

Jet substructure and infrared QCD dynamics

Mrinal Dasgupta

The University of Manchester

Trento, 19 September 2013

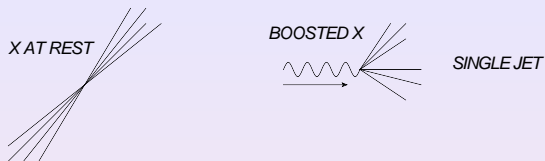
In collaboration with Gavin Salam, Simone Marzani,
Alessandro Fregoso, Alex Powling

- Boosted object LHC searches and jet substructure
- Substructure techniques and recent advances
- Infrared QCD dynamics and **understanding jet substructure**
 - Resummed calculations for jet substructure observables
 - Comparisons to event generator tools
 - Designing modified tools
- Outlook

LHC searches in the highly boosted regime

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Exploits situations where $p_T \gg M_X$. Decay products encompassed in a single **fat jet**.

$$\theta^2 = \frac{M_X^2}{p_T^2 z(1-z)}$$

Either

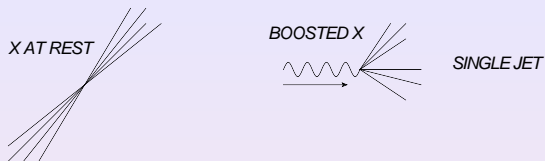
- New heavy particles decay to lighter (boosted) EW scale particles
- Look at high p_T regime of say Higgs production

Initial idea goes back to Seymour 1993

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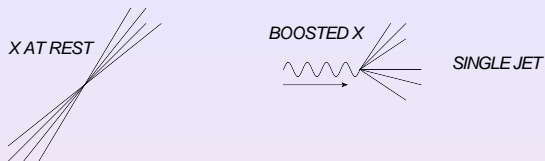
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Jet substructure methods – basic ideas

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$$\phi(z) \propto 1 \text{ vs } \phi(z) \propto \frac{1+z^2}{1-z}$$

Jet substructure methods become **powerful** discovery tools.
Main ideas are

- Use knowledge about QCD radiation to **discriminate** against background and **tag** signal. **Cut on z** to discriminate against bckgd.
- Use **grooming** techniques to clean signal of contamination from ISR, UE/pile-up. Typically **Smaller angular scale** involved.

10-20 different techniques introduced.
the last 5 years

Over 100 papers in

Jet substructure methods – basic ideas

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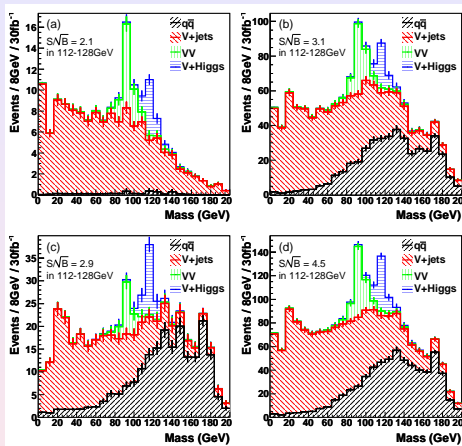
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Example : The BDRS method for Higgs searches

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Rescued an unpromising channel. Associated Higgs production $V + H$ with Higgs decays to $b\bar{b}$. Uses the **mass-drop+filtering** substructure method of BDRS.

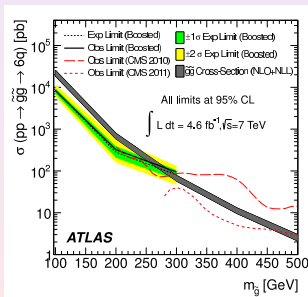
Butterworth, Davison, Rubin and Salam 2008. 

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- A plethora of different methods exist by now
 YSplitter, Mass-drop + filtering, pruning, trimming, ATLAS top tagger, JH top tagger, CMS top tagger, Planar Flow, N subjettiness, Q jets, Templates etc.
- Many methods are being implemented in searches



ATLAS collaboration, 2012

A list of open questions

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- Do we really need so many different taggers?
- In what ways are they similar and where are the differences?
- Are some methods better than others?
- How do results obtained depend on the **many** parameters of the taggers?
- How to make the best choice of a tagger for a given search?

Field may look bewildering to an outsider. Insiders need to really understand techniques in more detail to ensure robustness.

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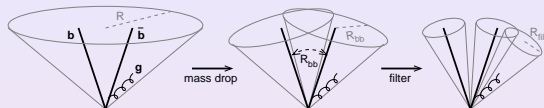
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Current taggers – mass drop

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Definition

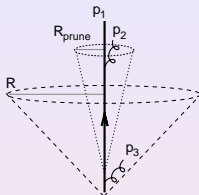
- Break the jet j into two subjects by undoing its last stage of clustering. Label the two subjects j_1, j_2 such that $m_{j_1} > m_{j_2}$.
- If there was a significant mass drop, $m_{j_1} < \mu m_j$, and the splitting is not too asymmetric, $y = \min(p_{t_1}^2, p_{t_2}^2) \Delta R_{j_1 j_2}^2 / m_j^2 > y_{\text{cut}}$, then deem j to be the tagged jet
- Otherwise redefine j to be equal to j_1 and go back to step 1 (unless j consists of just a single particle, in which case the original jet is deemed untagged).

Definition changed to follow more **energetic** branch rather than heavier branch - **modified** Mass Drop Tagger.

Current-taggers –pruning

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Definition

Pruning [7,8] takes an initial jet, and from its mass deduces a pruning radius $R_{\text{prune}} = R_{\text{fact}} \cdot \frac{2m}{p_t}$, where R_{fact} is a parameter of the tagger. It then reclusters the jet and for every clustering step, involving objects a and b , it checks whether $\Delta_{ab} > R_{\text{prune}}$ and $\min(p_{ta}, p_{tb}) < z_{\text{cut}} p_{t,(a+b)}$, where z_{cut} is a second parameter of the tagger. If so, then the softer of the a and b is discarded. Otherwise a and b are recombined as usual. Clustering then proceeds with the remaining objects, applying the pruning check at each stage.

Several techniques around. Natural to compare them.

The [Monte Carlo] findings discussed above indicate that while [pruning, trimming and filtering] have qualitatively similar effects, there are important differences. For our choice of parameters, pruning acts most aggressively on the signal and background followed by trimming and filtering.

Boost 2010 proceedings

- No clear picture of why taggers are similar or different
- No idea of how these findings depend on tagger parameters or jet masses or p_t .

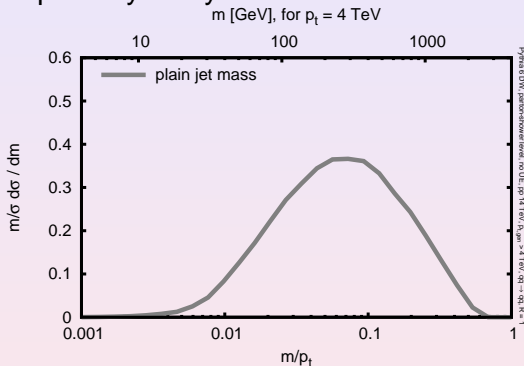
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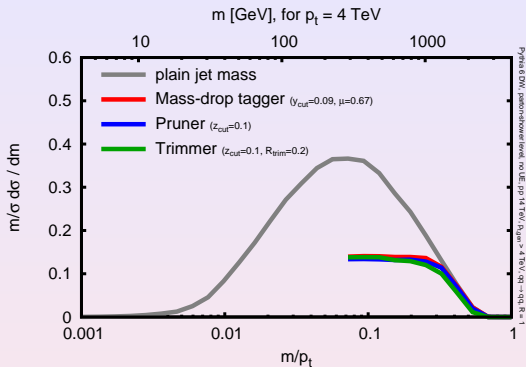
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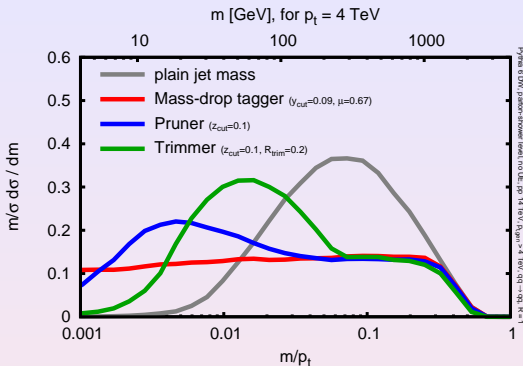
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The right MC study can already be instructive. But is often inspired by analytics!



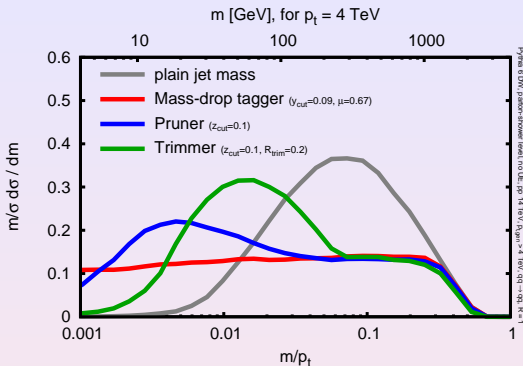


Taggers look similar



But only for a limited mass range How do we understand what we are seeing? Why do pruning and trimming have kinks? Can we compute the positions?

Needs analysis and calculation



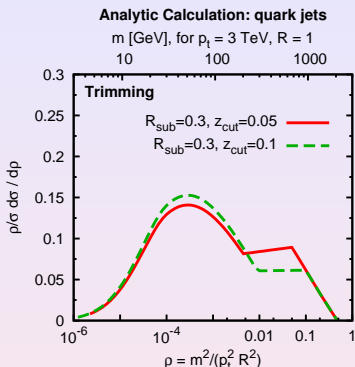
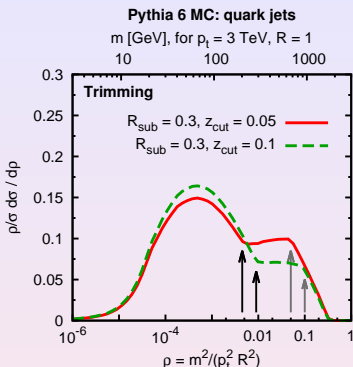
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Analytic calculations v MC simulation—trimming

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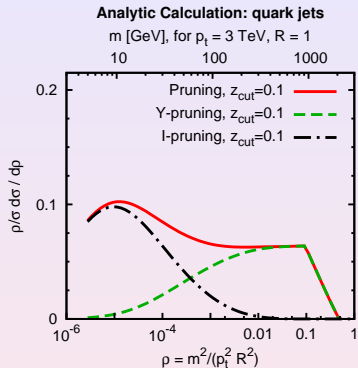
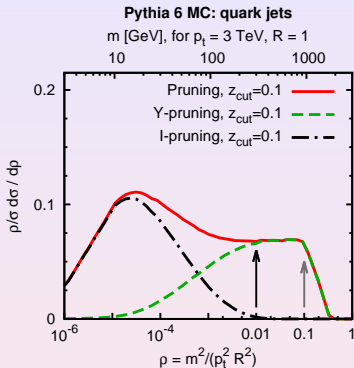
$$\frac{\rho}{\sigma} \frac{d\sigma}{d\rho} \simeq \rho \frac{d}{d\rho} \exp \left[-\frac{\alpha_s C_F}{2\pi} \left(-\frac{3}{2} \ln \frac{1}{\rho} + \Theta(\rho - z) \ln^2 \frac{1}{\rho} + \right. \right. \\ \left. \left. + \Theta(z - \rho) \left(\ln^2 \frac{1}{z} + 2 \ln \frac{z}{\rho} \ln \frac{1}{z} \right) + \Theta(zr^2 - \rho) \ln^2 \frac{zr^2}{\rho} \right) \right].$$

Navigation icons: back, forward, search, etc.

Analytic calculations v MC simulation –pruning

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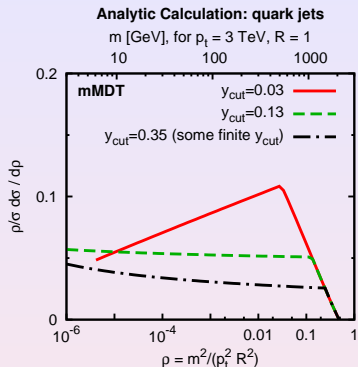
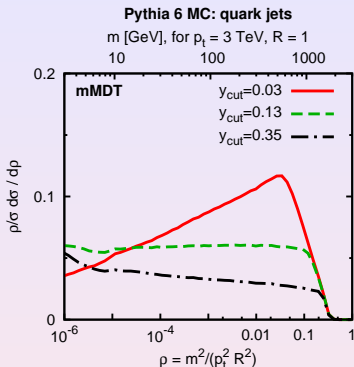


Pruning result comprises 2 distinct components, **Sane** or **Y**
pruning is better behaved.

Analytic calculations v MC simulation –mMDT

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$$\frac{\rho}{\sigma} \frac{d\sigma}{d\rho} \sim \rho \frac{d}{d\rho} \exp \left[-\frac{C_F \alpha_s}{\pi} \left(\ln \frac{1}{y_{\text{cut}}} \ln \frac{1}{\rho} - \frac{3}{4} \ln \frac{1}{\rho} \right) \right]$$

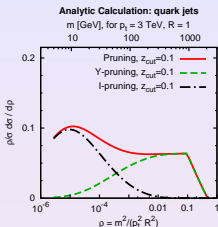
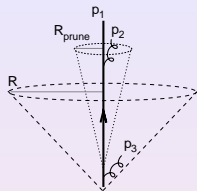
Note **flatness** for particular y_{cut} . **Unique** single-log structure.
Tagged distribution can be possibly described by **NLO calculations!**



Improving pruning –the Y pruning modification

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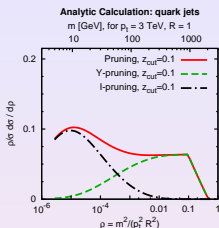
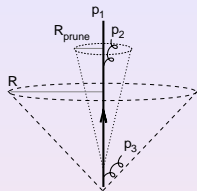
Pruning has a flaw which leads to anomalous behaviour. Situation when **dominant** emission is pruned away leaving core of jet i.e **single prong – I-pruning**. Define sane or **Y-pruning** as pruning with condition that at least one emission is tested for and passes cuts. Implies desirable **two-pronged structure**. Also removes undesirable double logs from pruning:

$$\frac{\rho}{\sigma} \frac{d\sigma^{Y\text{-prune}}}{d\rho} \sim \frac{C_F \alpha_s}{\pi} \left(\ln \frac{1}{z_{cut}} \right) \exp \left(-\frac{C_F \alpha_s}{2\pi} \ln^2 \rho \right)$$

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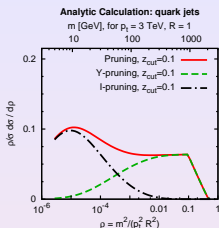
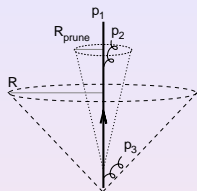
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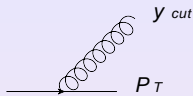
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Non-perturbative effects

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Taggers performance also critically depends on sensitivity to hadronisation UE and pile-up. Estimate hadronisation sensitivity by taking soft emission with $k_t = \mu_I$ with $\mu_I \sim 1$ GeV. Then

$$m^2 = \omega p_T \theta^2 = \mu_I p_T \theta \sim \mu_I p_T$$

For $p_T = 3$ TeV gives $m \sim 55$ GeV!

Compare mMDT for fixed $k_t = \mu_I$

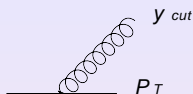
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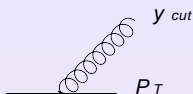
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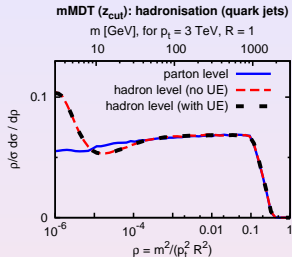
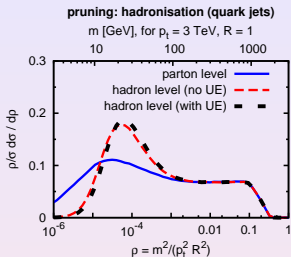
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Monte Carlo studies reveal pruning and trimming indeed v. affected by hadronisation even around EW scale. mMDT is relatively safe.

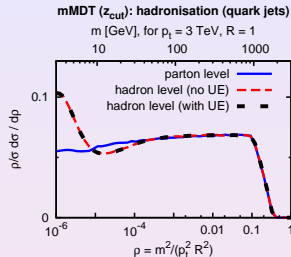
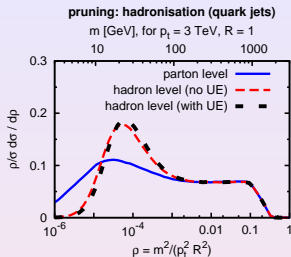
UE effects are much more modest for all methods.

Y pruning less affected than pruning by hadronisation but more by UE.

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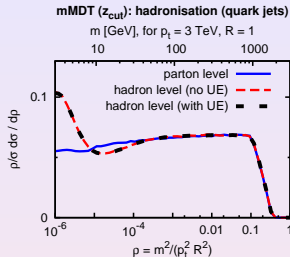
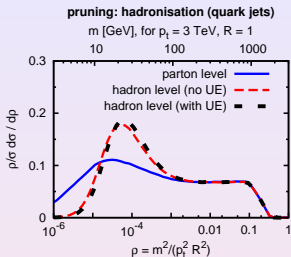
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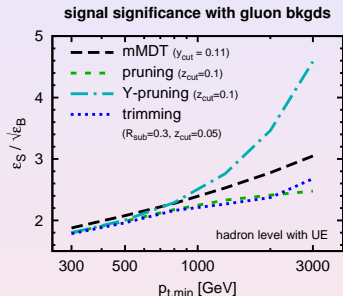
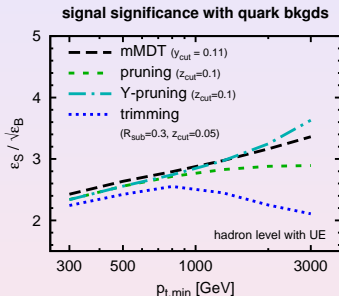
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In the final analysis....

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It is performance that counts ! We now understand what features of the taggers drive the signal efficiencies.



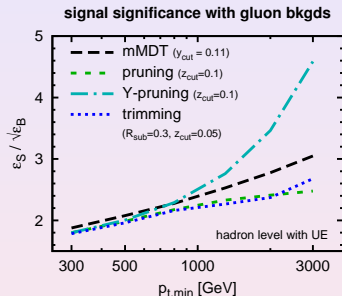
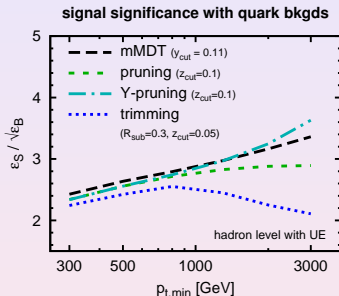
Trimming does not work well because of the double log structure we highlighted. A similar less acute effect for pruning. Y pruning looks the best of these simple taggers but has signal loss to UE.

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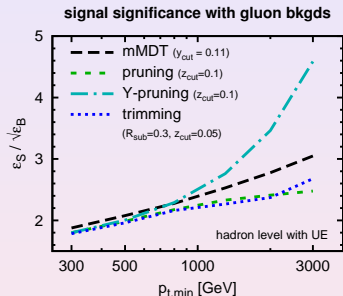
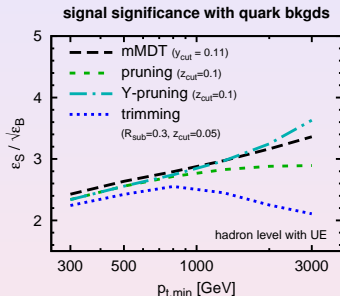
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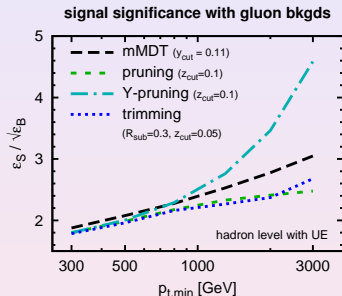
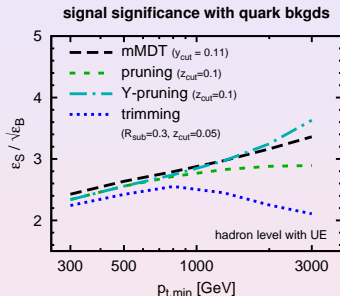
Trimming does not work well because of the double log structure we highlighted. A similar less acute effect for pruning. Y pruning looks the best of these simple taggers but has signal loss to UE.

In the final analysis....

and infrared
QCD
dynamics

Mrinal
Dasgupta

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- A partial analytical insight into jet substructure tools has recently been obtained.
- We can extend this understanding : analytical calculations for signal processes, higher log accuracy for the taggers, calculations for a wider range and combinations of taggers
- We should put this understanding to use in developing better more robust tools.