EFFECTIVE LAGRANGIAN FOR A LIGHT HIGGS

OR: HOW TO LOOK FOR NEW PHYSICS BY STUDYING THE HIGGS BOSON IN A MODEL-INDEPENDENT WAY

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based on R.C., Ghezzi, Grojean, Muehlleitner, Spira arXiv:1303.3876

In absence of a direct observation of new particles, our ignorance of the EWSB sector can be parametrized in terms of an effective Lagrangian

- The explicit form of the Lagrangian depends on the assumptions one makes
- If new particles are discovered they can be included in the Lagrangian in a bottom-up approach

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I WILL ASSUME:

- 1) $SU(2)_L x U(1)_Y$ is linearly realized at high energies
- 2) h(x) is a scalar (CP even) and is part of an SU(2)_L doublet H(x)
- 3) The EWSB dynamics has an (approximate) custodial symmetry global symmetry includes: $SU(2)_L \times SU(2)_R \rightarrow SU(2)_V$

Effective Lagrangian for a Higgs doublet

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_{i} \bar{c}_{i} O_{i} \equiv \mathcal{L}_{SM} + \Delta \mathcal{L}_{SILH} + \Delta \mathcal{L}_{F_{1}} + \Delta \mathcal{L}_{F_{2}}$$

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dimension-6 operators (only those relevant for Higgs physics)

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dimension-6 operators (only those relevant for Higgs physics)

The list of dim=6 operators of the effective Lagrangian has been known in the literature since long time

Buchmuller and Wyler NPB 268 (1986) 621

<u>Minimal</u> and complete list fist appeared in:

Grzadkowski et al. JHEP 1010 (2010) 085

I will follow the parametrization and the analysis of:

Giudice, Grojean, Pomarol, Rattazzi JHEP 0706 (2007) 045

$$\begin{split} \Delta \mathcal{L}_{SILH} &= \frac{\bar{c}_H}{2v^2} \,\partial^\mu \big(H^\dagger H \big) \,\partial_\mu \big(H^\dagger H \big) + \frac{\bar{c}_T}{2v^2} \, \Big(H^\dagger \overleftrightarrow{D^\mu} H \Big) \Big(H^\dagger \overleftrightarrow{D}_\mu H \Big) - \frac{\bar{c}_6 \,\lambda}{v^2} \, \big(H^\dagger H \big)^3 \\ &+ \Big(\frac{\bar{c}_u}{v^2} \, y_u \, H^\dagger H \, \bar{q}_L H^c u_R + \frac{\bar{c}_d}{v^2} \, y_d \, H^\dagger H \, \bar{q}_L H d_R + \frac{\bar{c}_l}{v^2} \, y_l \, H^\dagger H \, \bar{L}_L H l_R + h.c. \Big) \\ &+ \frac{i \bar{c}_W \, g}{2m_W^2} \, \Big(H^\dagger \sigma^i \overleftrightarrow{D^\mu} H \Big) \, (D^\nu W_{\mu\nu})^i + \frac{i \bar{c}_B \, g'}{2m_W^2} \, \Big(H^\dagger \overleftrightarrow{D^\mu} H \Big) \, (\partial^\nu B_{\mu\nu}) \\ &+ \frac{i \bar{c}_{HW} \, g}{m_W^2} \, (D^\mu H)^\dagger \sigma^i (D^\nu H) W^i_{\mu\nu} + \frac{i \bar{c}_{HB} \, g'}{m_W^2} \, (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} \\ &+ \frac{\bar{c}_\gamma \, g'^2}{m_W^2} \, H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{\bar{c}_g \, g_S^2}{m_W^2} \, H^\dagger H G^a_{\mu\nu} G^{a\mu\nu} \,, \end{split}$$

- Basis introduced by Giudice et al. (SILH basis)
- Absence of FCNC from tree-level exchange of the Higgs requires flavor alignment
- 12 operators in $\Delta \mathcal{L}_{SILH}$ + 5 made only of gauge fields (not shown)

$$\Delta \mathcal{L}_{SILH} = \frac{\bar{c}_H}{2v^2} \partial^{\mu} (H^{\dagger} H) \partial_{\mu} (H^{\dagger} H) + \frac{\bar{c}_T}{2v^2} \left(H^{\dagger} \overleftrightarrow{D^{\mu}} H \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) - \frac{\bar{c}_6 \lambda}{v^2} \left(H^{\dagger} H \right)^3 \\ + \left(\frac{\bar{c}_u}{v^2} y_u H^{\dagger} H \bar{q}_L H^c u_R + \frac{\bar{c}_d}{v^2} y_d H^{\dagger} H \bar{q}_L H d_R + \frac{\bar{c}_l}{v^2} y_l H^{\dagger} H \bar{L}_L H l_R + h.c. \right) \\ + \frac{i\bar{c}_W g}{2m_W^2} \left(H^{\dagger} \sigma^i \overleftrightarrow{D^{\mu}} H \right) (D^{\nu} W_{\mu\nu})^i + \frac{i\bar{c}_B g'}{2m_W^2} \left(H^{\dagger} \overleftrightarrow{D^{\mu}} H \right) (\partial^{\nu} B_{\mu\nu}) \\ + \frac{i\bar{c}_H W g}{m_W^2} (D^{\mu} H)^{\dagger} \sigma^i (D^{\nu} H) W_{\mu\nu}^i + \frac{i\bar{c}_{HB} g'}{m_W^2} (D^{\mu} H)^{\dagger} (D^{\nu} H) B_{\mu\nu} \\ + \frac{\bar{c}_{\gamma} {g'}^2}{m_W^2} H^{\dagger} H B_{\mu\nu} B^{\mu\nu} + \frac{\bar{c}_g g_S^2}{m_W^2} H^{\dagger} H G_{\mu\nu}^a G^{a\mu\nu} ,$$

- Basis introduced by Giudice et al. (SILH basis)
- Absence of FCNC from tree-level exchange of the Higgs requires flavor alignment
- 12 operators in $\Delta \mathcal{L}_{SILH}$ + 5 made only of gauge fields (not shown)

$$\begin{split} \Delta \mathcal{L}_{F_1} &= \frac{i \bar{c}_{Hq}}{v^2} \left(\bar{q}_L \gamma^{\mu} q_L \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) + \frac{i \bar{c}'_{Hq}}{v^2} \left(\bar{q}_L \gamma^{\mu} \sigma^i q_L \right) \left(H^{\dagger} \sigma^i \overleftrightarrow{D}_{\mu} H \right) \\ &+ \frac{i \bar{c}_{Hu}}{v^2} \left(\bar{u}_R \gamma^{\mu} u_R \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) + \frac{i \bar{c}_{Hd}}{v^2} \left(\bar{d}_R \gamma^{\mu} d_R \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) \\ &+ \left(\frac{i \bar{c}_{Hud}}{v^2} \left(\bar{u}_R \gamma^{\mu} d_R \right) \left(H^{c}^{\dagger} \overleftrightarrow{D}_{\mu} H \right) + h.c. \right) \\ &+ \frac{i \bar{c}_{HL}}{v^2} \left(\bar{L}_L \gamma^{\mu} L_L \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) + \frac{i \bar{c}'_{HL}}{v^2} \left(\bar{L}_L \gamma^{\mu} \sigma^i L_L \right) \left(H^{\dagger} \sigma^i \overleftrightarrow{D}_{\mu} H \right) \\ &+ \frac{i \bar{c}_{Hl}}{v^2} \left(\bar{l}_R \gamma^{\mu} l_R \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right), \end{split}$$

$$\begin{split} \Delta \mathcal{L}_{F_2} &= \frac{\bar{c}_{uB} \, g'}{m_W^2} \, y_u \, \bar{q}_L H^c \sigma^{\mu\nu} u_R \, B_{\mu\nu} + \frac{\bar{c}_{uW} \, g}{m_W^2} \, y_u \, \bar{q}_L \sigma^i H^c \sigma^{\mu\nu} u_R \, W^i_{\mu\nu} + \frac{\bar{c}_{uG} \, g_S}{m_W^2} \, y_u \, \bar{q}_L H^c \sigma^{\mu\nu} \lambda^a u_R \, G^a_{\mu\nu} \\ &+ \frac{\bar{c}_{dB} \, g'}{m_W^2} \, y_d \, \bar{q}_L H \sigma^{\mu\nu} d_R \, B_{\mu\nu} + \frac{\bar{c}_{dW} \, g}{m_W^2} \, y_d \, \bar{q}_L \sigma^i H \sigma^{\mu\nu} d_R \, W^i_{\mu\nu} + \frac{\bar{c}_{dG} \, g_S}{m_W^2} \, y_d \, \bar{q}_L H \sigma^{\mu\nu} \lambda^a d_R \, G^a_{\mu\nu} \\ &+ \frac{\bar{c}_{lB} \, g'}{m_W^2} \, y_l \, \bar{L}_L H \sigma^{\mu\nu} l_R \, B_{\mu\nu} + \frac{\bar{c}_{lW} \, g}{m_W^2} \, y_l \, \bar{L}_L \sigma^i H \sigma^{\mu\nu} l_R \, W^i_{\mu\nu} + h.c. \end{split}$$

8 ($\Delta \mathcal{L}_{F_1}$) + 8 ($\Delta \mathcal{L}_{F_2}$) operators + 22 four-fermion operators (not shown)

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$$\begin{split} \Delta \mathcal{L}_{F_{1}} &= \frac{i\bar{c}_{Hq}}{v^{2}} \left(\bar{q}_{L} \gamma^{\mu} q_{L} \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) + \frac{i\bar{c}_{Hq}}{v^{2}} \left(\bar{q}_{L} \gamma^{\mu} \sigma^{i} q_{L} \right) \left(H^{\dagger} \sigma^{i} \overleftrightarrow{D}_{\mu} H \right) \\ &+ \frac{i\bar{c}_{Hu}}{v^{2}} \left(\bar{u}_{R} \gamma^{\mu} u_{R} \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) + \frac{i\bar{c}_{Hd}}{v^{2}} \left(\bar{d}_{R} \gamma^{\mu} d_{R} \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) \\ &+ \left(\frac{i\bar{c}_{Hud}}{v^{2}} \left(\bar{u}_{R} \gamma^{\mu} d_{R} \right) \left(H^{c}^{\dagger} \overleftrightarrow{D}_{\mu} H \right) + h.c. \right) \\ &+ \frac{i\bar{c}_{HL}}{v^{2}} \left(\bar{L}_{L} \gamma^{\mu} L_{L} \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) + \frac{i\bar{c}_{HL}'}{v^{2}} \left(\bar{L}_{L} \gamma^{\mu} \sigma^{i} L_{L} \right) \left(H^{\dagger} \sigma^{i} \overleftrightarrow{D}_{\mu} H \right) \\ &+ \frac{i\bar{c}_{Hl}}{v^{2}} \left(\bar{l}_{R} \gamma^{\mu} l_{R} \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right), \end{split}$$
operators of the form $(\bar{\psi} \gamma^{\mu} \psi) (H^{\dagger} \overleftrightarrow{D}_{\mu} H)$

$$\begin{split} \Delta \mathcal{L}_{F_2} &= \frac{\bar{c}_{uB} \, g'}{m_W^2} \, y_u \, \bar{q}_L H^c \sigma^{\mu\nu} u_R \, B_{\mu\nu} + \frac{\bar{c}_{uW} \, g}{m_W^2} \, y_u \, \bar{q}_L \sigma^i H^c \sigma^{\mu\nu} u_R \, W^i_{\mu\nu} + \frac{\bar{c}_{uG} \, g_S}{m_W^2} \, y_u \, \bar{q}_L H^c \sigma^{\mu\nu} \lambda^a u_R \, G^a_{\mu\nu} \\ &+ \frac{\bar{c}_{dB} \, g'}{m_W^2} \, y_d \, \bar{q}_L H \sigma^{\mu\nu} d_R \, B_{\mu\nu} + \frac{\bar{c}_{dW} \, g}{m_W^2} \, y_d \, \bar{q}_L \sigma^i H \sigma^{\mu\nu} d_R \, W^i_{\mu\nu} + \frac{\bar{c}_{dG} \, g_S}{m_W^2} \, y_d \, \bar{q}_L H \sigma^{\mu\nu} \lambda^a d_R \, G^a_{\mu\nu} \\ &+ \frac{\bar{c}_{lB} \, g'}{m_W^2} \, y_l \, \bar{L}_L H \sigma^{\mu\nu} l_R \, B_{\mu\nu} + \frac{\bar{c}_{lW} \, g}{m_W^2} \, y_l \, \bar{L}_L \sigma^i H \sigma^{\mu\nu} l_R \, W^i_{\mu\nu} + h.c. \end{split}$$

• 8 ($\Delta \mathcal{L}_{F_1}$) + 8 ($\Delta \mathcal{L}_{F_2}$) operators + 22 four-fermion operators (not shown)

$$\begin{split} \Delta \mathcal{L}_{F_{1}} &= \frac{i\overline{c}_{Hq}}{v^{2}} \left(\overline{q}_{L} \gamma^{\mu} q_{L} \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) + \frac{i\overline{c}_{Hq}}{v^{2}} \left(\overline{q}_{L} \gamma^{\mu} \sigma^{i} q_{L} \right) \left(H^{\dagger} \sigma^{i} \overleftrightarrow{D}_{\mu} H \right) \\ &+ \frac{i\overline{c}_{Hu}}{v^{2}} \left(\overline{u}_{R} \gamma^{\mu} u_{R} \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) + \frac{i\overline{c}_{Hd}}{v^{2}} \left(\overline{d}_{R} \gamma^{\mu} d_{R} \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) \\ &+ \left(\frac{i\overline{c}_{Hud}}{v^{2}} \left(\overline{u}_{R} \gamma^{\mu} d_{R} \right) \left(H^{c} \dagger \overleftrightarrow{D}_{\mu} H \right) + h.c. \right) \\ &+ \frac{i\overline{c}_{HL}}{v^{2}} \left(\overline{L}_{L} \gamma^{\mu} L_{L} \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) + \frac{i\overline{c}_{HL}}{v^{2}} \left(\overline{L}_{L} \gamma^{\mu} \sigma^{i} L_{L} \right) \left(H^{\dagger} \sigma^{i} \overleftrightarrow{D}_{\mu} H \right) \\ &+ \frac{i\overline{c}_{HI}}{v^{2}} \left(\overline{L}_{R} \gamma^{\mu} l_{R} \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) + \frac{i\overline{c}_{uW} g}{m_{W}^{2}} y_{u} \overline{q}_{L} \sigma^{i} H^{c} \sigma^{\mu\nu} u_{R} W_{\mu\nu}^{i} + \frac{\overline{c}_{uG} g_{S}}{m_{W}^{2}} y_{u} \overline{q}_{L} H^{c} \sigma^{\mu\nu} \lambda^{a} u_{R} G_{\mu\nu}^{a} \\ &+ \frac{\overline{c}_{dB} g'}{m_{W}^{2}} y_{d} \overline{q}_{L} H^{c} \sigma^{\mu\nu} d_{R} B_{\mu\nu} + \frac{\overline{c}_{dW} g}{m_{W}^{2}} y_{d} \overline{q}_{L} \sigma^{i} H^{\sigma} \mu^{\mu\nu} d_{R} W_{\mu\nu}^{i} + \frac{\overline{c}_{dG} g_{S}}{m_{W}^{2}} y_{d} \overline{q}_{L} H^{\sigma} \mu^{\mu\nu} \lambda^{a} d_{R} G_{\mu\nu}^{a} \\ &+ \frac{\overline{c}_{lB} g'}{m_{W}^{2}} y_{l} \overline{L}_{L} H^{\sigma} \mu^{\mu\nu} l_{R} B_{\mu\nu} + \frac{\overline{c}_{W} g}{m_{W}^{2}} y_{l} \overline{L}_{L} \sigma^{i} H^{\sigma} \mu^{\mu\nu} l_{R} W_{\mu\nu}^{i} + h.c. \end{split}$$

8 ($\Delta \mathcal{L}_{F_1}$) + 8 ($\Delta \mathcal{L}_{F_2}$) operators + 22 four-fermion operators (not shown)

In total: 12+5+8+8+22 = 53 linearly independent + 2 redundant

$$O_W = -6 O_H + 2 (O_u + O_d + O_l) - 8 O_6 + O'_{Hq} + O'_{HL}$$
$$O_B = 2 \tan^2 \theta_W \Big(\sum_{\psi} Y_{\psi} O_{H\psi} - O_T \Big)$$

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Our basis equivalent to that of Grzadkowki et al. but more convenient for Higgs physics because:

[1] operators which parametrize oblique corrections are in the list (O_W, O_B)

[2] it isolates the contributions to the decays

$$h \to \gamma \gamma$$
 (from O_{γ})
 $h \to \gamma Z$ (from O_{γ} and $O_{HW} - O_{HB}$)

which occur at the 1-loop level in minimally coupled UV theories

[3] if the Higgs is a pNGB then O_γ is suppressed

(no cancellation among different operators occurs as in other basis)

- each extra derivative costs a factor 1/M
- each extra power of H(x) costs a factor $g_*/M \equiv 1/f$

For a strongly-interacting light Higgs (SILH):
$$~~rac{1}{f}\ggrac{1}{\Lambda}$$

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For a strongly-interacting light Higgs (SILH):
$$~~rac{1}{f}\gg rac{1}{\Lambda}$$

Naive estimate at the scale M:

$$\bar{c}_H, \bar{c}_T, \bar{c}_6, \bar{c}_\psi \sim O\left(\frac{v^2}{f^2}\right), \quad \bar{c}_W, \bar{c}_B \sim O\left(\frac{m_W^2}{M^2}\right), \quad \bar{c}_{HW}, \bar{c}_{HB}, \bar{c}_\gamma, \bar{c}_g \sim O\left(\frac{m_W^2}{16\pi^2 f^2}\right)$$
$$\bar{c}_{H\psi}, \bar{c}'_{H\psi} \sim O\left(\frac{\lambda_\psi^2}{g_*^2} \frac{v^2}{f^2}\right), \quad \bar{c}_{Hud} \sim O\left(\frac{\lambda_u \lambda_d}{g_*^2} \frac{v^2}{f^2}\right), \quad \bar{c}_{\psi W}, \bar{c}_{\psi B}, \bar{c}_{\psi G} \sim O\left(\frac{m_W^2}{16\pi^2 f^2}\right)$$

Specific symmetry protections might be at work in the UV theory

- Ex: in the MSSM $g_* \sim g$

R-parity
$$\bar{c}_W, \bar{c}_B \sim \frac{m_W^2}{M^2} \times \frac{g^2}{16\pi^2}$$

• Ex: if the Higgs is a pNGB

Goldstone symmetry
$$\overline{c}_{\gamma}, \overline{c}_{g} \sim \frac{m_{W}^{2}}{16\pi^{2}f^{2}} \times \frac{g_{\mathcal{G}}^{2}}{g_{*}^{2}}$$

 $-1.5 \times 10^{-3} < \bar{c}_T(m_Z) < 2.2 \times 10^{-3}$ $-1.4 \times 10^{-3} < \bar{c}_W(m_Z) + \bar{c}_B(m_Z) < 1.9 \times 10^{-3}$

$$\begin{array}{l} -0.008 < \bar{c}_{Hu} < 0.02 \\ -0.003 < \bar{c}_{Hd} < 0.02 \\ -0.003 < \bar{c}_{Hs} < 0.02 \end{array} \begin{array}{l} -0.03 < \bar{c}_{Hq1} < 0.02 \\ -0.005 < \bar{c}_{Hq2} < 0.003 \\ -0.002 < \bar{c}'_{Hq1} < 0.003 \end{array} \begin{array}{l} -0.004 < \bar{c}_{HL} + \bar{c}'_{HL} < 0.002 \\ -0.003 < \bar{c}_{HL} - \bar{c}'_{HL} < 0.0002 \\ -0.0003 < \bar{c}_{Hq2} < 0.005 \end{array} \begin{array}{l} -0.003 < \bar{c}_{Hq3} - \bar{c}'_{Hq3} < 0.009 \\ -0.0007 < \bar{c}_{Hl} < 0.003 \\ -0.0007 < \bar{c}_{Hl} < 0.003 \end{array} \begin{array}{l} -0.002 < \bar{c}_{Hq3} - \bar{c}'_{Hq3} < 0.009 \\ -0.002 < \bar{c}_{Hc} < 0.03 \\ -0.007 < \bar{c}_{Hl} < 0.003 \end{array} \end{array}$$

$$-0.4 \times 10^{-3} < \bar{c}_{Htb}(m_W) < 1.3 \times 10^{-3}$$

$$-0.03 < \bar{c}_{Hd} < 0.02 -0.03 < \bar{c}_{Hs} < 0.02 -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -0.003 < -$$

$$-0.057 < \operatorname{Re}(\bar{c}_{tW} + \bar{c}_{tB}) - 2.65 \operatorname{Im}(\bar{c}_{tW} + \bar{c}_{tB}) < 0.20 \qquad -6.12 \times 10^{-3} < \operatorname{Re}(\bar{c}_{tG}) < 1.94 \times 10^{-3} -1.39 \times 10^{-4} < \operatorname{Im}(\bar{c}_{tG}) < 1.21 \times 10^{-4} \qquad -1.2 < \operatorname{Re}(\bar{c}_{bW}) < 1.1 -0.01 < \operatorname{Re}(\bar{c}_{tW}) < 0.02$$

$$-7.01 \times 10^{-6} < \operatorname{Im}(\bar{c}_{uB} + \bar{c}_{uW}) < 7.86 \times 10^{-6} \qquad -1.64 \times 10^{-2} < \operatorname{Re}(\bar{c}_{eB} - \bar{c}_{eW}) < 3.37 \times 10^{-3} \\ -9.42 \times 10^{-7} < \operatorname{Im}(\bar{c}_{dB} - \bar{c}_{dW}) < 8.40 \times 10^{-7} \qquad 1.88 \times 10^{-4} < \operatorname{Re}(\bar{c}_{\mu B} - \bar{c}_{\mu W}) < 6.43 \times 10^{-4} \\ -1.62 \times 10^{-6} < \operatorname{Im}(\bar{c}_{uG}) < 2.01 \times 10^{-6} \qquad -2.97 \times 10^{-7} < \operatorname{Im}(\bar{c}_{eB} - \bar{c}_{eW}) < 4.51 \times 10^{-7} \\ -7.71 \times 10^{-7} < \operatorname{Im}(\bar{c}_{dG}) < 5.70 \times 10^{-7} \qquad -0.26 < \operatorname{Im}(\bar{c}_{\mu B} - \bar{c}_{\mu W}) < 0.29 \end{aligned}$$

LEP+Tevatron	-1.5×10^{-3}	$\bar{c}_T(m_Z) < 2.2 \times 10^{-3}$	
(EW fit from GFitter)	$-1.4 \times 10^{-3} < \bar{c}_V$	$W(m_Z) + \bar{c}_B(m_Z) < 1.9 \times 10^{-3}$	
$-0.008 < \bar{c}_{Hu} < 0.02$ $-0.03 < \bar{c}_{Hd} < 0.02$ $-0.03 < \bar{c}_{Hs} < 0.02$	$-0.03 < \bar{c}_{Hq1} < 0.02$ $-0.005 < \bar{c}_{Hq2} < 0.003$ $-0.002 < \bar{c}'_{Hq1} < 0.003$ $-0.003 < \bar{c}'_{Hq2} < 0.005$	$-0.004 < \bar{c}_{HL} + \bar{c}'_{HL} < 0.002$ $-0.003 < \bar{c}_{HL} - \bar{c}'_{HL} < 0.0002$ $-0.0007 < \bar{c}_{Hl} < 0.003$	$-0.02 < \bar{c}_{Hq_2} + \bar{c}'_{Hq_2} < 0.005$ $-0.003 < \bar{c}_{Hq_3} - \bar{c}'_{Hq_3} < 0.009$ $-0.02 < \bar{c}_{Hc} < 0.03$ $-0.07 < \bar{c}_{Hb} < -0.005$

 $-0.4 \times 10^{-3} < \bar{c}_{Htb}(m_W) < 1.3 \times 10^{-3}$

20
$$-6.12 \times 10^{-3} < \operatorname{Re}(\bar{c}_{tG}) < 1.94 \times 10^{-3}$$
$$-1.2 < \operatorname{Re}(\bar{c}_{bW}) < 1.1$$
$$-0.01 < \operatorname{Re}(\bar{c}_{tW}) < 0.02$$

$$\begin{aligned} (\bar{c}_{uB} + \bar{c}_{uW}) < 7.86 \times 10^{-6} & -1.64 \times 10^{-2} < \operatorname{Re}(\bar{c}_{eB} - \bar{c}_{eW}) < 3.37 \times 10^{-3} \\ (\bar{c}_{dB} - \bar{c}_{dW}) < 8.40 \times 10^{-7} & 1.88 \times 10^{-4} < \operatorname{Re}(\bar{c}_{\mu B} - \bar{c}_{\mu W}) < 6.43 \times 10^{-4} \\ \operatorname{Im}(\bar{c}_{uG}) < 2.01 \times 10^{-6} & -2.97 \times 10^{-7} < \operatorname{Im}(\bar{c}_{eB} - \bar{c}_{eW}) < 4.51 \times 10^{-7} \\ \operatorname{Im}(\bar{c}_{dG}) < 5.70 \times 10^{-7} & -0.26 < \operatorname{Im}(\bar{c}_{\mu B} - \bar{c}_{\mu W}) < 0.29 \end{aligned}$$

 $-0.057 < \operatorname{Re}(\bar{c}_{tW} + \bar{c}_{tB}) - 2.65 \operatorname{Im}(\bar{c}_{tW} + \bar{c}_{tB}) < 0.2$ $-1.39 \times 10^{-4} < \operatorname{Im}(\bar{c}_{tG}) < 1.21 \times 10^{-4}$

 $-7.01 \times 10^{-6} < \text{Im}($ $-9.42 \times 10^{-7} < \text{Im}($ $-1.62 \times 10^{-6} <$ $-7.71 \times 10^{-7} <$









Muon and electron (g-2), EDM

 $-1.5 \times 10^{-3} < \bar{c}_T(m_Z) < 2.2 \times 10^{-3}$ $-1.4 \times 10^{-3} < \bar{c}_W(m_Z) + \bar{c}_B(m_Z) < 1.9 \times 10^{-3}$

$$\begin{array}{l} -0.008 < \bar{c}_{Hu} < 0.02 \\ -0.003 < \bar{c}_{Hd} < 0.02 \\ -0.003 < \bar{c}_{Hs} < 0.02 \end{array} \begin{array}{l} -0.03 < \bar{c}_{Hq1} < 0.02 \\ -0.005 < \bar{c}_{Hq2} < 0.003 \\ -0.002 < \bar{c}'_{Hq1} < 0.003 \end{array} \begin{array}{l} -0.004 < \bar{c}_{HL} + \bar{c}'_{HL} < 0.002 \\ -0.003 < \bar{c}_{HL} - \bar{c}'_{HL} < 0.0002 \\ -0.0003 < \bar{c}_{Hq2} < 0.005 \end{array} \begin{array}{l} -0.003 < \bar{c}_{Hq3} - \bar{c}'_{Hq3} < 0.009 \\ -0.0007 < \bar{c}_{Hl} < 0.003 \\ -0.0007 < \bar{c}_{Hl} < 0.003 \end{array} \begin{array}{l} -0.002 < \bar{c}_{Hq3} - \bar{c}'_{Hq3} < 0.009 \\ -0.002 < \bar{c}_{Hc} < 0.03 \\ -0.007 < \bar{c}_{Hl} < 0.003 \end{array}$$

$$-0.4 \times 10^{-3} < \bar{c}_{Htb}(m_W) < 1.3 \times 10^{-3}$$

$$-0.057 < \operatorname{Re}(\bar{c}_{tW} + \bar{c}_{tB}) - 2.65 \operatorname{Im}(\bar{c}_{tW} + \bar{c}_{tB}) < 0.20 \qquad -6.12 \times 10^{-3} < \operatorname{Re}(\bar{c}_{tG}) < 1.94 \times 10^{-3} -1.39 \times 10^{-4} < \operatorname{Im}(\bar{c}_{tG}) < 1.21 \times 10^{-4} \qquad -1.2 < \operatorname{Re}(\bar{c}_{bW}) < 1.1 -0.01 < \operatorname{Re}(\bar{c}_{tW}) < 0.02$$

$$-7.01 \times 10^{-6} < \operatorname{Im}(\bar{c}_{uB} + \bar{c}_{uW}) < 7.86 \times 10^{-6} \qquad -1.64 \times 10^{-2} < \operatorname{Re}(\bar{c}_{eB} - \bar{c}_{eW}) < 3.37 \times 10^{-3} \\ -9.42 \times 10^{-7} < \operatorname{Im}(\bar{c}_{dB} - \bar{c}_{dW}) < 8.40 \times 10^{-7} \qquad 1.88 \times 10^{-4} < \operatorname{Re}(\bar{c}_{\mu B} - \bar{c}_{\mu W}) < 6.43 \times 10^{-4} \\ -1.62 \times 10^{-6} < \operatorname{Im}(\bar{c}_{uG}) < 2.01 \times 10^{-6} \qquad -2.97 \times 10^{-7} < \operatorname{Im}(\bar{c}_{eB} - \bar{c}_{eW}) < 4.51 \times 10^{-7} \\ -7.71 \times 10^{-7} < \operatorname{Im}(\bar{c}_{dG}) < 5.70 \times 10^{-7} \qquad -0.26 < \operatorname{Im}(\bar{c}_{\mu B} - \bar{c}_{\mu W}) < 0.29 \end{aligned}$$

custodial symmetry required to avoid strong bound on c_T $-1.5 \times 10^{-3} < \bar{c}_T(m_Z) < 2.2 \times 10^{-3}$ $-1.4 \times 10^{-3} < \bar{c}_W(m_Z) + \bar{c}_B(m_Z) < 1.9 \times 10^{-3}$

 $-0.03 < \bar{c}_{Hq1} < 0.02$

$$-0.02 < \bar{c}_{Hq_2} + \bar{c}'_{Hq_2} < 0.005$$
$$-0.003 < \bar{c}_{Hq_3} - \bar{c}'_{Hq_3} < 0.009$$
$$-0.02 < \bar{c}_{Hc} < 0.03$$
$$-0.07 < \bar{c}_{Hb} < -0.005$$

$$-0.005 < \bar{c}_{Hq2} < 0.003 \qquad -0.004 < \bar{c}_{HL} + \bar{c}'_{HL} < 0.002 -0.002 < \bar{c}'_{Hq1} < 0.003 \qquad -0.003 < \bar{c}_{HL} - \bar{c}'_{HL} < 0.0002 -0.0007 < \bar{c}_{Hl} < 0.003 -0.0007 < \bar{c}_{Hl} < 0.003$$

 $-0.008 < \bar{c}_{Hu} < 0.02$ $-0.03 < \bar{c}_{Hd} < 0.02$ $-0.03 < \bar{c}_{Hs} < 0.02$

 $-0.4 \times 10^{-3} < \bar{c}_{Htb}(m_W) < 1.3 \times 10^{-3}$

$$-0.057 < \operatorname{Re}(\bar{c}_{tW} + \bar{c}_{tB}) - 2.65 \operatorname{Im}(\bar{c}_{tW} + \bar{c}_{tB}) < 0.20 \qquad -6.12 \times 10^{-3} < \operatorname{Re}(\bar{c}_{tG}) < 1.94 \times 10^{-3} \\ -1.39 \times 10^{-4} < \operatorname{Im}(\bar{c}_{tG}) < 1.21 \times 10^{-4} \qquad -1.2 < \operatorname{Re}(\bar{c}_{bW}) < 1.1 \\ -0.01 < \operatorname{Re}(\bar{c}_{tW}) < 0.02 \end{aligned}$$

$$-7.01 \times 10^{-6} < \operatorname{Im}(\bar{c}_{uB} + \bar{c}_{uW}) < 7.86 \times 10^{-6} \qquad -1.64 \times 10^{-2} < \operatorname{Re}(\bar{c}_{eB} - \bar{c}_{eW}) < 3.37 \times 10^{-3} \\ -9.42 \times 10^{-7} < \operatorname{Im}(\bar{c}_{dB} - \bar{c}_{dW}) < 8.40 \times 10^{-7} \qquad 1.88 \times 10^{-4} < \operatorname{Re}(\bar{c}_{\mu B} - \bar{c}_{\mu W}) < 6.43 \times 10^{-4} \\ -1.62 \times 10^{-6} < \operatorname{Im}(\bar{c}_{uG}) < 2.01 \times 10^{-6} \qquad -2.97 \times 10^{-7} < \operatorname{Im}(\bar{c}_{eB} - \bar{c}_{eW}) < 4.51 \times 10^{-7} \\ -7.71 \times 10^{-7} < \operatorname{Im}(\bar{c}_{dG}) < 5.70 \times 10^{-7} \qquad -0.26 < \operatorname{Im}(\bar{c}_{\mu B} - \bar{c}_{\mu W}) < 0.29 \end{aligned}$$



 $-0.4 \times 10^{-3} < \bar{c}_{Htb}(m_W) < 1.3 \times 10^{-3}$

$$-0.057 < \operatorname{Re}(\bar{c}_{tW} + \bar{c}_{tB}) - 2.65 \operatorname{Im}(\bar{c}_{tW} + \bar{c}_{tB}) < 0.20 \qquad -6.12 \times 10^{-3} < \operatorname{Re}(\bar{c}_{tG}) < 1.94 \times 10^{-3} -1.39 \times 10^{-4} < \operatorname{Im}(\bar{c}_{tG}) < 1.21 \times 10^{-4} \qquad -1.2 < \operatorname{Re}(\bar{c}_{bW}) < 1.1 -0.01 < \operatorname{Re}(\bar{c}_{tW}) < 0.02$$

$$-7.01 \times 10^{-6} < \operatorname{Im}(\bar{c}_{uB} + \bar{c}_{uW}) < 7.86 \times 10^{-6} \qquad -1.64 \times 10^{-2} < \operatorname{Re}(\bar{c}_{eB} - \bar{c}_{eW}) < 3.37 \times 10^{-3} \\ -9.42 \times 10^{-7} < \operatorname{Im}(\bar{c}_{dB} - \bar{c}_{dW}) < 8.40 \times 10^{-7} \qquad 1.88 \times 10^{-4} < \operatorname{Re}(\bar{c}_{\mu B} - \bar{c}_{\mu W}) < 6.43 \times 10^{-4} \\ -1.62 \times 10^{-6} < \operatorname{Im}(\bar{c}_{uG}) < 2.01 \times 10^{-6} \qquad -2.97 \times 10^{-7} < \operatorname{Im}(\bar{c}_{eB} - \bar{c}_{eW}) < 4.51 \times 10^{-7} \\ -7.71 \times 10^{-7} < \operatorname{Im}(\bar{c}_{dG}) < 5.70 \times 10^{-7} \qquad -0.26 < \operatorname{Im}(\bar{c}_{\mu B} - \bar{c}_{\mu W}) < 0.29 \end{aligned}$$





$$\begin{split} \Delta \mathcal{L}_{SILH} &= \frac{\bar{c}_H}{2v^2} \,\partial^\mu \big(H^\dagger H \big) \,\partial_\mu \big(H^\dagger H \big) + \frac{\bar{c}_T}{2v^2} \, \Big(H^\dagger \overleftrightarrow{D^\mu} H \Big) \Big(H^\dagger \overleftrightarrow{D}_\mu H \Big) - \frac{\bar{c}_6 \,\lambda}{v^2} \, \big(H^\dagger H \big)^3 \\ &+ \Big(\frac{\bar{c}_u}{v^2} \, y_u \, H^\dagger H \, \bar{q}_L H^c u_R + \frac{\bar{c}_d}{v^2} \, y_d \, H^\dagger H \, \bar{q}_L H d_R + \frac{\bar{c}_l}{v^2} \, y_l \, H^\dagger H \, \bar{L}_L H l_R + h.c. \Big) \\ &+ \frac{i \bar{c}_W \, g}{2m_W^2} \, \Big(H^\dagger \sigma^i \overleftrightarrow{D^\mu} H \Big) \, (D^\nu W_{\mu\nu})^i + \frac{i \bar{c}_B \, g'}{2m_W^2} \, \Big(H^\dagger \overleftrightarrow{D^\mu} H \Big) \, (\partial^\nu B_{\mu\nu}) \\ &+ \frac{i \bar{c}_{HW} \, g}{m_W^2} \, (D^\mu H)^\dagger \sigma^i (D^\nu H) W^i_{\mu\nu} + \frac{i \bar{c}_{HB} \, g'}{m_W^2} \, (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} \\ &+ \frac{\bar{c}_\gamma \, {g'}^2}{m_W^2} \, H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{\bar{c}_g \, g_S^2}{m_W^2} \, H^\dagger H G^a_{\mu\nu} G^{a\mu\nu} \,, \end{split}$$

$$\begin{split} \Delta \mathcal{L}_{SILH} &= \frac{\bar{c}_{H}}{2v^{2}} \partial^{\mu} \left(H^{\dagger} H \right) \partial_{\mu} \left(H^{\dagger} H \right) + \frac{\bar{c}_{T}}{2v^{2}} \left(H^{\dagger} \overleftarrow{D^{\mu}} H \right) \left(H^{\dagger} \overleftarrow{D}_{\mu} H \right) - \frac{\bar{c}_{6} \lambda}{v^{2}} \left(H^{\dagger} H \right)^{3} \\ &+ \left(\frac{\bar{c}_{u}}{v^{2}} y_{u} H^{\dagger} H \, \bar{q}_{L} H^{c} u_{R} + \frac{\bar{c}_{d}}{v^{2}} y_{d} H^{\dagger} H \, \bar{q}_{L} H d_{R} + \frac{\bar{c}_{l}}{v^{2}} y_{l} H^{\dagger} H \, \bar{L}_{L} H l_{R} + h.c. \right) \\ &+ \frac{i \bar{c}_{W} g}{2m_{W}^{2}} \left(H^{\dagger} \sigma^{i} \overleftarrow{D^{\mu}} H \right) \left(D^{\nu} W_{\mu\nu} \right)^{i} + \frac{i \bar{c}_{B} g'}{2m_{W}^{2}} \left(H^{\dagger} \overleftarrow{D^{\mu}} H \right) \left(\partial^{\nu} B_{\mu\nu} \right) \\ &+ \frac{i \bar{c}_{HW} g}{m_{W}^{2}} \left(D^{\mu} H \right)^{\dagger} \sigma^{i} \left(D^{\nu} H \right) W_{\mu\nu}^{i} + \frac{i \bar{c}_{HB} g'}{m_{W}^{2}} \left(D^{\mu} H \right)^{\dagger} \left(D^{\nu} H \right) B_{\mu\nu} \\ &+ \frac{\bar{c}_{\gamma} g'^{2}}{m_{W}^{2}} H^{\dagger} H B_{\mu\nu} B^{\mu\nu} + \frac{\bar{c}_{g} g_{S}^{2}}{m_{W}^{2}} H^{\dagger} H G_{\mu\nu}^{a} G^{a\mu\nu} \,, \end{split}$$

Parametrize corrections to tree-level Higgs couplings:

$$\frac{\Delta c}{c_{SM}} = O\left(\frac{v^2}{f^2}\right)$$

Probe Higgs interaction strength g_*

$$\begin{split} \Delta \mathcal{L}_{SILH} &= \frac{\bar{c}_H}{2v^2} \,\partial^\mu \big(H^\dagger H \big) \,\partial_\mu \big(H^\dagger H \big) + \frac{\bar{c}_T}{2v^2} \, \Big(H^\dagger \overleftrightarrow{D^\mu} H \Big) \Big(H^\dagger \overleftrightarrow{D}_\mu H \Big) - \frac{\bar{c}_6 \,\lambda}{v^2} \, \big(H^\dagger H \big)^3 \\ &+ \Big(\frac{\bar{c}_u}{v^2} \, y_u \, H^\dagger H \, \bar{q}_L H^c u_R + \frac{\bar{c}_d}{v^2} \, y_d \, H^\dagger H \, \bar{q}_L H d_R + \frac{\bar{c}_l}{v^2} \, y_l \, H^\dagger H \, \bar{L}_L H l_R + h.c. \Big) \\ &+ \frac{i \bar{c}_W \, g}{2m_W^2} \, \Big(H^\dagger \sigma^i \overleftrightarrow{D^\mu} H \Big) \, (D^\nu W_{\mu\nu})^i + \frac{i \bar{c}_B \, g'}{2m_W^2} \, \Big(H^\dagger \overleftrightarrow{D^\mu} H \Big) \, (\partial^\nu B_{\mu\nu}) \\ &+ \frac{i \bar{c}_H W \, g}{m_W^2} \, (D^\mu H)^\dagger \sigma^i (D^\nu H) W^i_{\mu\nu} + \frac{i \bar{c}_{HB} \, g'}{m_W^2} \, (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} \\ &+ \frac{\bar{c}_\gamma \, g'^2}{m_W^2} \, H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{\bar{c}_g \, g_S^2}{m_W^2} \, H^\dagger H G^a_{\mu\nu} G^{a\mu\nu} \,, \end{split}$$

Modify the $h \rightarrow WW$, ZZ decay rates

$$\frac{\delta\Gamma}{\Gamma_{SM}} = \hat{c}_{W,B} \times O\left(\frac{m_W^2}{M^2}\right) + \hat{c}_{HW+HB,\gamma} \times O\left(\frac{m_W^2}{16\pi^2 f^2}\right)$$

$$\begin{split} \Delta \mathcal{L}_{SILH} &= \frac{\bar{c}_H}{2v^2} \,\partial^\mu (H^\dagger H) \,\partial_\mu (H^\dagger H) + \frac{\bar{c}_T}{2v^2} \left(H^\dagger \overleftrightarrow{D^\mu} H \right) \left(H^\dagger \overleftrightarrow{D}_\mu H \right) - \frac{\bar{c}_6 \,\lambda}{v^2} \left(H^\dagger H \right)^3 \\ &+ \left(\frac{\bar{c}_u}{v^2} \,y_u \,H^\dagger H \,\bar{q}_L H^c u_R + \frac{\bar{c}_d}{v^2} \,y_d \,H^\dagger H \,\bar{q}_L H d_R + \frac{\bar{c}_l}{v^2} \,y_l \,H^\dagger H \,\bar{L}_L H l_R + h.c. \right) \\ &+ \frac{i \bar{c}_W \,g}{2m_W^2} \left(H^\dagger \sigma^i \overleftrightarrow{D^\mu} H \right) \left(D^\nu W_{\mu\nu} \right)^i + \frac{i \bar{c}_B \,g'}{2m_W^2} \left(H^\dagger \overleftrightarrow{D^\mu} H \right) \left(\partial^\nu B_{\mu\nu} \right) \\ &+ \frac{i \bar{c}_H W \,g}{m_W^2} \left(D^\mu H \right)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i + \frac{i \bar{c}_H B \,g'}{m_W^2} \left(D^\mu H \right)^\dagger (D^\nu H) B_{\mu\nu} \\ &+ \frac{\bar{c}_\gamma \,g'^2}{m_W^2} \,H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{\bar{c}_g \,g_S^2}{m_W^2} \,H^\dagger H G^a_{\mu\nu} G^{a\mu\nu} \,, \end{split}$$

Modify the $h \rightarrow WW$, ZZ decay rates

$$\frac{\delta\Gamma}{\Gamma_{SM}} = \hat{c}_{W,B} \times O\left(\frac{m_W^2}{M^2}\right) + \hat{c}_{HW+HB,\gamma} \times O\left(\frac{m_W^2}{16\pi^2 f^2}\right)$$

Probe NP scale $\lesssim 10^{-3}$ due to LEP bounds

$$\begin{split} \Delta \mathcal{L}_{SILH} &= \frac{\bar{c}_{H}}{2v^{2}} \,\partial^{\mu} \big(H^{\dagger} H \big) \,\partial_{\mu} \big(H^{\dagger} H \big) + \frac{\bar{c}_{T}}{2v^{2}} \left(H^{\dagger} \overrightarrow{D^{\mu}} H \right) \Big(H^{\dagger} \overrightarrow{D}_{\mu} H \Big) - \frac{\bar{c}_{6} \,\lambda}{v^{2}} \left(H^{\dagger} H \big)^{3} \\ &+ \left(\frac{\bar{c}_{u}}{v^{2}} \,y_{u} \,H^{\dagger} H \,\bar{q}_{L} H^{c} u_{R} + \frac{\bar{c}_{d}}{v^{2}} \,y_{d} \,H^{\dagger} H \,\bar{q}_{L} H d_{R} + \frac{\bar{c}_{l}}{v^{2}} \,y_{l} \,H^{\dagger} H \,\bar{L}_{L} H l_{R} + h.c. \right) \\ &+ \frac{i \bar{c}_{W} \,g}{2m_{W}^{2}} \left(H^{\dagger} \sigma^{i} \overleftrightarrow{D^{\mu}} H \right) \left(D^{\nu} W_{\mu\nu} \right)^{i} + \frac{i \bar{c}_{B} \,g'}{2m_{W}^{2}} \left(H^{\dagger} \overleftrightarrow{D^{\mu}} H \right) \left(\partial^{\nu} B_{\mu\nu} \right) \\ &+ \frac{i \bar{c}_{HW} \,g}{m_{W}^{2}} \left(D^{\mu} H \right)^{\dagger} \sigma^{i} (D^{\nu} H) W_{\mu\nu}^{i} + \frac{i \bar{c}_{HB} \,g'}{m_{W}^{2}} \left(D^{\mu} H \right)^{\dagger} (D^{\nu} H) B_{\mu\nu} \\ &+ \frac{\bar{c}_{\gamma} \,g'^{2}}{m_{W}^{2}} \,H^{\dagger} H B_{\mu\nu} B^{\mu\nu} + \frac{\bar{c}_{g} \,g_{S}^{2}}{m_{W}^{2}} \,H^{\dagger} H G_{\mu\nu}^{a} G^{a\mu\nu} \,, \end{split}$$

Modify the $h \rightarrow WW$, ZZ decay rates

$$\frac{\delta\Gamma}{\Gamma_{SM}} = \hat{c}_{W,B} \times O\left(\frac{m_W^2}{M^2}\right) + \hat{c}_{HW+HB,\gamma} \times O\left(\frac{m_W^2}{16\pi^2 f^2}\right)$$
Probe NP scale
$$\lesssim 10^{-3} \text{ due to}$$
LEP bounds

$$\begin{split} \Delta \mathcal{L}_{SILH} &= \frac{\bar{c}_H}{2v^2} \,\partial^\mu (H^\dagger H) \,\partial_\mu (H^\dagger H) + \frac{\bar{c}_T}{2v^2} \left(H^\dagger \overleftrightarrow{D^\mu} H \right) \left(H^\dagger \overleftrightarrow{D}_\mu H \right) - \frac{\bar{c}_6 \,\lambda}{v^2} \left(H^\dagger H \right)^3 \\ &+ \left(\frac{\bar{c}_u}{v^2} \,y_u \,H^\dagger H \,\bar{q}_L H^c u_R + \frac{\bar{c}_d}{v^2} \,y_d \,H^\dagger H \,\bar{q}_L H d_R + \frac{\bar{c}_l}{v^2} \,y_l \,H^\dagger H \,\bar{L}_L H l_R + h.c. \right) \\ &+ \frac{i \bar{c}_W \,g}{2m_W^2} \left(H^\dagger \sigma^i \overleftrightarrow{D^\mu} H \right) (D^\nu W_{\mu\nu})^i + \frac{i \bar{c}_B \,g'}{2m_W^2} \left(H^\dagger \overleftrightarrow{D^\mu} H \right) (\partial^\nu B_{\mu\nu}) \\ &+ \frac{i \bar{c}_{HW} \,g}{m_W^2} \left(D^\mu H \right)^\dagger \sigma^i (D^\nu H) W^i_{\mu\nu} + \frac{i \bar{c}_{HB} \,g'}{m_W^2} \left(D^\mu H \right)^\dagger (D^\nu H) B_{\mu\nu} \\ &+ \frac{\bar{c}_\gamma \,g'^2}{m_W^2} \,H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{\bar{c}_g \,g_S^2}{m_W^2} \,H^\dagger H G^a_{\mu\nu} G^{a\mu\nu} \,, \end{split}$$

Modify the $h \rightarrow WW$, ZZ decay rates

Possible strategy: study angular distributions of final fermions

$$\frac{\delta(d\Gamma/d\Omega)}{(d\Gamma/d\Omega)_{SM}} \lesssim \hat{c}_{W,B} \times O\left(\frac{m_W^2}{M^2} \times \frac{16\pi^2}{g^2}\right) + \hat{c}_{HW+HB,\gamma} \times O\left(\frac{m_W^2}{16\pi^2 f^2} \times \frac{16\pi^2}{g^2}\right)$$

$$\begin{split} \Delta \mathcal{L}_{SILH} &= \frac{\bar{c}_H}{2v^2} \,\partial^\mu \big(H^\dagger H \big) \,\partial_\mu \big(H^\dagger H \big) + \frac{\bar{c}_T}{2v^2} \left(H^\dagger \overleftrightarrow{D^\mu} H \right) \Big(H^\dagger \overleftrightarrow{D}_\mu H \Big) - \frac{\bar{c}_6 \,\lambda}{v^2} \left(H^\dagger H \big)^3 \\ &+ \Big(\frac{\bar{c}_u}{v^2} \,y_u \,H^\dagger H \,\bar{q}_L H^c u_R + \frac{\bar{c}_d}{v^2} \,y_d \,H^\dagger H \,\bar{q}_L H d_R + \frac{\bar{c}_l}{v^2} \,y_l \,H^\dagger H \,\bar{L}_L H l_R + h.c. \Big) \\ &+ \frac{i \bar{c}_W \,g}{2m_W^2} \left(H^\dagger \sigma^i \overleftrightarrow{D^\mu} H \right) \left(D^\nu W_{\mu\nu} \right)^i + \frac{i \bar{c}_B \,g'}{2m_W^2} \left(H^\dagger \overleftrightarrow{D^\mu} H \right) \left(\partial^\nu B_{\mu\nu} \right) \\ &+ \frac{i \bar{c}_H W \,g}{m_W^2} \left(D^\mu H \right)^\dagger \sigma^i (D^\nu H) W^i_{\mu\nu} + \frac{i \bar{c}_{HB} \,g'}{m_W^2} \left(D^\mu H \right)^\dagger (D^\nu H) B_{\mu\nu} \\ &+ \frac{\bar{c}_\gamma \,g'^2}{m_W^2} \,H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{\bar{c}_g \,g_S^2}{m_W^2} \,H^\dagger H G^a_{\mu\nu} G^{a\mu\nu} \,, \end{split}$$

Modify the $h \rightarrow \gamma Z$, $\gamma \gamma$, gg decay rates

$$\frac{\delta\Gamma}{\Gamma_{SM}} = \hat{c}_{HW-HB,\gamma,g} \times O\left(\frac{v^2}{f^2}\right)$$

$$\begin{split} \Delta \mathcal{L}_{SILH} &= \frac{\bar{c}_H}{2v^2} \,\partial^\mu \left(H^\dagger H \right) \partial_\mu \left(H^\dagger H \right) + \frac{\bar{c}_T}{2v^2} \left(H^\dagger \overleftrightarrow{D^\mu} H \right) \left(H^\dagger \overleftrightarrow{D}_\mu H \right) - \frac{\bar{c}_6 \,\lambda}{v^2} \left(H^\dagger H \right)^3 \\ &+ \left(\frac{\bar{c}_u}{v^2} \,y_u \,H^\dagger H \,\bar{q}_L H^c u_R + \frac{\bar{c}_d}{v^2} \,y_d \,H^\dagger H \,\bar{q}_L H d_R + \frac{\bar{c}_l}{v^2} \,y_l \,H^\dagger H \,\bar{L}_L H l_R + h.c. \right) \\ &+ \frac{i \bar{c}_W \,g}{2m_W^2} \left(H^\dagger \sigma^i \overleftrightarrow{D^\mu} H \right) \left(D^\nu W_{\mu\nu} \right)^i + \frac{i \bar{c}_B \,g'}{2m_W^2} \left(H^\dagger \overleftrightarrow{D^\mu} H \right) \left(\partial^\nu B_{\mu\nu} \right) \\ &+ \frac{i \bar{c}_H W \,g}{m_W^2} \left(D^\mu H \right)^\dagger \sigma^i (D^\nu H) W^i_{\mu\nu} + \frac{i \bar{c}_H B \,g'}{m_W^2} \left(D^\mu H \right)^\dagger (D^\nu H) B_{\mu\nu} \\ &+ \frac{\bar{c}_\gamma \,g'^2}{m_W^2} \,H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{\bar{c}_g \,g_S^2}{m_W^2} \,H^\dagger H G^a_{\mu\nu} G^{a\mu\nu} \,, \end{split}$$

Modify the $h \rightarrow \gamma Z$, $\gamma \gamma$, gg decay rates

$$\frac{\delta\Gamma}{\Gamma_{SM}} = \hat{c}_{HW-HB,\gamma,g} \times O\left(\frac{v^2}{f^2}\right)$$

If the Higgs is a pNGB: $\gamma\gamma$, gg suppressed, only γZ probes Higgs strong coupling

$$\begin{split} \Delta \mathcal{L}_{F_2} &= \frac{\bar{c}_{uB} \, g'}{m_W^2} \, y_u \, \bar{q}_L H^c \sigma^{\mu\nu} u_R \, B_{\mu\nu} + \frac{\bar{c}_{uW} \, g}{m_W^2} \, y_u \, \bar{q}_L \sigma^i H^c \sigma^{\mu\nu} u_R \, W^i_{\mu\nu} + \frac{\bar{c}_{uG} \, g_S}{m_W^2} \, y_u \, \bar{q}_L H^c \sigma^{\mu\nu} \lambda^a u_R \, G^a_{\mu\nu} \\ &+ \frac{\bar{c}_{dB} \, g'}{m_W^2} \, y_d \, \bar{q}_L H \sigma^{\mu\nu} d_R \, B_{\mu\nu} + \frac{\bar{c}_{dW} \, g}{m_W^2} \, y_d \, \bar{q}_L \sigma^i H \sigma^{\mu\nu} d_R \, W^i_{\mu\nu} + \frac{\bar{c}_{dG} \, g_S}{m_W^2} \, y_d \, \bar{q}_L H \sigma^{\mu\nu} \lambda^a d_R \, G^a_{\mu\nu} \\ &+ \frac{\bar{c}_{lB} \, g'}{m_W^2} \, y_l \, \bar{L}_L H \sigma^{\mu\nu} l_R \, B_{\mu\nu} + \frac{\bar{c}_{lW} \, g}{m_W^2} \, y_l \, \bar{L}_L \sigma^i H \sigma^{\mu\nu} l_R \, W^i_{\mu\nu} + h.c. \end{split}$$

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Potentially sizable effects may come from the gluon dipole operator involving the right-handed top quark:

$$\frac{\delta\sigma(gg \to h)}{\sigma(gg \to h)} \sim \hat{c}_{tG} \equiv \operatorname{Re}(\bar{c}_{tG}) \left(\frac{m_t^2}{m_W^2}\right) \sim \frac{m_t^2}{16\pi^2 f^2} \simeq 3 \times 10^{-3} \left(\frac{v^2}{f^2}\right)$$
$$\frac{\delta\sigma(gg \to t\bar{t})}{\sigma(gg \to t\bar{t})} \sim \hat{c}_{tG} \frac{\sqrt{s}}{m_t}, \qquad \frac{\delta\sigma(gg \to t\bar{t}h)}{\sigma(gg \to t\bar{t}h)} \sim \hat{c}_{tG} \frac{s}{m_t^2}$$

Strong vs Weak UV completions

- Prototype of weak UV theory: the MSSM
 - no separation of scales: $\left(\frac{v^2}{f^2}\right) \approx \left(\frac{m_W^2}{M^2}\right)$
 - tree-level shifts in the couplings from mixing:

$$c_V = 1 + O\left(\frac{m_Z^4}{m_H^4}\right) \qquad c_u = 1 - O\left(\frac{m_Z^2}{m_H^2}\right) \frac{1}{\tan\beta} \qquad c_d = 1 + O\left(\frac{m_Z^2}{m_H^2}\right)$$

- potentially sizable corrections to $\gamma\gamma$, gg

$$c_{\gamma,g} = O\left(\frac{m_W^2}{16\pi^2} \frac{g_*^2}{m_{\tilde{t}}^2}\right) \qquad g_* = \frac{A_t}{m_{\tilde{t}}}, y_t$$

- Prototype of strong UV theory: composite pNGB Higgs
 - leading effect in tree-level couplings and $Z\gamma$ rate

$$c_V, c_u, c_d = 1 + O\left(\frac{v^2}{f^2}\right)$$
 $\frac{\Gamma(h \to Z\gamma)}{\Gamma_{SM}} = 1 + O\left(\frac{v^2}{f^2}\right)$

- c_g, c_γ suppressed

Effective Lagrangian in the unitary basis

$$\begin{aligned} \mathcal{L} &= \frac{1}{2} \partial_{\mu} h \ \partial^{\mu} h - \frac{1}{2} m_{h}^{2} h^{2} - c_{3} \frac{1}{6} \left(\frac{3m_{h}^{2}}{v} \right) h^{3} - \sum_{\psi=u,d,l} m_{\psi^{(i)}} \bar{\psi}^{(i)} \psi^{(i)} \left(1 + c_{\psi} \frac{h}{v} + \dots \right) \\ &+ m_{W}^{2} W_{\mu}^{+} W^{-\mu} \left(1 + 2c_{W} \frac{h}{v} + \dots \right) + \frac{1}{2} m_{Z}^{2} Z_{\mu} Z^{\mu} \left(1 + 2c_{Z} \frac{h}{v} + \dots \right) + \dots \\ &+ \left(c_{WW} W_{\mu\nu}^{+} W^{-\mu\nu} + \frac{c_{ZZ}}{2} Z_{\mu\nu} Z^{\mu\nu} + c_{Z\gamma} Z_{\mu\nu} \gamma^{\mu\nu} + \frac{c_{\gamma\gamma}}{2} \gamma_{\mu\nu} \gamma^{\mu\nu} + \frac{c_{gg}}{2} G_{\mu\nu}^{a} G^{a\mu\nu} \right) \frac{h}{v} \\ &+ \left(c_{W\partial W} \left(W_{\nu}^{-} D_{\mu} W^{+\mu\nu} + h.c. \right) + c_{Z\partial Z} Z_{\nu} \partial_{\mu} Z^{\mu\nu} + c_{Z\partial\gamma} Z_{\nu} \partial_{\mu} \gamma^{\mu\nu} \right) \frac{h}{v} + \dots \end{aligned}$$

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The same effective Lagrangian describes a generic scalar h (custodial singlet) with SU(2)_LxU(1)_Y non-linearly realized

Each term can be dressed up with Nambu-Goldstone bosons and made manifestly $SU(2)_L x U(1)_Y$ invariant

Coleman, Wess Zumino PR 177 (1969) 2239; Callan, Coleman, Wess, Zumino PR 177 (1969) 2247

RC, Grojean, Moretti, Piccinini, Rattazzi JHEP 1005 (2010) 089 Azatov, RC, Galloway JHEP 04 (2012) 127

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 $ar{c}_W,ar{c}_B$

2 more parameters (couplings) compared to SILH Lagrangian:

 $c_{WW}, c_{ZZ}, c_{Z\gamma}, c_{\gamma\gamma} \longrightarrow \bar{c}_{HW}, \bar{c}_{HB}, \bar{c}_{\gamma}$

 \longrightarrow

 $c_{W\partial W}, c_{Z\partial Z}, c_{Z\partial \gamma}$

20

2 identities hold if the Higgs is a doublet

$$c_{WW} - c_{ZZ} \cos^2 \theta_W = c_{Z\gamma} \sin 2\theta_W + c_{\gamma\gamma} \sin^2 \theta_W$$
$$c_{W\partial W} - c_{Z\partial Z} \cos^2 \theta_W = \frac{c_{Z\partial\gamma}}{2} \sin 2\theta_W$$

They follow from custodial invariance, which is accidental in the SILH Lagrangian at the level of dim-6 operators if one restricts to derivative couplings.

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A third identity on the tree-level couplings follows after imposing custodial symmetry (so that $\bar{c}_T = 0$):

 $c_W = c_Z$

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All three identities are special cases of a more general relation among form factors implied by custodial invariance:







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Custodial symmetry can be broken in the SILH Lagrangian at the level of dim-8 operators and the above identities are violated.

$$\mathsf{Ex:} \qquad \frac{\overline{c}_{8WW} g^2}{m_W^2 v^2} \left(H^{\dagger} W^a_{\mu\nu} \sigma^a H \right) \left(H^{\dagger} W^{b\,\mu\nu} \sigma^b H \right) \,, \qquad \frac{i \overline{c}_{8W} g}{v^2 m_W^2} \left(H^{\dagger} \sigma^a H \right) \left(D^{\mu} W_{\mu\nu} \right)^a \left(H^{\dagger} \overleftrightarrow{D^{\nu}} H \right)$$

$$c_{Z\partial Z} = -4\bar{c}_{8W},$$

$$c_{Z\partial\gamma} = -4\tan\theta_W \,\bar{c}_{8W}$$

$$c_{Z\gamma} = 8\cos^2\theta_W \,\bar{c}_{8WW}$$

$$c_{Z\gamma} = 4\sin2\theta_W \,\bar{c}_{8WW}$$

$$c_{\gamma\gamma} = 8\sin^2\theta_W \,\bar{c}_{8WW}$$

- If the EWSB dynamics has custodial invariance, the non-linear and SILH Lagrangians give the same predictions for single-Higgs processes
 - That is: There is no way to tell if the Higgs is a doublet by looking at single-Higgs processes alone

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(in that case the evidence is for a specific model: the SM)

If deviations from the SM values are found, to tell if the Higgs is part of a doublet one has to go beyond single-Higgs production

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 Large deviations from SM couplings do not necessarily disprove a Higgs doublet (e.g. non-linearities can be large)

In that case the SILH Lagrangian cannot be used: higher order terms must be resummed

Implementing the Effective Lagrangian: eHDECAY

- eHDECAY fully implements the SILH and non-linear Lagrangians (plus two benchmark CH models) for the calculation of Higgs decay rates and BRs
- Software based on HDECAY v5.10; Freely available at the web page: http://www-itp.particle.uni-karlsruhe.de/~maggie/eHDECAY
- Perturbative expansion in the parameters $\alpha_{SM}/4\pi$, $(E/M)^2$, $(v/f)^2$ performed consistently
 - Ex: 1-loop EW corrections included only for the SILH Lagrangian
- Numerical approximate formulas for the decay rates are given in the paper

$$\begin{split} \frac{\Gamma(\bar{\psi}\psi)}{\Gamma(\bar{\psi}\psi)_{SM}} &\simeq 1 - \bar{c}_H - 2\,\bar{c}_\psi\,, \\ \\ \frac{\Gamma(h \to W^{(*)}W^*)}{\Gamma(h \to W^{(*)}W^*)_{SM}} &\simeq 1 - \bar{c}_H + 2.2\,\bar{c}_W + 3.7\,\bar{c}_{HW}\,, \\ \\ \frac{\Gamma(h \to Z^{(*)}Z^*)}{\Gamma(h \to Z^{(*)}Z^*)_{SM}} &\simeq 1 - \bar{c}_H + 2.0\,\left(\bar{c}_W + \tan^2\theta_W\,\bar{c}_B\right) \\ &+ 3.0\,\left(\bar{c}_{HW} + \tan^2\theta_W\,\bar{c}_{HB}\right) - 0.26\,\bar{c}_\gamma\,, \\ \\ \frac{\Gamma(h \to Z\gamma)}{\Gamma(h \to Z\gamma)_{SM}} &\simeq 1 - \bar{c}_H + 0.12\,\bar{c}_t - 5\cdot10^{-4}\,\bar{c}_c - 0.003\,\bar{c}_b - 9\cdot10^{-5}\,\bar{c}_r \\ &+ 4.2\,\bar{c}_W + 0.19\,\left(\bar{c}_{HW} - \bar{c}_{HB} + 8\,\bar{c}_\gamma\,\sin^2\theta_W\right)\,\frac{4\pi}{\sqrt{\alpha_2\alpha_{em}}}\,, \\ \\ \frac{\Gamma(h \to \gamma\gamma)}{\Gamma(h \to \gamma\gamma)_{SM}} &\simeq 1 - \bar{c}_H + 0.54\,\bar{c}_t - 0.003\,\bar{c}_c - 0.007\,\bar{c}_b - 0.007\,\bar{c}_r \\ &+ 5.04\,\bar{c}_W - 0.54\,\bar{c}_\gamma\,\frac{4\pi}{\alpha_{em}}\,, \\ \\ \frac{\Gamma(h \to gg)}{\Gamma(h \to gg)_{SM}} &\simeq 1 - \bar{c}_H - 2.12\,\bar{c}_t + 0.024\,\bar{c}_c + 0.1\,\bar{c}_b + 22.2\,\bar{c}_g\,\frac{4\pi}{\alpha_2}\,. \end{split}$$

$$\alpha_2 \equiv \frac{\sqrt{2} G_F m_W^2}{\pi} \qquad \qquad \alpha_{em} \equiv \alpha_{em} (q^2 = 0)$$

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Basis of SILH effective Lagrangian is the most convenient one to determine the nature of the Higgs boson

- Probe of the Higgs interaction strength comes from:
 i) deviations of tree-level couplings; ii) h→Zγ
- Difficult but potentially interesting: study of angular distributions of daughter fermions in h→ZZ,WW
- Single-Higgs processes alone cannot test if the Higgs belongs to a doublet: double-Higgs processes required



$$A(h \to ZZ) = v^{-1} \epsilon_1^{\mu} \epsilon_2^{\nu} \left(a_1 m_H^2 \eta_{\mu\nu} + a_2 q_{\mu} q_{\nu} + a_3 \epsilon_{\mu\nu\rho\sigma} q_1^{\rho} q_2^{\sigma} \right)$$

