

Trento ECT\*, April 10, 2013  
Workshop: Constraining the  
hadronic contribution to  $(g-2)_\mu$

# Review of R-Measurements and Perspectives at BES-III

Constraining the hadronic contributions to the muon  
anomalous magnetic moment



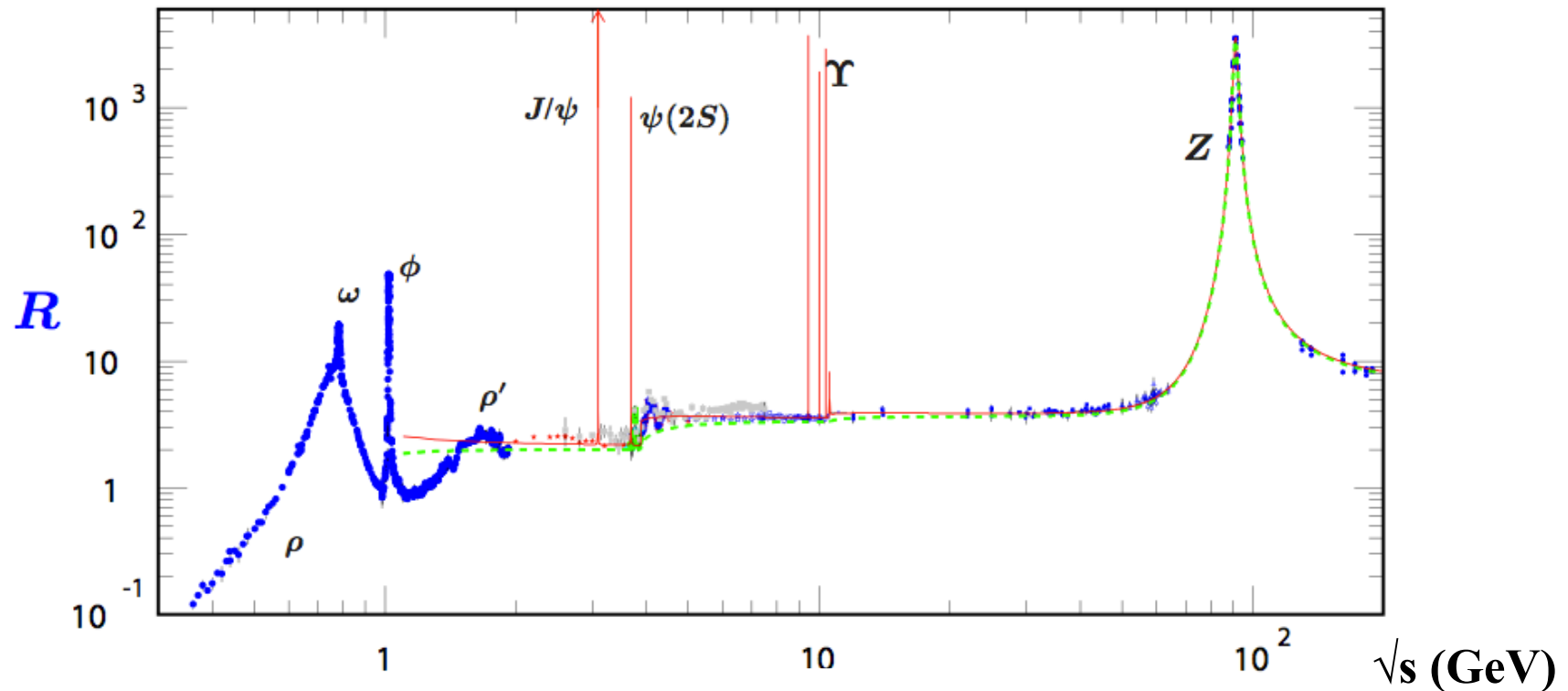
Achim Denig  
University of Mainz  
Institute for Nuclear Physics

# The R Ratio

$$R = \frac{\sigma^{(0)}(e^+e^- \rightarrow \text{hadrons})}{\sigma^{(0)}(e^+e^- \rightarrow \mu^+\mu^-)}$$

**R lead to formulation of Standard Model**

- Number of colours  $N_c = 3$
- Number of quark flavours  $N_f > 2$

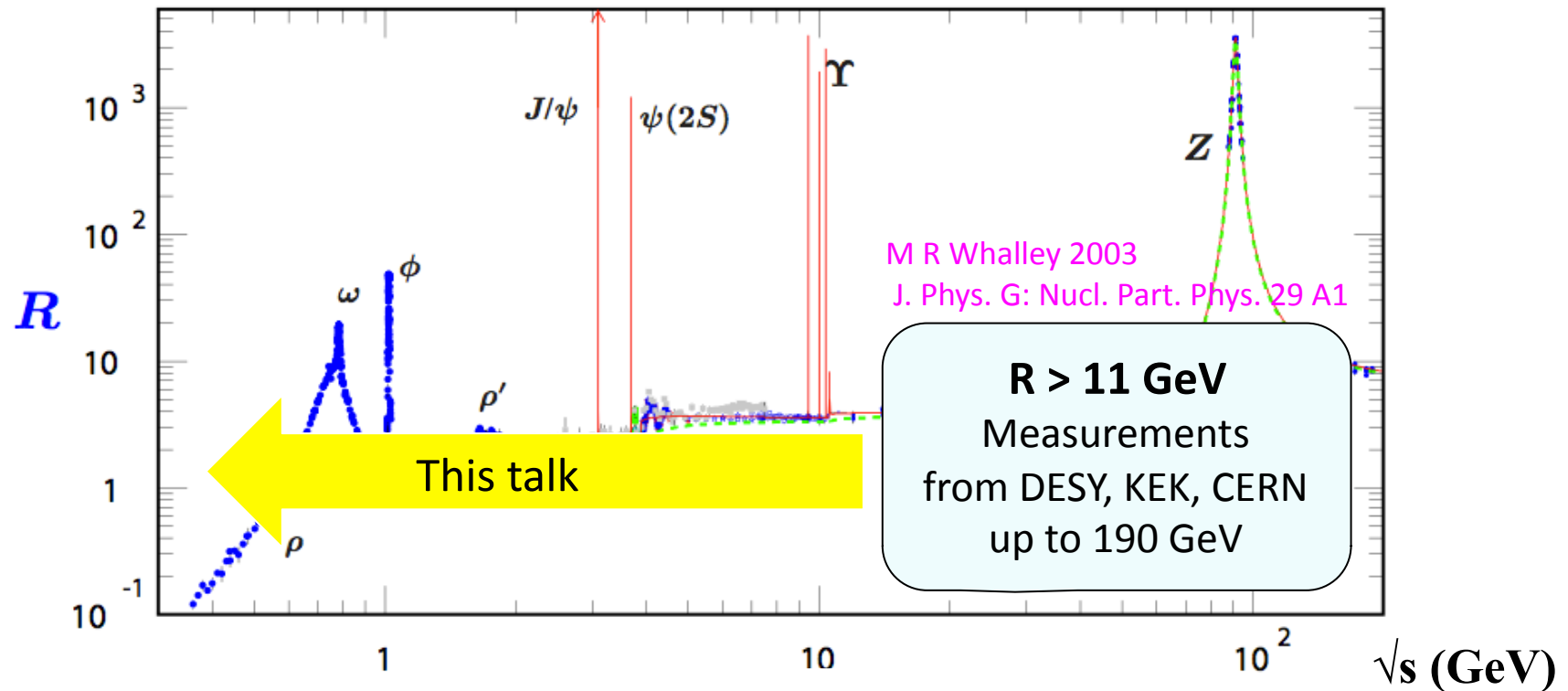


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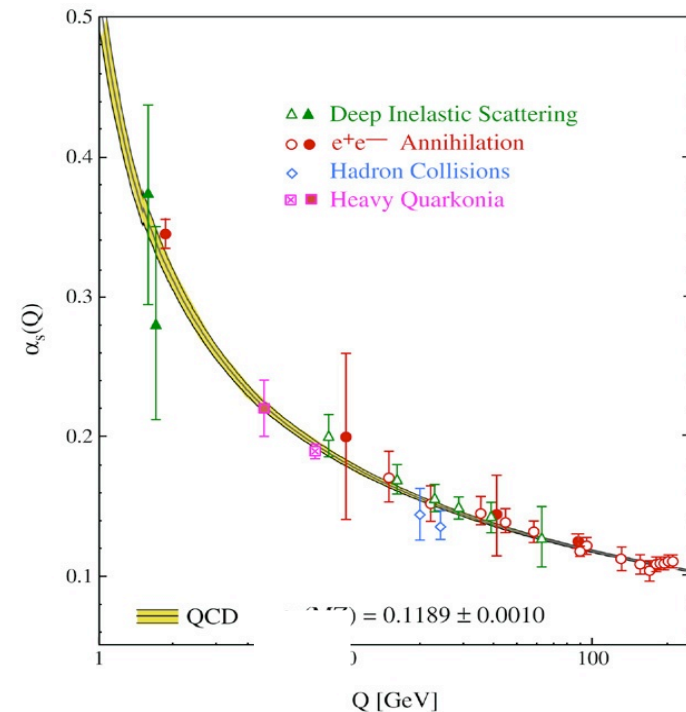
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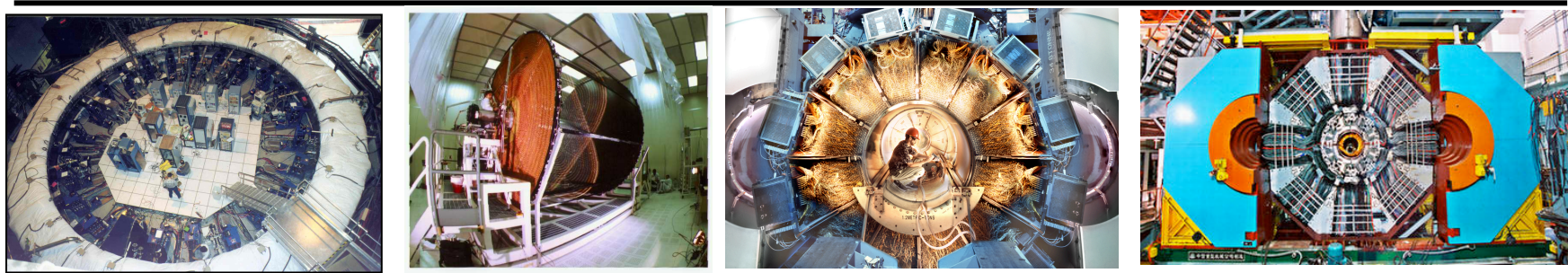


# Extracting Fundamental Parameters of QCD from $R$ Measurements

- Extraction of quark masses (c, b)
- Chiral condensates
- Extraction of strong coupling constant
- Hadron spectroscopy
- Timelike nucleon EM Form Factors

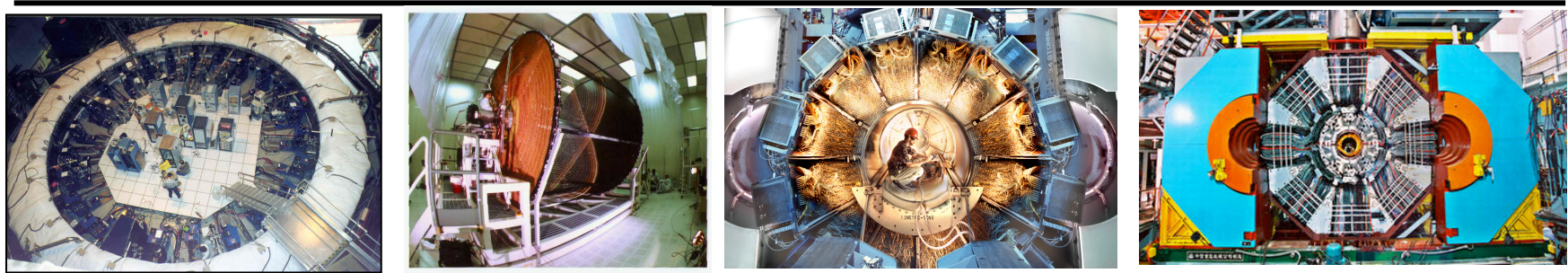
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## *Outline*

- **Motivation:  $(g-2)_\mu$  &  $\alpha_{\text{QED}}(M_Z^2)$**
- **Results Energy Scan**
- **Perspectives at BES-III**
- **Conclusions and Future Perspectives**



## Outline

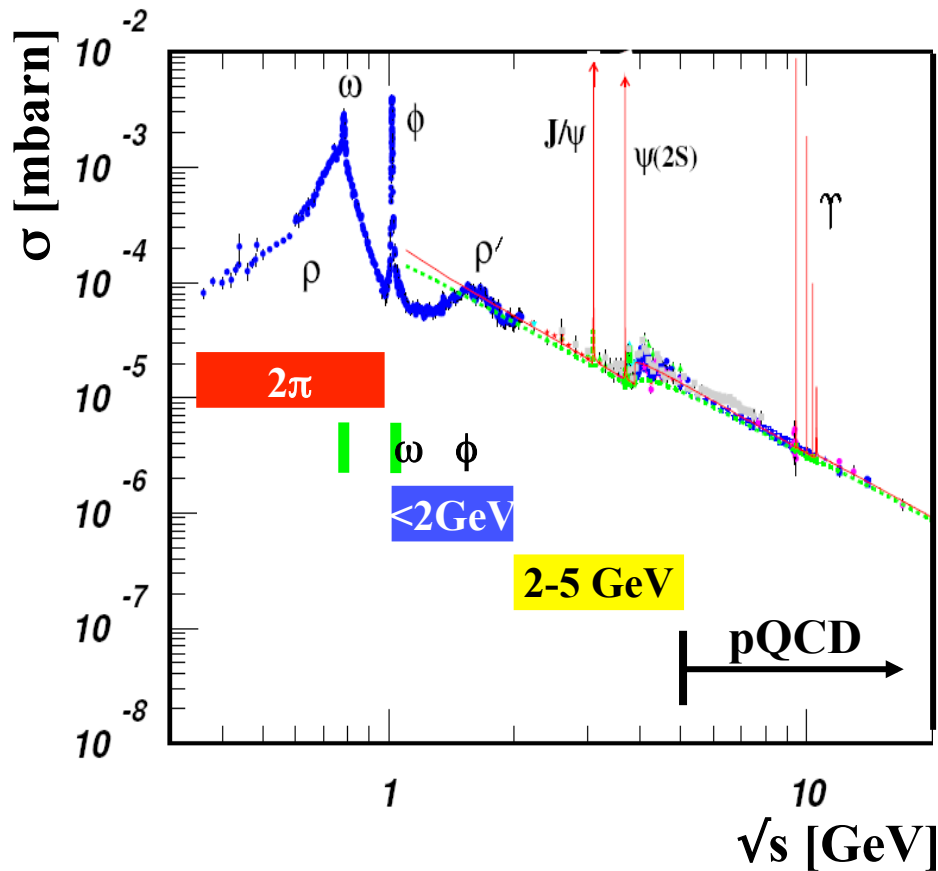
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# Hadronic Cross Section Data and $(g-2)_\mu$



Determine the hadronic contribution to  $a_\mu = (g-2)_\mu$

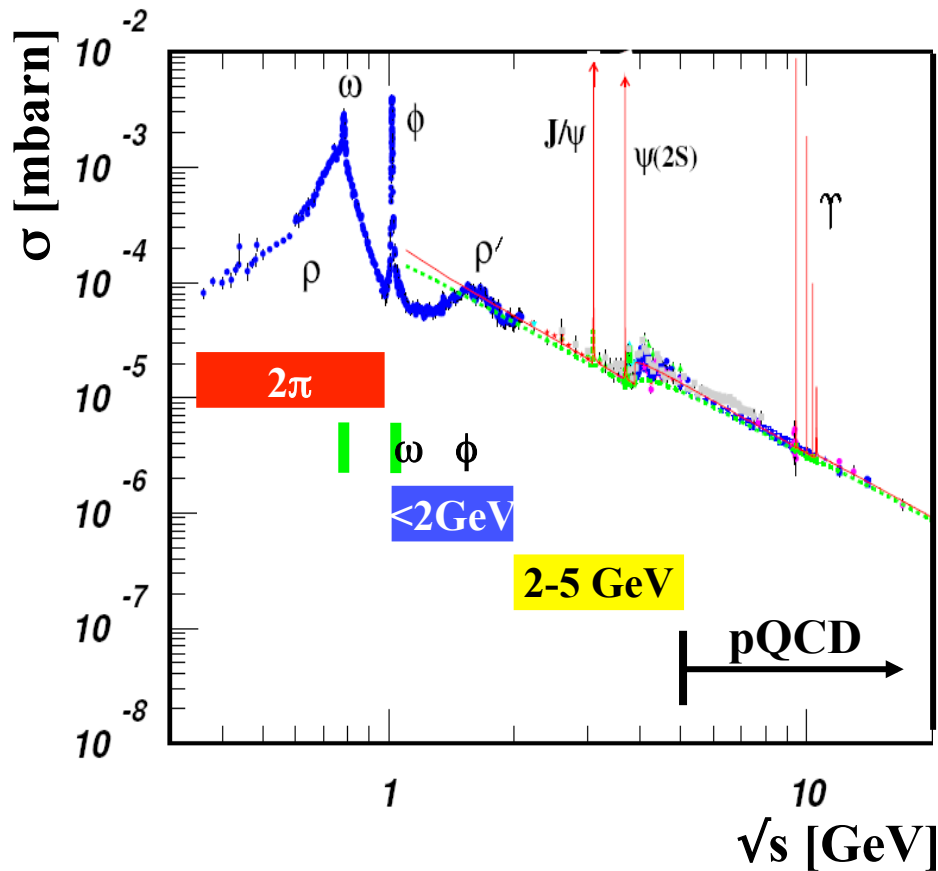
$$a_\mu^{had} = \frac{1}{4\pi^3} \int_{4m_\pi^2}^{\infty} ds K(s) \sigma_{had}$$



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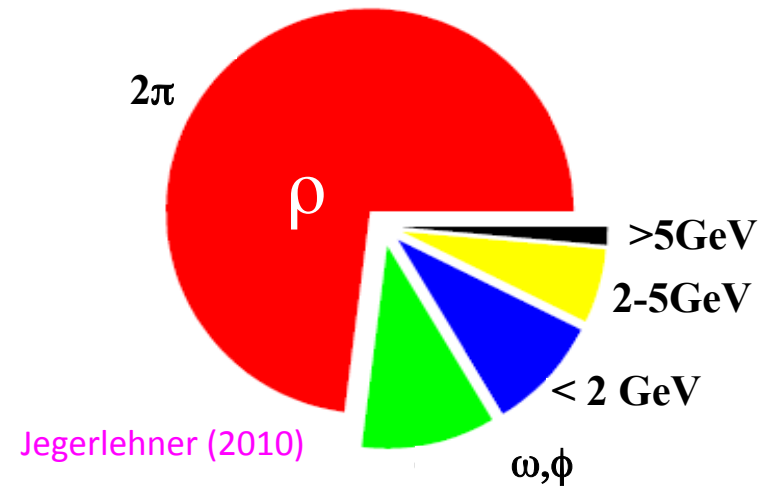


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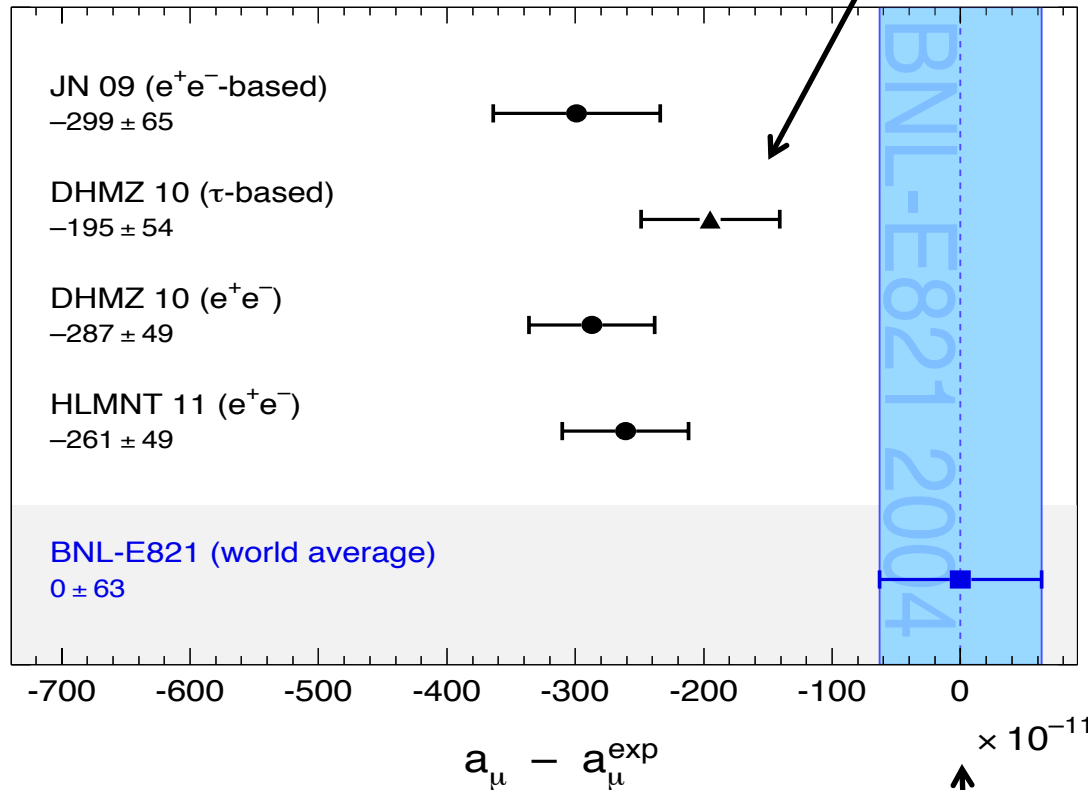
Intrinsic  $\sim 1/s^2$   
**low energy contributions**  
 especially important!





# Muon Anomaly $(g-2)_\mu$

## Standard Model predictions $(g-2)_\mu$



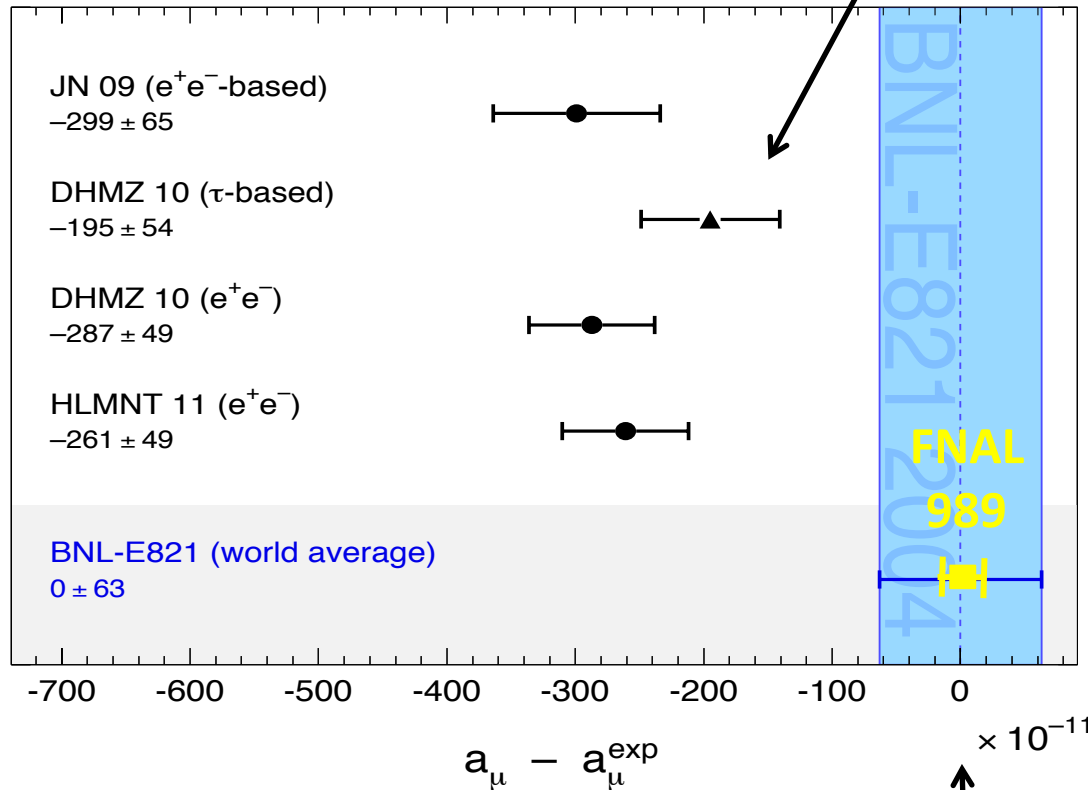
$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (28.7 \pm 8.0) \cdot 10^{-10} \quad (3.6 \sigma)$$

**Error(s) or New Physics ?**

**E821 measurement of  $(g-2)_\mu$**

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**Error(s) or New Physics ?**

**New FNAL 989  $(g-2)_\mu$  measurement (2015):**

Factor 4 improvement  
in experimental error

# *Hadronic Cross Section Data and $\alpha_{em}(M_Z^2)$*

---

## Running of $\alpha_{em}(s)$ with $s$ due to vacuum polarization corrections

- Leptonic Vacuum Polarization calculable within QED
- Hadronic Vacuum Polarization not accessible in pQCD → **Dispersion relation**

$$\alpha_{em}(s) = \frac{\alpha(0)}{(1 - \Delta\alpha_{em}(s))} \quad \alpha^{-1}(M_Z^2) = 128.962 \pm 0.014$$

Davier, et al. (2010)

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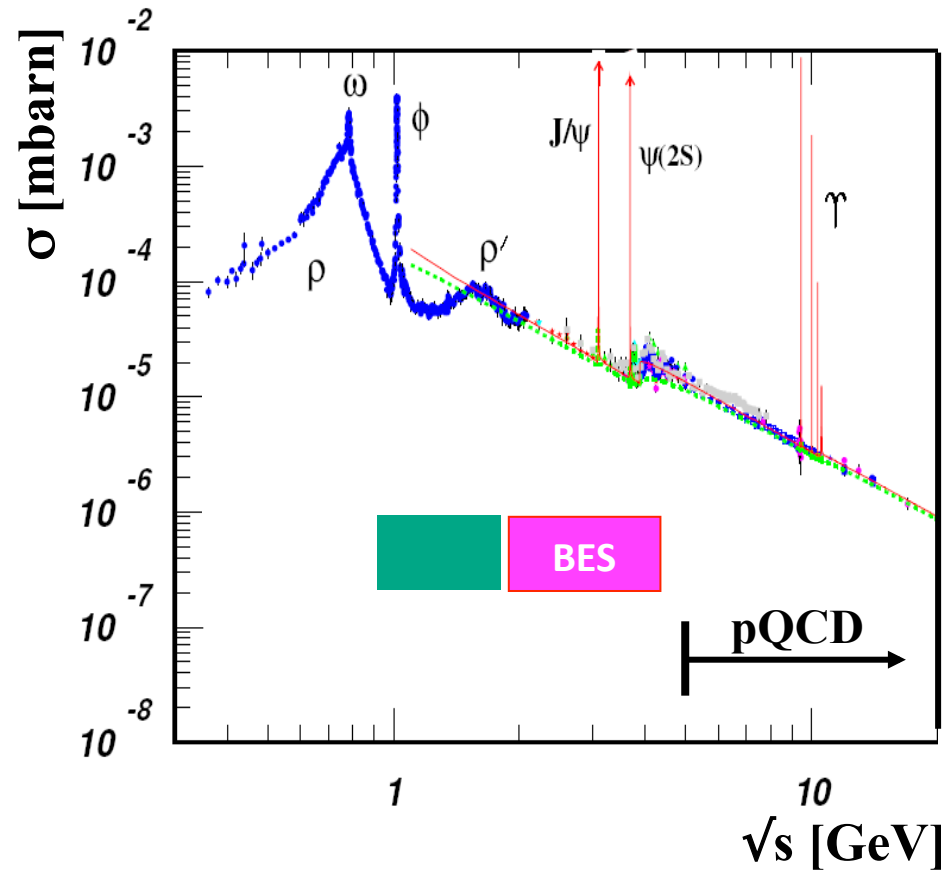
Davier, et al. (2010)

$$\begin{aligned} \text{QED } \Delta\alpha_{lep}(M_Z^2) &= 314.97686 \cdot 10^{-4} \\ \text{strong } \Delta\alpha_{had}(M_Z^2) &= (274.2 \pm 1.0) \cdot 10^{-4} \end{aligned}$$

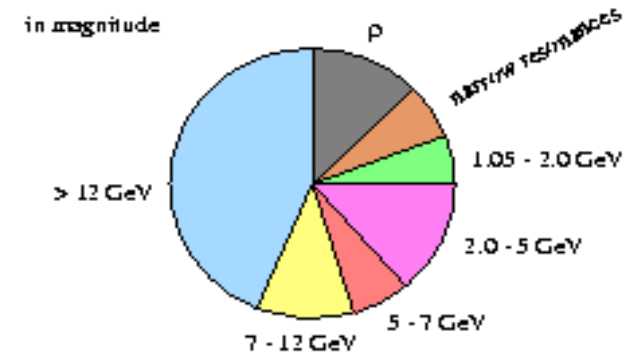
dispersion integral relates  $\sigma_{had}$   
with  $\Delta\alpha_{em}^{had}$

→ R data up to few GeV essential, above use pQCD !

# Hadronic Cross Section Data and $\alpha_{em}(M_Z^2)$



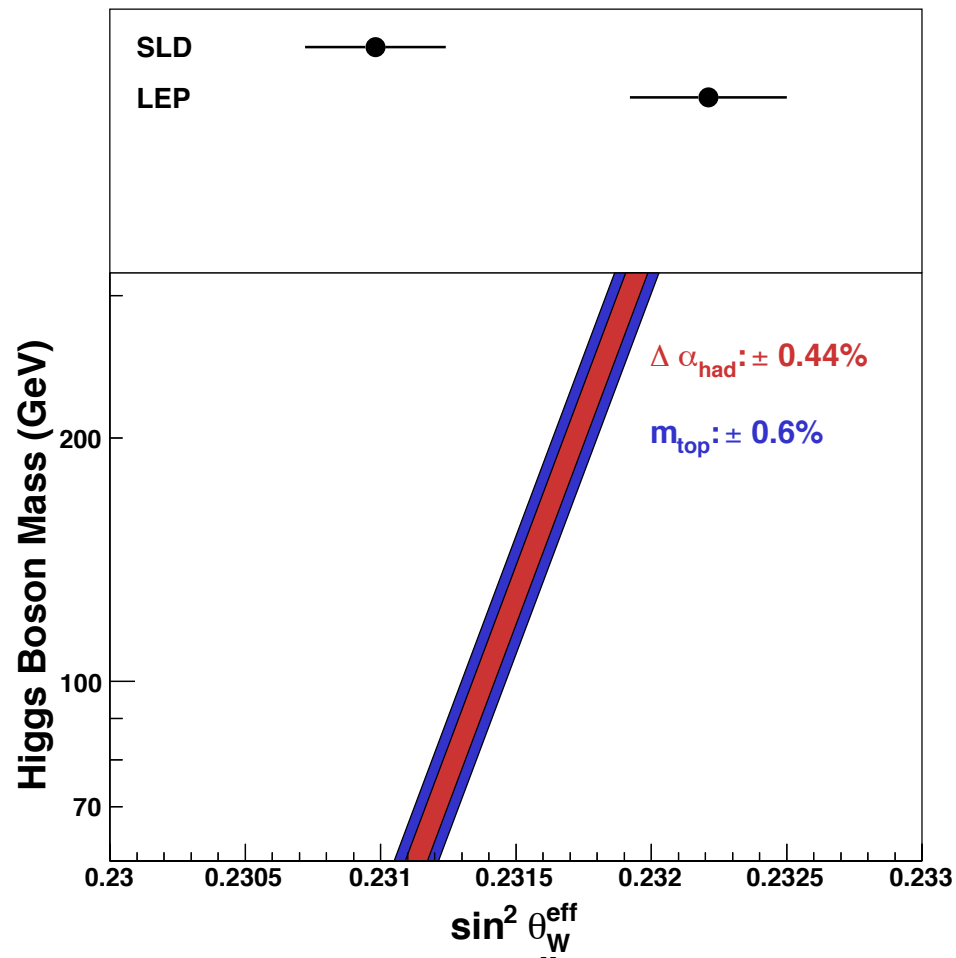
contributions at  $m_Z$  Burkhardt, Pietrzyk 2001



# Electroweak Precision Physics

## $\alpha_{em}(M_Z^2)$ limiting electroweak precision fits

- Test overall consistency of the electroweak Standard Model
- Since the discovery of the Higgs boson more timely than ever

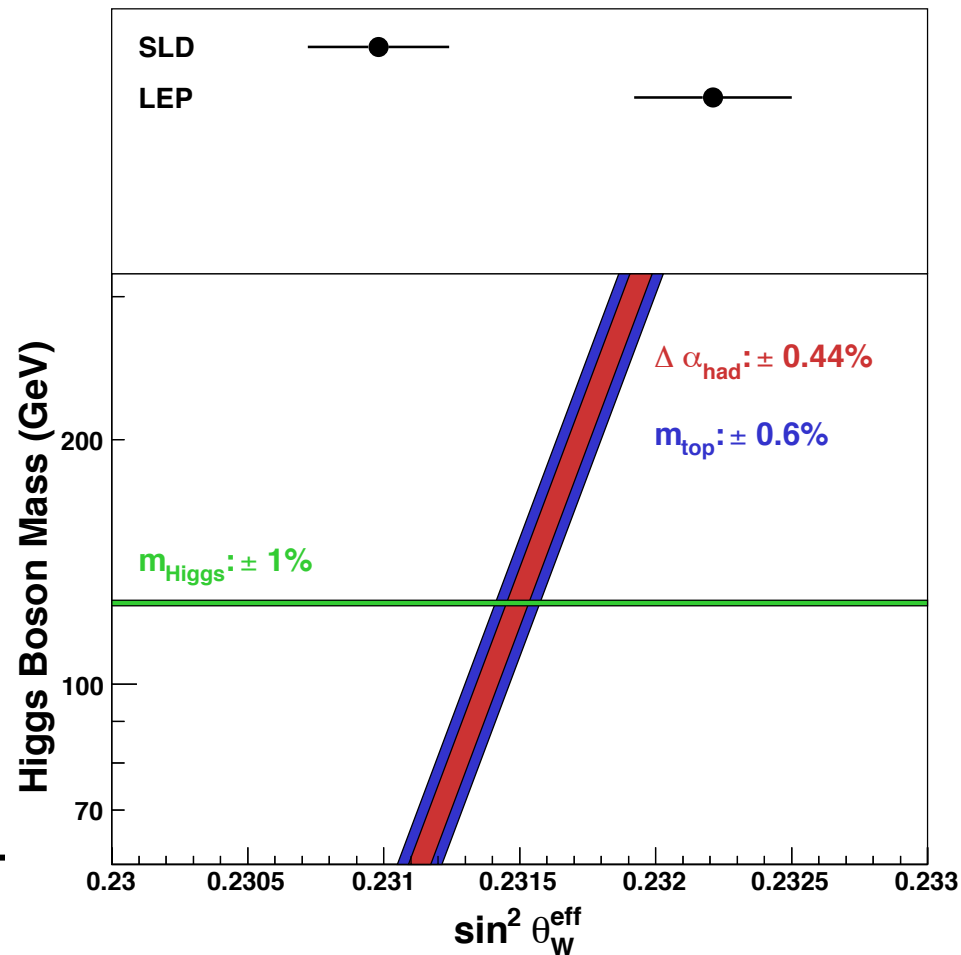


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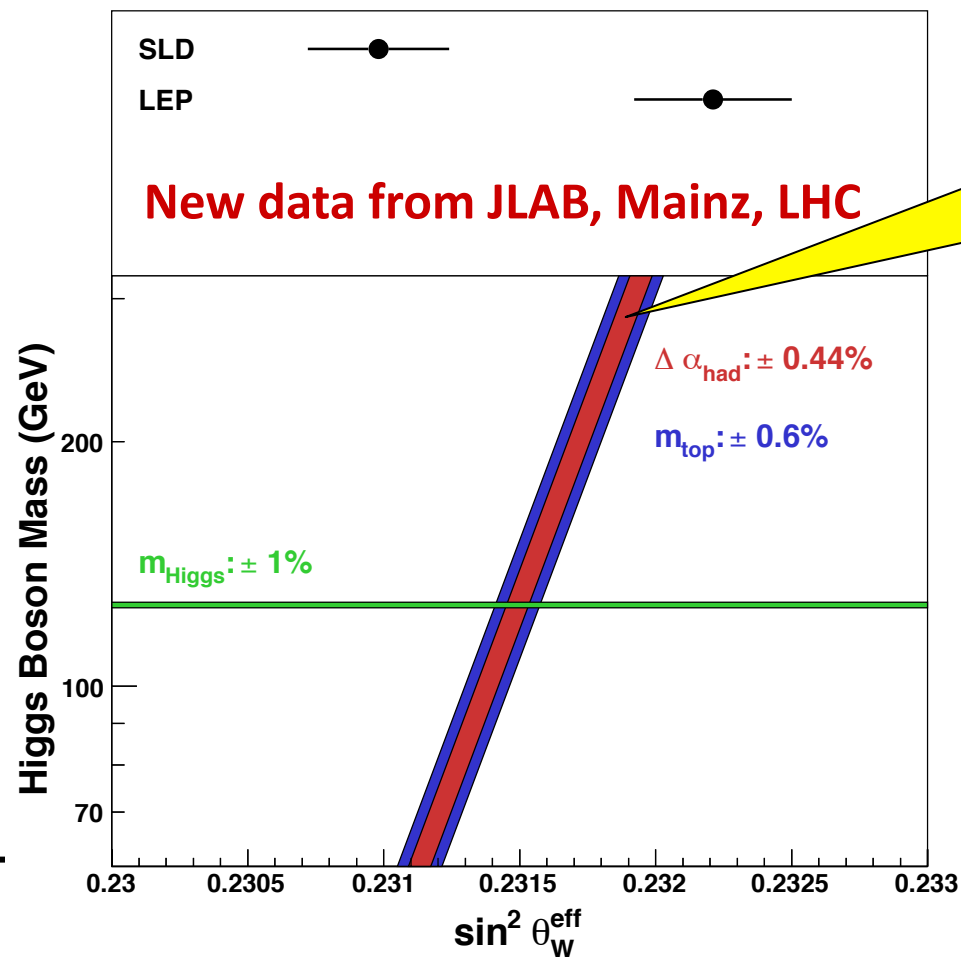


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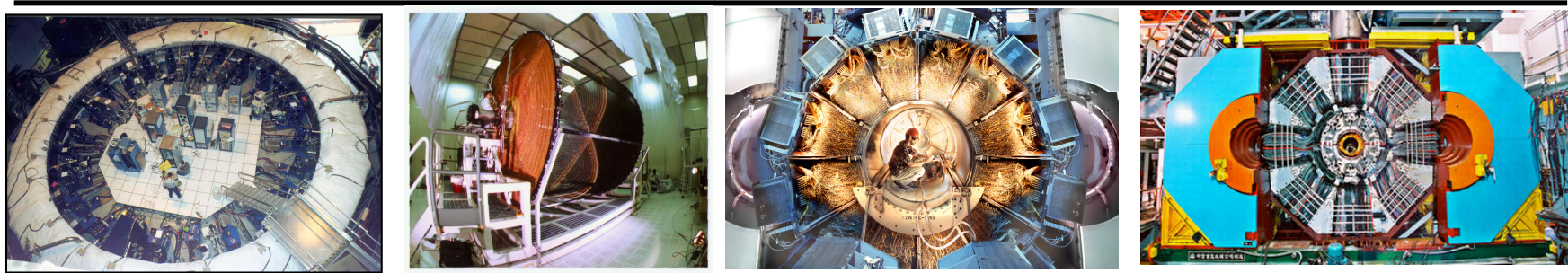
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SM running  
 $\sin^2 \theta_W (M_{\text{Higgs}})$   
 limited by  $\alpha_{em}$



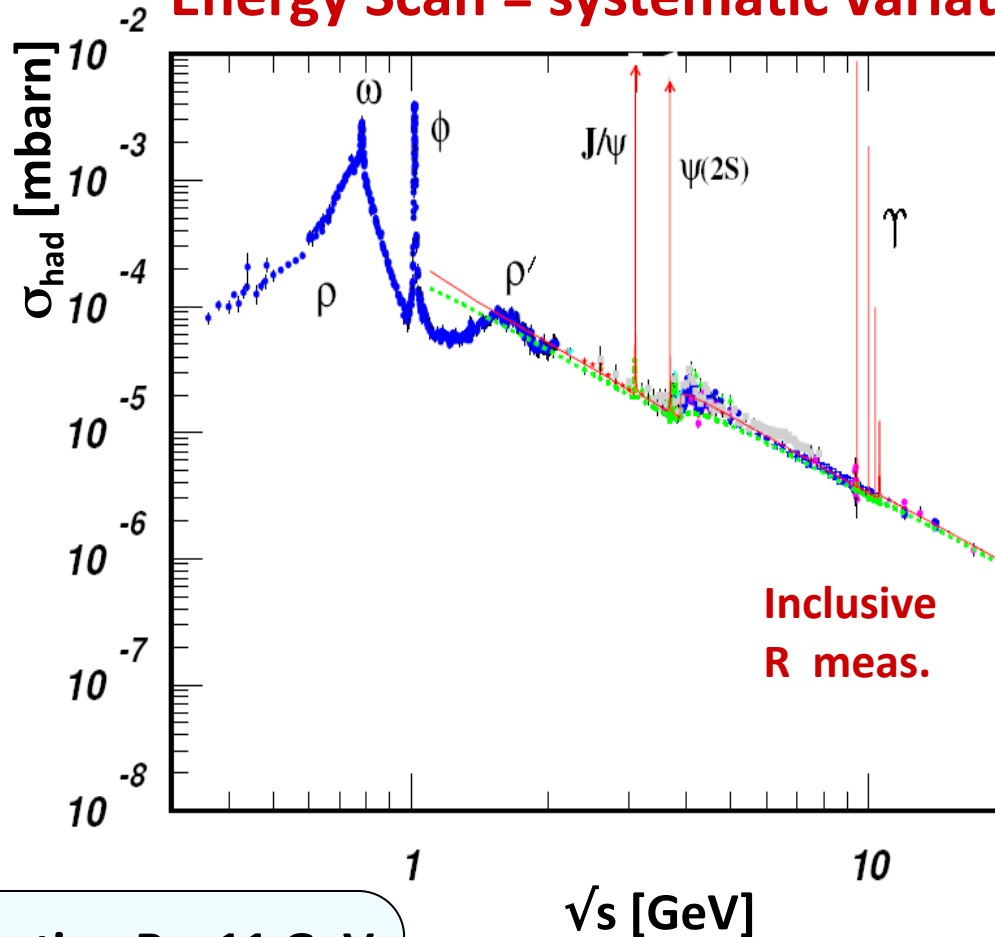


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- Motivation:  $(g-2)_\mu$  &  $\alpha_{\text{QED}}(M_Z^2)$
- **Results Energy Scan and ISR**
- Perspectives at BES-III
- Conclusions and Future Perspectives

# Hadronic Cross Section via Energy Scan

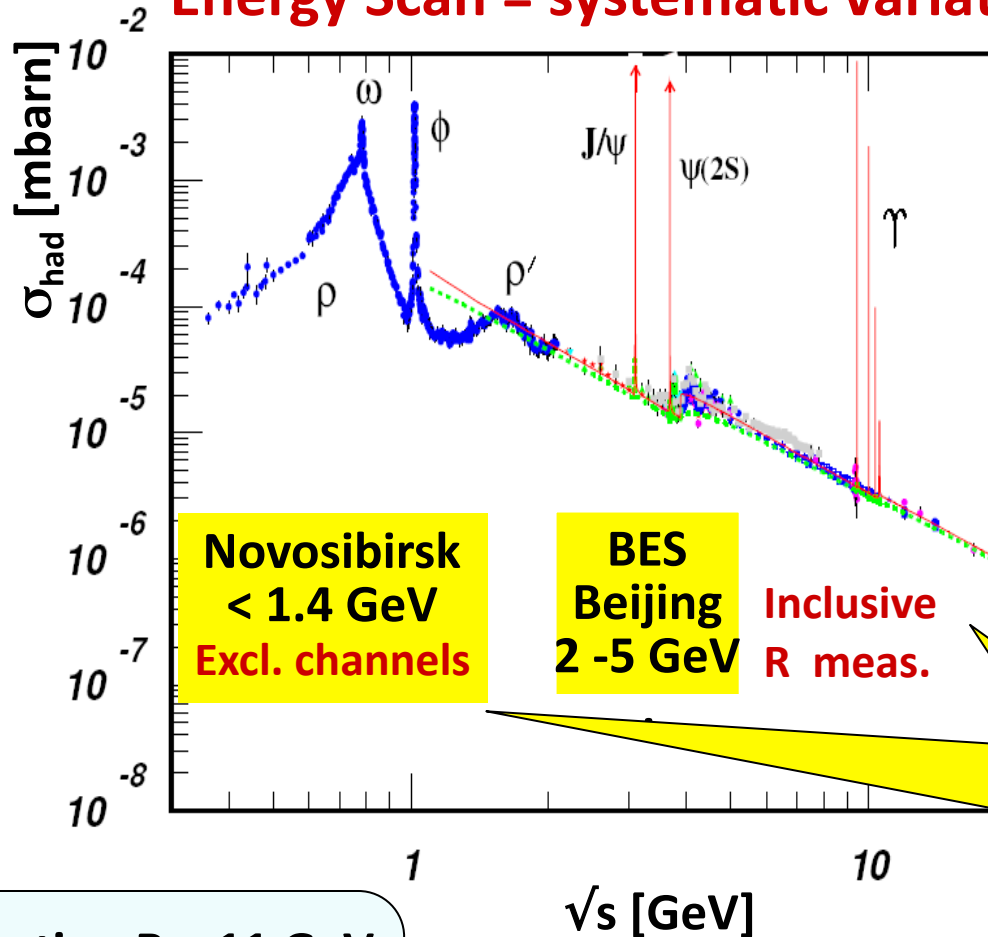
**Energy Scan = systematic variation of collider's  $\sqrt{s}$**



**1<sup>st</sup> Generation R < 11 GeV**  
 → 60's, 70's, 80's, 90's  
 measurements from Orsay,  
 Frascati, SLAC, Novosibirsk

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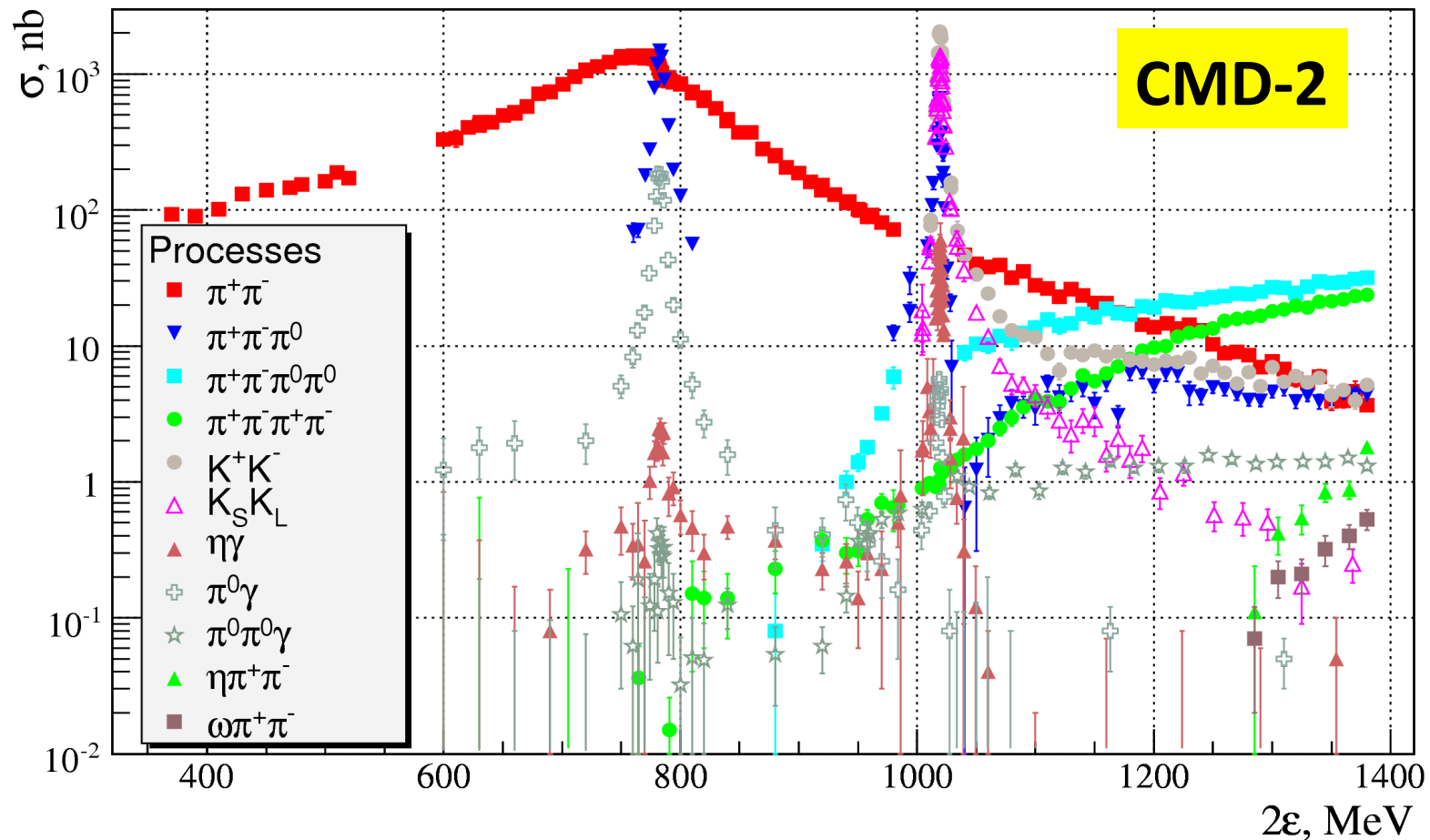


**2<sup>nd</sup> Generation Expts.**  
 → new millenium  
 VEPP-2M Novosibirsk  
 BEPC Beijing

**1<sup>st</sup> Generation R < 11 GeV**  
 → 60's, 70's, 80's, 90's  
 measurements from Orsay,  
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# Overview Novosibirsk Results

- **CMD-2:  $\pi^+\pi^- < 1\%$ , higher multiplicities few % accuracy**
- **SND measurement of  $\pi^+\pi^-$  with 1.2% accuracy**



# VEPP-2000: Upgrade towards $E_{\max} = 2.0 \text{ GeV}$

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## VEPP-2000 (since 2010):

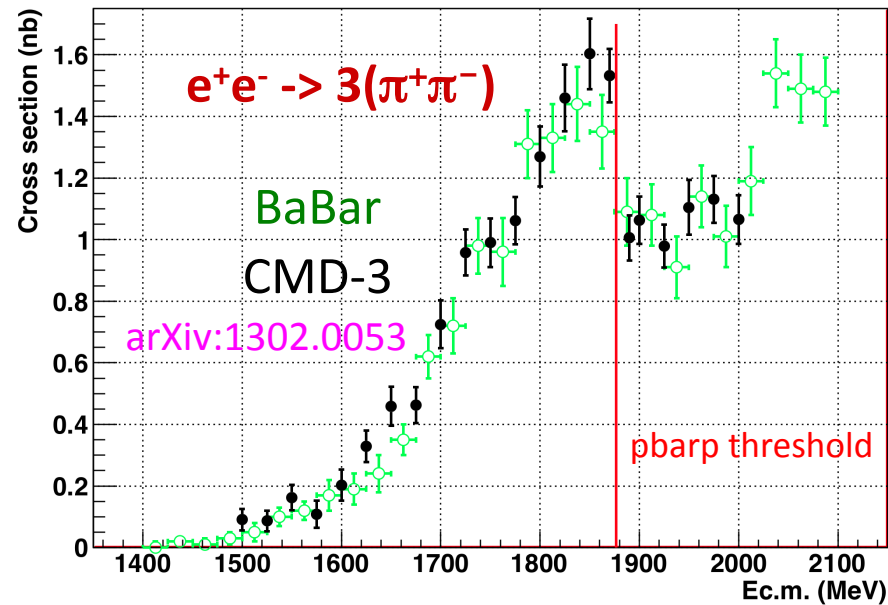
- Upgrade towards  $E_{\max} = 2.0 \text{ GeV}$
- $L_{\max} = 1 \cdot 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$  at 2 GeV
- Upgrade of detectors CMD-3, SND

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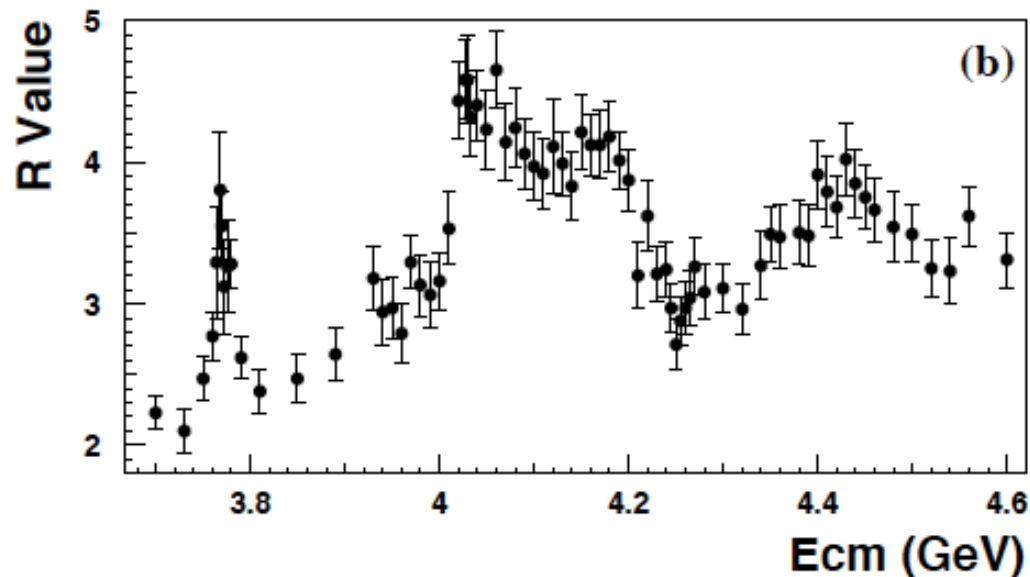
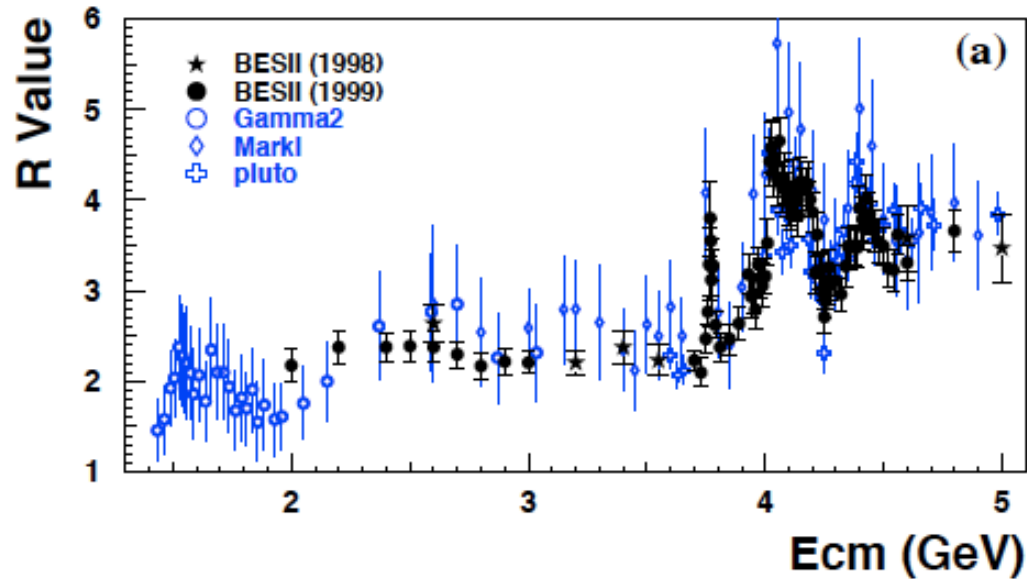


## *Brief History of BES R Measurements*

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- Pre-study, using BES I tau mass data, 12 points around 3.55 GeV,  $\sim 8.5\%$ , HEP&NP24, 609 (2000);
- Test run, 6 continuum points in 2.6 ~ 5.0 GeV, PRL84, 594 (2000);
- **Full scan, 85 points in 2 ~ 4.8 GeV, PRL88, 101802 (2002);**
- R around  $\psi(3770)$ , 2 points off-resonance, 1 on-resonance, PLB641, 145 (2006);
- **Improvements at 3 continuum points, PLB677, 239 (2009).**

# BEPC: $\sigma_{incl}(e^+e^- \rightarrow \text{Hadrons})$



## Results

- 3-5 % statistical accuracy per scan point
- Systematic uncertainty:  $\sim 5 \dots 8\%$

- **Major improvement of R**
- **Best measurement to date**
- **Important QCD test**
- **Of utmost importance for  $\alpha_{em}(m_Z^2)$**



# Initial State Radiation (ISR)

**New and completely complementary ansatz:**

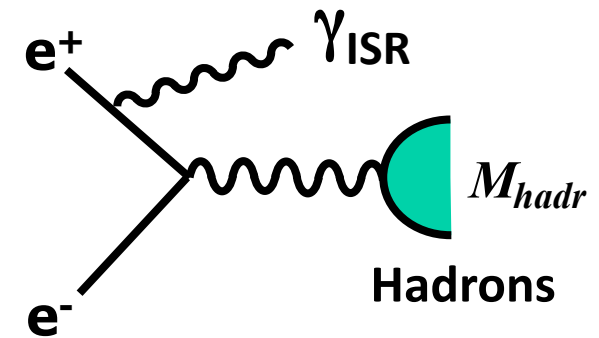
Consider events with **Initial State Radiation (ISR)**

**W. Kluge: "A success story"**

Binner, Kühn, Melnikov, Phys.Lett. B459 (1999) 279

Benayoun, Eidelman, Invanchenko, Silagadze, 1999, Mod. Phys. Lett. 14, 2605

Druzhinin, Eidelman, Serednyakov, Solodov, Rev. Mod. Phys. 83 (2011) 1545



Charmonium  
production  
Spectroscopy  
e.g.  $\Upsilon(4260)$



Multihadronic form factors  
 $e^+e^- \rightarrow 2\pi, 3\pi, 4\pi, >4 \text{ hadr.}$   
 $(g-2)_\mu, \alpha_{em}(M_Z^2)$   
Light hadron spectroscopy

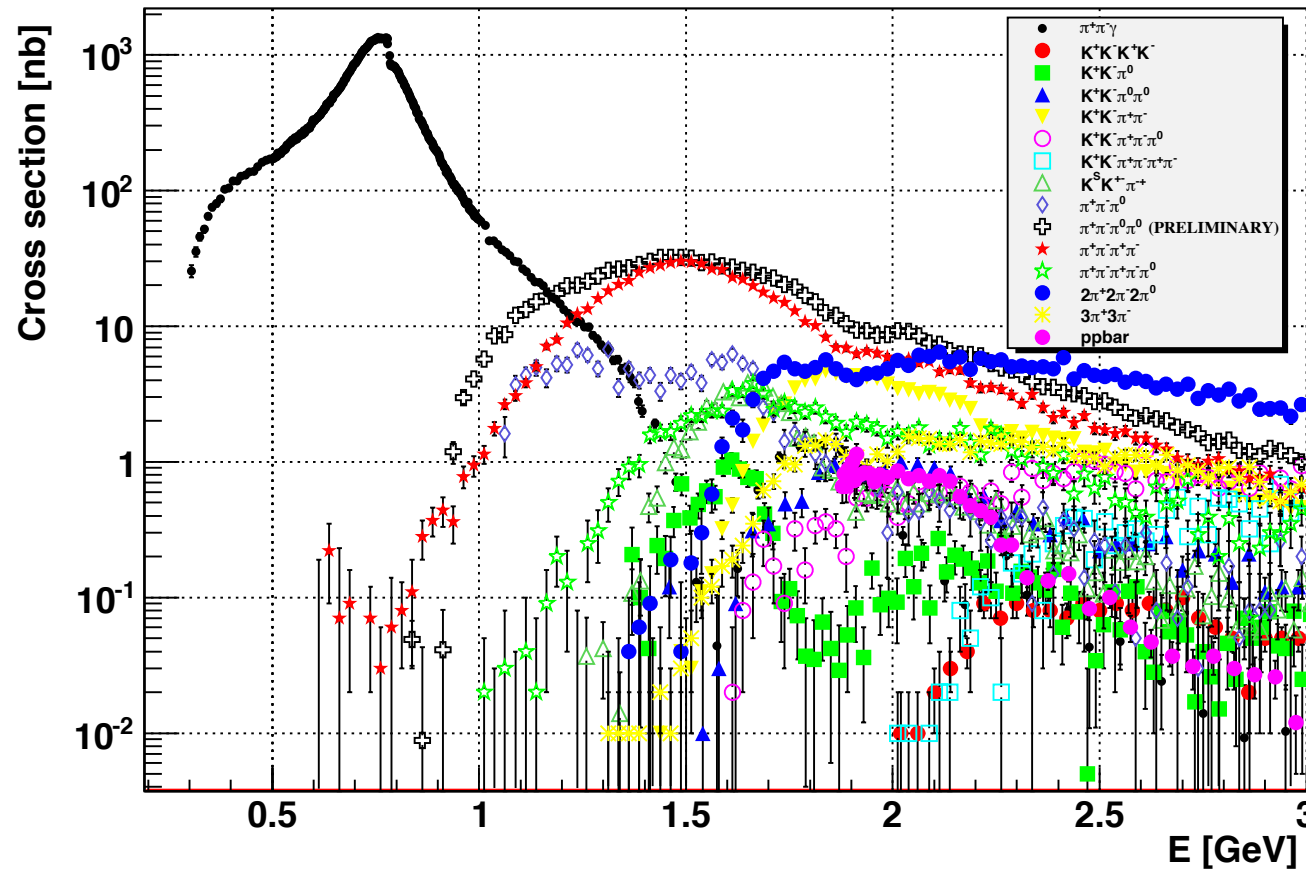


Timelike baryon  
form factors  
Hadron structure




**BABAR**

# Summary of ISR Results



**Precision:**

$2\pi$ : < 1%

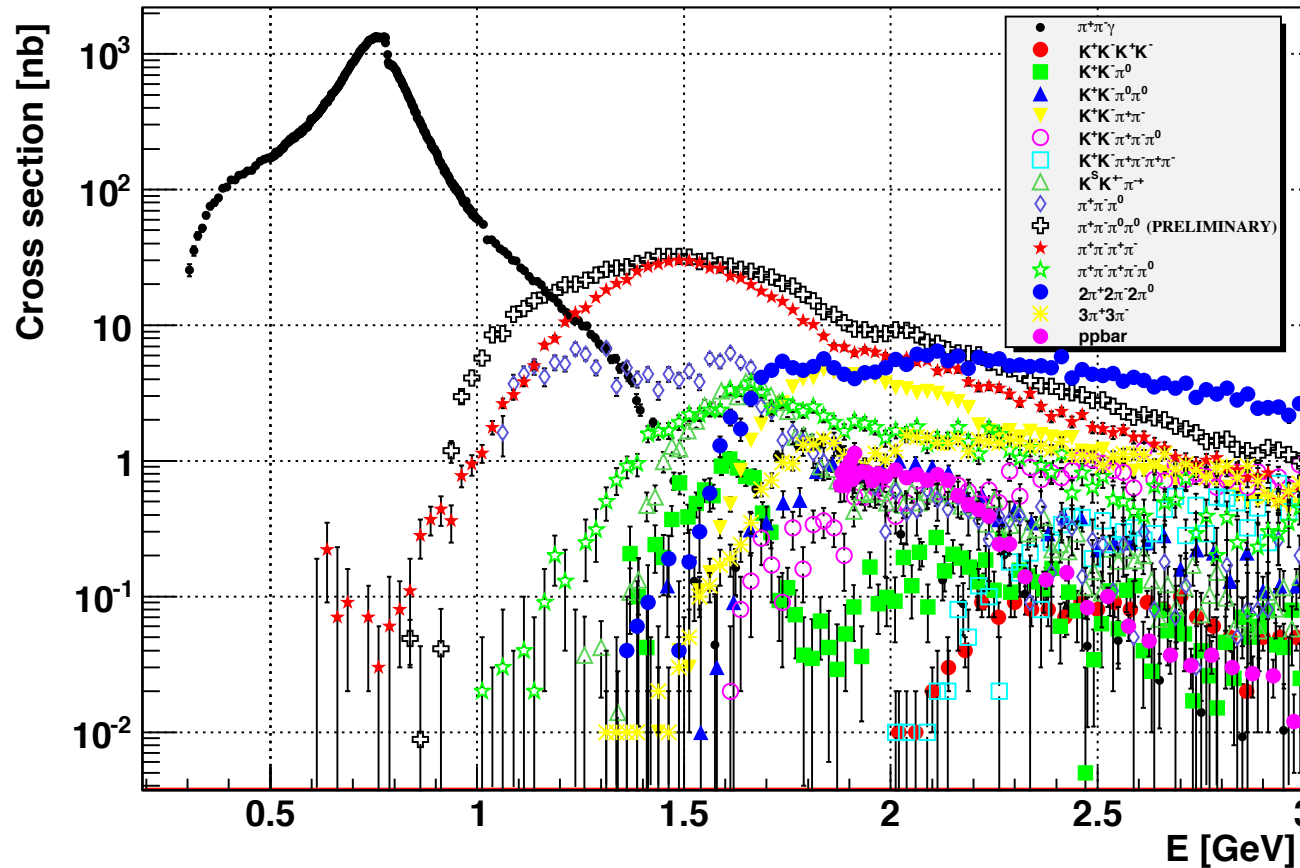
$3\pi$ : ~10%

$4\pi$ : ~3%

$\geq 5\pi$ : 10% and higher


**BABAR**

# Summary of ISR Results



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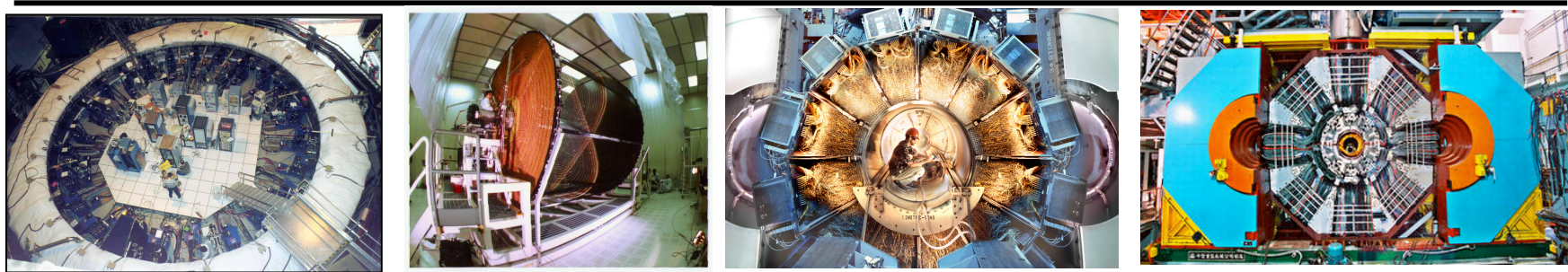
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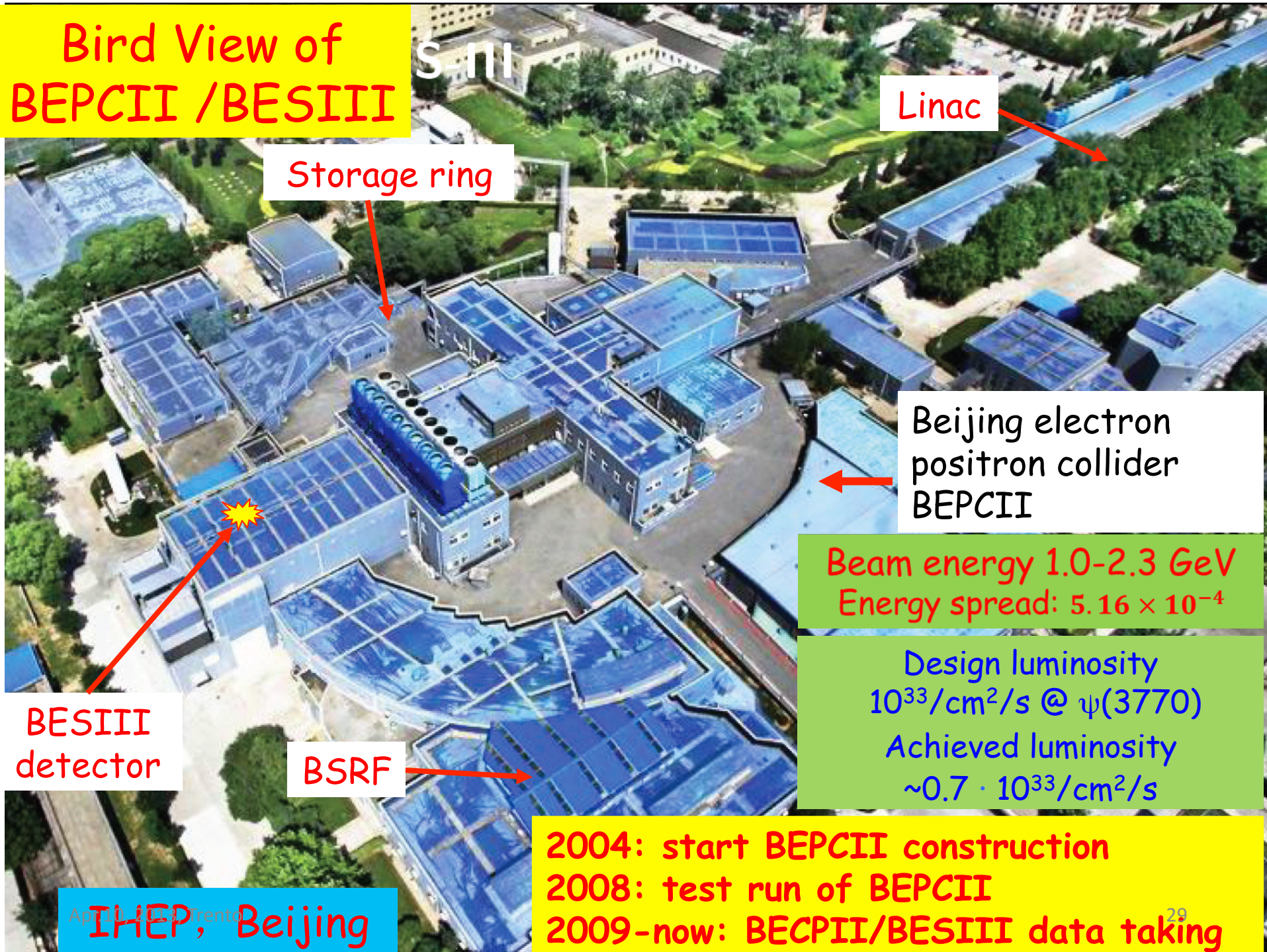
**Measurement of exclusive channels:  
Utmost importance for  $(g-2)_\mu$  but not (yet) competitive with  $R_{\text{incl}} > 2 \text{ GeV}$**



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- Motivation:  $(g-2)_\mu$  &  $\alpha_{\text{QED}}(M_Z^2)$
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# Bird View of BEPCII / BESIII



S III

Linac

Storage ring

Beijing electron positron collider BEPCII

Beam energy 1.0-2.3 GeV  
Energy spread:  $5.16 \times 10^{-4}$

Design luminosity  $10^{33}/\text{cm}^2/\text{s}$  @  $\psi(3770)$   
Achieved luminosity  $\sim 0.7 \cdot 10^{33}/\text{cm}^2/\text{s}$

BESIII detector

BSRF

2004: start BEPCII construction  
2008: test run of BEPCII  
2009-now: BEPCII/BESIII data taking

IHEP, Beijing

# The BESIII Detector

Drift Chamber (MDC)

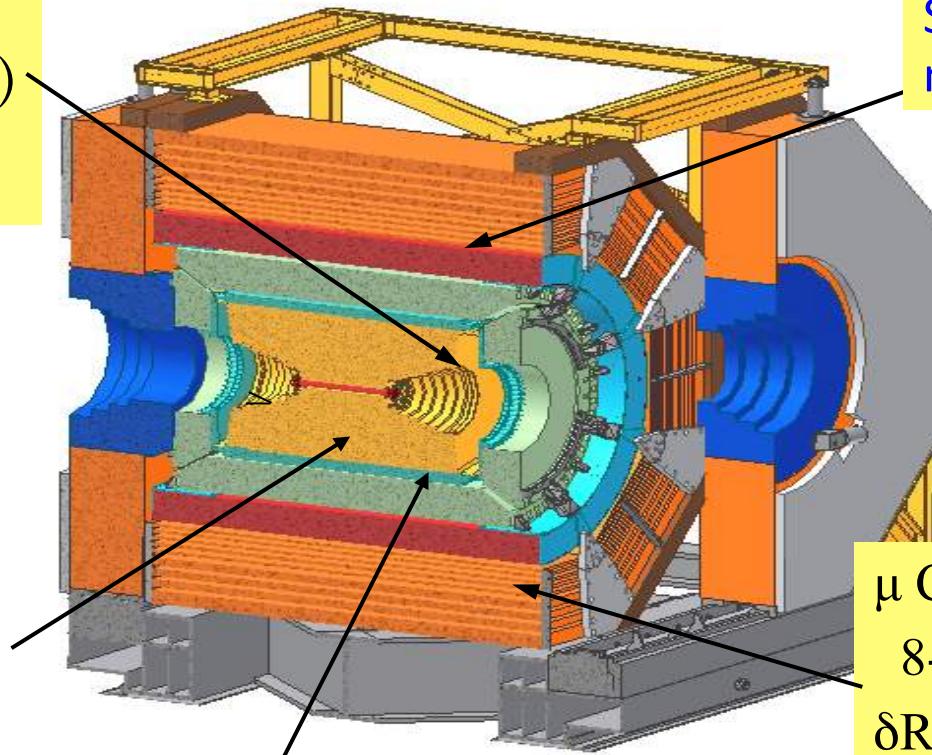
$$\sigma_{p/p} (\%) = 0.5\% (1\text{GeV})$$

$$\sigma_{dE/dx} (\%) = 6\%$$

Time Of Flight (TOF)

$$\sigma_T: 90 \text{ ps Barrel}$$

$$110 \text{ ps endcap}$$



Super-conducting  
magnet (1.0 Tesla)

$\mu$  Counter

8- 9 layers RPC

$$\delta R\Phi = 1.4 \text{ cm} \sim 1.7 \text{ cm}$$

EMC:  $\sigma_{E/\sqrt{E}} (\%) = 2.5\% (1 \text{ GeV})$   
(CsI)  $\sigma_{z,\phi} (\text{cm}) = 0.5 - 0.7 \text{ cm}/\sqrt{E}$

# *Run Planning*

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## R measurement foreseen in 3 phases

- Phase 1:**      **R in range 2 – 4.5 GeV**  
~ $10^4$  events per scan point, 3% systematic accuracy  
→ improve  $\alpha_{\text{QED}}(m_Z^2)$  by factor 2
- Phase 2:**      **R in range 2 – 3 GeV, high statistics**  
> $10^5$  events per scan point  
→ Improve nucleon  $|G_E|/|G_M|$  ratio, Nucleon FF
- Phase 3:**      **Fine binning R ratio in charmonium region**  
→ charmonium spectroscopy

# Phase 1: Precision R Scan

---

$$R = \frac{1}{\sigma_{\mu+\mu^-}} \cdot \frac{N_{had} - N_{bg}}{L \cdot \epsilon_{had} \cdot (1 + \delta)}$$

$N_{had}$ : observed hadronic events

$N_{bg}$ : background events

$L$ : integrated luminosity

$\epsilon_{had}$ : detection efficiency for  $N_{had}$

$\delta$ : radiative correction factor

$\sigma_{\mu\mu}$ : calculated within QED.

Measurement of  $R$  is a measurement of  $\sigma(e^+e^- \rightarrow \text{hadrons})$

**Except for controlling each item to the precision requested, stable long term machine and detector performance is crucial.**



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**Except for controlling each item to the precision requested, stable long term machine and detector performance is crucial.**

**Our goal:  
3% precision**

## *Phase 1: Mini R Scan (2012)*

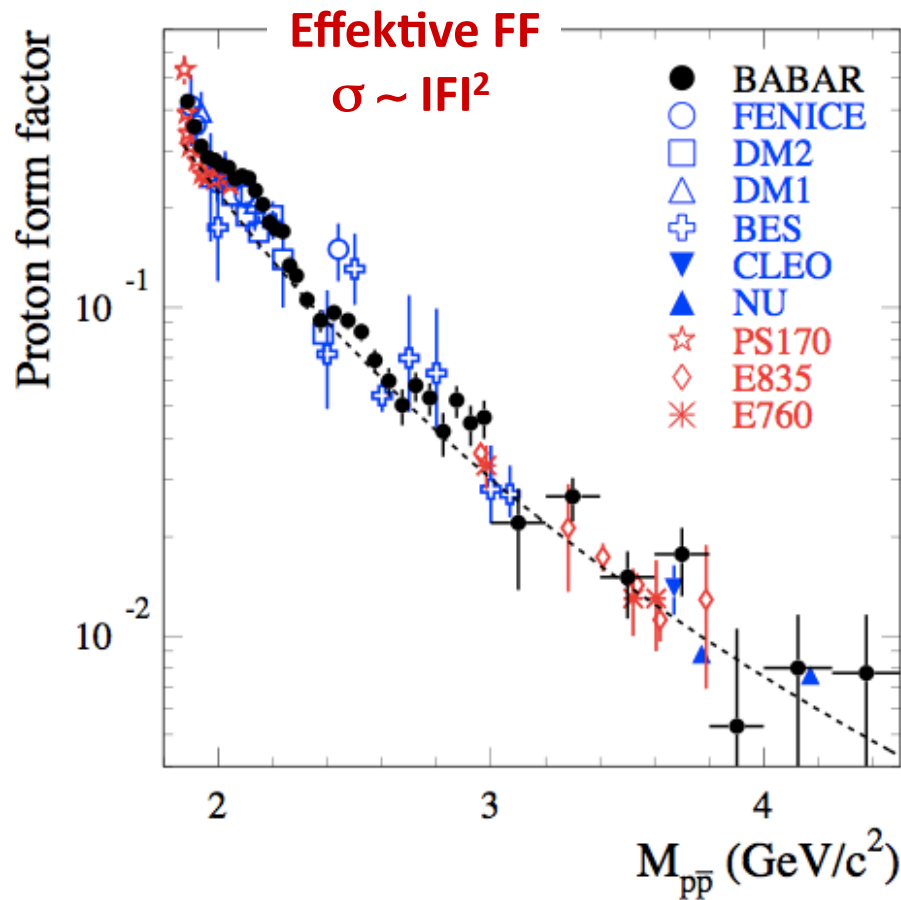
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- BESIII collected data at 2.23, 2.4, 2.8 and 3.4 GeV during June 8-16, 2012;
- Total integrated luminosity  $\sim 12 \text{ pb}^{-1}$ ;
- Useful information for machine at low energy;
- The data being used for MC generator tuning;
- Necessary to establish analysis chain;
- Baryon form factors, fragmentation function study underway.

# Phase 2: Nucleon EM Form Factors

$$\sigma_{e^+e^- \rightarrow N\bar{N}} = \frac{4\pi\alpha^2\beta}{3s} C_N(s) \left[ |G_M^N(q^2)|^2 + \frac{2M_N^2}{s} |G_E^N(q^2)|^2 \right]$$

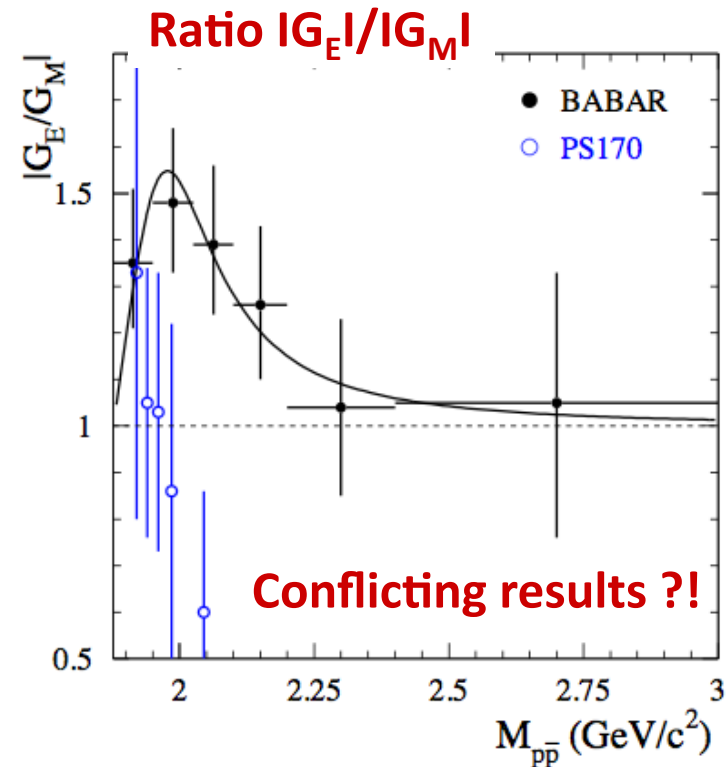
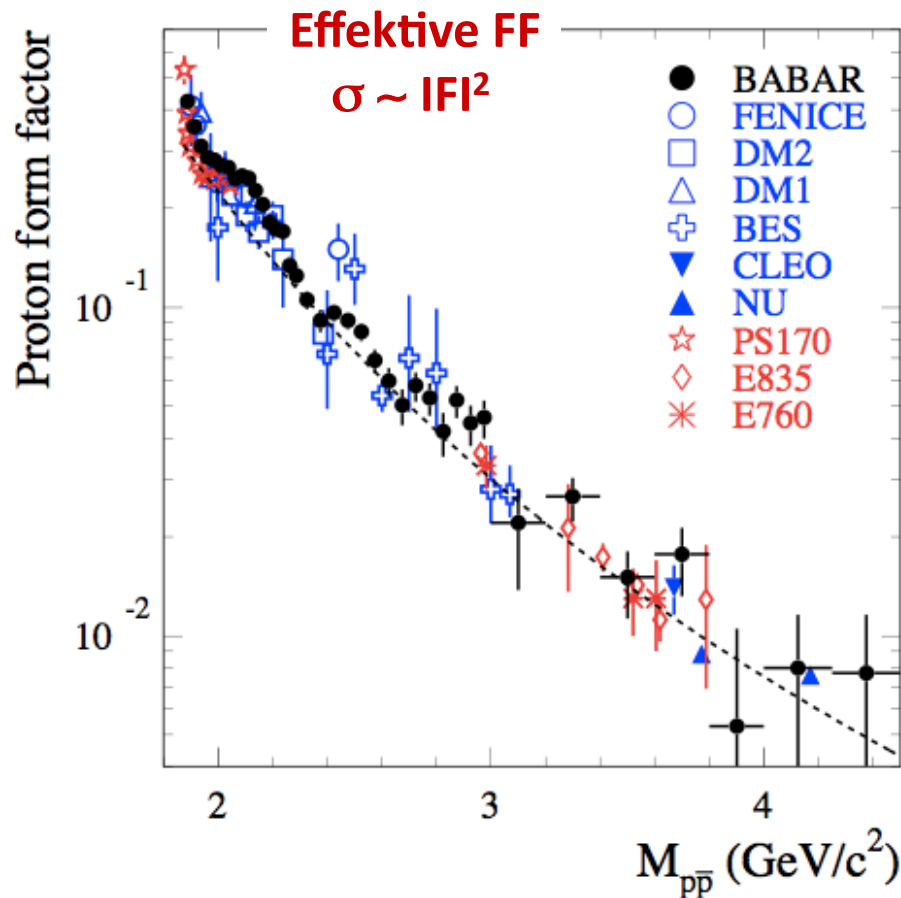
Cross section parametrized by magnetic and electric form factors  $G_M$  and  $G_E$



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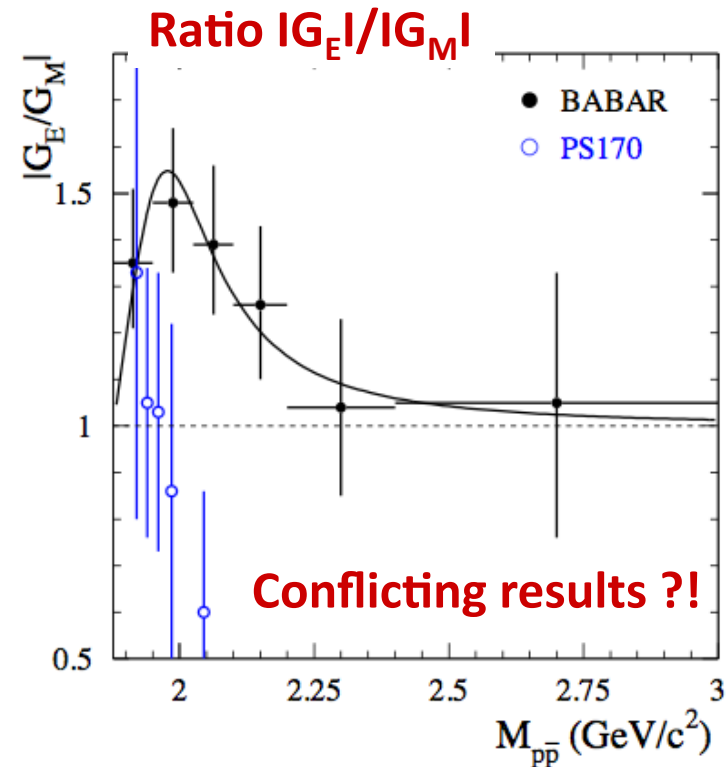
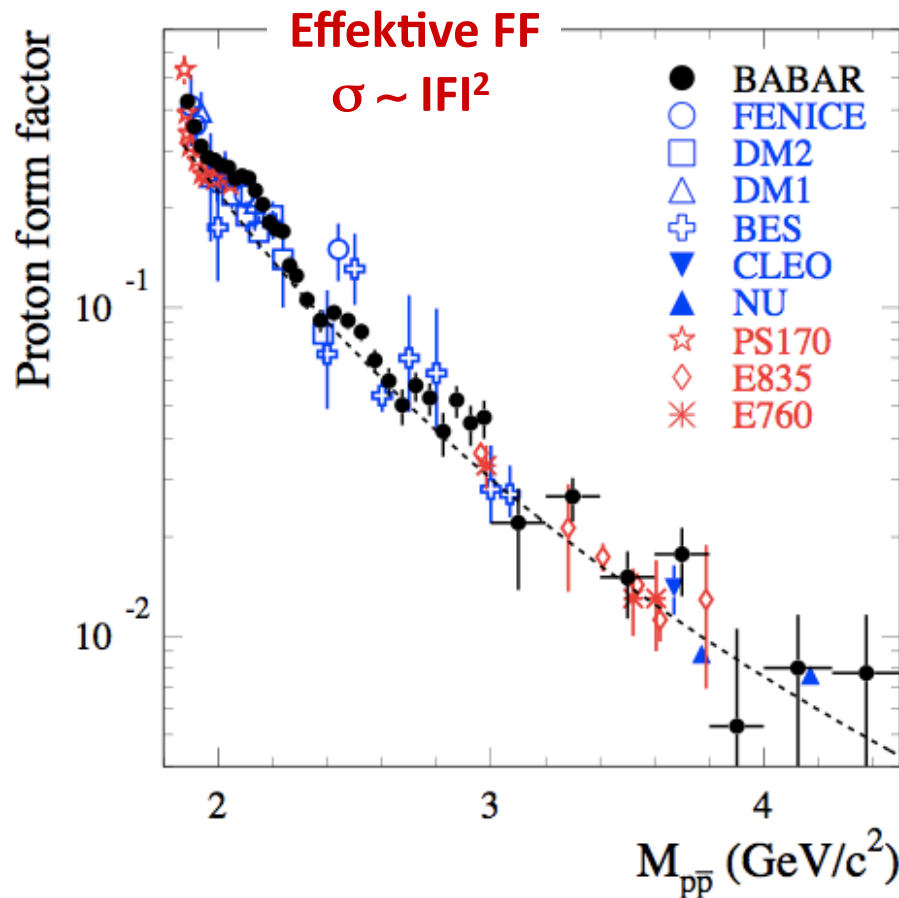
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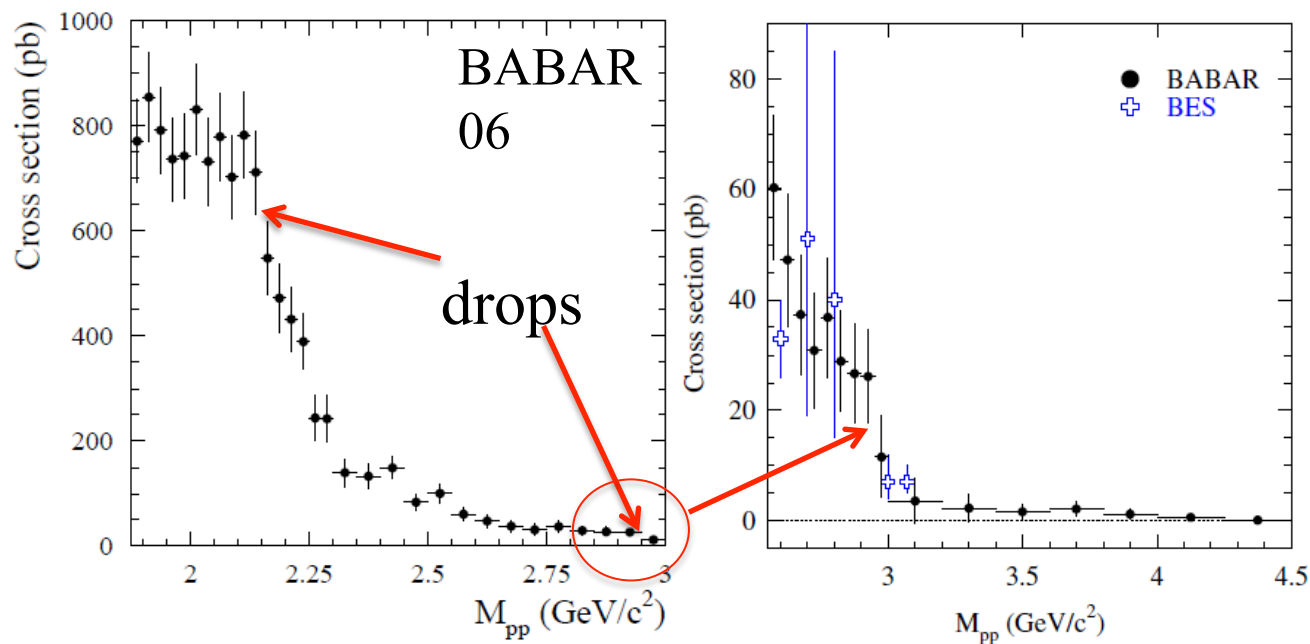
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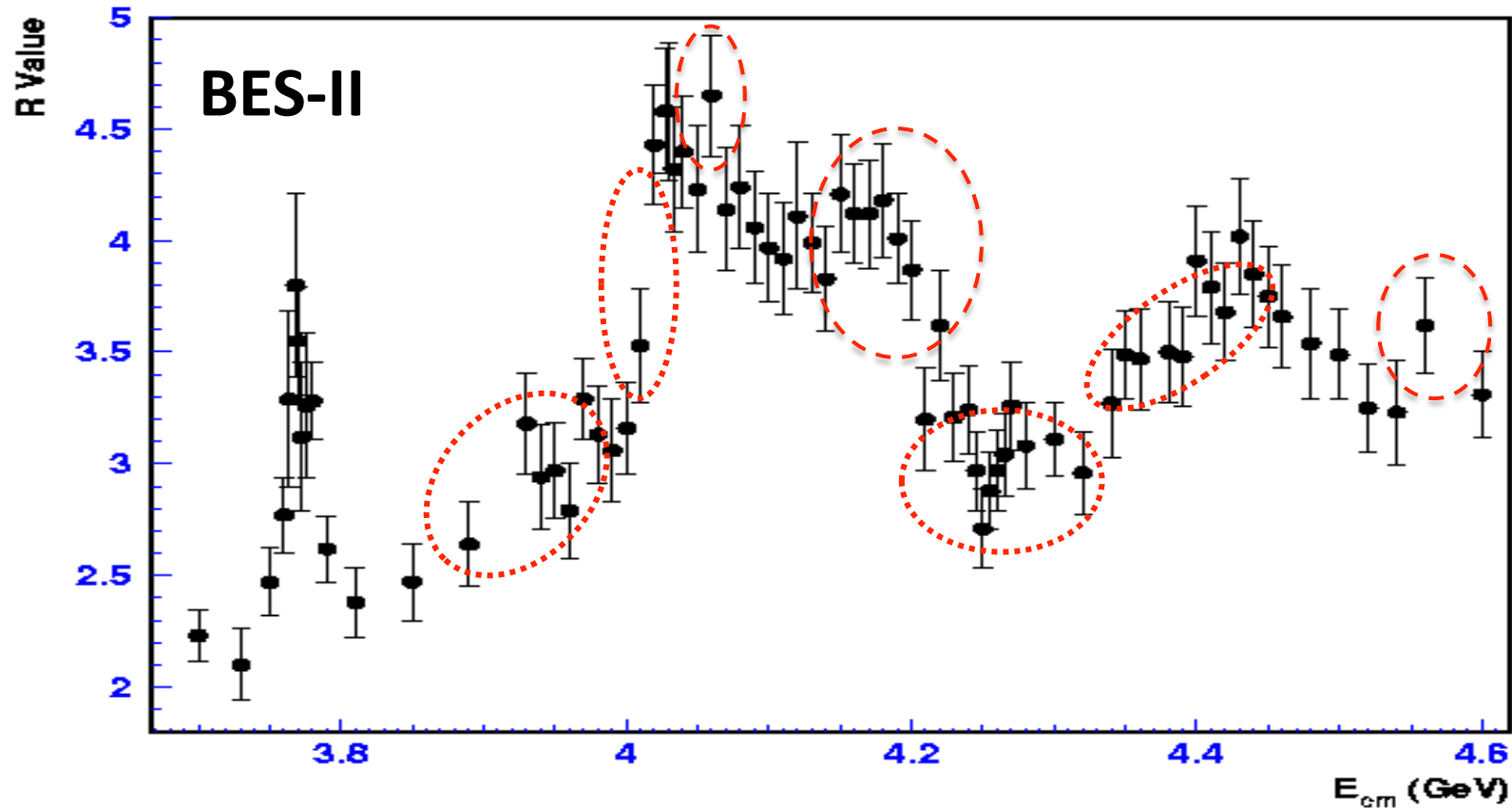


## Phase 2: Nucleon EM Form Factors

- Finer scan around 2.15 GeV:  $\Upsilon(2175)$ ? Where there is also a drop in the  $pp$  invariant mass;
- And another drop at 2.9 GeV;
- To explore even lower energy 1.8-2 GeV ?  $\rightarrow$  ISR, Scan?

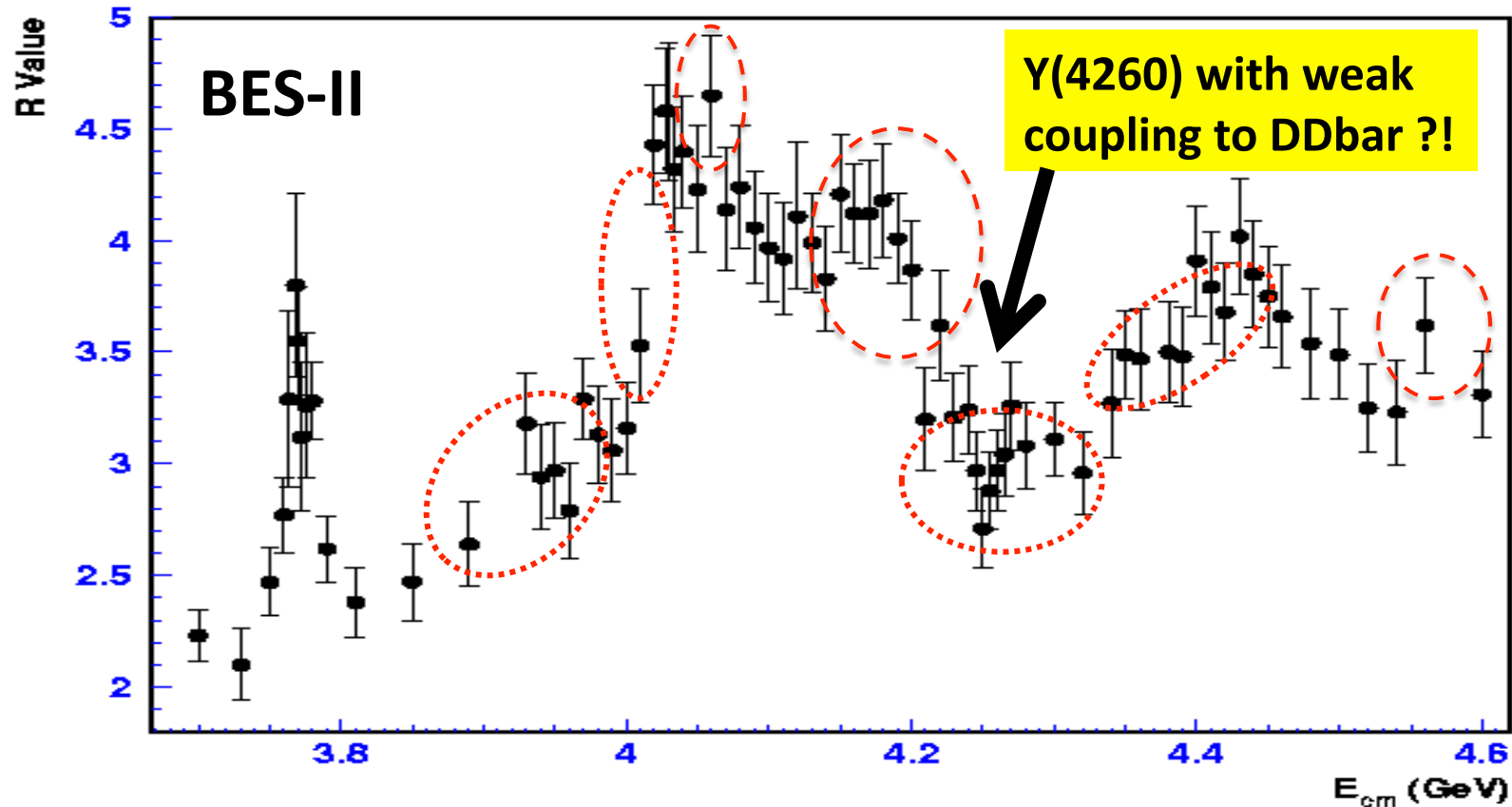


# Phase 3: Charmonium Spectroscopy



- **What** are these broad resonances?
- Mass region where some **X, Y, Z particles** are found.
- Possible **new** resonance which are not yet discovered?

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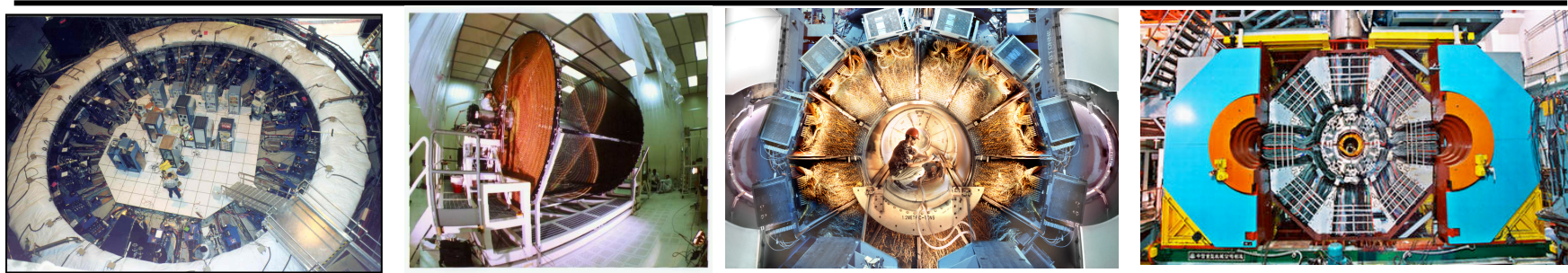
### Understanding the nature of charmonium resonances:

All possible two-body decays of  $\psi(3770)$ ,  $\psi(4040)$ ,  $\psi(4160)$ ,  $\psi(4415)$  need to be included in the fit

$$\begin{aligned} \psi(3770) &\Rightarrow D\bar{D}; \\ \psi(4040) &\Rightarrow D\bar{D}, D^*\bar{D}^*, D\bar{D}^*, \bar{D}D^*, D_s\bar{D}_s; \\ \psi(4160) &\Rightarrow D\bar{D}, D^*\bar{D}^*, D\bar{D}^*, \bar{D}D^*, D_s\bar{D}_s, D_s\bar{D}_s^*; \\ \psi(4415) &\Rightarrow D\bar{D}, D^*\bar{D}^*, D\bar{D}^*, \bar{D}D^*, D_s\bar{D}_s, D_s\bar{D}_s^*, D_s^*\bar{D}_s^*. \end{aligned}$$

We need **high statistic data taken at each peak** position to measure the resonance parameters and to know the cross section of their **exclusive decay channels**.

- Non-resonant contribution
- Open charm threshold



## *Outline*

- Motivation:  $(g-2)_\mu$  &  $\alpha_{\text{QED}}(M_Z^2)$
- Results Energy Scan
- Results Radiative Return
- **Conclusions and Future Perspectives**

# Summary

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- Tremendous progress over past years in our knowledge of  $R$  at low energies
- Pivotal role of Radiative Return technique
- Relevant for determination of QCD parameters
- Precision Test of the Standard Model
  - Muon anomaly  $(g-2)_\mu$ :  
Improvement by  $\sim$ factor 3 in knowledge of hadronic vacuum polarization;  
in ca. 10 years; Timely topic: new FNAL experiment
  - Electromagnetic fine structure constant  $\alpha_{em}(m_Z^2)$ :  
After Higgs discovery new quality of electroweak precision fits possible

# Outlook

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## New e+e- facilities have started data taking or will start shortly

- Upgraded DAPHNE Frascati
  - ISR < 1 GeV
- VEPP-2000 Novosibirsk
  - Energy Scan < 2 GeV
- BES-III @ BEPC-II
  - ISR < 3 GeV, R scan 2-5 GeV
- BELLE-2 @ Super-KEKB
  - ISR < 5 GeV

**Within this decade (likely earlier?) further reduction of factor 2 in precision on our knowledge of R not impossible !**

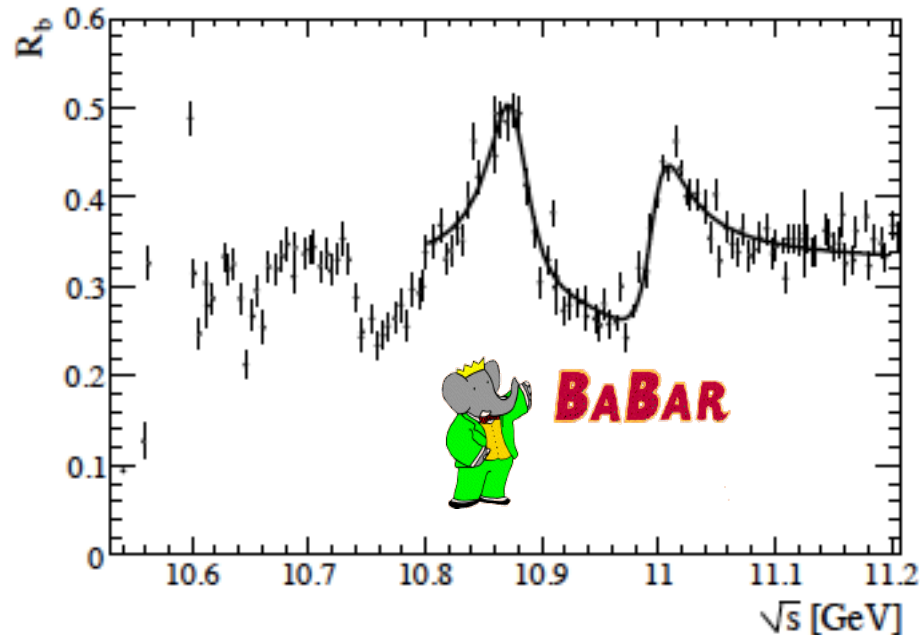
# Additional slides



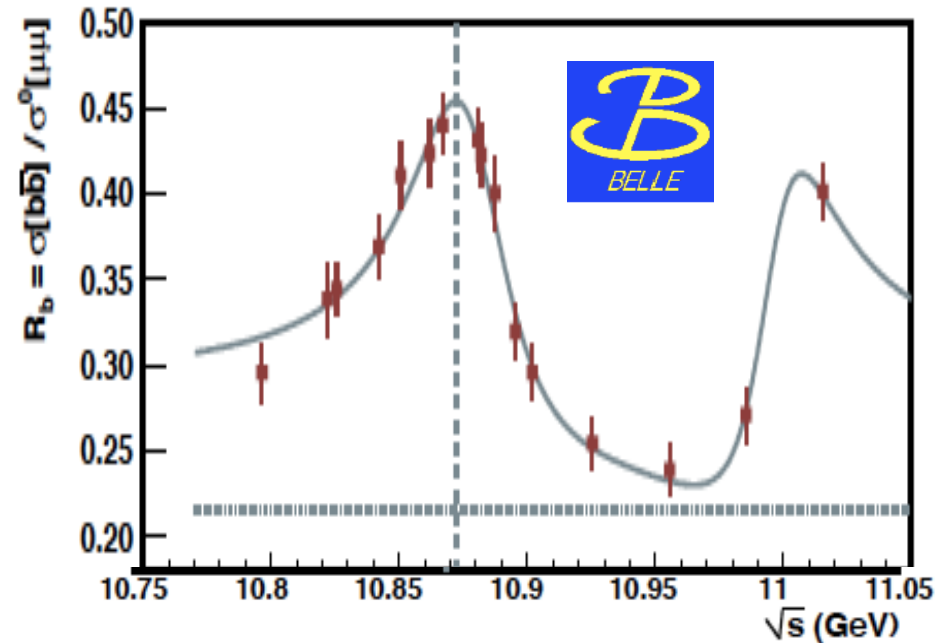
# BABAR and BELLE Scan Bottomonium

## Scan of $R_b = \sigma(e+e^- \rightarrow b\bar{b}) / \sigma(e+e^- \rightarrow \mu+\mu^-)$ in Bottomonium region

arXiv:0808.2445



arXiv:0710.2577



- Identify  $b\bar{b}$  by event shape
- Asymmetric  $Y(5S)$  peak observed
- Difficult interpretation (many channels)
- $Y(5S)$  peak observed as in BABAR
- Anomalous decay patterns of decays from  $Y(5S)$  in lower lying  $Y$  resonances

## *BESIII Data Taking*

---

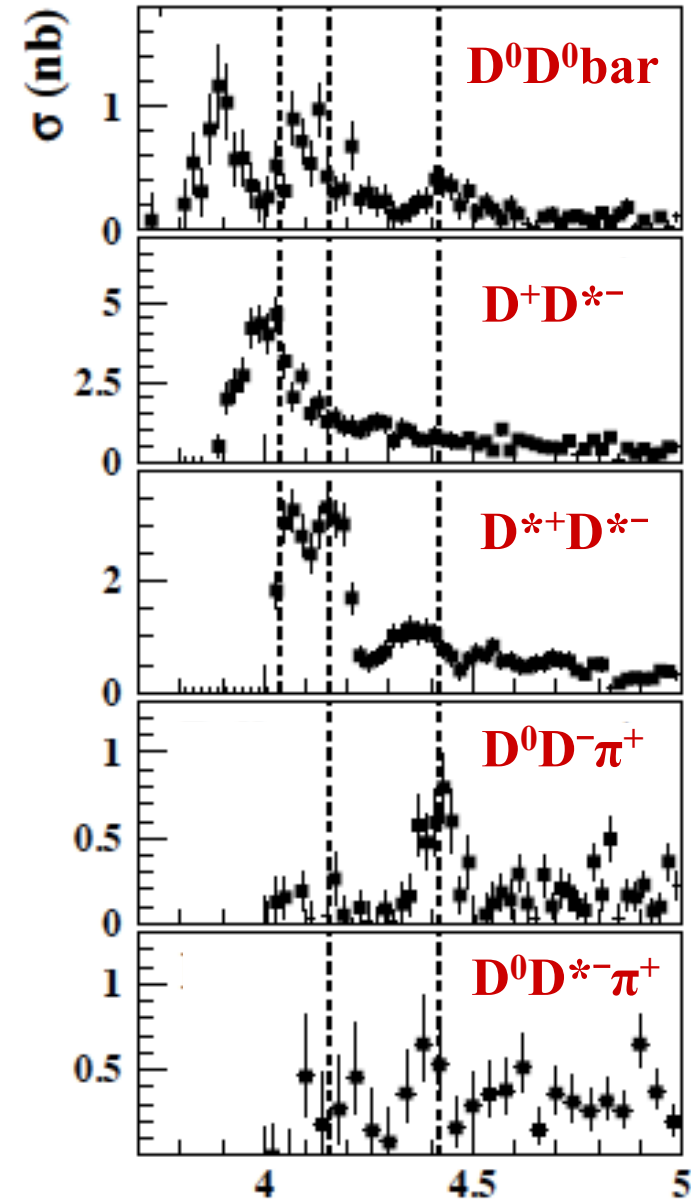
- **July 19, 2008: first  $e^+e^-$  collision event in BESIII**
- **Nov. 2008:  $\sim 14\text{M}$   $\psi(2\text{S})$  events for detector calibration**
- **2009:  $106\text{M}$   $\psi(2\text{S})$       $4\times\text{CLEO-c}$   
 $225\text{M}$   $\text{J}/\psi$       $4\times\text{BESII}$**
- **2010:  $\sim 0.9 \text{ fb}^{-1} \psi(3770)$**
- **2011:  $\sim 2.0 \text{ fb}^{-1} \psi(3770)$**  }  **$3.5\times\text{CLEO-c}$**   
 $\sim 0.5 \text{ fb}^{-1} @ 4.01 \text{ GeV}$
- **2012: tau mass scan:  $\sim 5.0 \text{ pb}^{-1}$  ;  $\psi(2\text{S})$ : 0.4B;  $\text{J}/\psi$ : 1B;  
 $\text{J}/\psi$  lineshape, **R scan (2.23, 2.4, 2.8, 3.4 GeV)****
- **2013:  $\sim 0.5 \text{ fb}^{-1} @ 4.26, 4.36 \text{ GeV}$  and scan in vicinity**

World's largest sample of  $\text{J}/\psi, \psi(2\text{S})$  and  $\psi(3770)$

# Radiative Return at BELLE

- BELLE ISR programme lead to important results on charmonium spectroscopy
- So far no publication on light hadron systems below 3 ... 4 GeV (preliminary result on  $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ )
- No clear indication of e.g.  $\Upsilon(4260)$  resonance which is seen in  $J/\psi \pi\pi$

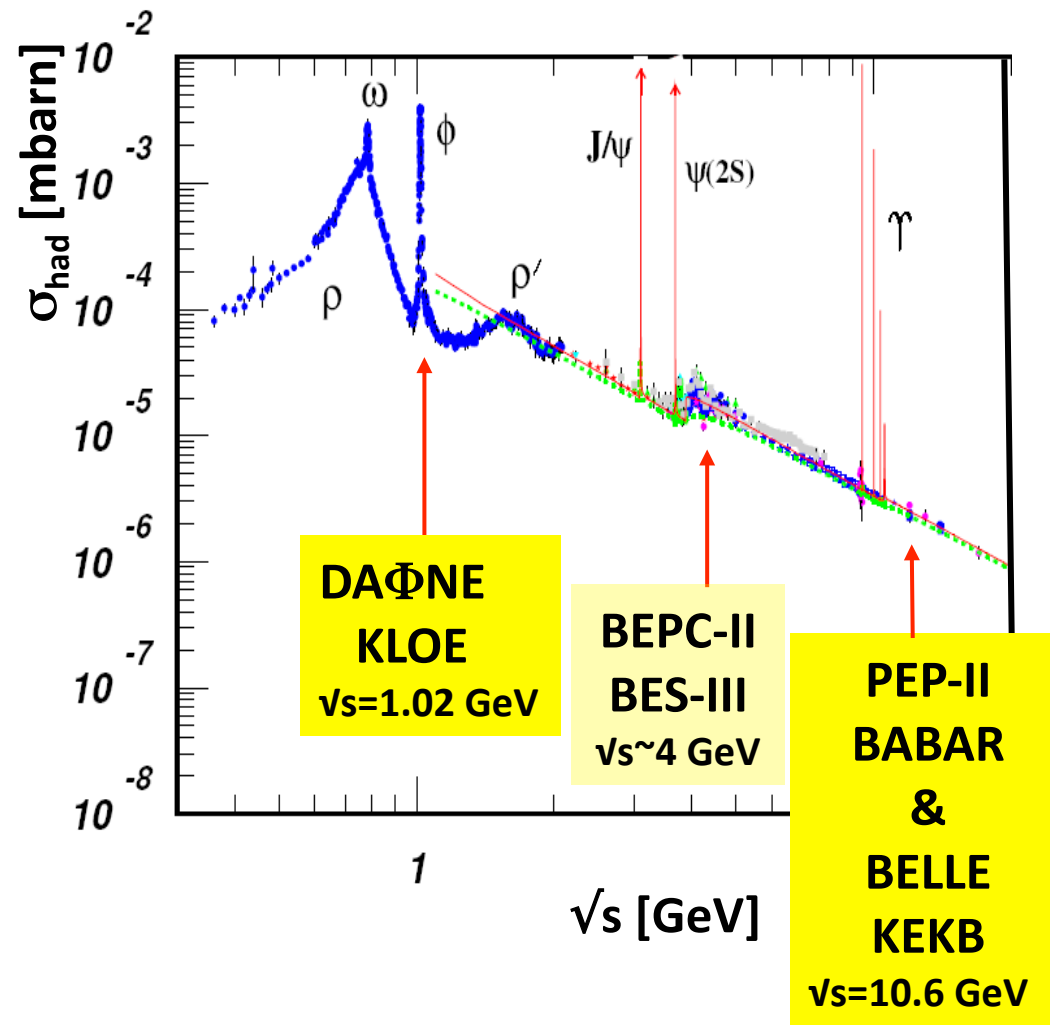
PRL 98 (2007) 092001	$e^+e^- \rightarrow D^*+D^{*-}, D^+-D^{*-+}$
PRL 99 (2007) 182004	$e^+e^- \rightarrow \pi^+\pi^- J/\psi$
PRL 99 (2007) 142002	$e^+e^- \rightarrow \pi^+\pi^- \psi(3685)$
PRD 77(2008) 011103	$e^+e^- \rightarrow D^0+D^0\text{bar}^-, D^+-D^-$
PRL 100 (2008) 062001	$e^+e^- \rightarrow D^0+D^-\pi^+$
PRL 101 (2008) 172001	$e^+e^- \rightarrow \Lambda_c^+ \Lambda_c^-, \Lambda_c^0 \Lambda_c^0\text{bar}$



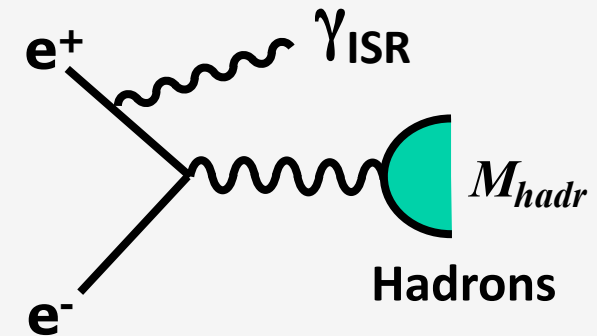


# Hadronic Cross Section via Radiative Return

Rev. Mod. Phys. 83, 1545–1588 (2011)



## Initial State Radiation (ISR) aka Radiative Return

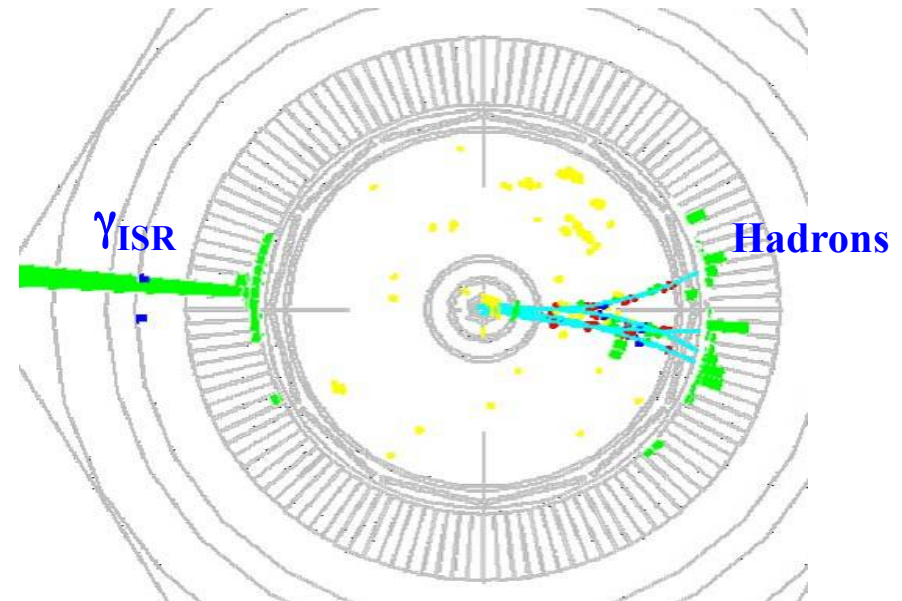


- Possible at modern particle factories
  - Needs no systematic variation of beam energy
  - High statistics due to high integrated luminosities
- Entire E range  $<\sqrt{s}$  accessible

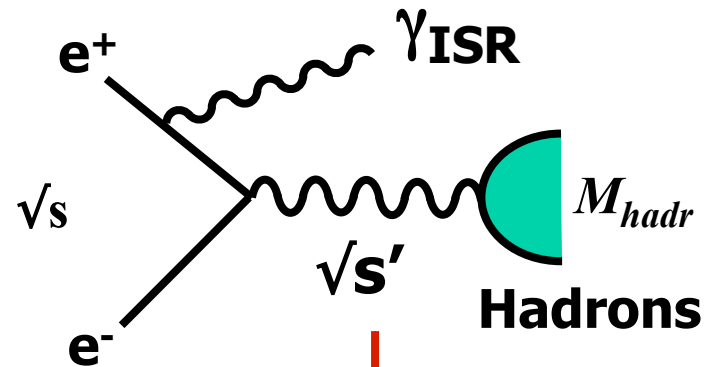
# *BABAR: ISR at 10.6 GeV*

## Features:

- Rely on **tagged (=measured) photon** for identifying ISR-events
- High **fiducial efficiency** :  
wide-angle ISR-g forces hadronic system into detector fiducial region at large polar angles
- Harder momentum spectrum due to boost
  - **fewer problems with soft particles;**
  - **allows to go down to threshold**
- Can access a very **wide mass range** in one single experiment:  
from threshold to **4 ... 5 GeV**



# Initial State Radiation (ISR)



Charmonium  
production  
Spectroscopy  
e.g.  $\Upsilon(4260)$



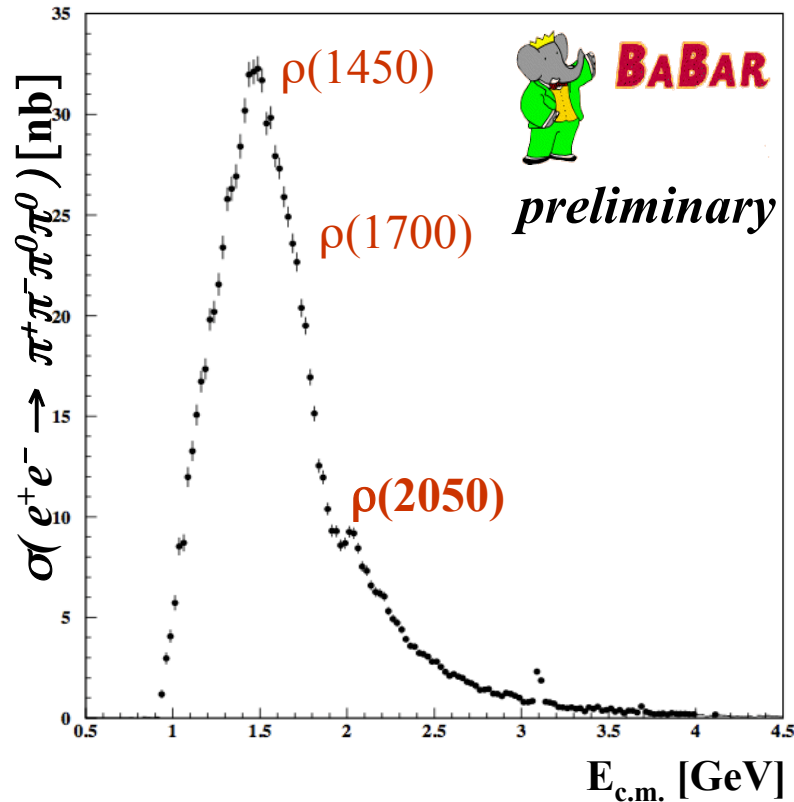
Multihadronic form factors  
 $e^+e^- \rightarrow 2\pi, 3\pi, 4\pi, >4 \text{ hadr.}$   
 $(g-2)_\mu, \alpha_{em}(M_Z^2)$   
Light hadron spectroscopy



Timelike baryon  
form factors  
Hadron structure

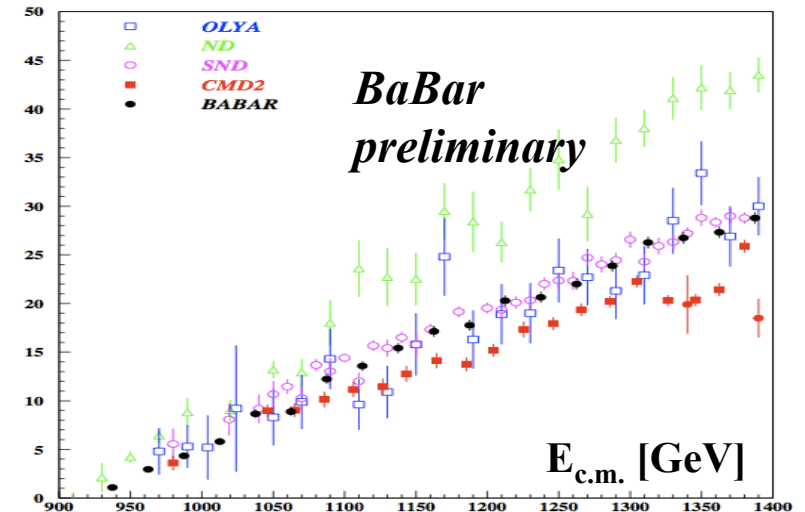
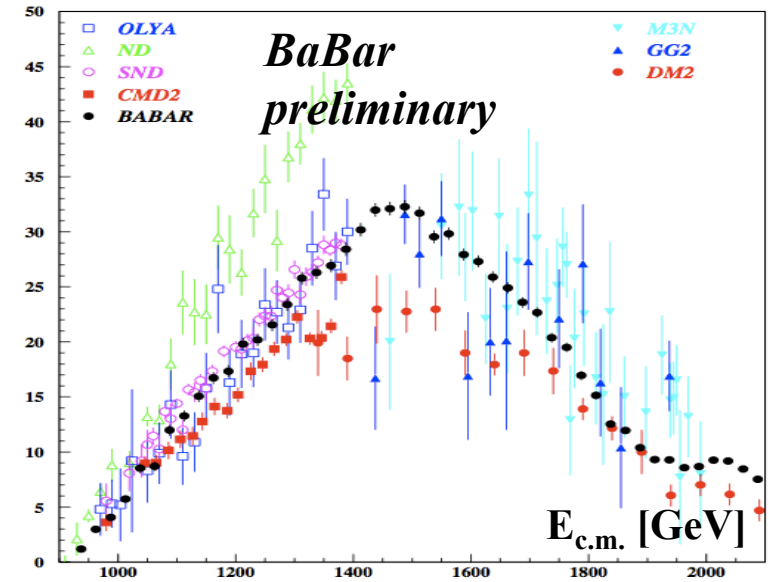


# ISR-channel $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$

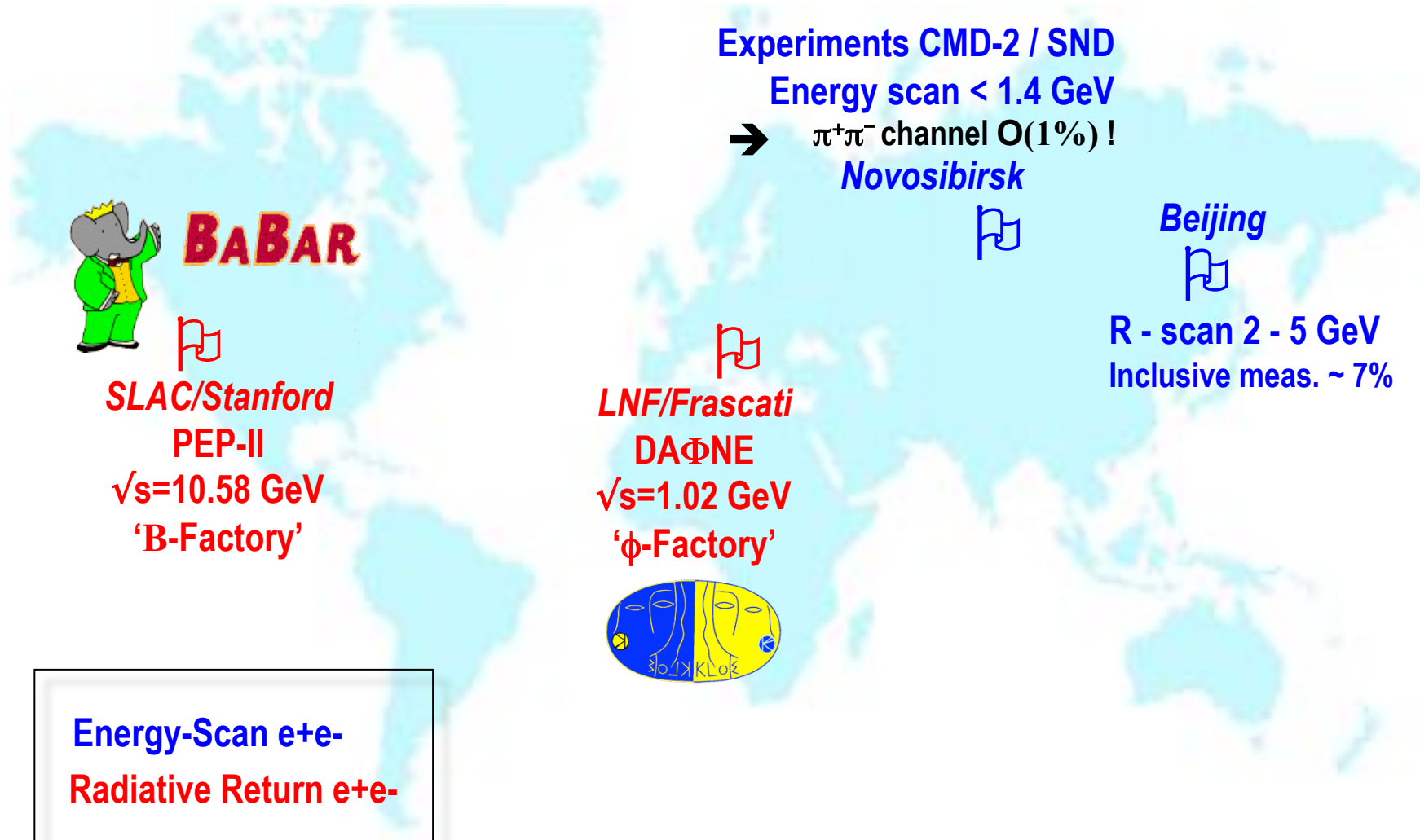


## Typical features:

- Second most important contribution for  $(g-2)_\mu$
- Precision (preliminary result): 8%
- Analysis on full data ( $454 \text{ fb}^{-1}$ ) sample almost ready:  $\sim 4\%$  systematic uncertainty



# Cross Section Data from $e^+e^-$



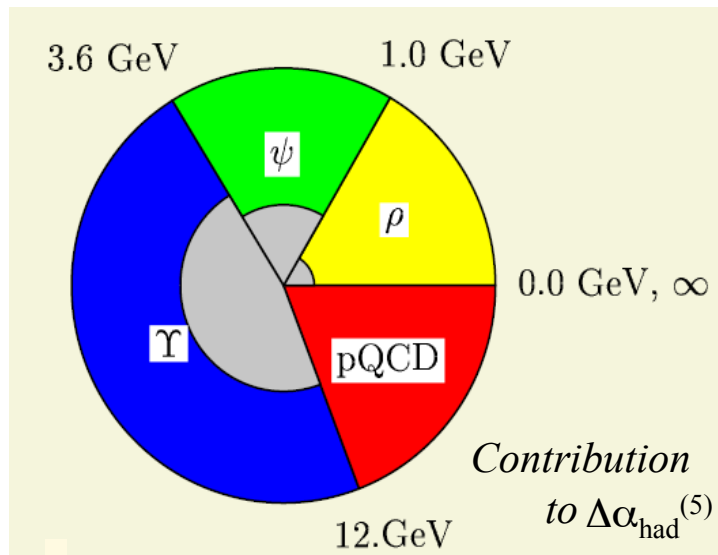
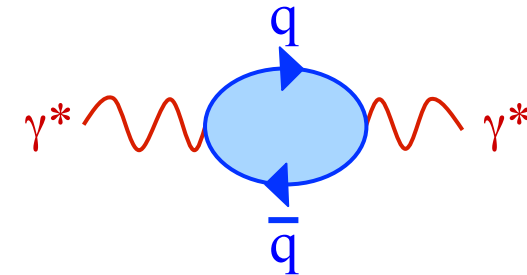
# Running Fine Structure Constant

$$\alpha_{\text{QED}}(0) = 1 / 137$$

$$\alpha_{\text{QED}}(M_Z^2) = 1 / 129$$

$$\alpha(s) = \frac{\alpha(0)}{1 - \Delta\alpha(s)} \begin{cases} \Delta\alpha_{\text{lept}}(M_Z^2) = 0.0314 \\ \Delta\alpha_{\text{had}}^{(5)}(M_Z^2) = 0.027515 \pm 0.000149 \end{cases}$$

$$\Delta\alpha_{\text{had}}^{(5)}(s) = -\frac{\alpha s}{3\pi} \int_{4m_\pi^2}^{E_{\text{cut}}^2} ds' \frac{R_\gamma^{\text{data}}(s')}{s'(s' - s)}$$

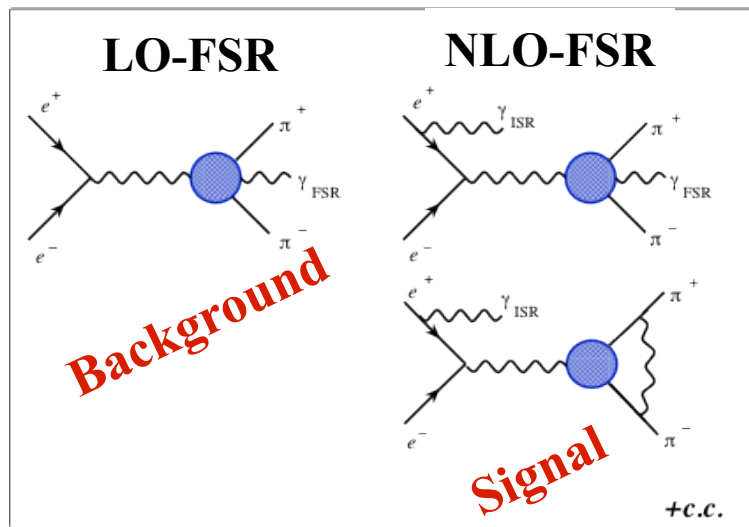


[ F. Jegerlehner ArXiv:0807.4206 ]

- $\Delta\alpha_{\text{had}}^{(5)}$  is the **hadronic vacuum polarization contribution** of the five lightest quarks u,d,s,c,b
- **Low energy contributions are less weighted in dispersion integral**  
 $\Rightarrow$  **from which energy range on use pQCD?**

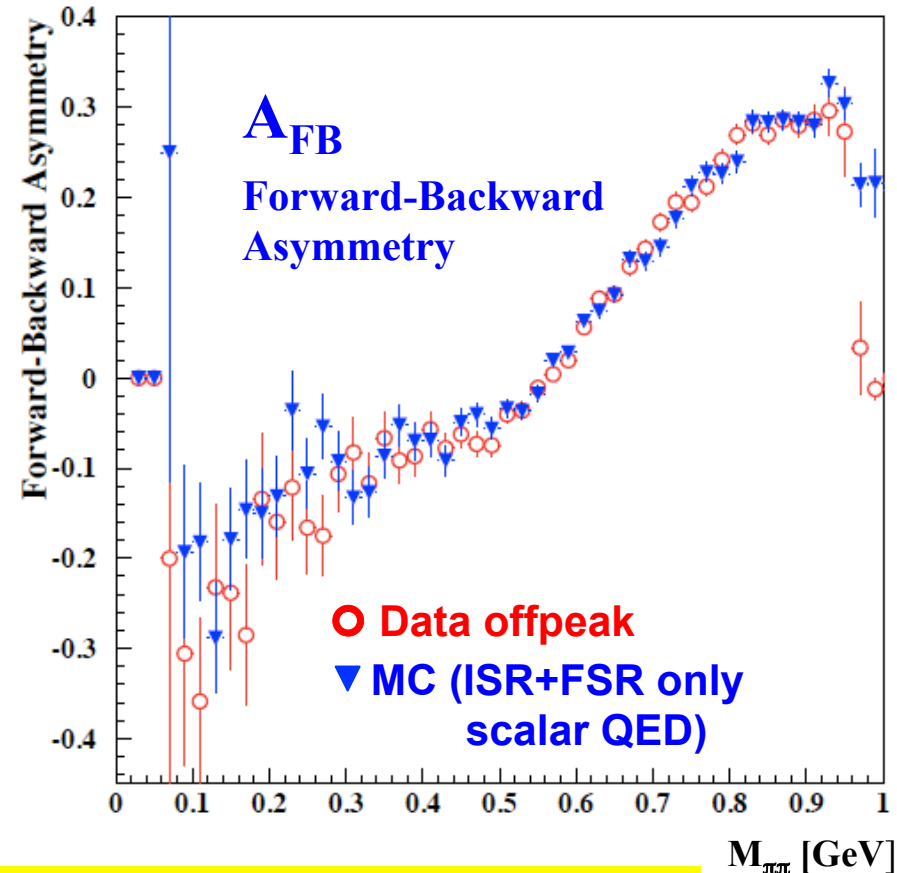
# The Issue of Final State Radiation

FSR - corrections are model dependent, typically model of scalar QED is used



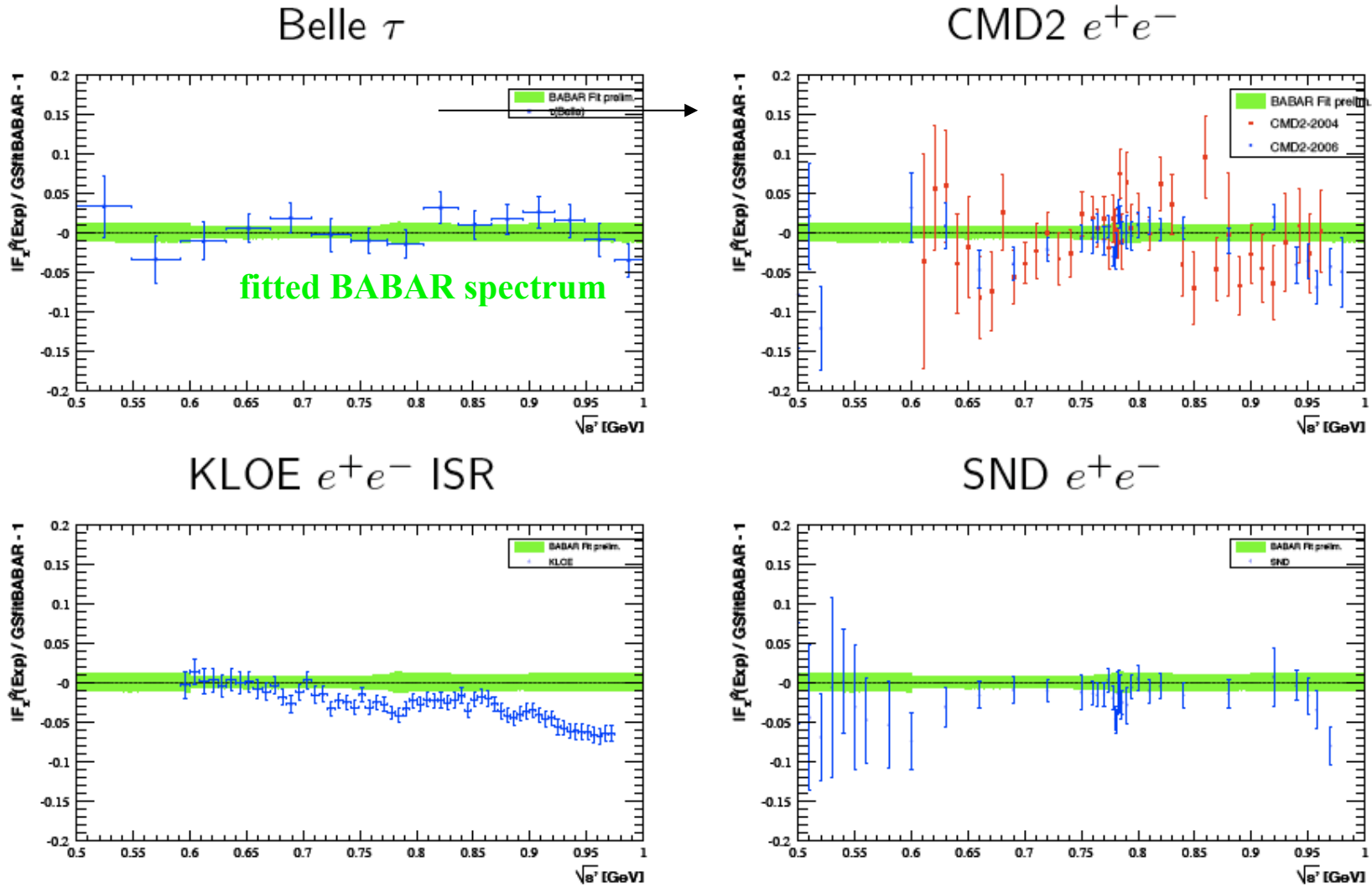
**F-B- Asymmetry** is a consequence of ISR-FSR-interference and is a direct test of model of scalar QED for FSR!

Binner, Kühn, Melnikov, Phys. Lett. B 459, 1999



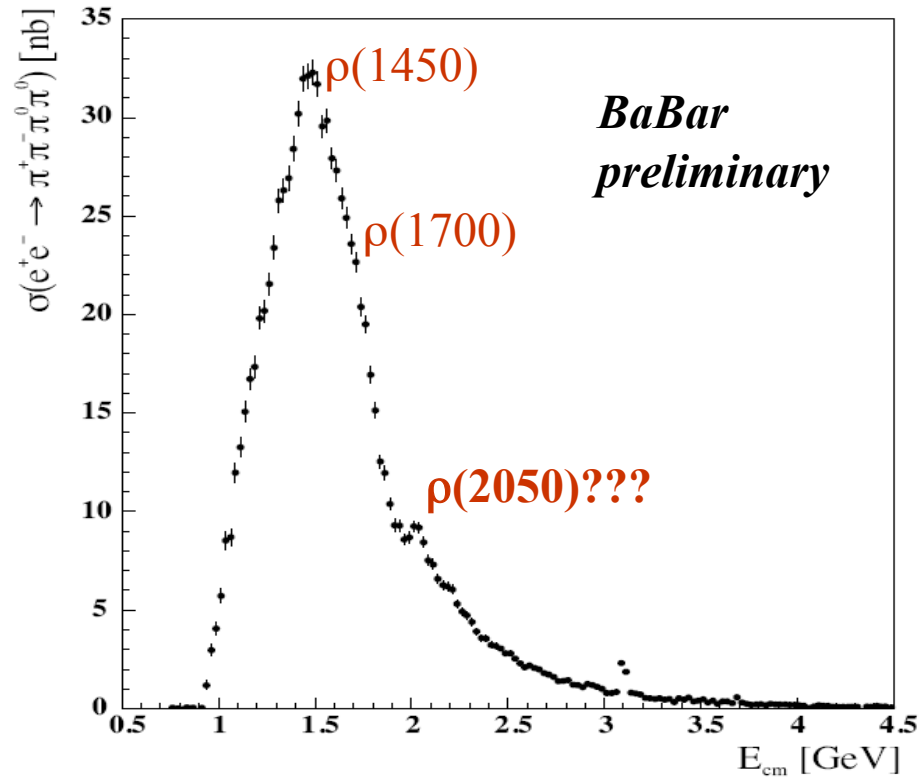
$A_{FB}$ : unique opportunity to test final state radiation

# Fractional Difference BABAR-other Expts.



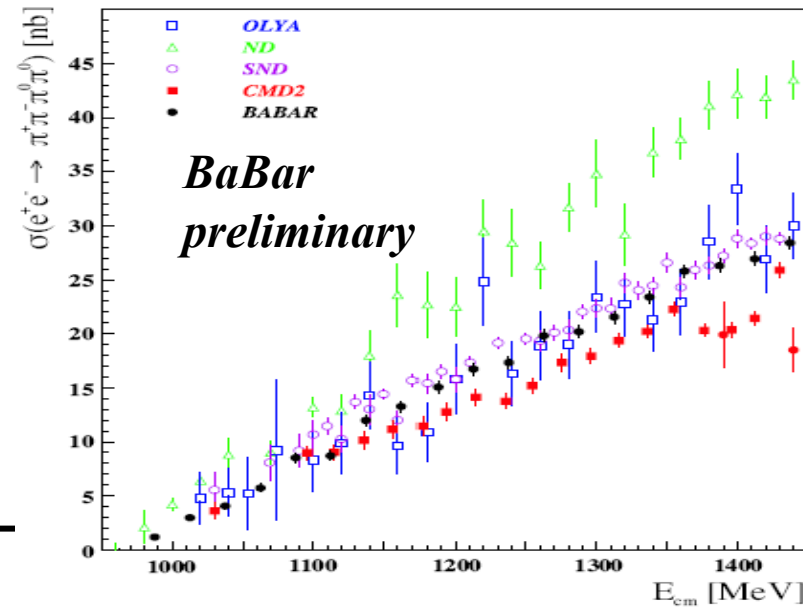
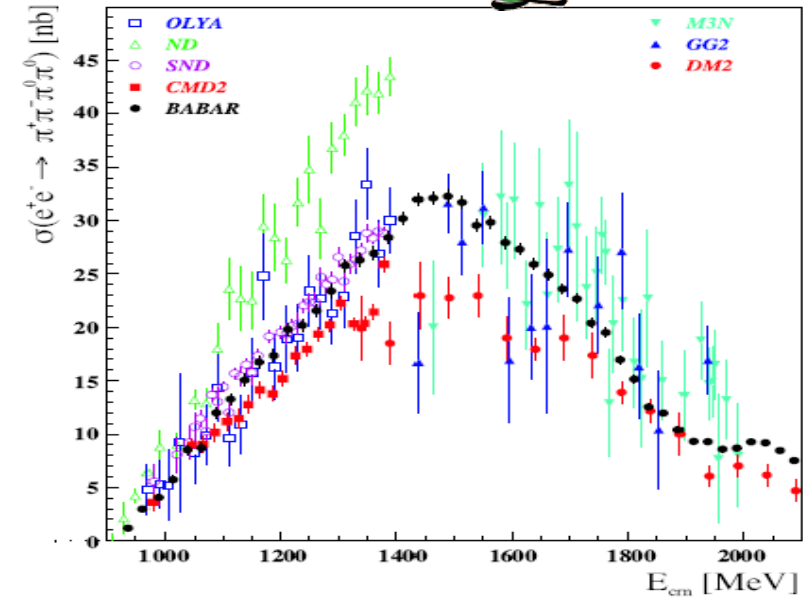


$$e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$$



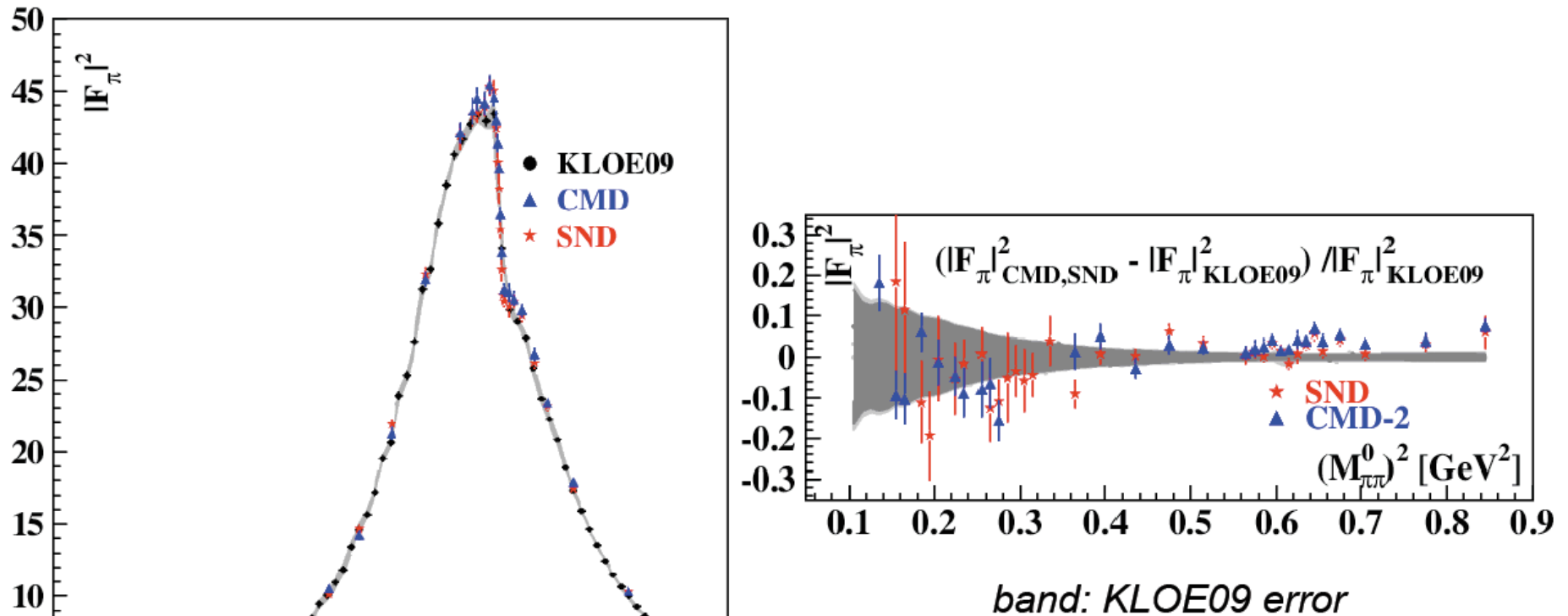
### Features:

- Important mode for  $a_\mu$  and  $\alpha_{\text{QED}}$
- Preliminary precision: 8% in peak  $\rightarrow$  5%
- Good agreement with SND  $< 1.4$  GeV
- Huge improvement  $> 1.4$  GeV
- First measurement  $> 2.5$  GeV



# Comparison KLOE vs. Novosibirsk Experim.

CMD and SND results compared to KLOE09: Fractional difference



Fair agreement btw. energy scan  
and radiative return experiments



## Ein erfolgreiches Forschungsgebiet bei BABAR/Stanford:

- $e^+e^- \rightarrow \pi^+\pi^-\pi^0$
- $e^+e^- \rightarrow 2(\pi^+\pi^-), \pi^+\pi^-K^+K^-, 2(K^+K^-)$
- $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0, K^+K^-\pi^+\pi^-, K^+K^-\pi^0\pi^0$
- $e^+e^- \rightarrow 3(\pi^+\pi^-), 3(\pi^+\pi^-\pi^0), 2(\pi^+\pi^-)K^+K^-$
- $e^+e^- \rightarrow 2(\pi^+\pi^-\pi^0), 2(\pi^+\pi^-\eta), \pi^+\pi^-K^+K^-\pi^0, \pi^+\pi^-K^+K^-\eta$
- $e^+e^- \rightarrow K^+K^-\pi^0, K^+K_S\pi^-, K^+K_S\eta$
- $e^+e^- \rightarrow p\bar{p}$
- $e^+e^- \rightarrow \Lambda^0\bar{\Lambda}^0, \Lambda^0\bar{\Sigma}^0, \Sigma^0\bar{\Sigma}^0$

1) Relevante Kanäle für  $(g-2)_\mu$

2) Hadronspektroskopie und  $J/\psi$  - Verzweigungsverhältnisse

3) Nukleon-Struktur durch Messung der zeitartigen Baryon-Formfaktoren

# BABAR Radiative Return Resultate



## BABAR

$$- e^+e^- \rightarrow \pi^+\pi^-$$

*Höchst relevant für  $(g-2)_\mu$*

$$- e^+e^- \rightarrow \pi^+\pi^-\pi^0$$

$$- e^+e^- \rightarrow 2(\pi^+\pi^-), \pi^+\pi^-\text{K}^+\text{K}^-, 2(\text{K}^+\text{K}^-)$$

$$- e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0, \text{K}^+\text{K}^-\pi^+\pi^-, \text{K}^+\text{K}^-\pi^0\pi^0$$

$$- e^+e^- \rightarrow 3(\pi^+\pi^-), 3(\pi^+\pi^-\pi^0), 2(\pi^+\pi^-\text{K}^+\text{K}^-)$$

$$- e^+e^- \rightarrow 2(\pi^+\pi^-\pi^0), 2(\pi^+\pi^-\eta), \pi^+\pi^-\text{K}^+\text{K}^-\pi^0, \pi^+\pi^-\text{K}^+\text{K}^-\eta$$

$$- e^+e^- \rightarrow \text{K}^+\text{K}^-\pi^0, \text{K}^+\text{K}_S\pi^-, \text{K}^+\text{K}_S\eta$$

$$- e^+e^- \rightarrow p\bar{p}$$

$$- e^+e^- \rightarrow \Lambda^0\bar{\Lambda}^0, \Lambda^0\bar{\Sigma}^0, \Sigma^0\bar{\Sigma}^0$$

*Weniger relevant für  $(g-2)_\mu$*

*Mesonspektroskopie*

*Nukleonstruktur*

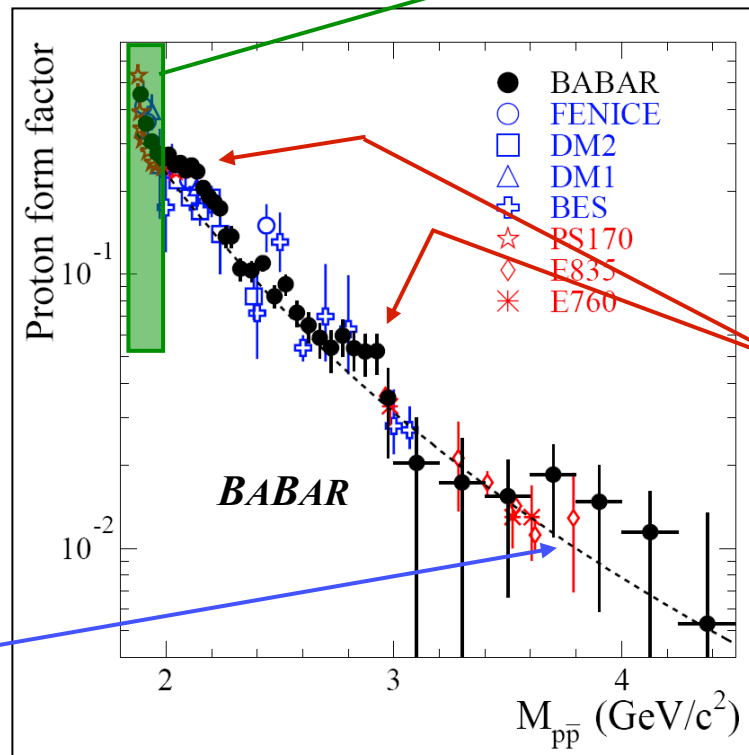
$$e^+e^- \rightarrow p\bar{p}$$

Defining the effective form factor  $|F|$  ( $|G_E| = |G_M|$ ):

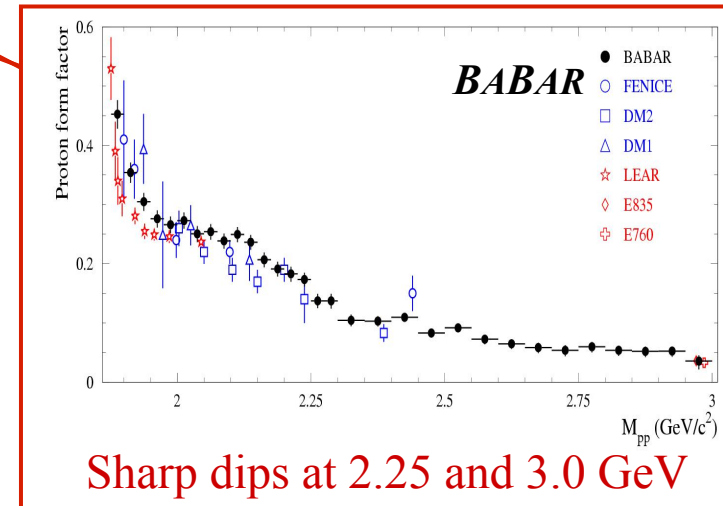
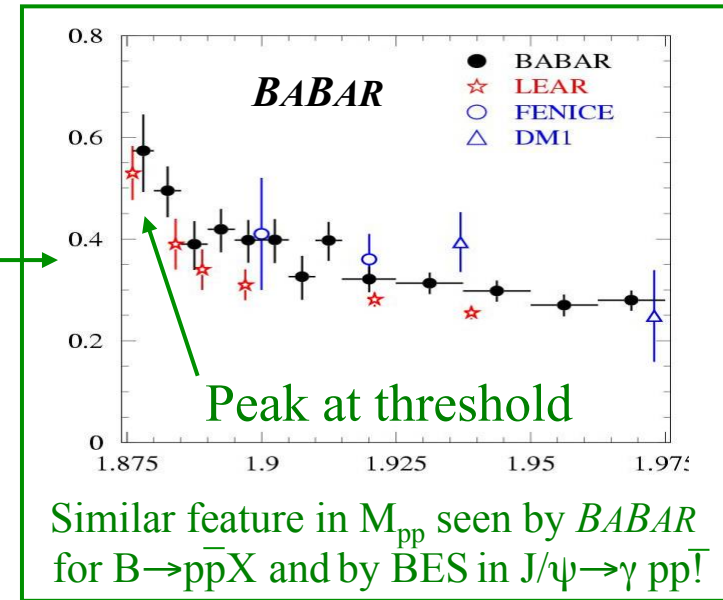
$$\sigma = \frac{4\pi\alpha^2\beta C}{3m_{p\bar{p}}^2} \cdot \left(1 + \frac{2m_p^2}{m_{p\bar{p}}^2}\right) \cdot |F|^2$$

allows comparison with other experiments ( $p\bar{p} \rightarrow e^+e^-$ ,  $e^+e^- \rightarrow p\bar{p}$ )

Complicated structure observed:



Agreement with pQCD-fit at high masses



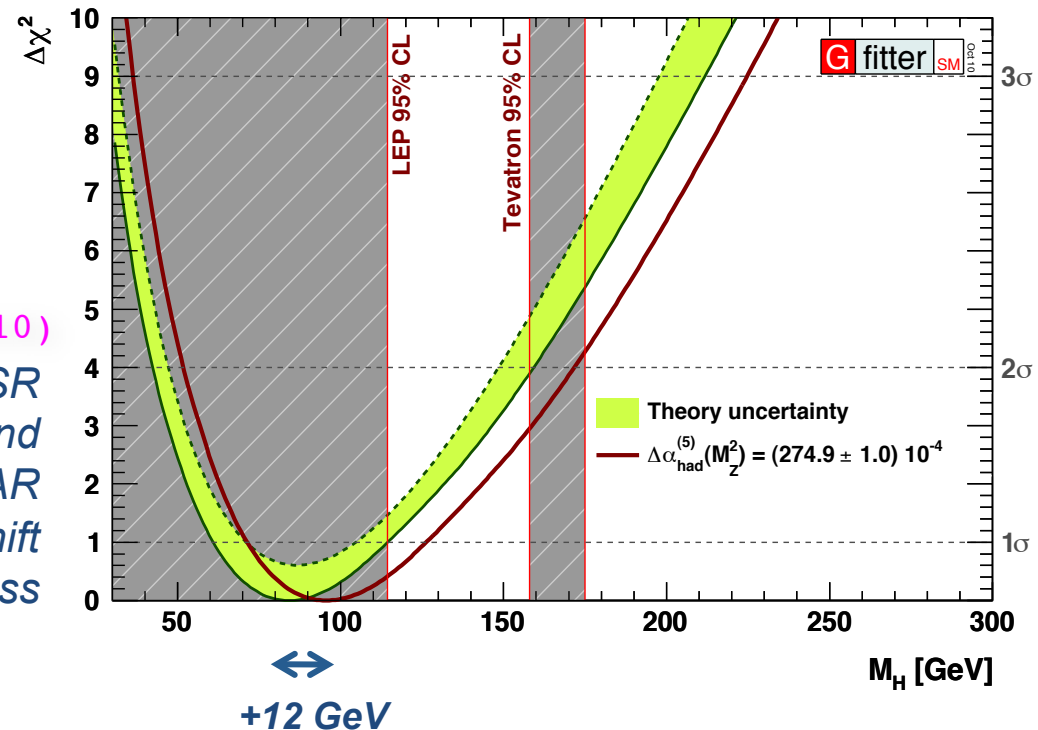
# Impact of $\alpha_{em}(M_Z^2)$

**Reduction of uncertainty of  $\alpha_{em}(M_Z^2)$  : Needed for electroweak physics**

→ least known input for electroweak precision fits to SM,  
e.g. Higgs mass prediction

→ **Project P2**

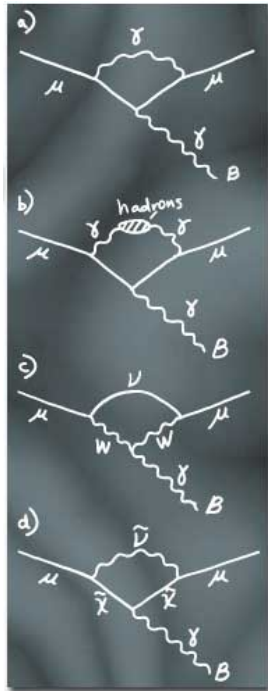
Davier et al. (2010)  
Including recent ISR  
data by KLOE and  
BABAR  
lead to significant shift  
of predicted Higgs mass



→ **Project P1: Reduce uncertainty of  $\Delta\alpha_{em}^{had(5)}$  by ~factor 2**

**A must for future International Linear Collider ILC**

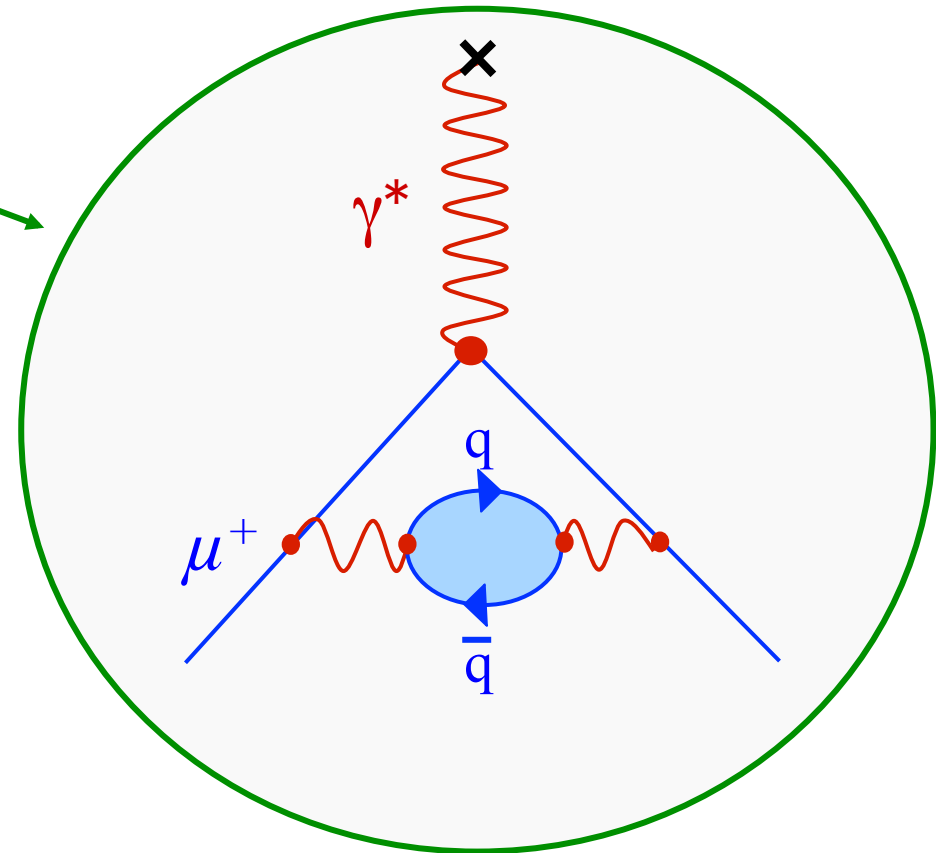
# Theory contributions to $(g-2)_\mu$



QED  
contribution

**Hadronic  
vacuum  
polarization**

Electroweak  
contribution



# Muon Anomaly $(g-2)_\mu$

**Magnetic Moment:**  $\vec{m} = \mu_B g \vec{S}$   $\mu_B$ : Bohr magneton,  $g$ : gyromagnetic factor  $\sim 2$

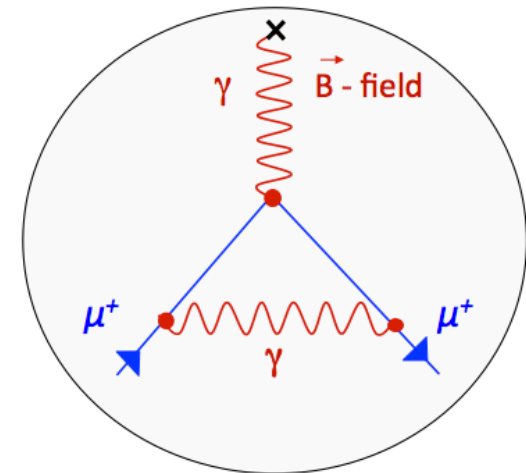
**Muon Anomaly:**  $a_\mu = (g-2)_\mu / 2 = \alpha_{em} / 2\pi + \dots = 0.001161\dots$

■ **Standard Model (SM) prediction  $a_\mu^{SM}$ :**

- QED:  $a_\mu^{QED} = (11\,658\,471.809 \pm 0.015) \cdot 10^{-10}$
- weak:  $a_\mu^{weak} = (15.4 \pm 0.2) \cdot 10^{-10}$
- strong:  $a_\mu^{strong} = (693.0 \pm 4.9) \cdot 10^{-10}$

$$a_\mu^{SM} = (11\,659\,180.2 \pm 4.9) \cdot 10^{-10}$$

**SM prediction entirely limited by strong interactions !**



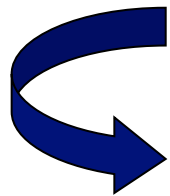
■ **Direct measurement BNL-E821  $a_\mu^{exp}$ :**

$$a_\mu^{exp} = (11\,659\,208.9 \pm 6.3) \cdot 10^{-10}$$



# Initial State Radiation (ISR)

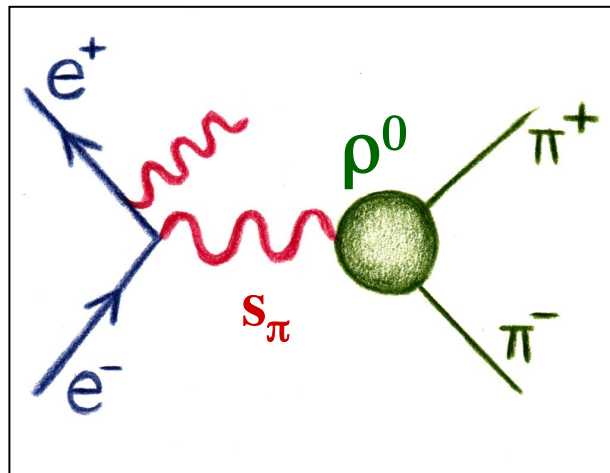
Modern  $e^+e^-$  particle factories :  $\sqrt{s} = m_{\phi(1020)} = 1.02$  GeV bei DAΦNE  
 $\sqrt{s} = m_{\Upsilon(4S)} = 10.6$  GeV bei PEP-II



energy scan impossible over a wide energy range!

Complementary ansatz:

Consider events via **Initial State Radiation (ISR)**



“**Radiative Return**” to  $\rho$ -resonance:

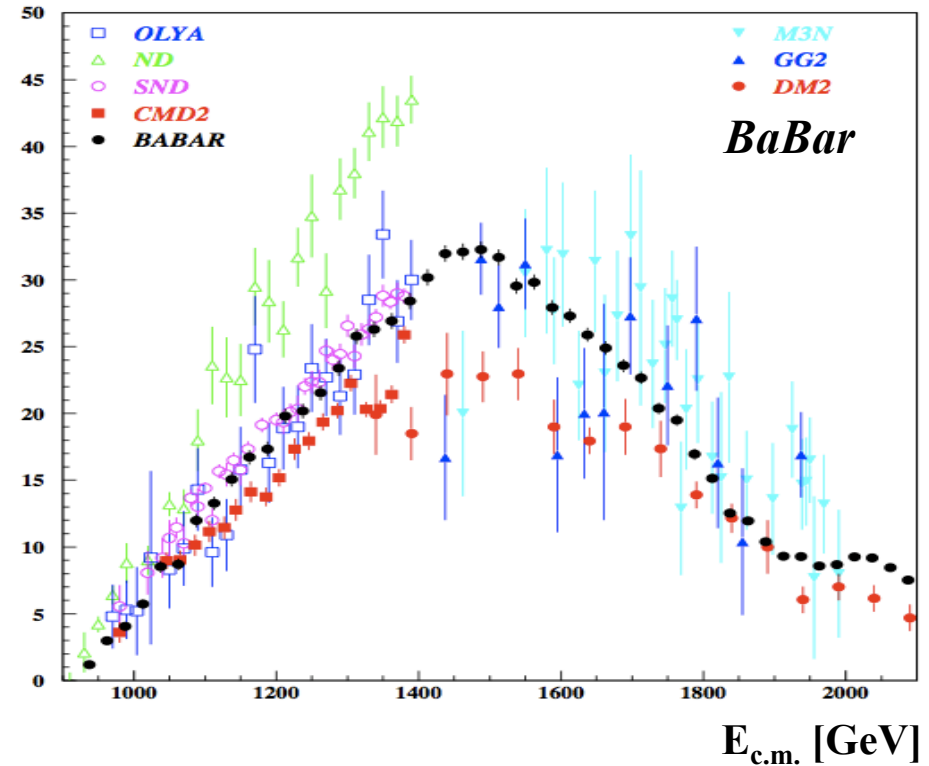
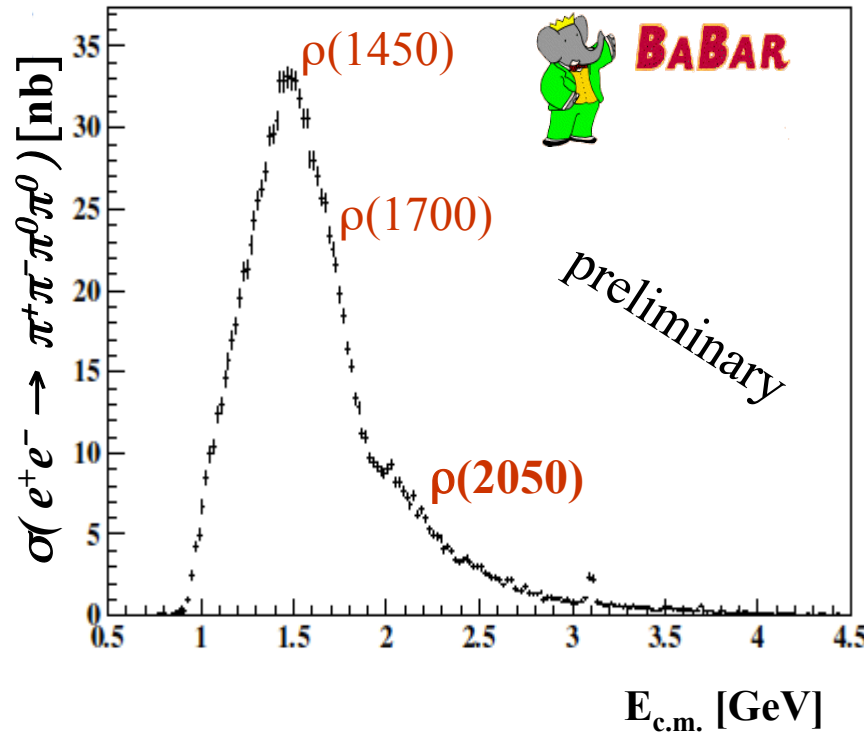
$$e^+e^- \rightarrow \rho + \gamma \rightarrow \pi^+ \pi^- + \gamma$$

Measure  $2\pi$  invariant mass

$$s_\pi = M_{\pi\pi}^2$$

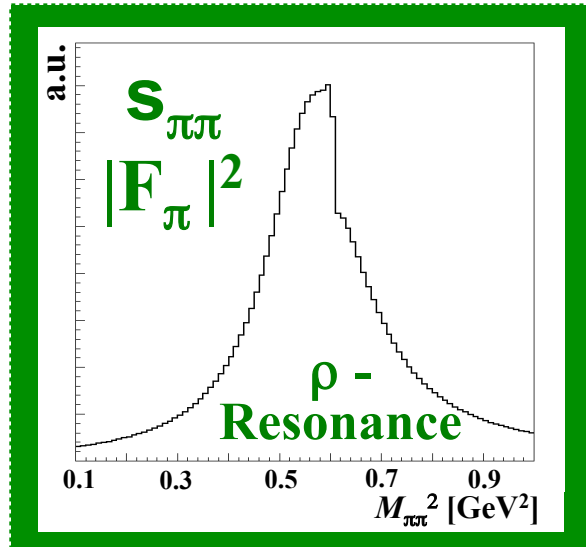
$$\frac{d\sigma(e^+e^- \rightarrow \pi^+ \pi^- \gamma)}{dM_{\pi\pi}^2}$$

# BABAR Example 2: $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$



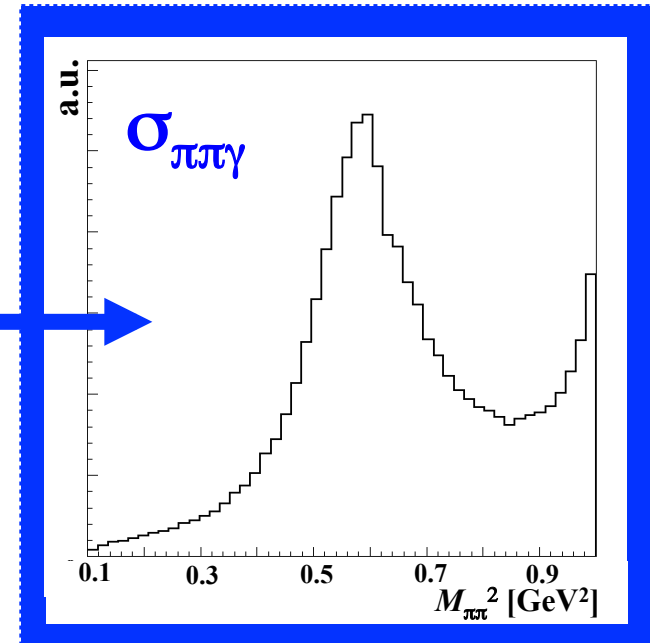
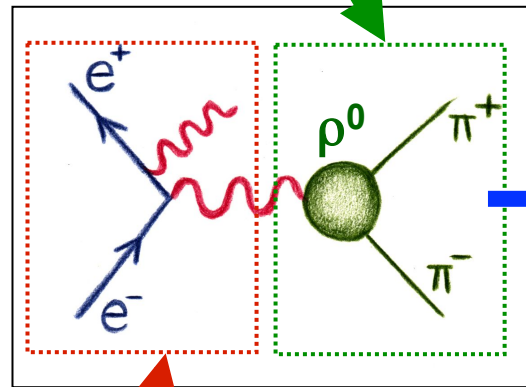
- Second most important contribution for  $(g-2)_\mu$
- Significant improvement  $>1.4$  GeV
- Precision (preliminary result): 8%
- Analysis on full data ( $454 \text{ fb}^{-1}$ ) sample ongoing:  $\sim 4\%$  or lower

# Radiative Return

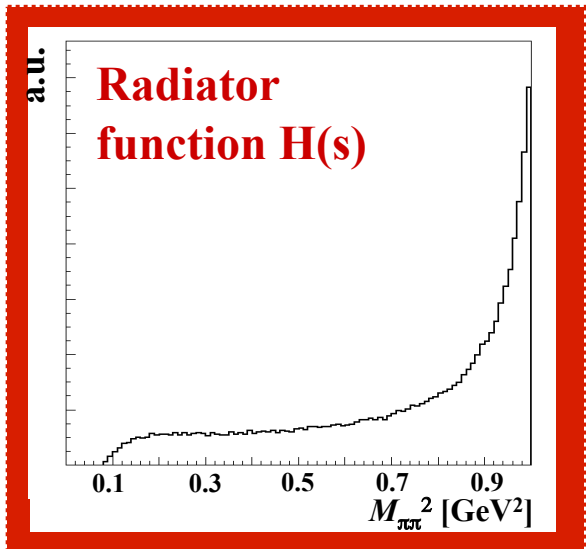


Non-radiative  
cross section

$$M_{\pi\pi}^2 \frac{d\sigma_{\pi\pi\gamma}}{dM_{\pi\pi}^2} = \sigma_{\pi\pi}(s) \times H(s)$$



radiative cross section



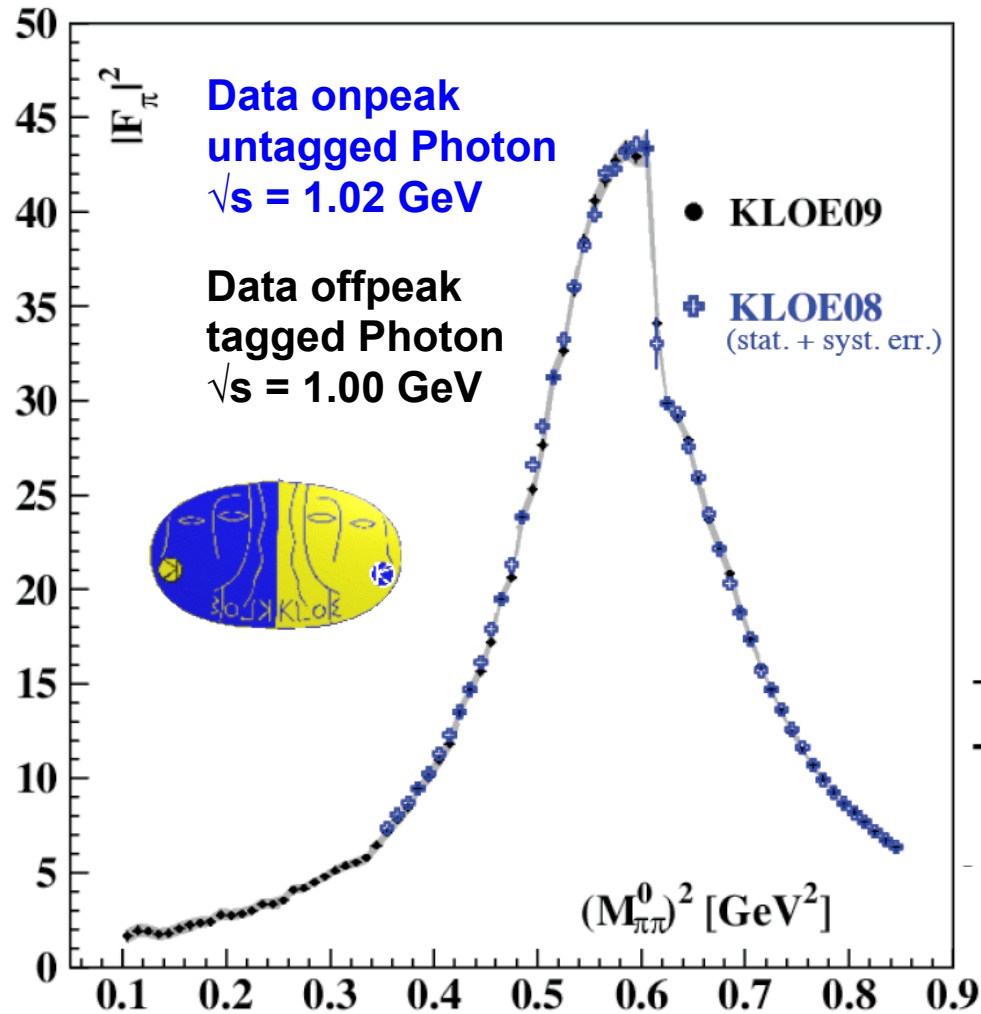
J. Kühn, H. Czyż, G. Rodrigo

Radiator function

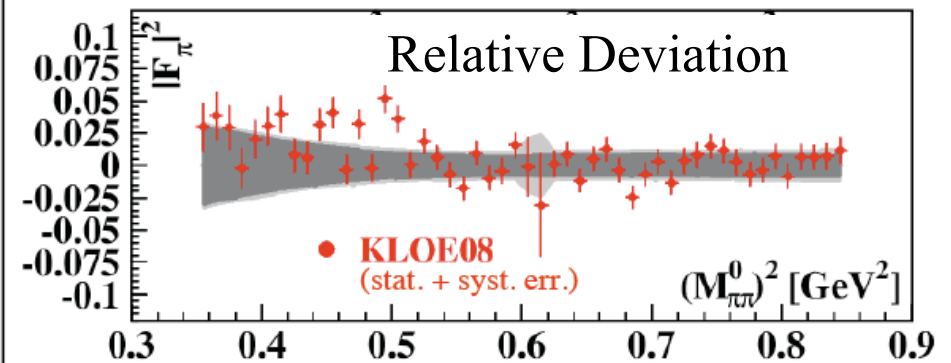
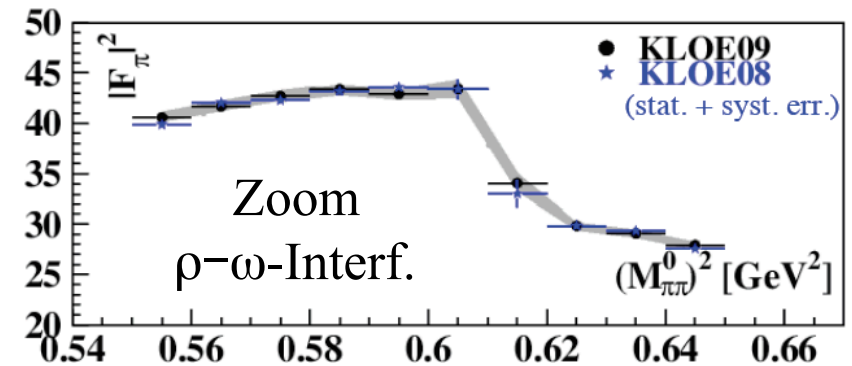
MC- Generator PHOKHARA



# Pion Formfactor: KLOE Results



PLB 670 (2009) 285



Good agreement  
with  $\sim 1\%$  systematic uncertainty

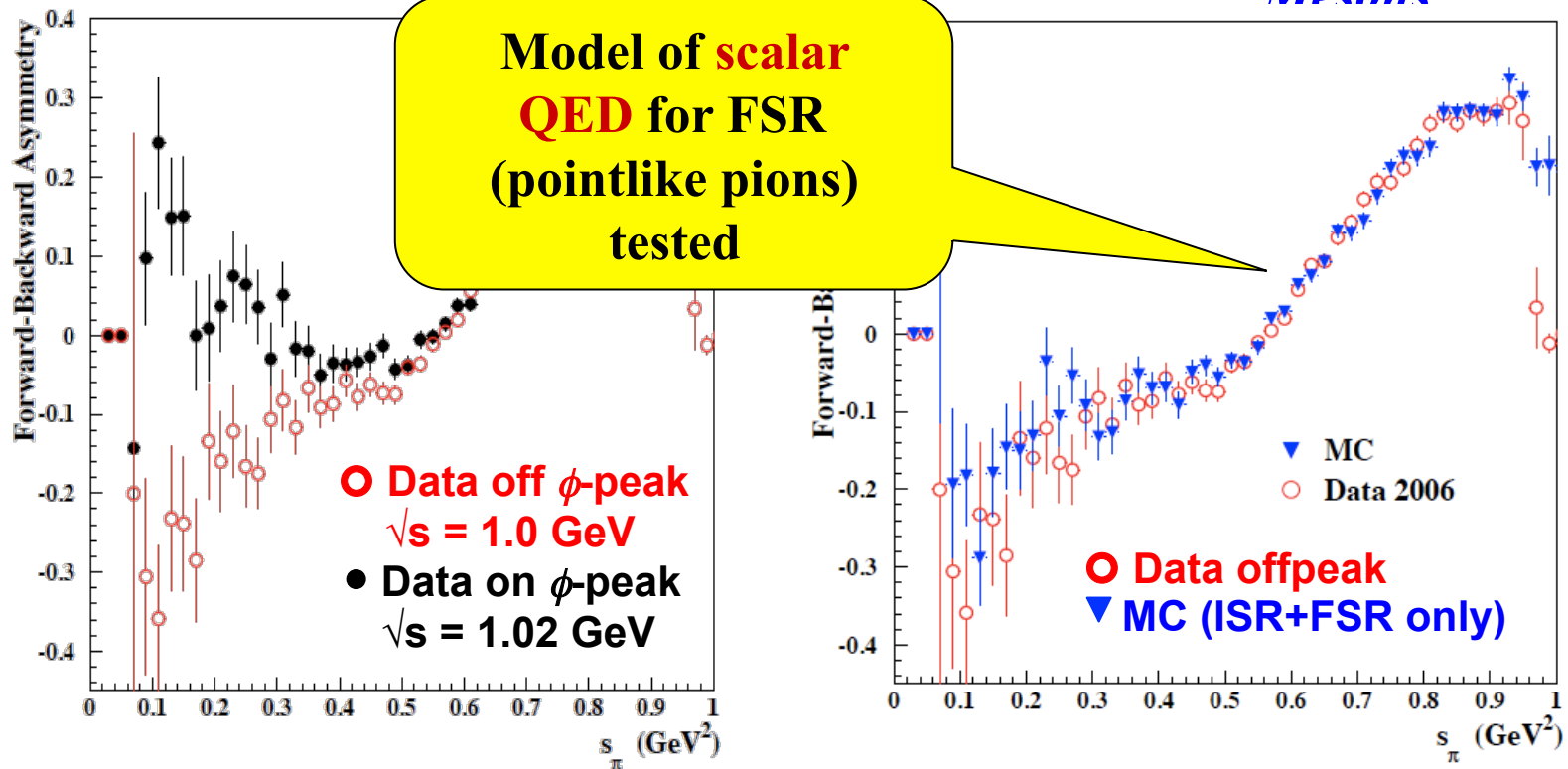
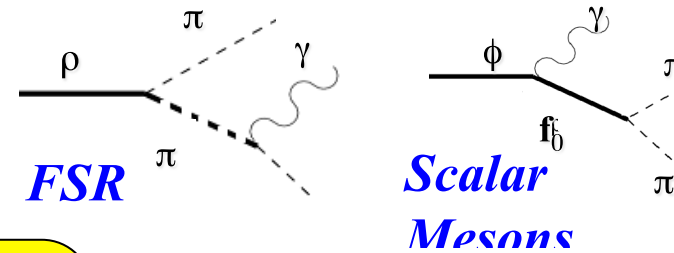


# Forward-Backward-Asymmetry

## Forward-Backward-Asymmetry

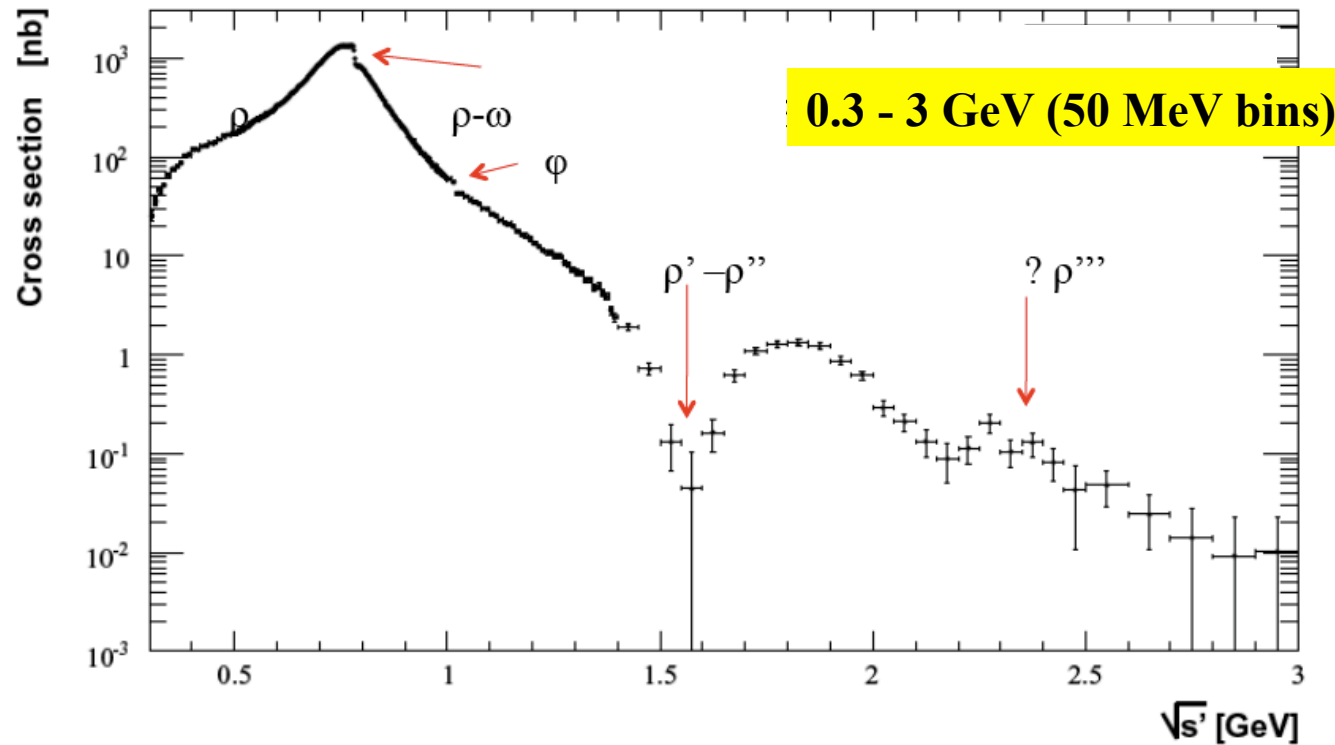
$$A = \frac{N(\theta^+ > 90^\circ) - N(\theta^+ < 90^\circ)}{N(\theta^+ > 90^\circ) + N(\theta^+ < 90^\circ)}$$

$A$  very sensitive to:



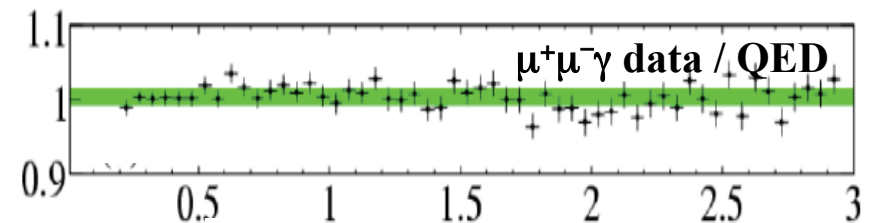


# Pion Formfactor: BABAR Results



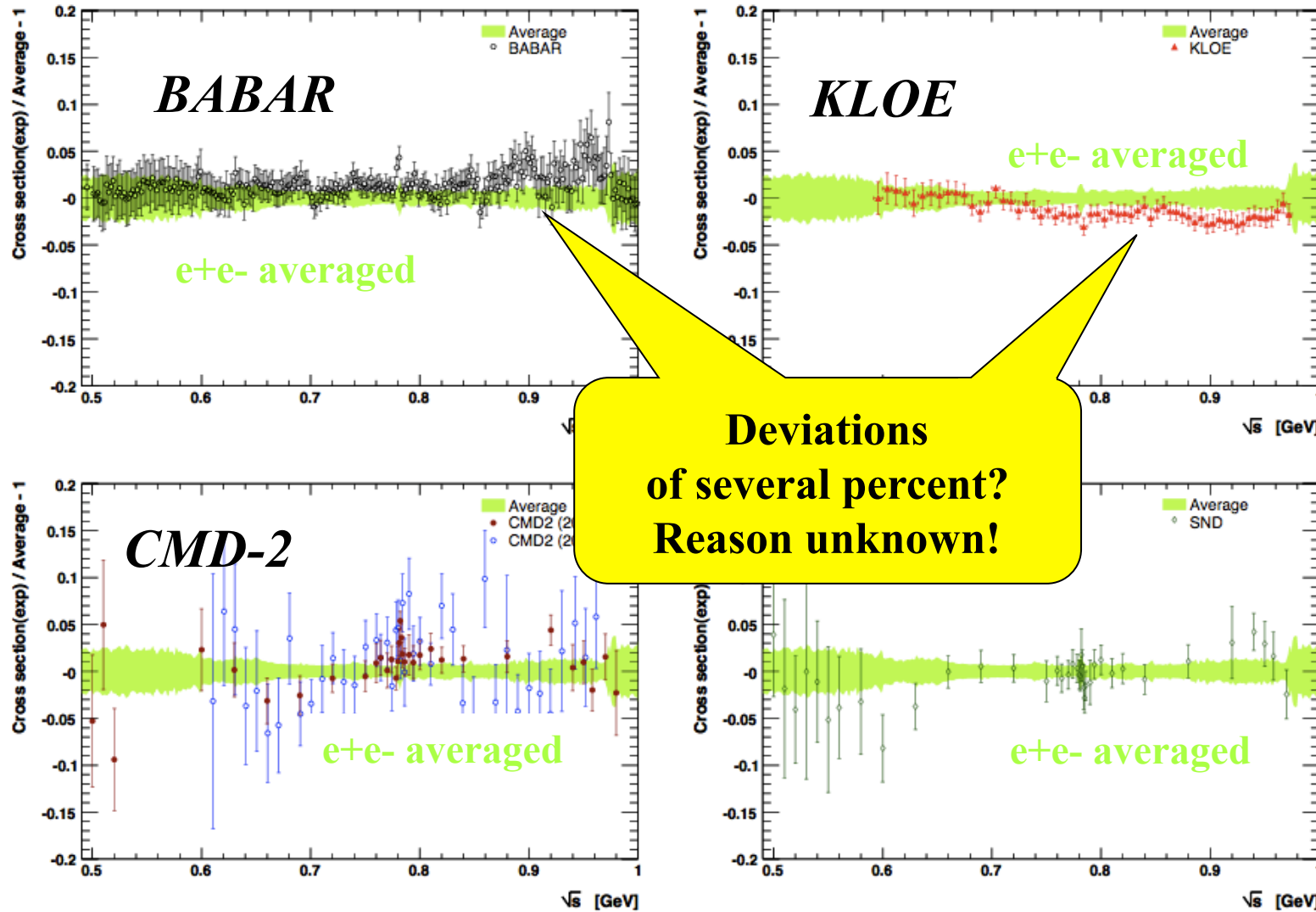
- Tagged ISR photons
- Wide energy range  $< 3$  GeV
- Systematic uncertainty: 1.4% at threshold  
0.6% on  $\rho$  peak

- Normalized to  $\mu^+\mu^-\gamma$  events:

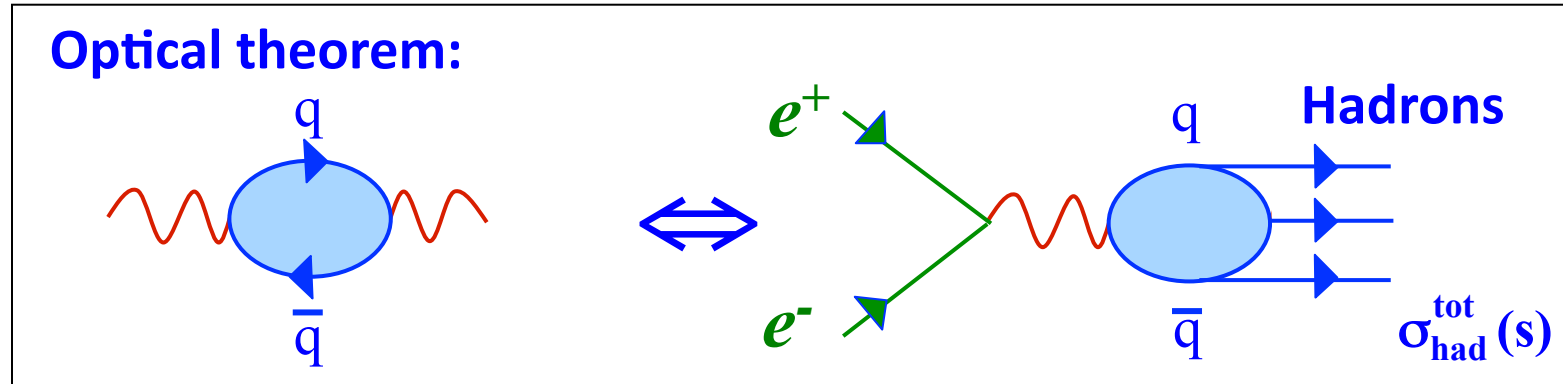


# Comparison $F_\pi$ among $e^+e^-$ Experiments

Relative deviation



# Optical Theorem & Dispersion Relation



Hadronic contribution  $a_{\mu}^{had}$  can be computed using as input  
 $e^+e^-$  annihilation data

**Dispersion integral:**

$$a_{\mu}^{had} = \frac{1}{4\pi^3} \int_{4m_{\pi}^2}^{\infty} ds K(s) \sigma_{had}(s)$$

$$s = (p_{e^+}^{(4)} + p_{e^-}^{(4)})^2$$

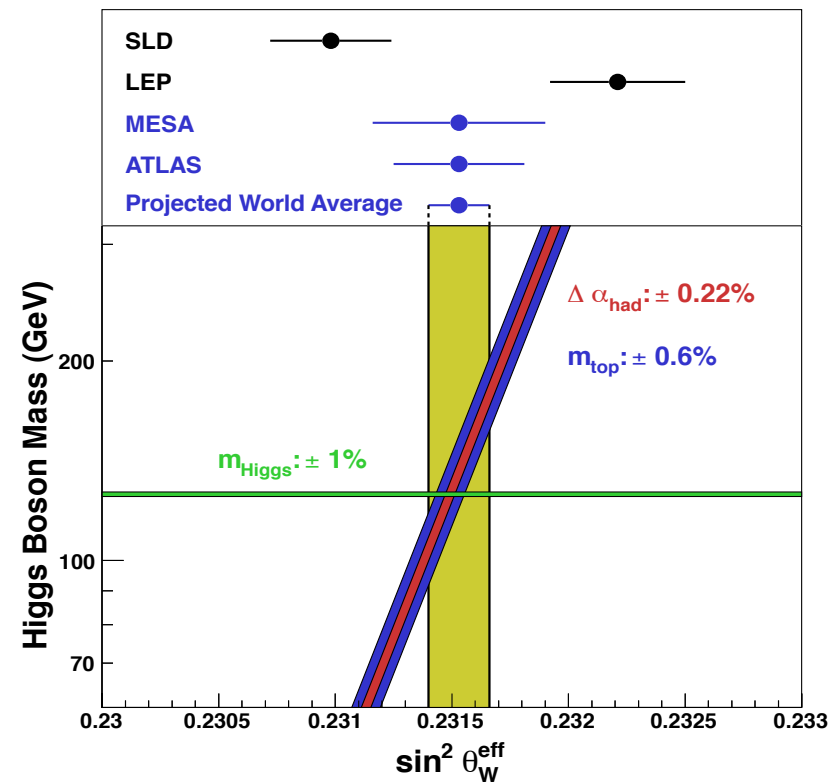
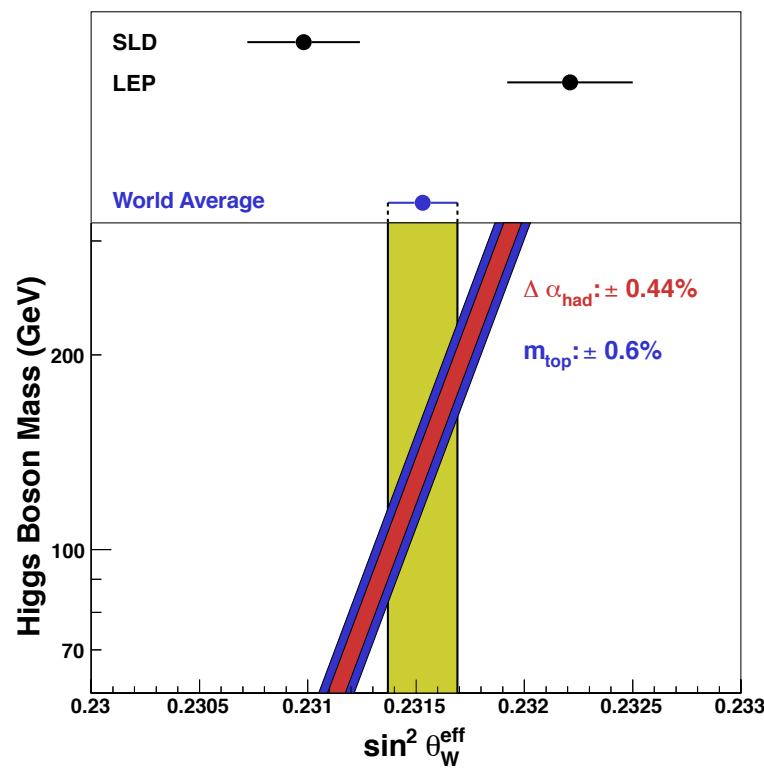
$K(s)$  analytically known  $\sim 1/s$

**Input:** hadronic electron-positron cross section data  
 or hadronic  $\tau$ -decays  $\rightarrow$  next talk



# Electroweak Precision Physics

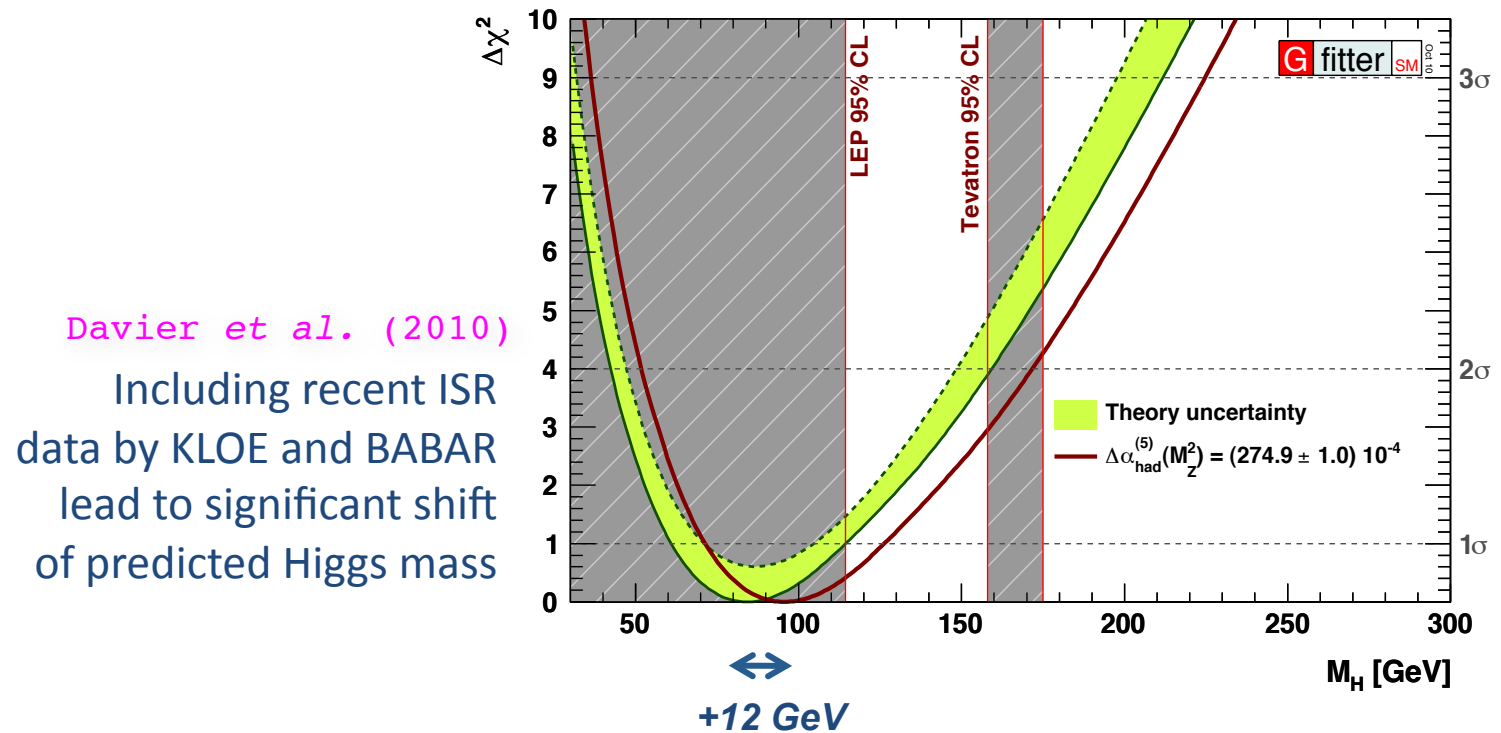
- Running of **electroweak mixing angle**  $\sin^2\Theta_W$  as function of Higgs mass
- After Higgs discovery even more interesting
- Theory curve limited by electromagnetic fine structure constant



# $\alpha_{em}(M_Z^2)$ and Electroweak Physics

## $\alpha_{em}(M_Z^2)$ limiting electroweak precision fits

- Test overall consistency of the electroweak Standard Model
- Since the discovery of the Higgs boson more timely than ever

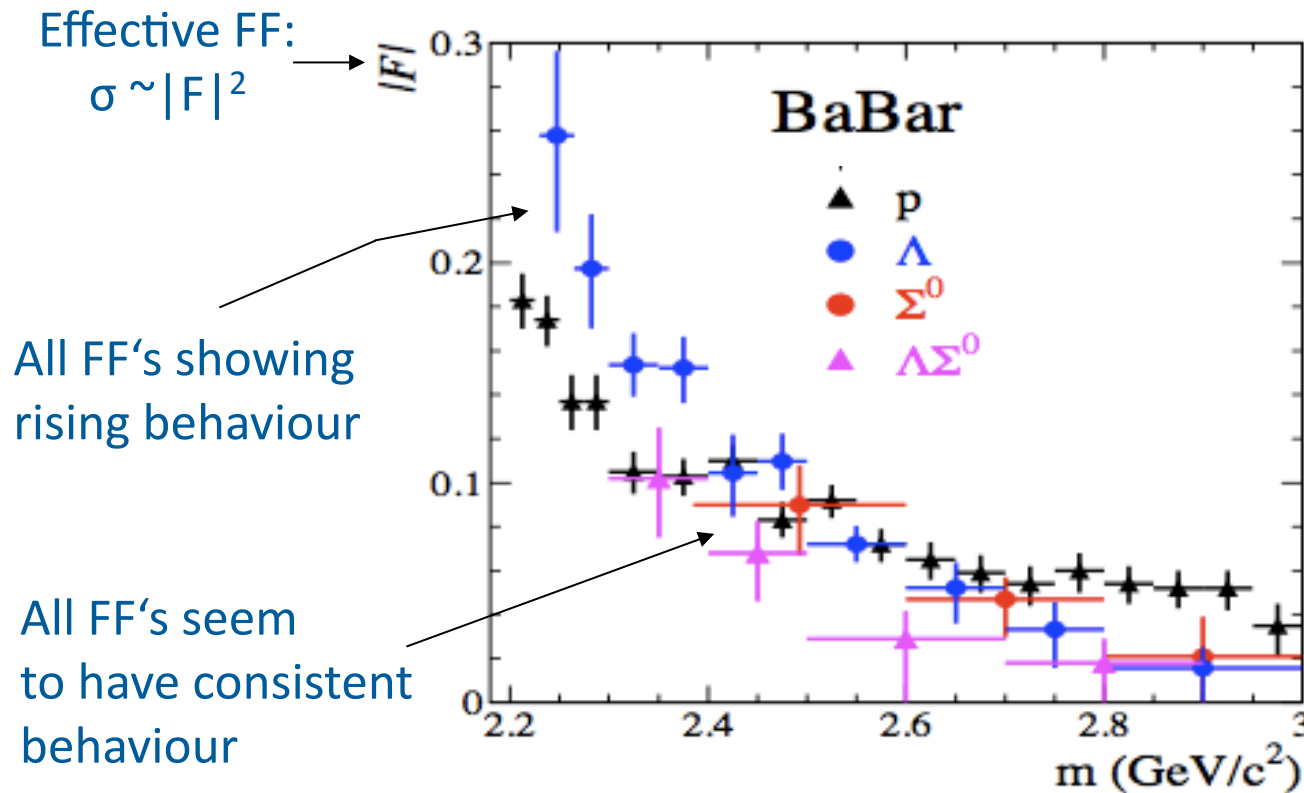


# BABAR: Nucleon Form Factors

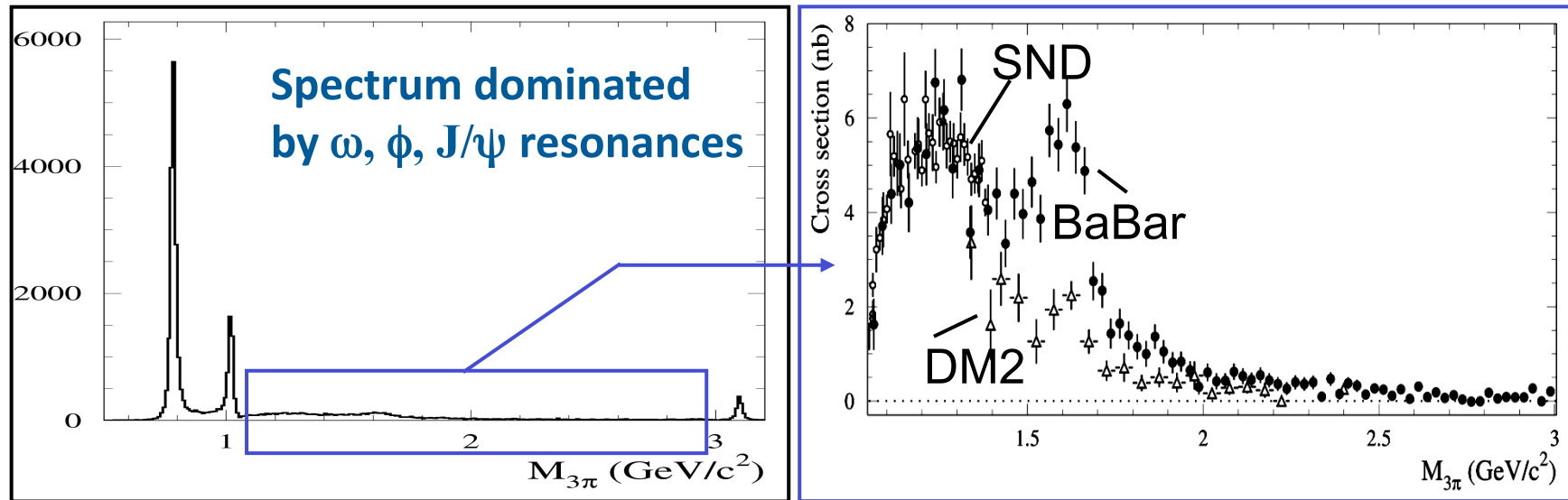
$$\sigma_{B\bar{B}}(m) = \frac{4\pi\alpha^2\beta}{3m^2} \left[ |G_M(m)|^2 + \frac{1}{2\tau} |G_E(m)|^2 \right]$$

Cross section parametrized by magnetic and electric form factors  $G_M$  and  $G_E$

$$\tau = m^2/4m_B^2$$



# ISR-channel $e^+e^- \rightarrow \pi^+\pi^-\pi^0$



## Typical features:

- Precision data up to 1.4 GeV from VEPP-2M
- Above 1.4 GeV: BABAR data provides first high-statistics sample ever
- Large deviation seen with DM2
- World's most precise extraction of  $J/\psi$  branching ratio:  $B(J/\psi \rightarrow 3\pi) = (2.18 \pm 0.19)\%$

# Muon Anomaly $(g-2)_\mu$

**Magnetic Moment:**  $\vec{m} = \mu_B g \vec{S}$   $\mu_B$ : Bohr magneton,  $g$ : gyromagnetic factor  $\sim 2$

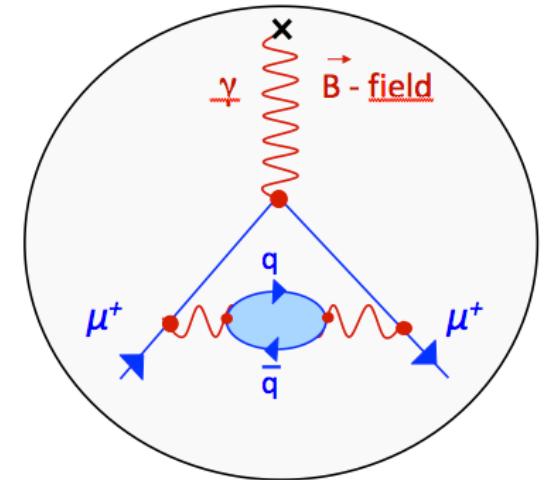
**Muon Anomaly:**  $a_\mu = (g-2)_\mu / 2 = \alpha_{em} / 2\pi + \dots = 0.001161\dots$

■ **Standard Model (SM) prediction  $a_\mu^{SM}$ :**

- QED:  $a_\mu^{QED} = (11\,658\,471.809 \pm 0.015) \cdot 10^{-10}$
- weak:  $a_\mu^{weak} = (15.4 \pm 0.2) \cdot 10^{-10}$
- hadronic:  $a_\mu^{hadr} = (693.0 \pm 4.9) \cdot 10^{-10}$

$$a_\mu^{SM} = (11\,659\,180.2 \pm 4.9) \cdot 10^{-10} \quad \text{Davier et al., 2010}$$

**SM prediction entirely limited by hadronic contribution!**



■ **Direct measurement BNL-E821  $a_\mu^{exp}$ :**

$$a_\mu^{exp} = (11\,659\,208.9 \pm 6.3) \cdot 10^{-10}$$

# Collider BEPC-II and BES-III



**NEW**

## BEPC-II (since 2009):

- Major upgrade of BEPC and BES-III
- Design luminosity:  $10^{33} \text{ cm}^{-2}\text{s}^{-1}$
- R-measurements btw. 2 – 4.5 GeV

## R measurement foreseen in 3 phases

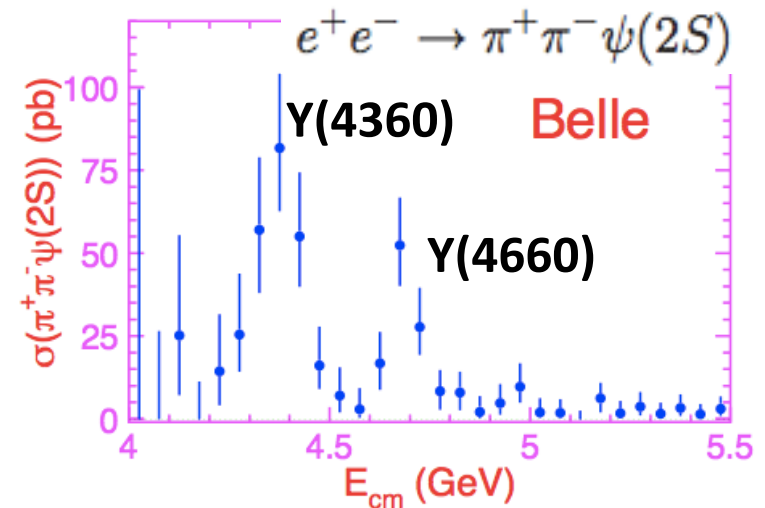
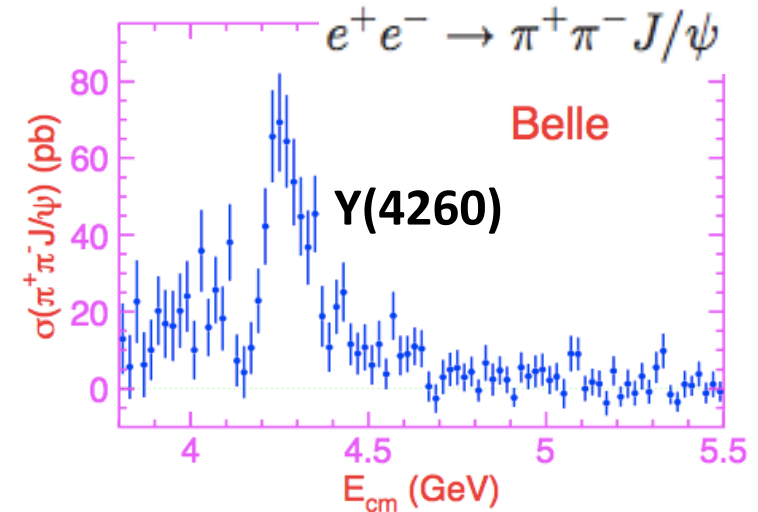
- R in range 2 – 4.5 GeV  
~1% statistical, 3% systematic accuracy  
→ improve  $\alpha_{\text{QED}}(m_Z^2)$  by factor 2
- R in range 2 – 3 GeV, high statistics  
→ Improve nucleon  $|G_E|/|G_M|$  ratio
- Fine binning R ratio in charmonium region → charmonium spectroscopy

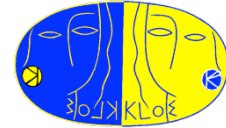


# Radiative Return at BELLE

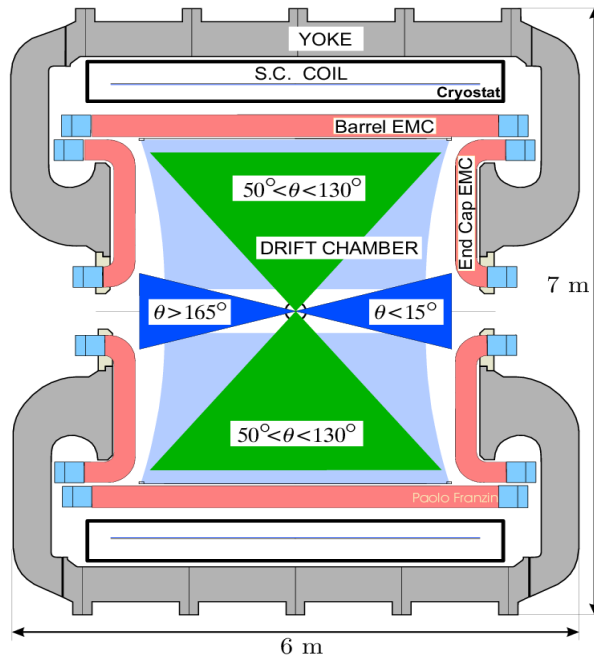
- ISR programme lead to important results on charmonium spectroscopy
- So far no publication on light hadron systems below 3 ... 4 GeV (preliminary result on  $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ )

PRL 98 (2007) 092001	$e^+e^- \rightarrow D^*+D^{*-}, D^+D^{*-}$
PRL 99 (2007) 182004	$e^+e^- \rightarrow \pi^+\pi^- J/\psi$
PRL 99 (2007) 142002	$e^+e^- \rightarrow \pi^+\pi^- \psi(3685)$
PRD 77(2008) 011103	$e^+e^- \rightarrow D^0+D^0\bar{c}, D^+-D^-$
PRL 100 (2008) 062001	$e^+e^- \rightarrow D^0+D^-\pi^+$
PRL 101 (2008) 172001	$e^+e^- \rightarrow \Lambda_c^+ \Lambda_c^-, \Lambda_c^0 \Lambda_c^0\bar{c}$





# KLOE: ISR at 1.02 GeV (DAΦNE)



$$\sigma(e^+e^- \rightarrow \pi^+\pi^-\gamma_{\text{ISR}})$$

## Tagged analysis:

ISR photon measured in KLOE-Calorimeter

- Increased amount of Final State Radiation (FSR)

## Untagged analysis:

No ISR detection; cut on missing momentum

- Threshold mass region not accessible

\*full KLOE statistics 2,500 pb<sup>-1</sup>

Publication	Mode	Normalization	Int. Luminosity*
Phys.Lett. B606 (2005) 12	untagged	Radiator	141 pb <sup>-1</sup>
Phys.Lett. B670 (2009) 285	untagged	Radiator	240 pb <sup>-1</sup>
Phys.Lett. B700 (2011) 102	tagged	Radiator	232 pb <sup>-1</sup>
ArXiv:1212.4524	untagged	$\mu^+\mu^-\gamma$	240 pb <sup>-1</sup>

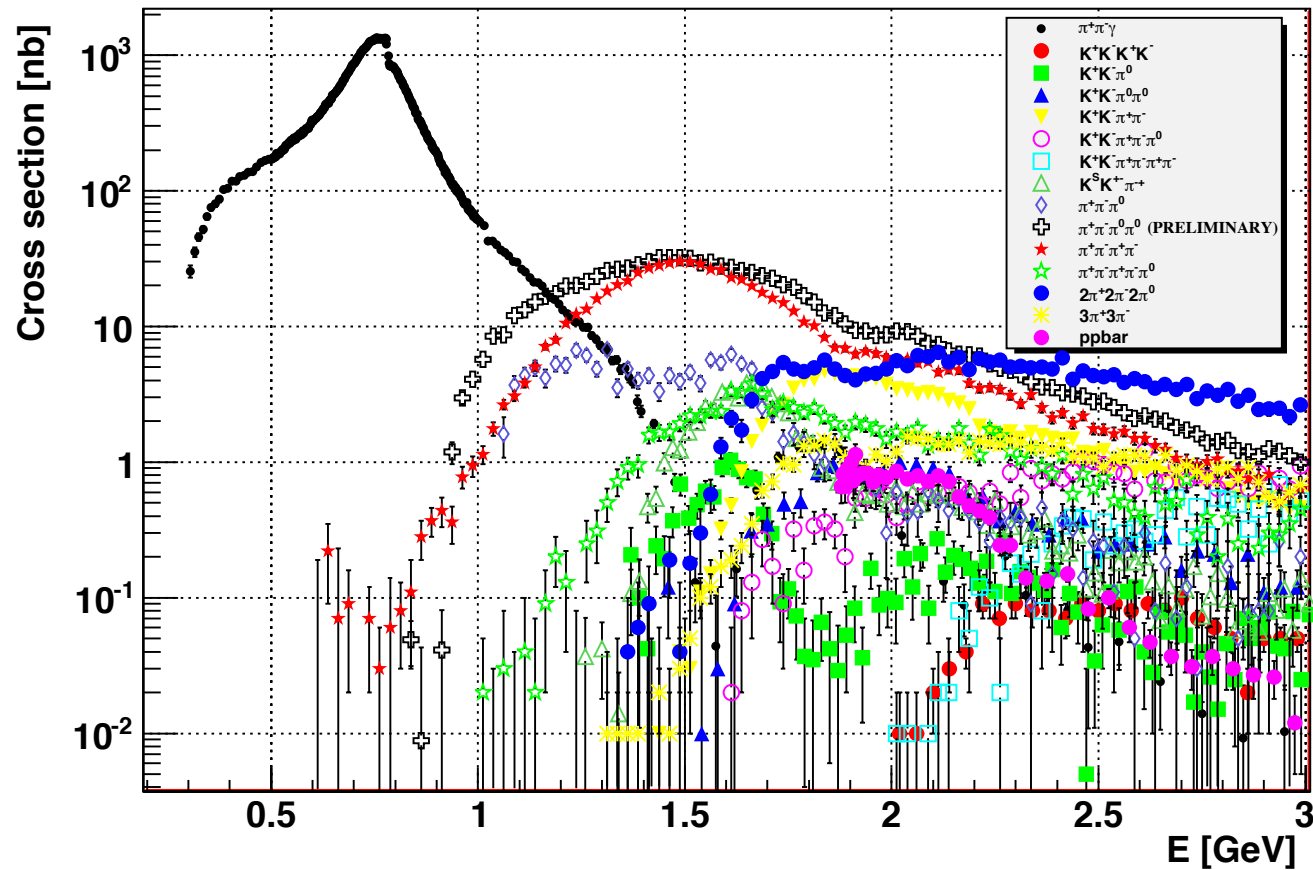


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**BABAR**

# Summary of ISR Results



**Precision:**

$2\pi$ : < 1%

$3\pi$ : ~10%

$4\pi$ : ~3%

$\geq 5\pi$ : 10% and higher

# BABAR: Nucleon Form Factors

$$\sigma_{e^+e^- \rightarrow N\bar{N}} = \frac{4\pi\alpha^2\beta}{3s} C_N(s) \left[ |G_M^N(q^2)|^2 + \frac{2M_N^2}{s} |G_E^N(q^2)|^2 \right]$$

Cross section parametrized by magnetic and electric form factors  $G_M$  and  $G_E$

