



# Higgs Physics as a probe of new physics

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*LC13 Workshop*

*exploring QCD from the infrared regime to heavy flavour scales at B-factories,  
the LHC and a Linear Collider 16-20 September 2013, ECT\*, Villa Tambosi, Italy*

# Introduction

Why Higgs is important?

# Introduction

Higgs field couples to all particles

Higgs field gets a VEV ( $v$ ) by EWSB

Higgs mechanism

$$m_W = g v$$

Yukawa interaction

$$m_{q,l} = Y_{q,l} v$$

Dimension 5 operator  
(neutrino mass)

$$m_\nu = C_\nu v^2/M$$

**Higgs field = Origin of Mass**

# Introduction

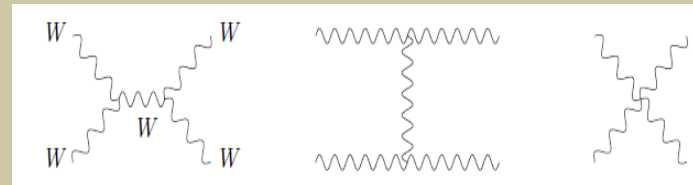
$W_L^+ W_L^-$  Elastic Scattering

$$a^0(W_L^+ W_L^- \rightarrow W_L^+ W_L^-) \approx A E^4 + B E^2 + C \quad (E \rightarrow \infty)$$

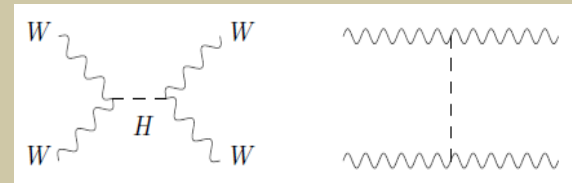
Unitarity Violation if  $A, B \neq 0$

$A=0$  because of gauge symmetry

To make  $B=0$ , **diagrams mediated by a scalar field  $h$  must be added**



**Higgs field is required to save unitarity**



Perturbative Unitarity

$$|a^0(W_L^+ W_L^- \rightarrow W_L^+ W_L^-)| < 1 \Rightarrow m_h < 1 \text{ TeV}$$

# Introduction

Higgs Sector in the SM:  
One  $SU(2)$  doublet  $\Phi$

$$V(\Phi) = +\mu^2|\Phi|^2 + \lambda|\Phi|^4$$

Assumption of  $\mu^2 < 0 \Rightarrow$  **EWSB**

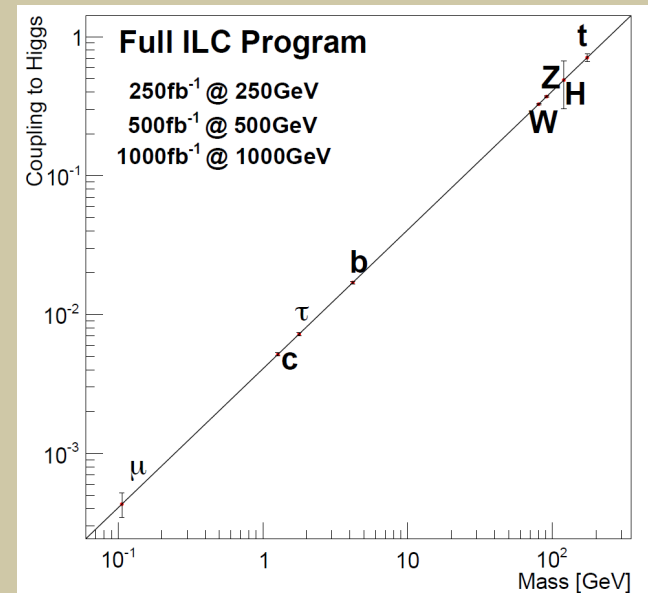
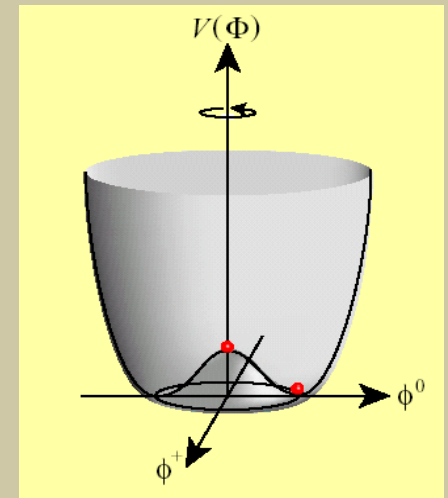
This is simple but ...

Question:

Why **minimal?** (no principle)

Why  $\mu^2 < 0$

What is Origin of the **Higgs force  $\lambda$** ?



# In 2012 July, a boson $h$ was found

The mass is 126 GeV

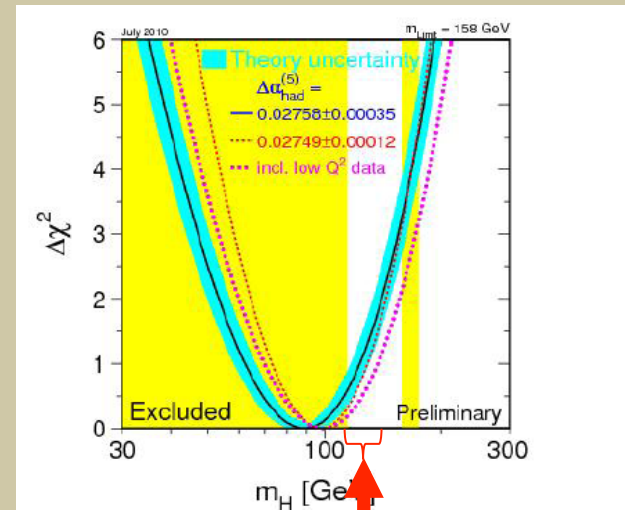
Spin/Parity  $0^+$

It couples to

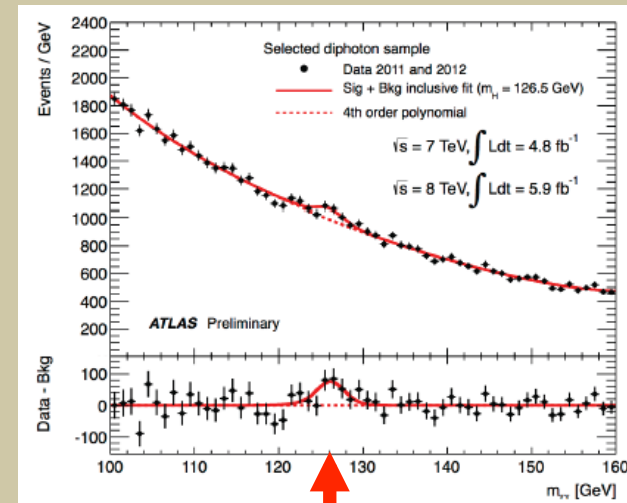
$\gamma\gamma$ ,  $WW$ ,  $ZZ$ ,  $bb$ ,  $\tau\tau$

This is really a SM-like Higgs!

Why SM-like?



Higgs Mass indicated by LEP/SLC



ATLAS/CMS July 2012

New Particle !

# Introduction

## Second Higgs boson?

**SM Higgs sector = just a guess!**

No principle for the minimal Higgs sector of the SM

Many possibilities for **non-minimal** Higgs sectors

These extended Higgs sectors provide source for

- Baryogenesis (CP violation/1st Order Phase Transition)
- Dark Matter
- Neutrino Mass

**Higgs sector = Window for new physics**

# Introduction

Scalar field in the SM is problematic

Problem of quadratic divergences

**Hierarchy problem**

Ideas of new physics to solve the problem

- Supersymmetry
- Dynamical Symmetry Breaking (Technicolor)
- Little Higgs mechanism
- Extra Dimensions
- ...

Many of these NP models predict specific extended Higgs sectors

**Higgs sector = Window for new physics**

$$\delta m_H^2 = \frac{\Lambda_{cutoff}^2}{16\pi^2}$$



# Introduction

Higgs is important not only for EWSB but also as **Window** to new physics beyond SM

Discovery of the 126GeV **SM-like Higgs  $h$**  at LHC is a great step to determine the shape and to understand the essence of the Higgs sector

From the detailed study of the Higgs sector, we can determine models of new physics

**New era has just started !**

# Contents

- Introduction
- Extended Higgs Sectors and New Physics
- Higgs as a probe of new physics
  - Precision measurement of the SM-like Higgs boson  $h$
  - Properties of extra Higgs bosons  $H, A, H^+, H^{++}, \dots$
- Summary

# **Extended Higgs Sector and New Physics**

# Higgs Sector

- LHC found the SM-like Higgs boson  $h$  !
- But, the “SM-like” does not necessarily mean the SM
- Non-minimal Higgs models necessarily can contain the SM-like Higgs boson, and this can satisfy the current LHC data.

The shape of the Higgs sector must be determined by future experiments

# Extended Higgs

If the Higgs sector contains more than one scalar bosons, possibility would be

- SM + Extra singlets (NMSSM, B-L Higgs, ...)
- SM + Extra doublets (SUSY, CPV, EW Baryogenesis, Neutrino mass, ...)
- SM + Extra triplets (Type II seesaw, LR models....)
- ....

**Basic experimental quantities:**

- Electroweak rho parameter
- Flavor Changing Neutral Current (FCNC)

# Electroweak rho parameter

$$\rho_{\text{exp}} = 1.0008^{+0.0017}_{-0.0007}$$

$$Q = I_3 + Y/2$$

$$\rho \equiv \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} = \frac{\sum_i [4T_i(T_i + 1) - Y_i^2] |v_i|^2 c_i}{\sum_i 2Y_i^2 |v_i|^2}$$

$T_i$  : SU(2)<sub>L</sub> isospin

$Y_i$  : hypercharge

$v_i$  : v.e.v.

$c_i$  : 1 for complex representation

1/2 for real representation

## Possibility of $\rho \approx 1$

### 1. SM + doublets ( $\phi$ ) + singlets (S)

### 2. SM + Triplets ( $\Delta$ )

$$\rho_{\text{tree}} = \frac{1 + \frac{2v_\Delta^2}{v_\Phi^2}}{1 + \frac{4v_\Delta^2}{v_\Phi^2}} \simeq 1 - \frac{2v_\Delta^2}{v_\Phi^2}$$

a)  $v_\Delta \ll v_\Phi$

b) Combination of several representations

[ (ex) Georgi-Machasek model]  $v_\Delta \approx v_\Phi$

**Multidoublets (+singlets) seem the most natural choice?**

# 2 Higgs Doublet Model

$$\begin{aligned}
 V_{\text{THDM}} = & +m_1^2 |\Phi_1|^2 + m_2^2 |\Phi_2|^2 - \underline{m_3^2 (\Phi_1^\dagger \Phi_2 + \Phi_2^\dagger \Phi_1)} \\
 & + \frac{\lambda_1}{2} |\Phi_1|^4 + \frac{\lambda_2}{2} |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 \\
 & + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \frac{\lambda_5}{2} \left[ (\Phi_1^\dagger \Phi_2)^2 + (\text{h.c.}) \right]
 \end{aligned}$$

$\Phi_1$  and  $\Phi_2 \Rightarrow h, H, A^0, H^\pm \oplus$  Goldstone bosons

$\begin{array}{cccc} \uparrow & \uparrow & \uparrow & \text{charged} \\ \text{CPEven} & \text{CPodd} & & \end{array}$

$$m_h^2 = v^2 \left( \lambda_1 \cos^4 \beta + \lambda_2 \sin^4 \beta + \frac{\lambda}{2} \sin^2 2\beta \right) + \mathcal{O}\left(\frac{v^2}{M_{\text{soft}}^2}\right),$$

$$m_H^2 = M_{\text{soft}}^2 + v^2 (\lambda_1 + \lambda_2 - 2\lambda) \sin^2 \beta \cos^2 \beta + \mathcal{O}\left(\frac{v^2}{M_{\text{soft}}^2}\right),$$

$$m_{H^\pm}^2 = M_{\text{soft}}^2 - \frac{\lambda_4 + \lambda_5}{2} v^2,$$

$$m_A^2 = M_{\text{soft}}^2 - \lambda_5 v^2.$$

$M_{\text{soft}}$ : soft breaking scale

$$\Phi_i = \begin{bmatrix} w_i^+ \\ \frac{1}{\sqrt{2}}(h_i + v_i + i a_i) \end{bmatrix} \quad (i = 1, 2)$$

**Diagonalization**

$$\begin{aligned}
 \begin{bmatrix} h_1 \\ h_2 \end{bmatrix} &= \begin{bmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{bmatrix} \begin{bmatrix} H \\ h \end{bmatrix} & \begin{bmatrix} z_1^0 \\ z_2^0 \end{bmatrix} &= \begin{bmatrix} \cos \beta & -\sin \beta \\ \sin \beta & \cos \beta \end{bmatrix} \begin{bmatrix} z^0 \\ A^0 \end{bmatrix} \\
 \begin{bmatrix} w_1^\pm \\ w_2^\pm \end{bmatrix} &= \begin{bmatrix} \cos \beta & -\sin \beta \\ \sin \beta & \cos \beta \end{bmatrix} \begin{bmatrix} w^\pm \\ H^\pm \end{bmatrix}
 \end{aligned}$$

$$\frac{v_2}{v_1} \equiv \tan \beta$$

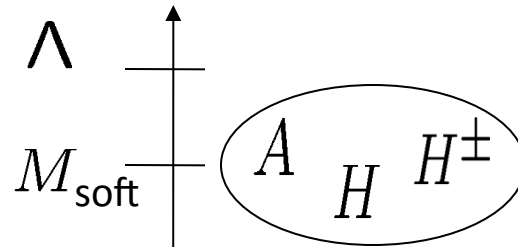
$$M_{\text{soft}} \left( = \frac{m_3}{\sqrt{\cos \beta \sin \beta}} \right):$$

soft-breaking scale  
of the discrete symm.

# Extended Higgs (2 cases of SM-like $h$ )

$\Lambda$ : Cutoff

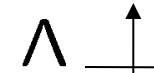
$M$ : Mass scale irrelevant to VEV



$$m_{A,H,H^\pm}^2 \simeq M^2 + \lambda_i v^2$$

$gv \sim m_W$  —  $h = \text{SM like}$

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \frac{v^2}{M_{\text{soft}}^2} \mathcal{O}^{(6)}$$



$\cos(\beta-\alpha) \approx 0$   
Mixing is weak  
 $\Rightarrow$  SM like

$gv \sim m_W$  —  $h = \text{SM like}$

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{nonSM}} + \frac{v^2}{\Lambda^2} \mathcal{O}^{(6)}$$



# FCNC Suppression

Multi-Higgs model: **FCNC appears via Higgs mediation**

ex) **2 Higgs doublet models:**

to avoid FCNC, impose a discrete symmetry

$$\Phi_1 \rightarrow +\Phi_1, \quad \Phi_2 \rightarrow -\Phi_2$$

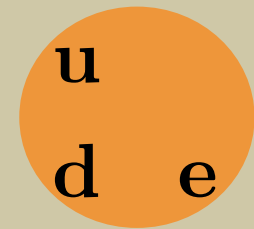
Each quark or lepton couples only one Higgs doublet

**No FCNC at tree level**

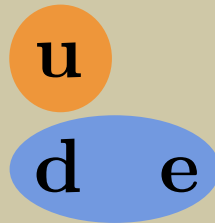
## Four Types of Yukawa coupling

*Barger, Hewett, Phillip*

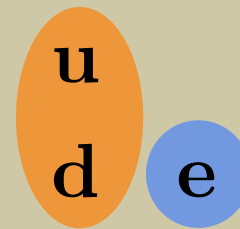
Classified by  $Z_2$  charge assignment



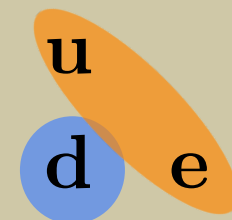
Type-I



Type-II



Type-X



Type-Y

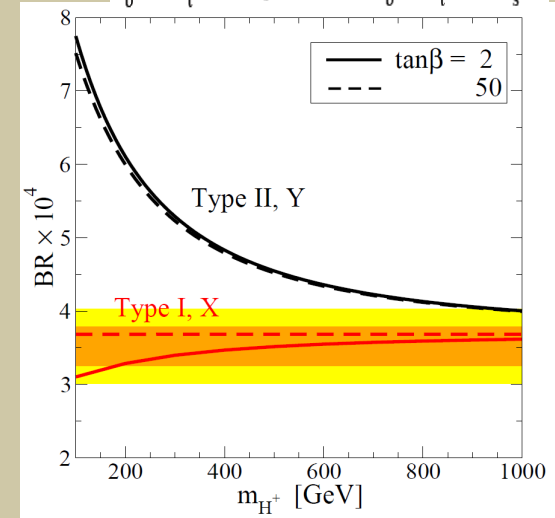
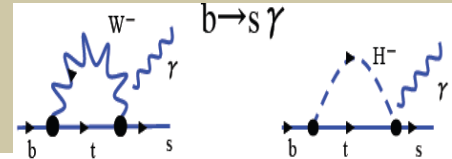
# Type of 2HDM

**Type-I** Fermiophobic 2HDM  
Neutrinophilic 2HDM

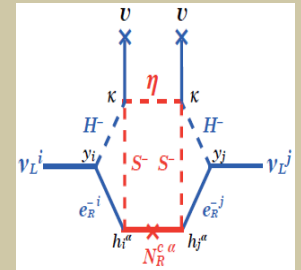
**Type-II** MSSM, NMSSM, other  
SUSY extended Higgs models

**Type-X** Lepton-specific 2HDM  
Models of Neutrino Masses  
Positron Excess  
(models with light  $H, A, H^\pm$ )

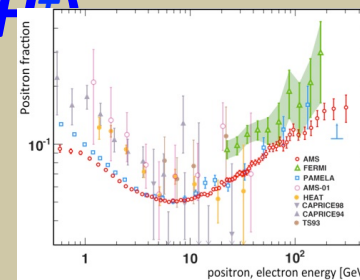
**Type-Y** Flipped 2HDM



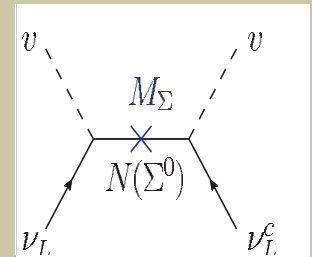
Aoki, SK, Tsumura, Yagyu (09)



Aoki, SK, Seto (09)



Goh, Hall, Kumar (09)



Ma (02)

# Search for Extended Higgs sectors

Many new physics models predict **non-minimal** Higgs sectors

Experimental determination of the Higgs sector is the Key to clarify the EWSB and also to explore new physics!

- **Direct Search**
  - Discovery of the “second” Higgs boson at LHC
- **Indirect Search (find deviation in Higgs couplings)**
  - How we can extract the shape of the Higgs sector from detailed measurement of the 126GeV SM-like Higgs boson ***h?***
  - It is **a solid target!**

# Precision measurement of the SM-like Higgs boson *h*

# Discrimination of models via coupling of the 125GeV Higgs boson $h$

Models can be distinguished by the pattern in deviations of the SM-like Higgs couplings

$h\gamma\gamma$ ,  $hgg$ ,  $hWW$ ,  $hZZ$ ,  $htt$ ,  $hff$ ,  $hhh$

**Mixing ( $h \Leftrightarrow \varphi$ )**

Gauge couplings ( $hVV$ ):

Yukawa couplings ( $hff$ ):

The pattern of deviation strongly depend on the model

**Quantum effects**

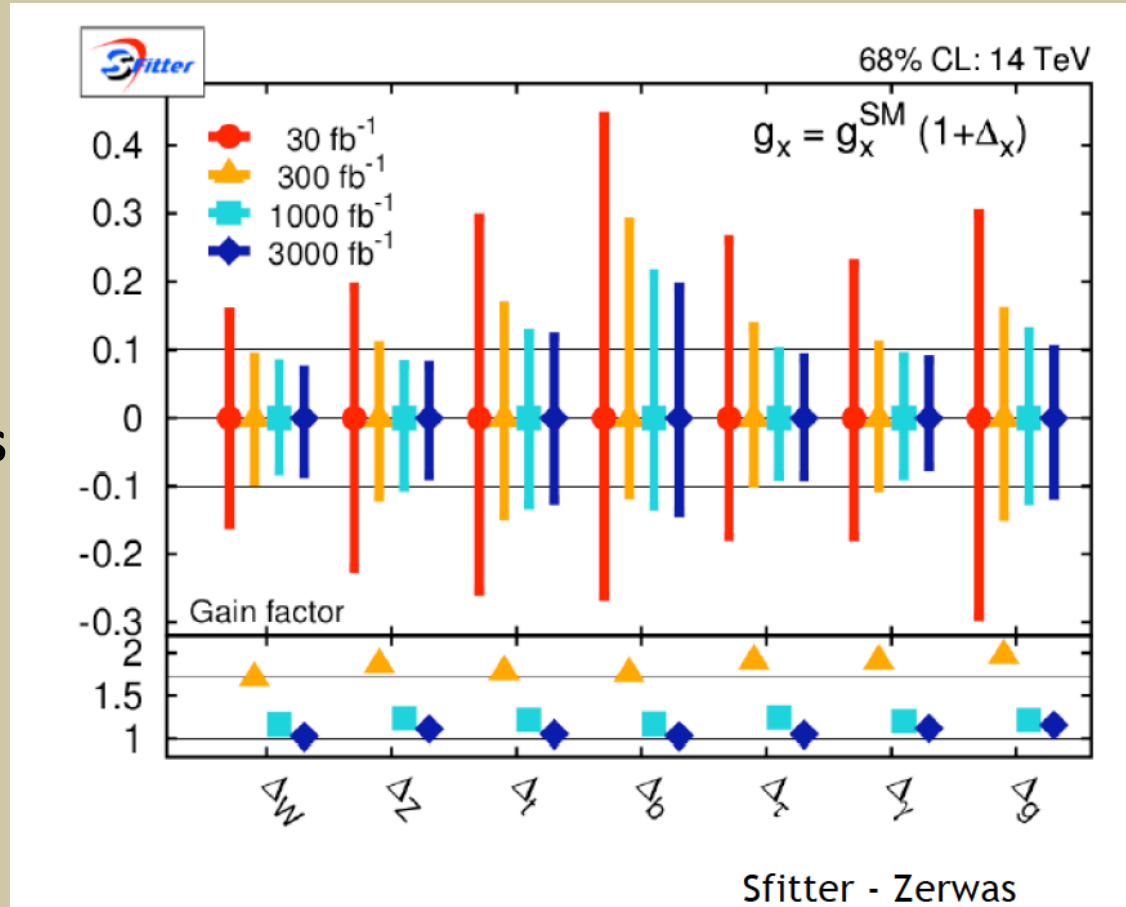
Large deviation in loop-induced processes ( $h \rightarrow \gamma\gamma$  and  $h \rightarrow gg$ )

Large quantum correction can also appear in the  $hhh$  coupling

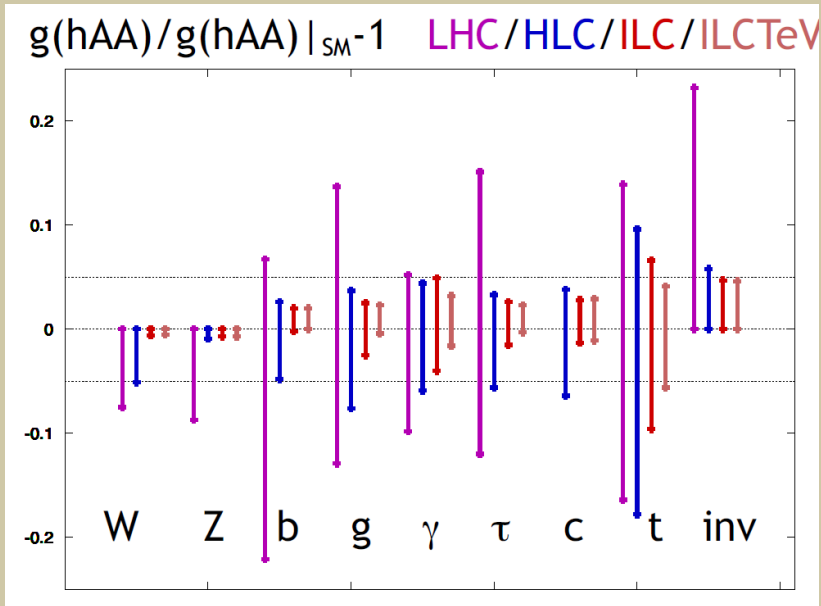
# Higgs coupling measurement at the LHC

Accuracy is typically  
 $O(10)$  %

Not very well improved  
for  $300 \rightarrow 3000 \text{ fb}^{-1}$   
due to systematic errors

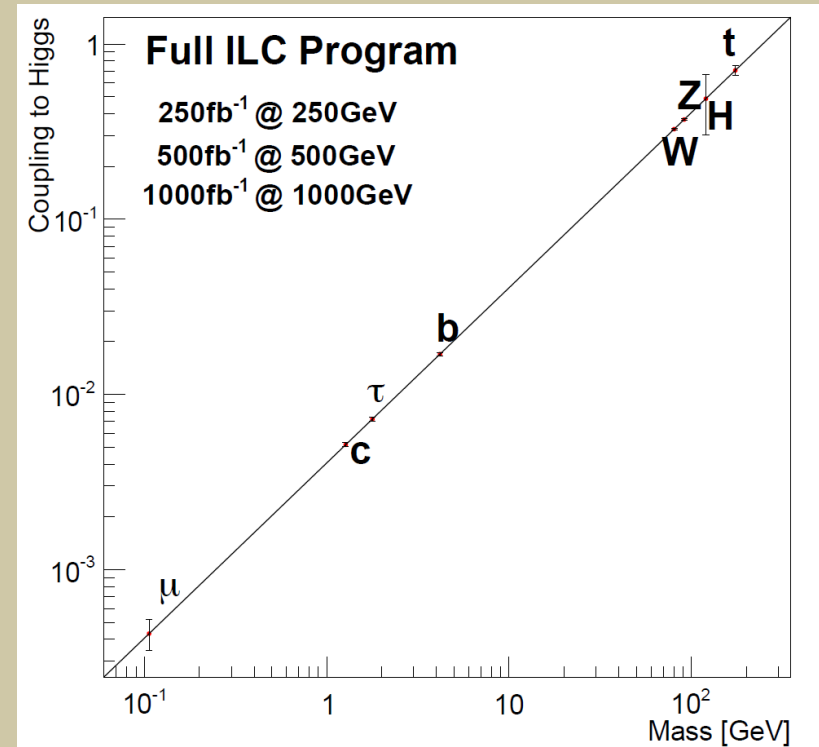


# International Linear Collider



M. Peskin, 2012

Coupling measurable by **a few%**, and  $hhh$  can also be measured by around O(10) %



At ILC, we may be able to distinguish models by detecting a pattern of deviations in the **h** couplings from the SM values!

# Snowmass White Paper (Aug. 2013)

| Facility                            | LHC      | HL-LHC    | ILC500  | ILC500-up | ILC1000      | ILC1000-up     | CLIC            | TLEP (4 IPs) |
|-------------------------------------|----------|-----------|---------|-----------|--------------|----------------|-----------------|--------------|
| $\sqrt{s}$ (GeV)                    | 14,000   | 14,000    | 250/500 | 250/500   | 250/500/1000 | 250/500/1000   | 350/1400/3000   | 240/350      |
| $\int \mathcal{L} dt$ (fb $^{-1}$ ) | 300/expt | 3000/expt | 250+500 | 1150+1600 | 250+500+1000 | 1150+1600+2500 | 500+1500+2000   | 10,000+2600  |
| $\kappa_\gamma$                     | 5 – 7%   | 2 – 5%    | 8.3%    | 4.4%      | 3.8%         | 2.3%           | –/5.5/<5.5%     | 1.45%        |
| $\kappa_g$                          | 6 – 8%   | 3 – 5%    | 2.0%    | 1.1%      | 1.1%         | 0.67%          | 3.6/0.79/0.56%  | 0.79%        |
| $\kappa_W$                          | 4 – 6%   | 2 – 5%    | 0.39%   | 0.21%     | 0.21%        | 0.13%          | 1.5/0.15/0.11%  | 0.10%        |
| $\kappa_Z$                          | 4 – 6%   | 2 – 4%    | 0.49%   | 0.24%     | 0.44%        | 0.22%          | 0.49/0.33/0.24% | 0.05%        |
| $\kappa_\ell$                       | 6 – 8%   | 2 – 5%    | 1.9%    | 0.98%     | 1.3%         | 0.72%          | 3.5/1.4/<1.3%   | 0.51%        |
| $\kappa_d$                          | 10 – 13% | 4 – 7%    | 0.93%   | 0.51%     | 0.51%        | 0.31%          | 1.7/0.32/0.19%  | 0.39%        |
| $\kappa_u$                          | 14 – 15% | 7 – 10%   | 2.5%    | 1.3%      | 1.3%         | 0.76%          | 3.1/1.0/0.7%    | 0.69%        |

$$g(hxx) = \kappa_x g(hxx)_{SM}$$

ILC Higgs White Paper  
*To appear at the end  
of this month.*

Asner, Barklow, Fujii,  
Haber, Kanemura,  
Miyamoto, Weiglein

|                  | ILC(250) | ILC(500) | ILC(1000)    | ILC(LumUp)     |
|------------------|----------|----------|--------------|----------------|
| $\sqrt{s}$ (GeV) | 250      | 250+500  | 250+500+1000 | 250+500+1000   |
| L (fb $^{-1}$ )  | 250      | 250+500  | 250+500+1000 | 1150+1600+2500 |
| $\gamma\gamma$   | 17 %     | 8.3 %    | 3.8 %        | 2.3 %          |
| $gg$             | 6.1 %    | 2.0 %    | 1.1 %        | 0.7 %          |
| $WW$             | 4.7 %    | 0.4 %    | 0.3 %        | 0.2 %          |
| $ZZ$             | 0.7 %    | 0.5 %    | 0.5 %        | 0.3 %          |
| $t\bar{t}$       | 6.4 %    | 2.5 %    | 1.3 %        | 0.9 %          |
| $b\bar{b}$       | 4.7 %    | 1.0 %    | 0.6 %        | 0.4 %          |
| $\tau^+\tau^-$   | 5.2 %    | 1.9 %    | 1.3 %        | 0.7 %          |
| $\Gamma_T(h)$    | 9.0 %    | 1.7 %    | 1.1 %        | 0.8 %          |
| $\mu^+\mu^-$     | 91 %     | 91 %     | 16 %         | 10 %           |
| $hhh$            | –        | 83 %     | 21 %         | 13 %           |
| BR(invis.)       | < 0.7 %  | < 0.7 %  | < 0.7 %      | < 0.3 %        |
| $c\bar{c}$       | 6.8 %    | 2.9 %    | 2.0 %        | 1.1 %          |

*Preliminary*

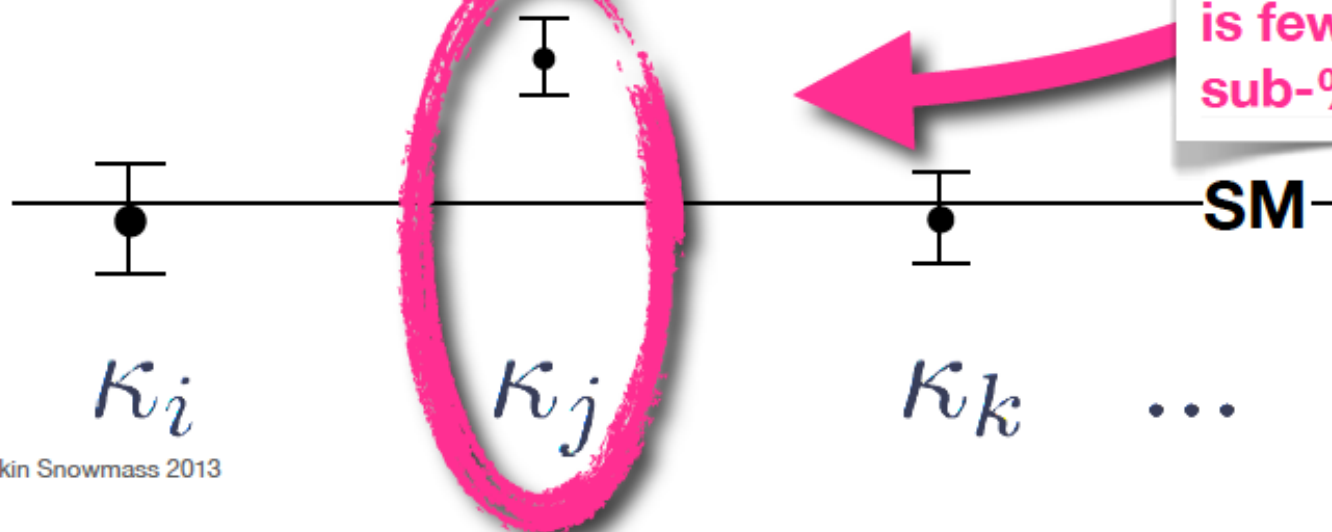


# precision for precision's sake?

No - this is a discovery search

|                 | $\kappa_V$       | $\kappa_b$        | $\kappa_\gamma$ |
|-----------------|------------------|-------------------|-----------------|
| Singlet Mixing  | $\sim 6\%$       | $\sim 6\%$        | $\sim 6\%$      |
| 2HDM            | $\sim 1\%$       | $\sim 10\%$       | $\sim 1\%$      |
| Decoupling MSSM | $\sim -0.0013\%$ | $\sim 1.6\%$      | $< 1.5\%$       |
| Composite       | $\sim -3\%$      | $\sim -(3 - 9)\%$ | $\sim -9\%$     |
| Top Partner     | $\sim -2\%$      | $\sim -2\%$       | $\sim -3\%$     |

Benchmark  
for discovery  
is few % to  
sub-%



# Gauge Couplings $hVV$

$$L = g \sin(\beta-\alpha) hVV + g \cos(\beta-\alpha) HVV$$

- Changed by mixing with the other scalars
- Sum-rule for a multi-doublet structure  $g_{hVV}^2 + g_{HVV}^2 = g_V^2$

$$\sin^2(\beta-\alpha) < 1 \Leftrightarrow (g_{hVV}/g_{hVV}^{\text{SM}})^2 < 1$$

- Higgs sector with an exotic representation

$$(g_{hVV}/g_{hVV}^{\text{SM}})^2 > 1 \text{ is also possible!}$$

$$\frac{g_{hVV}^{\text{THDM}}}{g_{hVV}^{\text{SM}}} = \sin(\beta - \alpha)$$

SM-like case  
 $\sin^2(\beta-\alpha) \approx 1$

Higgs triplet model  
Georgi-Machasek model  
Models with a septet field, ...

*Hisano, Tsumura (13)*

*SK, Kikuchi, Yagyu (13)*

# Yukawa couplings $hff$

Effects of the mixing ( $\alpha$ ,  $\tan\beta$ ) change Yukawa couplings of  $h$

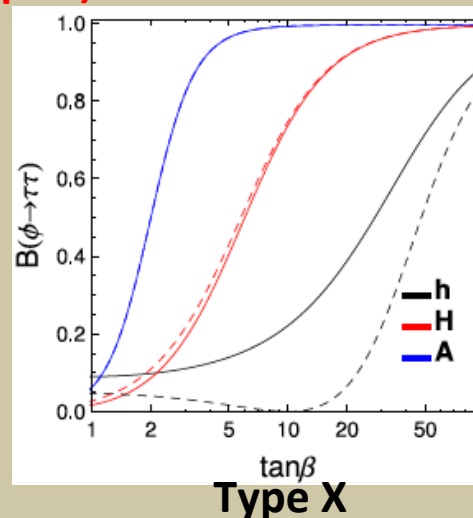
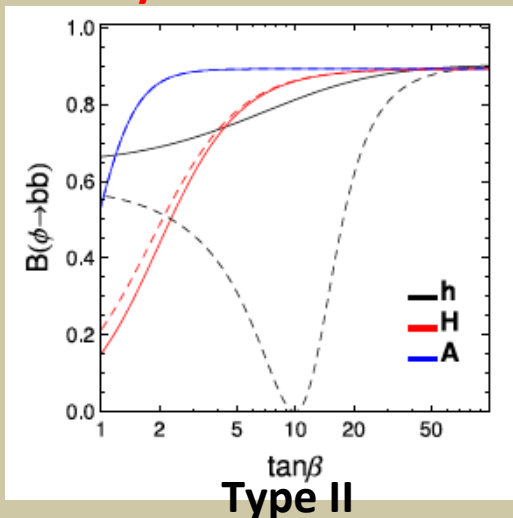
**Type-II**  $hbb \propto \sin(\beta-\alpha) - \tan\beta \cos(\beta-\alpha)$   
 $h\tau\tau \propto \sin(\beta-\alpha) - \tan\beta \cos(\beta-\alpha)$

**Type-X**  $hbb \propto \sin(\beta-\alpha) + \cot\beta \cos(\beta-\alpha)$   
 $h\tau\tau \propto \sin(\beta-\alpha) - \tan\beta \cos(\beta-\alpha)$

|                          | $\Phi_1$ | $\Phi_2$ | $u_R$ | $d_R$ | $\ell_R$ | $Q_L, L_L$ |
|--------------------------|----------|----------|-------|-------|----------|------------|
| Type I                   | +        | -        | -     | -     | -        | +          |
| Type II (SUSY)           | +        | -        | -     | +     | +        | +          |
| Type X (Lepton-specific) | +        | -        | -     | -     | +        | +          |
| Type Y (Flipped)         | +        | -        | -     | +     | -        | +          |

|         | $\xi_h^u$          | $\xi_h^d$           | $\xi_h^\ell$        |
|---------|--------------------|---------------------|---------------------|
| Type-I  | $c_\alpha/s_\beta$ | $c_\alpha/s_\beta$  | $c_\alpha/s_\beta$  |
| Type-II | $c_\alpha/s_\beta$ | $-s_\alpha/c_\beta$ | $-s_\alpha/c_\beta$ |
| Type-X  | $c_\alpha/s_\beta$ | $c_\alpha/s_\beta$  | $-s_\alpha/c_\beta$ |
| Type-Y  | $c_\alpha/s_\beta$ | $-s_\alpha/c_\beta$ | $c_\alpha/s_\beta$  |

Nearly SM-like case:  $\sin^2(\beta-\alpha)=0.99$



Coefficient of  $hff$

S.K., K. Tsumura, H. Yokoya 2013

# Decoupling and heavy Higgs mass

Mass scales of  $H, A, H^\pm$  can be determined by precision measurements of the  $h$  couplings

**MSSM** ( $\alpha$  is a function of  $\tan\beta$  and  $m_A$ )  
Ratio of branching ratios

$$R_{cc+gg/bb} \simeq \left( \frac{m_A^2 - m_h^2}{m_A^2 + m_Z^2} \right)^2 R_{cc+gg/bb}(SM)$$

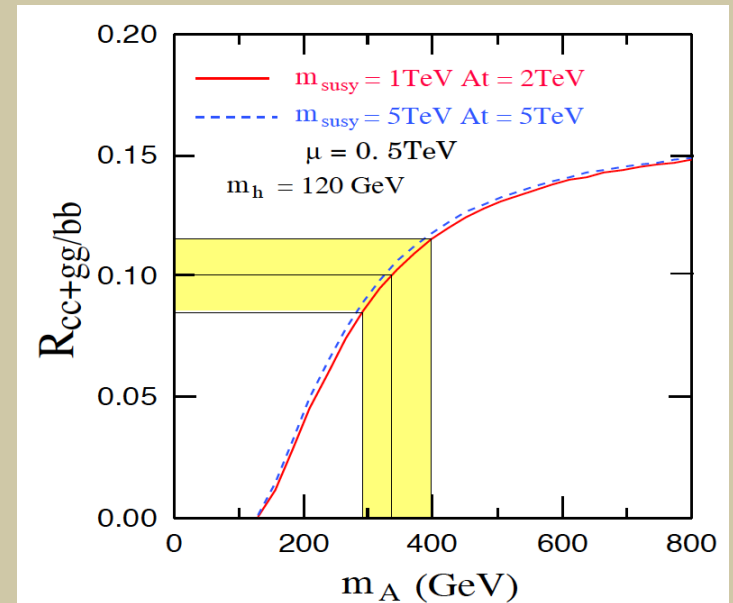
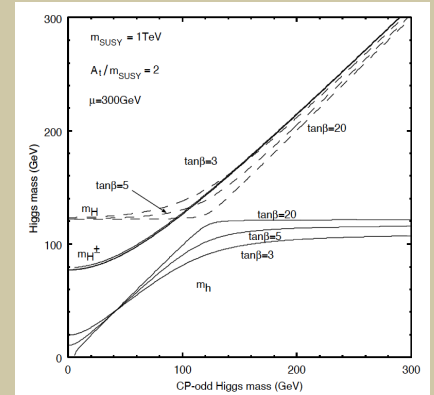
$\tan\beta=5$

$$\frac{g_{hVV}}{g_{SMVV}} \simeq 1 - 0.3\% \left( \frac{200 \text{ GeV}}{m_A} \right)^4$$

$$\frac{g_{htt}}{g_{SMtt}} = \frac{g_{hcc}}{g_{SMcc}} \simeq 1 - 1.7\% \left( \frac{200 \text{ GeV}}{m_A} \right)^2$$

$$\frac{g_{hbb}}{g_{SMbb}} = \frac{g_{h\tau\tau}}{g_{SM\tau\tau}} \simeq 1 + 40\% \left( \frac{200 \text{ GeV}}{m_A} \right)^2.$$

*Peskin et. al (2012)*



*Y. Okada (01)*

# Pattern in deviations of $g_{hVV}$ and $Y_{hff}$

| Model                    | $\mu$ | $\tau$ | $b$ | $c$ | $t$ | $g_V$ |
|--------------------------|-------|--------|-----|-----|-----|-------|
| Singlet mixing           | ↓     | ↓      | ↓   | ↓   | ↓   | ↓     |
| 2HDM-I                   | ↓     | ↓      | ↓   | ↓   | ↓   | ↓     |
| 2HDM-II (SUSY)           | ↑     | ↑      | ↑   | ↓   | ↓   | ↓     |
| 2HDM-X (Lepton-specific) | ↑     | ↑      | ↓   | ↓   | ↓   | ↓     |
| 2HDM-Y (Flipped)         | ↓     | ↓      | ↑   | ↓   | ↓   | ↓     |

$\cos(\beta-\alpha) < 0$

Singlet can be distinguished from the Type-I 2HDM

$Y_{hff}/g_V=1$  in the singlet model but  $Y_{hff}/g_V \neq 1$  in the 2HDM-I

In the triplet model, quark-Yukawa couplings are universally smaller, Lepton-Yukawa deviate univarsal.  $g_V$  can be greater than 1

$g_V > 1$  is a signature of exotic Higgs (with higher representations)

Extended Higgs models are distinguishable by precisely measuring  $hVV$  and  $hff$

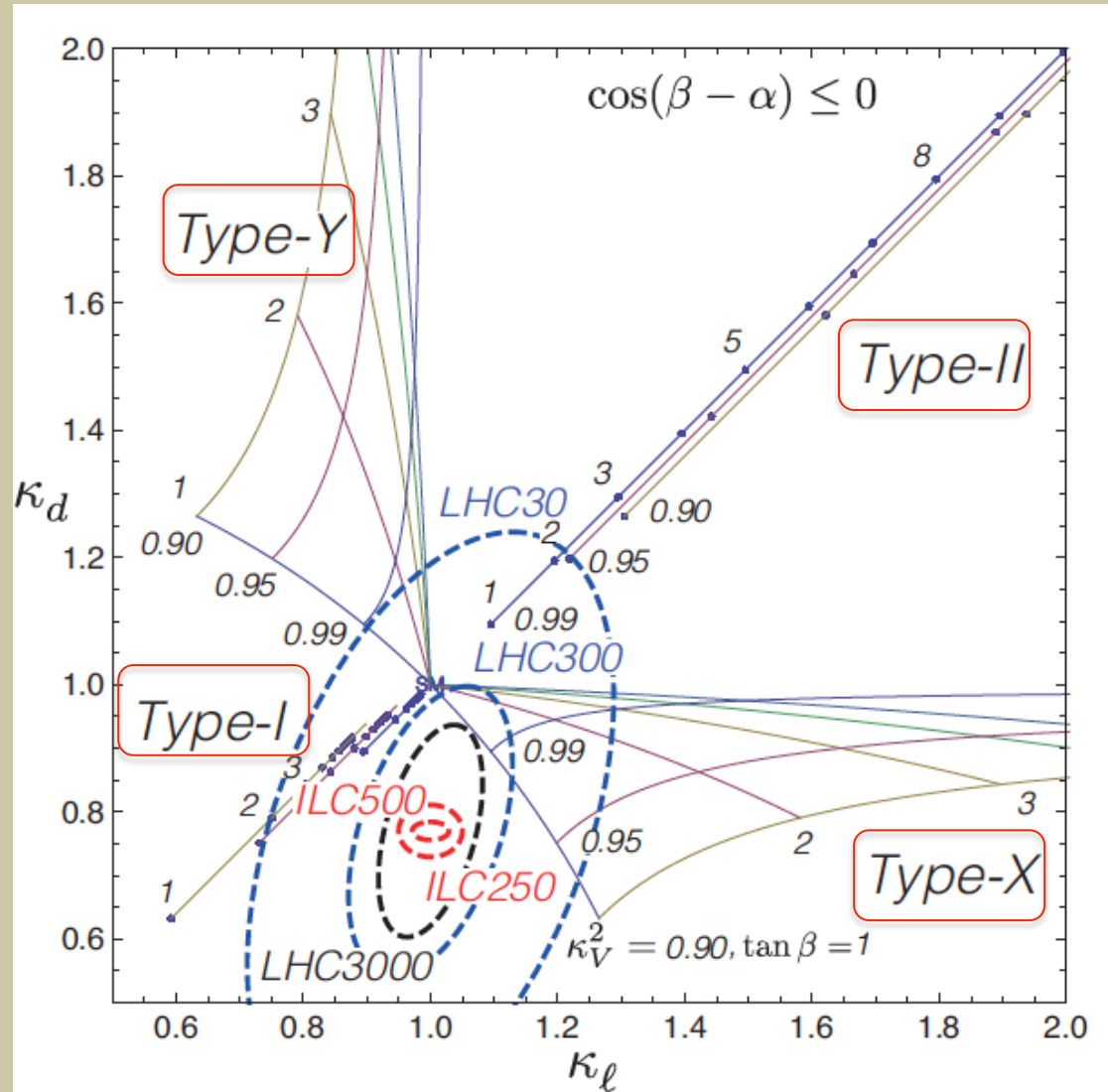
# Fingerptinting the model (2HDM)

SK, K. Tsumura, K. Yagyu, H. Yokoya

**hbb vs h $\tau\tau$**

We can determine  
the type of  
Yukawa interaction  
in the 2HDM

**Ellipse = 68.27% CL**



# Fingerpointing the model (Exotics)

SK, K. Tsumura, K. Yagyu, H. Yokoya

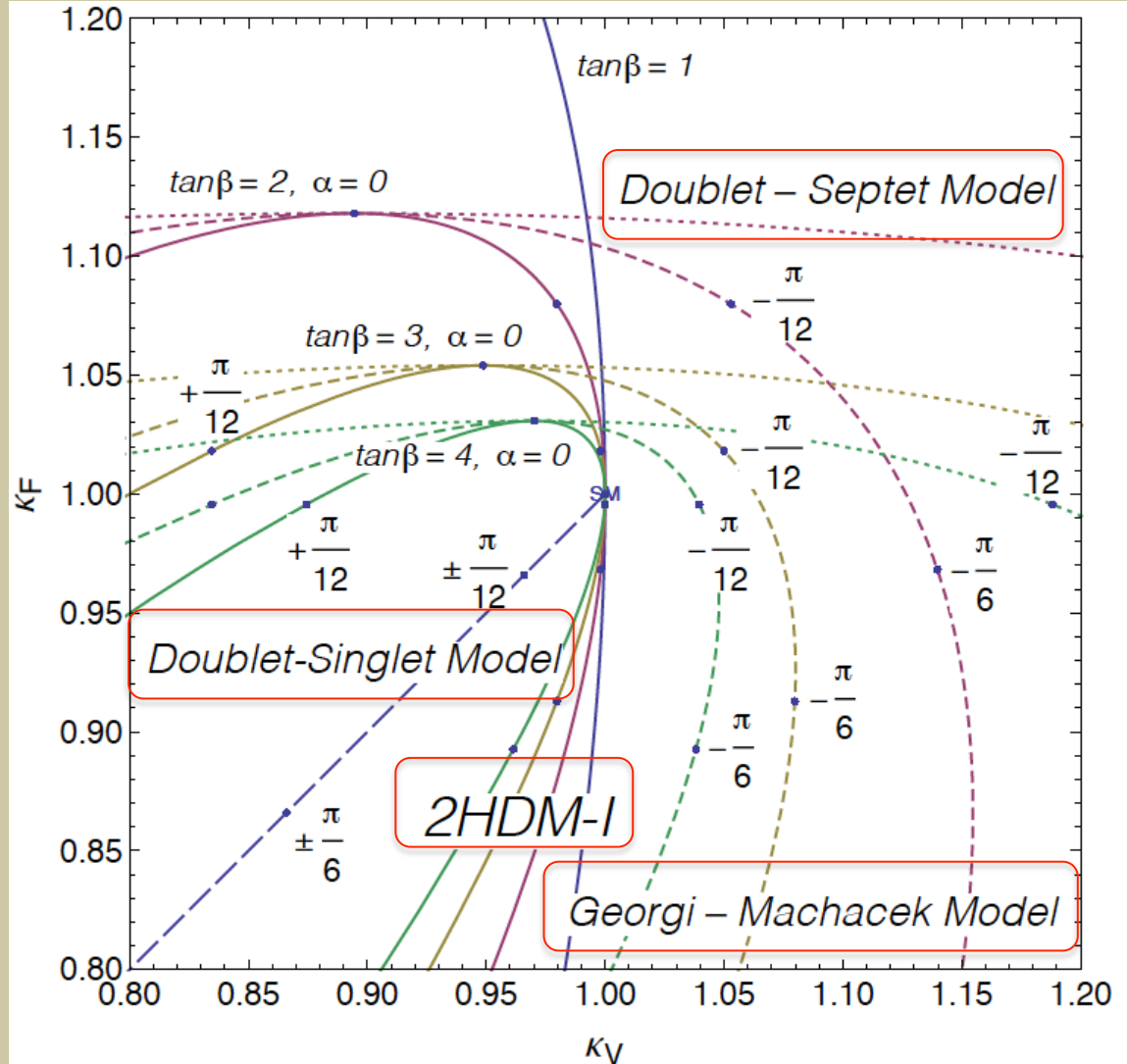
Universal Fermion  
Coupling ( $\kappa_F$ )

VS

$hVV$  coupling ( $\kappa_V$ )

Exotic models  
predict  $\kappa_V > 1$

We can discriminate  
Exotic models



# Fingerpointing the model (Exotics)

SK, K. Tsumura, K. Yagyu, H. Yokoya

Universal Fermion  
Coupling ( $\kappa_F$ )

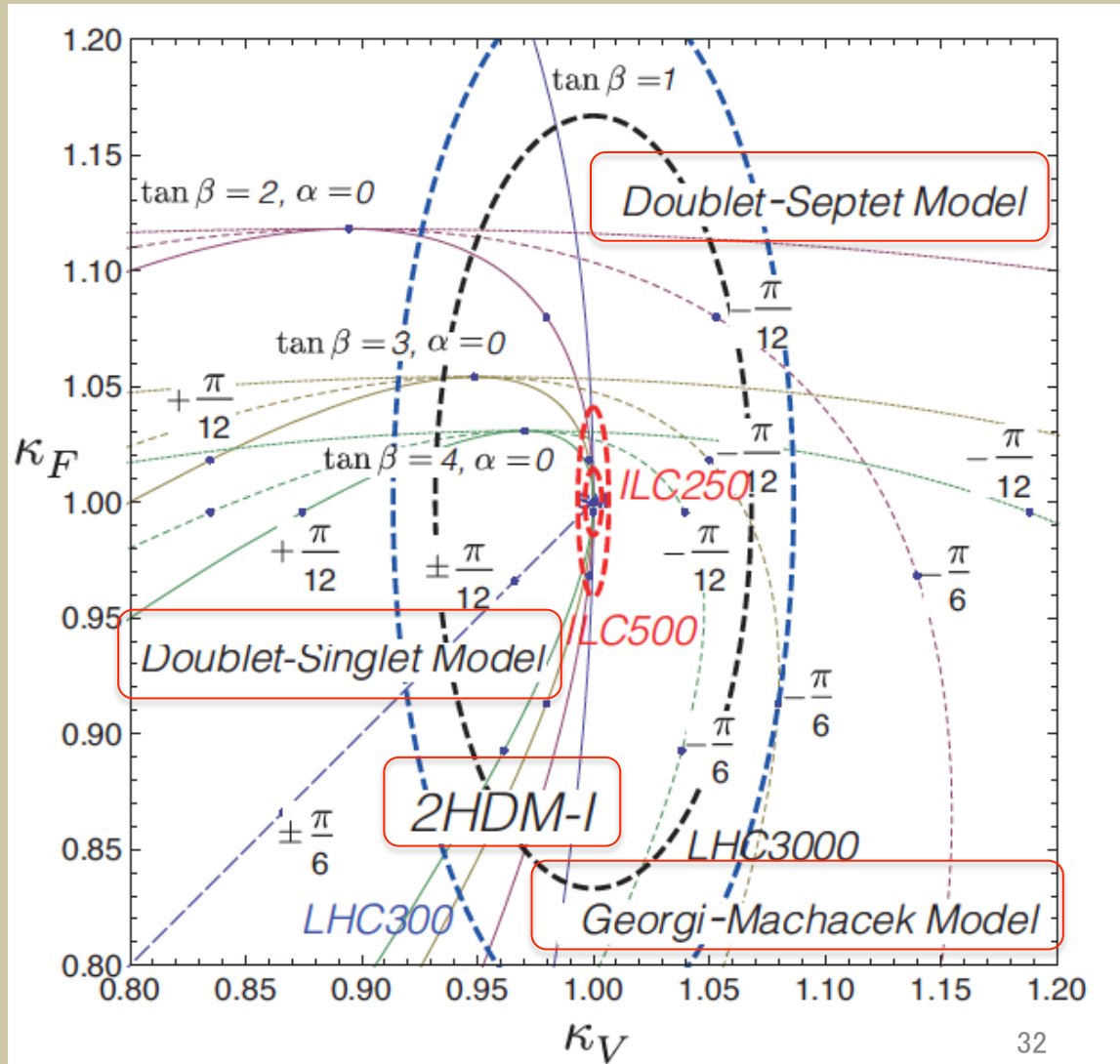
VS

$hVV$  coupling ( $\kappa_V$ )

Exotic models  
predict  $\kappa_V > 1$

We can discriminate  
Exotic models

Ellipse = 68.27% CL





# Measurement of $\tan\beta$ at ILC

SK, Tsumura, Yokoya, arXiv:1305.5424

$\sin(\beta-\alpha)$  and  $\tan\beta$  are important

$hVV \rightarrow \sin(\beta-\alpha)$

How about  $\tan\beta$ ?

## $\tan\beta$ determination

1. Branching ratio of  $H, A$

useful for small  $\tan\beta$

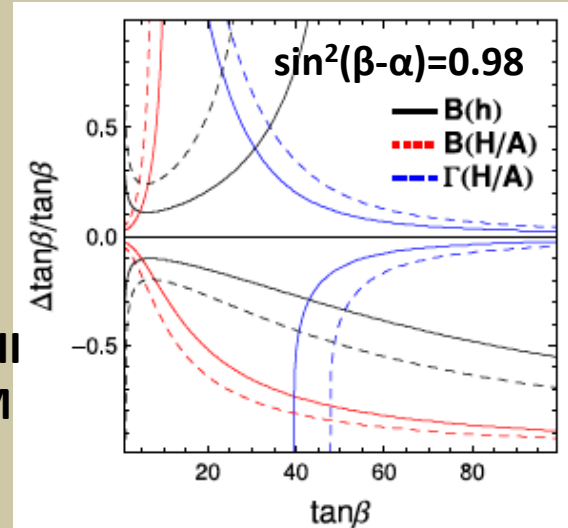
2. Total width of  $H, A$  Berger, Han, jiang (01)  
Gunion, Han, Jiang, Sopczak (03)

useful for large  $\tan\beta$

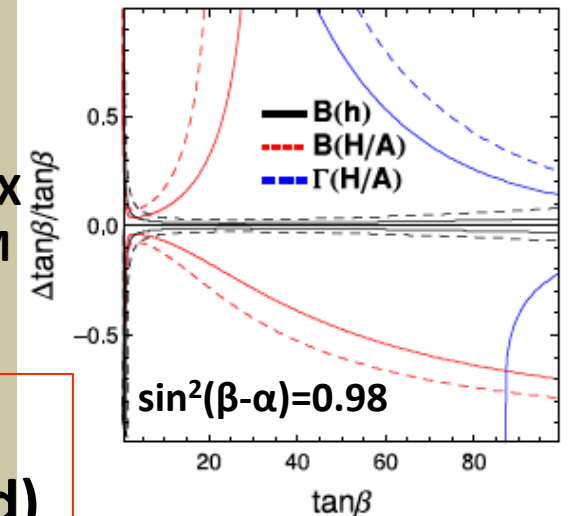
3. Decay of **SM-like Higgs  $h$**  when  $\sin(\beta-\alpha)$  is slightly smaller than 1

SK, Tsumura, Yokoya, arXiv:1305.5424

Type-II  
2HDM



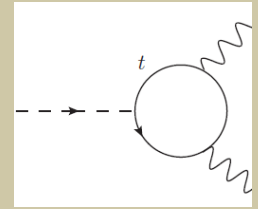
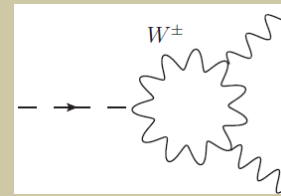
Type-X  
2HDM



Precision measurement of **the  $h$  decay at ILC** is very useful (information of  $H, A$  not required)

# Di-photon Decay Width

Loop induced process in the SM  
New physics effect enters at the same order of perturbation



SM loop destructive

New physics particles which realized a large deviation in  $h \rightarrow \gamma\gamma$

- $W'$  boson
- Singly/Doubly charged scalars
- New charged leptons
- SUSY
- .....

In MSSM, stop effect

$$\frac{g_{h\gamma\gamma}}{g_{h_{SM}\gamma\gamma}} \simeq 1 - 0.4\% \left( \frac{1 \text{ TeV}}{m_T} \right)^2$$

Inner parameters (BSM mass, coupling) can be constrained  
 $\Rightarrow$  Test a model by seeing correlation to the other observable

# Self-coupling $hhh$

It is important to determine the structure of Higgs potential

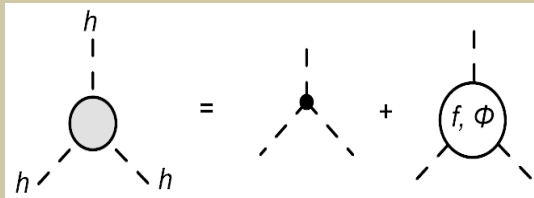
$$V_{\text{Higgs}} = \frac{1}{2} m_h^2 h^2 + \frac{1}{3!} \lambda_{hhh} h^3 + \frac{1}{4!} \lambda_{hhhh} h^4 + \dots$$

Even if  $h$  is SM-like ( $\sin(\alpha-\beta)=1$ ), a large deviation can appear due to non-decoupling loop effects

SM

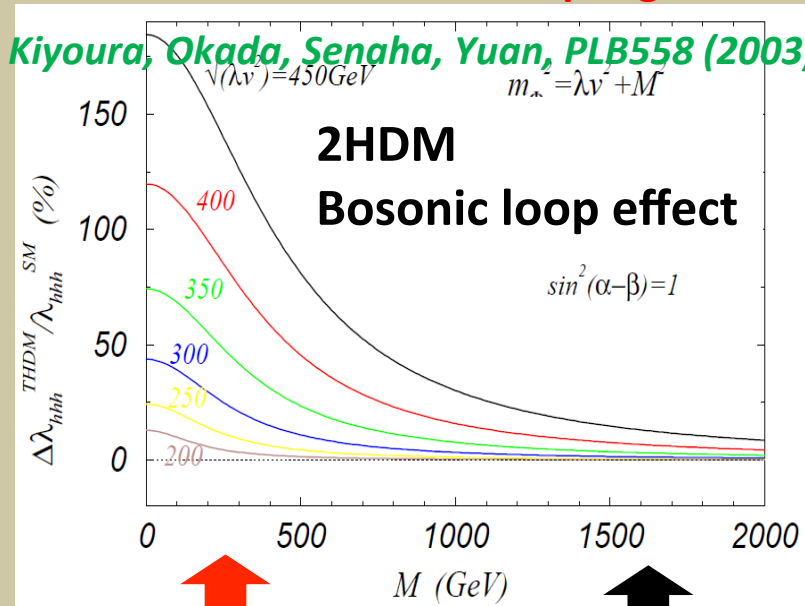
$$\lambda_{hhh}^{\text{SMloop}} \sim \frac{3m_h^2}{v} \left( 1 - \frac{N_c m_t^4}{3\pi^2 v^2 m_h^2} + \dots \right)$$

Non-decoupling effect



$\Phi = H, A, H^\pm$   
 $m_\Phi^2 = M^2 + \lambda_i v^2$

SK, Kiyoura, Okada, Senaha, Yuan, PLB558 (2003)



Non-decoupling effect

Decoupling

In extended Higgs models the deviation can be  $\sim 100\%$  by bosonic loop effect

# EW Baryogenesis and the $hhh$ coupling

SK, Okada, Senaha (2005)

## Higgs Potential at Finite Temperatures

$$V_T(\phi, T) = D(T^2 - T_0^2)\phi^2 - ET\phi^3 + \frac{\lambda_T}{4}\phi^4 + \dots$$

$$\phi_c/T_c = 2E/\lambda_{T_c}$$

$$E = \frac{1}{12\pi v^3}(6m_W^3 + 3m_Z^3) + \text{Non-decoupling effect of new particles}$$

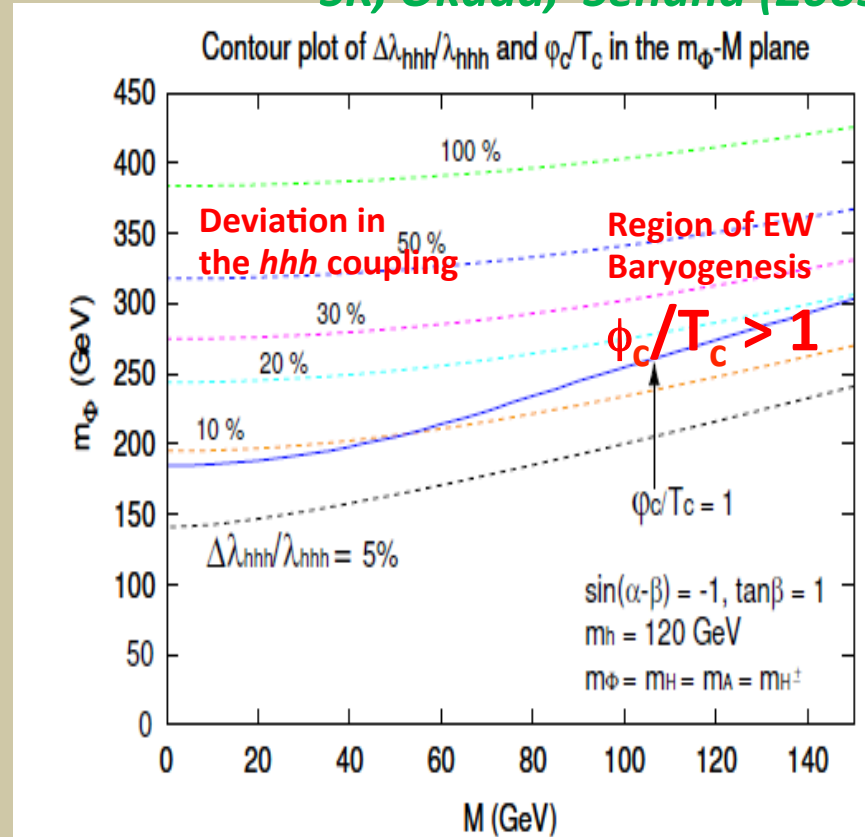
$$\lambda_T = m_h^2/2v^2 + \text{log corrections}$$

### Condition of strongly 1<sup>st</sup> OPT

$$\phi_c/T_c > 1 \Rightarrow 2E/\lambda_{T_c} > 1$$

SM:  $m_h < 60\text{GeV}$ : Excluded !

2HDM:  $m_h = 125\text{GeV}$ : Possible



EW Baryogenesis  $\Leftrightarrow$  Nondecoupling effect  $\Leftrightarrow$  large deviation in  $hhh$

If  $hhh$  can be measured by O(10) %, the scenario of EW Baryogenesis can be tested

Connection between cosmology and collider physics

# Properties of extra Higgs bosons

*$H, A, H^+, H^{++}$*

# MSSM (Type-II 2HDM)

SM-like Higgs  
 $m_h = 126$  GeV

$h$

$hVV$ :  $\sin(\beta - \alpha) \approx 1$

$$\sin(\beta - \alpha) \simeq 1 - \frac{2m_Z^4}{m_A^4 \tan^2 \beta}$$

Extra Higgs bosons

$H, A, H^\pm$

$HVV$ :  $\cos(\beta - \alpha) \ll 1$

$HAZ$ :  $\sin(\beta - \alpha) \approx 1$

$H^+H^-\gamma$ :  $1$

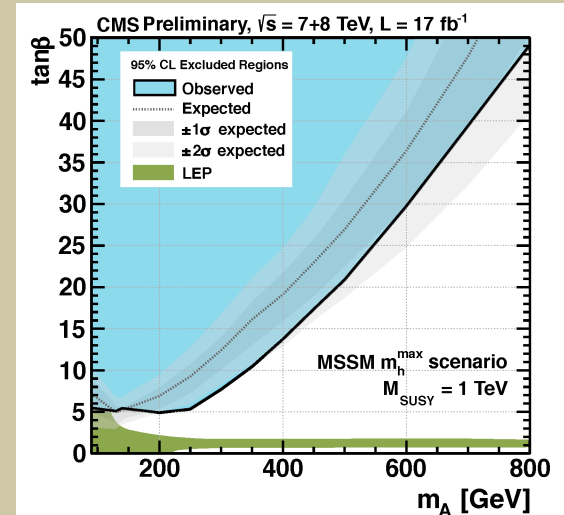
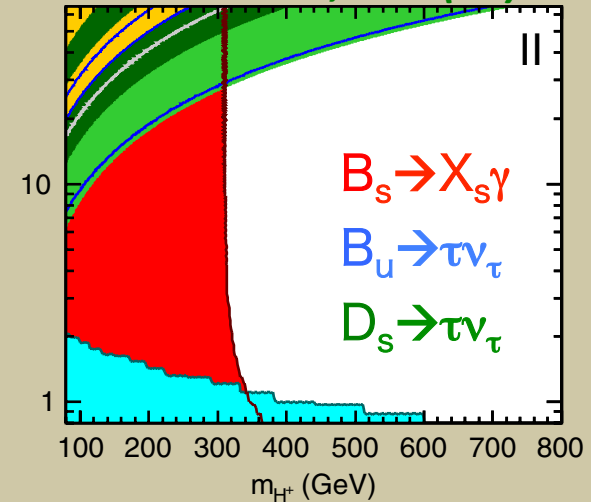
$Htt$  ( $Att$ ):  $m_t \cot \beta$

$Hbb$  ( $Abb$ ):  $m_b \tan \beta$

$H\tau\tau$  ( $A\tau\tau$ ):  $m_\tau \tan \beta$

Flavor experiments and LHC give strong constraints on MSSM (Type-II 2HDM)

Mahmoudi, Stal (09)



# MSSM vs Type X 2HDM

**Type II:  $H, A$  decay into  $bb$**

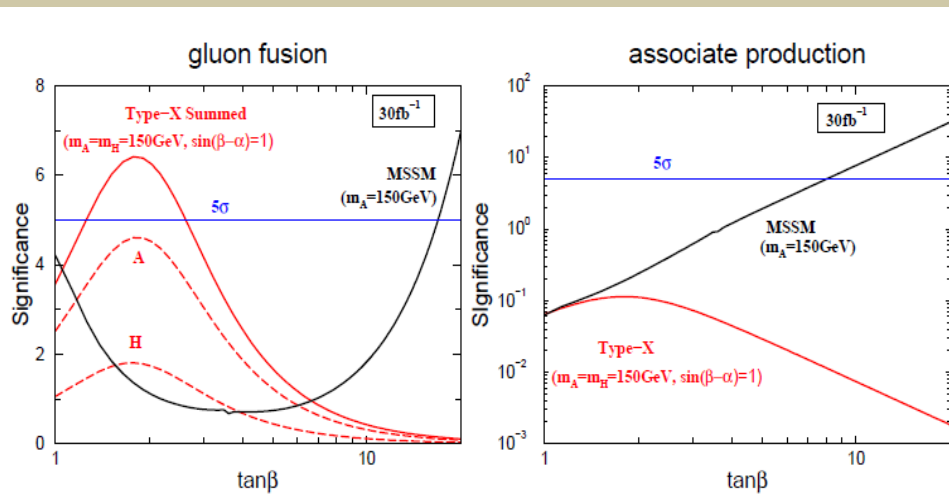
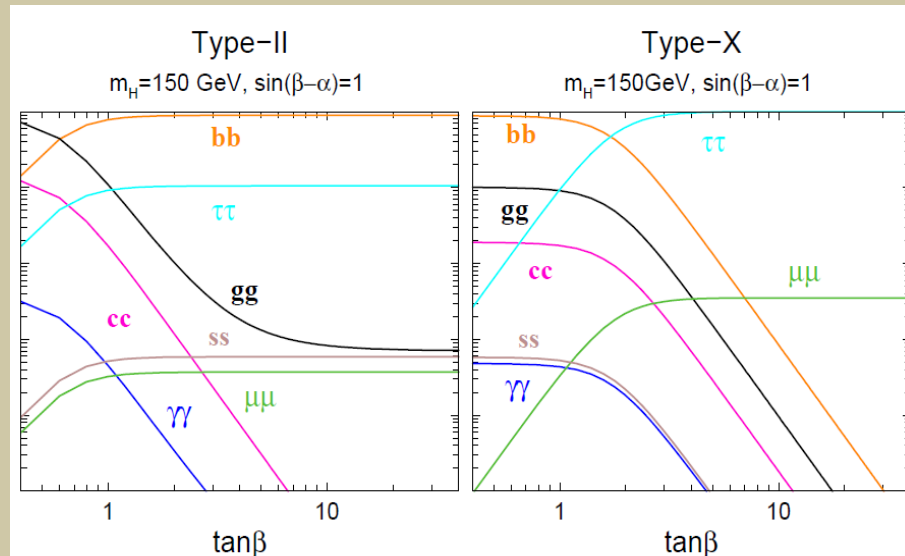
**Type X:  $H, A$  decay into  $\tau\tau$**

At LHC, **Type X 2HDM** can be discriminated from **MSSM (Type-II)** by the combination of  $\tau\tau$  gluon fusion

$$pp \rightarrow A (H) \rightarrow \tau\tau$$

and  $bb$  associate (H)A production

$$pp \rightarrow bbA (bbH)$$

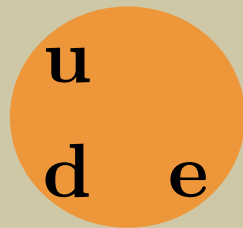
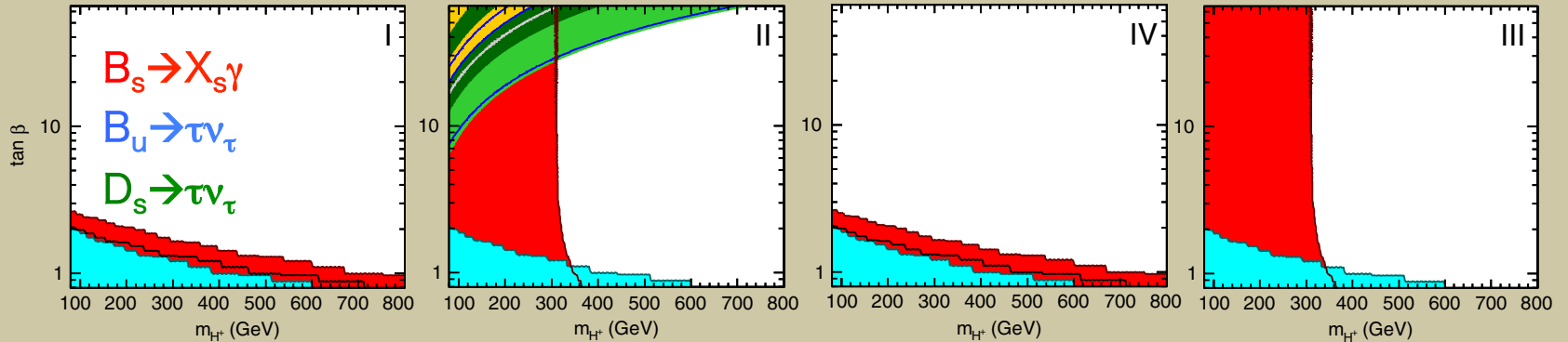


|         | $\xi^u$       | $\xi^d$        | $\xi^\ell$     |
|---------|---------------|----------------|----------------|
| Type-I  | $1/\tan\beta$ | $-1/\tan\beta$ | $-1/\tan\beta$ |
| Type-II | $1/\tan\beta$ | $\tan\beta$    | $\tan\beta$    |
| Type-X  | $1/\tan\beta$ | $-1/\tan\beta$ | $\tan\beta$    |
| Type-Y  | $1/\tan\beta$ | $\tan\beta$    | $-1/\tan\beta$ |

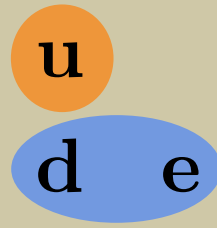
# Non-SUSY 2HDM

## Constraint from flavor physics

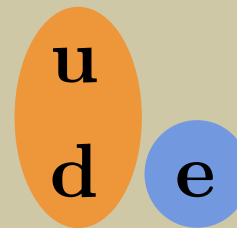
*Mahmoudi, Stal (09)*



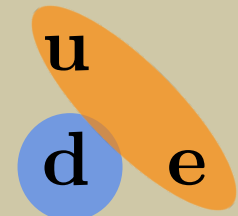
Type-I



Type-II



Type-X



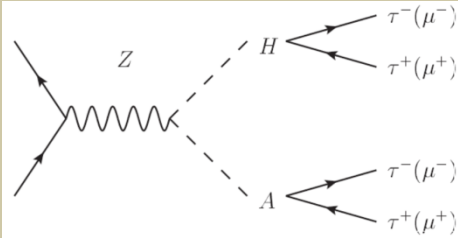
Type-Y

In Type-I and **Type-X**, **light**  $H, A, H^+$  can be allowed  
 $\Rightarrow$  **Pair Production**



# HA Production (Type X 2HDM)

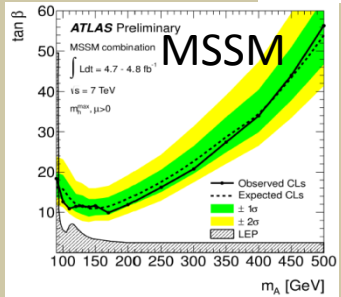
LHC



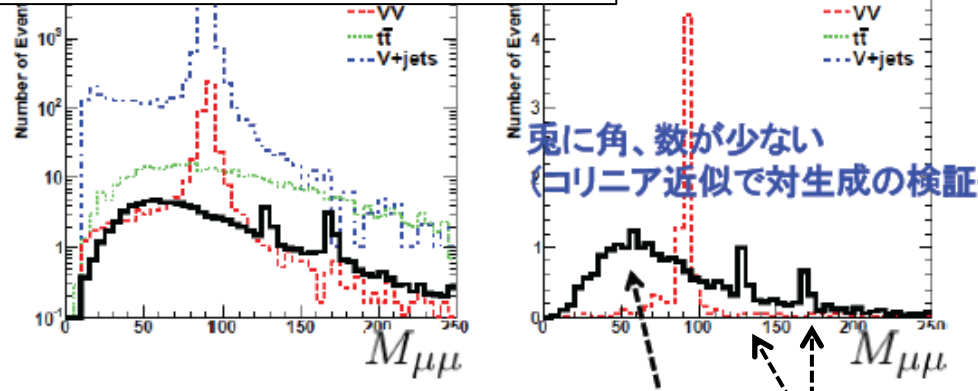
$$\sigma(pp \rightarrow HA) = \mathcal{O}(10-100) \text{ fb}$$

Differently from MSSM  
( $bbH, H \rightarrow \mu\mu, \tau\tau$ )

Rather hard to see Type-X at LHC



$\tau_h \tau_h \mu\mu$  event ( $100 \text{ fb}^{-1}$ )



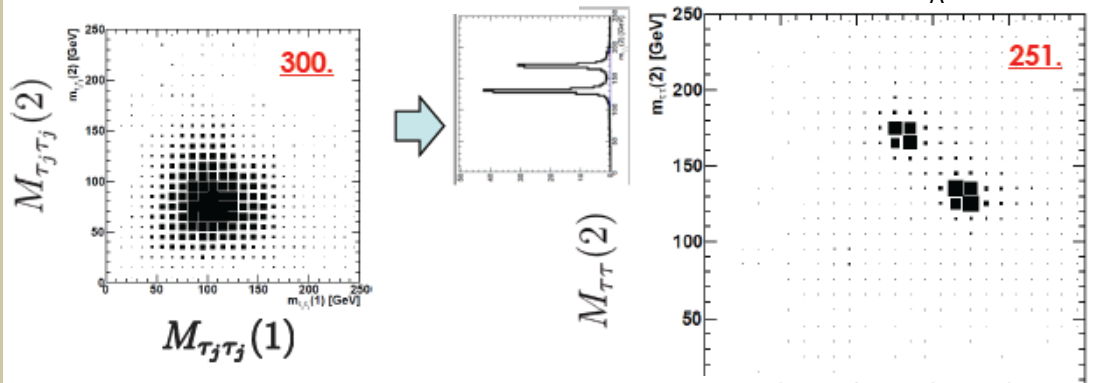
$4\tau \rightarrow 2\mu 2\tau_j$   
 $m_H = 130 \text{ GeV}$   
 $m_A = 170 \text{ GeV}$

ILC

HA can be reconstructed  
by collinear approximation

$$\vec{p}_\nu \simeq c \vec{p}_{\tau_j} \quad \vec{p}_{\tau_j} \simeq z \vec{p}_\tau = \frac{1}{1+c} \vec{p}_\tau$$

| $4\tau_h$ event analysis              | HA   | VV   | $t\bar{t}$ | $S$ ( $100 \text{ fb}^{-1}$ ) |
|---------------------------------------|------|------|------------|-------------------------------|
| Pre-selection                         | 300. | 10.6 | 1.2        | 38.                           |
| $0 \leq z_{1-4} \leq 1$               | 251. | 6.2  | 0.1        | 38.                           |
| $(m_Z)_{\tau\tau} \pm 20 \text{ GeV}$ | 238. | 1.8  | 0.         | 43.                           |



Reconstruction of invariant  
masses of the two  $\tau$  systems is  
possible

SK, Tsumura, Yokoya (11)

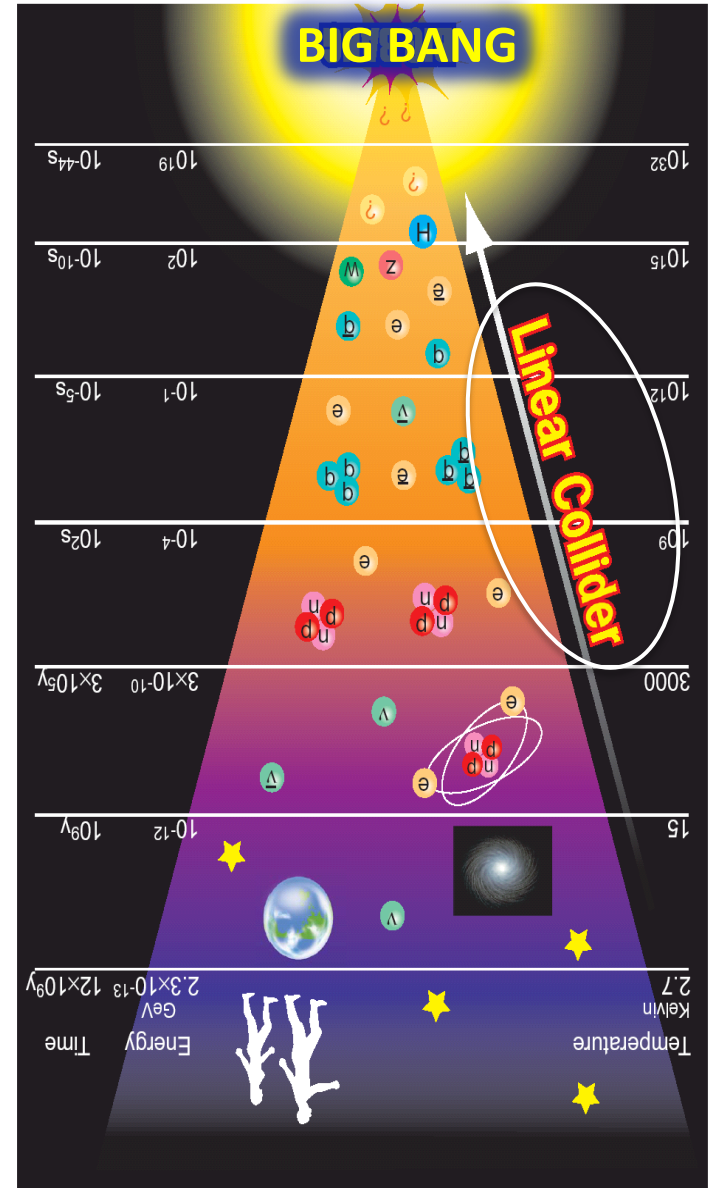
# Summary

- A SM-like Higgs boson  $h$  was discovered
- The Higgs sector remains unknown **SM-like  $\neq$  SM**

## Extended Higgs $\Leftrightarrow$ New Physics

- Detailed study of  $h$  makes it clear the shape and dynamics of Higgs sector (**Finger printing models**)
- Direct Searches of  $H, A, H^+, H^{++}$  at LHC (and ILC)
- **Higgs is a good probe of new physics BSM!**

# We need LC



# ***Back Up Slides***

## Higgs self-coupling @ 1 TeV

$$P(e^-, e^+) = (-0.8, +0.2) \quad e^+ + e^- \rightarrow \nu\bar{\nu}HH \quad M(H) = 120\text{GeV} \quad \int L dt = 2\text{ab}^{-1}$$

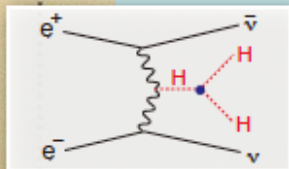
|              | Expected           | After Cut |
|--------------|--------------------|-----------|
| vvhh (WW F)  | 272                | 35.7      |
| vvhh (ZHH)   | 74.0               | 3.88      |
| BG (tt/vvZH) | $7.86 \times 10^5$ | 33.7      |
| significance | 0.30               | 4.29      |

- better sensitive factor
- benefit more from beam polarization
- BG tt x-section smaller
- more boosted b-jets

$$\frac{\Delta\sigma}{\sigma} \approx 23\% \quad \frac{\Delta\lambda}{\lambda} \approx 18\%$$

Double Higgs excess significance:  $> 7\sigma$

Higgs self-coupling significance:  $> 5\sigma$



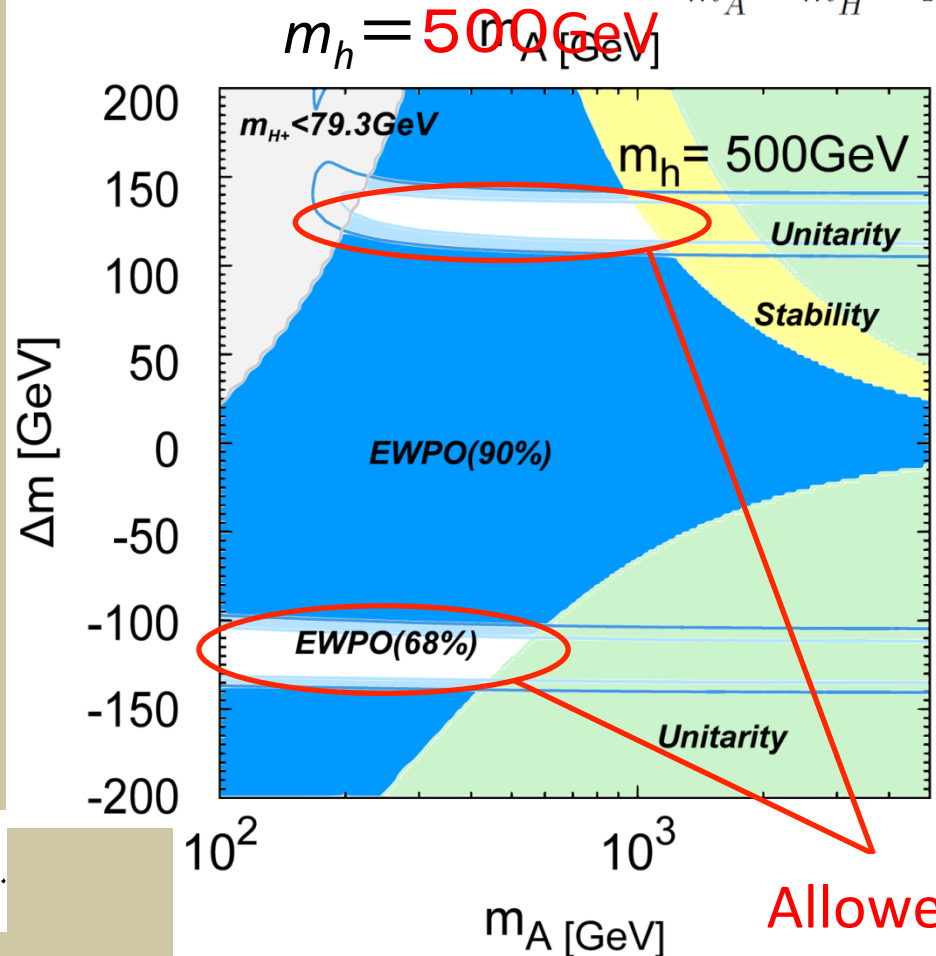
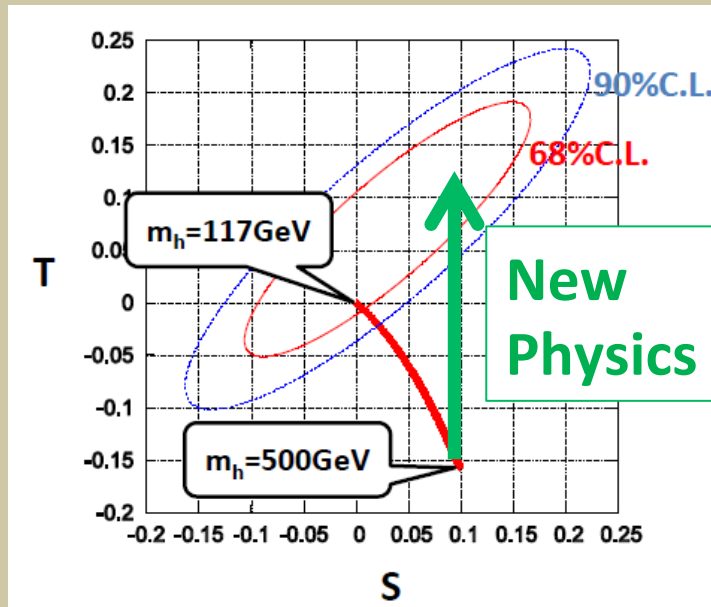
# LEP/SLC did not require SM-like Higgs

A heavy  $h$  was also allowed by non-standard effects

$$\Delta m = m_A - m_{H^\pm}$$

$$\sin(\beta - \alpha) = 1$$

$$m_A^2 = m_H^2 = M^2$$



Case of the 2 Higgs doublet model

$$\Delta T_{\text{Higgs}} \sim -\ln \frac{m_h^2}{M_W^2} + \frac{(m_A^2 - m_{H^\pm}^2)^2}{M_W^2 m_A^2} (\sim 0).$$

Allowed

# SUSY and $m_h=126\text{GeV}$

Higgs potential

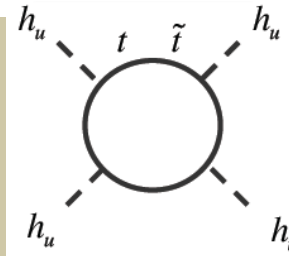
$$V = |D|^2 + |F|^2 + (\text{soft-breaking})$$

MSSM is type-II 2HDM ( $H_u, H_d$ )

Self-coupling comes from gauge couplings  $g, g' \Rightarrow m_h < m_Z$  at tree level

$$m_h^2 < m_Z^2 \cos^2 2\beta + \frac{3m_t^4}{2\pi^2 v^2} \left[ \ln \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{A_t^2}{m_t^2} \left( 1 - \frac{A_t^2}{12m_{\tilde{t}}^2} \right) \right]$$

Loop effect



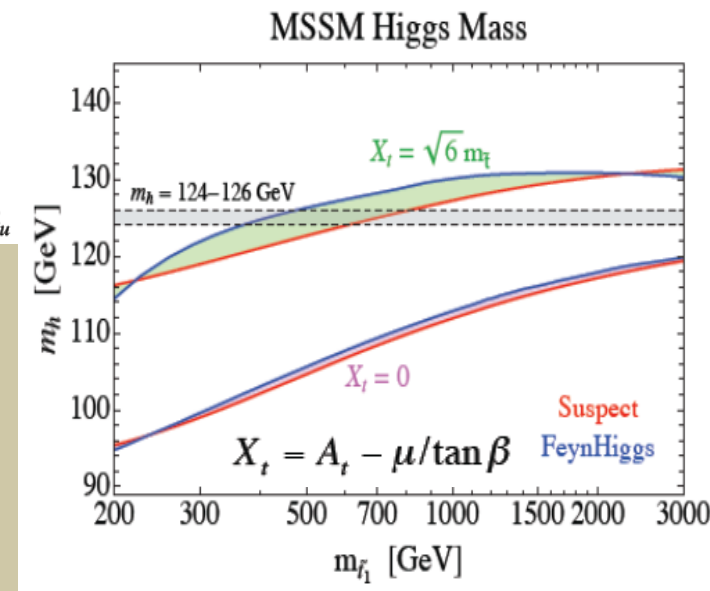
126 GeV can be realized by

Large Stop Masses OR Large Stop LR-mixing

$$M_{SUSY} \sim 10\text{TeV} (X_t=0)$$

Consistent with the data

But tension with Hierarchy Problem



Hall, Pinner, Ruderman (2011)

# Extended SUSY models

It is possible to gain  $m_h$  by NEW F-term, D-term or loop effects

$$m_h^2 = \left[ \text{Diagram 1} + \text{Diagram 2} \right] \text{MSSM}$$

Diagram 1: Tree-level Higgs mass from  $D_{W,B}$  term with couplings  $g_{1,2}$  and external legs  $h_u$ .

Diagram 2: Loop-level Higgs mass from top quark and stop squark ( $t, \tilde{t}$ ) loop with external legs  $h_u$ .

**F-term** +  $\left[ \text{Diagram 3} \right]$

Diagram 3: Tree-level Higgs mass from  $F_S$  term with couplings  $\lambda$  and external legs  $h_u$ .

**D-term** +  $\left[ \text{Diagram 4} \right]$

Diagram 4: Tree-level Higgs mass from  $D_{Z'}$  term with couplings  $g_X$  and external legs  $h_u$ .

**Loop-effect** +  $\left[ \text{Diagram 5} \right]$

Diagram 5: Loop-level Higgs mass from new matter particles ( $Q', U', Y'$ ) loop with external legs  $h_u$ .

**Addition of new Singlet, Triplet**

Ex) NMSSM

$$\Delta m_h^2 = \frac{\lambda_S^2 v^2}{2} \sin^2 2\beta$$

**New gauge symmetry  $U(1)_X$**

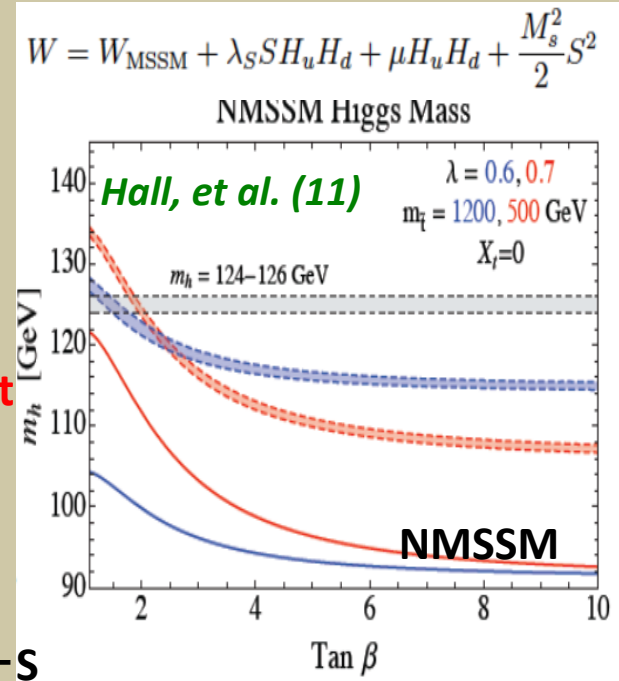
Ex) MSSM + RH-Neutrino + S + S

$$\Delta m_h^2 \simeq 2g_X^2 x^2 (v_{H_u}^2 + v_{H_d}^2) \cos^2(2\beta) \frac{2m_S^2}{2m_S^2 + m_{Z'}^2}$$

**Loop effect by new matter particles**

Ex) Strong-but-Light Scenario (for EWBG)

$$\Delta m_h^2 = \frac{3Y'^4 v^2}{4\pi^2} \ln \frac{m_S^2}{m_F^2}$$

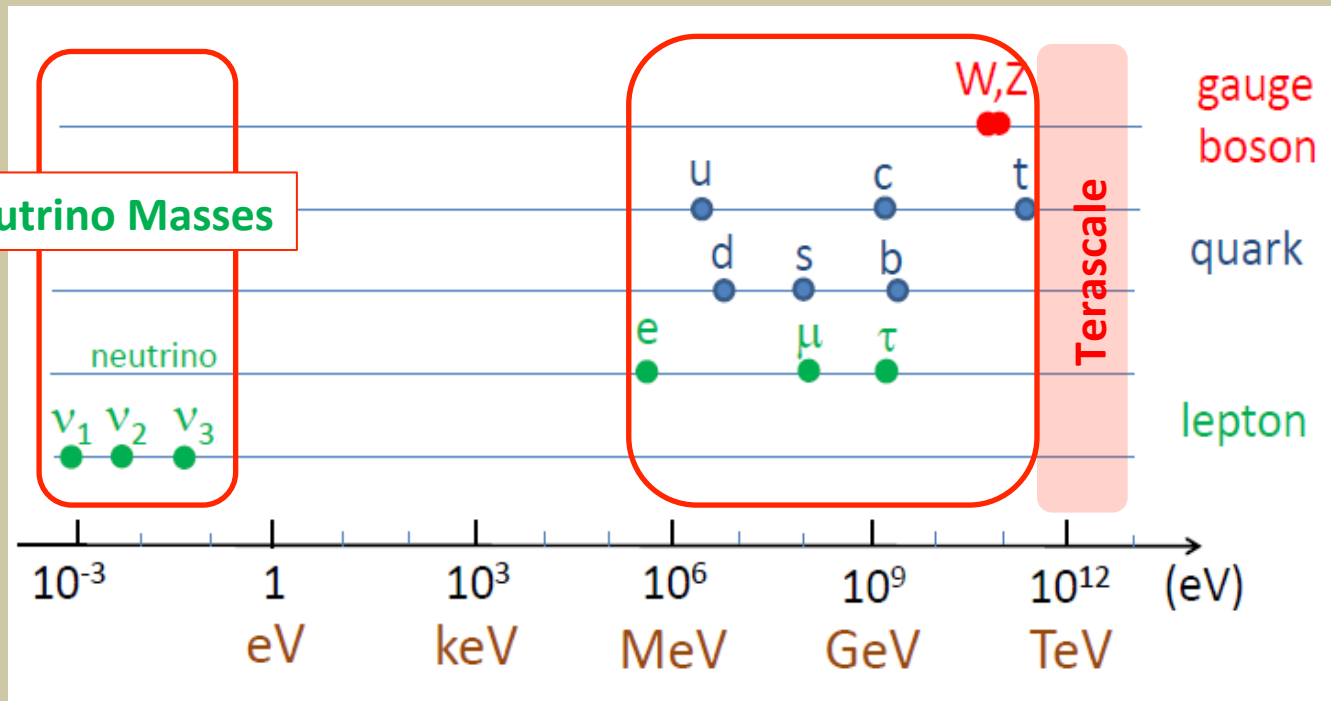


*Endo, Hamaguchi, Iwamoto, Yokozaki (11)*

*SK, Shindo, Yamada (12)*



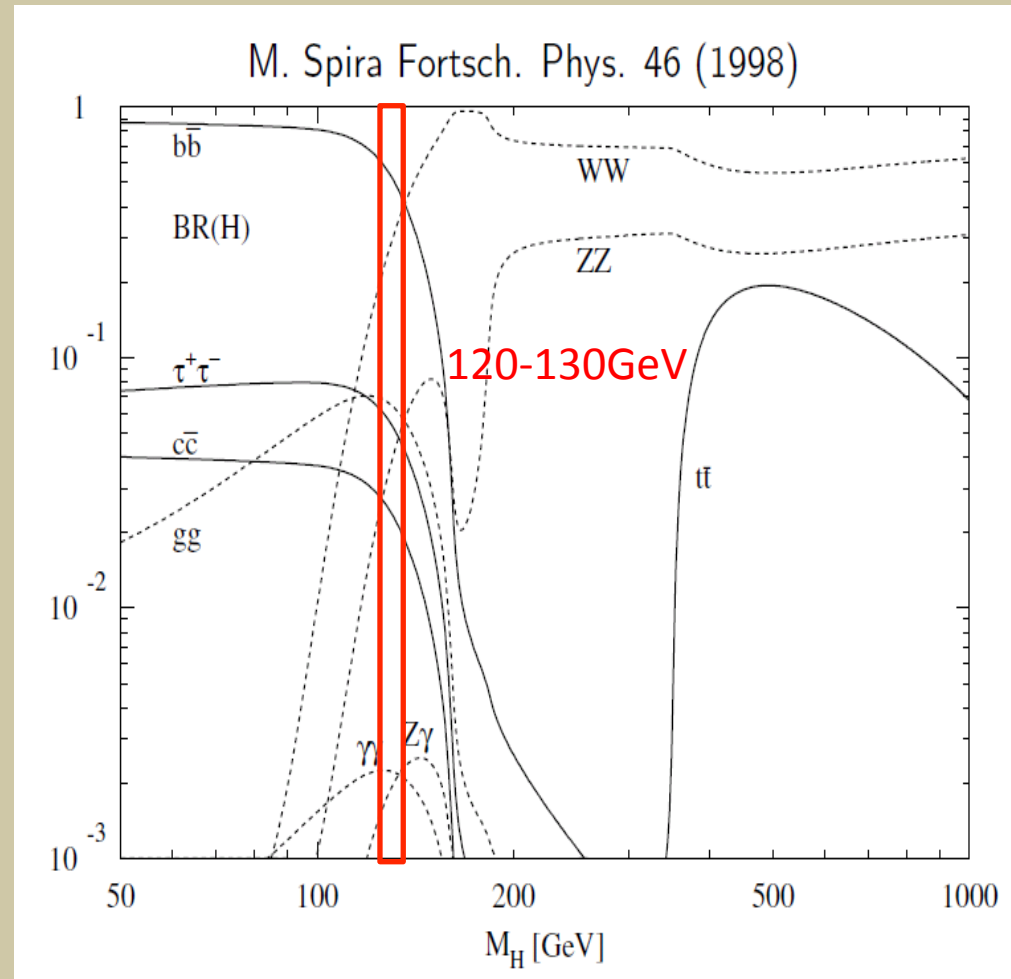
# Mass spectrum of particles

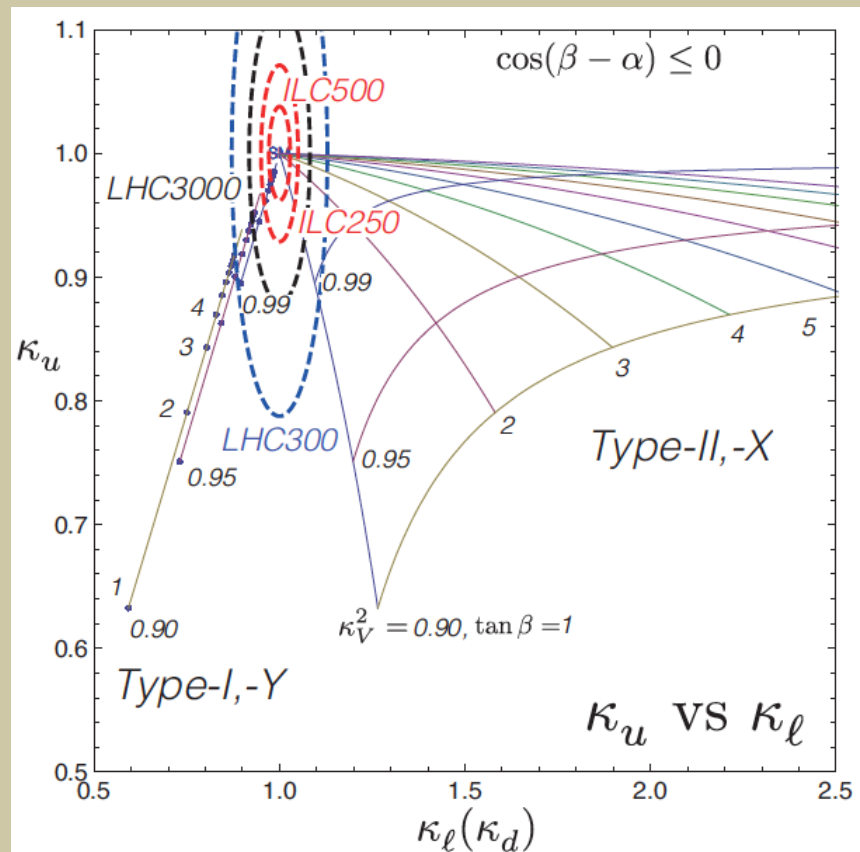
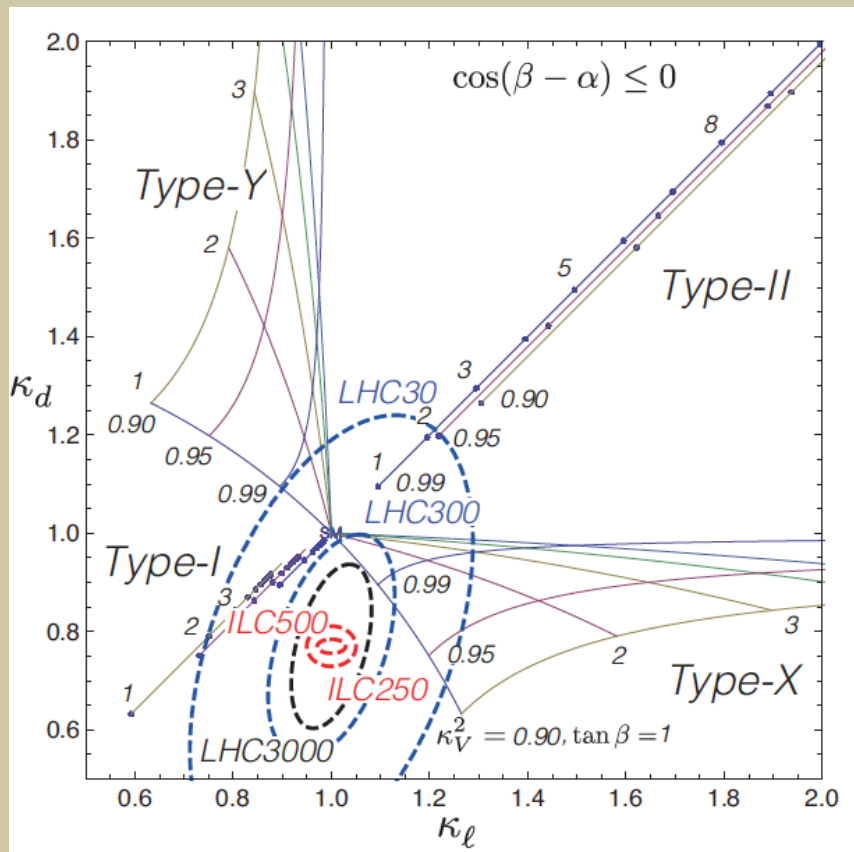


Masses of particles are zero in the Lagrangian Vacuum gives masses to them by EWSB

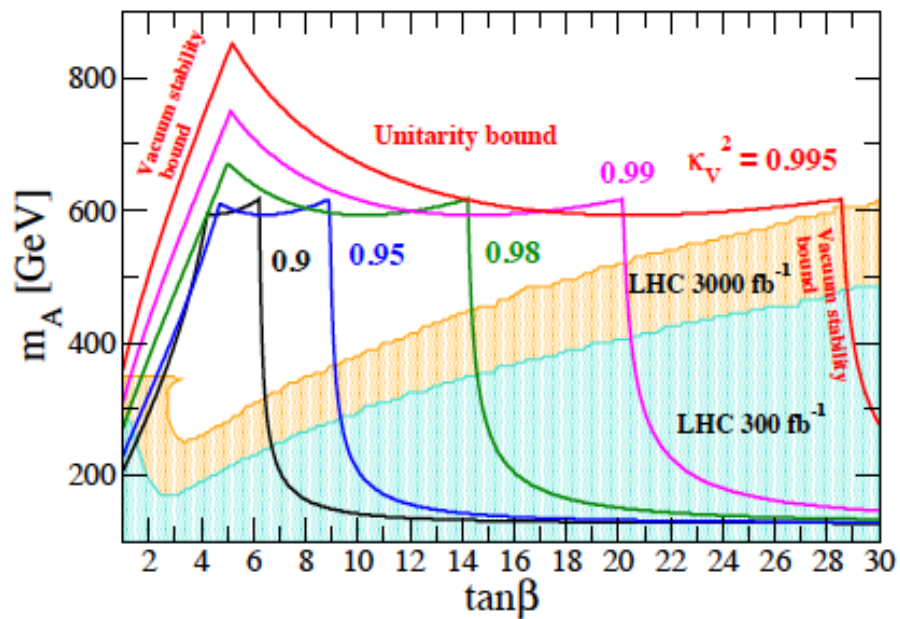
# Decay branching ratios of SM Higgs

- SM Higgs couples to all the particles  
[ $h\gamma\gamma$ ,  $hgg$  (via loop)  
 $hh\nu\nu$  (dim-5)]
- For  $m_h=126$  GeV,  
various decay modes  
can be available





Type-II THDM



Type-X THDM

