

Rare B meson decays

Francesco Dettori¹, Paolo Iengo², Luca Martini³

¹ NIKHEF and Vrije Universiteit, Amsterdam

² INFN Napoli

³ INFN Pisa

VI Workshop Italiano sulla Fisica p-p a LHC

8-10 May 2013

Genova

Introduction and outline

Rare decays are a crucial probe of physics beyond the Standard Model

- High precision predictions of SM observables
- Tiny effects so NP can be at the same level of SM
- Higher energy scales than directly accessible for production of new particles
- Probing the flavour structure leads to clear signatures of the type of new physics to expect

B meson rare decays:

- FCNC - Suppressed by GIM mechanism
- Forbidden decays (e.g. Lepton or Baryon number violation)

Today:

- Searches for $B_{d,s}^0 \rightarrow \mu^+ \mu^-$ decays at LHC
- Search for $B_{d,s}^0 \rightarrow \mu^+ \mu^- \mu^+ \mu^-$

The $B_{d,s}^0 \rightarrow \mu^+ \mu^-$ decays in theory

- Standard Model prediction for CP averaged branching fractions at $t = 0$:

$$\begin{aligned}\mathcal{B}^{t=0}(B_s^0 \rightarrow \mu^+ \mu^-) &= (3.25 \pm 0.17) \times 10^{-9} && [\text{A. Buras et al. arXiv:1303.3820}] \\ \mathcal{B}^{t=0}(B^0 \rightarrow \mu^+ \mu^-) &= (1.07 \pm 0.10) \times 10^{-10} && [\text{Eur.Phys.J. C72 (2012) 2172}]\end{aligned}$$

To compare with experimental values, which are time integrated, a correction due to the finite $B_s^0 - \bar{B}_s^0$ width difference has to be applied [De Bruyn et al. [PRL 109, 041801]]

[Phys.Rev.Lett.108 (2012) 101803]

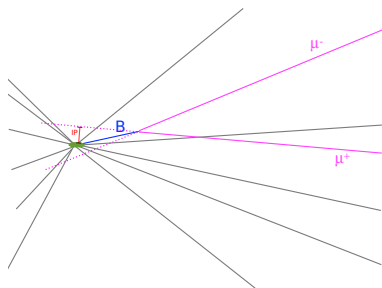
$$\mathcal{B}^{(t)}(B_s^0 \rightarrow \mu^+ \mu^-) = \left(\frac{1 + \mathcal{A}_{\Delta\Gamma} y_s}{1 - y_s^2} \right) \mathcal{B}^{t=0}(B_s^0 \rightarrow \mu^+ \mu^-) \stackrel{SM}{=} (3.56 \pm 0.18) \times 10^{-9}$$

- New Physics models predict various and different enhancements or suppressions

Analysis strategy

The strategy is very similar for the three experiments.

1. Loose pre-selection:
 - * Pairs of opposite charged muons
 - * Vertex displaced with respect to interaction point
 - * p_T , IP and quality requirements
2. Blind analysis
3. Normalisation to $B^+ \rightarrow J/\psi K^+$ (and $B^0 \rightarrow K^- \pi^+$ for LHCb)
4. Final classification with tight selection
 - * Straight cuts for CMS
 - * Multivariate cut for ATLAS
 - * Multivariate and 2D classification for LHCb
5. CLs method for the limits

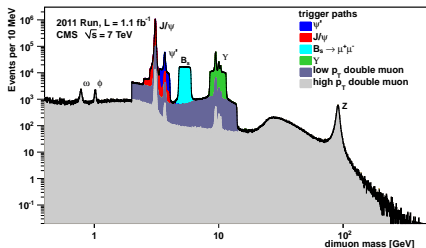


CMS analysis

2011 analysis based on 5 fb^{-1} at $\sqrt{s} = 7 \text{ TeV}$

Trigger

- Dimuon triggers
 - Tightening with increasing instantaneous luminosity
 - Trigger selection based on
 - * p_T and η of muons
 - * invariant mass
 - * secondary vertex probability
 - * impact parameters
 - * flight length
 - * pointing angle
- Evaluated both with MC methods and on data with tag & probe

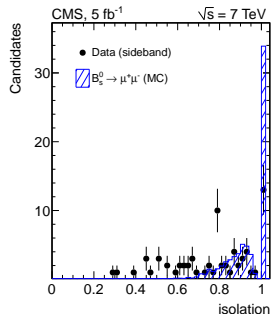
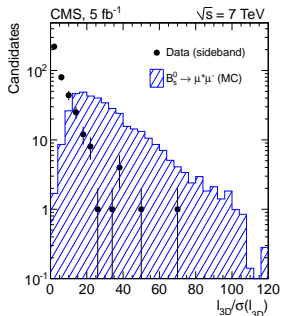
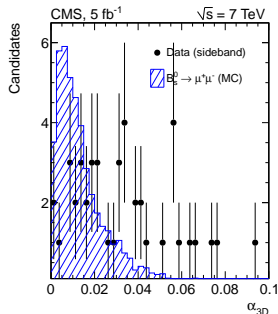


CMS analysis: selection

Selections optimized (random grid search) for best upper limit

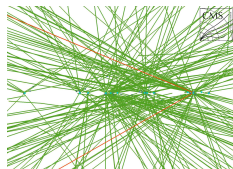
- Pointing angle α_{3D}
- Flight length significance $l_{3D}/\sigma(l_{3D})$
- Impact parameter significance
- Isolation cone around primary vertex: $I = p_T(B)/(p_T(B) + \sum_{\text{trk}} |p_T|)$
- Isolation of secondary vertex

Data sidebands vs Blue MC



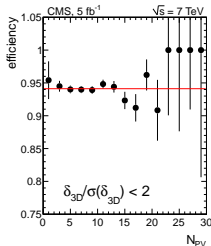
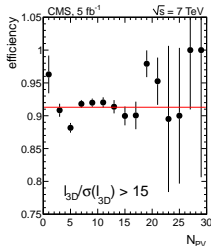
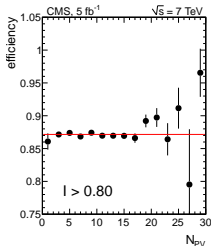
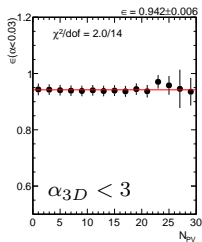
CMS analysis: Pile-up

- In 2011: $\langle N_{PV} \rangle = 8$, $\text{RMS}(z) = 5.6$ cm
- Selections have been tuned to be pile-up independent (e.g. isolation searches only for tracks coming from the same primary vertex or not associated to any.)
- Efficiencies of all selection criteria have been evaluated versus N_{PV}
- All selections are compatible with a constant at least until 30 PV
- The same conclusion is also obtained from MC simulations, looking at samples with low (< 6) or high (10) PU events



$$B^+ \rightarrow J/\psi K^+$$

$$B_s^0 \rightarrow J/\psi \phi$$



ATLAS analysis: trigger and selection

ATLAS 2011 analysis based on 2.4 fb^{-1} at $\sqrt{s} = 7 \text{ TeV}$

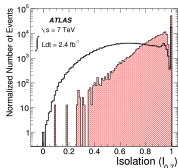
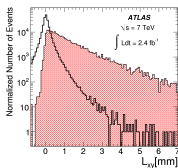
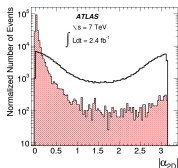
- Trigger L1 dimuon trigger $p_T > 4 \text{ GeV}$
- 2- (B0s) or 3- (B) prong vertex constraint
- Primary vertex selection:
 - * The closest in z to the B candidate
 - * Re-fit excluding B daughters
- Tracks:
 - * $|\eta| < 2.5$ and $p_T > 4$ (2.5) GeV for muons (kaons)
 - * At least 1 pixel, 6 SCT and 9 TRT hits
 - * ID tracks matching tracks in Muon Spectrometer for muons

B candidates

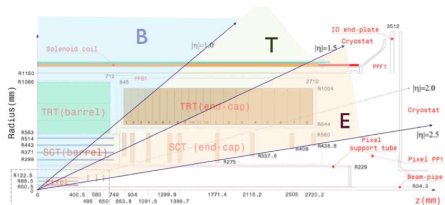
- * $p_T > 8 \text{ GeV}$ and $|\eta| < 2.5$

Signal/Bkg discrimination

- * Boost Decision Tree on 14 variables
- * Optimisation with $\mathcal{P} = \frac{\epsilon_{sig}}{\frac{a}{2} + \sqrt{N_{bkg}}}$



- Mass resolution for dimuon candidates changes substantially between barrel and end-cap detectors
- Data sample divided in three mass resolution bin categories according to the largest pseudorapidity of the muons



$ \eta_{max} $	1.0	1.5	2.5
σ_m [MeV]	60	80	110
Relative fraction [%]	51	24	25
Invariant mass window [MeV]	± 116	± 133	± 171
BDT output threshold	0.234	0.245	0.270

LHCb analysis: trigger and preselection

LHCb analysis: 1fb^{-1} at $\sqrt{s} = 7$ TeV (2011) and 1.1fb^{-1} at $\sqrt{s} = 8$ TeV (2012)

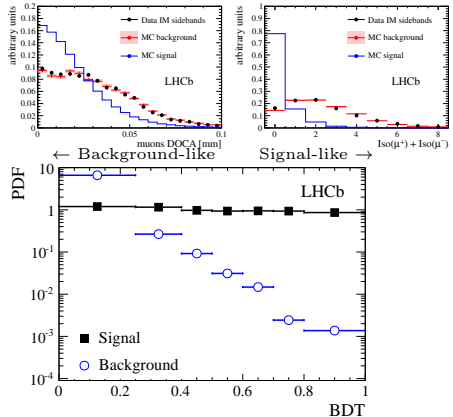
- L0 Single and dimuon triggers
- Signal trigger efficiency about 90%

Soft preselection based on

- High quality dimuon displaced from PV
- Flight distance significance
- Impact parameters
- Transverse momenta

Final classification with multivariate analysis:

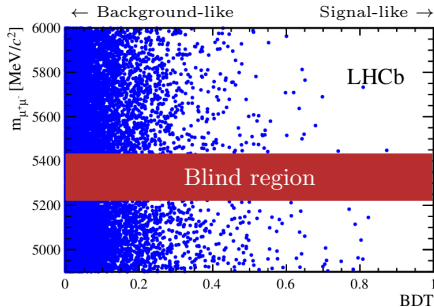
- Boosted Decision Tree with 9 variables:
 B IP, B isolation, B p_T , B τ , μ IP, $\min(\mu p_T)$, μ isolation, DOCA, μ to B angle
- Training with MC
- Calibration with data



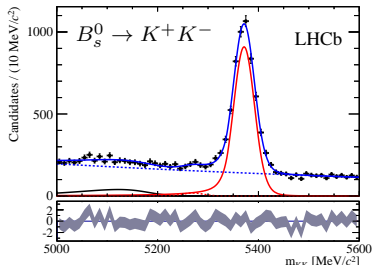
LHCb analysis: classification

Search performed in 8×6 bins of invariant mass ($m_{\mu\mu} \in [m_B \pm 60 \text{ MeV}/c^2]$) and BDT

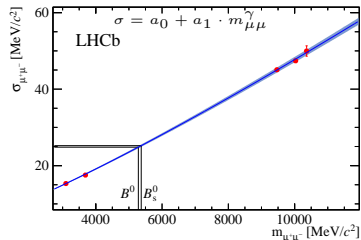
- Signal PDFs calibrated with $B \rightarrow h^+ h^-$ and quarkonia
- Background with sidebands



Calibration of mass central value



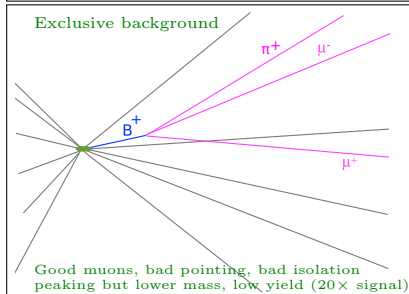
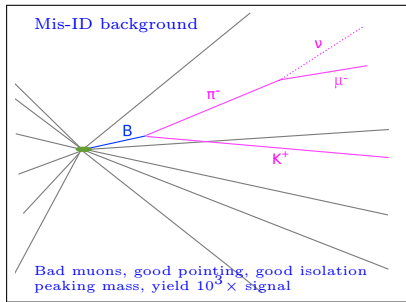
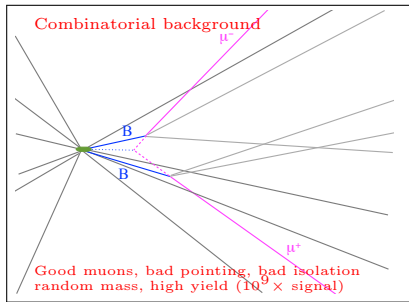
Calibration of mass central resolution



$$\sigma_{B^0} = (24.6 \pm 0.4) \text{ MeV}/c^2$$

$$\sigma_{B_s^0} = (25.0 \pm 0.4) \text{ MeV}/c^2$$

Backgrounds



Hadronic	$B \rightarrow h^+ h'^- \text{ with } h = \pi, K$
Semileptonic	$B^0 \rightarrow \pi^- \mu^+ \nu$
	$B_s^0 \rightarrow K^- \mu^+ \nu$
	$\Lambda_b^0 \rightarrow \bar{p} \mu^+ \nu$
	$B_c^+ \rightarrow J/\psi \mu^+ \nu \mu^-$
	$B_s^0 \rightarrow D_s^- (\rightarrow \mu^- \nu) \mu^+ \nu$
Rare decays	$B^+(0) \rightarrow \pi^+(0) \mu^+ \mu^-$
	$B_s^0 \rightarrow \mu^+ \mu^- \gamma$

Normalisation

The normalisation is very similar for the three experiments:

$$\mathcal{B} = \frac{\epsilon_{cc}}{\epsilon_{\text{sig}}} \cdot \frac{f_{cc}}{f_q} \cdot \frac{N_{B_q^0 \rightarrow \mu^+ \mu^-}}{N_{cc}} \cdot \mathcal{B}_{cc} = \alpha_q \cdot N_{B_q^0 \rightarrow \mu^+ \mu^-}$$

- Reconstruction and selection efficiencies from MC but cross-checked with data
- Trigger efficiency from data where possible
- Hadronisation fractions from updated LHCb measurement
 $f_s/f_d = 0.256 \pm 0.020$
→ ATLAS and CMS assume no kinematic dependence:
verified within statistical accuracy by CMS with $B_s^0 \rightarrow J/\psi\phi/B^+ \rightarrow J/\psi K^+$
- LHCb exploits also $B^0 \rightarrow K^- \pi^+$

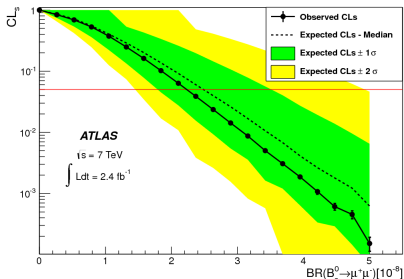
Single event sensitivities examples:

- ATLAS 2011 2.4 fb^{-1} $\alpha_{B_s^0 \rightarrow \mu^+ \mu^-} = 3.6 \cdot 10^{-9}$
- CMS 2011 5 fb^{-1} Barrel $\alpha_{B_s^0 \rightarrow \mu^+ \mu^-} = 1.03 \cdot 10^{-9}$
- LHCb 2012 1 fb^{-1} $\alpha_{B_s^0 \rightarrow \mu^+ \mu^-} = 2.80 \cdot 10^{-10}$

	Mass Resolution bins		
	$ \eta < 1.0$	$1.0 < \eta < 1.5$	$1.5 < \eta < 2.5$
Events in sidebands	5	0	2
Exp. bkg in SR	3.86	0	2.28
Exp. resonant bkg	0.1	0.06	0.8
Observed events in SR	2	1	0

Limit extracted with modified frequentist method CLs.

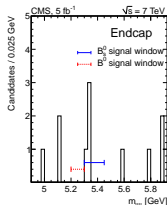
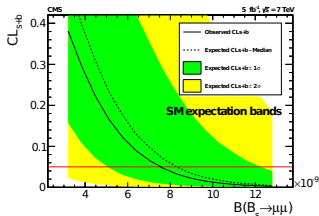
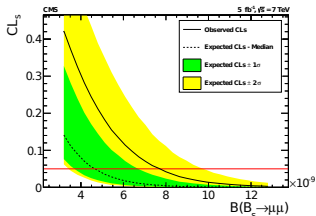
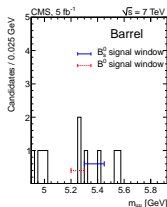
$$\mathcal{L} = \text{Gauss}(\epsilon_{\text{obs}} | \epsilon, \sigma_{\epsilon}) \times \text{Gauss}(R_{\text{obs}}^{\text{bkg}} | R^{\text{bkg}}, \sigma_{R^{\text{bkg}}}) \times \prod_{i=1}^{N_{\text{bin}}} \text{Poisson}(N_i^{\text{obs}} | \epsilon \epsilon_i \text{BR} + N_i^{\text{bkg}} + N_i^{B \rightarrow hh}) \times \text{Poisson}(N_{\text{obs},i}^{\text{bkg}} | R^{\text{bkg}} R_i^{\text{bkg}} N_i^{\text{bkg}}) \times \text{Gauss}(\epsilon_{\text{obs},i} | \epsilon_i, \sigma_{\epsilon_i}).$$



Expected limit at 95% CL (Extracted from unbiased sidebands): 2.3×10^{-8}

Observed limit at 95% CL: 2.2×10^{-8}

Variable	$B^0 \rightarrow \mu^+ \mu^-$ Barrel	$B_s^0 \rightarrow \mu^+ \mu^-$ Barrel	$B^0 \rightarrow \mu^+ \mu^-$ Endcap	$B_s^0 \rightarrow \mu^+ \mu^-$ Endcap
$N_{\text{signal}}^{\text{exp}}$	0.24 ± 0.02	2.70 ± 0.41	0.10 ± 0.01	1.23 ± 0.18
$N_{\text{peak}}^{\text{exp}}$	0.33 ± 0.07	0.18 ± 0.06	0.15 ± 0.03	0.08 ± 0.02
$N_{\text{comb}}^{\text{exp}}$	0.40 ± 0.34	0.59 ± 0.50	0.76 ± 0.35	1.14 ± 0.53
$N_{\text{total}}^{\text{exp}}$	0.97 ± 0.35	3.47 ± 0.65	1.01 ± 0.35	2.45 ± 0.56
N_{obs}	2	2	0	4

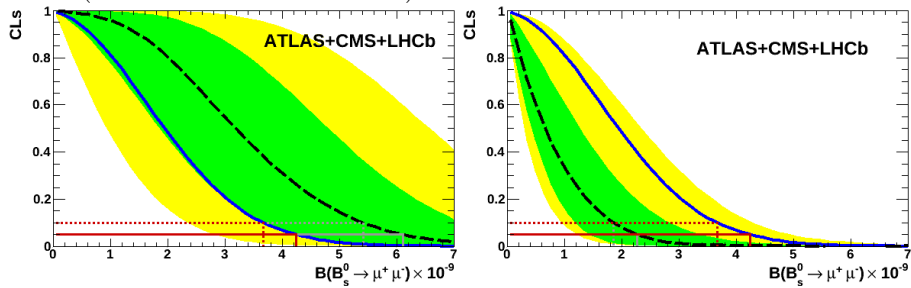


Limit with CLs method:

	Observed	Median expected
$\mathcal{B}(B^0 \rightarrow \mu^+\mu^-)$	$< 7.7 \cdot 10^{-9}$	$< 8.4 \cdot 10^{-9}$
$\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-)$	$< 1.8 \cdot 10^{-9}$	$< 1.6 \cdot 10^{-9}$

LHC Combination

Combination of analysis by the three experiments: ATLAS (2.4fb^{-1}), CMS (5fb^{-1})
LHCb (1fb^{-1} 2011 + 0.037fb^{-1} 2010)

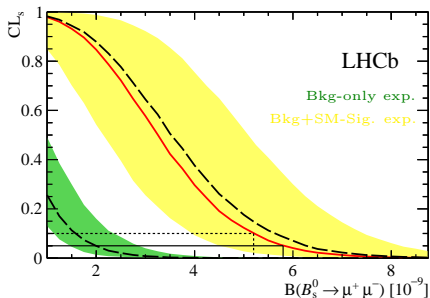


Mode	Limit	ATLAS	CMS	LHCb 2010	LHCb 2011	Combined
$B_s^0 \rightarrow \mu^+ \mu^-$ (10^{-9})	Bkg Only	23	(3.6)	65	3.4	2.3
	Bkg+SM		8.4		7.2	6.1
	Obs	22	7.7 (7.2)	56	4.5	4.2

- Compatible with SM signal within 1σ ($1 - CL_{s+b} = 84\%$)
- P-value bkg-only hypothesis: 5%

ATLAS-CONF-2012-061, CMS-PAS-BPH-12-009, LHCb-CONF-2012-017

LHCb updated results

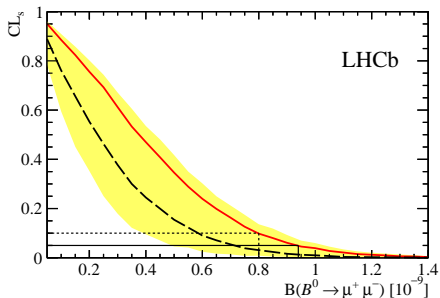


Upper limit at 95% CL	$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)$
Exp. bkg+SM	6.3×10^{-9}
Exp. bkg	2.0×10^{-9}
Observed	5.8×10^{-9}

Compatibility with background p-value ($1-CL_b$) is 5×10^{-4}

Excess of $B_s^0 \rightarrow \mu^+ \mu^-$ events with a significance of 3.5σ .

First evidence of $B_s^0 \rightarrow \mu^+ \mu^-$ decay

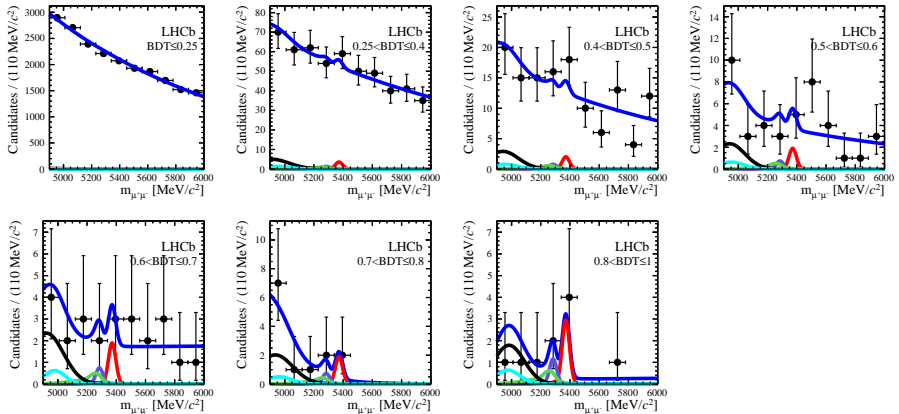


Upper limit at 95% CL	$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-)$
Exp. bkg+SM	7.1×10^{-10}
Exp. bkg	6.0×10^{-10}
Observed	9.4×10^{-10}

LHCb results: full fit to combined dataset

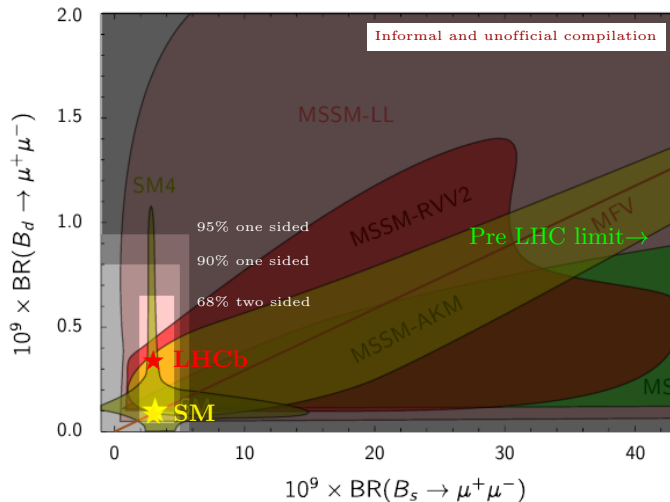
- Simultaneous fit to the two years dataset
- Shared branching ratio parameters

2012 dataset, 7 BDT bins



$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (3.2^{+1.4}_{-1.2}(\text{stat})^{+0.5}_{-0.3}(\text{syst})) \times 10^{-9}$$

The parameter space and outlook

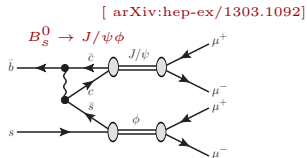


Original figure from D. Straub - *Nuovo Cim.* C035N1 (2012) 249-256

Search for $B_{(s)}^0 \rightarrow \mu^+ \mu^- \mu^+ \mu^-$ decays

Standard Model

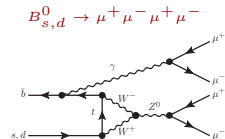
- Main resonant component: $B_s^0 \rightarrow J/\psi \phi$, with J/ψ and ϕ decaying in two muons. [$\mathcal{B} = (2.3 \pm 0.9) \times 10^{-8}$]
- SM non-resonant: $B_{(s)}^0 \rightarrow \mu\mu\gamma(\rightarrow \mu\mu)$
 $\mathcal{B} < 10^{-10}$ [Phys.Rev.D 70 (2004) 114028]



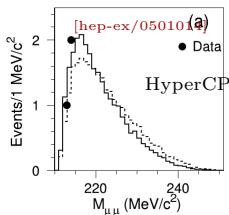
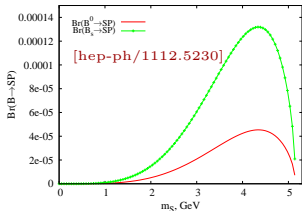
In NP models scalar and pseudoscalar particles can enhance the branching fraction via $B \rightarrow PS$ intermediate states.

In particular it is sensitive to sgoldstino mediated decays

decays in MSSM models.



hypothesized pseudoscalar particle to explain HyperCP evidence in $\Sigma^+ \rightarrow p\mu\mu$ tested.



- Four muons with high IP χ^2 with good vertex ($\chi^2 < 30$)
- Tight muon PID criteria:
 $\varepsilon_\mu = 78.5\%$, $\varepsilon_{\pi \rightarrow \mu} = 1.4\%$
- Resonant component ($m_{\mu\mu} \in [950, 1090]$ and $[3000, 3200]$) excluded and used as control channel
- $N = 5.5 \pm 2.3$ expected $B_s^0 \rightarrow J/\psi\phi$, 7 observed events
- Dominant background: combinatorial
- Peaking backgrounds negligible. Largest one $B \rightarrow \psi(2S)K^*$ with expected yield 0.44 events

Search for $B_{(s)}^0 \rightarrow \mu^+ \mu^- \mu^+ \mu^-$ decays

Normalisation

- $B^0 \rightarrow J/\psi(\rightarrow \mu^+ \mu^-) K^{*0}(\rightarrow K^+ \pi^-)$ with S-wave excluded
- Same selection (apart from PID)

$$\mathcal{B}(B_{(s)}^0 \rightarrow \mu^+ \mu^- \mu^+ \mu^-) = \mathcal{B}(B^0 \rightarrow J/\psi K^{*0}) \frac{f_s}{f_d} \frac{\epsilon_{J/\psi K^*}}{\epsilon_{4\mu}} \frac{N_{B_{(s)}^0 \rightarrow \mu^+ \mu^- \mu^+ \mu^-}}{N_{B^0 \rightarrow J/\psi K^{*0}}} \kappa$$

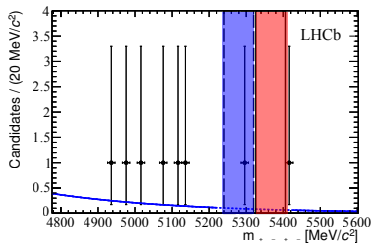
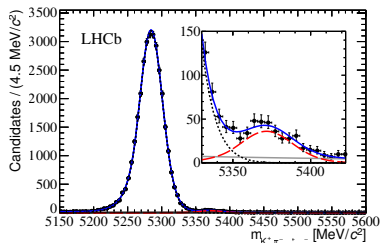
κ is a correction for the S-wave exclusion

Upper limits at 90% (95%) CL for phase space decays:

- $\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^- \mu^+ \mu^-) < 1.2(1.6) \times 10^{-8}$
- $\mathcal{B}(B^0 \rightarrow \mu^+ \mu^- \mu^+ \mu^-) < 5.3(6.6) \times 10^{-9}$

Upper limits at 90% (95%) CL for the MSSM models ($m_{P(S)} = 214.3 \text{ MeV}/c^2 (2.5 \text{ GeV}/c^2)$):

- $\mathcal{B}(B_s^0 \rightarrow SP \rightarrow 4\mu) < 1.2(1.6) \times 10^{-8}$
- $\mathcal{B}(B^0 \rightarrow SP \rightarrow 4\mu) < 5.1(6.6) \times 10^{-9}$



Other rare decay results

- First observation of $B^+ \rightarrow \pi^+ \mu^+ \mu^-$
LHCB-PAPER-2012-020 - JHEP 12 (2012) 125 [[hep-ex/1210.2645](#)]
- Searches for Majorana neutrinos in B^- decays
LHCB-PAPER-2011-038 - Phys. Rev. D 85, 112004 (2012) [[hep-ex/1201.5600](#)]
- Search for the lepton number violating decays $B^+ \rightarrow \pi^- \mu^+ \mu^+$ and $B^+ \rightarrow K^- \mu^+ \mu^+$
LHCB-PAPER-2011-009 - Phys.Rev.Lett. 108 (2012) 101601 [[hep-ex/1110.0730](#)]
- Measurement of the ratio of branching fractions $\mathcal{B}(B^0 \rightarrow K^{*0} \gamma) / \mathcal{B}(B_s^0 \rightarrow \phi \gamma)$ and the direct CP asymmetry in $B^0 \rightarrow K^{*0} \gamma$
LHCb-PAPER-2012-019 - Nucl. Phys. B 867 (2013) 1-18 [[hep-ex/1209.0313](#)]

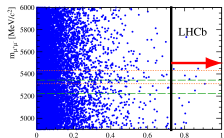
Plus all the $B \rightarrow K^* \mu \mu$ physics will be discussed in the next session.

Conclusions and outlook

- B rare decays are fundamental tools to explore New Physics and to probe its flavour structure
- $B_s^0 \rightarrow \mu^+ \mu^-$ and $B^0 \rightarrow \mu^+ \mu^-$ decays have been searched for 30 years now tightening the space of new physics parameters
- First evidence of $B_s^0 \rightarrow \mu^+ \mu^-$ seen
 - * To be confirmed soon by other experiments and by increased data samples
 - * The precision era is just at the beginning
- All the three experiments are in the process of finalizing their updated analysis
- The playground of rare decays is large and yet to be fully exploited

Additional material

Invariant mass distribution



- Full PDF
- [Phys. Rev. Lett. 110, 021801 (2013)] $B_s^0 \rightarrow \mu^+ \mu^-$
- - - $B^0 \rightarrow \mu^+ \mu^-$
- - - Comb. background
- ⋯ $B_{(s)}^0 \rightarrow h^+ h'^-$
- ⋯ $B^0 \rightarrow \pi^- \mu^+ \nu_\mu$
- · - $B^{0(+)} \rightarrow \pi^{0(+)} \mu^+ \mu^-$

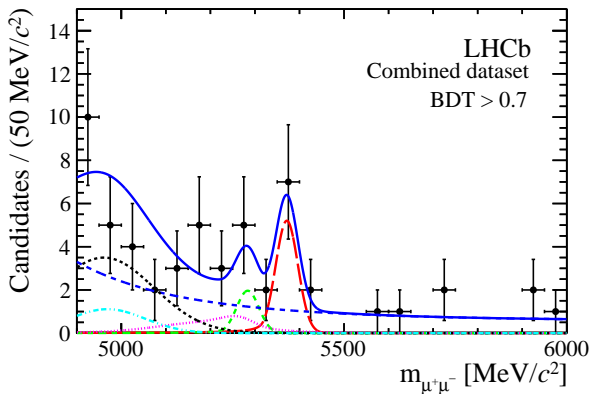


TABLE II. Expected combinatorial background, $B_{(s)}^0 \rightarrow h^+ h'^-$ peaking background, cross-feed, and signal events assuming SM prediction, together with the number of observed candidates in the $B_s^0 \rightarrow \mu^+ \mu^-$ and $B^0 \rightarrow \mu^+ \mu^-$ mass signal regions, in bins of BDT for the 2012 data sample. The quoted errors include statistical and systematic uncertainties.

Mode	BDT bin	0.0 – 0.25	0.25 – 0.4	0.4 – 0.5	0.5 – 0.6	0.6 – 0.7	0.7 – 0.8	0.8 – 1.0
$B_s^0 \rightarrow \mu^+ \mu^-$	Exp. comb. bkg	2345_{-40}^{+40}	$56.7_{-2.9}^{+3.0}$	$13.1_{-1.5}^{+1.4}$	$4.42_{-0.81}^{+0.91}$	$2.10_{-0.56}^{+0.67}$	$0.35_{-0.22}^{+0.42}$	$0.39_{-0.21}^{+0.33}$
	Exp. peak. bkg	$0.250_{-0.068}^{+0.083}$	$0.145_{-0.040}^{+0.049}$	$0.081_{-0.023}^{+0.027}$	$0.075_{-0.020}^{+0.024}$	$0.071_{-0.019}^{+0.023}$	$0.062_{-0.017}^{+0.021}$	$0.104_{-0.028}^{+0.034}$
	Exp. signal	$3.69_{-0.52}^{+0.59}$	$2.14_{-0.33}^{+0.37}$	$1.20_{-0.18}^{+0.21}$	$1.16_{-0.16}^{+0.18}$	$1.17_{-0.16}^{+0.18}$	$1.15_{-0.17}^{+0.19}$	$2.13_{-0.29}^{+0.33}$
	Observed	2274	65	19	5	3	1	3
$B^0 \rightarrow \mu^+ \mu^-$	Exp. comb. bkg	2491_{-42}^{+42}	$59.5_{-3.2}^{+3.3}$	$13.9_{-1.5}^{+1.6}$	$4.74_{-0.89}^{+1.00}$	$2.10_{-0.61}^{+0.74}$	$0.55_{-0.31}^{+0.50}$	$0.29_{-0.19}^{+0.34}$
	Exp. peak. bkg	$1.49_{-0.36}^{+0.50}$	$0.86_{-0.22}^{+0.29}$	$0.48_{-0.12}^{+0.16}$	$0.44_{-0.11}^{+0.15}$	$0.42_{-0.10}^{+0.14}$	$0.369_{-0.093}^{+0.126}$	$0.62_{-0.15}^{+0.21}$
	Exp. cross-feed	$0.627_{-0.091}^{+0.104}$	$0.363_{-0.057}^{+0.066}$	$0.204_{-0.032}^{+0.036}$	$0.197_{-0.027}^{+0.032}$	$0.199_{-0.028}^{+0.032}$	$0.196_{-0.030}^{+0.034}$	$0.362_{-0.051}^{+0.058}$
	Exp. signal	$0.442_{-0.057}^{+0.062}$	$0.256_{-0.036}^{+0.040}$	$0.144_{-0.020}^{+0.022}$	$0.139_{-0.017}^{+0.019}$	$0.140_{-0.018}^{+0.019}$	$0.138_{-0.019}^{+0.021}$	$0.255_{-0.031}^{+0.035}$
Observed	2433	59	19	3	2	2	2	

TABLE III. Expected combinatorial background, $B_{(s)}^0 \rightarrow h^+ h'^-$ peaking background, cross-feed, and signal events assuming SM prediction, together with the number of observed candidates in the $B_s^0 \rightarrow \mu^+ \mu^-$ and $B^0 \rightarrow \mu^+ \mu^-$ mass signal regions, in bins of BDT for the 2011 data sample. The quoted errors include statistical and systematic uncertainties.

Mode	BDT bin	0.0 – 0.25	0.25 – 0.4	0.4 – 0.5	0.5 – 0.6	0.6 – 0.7	0.7 – 0.8	0.8 – 0.9	0.9 – 1.0
$B_s^0 \rightarrow \mu^+ \mu^-$	Exp. comb. bkg	1880_{-33}^{+33}	$55.5_{-2.9}^{+3.0}$	$12.1_{-1.3}^{+1.4}$	$4.16_{-0.79}^{+0.88}$	$1.81_{-0.51}^{+0.62}$	$0.77_{-0.38}^{+0.52}$	$0.47_{-0.36}^{+0.48}$	$0.24_{-0.20}^{+0.44}$
	Exp. peak. bkg	$0.129_{-0.050}^{+0.066}$	$0.066_{-0.019}^{+0.024}$	$0.052_{-0.015}^{+0.018}$	$0.047_{-0.013}^{+0.015}$	$0.053_{-0.014}^{+0.017}$	$0.050_{-0.013}^{+0.016}$	$0.052_{-0.014}^{+0.017}$	$0.042_{-0.014}^{+0.018}$
	Exp. signal	$2.70_{-0.80}^{+0.81}$	$1.30_{-0.23}^{+0.27}$	$1.03_{-0.17}^{+0.20}$	$0.92_{-0.13}^{+0.15}$	$1.06_{-0.15}^{+0.17}$	$1.10_{-0.15}^{+0.17}$	$1.26_{-0.17}^{+0.20}$	$1.31_{-0.25}^{+0.28}$
	Observed	1818	39	12	6	1	2	1	1
$B^0 \rightarrow \mu^+ \mu^-$	Exp. comb. bkg	1995_{-34}^{+34}	$59.2_{-3.2}^{+3.3}$	$12.6_{-1.5}^{+1.6}$	$4.44_{-0.86}^{+0.99}$	$1.67_{-0.54}^{+0.66}$	$0.75_{-0.40}^{+0.58}$	$0.44_{-0.38}^{+0.57}$	$0.22_{-0.20}^{+0.48}$
	Exp. peak. bkg	$0.78_{-0.29}^{+0.38}$	$0.40_{-0.10}^{+0.14}$	$0.311_{-0.079}^{+0.107}$	$0.280_{-0.068}^{+0.092}$	$0.314_{-0.076}^{+0.103}$	$0.297_{-0.071}^{+0.096}$	$0.309_{-0.073}^{+0.101}$	$0.296_{-0.079}^{+0.107}$
	Exp. cross-feed	$0.43_{-0.13}^{+0.13}$	$0.205_{-0.037}^{+0.044}$	$0.163_{-0.027}^{+0.032}$	$0.145_{-0.021}^{+0.025}$	$0.168_{-0.025}^{+0.029}$	$0.174_{-0.024}^{+0.029}$	$0.199_{-0.029}^{+0.033}$	$0.206_{-0.040}^{+0.046}$
	Exp. signal	$0.328_{-0.097}^{+0.096}$	$0.158_{-0.027}^{+0.030}$	$0.125_{-0.019}^{+0.022}$	$0.112_{-0.015}^{+0.016}$	$0.129_{-0.017}^{+0.019}$	$0.134_{-0.016}^{+0.019}$	$0.153_{-0.019}^{+0.022}$	$0.159_{-0.029}^{+0.032}$
Observed	1904	50	20	5	2	1	4	1	