# Dihadron production in SIDIS experiments

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NATURWISSENSCHAFTLICHE FAKULTÄT





### Outline

# 1 The experiments

- 2 Theoretical framework
- 3 Data selection
- 4 The asymmetries
- **5** Conclusion and outlook

# The experiments

#### The experiments ► overview

### COMPASS





### **CLAS Hall-B**









### The experiments ► beams and targets



### The experiments $\blacktriangleright$ particle ID



# Theoretical framework

### Theoretical framework $\blacktriangleright$ leading twist PDFs 1

3 independent parton distribution functions (PDFs) are necessary to describe the spin structure of the nucleon in leading twist in the collinear case:



### Theoretical framework $\blacktriangleright$ leading twist PDFs 2

Taking into account the quark intrinsic transverse momentum  $k_T$ , at leading twist in total 8 PDFs are needed:



### Theoretical framework ► subleading twist PDFs

Envolving to subleading twist adds another 16 PDFs:



#### Theoretical framework ► dihadron cross section

Selection of relevant parts of the full dihadron cross section:

$$\begin{split} \mathrm{d}^{7}\sigma_{UT} &= \\ \frac{\alpha^{2}}{2\pi Q^{2}y} \left| \vec{S}_{\perp} \right| \sum_{a} e_{a}^{2} B(y) \mathrm{sin}(\phi_{R} + \phi_{S}) \frac{\left| \vec{R}_{T} \right|}{M_{hh}} h_{1}^{a}(x) H_{1}^{\triangleleft,a}(z,\xi,M_{hh}^{2}) + \dots \\ \mathrm{d}^{7}\sigma_{UL} &= \\ \frac{\alpha^{2}}{2\pi Q^{2}y} \vec{S}_{L} \sum_{a} e_{a}^{2} V(y) \mathrm{sin} \phi_{R} \frac{\left| \vec{R}_{T} \right|}{Q} \frac{M}{M_{hh}} x h_{L}^{a}(x) H_{1}^{\triangleleft,a}(z,\xi,M_{hh}^{2}) + \dots \\ \mathrm{d}^{7}\sigma_{LU} &= \\ \frac{\alpha^{2}}{2\pi Q^{2}y} \lambda \sum_{a} e_{a}^{2} W(y) \mathrm{sin} \phi_{R} \frac{\left| \vec{R}_{T} \right|}{Q} \frac{M}{M_{hh}} x e^{a}(x) H_{1}^{\triangleleft,a}(z,\xi,M_{hh}^{2}) + \dots \\ h_{1} \text{ Transversity PDF} \\ h_{L} \text{ subleading twist PDF of transv. polarized quark in long. polarized nucleon} \\ H_{1}^{\triangleleft} \text{ Interference Fragmentation Function (IFF)} \end{split}$$

Bacchetta A. & Radici M. arXiv:hep-ph/0311173 (2003)

### Theoretical framework $\blacktriangleright$ kinematics 1

$$\ell + N^{\uparrow} \to \ell' + h_1 + h_2 + X$$

Fragmentation of a transversely polarized quark into a pair of unpolarized hadrons



- k, k' and q are 3-momenta of incoming, scattered lepton and virtual photon
- $\phi_{S}$  azimuthal angle of the spin S of the fragmenting quark
- $p_i$  is the 3-momenta of  $h_i$
- $z_i$  is the fraction of the virtual-photon energy carried by  $h_i$
- $P_h$  is the sum of  $p_1$  and  $p_2$

### Theoretical framework $\blacktriangleright$ kinematics 2



- Definition of relative vector of the two hadrons slightly different between HERMES and COMPASS:
  - HERMES:  $\mathbf{R} = (\mathbf{p_1} \mathbf{p_2})/2$ ,  $\mathbf{R_T} = \mathbf{R} (\mathbf{R} \cdot \hat{\mathbf{P}_h})\hat{\mathbf{P}_h}$  thus  $\mathbf{R_T}$  is the component of  $\mathbf{p_1}$  orthogonal to perp. to  $\mathbf{P_h}$  and  $\phi_{R(\perp)}$  the zimuthal angle of  $\mathbf{R_T}$  about the  $\gamma^*$  direction
  - $\blacktriangleright$  COMPASS:  $\pmb{R}=\frac{z_2p_1-z_1p_2}{z_1+z_2}$  , which is invariant against boosts in the  $\gamma^*$  direction  $^1$

 $\hookrightarrow$  The azimuthal angle of  $\phi_{R(\perp)}$ :

$$\phi_{R(\perp)} = \frac{(q \times k) \cdot R_{(T)}}{|(q \times k) \cdot R_{(T)}|} \arccos\left(\frac{(q \times k) \cdot (q \times R_{(T)})}{|q \times k||q \times R_{(T)}|}\right)$$
$$\phi_{S} = \frac{(q \times k) \cdot S_{(T)}}{|(q \times k) \cdot S_{(T)}|} \arccos\left(\frac{(q \times k) \cdot (q \times S_{(T)})}{|q \times k||q \times S_{(T)}|}\right)$$

<sup>1</sup> cf. Artru & Collins, Z.Phys. **C69** (1996) 277-286

### **Theoretical framework** $\triangleright$ asymmetry extraction *e.g.* $A_{UT}$

$$N_{h^+h^-}(x, y, z, M_{hh}^2, \cos\theta, \phi_{RS}) \propto \sigma_{UU}(1 \pm f P_T D_{NN} A_{UT}^{\sin\phi_{RS}} \sin\theta \sin\phi_{RS})$$

 $\phi_{RS} = \phi_{R(\perp)} + \phi_S$  (COMPASS uses additional phase of  $-\pi$  leading to sign change)

 $\theta$  polar angle of  $h_1$  in the dihadron rest frame w.r.t. the  $P_h$  direction

- $\sigma_{UU}$  unpolarized cross section
  - $\pm$  indicates nucleon spin orientation
  - f target dilution factor
  - $P_T$  target polarization

 $D_{NN}(y)$  transv. spin transfer coef.

$$A_{UT}^{\sin\phi_{RS}\sin\theta} \propto \frac{\sum_{q} e_{q}^{2} h_{1}^{q}(x) H_{1,q}^{\triangleleft}(z, M_{h}^{2}, \cos\theta)}{\sum_{q} e_{q}^{2} f_{1}^{q}(x) D_{1,q}(z, M_{h}^{2}, \cos\theta)}$$

 $f_1$  number density

 $D_1$  unpolarized Interference Fragmentation Function

# Data selection

#### Data selection $\blacktriangleright$ cuts



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#### Data selection $\blacktriangleright$ kinematic distributions 1



#### Data selection $\blacktriangleright$ kinematic distributions 2



Clear contributions from resonance decay in the invariant mass distribution in the data of all three experiments

•  $\eta~(548\,{\rm GeV}/c^2)$  and  $\eta'~(958\,{\rm GeV}/c^2)$ 

Data selection  $\blacktriangleright$  kinematic distributions 3

- $\omega ~(783\,{\rm GeV}/c^2)$
- $K^0 (498 \,{
  m GeV}/c^2)$
- $\rho^0 \ (776 \, {\rm GeV}/c^2)$
- indication for higher mass resonances in COMPASS data

#### Data selection $\blacktriangleright$ mean values 1



#### Data selection $\blacktriangleright$ mean values 2



# The asymmetries

 $A_{UT}$ 

 $\pi^+\pi^-$  pairs

# HERMES and COMPASS

### **HERMES** $\triangleright \pi^+\pi^-$ dihadron asymmetries $A_{UT}$



Clear non-zero asymmetry amplitudes in high x region and in  $\rho^0$  mass bin

 $\hookrightarrow$  First indication of a non-zero  $h_1$  Transversity PDF and  $H_1^{\triangleleft}$  IFF

A. Airapetian et al. [HERMES Collaboration], JHEP 0806 (2008) 017

## **COMPASS** $\triangleright \pi^+\pi^-$ asymmetries $A_{UT}$



 $\hookrightarrow$  Clear asymmetry amplitudes of  $\pi^+\pi^-$  pairs in high x region and around the  $\rho^0$  mass

 $\hookrightarrow$  Confirmation of HERMES results with increased statistical precision in a larger kinematic range in x and  $M_{inv}$  with a higher  $\langle Q^2 \rangle$ .

### **HERMES** vs. COMPASS $\triangleright \pi^+\pi^-$ asymmetries $A_{UT}$



 $\hookrightarrow$  Good agreement between HERMES and COMPASS results within the uncertainties.

HERMES data scaled with 
$$\frac{1}{D_{nn}} = \frac{1-y+y^2/2}{1-y}$$
 and sign changed

### **HERMES** vs. COMPASS $\triangleright \pi^+\pi^-$ asymmetries $A_{IIT}$



 $\hookrightarrow$  Common trend of data and model predictions

- Good agreement in x and z dependence
- Very good agreement around  $\rho^0$  mass in strength and shape
- No significant asymmetry amplitude from in  $\eta$ ,  $\eta'$ ,  $K^0$  and  $\omega$  region?

Bacchetta A. and Radici M., Phys. Rev. D **74** (2006) 114007 Ma B.-Q. *et al.*, Phys. Rev. D **77** (2008) 014035 **COMPASS**  $\triangleright$   $h^+h^-$  asymmetries  $A^d_{UT}$ 



Adolph C. et al. [COMPASS Collaboration], Phys. Lett. B **713** (2012) 10 Bacchetta A. and Radici M., Phys. Rev. D **74** (2006) 114007 Ma B.-Q. et al., Phys. Rev. D **77** (2008) 014035

 $\hookrightarrow$  Asymmetries for deuteron target compatible with zero within the uncertainties

The models also predict a cancellation of the u and d quark transversity on the deuteron.

### **HERMES & COMPASS** ► extraction of transversity



talk by A. Courtoy A. Bachetta, A. Courtoy and M. Radici, PRL **107** (11), arXiv:1206.1836

# The asymmetries

 $A_{UT}$ 

# $\pi^+\pi^0$ and $\pi^-\pi^0$ pairs

# HERMES

# **HERMES** $\triangleright \pi^+\pi^0$ & $\pi^-\pi^0$ new formalism 1



- Artru/Lund string fragmentation model cannot be easily related to the published notation
- $D_1$  is unpolarized FF with  $(\chi = \chi')$
- $H_1^{\perp}$  is generalized Collins FF with  $(\chi \neq \chi')$
- Fragmentation functions expanded into partial waves in the direct sum basis  $|\ell, m\rangle$  (rather then direct product basis  $|\ell_1, m_1\rangle |\ell_2, m_2\rangle$ ):

$$D_{1} = \sum_{\ell=1}^{\infty} \sum_{\substack{m=-\ell \\ m=-\ell}}^{\ell} P_{\ell,m}(\cos\vartheta) e^{\imath m(\phi_{R}-\phi_{k})} D_{1}^{|\ell,m\rangle}(z, M_{hh}, |\boldsymbol{k}_{T}|)$$
$$H_{1}^{\perp} = \sum_{\ell=1}^{\infty} \sum_{\substack{m=-\ell \\ m=-\ell}}^{\infty} P_{\ell,m}(\cos\vartheta) e^{\imath m(\phi_{R}-\phi_{k})} H_{1}^{\perp|\ell,m\rangle}(z, M_{hh}, |\boldsymbol{k}_{T}|)$$

Gliske S. PhD thesis (2011)

# **HERMES** $\triangleright \pi^+\pi^0$ & $\pi^-\pi^0$ new formalism 2

# $\frac{1}{2} \otimes \frac{1}{2} = 1 \oplus 0 = 1 \text{ PSM} + 1 \text{ long. VM} + 2 \text{ transv. VM}$

- PSM =  $|0,0\rangle$ ; long. VM =  $|1,0\rangle$ ; transv. VM =  $|1,\pm1\rangle$
- Artru/Lund: PSM asymmetry has opposite sign of transv. pol. VM (left vs. right) and  $|1,0\rangle$  is zero
- Collins FF includes pairs of dihadrons: CG algebra  $\rightarrow |2, \pm 2\rangle$  with opposite sign as PS (*cf.* Collins  $\pi^+ vs. \pi^-$ )

 $|1,\pm1\rangle$  moments allow collinear access to the transversity PDF  $\Rightarrow H_1^{\perp|1,1\rangle}$  is related to usual IFF  $H_1^{\triangleleft}$  including also pp interference

 $|2,\pm2\rangle$  moments are transverse momentum dependent and related to string fragmentation models

 $\Rightarrow \text{Cross-section has direct access to } H_1^{\perp|2,\pm2\rangle} \\\Rightarrow H_1^{\perp|2,\pm2\rangle} \text{ should have opposite sign as pseudo-scalar } H_1^{\perp}$ 

# **HERMES** $\triangleright \pi^+\pi^0$ & $\pi^-\pi^0$ dihadron asymmetries $|1,1\rangle$



- $\hookrightarrow |1,1\rangle$  limited statistics for  $\pi^{\pm}\pi^{0}$ 
  - still sizeable mean asymmetry
  - consistent signs of all  $\pi^{\pm}\pi^{0}$  pairs
  - Despite uncertainties, may still help constrain global fits

**HERMES**  $\triangleright \pi^+\pi^-, \pi^+\pi^0 \& \pi^-\pi^0$  dihadron asymmetries  $|2,\pm 2\rangle$ 



 $\hookrightarrow |2, -2\rangle$  moment is compatible with zero for all combinations: Transversity TMD causes frag. quark to have positive polarization  $\rightarrow$  $|2, -2\rangle$  must be zero as this PW requires negative polarization

 $\hookrightarrow |2,+2\rangle$  moment is consistent with model expectations: No indication of any signal outside the  $\rho$  mass bin  $\rightarrow$  no non-resonant pion-pairs in *p*-wave

# The asymmetries

 $A_{UL}$  and  $A_{LU}$ 

 $\pi^+\pi^-$  pairs

JLab

# **JLab** $\triangleright \pi^+\pi^-$ dihadron asymmetries $A_{LU}$



- $\begin{array}{l} \hookrightarrow \text{Sizeable asymmetry amplitudes, from independent data sets} \\ \hookrightarrow \text{Very small statistical uncertainties} \\ \Rightarrow \text{Compatible results from 2 different setups} \end{array}$ 
  - e1f (21 fb<sup>-1</sup>): unpol. liquid hydrogen target,  $E_{beam} = 5.5 \text{ GeV}$ ,  $\langle \lambda \rangle = 75 \%$
  - eg1-dvcs (50 fb<sup>-1</sup>): long. pol.  $NH_3$  target,  $E_{beam} = 5.967 \,\text{GeV}$ ,  $\langle P_T \rangle = 80 \,\%, \, \langle \lambda \rangle = 85 \,\%$

#### **JLab** $\blacktriangleright$ dihadron asymmetries $A_{UL}$



 $\begin{array}{l} \hookrightarrow \text{Sizeable asymmetry amplitudes} \\ \hookrightarrow \text{Very small statistical uncertainties} \end{array}$ 

Pereira S.A. Como2013

# The asymmetries

 $A_{UT}$ 

# pairs with strangeness: $K^+K^-$ , $K^+\pi^-$ and $\pi^+K^-$

# HERMES & COMPASS

#### **COMPASS** $\triangleright$ $z_1 + z_2$ , $M_{inv}$ and $E_{miss}$ distributions



38 / 53

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Dihadron production in SIDIS exp.

### **COMPASS** $\triangleright$ $Q_2$ vs. x distributions



### **COMPASS** $\blacktriangleright$ $M_{inv}$ vs. z distributions



### **COMPASS** $\triangleright$ $K^+K^-$ asymmetries $A_{UT}$



 $\hookrightarrow$  no clear trend & large statistical uncertainties

- weak indication of a non-zero asymmetry at high x
- weak indication of a non-zero asymmetry at high z
- indication of a wide dip at  $M_{inv} \approx 1.4 \,\mathrm{GeV}/c^2$

### **COMPASS** $\triangleright$ $K^+K^-$ asymmetries $A_{UT}$



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 $\hookrightarrow$  indication of a signal

- top row:  $|0,0\rangle$ ,  $|1,\pm1\rangle$ : signal in  $\phi(1020)$  bin?
- bottom row:  $|2,\pm1\rangle$ ,  $|2,\pm2\rangle$ : opposite signs to  $|0,0\rangle$

**COMPASS**  $\triangleright \pi^+\pi^- \& K^+K^-$  asymmetries  $A^d_{UT}$ 



2002-04 deuteron data 2-hadron asymmetries:  $\pi^+\pi^-$  pairs (top),  $K^+K^-$  pairs (bottom)

### $\hookrightarrow h^+h^-$ asymmetries follow mostly $\pi^+\pi^-$ signal

 $\pi^+\pi^-$  asymmetries are small and compatible with zero  $K^+K^-$  no signal & low statistics

**COMPASS**  $\triangleright \pi^+ K^- \& K^+ \pi^- \text{ asymmetries } A^d_{UT}$ 



2002-04 deuteron data 2-hadron asymmetries: all  $\pi^+ K^-$  pairs (top),  $K^+ \pi^-$  pairs (bottom)

 $\hookrightarrow \pi^+ K^- \& K^+ \pi^-$  signal compatible with zero

weak indication of opposite sign of the signal in x dependence

### **COMPASS** $\triangleright$ $K^+\pi^-$ asymmetries $A_{UT}$



- negative mean value with constant trend in x
- $\bullet$  weak indication of a non-zero asymmetry at low and high z
- indication of a wide dip at  $M_{inv} \approx 1.0 \,\mathrm{GeV}/c^2$
- $\Rightarrow$  indication of signals from  $K^*/K_{1/2}$  decays

# **COMPASS** $\triangleright$ $K^+\pi^-$ asymmetries $A_{UT}$



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# **COMPASS** $\triangleright \pi^+ K^-$ asymmetries $A_{UT}$



- x no signal
- z significant slope with a relative maximum around 0.45
- $M_{inv}$  no clear signal
- $\Rightarrow$  No clear signal in mass range

### **COMPASS** $\triangleright$ all identified pairs $A_{UT}$



# Conclusion and outlook

### **Conclusion and outlook** ► **Conclusion**

General

• non-zero Transversity TMD PDF  $h_1$  and IFF  $H_1^{\triangleleft}$ 

COMPASS

• Full set  $\pi^+\pi^-$ ,  $K^+K^-$ ,  $K^+\pi^-$ ,  $\pi^+K^-$  from proton data

HERMES

- $\pi^{\pm}\pi^{0}$  pairs will assist in the *u*-*d* flavor separation
- Unique access to the TMD spin structure of fragmentation
- Testing the Lund/Artru model via  $|2,\pm2\rangle$  moments
- $|2, -2\rangle$  must be zero if  $h_1$  causes the fragmenting quark to have positive polarization as this partial wave requires negative polarization
- $|2,+2\rangle$  no non-resonant pion-pairs in p-wave, sizeable for  $\rho^\pm,$  zero for  $\rho^0$  JLab 6 GeV
  - sizeable  $A_{LU}$ ,  $A_{UL}$  asymmetries of  $\pi^+\pi^-$  with very small statistical uncertainties

## **Conclusion and outlook** ► **Outlook**

COMPASS

- Reanalysis of deuteron data with homogeneous cuts, binning and methods w.r.t. proton 2007/2010 analyses for a full flavor separation incl. strangeness
- $\pi^{\pm}\pi^{0}$  pair asymmetries
- $A_{UL}$ ,  $A_{LL}$  asymmetries

HERMES

•  $K^+K^-$  (some data near  $\phi$  mass),  $\pi^+\gamma\gamma$ ,  $\pi^-\gamma\gamma$ ,  $K^+\pi^-$ ,  $\pi^+K^-$ 

JLab  $6\,\mathrm{GeV}$ 

- $\pi^+\pi^0$  pair asymmetries
- double spin asymmetries

JLab  $12 \,\mathrm{GeV}$ 

- larger  $Q^2$  coverage
- data with x up to 0.6
- Kaon sample with  $\pi/K$  separation at  $3 8 \,\text{GeV}/c \Rightarrow \text{strangeness}$
- Transversal and longitudinally polarized H, D (CLAS12) and  ${}^{3}He$  (SolID) targets



# Thank you for your attention!



electronic address:christopher.braun@cern.chChr. Braun (Univ. Erlangen)Dihadron production in SIDIS exp.PSHP 2013, Frascati53 / 53