



Light Hadron Production @ BABAR

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On behalf of the BaBar Collaboration



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OUTLINE

INTRODUCTION

- Hadron production in e^+e^- annihilation
 - Fragmentation Functions
- PEP-II and the BABAR detector at SLAC

UNPOLARIZED FRAGMENTATION FUNCTIONS

- Inclusive production of light hadrons at BABAR
- Charged hadron identification
- BABAR results: π^\pm , K^\pm , p/\bar{p} cross section
 - π^\pm , K^\pm , p/\bar{p} scaling properties

POLARIZED FRAGMENTATION FUNCTION

- Collins fragmentation function
- Reference frames and analysis strategy
- BABAR preliminary results: Collins asymmetries *vs.* fractional energies, pion transverse momentum, and analysis axis polar angle

SUMMARY and CONCLUSIONS

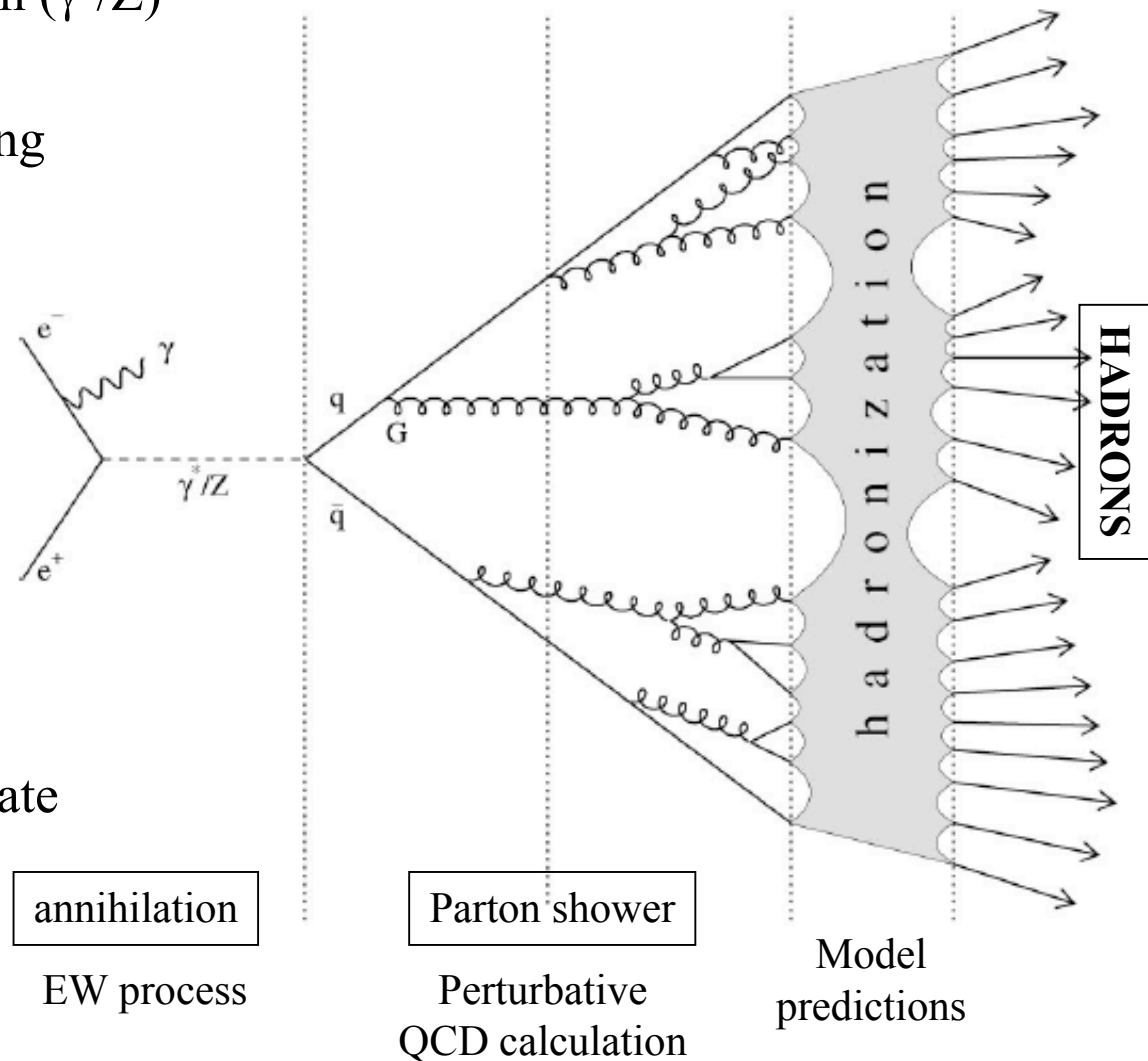
Hadron production in e^+e^- annihilation

The $e^+e^- \rightarrow \gamma^*/Z \rightarrow \text{hadrons}$ process can be subdivided into four steps:

- 1) e^+e^- annihilate into an intermediate boson (γ^*/Z) which decays into a quark-antiquark pair
- 2) the radiation of gluons and gluon-splitting into $q\bar{q}$ pairs leads to a **parton shower**
- 3) the process of hadronization which summarizes the transition of quarks and gluons into hadrons
- 4) The hadrons **decay** into “stable” particles...that can be **observed** in a detector

ADVANTAGES:

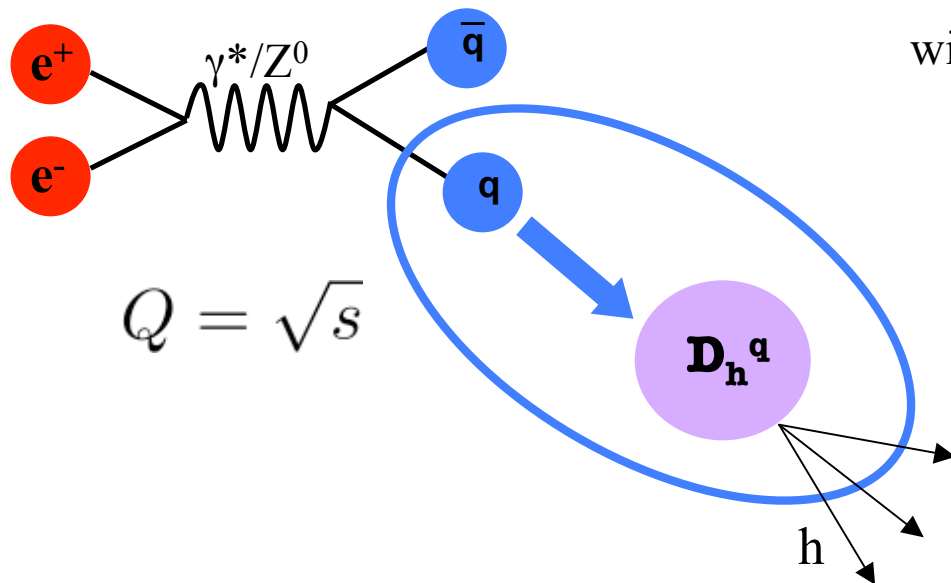
- no interference between initial and final state
- 4-momentum of initial state fully transferred to the final state (no ISR)
- more e^+e^- data



Fragmentation Function

Fragmentation functions (FFs) are the most important physics quantities in describing the hadron production in high energy reactions \implies they quantify the hadronization of quarks and/or gluons that occur when hadron is produced

$$e^+e^- \rightarrow \gamma/Z \rightarrow h + X \quad \frac{1}{\sigma_0} \frac{d^2\sigma^h}{dx d\cos\theta} = \frac{3}{8}(1 + \cos^2\theta)F_T^h + \frac{3}{4}\sin^2\theta F_L^h + \frac{3}{4}\cos\theta F_A^h$$



with $x=2E_h/\sqrt{s}$. Integrating over θ , we obtain the total FF:

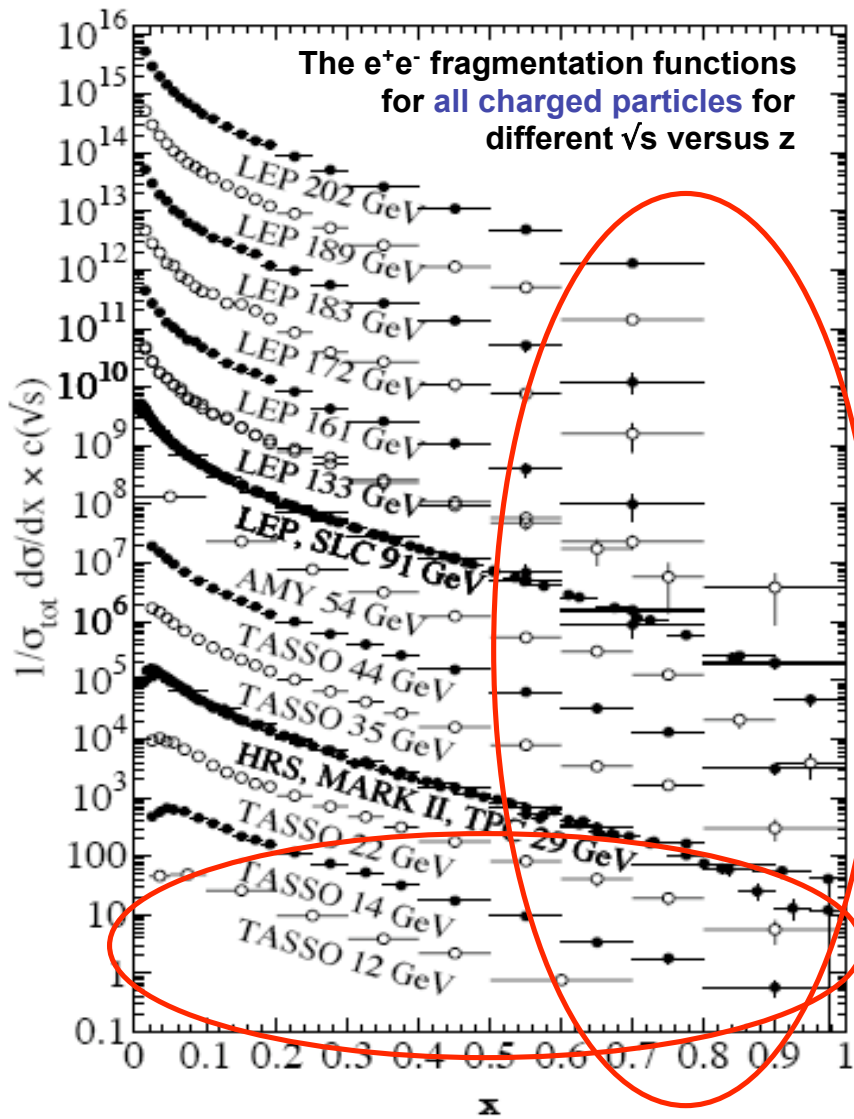
$$\frac{1}{\sigma_0} \frac{d\sigma^h}{dx} = F^h(x, s) = \sum_i \int_x^1 \frac{dz}{z} C_i(z, \alpha_s(\mu), \frac{s}{\mu^2}) D_i^h(\frac{x}{z}, \mu^2) + \mathcal{O}(\frac{1}{\sqrt{s}})$$

Coefficient functions;
calculable in pQCD

Parton FF \rightarrow non-perturbative informations

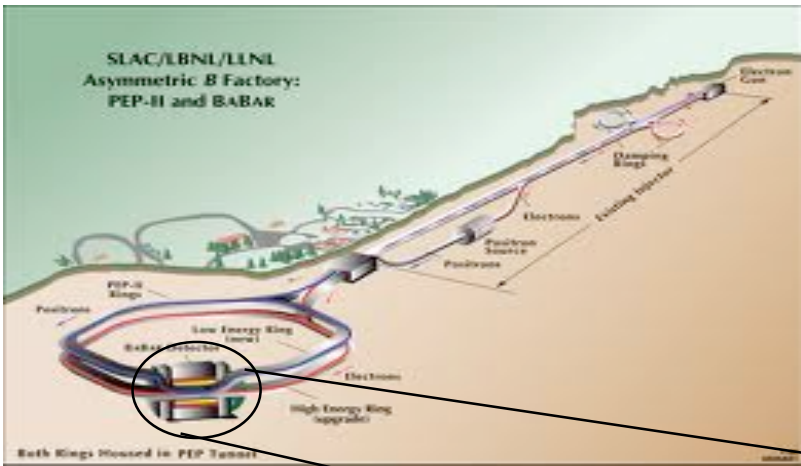
Ideally, given a (hard) parton i ($i=u/\bar{u}, d/\bar{d}, s/\bar{s}, c/\bar{c}, b/\bar{b}, g$), we want to find the **probability** D_i^h that it fragments into a hadron h carrying away a fraction z of the parton momentum

e^+e^- data



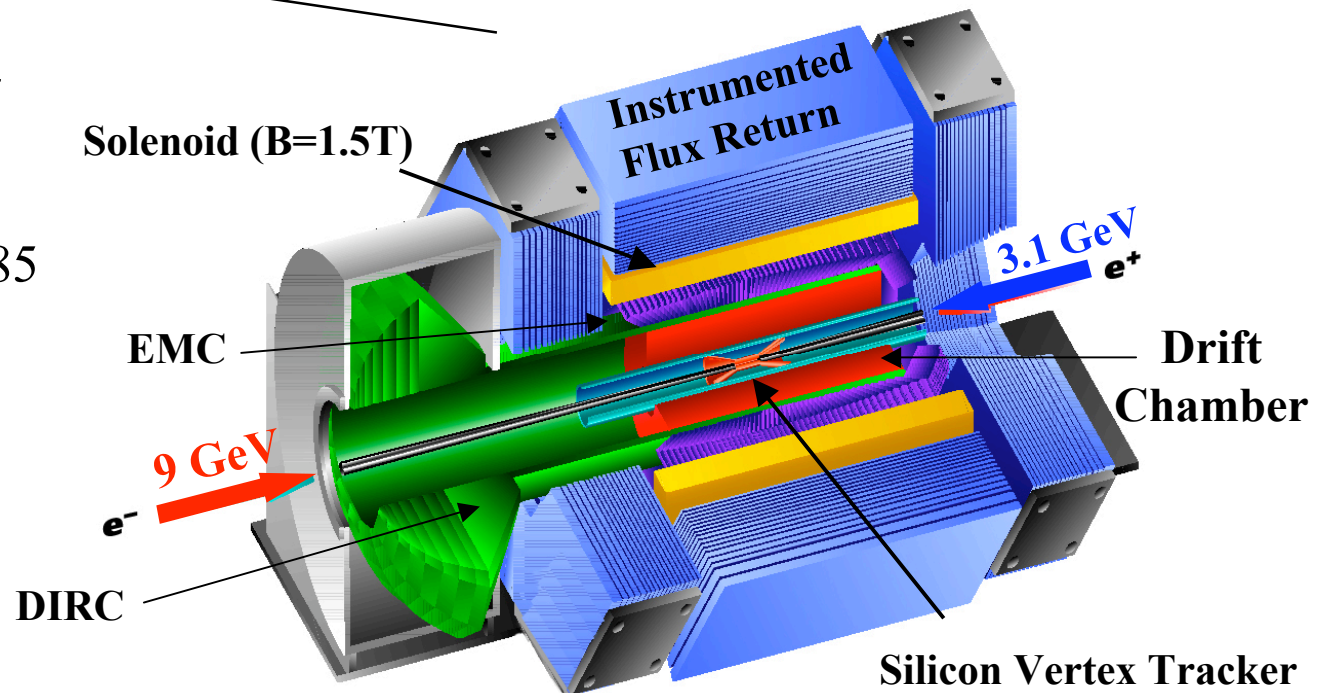
- Perturbative QCD corrections lead to logarithmic scaling violations via the evolution equations (DGLAP)
 - Most of the data are obtained at the Z^0
 - Measurement of both quark and antiquark fragmentation
 - 3-jet fragmentation to access gluon FF difficult
 - The information on how the individual q flavour fragments into h depends on the “tagging techniques”
 - Many attempts to extract FF from e^+e^- data: KKP, AKK, HKNS, Kretzer ...
NPB 725,181(2006), NPB 803,42(2008), PRD 75,094009(2007), PRD 62,054001(2000), NPB 582,514(2000);
 - Global analysis: e^+e^- , SIDIS, and pp
PRD 75,114010(2007), PRD 76,074033(2007), arXiv:1209.3240
- ➔ Few data at high x and at low energy
Less information for identified charged particles

PEP-II and the BaBar detector at SLAC



- Asymmetric-energy e^+e^- collider operating at the $\Upsilon(4S)$ resonance ($\sqrt{s}=10.58$ GeV)
 - High Energy Ring (**HER**): 9.0 GeV e^-
 - Low Energy Ring (**LER**): 3.1 GeV e^+
 - c.m.-lab boost, $\beta\gamma \approx 0.56$
- High luminosity: $\int \mathcal{L} \sim 500 \text{ fb}^{-1}$

- Asymmetric detector
 - c.m. acceptance $-0.9 < \cos\theta^* < 0.85$ wrt e^- beam
- Excellent performance
 - good tracking, mass resolution
 - good γ , π^0 reconstruction
 - full e , μ , π , K , and p identification



Production of charged pions, kaons, and protons @ BABAR

$$e^+e^- \rightarrow \gamma^* \rightarrow u\bar{u}, d\bar{d}, s\bar{s}, c\bar{c} \rightarrow hX \quad (h = \pi^\pm, K^\pm, p/\bar{p})$$

4 : 1 : 1 : 4 @ 10.54 GeV

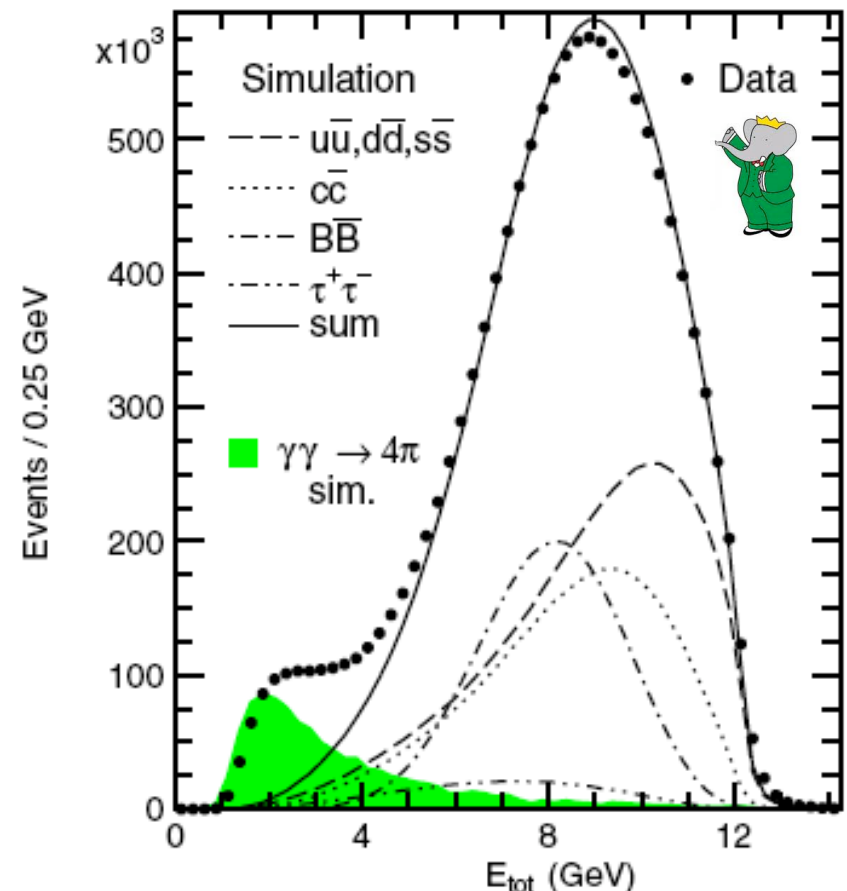
- ✓ PRD **88**, 032011 (2013)
- ✓ Data samples used: 0.91 fb⁻¹ @ 10.54 GeV + 3.6 fb⁻¹ on-peak for checks and calibrations
- ✓ “**Prompt**” and “**conventional**” hadrons:
 - prompt: primary hadrons or products of a decay chain in which all particles have lifetimes shorter than 10⁻¹¹ s
 - conventional: includes the decay daughters of particles with lifetimes in the range 1-3x10⁻¹¹ (i.e. K_s⁰ and weakly decaying strange baryons)
- ✓ The uncertainties on the results are dominated by systematic contributions.

Hadronic event selection

2.2 million of events:

- 3 or more reconstructed charged-particle tracks and one good vertex ($\chi^2 < 0.01$)
- Event well contained within the sensitive volume:
 - thrust axis well within DIRC detector acceptance region
 - $5 < E_{\text{tot}} < 14$ GeV
- reject leptonic events
 - Fox-Wolfram moment < 0.9
 - electron veto

- Consistency between data and simulation:
 E_{tot} distributions limit efficiency error to 0.5%
- τ -pairs: 4% of events, but up to 20% of high- p_{lab} tracks
- radiative Bhabhas: few % of high- p_{lab} forward/backward tracks
- two-photon events: $< 1\%$
- negligible contribution from the other background sources

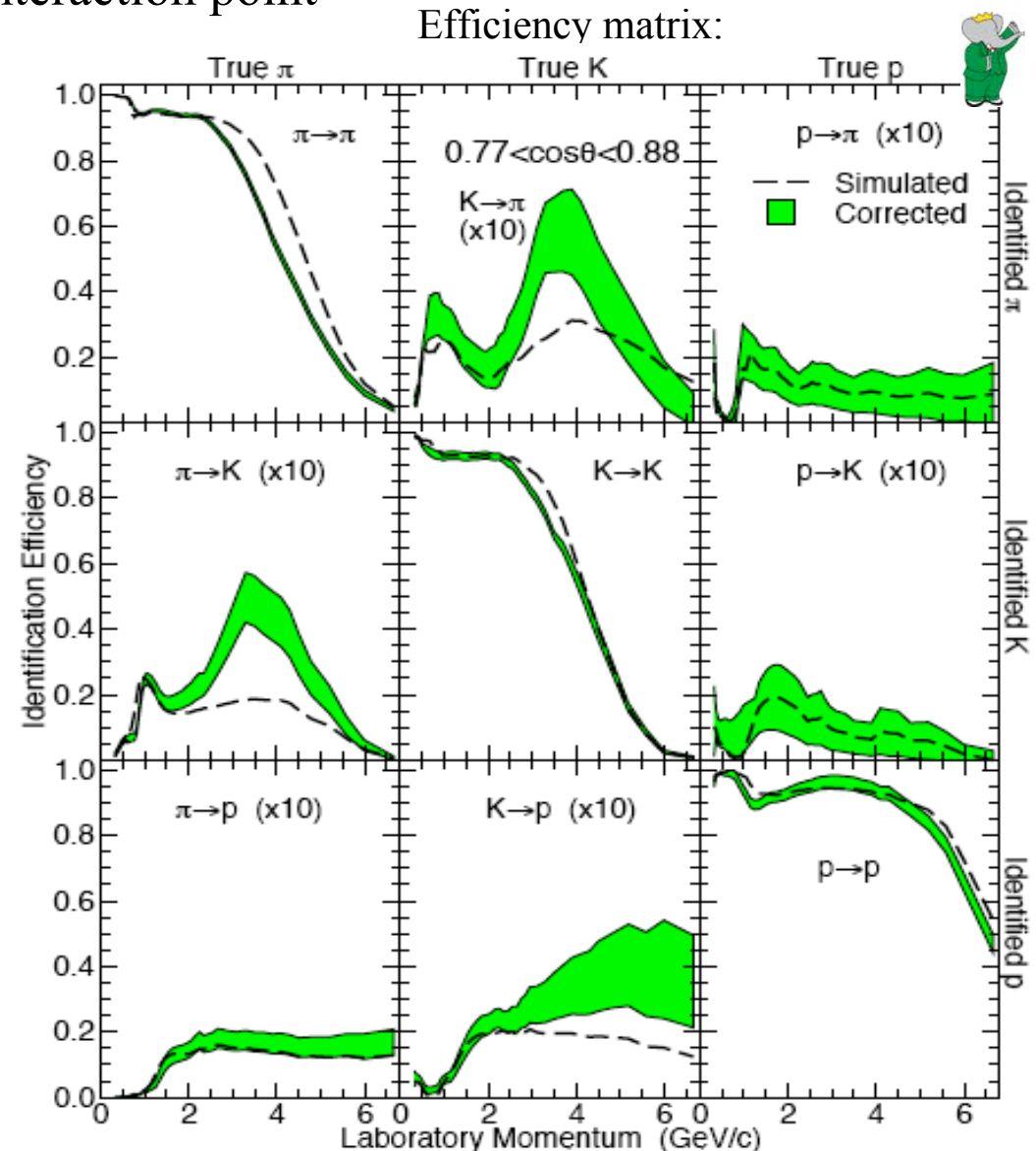


Charged hadron identification

- Well-reconstructed tracks from the primary interaction point
- **Excellent** identification of π^\pm , K^\pm , and p/\bar{p}
 \Rightarrow Cherenkov light plus dE/dx

- **Efficiency matrix** E_{ij} : performance of our hadron identification procedure as a function of p_{lab}

- very high at low p_{lab} (good dE/dx)
- plateau for p_{lab} where DIRC provides good separation
- fall off at highest p_{lab} , where the Cherenkov angles for different particles converge
- calibrated using data control samples
 \rightarrow we derive corrections to the simulated efficiency matrix (green band)
- large efficiency over much of the momentum range
- few-% mis-identification



Differential cross section measurements

- We use E_{ij} to construct the raw production rates $(1/N_{\text{evt}}^{\text{sel}})(dn_i/dp_{\text{lab}})$, defined as the number reconstructed particles per selected event per unit momentum in the lab frame

- we count $n_j = n \sum_i E_{ij} f_i$, and calculate f_i , the true fraction of tracks of type i

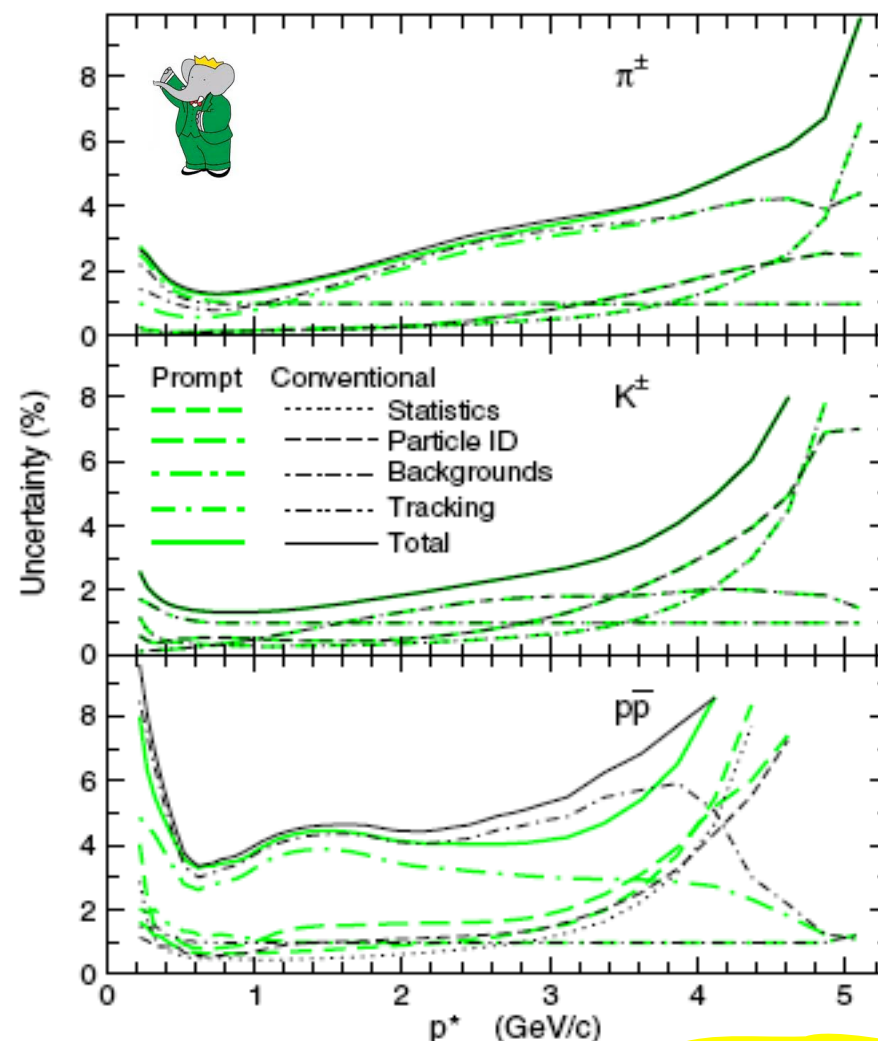
- Correct these spectra for

- **physics background** (mostly $\tau^+\tau^-$) and normalize by the estimated number of hadronic events in the selected sample
- interaction in the detector material (up to 4% at low momentum)

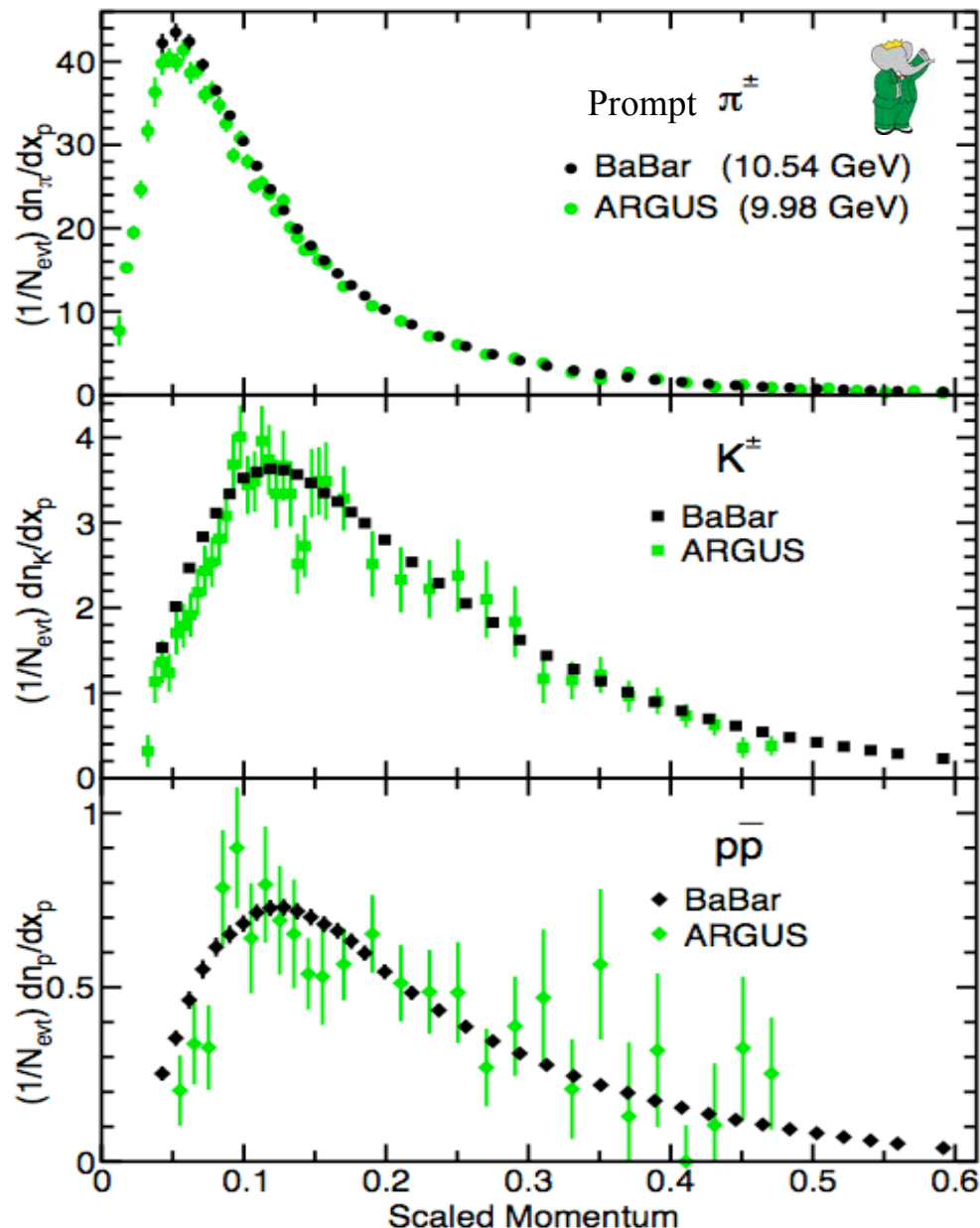
- **track and event selection efficiencies, momentum resolution, transform to c.m. frame**

- **extensive systematic cross checks:** data-MC comparison, check for θ, ϕ, \dots dependence, compare positive and negative charged tracks,...

- largest uncertainties from particle identification, backgrounds, and tracking efficiencies



Cross section results



- **Cross section results in term of scaled momentum $x_p = 2p^*/E_{\text{cm}}$**

- coverage from 0.2 GeV/c to the kinematic limit of 5.27 GeV/c

- **Compare nicely with previous data from ARGUS^[1]**

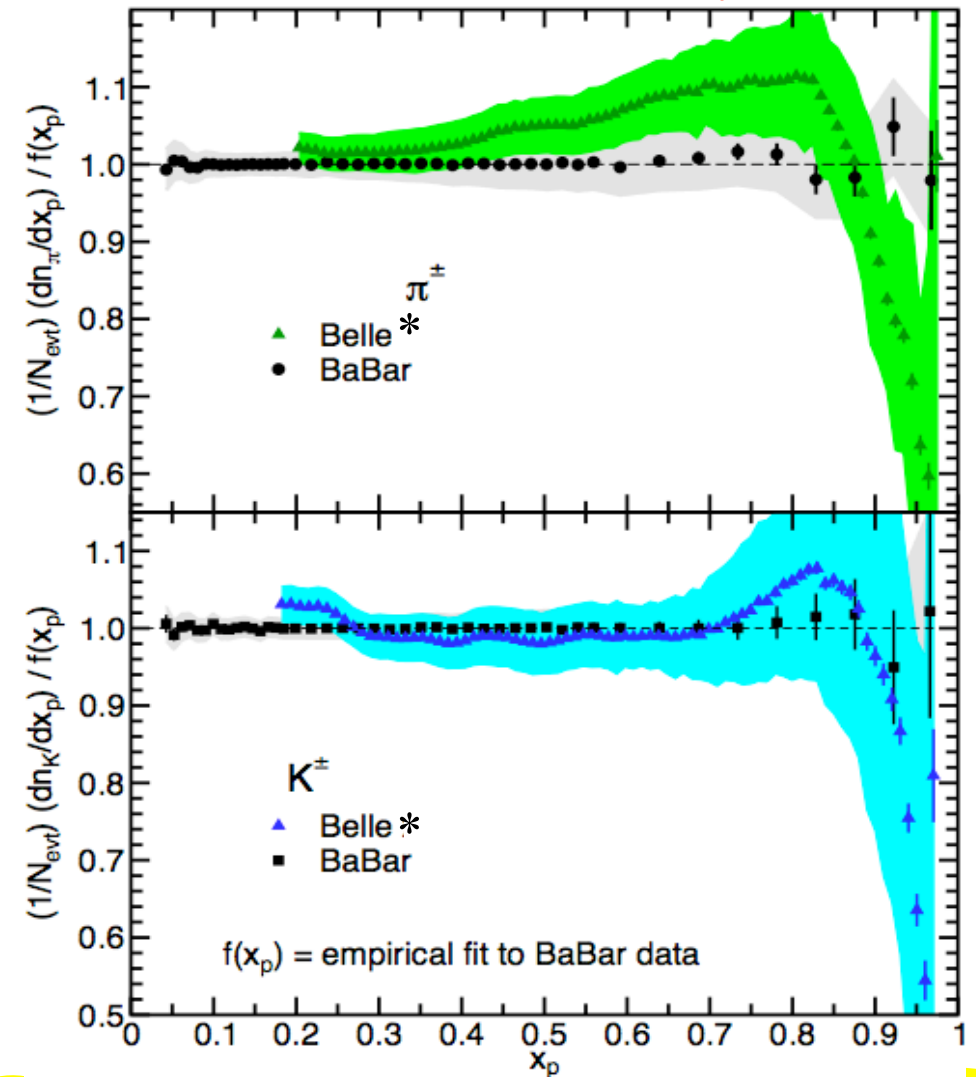
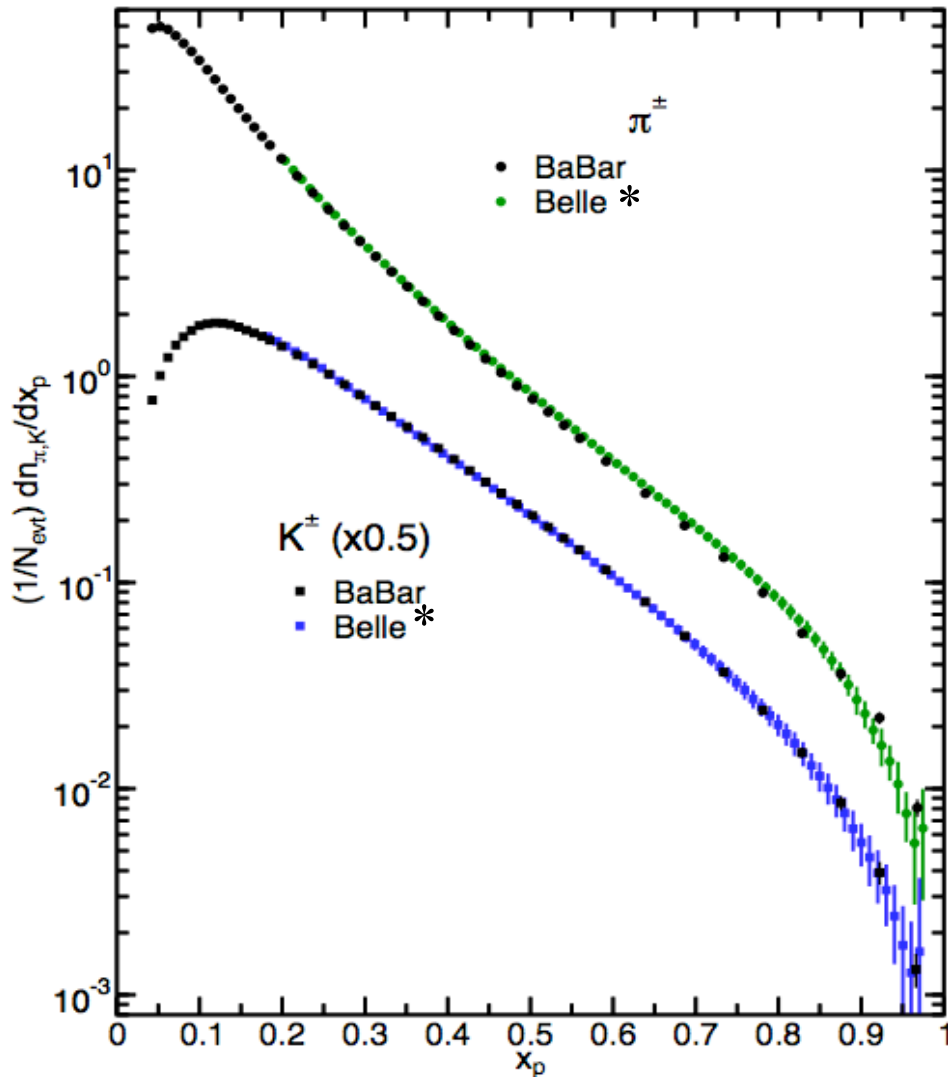
- consistent everywhere for $x_p > 0.1$
- mass driven scaling violation for $x_p < 0.1$: ARGUS data systematically below
- BABAR more precise
- BABAR better coverage at high x_p
- ARGUS extends to low momentum for $\pi^\pm \rightarrow$ complementary information

[1] H. Albrecht *et al.* (ARGUS Collaboration) Z. Phys. C **44**, 547 (1989).

BaBar/Belle comparison

- Belle have measured differential cross section $d\sigma/dz$ [PRL 111, 062002 (2013)]
 - we renormalize arbitrarily to compare the shapes

Courtesy of David Muller

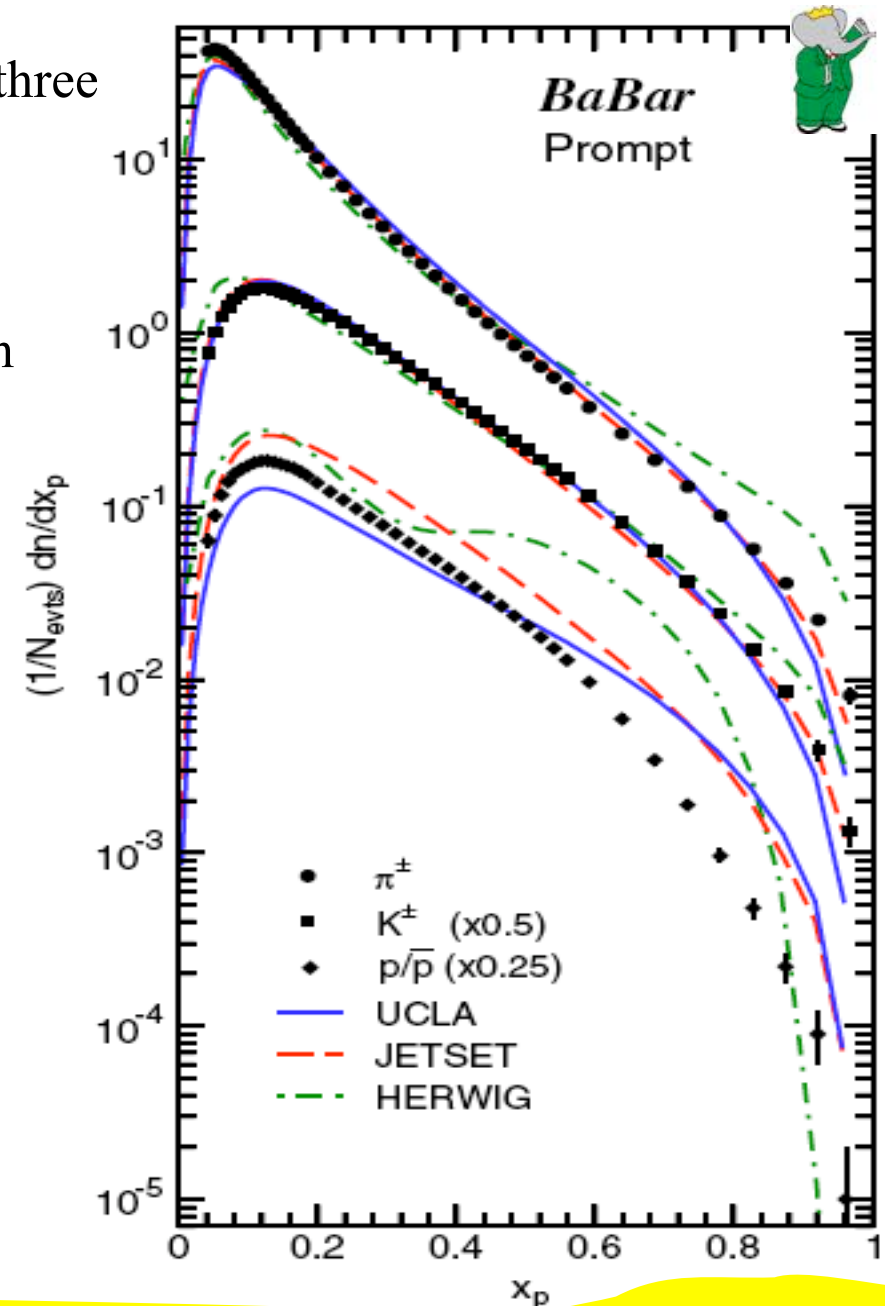


Comparison with hadronization models

We compare our cross section with the predictions of three hadronization models: **JETSET**, **HERWIG**, **UCLA**:

- each model contains free parameters controlling various aspects of the hadronization process
- many parameters for JETSET \Rightarrow model many hadron species in detail
- few free parameters for UCLA and HERWIG \Rightarrow global description

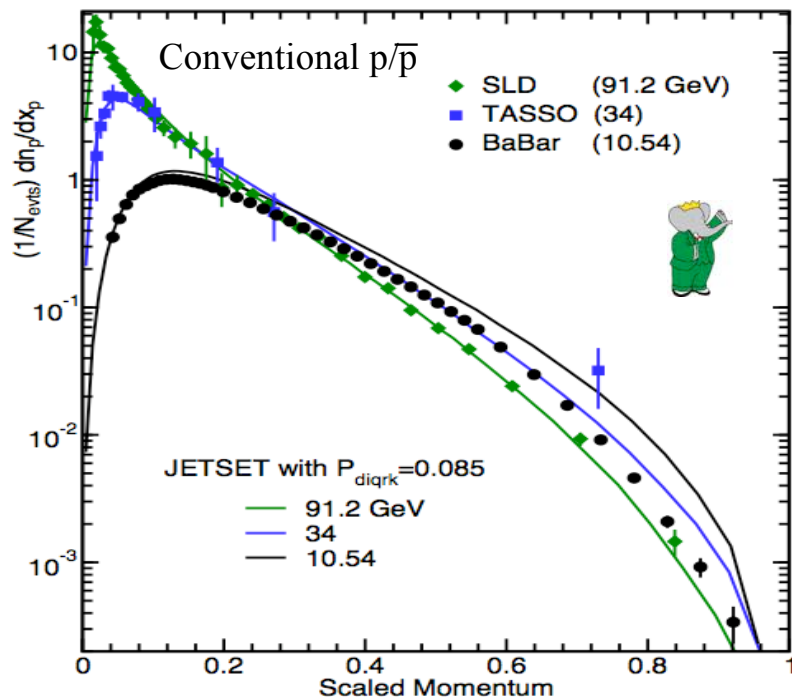
- **Default parameters used** (based on previous data: higher energies plus ARGUS data)
- **Large discrepancies in general**
 - all the models qualitatively describe the bulk of the spectra
 - no model describes any spectrum in detail
- **Peak positions consistent with data** (except for the HERWIG K^\pm)
- **Similar discrepancies observed at higher energies**



Scaling Properties

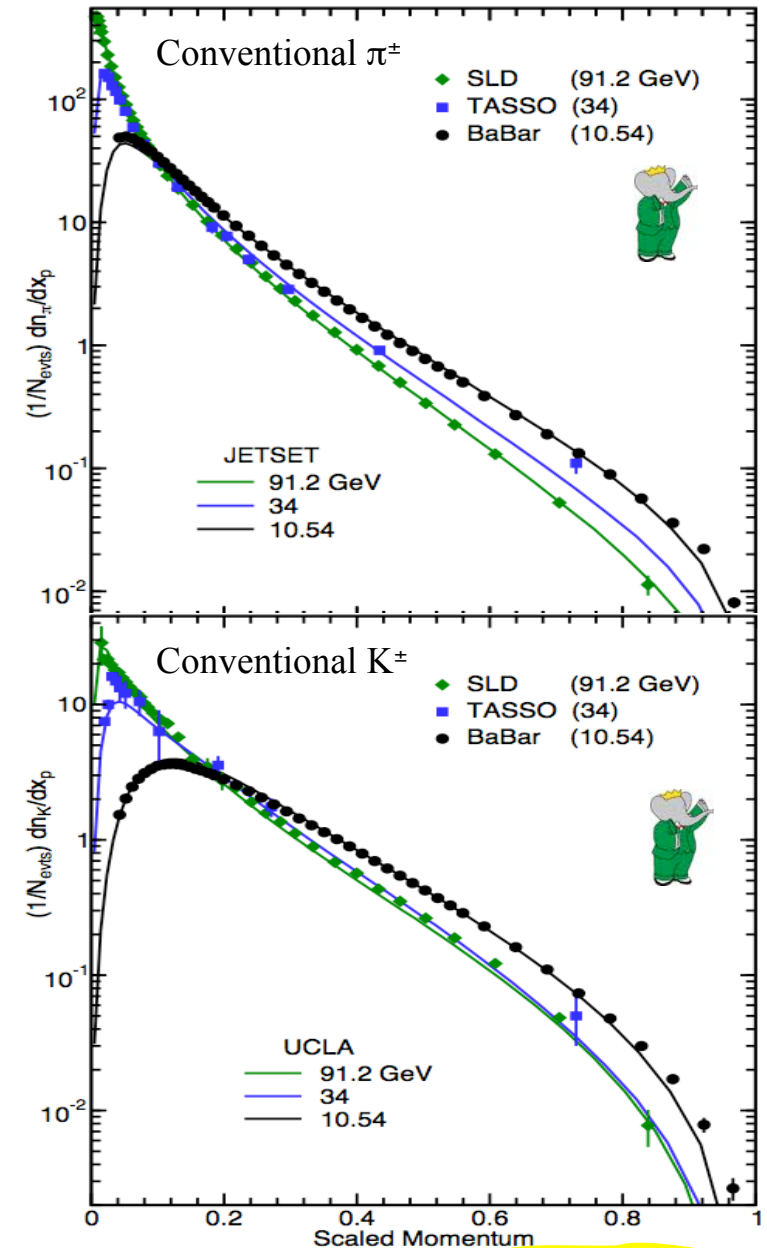
Consider π , K, and p from BABAR, TASSO and SLD

- **Strong scaling violation** at **high x_p** (running of α_s) and at **low x_p** (pion mass)
- **K^\pm** : the different flavor composition of the three samples modifies the expected scaling violation
 - models predict about 10%-15% more scaling violation than is observed



- p/\bar{p} : the scaling prediction for 10.54 GeV is consistent with data for $x_p < 0.07$, but exceeding it by as much as a factor 3 at $x_p = 0.8$

Is there something missing?

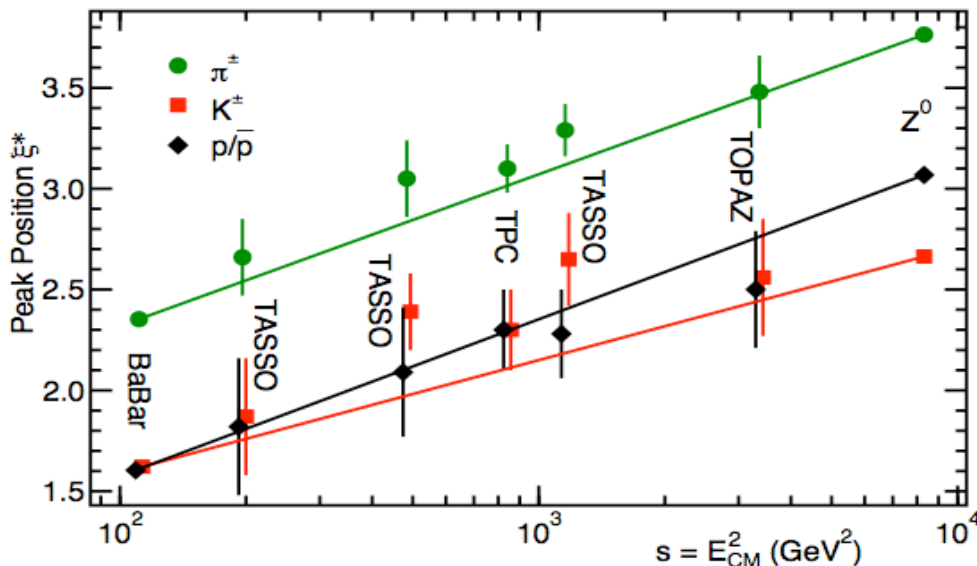
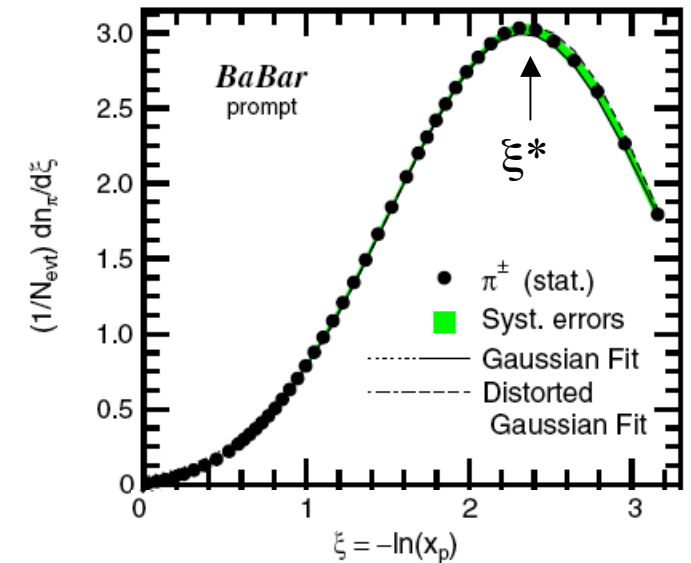


Test of MLLA+LPHD QCD

Transform our cross section into the variable $\xi = -\ln(x_p)$

Modified Leading Logarithm Approximation (MLLA) with Local Parton-Hadron Duality (LPHD) ansatz:

- a Gaussian function should provide a good description of these spectra
 - fit the spectra with a (distorted) Gaussian function ==> **reasonable description of the data**
- the peak position ξ^* should **decrease exponentially with increasing hadron mass at a given E_{cm}**
 - $\xi^*_\pi > \xi^*_K$, but $\xi^*_K \sim \xi^*_{p/\bar{p}}$ (consistent with behavior at higher E)
- should **increase logarithmically with E_{cm} for a given hadron type**



- **BABAR and Z⁰ data provide precise slope;** the other data are consistent with the line that joins BABAR and Z⁰ data
- **Similar slopes of the lines for pions and protons; different for kaons ==> changing flavor composition** with increasing E_{CM}

Inclusive production of charged pion pairs

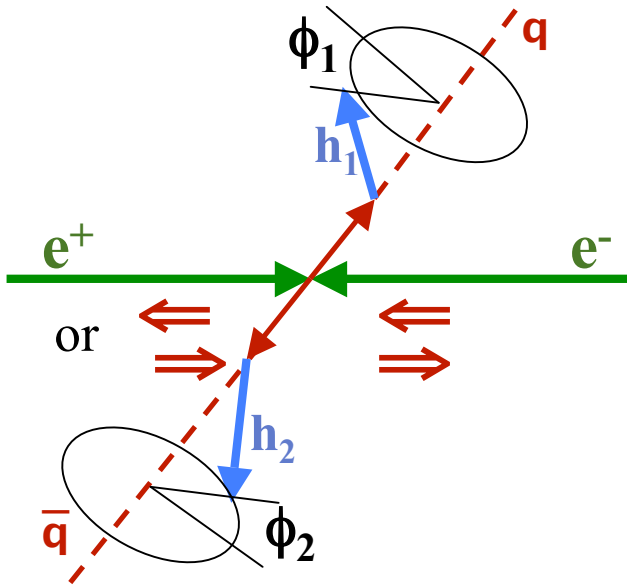
Collins Fragmentation Function @ BABAR

$$e^+e^- \rightarrow \gamma^* \rightarrow u\bar{u}, d\bar{d}, s\bar{s} \rightarrow \pi^\pm \pi^\pm X$$

- ✓ Preliminary results \Rightarrow SUBMITTED TO PRD ([arXiv:1309.5278](https://arxiv.org/abs/1309.5278))
- ✓ Data samples used: 468 fb^{-1} at $E_{\text{CM}} \sim 10.58 \text{ GeV}$

Collins Fragmentation Function

Polarized FF (Collins FF): dependence on $z=2E_h/\sqrt{s}$, P_\perp , and s_q



“Standard” unpolarized FF

$$D_1^{q\uparrow}(z, \mathbf{P}_\perp; s_q) = D_1^q(z, P_\perp) + \frac{P_\perp}{zM_h} H_1^{\perp q}(z, P_\perp) \mathbf{s}_q \cdot (\mathbf{k}_q \times \mathbf{P}_\perp)$$

- H_1^\perp is the **polarized** fragmentation function or **Collins FF**
- **Chiral-odd** function
- could arise from a **spin-orbit** coupling
- leads to an asymmetry in the angular distribution of final state particles (**Collins effect**) NPB 396,161(1993)
- first non-zero Collins effect observed in SIDIS PRL 94,012002(2005)
NPB 765, 31(2007)

In e^+e^- annihilation, γ^* (spin-1) \rightarrow spin-1/2 q and \bar{q}

- in a given event, the spin directions are unknown, but they must be parallel
- they have a polarization component transverse to the q direction $\sim \sin^2\theta$ (θ wrt the e^+e^-)
- exploit this correlation by using hadrons in opposite jets

$$e^+e^- \rightarrow q\bar{q} \rightarrow \pi_1\pi_2 X \quad (q=u, d, s) \implies \sigma \propto \cos(\phi_i) H_1^\perp(z_1) \otimes H_1^\perp(z_2),$$

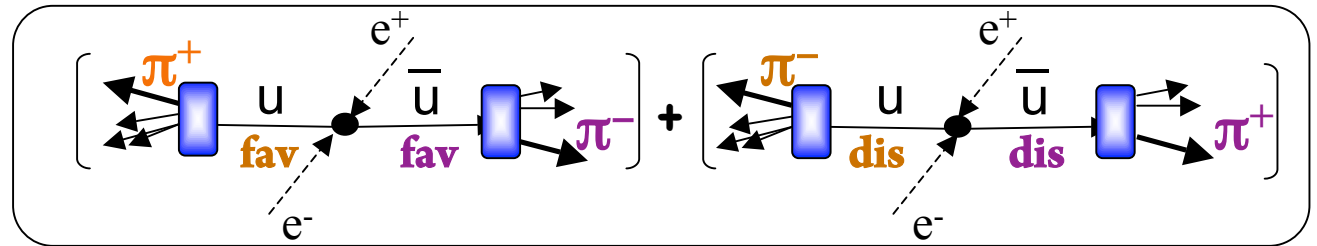
Favored and Disfavored processes

$$e^+e^- \rightarrow q\bar{q} \rightarrow \pi_1^\pm \pi_2^\pm X \quad (q\bar{q} = u\bar{u}, d\bar{d}, s\bar{s})$$

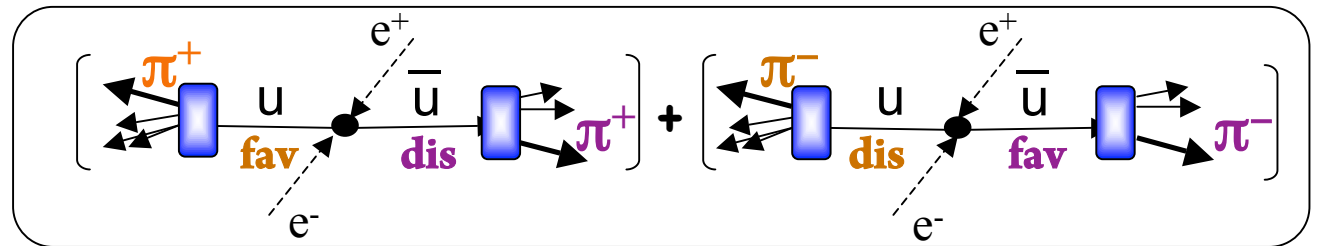
Different combinations of charged pions \Rightarrow sensitivity to **favored** or **disfavored** FFs

- **favored** fragmentation process describes the fragmentation of a quark of flavor q into a hadron with a valence quark of the same flavor: i.e.: $u \rightarrow \pi^+$, $d \rightarrow \pi^-$
- **disfavored** for $d \rightarrow \pi^+$, $u \rightarrow \pi^-$, and $s \rightarrow \pi^\pm$

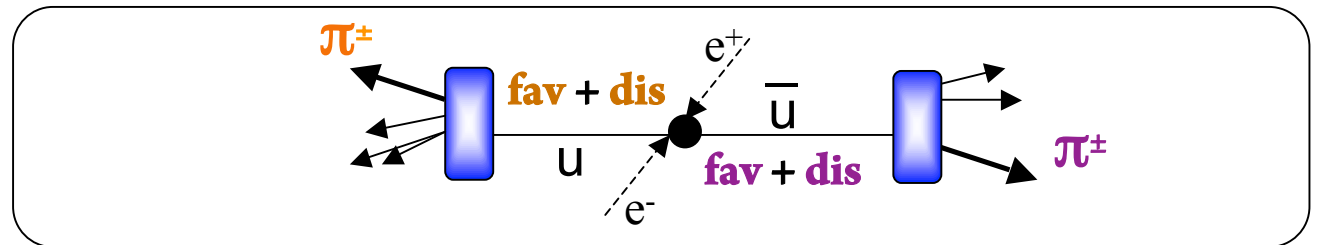
Unlike-sign pion pair = **U**:
 $\pi^+ \pi^-$: (**fav** x **fav**) + (**dis** x **dis**)



Like-sign pion pair = **L**:
 $\pi^\pm \pi^\pm$: (**fav** x **dis**) + (**dis** x **fav**)

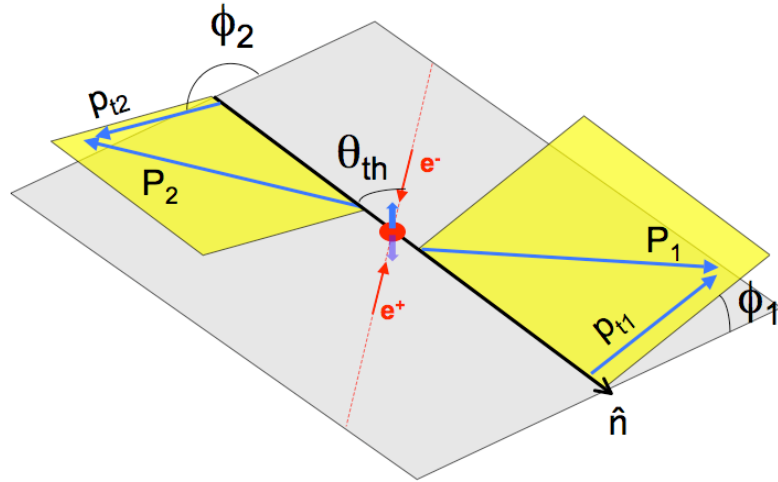


Charged pion pair = **C (U+L)**:
 $\pi\pi$: (**fav** + **dis**) x (**fav** + **dis**)
 $\pi = \pi^\pm$



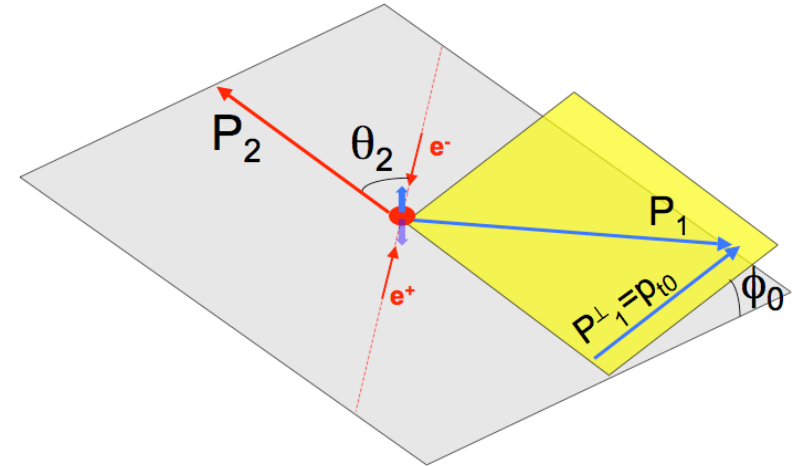
Analysis Reference Frame (RF)

RF12 or Thrust RF



$$\sigma \sim 1 + \frac{\sin^2 \theta_{th}}{1 + \cos^2 \theta_{th}} \cos(\phi_1 + \phi_2) \frac{H_1^\perp(z_1) \bar{H}_1^\perp(z_2)}{D_1(z_1) \bar{D}_1(z_2)}$$

RF0 or Second hadron RF



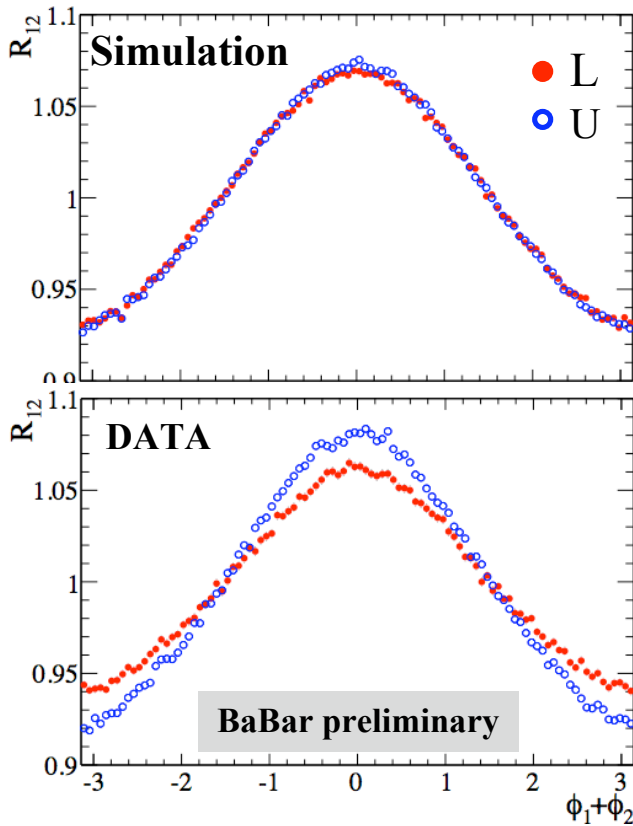
$$\sigma \sim 1 + \frac{\sin^2 \theta_2}{1 + \cos^2 \theta_2} \cos(2\phi_0) \mathcal{F} \left[\frac{H_1^\perp(z_1) \bar{H}_1^\perp(z_2)}{D_1(z_1) \bar{D}_1(z_2)} \right]$$

All quantities in e^+e^- center of mass

[See NPB 806, 23 (2009)]

- Selection of hadronic events:
 - number of well-reconstructed charged tracks > 2 from the interaction point
- Selection of two-jet topology events: **thrust** >0.8
- Selection of pions in the detector acceptance region: $0.41 < \theta_{lab} < 2.54$ rad
- Pion fractional energies: **$0.15 < z = 2E_h/\sqrt{s} < 0.9$**

Raw asymmetries and double ratios



- **Collins asymmetry:**

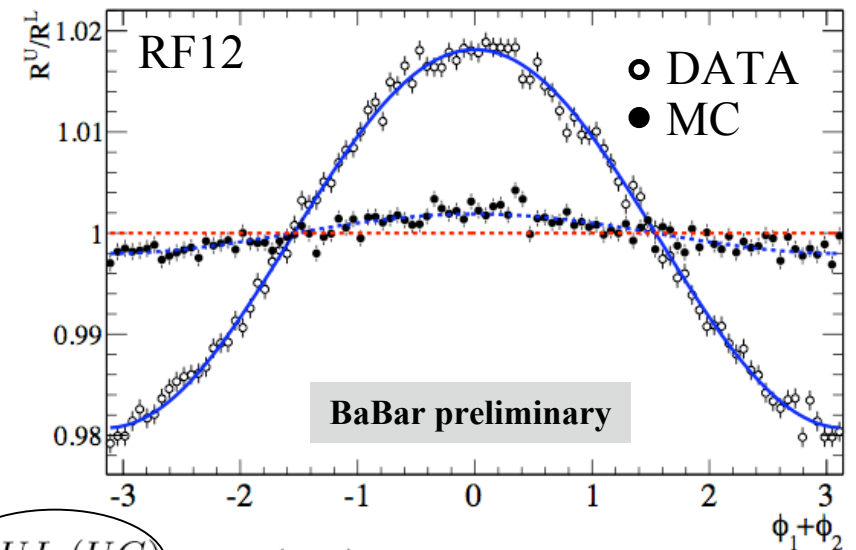
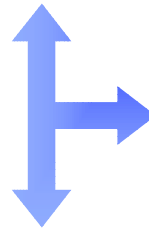
- consider all the **U** (unlike) and **L** (like) sign pion pairs
- make histograms of $\phi_\alpha = \phi_1 + \phi_2$ or $2\phi_0$ ($\alpha=12,0$)

- **The MC generator (JETSET) does not include the Collins effect**

→ flat distribution is expected

- strong modulation due to acceptance of the detector
- but similar distribution for **U** and **L** pairs

• Data shows difference between U and L distributions, that can be ascribed to the **Collins effect**



Acceptance effects can be reduced by performing the ratio of **U/L** sign pion pairs (or **U/C**):

- MC: consistent with a flat distribution
- Data: cosine modulation clearly visible

$$\frac{R_\alpha^U}{R_\alpha^{L(C)}} = \frac{N^U(\phi_\alpha) / \langle N^U(\phi_\alpha) \rangle}{N^{L(C)}(\phi_\alpha) / \langle N^{L(C)}(\phi_\alpha) \rangle} \rightarrow B_\alpha^{UL(UC)} + A_\alpha^{UL(UC)} \cdot \cos(\phi_\alpha)$$

Asymmetry binning and corrections

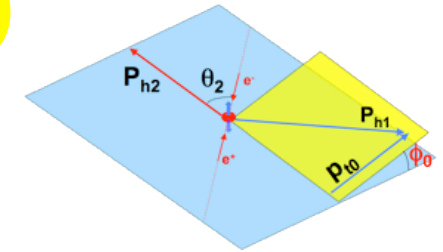
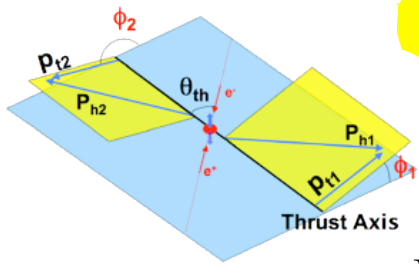
- The Collins effect is expected to depend on z_1, z_2, p_{t1}, p_{t2} (or p_{t0}), as well as $\cos\theta_{th}$ (or $\cos\theta_2$)
 \Rightarrow analyze in bins of these quantities
- Simulated asymmetries also depend on these quantities \rightarrow must correct in each bin independently
 \Rightarrow Systematic on MC value evaluated by varying track selection/acceptance
- **Asymmetry dilution due to the thrust axis approximation.** The corrections in the RF12 frame range between 1.3-2.3 as a function of z , and between 1.3-3 as a function of p_t
 \Rightarrow No correction needed in the RF0 frame
- **Contribution of background events to the asymmetries:**
 - $B\bar{B}$ events (very small, mostly at low z)
 - $\tau^+\tau^-$ events (small, important only at high z)
 - $C\bar{C}$ events (important at low/medium z) \Rightarrow contribution of about 30% on average
 - We used a **$D^{*\pm}$ -enhanced control sample** to estimate its effect

$$A_{\alpha}^{meas} = (1 - F_c - F_B - F_{\tau}) \cdot A_{\alpha} + F_c \cdot A_{\alpha}^{ch}$$

$$A_{\alpha}^{D^*} = f_c \cdot A_{\alpha}^{ch} + (1 - f_c - f_B) \cdot A_{\alpha}$$

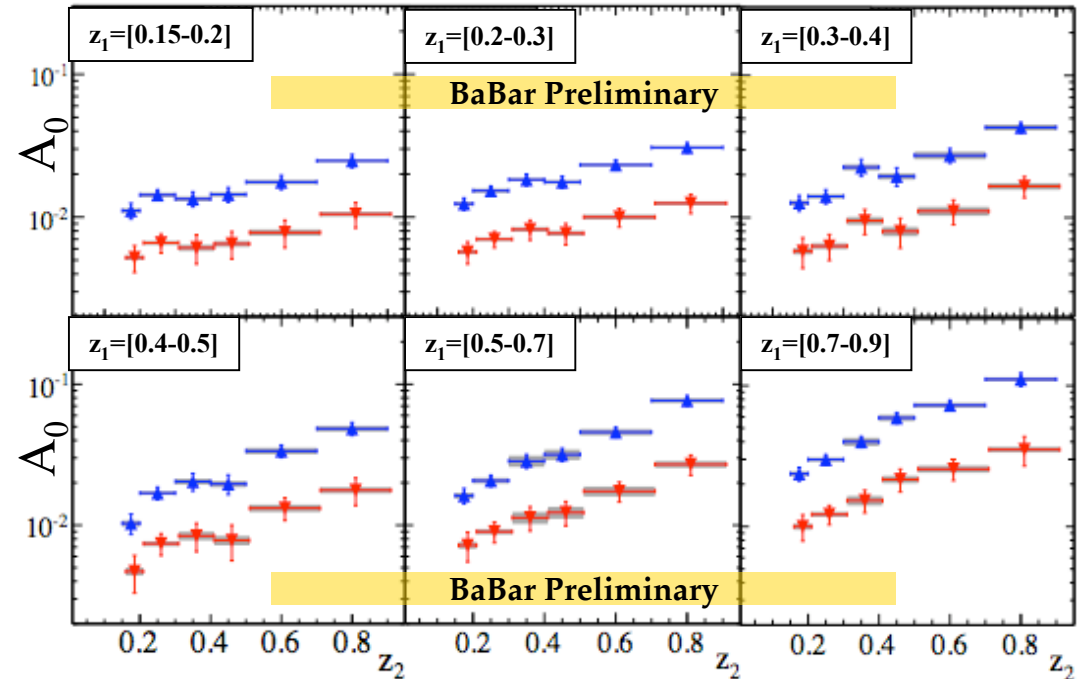
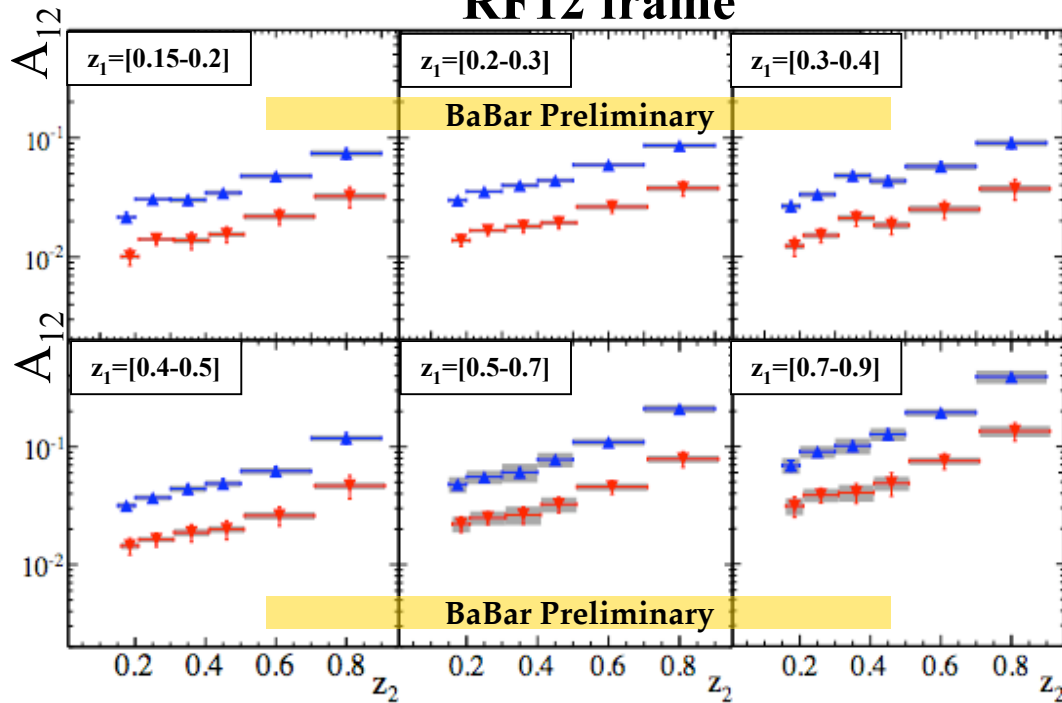
- F_i using MC samples
- $A^{B\bar{B}} = 0$
- A^{τ} small in simulation; checked in data; we set $A^{\tau} = 0$

Results: $A_{12,0}$ vs. (z_1, z_2)



RF12 frame

RF0 frame



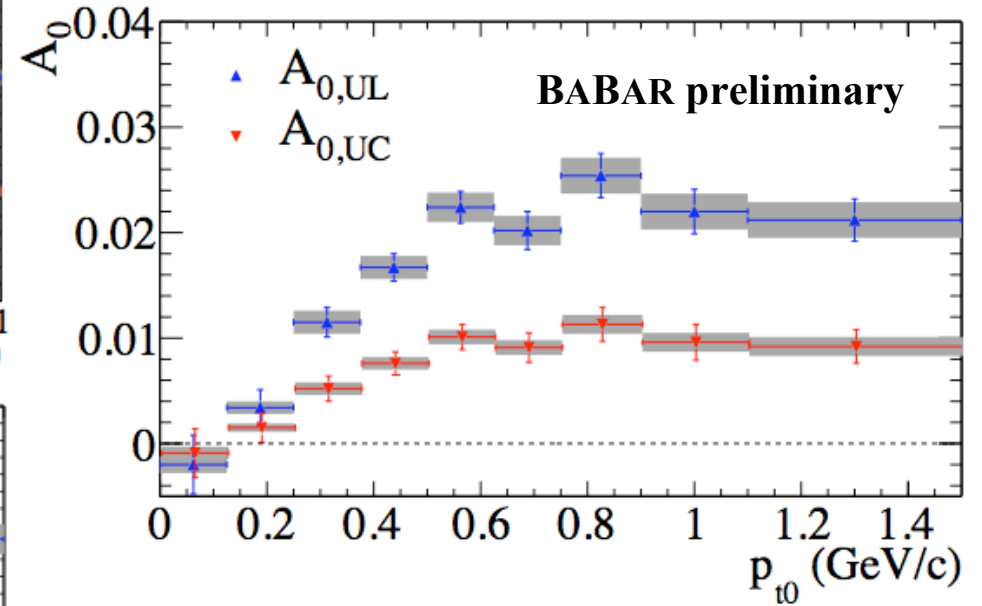
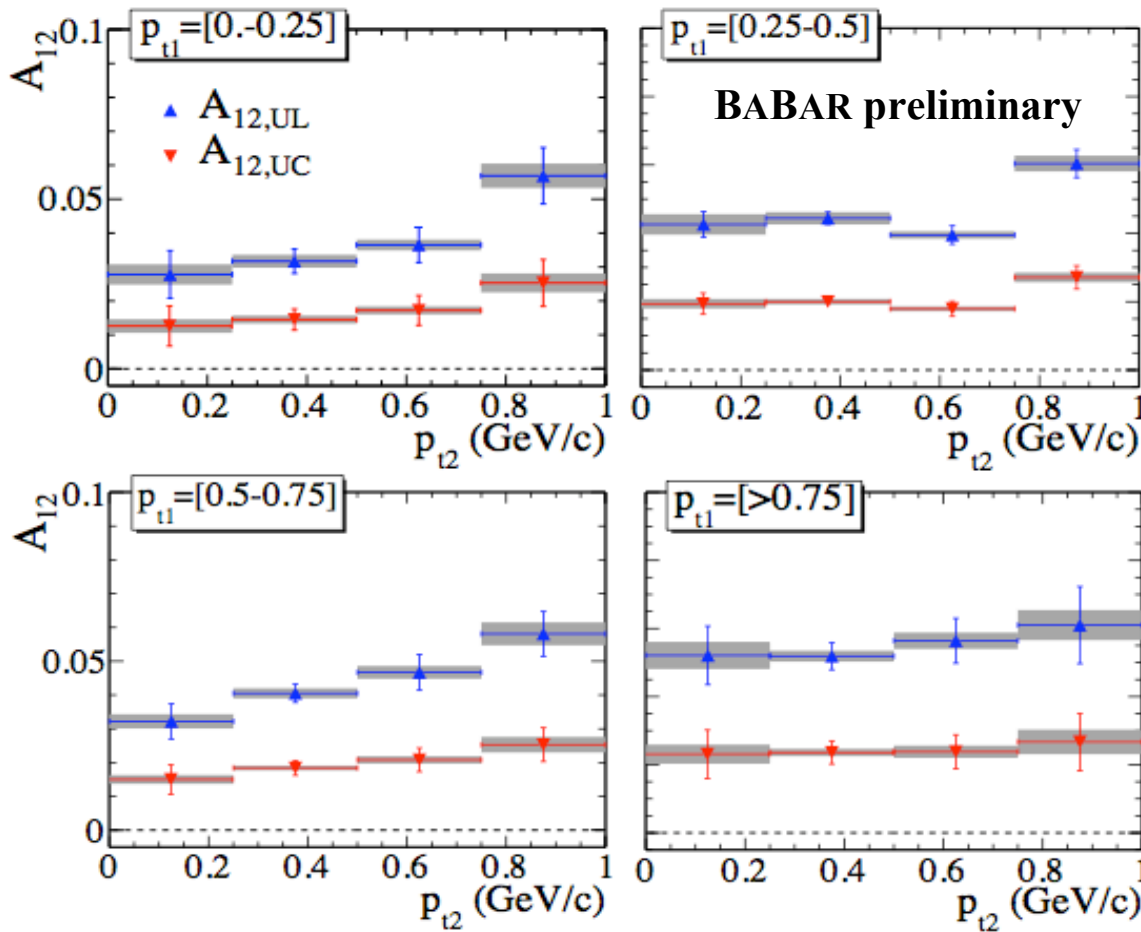
- **Very significant non-zero A^{UL} and A^{UC} in all bins**

- ⇒ strong dependence on (z_1, z_2) : $A_{12} \sim 1-39\%$, $A_0 \sim 0.5-11\%$

- ⇒ $A^{UC} < A^{UL}$ as expected; complementary information about the favored and disfavored fragmentation processes (PRD 73, 094025 (2006))

- ⇒ consistent with $z_1 \Leftrightarrow z_2$ symmetry

Results: A_{12} vs. (p_{t1}, p_{t2}) ; A_0 vs. p_{t0}



FIRST MEASUREMENT of Collins asymmetries vs. p_t in e^+e^- annihilation at $Q^2 \sim 110$ (GeV/c)²

- **non-zero A^{UL} and A^{UC}**

- \Rightarrow only modest dependence on (p_{t1}, p_{t2}) ; disagreement with the expectation ???

- $\Rightarrow A^{UC} < A^{UL}$; complementary information on $H_1^{\perp, fav}$ and $H_1^{\perp, dis}$

- $\Rightarrow A_0 < A_{12}$, but interesting structure in p_t

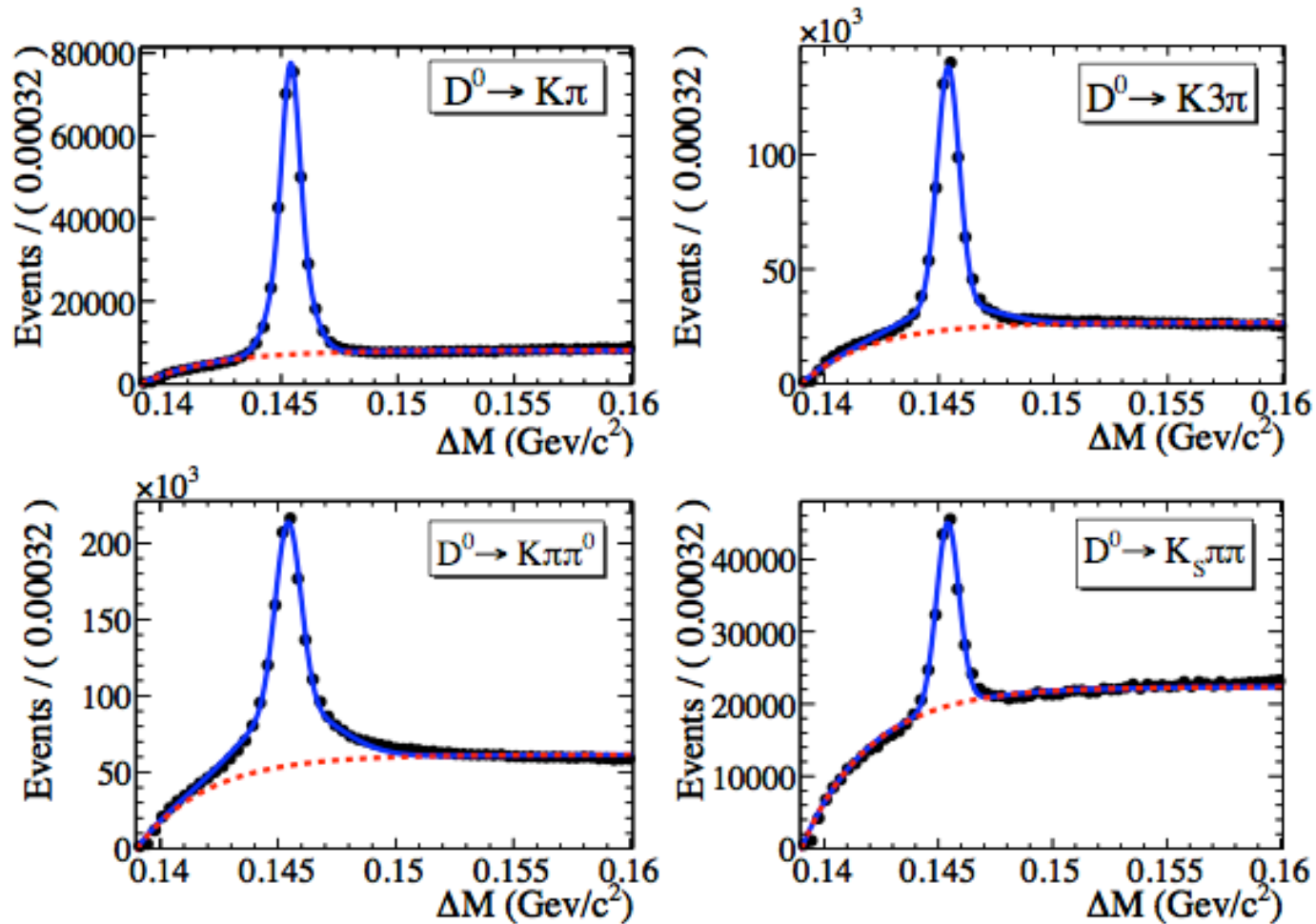
Summary and conclusions

- Measurement of the inclusive spectra for π^\pm , K^\pm , and p/\bar{p} hadrons in e^+e^- annihilation at the center of mass energy of 10.54 GeV at BABAR ([PRD 88,032011\(2013\)](#))
 - precise data at high x_p
 - consistent with ARGUS data
 - shape consistent with Belle results
 - Scaling properties:
 - no models predict the correct scaling properties for protons
- Collins effect for light quarks (uds) in two different reference frames (RF12 and RF0)
 - submitted to PRD ([arXiv:1309.5278](#))
 - A_{12} and A_0 increase with increasing z_1, z_2
 - consistent with theoretical expectations
 - general agreement with Belle results (PRD 86, 039905(E) (2012))
 - A_{12} (A_0) increases with p_{t1}, p_{t2} (p_{t0}) for $0 < p_t < 1$ GeV/c
 - first measurement in e^+e^- annihilation at $Q^2 \sim 110$ (GeV/c)²
 - important for understanding the evolution of the fragmentation function

Thanks for your attention

BACKUP SLIDES

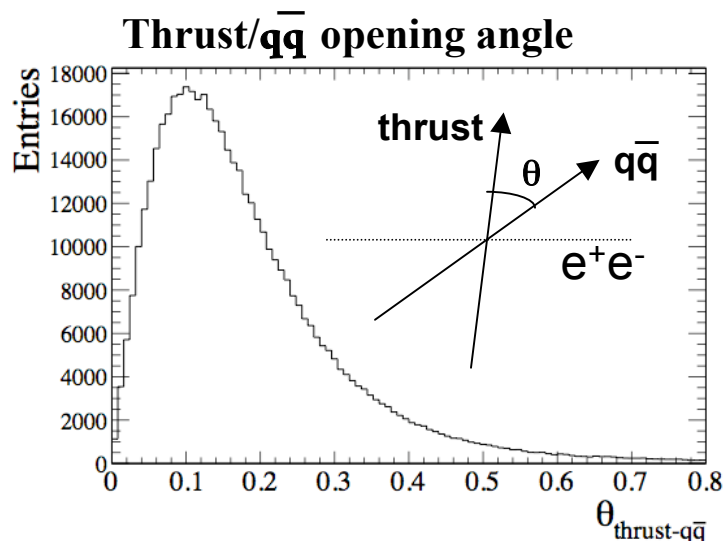
$D^{*\pm}$ -enhanced control sample



$D^{*\pm} \rightarrow D^0 \pi^\pm$, $D^0 \rightarrow K\pi$ (mode 1)
 $D^0 \rightarrow K3\pi$ (mode 2)
 $D^0 \rightarrow K\pi\pi^0$ (mode 3)
 $D^0 \rightarrow K_S \pi \pi$ (mode 4)

$1.835 < M_{D^0} < 1.895 \text{ GeV}/c^2$
 $0.1425 < \Delta M < 0.149 \text{ GeV}/c^2$
 $(\Delta M = M_{D^{*\pm}} - M_{D^0})$

Asymmetry dilution



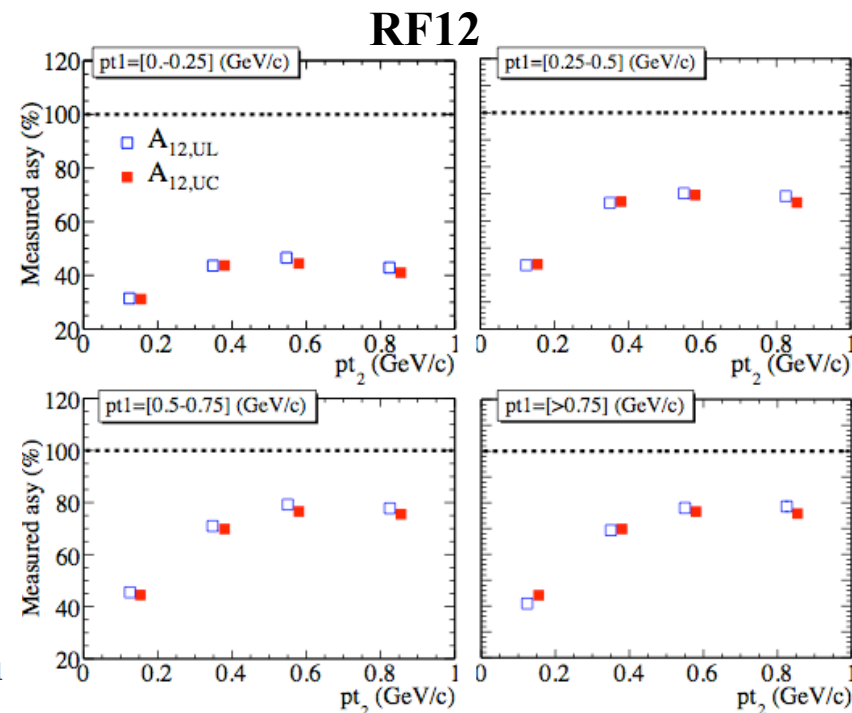
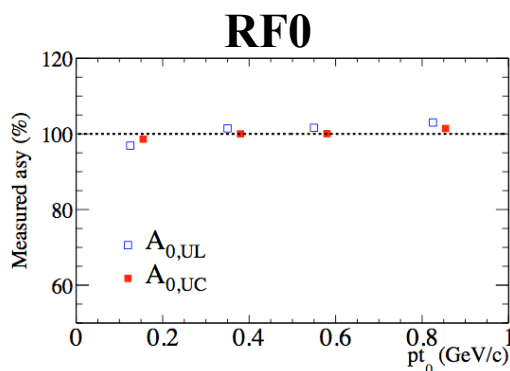
The experimental method assumes the thrust axis as $q\bar{q}$ direction: this is only a rough approximation

RF12: large smearing since the azimuthal angles ϕ_1 and ϕ_2 are calculated with respect to the thrust axis; additional dilution due to very energetic tracks close to the thrust axis.

RF0: the azimuthal angle ϕ_0 is calculated with respect to the second hadron momenta \rightarrow small smearing due to PID and tracking resolution.

\rightarrow We study the influence of the detector effects by correcting a posteriori the generated angular distribution: weights defined as $w^{UL(UC)} = 1 \pm a \cdot \cos(\phi_{gen12,0})$ are applied to every selected pion pairs.

RF12: correction performed for each bins of z and p_t :
 (1.3-2.3) as a function of z , and
 (1.3-3) as a function of p_t .
RF0: no correction needed.

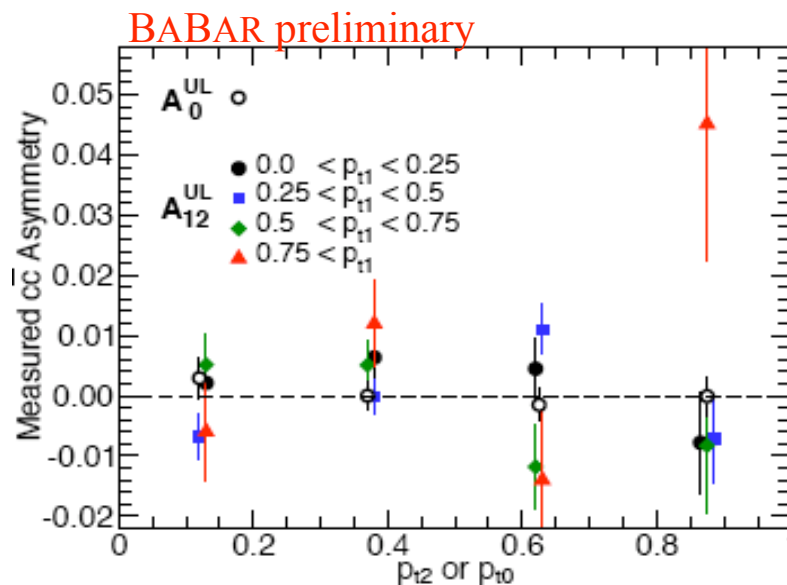
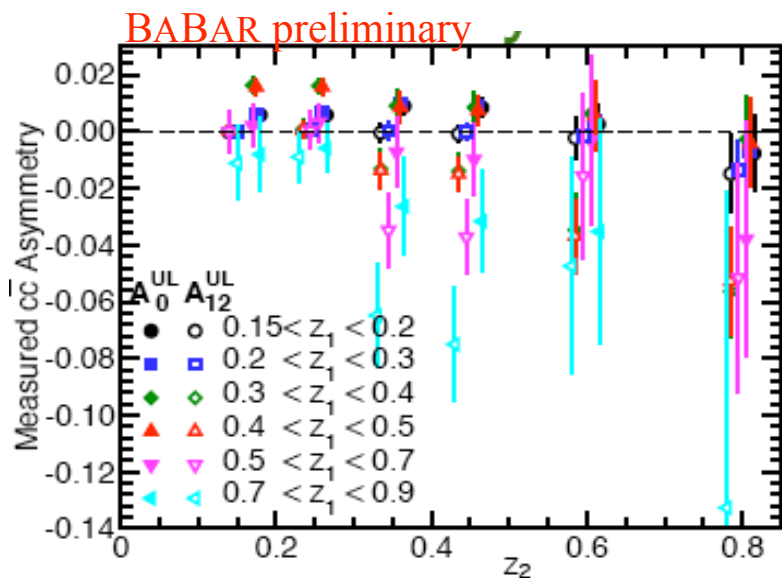


Extraction of the uds asymmetry

- Charm background contribution is about 30% on average
 - Both fragmentation processes and weak decays can introduce azimuthal asymmetries
 - We used a **D^{*±}-enhanced control sample** to estimate its effect on a **bin-by-bin basis**
 - 4 complementary decay modes D^{*±}→D⁰π[±], with D⁰→Kπ,K3π,Kππ⁰,K_sππ
 - mostly c \bar{c} events, some B \bar{B}
- Again, f_i from MC, data-MC difference as systematic error

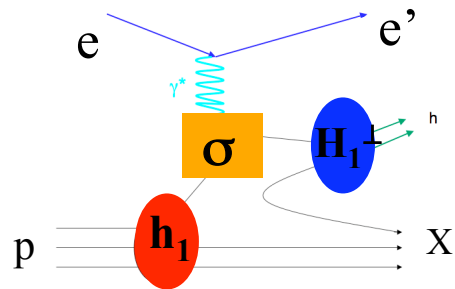
$$A_{\alpha}^{meas} = (1 - F_c - F_B - F_{\tau}) \cdot A_{\alpha} + F_c \cdot A_{\alpha}^{ch}$$

$$A_{\alpha}^{D^*} = f_c \cdot A_{\alpha}^{ch} + (1 - f_c - f_B) \cdot A_{\alpha}$$



• the A^{ch} are very small (slightly negative?)

Extraction of Collins FF from data



SIDIS

HERMES: PRL **94**, 012002 (2005)
 COMPASS: NP **B765**, 31 (2007)

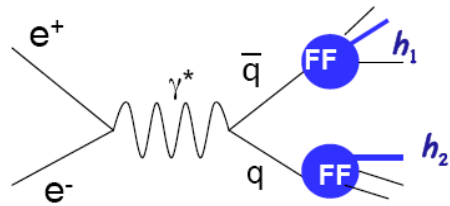
$$A_T \propto h_1(x_B) \otimes H_1^\perp(z)$$

+

e^+e^- annihilation

BELLE: PRL **96**, 232002(2006),
 PRD **78**, 03201 (2008)

$$A \propto H_1^\perp(z_1) \otimes H_1^\perp(z_2)$$



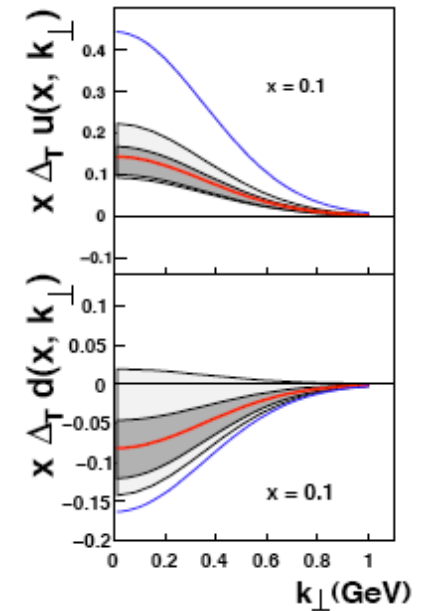
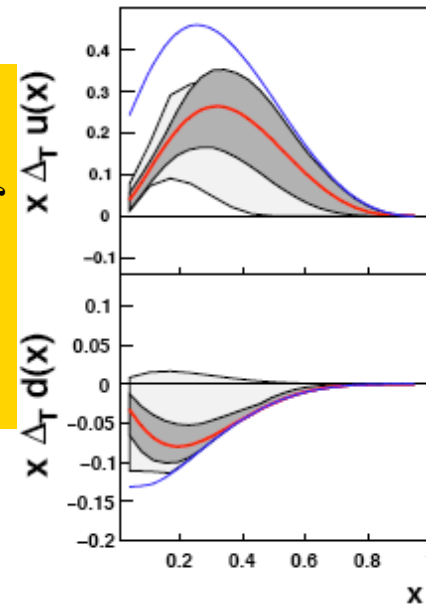
GLOBAL ANALYSIS: simultaneous determination of H_1^\perp and the transversity parton distribution function h_1

*Anselmino et al., PRD **75**, 054032(2007), NP Proc.Suppl. **191**, 98(2009)*

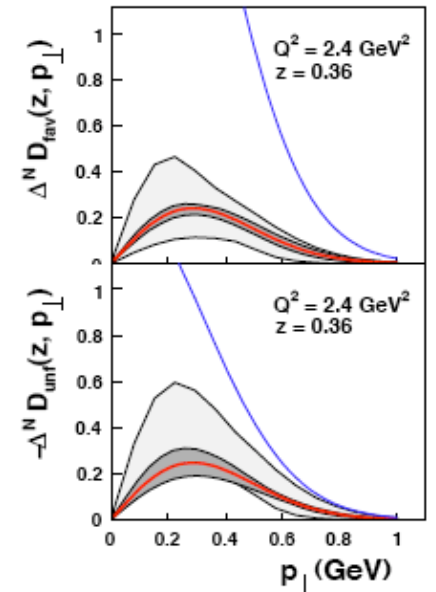
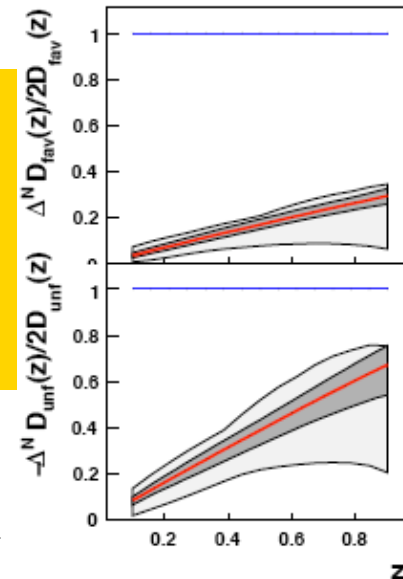
Improvements from BABAR studies:

- Increase in the number of pion fractional energy intervals
- Collins asymmetry behavior vs. pion transverse momenta

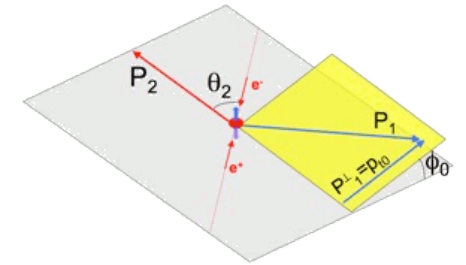
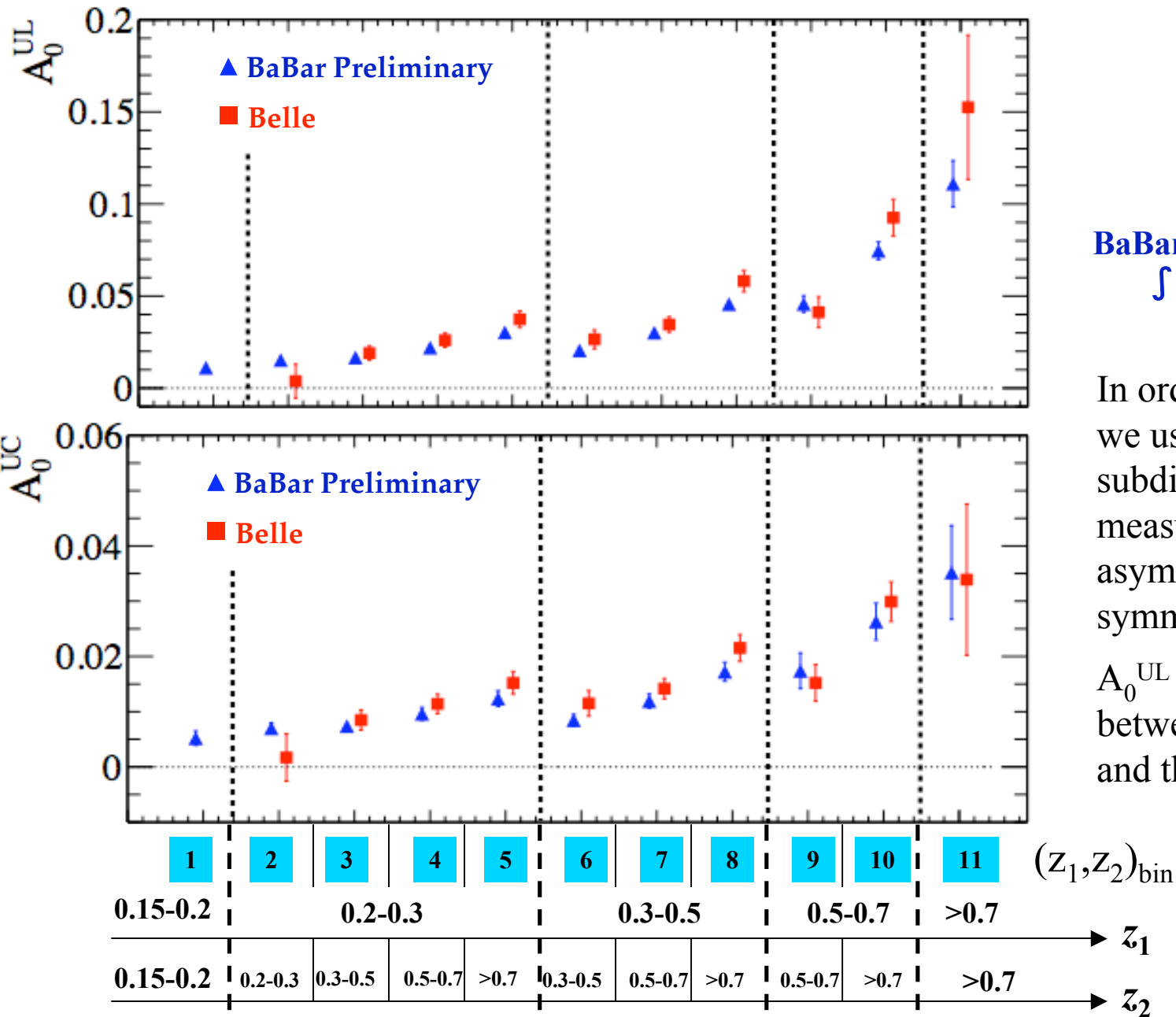
Transversity PDF



Collins FF



RFO: Comparison of BaBar/Belle asymmetries

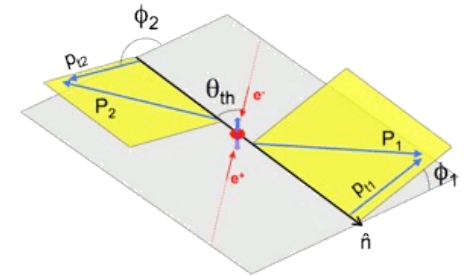
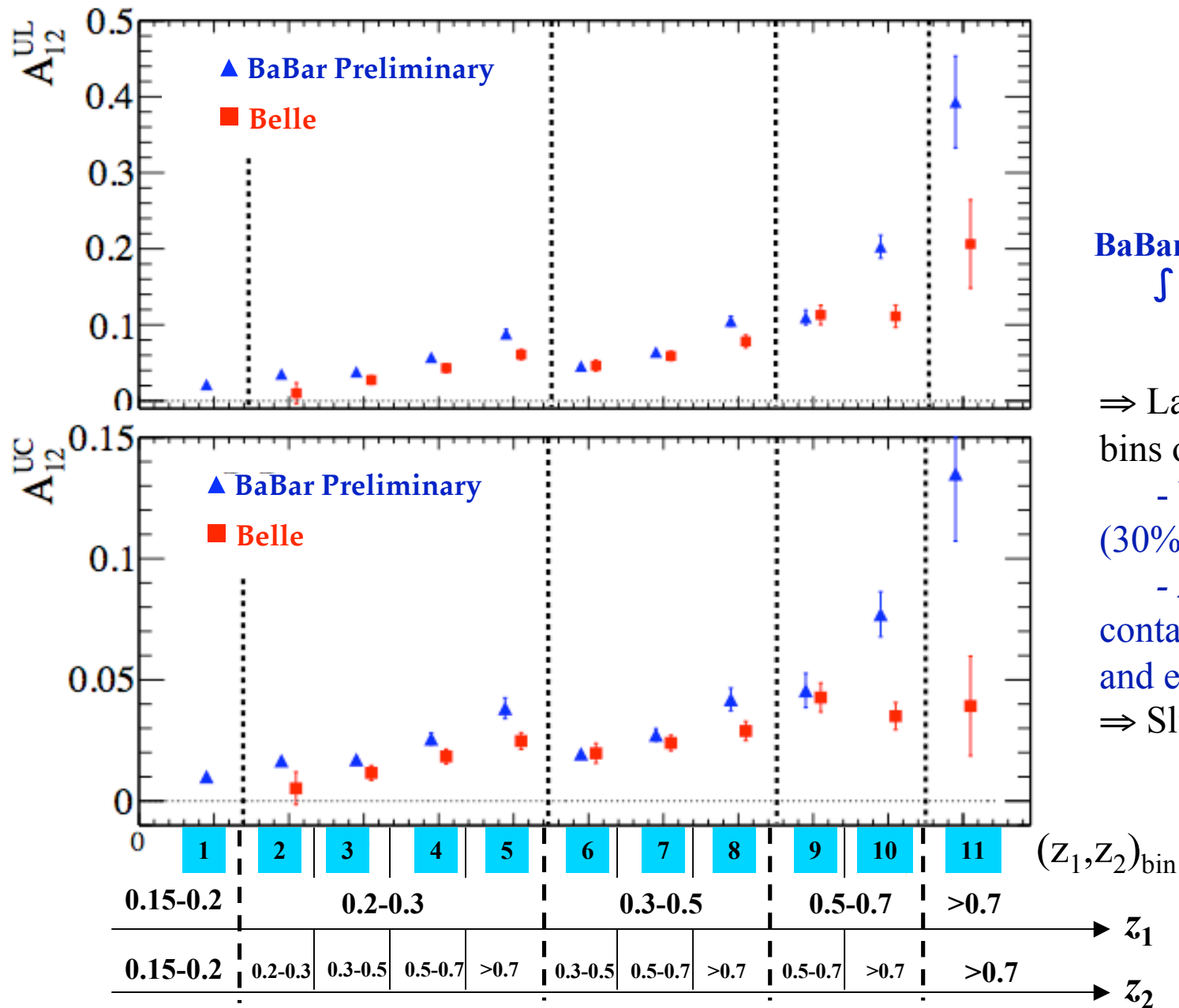


BaBar ($0.15 < z < 0.9$) **Belle** ($0.2 < z < 1$)
 $\int \mathcal{L} \sim 468 \text{ fb}^{-1}$ $\int \mathcal{L} \sim 547 \text{ fb}^{-1}$
 PRD 86, 039905(E) (2012)

In order to perform this comparison, we used 10 (+1) symmetrized z -bin subdivisions, averaging the measured Belle and BaBar asymmetries which fell in the same symmetric bins

A_0^{UL} and A_0^{UC} : good agreement between the **BaBar** asymmetries and the **Belle** results.

RF12: Comparison of BaBar/Belle asymmetries



BaBar ($0.15 < z < 0.9$) **Belle ($0.2 < z < 1$)**
 $\int \mathcal{L} \sim 468 \text{ fb}^{-1}$ $\int \mathcal{L} \sim 547 \text{ fb}^{-1}$
 PRD 86, 039905(E) (2012)

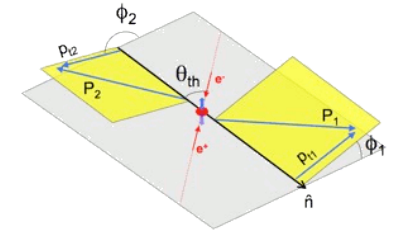
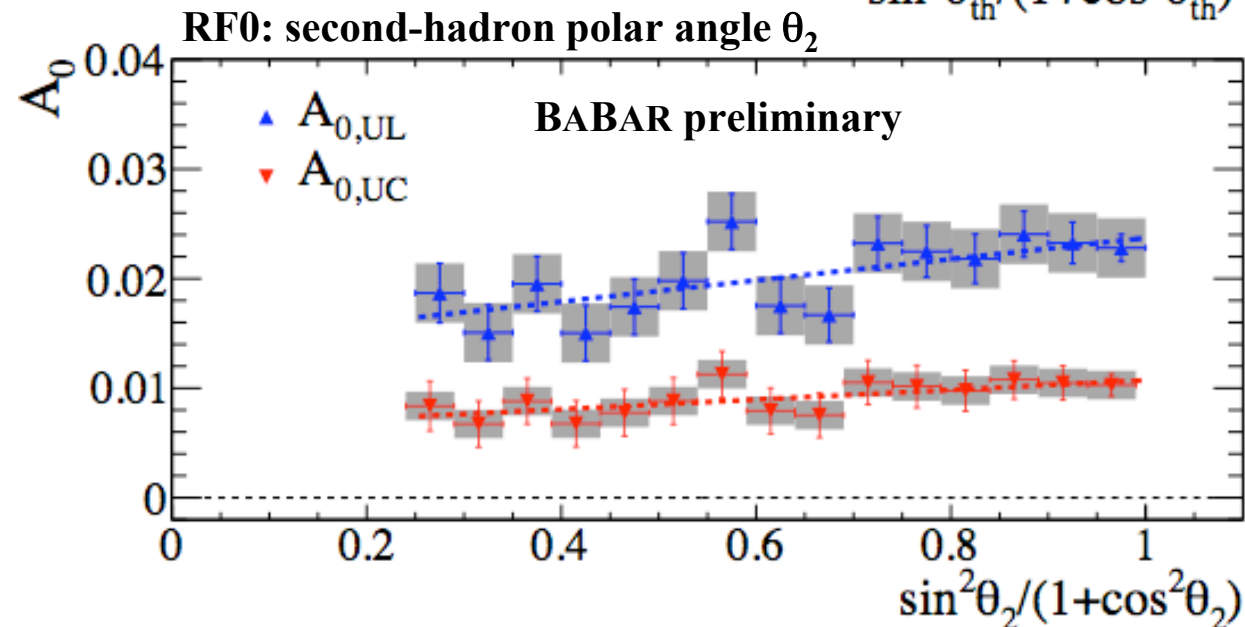
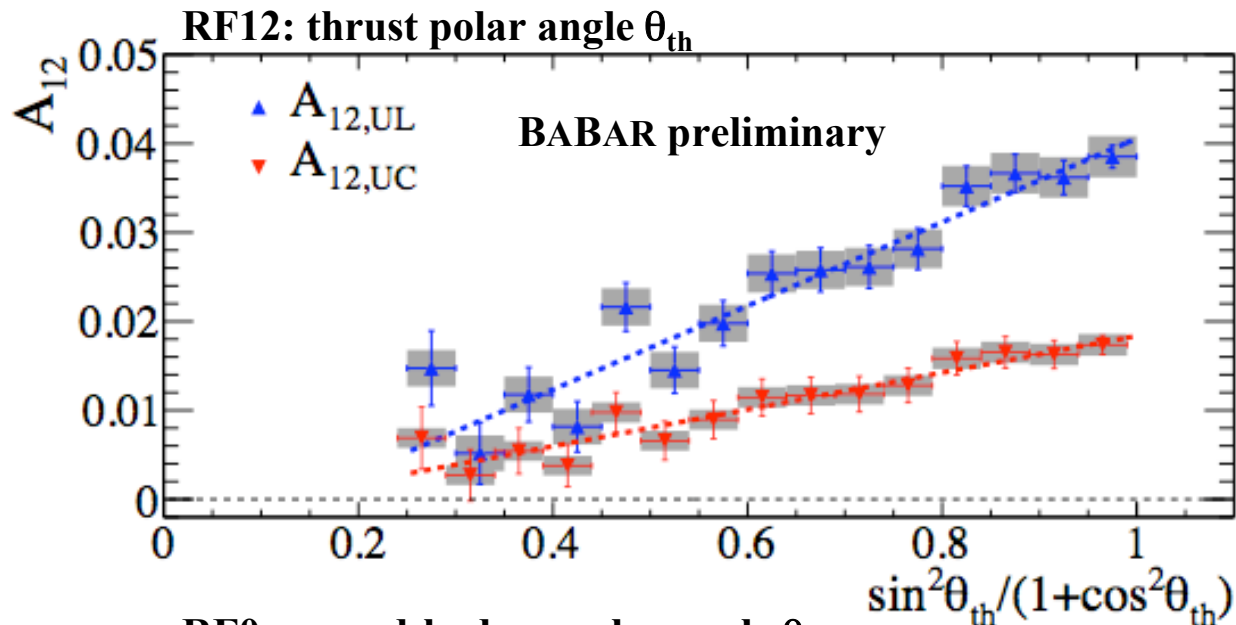
⇒ Large discrepancy in the last two bins of z :

- bin-by-bin correction factors (30%)

- $z < 0.9$ to remove the contamination from $\mu\mu\gamma$ background and exclusive events

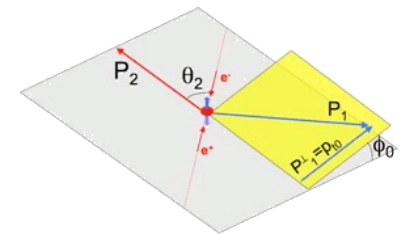
⇒ Slightly higher at lower z

Results: A_{12} vs. θ_{th} ; A_0 vs. θ_2



$$A_{12} \propto \frac{\sin^2 \theta_{th}}{1 + \cos^2 \theta_{th}} \cos(\phi_1 + \phi_2) \frac{H_1^\perp(z_1) \bar{H}_1^\perp(z_2)}{D_1(z_1) \bar{D}_1(z_2)}$$

==> Intercept consistent with zero, as expected (consistent with Belle results)



$$A_0 \propto \frac{\sin^2 \theta_2}{1 + \cos^2 \theta_2} \cos(2\phi_0) \mathcal{F} \left[\frac{H_1^\perp(z_1) \bar{H}_1^\perp(z_2)}{D_1(z_1) \bar{D}_1(z_2)} \right]$$

==> The linear fit gives a non-zero constant parameter \rightarrow the second hadron momentum provides a worse estimation of the $q\bar{q}$ direction (consistent with Belle results)