



# **BABAYAGA@NLO vs. BHWIDE**

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**Sighad07  
LNF Frascati  
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# Luminosity needs

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**Two main motivations for a precision measurement of the integrated luminosity with a precision  $<1\%$**

- 1)  $\sigma_{\text{hadr}}$  with so far typical precisions  $>5\%$ ;  
cross check normalization to rad. muon pairs with the normalization to luminosity x radiator function
- 2) high-precision  $\tau$ -analyses  
which need as a normalization the  $\tau^+\tau^-$  cross section AND the integrated luminosity



# Luminosity needs

## Normalitization:

### 1) Integr. Luminosity $L_{int}$ x Radiator Function $H$

↳ Large angle Bhabhas

↳ LO-Theory  
(analytic formula)

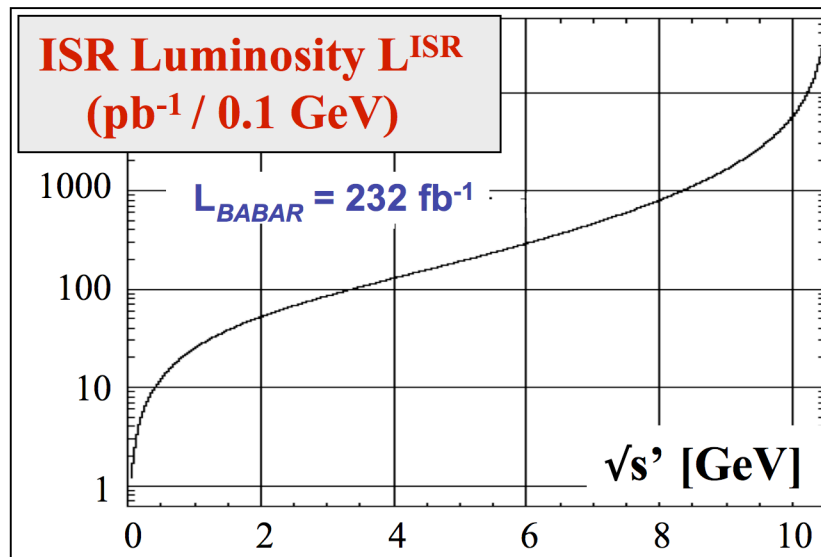
OR

### 2) Use $e^+e^- \rightarrow \mu^+\mu^-\gamma$ events

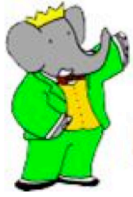
$$dL^{ISR}(M) = \frac{dN_{\mu\mu\gamma}(M)}{\epsilon_{\mu\mu\gamma}(M)(1 + \delta_{FSR}(M))\sigma_{\mu\mu}^{Bom}(M)} = L_{int} x dH$$

Up to ca. 3% difference  
btw. 1) and 2)

Reasons?!



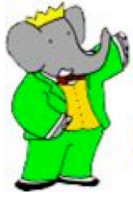
- Luminosity measurement using Large-Angle-Bhabha ca. 1% precision
- Radiator function @ Born level only
- Muon efficiency determination highly non-trivial, up to now precision ca. 2-3% (high-precision determination underway)

**BABAR**

# Luminosity measurement

$e^+e^- \rightarrow$	exp. error	theo. error	total error	event-generator
$e^+e^- (\gamma)$	0.7%	0.7%	1.0%	<b>BHWIDE</b> (S.Jadach, W.Placzek and B.F.L. Ward, Phys.Lett.B390 (1997) 298)
$\mu^+\mu^- (\gamma)$	0.5%	1.4%	1.5%	<b>BKQED</b> (F.Berends and R. Kleiss, Nucl.Phys.B228 (1983) 537)
$\gamma\gamma$	1.6%	2.0%	2.6%	





**BABAR**

# Luminosity measurement

---

## Selection cuts on Bhabha sample:

- two tracks with net charge zero
- $\cos(\theta_{1,\text{CMS}}) < 0.7$  &  $\cos(\theta_{2,\text{CMS}}) < 0.65$
- $P_{1,\text{CMS}}/E_{\text{Beam}} > 0.75$  &  $P_{2,\text{CMS}}/E_{\text{Beam}} > 0.50$
- $|\text{3-d acollinearity} - 180^\circ| < 30^\circ$
- EMC,  $E_1/P_1 > 0.7$  and ( $E_2/P_2 > 0.4$  OR  $E_2/P_2 = 0$ )



**BABAR**

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Luminosity determination with a  
precision of 0.94%

(Ref.: BaBar Analysis Document #229)



# New event generator Babayaga@NLO

Bhabha-Scattering:  
 $e^+e^- \rightarrow e^+e^- (\gamma)$

Theoretical  
precision

- BHWIDE (leading log)  $\sim 0.5\%$
- Babayaga@NLO (parton shower)  $\sim 0.1\%$
- Babayaga (version 3.5)  $\sim 0.5\%$

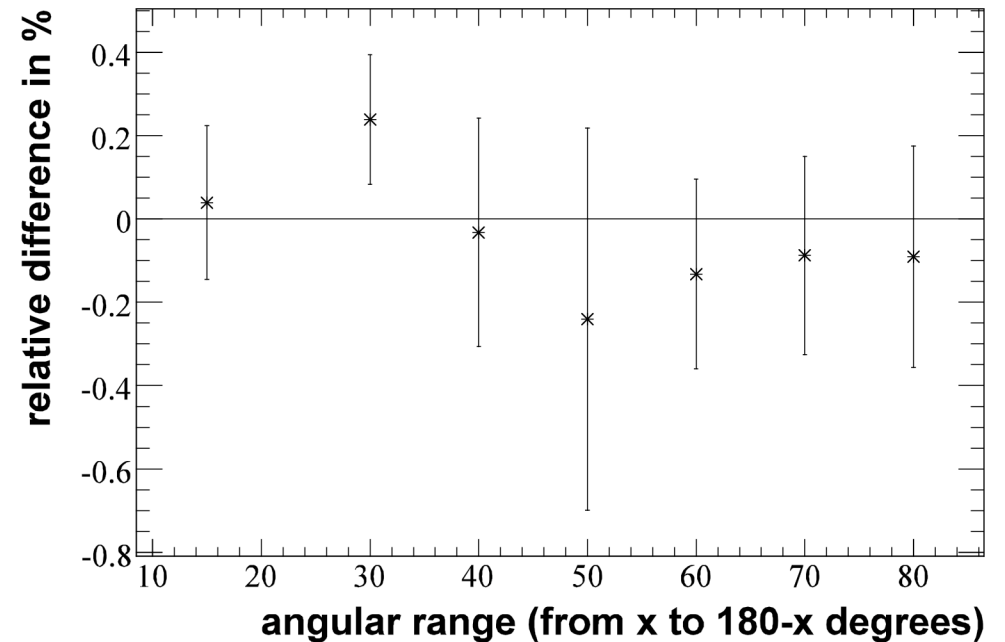
Authors of Babayaga@NLO: G. Balossini, C.M. Carloni Calame,  
G.Montagna, O.Nicrosini, F.Piccinini ([hep-ph/0607181])



# Total $\sigma_{\text{eff}}$

$\theta$  = polar angle between incoming and outgoing lepton ( $x < \theta < 180^\circ - x$ )

Angular range of outgoing leptons (CMS)	cross section / [nb]	
	BHWIDE	Babayaga@NLO
15°-165°	124.89±0.08	124.85±0.15
30°-150°	25.568±0.016	25.507±0.024
40°-140°	12.363±0.008	12.367±0.026
50°-130°	6.690±0.005	6.706±0.026
60°-120°	3.784±0.003	3.789±0.006
70°-110°	2.060±0.002	2.062±0.003
80°-100°	0.881±0.001	0.881±0.002

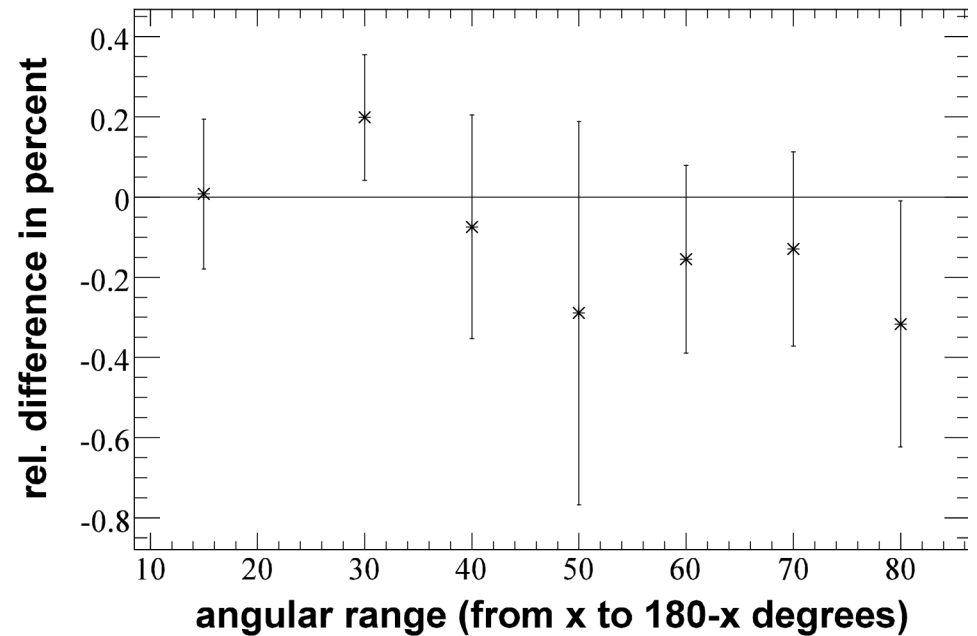




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Angular range of outgoing leptons (CMS)	cross section / [nb]	
	BHWIDE	Babayaga@NLO
15°-165°	119.53±0.08	119.5±0.1
30°-150°	24.22±0.016	24.17±0.02
40°-140°	11.660±0.008	11.67±0.03
50°-130°	6.289±0.004	6.31±0.03
60°-120°	3.549±0.003	3.554±0.006
70°-110°	1.928±0.002	1.931±0.003
80°-100°	0.822±0.001	0.824±0.002

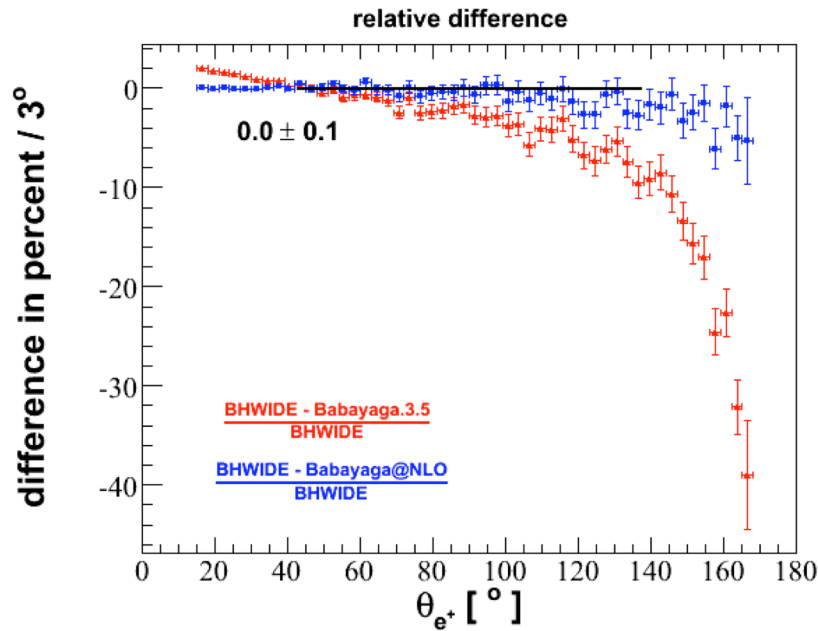
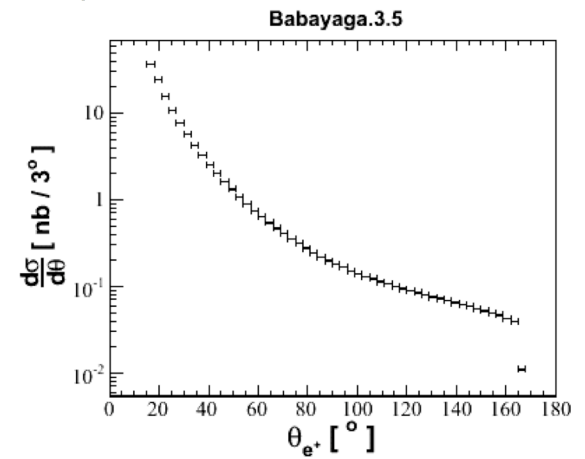
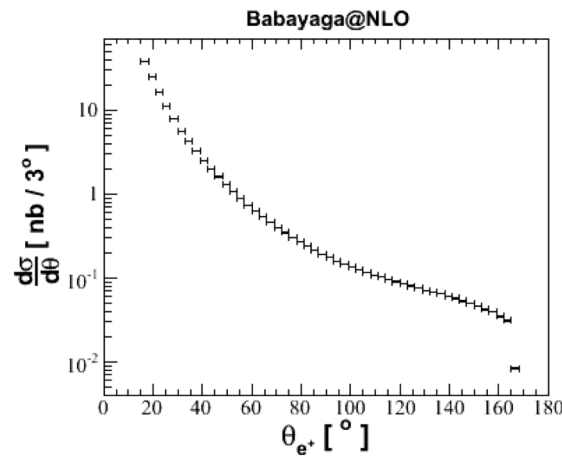
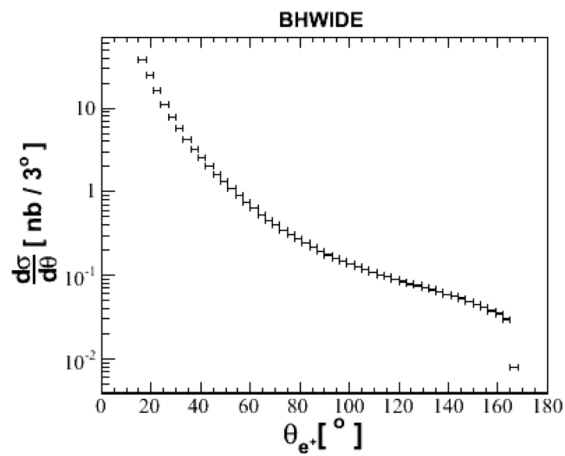


**without vacuum polarization**



# $\sigma_{\text{eff}}$ as a function of $\theta_{e^-}$

$$15^\circ < \theta_{\text{lep}} < 165^\circ$$

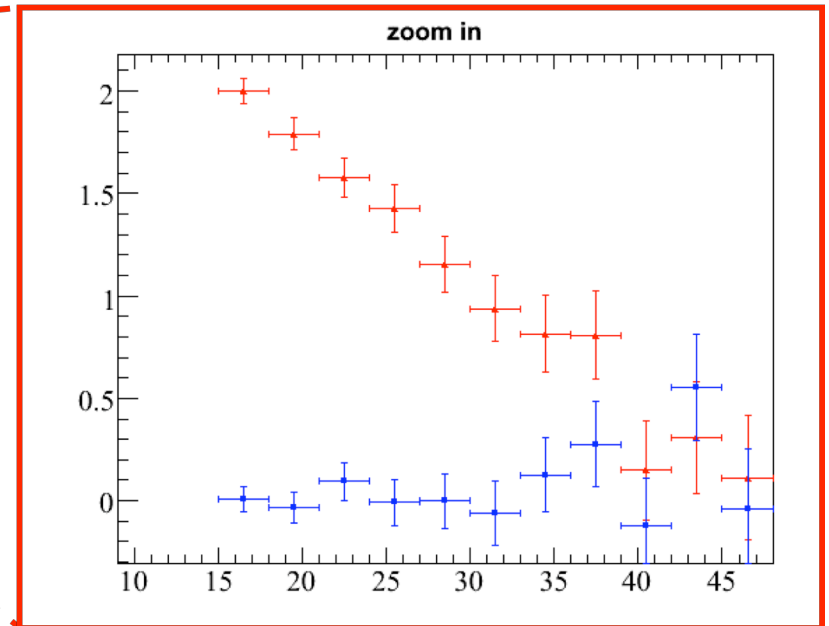
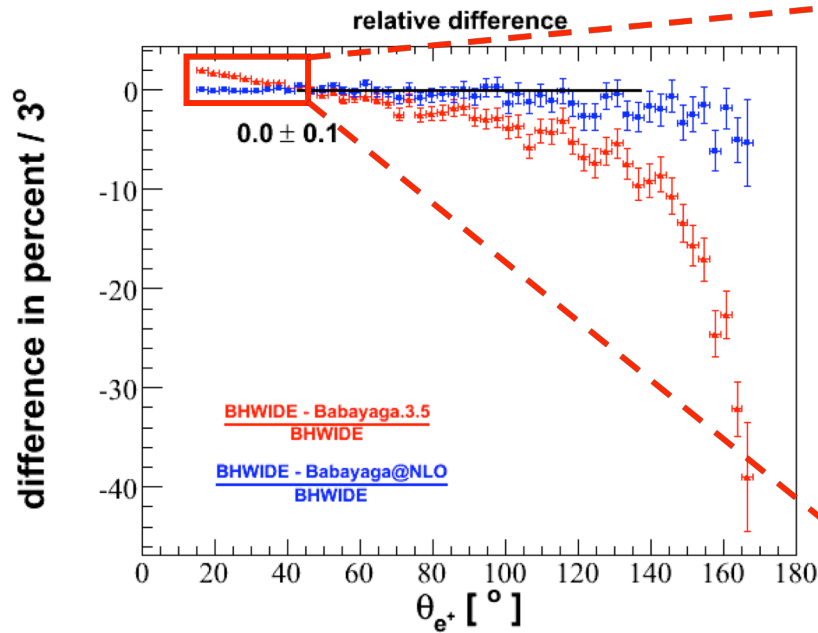
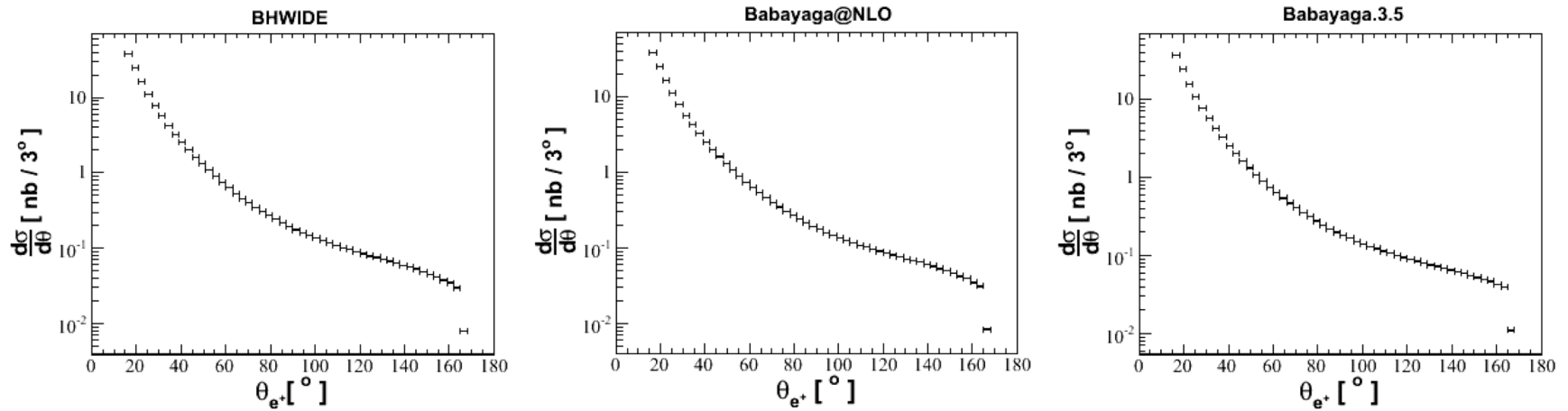




# BABAR

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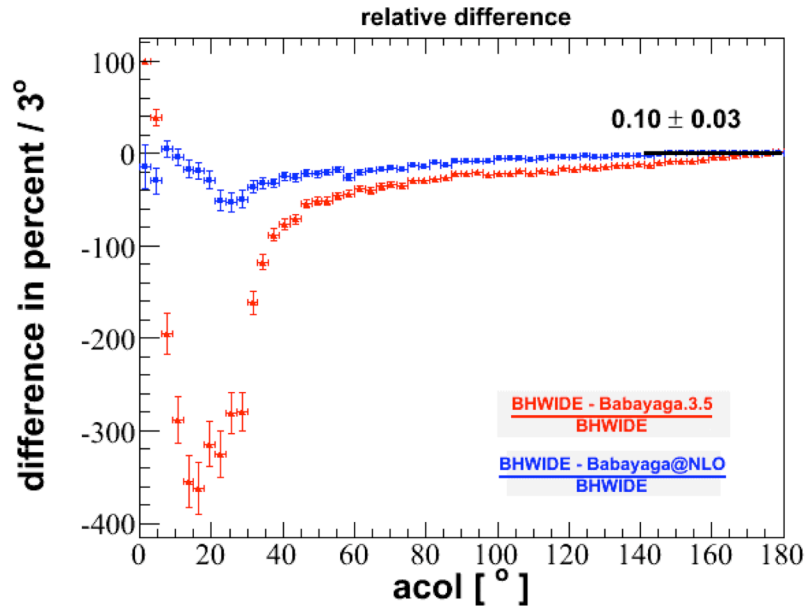
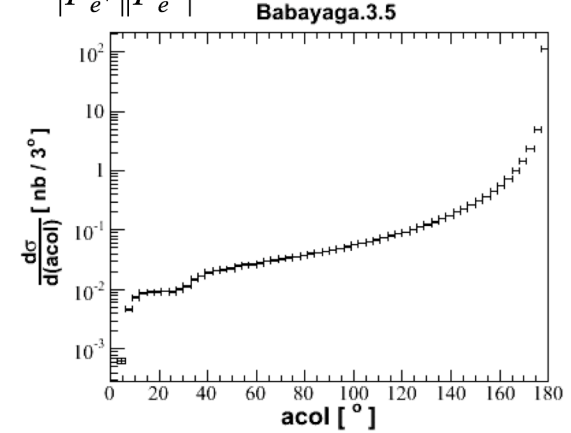
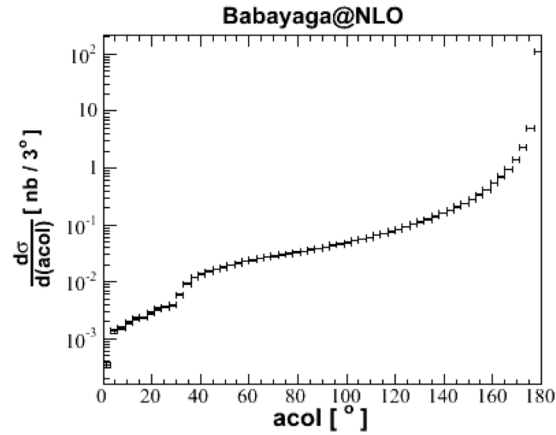
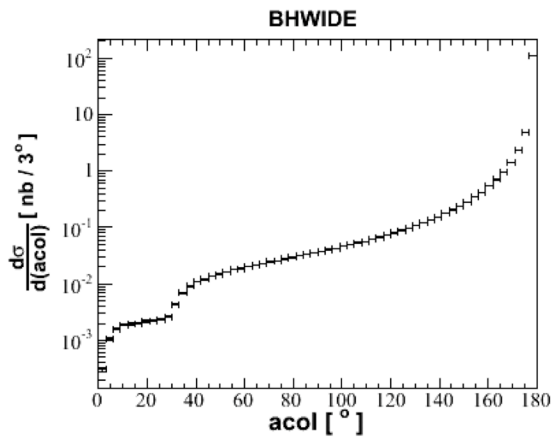
$$15^\circ < \theta_{\text{lep}} < 165^\circ$$





# $\sigma_{\text{eff}}$ as a function of $acol$

$$acol = a \cos\left(\frac{\vec{p}_{e^+} \cdot \vec{p}_{e^-}}{|\vec{p}_{e^+}| |\vec{p}_{e^-}|}\right)$$

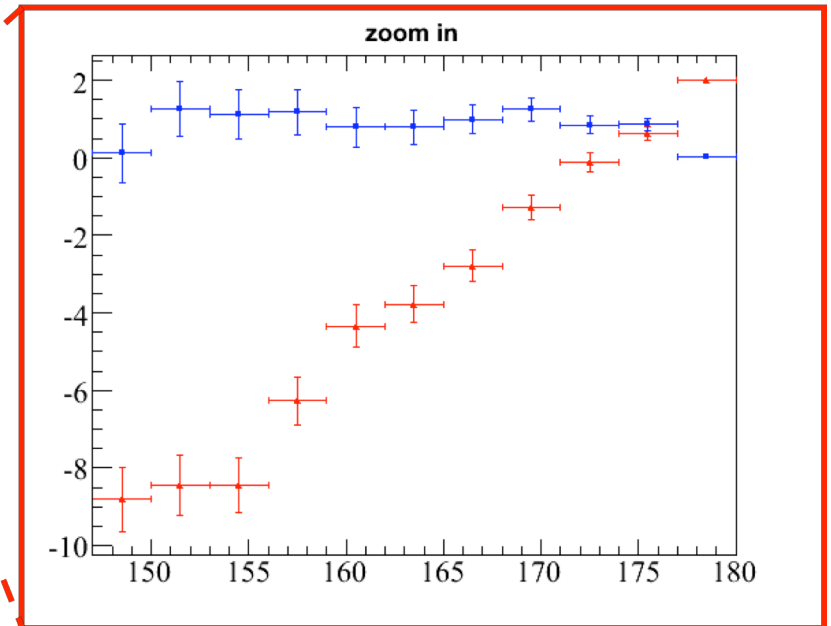
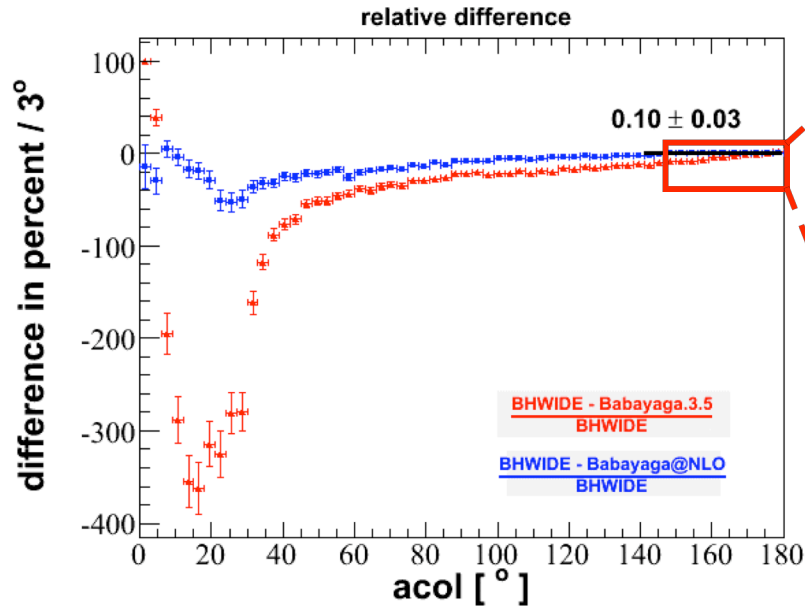
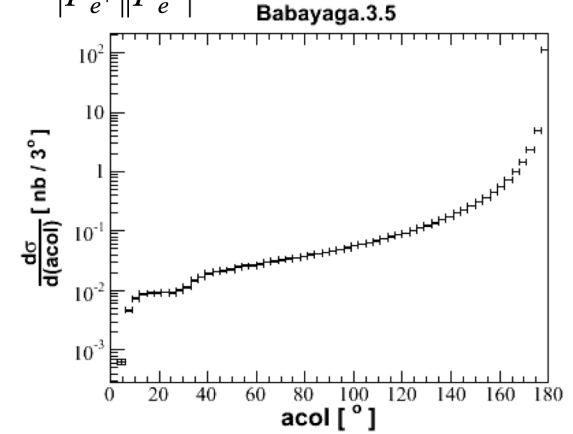
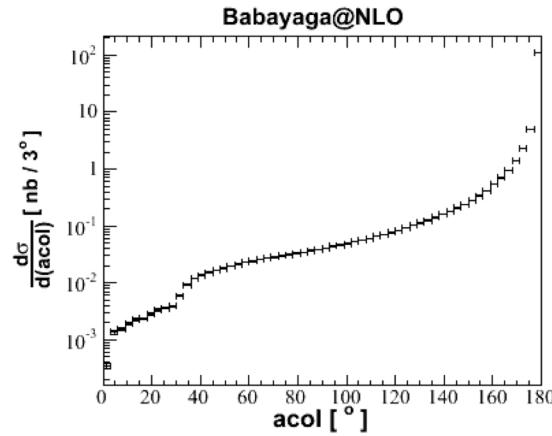
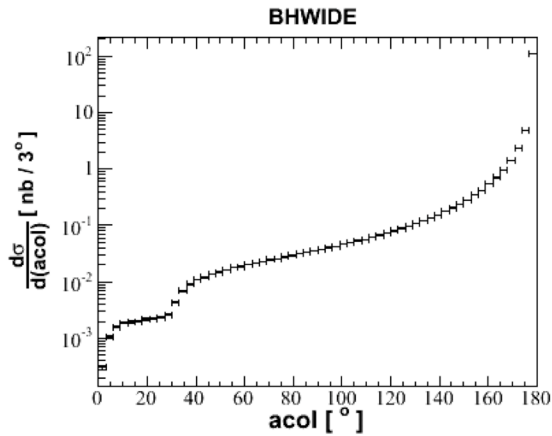






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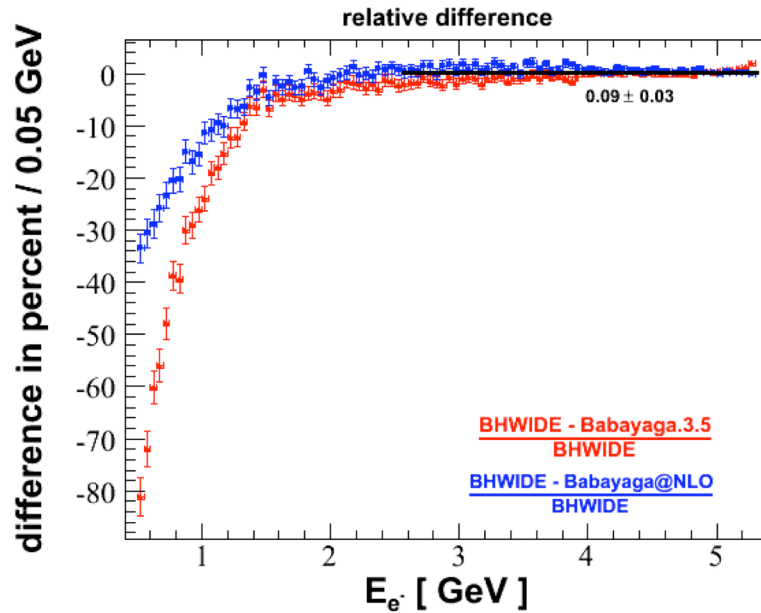
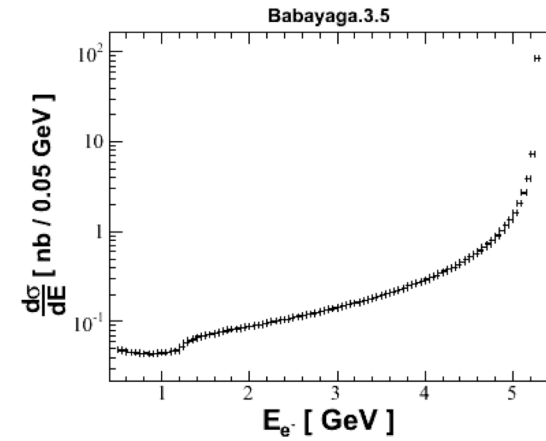
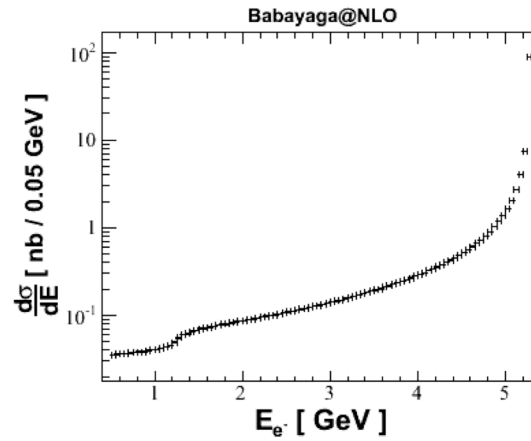
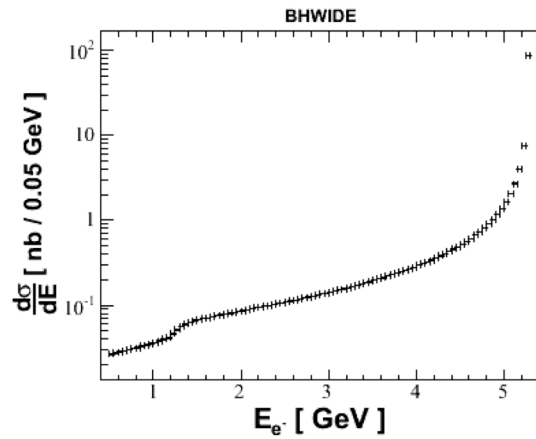
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# $\sigma_{\text{eff}}$ as a function of $E_{e^-}$

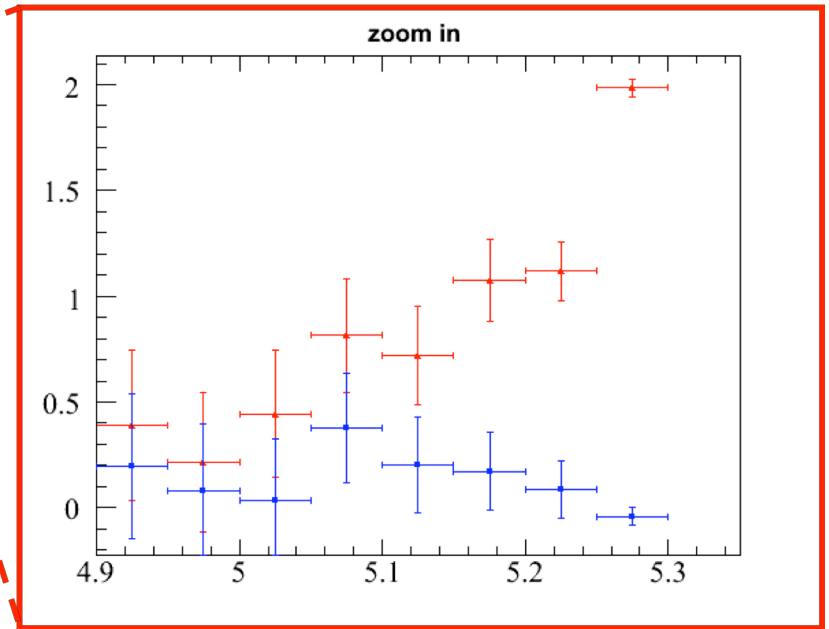
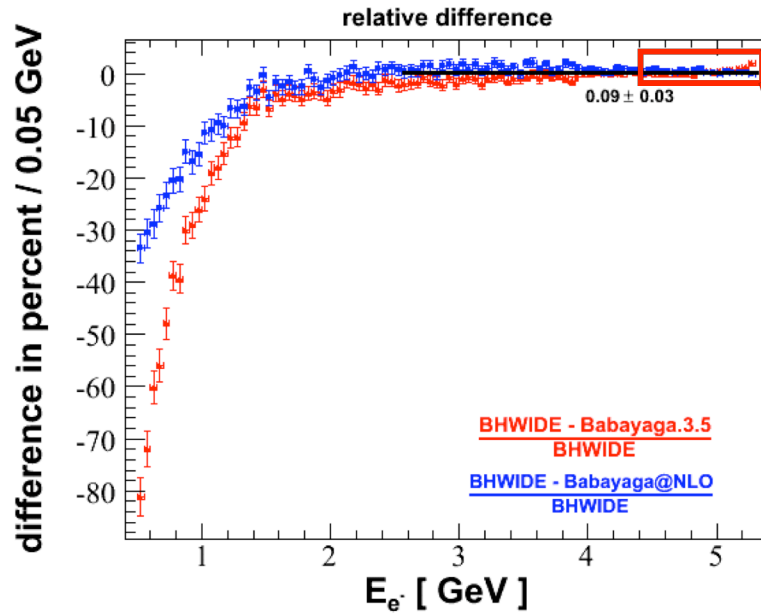
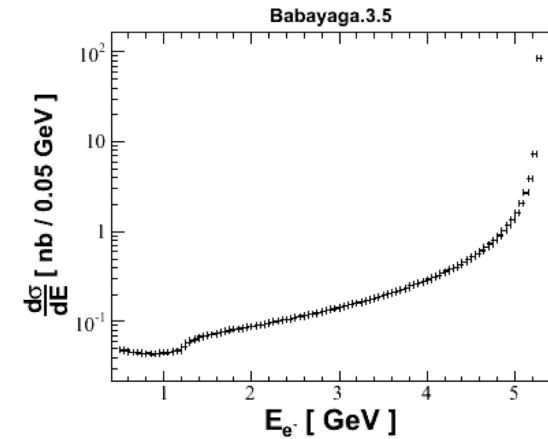
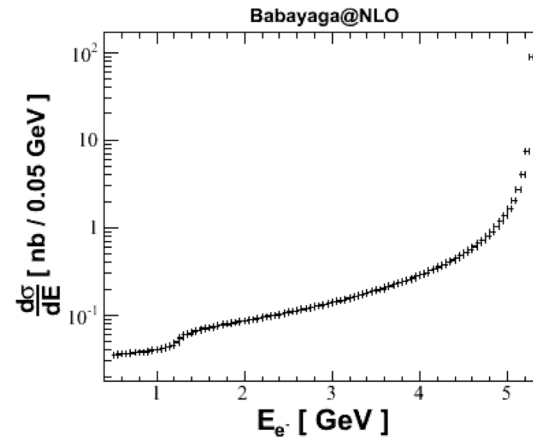
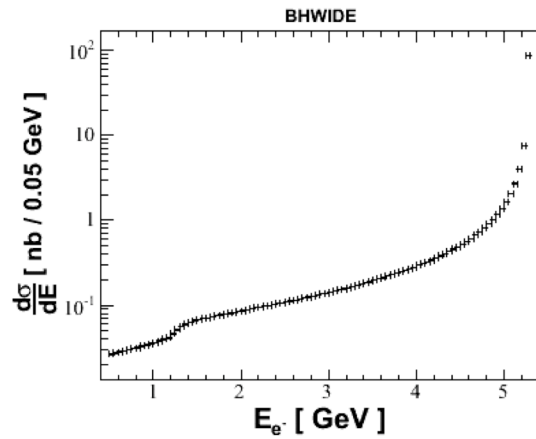
$$E_{e^-, \text{min}} = 0.5 \text{ GeV}$$





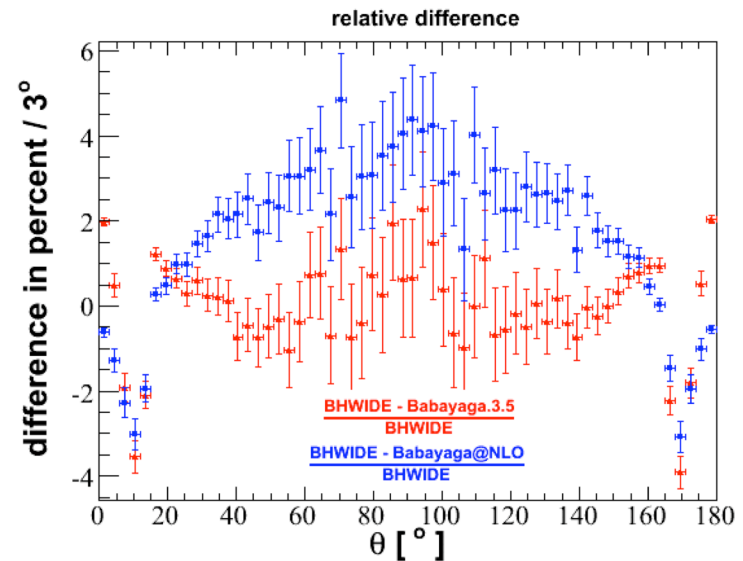
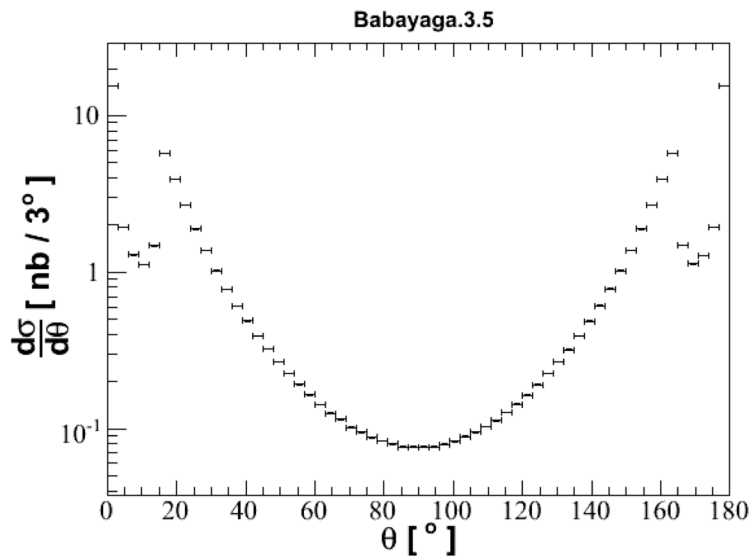
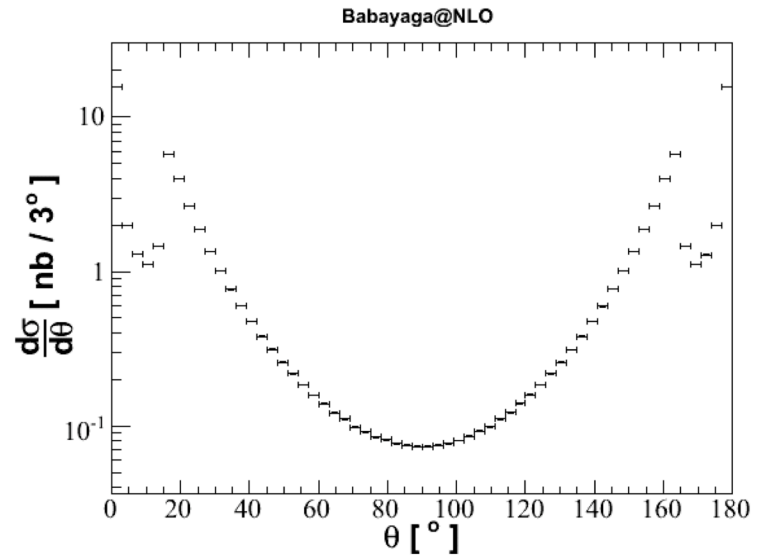
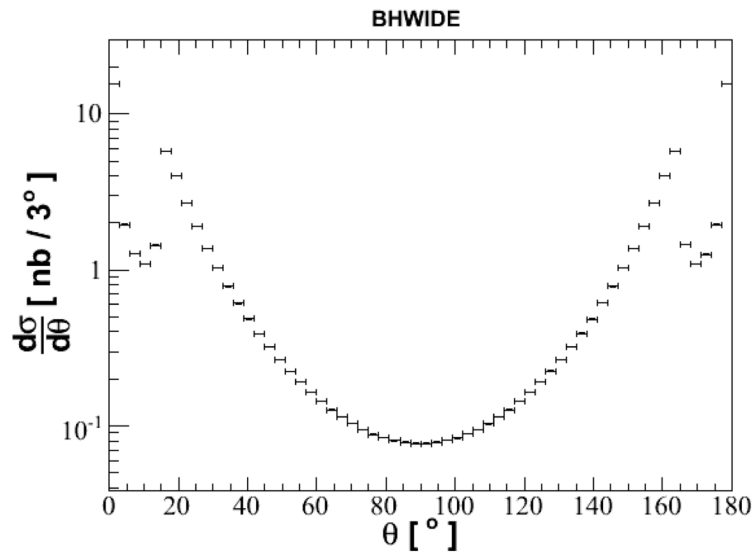
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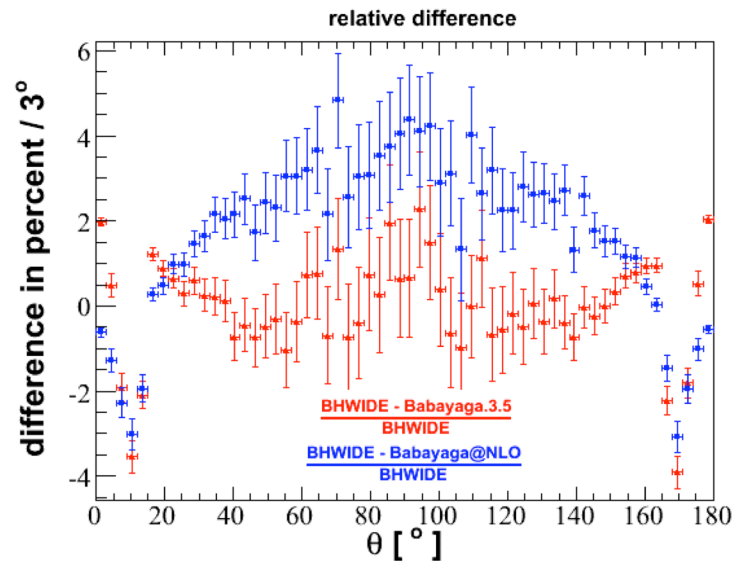
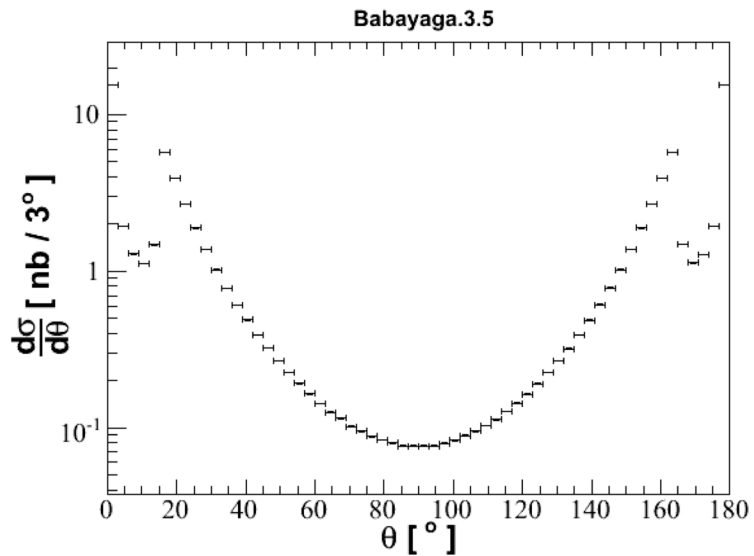
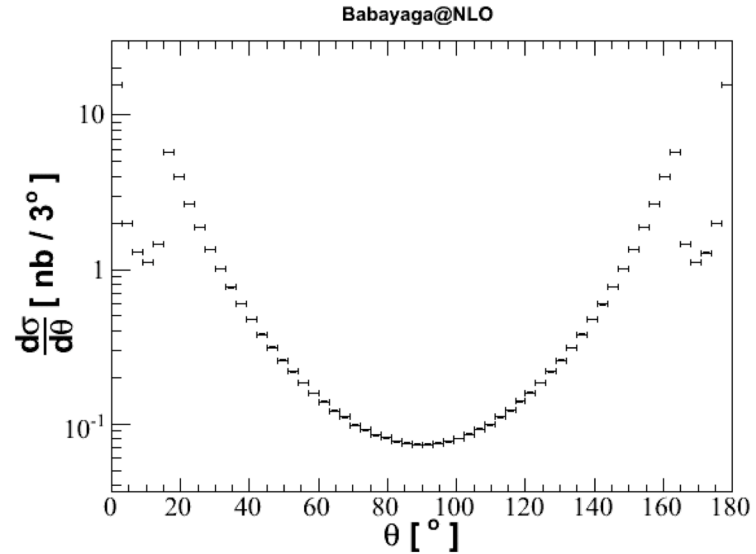
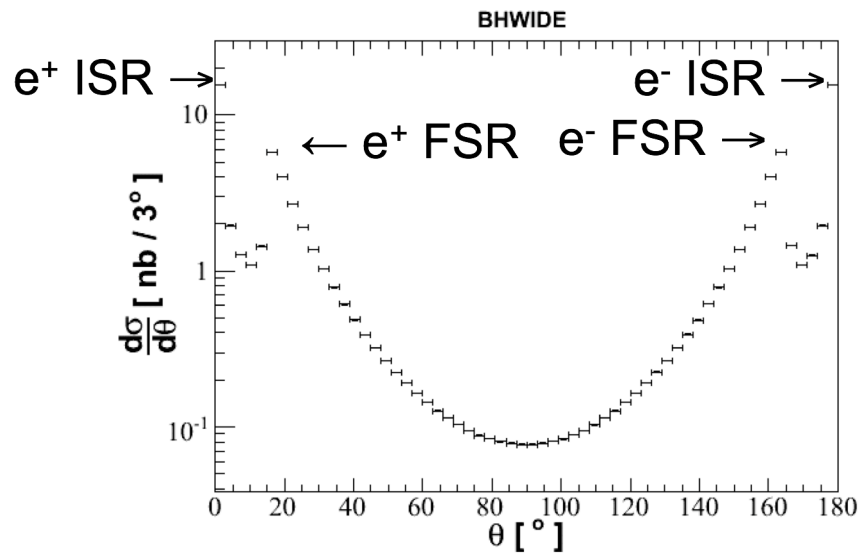


# Hardest photon





# Hardest photon





total  $\sigma_{\text{eff}}$

with cuts of the luminosity determination:

- BHWIDE:  $\sigma_{\text{eff}} = (6.815 \pm 0.009_{\text{stat}})\text{nb}$
- Babayaga:  $\sigma_{\text{eff}} = (6.793 \pm 0.013_{\text{stat}})\text{nb}$

rel. difference of  $\sim 0.29\% \pm 0.24_{\text{stat}}\%$



# Conclusions

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→ extremely interesting for BABAR



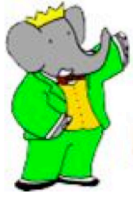
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**BABAR**

# Luminosity measurement

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$\gamma\gamma$	1.6%	2.0%	2.6%	



# Arxiv:0706.3235

**Motivation: tau analyses @ BaBar, which are limited in precision by both the  $e^+e^- \rightarrow \tau^+\tau^-$  cross section as the luminosity, i.e. the  $e^+e^- \rightarrow \mu^+\mu^-$  cross section**

## Tau and muon pair production cross-sections in electron-positron annihilations at $\sqrt{s} = 10.58$ GeV

Swagato Banerjee,<sup>1</sup> Bolek Pietrzyk,<sup>2</sup> J. Michael Roney,<sup>1</sup> and Zbigniew Was<sup>3</sup>

<sup>1</sup>*Dept. Physics and Astronomy, University of Victoria, Victoria, British Columbia, Canada*

<sup>2</sup>*Laboratoire d'Annecy-le-Vieux de Physique des Particules LAPP, IN2P3/CNRS, Université de Savoie, F-74019 Annecy-le-Vieux cedex, France*

<sup>3</sup>*Institute of Nuclear Physics, P.A.N. ul. Radzikowskiego 152 PL-31342 Kraków, Poland*

(Dated: June 21, 2007)

The calculational precision of  $e^+e^- \rightarrow \tau^+\tau^-$  and  $e^+e^- \rightarrow \mu^+\mu^-$  production cross-sections in electron-positron annihilations at  $\sqrt{s} = 10.58$  GeV are studied for the KKMC Monte Carlo simulation program. We determine  $\sigma(e^+e^- \rightarrow \tau^+\tau^-) = (0.919 \pm 0.003)$  nb and  $\sigma(e^+e^- \rightarrow \mu^+\mu^-) = (1.147 \pm 0.004)$  nb, where the error represents the precision of the calculation.

**0.31% error**

**0.35% error**



Arxiv:0706.3235

- Comparison  $\tau^+\tau^-$  cross section btw. **KKMC** and **KORALB**

NNLO by exponentiation

NLO

--> validate KKMC and obtain then  $\mu^+\mu^-$  cross section

- Checks done in **collaboration btw. theory & experiment**
  - treatment of vacuum polarization ( $\pm 0.18$ ,  $\pm 0.22$ )
  - treatment of ISR/FSR corrections ( $\pm 0.20$ ,  $\pm 0.20$ )
  - interference effects ( $\gamma$ - $Z^0$ ) and box diagrams ( $\pm 0.04$ ,  $\pm 0.04$ )
  - add. lepton pair, lepton pair vertex correction ( $\pm 0.15$ ,  $\pm 0.15$ )
  - impact of resonances ( $\pm 0.04$ ,  $\pm 0.10$ )





# Conclusions

A lot of improvements on the theory side  
for what concerns the luminosity  
determination at BABAR

Work needed on the experimental  
side to catch up



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