

“Sapienza” Università di Roma – INFN sez. Roma 1

Exotic Hadron Spectroscopy

A. Pilloni

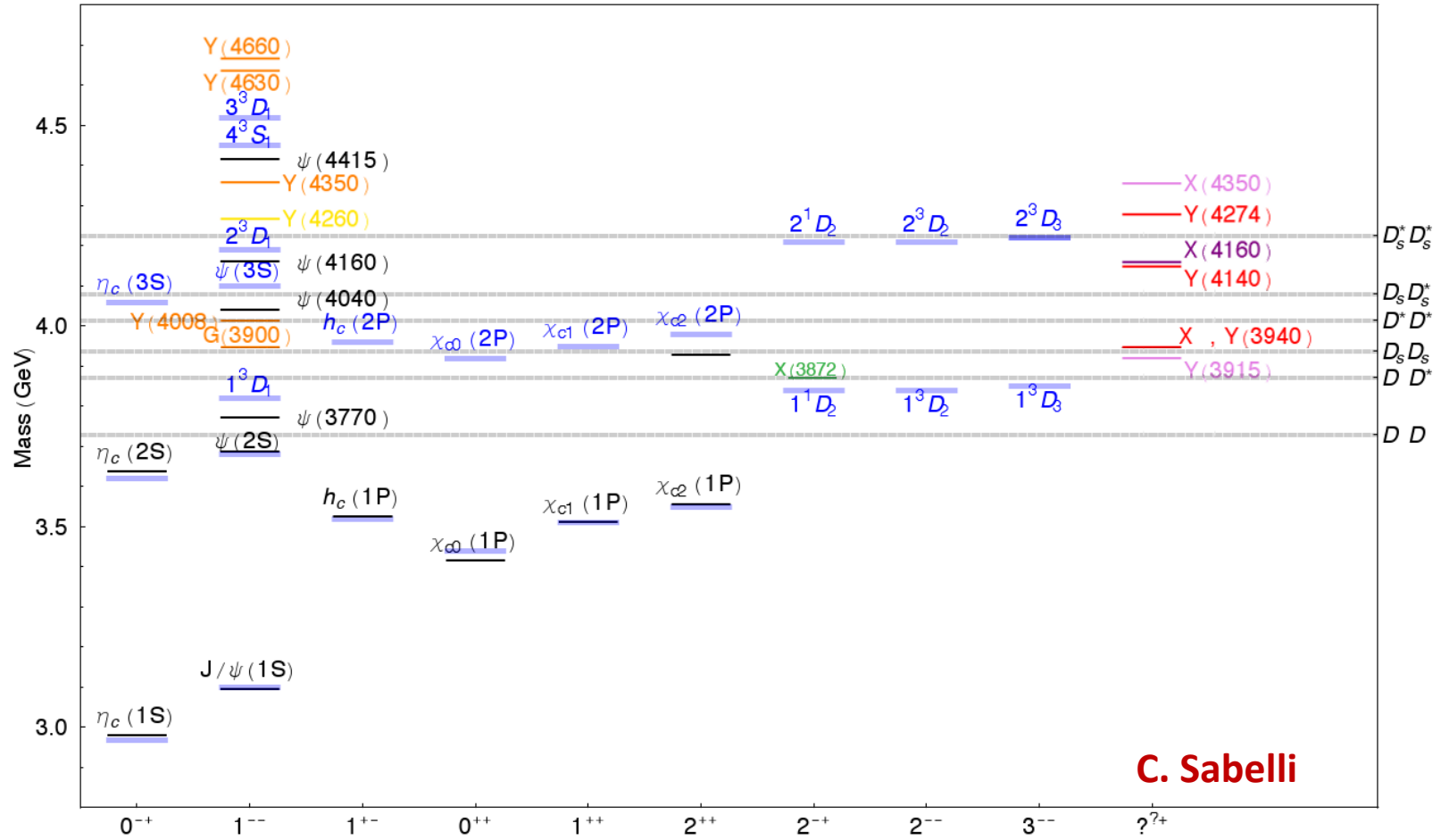
LHPMF 2013, Messina – October 15th, 2013

in coll. w/ Esposito, Faccini, Maiani, Papinutto,
Piccinini, Polosa, Riquer, Tantalò

Outline

- «Exotic landscape»
- $Z_c(3900)$ and $Z'_c(4025)$: tetraquarks?
- Feshbach resonances
- A production mechanism for $X(3872)$
- Doubly charmed tetraquarks
- Conclusions

Exotic landscape



Exotic landscape

In last ten years a lot of **exotic resonances** that do not fit the quarkonium model have appeared

Nowadays, the most assessed are

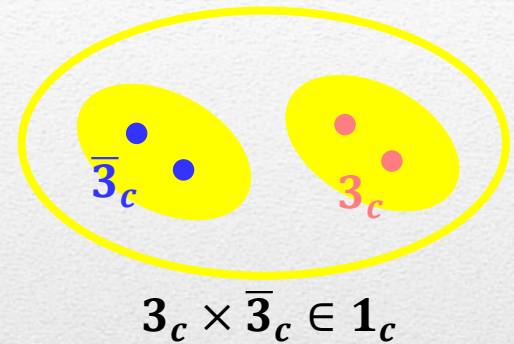
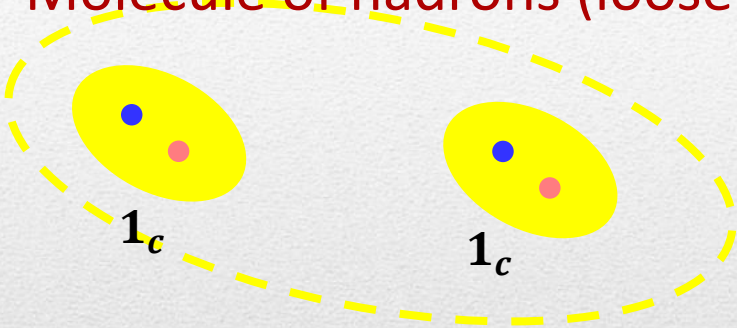
- $X(3872)$, $J^{PC} = 1^{++}$, no charged partners, huge isospin violation
- $Z_c(3900)$, $J^{PC} = 1^{+-}$, charged state
- $Y(4260)$, $J^{PC} = 1^{--}$, no charged partners

- $Z_b(10610)$ with $J^{PC} = 1^{+-}$, charged state
- $Z'_b(10650)$ with $J^{PC} = 1^{+-}$, charged state

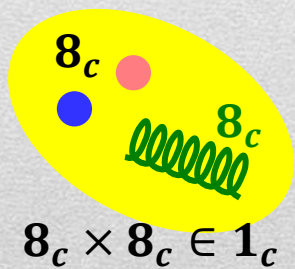
A convincing comprehensive framework which includes all these states is still missing

Proposed models

Molecule of hadrons (loosely bound)

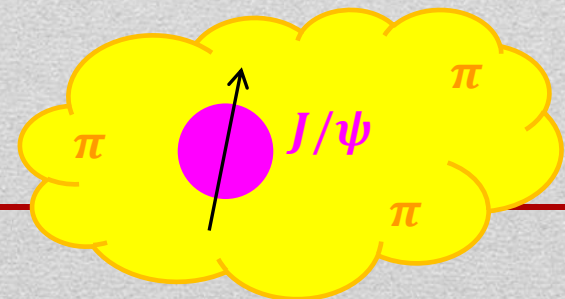


Diquark-antidiquark
(tetraquark)



Glueball & Hybrids
(with valence gluons)

Hadrocharmonium
(Van der Waals forces)



...or a superposition of all these

$Z_c(3900)$

Found in $Y(4260) \rightarrow Z_c^\pm(3900) \pi^\mp \rightarrow J/\psi \pi^\pm \pi^\mp$

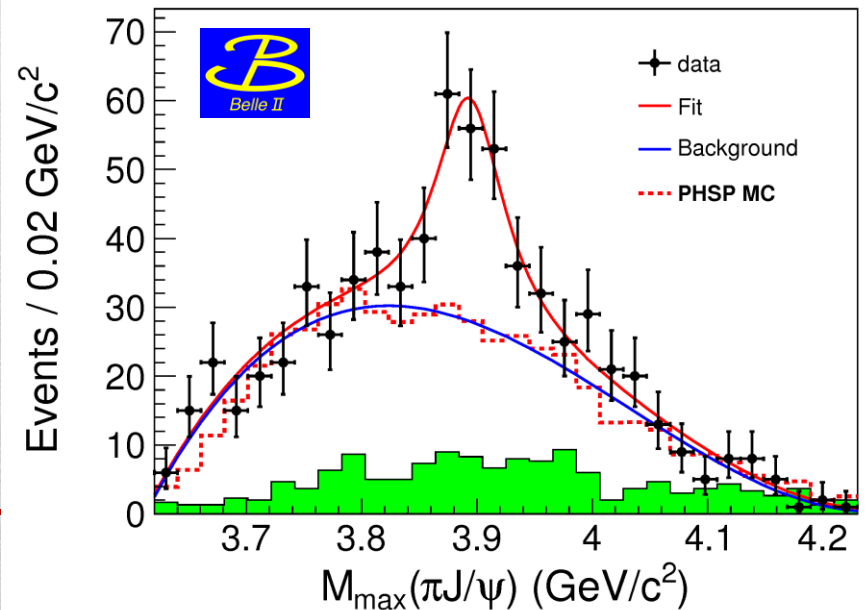
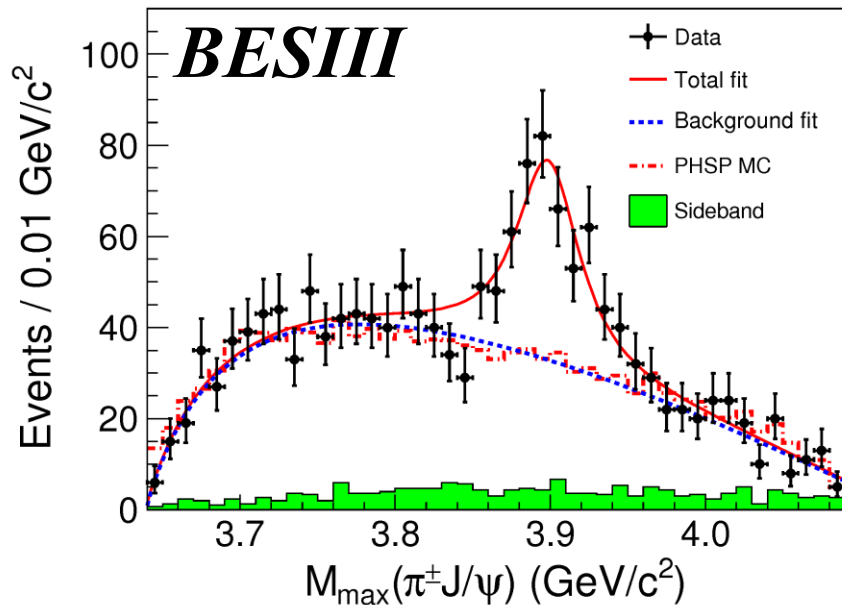
Exotic charged charmonium-like state! $I^G J^{PC} = 1^+ 1^{+-}$ (tbc)
(note that the DD^* threshold is at 3876 MeV)

BESIII, PRL110 (2013) 252001

$$M = 3899.0 \pm 3.6 \pm 4.9 \text{ MeV}$$
$$\Gamma = 46 \pm 10 \pm 20 \text{ MeV}$$

Belle, PRL110 (2013) 252002

$$M = 3894.5 \pm 6.6 \pm 4.5 \text{ MeV}$$
$$\Gamma = 63 \pm 24 \pm 26 \text{ MeV}$$



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Events / 0.01 GeV/c²

>Breaking News< -- Last week BESIII on [arXiv:1310.1163](https://arxiv.org/abs/1310.1163)

$Y(4260) \rightarrow Z_c(3885) \pi \rightarrow DD^* \pi$

$$M = 3883.9 \pm 1.5 \pm 4.2 \text{ MeV}$$

$$\Gamma = 24.8 \pm 3.3 \pm 11.0 \text{ MeV}$$

Is $Z_c(3900) = Z_c(3885)$?

$M_{\max}(\pi^\pm J/\psi)$ (GeV/c²)

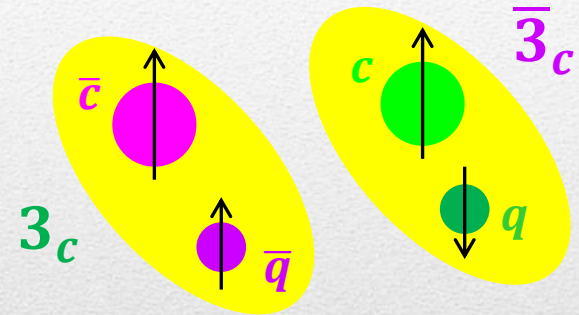
$M_{\max}(\pi J/\psi)$ (GeV/c²)

Tetraquark

One of the models for the **X(3872)** is a compact **diquark-antidiquark bound state**

$$[cq]_{s=0}[\bar{c}\bar{q}]_{s=1} + h.c.$$

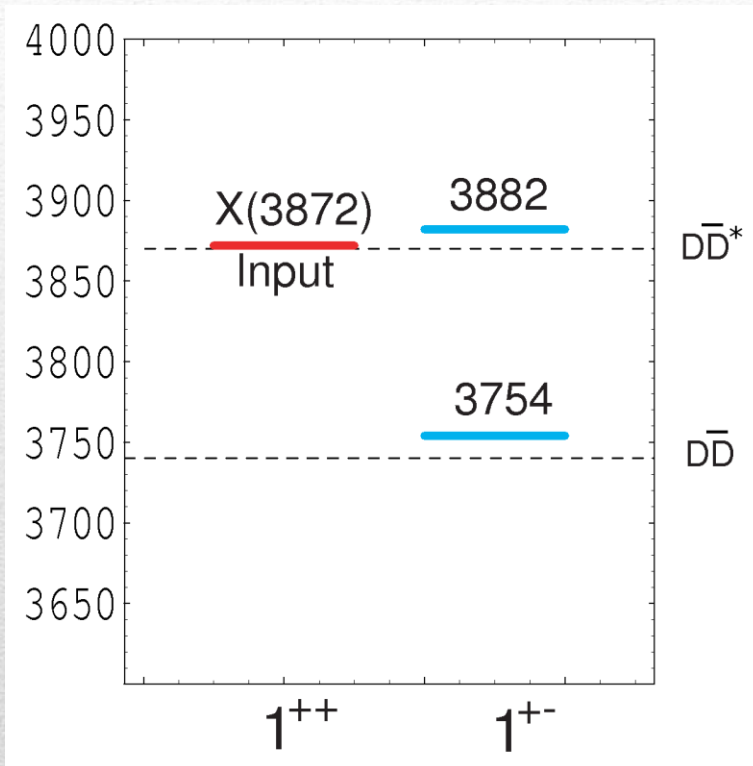
Maiani *et al.* PRD71 014028



We can evaluate mass spectrum in a constituent quark model

$$H = -2 \sum_{i < j} \kappa_{ij} \vec{S}_i \cdot \vec{S}_j \frac{\lambda_i^a}{2} \frac{\lambda_j^a}{2}$$

Tetraquark



1^{+-} state at 3882 MeV
compatible with $Z_c(3900)$!

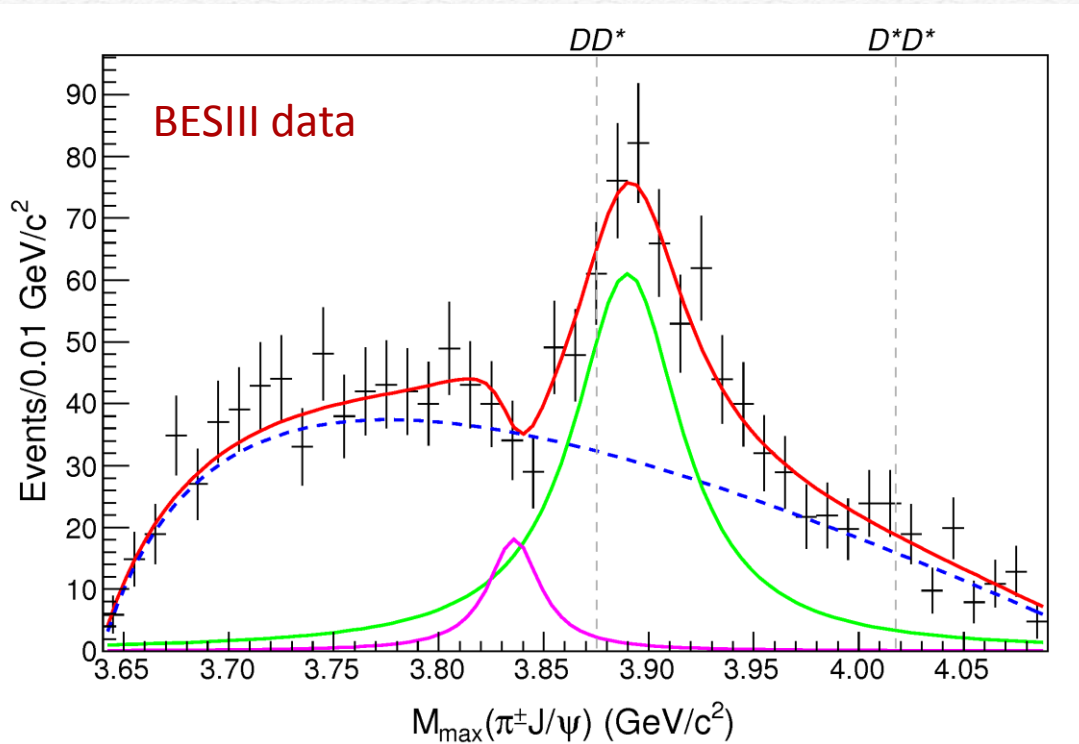
Prevision for other states:

- Neutral $I^G = 1^+$ partner
~ 3900 MeV
- Neutral $I^G = 0^-$ partner
~ 3900 MeV
- Charged/neutral 1^{+-} states
~ 3755 MeV

- Look for a $Z'_c(3760)$ about ~ 100 MeV below $Z_c(3900)$
- Look for the prominent decay $Z_c(3900) \rightarrow \eta_c \rho$

Combined BES-Belle fit

Is there room for a lighter resonance?



Faccini, Maiani, Piccinini, AP, Polosa,
Riquer PRD87 (2013) 111102

$$Z_c \quad \begin{aligned} M &= 3890 \pm 6 \text{ MeV} \\ \Gamma &= 62 \pm 12 \text{ MeV} \end{aligned}$$

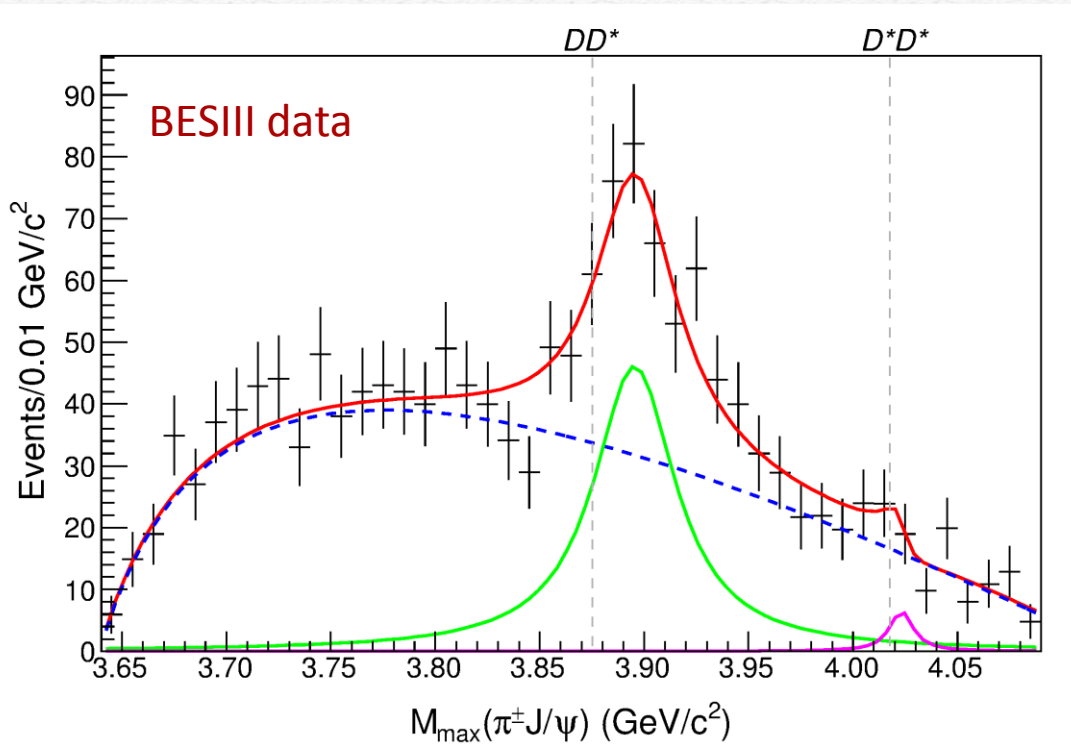
$$Z'_c \quad \begin{aligned} M' &= 3836 \pm 13 \text{ MeV} \\ \Gamma' &= 30 \pm 18 \text{ MeV} \end{aligned}$$

$$\Delta\phi = (109 \pm 30)^\circ$$

$$\chi^2/\text{DOF}=41/65, CL = 99.0\%$$

Combined BES-Belle fit

What about the D^*D^* molecule?



Faccini, Maiani, Piccinini, AP, Polosa,
Riquer PRD87 (2013) 111102

$$Z_c \quad M = 3895 \pm 3 \text{ MeV}$$
$$\Gamma = 48 \pm 8 \text{ MeV}$$

$$Z'_c \quad M' = 4023 \pm 6 \text{ MeV}$$
$$\Gamma' = 13 \pm 26 \text{ MeV}$$

$$\Delta\phi = (196 \pm 77)^\circ$$

$$\chi^2/\text{DOF}=47/65, CL = 95.0\%$$

But Nature is malicious...

$Z'_c(4020), Z'_c(4025)$

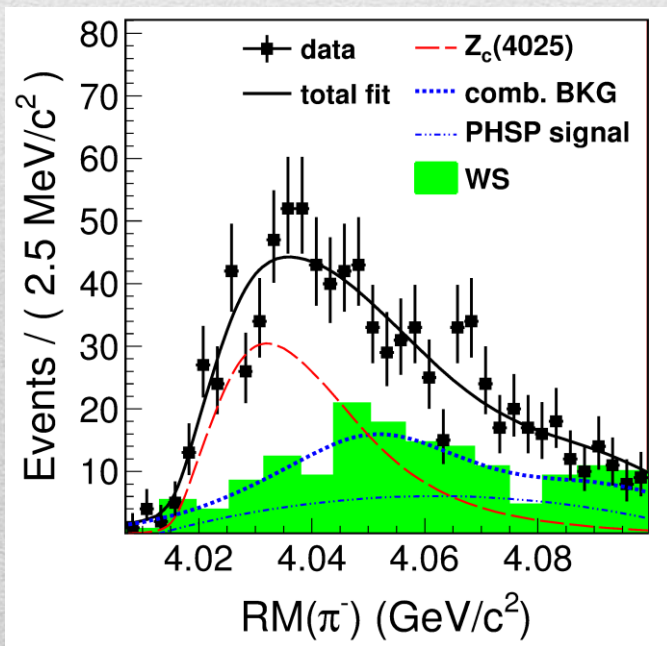
BESIII, arXiv:1308.2760

$Y(4260) \rightarrow Z'_c(4025) \pi \rightarrow D^* D^* \pi$

$$I^G J^{PC} = 1^+ 1^{+-}$$

$$M = 4026.3 \pm 2.6 \pm 3.7 \text{ MeV}$$

$$\Gamma = 24.8 \pm 5.6 \pm 7.7 \text{ MeV}$$



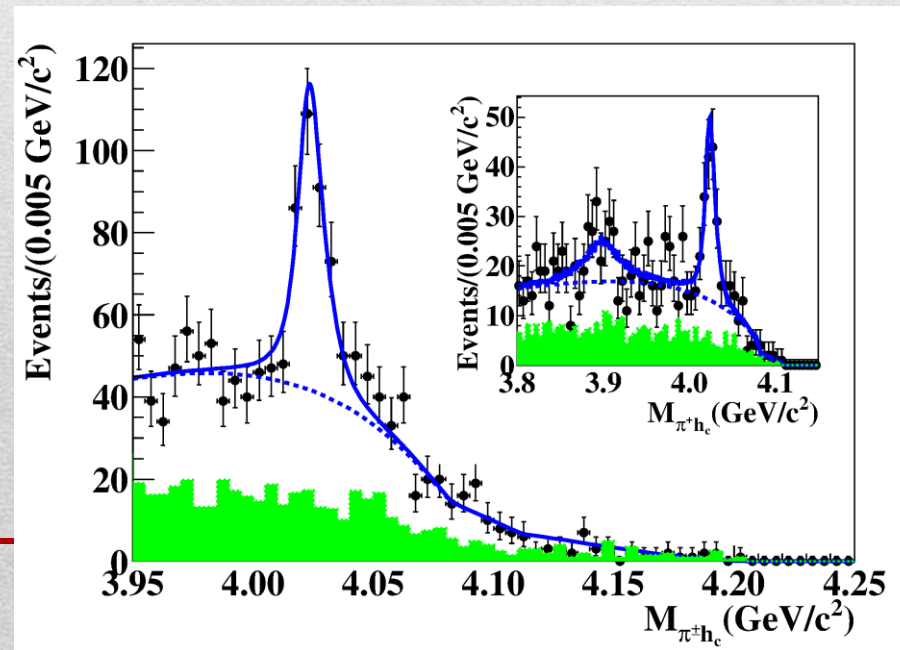
BESIII, arXiv:1309.1896

$Y(4260) \rightarrow Z'_c(4020) \pi \rightarrow h_c \pi \pi$

$$I^G J^{PC} = 1^+ 1^{\bar{-}}$$

$$M = 4022.9 \pm 0.8 \pm 2.7 \text{ MeV}$$

$$\Gamma = 7.9 \pm 2.7 \pm 2.6 \text{ MeV}$$



X, Z_c, Z'_c : summary

Molecule

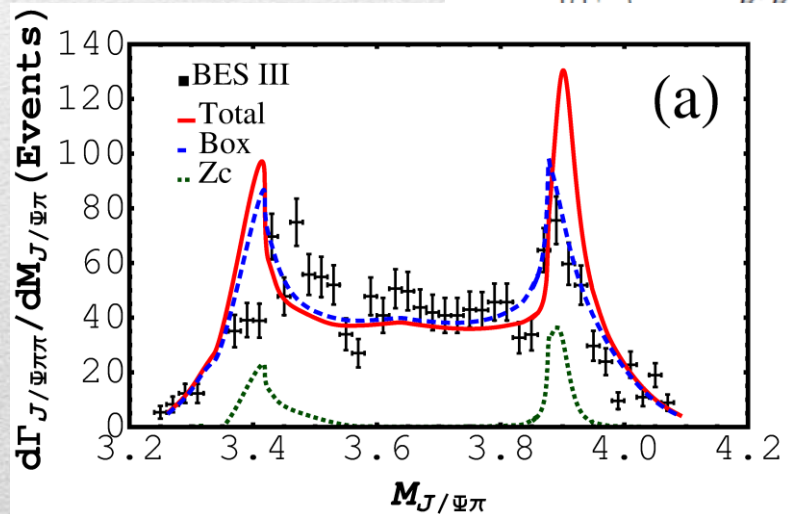
- ✓ The states are near thresholds
- ✓ Large decay into open charm
- ✗ Dynamical effects make the pattern obscure
- ✗ How to justify bound states with positive binding energy?

Tetraquark

- ✓ The pattern is simple, based on $SU(3)$
 - ✗ Many states are missing, in particular charged partners of $X(3872)$
 - ✗ Who is $Z'_c(4025)$?
-

X, Z_c, Z'_c : summary

V_C	$I(J^{PC})$	States	Thresholds	Masses ($\Lambda = 0.5$ GeV)	Masses ($\Lambda = 1$ GeV)	Measurements
C_{0X}	$0(1^{++})$	$\frac{1}{\sqrt{2}}(D\bar{D}^* - D^*\bar{D})$	3875.87	3871.68 (input)	3871.68 (input)	3871.68 ± 0.17 [33]
	$0(2^{++})$	$D^*\bar{D}^*$	4017.3	4012^{+4}_{-5}	4012^{+5}_{-12}	?
	$0(1^{++})$	$\frac{1}{\sqrt{2}}(B\bar{B}^* - B^*\bar{B})$	10604.4	10580^{+9}_{-8}	10539^{+25}_{-27}	?
	$0(2^{++})$	$B^*\bar{B}^*$	10650.2	10626^{+8}_{-9}	10584^{+25}_{-27}	?
	$0(2^+)$	D^*B^*	7333.7	7322^{+6}_{-7}	7308^{+16}_{-20}	?
C_{0Z}	$1(1^{+-})$	$\frac{1}{\sqrt{2}}(B\bar{B}^* + B^*\bar{B})$	10604.4	10602.4 ± 2.0 (input)	10602.4 ± 2.0 (input)	10607.2 ± 2.0 [5]
	$1(1^{+-})$	$D^*\bar{D}^*$	10650.2	10648.1 ± 2.1	$10648.1^{+2.1}_{-2.5}$	10597 ± 9 [34]
	$1(1^{+-})$	$D^*\bar{D}$	3875.87	3871^{+4}_{-12} (V)	3837^{+17}_{-35} (V)	$3899.0 \pm 3.6 \pm 4.9$ [24]
	$1(1^{+-})$	$D^*\bar{D}^*$	4017.3	4013^{+4}_{-11} (V)	3983^{+17}_{-32} (V)	?
			7333.7	$7333.6^{+1}_{-4.2}$ (V)	7328^{+5}_{-14} (V)	?



Nieves *et al.* PRD88 (2013) 054007

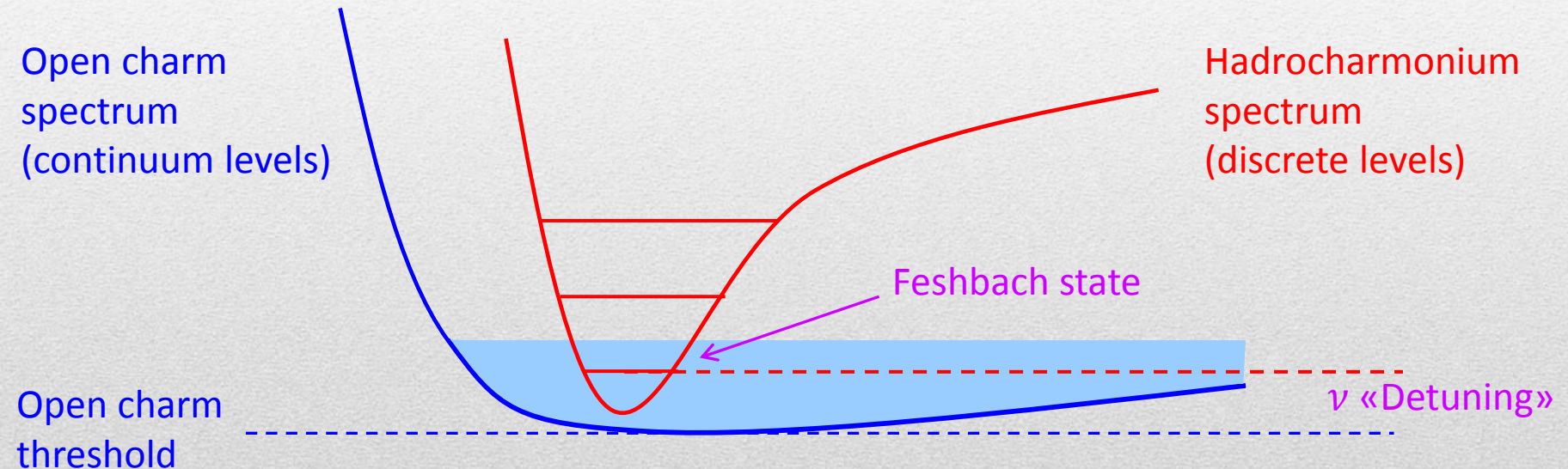
Hanhart *et al.* PRL111 (2013) 132003

In all calculations, molecular resonances are **at** or **below threshold**.
Is there a mechanism to push a bound state **above threshold**?

Feshbach resonances

Work in progress w/ Esposito, Papinutto, Piccinini, Polosa, Tantalò

In cold atoms there is a mechanism that occurs when two atoms can interact with **two potentials**, one in a **discrete level** and the other in the **continuum**



A virtual state can form in correspondance of the discrete level with $\Gamma \propto \nu$ only if it is **above threshold**

Feshbach resonances

The Hadrocharmonium spectrum is unknown, it can be deduced from the mass of the resonance, otherwise one can naively expect $M_{\text{Hch}} \approx M_{c\bar{c}} + M_{\text{light}}$

We impose a cutoff on ν and $\Gamma_D < \nu$

Open channel	Hadroch.	M_{Hch} (MeV)	ν (MeV)	$I^G J^{PC}$	name
$D^{*0} \bar{D}^0$	$J/\psi \rho^0$	3872	0	$1^- 1^{++}$	$X(3872)$
$D^{*+} \bar{D}^0$	$\psi(3770) \pi^+$	3900	24	$1^+ 1^{+-}$	$Z_c(3900)$
$D_1^+(2420) D_1^-(2420)$	$h_c(2P) f_0(980)$	4875 ?	30	$0^- 1^{+-}$?
$D^{*+} \bar{D}^0$	$h_c(2P) \pi^+$ (P-wave)	4025	8	$1^+ 1^{+-}$	$Z'_c(4025)$

The vector state $Y(4260)$ does not fit this scheme \rightarrow [Hybrid?](#)

[Hadron Spectrum coll. JHEP 1207 \(2012\) 126](#), see also [next talk by J. Ferretti](#)

Feshbach resonances

$X(3872)$ should be a $I = 1$ state, but $M(J/\psi \rho^+) < M(D^{*+} \bar{D}^0)$

No charged states, isospin violation!

If we assume $\Gamma = a \nu$, we can use $Z_c(3900)$ as input
to extract $a = 1.9 \pm 0.9$

The estimated width of $Z'_c(4025)$ is $\Gamma = 16 \pm 7$ MeV,
compatible with data

Bottom sector

Open channel	Hadrobott.	M_{Hbt} (MeV)	ν (MeV)	$I^G J^{PC}$	name
$B^{*+} \bar{B}^0$	$\chi_{b0}(1P) \rho^+$ (P-wave)	10610	3	$1^+ 1^{+-}$	$Z_b(10610)$
$B^{*+} \bar{B}^{*0}$	$\chi_{b0}(1P) \rho^+$ (P-wave)	10650	2	$1^+ 1^{+-}$	$Z'_b(10650)$

We remark that $\Gamma(Z'_b)/\Gamma(Z_b) \approx 0.63$, $\nu(Z'_b)/\nu(Z_b) \approx 0.67$

Prompt production of $X(3872)$

$X(3872)$ is the Queen of exotic resonances

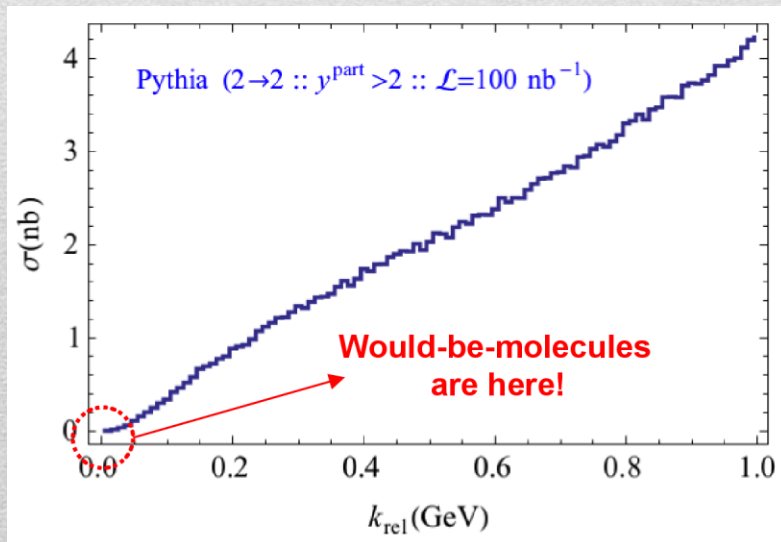
The most popular interpretation is a $D^0\bar{D}^{0*}$ molecule

But the binding energy is $E_B \approx -0.14 \pm 0.22$ MeV: **very small!**

A simple square well model shows that $k_{\text{rel}} \approx 50$ MeV

How many pairs can we produce at hadron colliders with such a small relative momentum?

Bignamini *et al.* PRL103 (2009) 162001



We obtain

$$\sigma(p\bar{p} \rightarrow DD^*) \approx 0.1 \text{ nb} @ \sqrt{s} = 1.96 \text{ TeV}$$

Experimentally

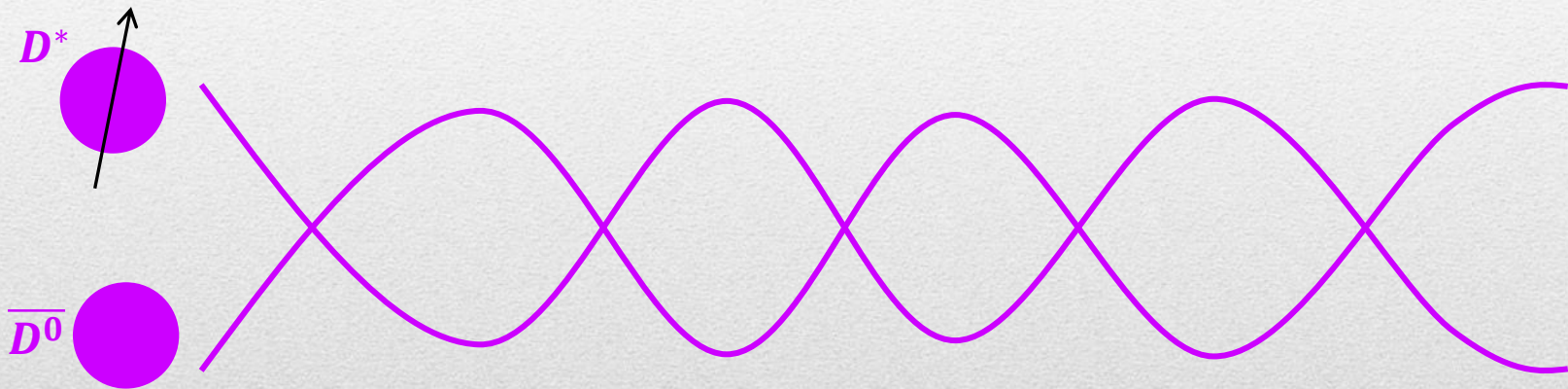
$$\sigma(p\bar{p} \rightarrow X(3872)) \approx 30 \text{ nb!!!}$$

Molecule challenged!!!

Prompt production of $X(3872)$

A solution can be Final State Interaction
(rescattering of DD^*)...

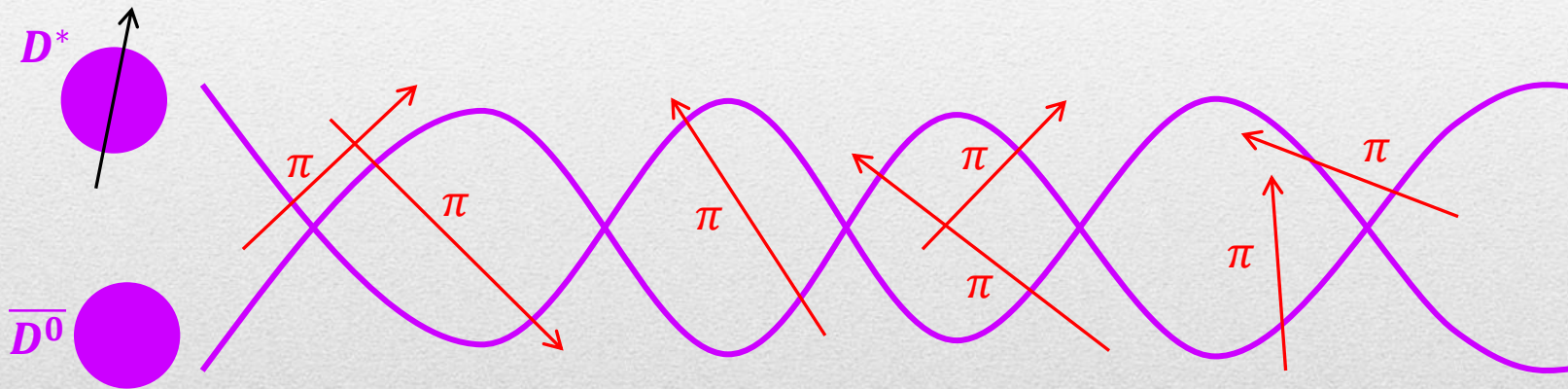
Artoisenet and Braaten PRD81 (2010) 114018



Prompt production of $X(3872)$

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Artoisenet and Braaten PRD81 (2010) 114018

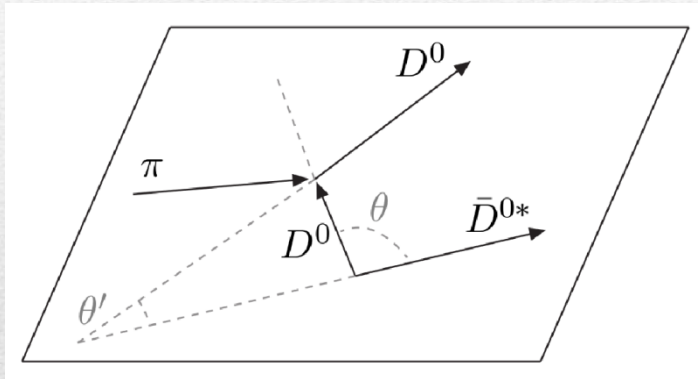


...but the application of Watson Theorem is spoiled by the presence of pions that interfere with DD^* propagation, [Bignamini et al. PLB684 \(2010\) 228-230](#)

(FSI have been used also by [Meissner et al. arXiv:1308.0193](#) to estimate Z_c and Z_b prompt xsects, but the application to above-threshold states is unclear)

A new mechanism?

However, these pions can **elastically interact** with $D(D^*)$,
and **slow down** the pairs DD^*



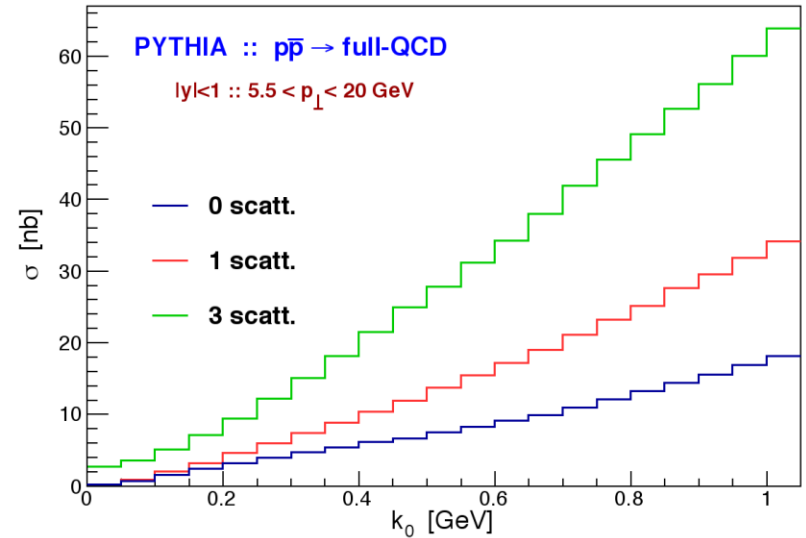
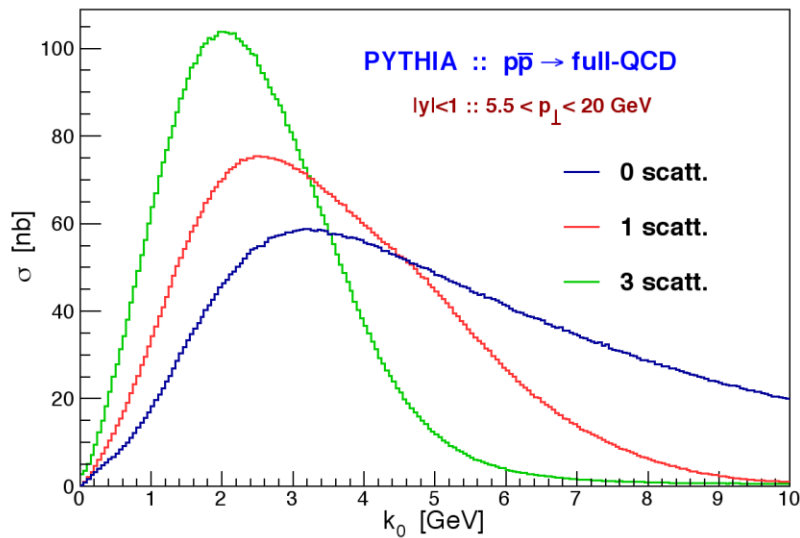
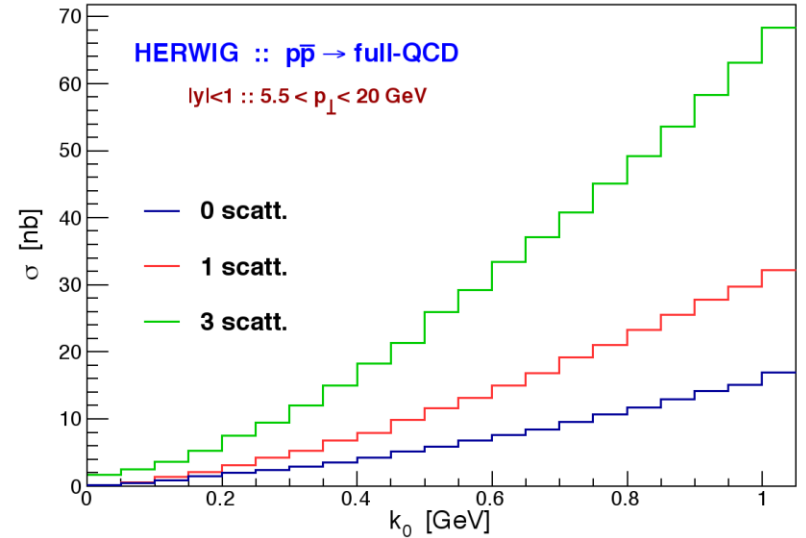
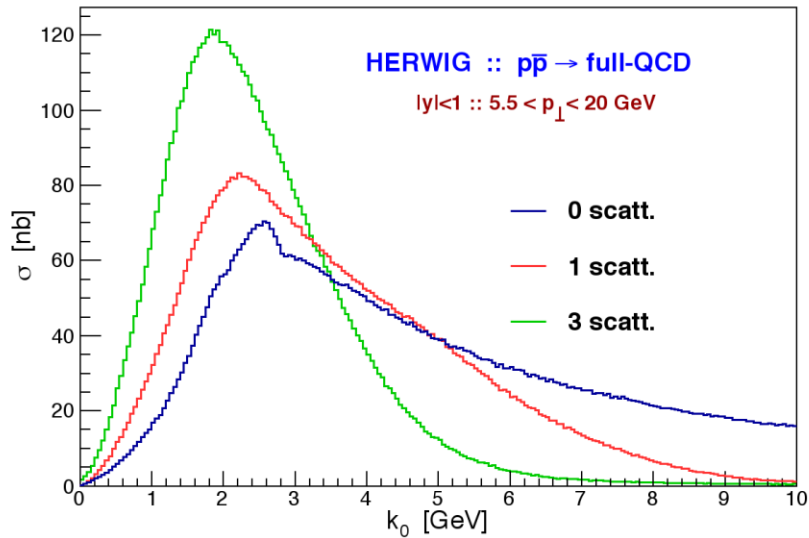
Esposito, Piccinini, AP, Polosa arXiv:1305.0527

The mechanism also implies: D mesons actually “**pushed**” inside
the potential well (the **classical 3-body problem!**)

$X(3872)$ is a **real, negative energy bound state** (stable)

It also explains a small width $\Gamma_X \sim \Gamma_{D^*} \sim 100$ keV

A new mechanism?



A new mechanism?

A. Esposito		HERWIG		PYTHIA	
k_0^{\max}		50 MeV	100 MeV	50 MeV	100 MeV
No. of events	0 scatt.	52	253	240	1560
	1 scatt.	44	299	283	1984
	3 scatt.	843	2069	4843	11679
	4 scatt.	1166	2802	6489	14916
	5 scatt.	1689	4167	7770	18284
σ [nb]	0 scatt.	0.10	0.50	0.13	0.83
	1 scatt.	0.09	0.59	0.15	1.05
	3 scatt.	1.67	4.10	2.57	6.20
	4 scatt.	2.31	5.55	3.44	7.92
	5 scatt.	3.34	8.25	4.12	9.71

Striking increase of σ
after each scattering!

Down by a factor 5-7
wrt $\sigma_{\text{exp}} \approx 30$ nb,
further increases with
4-5 scatterings

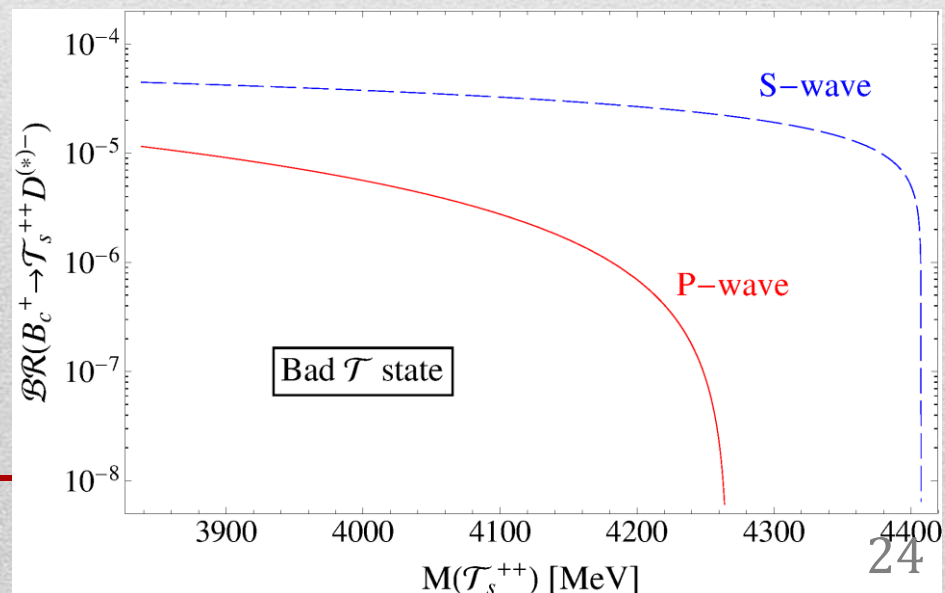
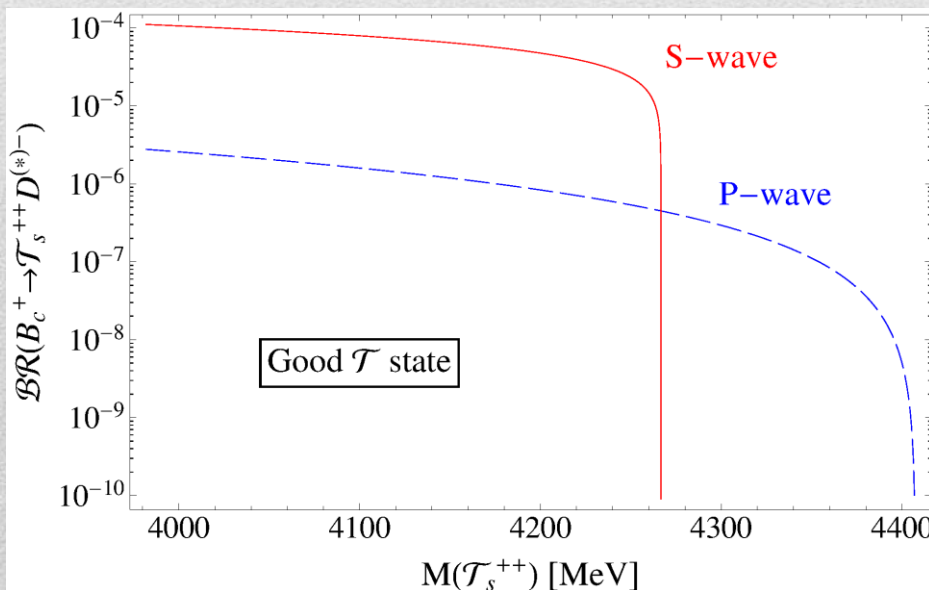
Doubly charmed states

Another approach to choose among models, is to predict states who fit only in one model

For example, we proposed to look for **doubly charmed states**, which in tetraquark model are $[cc]_{S=1}[\bar{q}\bar{q}]_{S=0,1}$

These states could be observed in **B_c decays @LHC**

Esposito, Papinutto, AP, Polosa, Tantalò, PRD88 (2013) 054029



Doubly charmed states

Another approach to choose among models,
is to **predict states who fit only in one model**

The **doubly charged** state $T_s^{++} = [cc]_{S=1}[\bar{d}\bar{s}]_{S=0}$
could not be explained in the molecular picture
because of the Coulombian repulsion.

If $M(T_s^{++}) > 3979$ MeV the state could decay into $D^{*+}D_s^+$
and could be seen @LHC

This state is particularly **well-defined on the lattice**,
because no disconnected diagrams are involved.

The calculation is ongoing...

Conclusions

The study of exotic resonances in heavy quark sector
is still puzzling

- The tetraquark picture predicts $Z_c(3900)$, but misses $Z'_c(4025)$
- The molecular picture has troubles with above-threshold states and production mechanisms
- Look for missing states and decay modes who can help in excluding models
- Explore new production mechanisms to take into account at- and above-threshold states
- Propose and search new states who can falsify some models

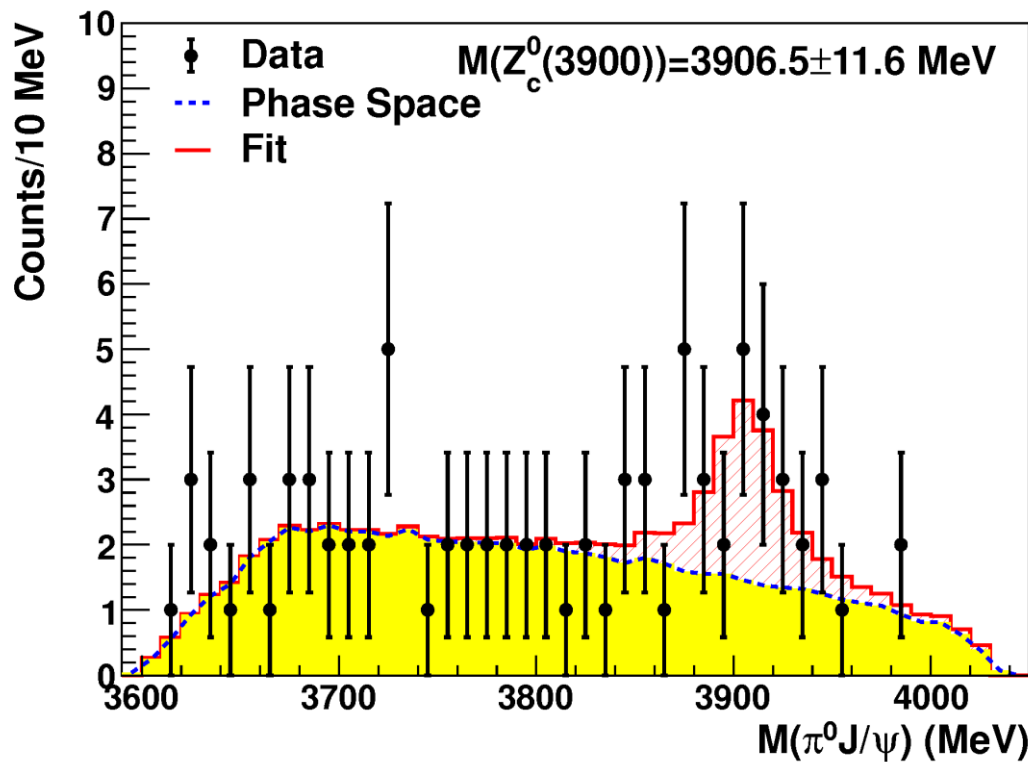
Thank you

BACKUP

$Z_c^0(3900)$ at CLEO?

A reanalysis of CLEO data shows a 3σ neutral resonance in

$$\psi(4160) \rightarrow \pi^0 Z_c^0 \rightarrow J/\psi \pi^0 \pi^0$$



Xiao et al.

arXiv:1304.3036

$$M = 3907 \pm 12 \text{ MeV}$$

$$\Gamma = 34 \pm 29 \text{ MeV}$$

Isospin violation?

Look for $Z_c^0 \rightarrow J/\psi \eta$

Decay channels

Two questions:

- What can $Z_c(3900)$ decay into?
 - Why is $Z_c(3900)$ much broader than $X(3872)$?
- $J/\psi \pi^+$
 - $\psi(2S)\pi^+$
 - $D^+ \overline{D}^{*0}, D^{*+} \overline{D}^0 \sim 4 \text{ MeV}$
 - $\eta_c \rho^+$
 - $h_c \pi^+$ in P-wave
 - Radiative decays

We suppose

$$g_{DD^*X(3872)} = g_{DD^*Z(3900)}$$

Decay channels

Two questions:

- What can $Z_c(3900)$ decay into?
- Why is $Z_c(3900)$ much broader than $X(3872)$?

- $J/\psi \pi^+ \sim 29 \text{ MeV}$
- $\psi(2S)\pi^+ \sim 6 \text{ MeV}$
- $D^+ \overline{D^{*0}}, D^{*+} \overline{D^0} \sim 4 \text{ MeV}$
- $\eta_c \rho^+ \sim 19 \text{ MeV}$
- $h_c \pi^+$ in P-wave
- Radiative decays

No grounds for other couplings

We only suppose

$$g = M_{Z_c}$$

Some agreement with QCD sum rules

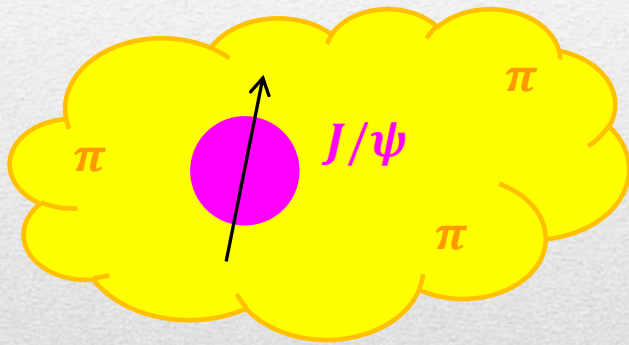
Dias *et al.* arXiv:1304.6433

$\Gamma \sim 60 \text{ MeV}$, agrees with experimental value

Other models

Hadro-charmonium

Voloshin arXiv:1304.0380



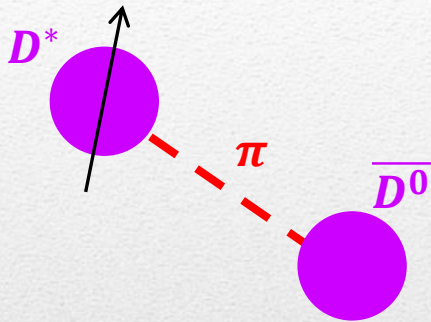
A $c\bar{c}$ state surrounded by light matter

Decay into $\eta_c \rho$ forbidden by HQSS

A light $Z'_c(3785)$ expected with $I^G J^{PC} = 1^- 0^{++}$
(not visible in $J/\psi \pi$ channel)

Other models

Molecule



Wang *et al.* arXiv:1303.6355

DD^* loosely bound molecule

$1-\pi$ exchange attractive in $I^C = 1^-$ channel,
although less than in $I^C = 0^+$ ($X(3872)$)

Tornqvist *Z.Phys.* C61 525-537

A molecule decays mostly **into its constituents**
(long range decay)

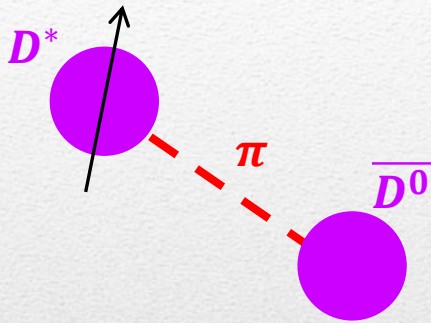
Decays into **charmonium + light mesons**
suppressed by $1/a$ (short range decay)

Braaten *et al.* PRD69, 074005

e.g. $BR(X(3872) \rightarrow DD^*) \sim 70\%$, $BR(X(3872) \rightarrow J/\psi \rho) \sim 5\%$

Other models

Molecule



Wang *et al.* arXiv:1303.6355

DD^* loosely bound molecule

$1-\pi$ exchange attractive in $I^C = 1^-$ channel,
although less than in $I^C = 0^+$ ($X(3872)$)

Tornqvist Z.Phys. C61 525-537

Expected with $\text{BR}(Z_c \rightarrow DD^*) \sim 70\text{-}80\%$

But we estimated $\Gamma(Z_c \rightarrow DD^*) \sim 4 \text{ MeV}$,

How to reach $\Gamma = 40 \text{ MeV}$?

A light $Z'_c(3760)$ expected with $I^G J^{PC} = 1^- 0^{++}$

A heavy $Z''_c(4020)$ expected at D^*D^* threshold

Voloshin

PRD 84, 031502

Other models

Molecule

$Z_c^0(3900)$ could violate isospin just like $X(3872)$

A $Y(4260) \rightarrow Z_c^0 \pi^0 \rightarrow J/\psi \eta \pi^0$ could occur

If so, it cannot be accommodated into molecular picture:

In $X(3872)$ isospin violation is due to

$$\Delta = M(D^+ D^{*-}) - M(D^0 D^{0*}) \sim 8 \text{ MeV}$$

Hanhart *et al.* PRD85 011501

Z_c^0 is above both thresholds, and $\Delta \ll \Gamma$

In molecular picture Z_c^0 should be a pure isovector

Strong couplings

How do we evaluate $g_{DD^*X(3872)}$?

$$g_{DD^*X(3872)}^2 = BR(X \rightarrow DD^*) \Gamma_X \left(\frac{p^*}{8\pi M_x^2} \overline{|M(X \rightarrow DD^*)|^2} \right)^{-1}$$

But if $M_X < M_D + M_{D^*}$ the decay momentum p^* is undefined

We average over a random set $(M_X)_i$, distributed as a Breit-Wigner, centered at $M_X = 3872$ MeV and with a width $\Gamma_X = 1.2$ MeV respecting the kinematical limits

$$M_D + M_{D^*} < (M_X)_i < M_B - M_K$$

We get $g_{DD^*X(3872)} = 2.5$ GeV

Strong couplings

The matrix element can be evaluated in an effective theory

$$\langle D(p) D^*(\eta, q) | X(\lambda, P) \rangle = g_{DD^*X} \eta \cdot \lambda$$
$$\frac{1}{3} \sum_{\text{pol}} |\langle D(p) D^*(\eta, q) | X(\lambda, P) \rangle|^2 = \frac{1}{3} g_{DD^*X}^2 \left(3 + \frac{p^{*2}}{M_X^2} \right)$$

The D-wave component is negligible with respect to the S-wave one

We get $g_{DD^*X(3872)} = 2.5 \text{ GeV}$

Strong couplings

What about other couplings?

We cannot relate $g_{X\psi\rho}$ to $g_{Z_c\psi\pi}$
(no chiral symmetry or HQSS)

But we are talking about **S-wave decays**
and we need couplings with the **dimension of a mass**

The main **mass scale** is the **mass of the $Z_c(3900)$**

So we estimate

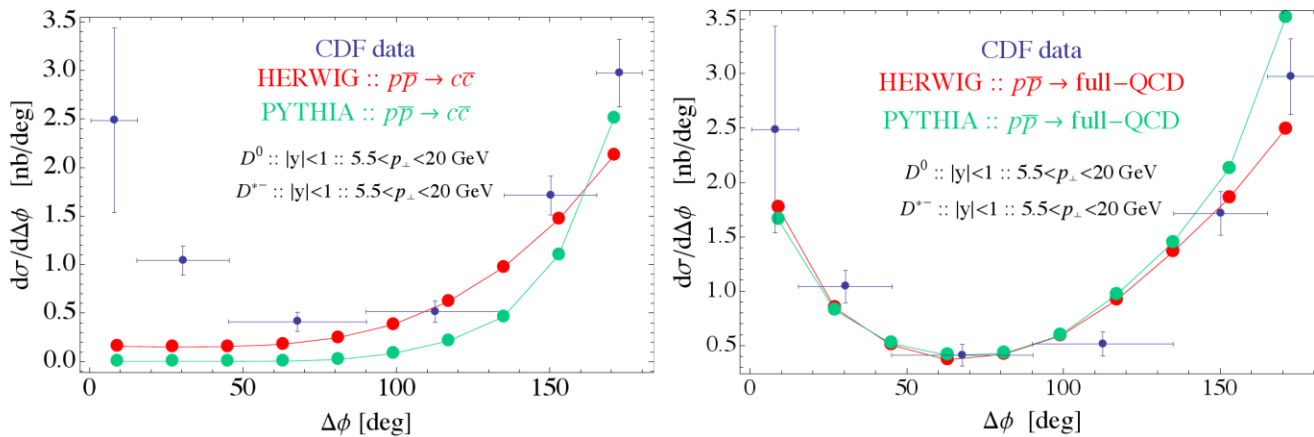
$$g \sim M_{Z_c} \sim 3900 \text{ MeV}$$

Tuning of MC

Monte Carlo simulations

A. Esposito

- We compare the $D^0 D^{*-}$ pairs produced as a function of relative azimuthal angle with the results from CDF:



The c-cbar run underestimate the low angles (low- k_T) region!

Such distributions of charm mesons are available at Tevatron
No distribution has been published (yet) at LHC