

Electron-positron and electron-electron colliders

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INFN- LNF



e⁺e⁻ collider

Physics opportunities with an e⁺e⁻ collider with c.o.m. energy tunable within [$\sim 0.5, \sim 3.0$] GeV

- ✓ the hadronic contribution to muon anomalous magnetic moment a_μ
- ✓ the hadronic contribution to α_{em}
- ✓ spectroscopy and $\gamma\gamma$ physics
- ✓ exotics (**dark forces**)

e⁺e- collider

LNF-10/17(P)

see also Eur. Phys. J. C 50 (2007) 729

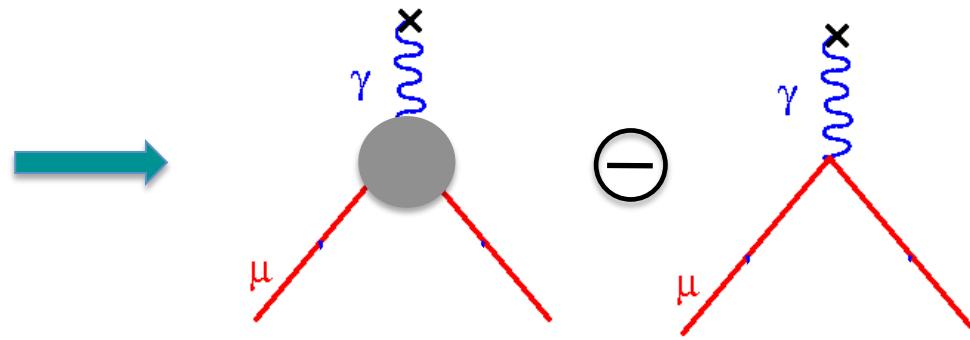
Proposal for taking data with the KLOE-2 detector at the DAΦNE collider upgraded in energy

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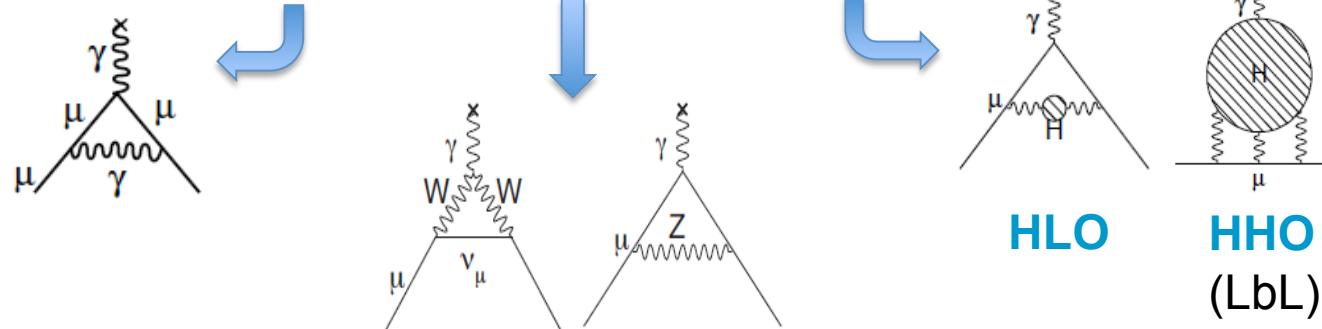
a_μ

one of the most (if not **the most**) significant low-energy constraint
on a wide class of new-physics models

$$a_\mu = \frac{g_\mu - 2}{2}$$



$$a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{Weak}} + a_\mu^{\text{Had}}$$



a_μ

QED & Weak → precisely known

Had → large uncertainty (significant work ongoing)

Contribution	Result ($\times 10^{-11}$) Units
QED (leptons)	$116\ 584\ 718.09 \pm 0.14 \pm 0.4_\alpha$
Weak	$154 \pm 2_{\text{Higgs}} \pm 1_{\text{had}}$
HLO (vac. pol.)	$6\ 923 \pm 42$
HHO (vac. pol.)	-97.9 ± 0.9
HHO (LbL)	105 ± 26
Total SM	$116\ 591\ 802 \pm 42 \pm 26 \pm 2 (49)_{\text{tot}}$

*a*_μ

Experimental result → E821 @ BNL (1997- 2001)



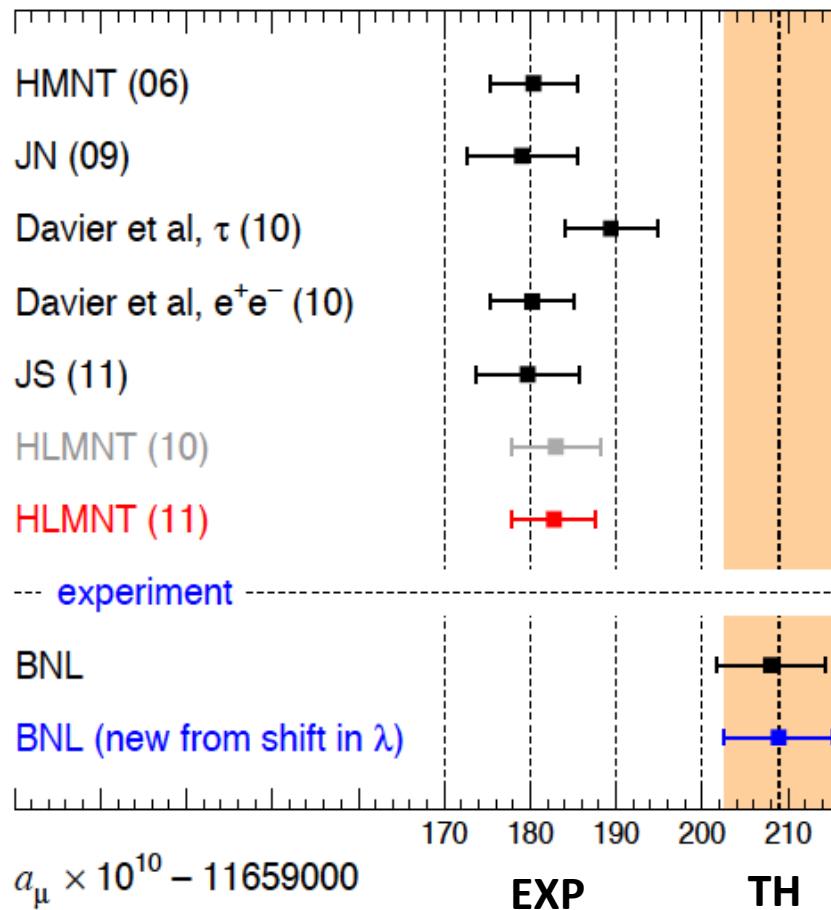
$$a_\mu = 116\,592\,089(54)_{\text{stat}}(33)_{\text{sys}}(63)_{\text{tot}} \times 10^{-11}$$

(0.54 ppm !)

a_μ



$$\text{EXP} - \text{TH} = (28.7 \pm 8.4) \times 10^{-10}$$

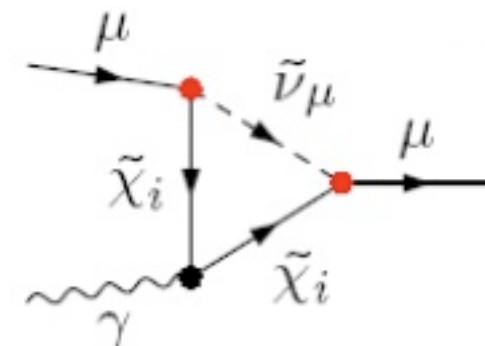


$\sim 3.4\sigma$

NB - the discrepancy is large
compared to Weak contribution

new physics ?

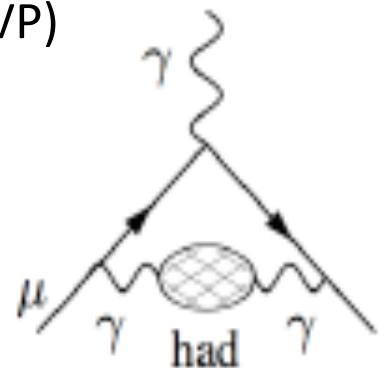
SUSY



a_μ : hadronic contribution

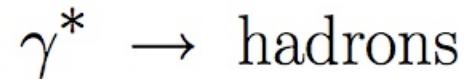
theoretical error $(5 \div 6) \times 10^{-10}$ dominated by hadronic contributions (HLO and LbL)

HLO (VP)

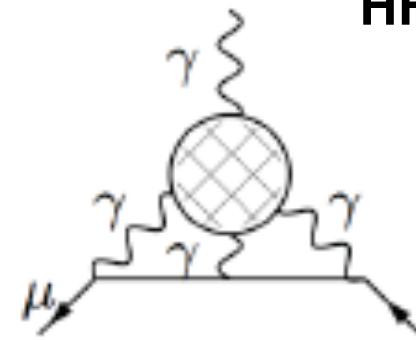


$$a_\mu^{\text{HLO}} = (690.9 \pm 4.4) \times 10^{-10}$$

$\sim 0.6\%$

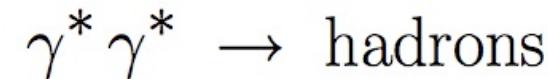


HHO (LbL)



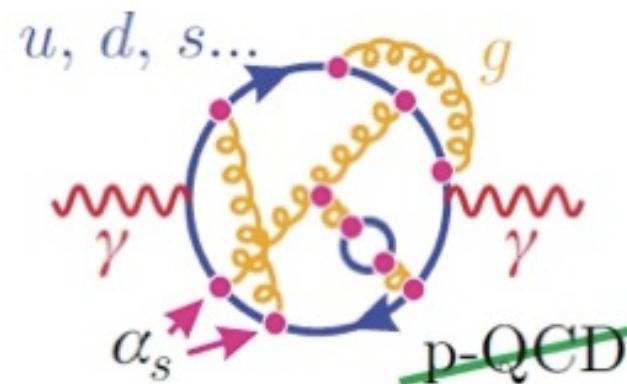
$$a_\mu^{\text{LbL}} = (11 \pm 4) \times 10^{-10}$$

$\sim 40\%$

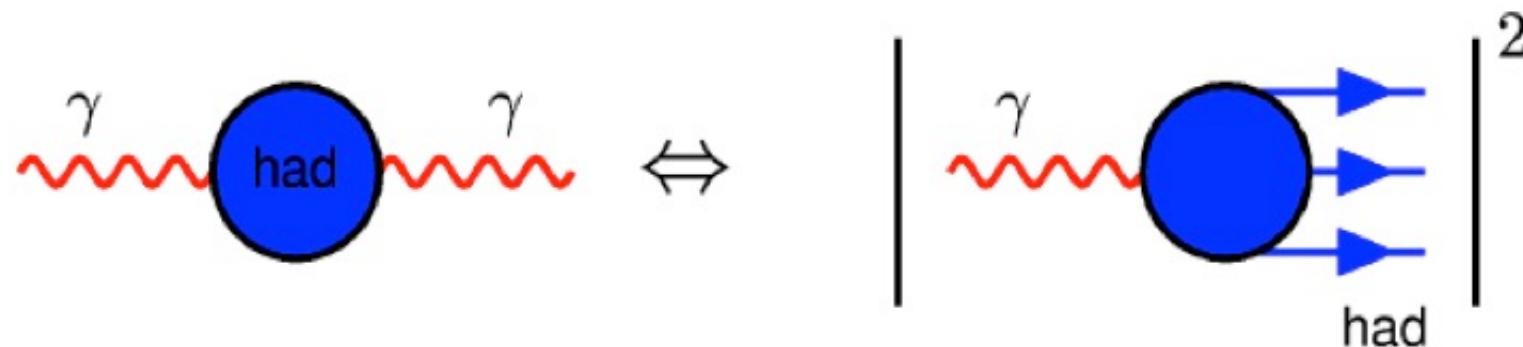


a_μ : hadronic contribution

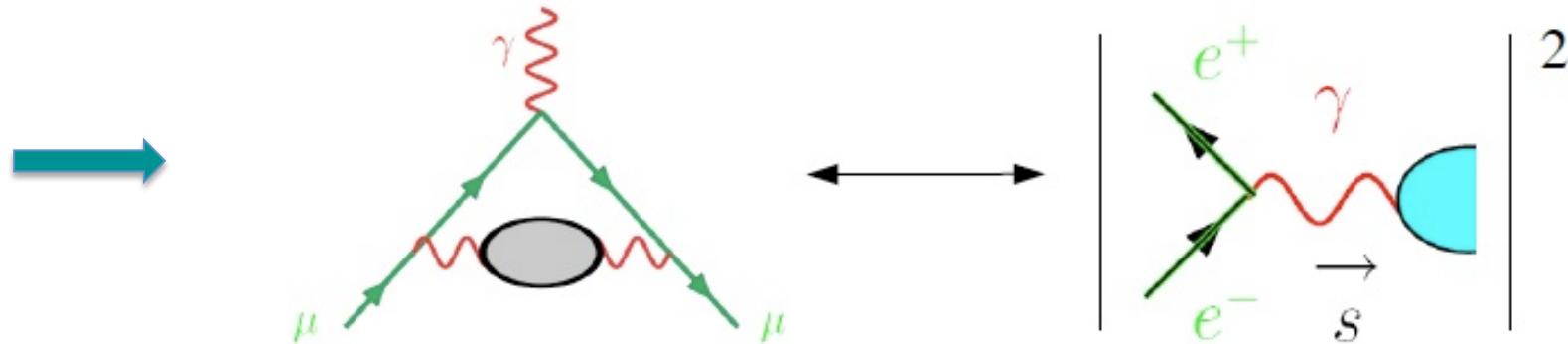
hadronic contribution to vacuum polarization



not calculable at low q^2 ... optical theorem



a_μ : hadronic contribution



$$a_\mu^{\text{HLO}} = \frac{1}{3} \left(\frac{\alpha m_\mu}{\pi} \right)^2 \int_{4m_\pi^2}^\infty \frac{ds}{s^2} \hat{K}(s) R(s)$$

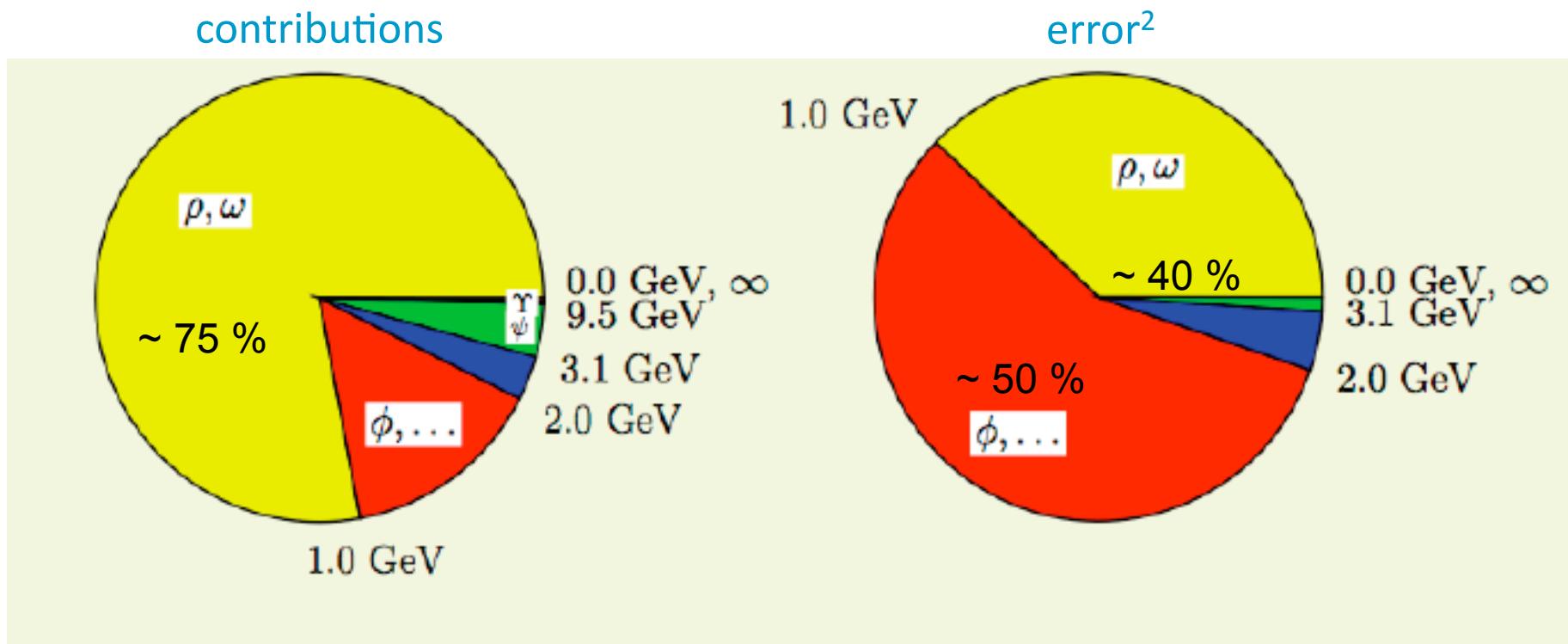
makes important **low**
energy contribution

$$R(s) = \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$$

$$\downarrow \\ e^+e^- \rightarrow \pi^+\pi^-$$

a_μ : hadronic contribution

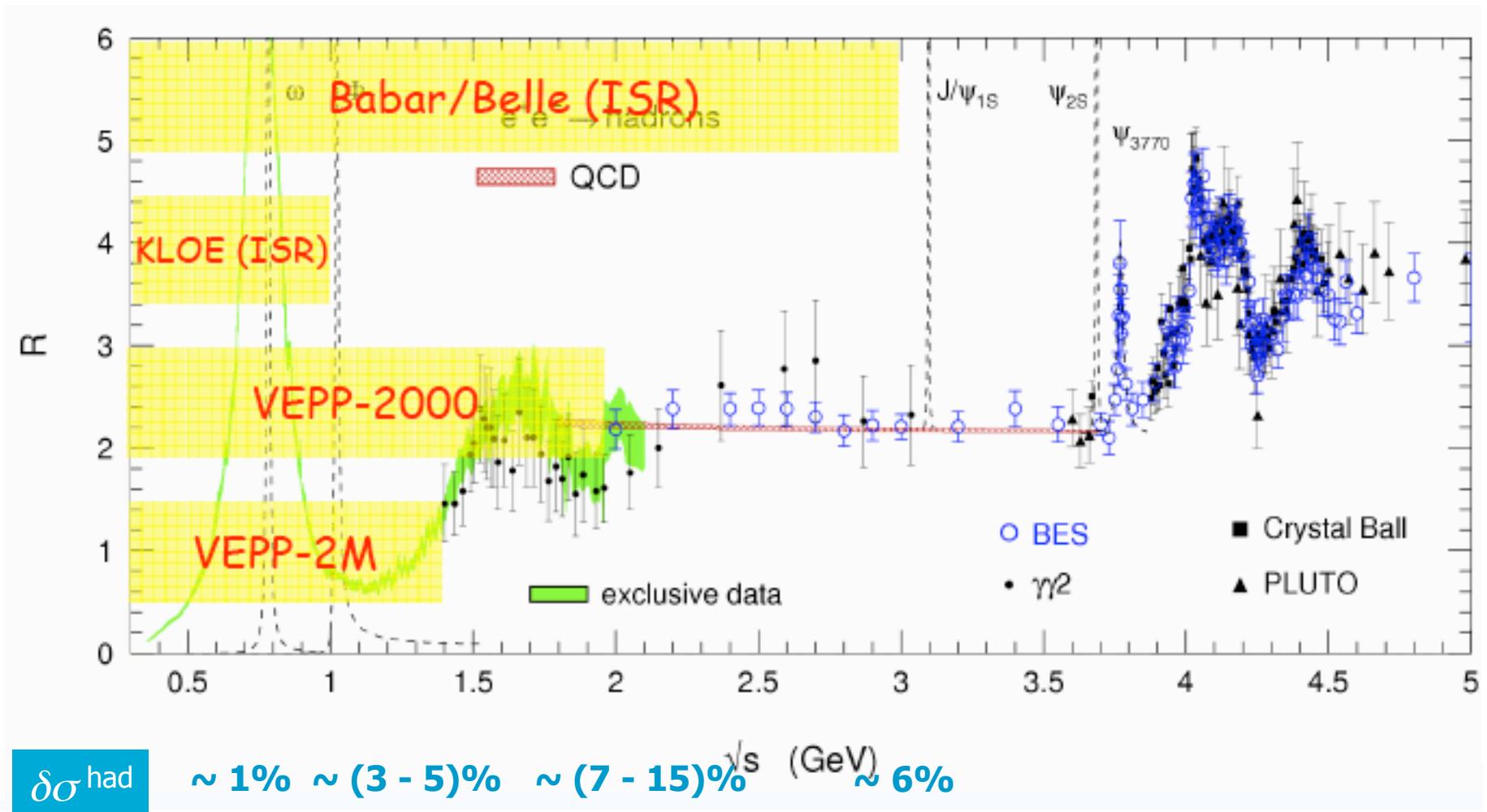
experimental errors on σ^{had} translate into theoretical uncertainty of a_μ^{HLO}



region $< 3 \text{ GeV}$ exhausts dispersion integral

a_μ : hadronic contribution

e^+e^- data: present situation



a_μ : hadronic contribution

$$\text{EXP} - \text{TH} = (28.7 \pm 8.4) \times 10^{-10}$$

$$8.4 = \sim 5 \text{ (HLO)} \oplus \sim 3 \text{ (LbL)} \oplus \sim 6 \text{ (E821)}$$

↓

4.0

2.5

2.5

1.6

new meas.
 $e^+e^- \rightarrow \text{had.}$

$\gamma\gamma$ -physics

new (g - 2)
meas. @ FNAL



(7 - 8) σ

(if 28.7 will remain the same)

this means: $\delta\sigma^{\text{had}} \left\{ \begin{array}{lll} \sim 0.4 \% & \sqrt{s} < 1 \text{ GeV} & 0.7 \% \text{ now} \\ \sim 2 \% & \sqrt{s} \in (1, 2) \text{ GeV} & 6 \% \text{ now} \end{array} \right.$

α_{em} : hadronic contribution

fine-structure constant at the scale M_Z plays a crucial role
in basic EW radiative corrections to SM

$$\alpha(M_Z^2) = \frac{\alpha(0)}{1 - \Delta\alpha(M_Z^2)}$$

(u, d, s, c, b
quarks only)

$$\Delta\alpha_{\text{lept}} + \Delta\alpha_{\text{had}}^{(5)}$$

- ✓ $\Delta\alpha_{\text{lept}}$ → perturbation theory: known up to 3-loop
- ✓ $\Delta\alpha_{\text{had}}^{(5)}$ → dispersion relation:

$$\Delta\alpha_{\text{had}}^{(5)} = -\frac{\alpha M_Z^2}{3\pi} \operatorname{Re} \int_{4m_\pi^2}^\infty ds \frac{R(s)}{s(s - M_Z^2 - i\epsilon)}$$

α_{em} : hadronic contribution

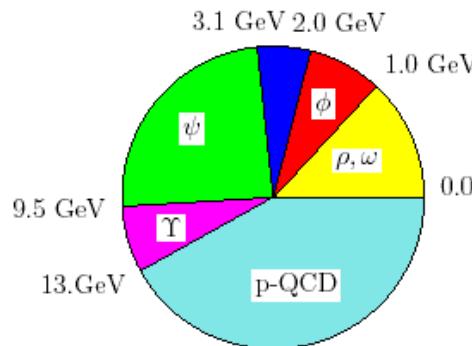
current data:

$$\Delta \alpha_{\text{had}}^{(5)}(M_Z^2) = 0.027607 \pm 0.000225$$

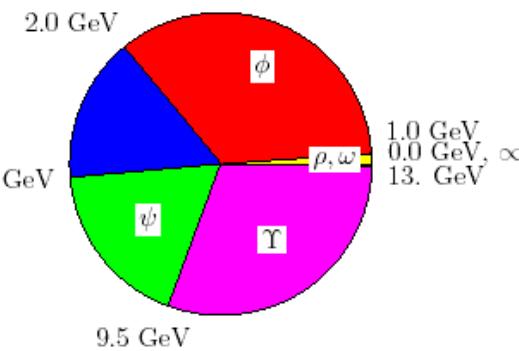


$$\alpha^{-1}(M_Z^2) = 128.947 \pm 0.035 \quad \text{i.e.} \quad \frac{\delta \alpha(M_Z^2)}{\alpha(M_Z^2)} = 2.7 \times 10^{-4}$$

~ one order of magnitude worse than that of M_Z and $G_\mu \rightarrow$
limiting factor in calculation of precise SM predictions



$$\Delta \alpha_{\text{had}}^{(5)}(M_Z^2)$$



$$\delta^2 \Delta \alpha_{\text{had}}^{(5)}(M_Z^2)$$

high-energy region is not a problem: error reduction by theory;
the key problem is the $E < 2.5 \text{ GeV}$ region

ILC with GigaZ

A future linear collider would tremendously improve the precision of electroweak observables

► **$t\bar{t}$ threshold**

- obtain m_t indirectly from production cross section: $\delta m_t = 1 \rightarrow 0.1$ GeV

► **Z peak measurements**

- polarised beams, uncertainty $\delta A^{0,f}_{LR}$: $10^{-3} \rightarrow 10^{-4}$
translates to $\delta \sin^2 \theta_{\text{eff}}^l$: $10^{-4} \rightarrow 1.3 \cdot 10^{-5}$

- high statistics: 10^9 Z decays: $\delta R^0_{\text{lep}} : 2.5 \cdot 10^{-2} \rightarrow 4 \cdot 10^{-3}$

► **WW threshold**

- from threshold scan: $\delta M_W = 15 \rightarrow 6$ MeV

► **Low energy data**

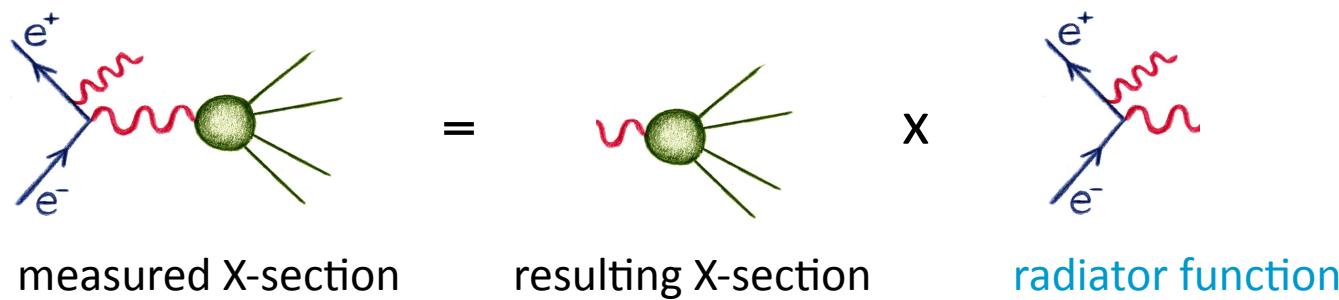
- $\Delta \alpha_{\text{had}}$: more precise cross section data for low energy ($\sqrt{s} < 1.8$ GeV) and around $c\bar{c}$ resonance (BES-III),
improved α_s , improvements in theory: $10^{-4} \rightarrow 5 \cdot 10^{-5}$

σ^{had} measurement

at low energies (≤ 2 GeV) only measurements of exclusive chs. are feasible → two approaches:

✓ Radiative return (KLOE, BABAR, BELLE)

- runs at **fixed-energy** machines (meson factories)
- use **initial state radiation (ISR)** to access lower energies

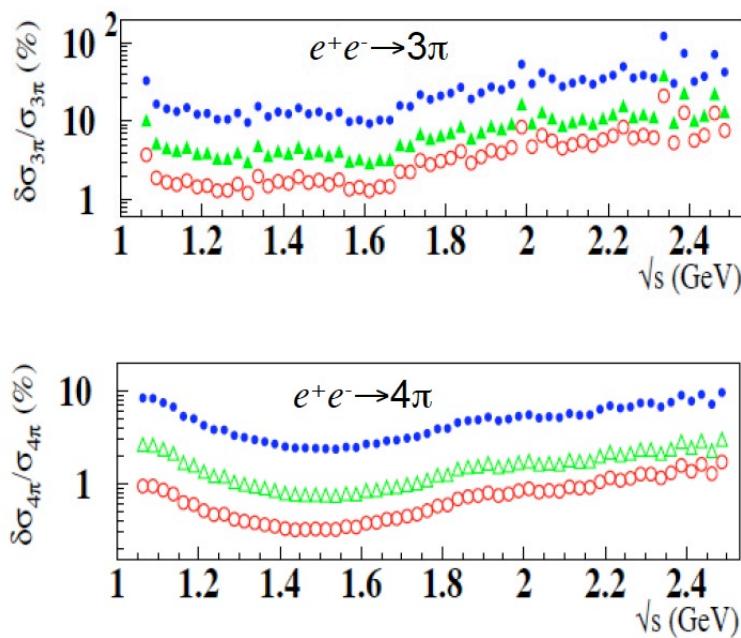


- data as by-product of standard physics program
- requires precise theoretical calculation of **radiator function**
- luminosity and beam energy enter only once for all energy points

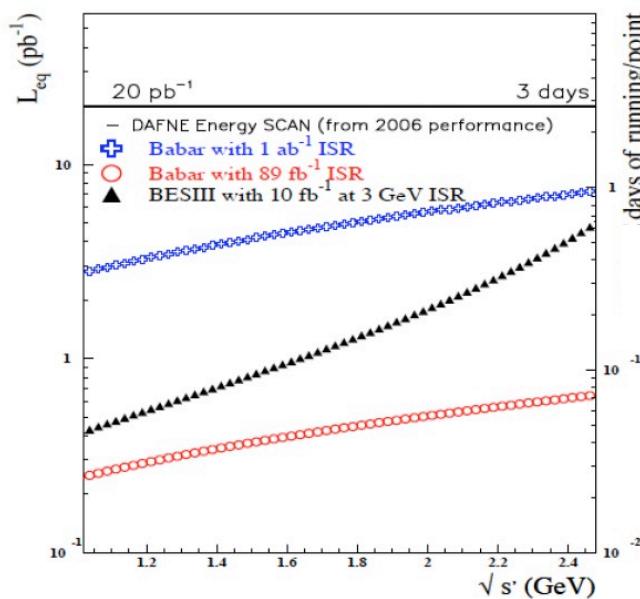
σ^{had} measurement

✓ Energy scan (CMD2, SND)

- energy of colliding beams is tuned to desired value
- “direct” measurement of X-sections
- needs dedicated accelerator/physics program
- needs to measure luminosity and beam energy for every data point



- Published BaBar results: 89 fb^{-1} (ISR)
- “BaBar” $\times 10$ (890 fb^{-1})
- energy scan: $20 \text{ pb}^{-1}/\text{point}$ @ $L = 10^{32} \text{ cm}^{-2}\text{s}^{-1}$,
 $25 \text{ MeV bin} \rightarrow 1 \text{ year data-taking}$



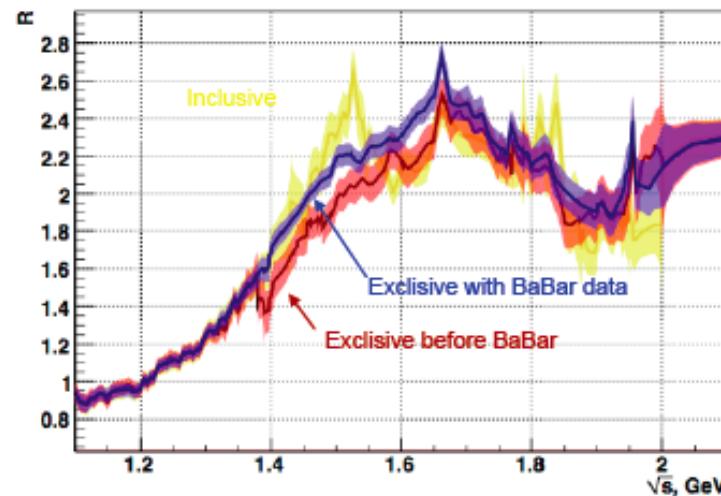
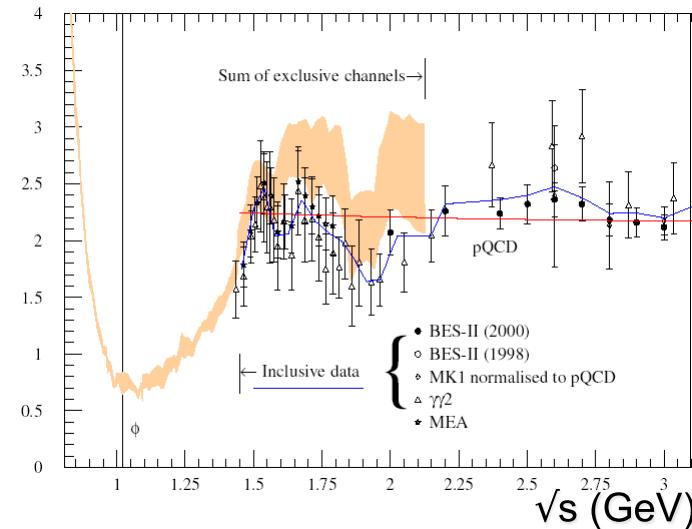
statistically better than a $O(1 \text{ ab}^{-1})$ @ B-factories

σ^{had} measurement

Exclusive vs inclusive measurements

most recent incl. meas.: MEA
and $B\text{-anti}B \rightarrow L_{\text{int}} = 200 \text{ nb}^{-1}$
(1 hour @ $10^{32} \text{ cm}^{-2} \text{ s}^{-1}$): error
 $= 10\% \text{ (stat.)} + 15\% \text{ (sys.)}$

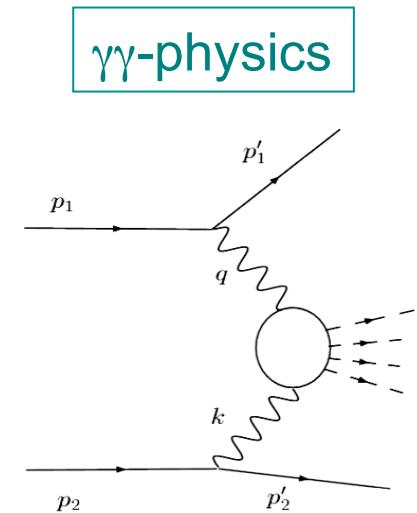
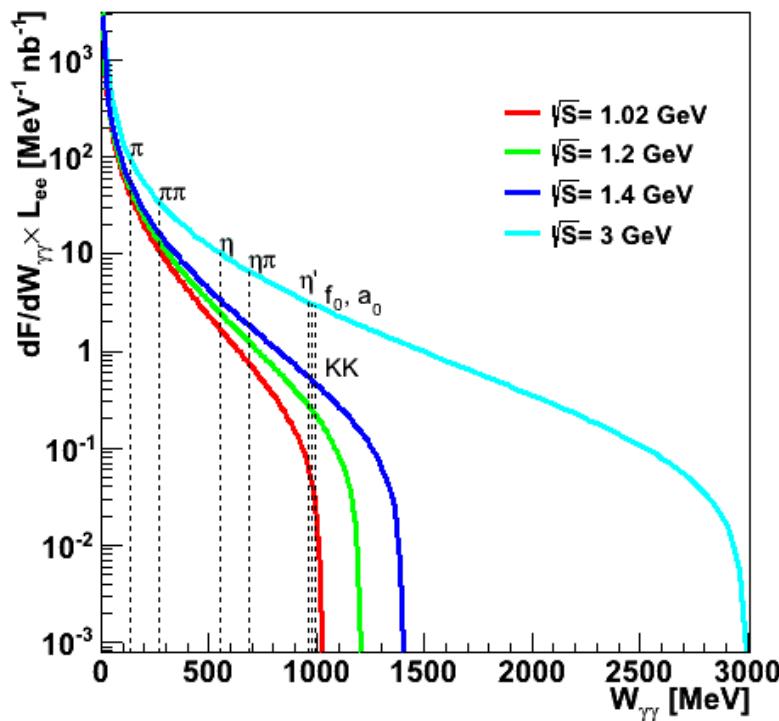
new BaBar data is improving a lot this region, however still remains the question on the completeness of excl. data vs systematics of old incl. meas.



Spectroscopy and $\gamma\gamma$ -physics

Interesting open issues in low-energy spectroscopy (4q states, glueballs, ...) which would strongly benefit from high-precision measurements of

$$e^+e^- \rightarrow \gamma^* \rightarrow X \quad \& \quad e^+e^- \rightarrow e^+e^- \gamma^*\gamma^* \rightarrow e^+e^- X$$



$$\frac{dN_X}{dW_{\gamma\gamma}} = L_{\text{int}} \frac{dF}{dW_{\gamma\gamma}} \sigma(\gamma^*\gamma^* \rightarrow X)$$

$\gamma\gamma$ -physics

Hadronic LbL contribution to $a_\mu \rightarrow$ largely dominated by term



uncertainty due to our ignorance about $F(q_1^2, q_2^2)$ ($q^2 < 0.5 \text{ GeV}^2$)

what we really miss is the function $\frac{d^2 F(q_1^2, q_2^2)}{dq_1^2 dq_2^2}$ $\gamma^* \gamma^* \rightarrow PS$
 $\gamma^* \rightarrow PS \gamma^*$

also O(%) - level measurements of $\Gamma(PS \rightarrow \gamma\gamma)$ are necessary to constrain $F(0, 0)$ (\rightarrow Venanzoni's talk)

NB – $\gamma\gamma$ -physics program can also be carried out at an (same luminosity) e^-e^- collider \rightarrow no bckg from annihilation channel

Dark Forces

(more details in Venanzoni's talk)

Recent astrophysical puzzles:

- ✓ the positron excess observed by the **PAMELA** satellite within a kpc, without observing an excess of antiprotons
- ✓ the 511 keV line from the galactic core observed by **INTEGRAL**
- ✓ the annual modulation observed by the **DAMA/LIBRA** together with the absence of a similar signal from silicon based detectors
- ✓ the low energy spectrum of nuclear recoil events observed by **CoGent**

and the long-standing **Dark Matter** problem → construction of various exotic extensions of the SM characterized by

- new light states (vectors & scalars w/ masses $\in (0.1, 1)$ GeV)
- weakly coupled to γ , or directly coupled to μ and/or e

Dark Forces

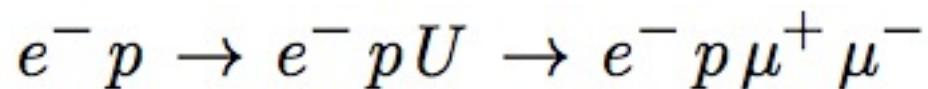


precision differential measurements of

- $e^+e^- \rightarrow e^+e^- + \gamma$
- and/or $e^+e^- \rightarrow \mu^+\mu^- + \gamma$
- and/or $e^+e^- \rightarrow E_{\text{miss}} + \gamma$

at **low energies** are the best way to constrain (or find evidencies of ...) such model

NB – different option: fixed target experiment, e.g.



(see Venanzoni's talk)

e⁺e⁻ collider: conclusion

There is a rich physics program both **below** and **above** 1 GeV:

- ✓ Low-energy program (0.6 ÷ 1.4) GeV is really unique → **NO** competition from other facilities
- ✓ High-energy region (1.4 ÷ 3.0) GeV is still poorly known: fractional accuracy of $\sigma^{\text{had}} \sim 6\%$ → reduction to 2% would have strong impact on precision tests of SM via a_μ and $\alpha_{em}(M_Z)$
- ✓ Interesting $\gamma\gamma$ -physics program → improvement in accuracy of LbL contribution to a_μ + spectroscopy
- ✓ Searches for an hidden “parallel” world with potential manifestations at ~ 1 GeV

e⁺e⁻ collider: conclusion

This physics program, to be completed in a reasonable time (2-3 years of data-taking), requires a collider with:

- ✓ Luminosity $\sim (2 - 3) \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$

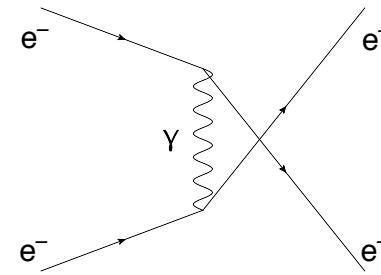
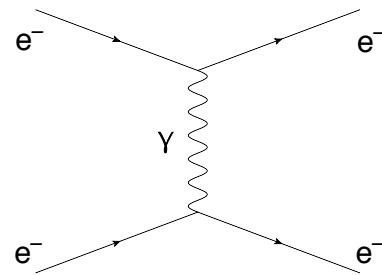
and, for σ^{had} measurement,

- ✓ variable energy in the range $\sqrt{s} = (0.6 \div 3.0) \text{ GeV}$
(in steps of $\sim 25 \text{ MeV}$)

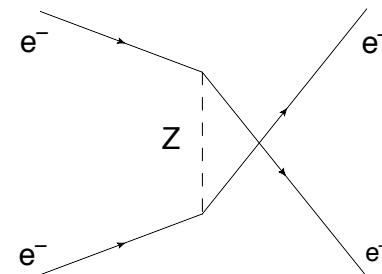
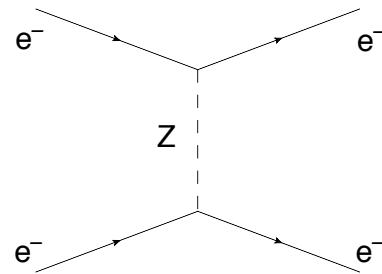
e⁻e⁻ collider

Physics opportunities with an e⁻e⁻ collider have also been explored

- ✓ $\gamma\gamma$ physics → as for e⁺e⁻ but w/out the bckg associated to the annihilation channel



- ✓ weak mixing angle θ_W → Moller scattering: γ -Z⁰ interference



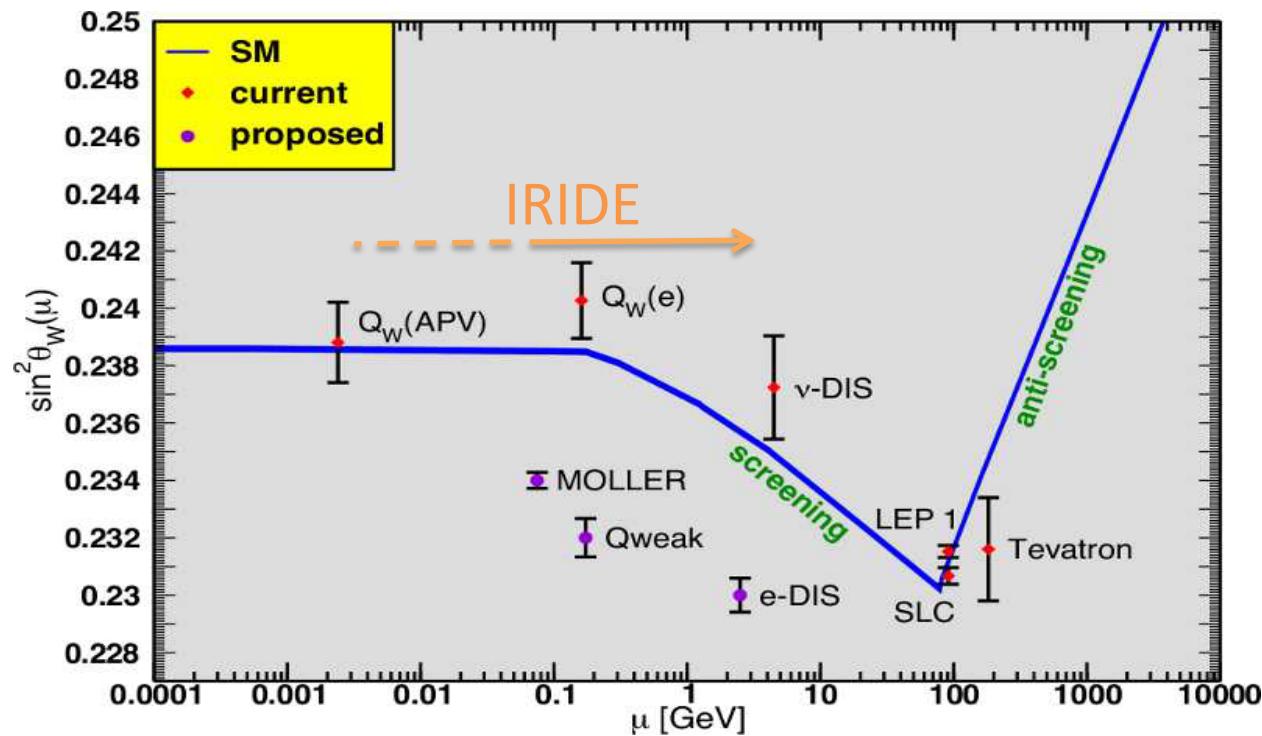
e⁻e⁻ collider



measurement of parity violating asymmetry

$$A_{\text{PV}}^{(2)} = \frac{\sigma_{RR} - \sigma_{LL}}{\sigma_{RR} + \sigma_{LL}}$$

(subscripts denote initial e⁻e⁻ states' polarization)



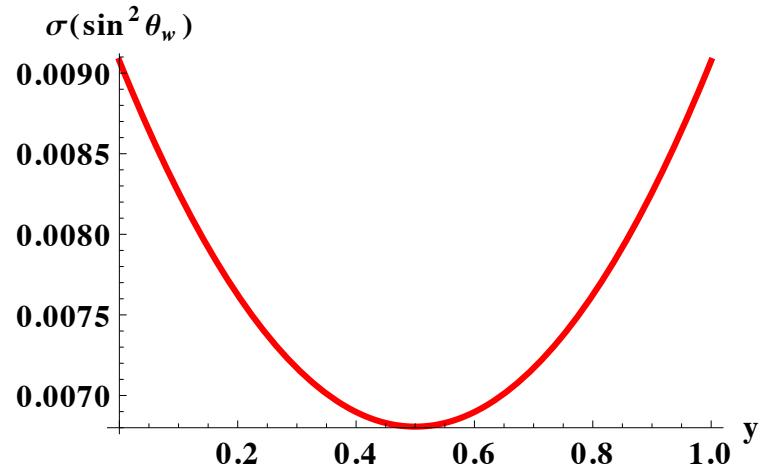
$$= Q = \sqrt{y s} \quad \left(y = \frac{1 - \cos \theta_{\text{cm}}}{2} \right)$$

e⁻e⁻ collider

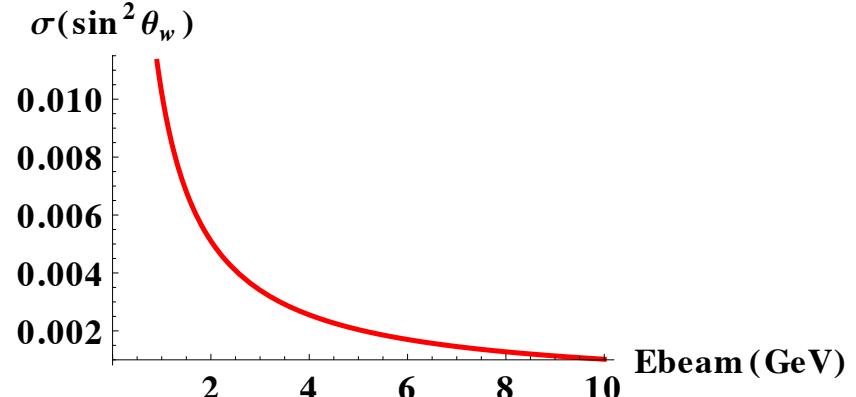
required accuracy: $\sigma(\sin^2 \theta_W) \leq 4 \times 10^{-3}$

↳ MOLLER@JLAB

$$\begin{cases} E_{\text{beam}}(\text{GeV}) = 1.5 \\ L(\text{fb}^{-1}) = 100 \end{cases}$$



$$\begin{cases} y = 0.5 \\ L(\text{fb}^{-1}) = 100 \end{cases}$$

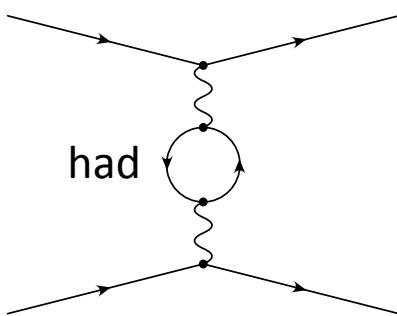


→ at least 100 fb^{-1} in the μ -region covered by IRIDE (!!)

e⁻e⁻ collider

... but the measurement of $\sin^2 \theta_W$ can also be done with an e⁻ beam against a fixed target (e.g., Qweak @ JLAB, P2 @ Mainz), were effective luminosity compensate for the low asymmetry (see Venanzoni's talk)

- ✓ vacuum polarization → possibility to obtain a_μ^{had} from t-channel diagram in Moller scattering



(M. Passera, L. 32, G. Venanzoni
in progress)