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# Saturation effects in final states due to CCFM with absorptive boundary

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## Motivation

- HERA → hints that at small fraction of proton momentum  $x \sim 10^{-4}$  and low virtuality of the parton → new kind of dynamics: BFKL growth? saturation?
- However, at HERA we cannot clearly see it. In the future we will probe gluon density at smaller proton momentum fraction.
- We know that NLO corrections to BFKL and for DGLAP are large.
- Important → use BFKL + DGLAP → one is source of subleading corrections for the other. Compact way → CCFM.
- Be prepared for description of dense partonic system → possible saturation effects
- In  $k_T$  factorisation approach one can address problems of saturation.
- Monte Carlo approach allows us to study exclusive processes.
- CASCADE is MC in  $k_T$  factorisation approach where saturation -high density physics can be addressed

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## CCFM evolution equation

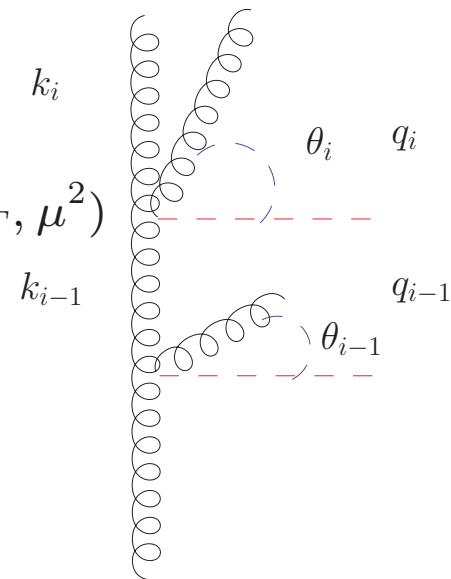
Strong ordering in angle of emitted gluons:  $\theta_i \gg \theta_{i-1}$

Integral equation:

$$xA(x, k_T, \mu^2) = xA_0(x, k_T, \mu^2) + K \otimes xA(x, k_T, \mu^2)$$

Contains information on angular distribution.

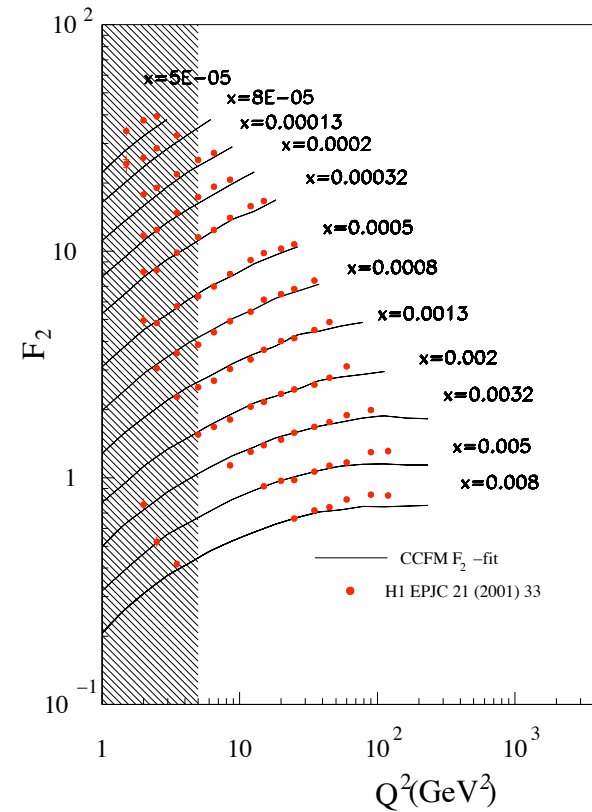
$k_T$  transverse momentum of the most upper gluon  $\mu$ , factorization scale,  $xA_0(x, k_T, \mu^2)$  ← to be determined by fit. Implementation of CCFM in Monte Carlo → CASCADE (H.Jung)



## $F_2$ from CCFM

$$F_2(x, Q^2) = \Phi(k_T^2) \otimes x A(x, k_T^2, Q^2)$$

- Good description
- However, at lower  $x$ ...



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## Possible new effects

- CCFM is a linear  $A(x, k_T, \mu^2) \sim x^\beta$
- Unitarity requirements  $\rightarrow A(x, k_T, \mu^2)$  "less steep growth" e. g.  $\log(x) \rightarrow$  saturation

Saturation sort of recombination of partons

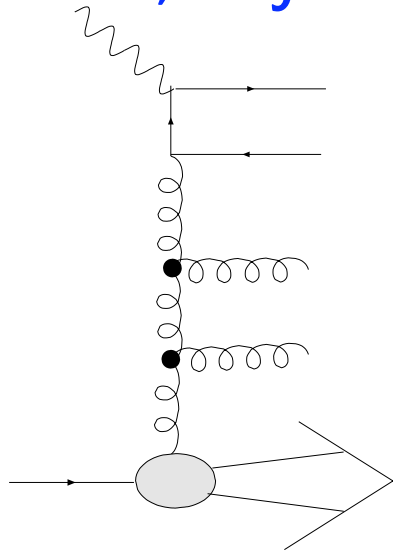


introduces part of unitarity corrections

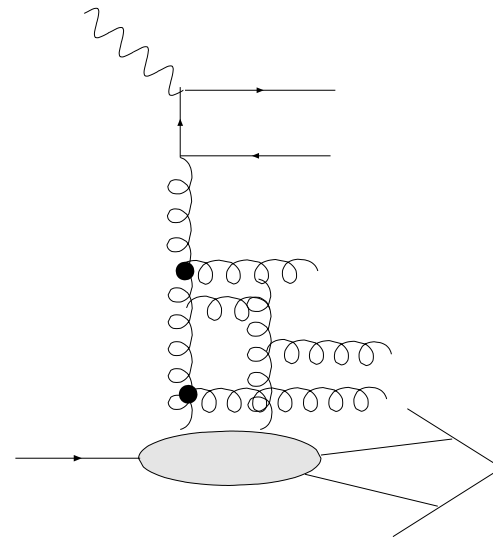


modeled by nonlinear evolution equations (Balitsky-Kovchegov, JIMWLK)

# Saturation, Feynman diagrams and evolution equation



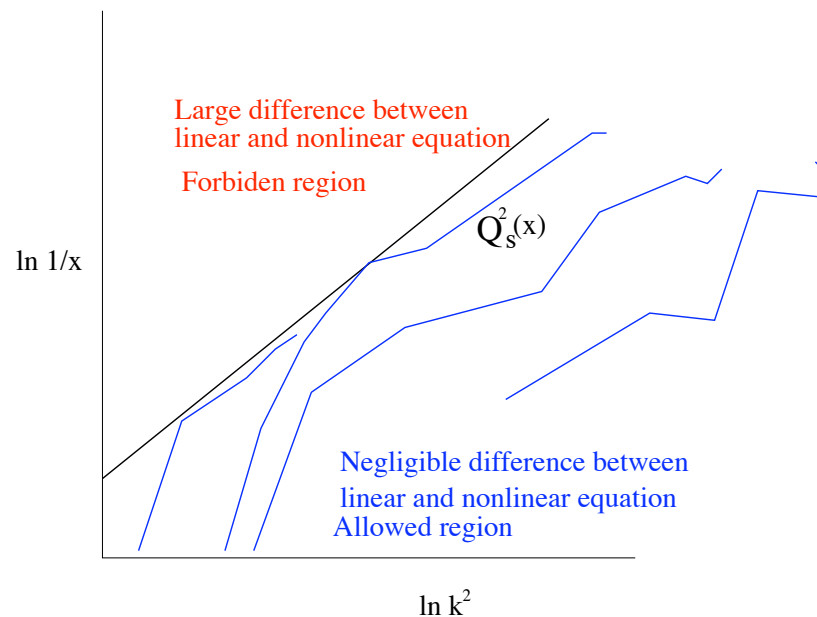
Leads to linear evolution equation  
BFKL, CCFM,...



Leads to nonlinear evolution equation  
BK, GLR, GLRMQ

- Nonlinearity  $\rightarrow$  saturation scale emerges  $Q_{sat}$
- On solid grounds for nuclei, model for nucleon
- Leads to geometric scaling  $\rightarrow \sigma_{\gamma^*p}(x, Q^2) = \sigma_{\gamma^*p}(Q^2/Q_s^2)$

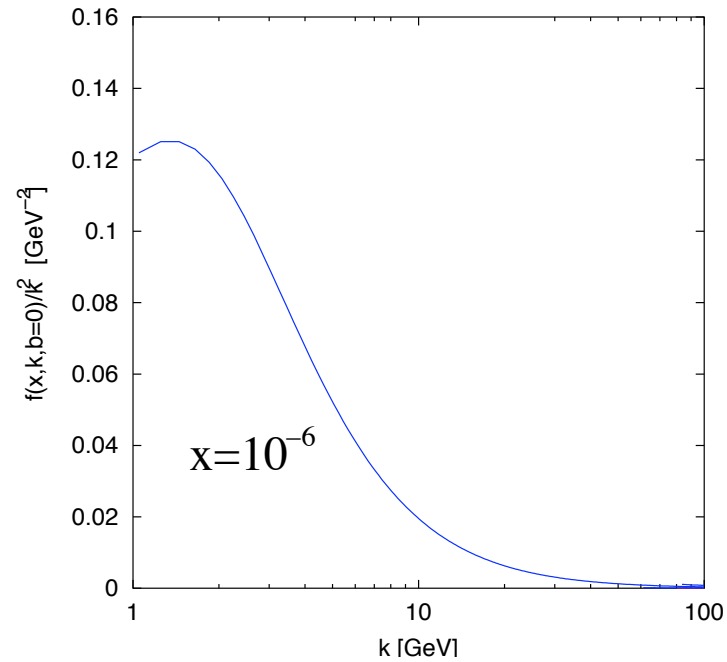
## Saturation and linear evolution equation



- One can require the amplitude coming from linear evolution equation (BFKL, CCFM) for some combination of gluon momentum and rapidity to be constant and close to unity  $\rightarrow$  this defines saturation line in "linear approach" (Mueller, Trintafyllopoulos).
- Monte Carlo  $\rightarrow$  it means that events that end up in saturated region are rejected
- At present we use GBW saturation line  $Q_{sat} = Q_0(x_0/x)^{\frac{\lambda}{2}}$

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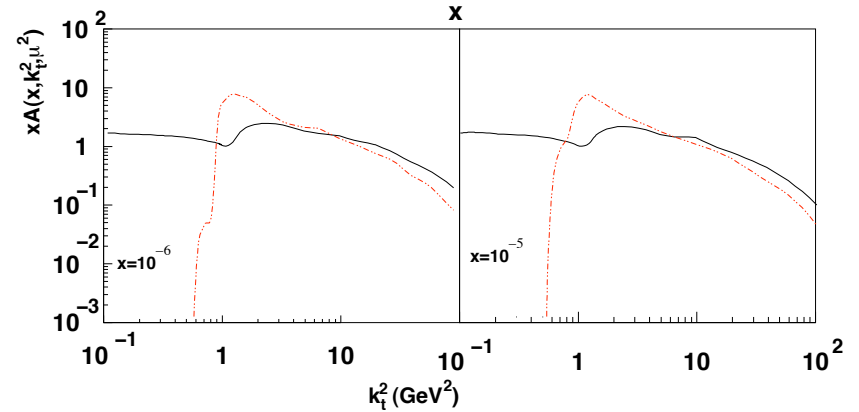
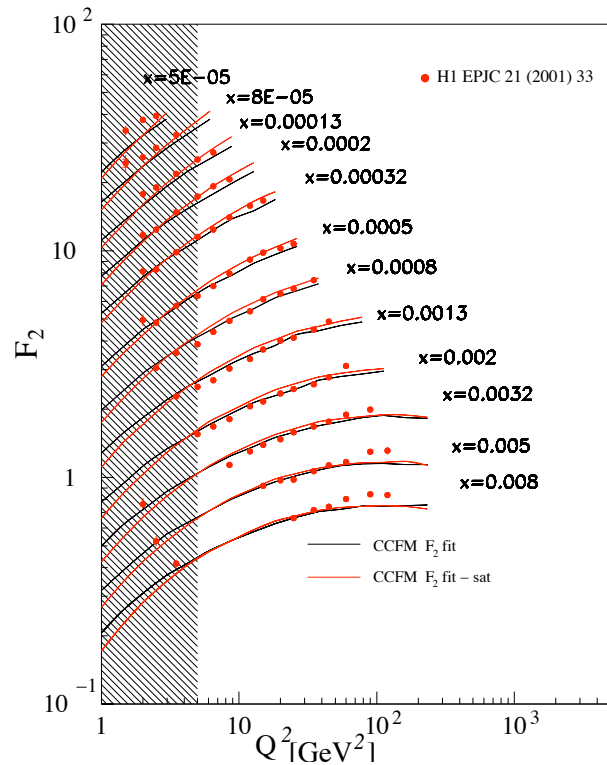
## Example and lesson from BK for unintegrated gluon density



- Saturation scale emerges
- Universal shape for fixed impact parameter

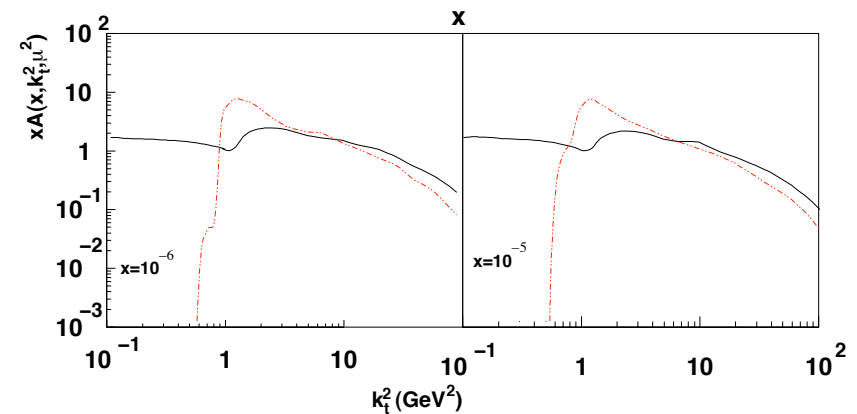
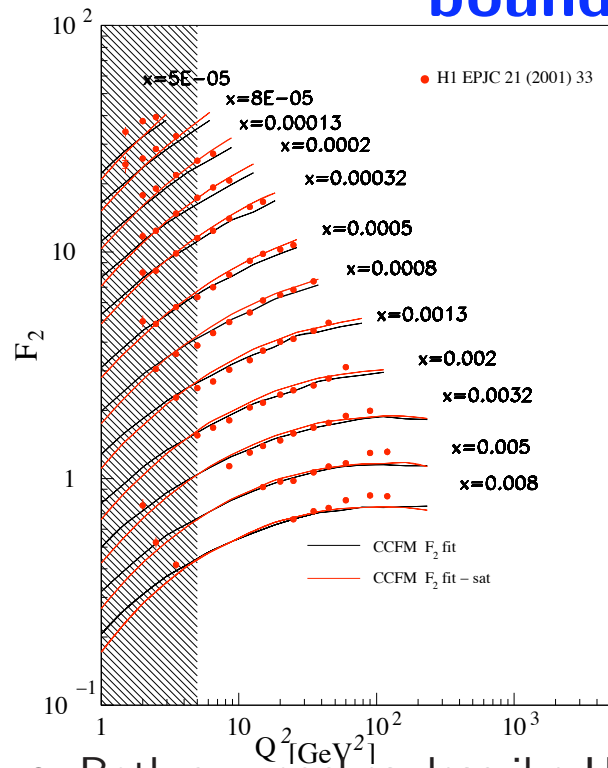


# $F_2$ and gluon density from CCFM with absorptive boundary - preliminary results



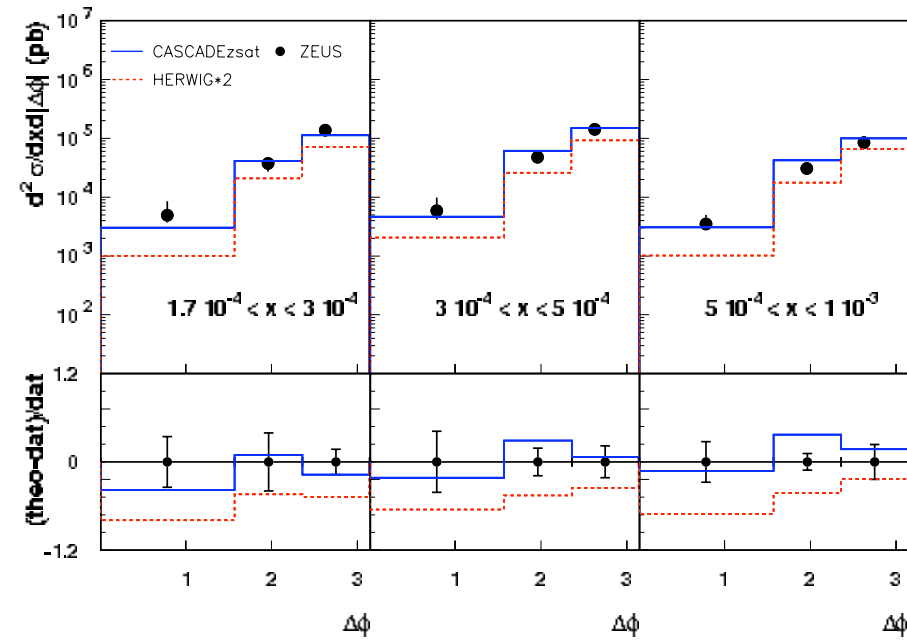
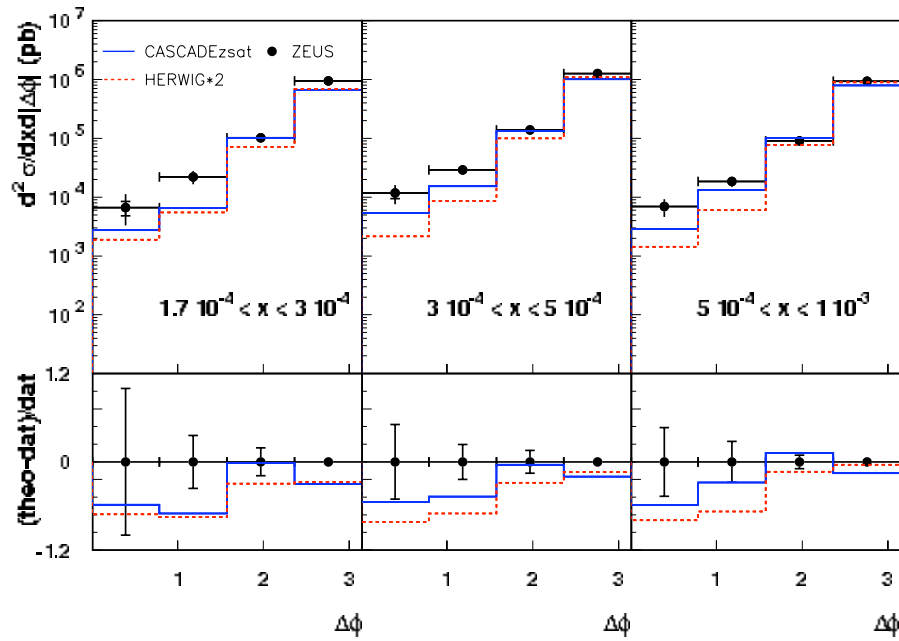
Parameters  $\rightarrow xA_0(x, k^2) = Nx^\alpha(1-x)^4 e^{(k^2-k_0^2)/\mu}$ ,  $Q_{sat} = Q_0(x_0/x)^{\lambda/2}$

# $F_2$ and gluon density from CCFM with absorptive boundary - preliminary results



- Both approaches describe HERA data equally well. However, gluon densities are different...
- Possible implications for exclusive directly sensitive to  $k_T$  observables...

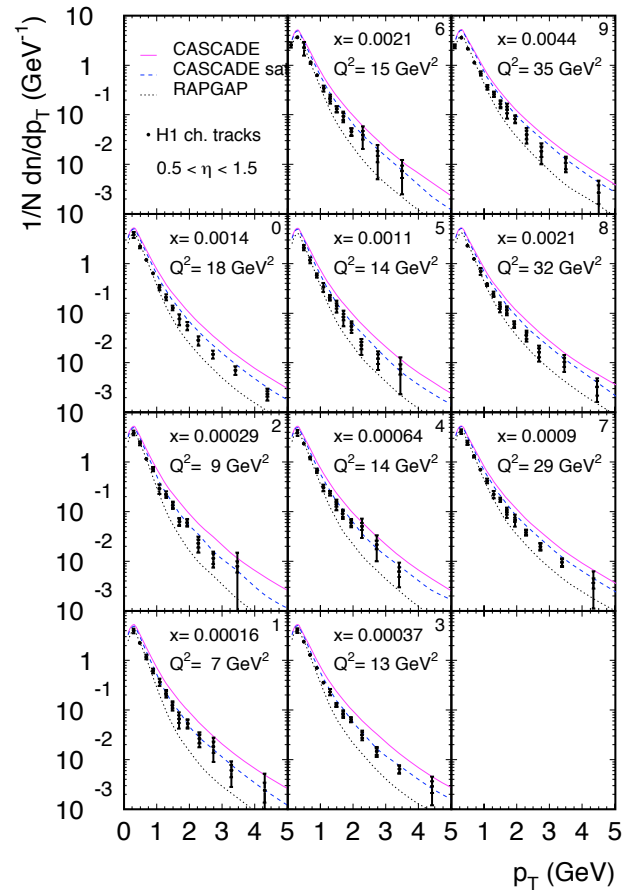
# Angular distribution of jets in DIS



- left figure → dijets
- right figure → three jets

# Distribution of charged particles

Data → desy96-215-1



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## Conclusions and outlook

- We addressed successfully saturation issues within CCFM Monte Carlo approach
  - We obtained reasonable description of  $F_2$  data
  - We have description of exclusive observables with saturation
  - We studied DIS but we can also address hadron-hadron questions.
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- Impact parameter issues
  - Various scenarios for input distribution