

Anno 2012 Protocollo: RBFR12JF2Z





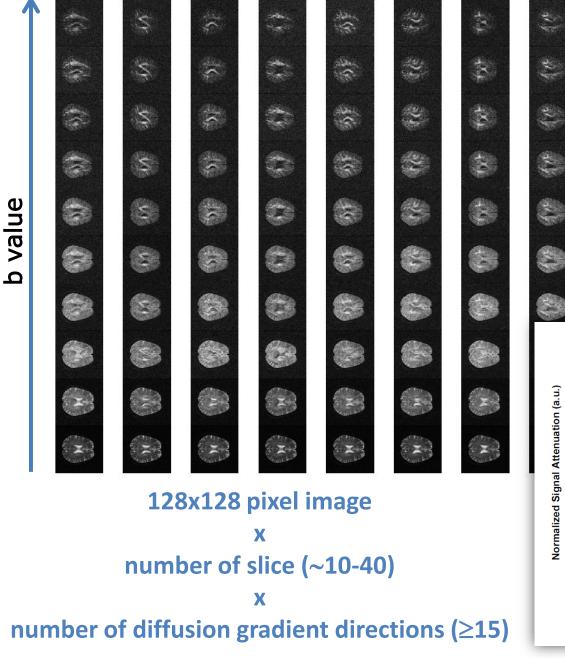
Unità A2: Imaging NMR, Roma

Accelerazione della ricostruzione di immagini NMR ottenute con il metodo del contrasto in diffusione

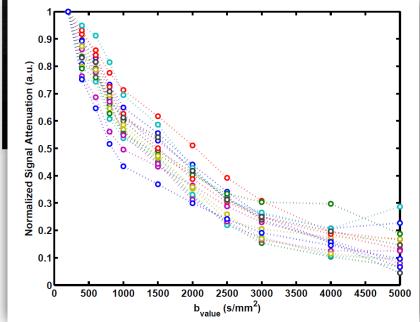
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direction



Typical NMR imaging post-processing



Cumulant expansion approach: kurtosis tensor measurement

$$S(b) \propto e^{-D_{app}b + \frac{1}{6}K_{app}[D_{app}b]^{2} + \dots}$$

$$S(b) = S(0) \exp\left[-b\sum_{i,j}n_{i}n_{j}D_{ij} + \frac{1}{6}b^{2}\left(\frac{1}{3}\sum_{i}D_{ii}\right)^{2}\sum_{i,j,k,l}n_{i}n_{j}n_{k}n_{l}W_{ijkl} + O(b^{3})\right]$$

$N \ge 15$ independent measures to get W_{ijkl}

$$K(\mathbf{n}) = \frac{\overline{D}^2}{\left[D(\mathbf{n})\right]^2} \sum_{i,j,k,l=1}^3 n_i n_j n_k n_l W_{ijkl}. \qquad \blacksquare \qquad MK = \frac{1}{N} \sum_{i=1}^N K(\mathbf{n}_i)$$

$$\begin{split} \overline{K} &= F_1(\lambda_1, \lambda_2, \lambda_3) \widetilde{W}_{1111} + F_1(\lambda_2, \lambda_1, \lambda_3) \widetilde{W}_{2222} \\ &+ F_1(\lambda_3, \lambda_2, \lambda_1) \widetilde{W}_{3333} + F_2(\lambda_1, \lambda_2, \lambda_3) \widetilde{W}_{2233} \\ &+ F_2(\lambda_2, \lambda_1, \lambda_3) \widetilde{W}_{1133} + F_2(\lambda_3, \lambda_2, \lambda_1) \widetilde{W}_{1122}, \end{split}$$

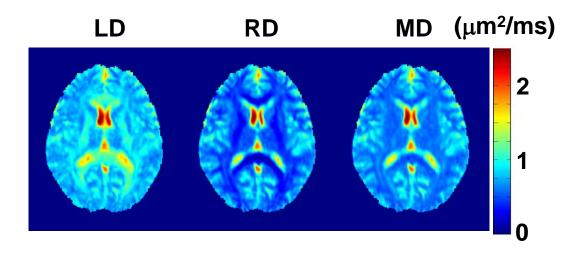
$$K_{\parallel} = \frac{\left(\lambda_1 + \lambda_2 + \lambda_3\right)^2}{9\lambda_1^2} \tilde{W}_{1111},$$

$$\begin{split} \mathcal{K}_{\perp} &= \mathcal{G}_1(\lambda_1,\lambda_2,\lambda_3) \tilde{W}_{2222} + \mathcal{G}_1(\lambda_1,\lambda_3,\lambda_2) \tilde{W}_{3333} \\ &+ \mathcal{G}_2(\lambda_1,\lambda_2,\lambda_3) \tilde{W}_{2233}, \end{split}$$

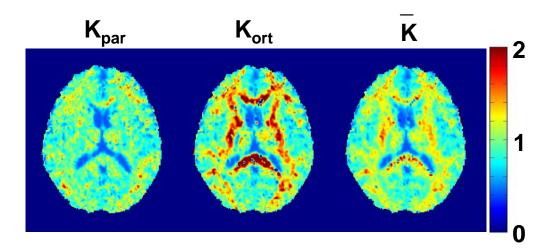
$$\begin{split} G_1(\lambda_1,\lambda_2,\lambda_3) &= \frac{\left(\lambda_1+\lambda_2+\lambda_3\right)^2}{18\lambda_2(\lambda_2-\lambda_3)^2} \bigg(2\lambda_2+\frac{\lambda_3^2-3\lambda_2\lambda_3}{\sqrt{\lambda_2\lambda_3}}\bigg),\\ G_2(\lambda_1,\lambda_2,\lambda_3) &= \frac{\left(\lambda_1+\lambda_2+\lambda_3\right)^2}{3\left(\lambda_2-\lambda_3\right)^2} \bigg(\frac{\lambda_2+\lambda_3}{\sqrt{\lambda_2\lambda_3}}-2\bigg). \end{split}$$

$$F_{1}(\lambda_{1},\lambda_{2},\lambda_{3}) \equiv \frac{(\lambda_{1}+\lambda_{2}+\lambda_{3})^{2}}{18(\lambda_{1}-\lambda_{2})(\lambda_{1}-\lambda_{3})} \left[\frac{\sqrt{\lambda_{2}\lambda_{3}}}{\lambda_{1}} R_{F}\left(\frac{\lambda_{1}}{\lambda_{2}},\frac{\lambda_{1}}{\lambda_{3}},1\right) + \frac{3\lambda_{1}^{2}-\lambda_{1}\lambda_{2}-\lambda_{2}\lambda_{3}-\lambda_{1}\lambda_{3}}{3\lambda_{1}\sqrt{\lambda_{2}\lambda_{3}}} R_{D}\left(\frac{\lambda_{1}}{\lambda_{2}},\frac{\lambda_{1}}{\lambda_{3}},1\right) - 1 \right],$$
and

$$F_{2}(\lambda_{1},\lambda_{2},\lambda_{3}) \equiv \frac{(\lambda_{1}+\lambda_{2}+\lambda_{3})^{2}}{3(\lambda_{2}-\lambda_{3})^{2}} \left[\frac{\lambda_{2}+\lambda_{3}}{\sqrt{\lambda_{2}\lambda_{3}}} R_{F}\left(\frac{\lambda_{1}}{\lambda_{2}},\frac{\lambda_{1}}{\lambda_{3}},1\right) + \frac{2\lambda_{1}-\lambda_{2}-\lambda_{3}}{3\sqrt{\lambda_{2}\lambda_{3}}} R_{D}\left(\frac{\lambda_{1}}{\lambda_{2}},\frac{\lambda_{1}}{\lambda_{3}},1\right) - 2 \right].$$



Conventional DTI 128x128x32x15 = 7.864320 10⁶ linear systems to solve ~ 15 s on CPU*



Kurtosis tensor imaging 128x128x32x15 = 7.864320 10⁶ non-linear fit to perform ~7200 s on CPU*

* 8 threads on an Intel Xeon E5-2609 CPU at 2.4 GHz

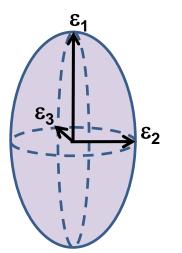
Stretched exponential model

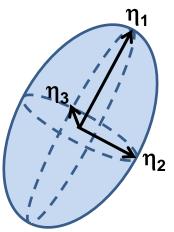
$$S(b) = S(0)e^{-A_1(b_1^*)^{\gamma_1} - A_2(b_2^*)^{\gamma_2} - A_3(b_3^*)^{\gamma_3}}$$

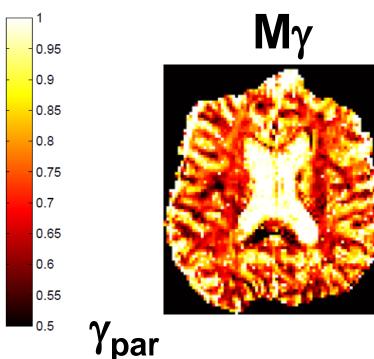
$$b_i^* = \vec{b} \cdot \vec{\eta}_i$$

Anomalous diffusion reference frame

DTI reference frame Anomalous Diffusion reference frame







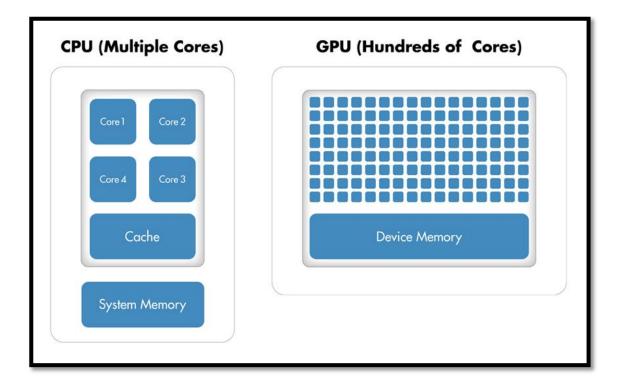
Conventional DTI 128x128x32x15 = 7.864320 10⁶ linear systems to solve ~ 15 s on CPU*

Stretched exponential imaging 128x128x32x15 = 7.864320 10⁶ non-linear fit to perform ~6600 s on CPU*

Yort

* 8 threads on an Intel Xeon E5-2609 CPU at 2.4 GHz

When GPU can accelerate an application



• Computationally intensive — The time spent on computation significantly exceeds the time spent on transferring data to and from GPU memory.

• Massively parallel — The computations can be broken down into hundreds or thousands of independent units of work.

Computationally intensive

Kurtosis tensor imaging non-linear fit ~7 ms per pixel vs ~ 10-80 ns to read data from memory

Stretched exponential imaging non-linear fit ~6 ms per pixel vs ~10-80 ns to read data from memory

Massively parallel

Kurtosis tensor imaging ~10⁶-10⁷ independent nonlinear fit

Stretched exponential imaging 10⁶-10⁷ **independent** nonlinear fit

Exemple: GPU acceleration of the solution of a wave equation in 2D*

$$\frac{\partial^2 u}{\partial t^2} = \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2}$$

Solution in space Chebyshev spectral method

Solution in time

Second-order central finite difference method (leap-frog method)

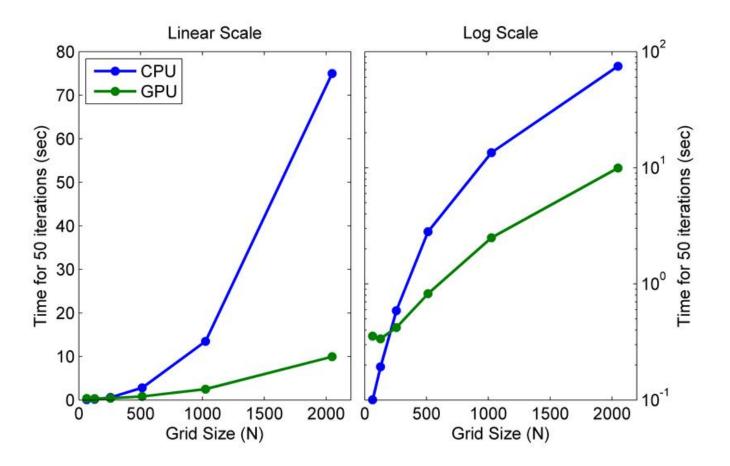
2048 x 2048 grid x 50 iterations ~ 80 s on CPU^{\$}

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* from:

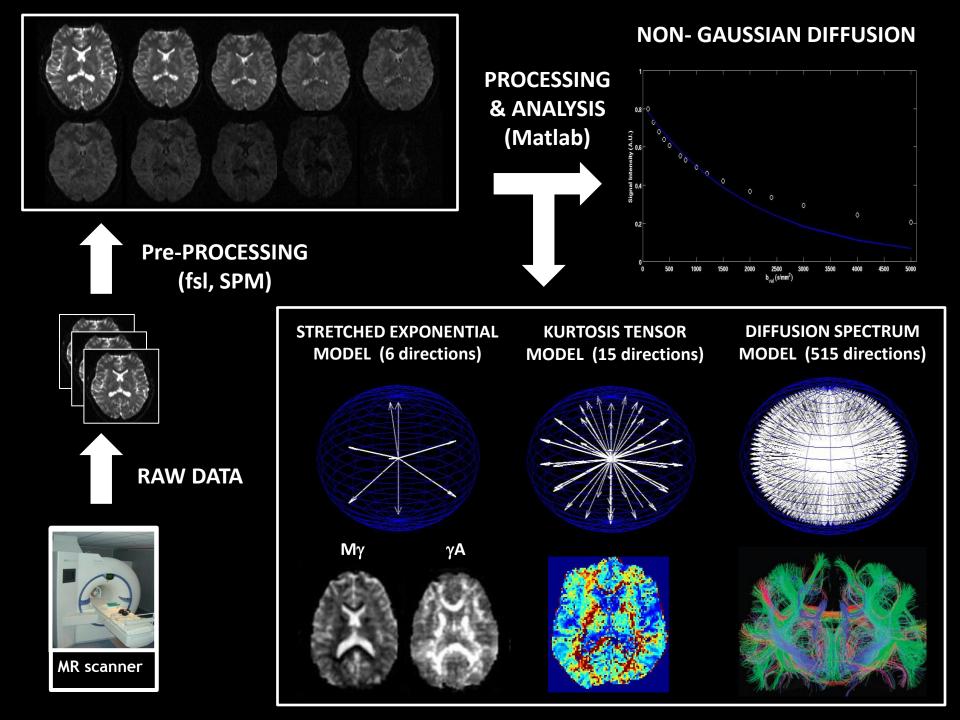
http://www.mathworks.it/company/newsletters/articles/qpu-programming-in-matlab.html \$ 12 thread on an Intel Xeon X5650 CPU at 2.66 GHz

By using GPU acceleration* 7.5x decrease in compute time 2048 x 2048 grid x 50 iterations ~ 10 s on GPU^{\$}



* from:

<u>http://www.mathworks.it/company/newsletters/articles/qpu-programming-in-matlab.html</u> \$ NVIDIA Tesla C2050 GPU with 448 CUDA cores at 1.15 GHz



• Development of highly parallelized non-conventional NMR image processing algorithms;

DONE

Non-conventional NMR image processing algorithms code optimization;

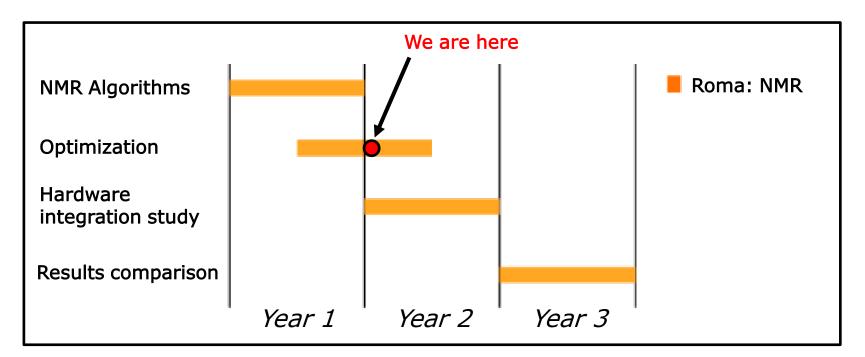
PARTIALLY DONE

• Algorithms porting on GPU and hardware integration study;

LESS THAN 1 YEAR REQUIRED

Results comparison.

LESS THAN 1 YEAR REQUIRED



• Development of highly parallelized non-conventional NMR image processing algorithms;

DONE

Non-conventional NMR image processing algorithms code optimization;

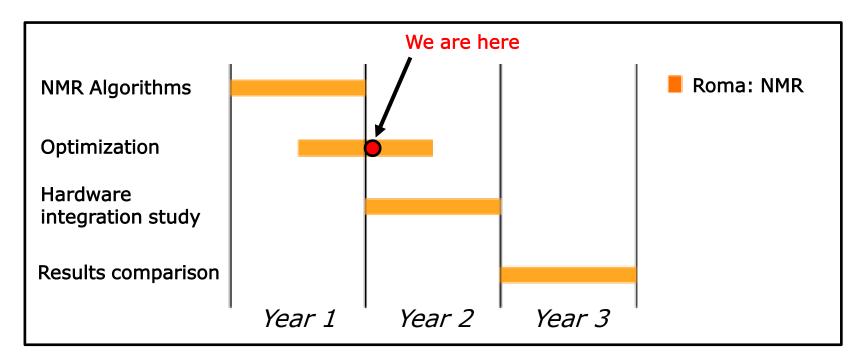
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