

MEASUREMENT OF $e^+e^- \rightarrow \pi^+\pi^-$ CROSS SECTION AT CMD-3

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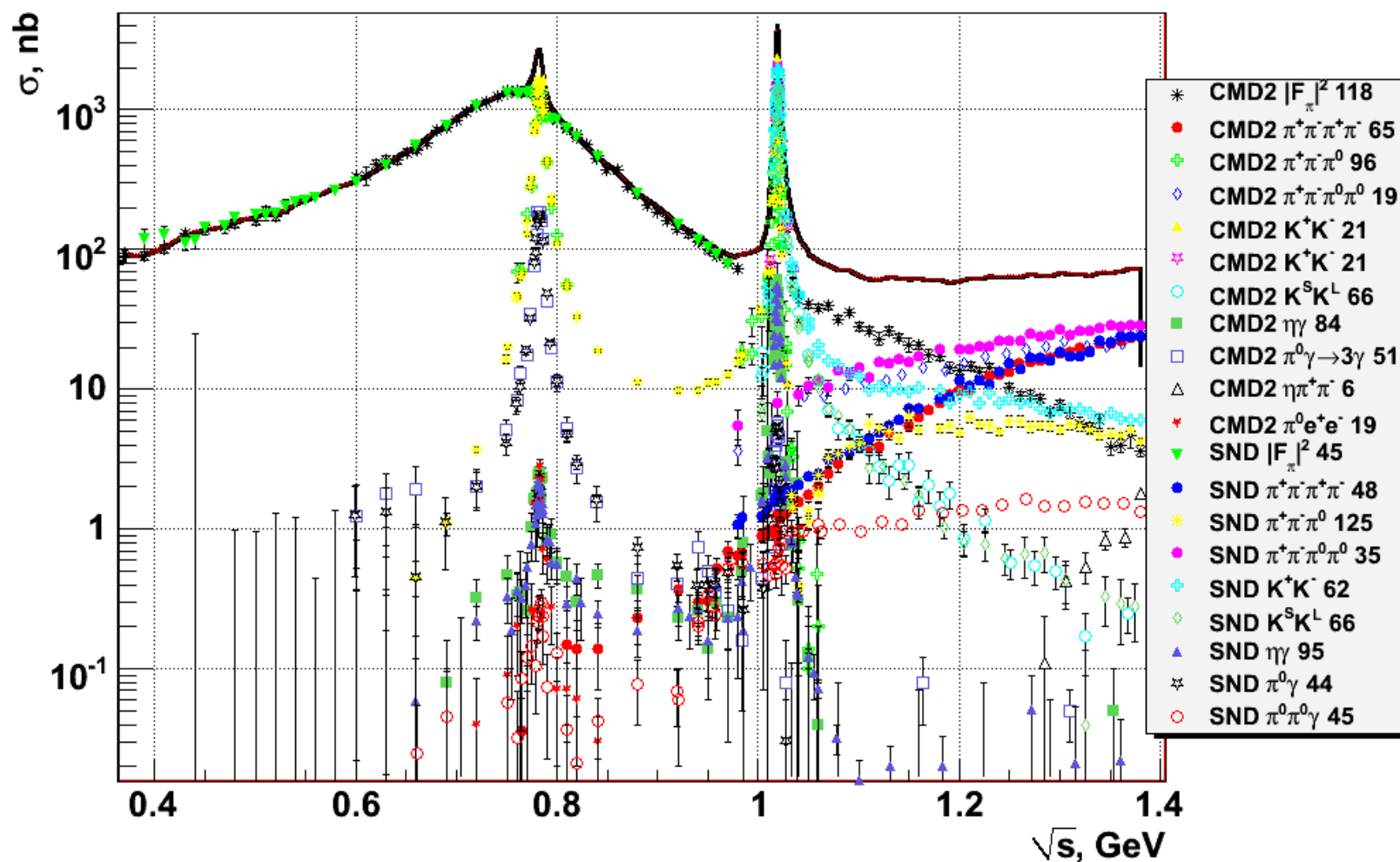
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Outline

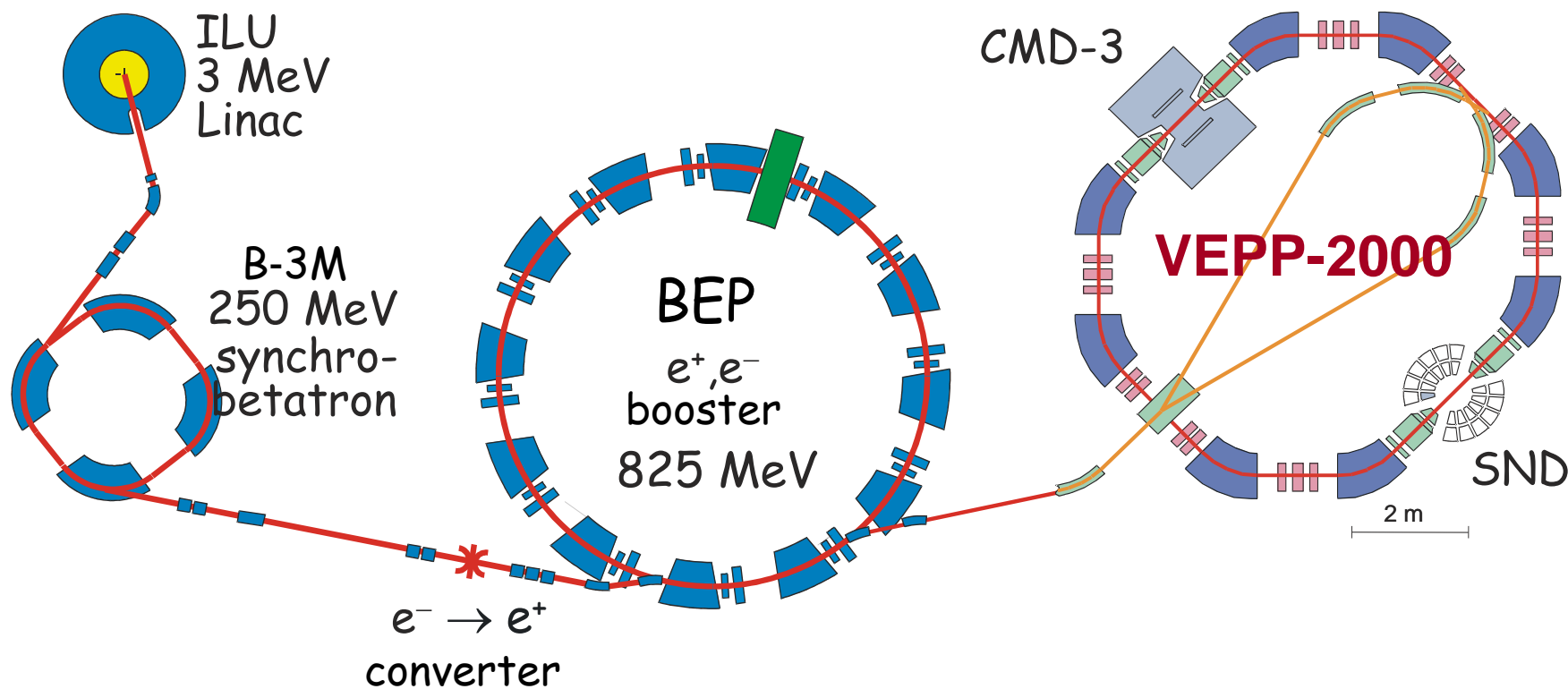
- VEPP-2000
- Detector CMD-3
- Pion formfactor measurement
- Systematic errors

Cross-section measurements at VEPP-2M



Hadronic cross-section measurements with precision from $<1\%$ to $\sim 5\%$

VEPP-2000

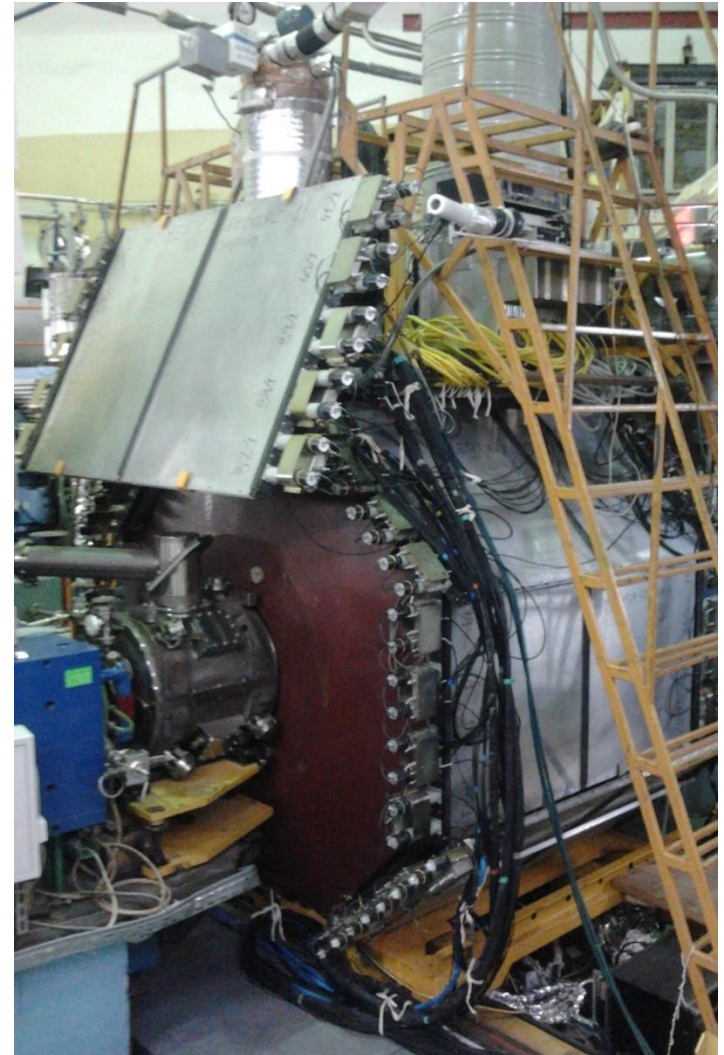
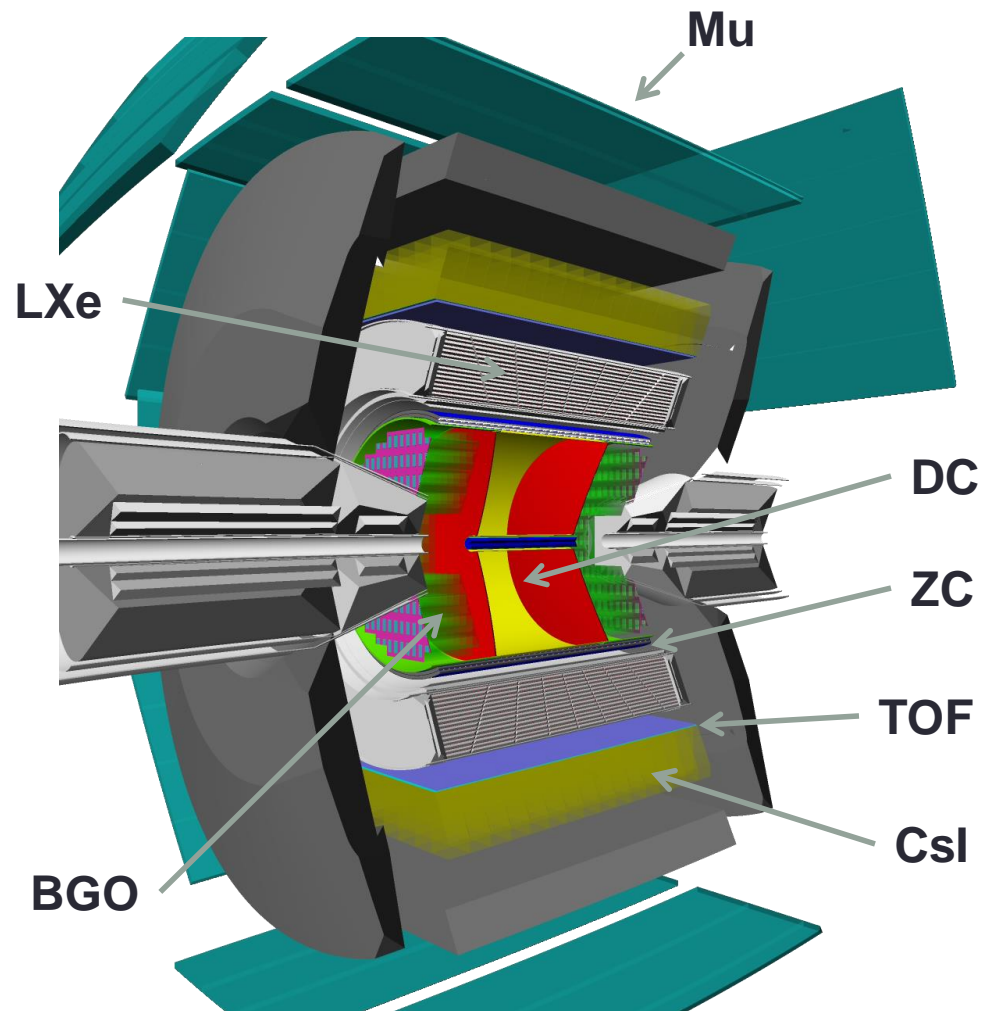


Maximum c.m. energy is 2 GeV, project luminosity is $L = 10^{32} 1/cm^2 s$ at $\sqrt{s} = 2$ GeV

Unique optics, “round beams”, allows to reach higher luminosity

Experiments with two detectors, CMD-3 and SND, started by the end of 2010

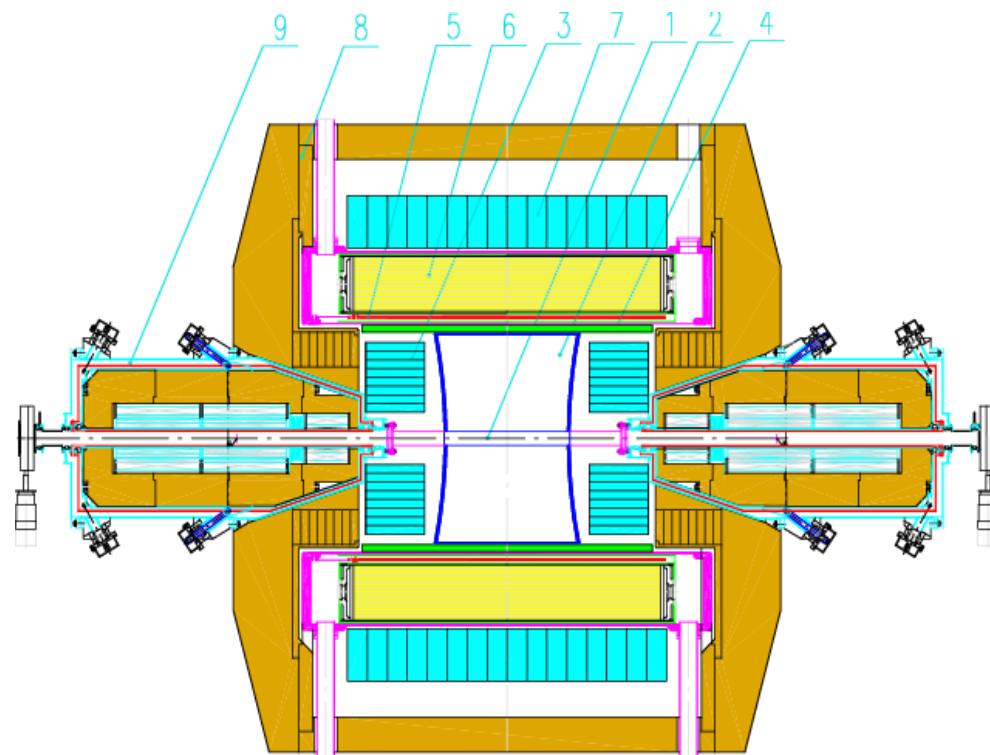
Detector CMD-3



CMD-3 vs CMD-2

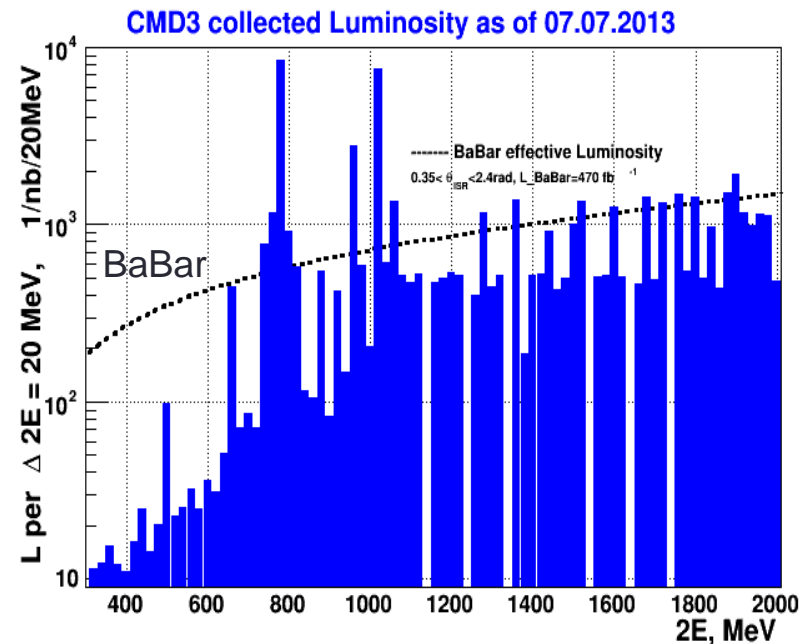
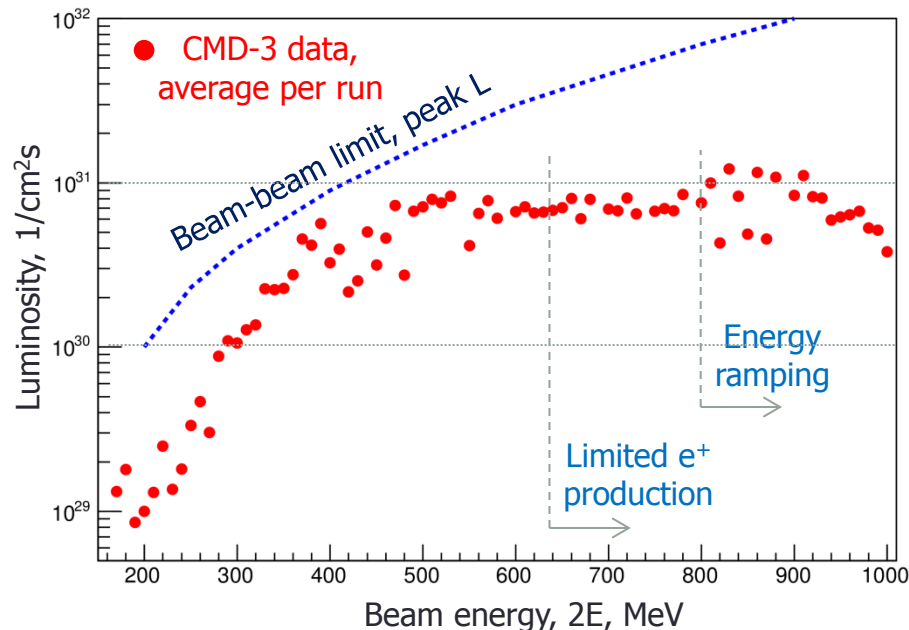
CMD-3 advantages compared to its predecessor CMD-2:

- new drift chamber with two times better resolution, higher B field
better tracking
better momentum resolution
- thicker barrel calorimeter ($8.3X_0 \rightarrow 13.4 X_0$)
better particle separation
- LXe calorimeter
measurement of conversion point for γ 's
measurement of shower profile
- TOF system
particle id (mainly p, n)



1 – IP, 2 – drift chamber, 3 – BGO (680 crystals), 4 – Z-chamber, 5 – SC solenoid, 6 – LXe (400 liters), 7 – CsI (1152 crystals), 8 – magnet yoke, 9 – ring solenoids, not shown – muon range system and TOF system

Collected luminosity



Currently the luminosity is limited by a deficit of positrons (from $E > 650$ MeV) and limited energy of the booster (from $E > 825$ MeV).

After upgrade in 2013-2014 we expect luminosity increase by up to factor 10 at maximum energy.

About 60 pb⁻¹ collected per detector

| | |
|---|-----------|
| $\omega(782)$ | 8.3 1/pb |
| $2E < 1 \text{ GeV}$ (except ω) | 9.4 1/pb |
| $\phi(1019)$ | 8.4 1/pb |
| $2E > 1.04 \text{ GeV}$ | 34.5 1/pb |

$$e^+ e^- \rightarrow \pi^+ \pi^-$$

It is a challenging channel at CMD-3, because of the high precision.

Reasons to measure pion formfactor yet again:

1. In units of hadronic contribution to $(g - 2)_\mu$:
 $\delta a_\mu^{HVP} = 0.6\%$, $\Delta a_\mu(\text{exp} - \text{theory}) \approx 4.0\% \pm 1.1\%$
 $\sigma(e^+ e^- \rightarrow \pi^+ \pi^-)$ attributes to 73% of a_μ^{HVP} and to 0.45% to δa_μ^{HVP} .
2. New experiment at FNAL is expected to measure $(g - 2)_\mu$ to 0.25%
3. There is good overall agreement between KLOE, BABAR, CMD-2 and SND, but there are local disagreements.

CMD-3 goal: measure $\sigma(e^+ e^- \rightarrow \pi^+ \pi^-)$ with systematic accuracy of 0.3% and small statistical errors.

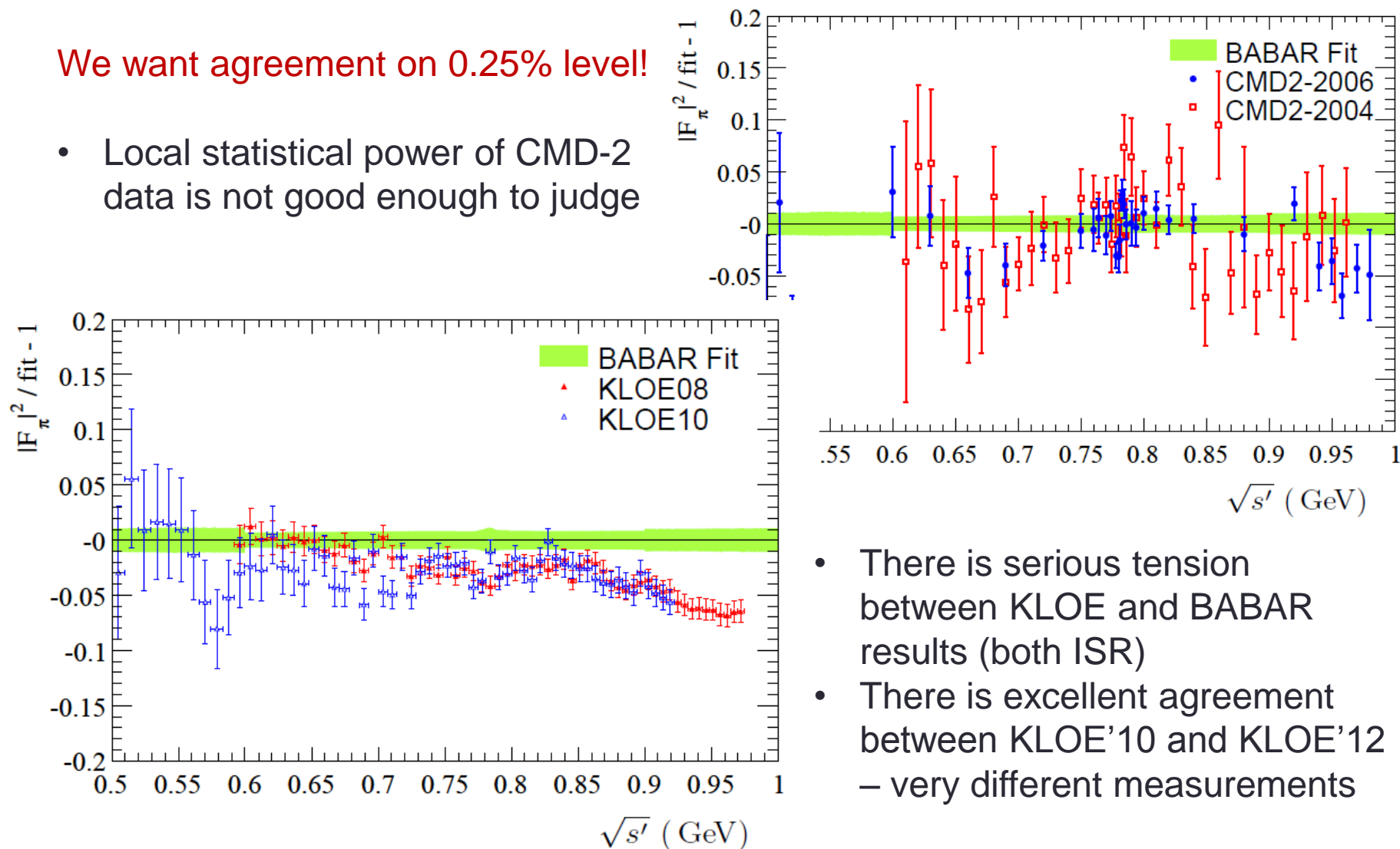
Means to improve systematics:

- Better $e/\mu/\pi$ separation – thick multilayer calorimeter, high resolution DC
- Continuous beam energy monitoring
- High statistics – allows to see systematic effects

Do existing measurements agree?

We want agreement on 0.25% level!

- Local statistical power of CMD-2 data is not good enough to judge



- There is serious tension between KLOE and BABAR results (both ISR)
- There is excellent agreement between KLOE'10 and KLOE'12 – very different measurements

The “usual” cross-section formula

The usual way to measure cross-section:

$$\sigma(e^+e^- \rightarrow H) = \frac{N_H - N_{bg}}{L \cdot \varepsilon \cdot (1 + \delta)}$$

- Luminosity L is measured using Bhabha scattering at large angles
- Detection efficiency ε is calculated via Monte Carlo with corrections for imperfect detector; detection efficiency includes acceptance
- Radiative correction δ often accounts only for initial state radiation

This approach is not optimal for $\sigma(e^+e^- \rightarrow \pi^+\pi^-)$:

- normalization final state looks very similar to signal
- acceptance part of detection efficiency is easily calculated
- much more sophisticated calculation of radiative corrections is required

Measurement of 2π cross-section

1. Select final state with 2 back-to-back charged particles

Cuts: $p_{avr}, \Delta p, \Delta\Theta, \Delta\varphi$

Fiducial volume:

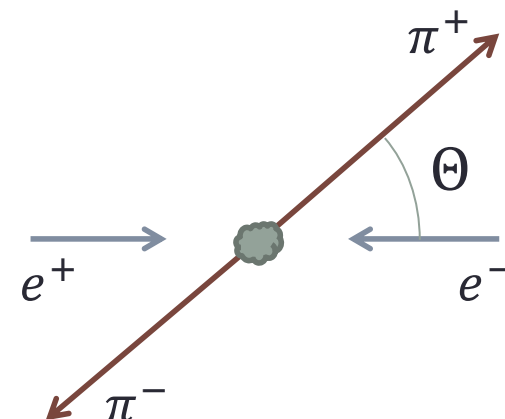
$$\Theta_0 \leq \Theta_{avr} \leq (\pi - \Theta_0), \quad \Theta_0 = 0.9 \dots 1.1$$

2. Identify e^+e^- , $\pi^+\pi^-$, $\mu^+\mu^-$ and background
3. Use “master” formula:

$$|F_\pi|^2 = \frac{N_{\pi\pi}}{N_{ee}} \frac{\sigma_{ee}^B (1 + \delta_{ee}) \varepsilon_{ee}}{\sigma_{\pi\pi}^B (1 + \delta_{\pi\pi}) \varepsilon_{\pi\pi}}$$

$$\sigma(e^+e^- \rightarrow \pi^+\pi^-) = \frac{\pi\alpha^2}{3s} \left(1 - \frac{4m_\pi^2}{s}\right)^{3/2} |F_\pi|^2$$

σ_X^B - “Born” cross-section $e^+e^- \rightarrow X$, point-like pions; δ_X - radiative correction; ε_X - detection efficiency (not including acceptance)



Separation of e^+e^- , $\mu^+\mu^-$, $\pi^+\pi^-$

Selected event sample consists of e^+e^- , $\mu^+\mu^-$, $\pi^+\pi^-$ final states and cosmic background.

Cosmic background is small ($\sim 1\%$) and easily identified by distance from the tracks to beam axis and interaction point.

Separation of different final states is based on [binned likelihood minimization](#):

- using energy deposition

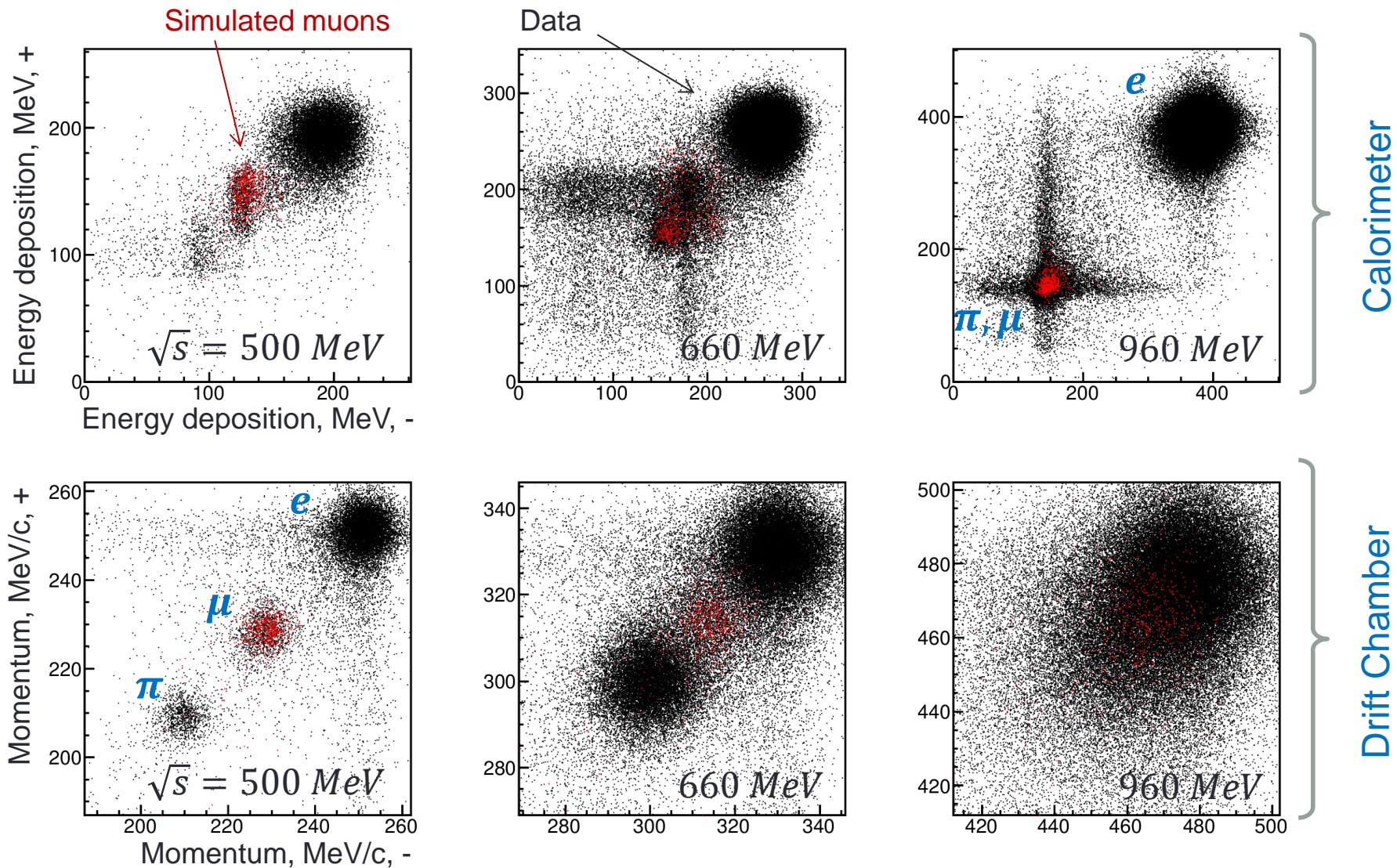
$$-\ln L = - \sum_{bins} n_i \ln \left[\sum_{X=e^+e^-, \mu^+\mu^-, \pi^+\pi^-, bg} N_X f_X(E^+, E^-) \right] + \sum_X N_X$$

- using momentum ($\sqrt{s} \lesssim 0.66$ GeV)

$$-\ln L = - \sum_{bins} n_i \ln \left[\sum_{X=e^+e^-, \mu^+\mu^-, \pi^+\pi^-, bg} N_X f_X(p^+, p^-) \right] + \sum_X N_X$$

\pm sign reflects energy deposition and momentum of particle with corresponding charge

Separation of e^+e^- , $\mu^+\mu^-$, $\pi^+\pi^-$



Where to get $f_X(p^+, p^-)$

In order to get number of events with different final states, we need to know 2D p.d.f.s f_X

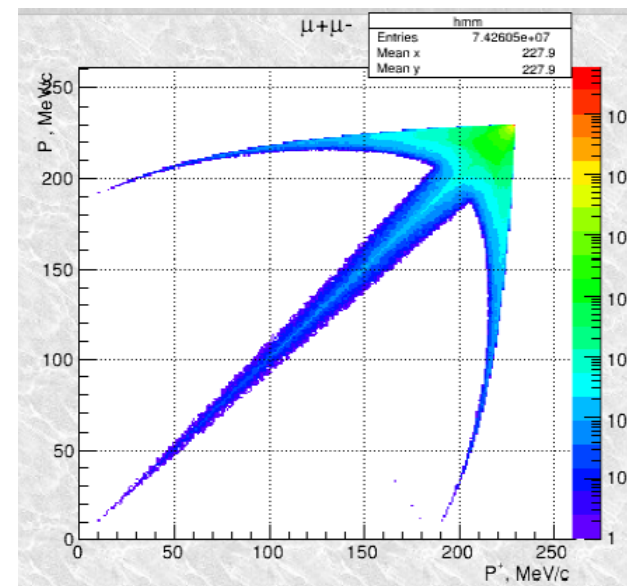
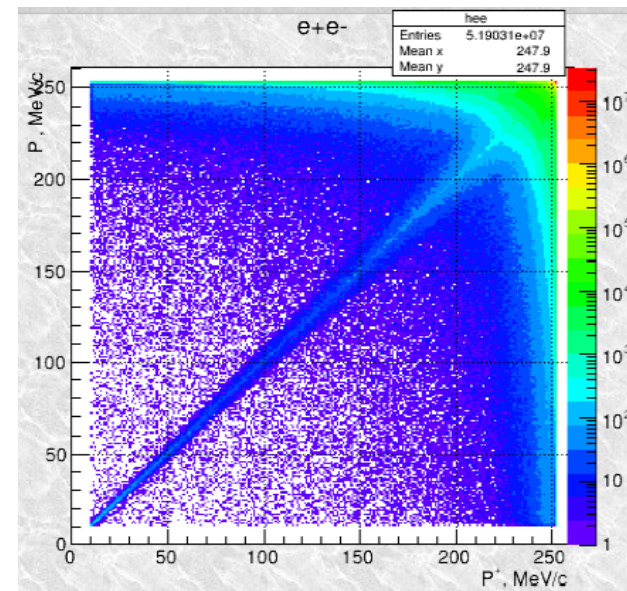
The momenta p.d.f.s are constructed via MC

1. The “ideal” distributions are generated using MC generator MCGPJ, which takes into account initial and final state radiation; selection cuts are applied
2. The ideal distribution is convoluted with detector response function (DC resolution):

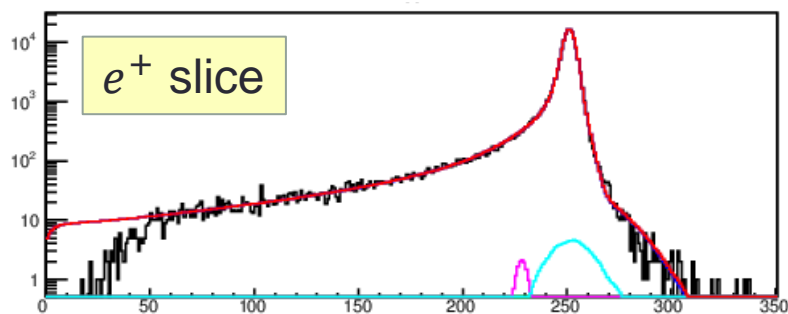
e^+e^- : 3 gaussians + bremsstrahlung on beam pipe

$\mu^+\mu^-, \pi^+\pi^-$: 2 gaussians

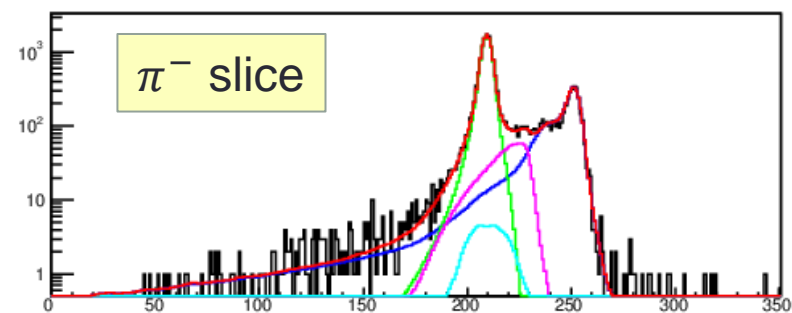
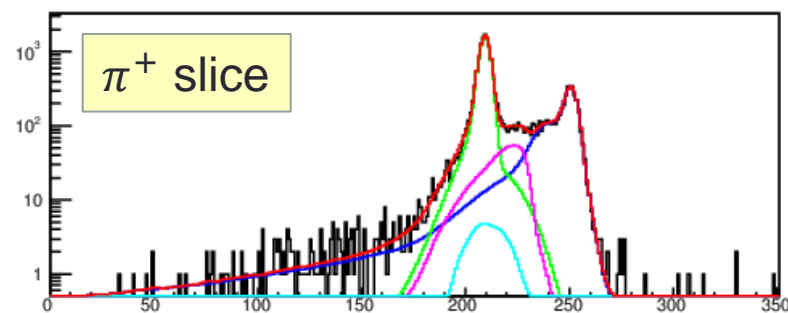
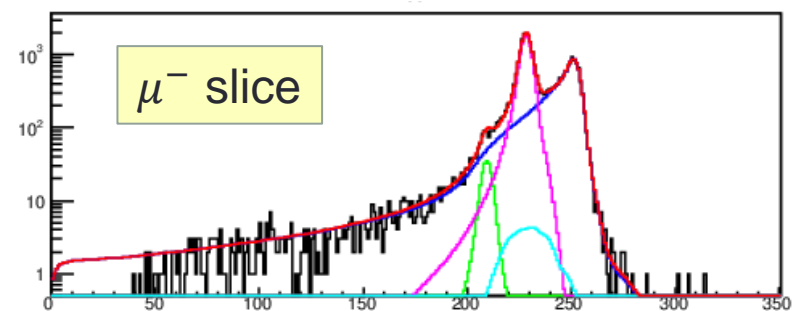
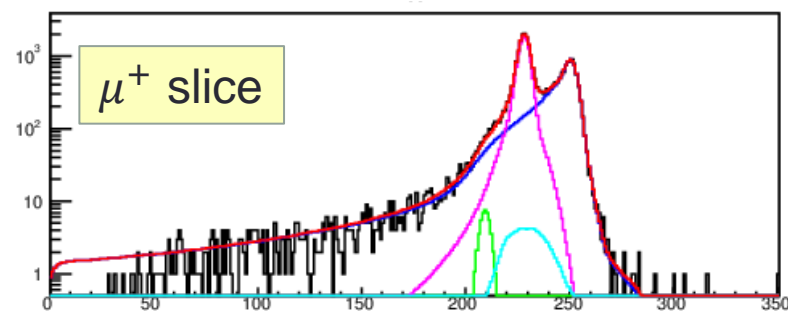
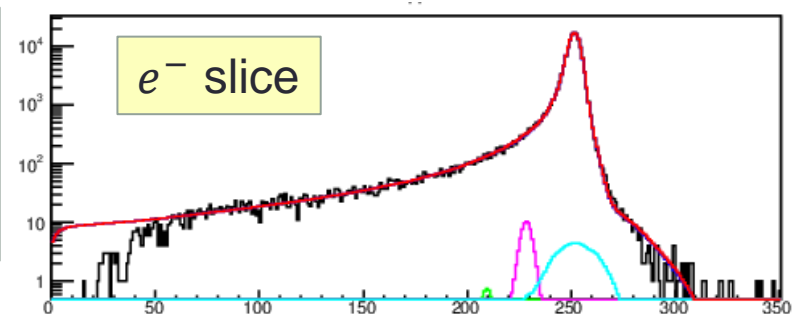
Currently, likelihood fit for momenta includes 42 free parameters



Example of momenta likelihood fit



\sqrt{s}
500
MeV



Where to get $f_X(E^+, E^-)$

- Electrons, $f_{ee}(E^+, E^-)$

From data: tag electron/positron on one side of detector and study response at the opposite side

- Cosmic, $f_{bg}(E^+, E^-)$

From data: using events with large impact parameter

- Muons, $f_{\mu\mu}(E^+, E^-)$

From simulation

Confirm simulation with data using tagged muons; tag by momentum or MVA response for shower profile

- Pions, $f_{\pi\pi}(E^+, E^-)$

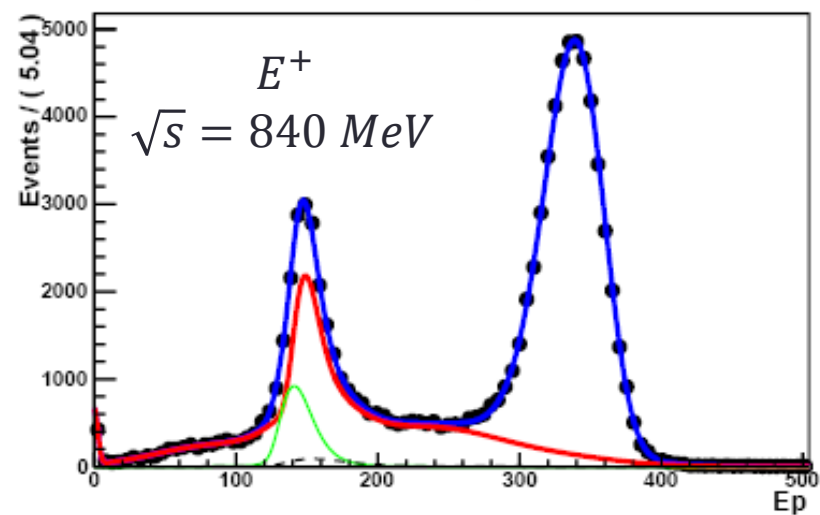
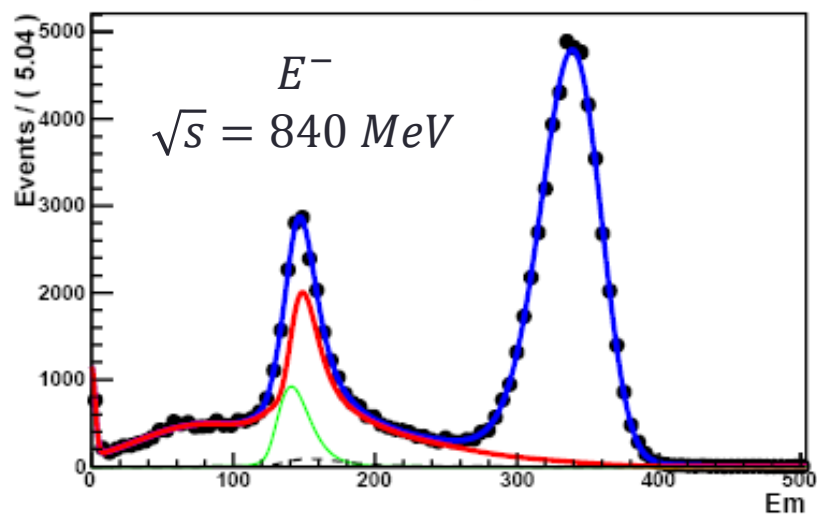
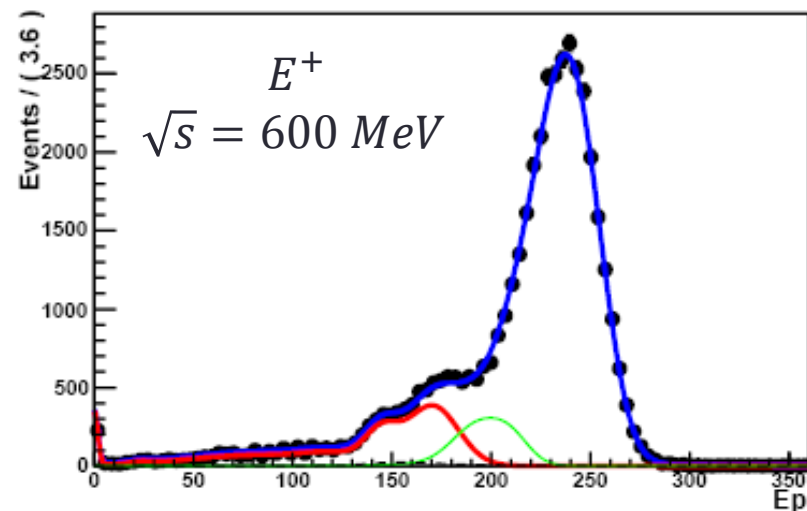
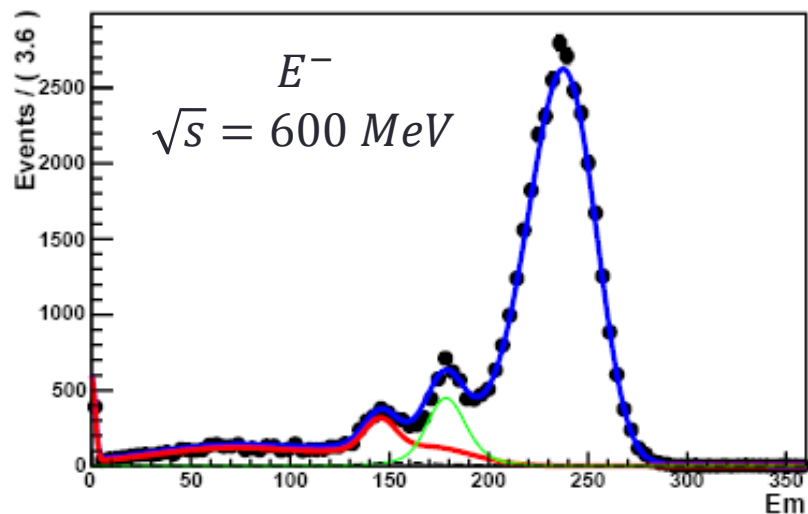
From data: clean sample of tagged pions from $\varphi \rightarrow \pi^+\pi^-\pi^0$ and $\omega \rightarrow \pi^+\pi^-\pi^0$ decays (we have few million such decays “in bag”). Works only for $\sqrt{s} < 1 \text{ GeV}$. **From simulation** above this energy.

Unlike momenta, there is rather small “native” correlation between E^+ and E^- , but they strongly correlate through common angle:

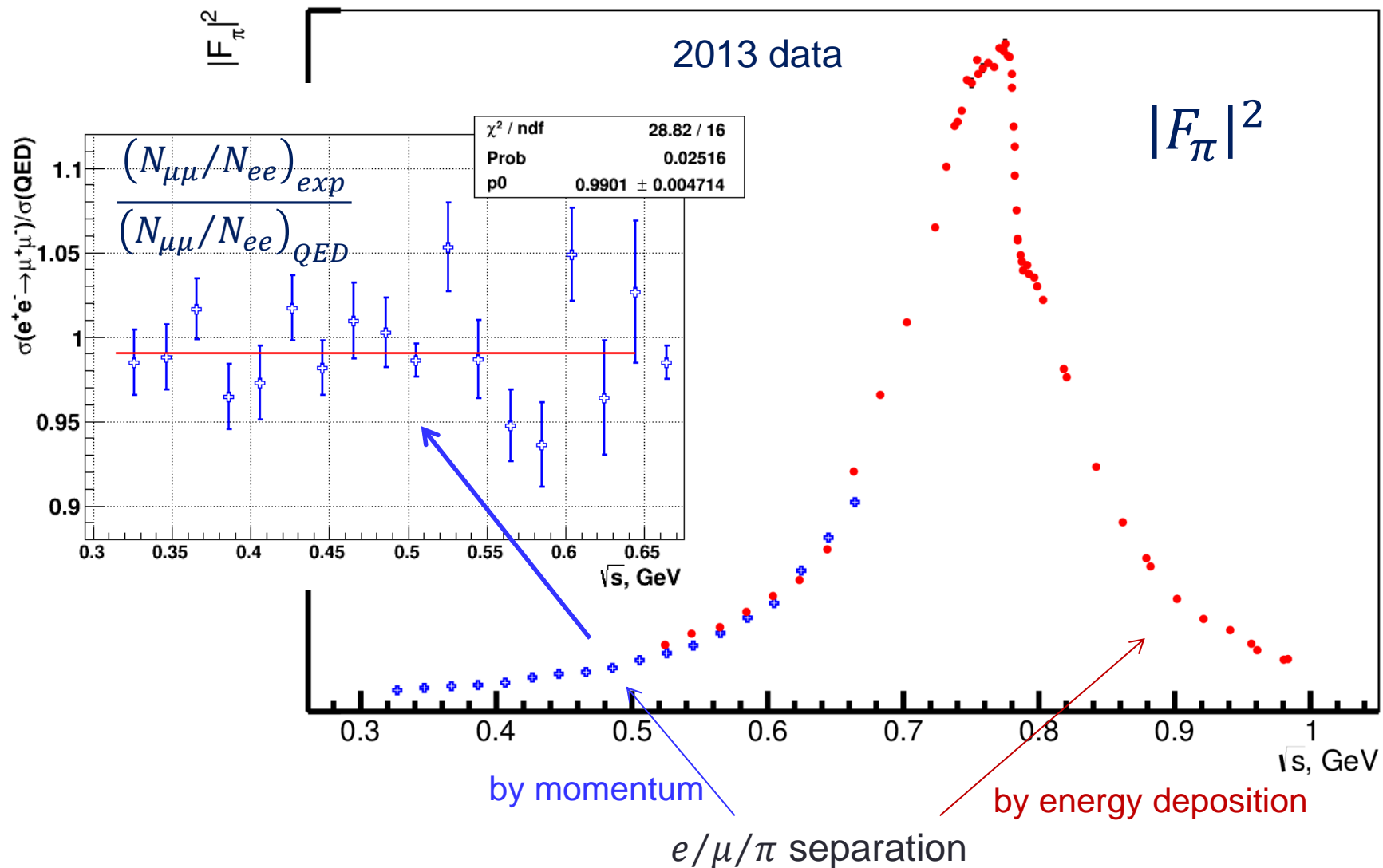
$$f(E^+, E^-) \approx f^+(E^+, \Theta) \cdot f^-(E^-, \Theta)$$

It might be necessary to introduce Θ to likelihood fit

Example of energy deposition likelihood fit



$e^+e^- \rightarrow \pi^+\pi^-$: VERY preliminary results



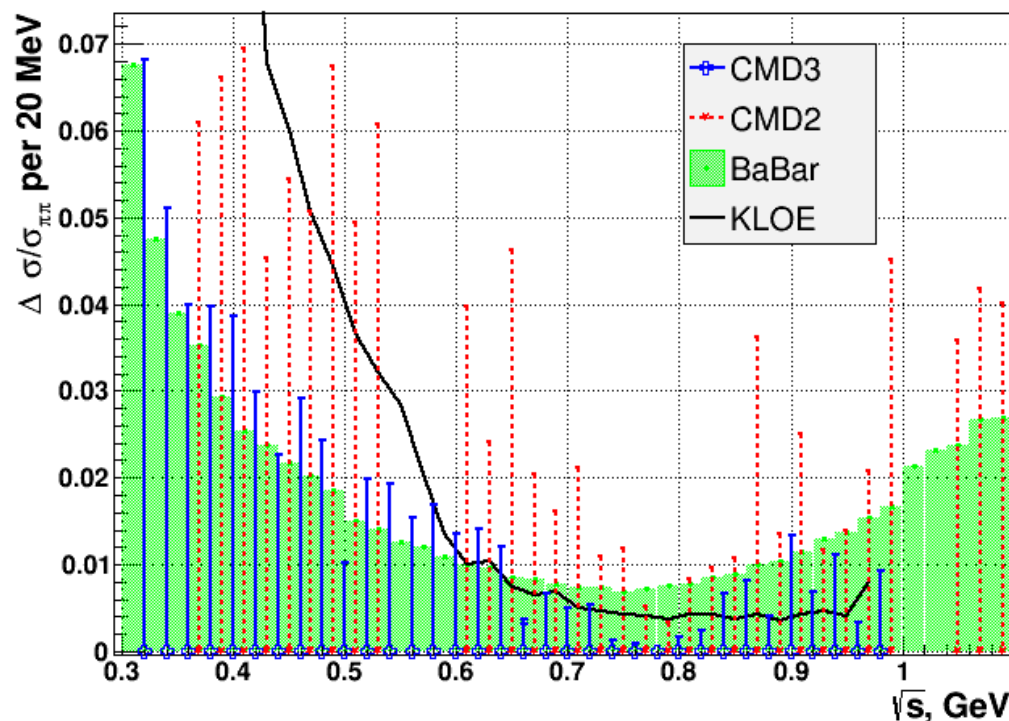
$e^+e^- \rightarrow \pi^+\pi^-$: statistics and systematics

Main sources of systematics:

- $e/\mu/\pi$ separation – 0.2%
multiple ways to get detector response from data itself
- fiducial volume – 0.1%
2 independent systems, which can be used to determine fiducial volume
- beam energy – 0.1%
continuous monitoring with Compton backscattering
- radiative corrections – 0.1%
check from data

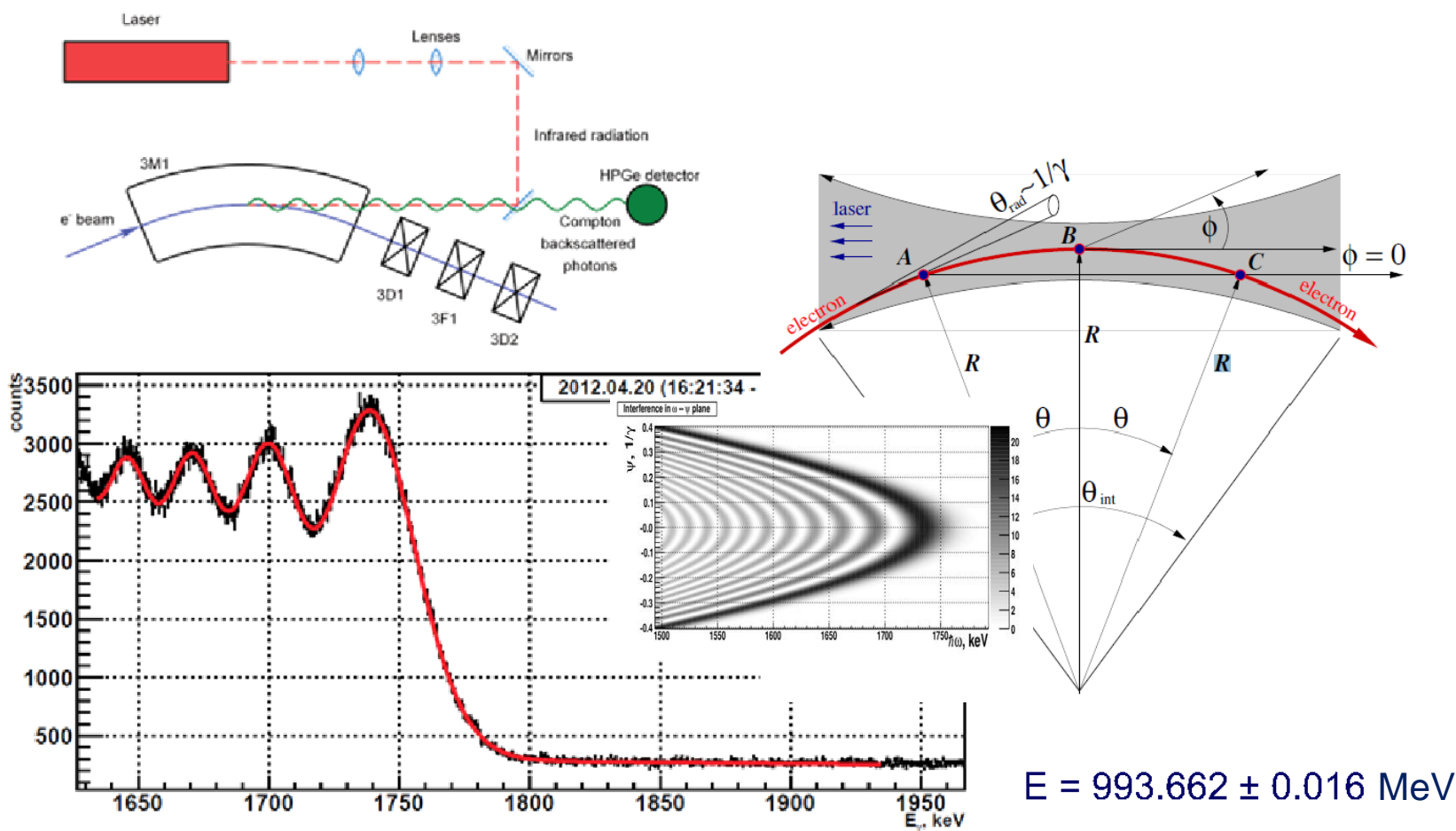
Many systematic studies rely on high statistics

Expected statistical error for 2013 data



Energy measurement

Starting from 2012, energy is monitored continuously using Compton backscattering



Radiative corrections

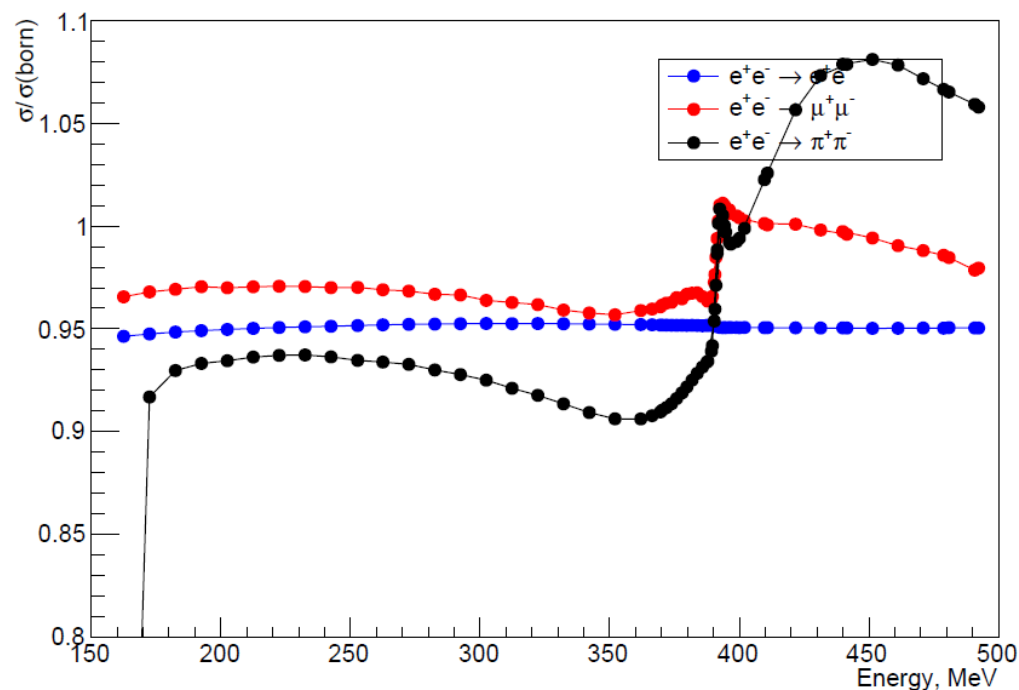
Radiative corrections are large $\sim 10\%$

Need to know to $\sim 0.1\%$ (absolute)

Most of existing generators claim necessary accuracy.

How to check that?

1. Compare generator MCGPJ, we use, with alternative high-precision generators (BABAYAGA, KKMC, BHWIDE, PHOKHARA)
2. Compare experimental radiative tails in p , $\Delta\Theta$, $\Delta\varphi, \dots$ with what is predicted from MC



Radiative corrections for 2013 data
for particular selection cuts

Radiative corrections (2)

Need to be careful with what is taken into account when calculating $\delta_{\pi\pi}$

- **Hadron spectroscopy**: vacuum polarization (VP) is the part of the cross-section (“dressed”), final state radiation (FSR) is not
- **Cross-section used in R**: FSR is the part of the cross-section, VP is not (“bare”)
- **Measured number of events** includes VP and part of FSR allowed by the event selection

We measure two kinds of cross-sections:

- $\sigma_{\pi\pi}, |F_\pi|^2$: “dressed” cross-section $e^+e^- \rightarrow \pi^+\pi^-$

Radiative correction includes FSR contribution, allowed by selection cuts, but does not include VP

This cross-section is used to get $M_\rho, \Gamma_\rho, \dots$

- $\sigma_{\pi\pi(\gamma)}^0$: “bare” cross-section $e^+e^- \rightarrow \pi^+\pi^-(\gamma)$

Calculated from $\sigma_{\pi\pi}$ as $\sigma_{\pi\pi(\gamma)}^0 = \sigma_{\pi\pi} \cdot |1 - \Pi(s)|^2 \cdot \left(1 + \frac{\alpha}{\pi} \Lambda(s)\right)$

Used to get R

remove
VP

add
FSR

Detector efficiencies

Trigger efficiency:

CMD-3 has two independent modes to trigger collinear events

Main mode, “charged”, is highly efficient and uses only tracking data

Many intermediate trigger arguments are readout, allowing for detailed monitoring of efficiency

Reconstruction efficiency:

track reconstruction is highly efficient (>99%)

monitored using test events

Efficiencies, specific for particular final state

e^+e^- : bremsstrahlung on beam pipe (~1%)

$\pi^+\pi^-$: decay in flight

 hadronic interactions with the beam pipe material (~1%)

These corrections are calculated via MC and tested from data

Conclusions

- In 2013 CMD-3 collected large data set with $\sqrt{s} < 1$ GeV
- The expected precision for $\sigma(e^+e^- \rightarrow \pi^+\pi^-)$ is at the level or better of the best existing measurements
- The existing data sample with $\sqrt{s} > 1$ GeV is collected without beam energy monitoring system
- After VEPP-2000 upgrade (scheduled to be finished in 2014) we plan to collect more data in the whole energy range