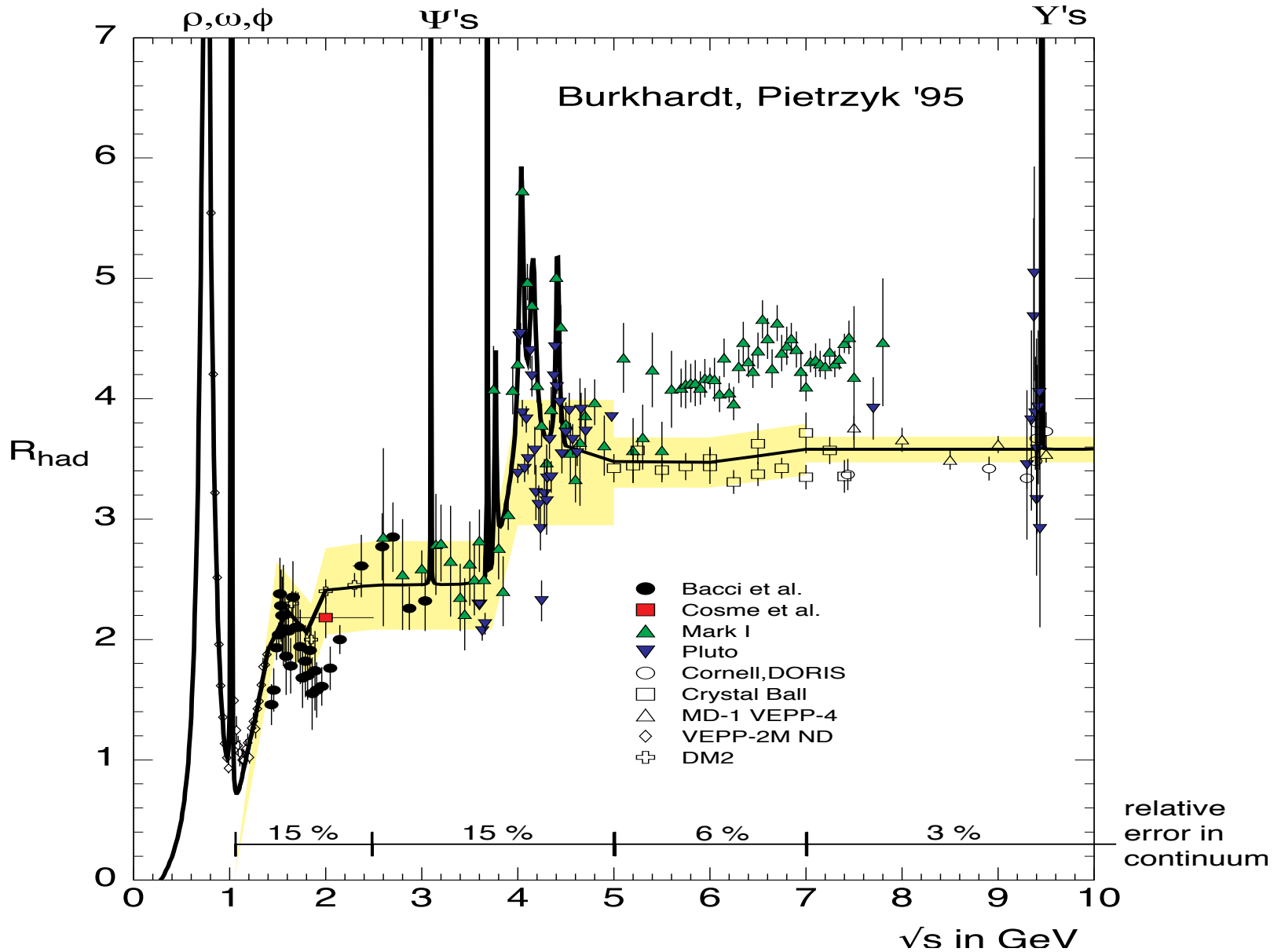
Energy scan (CMD2, SND, BES, CLEO):

- energy of colliding beams is changed to the desired value
- “direct” measurement of cross sections
- needs dedicated accelerator/physics program
- needs to measure luminosity and beam energy for every data point

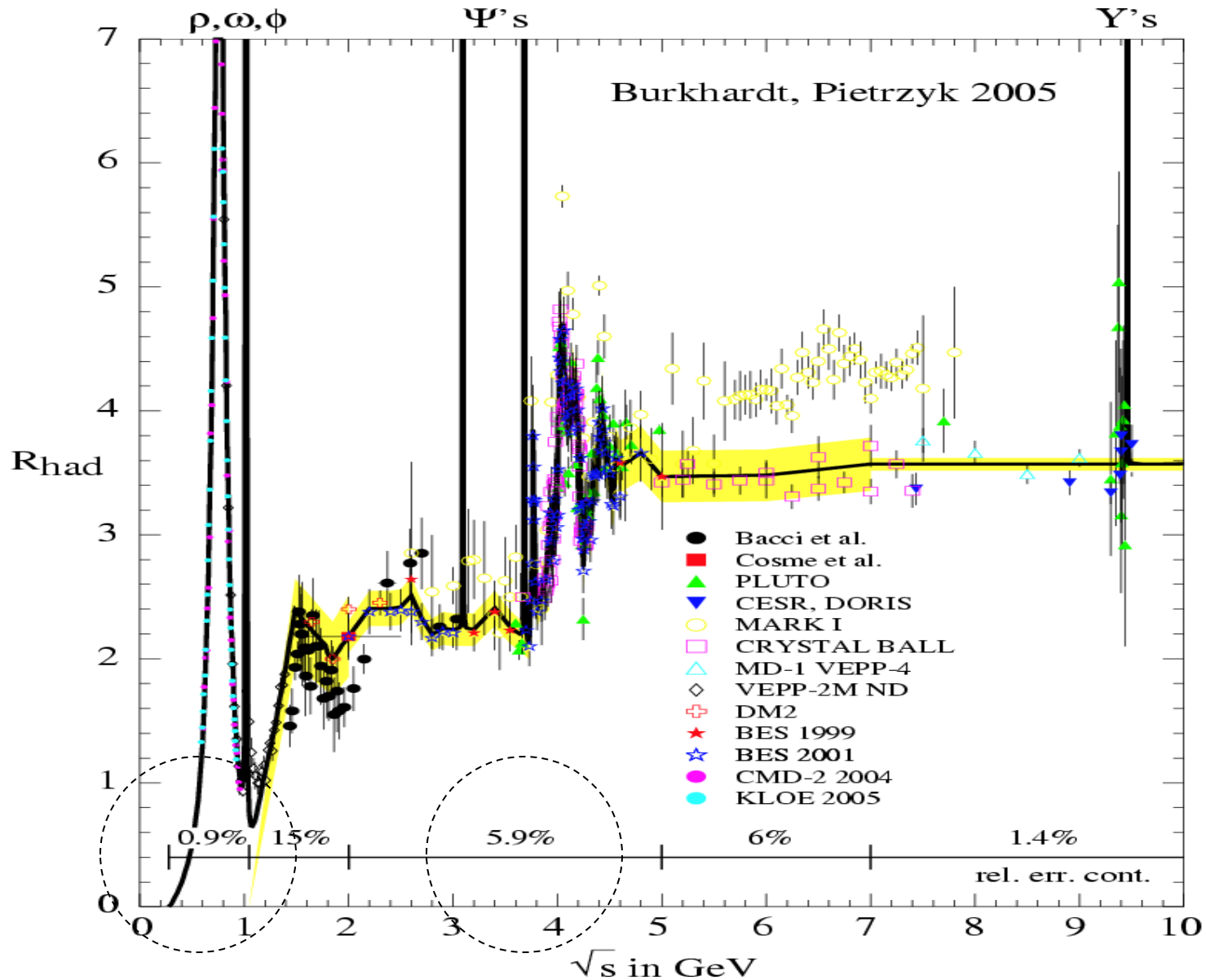
Radiative return (KLOE, BABAR, BELLE, BESIII?):

- runs at **fixed-energy machines** (meson factories)
- use **initial state radiation** process to access lower lying energies or resonances
- data come as by-product of standard physics program
- requires precise theoretical calculation of the **radiator function**
- luminosity and beam energy enter only once for all energy points
- needs larger integrated luminosity

Data at '95

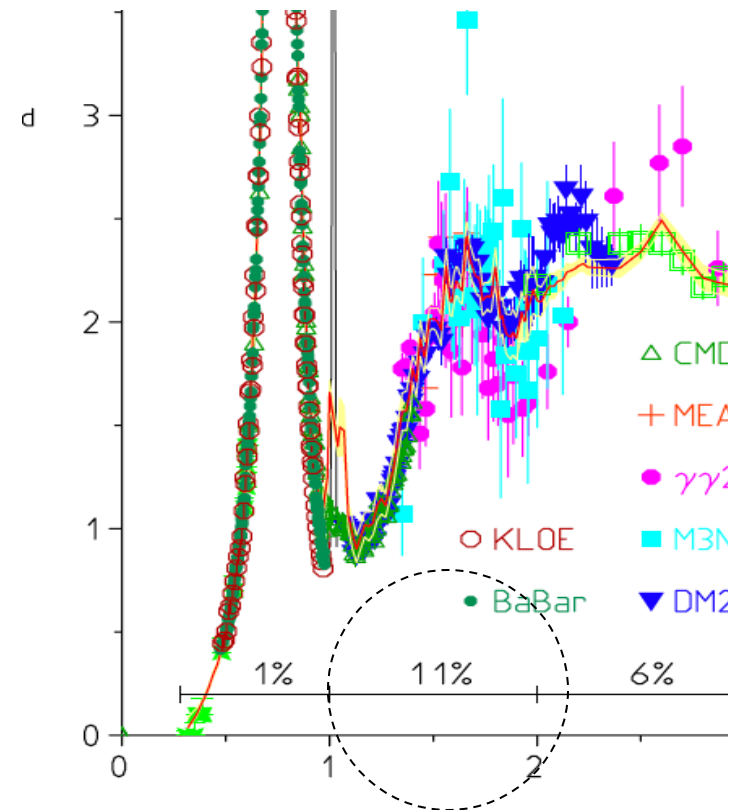
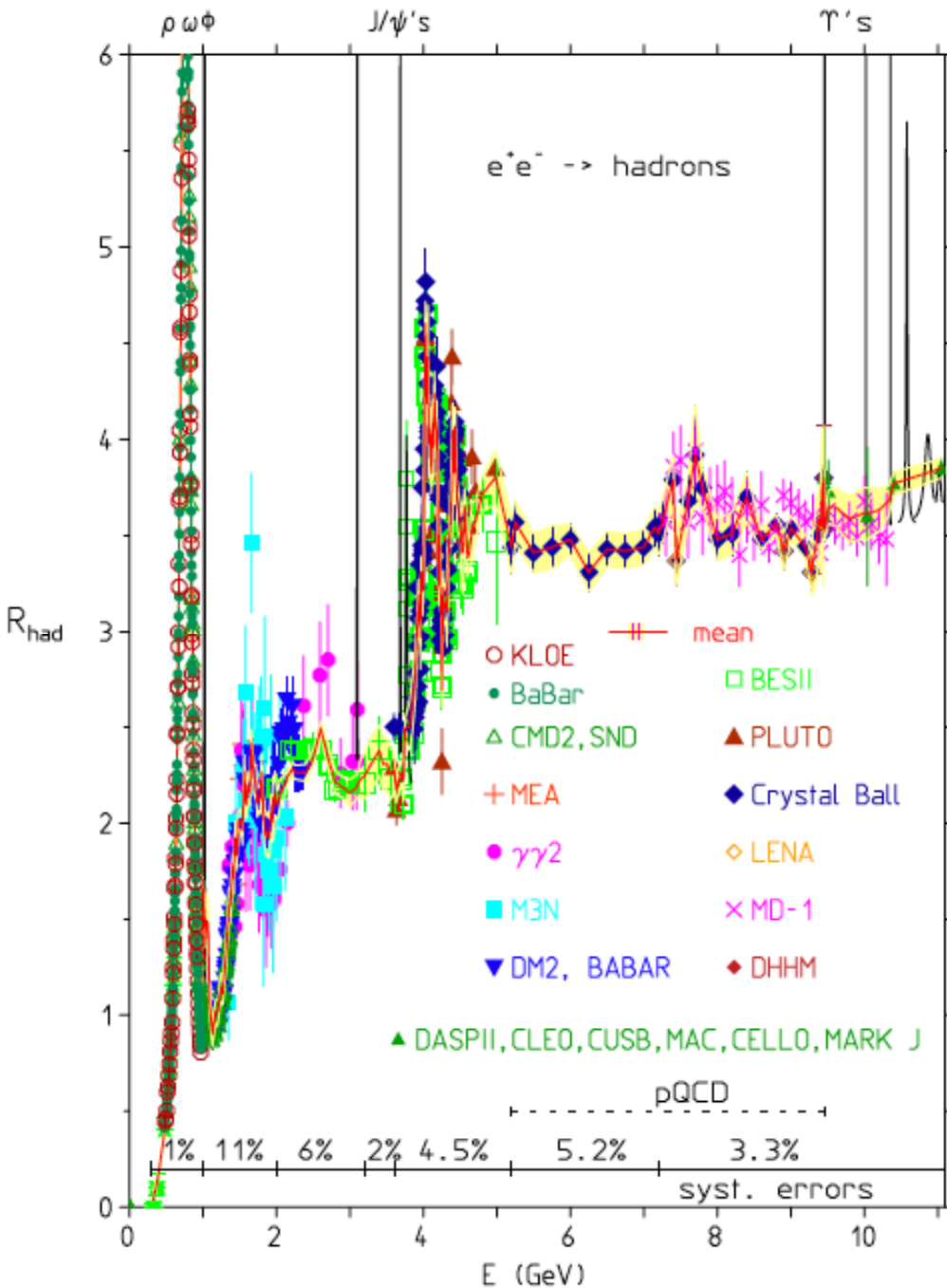


Data at '05



Data at 2012 (F.J.)

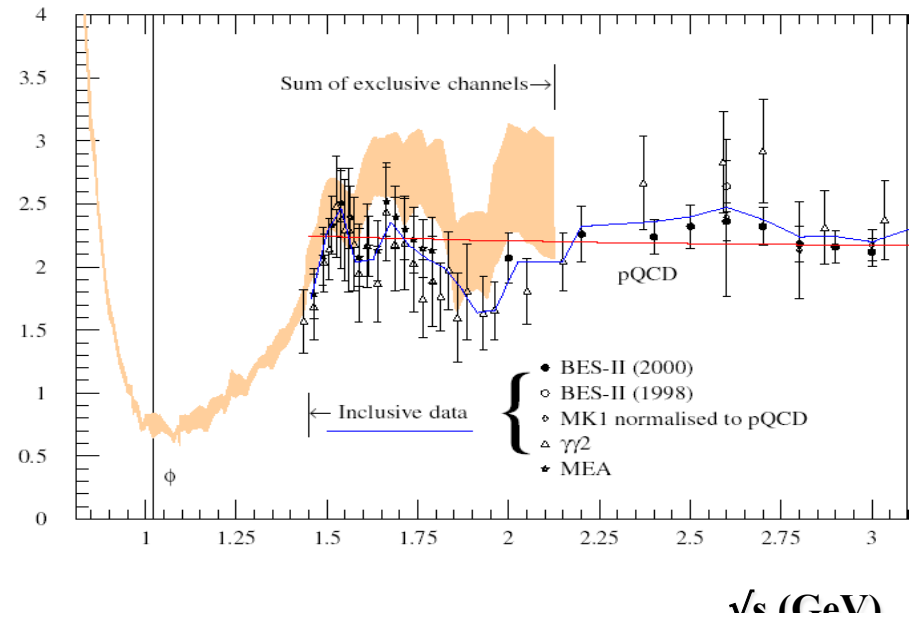
Many improvements (mostly due to BaBar ISR).
 However the region below 2.5 GeV is still poorly known ($\delta R \sim 5-15\%$)



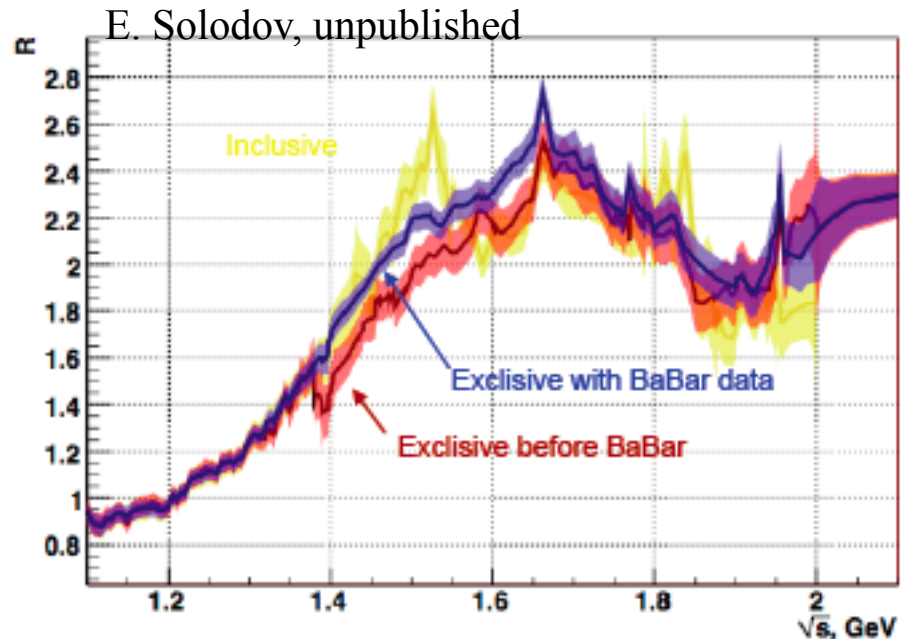
Exclusive vs inclusive measurements?

T. Teubner 08

1) Most recent inclusive measurements: MEA and B antiB, with **total** integrated luminosity of **200 nb⁻¹** (one hour of data taking at **10³² cm⁻² sec⁻¹**). **10% stat.+ 15% syst. Errors**



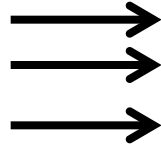
2) New BaBar data is improving a lot this region. However still the question on the completeness of exclusive data vs systematics of old inclusive measurements



Main contributions to a_μ^{HLO} and $\Delta\alpha(M_Z)$

Channel	$a_\mu^{\text{had,LO}} [10^{-10}]$	$\Delta\alpha_{\text{had}}(M_Z^2) [10^{-4}]$
$\pi^0\gamma$	$4.42 \pm 0.08 \pm 0.13 \pm 0.12$	$0.36 \pm 0.01 \pm 0.01 \pm 0.01$
$\eta\gamma$	$0.64 \pm 0.02 \pm 0.01 \pm 0.01$	$0.08 \pm 0.00 \pm 0.00 \pm 0.00$
$\pi^+\pi^-$	$507.80 \pm 1.22 \pm 2.50 \pm 0.56$	$34.43 \pm 0.07 \pm 0.17 \pm 0.04$
$\pi^+\pi^-\pi^0$	$46.00 \pm 0.42 \pm 1.03 \pm 0.98$	$4.58 \pm 0.04 \pm 0.11 \pm 0.09$
$2\pi^+2\pi^-$	$13.35 \pm 0.10 \pm 0.43 \pm 0.29$	$3.49 \pm 0.03 \pm 0.12 \pm 0.08$
$\pi^+\pi^-2\pi^0$	$18.01 \pm 0.14 \pm 1.17 \pm 0.40$	$4.43 \pm 0.03 \pm 0.29 \pm 0.10$
$2\pi^+2\pi^-\pi^0$ (η excl.)	$0.72 \pm 0.04 \pm 0.07 \pm 0.03$	$0.22 \pm 0.01 \pm 0.02 \pm 0.01$
$\pi^+\pi^-3\pi^0$ (η excl., from isospin)	$0.36 \pm 0.02 \pm 0.03 \pm 0.01$	$0.11 \pm 0.01 \pm 0.01 \pm 0.00$
$3\pi^+3\pi^-$	$0.12 \pm 0.01 \pm 0.01 \pm 0.00$	$0.04 \pm 0.00 \pm 0.00 \pm 0.00$
$2\pi^+2\pi^-2\pi^0$ (η excl.)	$0.70 \pm 0.05 \pm 0.04 \pm 0.09$	$0.25 \pm 0.02 \pm 0.02 \pm 0.03$
$\pi^+\pi^-4\pi^0$ (η excl., from isospin)	$0.11 \pm 0.01 \pm 0.11 \pm 0.00$	$0.04 \pm 0.00 \pm 0.04 \pm 0.00$
$\eta\pi^+\pi^-$	$1.15 \pm 0.06 \pm 0.08 \pm 0.03$	$0.33 \pm 0.02 \pm 0.02 \pm 0.01$
$\eta\omega$	$0.47 \pm 0.04 \pm 0.00 \pm 0.05$	$0.15 \pm 0.01 \pm 0.00 \pm 0.02$
$\eta2\pi^+2\pi^-$	$0.02 \pm 0.01 \pm 0.00 \pm 0.00$	$0.01 \pm 0.00 \pm 0.00 \pm 0.00$
$\eta\pi^+\pi^-2\pi^0$ (estimated)	$0.02 \pm 0.01 \pm 0.01 \pm 0.00$	$0.01 \pm 0.00 \pm 0.00 \pm 0.00$
$\omega\pi^0$ ($\omega \rightarrow \pi^0\gamma$)	$0.89 \pm 0.02 \pm 0.06 \pm 0.02$	$0.18 \pm 0.00 \pm 0.02 \pm 0.00$
$\omega\pi^+\pi^-, \omega2\pi^0$ ($\omega \rightarrow \pi^0\gamma$)	$0.08 \pm 0.00 \pm 0.01 \pm 0.00$	$0.03 \pm 0.00 \pm 0.00 \pm 0.00$
ω (non- $3\pi, \pi\gamma, \eta\gamma$)	$0.36 \pm 0.00 \pm 0.01 \pm 0.00$	$0.03 \pm 0.00 \pm 0.00 \pm 0.00$
K^+K^-	$21.63 \pm 0.27 \pm 0.58 \pm 0.36$	$3.13 \pm 0.04 \pm 0.08 \pm 0.05$
$K_S^0K_L^0$	$12.96 \pm 0.18 \pm 0.25 \pm 0.24$	$1.75 \pm 0.02 \pm 0.03 \pm 0.03$
ϕ (non- $K\bar{K}, 3\pi, \pi\gamma, \eta\gamma$)	$0.05 \pm 0.00 \pm 0.00 \pm 0.00$	$0.01 \pm 0.00 \pm 0.00 \pm 0.00$
$K\bar{K}\pi$ (partly from isospin)	$2.39 \pm 0.07 \pm 0.12 \pm 0.08$	$0.76 \pm 0.02 \pm 0.04 \pm 0.02$
$K\bar{K}2\pi$ (partly from isospin)	$1.35 \pm 0.09 \pm 0.38 \pm 0.03$	$0.48 \pm 0.03 \pm 0.14 \pm 0.01$
$K\bar{K}3\pi$ (partly from isospin)	$-0.03 \pm 0.01 \pm 0.02 \pm 0.00$	$-0.01 \pm 0.00 \pm 0.01 \pm 0.00$
$\phi\eta$	$0.36 \pm 0.02 \pm 0.02 \pm 0.01$	$0.13 \pm 0.01 \pm 0.01 \pm 0.00$
$\omega K\bar{K}$ ($\omega \rightarrow \pi^0\gamma$)	$0.00 \pm 0.00 \pm 0.00 \pm 0.00$	$0.00 \pm 0.00 \pm 0.00 \pm 0.00$

new meas

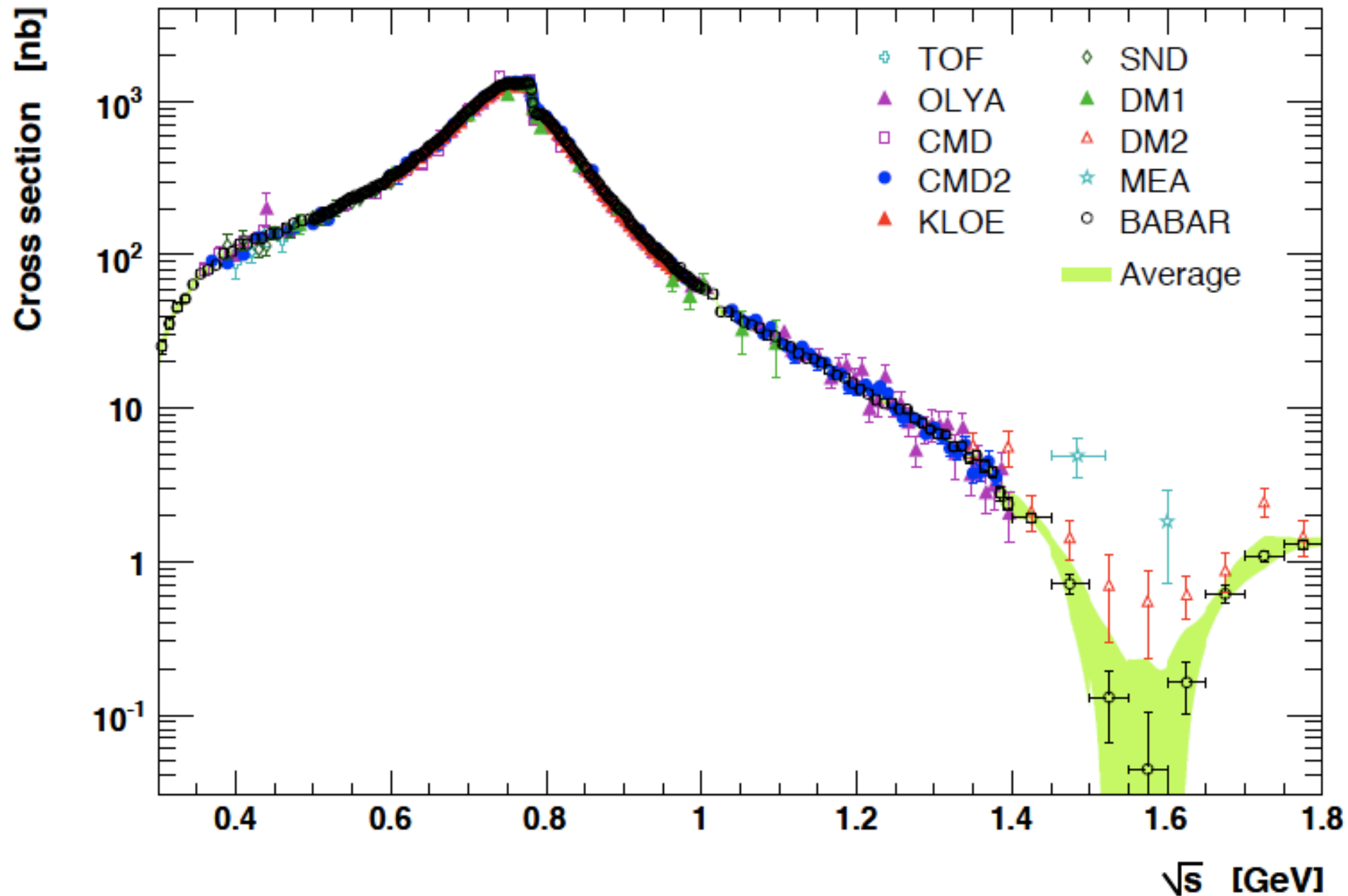


new meas



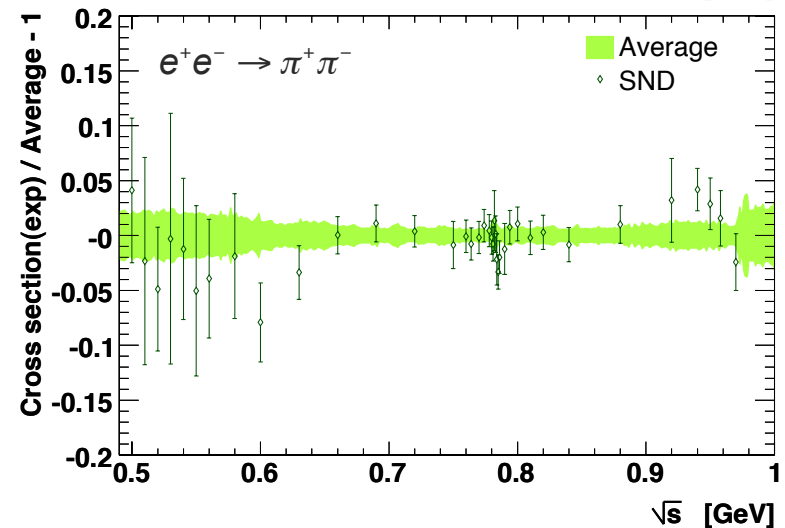
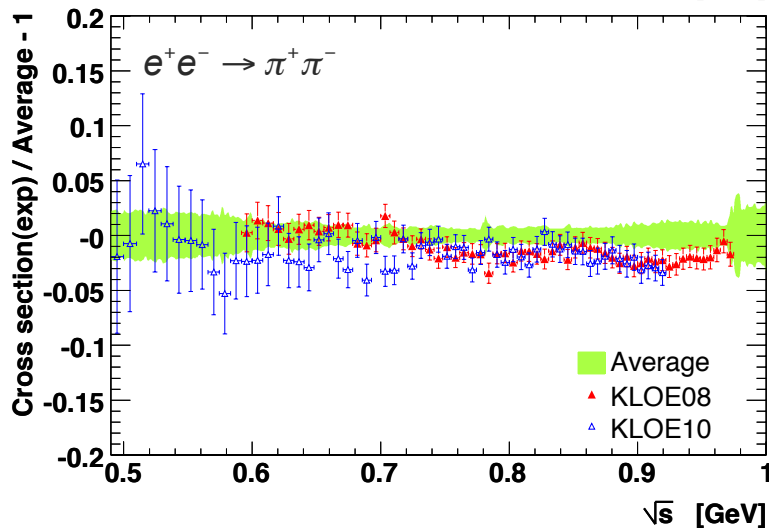
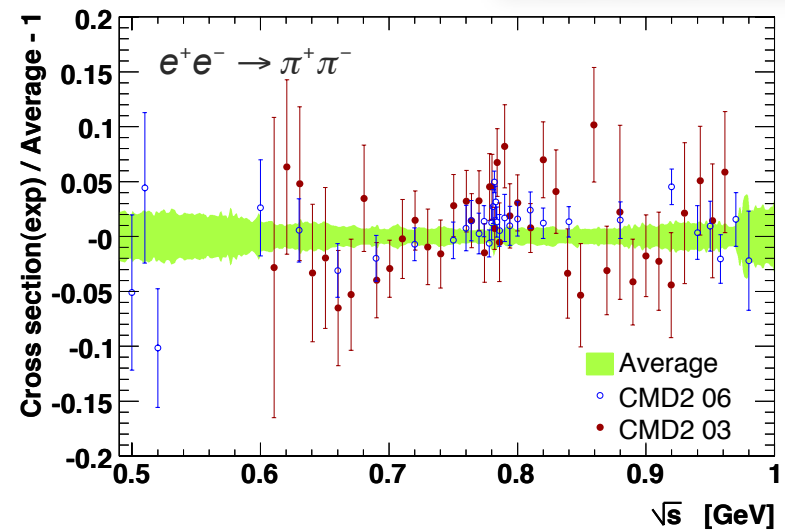
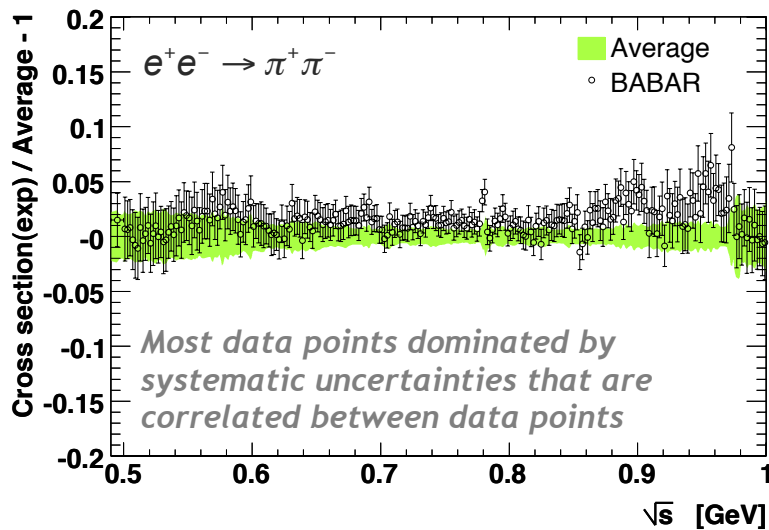
$$e^+e^- \rightarrow \pi^+\pi^-$$

Measured cross section for $e^+e^- \rightarrow \pi^+\pi^-$ (2010)

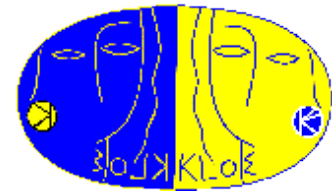


Situation of Two-pion channel

Davier *et al.*, EPJ C 71, 1515 (2011)



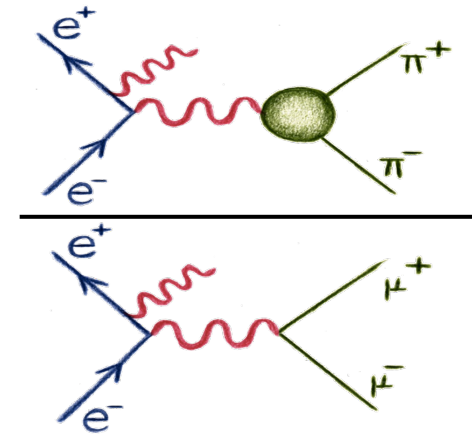
New (2013): KLOE $\sigma_{\pi\pi}$ from $\pi\pi\gamma/\mu\mu\gamma$



An alternative way to obtain $|F_\pi|^2$ is the bin-by-bin ratio of pion over muon yields (instead of using absolute normalization with Bhabhas).

$$|F_\pi(s')|^2 \approx \frac{4(1 + 2m_\mu^2/s')\beta_\mu}{\beta_\pi^3} \frac{d\sigma_{\pi\pi\gamma}/ds'}{d\sigma_{\mu\mu\gamma}/ds'}$$

$\underbrace{\hspace{10em}}_{\text{kinematical factor}} \quad \underbrace{\hspace{10em}}_{\text{meas. quantities}}$
 $(s_{\text{mm}}^{\text{Born}} / s_{\text{pp}}^{\text{Born}})$



Many radiative corrections drop out:

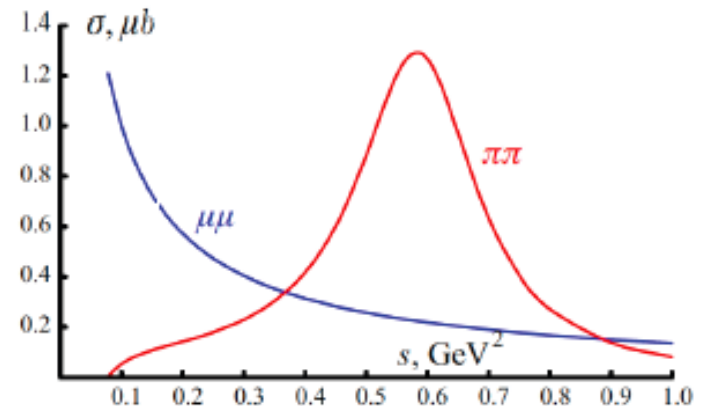
- *radiator function*
- *int. luminosity from Bhabhas*
- *Vacuum polarization*

Separation btw $\pi\pi\gamma$ and $\mu\mu\gamma$ using M_{TRK}

- *muons*: $M_{\text{Trk}} < 115 \text{ MeV}$
- *pions*: $M_{\text{Trk}} > 130 \text{ MeV}$

Very important control of π/μ separation in the ρ region! ($\sigma_{\pi\pi} \gg \sigma_{\mu\mu}$)

$\sigma(e^+e^- \rightarrow \pi^+\pi^-)$ and $\sigma(e^+e^- \rightarrow \mu^+\mu^-)$

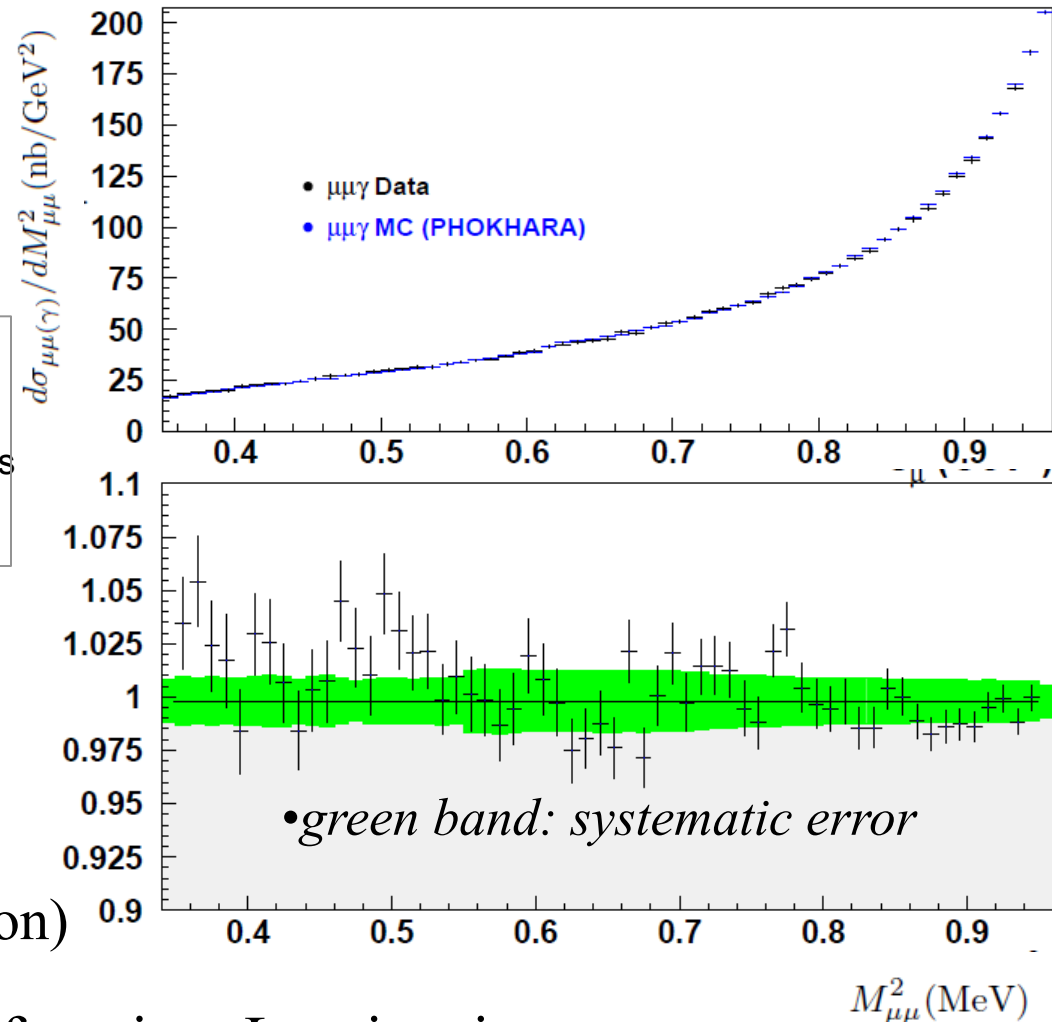


$\mu\mu\gamma$ cross section: data/MC comparison



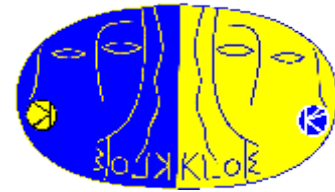
$$\frac{d\sigma_{\mu\mu(\gamma)}^{obs}}{dM_{\mu\mu}^2} = \frac{\Delta N_{Obs} - \Delta N_{Bkg}}{\Delta M_{\mu\mu}^2} \cdot \frac{1}{\epsilon_{Sel}} \cdot \frac{1}{\int L dt}$$

$$\frac{d\sigma_{\mu\mu(\gamma)}^{DATA}}{d\sigma_{\mu\mu(\gamma)}^{MC}} = 0.998 \pm 0.001_{stat} \pm 0.011_{sys}$$

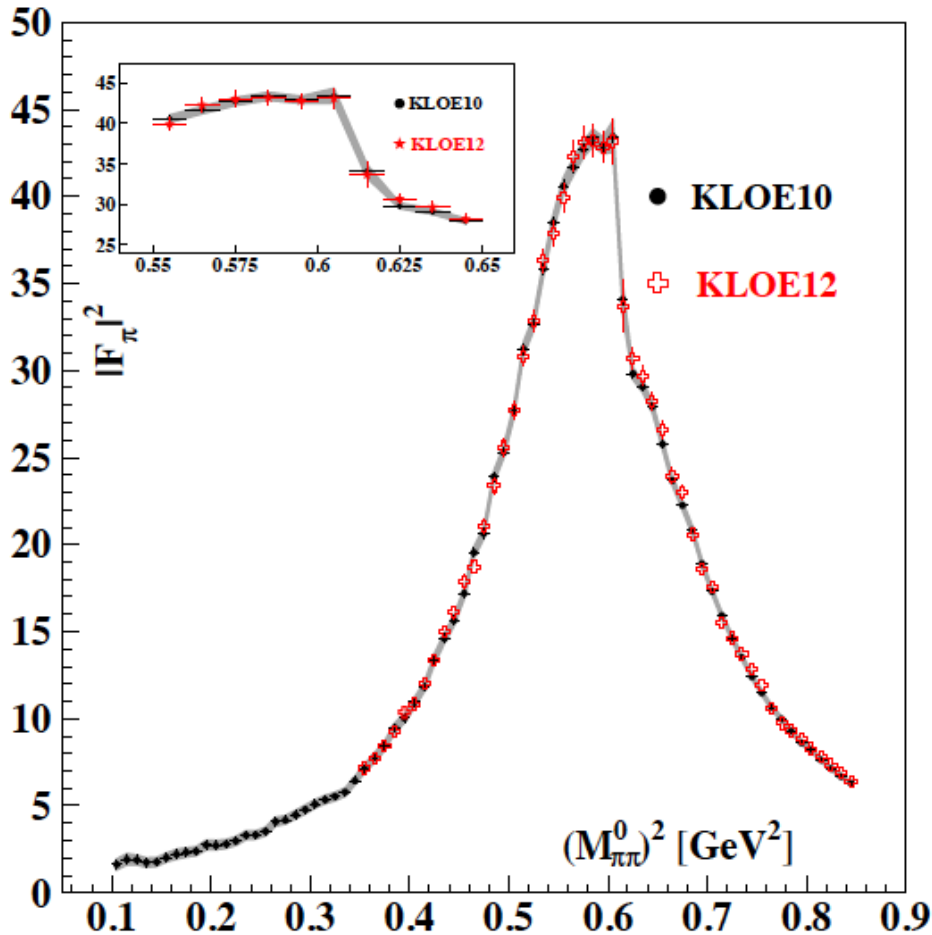


- The systematic error has been averaged on $M_{\mu\mu}^2$
- Good agreement with PHOKHARA MC (NLO Calculation)
- Consistency check of Radiator function, Luminosity, etc...

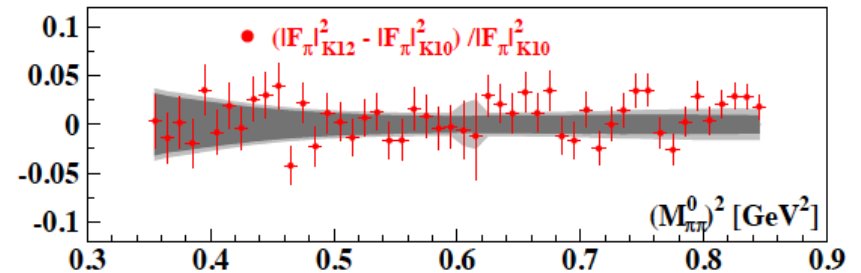
Comparison of results: KLOE12 vs KLOE10



KLOE12 result compared to KLOE10:



Fractional difference:



band: KLOE10 error

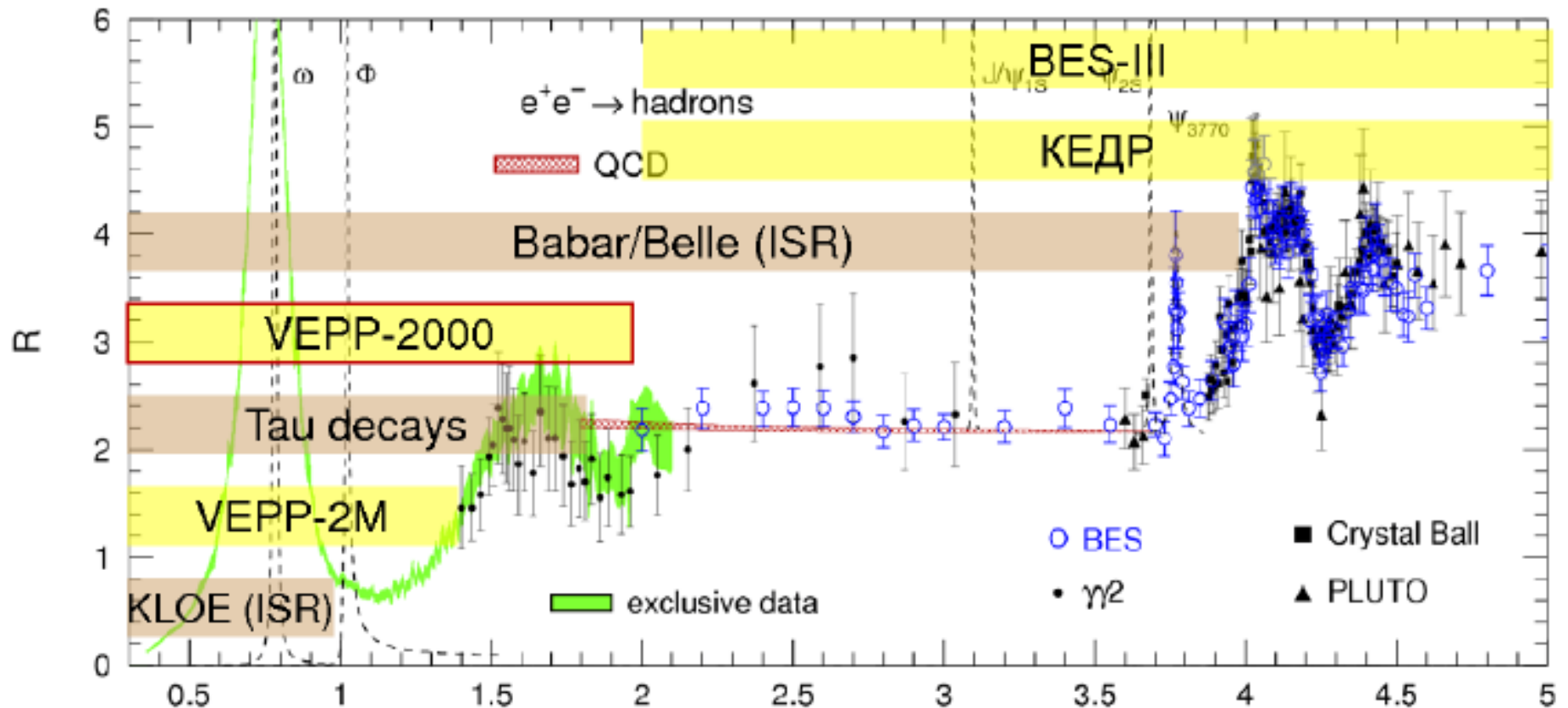
Excellent agreement between the two independent measurements!

• **PLB 720 (2013) 336–343**

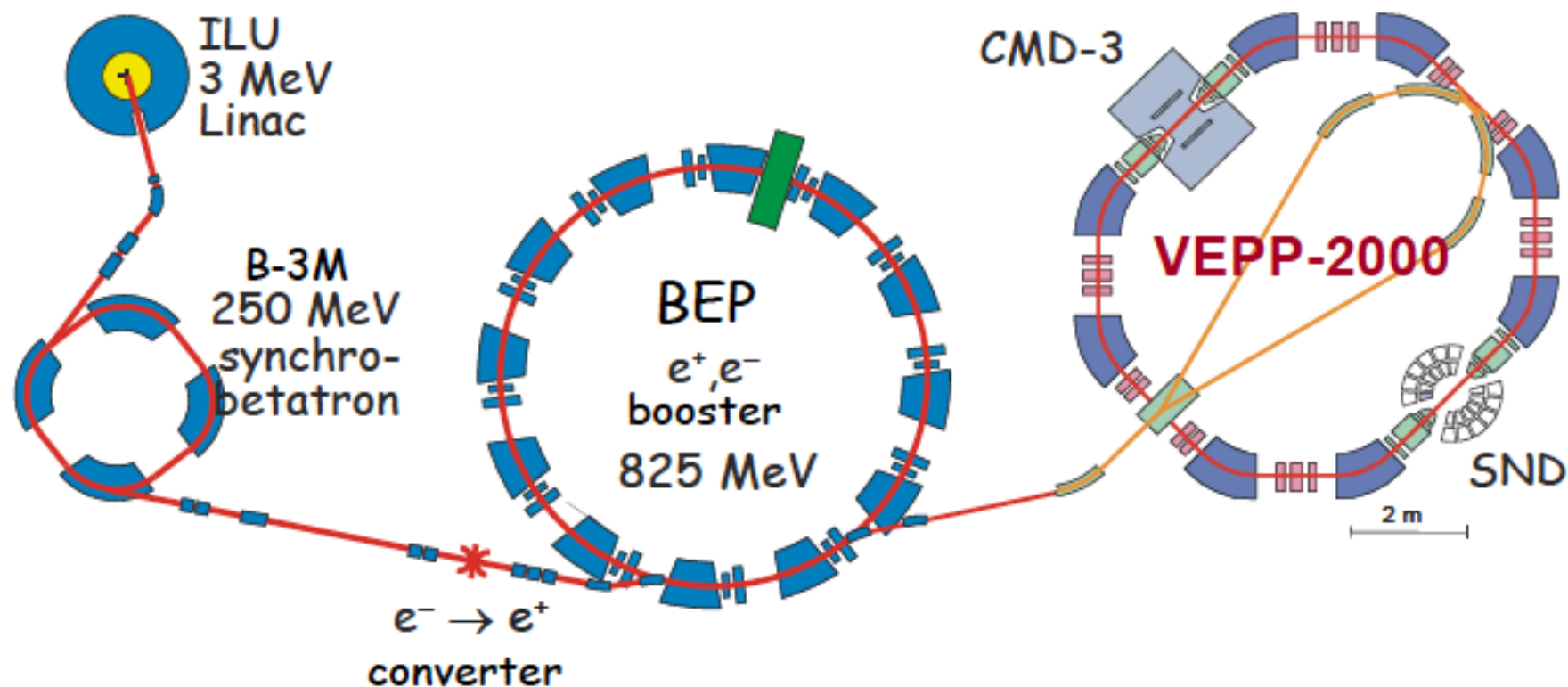
Analysis	$a_{\mu}^{\pi\pi}(0.35 - 0.85 \text{ GeV}^2) \times 10^{10}$
KLOE12	$377.4 \pm 1.1_{\text{stat}} \pm 2.7_{\text{sys+theo}}$
KLOE10	$376.6 \pm 0.9_{\text{stat}} \pm 3.3_{\text{sys+theo}}$

New measurements at the horizon

VEPP-2000 and the world



VEPP-2000

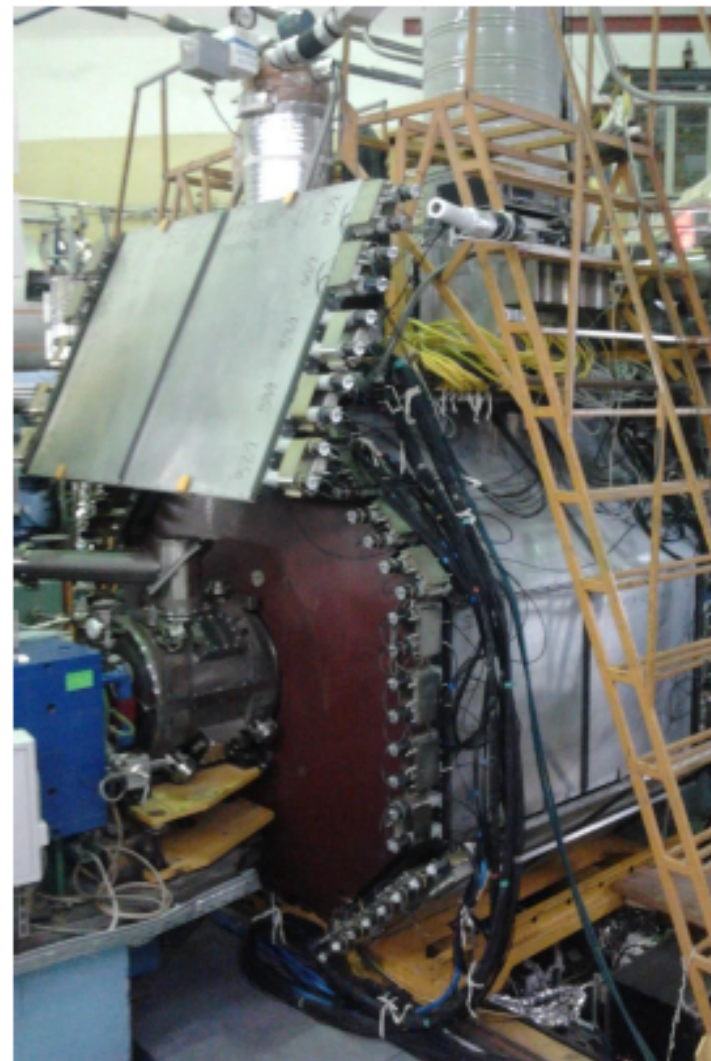
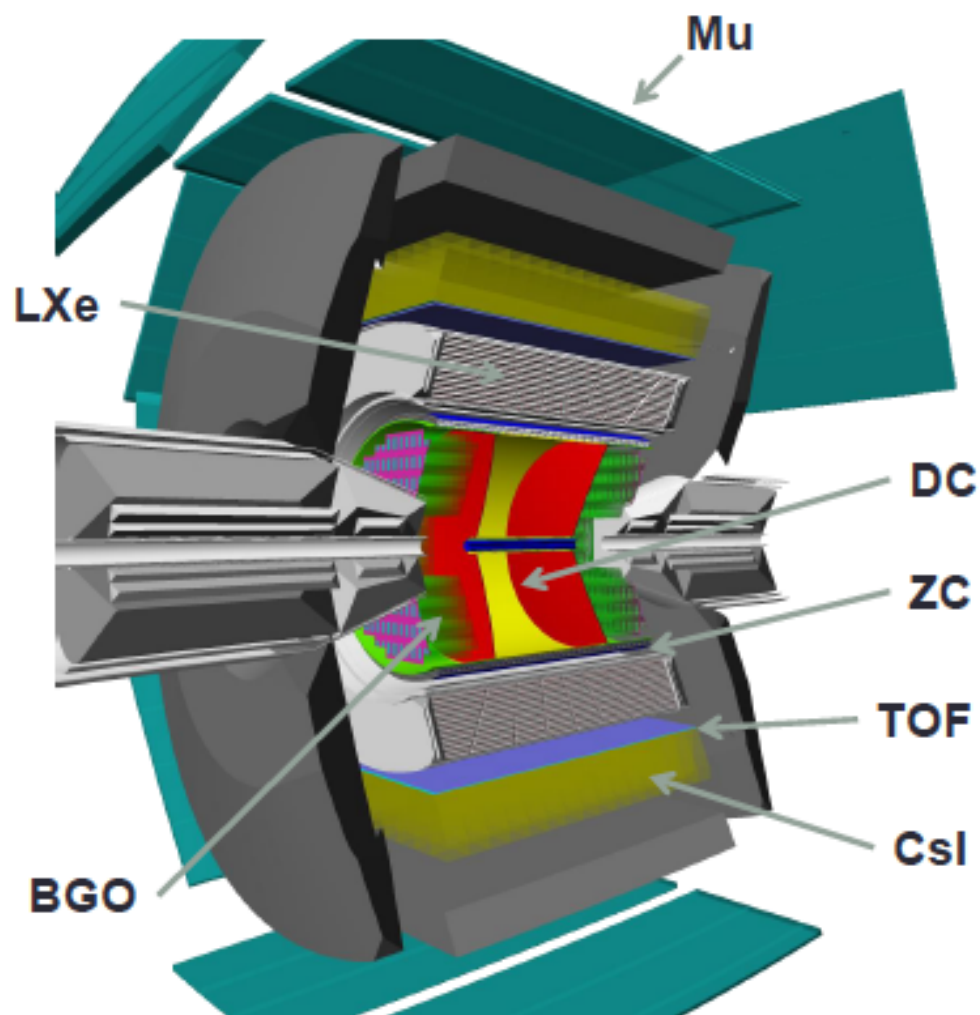


Maximum c.m. energy is 2 GeV, project luminosity is $L = 10^{32} 1/cm^2 s$ at $\sqrt{s} = 2$ GeV

Unique optics, "round beams", allows to reach higher luminosity

Experiments with two detectors, CMD-3 and SND, started by the end of 2010

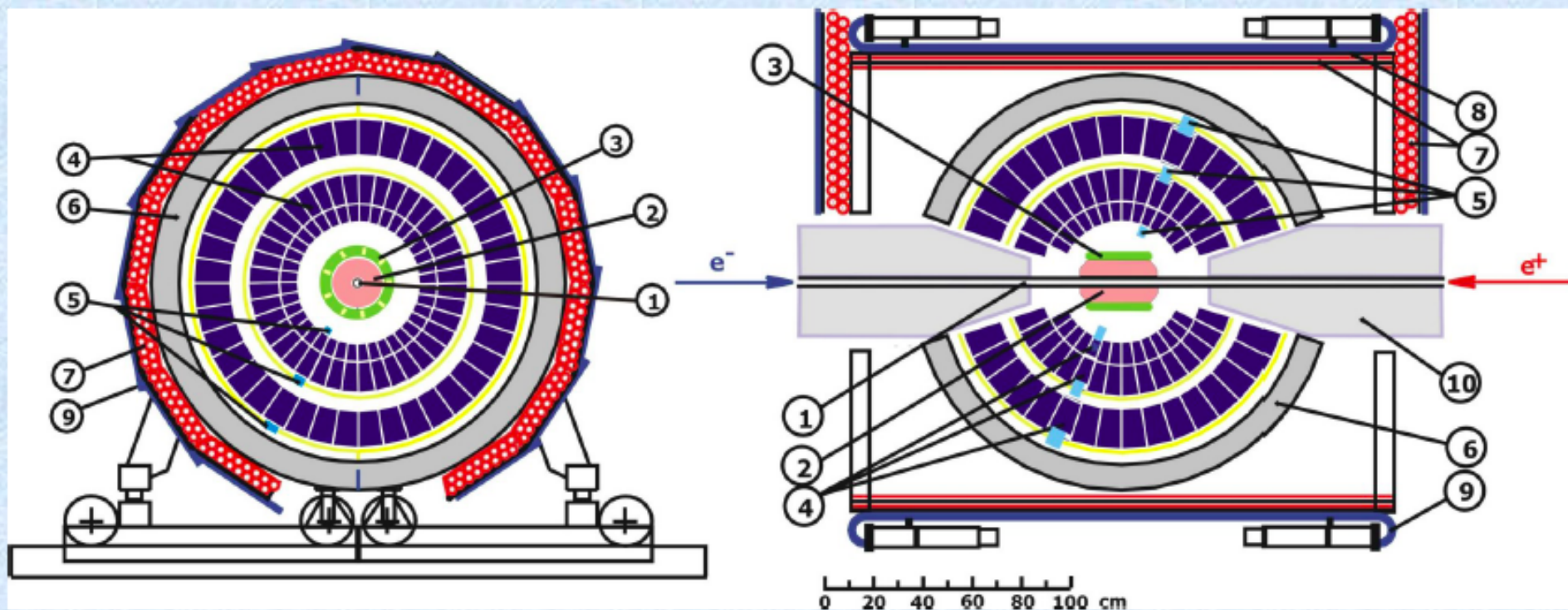
Detector CMD-3





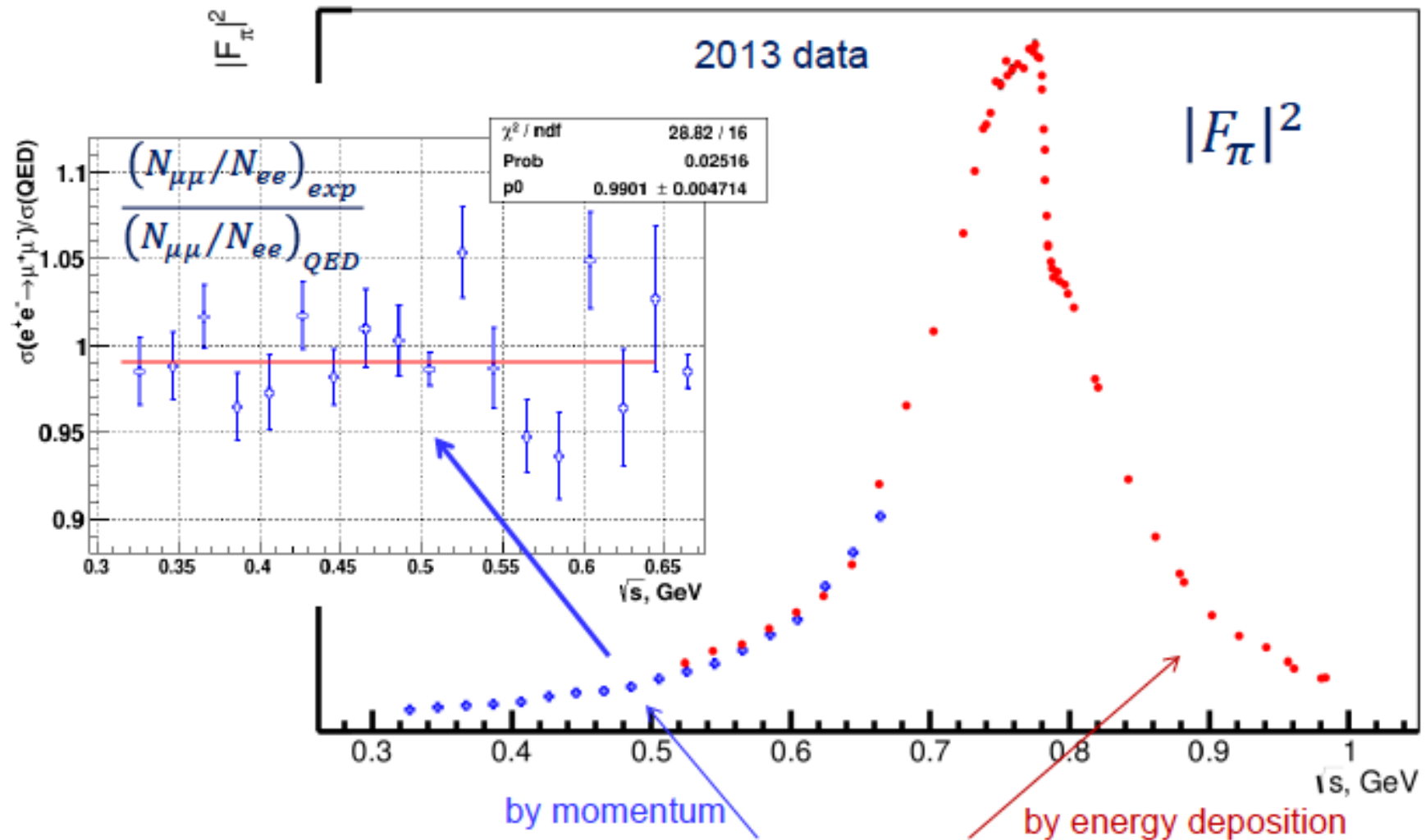
SND for VEPP-2000

NIM A449 (2000) 125-139



1 – beam pipe, 2 – tracking system, 3 – aerogel cherenkov counter, 4 – NaI(Tl) crystals, 5 – phototriodes, 6 – iron muon absorber, 7–9 – muon detector, 10 – focusing solenoids.

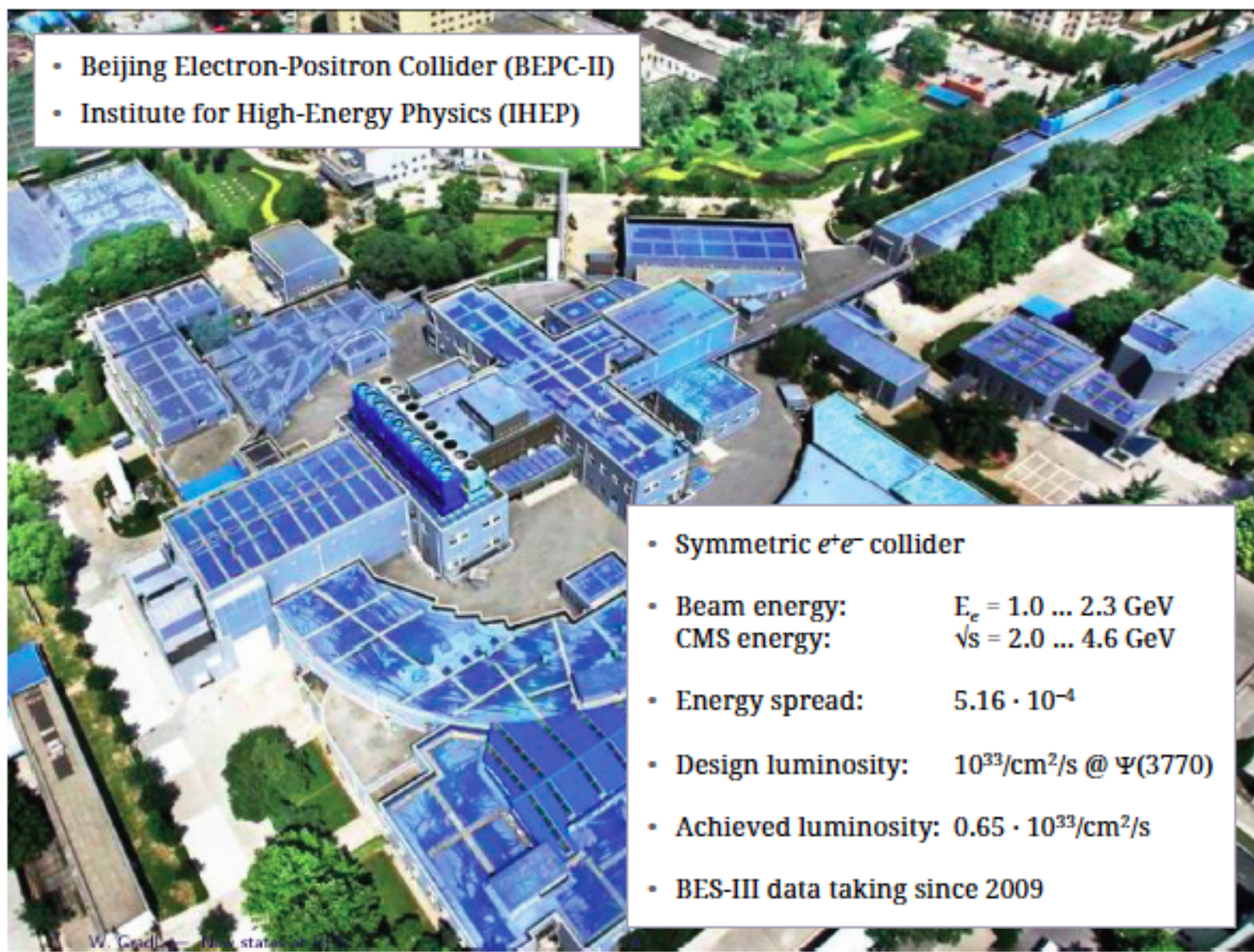
$e^+e^- \rightarrow \pi^+\pi^-$: very preliminary results



CMD3: By scan measurement

$e/\mu/\pi$ separation

- Beijing Electron-Positron Collider (BEPC-II)
- Institute for High-Energy Physics (IHEP)



- Symmetric e^+e^- collider
- Beam energy: $E_e = 1.0 \dots 2.3 \text{ GeV}$
CMS energy: $\sqrt{s} = 2.0 \dots 4.6 \text{ GeV}$
- Energy spread: $5.16 \cdot 10^{-4}$
- Design luminosity: $10^{33}/\text{cm}^2/\text{s}$ @ $\Psi(3770)$
- Achieved luminosity: $0.65 \cdot 10^{33}/\text{cm}^2/\text{s}$
- BES-III data taking since 2009

Cylindrical drift chamber

- $\sigma_p/p = 0.5\%$ @ 1 GeV

Super-conducting magnet

- $B = 1.0$ T

Time of Flight

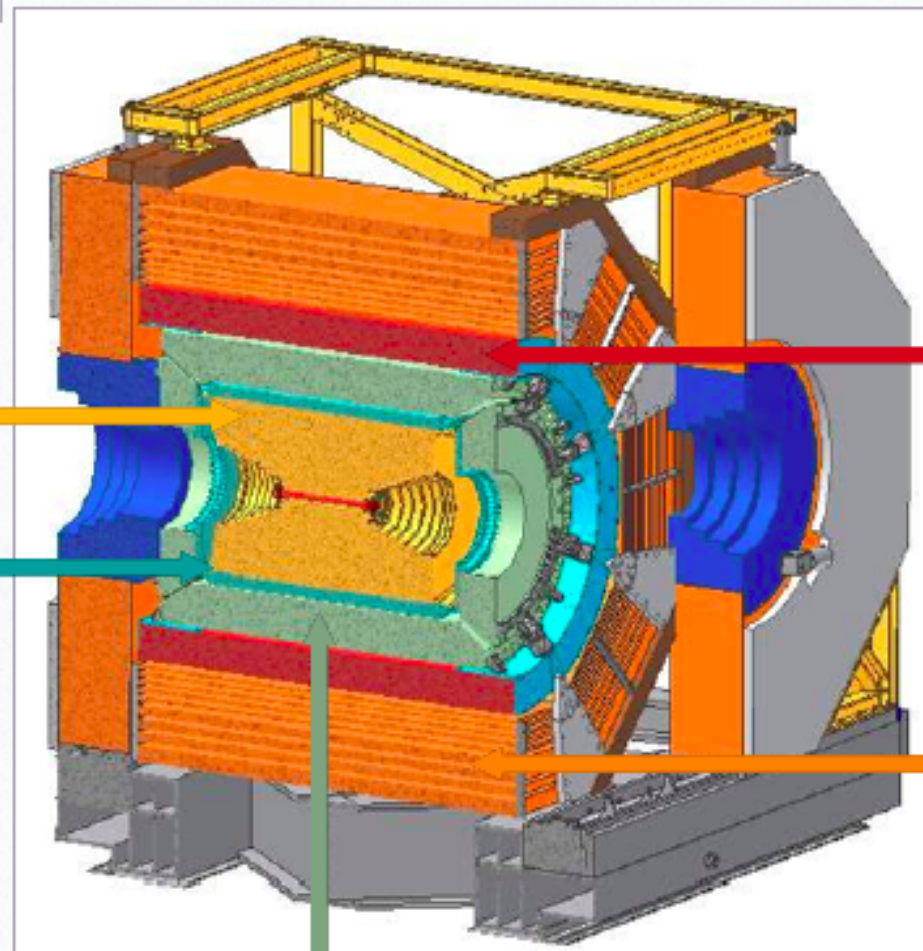
- $\sigma_T = 90$ ps (Barrel)
- 110 ps (Endcap)

EM calorimeter (CsI)

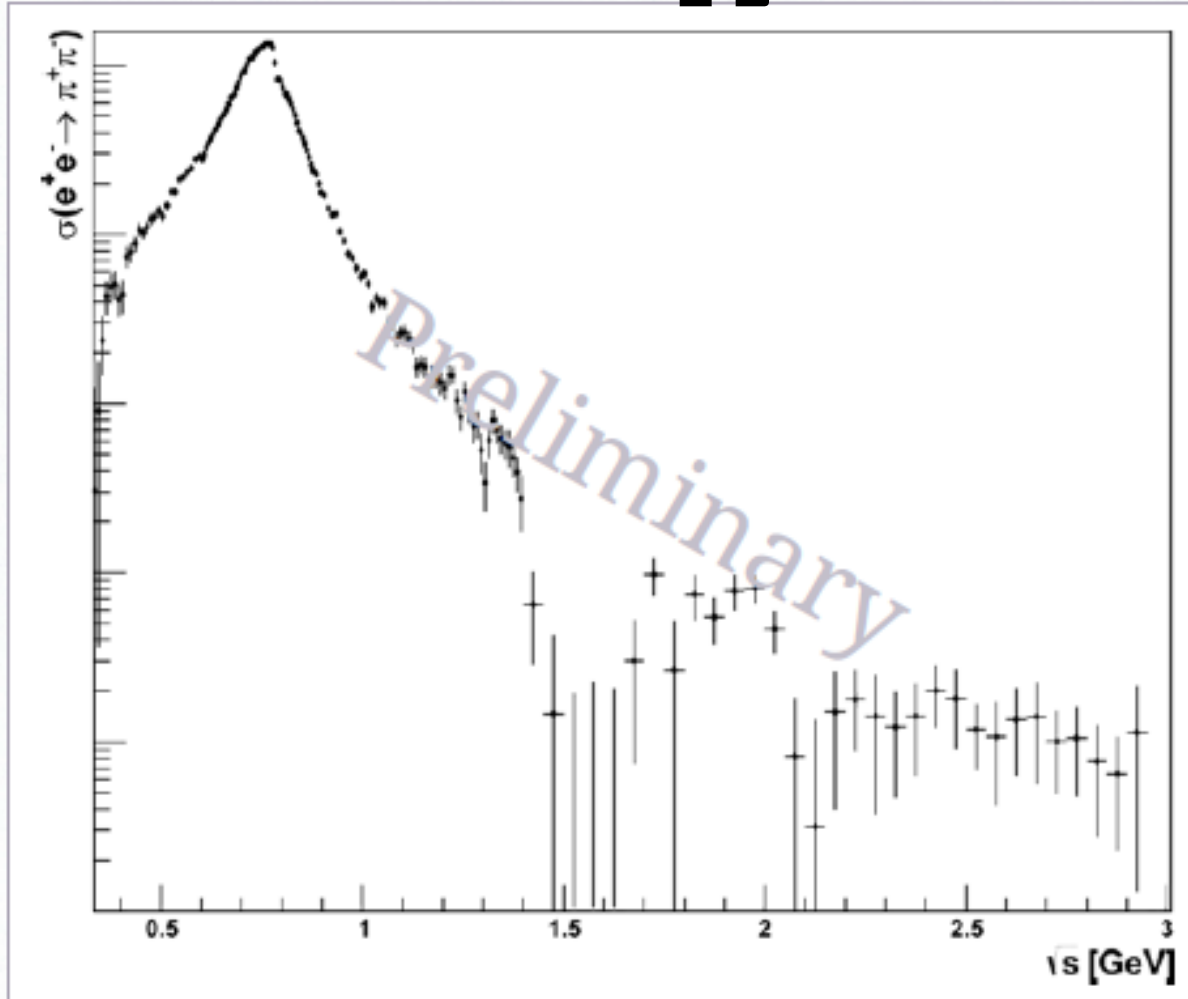
- $\sigma_E/\sqrt{E} = 2.5\%$ @ 1 GeV

Muon chamber

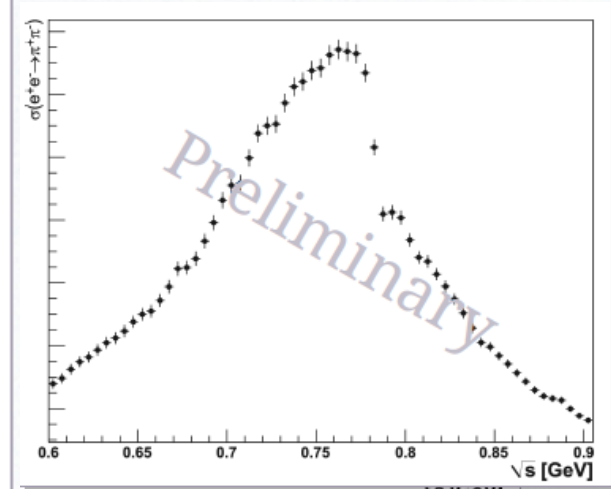
- 8-9 layers RPC



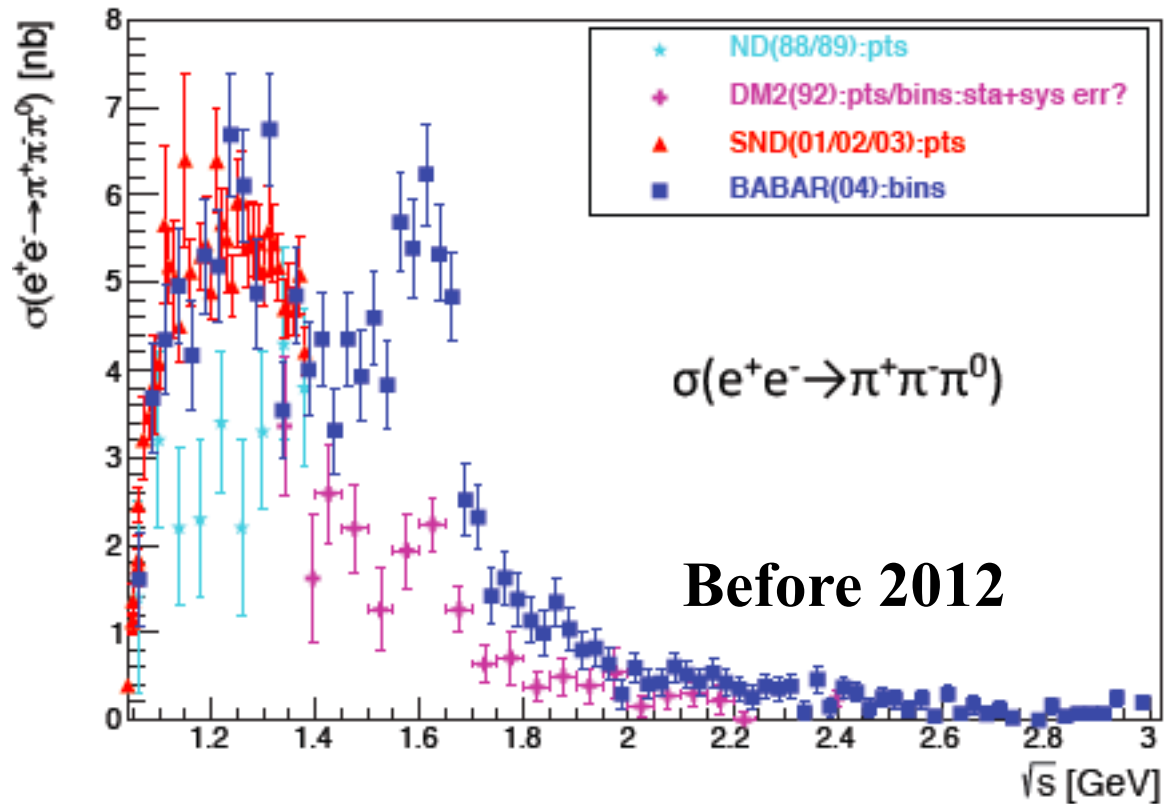
$\pi^+\pi^-$ cross section – extracted from ISR $\pi^+\pi^-\gamma$ data



- BES-III data
2.9 fb⁻¹ @ 3.770 GeV, tagged ISR
- Wide energy range
up to ~3 GeV
- No FSR correction yet



$$e^+e^- \rightarrow \pi^+\pi^-\pi^0$$



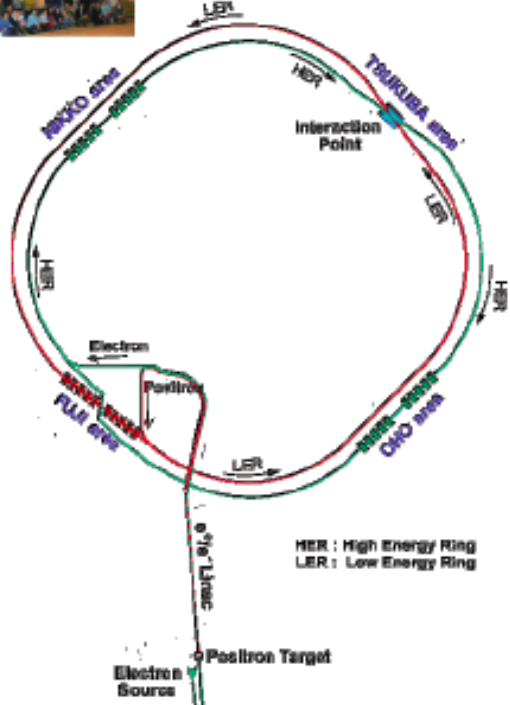
The international Belle experiment operates at a B-Factory, and uses a general purpose detector.



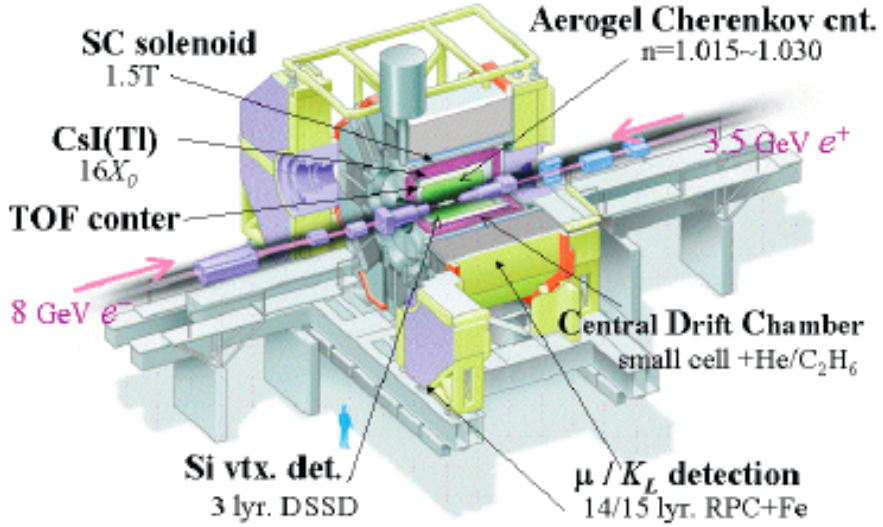
The Belle Collaboration



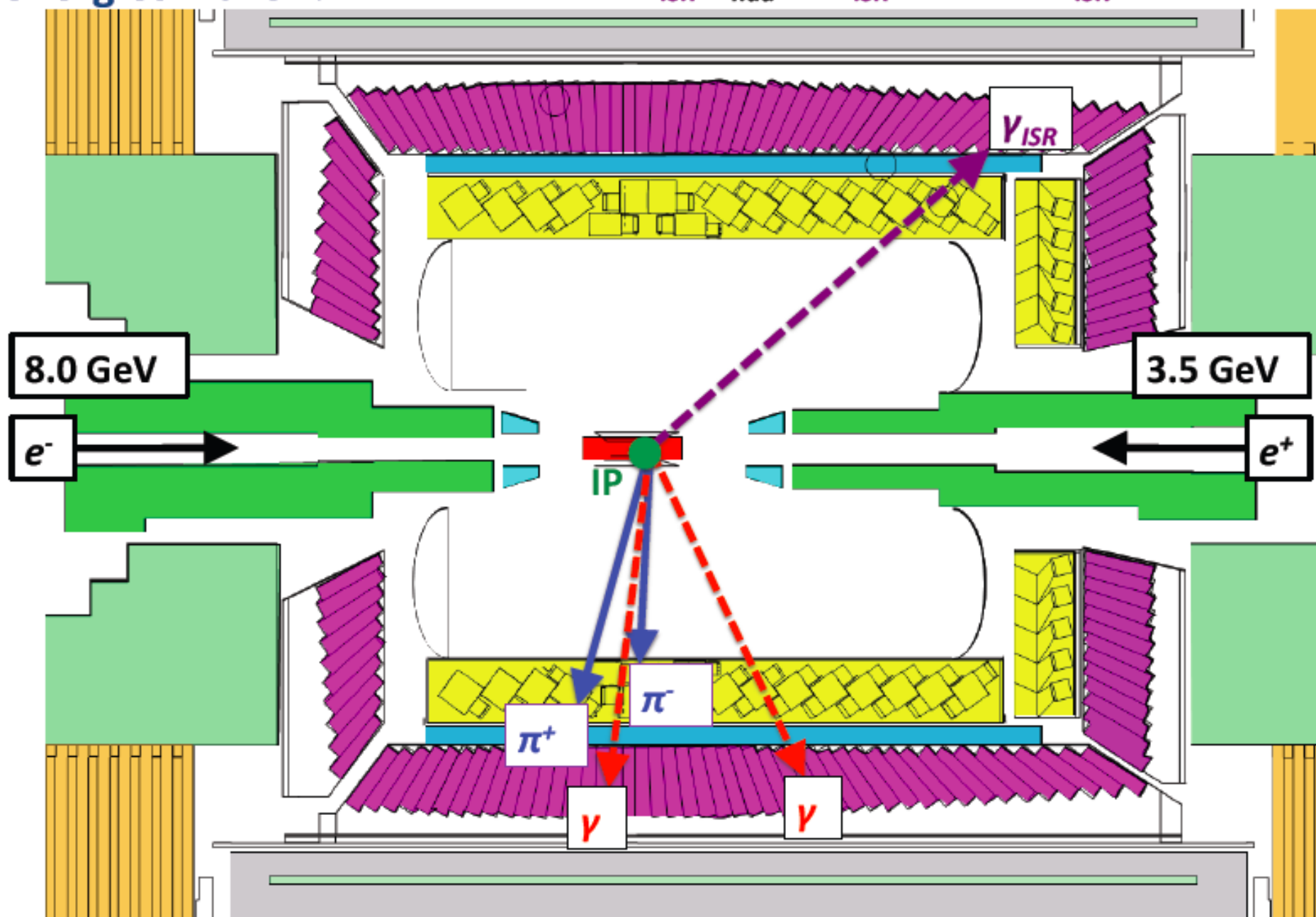
15 countries, 64 institutes, ~400 collaborators (as of Aug. 2011)



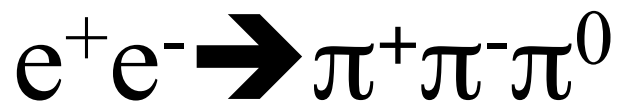
Belle Detector



Fixed-energy colliders can measure a wide range of center-of-mass energies via ISR. Example: $e^+e^- \rightarrow \gamma_{ISR} M_{had} \rightarrow \gamma_{ISR} \pi^+ \pi^- \pi^0 \rightarrow \gamma_{ISR} \pi^+ \pi^- \gamma \gamma$



Low energy (> 3 GeV) cross section measurements are focused precision measurements.

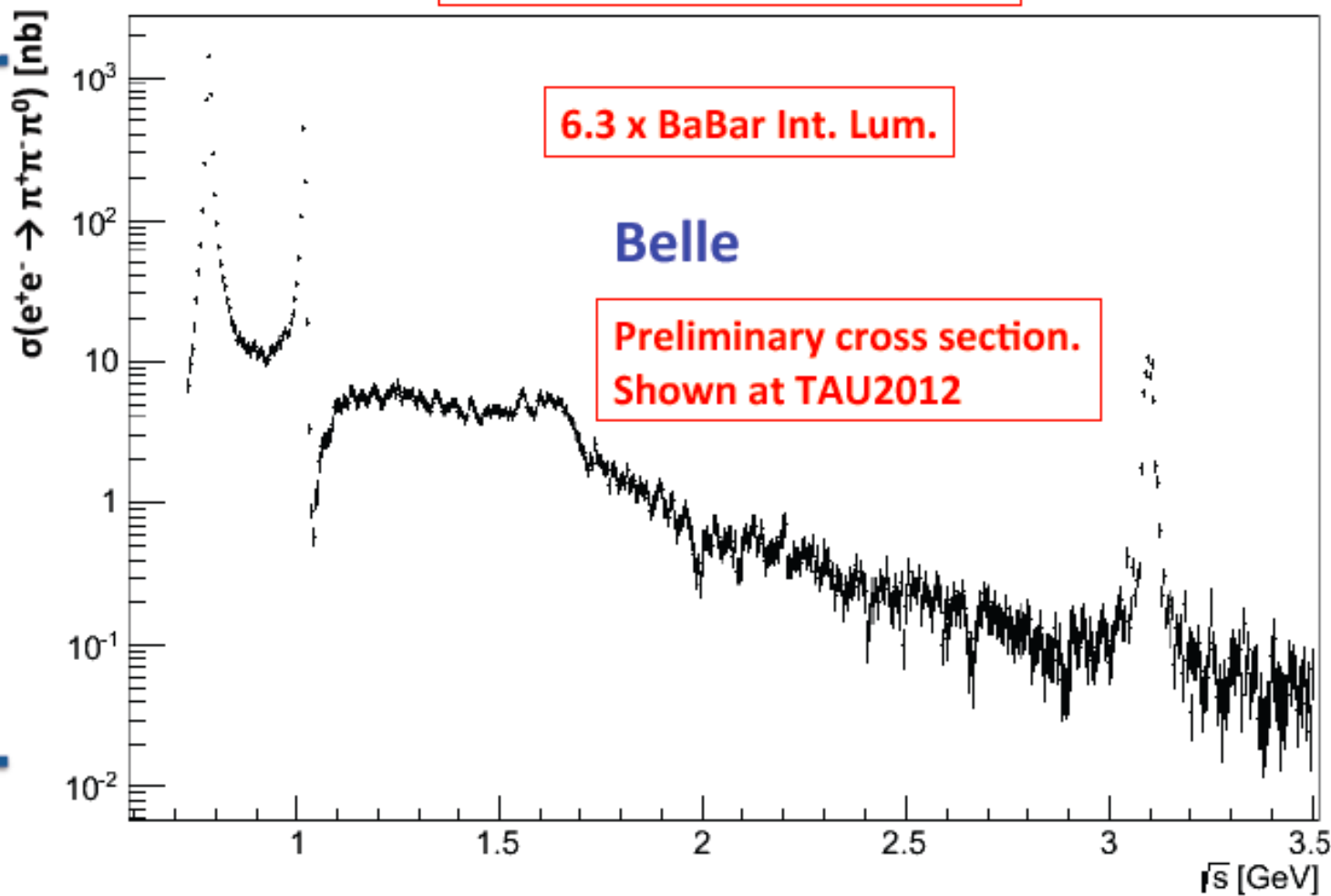


Belle systematic error goal is 5%.

6.3 x BaBar Int. Lum.

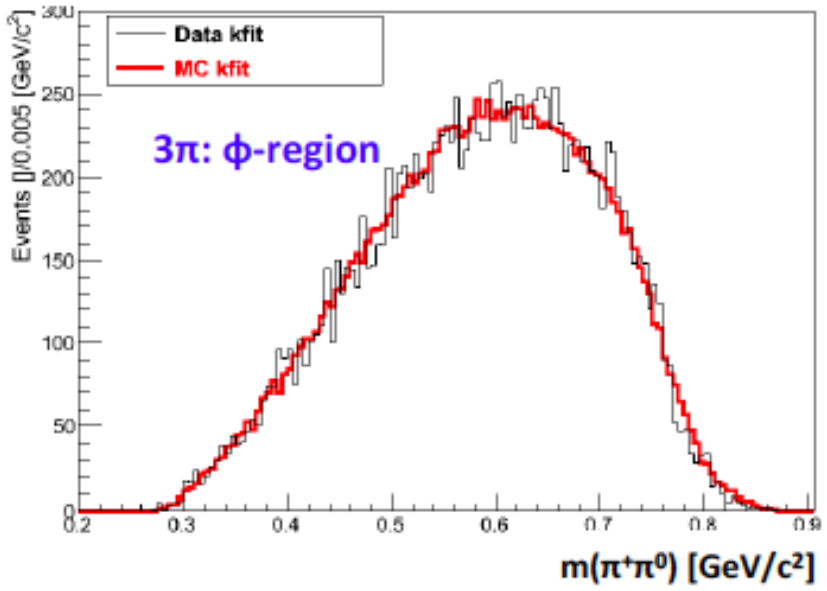
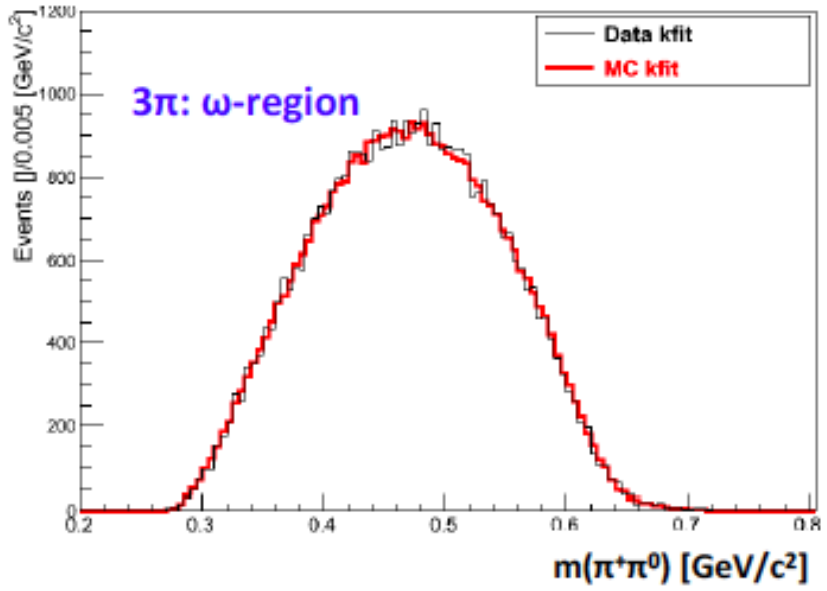
Belle

Preliminary cross section.
Shown at TAU2012

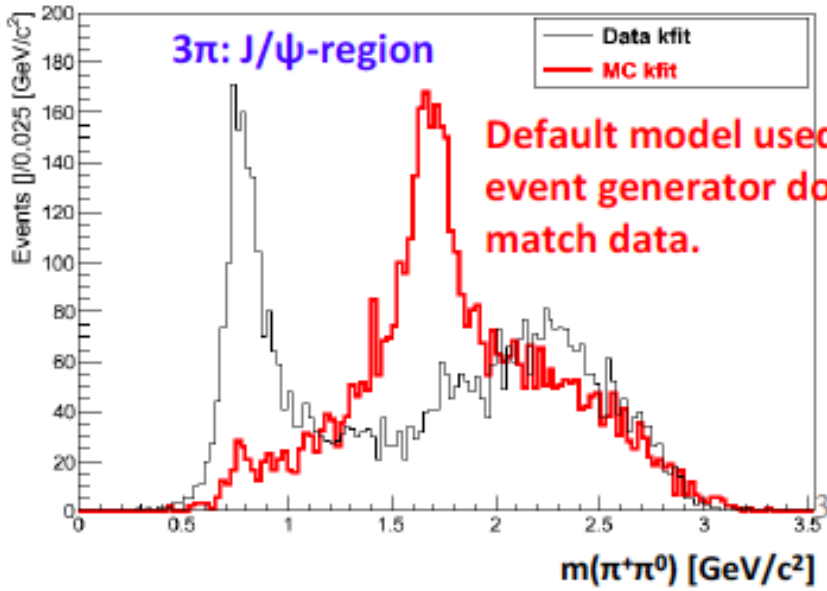
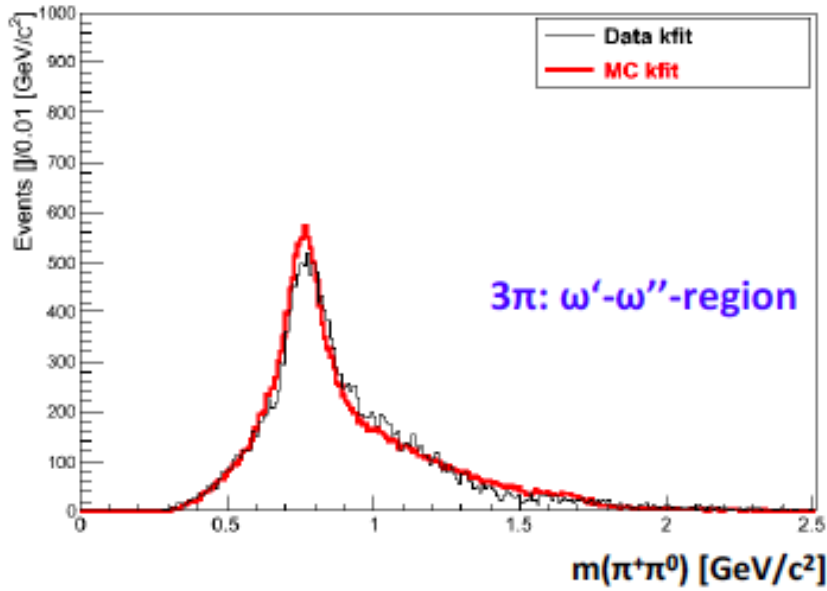


Systematic errors, background leakage, and small radiative correction checks to be completed in near future

Belle cross section measurements are also interested in looking at intermediate states.



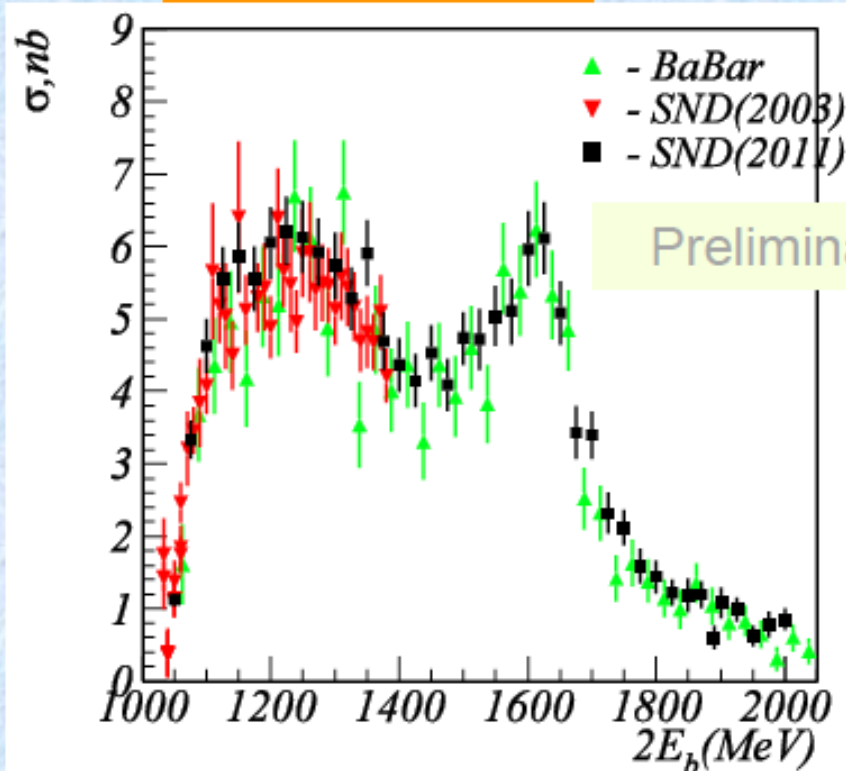
Belle $m(\pi^+\pi^0)$ distributions for $e^+e^- \rightarrow \pi^+\pi^-\pi^0\gamma_{ISR}$.





Process $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ (22pb^{-1})

Cross section



Only statistical errors

Systematic: ~5%

Selection criteria :

- 2 central charged particles
 - 2 γ 's
 - $\Delta\phi_{\text{ch.}} > 10^\circ$
 - total energy dep. $(0.3-0.8)E_{\text{beam}}$
- Kinematic fit:
- $\chi^2_{\text{R}} < 40$, $\chi^2_{\pi^+\pi^-\gamma\gamma} < 40$;
 - Fit to M_{π^0} spectrum (effect + background)

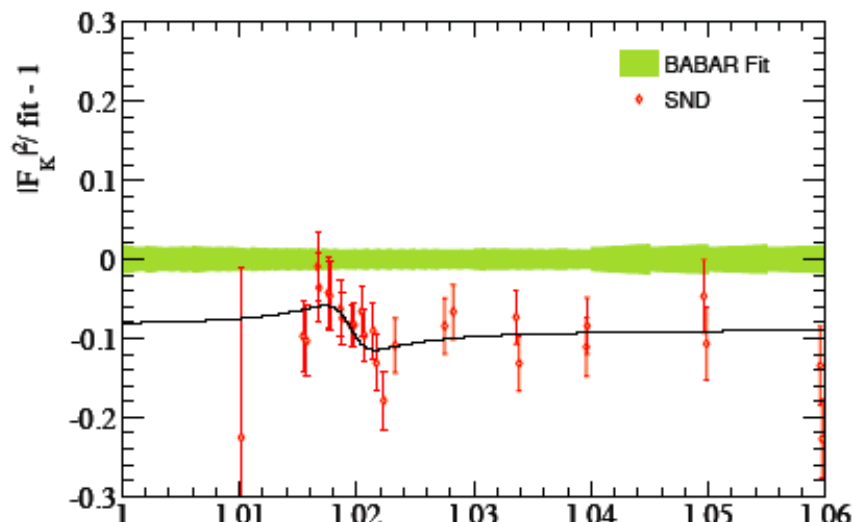
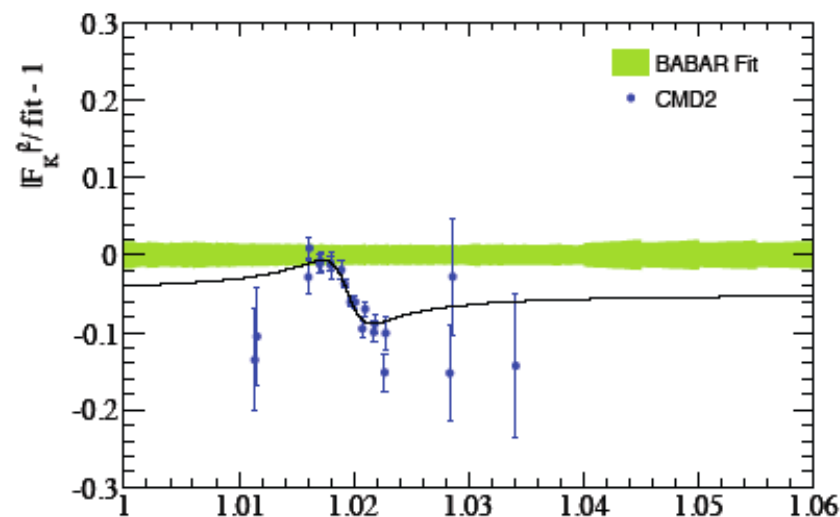
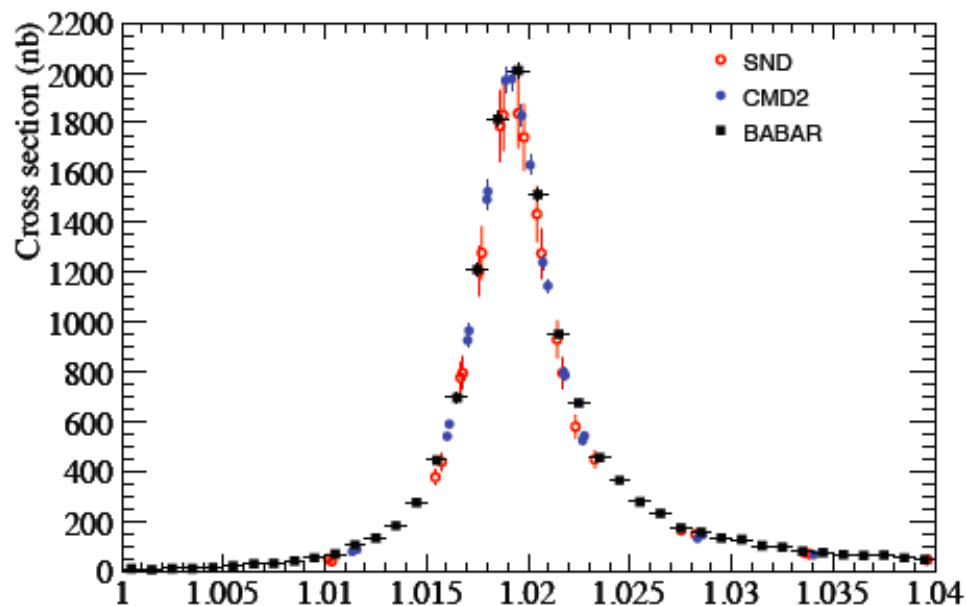
Spectrum is a sum of contributions from $\omega(782)$, $\omega'(1420)$, $\omega''(1650)$.

$$e^+e^- \rightarrow K^+K^-$$

σ_{had} : some recent new data: $K^+K^-(\gamma)$ from BaBar

arXiv:1306.3600,

- $a_\mu = 22.94 \pm 0.18 \pm 0.22$ up to 1.8 GeV vs. $21.63 \pm 0.27 \pm 0.68$ for combined previous data
- significant shift up
- may need to take into account mass shift for best combination
- Comp. plots BaBar vs Novosibirsk:



Other important channels

Motivation of ISR study at BaBar

- Low energy e^+e^- cross section dominates in hadronic contribution to $a_\mu = (g-2)/2$ of muon
- Direct e^+e^- data in 1.4 - 2.5 GeV region have very low statistic
- New inputs for the hadron spectroscopy at low masses and charmonium region

- ISR at BaBar gives competitive statistic
- BaBar has excellent capability for ISR study
- All major hadronic processes are under study (green == published)

$$e^+e^- \rightarrow 2\mu\gamma, 2\pi\gamma, 2K\gamma, 2p\gamma, 2\Lambda\gamma, 2\Sigma\gamma, \Lambda\Sigma\gamma, \Lambda_c\Lambda_c\gamma$$

$$e^+e^- \rightarrow 3\pi\gamma$$

$$e^+e^- \rightarrow 2(\pi^+\pi^-)\gamma, K^+K^-\pi^+\pi^-\gamma, K^+K^-\pi^0\pi^0\gamma, 2(K^+K^-)\gamma$$

$$e^+e^- \rightarrow 2(\pi^+\pi^-)\pi^0\pi^0\gamma, 3(\pi^+\pi^-)\gamma, K^+K^-2(\pi^+\pi^-)\gamma$$

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0\gamma, \pi^+\pi^-\pi^0\pi^0\pi^0\gamma, \pi^+\pi^-\pi^0\eta\gamma \dots$$

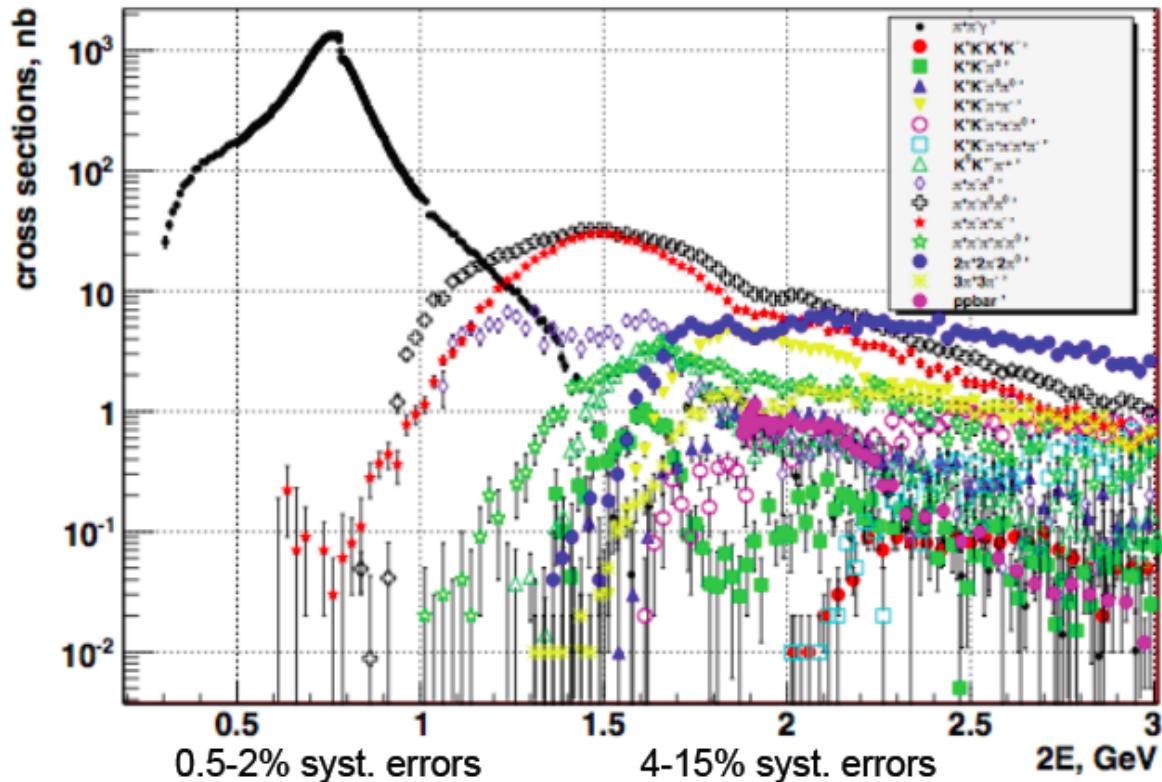
$$e^+e^- \rightarrow K^+K^-\pi^0\gamma, K^+K^-\eta\gamma \text{ (} KK^*\gamma, \phi\pi^0\gamma, \phi\eta\gamma \dots)$$

$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-\pi^0/\eta\gamma, K^+K^-\pi^+\pi^-\pi^0/\eta\gamma$$

$$e^+e^- \rightarrow KK_S\pi\pi^0/\eta\gamma, K_S K_L, K_S K_L \pi^+\pi^-, K_S K_S \pi^+\pi^-(K^+K^-)$$

Some reactions are being updated to full BaBar data with $\sim 500\text{fb}^{-1}$
(talk by V. Druzhinin on $e^+e^- \rightarrow 2p\gamma$)

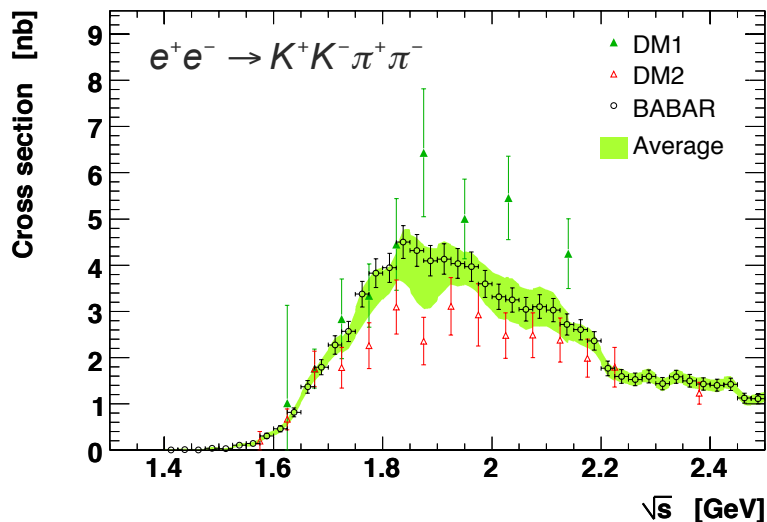
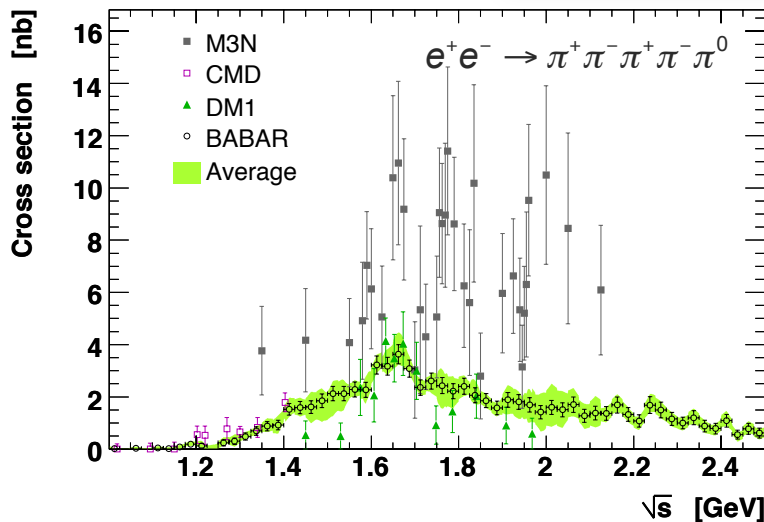
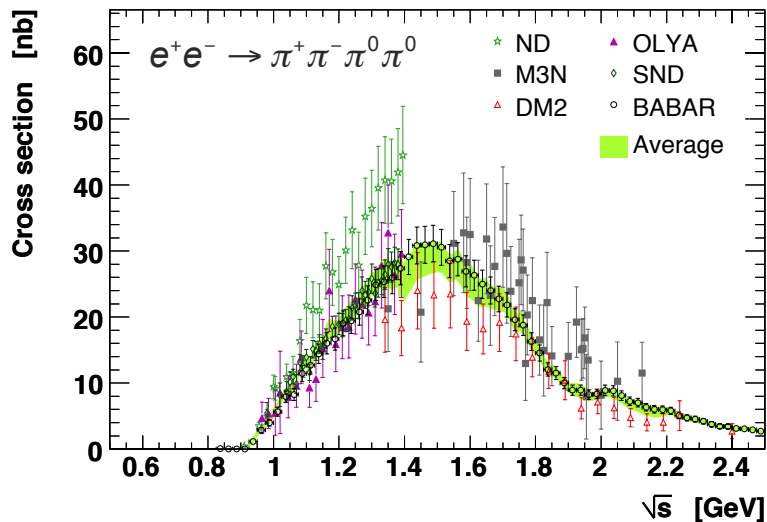
BaBar measurements summary



To calculate R in the energy range 1-2 GeV the processes $\pi^+\pi^-3\pi^0$, $\pi^+\pi^-4\pi^0$, $K_S K_L$, $K_S K_L \pi\pi$, $K_S K^+ \pi^-\pi^0$ are under study. The $\pi^+\pi^-2\pi^0$ is still preliminary. Work is in progress.

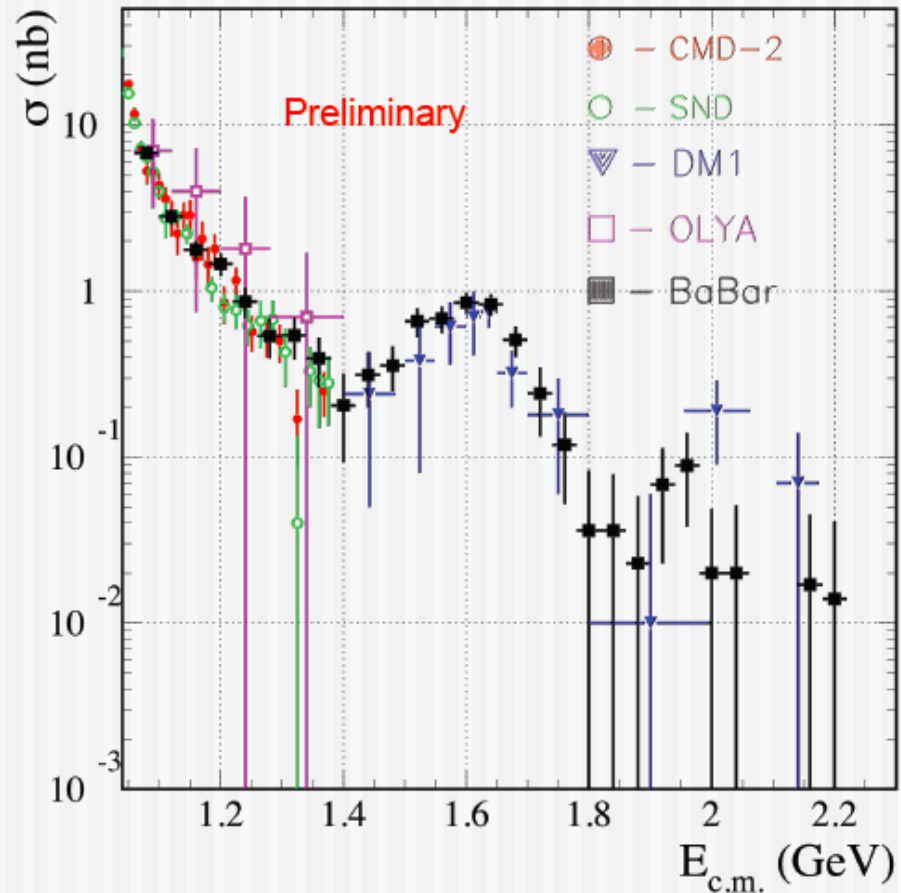
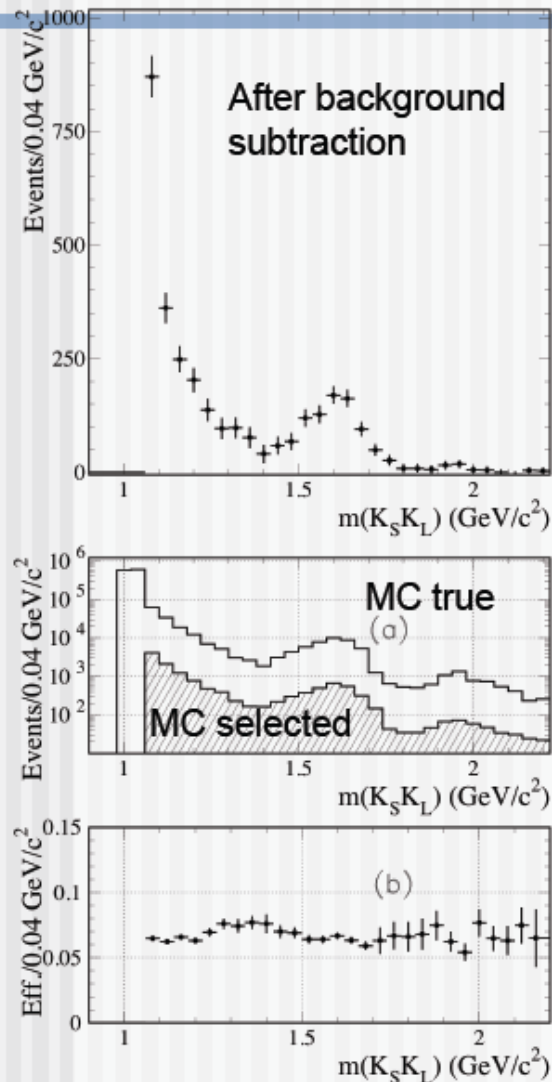
Multihadron channels between 1 and 2.5 GeV

Davier *et al.*, EPJ C 71, 1515 (2011)



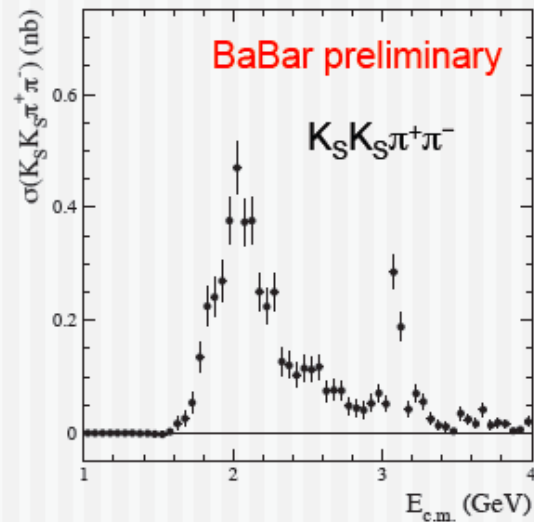
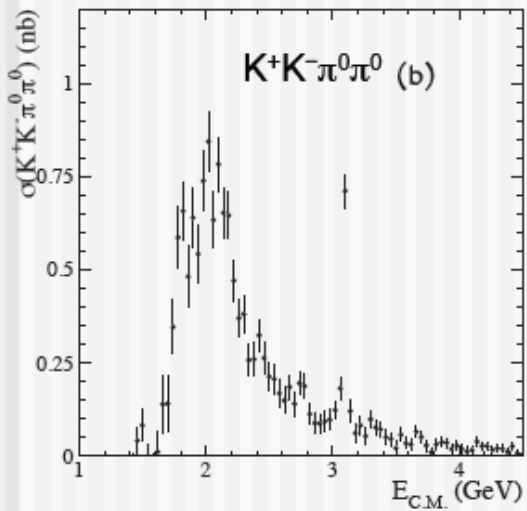
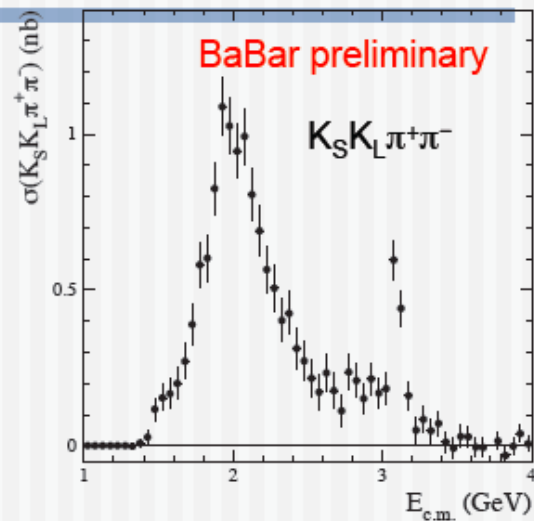
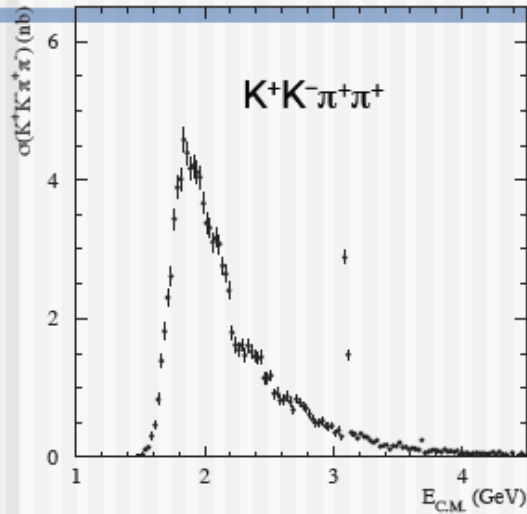
BABAR measured (almost) all the exclusive $e^+e^- \rightarrow$ hadrons modes
Many inconsistencies resolved
Huge impact on hadronic vacuum polarisation calculation

$e^+e^- \rightarrow K_S K_L$ cross section



Systematic error $\sim 10\%$ ($\sim 30\%$ for $\sigma < 0.3 \text{ nb}$),
dominated by background subtraction procedure.

The cross sections comparison



$K^+K^-\pi^+\pi^+$ vs. $K^+K^-\pi^0\pi^0$ vs. $K_S K_L \pi^+\pi^-$ vs. $K_S K_S \pi^+\pi^-$

Only $K^*(892)^+K^*(892)^-$ contribution can be compared using iso-spin relations:

$$N(K^+K^-\pi^+\pi^-) = 548 \pm 263 \quad \text{eff} = 22\% \quad (K^*(892)^0 K^*(892)^0)$$

$$N(K^+K^-\pi^0\pi^0) = 1750 \pm 60 \quad \text{eff} = 8\%$$

$$N(K_S K_L \pi^+\pi^-) = 2098 \pm 209 \quad \text{eff} = 5\%$$

$$N(K_S K_S \pi^+\pi^-) = 742 \pm 104 \quad \text{eff} = 4.5\%$$

E. Solodov,
Phipsi13, Rome,
9-12 September 2013

Iso-spin relations: ArXiv:1010.4180 (Davier)

$$N(K^+K^-\pi^0\pi^0) = \frac{1}{4} N(K^0 \underline{K}^0 \pi^+\pi^-)$$

$$N(K_S K_L \pi^+\pi^-) = \frac{1}{2} N(K^0 \underline{K}^0 \pi^+\pi^-)$$

$$N(K_S K_S \pi^+\pi^-) = N(K_L K_L \pi^+\pi^-) = \frac{1}{4} N(K^0 \underline{K}^0 \pi^+\pi^-)$$

Should be (after efficiency correction) :

$$2188 \pm 76 \quad \sim \quad 2098 \pm 209 \quad \sim \quad 1648 \pm 232$$

Some tension (~ 2 sigma)

30%

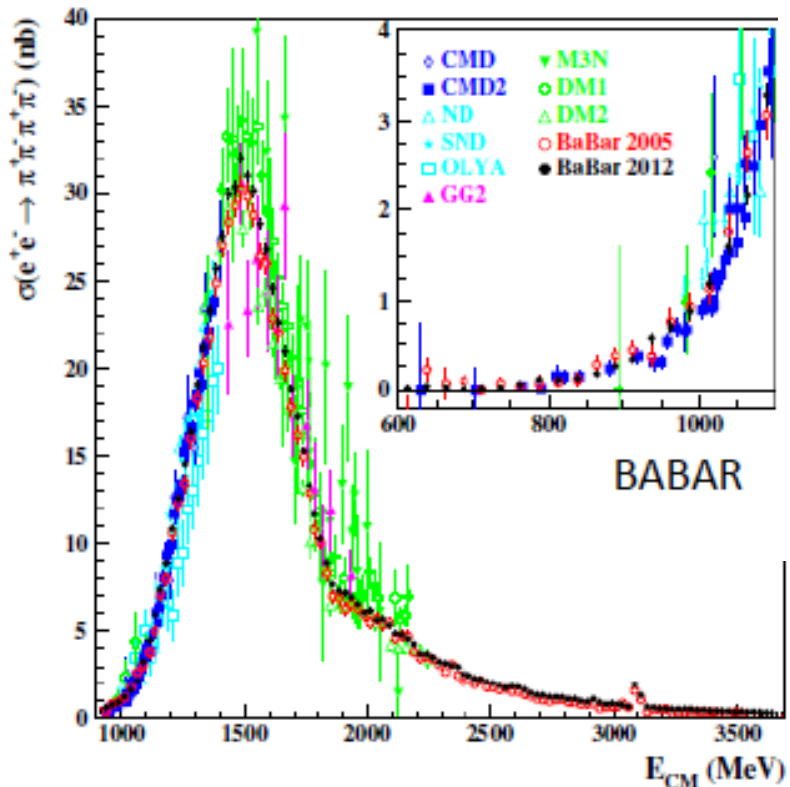
63%

50%

of all events – how the rest are related?
to g-2 relation?

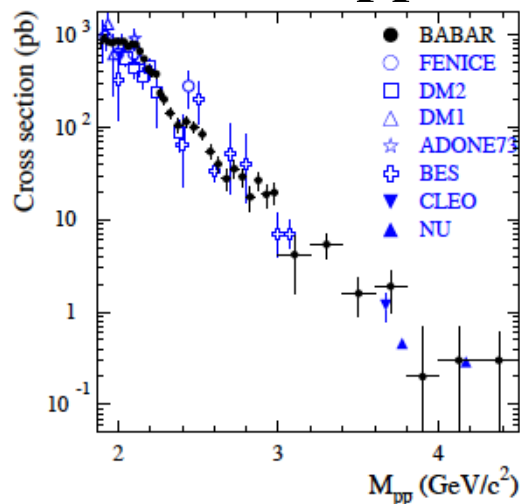
New cross section results

$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-(\gamma)$$



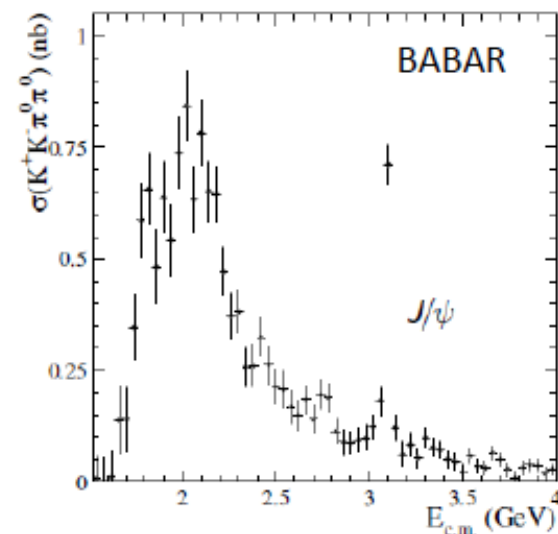
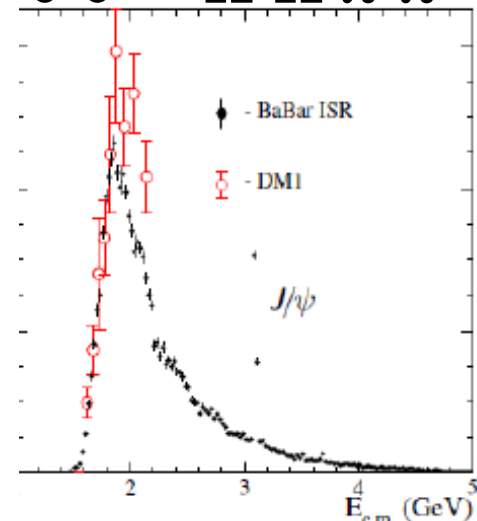
- < 1.4 GeV: agreement with previous *BABAR* results, SND and CMD-2 data
- > 1.4 GeV: highest precision (DM2, 20%)

$$e^+e^- \rightarrow p\bar{p}$$



**Systematic uncertainties
btw 2-15%**

$$e^+e^- \rightarrow K^+K^-\pi^+\pi^-$$



$$e^+e^- \rightarrow K^+K^-\pi^0\pi^0$$

Physics program

CMD3

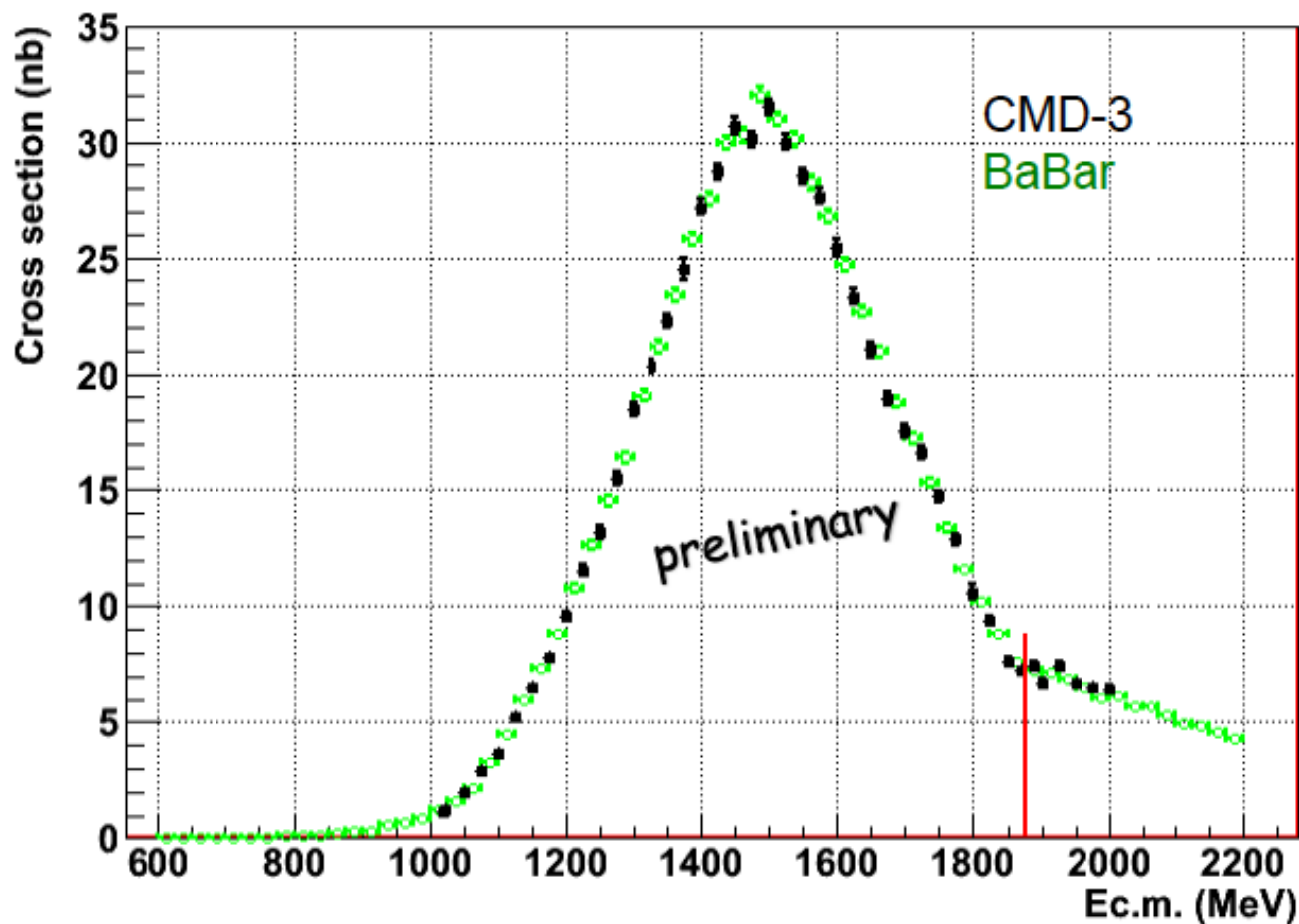
1. Precision measurement of $R = \sigma(e^+e^- \rightarrow \text{hadrons}) / \sigma(e^+e^- \rightarrow \mu^+\mu^-)$
exclusive approach, up to <1% for major modes
2. Study of hadronic final states:
$$e^+e^- \rightarrow 2h, 3h, 4h, \dots \quad h = \pi, K, \eta$$
3. Study of vector mesons and their excitations:
$$\rho', \rho'', \omega', \phi', \dots$$
4. Comparison of cross-sections $e^+e^- \rightarrow \text{hadrons} (T = 1)$ with spectral functions of τ -decays
5. Study of nucleon electromagnetic formfactor at threshold
$$e^+e^- \rightarrow p\bar{p}, n\bar{n}$$
6. Measurement of the cross-sections using ISR
7. Study of higher order QED processes

Overall, we plan to collect $0.5 \div 1$ 1/fb

Similar for SND

$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-$$

CMD3



Statistical errors 1-2% per point, systematics under study
Dynamics: confirm $a_1(1260)\pi$ dominance, $\rho f_0(600)$, $\rho f_0(980)$ are seen

$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-\pi^+\pi^-$$

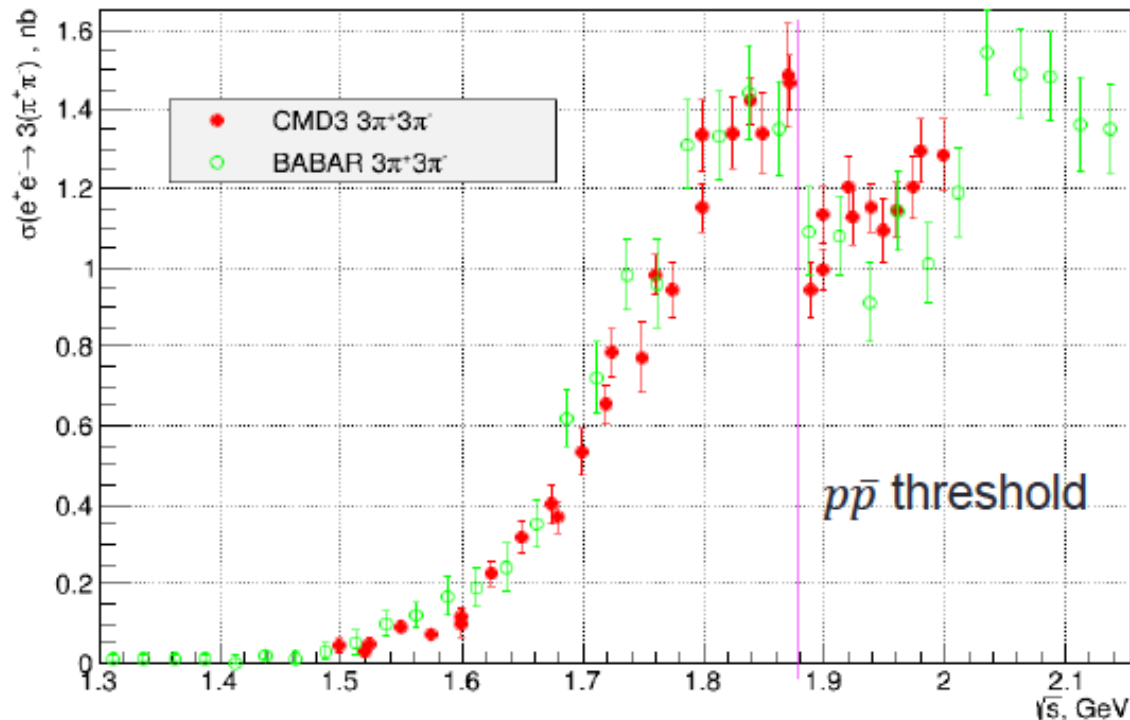
CMD3

First result, published by
CMD-3:

Phys.Lett. B723 (2013)
82-89

Based on about 22 1/pb,
8000 events selected

Systematic error is 6%,
main source is model
dependence, will be
reduced with more
statistics



Preliminary studies of dynamics:

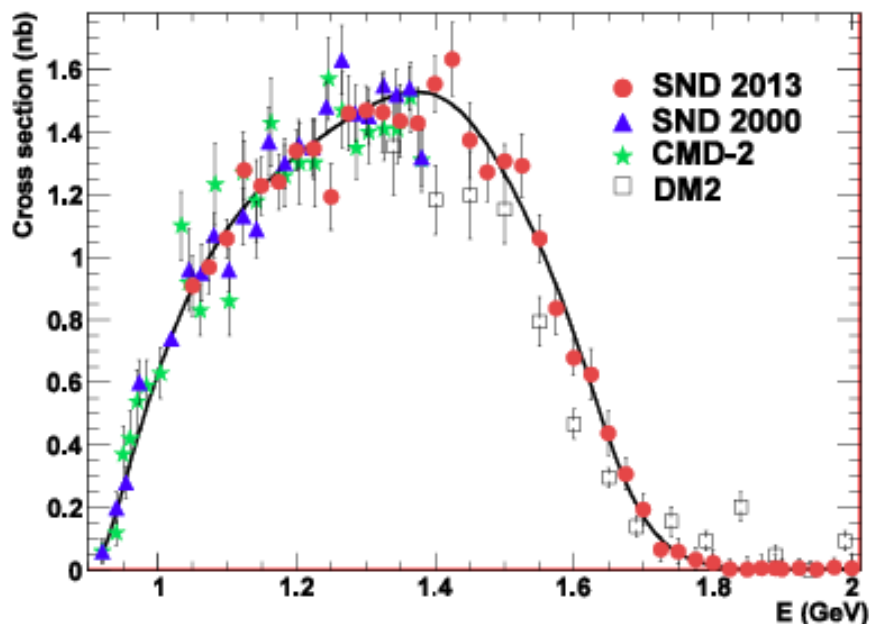
- Main production mode: $\rho(770) + 4\pi$ (phase space or $f_0(1370)$)
- Hint of energy dependent dynamics in 1.7-1.9 GeV energy range



Process $e^+e^- \rightarrow \omega\pi^0 \rightarrow \pi^0\pi^0\gamma$ (30 pb^{-1})

(arXiv:1303.5198[hep-ex])

The most accurate measurement for $2E > 1.4 \text{ GeV}$



Systematic error: 3.4%
($2E < 1.55 \text{ GeV}$)

Fit:
sum of $\rho(770)$, $\rho'(1450)$, $\rho''(1700)$

Selection criteria:

$\geq 5 \gamma$; no charged particles;
total energy depos. $> E_{\text{beam}}$;

kinematic fits:

$$\chi^2_{5\gamma} < 30; \chi^2_{\pi^0\pi^0\gamma} - \chi^2_{5\gamma} < 10;$$

$$|M_{\pi^0\gamma} - M_{\omega}| < 100 \text{ MeV}$$

SND using CVC hypothesis:

$$\text{Br}(\tau^- \rightarrow \omega\pi^- \nu_\tau) = (1.96 \pm 0.02 \pm 0.10)\%$$

PDG:

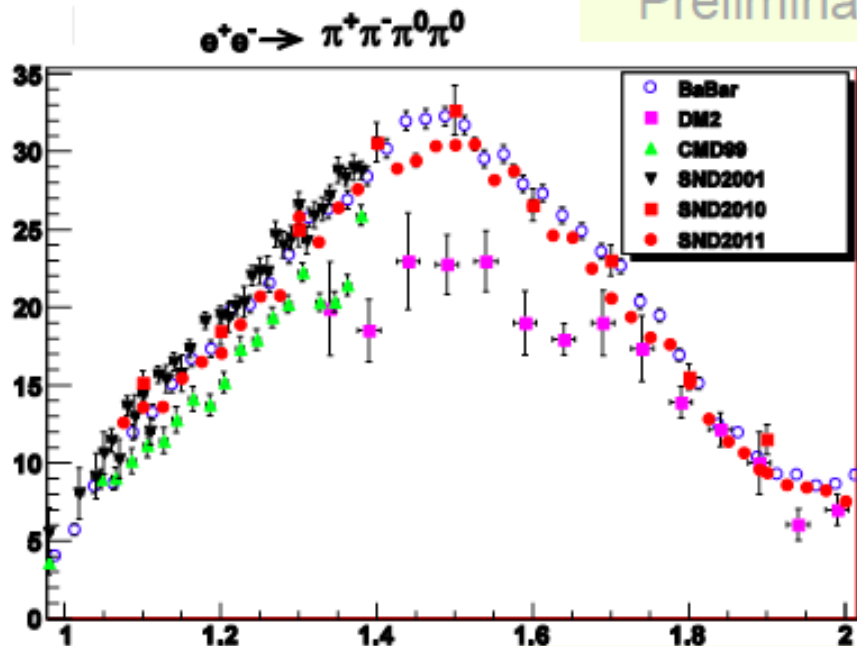
$$\text{Br}(\tau^- \rightarrow \omega\pi^- \nu_\tau) = (1.95 \pm 0.08)\%$$

No difference within experimental accuracy.



Process $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$ (30pb^{-1})

Preliminary



Only statistical errors

Systematics $\leq 10\%$

The bump is a sum of contributions of $\rho(770)$, $\rho'(1450)$, $\rho''(1700)$.

Main feature – many intermediate states: $\omega\pi^0$, $a_1\pi$, $\rho\pi\pi$, $\rho^+\rho^-$, ρf_0 .

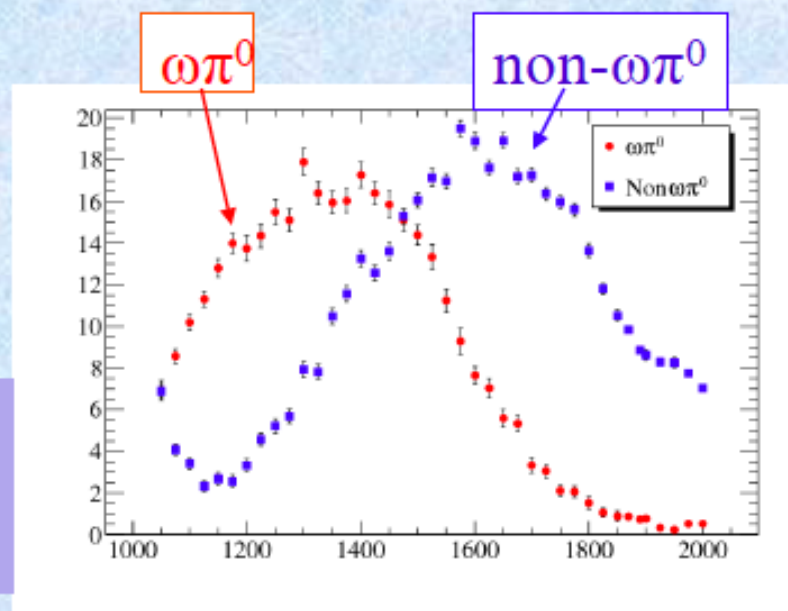
Selection criteria :

- at least 2 charged particles and 4 γ 's;
- 2 tracks are from IP;

Kinematic fit:

$$\chi^2 < 40$$

M_{π^0} in 70-200 MeV.



BES dominates the precision between 2 and 5 GeV

• BESII @ BEPC, Beijing (inclusive measurement) $2 < E_{cm} < 5 \text{ GeV}$

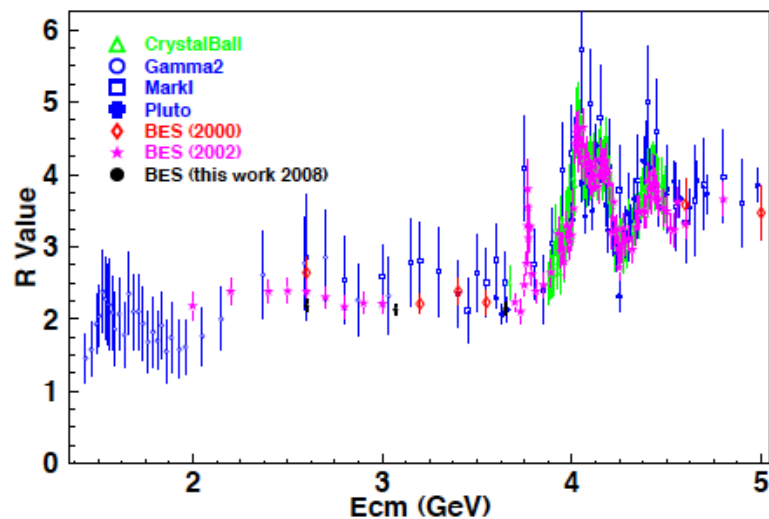
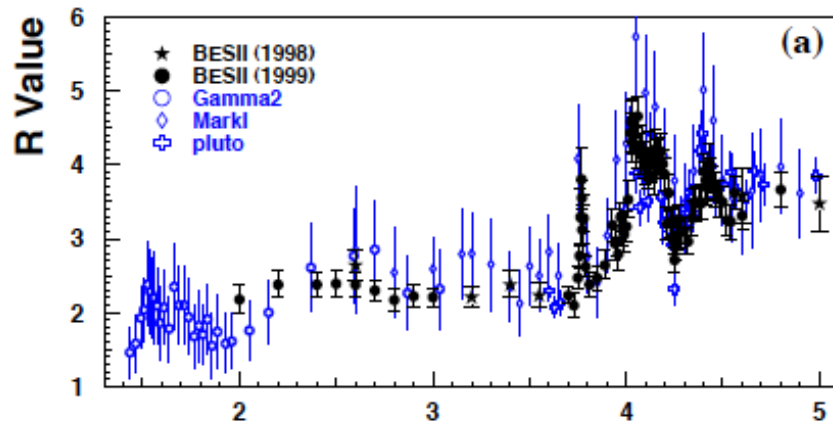
-1998/99 new result of R in $2 < E_{cm} < 5 \text{ GeV}$ from BESII, 91 points with $\sigma_R/R \sim 7\%$
(improvement of a factor 2)

2008: 3 points (2.6, 3.07 and 3.65 GeV)
with 3.5% precision

$$R = \frac{N_{had}^{obs} - N_{bg} - \sum_l N_{ll} - N_{\gamma\gamma}}{\sigma_{\mu\mu}^0 \cdot L \cdot \epsilon_{trg} \cdot \bar{\epsilon}_{had} \cdot (1 + \delta)},$$

TABLE II. Contributions to systematic errors: experimental selection of hadronic events, luminosity determination, theoretical modeling of hadronic events, trigger efficiency, radiative corrections and total systematic error. All errors are in percentages (%).

E_{cm} (GeV)	hadron selection	L	M.C. modeling	trigger	radiative correction	total
2.000	7.07	2.81	2.62	0.5	1.06	8.13
3.000	3.30	2.30	2.66	0.5	1.32	5.02
4.000	2.64	2.43	2.25	0.5	1.82	4.64
4.800	3.58	1.74	3.05	0.5	1.02	5.14

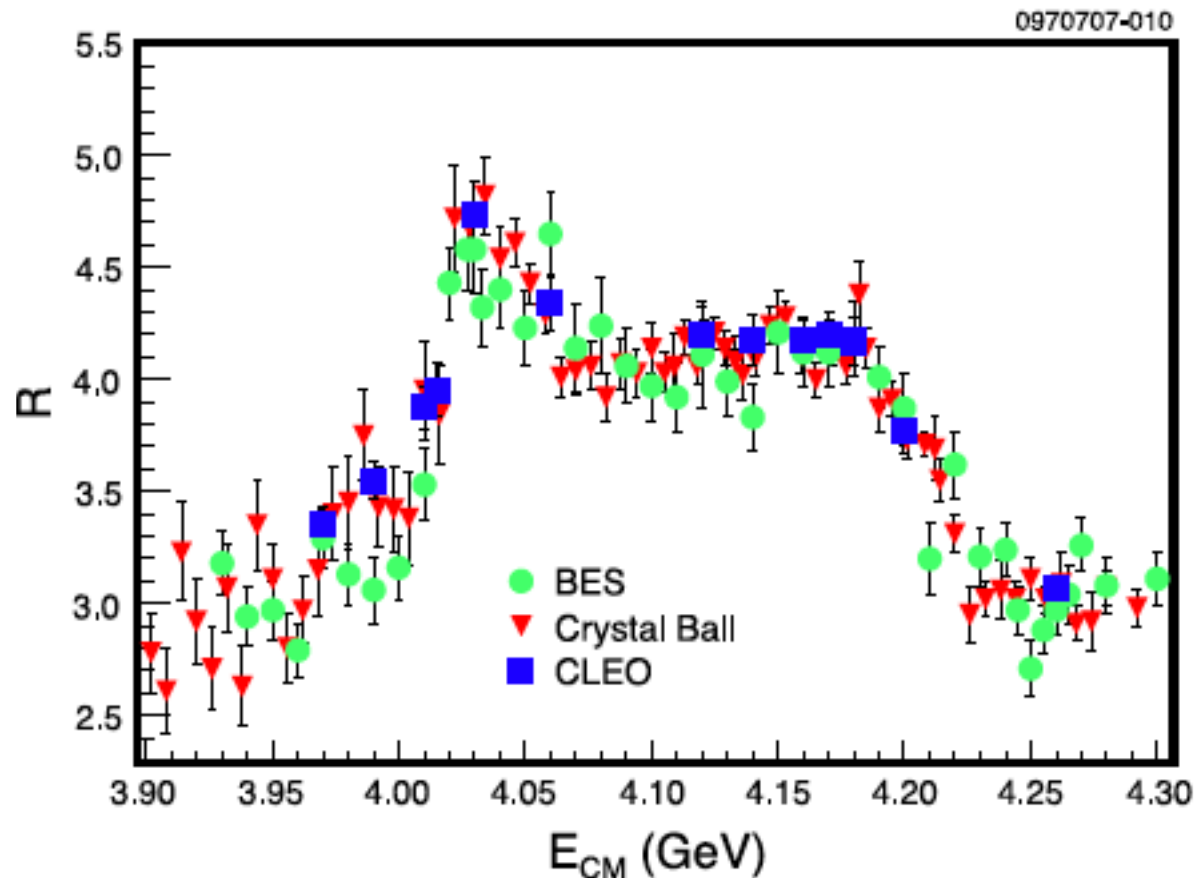


R measurement at CLEO

•CLEO@ CESR, Ithaca (inclusive measurement) $3.9 < E_{cm} < 4.3 \text{ GeV}$

-New result on R (inclusive measurement) in $3.97 < E_{cm} < 4.26 \text{ GeV}$ (above the open charm threshold) with a δ_{sys} between 5.2 and 6.1%. In agreement with the sum of exclusive measurement and previous experiments

Energy (MeV)	R (ISR-corrected)
3970	$3.36 \pm 0.04 \pm 0.05$
3990	$3.55 \pm 0.05 \pm 0.06$
4010	$3.88 \pm 0.04 \pm 0.08$
4015	$3.95 \pm 0.08 \pm 0.08$
4030	$4.74 \pm 0.07 \pm 0.12$
4060	$4.34 \pm 0.05 \pm 0.10$
4120	$4.21 \pm 0.06 \pm 0.10$
4140	$4.18 \pm 0.04 \pm 0.10$
4160	$4.18 \pm 0.03 \pm 0.10$
4170	$4.20 \pm 0.01 \pm 0.10$
4180	$4.17 \pm 0.04 \pm 0.10$
4200	$3.77 \pm 0.05 \pm 0.08$
4260	$3.06 \pm 0.02 \pm 0.04$



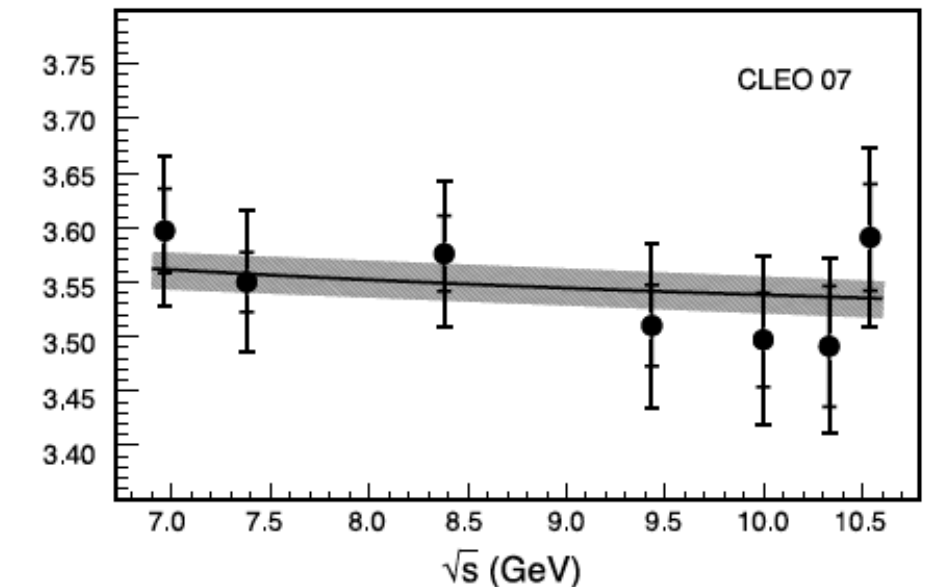
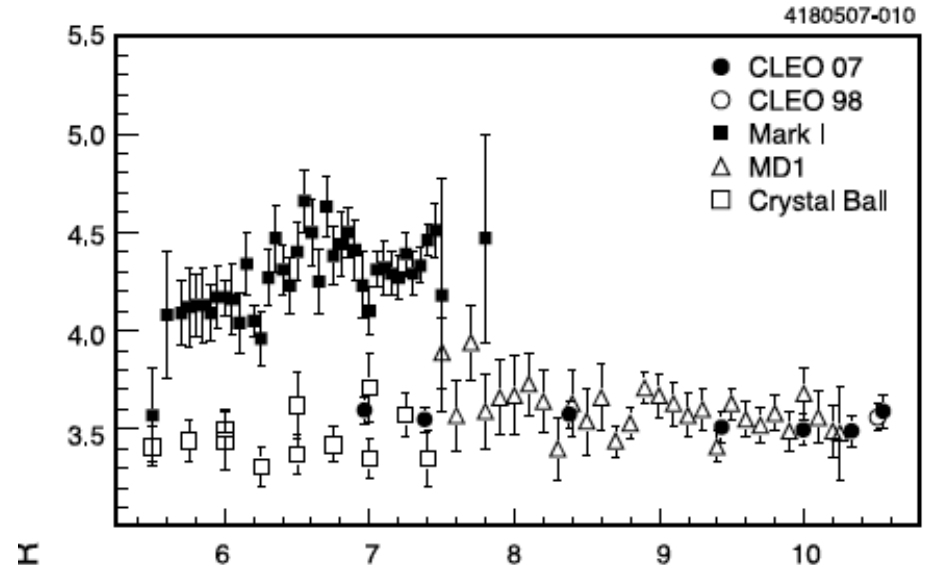
R measurement at CLEO

• CLEO@ CESR, Ithaca (inclusive measurement) $6.9 < E_{cm} < 10.5 \text{ GeV}$

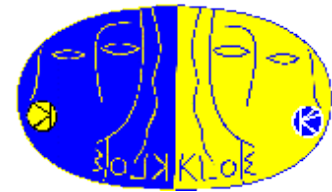
-New result on R (inclusive measurement) in $6.964 < E_{cm} < 10.538 \text{ GeV}$ (7 points) with a δ_{sys} of $\sim 2\%$. In agreement with previous experiments (but MARKI) and pQCD ($\Lambda=0.31 \text{ GeV}$)

$$R = \frac{N_{had}(1-f)}{\mathcal{L}\epsilon_{had}(1+\delta)\sigma_{\mu\mu}^0},$$

$\epsilon(1+\delta)$	1%
L	1%
Bckg/Hadr Modeling	0.7%
Dataset variation	0.3%
TOTAL	1.8%



$$a_\mu = (g_\mu - 2)/2:$$



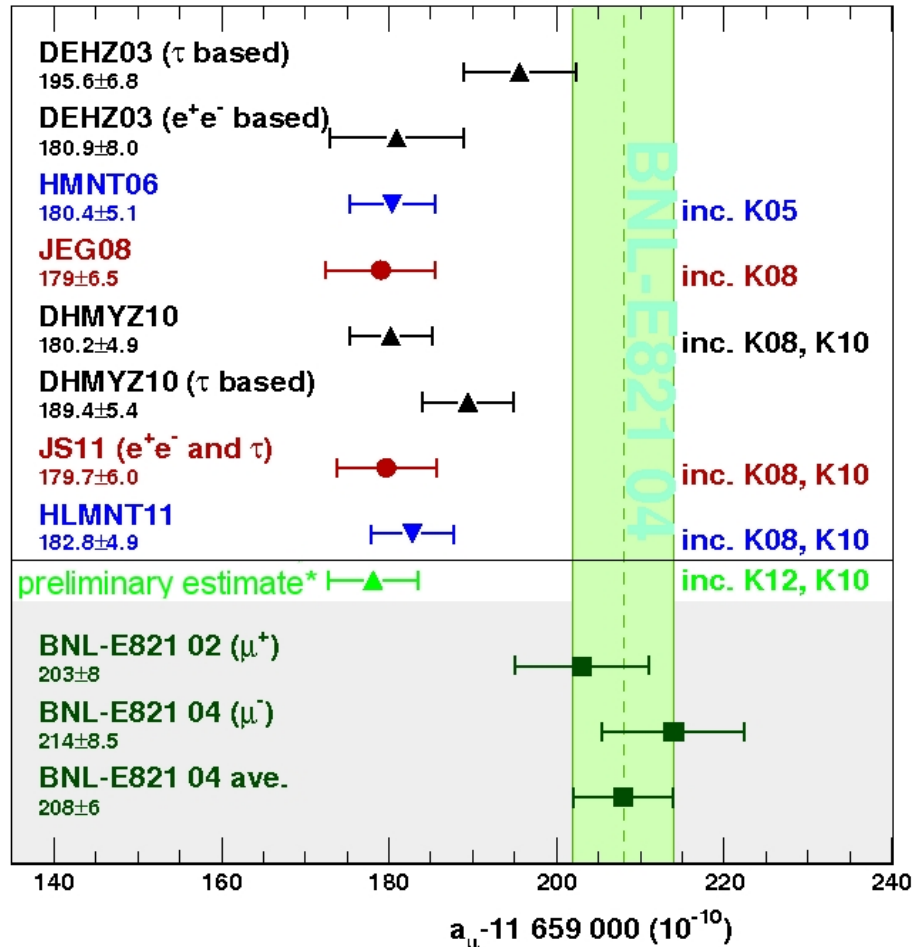
Theoretical predictions compared to the BNL result

- The latest inclusion of all e^+e^- data gives a discrepancy btw a_μ^{SM} and a_μ^{EXP} of 3 to 4σ

- Some differences on $\sigma_{\pi\pi}$ btw different experiments (mainly KLOE/BaBar) to be clarified [$\Delta a_\mu^{\text{EXP-SM}} = 2.4 \div 3.7\sigma$]

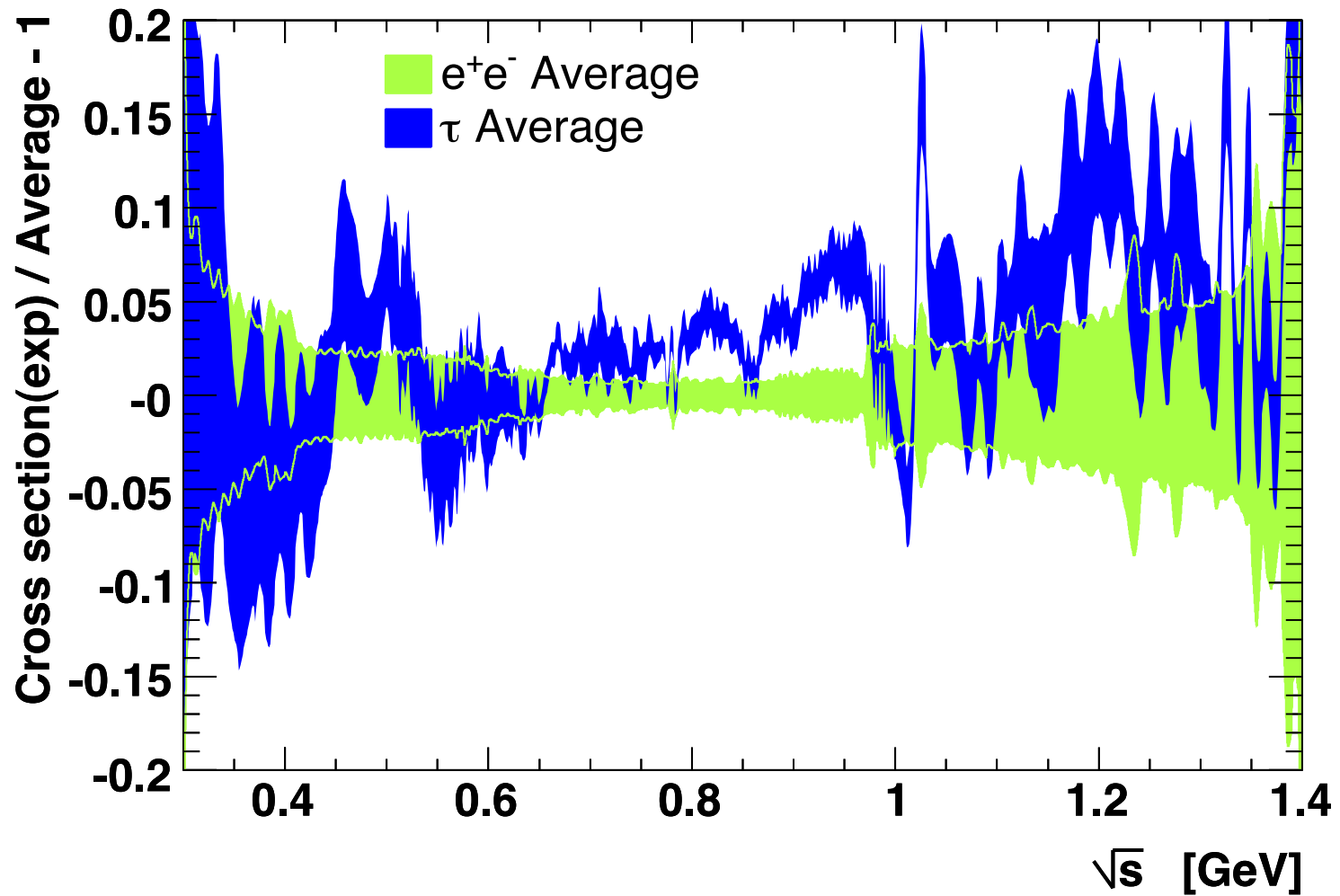
- (Reduced) discrepancy btw ee and τ data (new l. corr., ee, τ data). JS11 claims to have solved it

- Very important the new $g-2$ experiments (at FNAL and JPARC)!



* Our extrapolation based on DHMYZ10

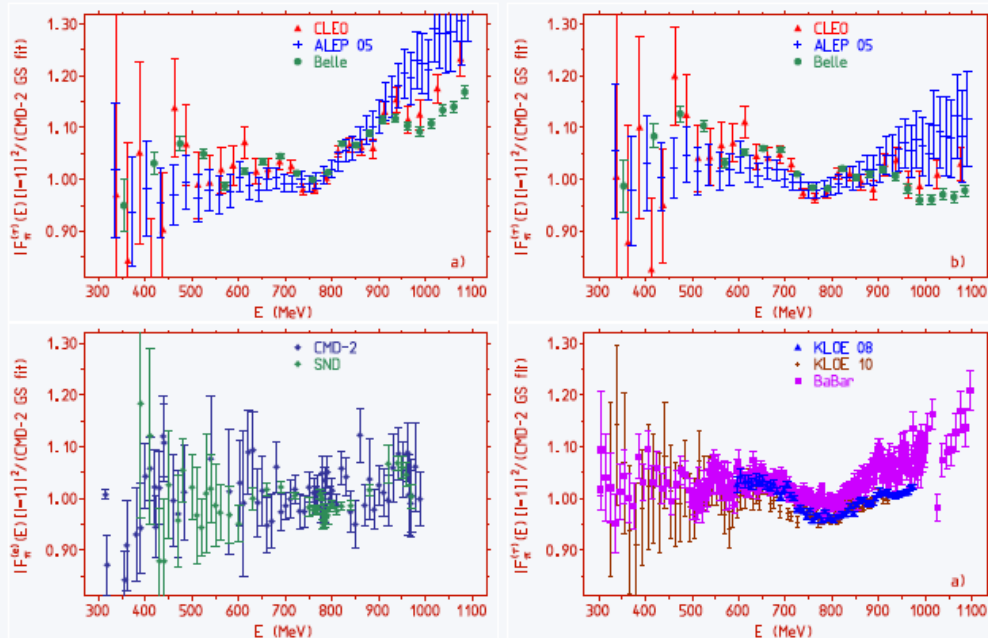
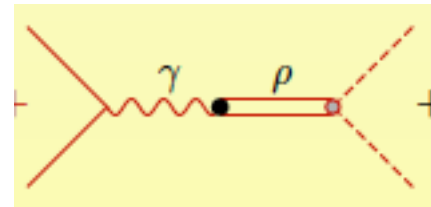
Two-pion e^+e^- vs τ spectral functions



Missing isospin corrections and/or problems with data? Additional data are needed. Meanwhile...

Jegerlehner and Szafron claim that the e^+e^- vs τ is solved if an additional correction (ρ - γ loop mix.) is included

F. Jegerlehner and R. Szafron, Eur. Phys. J. C71 (2011) 1632



$|F_\pi(E)|^2$ in units of $e^+e^- l=1$ (CMD-2 GS fit): a) τ data uncorrected for ρ - γ mixing, and b) after correcting for mixing. Lower panel: e^+e^- energy scan data [left] and e^+e^- radiative return data [right]

τ decays			
Belle			25.24 ± 0.39
CLEO			25.44 ± 0.44
ALEPH			25.49 ± 0.13
DELPHI			25.31 ± 0.24
L3			24.62 ± 0.61
OPAL			25.46 ± 0.34
τ average			25.42 ± 0.10
$e^+e^- + \text{CVC}$			
CMD2 03			25.03 ± 0.29
CMD2 06			24.94 ± 0.31
SND 06			24.90 ± 0.36
KLOE 08			24.64 ± 0.29
e^+e^- average			24.78 ± 0.28
KLOE 10			24.56 ± 0.34
BABAR 09			25.15 ± 0.28
PDG average			25.51 ± 0.09
		$B(\tau \rightarrow \pi\pi^0\nu_\tau)$	24 25 26 27 %

$$a_\mu^{\text{had,LO}}[e, \tau] = 690.96(1.06)(4.63) \times 10^{-10} \quad (e + \tau)$$

$$a_\mu^{\text{had,LO}}[e^+e^-] = (692.3 \pm 4.2_{ee+\text{QCD}}) \times 10^{-10}$$

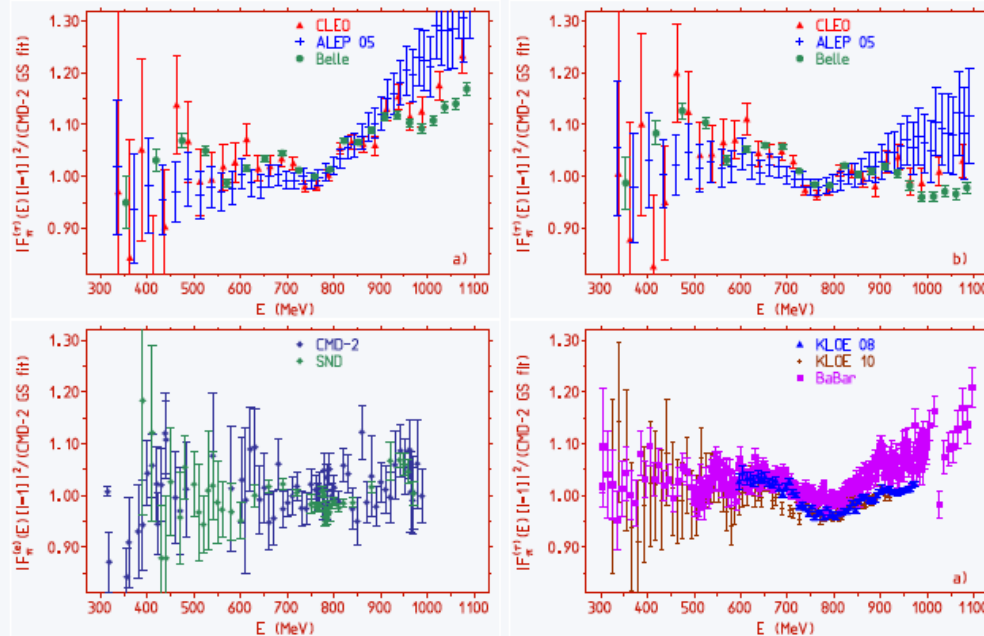
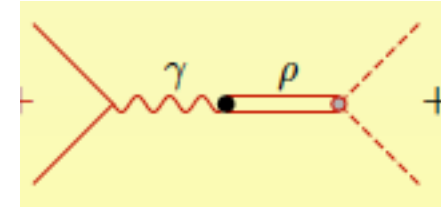
$$a_\mu^{\text{had,LO}}[\tau] = (701.5 \pm 3.5_\tau \pm 1.9_{\text{SU}(2)} \pm 2.4_{ee+\text{QCD}}) \times 10^{-10}$$

JS 11

DHMZ 11

Jegerlehner and Szafron claim that the e^+e^- vs τ is solved if an additional correction (ρ - γ loop mix.) is included

F. Jegerlehner and R. Szafron, Eur. Phys. J. C71 (2011) 1632



$|F_\pi(E)|^2$ in units of e^+e^- $|=1$ (CMD-2 GS fit): a) τ data uncorrected for ρ - γ mixing, and b) after correcting for mixing. Lower panel: e^+e^- energy scan data [left] and e^+e^- radiative return data [right]

τ decays			
Belle			25.24 ± 0.39
CLEO			25.44 ± 0.44
ALEPH			25.49 ± 0.13
DELPHI			25.31 ± 0.24
L3			24.62 ± 0.61
OPAL			25.46 ± 0.34
τ average			25.42 ± 0.10
$e^+e^- + \text{CVC}$			
CMD2 03			25.65 ± 0.29
CMD2 06			25.56 ± 0.31
SND 06			25.52 ± 0.36
KLOE 08			25.26 ± 0.29
e^+e^- average			25.40 ± 0.28
KLOE 10			25.18 ± 0.34
BABAR 09			25.77 ± 0.28
PDG average			25.51 ± 0.09
		$B(\tau \rightarrow \pi\pi^0\nu_\tau)$	24 25 26 27 %

$$a_\mu^{\text{had,LO}}[e, \tau] = 690.96(1.06)(4.63) \times 10^{-10} \quad (e + \tau)$$

$$a_\mu^{\text{had,LO}}[e^+e^-] = (692.3 \pm 4.2_{ee+\text{QCD}}) \times 10^{-10}$$

$$a_\mu^{\text{had,LO}}[\tau] = (701.5 \pm 3.5_\tau \pm 1.9_{\text{SU}(2)} \pm 2.4_{ee+\text{QCD}}) \times 10^{-10}$$

JS 11

DHMZ 11

An Update of the HLS Estimate of the Muon $g - 2$

M. Benayoun^a, P. David^a, L. DelBuono^a, F. Jegerlehner^{b,c}

Using the KLOE10 and the scan data samples leads to the most probable value for the muon anomalous moment :

EPJ C73 (2013) 2453

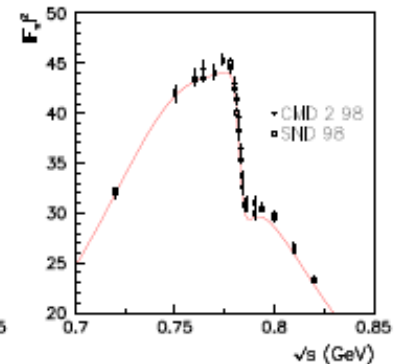
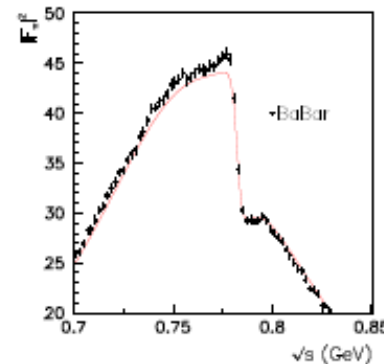
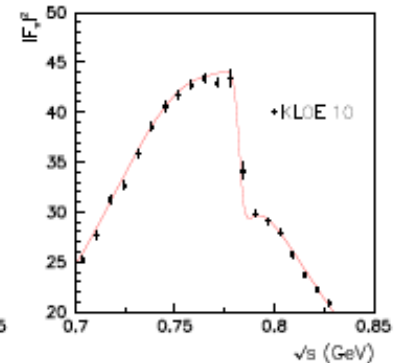
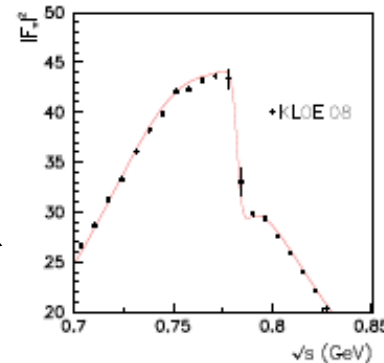
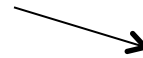
$$a_{\mu}^{th} = (11\,659\,169.55 + \left[\begin{smallmatrix} +1.26 \\ -0.59 \end{smallmatrix} \right]_{\phi} \pm 5.21_{th}) 10^{-10},$$

which exhibits a significance for $\Delta a_{\mu} = a_{\mu}^{exp} - a_{\mu}^{th}$ at a $(4.7 \div 4.9)\sigma$ level, significantly larger than the results fully derived by direct numerical integration of the experimental cross sections.

Pion form factor prediction based on τ data and PDG information in excellent agreement with KLOE but not with BaBar

However, the picture becomes quite different in the medium energy region ($0.70 \div 0.85$) GeV as illustrated by Figure 5. In this region, our τ +PDG prediction follows almost perfectly expectations²¹ from both KLOE08 and KLOE10 data and the detailed lineshape at the $\omega - \rho$ interference region is strikingly reproduced. Paradoxically, the NSK data are slightly less fa-

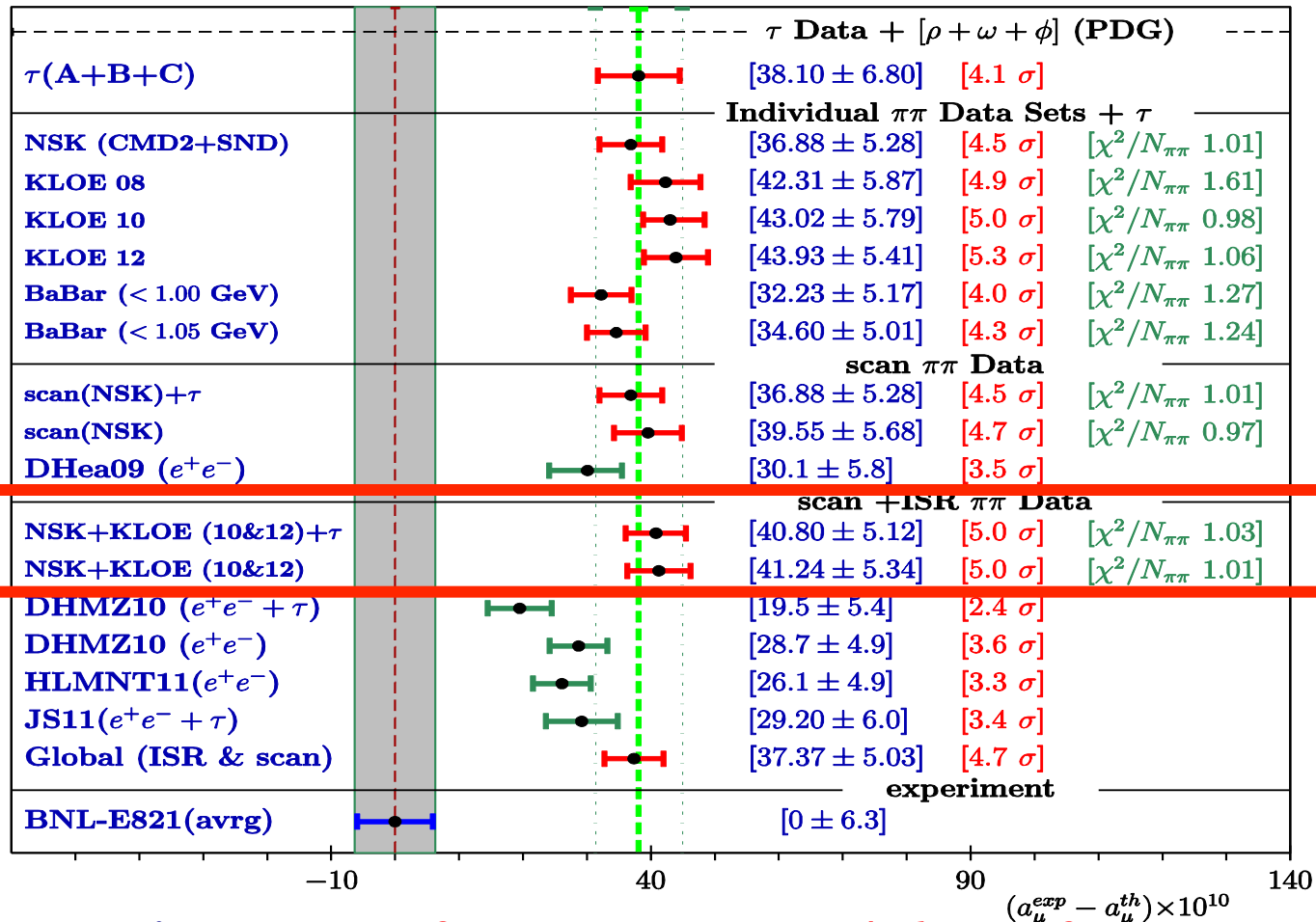
In contrast, the behavior of the BaBar data looks inconsistent with the τ +PDG prediction, especially on the low mass side of the interference region. Actually, the observed overestimate of the BaBar spectrum affects the whole region from threshold to the ω mass but is more important in the range ($0.74 \div 0.78$) GeV. At higher energies one observes a reasonable agreement



BHLS : A Global VMD Model

- The **(Broken) Hidden Local Symmetry (BHLS)** model :
 - is a unified **VMD** framework encompassing
 $e^+e^- \rightarrow \pi\pi / \text{KKbar} / \pi\gamma / \eta\gamma / \pi\pi\pi$ & $\tau \rightarrow \pi\pi \nu_\tau$ & $PV\gamma, P\gamma\gamma$ decays & $(\eta/\eta' \rightarrow \gamma\pi\pi/\gamma\gamma)$ &
 - BHLS :: (almost) an empty shell :
[$\alpha_{em}, G_F, f_\pi, V_{ud}, V_{us}, m_\pi$'s, m_K 's, $m_\eta, m_{\eta'}$]
 - **Present Limits** :
 - ✓ Up to the $\approx \phi$ mass region (≈ 1.05 GeV)
 - ✓ No scalars mesons, no ρ' , no ρ''

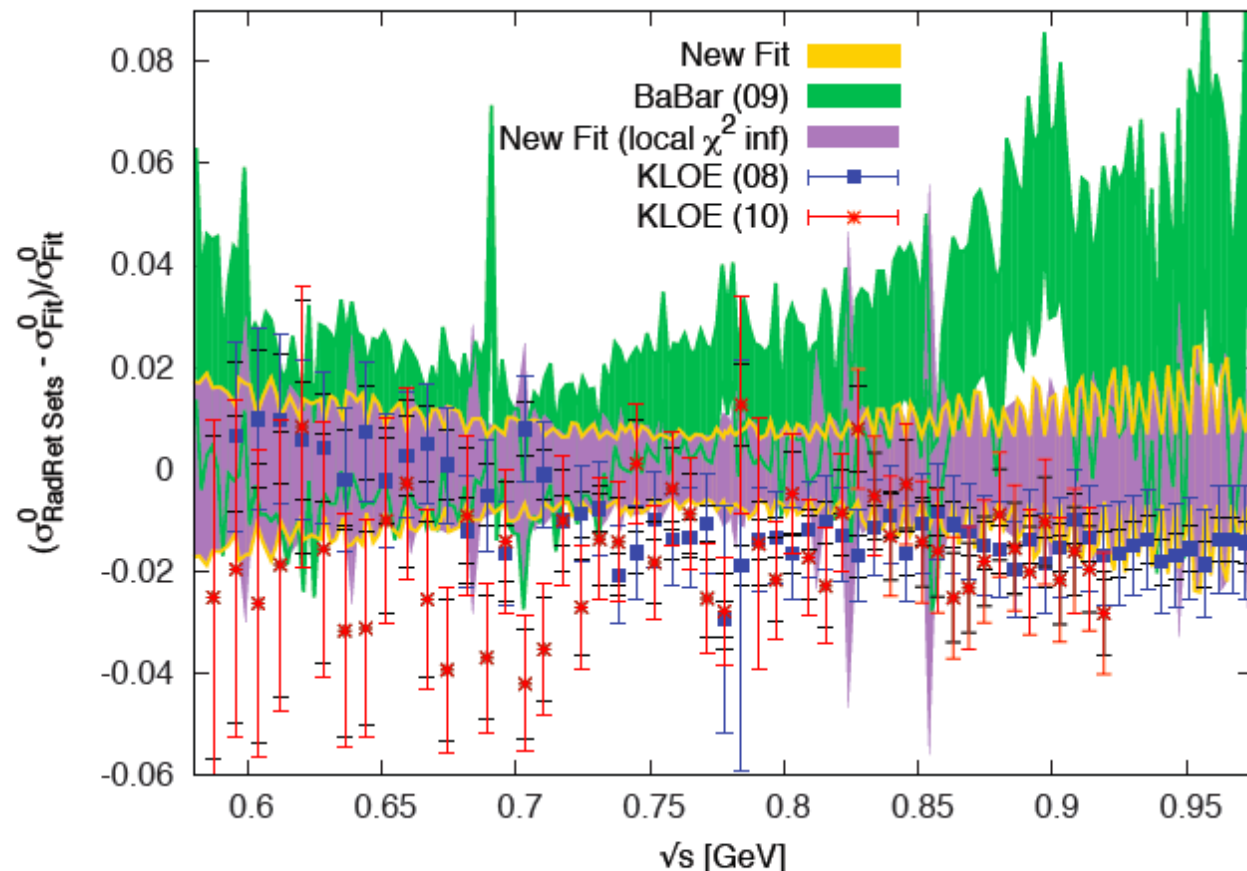
g-2 HLS Estimates & Others



Discrepancy with BNL g-2 value range [4.6 to 5.2] σ

Data combination in the $\pi^+\pi^-$ channel

Radiative Return data in the combined fit of HLMNT 11



T. Teubner,
PHIPSI13, Rome,
9-12 September 2013

2π fit: overall
 $\chi^2_{\min}/\text{dof} \sim 1.5$

Note: $a_{\mu}^{\pi\pi, \text{w/out Rad Ret}} = 498.7 \pm 3.3$ BUT $a_{\mu}^{\pi\pi, \text{with Rad Ret}} = 504.2 \pm 3.0$

➔ i.e. a shift of +5.5

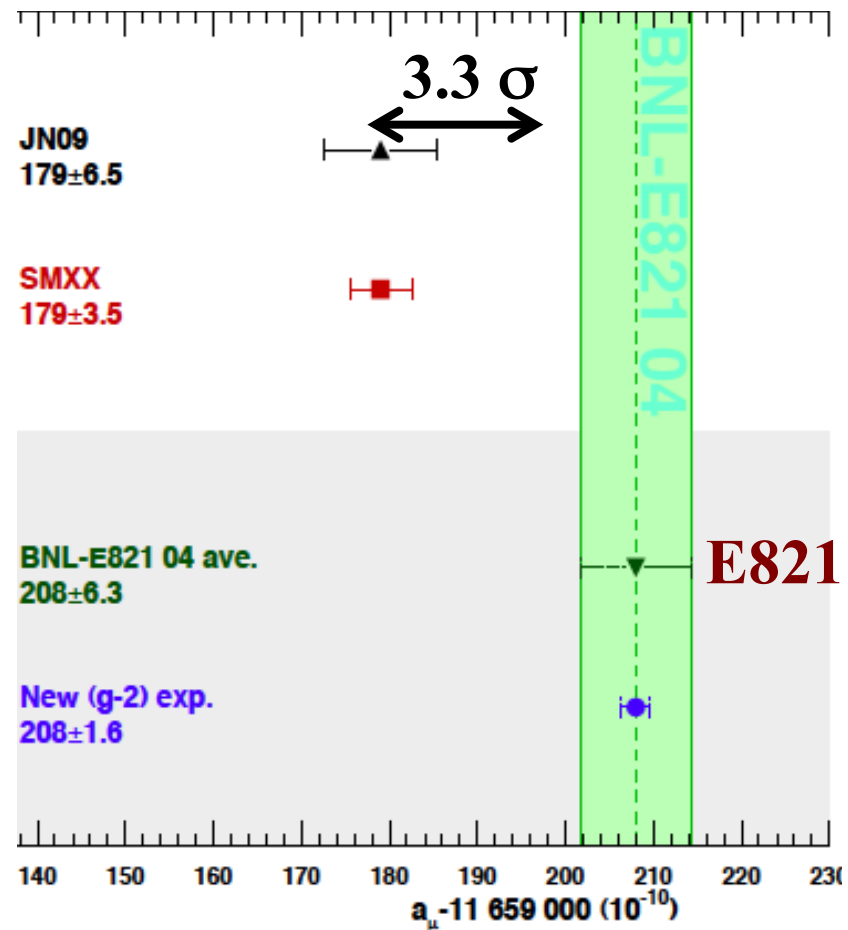
Data combination in the $\pi^+\pi^-$ channel

- **Benayoun et al:** -3.1 from HLS-based fit, -4.3 from KLOE10+12
- **HLMNT:** +5.5 from KLOE and BaBar (compared to scan only)
- So the extreme difference ($\sim 13 \times 10^{-10}$) comes mostly from the data input, i.e. if BaBar's 2π is used or not.
(If used: error relatively poor and inflated in addition.)
- How to solve this puzzle? **T. Teubner, RMCWG meeting, Frascati, 13 September 2013**
- Future SND, CMD-3, BELLE and BESIII 2π data may dilute the strong significance of BaBar.
Would be better to find out why the different data sets are not consistent. **If this can be achieved the 2π channel would be great!**
- **→ possible task for our WG: MC checks, comparison of analyses**

A rough estimate for g-2: now

$$a_{\mu}^{\text{exp}} - a_{\mu}^{\text{theo,SM}} = (27.7 \pm 8.4) 10^{-10} \quad (3.3\sigma)$$

$$8.4 = \sim 5_{\text{HLO}} \oplus \sim 3_{\text{HLbL}} \oplus 6_{\text{BNL}}$$



$$\delta a_{\mu}^{\text{HLO}} = 5.3 = 3.3(\sqrt{s} < 1 \text{ GeV}) \oplus 3.9(1 < \sqrt{s} < 2 \text{ GeV}) \oplus 1.2(\sqrt{s} > 2 \text{ GeV})$$

A rough estimate for g-2: ...and (possible) future

$$a_{\mu}^{\text{exp}} - a_{\mu}^{\text{theo,SM}} = (27.7 \pm 8.4)10^{-10} \quad (3.3\sigma)$$

$$8.4 = \sim 5_{\text{HLO}} \oplus \sim 3_{\text{HLbL}} \oplus 6_{\text{BNL}}$$

\downarrow \downarrow \downarrow \downarrow
 4 3 3 1.6 _{NEW G-2}

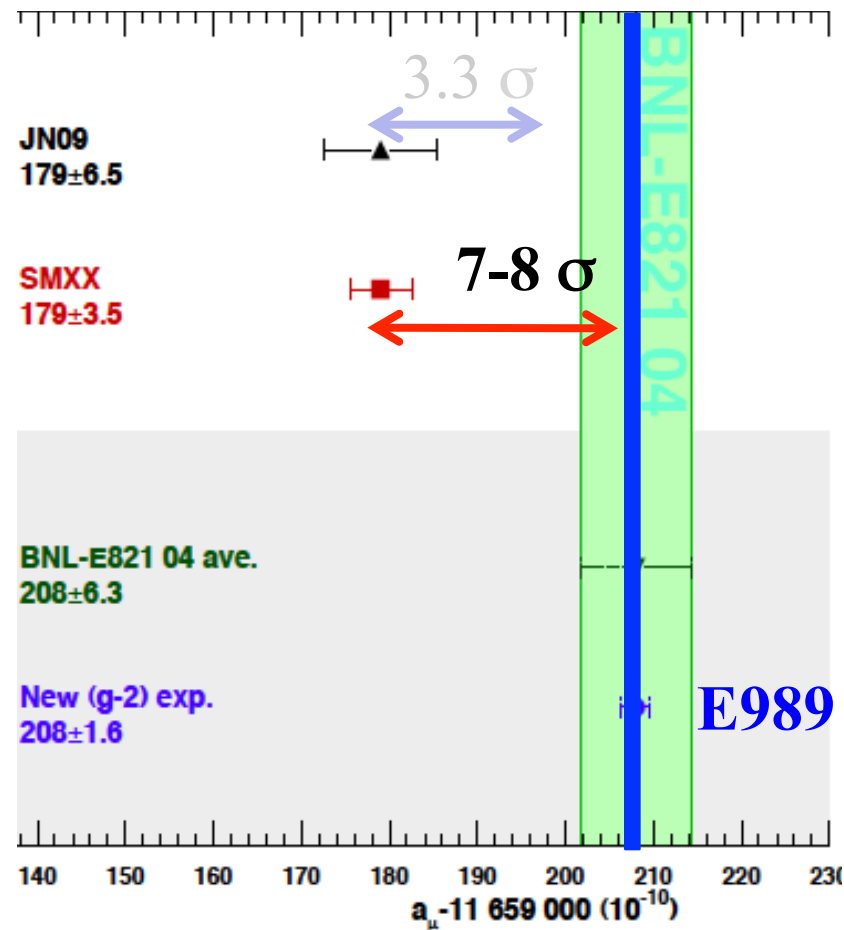
$$a_{\mu}^{\text{exp}} - a_{\mu}^{\text{theo,SM}} = (\text{XXX} \pm 3.8)10^{-10}$$

If central value is the same $\rightarrow 7-8\sigma$

(if no progress on theory $\rightarrow 5\sigma$)

$$\delta a_{\mu}^{\text{HLO}} \rightarrow 2.6 = 1.9 (\sqrt{s} < 1\text{GeV}) \oplus 1.3 (1 < \sqrt{s} < 2\text{GeV}) \oplus 1.2 (\sqrt{s} > 2\text{GeV})$$

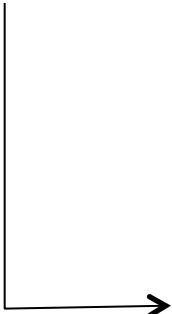
This is possible if:



- $\delta\sigma_{\text{HAD}} \sim 0.4\% \sqrt{s} < 1\text{GeV}$ (instead of 0.7% as now)
- $\delta\sigma_{\text{HAD}} \sim 2\% \mathbf{1 < \sqrt{s} < 2\text{GeV}}$ (instead of 6% as now)

(Possible with direct scan or ISR at Flavour factories, or new machines like IRIDE)

See M. Ferrario's talk

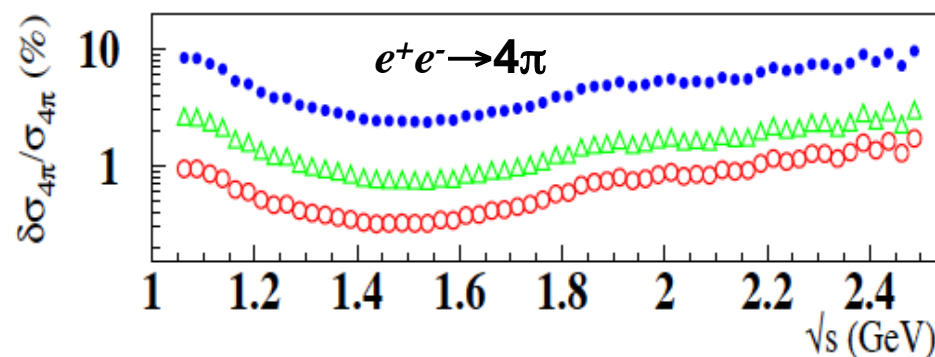
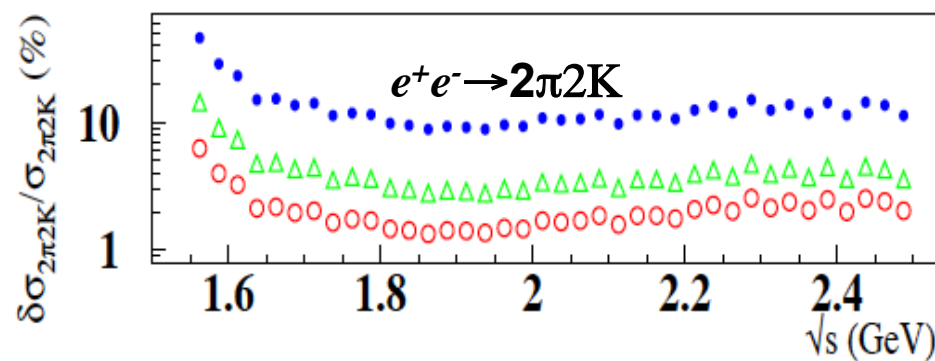
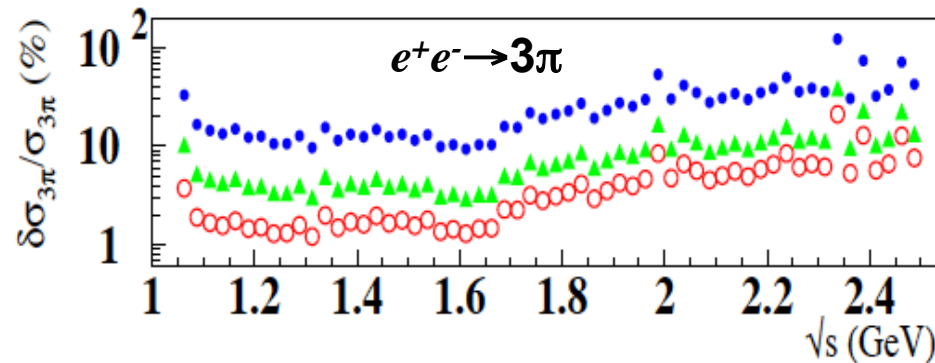


$$\delta a_{\mu}^{\text{HLO}} = \mathbf{2.6 \cdot 10^{-10}} \text{ (instead of } \sim 5 \text{ as now)}$$

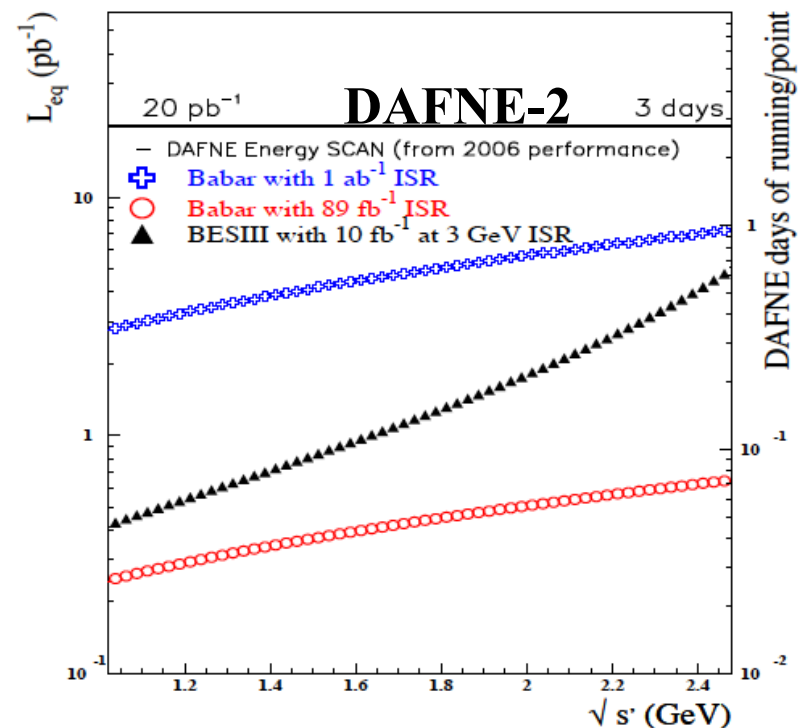
A similar improvement on $\delta\alpha_{\text{em}}(\text{Mz})$ using Adler function method

Impact of DAFNE-2 on exclusive channels in the range [1-2.5] GeV with a scan (Statistics only)

arXiv:1007.521



- Published BaBar results: 89 fb^{-1} (ISR)
- ▲ “BaBar” $\times 10$ (890 fb^{-1})
- DAFNE-2 energy scan: $20 \text{ pb}^{-1}/\text{point}$
- ④ $L = 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$, 25 MeV bin
- ⇒ 1 year data-taking



DAFNE-2 is statistically equivalent to $5\div 10 \text{ ab}^{-1}$ (Super)B-factory

Conclusion

- Significant improvement a_{μ}^{HLO} in the last 15 years due to more precise data. Interplay with theorists for the control of RC and development of MC
- ISR opened a new way to precisely measure the hadronic cross sections
- Still some (local) differences between data which current limit precision on a_{μ}^{HLO}
- New data are expected from DAFNE, VEPP2000, BESIII and (Super)B factories which will continue to improve the region below 5 GeV with ISR. Hopefully new machines (IRIDE, Super τ/c factory)
- These data would allow to reduce of a factor ~ 2 the uncertainty on a_{μ}^{HLO} to match the request from the next $g-2$ experiments (at FNAL and J-PARC). A similar improvement is expected on $\alpha_{\text{em}}(\text{Mz})$.

BNL ring arrived at FNAL for the new g-2 experiment

July 26 2013



*“Well, QED is very nice and impressive, but when everything is so neatly wrapped up in blue bows, with all experiments in exact agreement with each other and with the theory - that is when one is learning **absolutely nothing.**”*

“On the other hand, when experiments are in hopeless conflict - or when the observations do not make sense according to conventional ideas, or when none of the new models seems to work, in short when the situation is an unholy mess - that is when one is really making hidden progress and a breakthrough is just around the corner!” [143]

R. Feynman, 1973 Hawaii Summer Institute

Thanks!



SPARE

Conclusions

1/ HLS model succeeds → (other **global** approaches)

2/ **NO** signal for (e^+e^- vs τ) puzzle

3/ Consistent $\pi^+ \pi^-$ data sets : **CMD2, SND, KLOE 10 & 12**

4/ $10^{10} \times [a_{\mu}^{\text{exp}} - a_{\mu}^{\text{th}}] = 40.80 + \left[\begin{array}{c} +0.6 \\ -1.3 \end{array} \right]_{\phi} + \left[\begin{array}{c} +0.4 \\ -0.0 \end{array} \right]_{\tau} + \left[\begin{array}{c} +0.0 \\ -2.2 \end{array} \right]_{\text{mod}} \pm 5.12_{\text{th}} \pm 6.30_{\text{exp}}$

5/ Discrepancy with BNL **g-2** value range **[4.6 to 5.2] σ**

6/ Additional Breaking schemes may reduce systematics

HVP Results with scan & τ data

- (Updated) Central value shifted by $\approx 3 \cdot 10^{-10}$

Channel	Solution B	Direct Estimate
$\pi^+\pi^-$	495.40 \pm 1.92	498.53 \pm 3.73 (497.72 \pm 2.12)
$\pi^0 \gamma$	4.61 \pm 0.04	3.35 \pm 0.11
$\eta \gamma$	0.64 \pm 0.01	0.48 \pm 0.01
$\eta' \gamma$	0.01 \pm 0.00	---
$\pi^+ \pi^- \pi^0$	41.16 \pm 0.59	43.24 \pm 1.47
$K_L K_S$	11.90 \pm 0.08	12.31 \pm 0.33
K^+K^-	17.59 \pm 0.21	17.88 \pm 0.54
Total up to 1.05 GeV	571.30 \pm 2.02	575.79 \pm 4.06

Diff=3.1 units

↓ another shift by -4.3

Channel	NSK +KLOE 10&12 + τ (ABC < 1 GeV)	scan only(NSK) + τ (ABC < 1GeV)	Direct Estimate
$\pi^+\pi^-$	491.12 ± 1.35	495.40 ± 1.92	498.53 ± 3.73 (497.72 ± 2.12)
$\pi^0 \gamma$	4.63 ± 0.04	4.61 ± 0.04	3.35 ± 0.11
$\eta \gamma$	0.64 ± 0.01	0.64 ± 0.01	0.48 ± 0.01
$\eta' \gamma$	0.003 ± 0.000	0.003 ± 0.000	---
$\pi^+ \pi^- \pi^0$	40.78 ± 0.64	41.16 ± 0.59	43.24 ± 1.47
$K_L K_S$	11.94 ± 0.08	11.90 ± 0.08	12.31 ± 0.33
K^+K^-	17.48 ± 0.21	17.59 ± 0.21	17.88 ± 0.54
Total up to 1.05 GeV	566.58 ± 1.50	571.30 ± 2.02	575.79 ± 4.06

g-2 & Global Models/Fits

- NP Hadronic VP contributions to g-2

$$a_{\mu}(H_i) = \frac{1}{4\pi^3} \int_{s_{th}}^{s_{cut}} ds K(s) \sigma(e^+ e^- \rightarrow H_i, s)$$

← Measured Xsection

- Effective Lagrangians imply **physics correlations** among $e^+ e^- \rightarrow H_i$
- -> HLS cross-sections derived through a **global fit** (param. values & error covariance matrix)

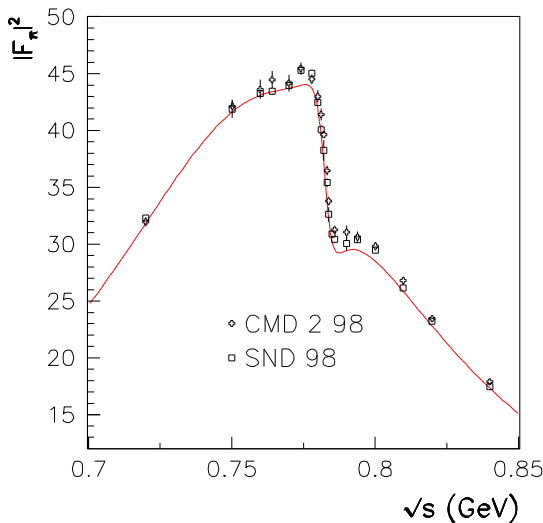
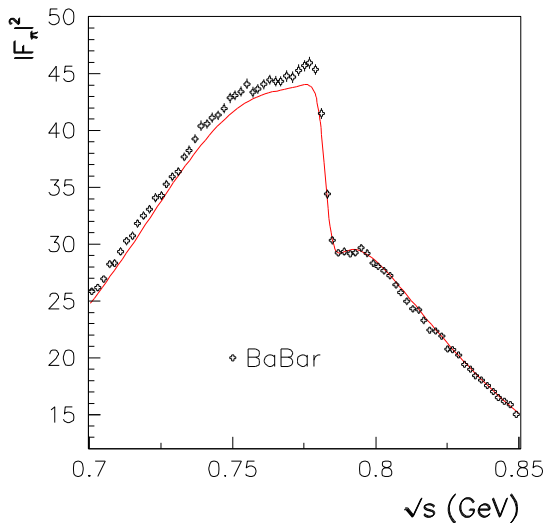
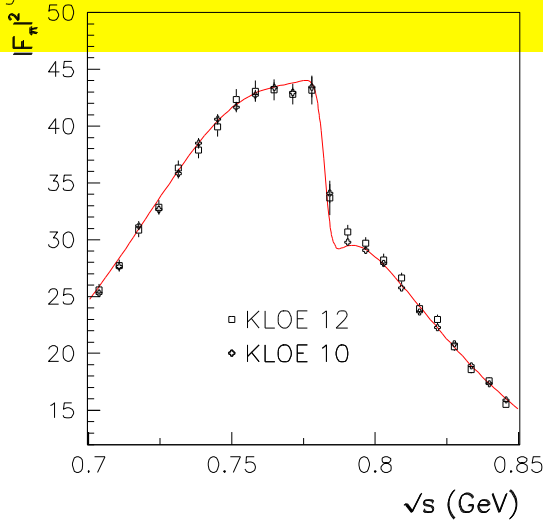
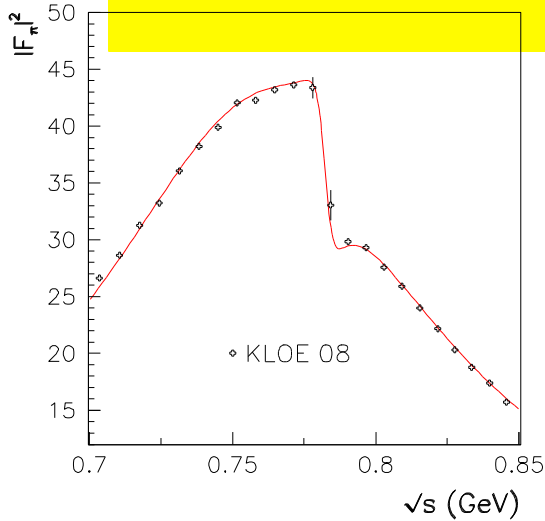
Measured Xsection



Model Xsection (ϕ)

τ + PDG Predictions

Breaking from PDG



PION Form Factor

$0.85 \text{ GeV} > m_{\pi\pi} > 0.70 \text{ GeV}$

**KLOE's almost perfect!
CMD2&SND \approx OK
BaBar too large below ω**

Radiative corrections are important!

- Unclear treatment of R.C. in old data.
- Reevaluation of RC leads to significant changes in recent data
- New data (CMD-2, SND, KLOE, Babar) paid more attention to :
 - ISR
 - Vacuum Polarization (VP)
 - FSR
- A lot of work for theorists to provide accurate MC generators (and for experimentalists to test it!)

$$\sigma_{bare} = \sigma_{dressed} |1 - \Pi(s)|^2 (1 + C_{FSR})$$

$$\bullet \sigma_{dressed} = \frac{N}{\int L dt \epsilon (1 + \delta_{ISR})}$$

$$\bullet \Pi(s) = \Pi_{lep}(s) + \Pi_{had}(s)$$

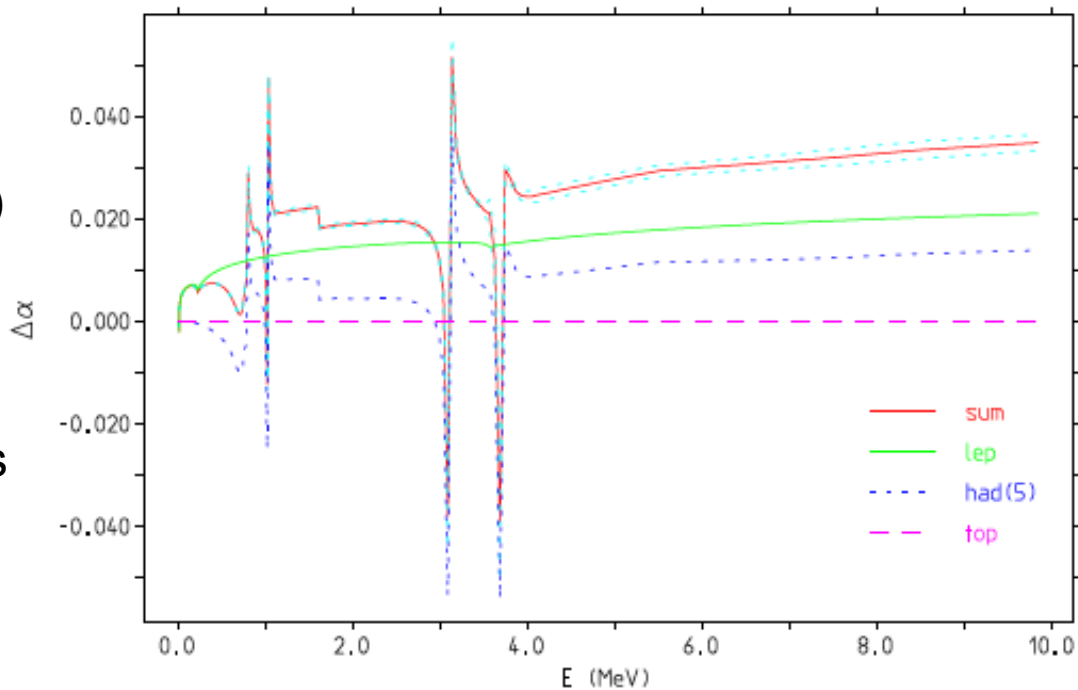


Figure from Fred Jegerlehner

A common effort for RC and Monte Carlo tools

Eur. Phys. J. C (2010) 66: 585–686
DOI 10.1140/epjc/s10052-010-1251-4

THE EUROPEAN
PHYSICAL JOURNAL C

Review

Quest for precision in hadronic cross sections at low energy: Monte Carlo tools vs. experimental data

Working Group on Radiative Corrections and Monte Carlo Generators for Low Energies

S. Actis³⁸, A. Arbuzov^{9,e}, G. Balossini^{32,33}, P. Beltrame¹³, C. Bignamini^{32,33}, R. Bonciani¹⁵, C.M. Carloni Calame³⁵, V. Cherepanov^{25,26}, M. Czakon¹, H. Czyż^{19,a,f,i}, A. Denig²², S. Eidelman^{25,26,g}, G.V. Fedotovitch^{25,26,e}, A. Ferroglia²³, J. Gluza¹⁹, A. Grzelińska⁸, M. Gunia¹⁹, A. Hafner²², F. Ignatov²⁵, S. Jadach⁸, F. Jegerlehner^{3,19,41}, A. Kalinowski²⁹, W. Kluge¹⁷, A. Korchin²⁰, J.H. Kühn¹⁸, E.A. Kuraev⁹, P. Lukin²⁵, P. Mastrolia¹⁴, G. Montagna^{32,33,b,d}, S.E. Müller^{22,f}, F. Nguyen^{34,d}, O. Nicrosini³³, D. Nomura^{36,h}, G. Pakhlova²⁴, G. Pancheri¹¹, M. Passera²⁸, A. Penin¹⁰, F. Piccinini³³, W. Placzek⁷, T. Przedzinski⁶, E. Remiddi^{4,5}, T. Riemann⁴¹, G. Rodrigo³⁷, P. Roig²⁷, O. Shekhovtsova¹¹, C.P. Shen¹⁶, A.L. Sibidanov²⁵, T. Teubner^{21,h}, L. Trentadue^{30,31}, G. Venanzoni^{11,c,i}, J.J. van der Bij¹², P. Wang², B.F.L. Ward³⁹, Z. Was^{8,g}, M. Worek^{40,19}, C.Z. Yuan²

~60 participants, 13 countries

See www.lnf.infn.it/wg/sighad for more information
(next meeting 11-12 April 2013, ECT*)

"Old" Results on R from energy scan at $\sqrt{s} < 10$ GeV

<u>Place</u>	<u>Ring</u>	<u>Detector</u>	<u>E_{cm} (GeV)</u>	<u>pts</u>	<u>Year</u>
Novosibirsk	VEPP-2M	CMD2,SND	<1.4	128	01-03
	VEPP-2	Olya,ND,CMD	<1.4		79-85 97-99
Beijing	BEPC	BESII	2-5	85	98-99
Orsay	DCI	M3N,DMI,DM2	1.35-2.13	33	'78
Frascati	Adone	$\gamma\gamma$ 2,MEA, Boson,BCF	1.42-3.09	31	'78
SLAC	Spear	MarkI	2.8-7.8	78	'82
Cornell	CESR	CLEO	3-5		'05
Hamburg	Doris	DASP	3.1-5.2	64	'79
		PLUTO	3.6-4.8,9.46	27	'77
		C.Ball	5.0-7.4	11	'90
		LENA	7.4-9.4	95	'82
Novosibirsk	VEPP-4	MD-1	7.23-10.34	30	'91