



η and η' Physics at MAMI

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University Mainz
Messina, 14th October 2013

Outline

- Crystal Ball Set-up at MAMI
- η/η' Cross Sections
- Timelike Transition Form Factor from $\eta/\eta' \rightarrow e^+e^-\gamma$
- Preliminary Results for $\eta \rightarrow \pi^0\gamma\gamma$
- Future Plans
- Summary



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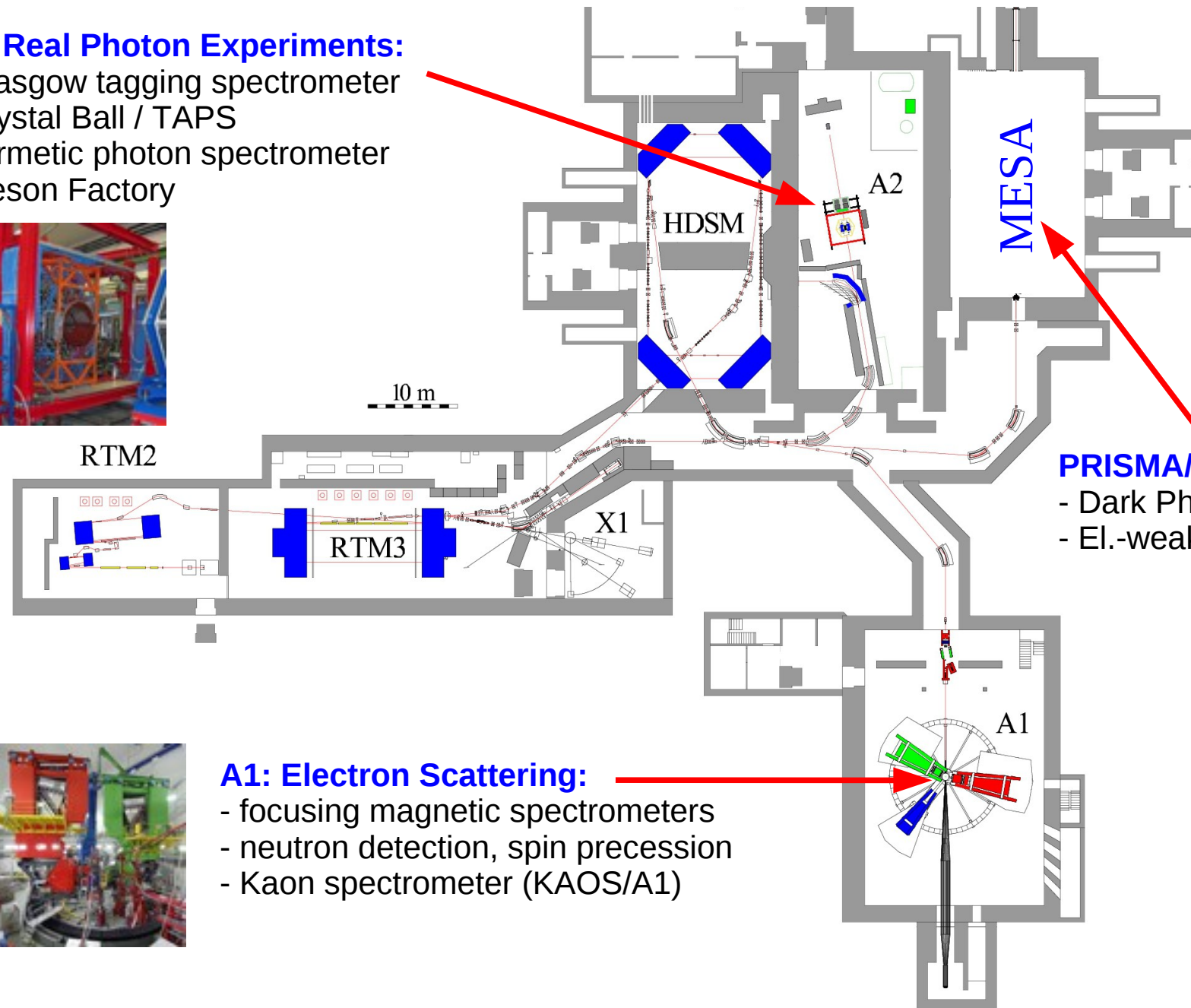
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Experiments at MAMI

A2: Real Photon Experiments:

- Glasgow tagging spectrometer
- Crystal Ball / TAPS hermetic photon spectrometer
- Meson Factory



PRISMA/SFB 1044:

- Dark Photon Search
- El.-weak Mixing Angle

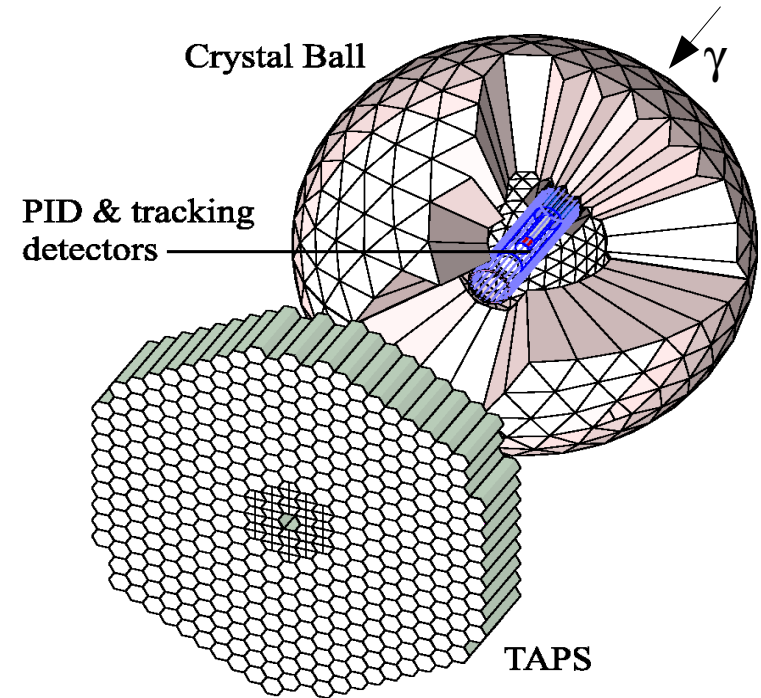
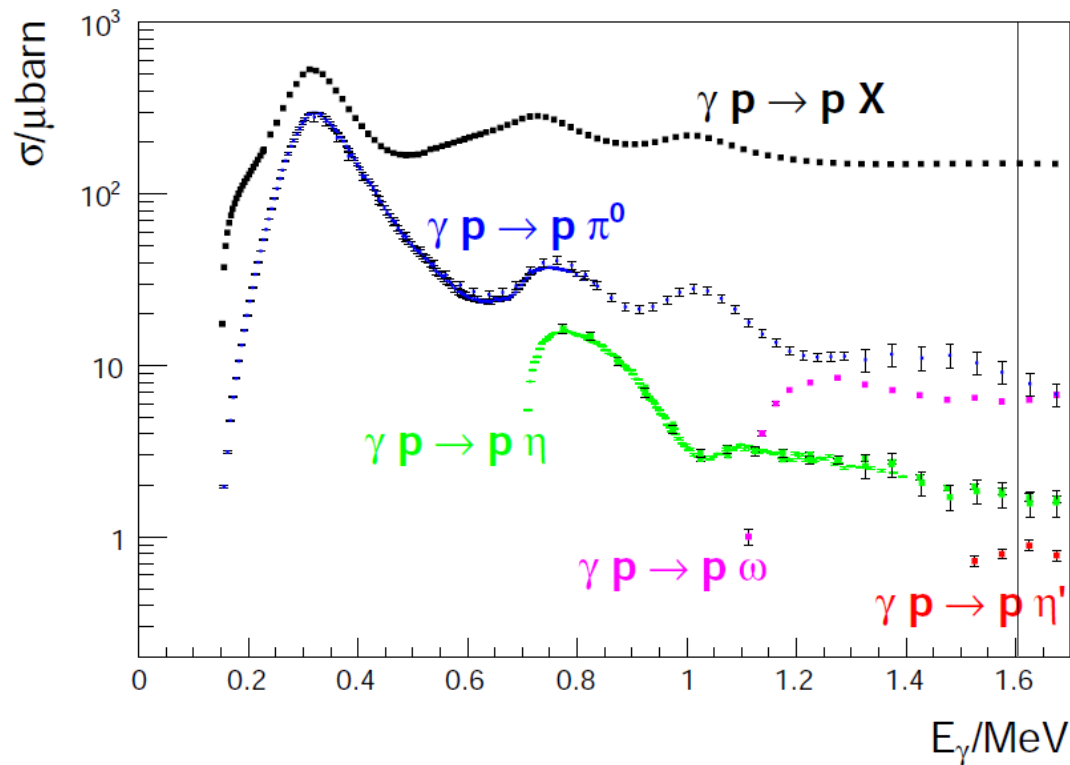
A1: Electron Scattering:

- focusing magnetic spectrometers
- neutron detection, spin precession
- Kaon spectrometer (KAOS/A1)



Meson Production with Real Photons

Data from CB@MAMI, CB@ELSA, CLAS, SAPHIR



Current production rates on IH_2 target feasible for taking data:

η : $10^5 \text{ h}^{-1} \Rightarrow \text{Goal } 10^6 \text{ h}^{-1}$

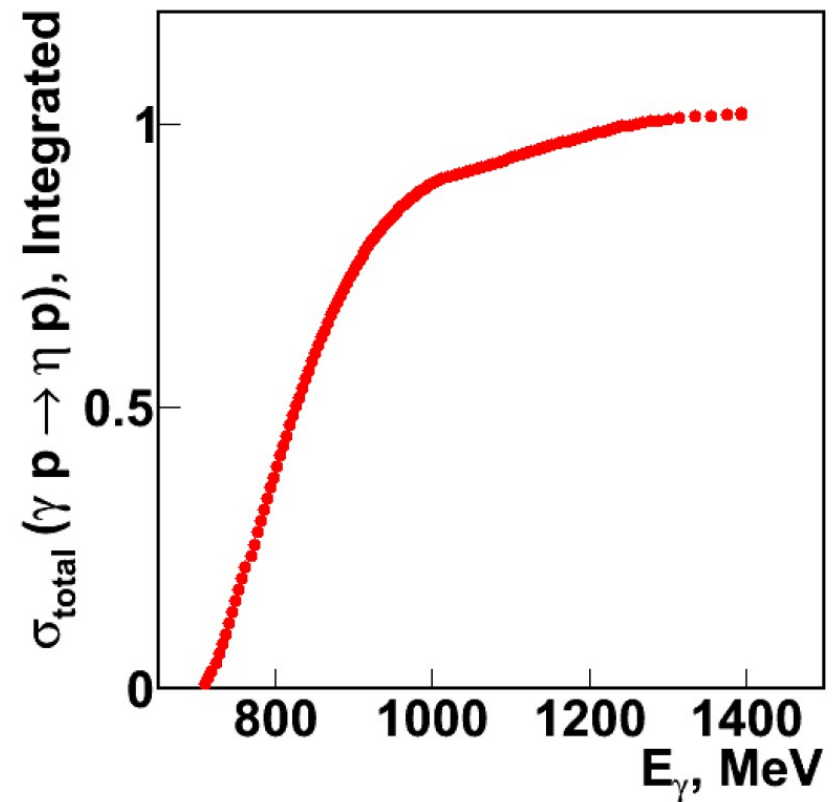
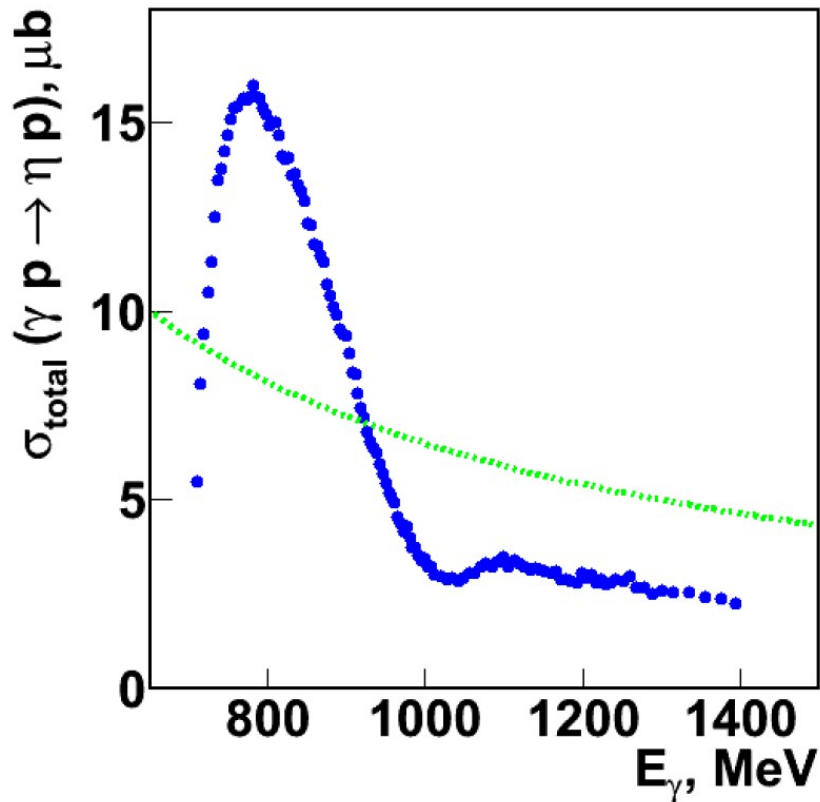
η' : $2 \cdot 10^3 \text{ h}^{-1} \Rightarrow \text{Goal } 1.5 \cdot 10^4 \text{ h}^{-1}$

Has to be imposed by detection and analysis efficiencies

\Rightarrow 4π Crystal Ball/TAPS setup, e.m. Production mechanism very clean

\Rightarrow Ideally suited to measure high rates of meson decays

η -Photoproduction



At MAMI a beam of tagged photons of excellent quality is available:

- High intensity photon beam
- Fine energy resolution
- Outstanding stability

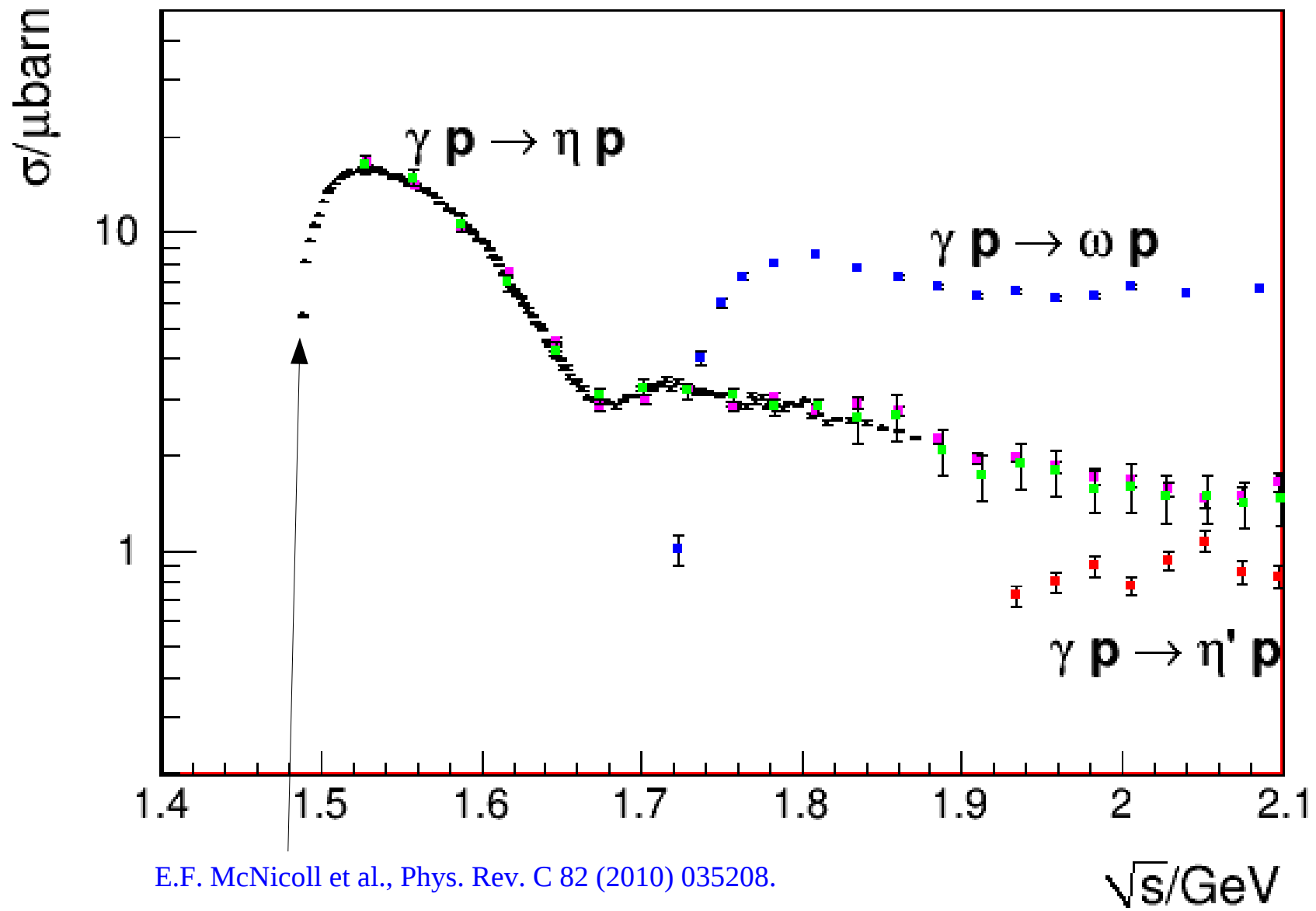
Beam energy nearly perfect for high statistics η photoproduction

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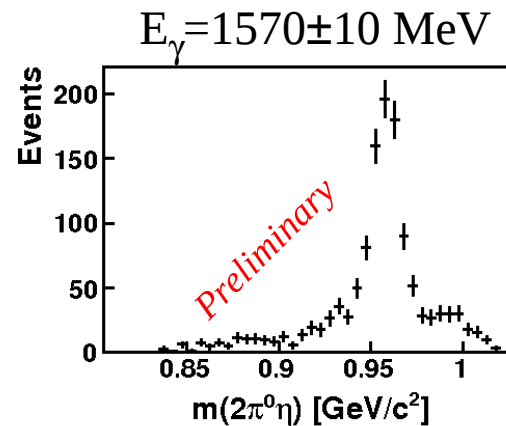
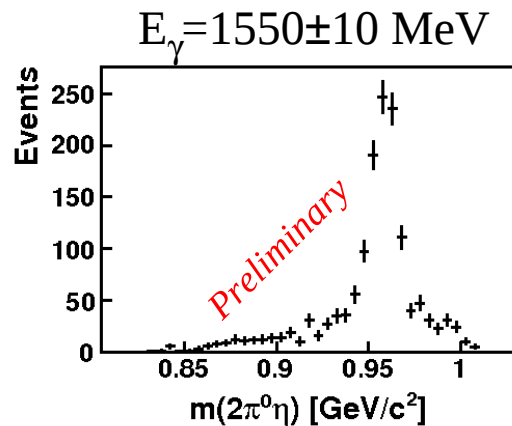
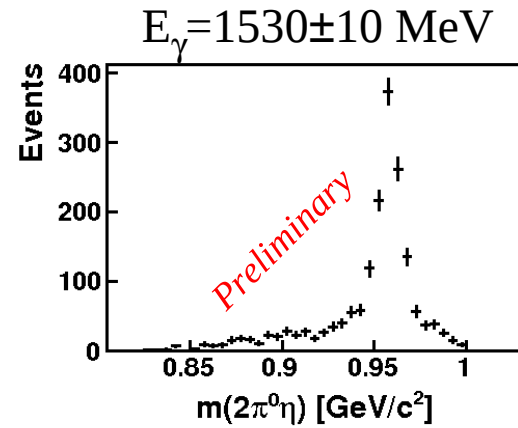
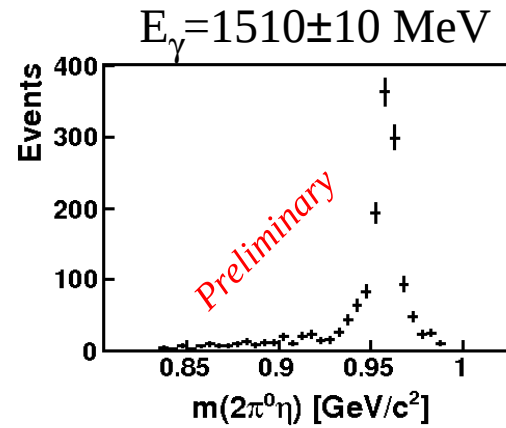
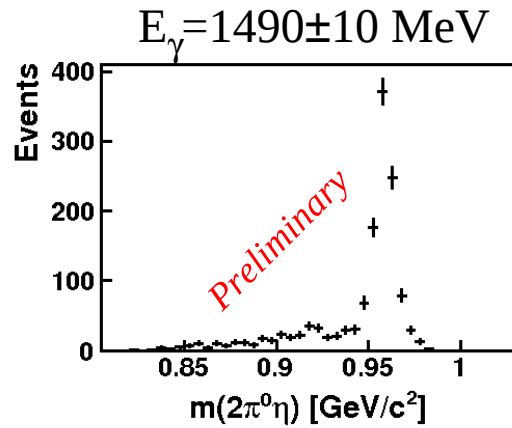
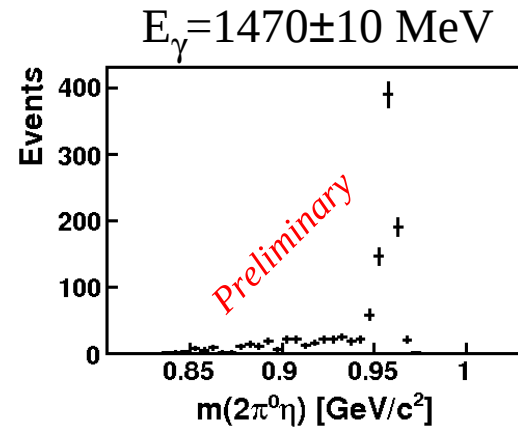
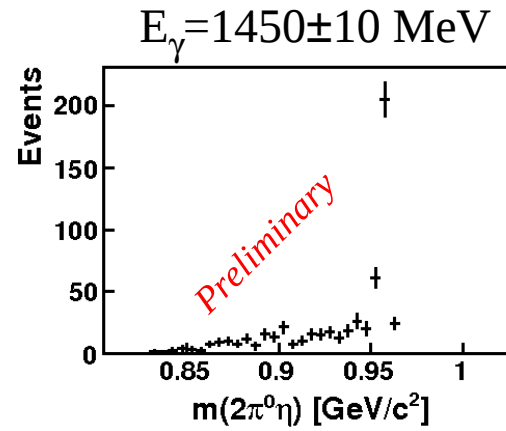
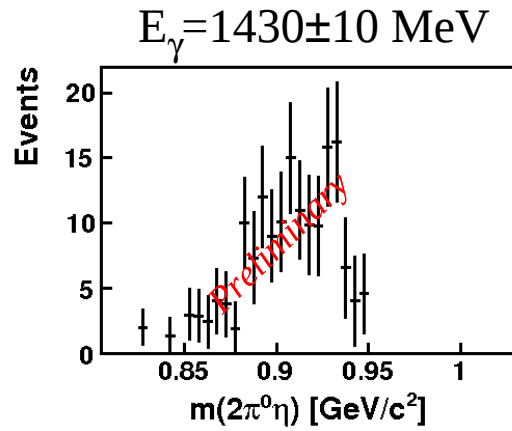
η Production



E.F. McNicoll et al., Phys. Rev. C 82 (2010) 035208.

Data from Crystal Ball, Crystal Barrel, SAPHIR, CLAS

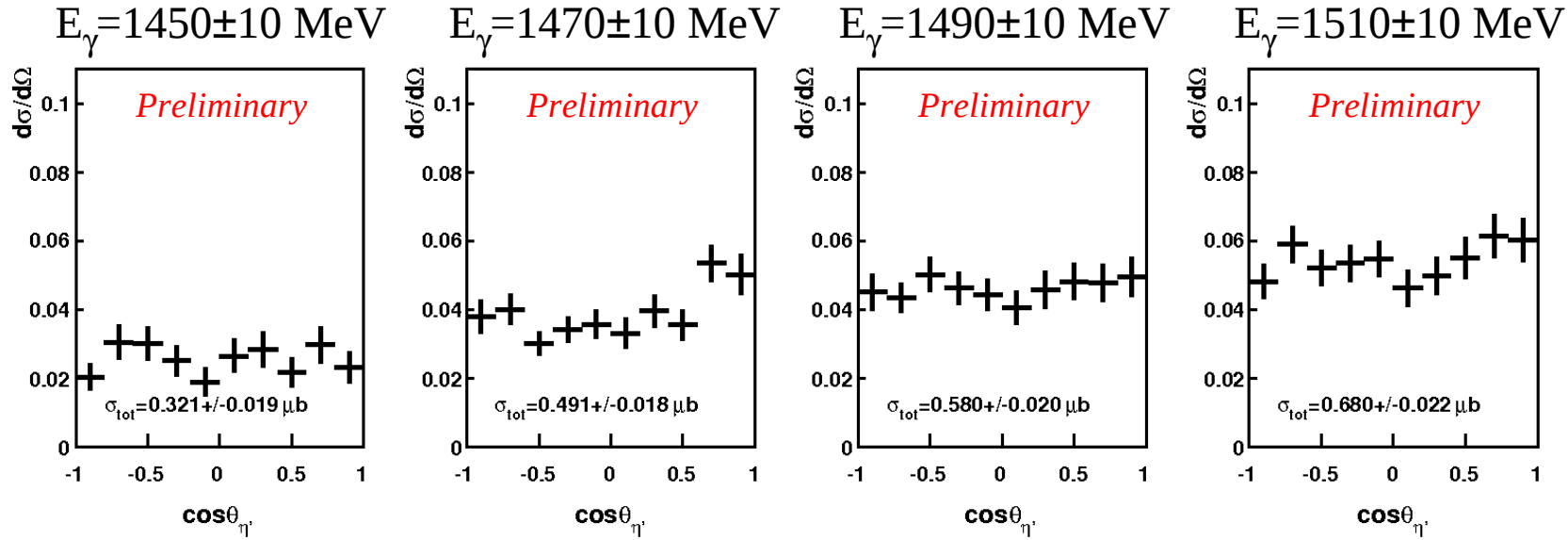
$\eta' \rightarrow \eta \pi^0 \pi^0$ Invariant Mass



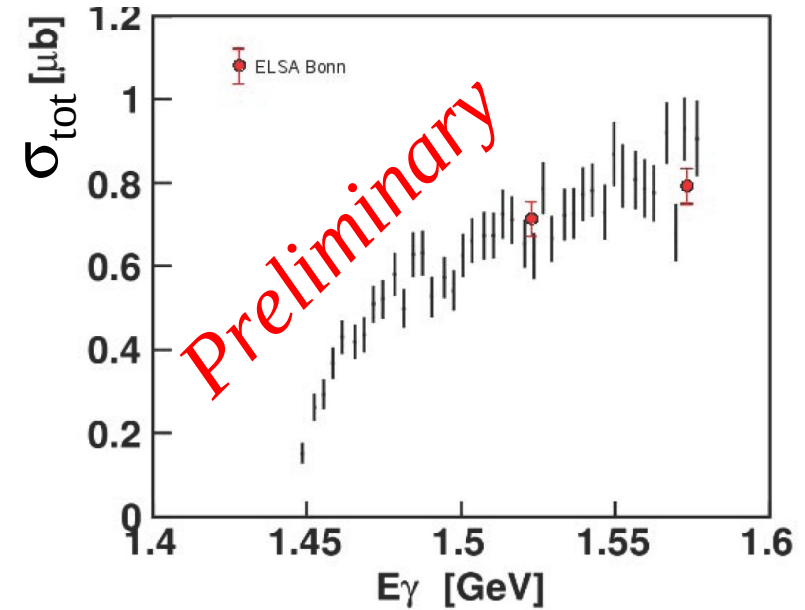
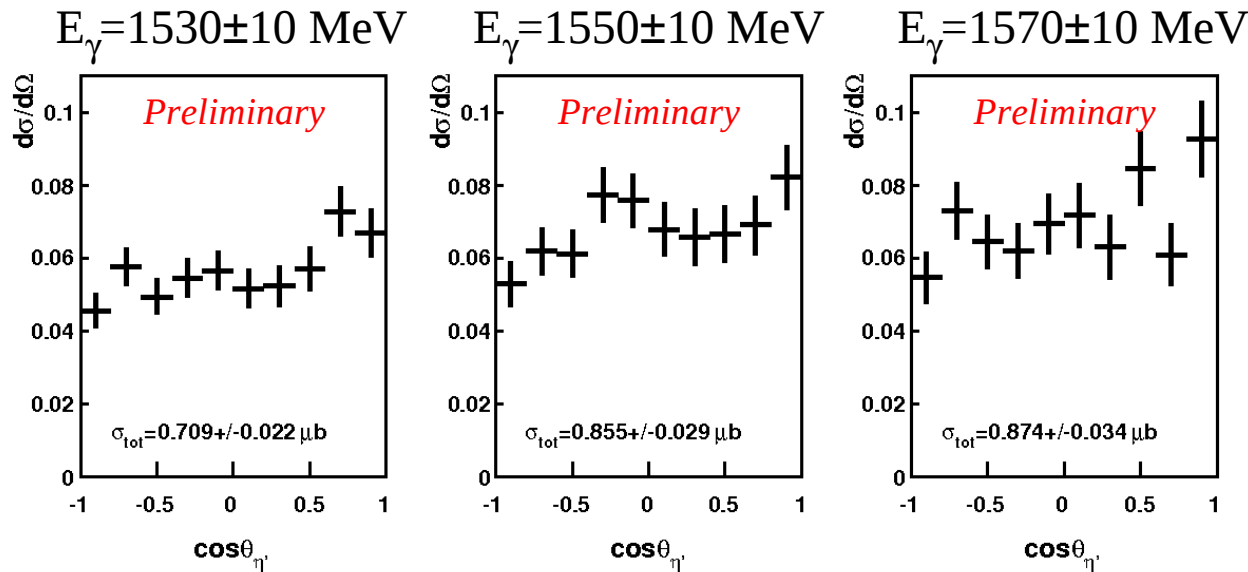
S. Prakhov (UCLA)
P. Ott (Mainz)

η' Cross Section

Using $\eta' \rightarrow \eta\pi^0\pi^0$



S. Prakhov (UCLA)
P. Ott (Mainz)



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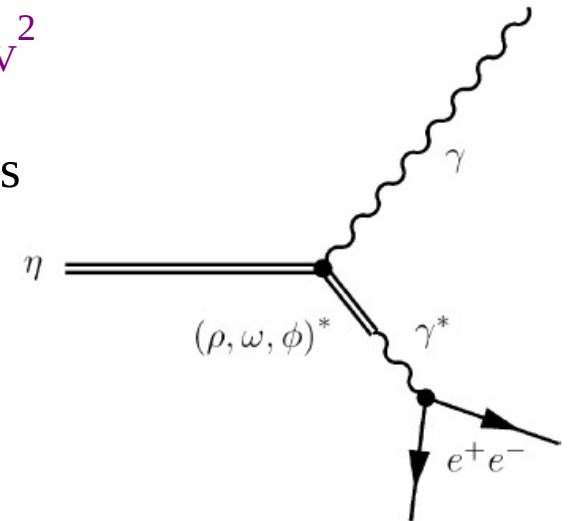
- Crystal Ball Set-up at MAMI
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Transition Form Factor with VMD

- Mechanism especially pronounced in timelike region at $q^2 \approx m_V^2$
 - Virtual meson reaches „mass shell“, becomes real
 - Strong resonance enhancement around vector meson mass
- TFF behaviour, especially for η' , not well known
- TFF modifies differential decay width

$$\frac{d\Gamma}{dm^2} = \left[\frac{d\Gamma}{dm^2} \right]_{\text{QED}} \cdot |F(m^2)|^2$$



- For η often one-pole approximation used:

$$|F(m^2)|^2 = \left(1 - \frac{m^2}{\Lambda^2} \right)^{-2} \quad \Lambda \approx 0.72 \text{ GeV} \quad \text{VMD: } \Lambda \approx m_\rho = 0.77 \text{ GeV}$$

- For η' resonance shape:

$$|F(m^2)|^2 = \frac{\Lambda^2(\Lambda^2 + \gamma^2)}{(\Lambda^2 - m^2)^2 + \Lambda^2\gamma^2} \quad \Lambda \approx 0.76 \text{ GeV} \quad \gamma \approx 0.10 \text{ GeV}$$

Hadronic LbL Contribution to $a_\mu = (g-2)_\mu$

- QED contributions:

$$a_\mu^{\text{QED}} = (11658471.895 \pm 0.008) \cdot 10^{-10}$$

T. Kinoshita et al., Phys. Rev. Lett. **109** (2012) 111808.

- Electro-Weak contribution:

$$a_\mu^{\text{Weak}} = (15.4 \pm 0.2) \cdot 10^{-10}$$

A. Czarnecki et al., Phys. Rev. D **67** (2003) 073006.

Erratum-ibid. D **73** (2006) 119901.

M. Knecht et al., JHEP 0211 (2002) 003.

- Hadronic vacuum polarisation:

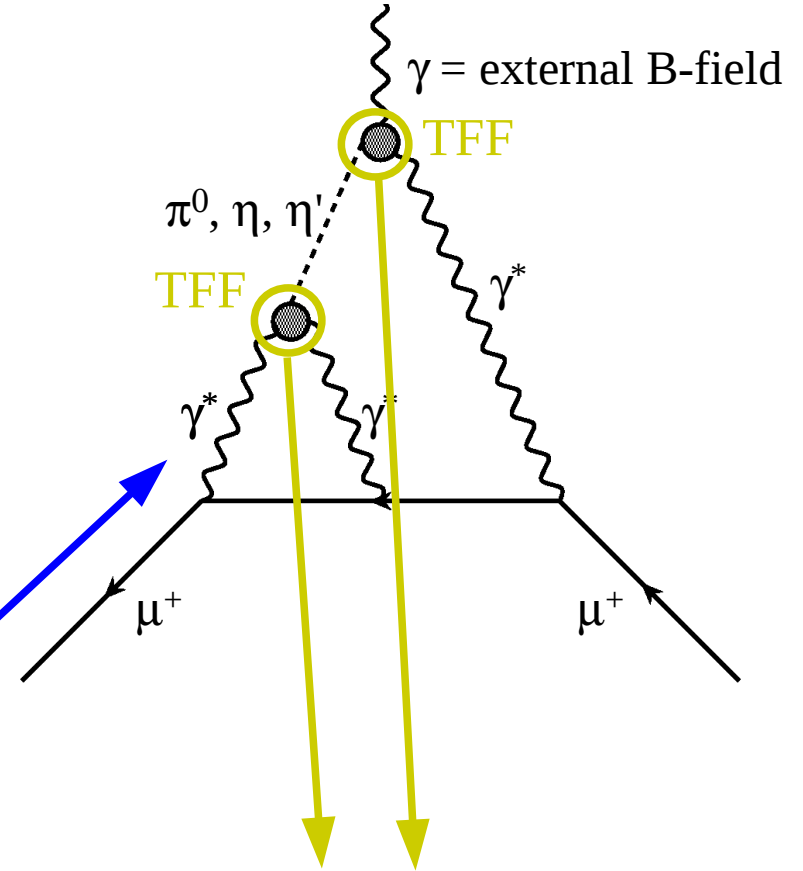
$$a_\mu^{\text{VP}} = (692.3 \pm 4.2) \cdot 10^{-10}$$

M. Davier et al., Eur. Phys. J. C **71** (2011) 1515.

- Hadronic light-by-light:

$$a_\mu^{\text{LbL}} = (10.5 \pm 2.6) \cdot 10^{-10}$$

J. Prades et al., arXiv:0901.0306 (2009).

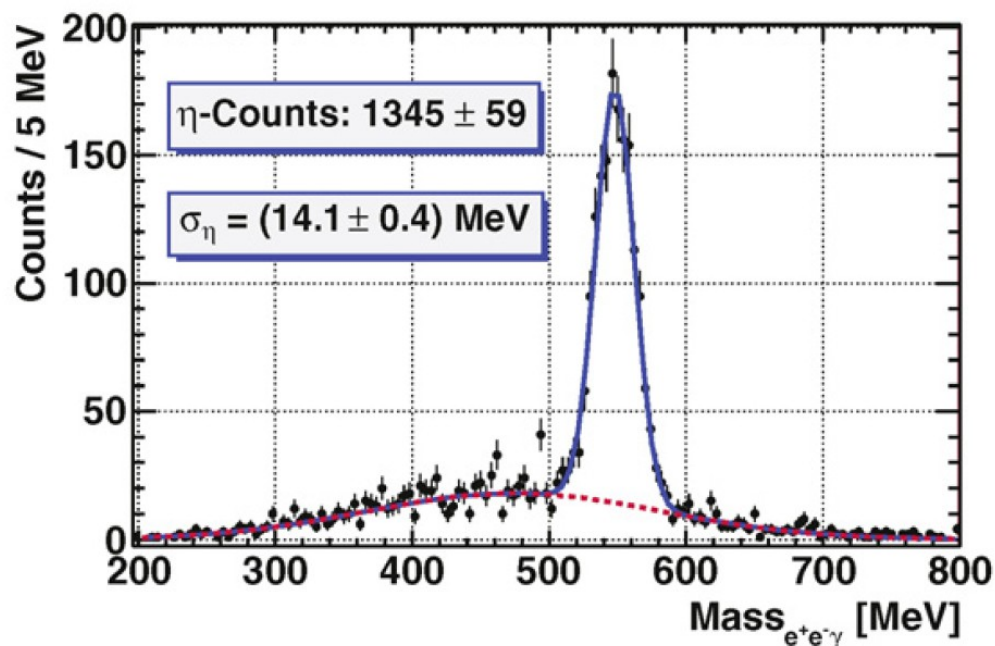


Transition Form Factors of light pseudoscalar mesons could give important input for SM calculations of $(g-2)_\mu$

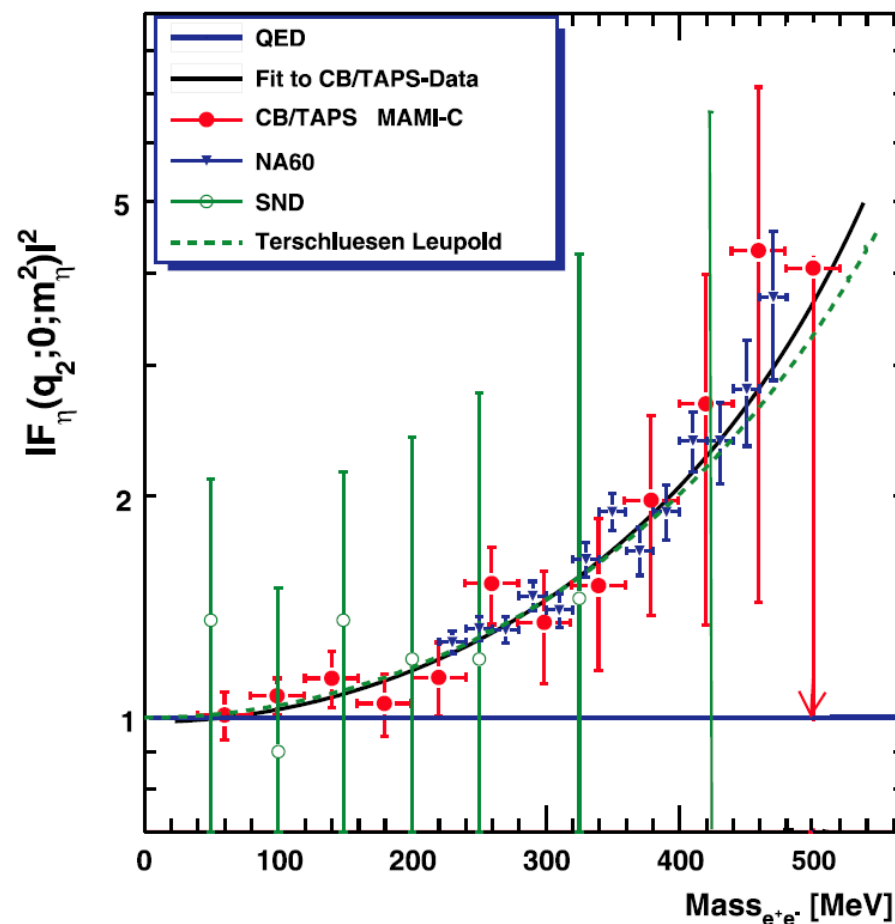
First A2 Result for η TFF

H. Berghäuser et al. (A2-Collaboration), Phys. Rev. B 701 (2011) 562-567.

- Based on **kinematic cuts**
- **Small amount of data**
- **Limited photoproduction energy range**



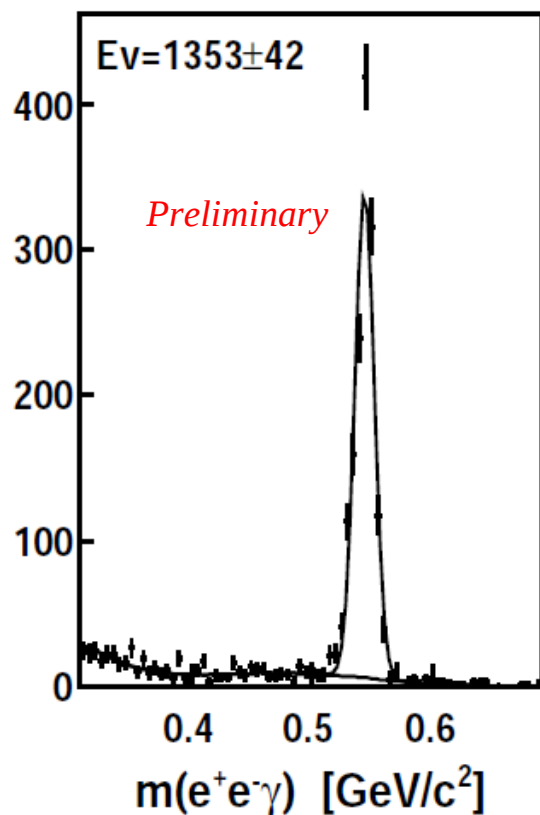
$$\Lambda^{-2} = (1.92 \pm 0.35_{\text{stat}} \pm 0.13_{\text{syst}}) \text{ GeV}^{-2}$$



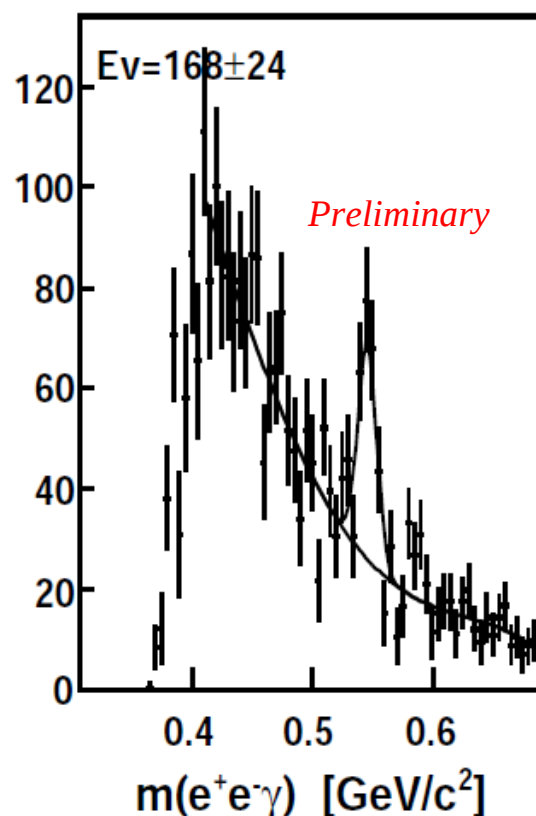
New Analysis of η TFF

- Based on **kinematic fitting**
- **3x** more data
- **Full η photoproduction** range accessible at MAMI used
- 18,000 events (no proton requirement: 22,000 events)

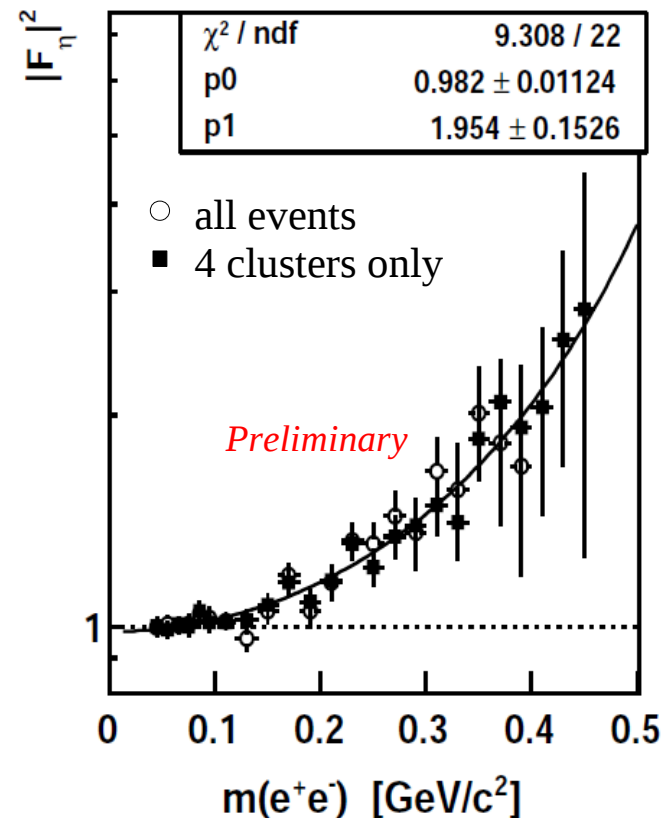
$m(e^+e^-)=45\pm 5$ MeV



$m(e^+e^-)=285\pm 5$ MeV

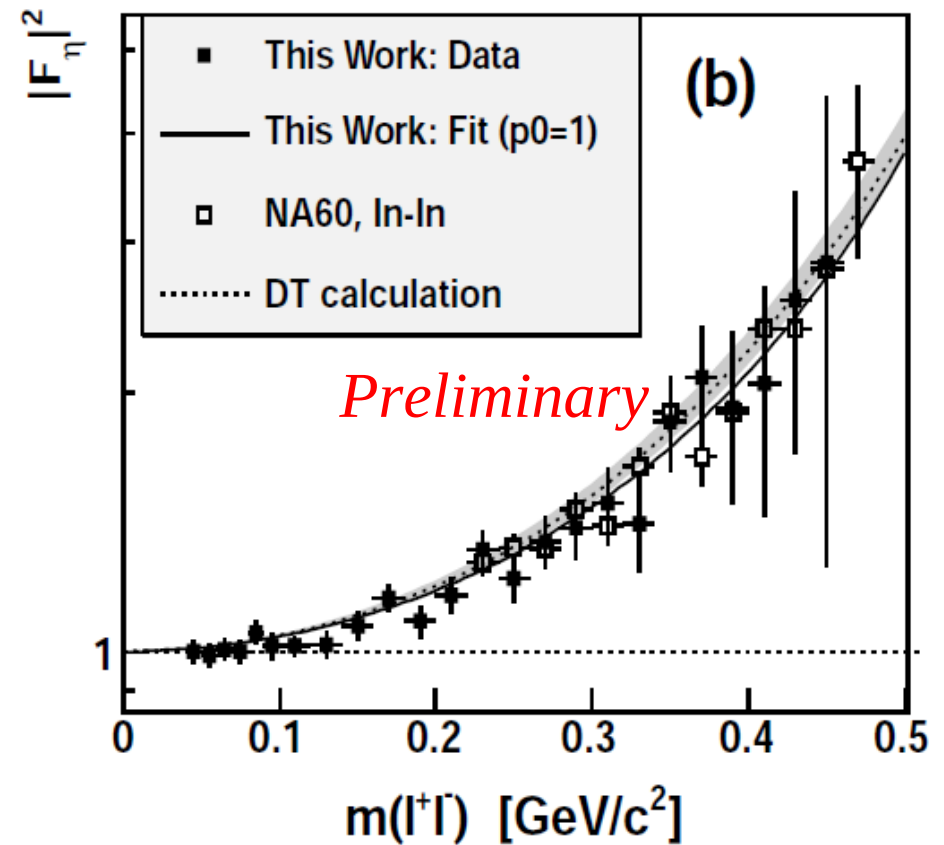
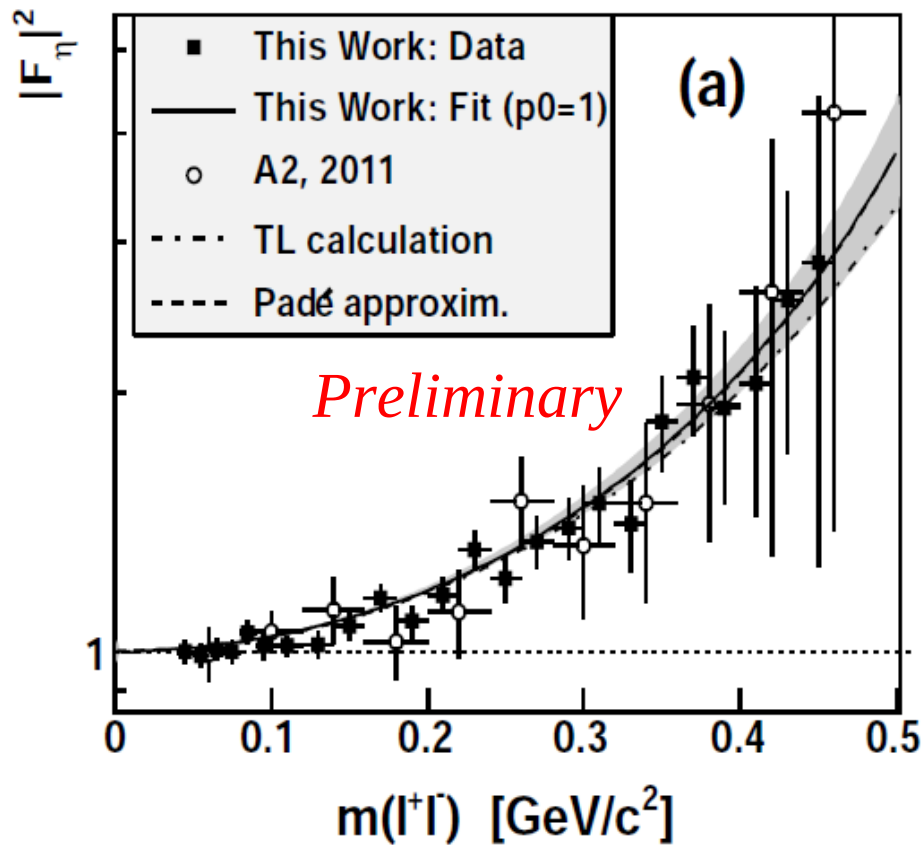


Solid line: Pole-approximation fit
Normalisation p_0 and $\Lambda^{-2}=p_1$ as free parameters



New A2 Result for η TFF

S. Prakhov, M. Unverzagt et al., submitted to Phys. Rev. C



$$\Lambda^{-2} = (1.95 \pm 0.15_{\text{stat}} \pm 0.10_{\text{syst}}) \text{ GeV}^{-2} \quad \textit{preliminary}$$

A2, 2011: H. Berghäuser et al., Phys. Rev. B 701 (2011) 562-567.

NA60, In-In: R. Arnaldi et al., Phys. Lett. B 677 (2009) 260.

TL calculation: C. Terschlüsen, Diploma thesis, University Gießen, 2010.

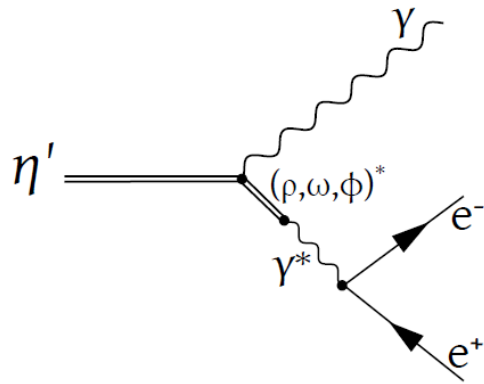
Padé-approximants: R. Escribano, P. Masjuan, P. Sanchez-Puertas, arXiv:1307.2061 [hep-ph].

DT calculation: C. Hahnart, A. Kupś, U.-G. Meißner, F. Stollenwerk, A. Wirzba, arXiv: 1307.5654 [hep-ph].

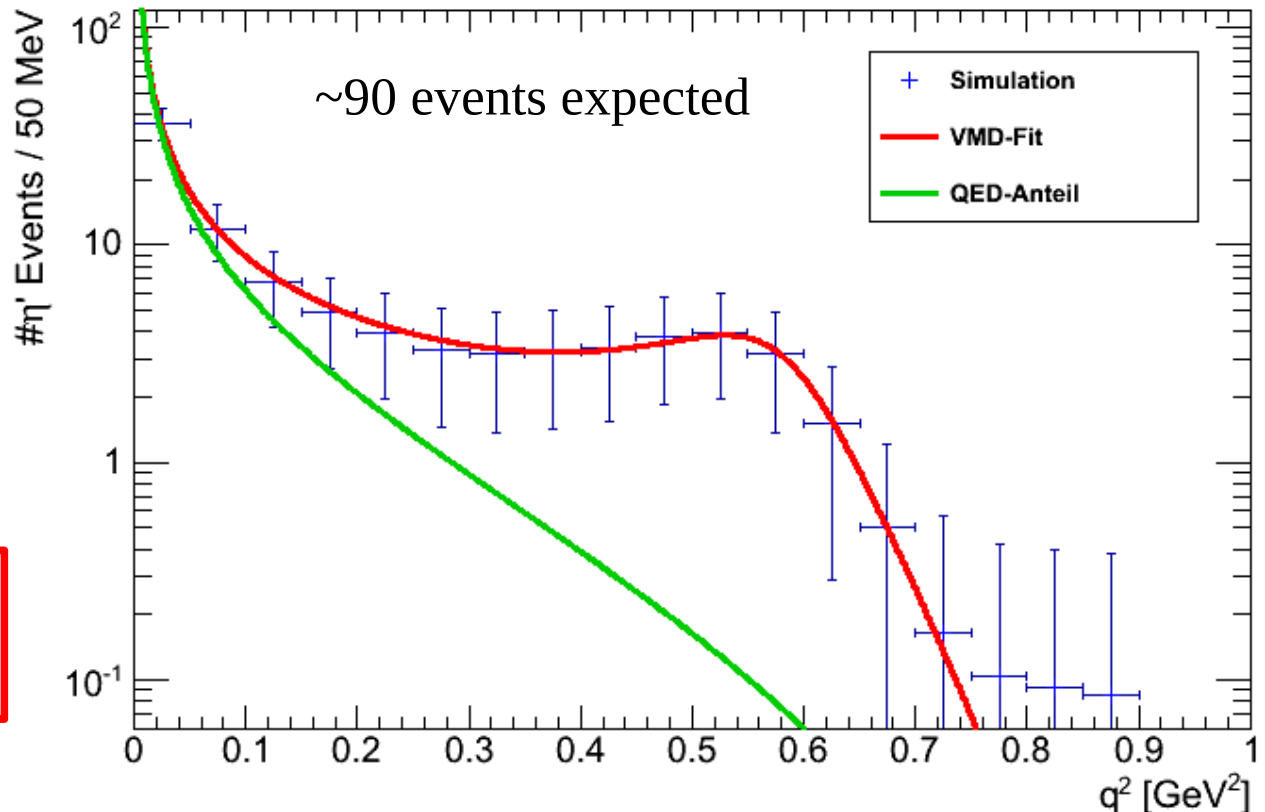
Timelike TFF for η'

S. Wagner, Master thesis, University Mainz, 2013
M. Unverzagt, A. Denig

- $\eta' \rightarrow e^+e^-\gamma$ no observation published yet
- Simulation based on
 - PDG upper limit for branching ratio
 - η' production rate at MAMI-C (5 weeks, total 1.65 million η')
 - Acceptance from $\sim 8.5\%$ (after background suppression)



$$|F(m^2)|^2 = \frac{\Lambda^2(\Lambda^2 + \gamma^2)}{(\Lambda^2 - m^2)^2 + \Lambda^2\gamma^2}$$



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Double Radiative $\eta \rightarrow \pi^0 \gamma \gamma$

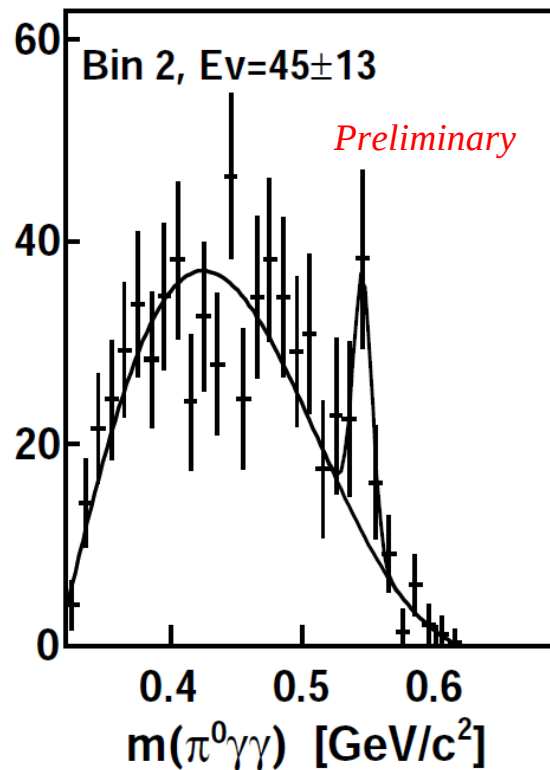
- Tree level amplitudes at $O(p^2)$ and $O(p^4)$ vanish
- π and K loops largely suppressed by G -parity and large Kaon mass
- First sizable contribution from (p^6)
- Coefficients must be determined using models (e.g. VMD)
 - \Rightarrow Stringent test for χ PT at $O(p^6)$ as well as models
- Calculations must describe $\Gamma(\eta \rightarrow \pi^0 \gamma \gamma)$ and differential decay width $d\Gamma/dm^2(\gamma\gamma)$
- Discrepancies between models in $d\Gamma/dm^2(\gamma\gamma)$
- Discrepancies in experimental results for $\Gamma(\eta \rightarrow \pi^0 \gamma \gamma)$
- Experimental challenges:
 - Small rate
 - Large background (e.g. $\pi^0 \pi^0$)
 - Only three measurements of $d\Gamma/dm^2(\gamma\gamma)$: [CB@AGS](#), [CB@MAMI](#), [WASA@COSY](#)
- New [CB@MAMI](#) analysis based on data taken in 2007 and 2009 ($6 \cdot 10^7$ η produced)

Analysis of $\eta \rightarrow \pi^0 \gamma \gamma$

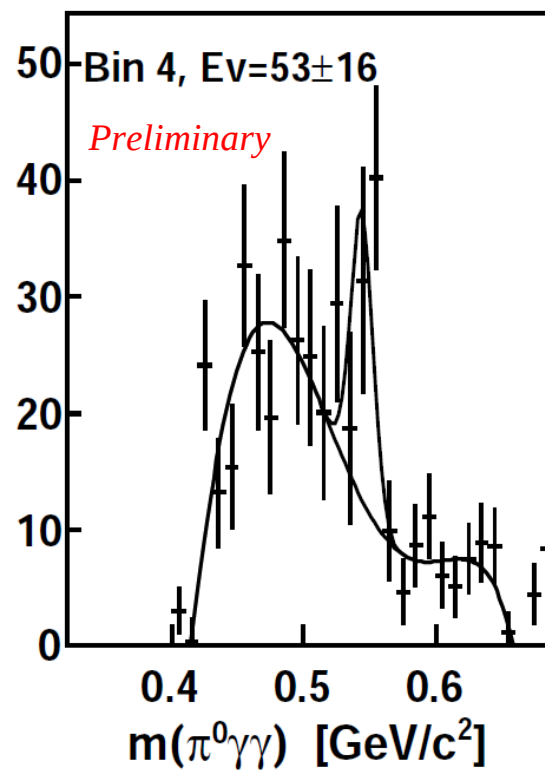
- Based on **kinematic fitting**
- $\pi^0 \pi^0$ background suppressed by anti-hypothesis
- Results based on $1.2 \cdot 10^3$ $\eta \rightarrow \pi^0 \gamma \gamma$ events

- **Below preliminary results from 2009**

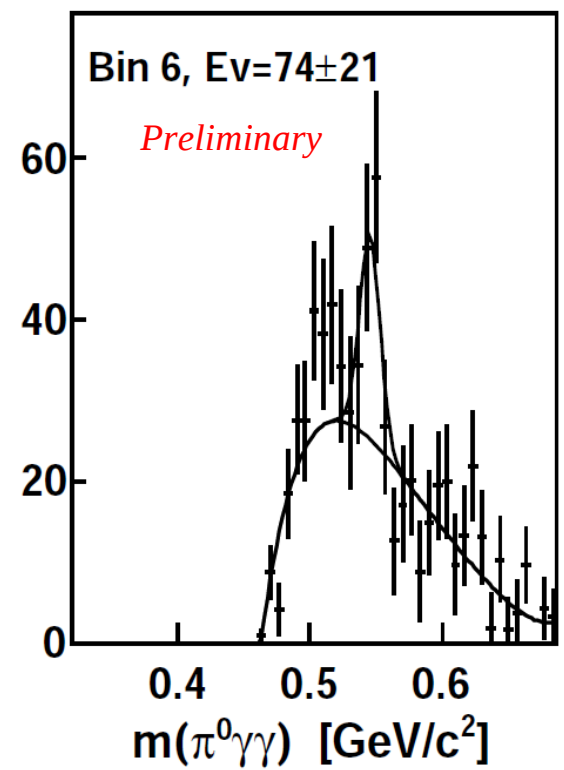
$$m^2(\gamma\gamma) = (0.0375 \pm 0.0100) \text{ GeV}^2/c^4$$



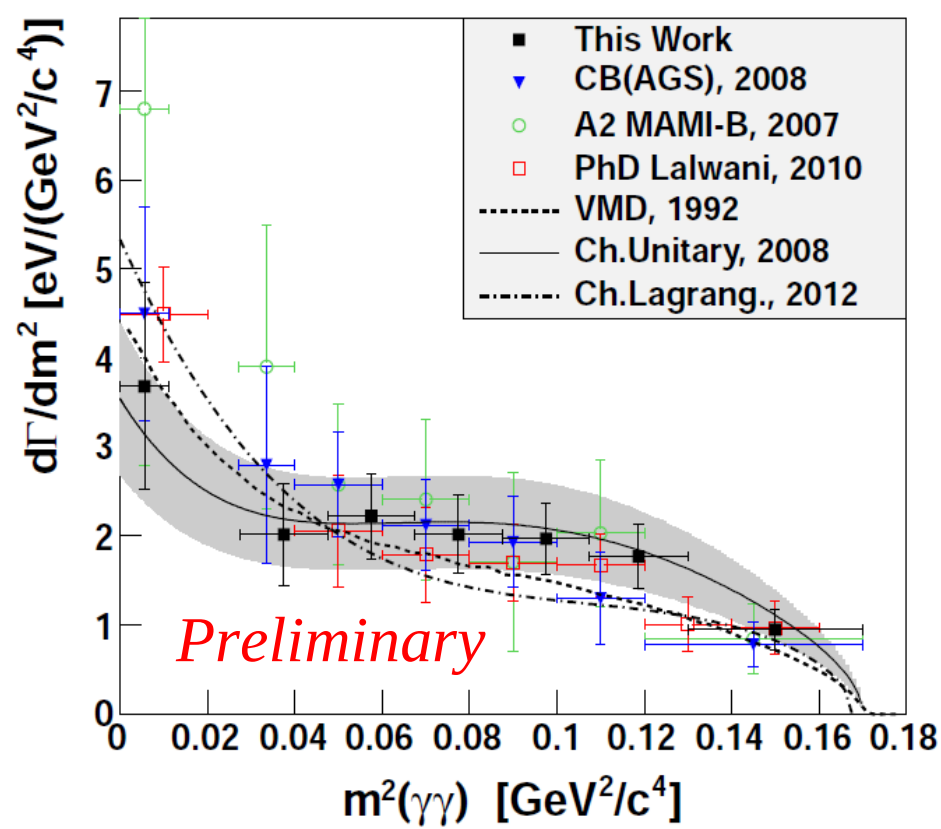
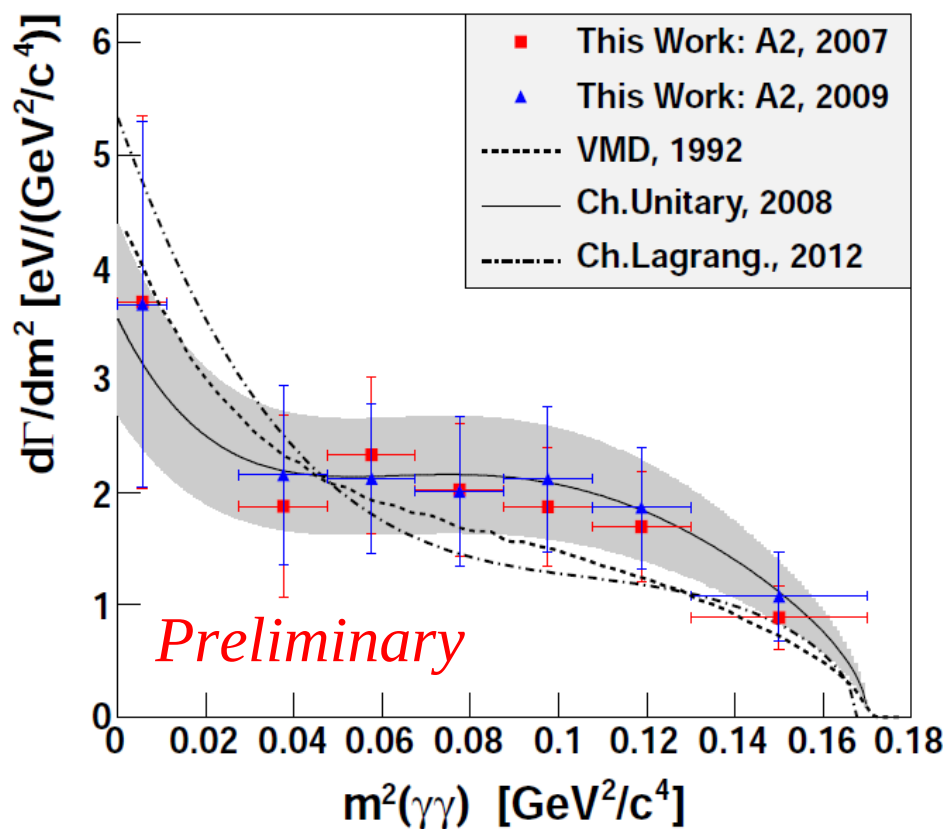
$$m^2(\gamma\gamma) = (0.0775 \pm 0.0100) \text{ GeV}^2/c^4$$



$$m^2(\gamma\gamma) = (0.11875 \pm 0.01125) \text{ GeV}^2/c^4$$



Decay Rate $\eta \rightarrow \pi^0 \gamma \gamma$



General agreement but statistics still not sufficient to distinguish between models.
To be submitted soon!

CB (AGS): S. Prakhov et al., Phys. Rev. C **78** (2008) 015206.

A2 MAMI-B: S. Prakhov, Proceedings of MENU 2007, published in eConf C070910 (2007) 159.

WASA: K. Lalwani, Ph.D. Thesis, Depart. of Physics, Indian Inst. of Technology, Bombay (2010).

VMD: J. N. Ng, D. J. Peters, Phys. Rev. D **46** (1992) 5034.

Ch. Unitary: E. Oset, J.R. Palaez, L. Roca, Phys. Rev. D **77** (2008) 073001.

Ch. Lagrang.: I. V. Danilkin, M. F. M. Lutz, S. Leupold, C. Terschlußen, arXiv:1211.1503 [hep-ph].

Decay Width of $\eta \rightarrow \pi^0 \gamma \gamma$

$\Gamma = (0.84 \pm 0.19) \text{ eV}$, GAMS2000, 1984

$\Gamma = (0.45 \pm 0.12) \text{ eV}$, CB(AGS), 2005

$\Gamma = (0.11 \pm 0.04) \text{ eV}$, KLOE, 2006 (preliminary)

$\Gamma = (0.290 \pm 0.063) \text{ eV}$, A2(MAMI B), 2007 (preliminary)

$\Gamma = (0.285 \pm 0.068) \text{ eV}$, CB(AGS), 2008 (reanalysis of 2005)

$\Gamma = (0.33 \pm 0.11) \text{ eV}$, WASA at COSY, Ph.D. thesis of K. Lalwani, 2010 (preliminary)

$\Gamma = (0.30^{+0.16}_{-0.13}) \text{ eV}$, VMD, 1992

$\Gamma = (0.33 \pm 0.08) \text{ eV}$, Ch. Unitary, 2008

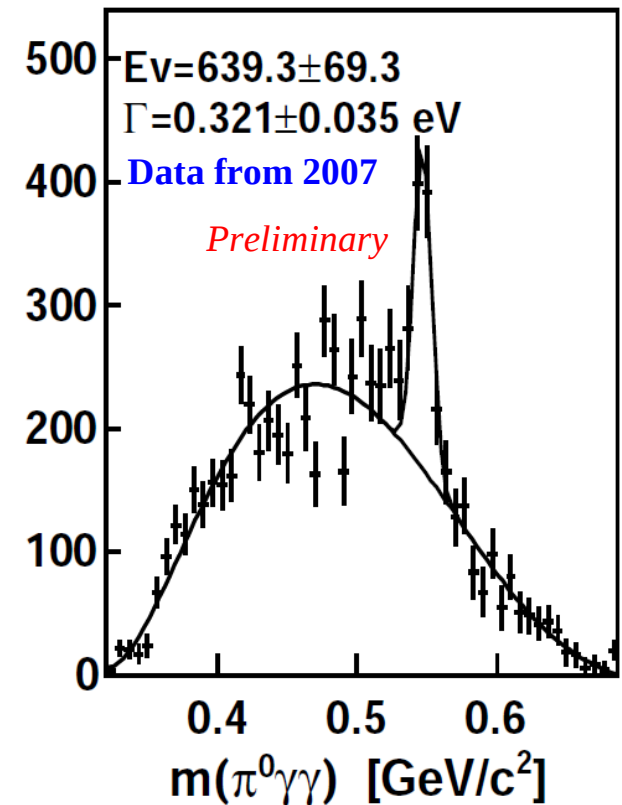
$\Gamma = 0.31 \text{ eV}$, Ch. Lagrang., 2012

CB at MAMI (2013): [S. Prakhov \(UCLA, University Mainz\)](#)

- **Data from 2007 and 2009 combined:**

$$\Gamma(\eta \rightarrow \pi^0 \gamma \gamma) = (0.33 \pm 0.03_{\text{tot}}) \text{ eV} \quad \textit{preliminary}$$

- Agreement with latest results, except KLOE
- Most precise value from CB@MAMI



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η/η' Programme

Precise Results in η/η' Physics:

- Cross sections, especially precise in threshold region
- $\eta \rightarrow 3\pi^0$ (Dalitz plot parameter α), $\eta \rightarrow e^+e^-\gamma$ (TFF), $\eta \rightarrow \pi^0\gamma\gamma$ (χ PT, VMD)
- First glances at $\eta' \rightarrow \eta\pi^0\pi^0$, $\eta' \rightarrow e^+e^-\gamma$

Next η' Production:

- Summer/fall 2014
- Measure with **x4 DAQ speed** and longer period
- Goal: 400,000 $\eta' \rightarrow \eta\pi^0\pi^0$ (Dalitz plot analysis)
~800 $\eta' \rightarrow e^+e^-\gamma$ (Transition Form Factor)

Future Goals:

- Improve **Transition Form Factors for η/η'** (single/double Dalitz decays) (and $\omega \rightarrow \pi^0 e^+ e^-$?)
- Improve **Dalitz plot analyses $\eta/\eta' \rightarrow 3\pi^0$, $\eta' \rightarrow \eta\pi^0\pi^0$** (cusp effects?)
- Radiative decays $\eta' \rightarrow \omega\gamma$, $\omega \rightarrow \pi^0/\eta\gamma$
- Long term plan: Charged decays

A. Denig, W. Gradl, A. Neiser, M. Ostrick, P. Ott, S. Prakhov, O. Steffen, M. Unverzagt, S. Wagner, M. Wolfes (University Mainz)

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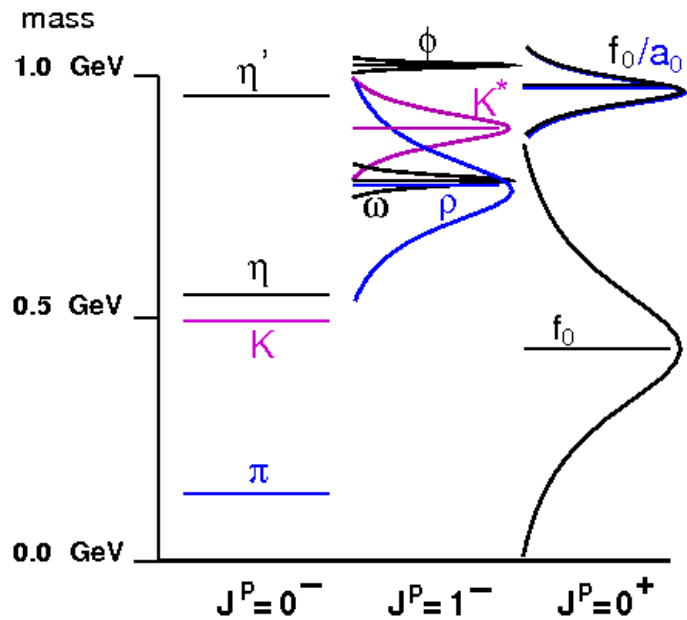


Summary

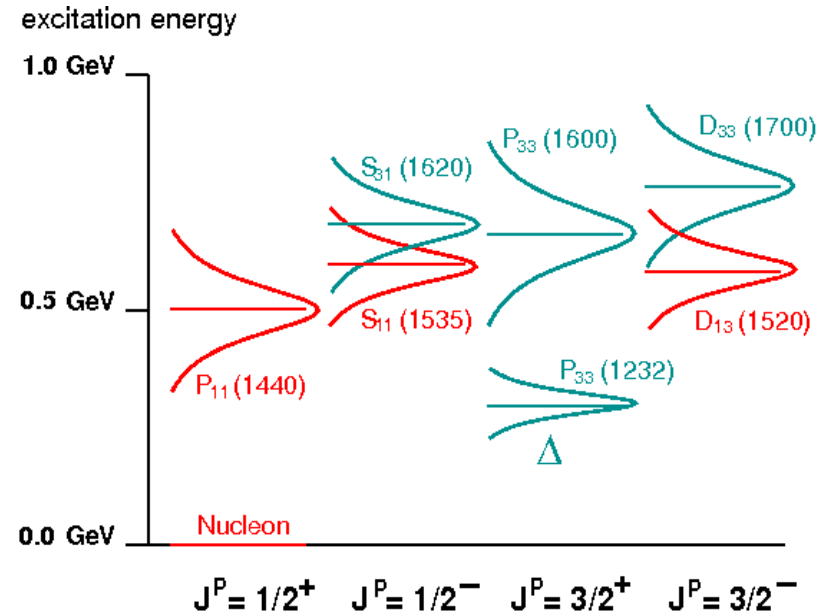
- Most precise η/η' photoproduction cross sections
 - Especially in the threshold regions up to $E_\gamma=1.6$ GeV
- η' production at MAMI possible now
 - Preliminary results on η' photoproduction cross section
 - First glances on $\eta'\rightarrow\eta\pi^0\pi^0$ Dalitz plot and η' Transition Form Factor
- New determination of the Transition Form Factor in $\eta\rightarrow e^+e^-\gamma$
 - More than one order of magnitude more than previous A2 analysis
 - Based on 18,000 events
 - Submitted to Phys. Rev. C
- Very accurate determination of $\eta\rightarrow\pi^0\gamma\gamma$ decay rate
 - Most precise result today
 - To be submitted soon
- 12 years physics programme funded through DFG (SFB 1044)
 - Broad physics programme including
 - Light Meson Dynamics
 - Transition Form Factors of pseudoscalar Mesons

A2 Experiments

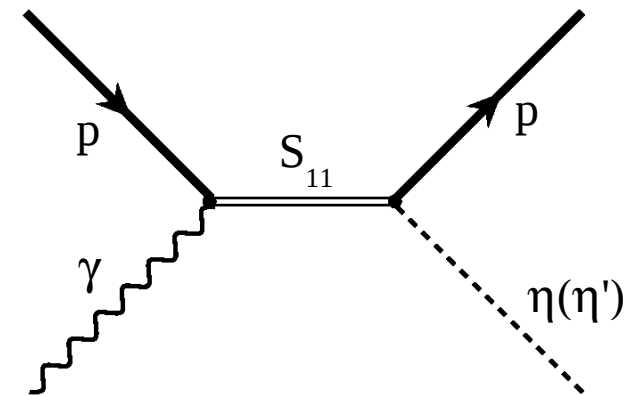
Mesons



Baryons



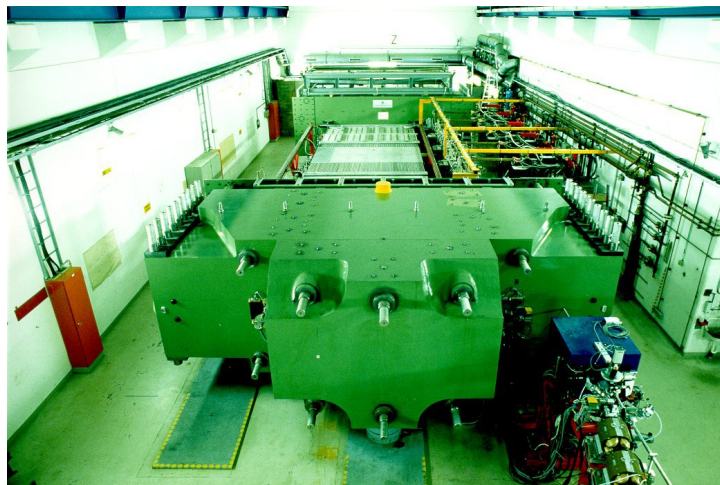
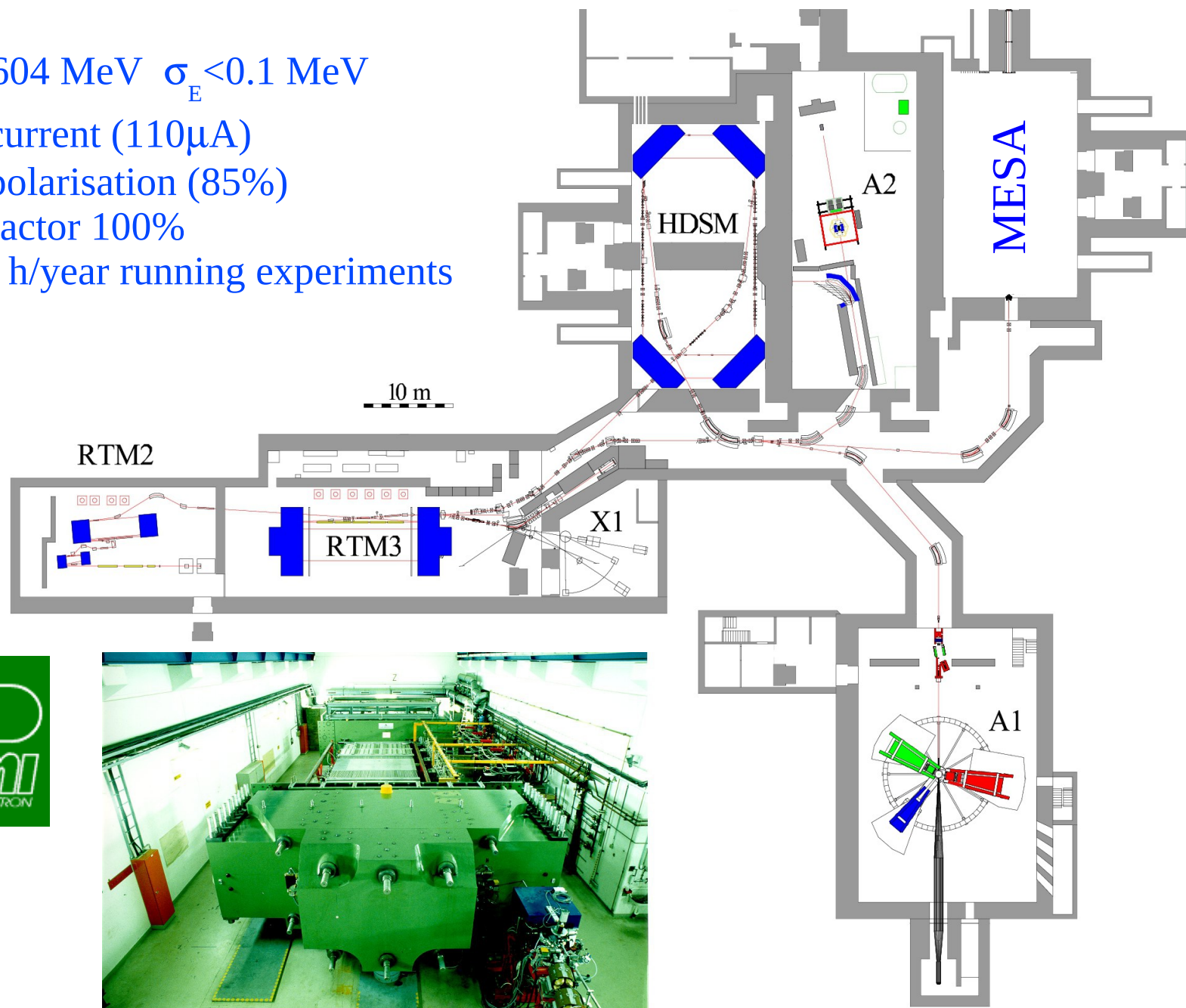
Meson decays with all including physical aspects
Polarisabilities of nucleons and pions
Properties of the first nucleon excitations



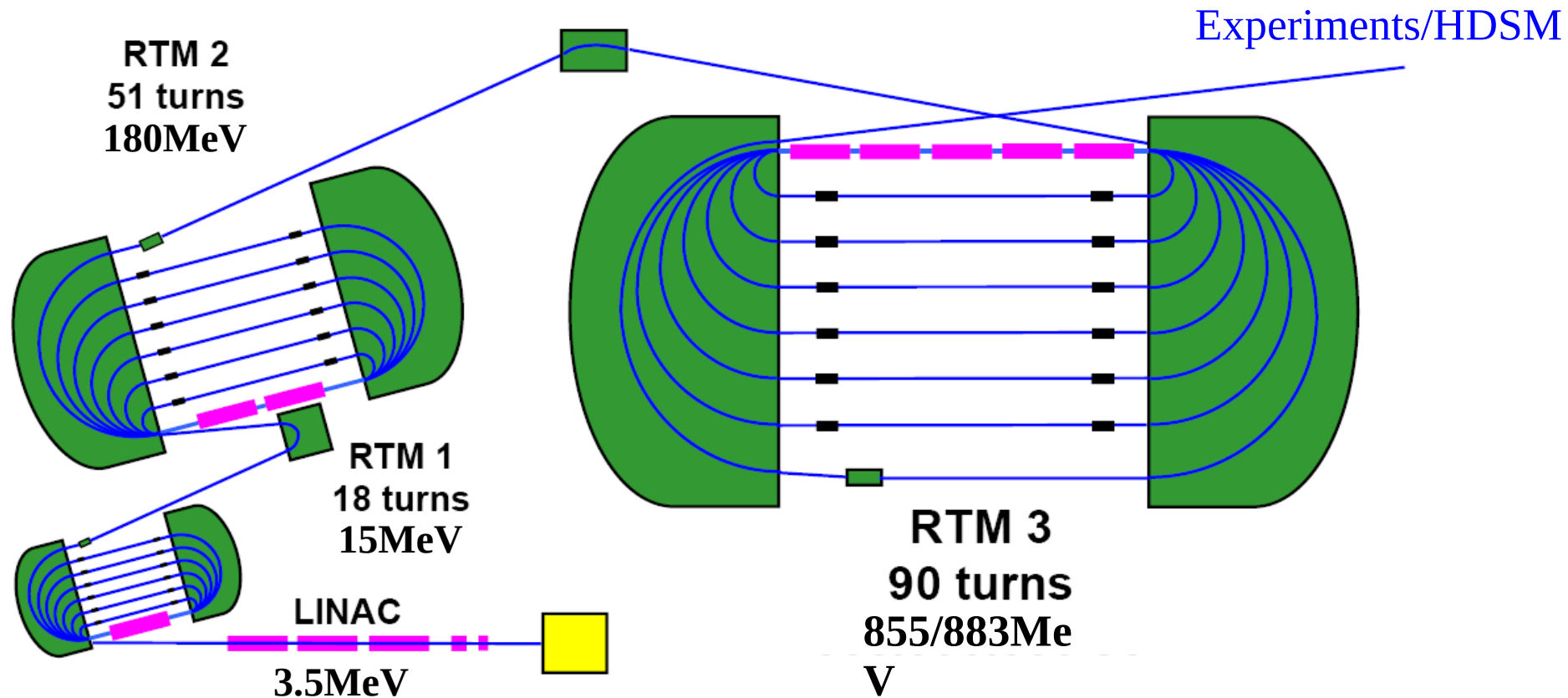
Photoproduction ($E_\gamma \leq 1604$ MeV)

Mainz Microtron

- $E_e < 1604 \text{ MeV}$ $\sigma_E < 0.1 \text{ MeV}$
- High current ($110 \mu\text{A}$)
- High polarisation (85%)
- Duty factor 100%
- $\sim 7000 \text{ h/year}$ running experiments

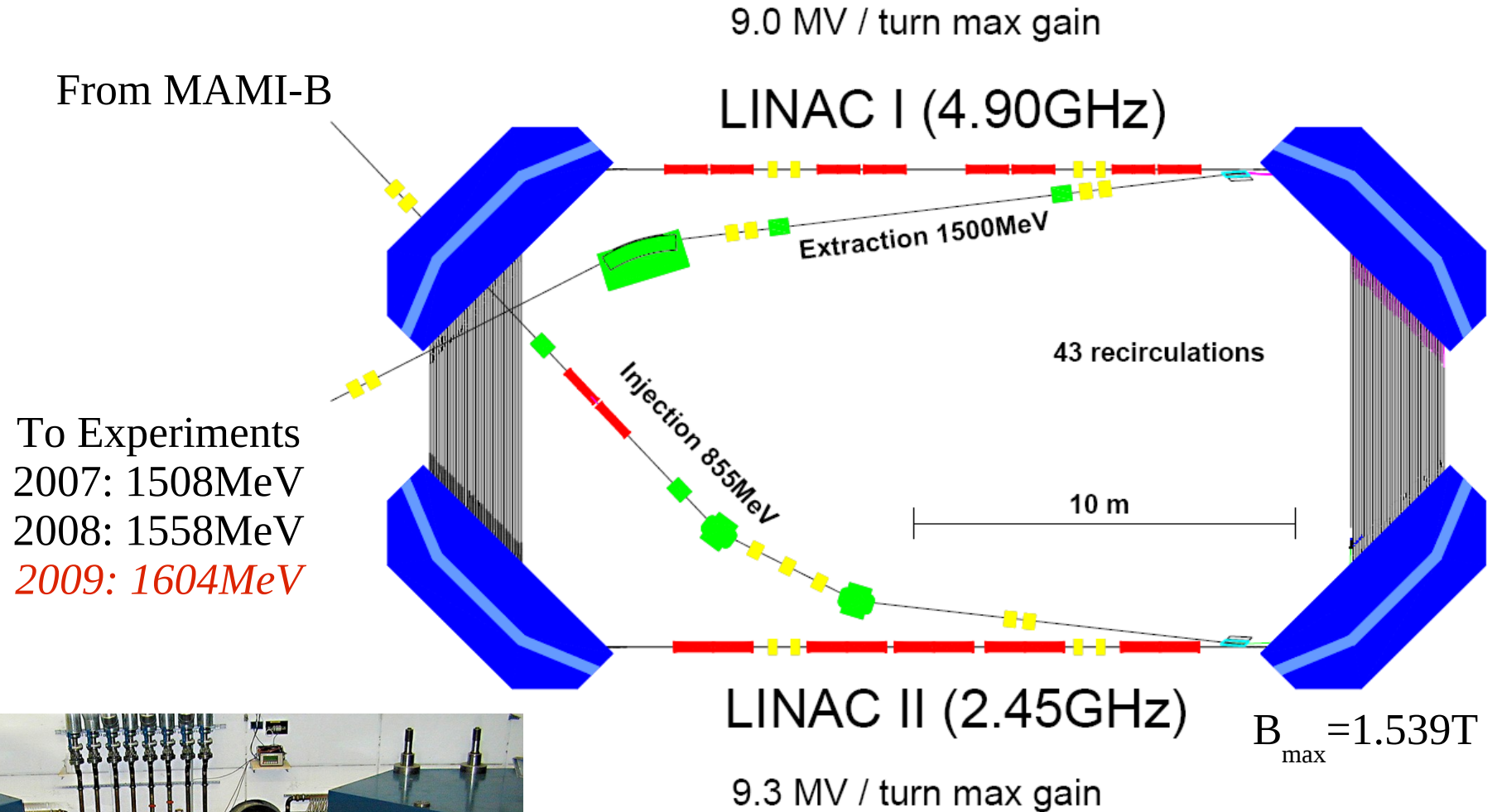


Mainz Microtron (MAMI-B)



Acceleration via em wave (2.45GHz)
cw: bunch structure ~ 0.4 ns
Injektion LINAC
3 cascaded Race-Track-Microtrons
Magnet of RTM 3 ~ 450 t per Magnet, 1.28T

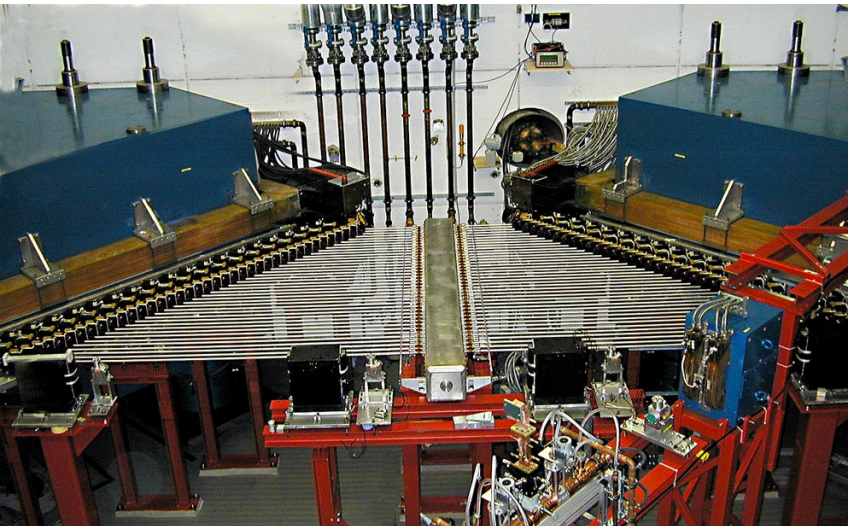
HDSM (MAMI-C)



To Experiments
2007: 1508MeV
2008: 1558MeV
2009: 1604MeV

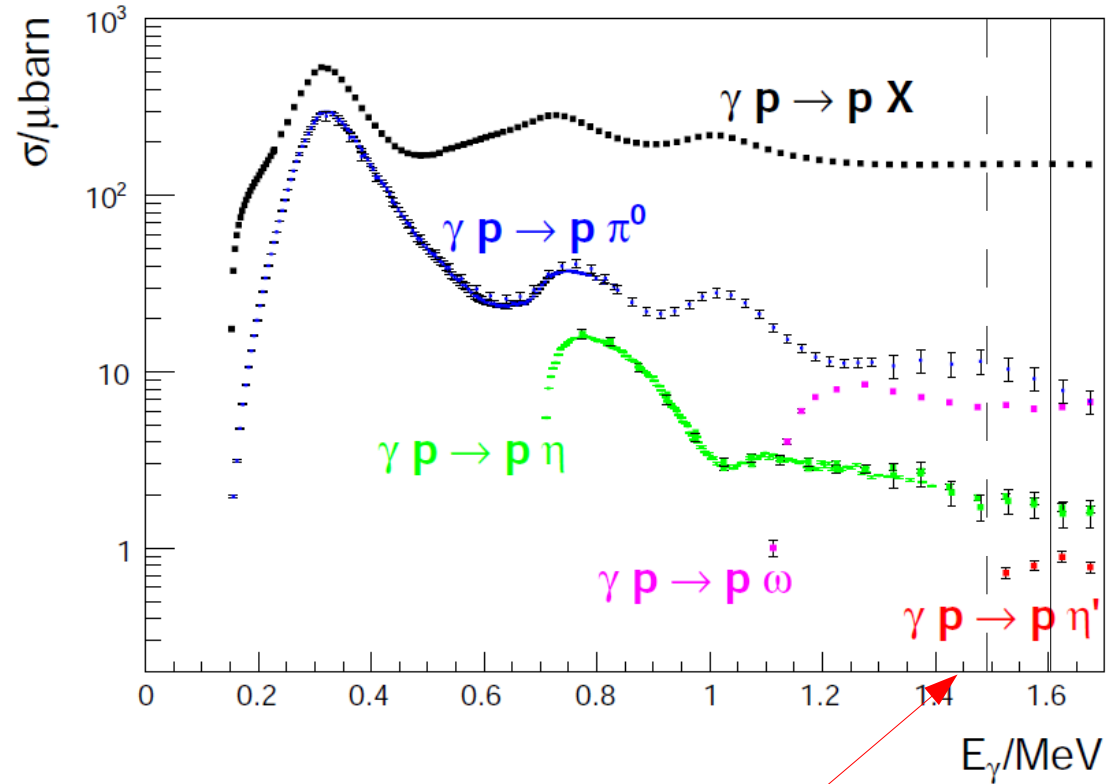
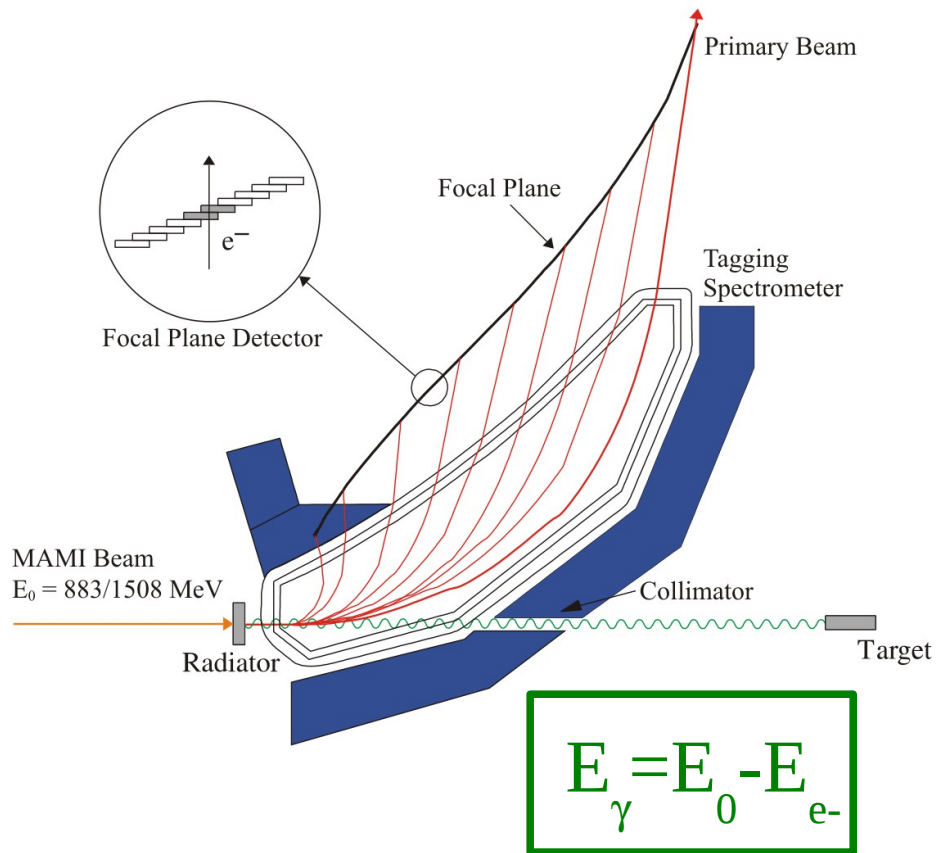
Harmonic Doubled Sided Microtron (HDSM)

K.-H. Kaiser et al., NIM A 593, 159 (2008).



Real Photons in A2

Data from CB@MAMI, CB@ELSA, CLAS, SAPHIR



$E_{\text{thr}} \approx 1447 \text{ MeV}$

High energy resolution: $\Delta E_\gamma \approx 2 \text{ MeV}$ at $E_{e^-} = 883 \text{ MeV}$

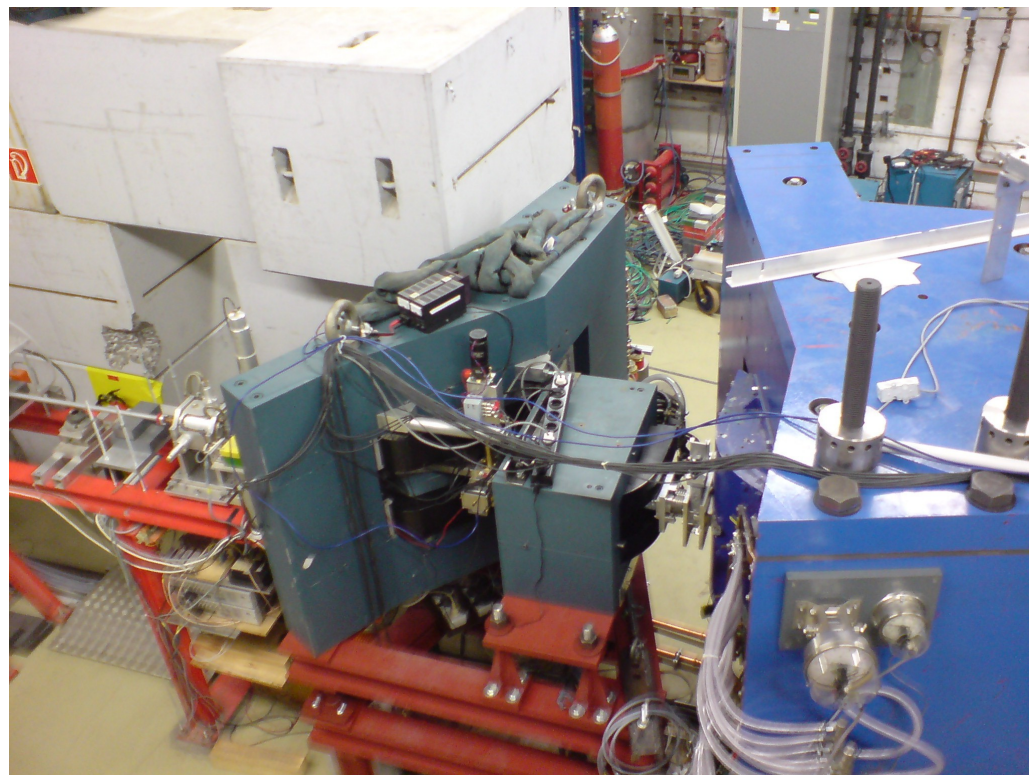
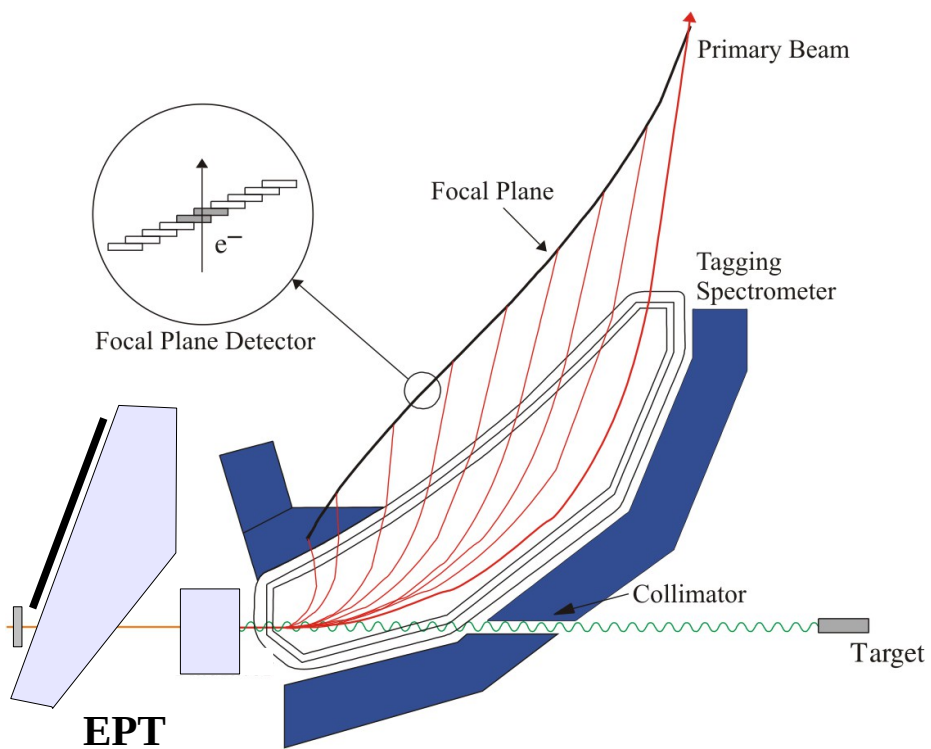
$\Delta E_\gamma \approx 4 \text{ MeV}$ at $E_{e^-} = 1558 \text{ MeV}$

Linearly and circularly polarised photon-beam

Tagging range: 5.1 to 93% of $E_\gamma \rightarrow$ Maximum energy tagged for $E_0 = 1604 \text{ MeV}$ is 1491 MeV

End-Point-Tagger

- Installation of EPT during 2012



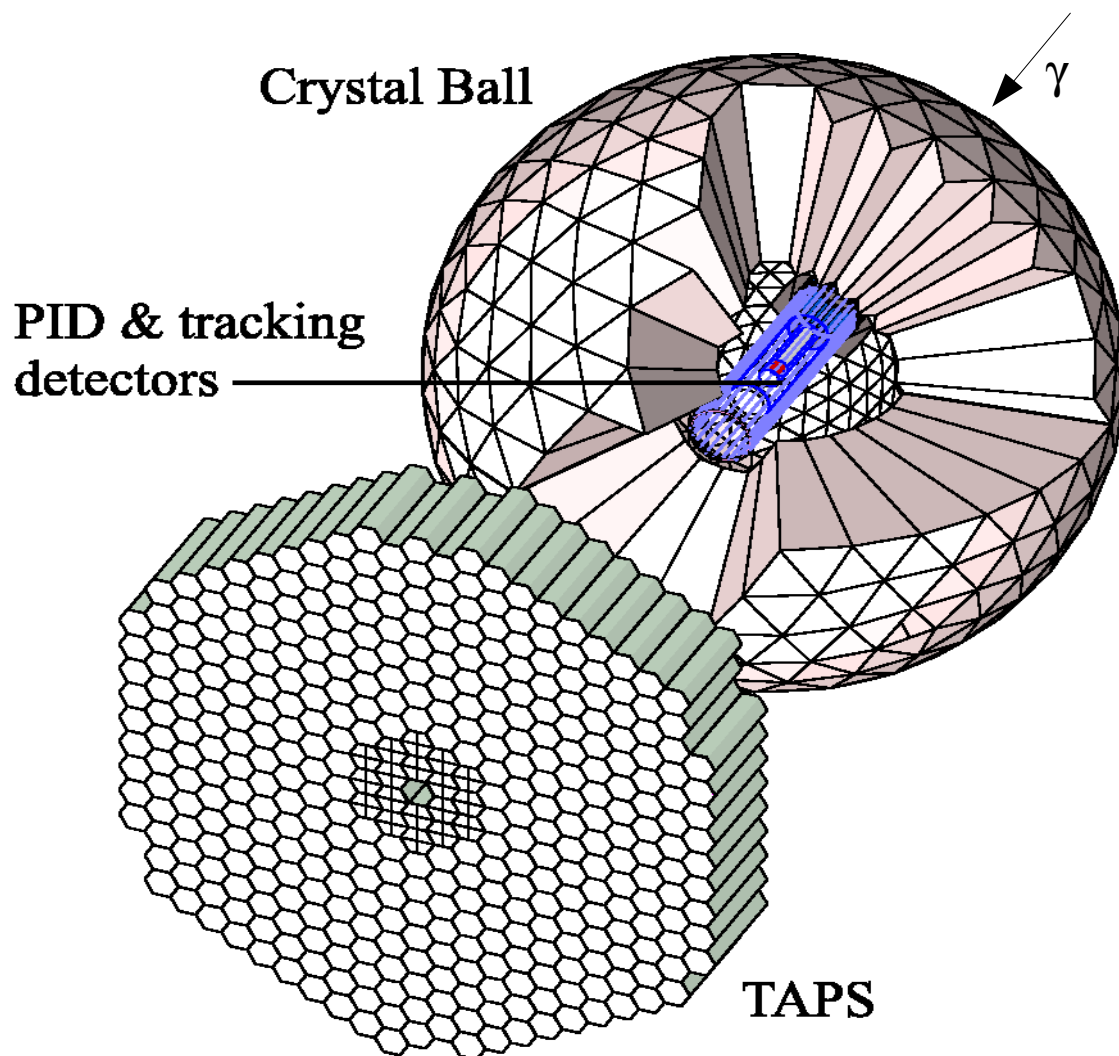
Same working principle as main tagging spectrometer

$E_{\gamma} \approx 1445-1595 \text{ MeV}$

$\Delta E_{\gamma} \approx 2.5 \text{ MeV}$

Non-permanent installation in front of main Tagger

4 π -Setup



Crystal Ball:

672 NaI(Tl) crystals

93,3% of total solid angle

Each crystal equipped with PMT

$$\frac{\sigma}{E_\gamma} = \frac{2\%}{(E_\gamma/\text{GeV})^{0.25}}$$

$$\Delta t = 2.5 \text{ ns FWHM}$$

$$\sigma(\theta) = 2^\circ \dots 3^\circ$$
$$\sigma(\phi) = \frac{2^\circ \dots 3^\circ}{\sin(\theta)}$$

TAPS:

Up to 510 BaF₂ crystals

Polar acceptance: 4-20°

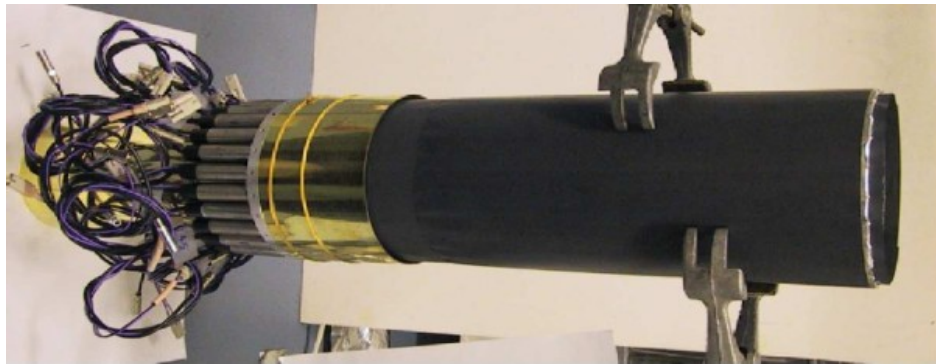
$$\Delta t = 0.5 \text{ ns FWHM}$$

$$\frac{\sigma}{E_\gamma} = \frac{0,79\%}{\sqrt{E_\gamma/\text{GeV}}} + 1,8\%$$

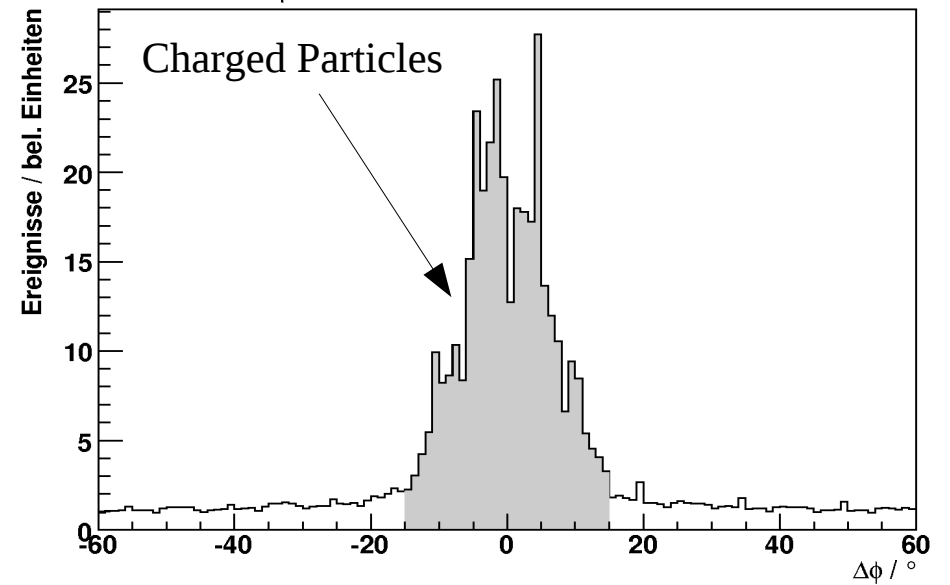
CB PID

Particle Identification Detector (PID):

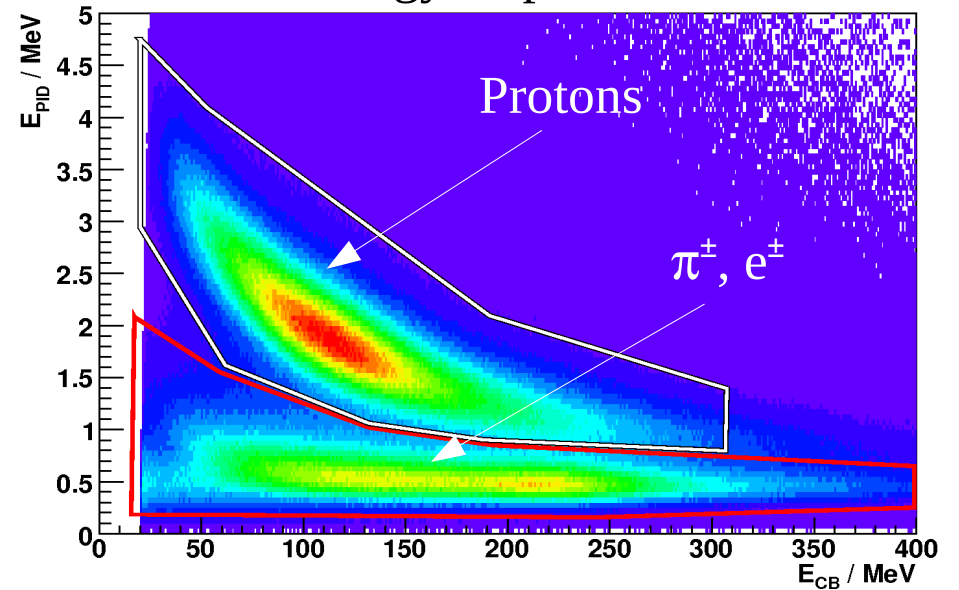
- Cylindrical Detector inside CB
- 24 scintillator strips
- PMT readout



$\Delta\phi$ - between CB and PID

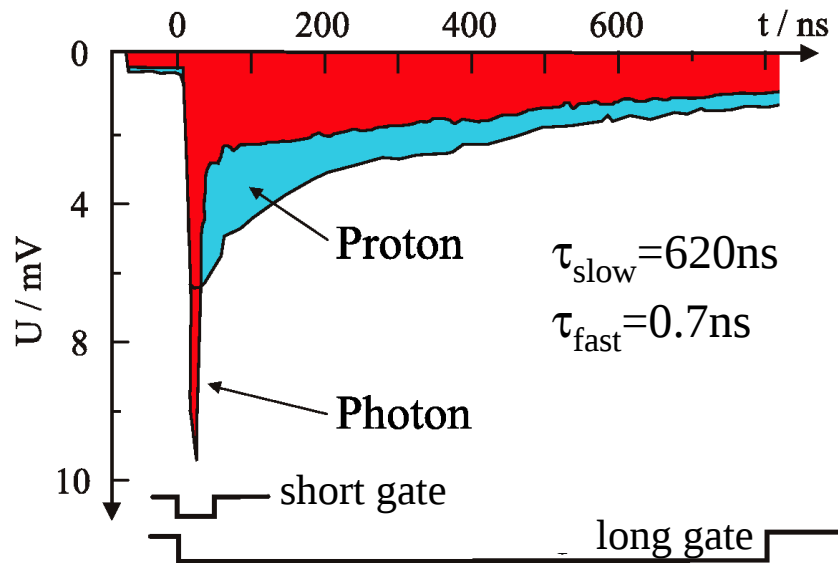
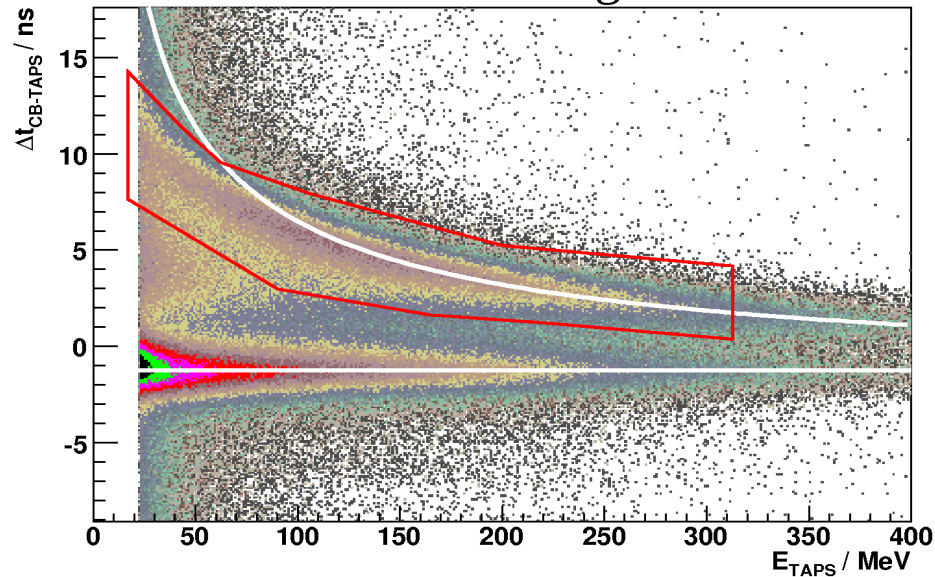


Energy Dependence



TAPS PI

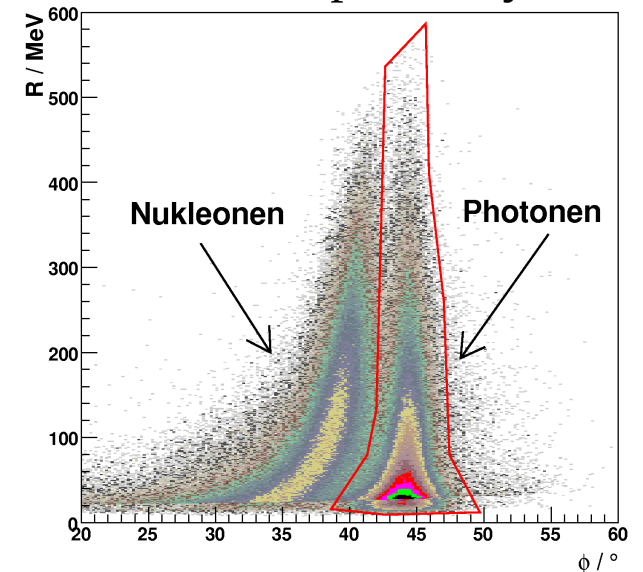
Time-of-Flight



$$R = \sqrt{E_{\text{short}}^2 + E_{\text{long}}^2}$$

$$\phi = \arctan\left(\frac{E_{\text{short}}}{E_{\text{long}}}\right)$$

Pulse-Shape-Analysis

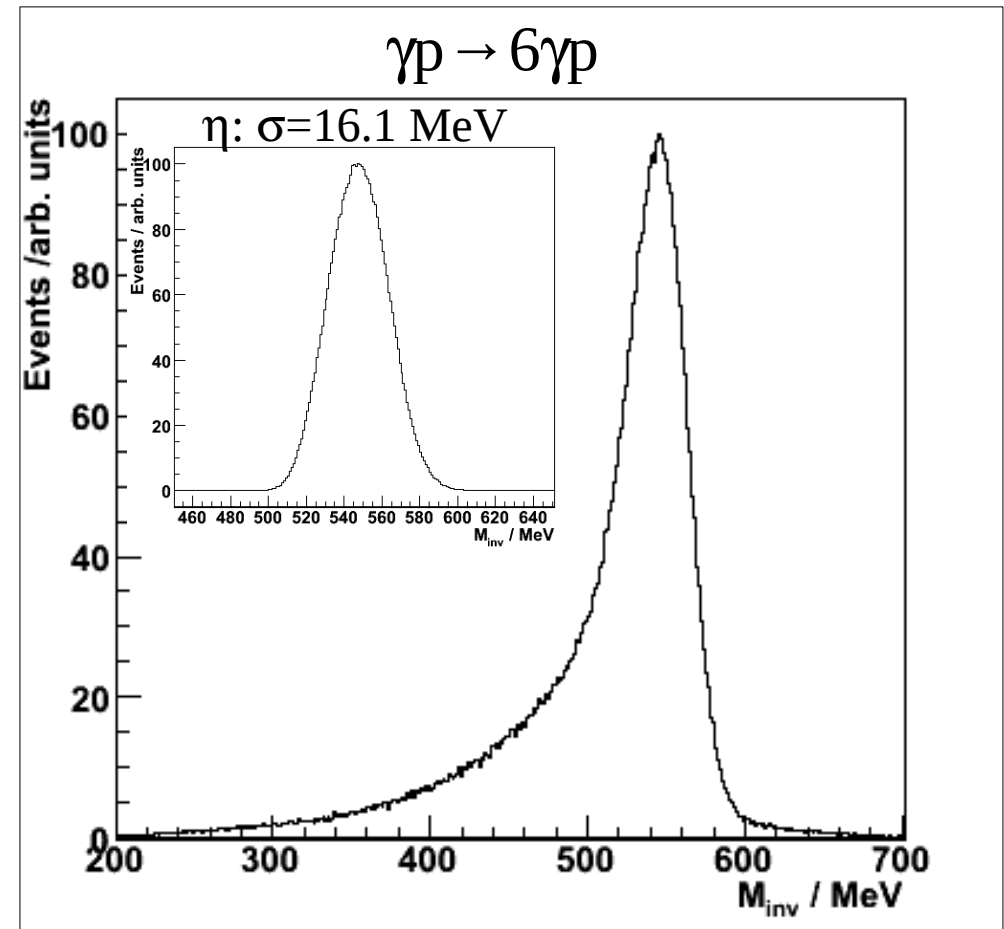
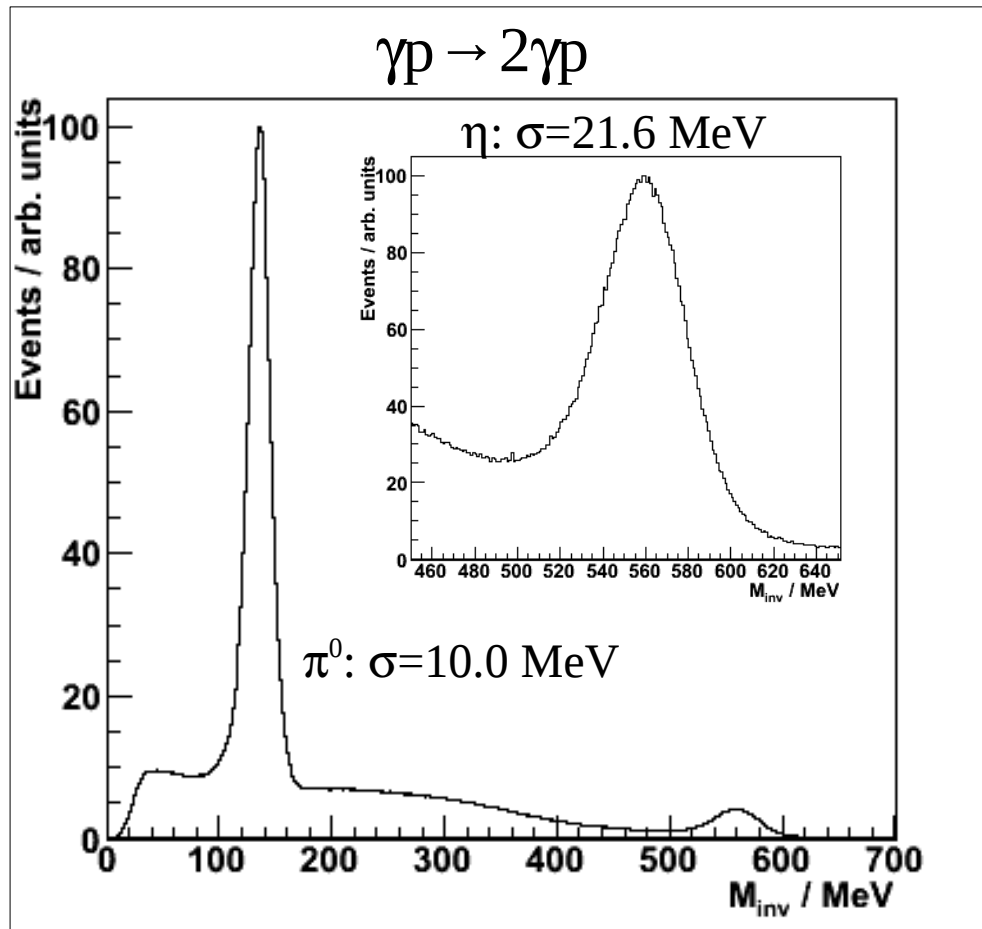


Setup Performance

Two main η decay modes:

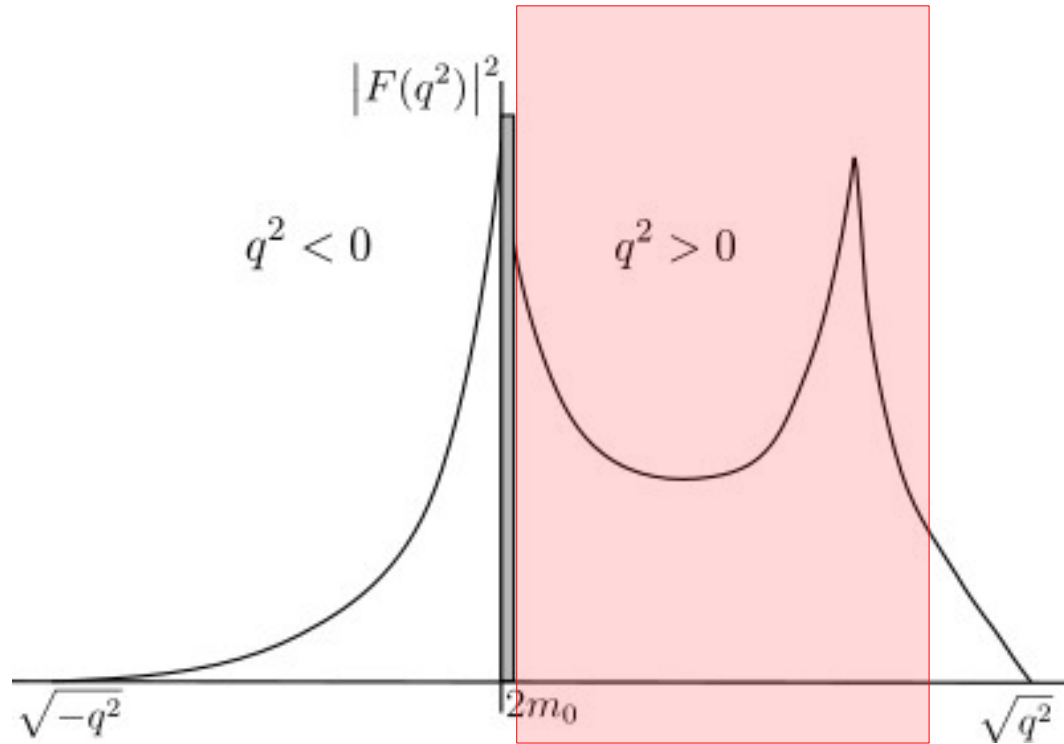
$$\text{BR}(\eta \rightarrow 2\gamma) = 39.38\%$$

$$\text{BR}(\eta \rightarrow 3\pi^0) = 32.51\%$$



$3 \cdot 10^6 \eta \rightarrow 3\pi^0$ analysed from ~ 6 weeks $\rightarrow 30M \eta$ produced

Measurement of TFFs

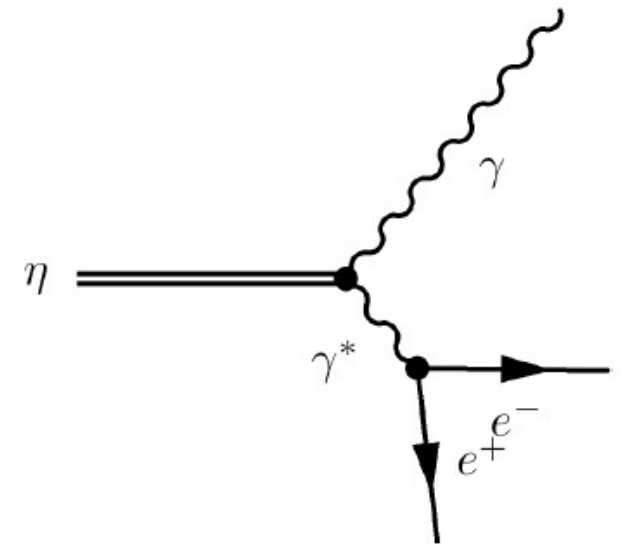


$q^2 = (\Delta E/c)^2 - \Delta p^2$
 momentum transfer carried
 by virtual photon

Time-like momentum transfer (meson decays):

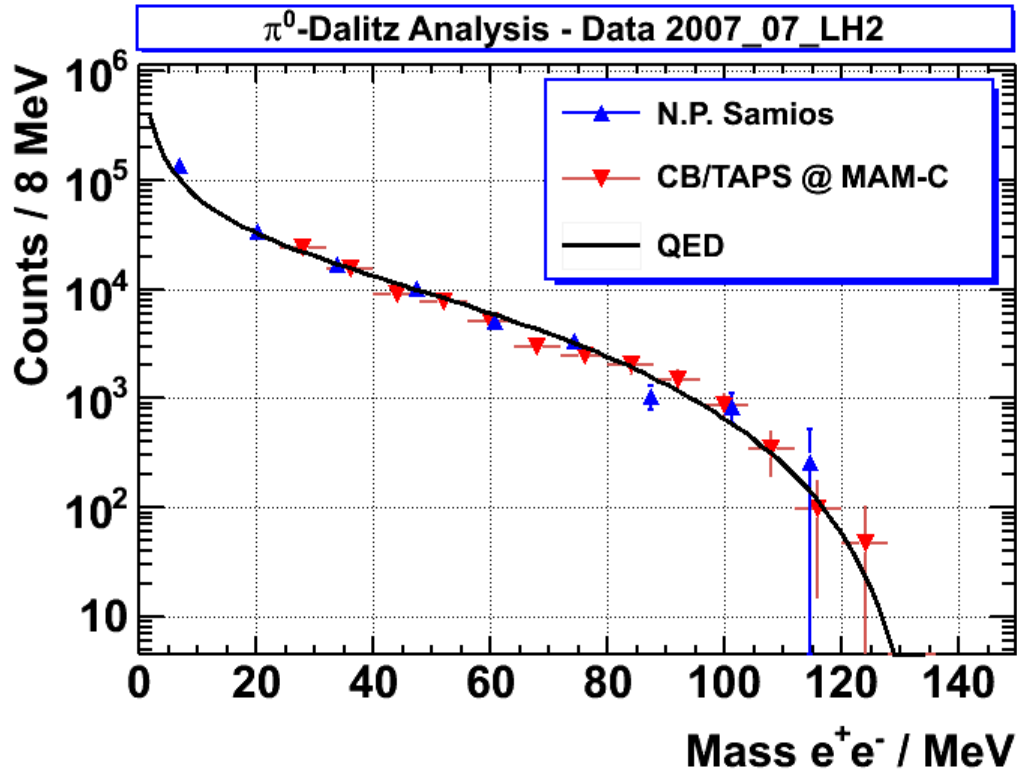
- $(2m_0)^2 < q^2 < M^2$
- CB, WASA, KLOE, Crystal Barrel, ...

$$\frac{d\Gamma(P \rightarrow e^+e^-\gamma)}{dm \Gamma(P \rightarrow \gamma\gamma)} = \frac{4\alpha}{3\pi m} \sqrt{1 - \frac{4m_e^2}{m^2}} \left(1 + \frac{2m_e^2}{m^2}\right) \left[1 - \frac{m^2}{m_p^2}\right]^3 |F(q^2)|^2$$



Time-like TFF in $\pi^0 \rightarrow e^+e^-\gamma$

H. Berghäuser, PhD thesis, University Gießen, 2010.
A2-Collaboration



N.P. Samios et al. (BNL), Phys. Rev. 121 (1961) 275-281.

- Expected behaviour:

$$F(m^2) = \frac{1}{1 - \frac{m^2}{\Lambda^2}} \quad m_\pi \ll \Lambda \quad \Rightarrow \quad F(m^2) \approx 1$$