

Top quark physics

Eric Laenen



UNIVERSITEIT VAN AMSTERDAM



Universiteit Utrecht



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La Sapienza, 29 April 2013

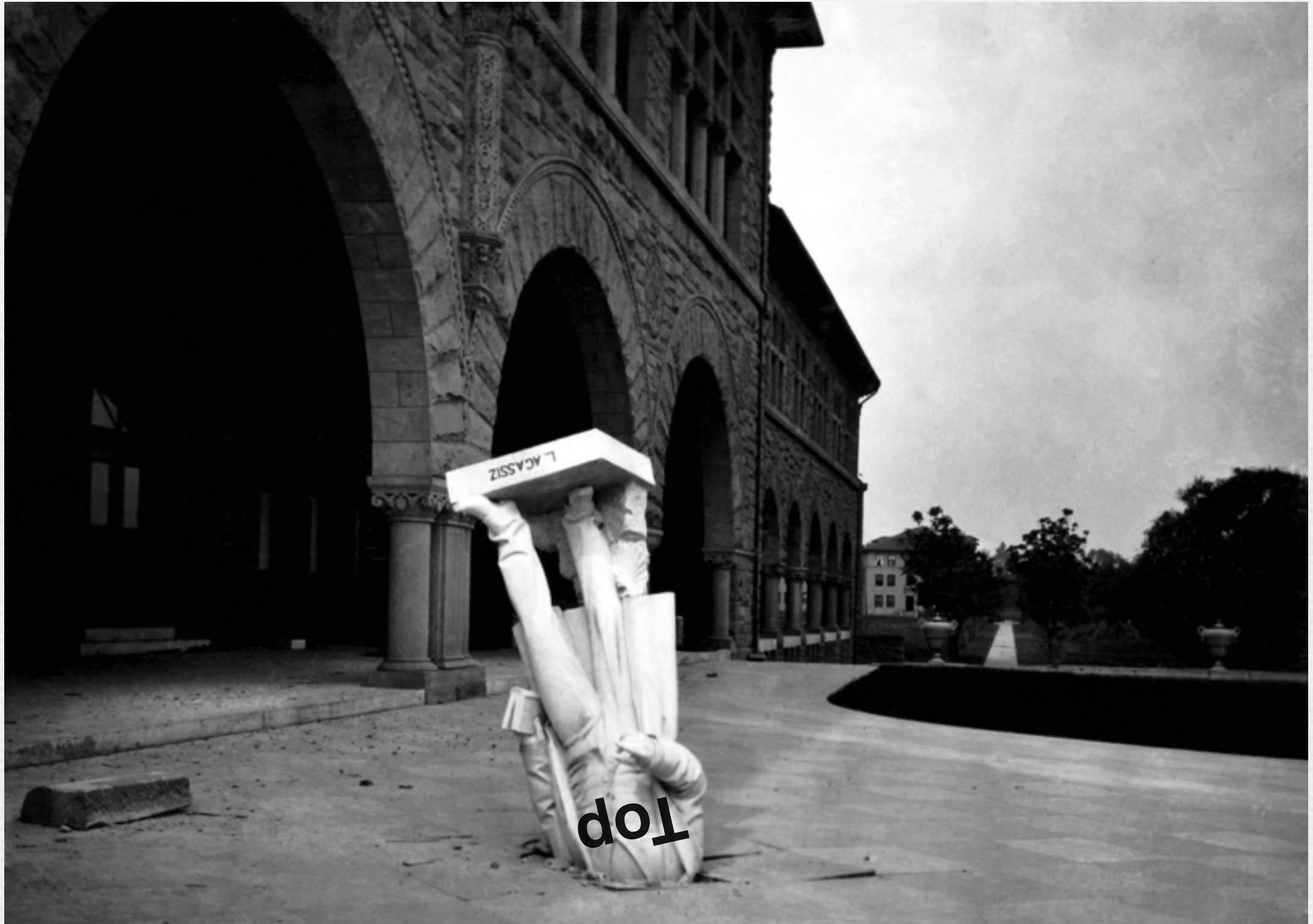
The manifold uses of top

- ▶ The heaviest elementary particle so far, that's already interesting
- ▶ A beautiful, shiny object



- ▶ Imperfections (indicating more than SM) easier to spot
- ▶ Gateway to physics above the EW scale (Higgs,..)
- ▶ Until recently, top was a rare creation, on a pedestal

But, things change.



Top sightings



Top sightings



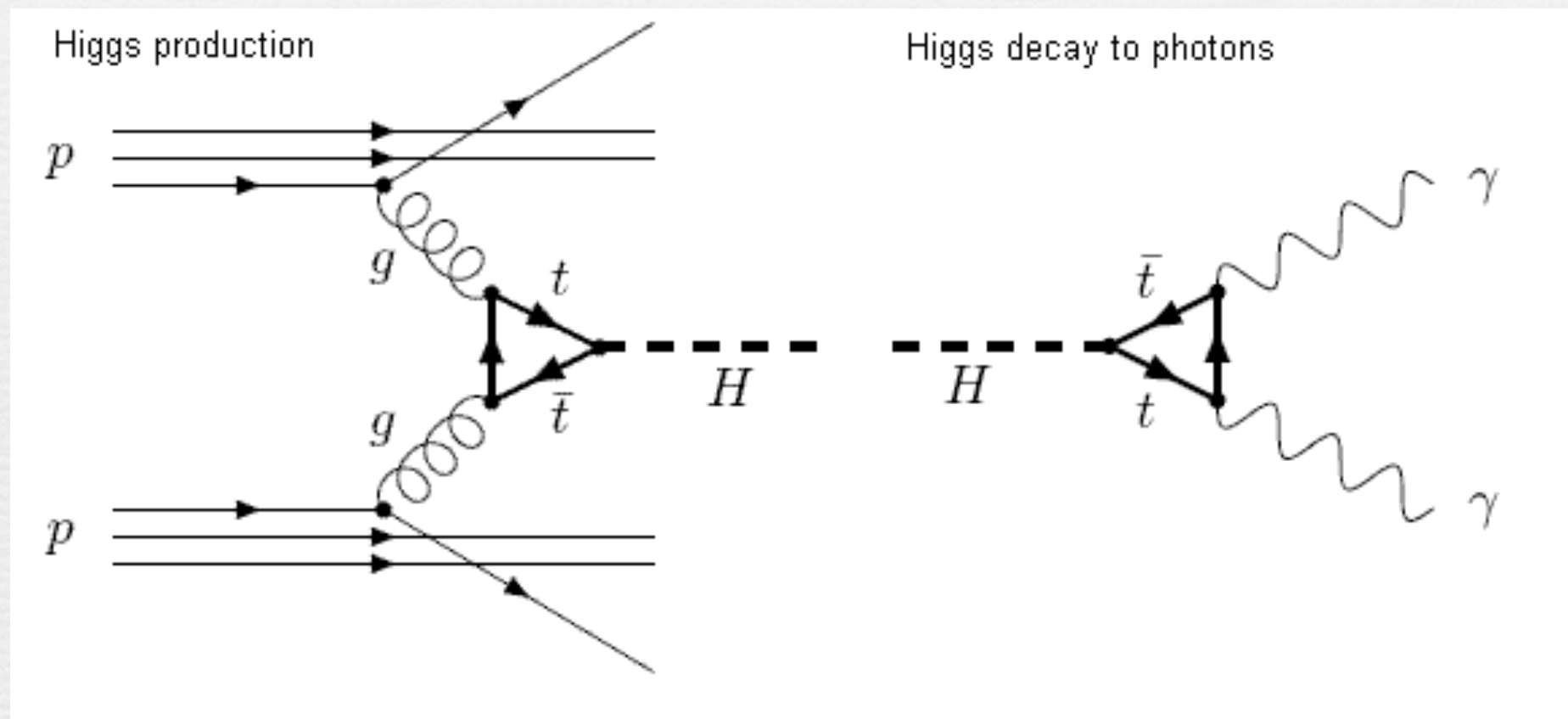
Top sightings



In fact, many many tops produced by now



Still, top = matter of life and death for Higgs



Outline

- Top in the Standard Model
- Top beyond the Standard Model
- Various top observables
 - Top pairs
 - Mass
 - Single top
 - Charge asymmetry
- Correlations, angular distributions
- Conclusions

Standard Model Lagrangian

$$\mathcal{L}_{SM} = \sum_f \bar{\psi}_f \not{D} \psi_f + \text{Tr} [D_\mu, D_\nu] [D^\mu, D^\nu] + D_\mu \Phi^\dagger D^\mu \Phi - V(\Phi) + Y(\psi, \Phi)$$

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- ▶ Lagrangian made of fields monomials (powers 2,3,4) and couplings
- ▶ Fields correspond to (anti)particles
- ▶ More quantum numbers than just spin: flavor, color, isospin,...
- ▶ Form dictated by symmetries, both global and local
- ▶ E.g. left-handed 3rd generation quark (fermionic) field

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Color: $i=1,2,3$ Isospin: $a=1$ (top), 2 (bottom)

Lefthanded $\psi_{L\alpha}^{i,a}(x^\mu)$ Spacetime coordinate

Lorentz spinor: $\alpha=1..4$

Mass generation in SM

Expanding Higgs doublet around the groundstate

$$\Phi(x) = e^{i\xi^i(x)\sigma_i} \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}$$

↑
Higgs boson field

$$y_f[v + h(x)]\bar{\psi}_f\psi_f = m_f\bar{\psi}_f\psi_f + y_fh(x)\bar{\psi}_f\psi_f$$

Fermion mass term *Higgs-fermion-fermion interaction*

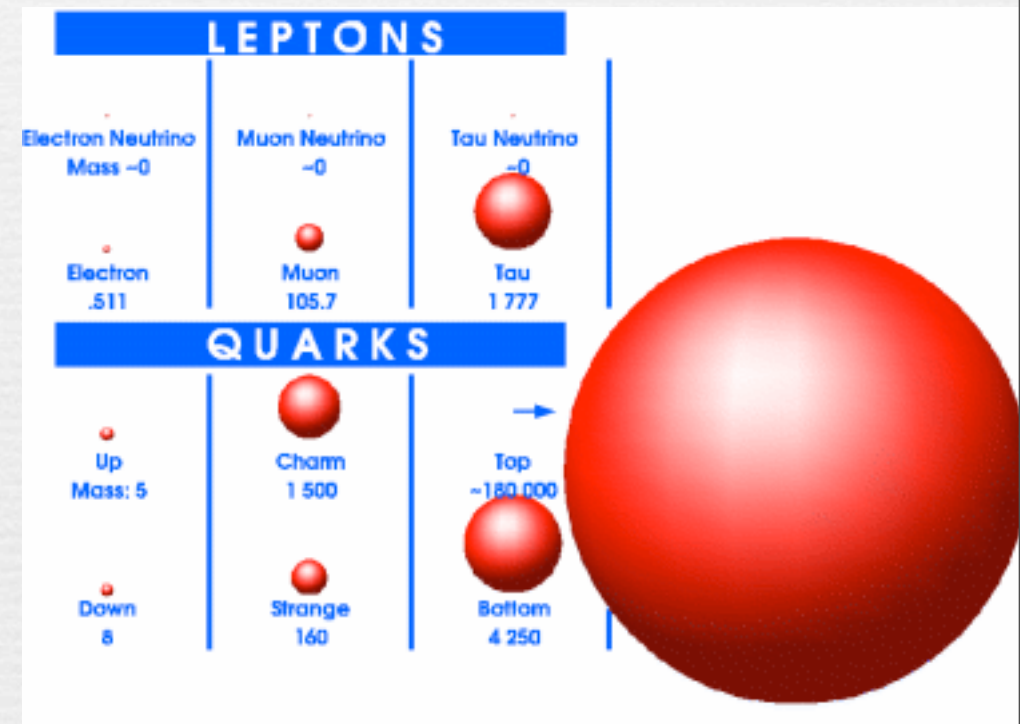
All SM masses are so generated, and have form: **coupling × v**

Same couplings that determine masses determine interactions

Analogous to Meissner-Ochsenfeld effect in BCS superconductors

Top value

- ▶ We learned much from Charm
 - ▶ Consistent SM, cemented belief in QCD
- ▶ and from Bottom
 - ▶ 3rd family, allows for CKM
- ▶ What will we learn from Top?
 - ▶ It's expensive...
 - ▶ Fermionic stepping stone at EW scale
 - ▶ Well calculable, measurable
 - ▶ Interacts strongly with all forces (gauge + Higgs) in SM



Top coupling

Exp. tested?

- ▶ to W boson: flavor mixing, lefthanded

- ▶ $g_W \sim 0.45$

$$\frac{g}{\sqrt{2}} V_{tq} (\bar{t}_L \gamma^\mu q_L) W_\mu^+ \quad \checkmark?$$

- ▶ to Z boson: parity violating

- ▶ $g_Z \sim 0.14$

$$\frac{g}{4 \cos \theta_w} \bar{t} \left(\left(1 - \frac{8}{3} \sin^2 \theta_w\right) \gamma^\mu - \gamma^\mu \gamma^5 \right) t Z_\mu \quad ?$$

- ▶ to photon: vectorlike, bare 2/3 charge

- ▶ $e_t \sim 2/3$

$$e_t \bar{t} \gamma^\mu t A_\mu \quad \checkmark?$$

- ▶ to gluon: vectorlike, non-trivial in color

- ▶ $g_s \sim 1.12$

$$g_s \left[T_a^{SU(3)} \right]^{ji} \bar{t}_j \gamma_\mu t_i A_\mu^a \quad \checkmark$$

- ▶ to Higgs: Yukawa type

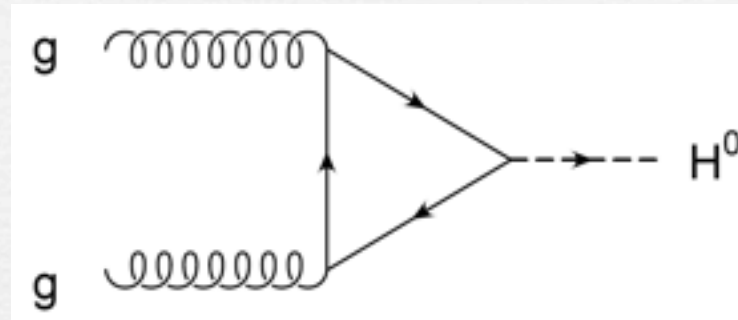
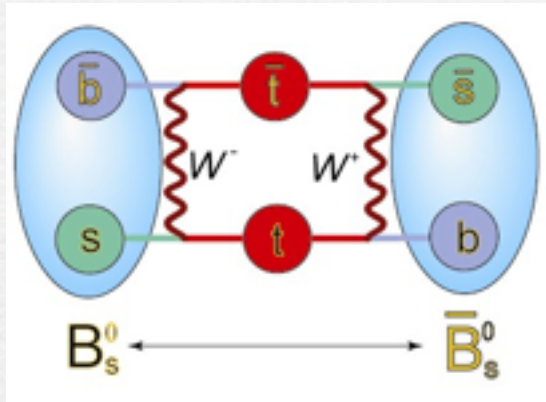
- ▶ $y_t \sim 1$

$$y_t h \bar{t} t \quad \checkmark?$$

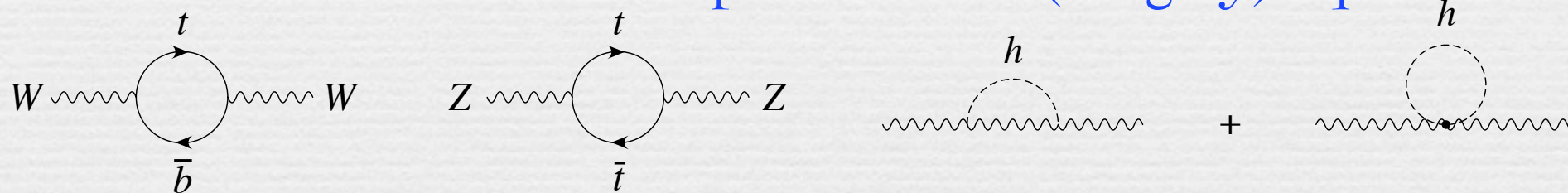
Check structure and strength of all these couplings

Top in loops

- ▶ Even if top is virtual, it makes itself loudly known



- ▶ in a loop integral a fixed mass scale always occurs in the result
- ▶ even more if there is no particle with (roughly) equal mass to compensate

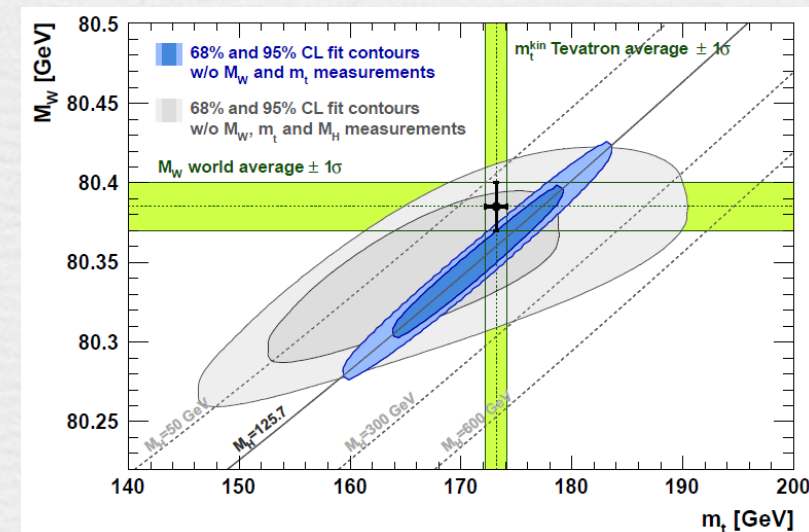


- ▶ Express the W mass in terms of 3 fundamental weak parameter, with loop corrections

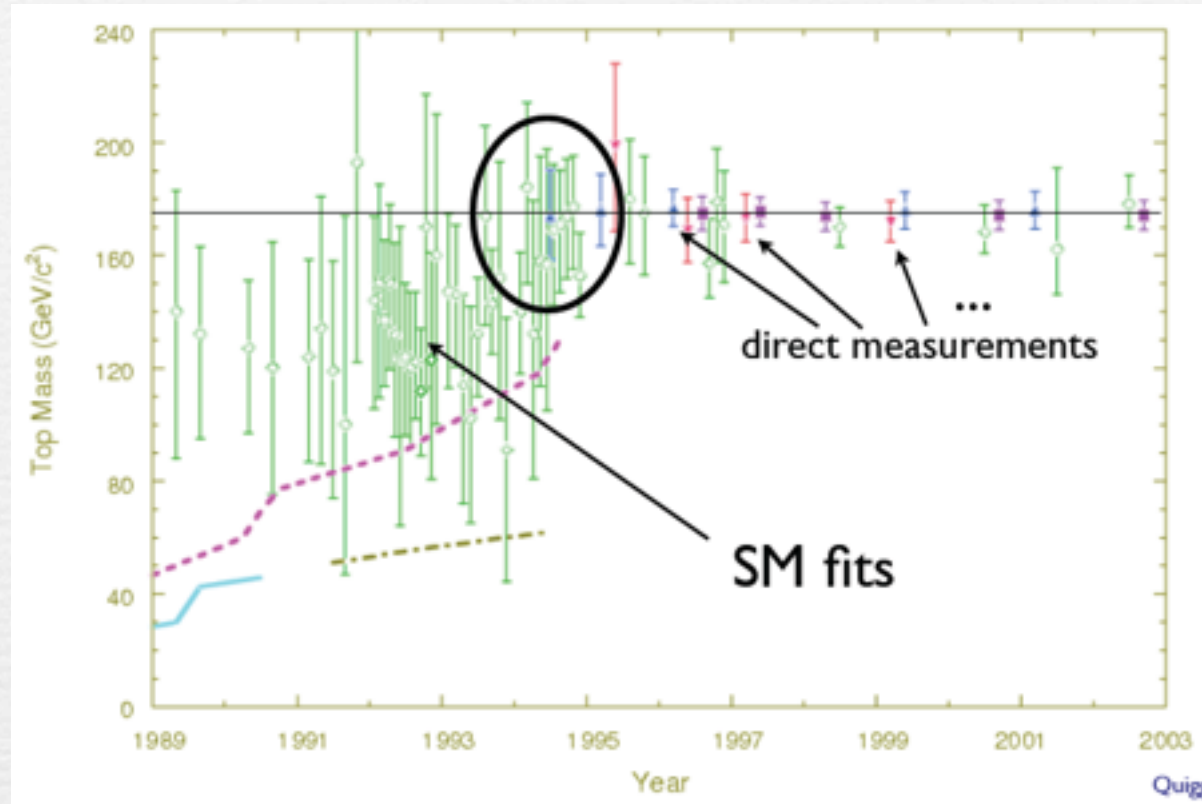
$$M_W^2 = \frac{\pi\alpha}{\sqrt{2}G_F \sin^2 \theta_w} \frac{1}{1 - \Delta r(m_t, m_H)}$$

$$\Delta r_{top} = -\frac{3}{8\pi^2} \frac{G_F}{\sqrt{2} \tan^2 \theta_w} m_t^2$$

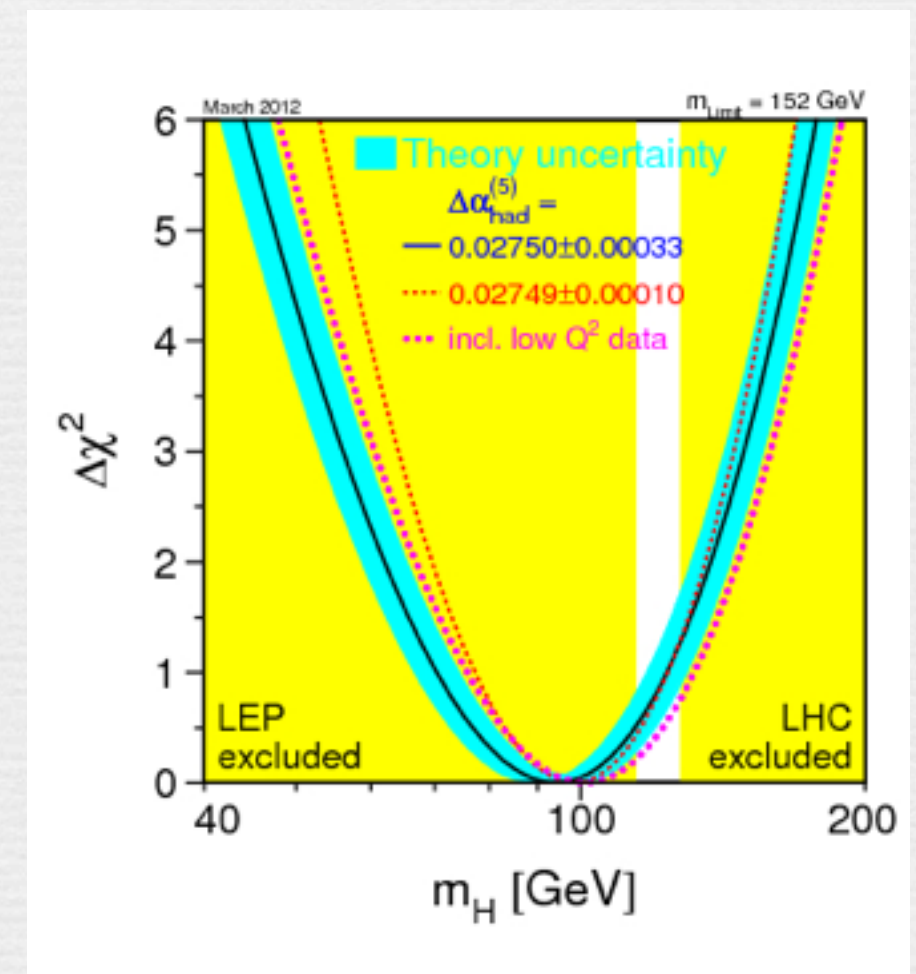
$$\Delta r_{Higgs} = \frac{3}{8\pi^2} \frac{G_F}{\sqrt{2} \tan^2 \theta_w} m_W^2 \left(2 \ln(m_H/m_Z) - 5/6 \right)$$



Top predicted in advance, by noise behind wall



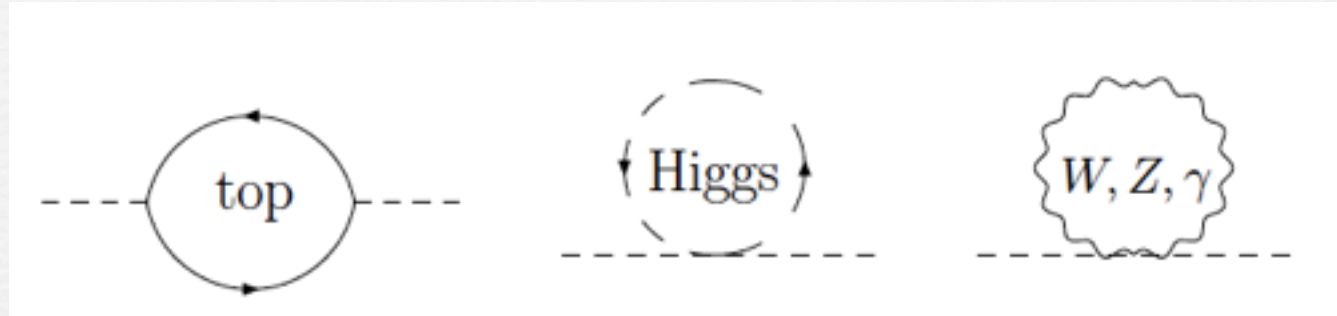
and it looks like it worked again



Top loop trouble: naturalness

- ▶ Top is a trouble maker for the Standard Model, if one values natural values of parameters.
 - ▶ 't Hooft: parameter is naturally small if, when it is zero, a new symmetry emerges
 - ▶ electron mass = 0: chiral symmetry
 - ▶ gauge coupling = 0: gauge fields are free particles, separately conserved
 - ▶ but scalar mass = 0, no extra symmetry
- ▶ Such symmetries protect the parameters
 - ▶ corrections to the electron mass are multiplicative
- ▶ But the Higgs mass is unprotected, so corrections can be very large
 - ▶ top is the worst bully here

Top and naturalness



$$\delta m_H^2 = -\frac{3}{8\pi^2} y_t^2 \Lambda^2 [\text{top}] + \frac{1}{16\pi^2} g^2 \Lambda^2 [\text{gauge}] + \frac{1}{16\pi^2} \lambda^2 \Lambda^2 [\text{Higgs}]$$

- ▶ Then for 10 TeV cutoff

$$m_H^2 = m_{\text{tree}}^2 - [100 - 10 - 5](200 \text{ GeV})^2$$

- ▶ even worse for GUT scale cut-off
- ▶ m_{tree} must precisely compensate: fine-tuning

Top and SUSY

- ▶ Top loop quadratic cut-off corrections to Higgs mass largely cancelled by “stop” loop corrections

$$\delta m_H^2 \propto (m_t^2 - m_{\tilde{t}}^2) \ln \frac{\Lambda}{m_t}$$

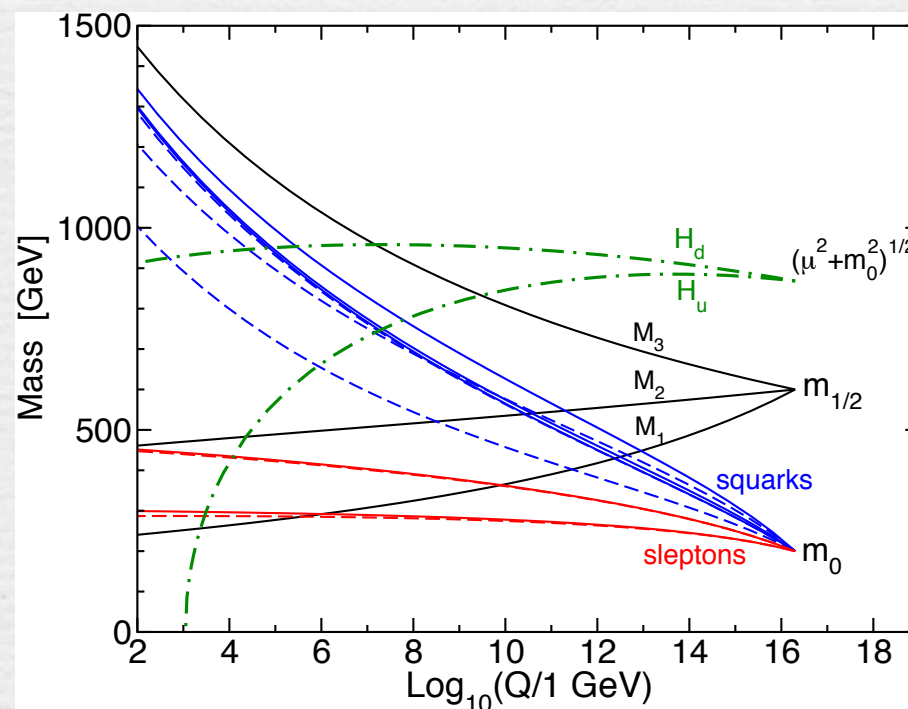
- ▶ minus due to fact that fermions in loop always get a minus sign
- ▶ makes dependence on cut-off logarithmic, which is acceptable/natural

Top: SUSY saviour

- Top keeps MSSM alive via (top, stop) m_t^4 corrections on lightest Higgs

$$\Delta(m_{h^0}^2) = \frac{3}{4\pi^2} \cos^2 \alpha \, y_t^2 m_t^2 \ln \left(m_{\tilde{t}_1} m_{\tilde{t}_2} / m_t^2 \right)$$

- otherwise the lightest Higgs could be no heavier than a Z boson
- giving about 130-140 GeV upper limit
- Top drives radiative EW symmetry breaking in SUSY



- Heavy Higgses may decay to top, can determine their CP properties

Top and Little Higgs

Little Higgs: models in which the Higgs is a pseudo-Goldstone boson, therefore light

- ▶ Symmetries forbid one-loop Higgs mass term: solves “little hierarchy” problem
- ▶ Little Higgs models cancel (top) quadratic divergences with similar particles of **same spin** (vectorlike top T e.g.)

$$2\lambda_1^2 + (-\lambda_1^2/f) + (-\lambda_1^2/f) = 0$$

Han, Logan, Wang

Various models (with various gauge groups, T -parity or not) have been proposed, could be unraveled by

- ▶ measuring couplings in the top, T sector, and m_T (cross section 0.01-100 fb)
- ▶ testing vector character of T

Higgs compositeness/strong dynamics

- ▶ Still a viable scenario, with top in leading role
 - ▶ Higgs = pseudo Nambu-Goldstone boson (like pion)
 - ▶ natural solution to naturalness problem
- ▶ E.g.: TC2: topcolor-assisted technicolor
 - ▶ Top mass dynamically generated by topcolor (like gap equation in BCS)
 - ▶ Technicolor for EW symmetry breaking
 - ▶ (Pseudo)Scalars: Top-Higgs = $t\bar{t}$ bound states (a la BCS), Top-pions
- ▶ Large class of models in trouble/excluded by LHC data
 - ▶ but not all

Chivukula, Ittisamai, Simmons, Coleppa, Logan, Martin, Ren

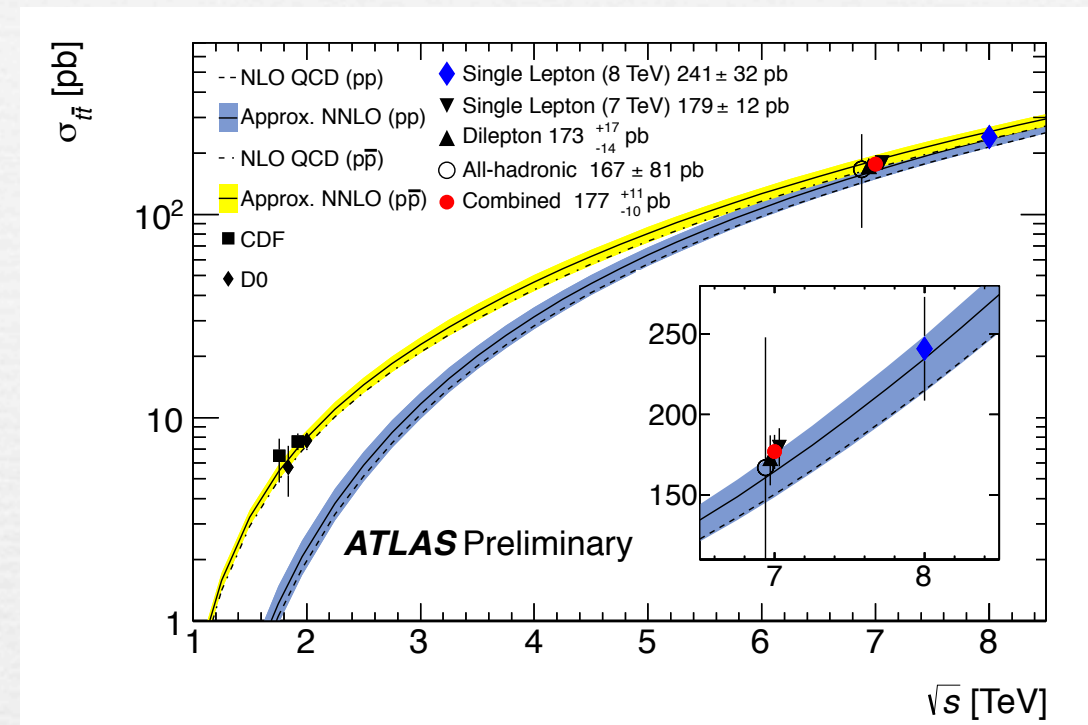
Top object

- ▶ Top should be extra-sensitive to BSM effects, real or virtual
- ▶ Large mass, short life, easy access
- ▶ Goal for this talk:
 - ▶ Visit important observables
 - ▶ σ , m_t , single top, A_{FB} , angular correlations
 - ▶ What is the state-of-the-art description? What do we learn?
 - ▶ Provide some background to these
 - ▶ Apologies in advance for omissions

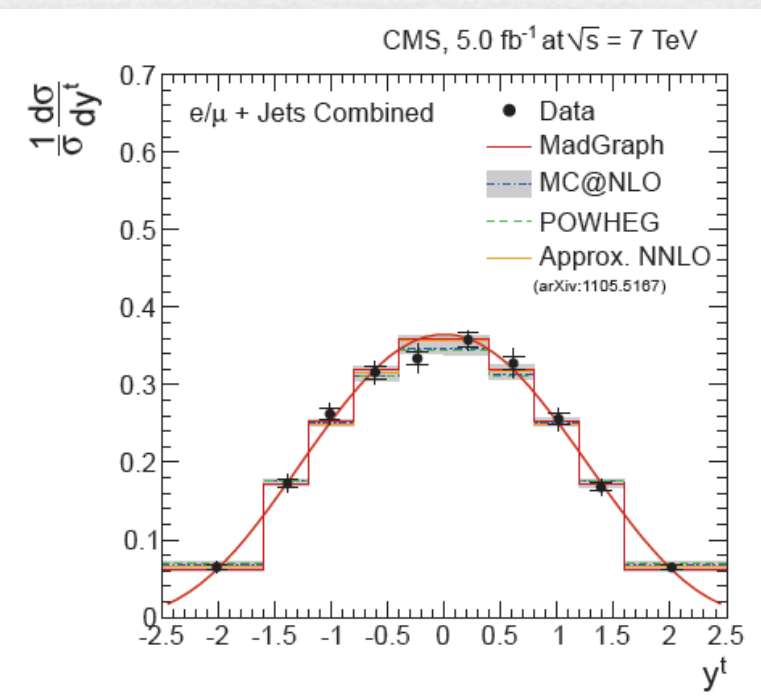
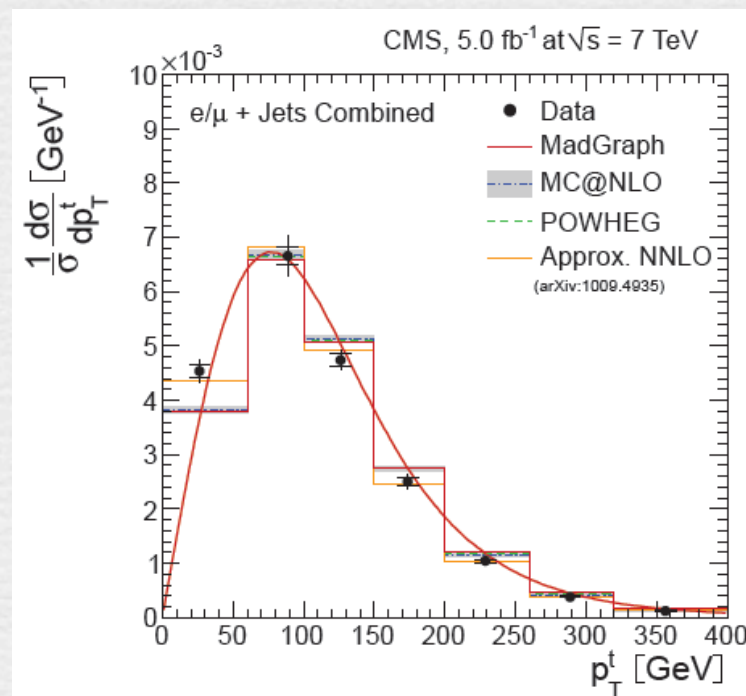
Doubles

Pair production cross section

- Measurements at 7, 8 TeV agree well with theory
 - ☺ New collider, much higher energy:
 - we really do understand how tops are produced
- Good confidence in Top QCD coupling
- Useable for PDF (gluon) determination

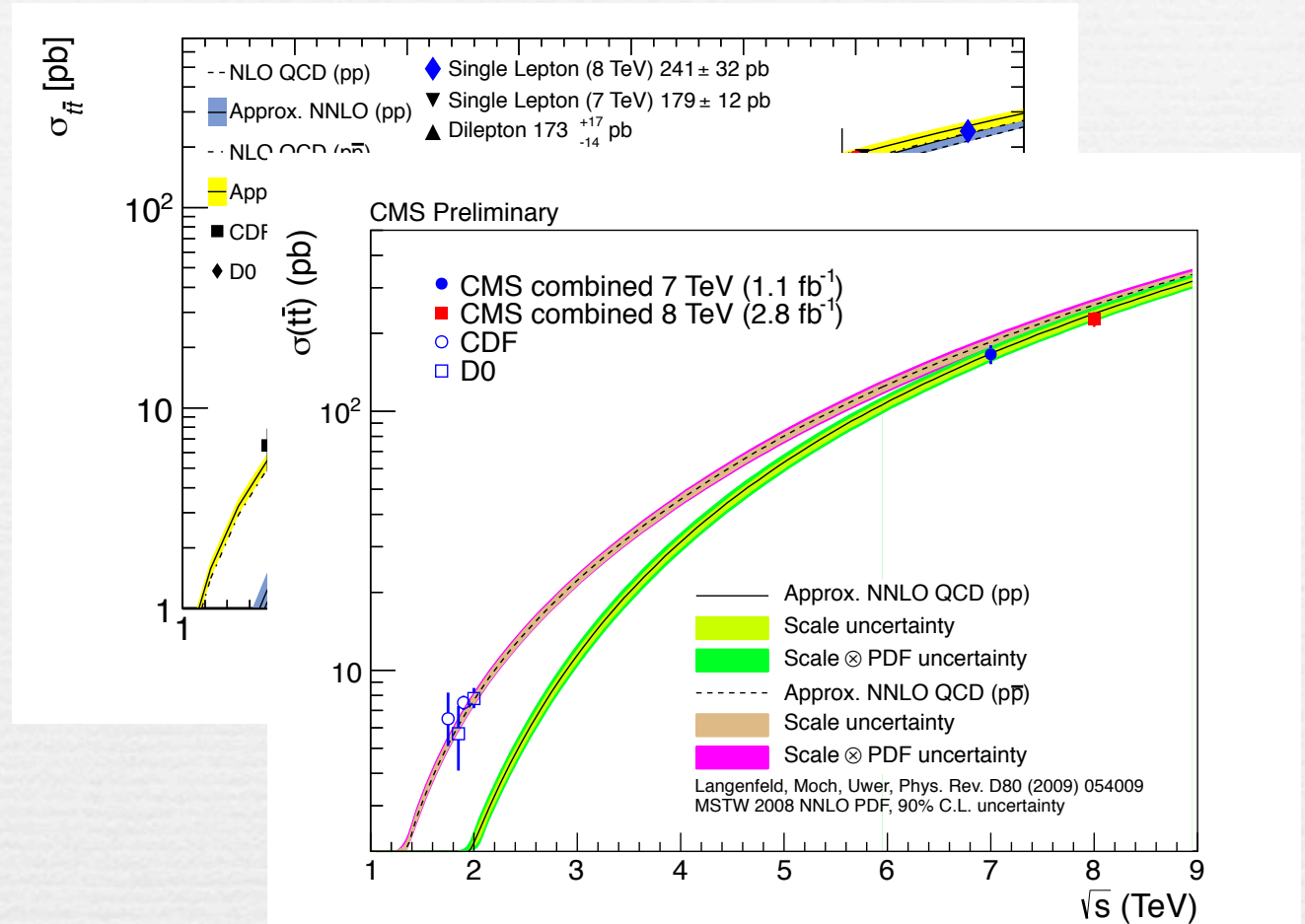


Differential distributions ok
(ATLAS, CMS, CDF, D0)

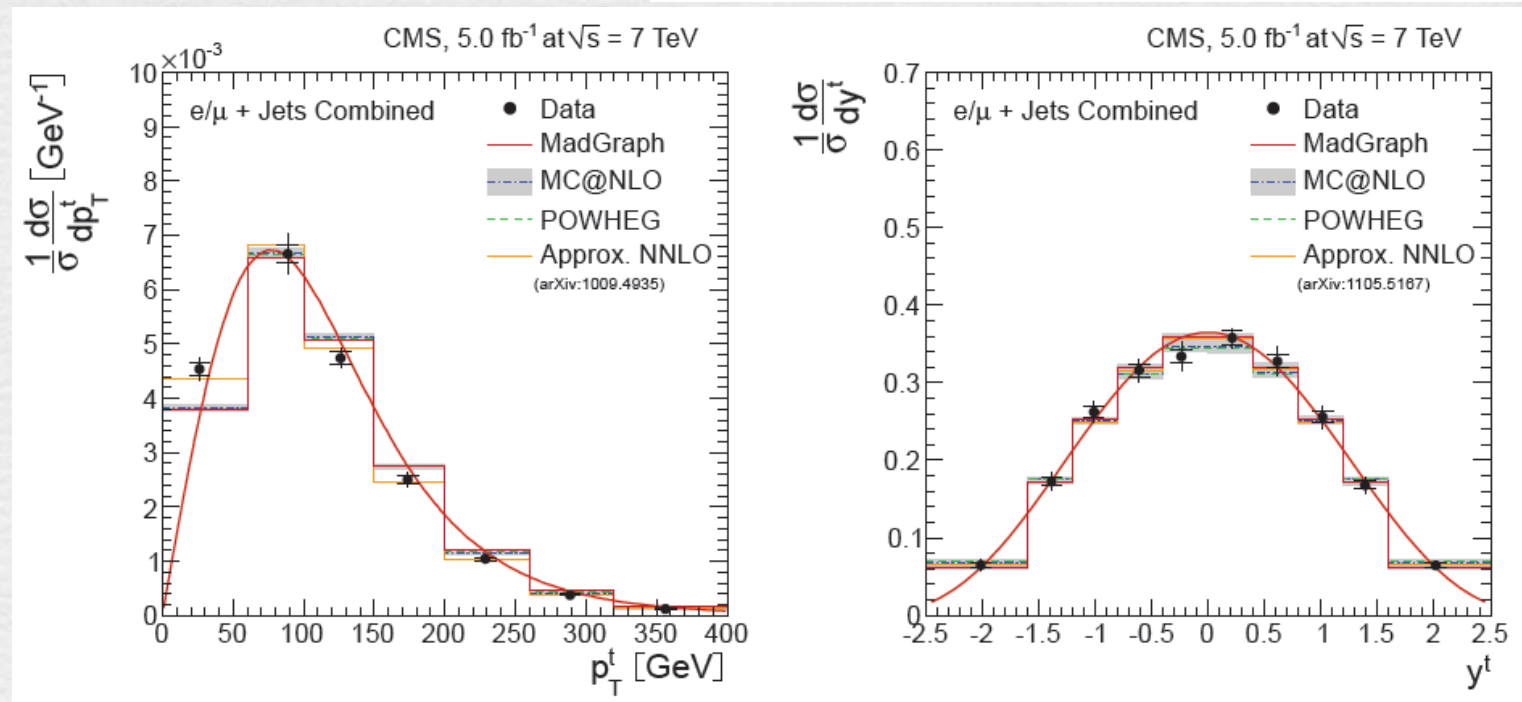


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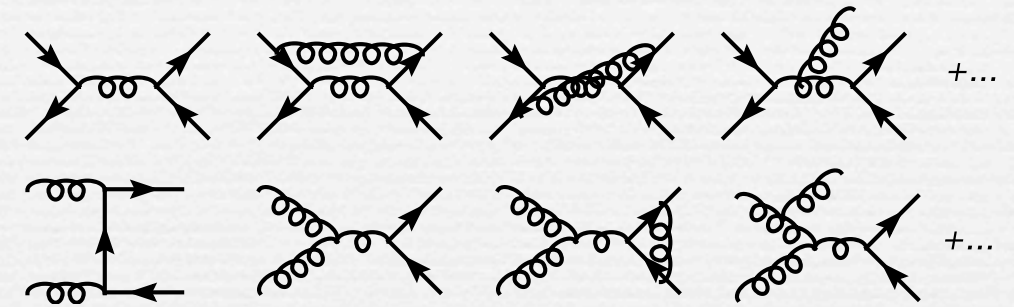


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Pair production cross section: theory I

- ▶ NLO since late 80's
 - ▶ single particle inclusive and fully differential.
Codes (MNR) still available
- ▶ Currently, NLO plus PS: MC@NLO, POWHEG
- ▶ Resummation-based, two varieties
 - ▶ all order predictions, to various accuracies
 - ▶ **Benefit: all-order, systematic, smaller scale uncertainty**
 - ▶ (Top has propelled much resummation research over the years)
 - ▶ after expanding resummed to second order, get $\text{NNLO}_{\text{approx}}$
 - ▶ **Instructive, already less scale uncertainty**



Beenakker, Kuijf, Smith, van Neerven, Meng, Schuler;
Nason, Dawson, Ellis; Mangano, Nason, Ridolfi

Frixione, Webber; Nason, Oleari

$$\sigma^{resum} = \left\{ \underbrace{\alpha_s^2 C_0}_{\text{LL,NLL}} + \underbrace{\alpha_s^3 C_1}_{\text{NNLL}} \right\} \times \exp \left[\underbrace{L g_1(\alpha_s L)}_{\text{LL}} + \underbrace{g_2(\alpha_s L)}_{\text{NLL}} + \underbrace{\alpha_s g_3(\alpha_s L)}_{\text{NNLL}} + \dots \right]$$

Pair production cross section: theory II

$$\sigma^{resum} = \left\{ \underbrace{\alpha_s^2 C_0}_{LL, NLL} + \underbrace{\alpha_s^3 C_1}_{NNLL} \right\} \times \exp \left[\underbrace{L g_1(\alpha_s L)}_{LL} + \underbrace{g_2(\alpha_s L)}_{NLL} + \underbrace{\alpha_s g_3(\alpha_s L)}_{NNLL} + \dots \right]$$

- ▶ Until recently the status was NLL

Kidonakis, Oderda, Sterman; Cacciari, Frixione, Bonciani, Mangano, Nason, Ridolfi

- ▶ All ingredients now upgraded

- ▶ Jet function & soft function (g_3), hard part (C_1)

Moch, Vermaseren, Vogt; Mitov, Sterman, Sung
Ahrens, Ferroglia, Neubert, Pecjak, Yang

- ▶ Also available: Coulomb exchange

Beneke, Falgari, Schwinn; +Czakon, Mitov

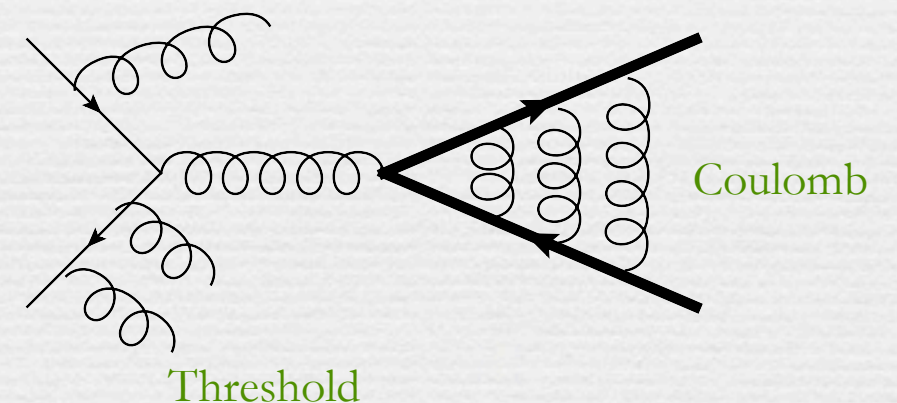
- ▶ Caveat: different thresholds are used

- ▶ e.g.

$$\sigma(s) = \int dp_T dy \frac{d^2 \sigma}{dp_T dy}$$

- ▶ Source of uncertainty, as long as NNLO not known exactly

Kidonakis, EL, Moch, Vogt; Ahrens, Ferroglia, Neubert, Pecjak, Yang



1. $\sum_n \alpha_s^n \ln^{2n}(s - 4m^2) \quad [\sigma(s)]$
2. $\sum_n \alpha_s^n \ln^{2n}(s - 4(m^2 + p_T^2)) \quad [d\sigma(s)/dp_T]$
3. $\sum_n \alpha_s^n \ln^{2n}(s - 4(m^2 + p_T^2) \cosh y) \quad [d^2\sigma(s)/dp_T dy]$

$\sigma_{tt}(\text{NNLO})$: approximations

▸ NNLO approximate

▸ Kidonakis (2008): **3** (PIM, 1PI)

$163 \pm 11 \text{ pb}$

▸ Hathor: **1**

Aliev, Lackner, Langenfeld, Moch, Uwer, Wiedermann

$164 \pm 12 \text{ pb}$

▸ Ahrens et al: **3** (PIM, 1PI). Have code.

Ahrens, Ferroglia, Neubert, Pecjak, Yang

$155 \pm 8 \text{ pb} \pm 14 \text{ pb}$

▸ Even though approximate, heavy theoretical machinery necessary. Errors now (at 7 TeV): 8 - 10%

▸ Calculations with threshold 3 useful for A_{FB}

▸ NNLO exact, very tough, but approaching:

▸ 2 real emission; done

▸ 1-loop, 1 real emission; done

▸ 2 loop; analytical+numerical largely done

Czakon; Abelof, Gehrmann-de-Ridder;
Bernreuther, Bogner, Dekkers, Mitov, Fiedler

Dittmaier, Uwer, Weinzierl
Melnikov, Schulze

Moch, Mitov, Czakon; Bernreuther,
Bonciani, Gehrmann, Mastrolia,
Heinrich, Leineweber, Remiddi;
Bonciani, Ferroglia, Gehrmann,
Manteuffel, Studerus

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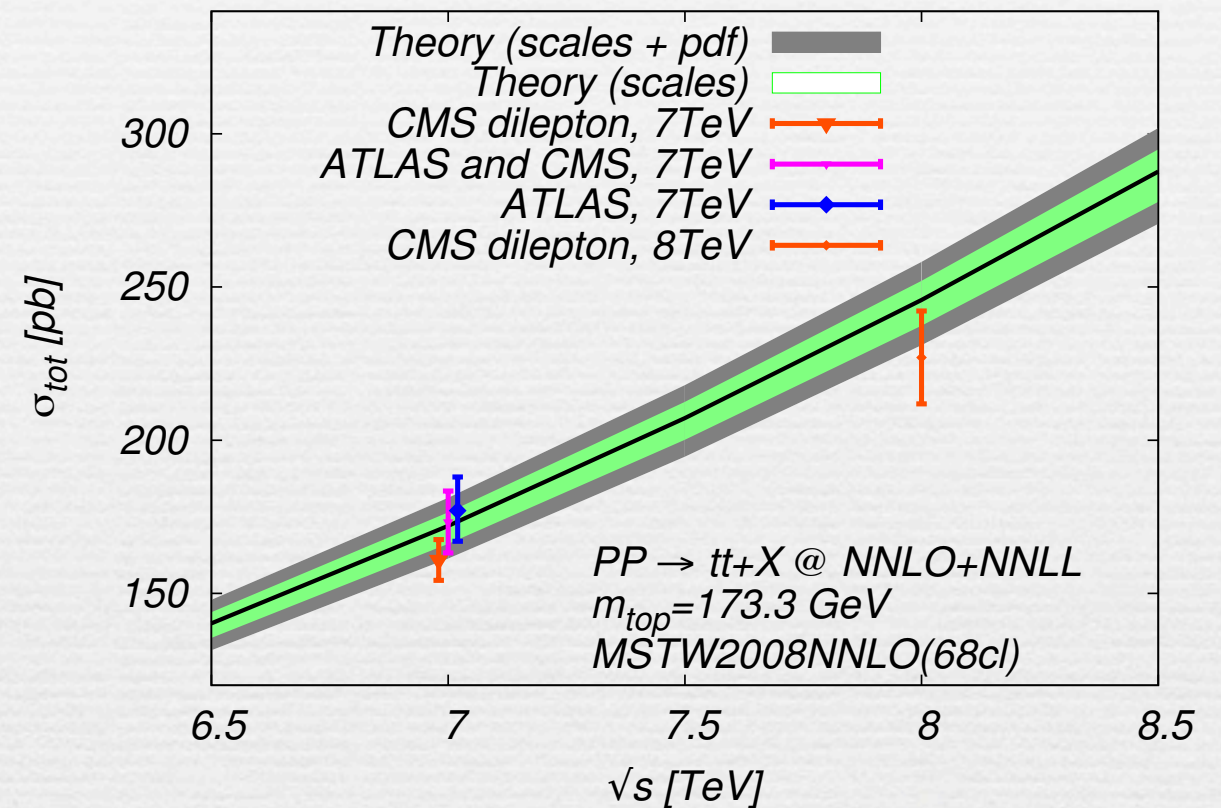
Excitement: NNLO top cross section finally here

LHC

Baernreuther, Fiedler, Mitov, Czakon, '12, '13

Collider	σ_{tot} [pb]	scales [pb]	pdf [pb]
Tevatron	7.009	+0.259(3.7%) -0.374(5.3%)	+0.169(2.4%) -0.121(1.7%)
LHC 7 TeV	167.0	+6.7(4.0%) -10.7(6.4%)	+4.6(2.8%) -4.7(2.8%)
LHC 8 TeV	239.1	+9.2(3.9%) -14.8(6.2%)	+6.1(2.5%) -6.2(2.6%)
LHC 14 TeV	933.0	+31.8(3.4%) -51.0(5.5%)	+16.1(1.7%) -17.6(1.9%)

Pure NNLO



- First full NNLO calculation with initial hadrons and full color structure
- Heroic effort plus innovative subtraction methods
- Uncertainty now only a few % at NNLO + NNLL
 - reduction of factor 3 in scale wrt. NLO+NLL
- Approximations: quality not terrible, but notable differences

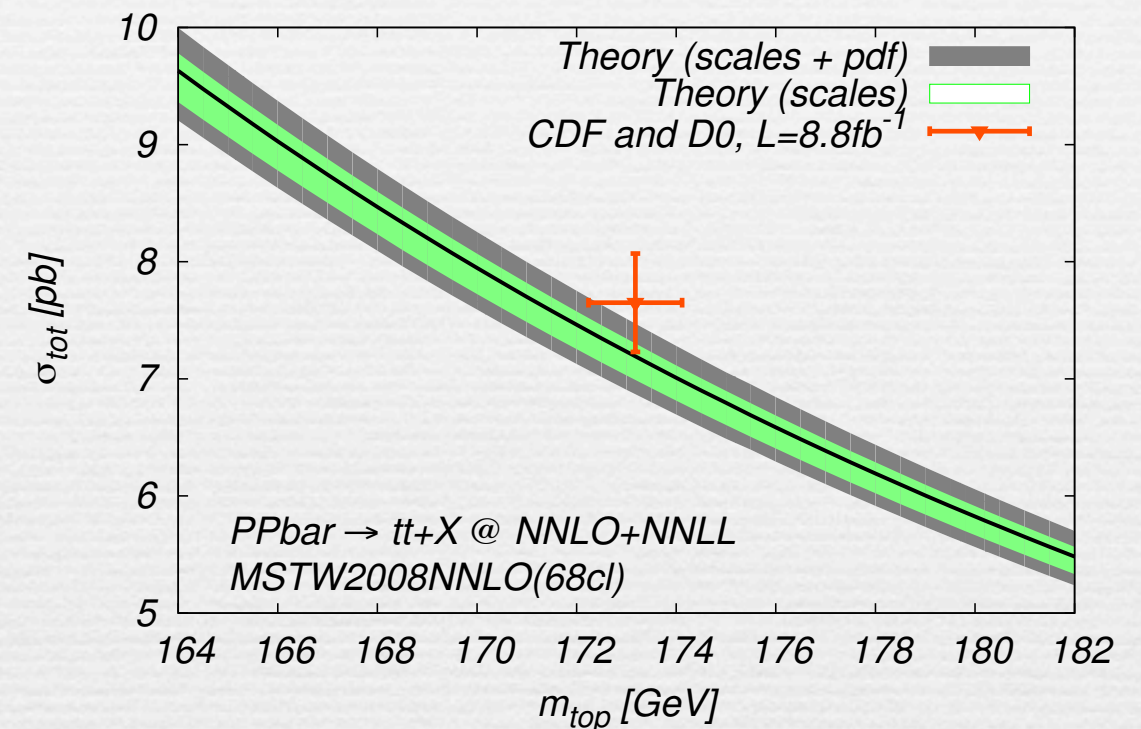
NNLO top cross section

Tevatron

Baernreuther, Fiedler, Mitov, Czakon, '12, '13

Collider	σ_{tot} [pb]	scales [pb]	pdf [pb]
Tevatron	7.164	+0.110(1.5%) -0.200(2.8%)	+0.169(2.4%) -0.122(1.7%)
LHC 7 TeV	172.0	+4.4(2.6%) -5.8(3.4%)	+4.7(2.7%) -4.8(2.8%)
LHC 8 TeV	245.8	+6.2(2.5%) -8.4(3.4%)	+6.2(2.5%) -6.4(2.6%)
LHC 14 TeV	953.6	+22.7(2.4%) -33.9(3.6%)	+16.2(1.7%) -17.8(1.9%)

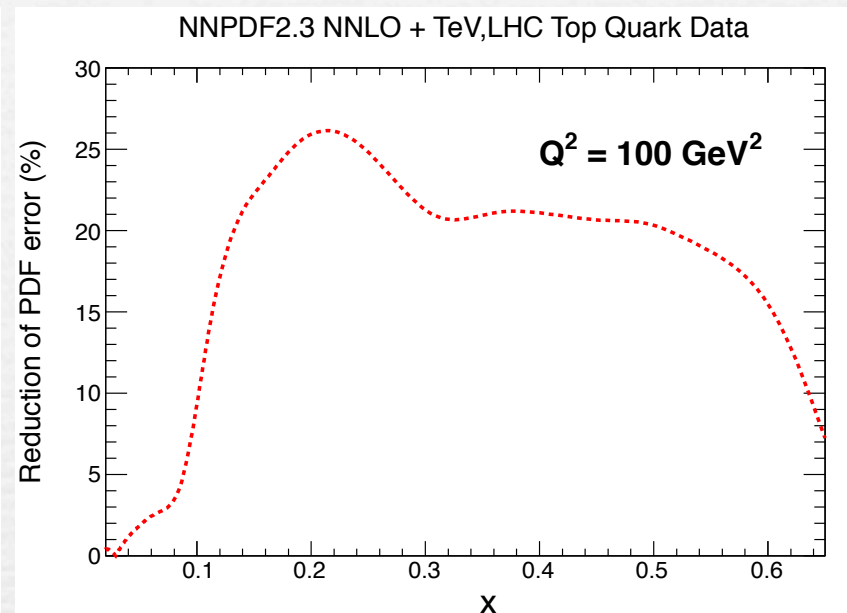
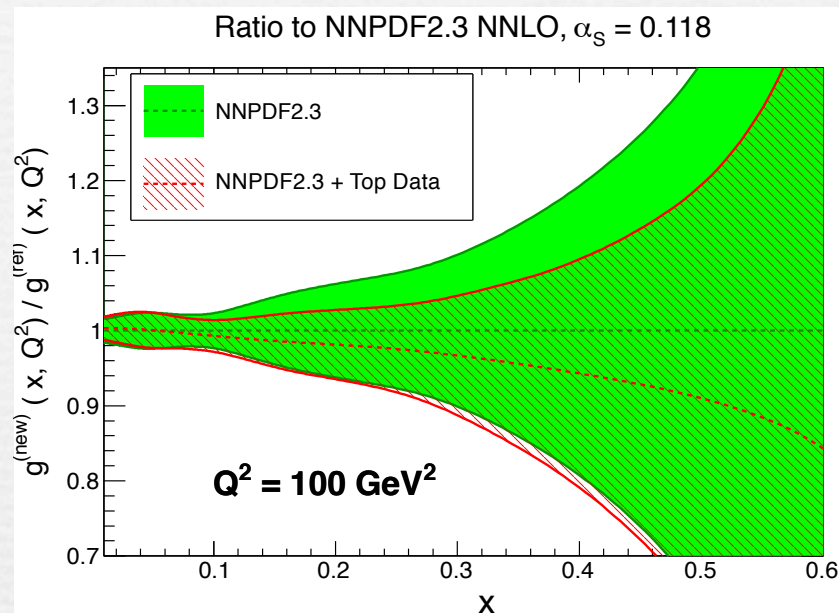
NNLO+NNLL



- ▶ Excellent agreement between experiment and NNLO theory
 - ▶ Update weakest link: PDF's, especially large-x gluon density

Mangano, Czakon, Mitov, Rojo, '13

Impact on PDF's (esp. large-x gluon)



Mangano, Czakon, Mitov, Rojo, '13

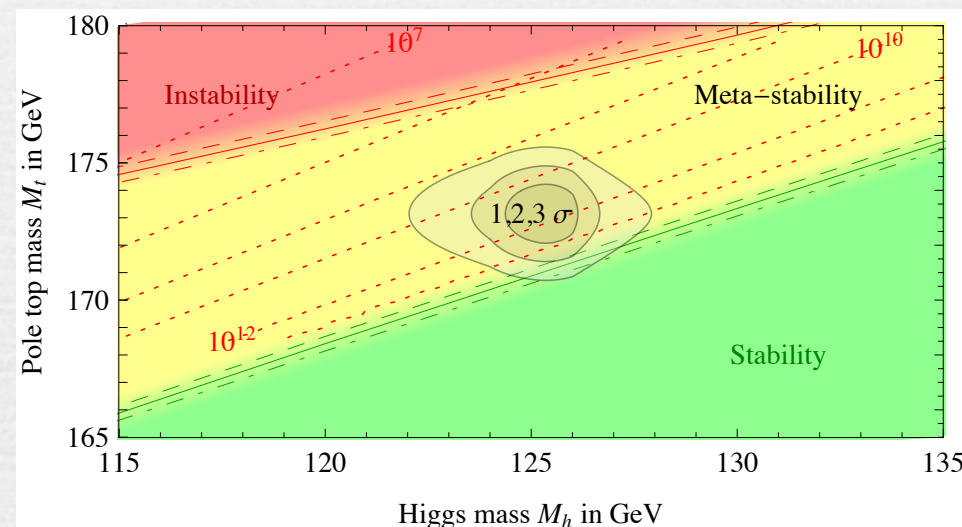
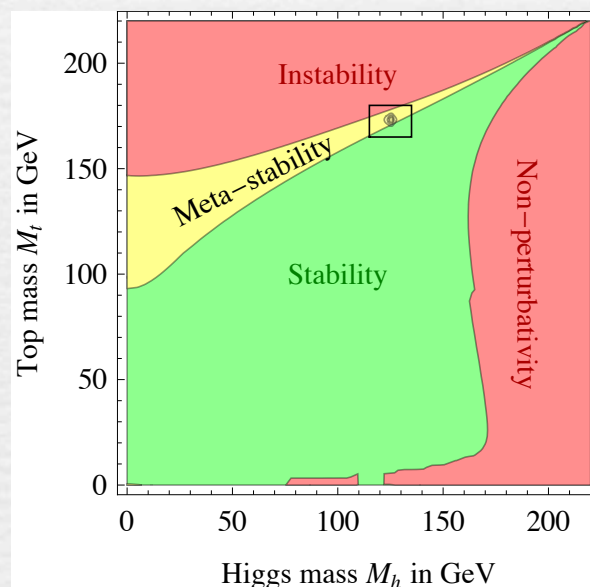
- ▶ Excellent probe, no NP contamination
- ▶ Less uncertainty in various BSM predictions that rely on large-x gluons

Mass

Top mass

- ▶ Important to measure well, because
 - ▶ m_t is a fundamental parameter of the Standard Model
 - ▶ it is important for stringent electroweak precision tests
 - ▶ is the Higgs mass in the funnel? Fate of universe depends on it!

Degrassi, di Vita, Elias-Miro,
Espinosa, Giudice, Isidori,
Strumia

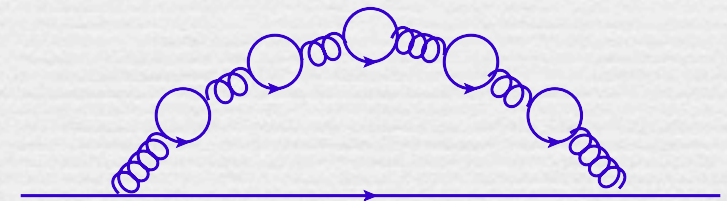


- ▶ Remember we are talking about a bare quark, so we must think about what a mass really means
 - ▶ we cannot use a quick rule like the following for c and b


$$m_c = \frac{1}{2} m_{J/\psi} \quad m_b = \frac{1}{2} m_{\Upsilon}$$

Top mass

- ▶ Electron mass definition is “easy”: defined by pole in full propagator
 - ▶ If particle momentum satisfies pole condition ($p^2=m^2$), can propagate to ∞
 - ▶ \Rightarrow there is no real ambiguity what electron “pole” mass is
- ▶ But: quarks are confined, so physical on-shell quarks cannot exist
 - ▶ Leads to non-perturbative ambiguity of few hundred MeV
 - ▶ (revealed by all-order pQCD!)
- ▶ Relevant questions
 - ▶ How can we define the top quark mass best?
 - ▶ What accuracy do we need?



Heavy quark mass, definition(s)



The diagram shows a horizontal line with an arrow pointing right, representing a quark. This is followed by a plus sign, then a loop diagram (a semi-circle of gluons) attached to the line, followed by another plus sign and an ellipsis. To the right of this is an equals sign followed by the expression $\frac{1}{\not{p} - m_0 - \Sigma(p, m_0)}$. An arrow points from the $\Sigma(p, m_0)$ term to the expression $m_0 \frac{\alpha_s}{\pi} \left[\frac{1}{\epsilon} + \text{finite stuff} \right]$.

$$= \frac{1}{\not{p} - m_0 - \Sigma(p, m_0)}$$

$$m_0 \frac{\alpha_s}{\pi} \left[\frac{1}{\epsilon} + \text{finite stuff} \right]$$

To make finite, substitute $m_0 = m_R \left(1 + \frac{\alpha_s}{\pi} \left[\frac{1}{\epsilon} + z_{finite} \right] \right)$

Mass definitions differ in the choice of z_{finite}

Pole mass: pretend quarks are free and long-lived $\frac{1}{\not{p} - m_0 - \Sigma(p, m_0)} = \frac{c}{\not{p} - m}$

MSbar mass: treat mass as a coupling $m_0 = m(\mu) \left(1 + \frac{\alpha_s}{\pi} \left[\frac{1}{\epsilon} \right] \right)$

One can translate between them,
relation is known to 3 loops

$$m = m(\mu) \left(1 + \alpha_s(\mu) d^1 + \alpha_s^2(\mu) d^2 + \dots \right)$$

What top mass is measured?

- ▶ What mass do hadron colliders determine?
 - ▶ Pole mass? “Pythia” mass?
 - ▶ Typically the path from data to a value for m involves Pythia (or other MC) templates, generated with the Pythia mass parameter
 - ▶ Many discussions, no universally accepted conclusion.
 - ▶ Map from data to theory parameter via Pythia, templates, cuts, not so clear. Interpreted as pole mass.
 - ▶ It matters numerically, as the two differ by about 10-15 GeV

Measuring the $\overline{\text{MS}}$ mass

- ▶ How to determine the $\overline{\text{MS}}$ mass?
 - ▶ Problem: on-shell condition of final state top must be pole mass

$$\text{Im}\left[\frac{1}{p^2 - m^2 + i\varepsilon}\right] = \delta(p^2 - m^2)$$

- ▶ Here's a recipe
 - ▶ compute cross section using pole mass
 - ▶ replace pole mass by $\overline{\text{MS}}$ mass, using
 - ▶ Fit to data, extract $\overline{\text{MS}}$ mass

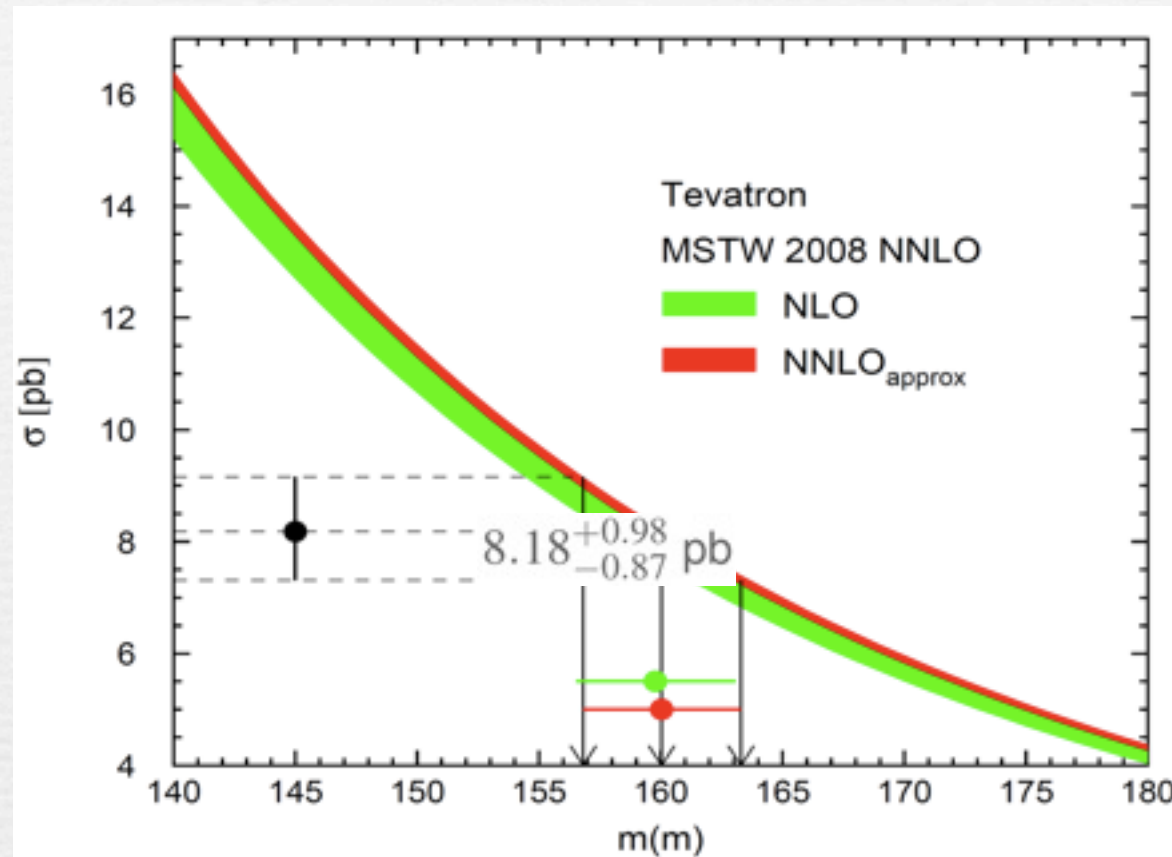
$$\sigma_{tt}(m, \alpha_s)$$

$$m = \overline{m}(\mu)(1 + \alpha_s(\mu)d^1 + \alpha_s(\mu)^2 d^2 + \dots)$$

Langenfeld, Moch, Uwer

MSbar mass extraction

Langenfeld, Moch, Uwer



	\bar{m} [GeV]	m_t [GeV]
LO	$159.2^{+3.5}_{-3.4}$	$159.2^{+3.5}_{-3.4}$
NLO	$159.8^{+3.3}_{-3.3}$	$165.8^{+3.5}_{-3.5}$
NNLO	$160.0^{+3.3}_{-3.2}$	$168.2^{+3.6}_{-3.5}$

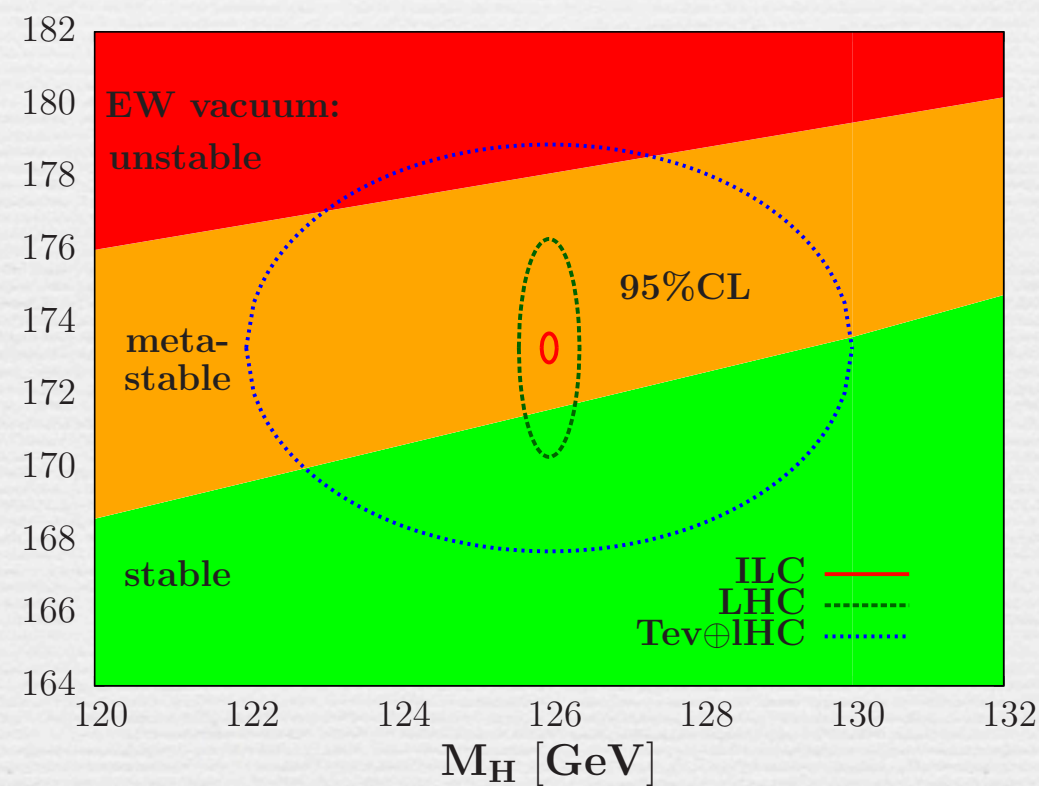
- Accuracy at this point limited by m_t sensitivity and PDF uncertainties
- Other proposals:
 - (moments of) the invariant mass distribution
 - $tt+1$ jet, more sensitive than tt cross section
 - other short-distance mass definitions

Alioli, Fernandez, Fuster, Irles, Moch, Uwer, Vos

Frederix, Maltoni

Top mass

- ▶ Pole mass from $\overline{\text{MS}}$ mass: $173.3 \pm 2.8 \text{ GeV}$
 - ▶ $m_H > 129.4 \pm 5.6 \text{ GeV}$
 - ▶ Universe's fate still uncertain



Alekhin, Djouadi, Moch

Singles

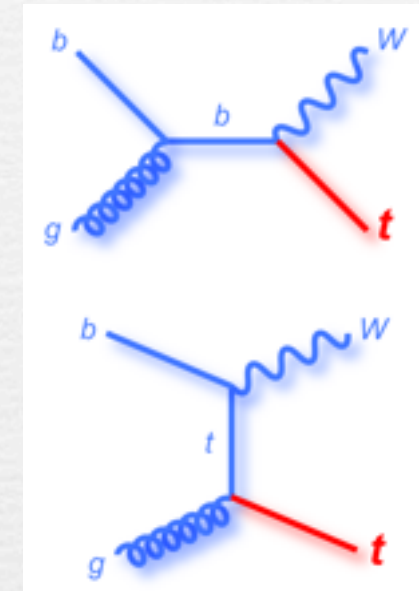
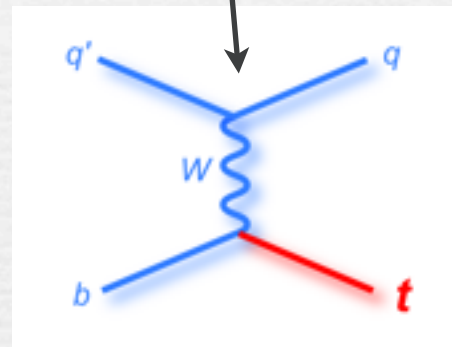
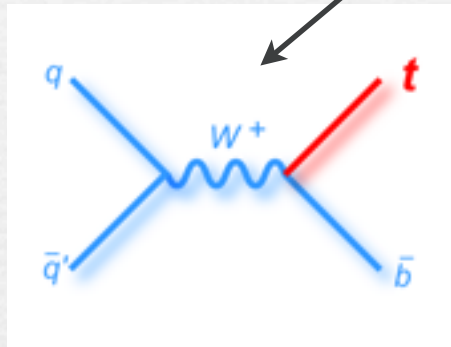
Basic facts about single top production

LO at α_w^2 for s and t channel, $\alpha_w\alpha_s$ for Wt channel

Cross section:

3 pb at Tevatron

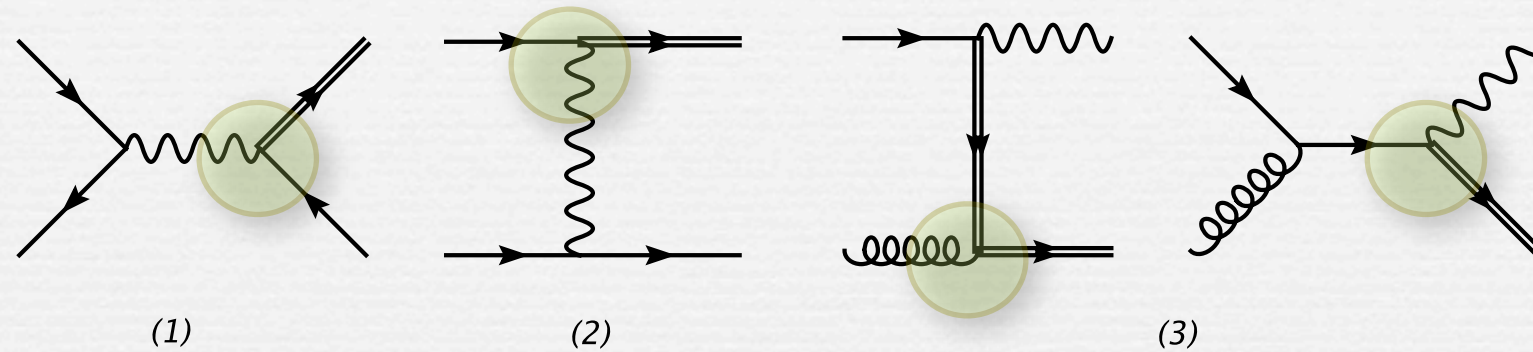
300 pb at LHC14 (60 pb) at LHC7



- ▶ s channel 1 pb at Tevatron, Wt negligible there
- ▶ s-channel like Drell-Yan, t-channel like Deep-Inelastic Scattering
- ▶ QCD corrections moderate
- ▶ Test different kinds of new physics

- ▶ 60pb at LHC14, s-channel negligible there
- ▶ NLO QCD corrections about 40%
- ▶ Tricky at LHC, hard to distinguish from top pair production. More on this later.

Single top production



s-channel:
timelike W

4 pb @ LHC7

t-channel:
spacelike W

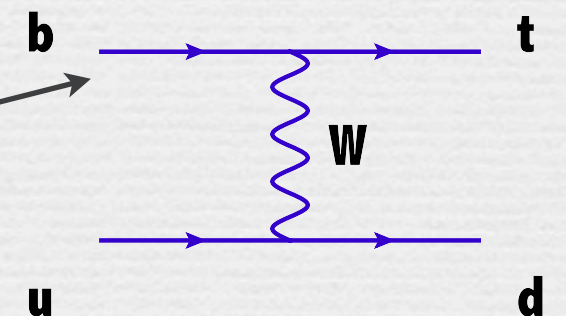
62 pb @ LHC7

Wt channel: real W

10 pb @ LHC7

Things you can do with single top production

- ▶ process is sensitive to different New Physics/channel (FCNC (t-channel), W' resonance (s-channel), non-4 fermion operators (Wt-channel))
- ▶ It helped determine (t-channel) the high-scale b-quark PDF
- ▶ It tests electroweak production of top, through left-handed coupling
- ▶ It allows measurement of V_{tb} per channel.



s & t fallacy

- One might think: since these cross sections are proportional to $|V_{tb}|^2$, we can just extract this value easily.

- But since

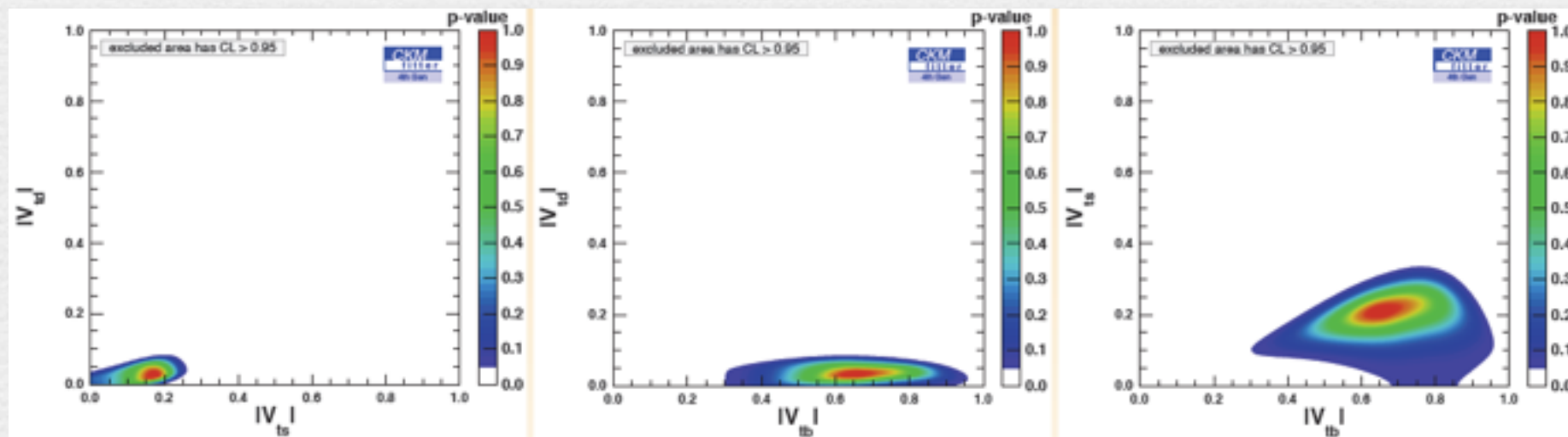
Alwall et al; Lackner et al

$$R = \frac{|V_{tb}|^2}{|V_{td}|^2 + |V_{ts}|^2 + |V_{tb}|^2}$$

- has recently been measured by D0 to be about 0.9, we cannot use

$$|V_{td}|^2 + |V_{ts}|^2 \ll |V_{tb}|^2$$

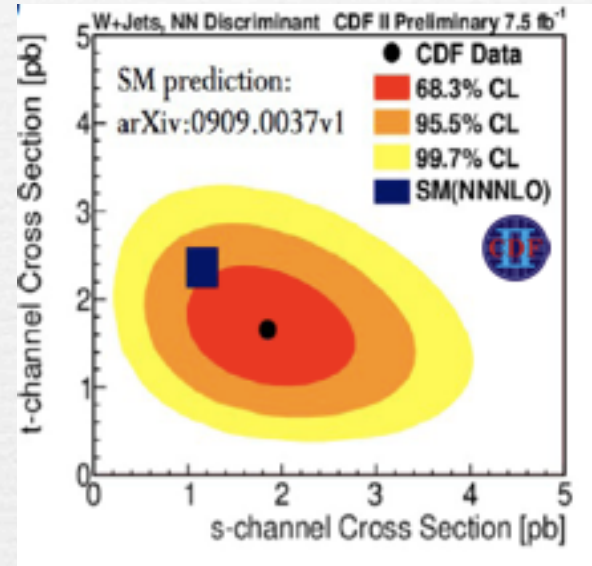
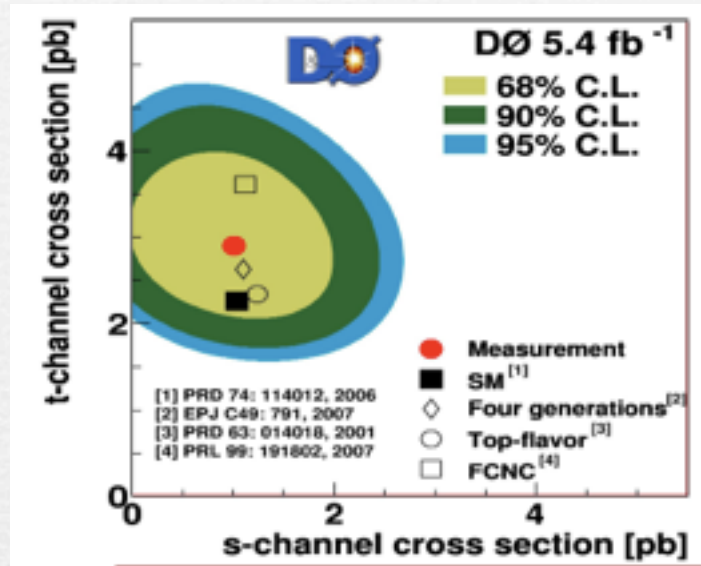
- so easily. A first attempt at doing it properly:



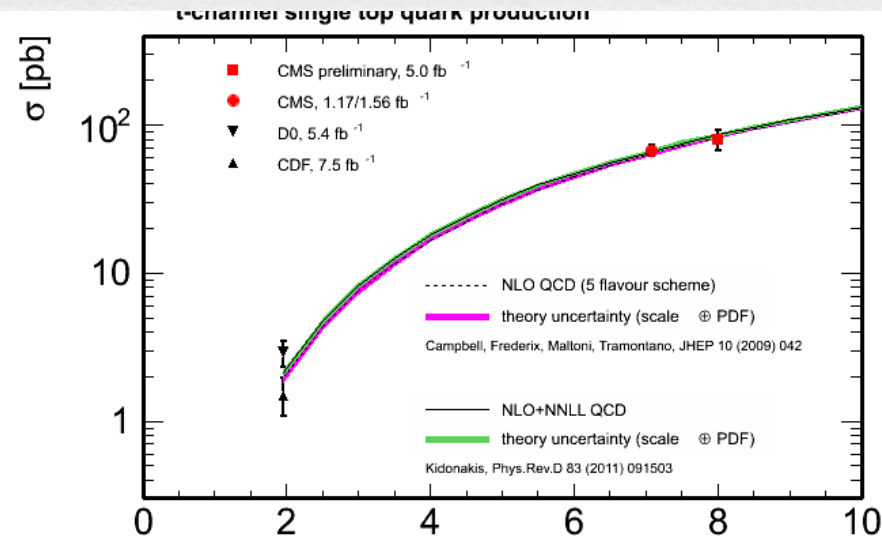
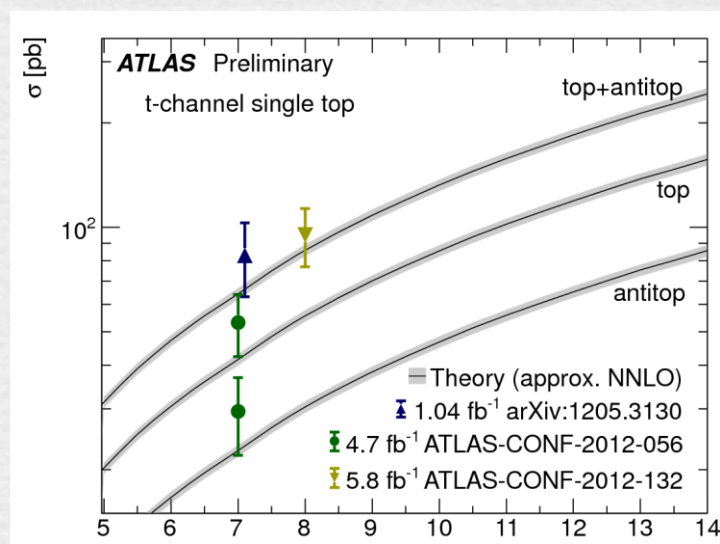
- $V_{tb} = 1$ not quite favored...

Recent results for s & t channel

- ▶ Clever: measure both channels at the same time, and confront with some NP models



- ▶ Also ATLAS and CMS have nice measurements, in general agreement with Standard Model (s-channel hard at LHC). T-channel:



Theory status: NLO to parton showers

- ▶ Issue: double counting

- ▶ emission from NLO and PS, should be counted once
- ▶ virtual part of NLO and Sudakov form factor should not overlap
- ▶ some freedom in this:

Frixione, Webber; Nason

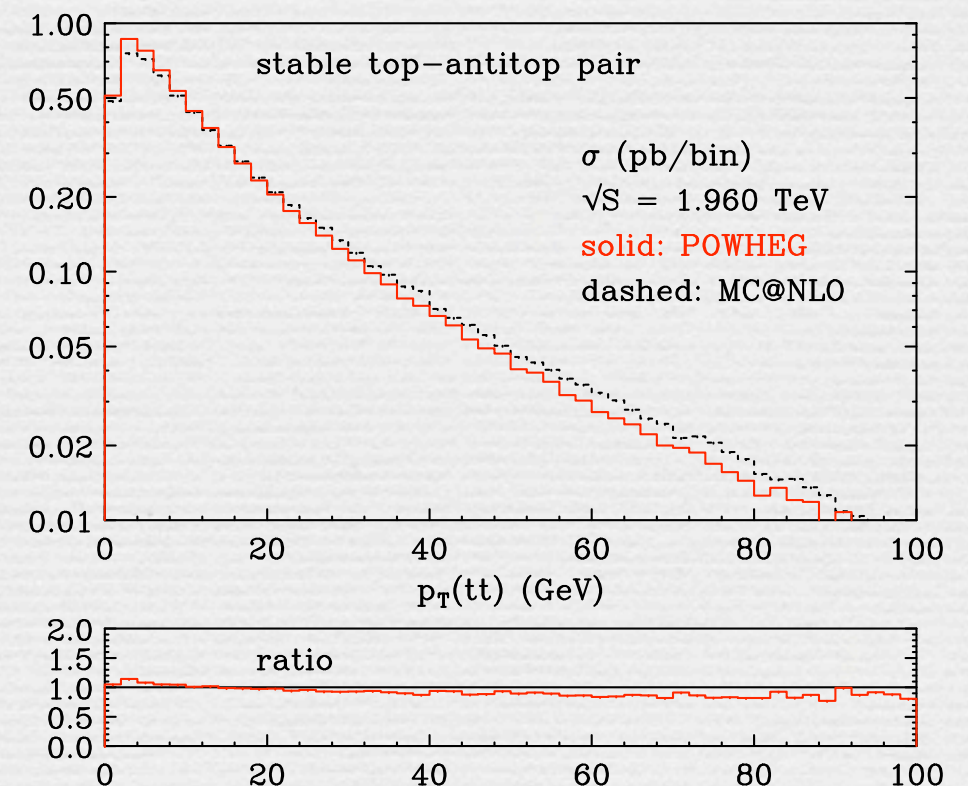
- ▶ MC@NLO matches to HERWIG(++) angular ordered showers (PYTHIA initial state).

Nason; Frixione, Oleari

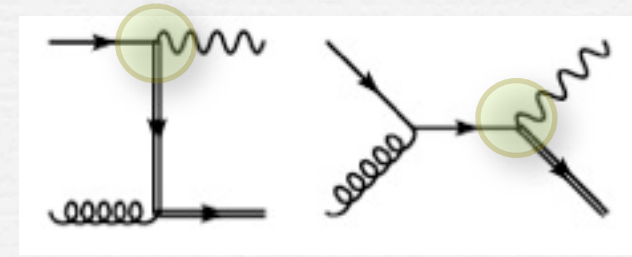
- ▶ POWHEG insists on having positive weights, exponentiates complete real matrix element (PYTHIA or HERWIG)

- ▶ Automatization: POWHEG Box, aMC@NLO

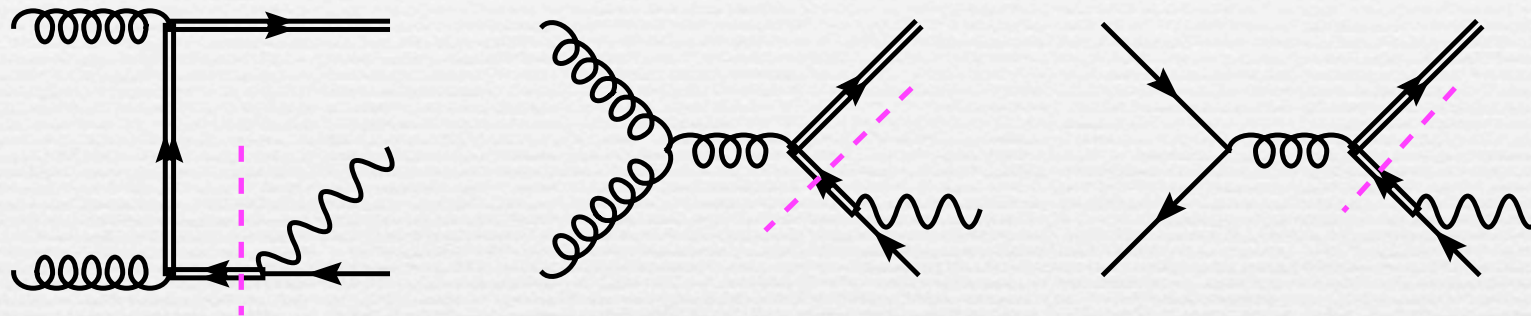
For most observables, good agreement
Increasingly important tools for experiment



Single top in Wt mode meets $t\bar{t}$.



Frixione, EL, Motylinski, Webber, White



+ non-resonant diagrams

Serious interference with pair production (15 times bigger) (same problem in Ht)

- ▶ In earlier calculations, subtract in calculation/cut on invariant mass
- ▶ What can one do in event generation? Prototypical for future cases.
- ▶ Can one actually define this process?
- ▶ Important cut: veto hard second b-jet suppress $t\bar{t}$

Campbell, Ellis, Tramontano

Can we define W_t as a process?

Frixione, EL, Motylinski, Webber, White

Two approaches in MC@NLO (now also in POWHEG (Re))

- ▶ I. Remove resonant diagrams (DR)
- ▶ II. Construct a gauge invariant, local counterterm: diagram subtraction (DS)
- ▶ DS - DR is measure of interference

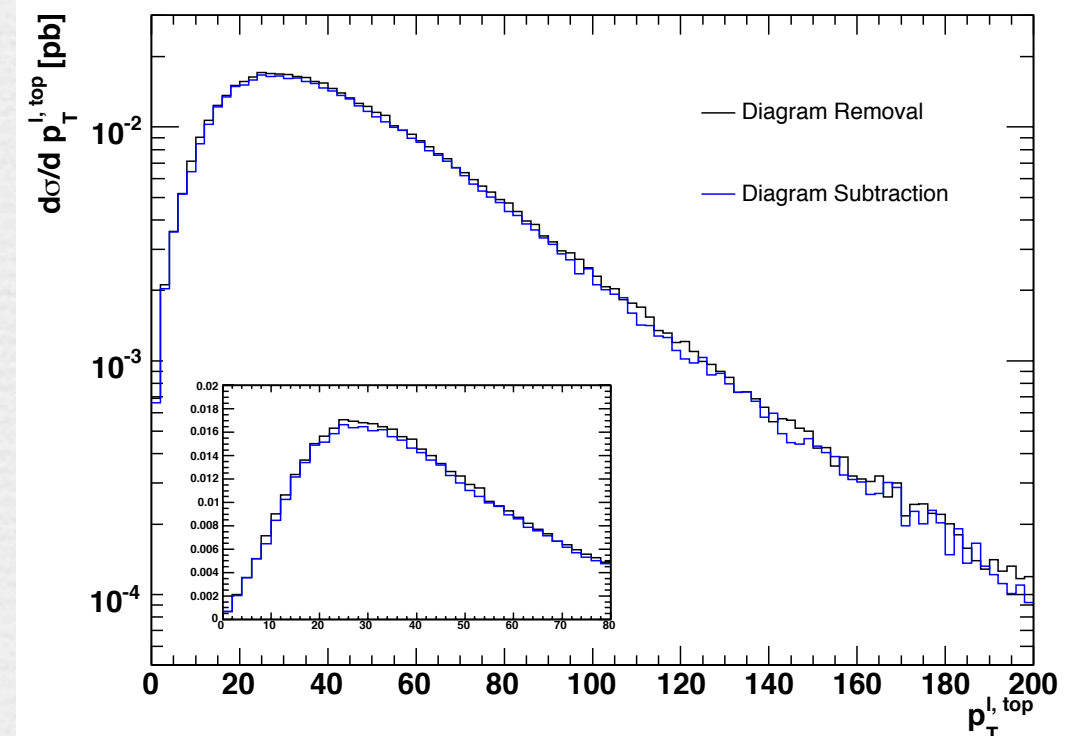
Momentum reshuffling

$$\tilde{\mathcal{D}}_{gg} = \frac{BW(M_{\bar{b}W})}{BW(M_t)} |A_{gg}^{t\bar{t}}|_{\text{reshuffled}}^2$$

$$d\sigma^{(2)} + \sum_{\alpha\beta} \int \frac{dx_1 dx_2}{2x_1 x_2 S} \mathcal{L}_{\alpha\beta} \left(\hat{\mathcal{S}}_{\alpha\beta} + \mathcal{I}_{\alpha\beta} + \mathcal{D}_{\alpha\beta} - \tilde{\mathcal{D}}_{\alpha\beta} \right) d\phi_3$$

Compare

- ▶ Interference effects quite small, in general
- ▶ Next question: can one isolate W_t ?



Isolating Wt

- ▶ Can we isolate Wt then? Answer subject to cuts. Some choices:

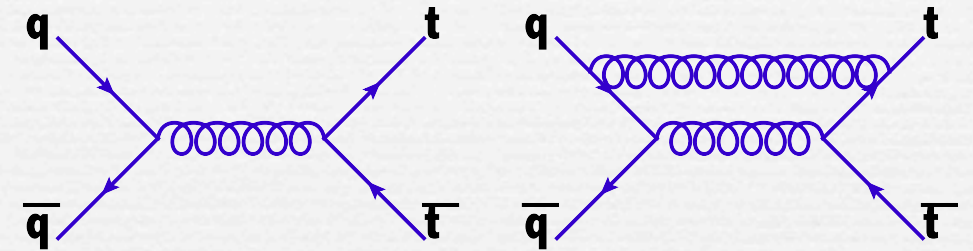
White, Frixione, EL, Maltoni

- ▶ Cuts to isolate Wt
 - ▶ Cuts to suppress Wt and $t\bar{t}$ as background to $H \rightarrow WW$
- ▶ Find:
 - ▶ Yes, can consider separate NLO corrections for $t\bar{t}$ (70%) and for Wt (40%)
- ▶ LHC experiments use boosted decision trees and neural nets, so far only evidence (in rough agreement with SM)

Forward-backward

Charge/forward-backward asymmetry

$$A_t(y) = \frac{N_t(y) - N_{\bar{t}}(y)}{N_t(y) + N_{\bar{t}}(y)}$$



- ▶ Why not present at LO, like W-charge asymmetry?
 - ▶ Incoming quark/antiquarks are already forward-backward asymmetric
 - ▶ But the produced gluon has no memory of that \Rightarrow charge symmetric
- ▶ At NLO, interference of tree and box produces a (small) asymmetry.
 - ▶ Already present in QED
 - ▶ “Measured” (1978)
 - ▶ in QCD, proportional to $SU(3)$ d_{abc} symbol
- ▶ Charge asymmetry is equivalent to FB asymmetry, since CP is conserved in QCD.
- ▶ Other test of $t\bar{t}$ production mechanism besides σ

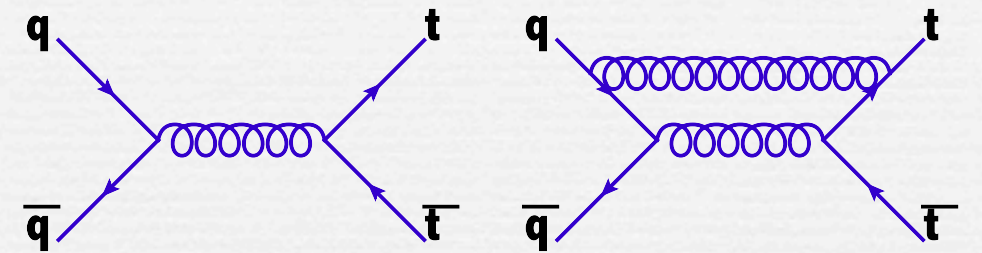
SLAC-LBL@SPEAR

Limits on Strength of Neutral Currents from $e^+e^- \rightarrow \mu^+\mu^-$

T. Himel, B. Richter, G. S. Abrams, M. S. Alam, A. M. Boyarski, M. Breidenbach, W. Chinowsky, G. J. Feldman, G. Goldhaber, G. Hanson, J. A. Jaros, R. R. Larsen, D. Lüke, V. Lüth, R. Schindler, R. F. Schwitters, J. L. Siegrist, and G. H. Trilling

$$A_{FB} = 0.013 \pm 0.010$$

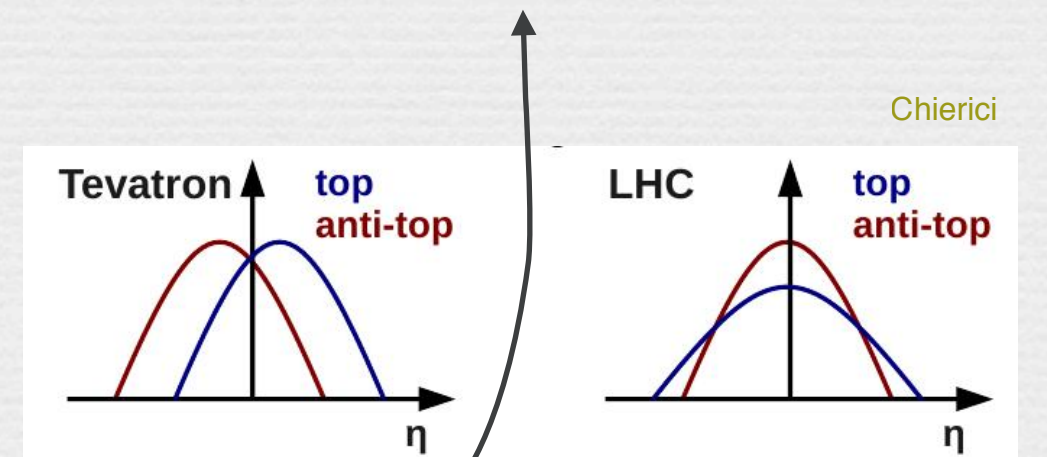
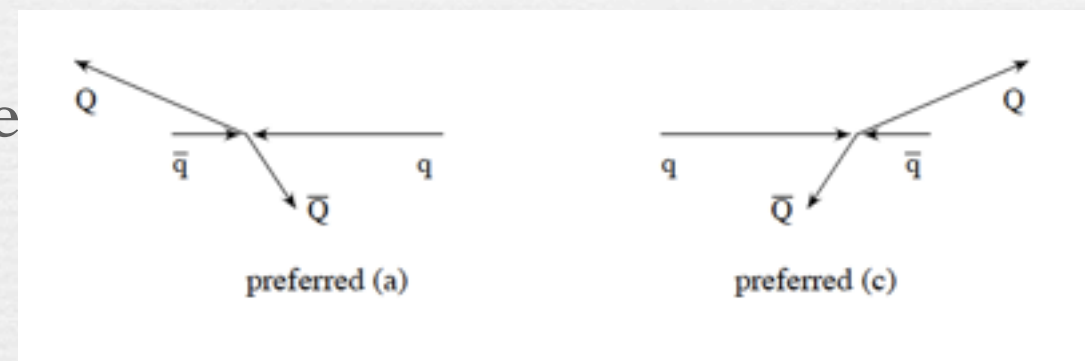
Some intuition about A_{FB}



- ▶ Compute matrix element as function of t, u
- ▶ Charge conjugation equivalent to t, u interchange

$$\propto \frac{t^2 + u^2}{s^2} + \frac{2m^2}{s} = A + B \cos^2 \theta$$

- ▶ In box contribution, find terms that are proportional to $t^2 - u^2 \Rightarrow$ linear in $\cos \theta$
- ▶ Quark “repels” top via second gluon, leading to “preferred” situations, or plots below



From resummation formulae:

$$\frac{\Delta\sigma}{\sigma} \simeq \exp \left\{ \alpha_s L \left[\frac{32}{6} - \frac{27}{6} \right] \ln \frac{u}{t} \right\}$$

A_{FB} in experiment

A plethora of asymmetries....

Westhoff

▶ Tevatron

▶ CDF (2010/11): defines 4: 2 in lab frame, 2 in $t\bar{t}$ frame

- ▶ using (or not) rapidity of leptonic/hadronic top
- ▶ differential (in $M_{t\bar{t}}$, and/or rapidity)
- ▶ now also in di-lepton channel

▶ CDF (2010, $l+jets$, 5.3/fb):

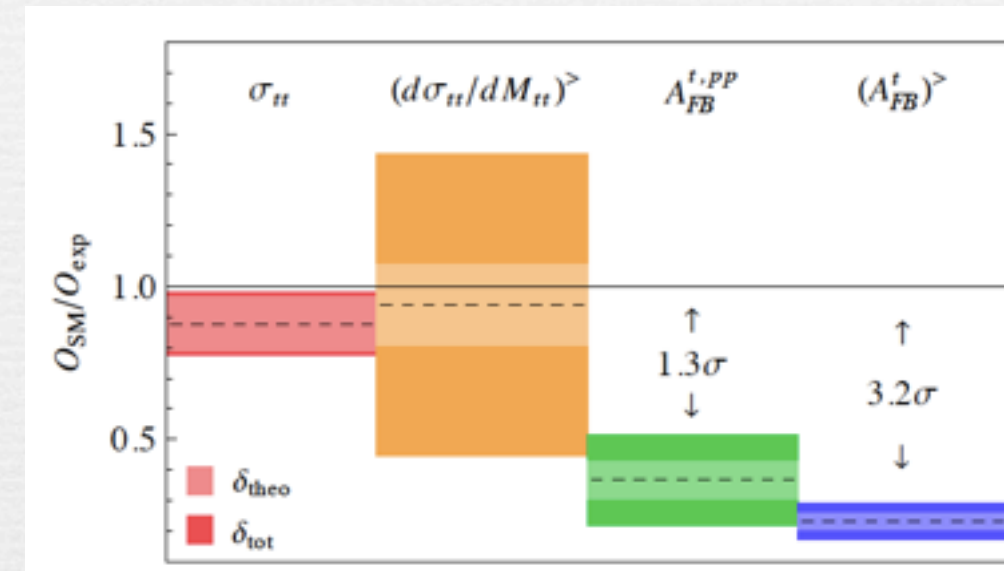
▶ DO (2011, $l+jets$, 5.4/fb): $19.6 \pm 6.5\%$ [2.4σ], larger for lepton-based asymmetry

- ▶ some trouble with modelling SM pair p_T

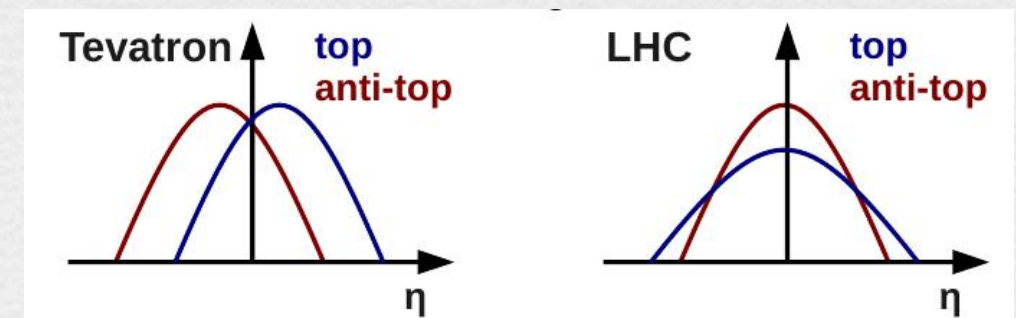
▶ LHC

▶ Suggested: asymmetry from events with (anti-)top above a minimum rapidity

▶ Not easy for NP models to change A_{FB} without changing σ



Chierici

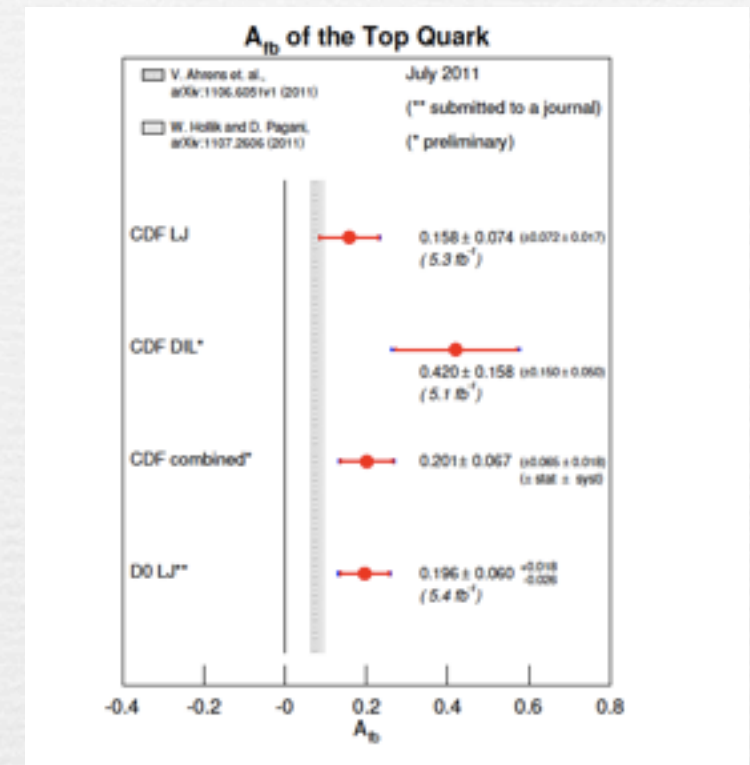


Higher orders in A_{FB}

NLL: Kidonakis, EL, Moch, Vogt

$$\frac{d^2\sigma^2}{dM^2 d\cos\theta} = C_4(\theta) \left[\frac{\ln^3(1 - M^2/s)}{1 - M^2/s} \right]_+ + C_3(\theta) \left[\frac{\ln^2(1 - M^2/s)}{1 - M^2/s} \right]_+ + \dots$$

- ▶ A_{FB} is zero at LO, hence the NLO cross section contributes at LO to A_{FB}
- ▶ Higher order contributions to A_{FB} from threshold resummation
 - ▶ Leading logs charge symmetric, cancel in numerator, but subleading ones remain Almeida, Sterman
 - ▶ Find: A_{FB} stable under higher orders
 - ▶ Similar conclusion at NNLL Ahrens, Ferroglia, Neubert, Pecjak, Yang; Kidonakis
- ▶ A_{FB} already at LO in $t\bar{t}$ +jet, but NLO corrections reduce this significantly Dittmaier, Uwer, Weinzierl; Melnikov, Schulze
 - ▶ likely stable under yet higher orders

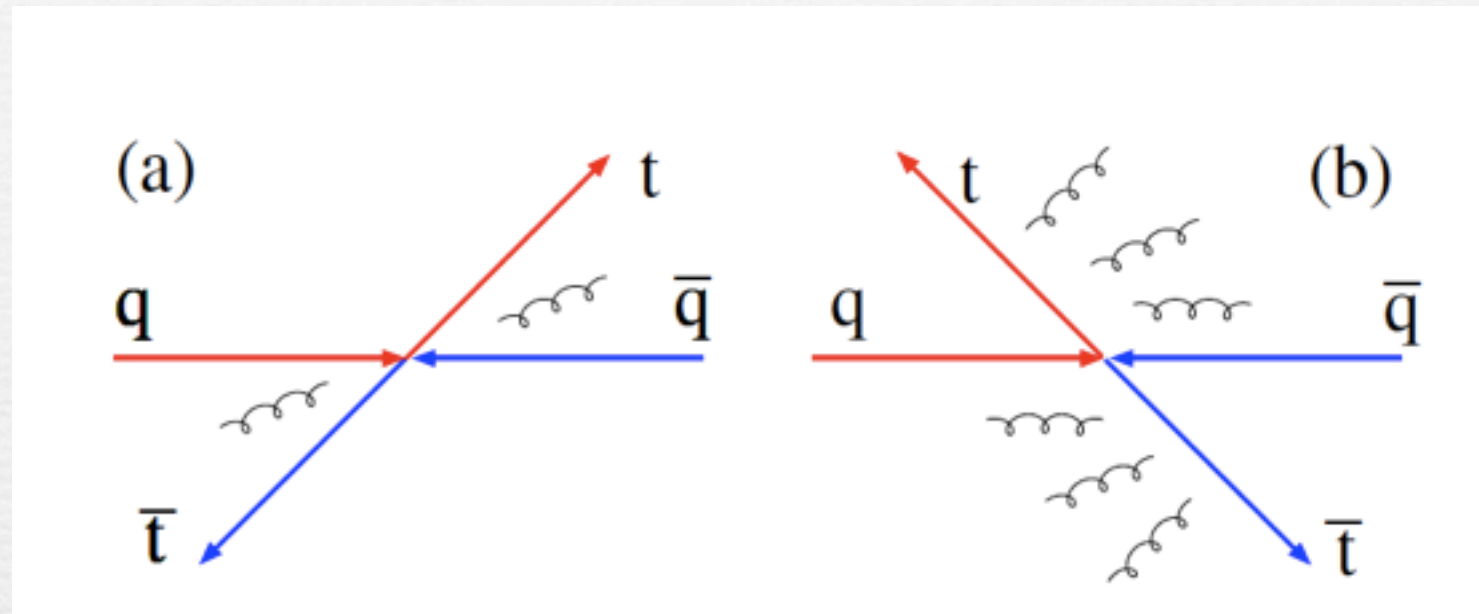


$$A_{\text{FB}}(t\bar{t}j) = \alpha_s^3 \frac{C}{\ln(m/p_{T,j})} + \alpha_s^4 D_{\text{hard}} \quad \text{Melnikov, Schulze}$$

- ▶ Also for $t\bar{t}j$ NLO term reduces LO A_{FB} Bevilacqua, Czakon, Papadopoulos, Worek
- ▶ Including EW effects reduce discrepancy Hollik, Pagani

Color coherence effects and A_{FB}

Skands, Webber, Winter



- ▶ Color coherence:
 - ▶ backward tops produce more QCD radiation
→ more central pair
 - ▶ forward tops “left behind”
- ▶ Full impact for prediction, and acceptance, to be studied

Asymmetry at LHC

- Can define forward charge asymmetry

- Find: best for $y_0 = 1.5$

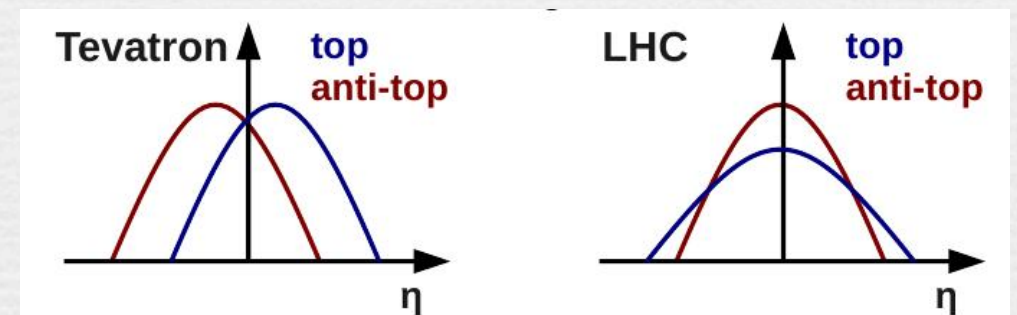
- Not easy for SM, but for new physics, doable:

- If SM: 5σ after 60/fb
 - If CDF: 5σ after 2/fb (with Z' model, $m_{Z'} = 160$ GeV)

Hewett, Shelton, Spannowsky, Tait, Takeuchi

$$A_F(y_0) = \frac{N_t(y_0 < |y|) - N_{\bar{t}}(y_0 < |y|)}{N_t(y_0 < |y|) + N_{\bar{t}}(y_0 < |y|)}$$

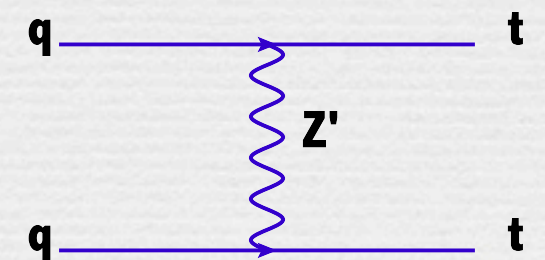
Chierici



Degrande, Gerard, Grojean, Maltoni, Servant

- Other (kinematic) possibility: same-sign tops

- Cross section can be $O(\text{pb})$ if new physics at 2 TeV



Mixed

(Associated) top production at higher order

Impressive recent progress

- ## ► Electroweak corrections

Bernreuther, Brandenburg, Si, Uwer; Kuhn, Scharf, Uwer; Maina, Moretti, Nolten, Ross

- Associated production at NLO (3+ particles in final state at LO)

- $t\bar{t} + \text{jet}$

Dittmaier, Uwer, Weinzierl
Melnikov, Schulze, Scharf

- $t\bar{t}$ + Higgs

Beenakker, Dittmaier, Krämer, Plumper, Spira, Zerwas;
Dawson, Jackson, Orr, Reina, Wackerroth
+PS: Frederix, Frixione, Hirshi, Maltoni, Pittau, Torrieli

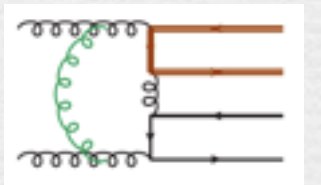
- $t\bar{t} + b\bar{b}$

Bredenstein, Denner, Dittmaier, Pozzorini
Bevilacqua, Czakon, Papadopoulos, Pittau, Worek

- $tt + j\bar{j}$

Bevilacqua, Czakon, Papadopoulos, Worek

10K X



- Calculations with off-shell top-decay (thus also with spin correlations)

- single top:

Falgari, Giannuzzi, Mellor, Signer

- $t\bar{t}$ (dileptons)

Bevilacqua, Czakon, Papadopoulos, Worek

Top self-analyzes its spin

- ▶ 100% correlation of charged lepton with top spin

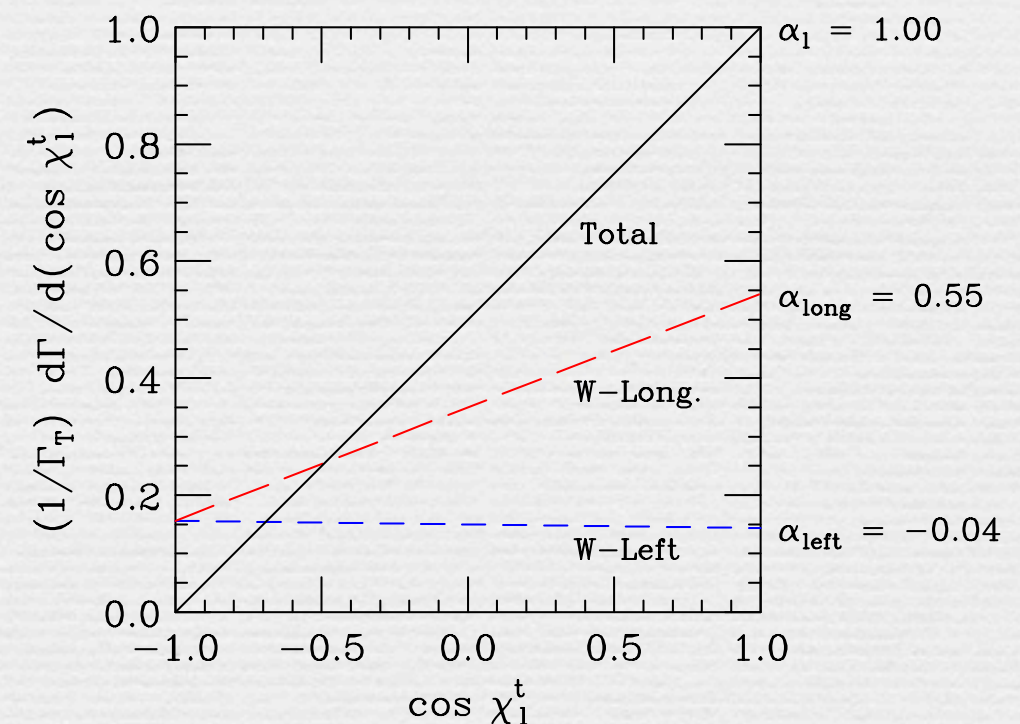
- ▶ Top self-analyzes its spin
- ▶ Charged leptons easy to measure

- ▶ For spin-up top the polar angle distribution is

$$\frac{1}{\Gamma_T} \frac{d\Gamma_{(\uparrow)}}{d(\cos \theta_{e+})} = \frac{1}{2}(1 + \cos \theta_{e+})$$

- ▶ Interesting quantum interference..

$$\frac{d \ln \Gamma_f}{d \cos \chi_f} = \frac{1}{2}(1 + \alpha_f \cos \chi_f)$$



$t\bar{t}$ spin correlations at NLO

Bernreuther, Brandenburg, Fückler, Si, Uwer

- ▶ At LHC, tops in pair production are produced essentially unpolarized
- ▶ But they do have clear mutual spin correlation (entanglement)

$$\frac{d\sigma}{d\cos\theta_a d\cos\theta_b} = \frac{\sigma}{4}(1 + B_1 \cos\theta_a + B_2 \cos\theta_b - C \cos\theta_a \cos\theta_b)$$

- ▶ C depends on quantization axis, highest in helicity basis in zero momentum frame

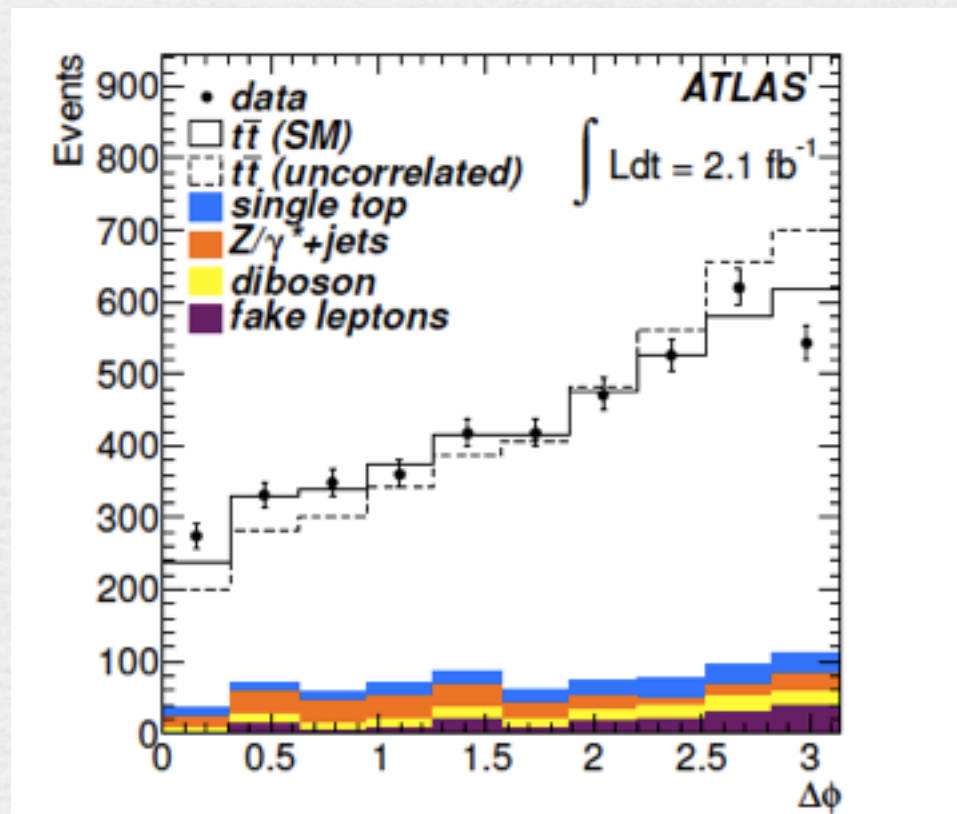
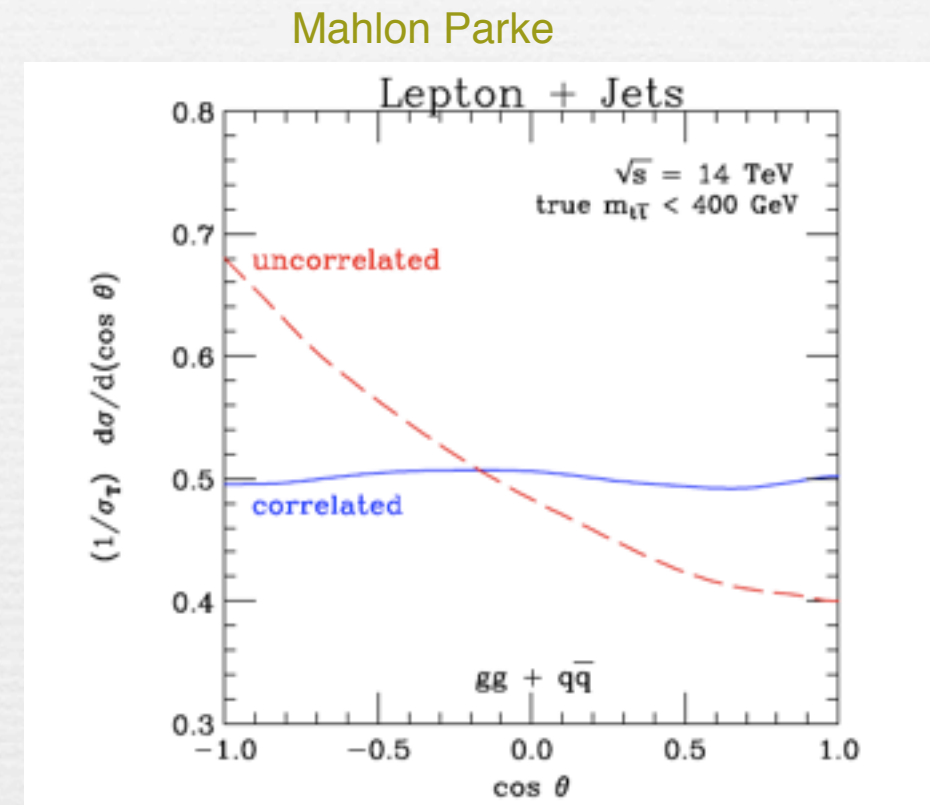
Mahlon, Parke

- ▶ $C_{\text{hel}} = 0.326$ ($C_{\text{beam}} = -0.07$) for LHC(14)
- ▶ NLO corrections small (EW corrections tiny)

Azimuthal angular distributions

- ▶ Can test SM spin correlations in $t\bar{t}$ using invariant mass cut, and dilepton decay channel
 - ▶ Visible through $\Delta\phi$ of leptons in lab frame
 - ▶ Even after summing over spurious neutrino momentum solutions
 - ▶ Can be upgraded to NLO, and a likelihood-based analysis

Melnikov, Schulze

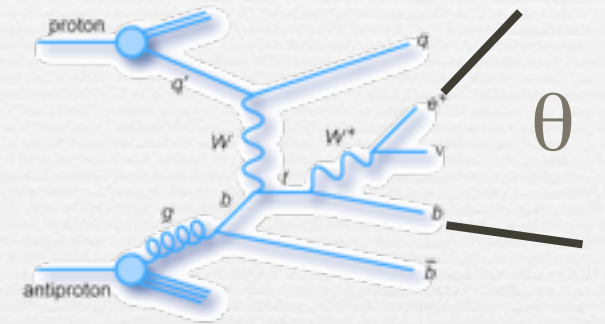


- ▶ ATLAS excludes zero correlation at 5.1σ
- ▶ Agrees with SM

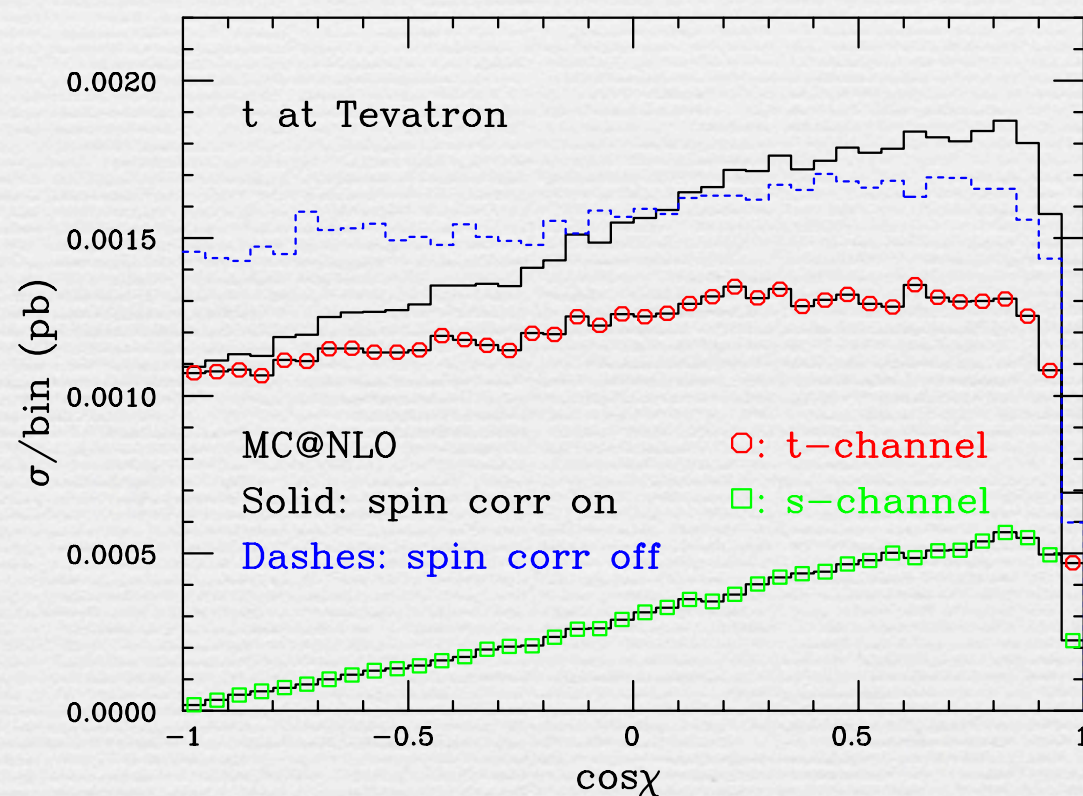
Spin correlations for single top in MC@NLO

Frixione, EL, Motylinski, Webber

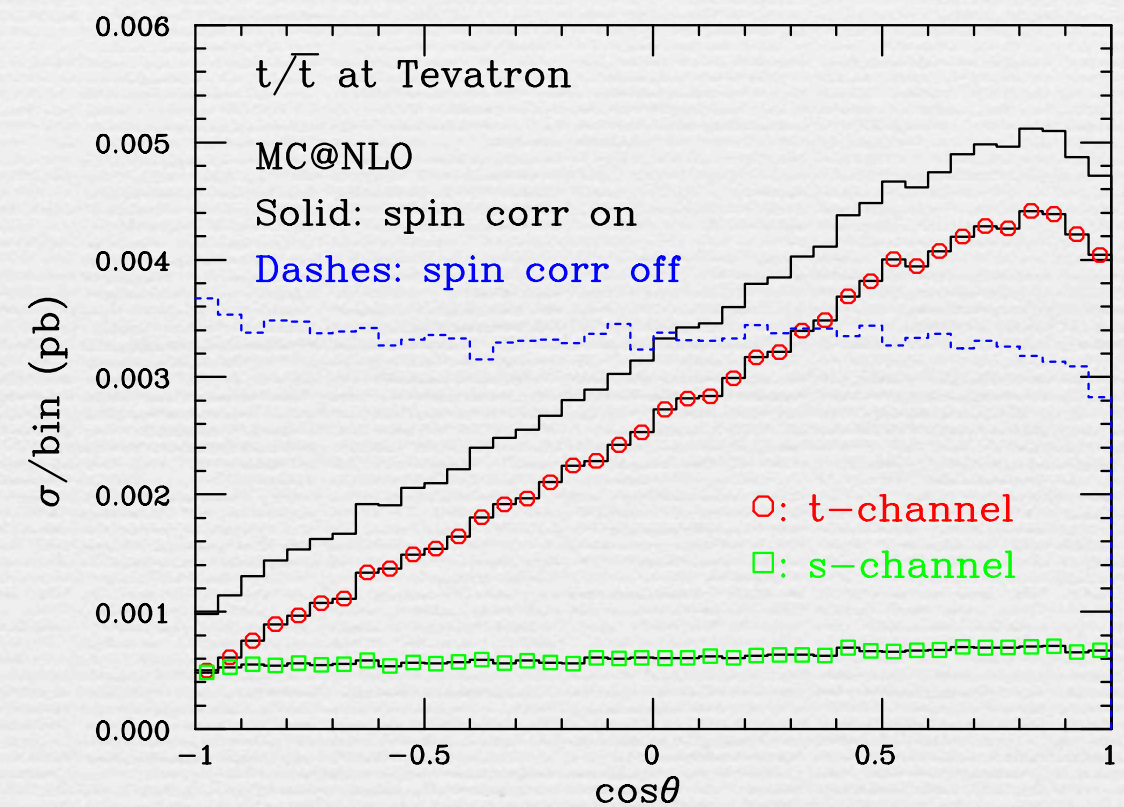
- Top is produced polarized by EW interaction
 - 100% correlation between top spin and charged lepton direction
- Angle of lepton with appropriate axis is different per channel
- Method included “a posteriori”. Also used in POWHEG



Aioli, Nason, Oleari, Re



Beam direction



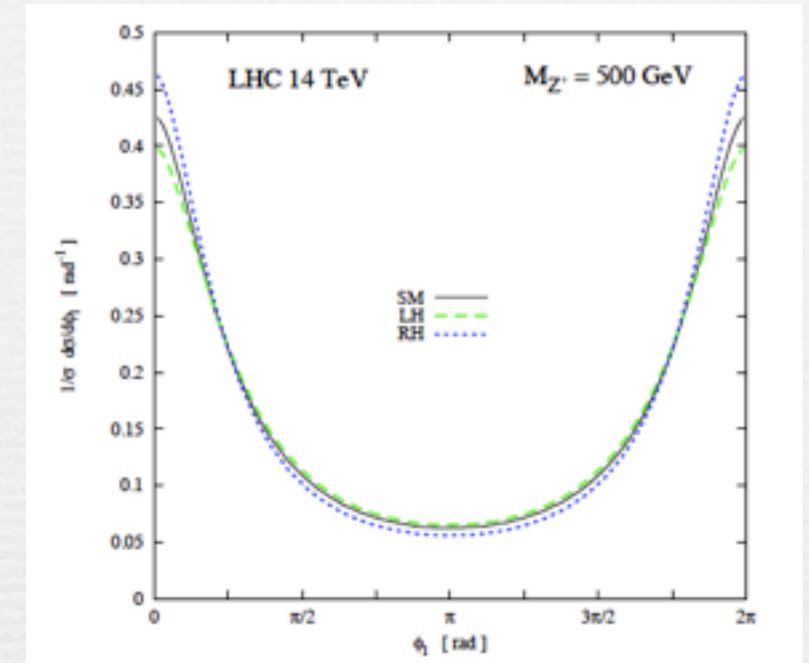
Hardest, non-b jet

Robust correlation in NLO event generation

Azimuthal distributions and BSM tests

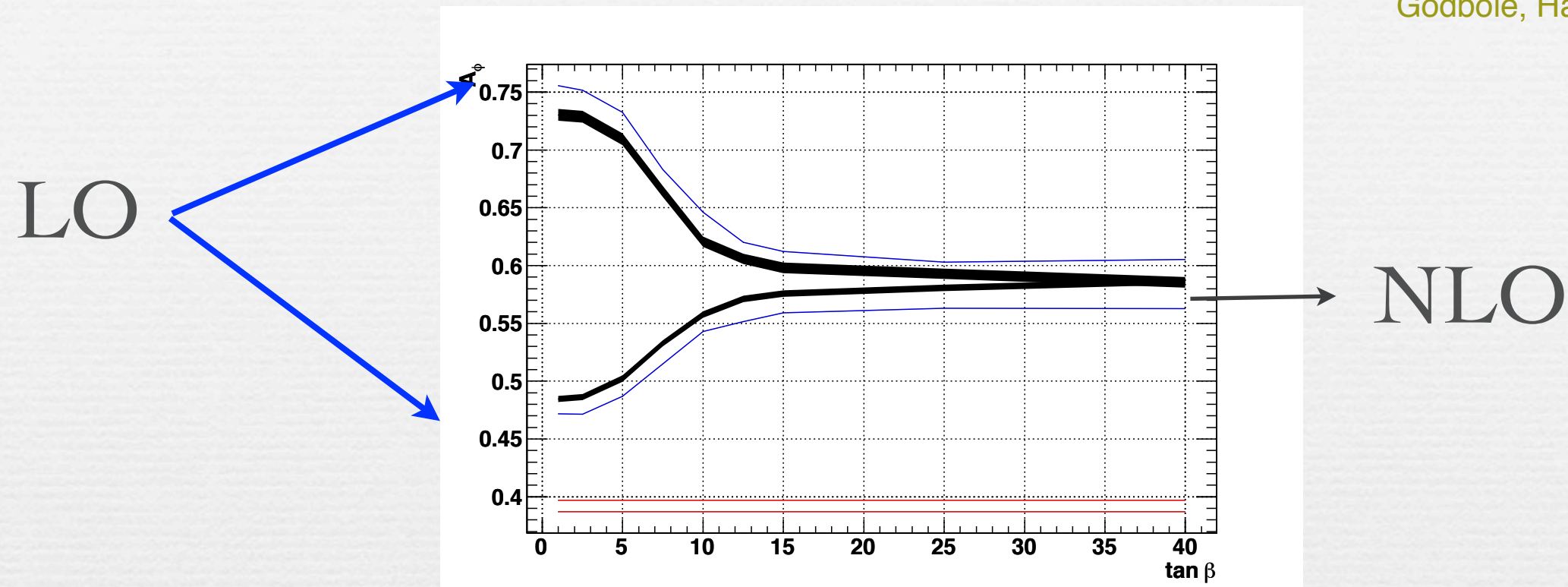
Godbole, Rao, Rindani, Singh

- ▶ Angular distributions (and others) can be selective probes of new physics
 - ▶ Rely on nearly 100% correlation of decay- lepton with top spin
 - ▶ If, e.g., Z' polarizes the tops, can use distribution in azimuthal angle of lepton (wrt. beam-top plane) to study dynamics
 - ▶ Enhance sensitivity by judicious cuts on p_T of top



H_t vs. W_t

Godbole, Hartgring, Niessen, White



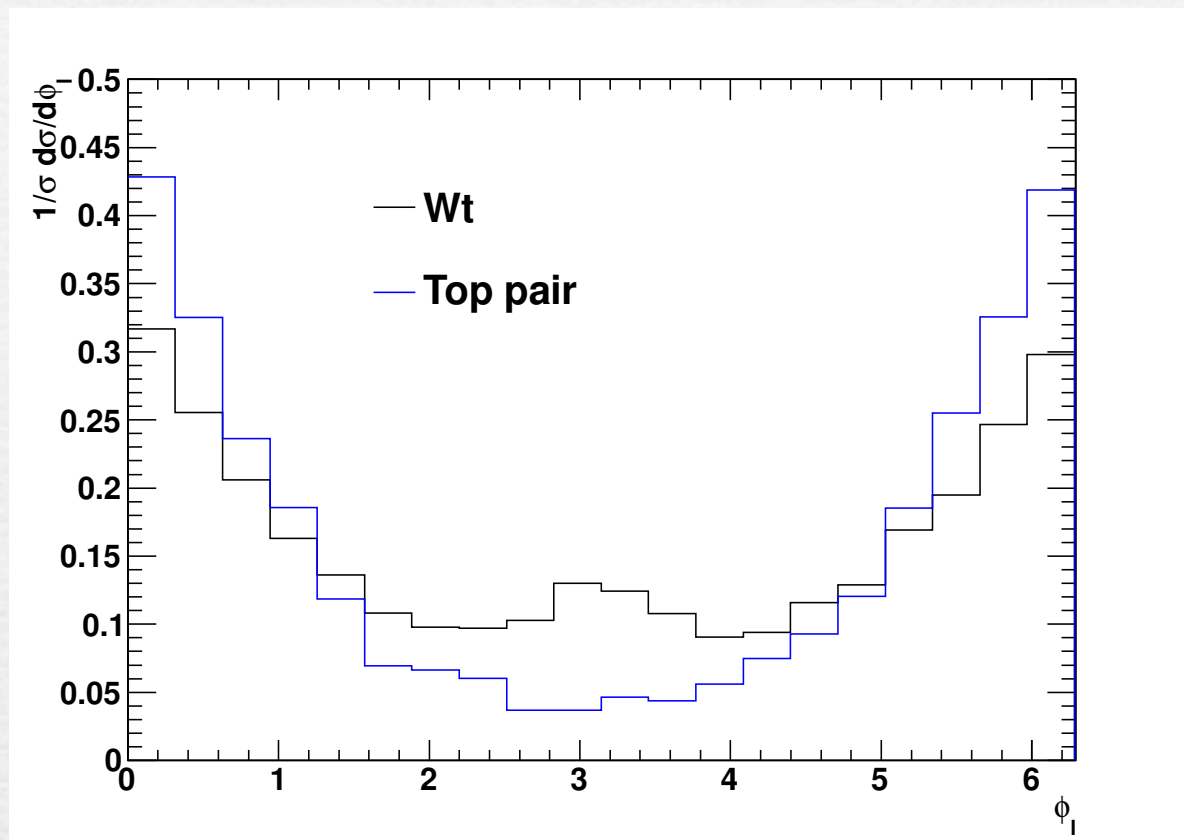
- Construct asymmetry

$$A = \frac{\sigma(\cos \phi_l > 0) - \sigma(\cos \phi_l < 0)}{\sigma(\cos \phi_l > 0) + \sigma(\cos \phi_l < 0)}$$

- Test robustness under HO corrections (via MC@NLO), quite ok

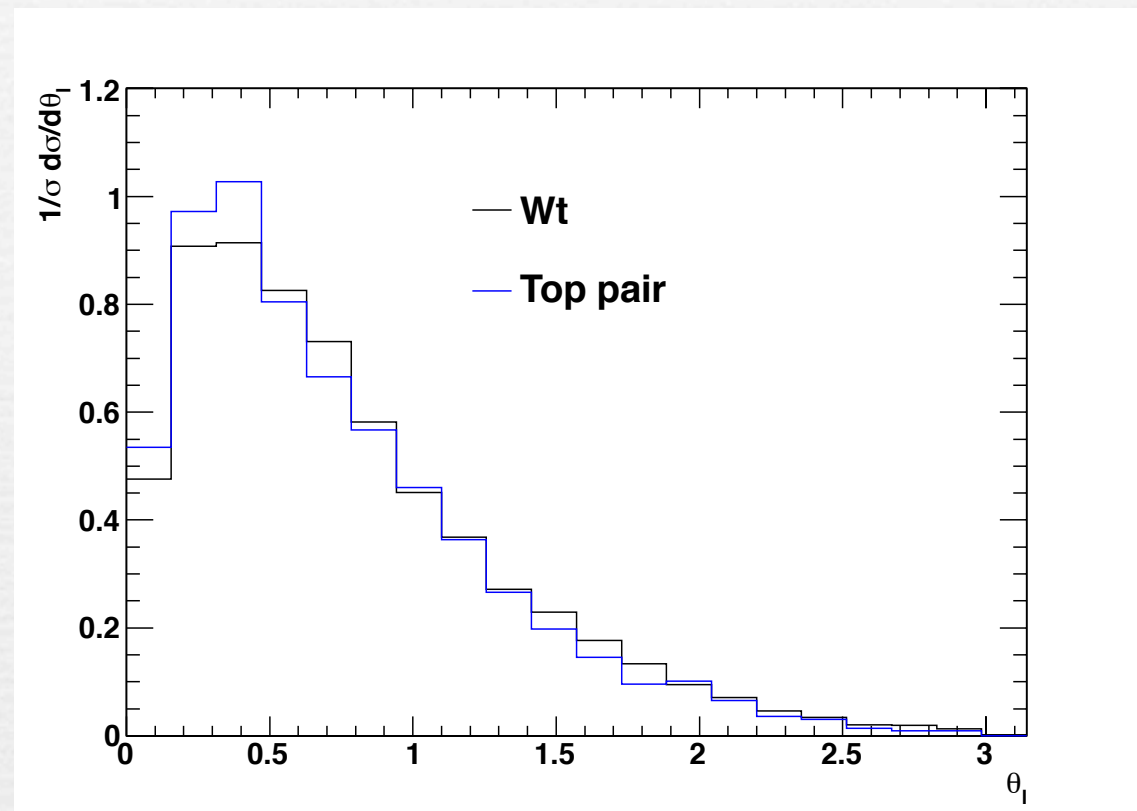
Angular distributions for Wt and $t\bar{t}$ separation

Godbole, Hartgring, Niessen, White



A_ϕ

B_{cut}	Wt	Top pair
0	0.33 ± 0.01	0.63 ± 0.02
0.8	0.41 ± 0.02	0.70 ± 0.05
0.9	0.42 ± 0.03	0.70 ± 0.07
0.95	0.44 ± 0.04	0.68 ± 0.08

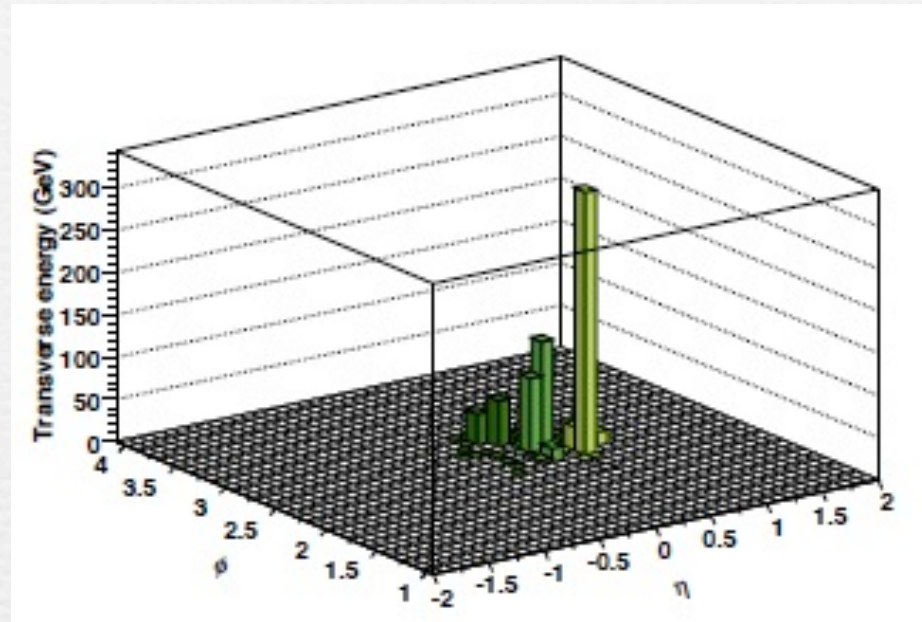


A_θ

B_{cut}	Wt	Top pair
0	0.02 ± 0.01	0.26 ± 0.02
0.8	0.18 ± 0.02	0.38 ± 0.04
0.9	0.49 ± 0.03	0.75 ± 0.07
0.95	0.70 ± 0.05	0.97 ± 0.10

Boosted Tops

Pruning, Trimming Grooming



Thaler, Wang
Kaplan, Rehermann, Schwartz, Tweedie
Almeida, Lee, Perez, Sung, Virzi

- ▶ Following ideas to tag Higgs bosons, can one efficiently tag high pt top jets?
Software:

Butterworth, Ellis, Salam, et al

- ▶ “Reverse engineer clustered fat top jet”, find 3 subjets.
- ▶ Can reduce di-jet backgrounds to $t\bar{t}$ resonances by factor order 10K!
 - ▶ depending on method
- ▶ (Semi-)analytical approach
- ▶ Enrich boosted top sample by weighting them with IR safe top decay templates

Almeida, Lee, Perez, Stermann, Sung, Virzi

See BOOST2010 report. Karagoz,
Spannowsky, Vos (eds)

Conclusions

- ▶ LHC has now definitely taken over for most top observables
 - ▶ but not all (A_{FB} , studies that need qq initial state,..)
- ▶ Analyses requiring large top samples are now here: LHC as T-factory
 - ▶ top is the new bottom
 - ▶ correlations, angular distributions, other complex final states, so far agreeing with SM
- ▶ SM theoretical understanding is very good now
 - ▶ can scale up extensive verification/falsification project for top
 - ▶ things work all too well..
 - ▶ but much remains to be done