

CP Violation and Rare Decays in the Charm System at LHCb

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The Charm system provides good tools to seek NP...

■ **SM: CPV is very small, Rare Decays are very rare**

- *Charm decays are essentially a two-family story: no CPV at first order*
- *FCNC's that provide higher order effects are very suppressed by GIM*

■ **This offers a list of 'surprises' that could sign the presence of NP**

- *CPV at $O(1\%)$ in the mixing or in certain decays*
- *Rare decays with a branching ratio $O(10^{-9}-10^{-8})$*
- *Bonus: charm involve up-type quark FCNC, thus NP couplings hardly tested with B, K*

■ **LHCb aims at a thorough exploration. In this talk:**

- *Charm mixing: x' & y' with WS $D^0 \rightarrow K^+ \pi^-$ decays*
- *CP violation: $D \rightarrow K^+ K^-$, $\pi^+ \pi^-$, $K^+ K^- \pi^+$, $\pi^+ \pi^- \pi^+ \pi^-$*
- *Rare decays: $D \rightarrow \mu^+ \mu^-$, $D \rightarrow \pi^+ \mu^+ \mu^-$*

2010/2011 data

$\sim 1 \text{ fb}^{-1}$

■ Huge b and c production in high E p-p collisions

- @ $\sqrt{s}=7$ TeV: $\sigma(pp \rightarrow b\bar{b}+X) = (284 \pm 20 \pm 49) \mu\text{b}$ [1]

$\sigma(pp \rightarrow c\bar{c}+X) = (6100 \pm 930) \mu\text{b}$ [2]

→ $\sim 10^{12}$ $c\bar{c}$ pairs per fb^{-1} in LHCb's acceptance. 3 fb^{-1} collected so far !

■ LHCb is optimized for Flavor Physics in a hadronic environment.

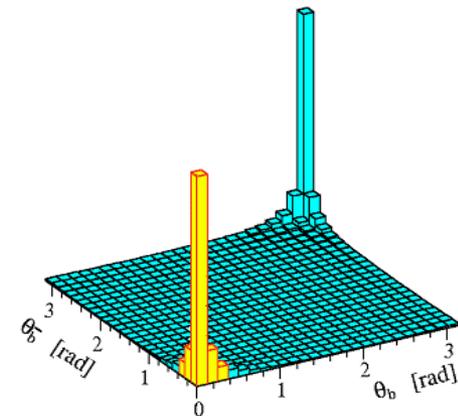
- Forward detector, performant vertexing, p and M reconstruction, particle-ID

- Very selective, polyvalent and configurable trigger:

- 1 hardware trigger (L0) followed by 2 software triggers (HLT1-2)

L0: ~ 15 MHz → 1 MHz

HLT: ~ 1 MHz to ~ 3 kHz (4.5 kHz) with ~ 1 kHz (2 kHz) for charm in 2011 (2012)

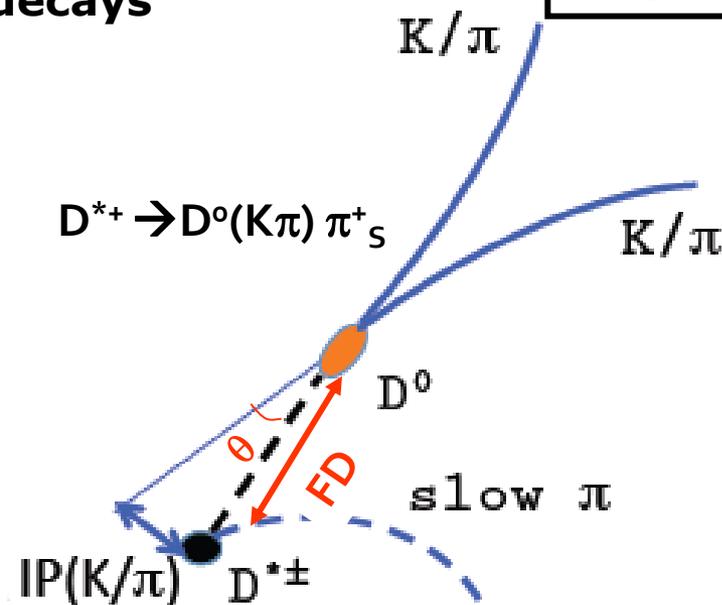


P, PT, IP,
PID,
cosθ, FD

S/B

■ All selections use typical features of D decays

- $D \rightarrow hh(h)$: *Cut based selection*
(low multiplicity, high BF's, low peaking BKG)
- $D \rightarrow hhhh$: *Multivariate analysis*
(high multiplicity so large BKG)
- *Rare decays: Multivariate analysis + PID*
(large combinatorial and peaking BKG,
Ex: $B(D^0 \rightarrow \pi^+ \pi^-) > 10^6 B(D \rightarrow \mu\mu)$)

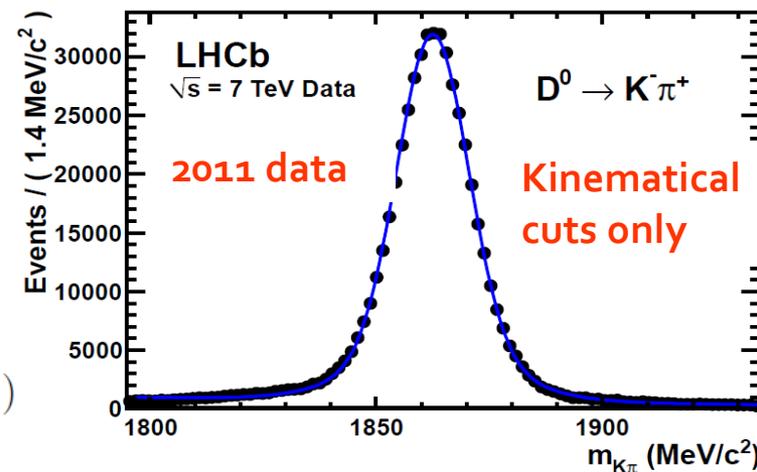


Reliable Meas't

■ Control modes and normalization

- Huge data samples of $D^0 \rightarrow K^- \pi^+$, $B \rightarrow J\psi(\mu\mu)X, \dots$ to determine tracking and PID efficiencies from data
- Modes similar to the signal with a larger and known BF to further minimize systematics.

$$\mathcal{B}(D^0 \rightarrow \mu^+ \mu^-) = \frac{N_{D^{*+} \rightarrow D^0(\rightarrow \mu^+ \mu^-) \pi^+} \varepsilon_{\pi\pi}}{N_{D^{*+} \rightarrow D^0(\rightarrow \pi^+ \pi^-) \pi^+} \varepsilon_{\mu\mu}} \cdot \mathcal{B}(D^0 \rightarrow \pi^+ \pi^-)$$



Charm Mixing

- Effective Hamiltonian that allows to focus on time evolution in $\{|D^0\rangle, |\bar{D}^0\rangle\}$ basis, but also accounts for its decay (non hermitian)

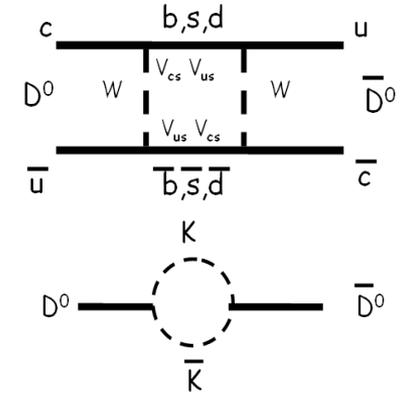
$$i\frac{\partial}{\partial t} \begin{pmatrix} D^0(t) \\ \bar{D}^0(t) \end{pmatrix} = \left(\mathbf{M} - \frac{i}{2}\mathbf{\Gamma} \right) \begin{pmatrix} D^0(t) \\ \bar{D}^0(t) \end{pmatrix}$$

Physical states

$$\begin{aligned} |D_1\rangle &= p|D^0\rangle + q|\bar{D}^0\rangle \\ |D_2\rangle &= p|D^0\rangle - q|\bar{D}^0\rangle \end{aligned}$$

Flavor states

$$\begin{aligned} |D^0(t)\rangle &= g_+(t)|D^0\rangle + \frac{q}{p}g_-(t)|\bar{D}^0\rangle \\ |\bar{D}^0(t)\rangle &= g_+(t)|\bar{D}^0\rangle + \frac{p}{q}g_-(t)|D^0\rangle \end{aligned}$$



- Physical states eigenvalues rule ($\mathbf{M}_{1,2} \pm i\mathbf{\Gamma}_{1,2}$) the mixing time evolution. $|g_{\pm}(t)|^2$ can be written in terms of x and y

$$x \equiv \frac{\Delta M}{\Gamma}, \quad \Delta M \equiv M_1 - M_2$$

$$y \equiv \frac{\Delta \Gamma}{2\Gamma}, \quad \Delta \Gamma \equiv \Gamma_1 - \Gamma_2$$

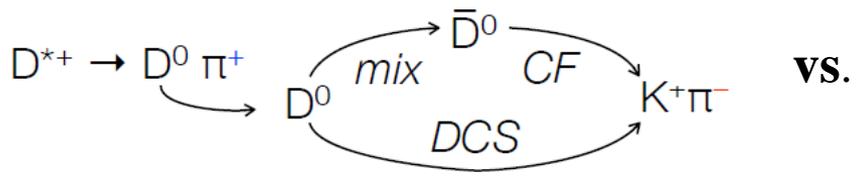
- Hard to predict. Expected small in SM (GIM suppr.): $x, y \sim 0.1$ to 1%
 - B-factories and FNAL: strong evidence that mixing exists.
 - CPV in this mixing still to be discovered: good probe for NP.

LHCb with 1fb^{-1} : observe mixing at $>5\sigma$ with one single measurement

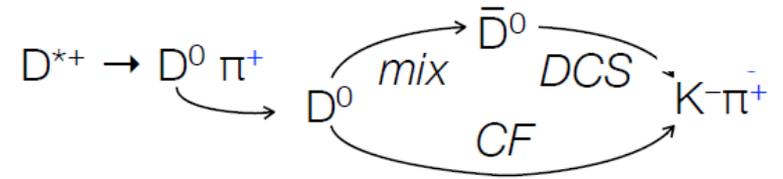
LHCb with 3fb^{-1} : search for CPV in mixing

Time dependent $D^0 \rightarrow K\pi$ WS/RS ratio

Wrong Sign events (WS)



Right Sign events (RS)



$$\rightarrow R(t) = \frac{N_{WS}(t)}{N_{RS}(t)} = R_D + \sqrt{R_D} y' t + \frac{x'^2 + y'^2}{4} t^2$$

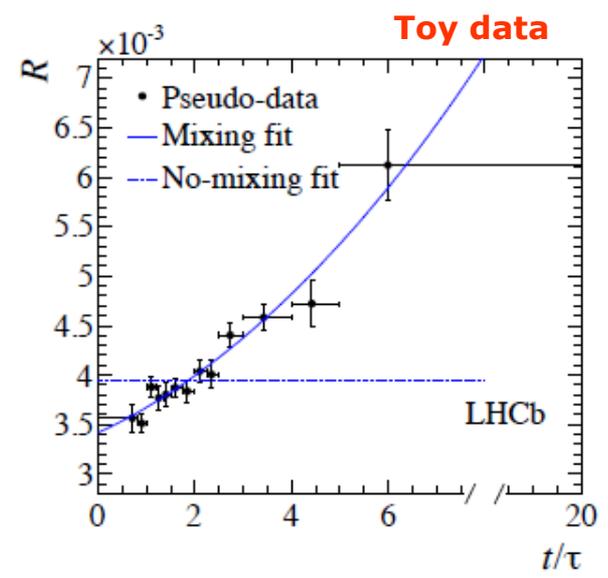
Assuming x, y small and no CPV

$$\begin{aligned} x' &= x \cos \delta + y \sin \delta \\ y' &= y \cos \delta - x \sin \delta \end{aligned}$$

Count decays in 13 bins of decay time to get

$$R_i = N(D^0 \rightarrow K^+ \pi^- + \bar{D}^0 \rightarrow K^+ \pi^-)_i / N(D^0 \rightarrow K^- \pi^+ + \bar{D}^0 \rightarrow K^- \pi^+)_i$$

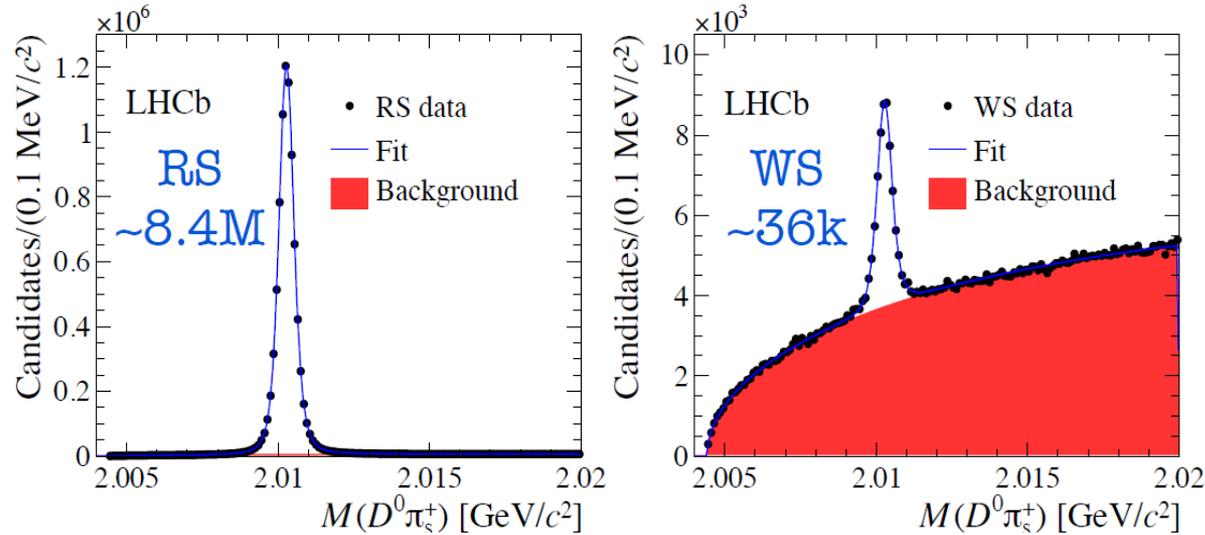
χ^2 fit of $R(t)$ this to these data points



Time dependent $D^0 \rightarrow K\pi$ WS/RS ratio

- Exploit $D^* \rightarrow D^0 \pi_s$ to tell D^0 from \bar{D}^0 , maximize S/B, extract $N(D \rightarrow K\pi)$'s

Time integrated yields



Clean signature

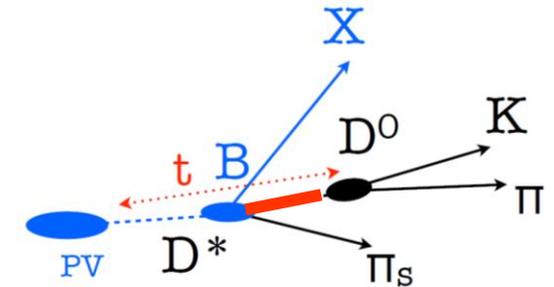
- $\sigma M(D^0 \pi_s) \sim \sigma p(\pi_s)$
- $\sigma M(D^0 \pi_s) < 1 \text{ MeV}$ thanks to a kinematical fit forcing to come from the Primary Vertex.

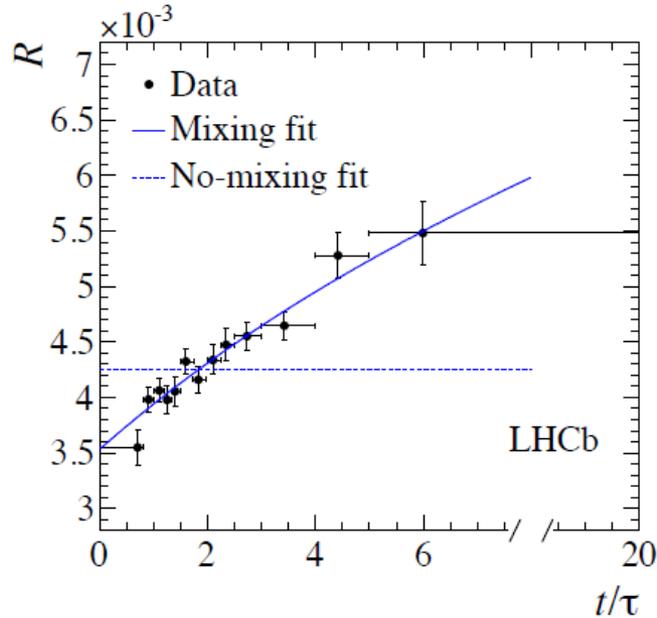
Large yields

- 4110 (949000) WS(RS) in bin 5
- 910 (165200) WS(RS) in bin 13

Systematic uncertainties mostly cancel in the ratio.
Remaining biases on R_i are included in the fit.

- D^0 from B decays (t wrong since B is long lived)
- Double mis-ID: $D^0 \rightarrow K^- \pi^+$ (RS) seen as $D^0 \rightarrow K^+ \pi^-$ (WS)



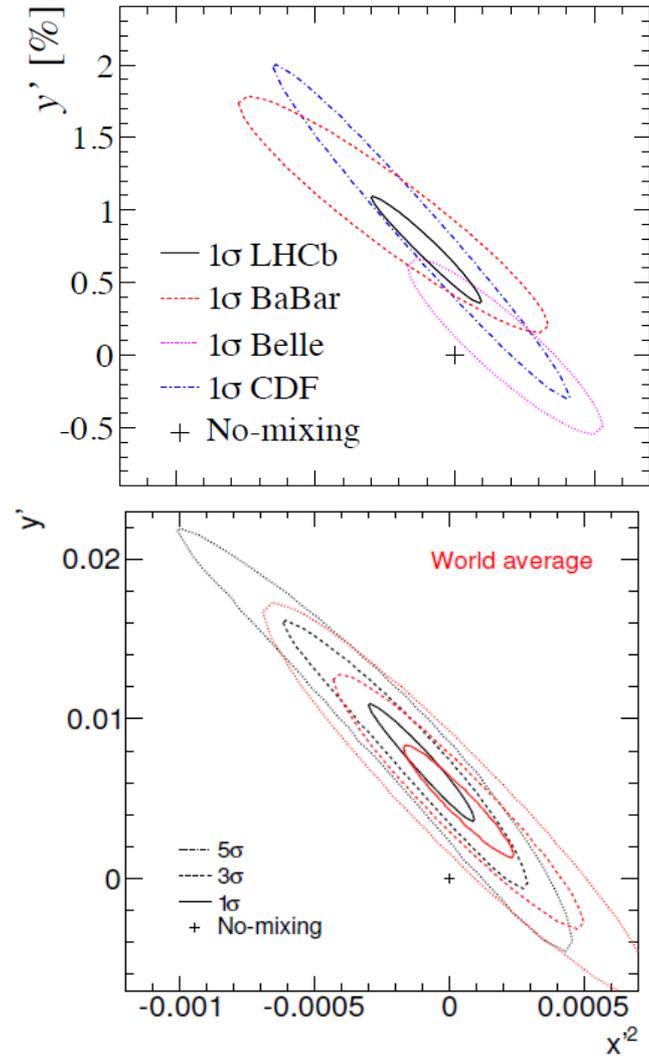
1 fb⁻¹, 2011 data

$$x'^2 = (-0.09 \pm 0.13) \times 10^{-3}$$

$$y' = (7.2 \pm 2.4) \times 10^{-3}$$

Systematic uncertainties:

10% of $\sigma_{y'}$; 11% of $\sigma_{x'^2}$



Mixing established at 9.1 σ ! 1st individual measurement > 5 σ

CPV in 2-body Charm Decays

$$\Delta A_{CP} = A_{CP}(D^0 \rightarrow K^+ K^-) - A_{CP}(D^0 \rightarrow \pi^+ \pi^-)$$

■ CPV we're after: $\sim 1\%$ at most.

→ Difficulty: Production and detection asymmetries can reach 1%.

Measure:
$$A_{raw}(f) = \frac{N(D^{*+} \rightarrow D^0(f)\pi_s^+) - N(D^{*-} \rightarrow \bar{D}^0(\bar{f})\pi_s^-)}{N(D^{*+} \rightarrow D^0(f)\pi_s^+) + N(D^{*-} \rightarrow \bar{D}^0(\bar{f})\pi_s^-)}$$

- First order Taylor Expansion:

$$A_{RAW}(f)^* = A_{CP}(f) + A_D(f) + A_D(\pi_s) + A_P(D^{*+})$$

Wanted Physics CP asymmetry

Detection asymmetry of D

Detection asymmetry of the slow pion

Production asymmetry

$$A_{CP}(f) = \frac{\Gamma(D^0 \rightarrow f) - \Gamma(\bar{D}^0 \rightarrow f)}{\Gamma(D^0 \rightarrow f) + \Gamma(\bar{D}^0 \rightarrow f)}$$

When $f = \pi^+ \pi^-$ or $K^+ K^-$: no detection asymmetry between D and \bar{D}
 $\rightarrow A_D(f) = 0$

Similar for $f = \pi^+ \pi^-$ and $K^+ K^-$
 $(D^*$ and π_s production/detection \sim independent of D^0 f -state)

$$\Delta A_{RAW} = A_{RAW}(K^+ K^-) - A_{RAW}(\pi^+ \pi^-) = \Delta A_{CP}$$

$$\Delta A_{CP} = A_{CP}(D^0 \rightarrow K^+ K^-) - A_{CP}(D^0 \rightarrow \pi^+ \pi^-)$$

0.6 fb⁻¹

Phys.Rev.Lett. 108 (2012) 111602

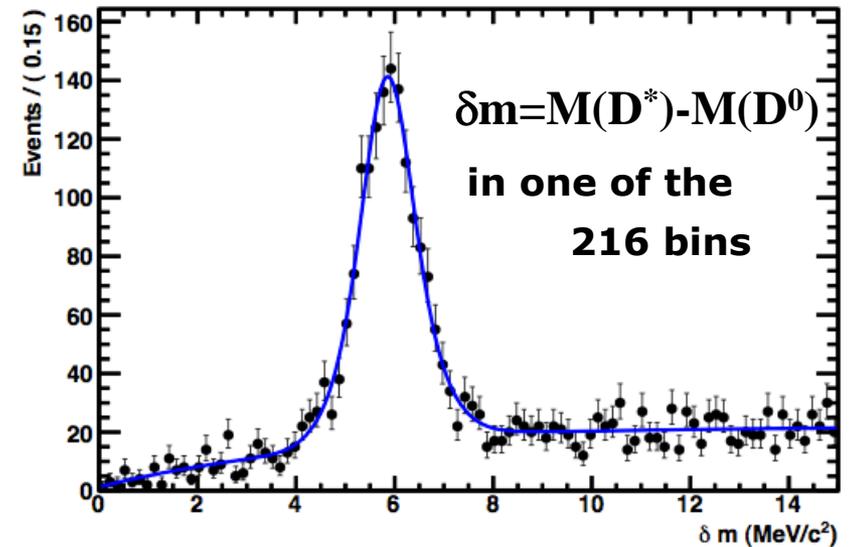
■ **Fit to δm distributions in 216 bins**

54 bins in $P_{T,D^*} \times \eta_{D^*} \times P_{slow\pi} \times left/right$

$\times 2$ Mag Up / Mag Down

$\times 2$ Before/After an LHC technical stop

→ **A_{RAW} and ΔA_{RAW} in each bin,**
then weighted average



$$\Delta A_{CP} = (-0.82 \pm 0.21_{stat} \pm 0.11)\%$$

($\chi^2 / \text{NDF} = 211/215$)

3.5 σ from no CPV.

World average (HFAG)

$$\Delta A_{CP}^{dir} = (-0.678 \pm 0.147)\%$$

CP Violation across the Dalitz Space

$$\mathbf{D^+ \rightarrow K^- K^+ \pi^+}$$

$$\mathbf{D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-}$$

Model independent search for CPV (Miranda Approach)

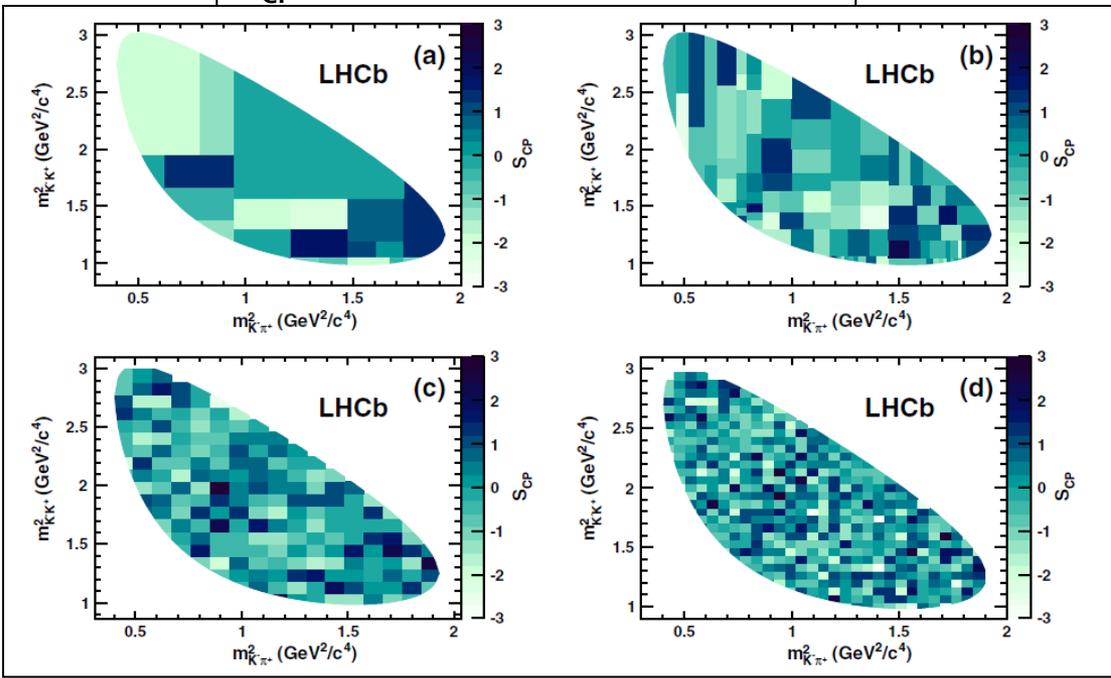
- Look for **local** asymmetries across Dalitz Plots.

$$\chi^2 = \sum_{i=1}^{N_{bins}} \left(S_{CP}^i \right)^2 \quad S_{CP}^i = \frac{N^i(D^+) - \alpha N^i(D^-)}{\sqrt{N^i(D^+) + \alpha^2 N^i(D^-)}}, \quad \alpha = \frac{N_{tot}(D^+)}{N_{tot}(D^-)}$$

- Sensitivity to a given CPV scenario depends on the binning: try several !
- Check detection asymmetries: compute χ^2 for non CPV control modes.

- First application of this method: $D^+ \rightarrow K^- K^+ \pi^+$ with 2010 data (35 pb⁻¹)**

S_{CP} across the DP for $D^+ \rightarrow K^+ K^- \pi^+$



Control modes: $D_S \rightarrow K^- K^+ \pi^+$, $D^+ \rightarrow K^- \pi^+ \pi^+$

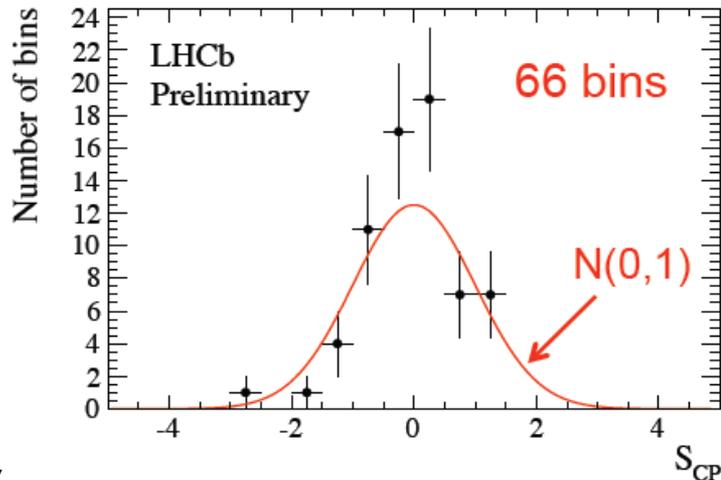
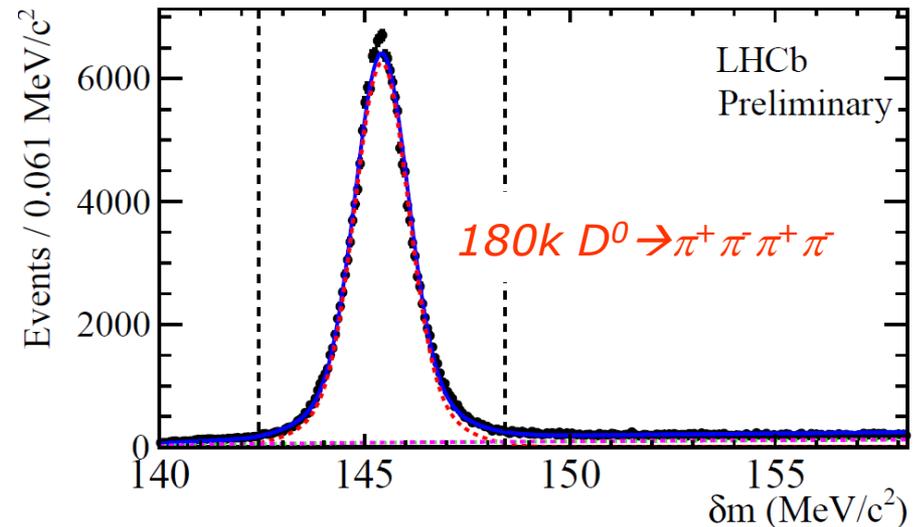
Binning	<i>p</i> -value (%)
Adaptive I	12.7
Adaptive II	10.6
Uniform I	82.1
Uniform II	60.5

No evidence for CPV !

PHYSICAL REVIEW D 84, 112008 (2011)

Model independent search for CPV: $D^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-$

- **High multiplicity causes large background: selection uses a NN.**
- **Control mode: $1.3\text{M } D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$**
- **4-body: S_{CP}^i measured in bins of a 5D Dalitz Plot.**
- **Tries 3 different binnings.**



1 fb⁻¹, LHCb-CONF-2012-019

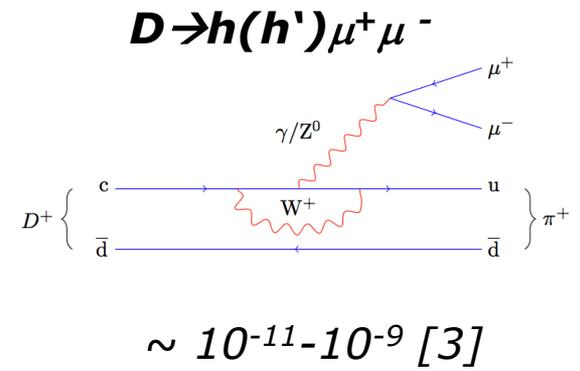
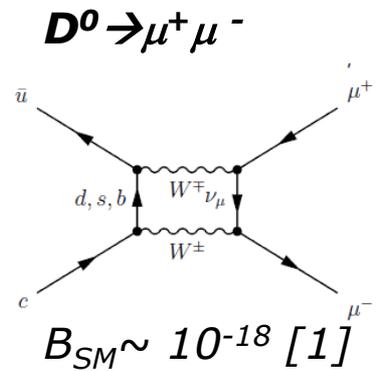
Bins	p-values (%)
15	97.1
29	95.6
66	99.8

→ No evidence for CPV

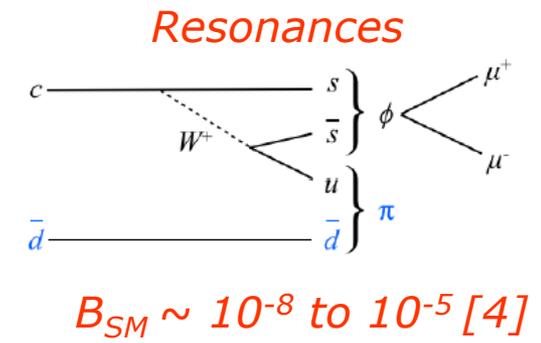
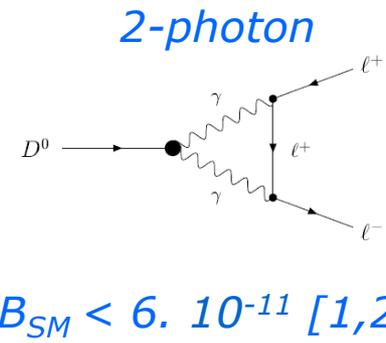
Rare decays

Motivations

- SD contributions are good tools to probe NP (very strong GIM suppression)

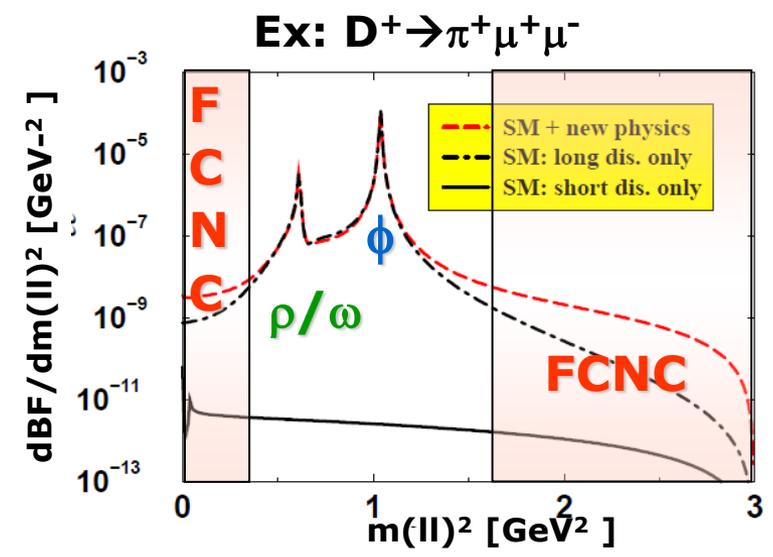


- Branching ratios dominated by LD effects, via intermediate states



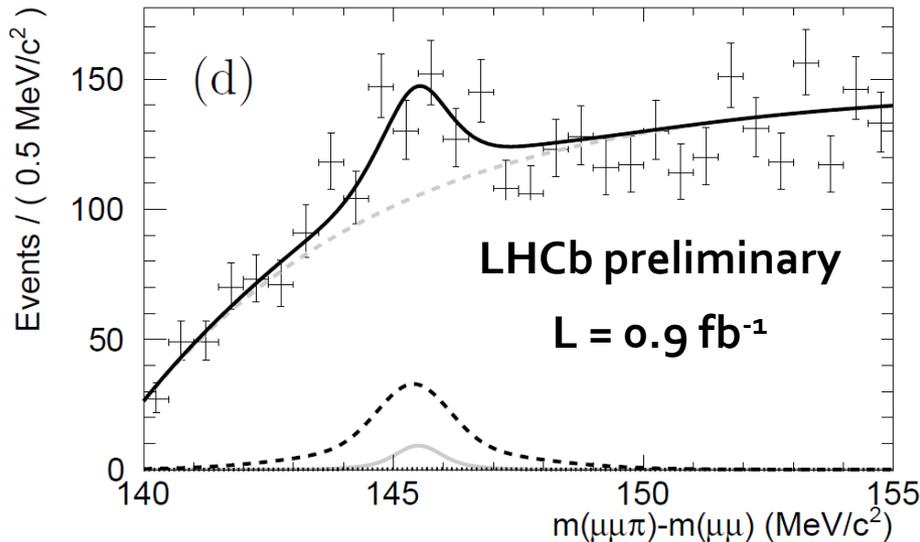
- NP might change the picture, making the SD contribution measurable

- Via the total BF: $D^0 \rightarrow \mu\mu$ [5]
- Via partial BF's or asymmetries (CP, FB, ...)
- to avoid LD contributions: $D \rightarrow h(h') \mu^+ \mu^-$ [6]



Measurement relative to the D⁰ → ππ channel

$$\mathcal{B}(D^0 \rightarrow \mu^+ \mu^-) = \frac{N_{D^{*+} \rightarrow D^0(\rightarrow \mu^+ \mu^-) \pi^+} \varepsilon_{\pi\pi}}{N_{D^{*+} \rightarrow D^0(\rightarrow \pi^+ \pi^-) \pi^+} \varepsilon_{\mu\mu}} \cdot \mathcal{B}(D^0 \rightarrow \pi^+ \pi^-)$$



— Signal

- - - - Comb. background:

- - - - Peaking backgrounds: D⁰ → π⁺π⁻

- Reduced using Muon ID.

- Yield floated in this fit within limits determined from MC + D → Kπ control sample to determine π ↔ μ misID rate

→ $\mathcal{B}(D^0 \rightarrow \mu^+ \mu^-) < 1.3 (1.1) \cdot 10^{-8}$ at 95 (90)%CL

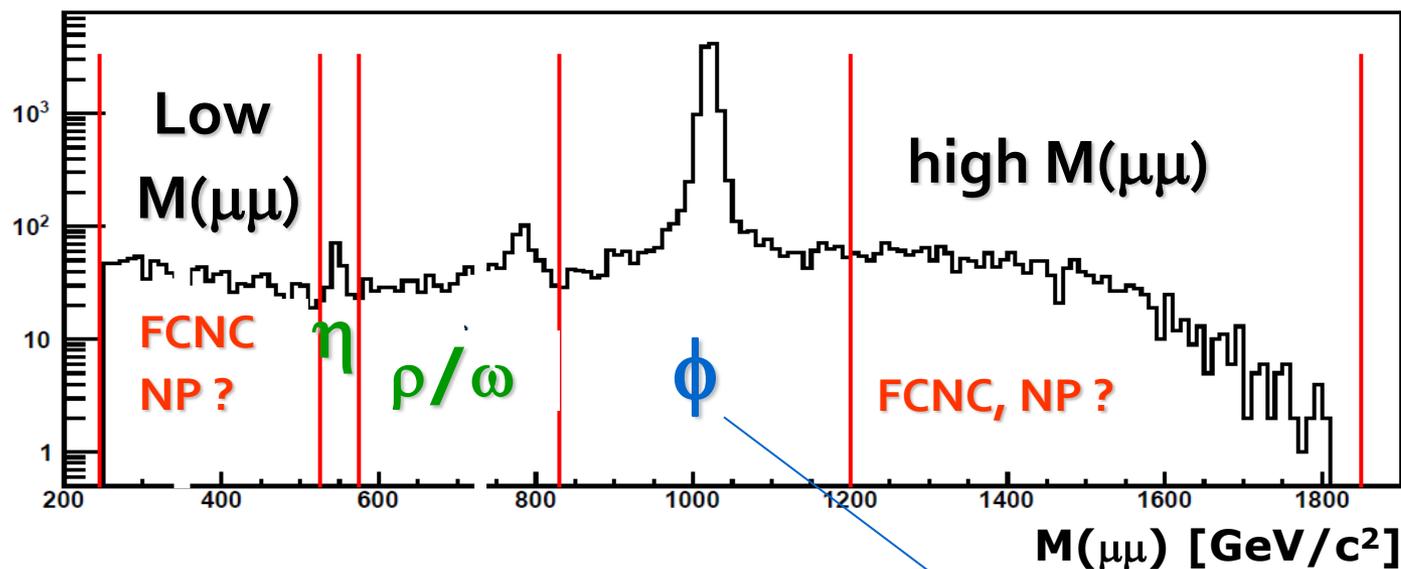
CERN-LHCb-CONF-2012-005

→ ~10 times better than Belle's limit.

(Phys. Rev. D81 (2010) 091102, arXiv:1003.2345)

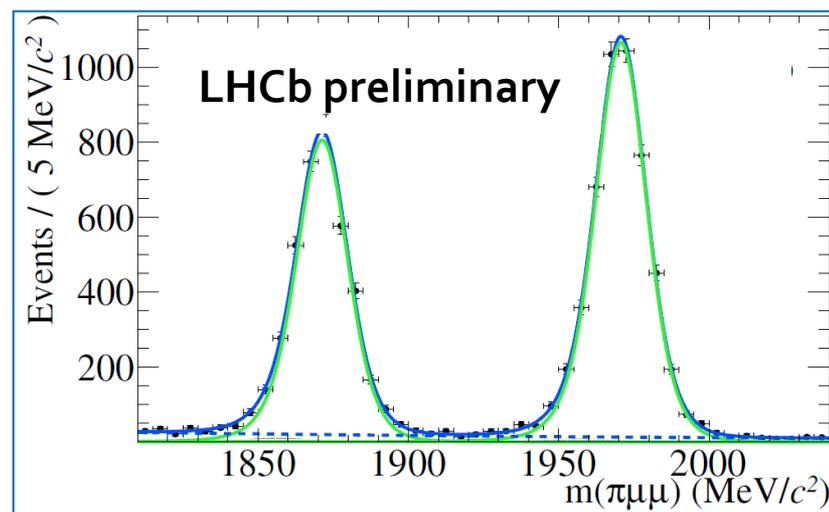
→ Still orders of magnitude above SM,
paper with improved analysis in preparation

5 regions of the dimuon spectrum studied simultaneously



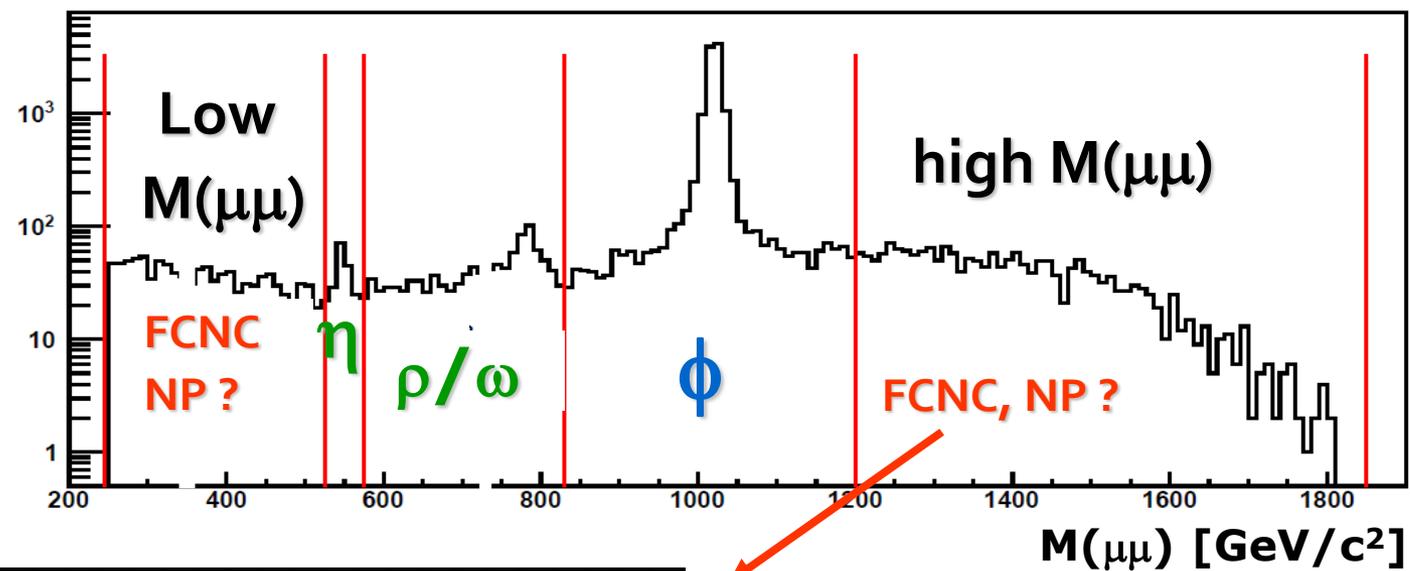
■ $D^+_{(s)} \rightarrow \pi^+ \phi(\mu^+ \mu^-)$ used as **Standard Candles**

- Normalization mode: minimize $\sigma(\text{syst})$ since the final state is the same as the signal.
- Signal proxy to optimize the selection (BDT + muon ID) and help the fit (provides signal shape)
- The error on their BF is the dominant systematic uncertainty in this analysis

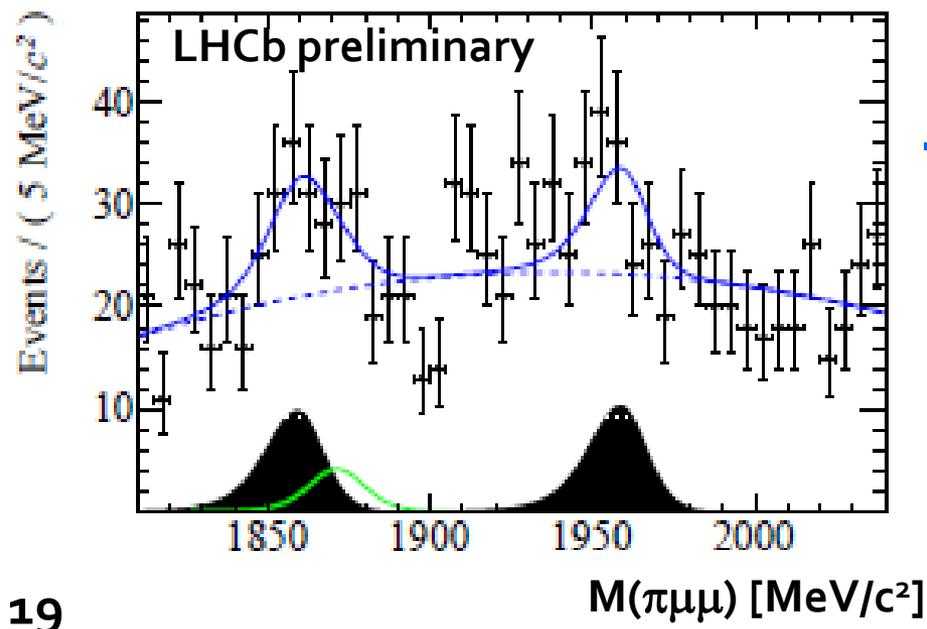


Search for $D^+_{(s)} \rightarrow \pi^+ \mu^+ \mu^-$ decays

5 regions of the dimuon spectrum studied simultaneously



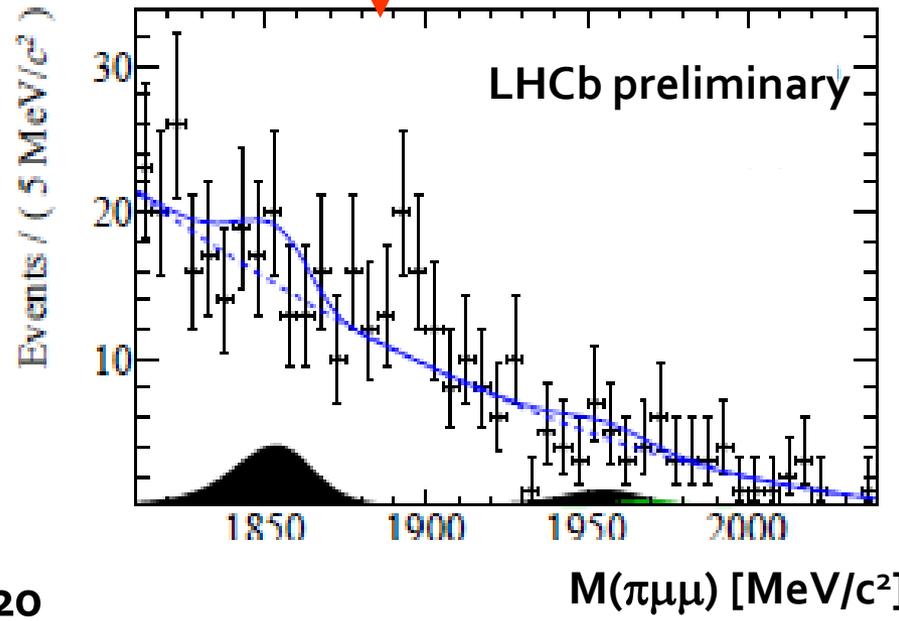
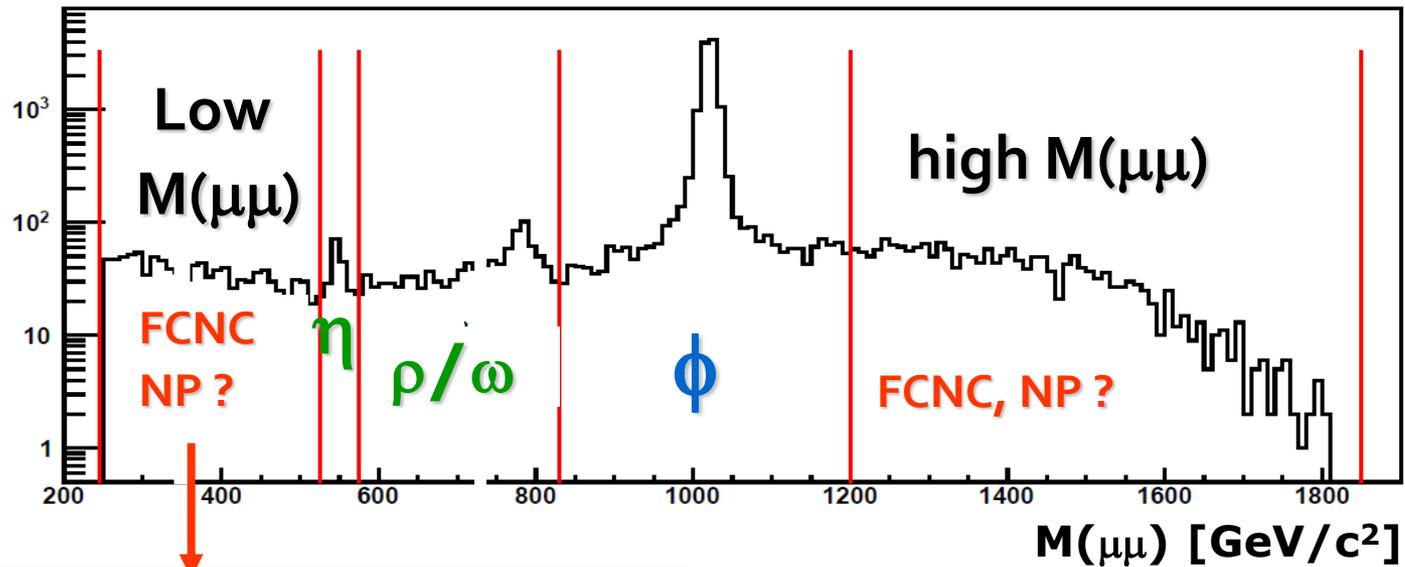
NEW!



- **Signal**
- - - **Comb. background:**
- **Peaking backgrounds: $D^+_{(s)} \rightarrow \pi^+ \pi^+ \pi^-$**
- Shapes determined by loosening muon ID
- Then the fit is able to determine the yields

Search for $D^+_{(s)} \rightarrow \pi^+ \mu^+ \mu^-$ decays

5 regions of the dimuon spectrum studied simultaneously



- **Signal**
- - - **Comb. background:**
- **Peaking backgrounds: $D^+_{(s)} \rightarrow \pi^+ \pi^+ \pi^-$**
- *Shapes determined by loosening muon ID*
- *Then the fit is able to determine the yields*

Upper limits $\times 10^{-8}$ @ 90% (95%) C.L.

Region	$B(D^+ \rightarrow \pi^+ \mu^+ \mu^-)$	$B(D_s \rightarrow \pi^+ \mu^+ \mu^-)$
Low $M(\mu\mu)$	2.0 (2.5)	6.9 (7.7)
High $M(\mu\mu)$	2.6 (2.9)	16.0 (18.6)
Total ⁽¹⁾	7.3 (8.3)	41.0 (47.7)

NEW!

(1) Total non resonant BF, extrapolated from the high $M(\mu\mu)$ region (phase space model).

Conclusion: - Limits of the order of a few 10^{-8} (10^{-7}) for D^+ (D_s) decays.

- 50 to 100 times better than before (D_0 , Babar).

(V. Abazov et al., Phys.Rev. Lett. 100 (2008) 101801, arXiv:0708.2094 ;
J. Lees et al., Phys.Rev. D84 (2011) 072006, arXiv:1107.4465)

- Still above largest theory predictions ($\sim 10^{-8}$).

- **Same approach as for $D^+_{(s)} \rightarrow \pi^+ \mu^+ \mu^-$ with 4 regions in $M(\mu\mu)$:**

(if mediated by a Majorana neutrino, larger significance in region where its mass peaks)

1 fb⁻¹

Upper limits $\times 10^{-8}$ @ 90% (95%) C.L.

Region [MeV/c ²]	$B(D^+ \rightarrow \pi^- \mu^+ \mu^+)$	$B(D^+_s \rightarrow \pi^- \mu^+ \mu^+)$
$250 < M(\mu\mu) < 1140$	1.4 (1.7)	6.2 (7.6)
$1140 < M(\mu\mu) < 1340$	1.1 (1.3)	4.4 (5.3)
$1340 < M(\mu\mu) < 1540$	1.3 (1.5)	6.0 (7.3)
$1540 < M(\mu\mu)$	1.3 (1.5)	7.5 (8.7)
Total	2.2 (2.5)	12.0 (14.1)

NEW!

- Conclusion:**
- No sign of LNV
 - Limits of the order of a few 10^{-8} (10^{-7}) for D^+ (D^+_s) decays.
 - **100 times better than before (Babar).**

(J. Lees et al., Phys.Rev. D84 (2011) 072006, arXiv:1107.4465)

- **LHCb has a copious Charm Physics program**
- **A good start with 2010/2011 data:**
 - *First evidence for Charm mixing in a single measurement*
 - *Intriguing $\Delta A_{CP}(KK/\pi\pi)$*
 - *3 body and 4 body Dalitz Analyses.*
 - *Limits on rare decays ($D \rightarrow (\pi)\mu\mu$) improved by two orders of magnitude*

And many on-going analyses

- *New rare decays: $D^+_{(S)} \rightarrow K^+ \mu^+ \mu^-$, $D^0 \rightarrow K^- K^+ \mu^+ \mu^-$, $D^0 \rightarrow K \pi \mu^+ \mu^-$*
- *WS/RS mixing including search for CPV*
- *$A_{CP}(D^+ \rightarrow \phi \pi^+ - D^0 \rightarrow K_S \pi^+)$*
- *T-odd asymmetry with $D^0 \rightarrow K^- K^+ \pi^- \pi^+$*
- *Mixing with $D^0 \rightarrow K_S hh$*
- *Λ_c decays*
- *...*

Back-up I

References on Rare decays

[1] G. Burdman et al, *Phys. Rev. D*66 (2002) 014009, *hep-ph/0112235*

[2] BABAR Collaboration Collaboration, *arXiv:1110.6480*

[3] S. Fajfer et al, *Phys. Rev. D*64 (2001) 114009, *hep-ph/0106333* ;

*Phys. Rev. D*76 (2007),074010, *arXiv0706.1133*;

M. Artuso et al., *Eur. Phys. J. C*57 (2008) 309, *arXiv:0801.1833* ;

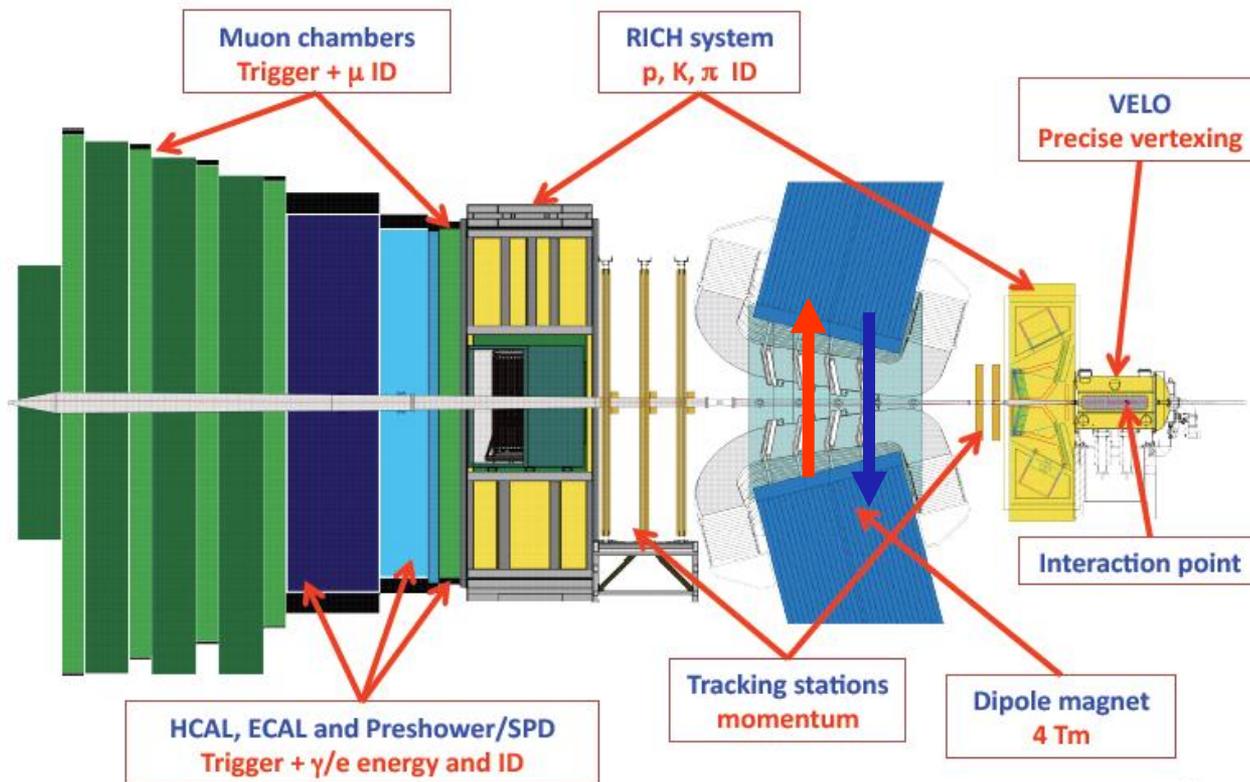
L. Cappiello et al., *arXiv:1209.4235v1*

[4] Particle Data Group.

[5] E. Golowich et al, *Phys. Rev. D*79 (2009) 11030, *arXiv:0903.2830*

[6] S. Fajfer et al, *arXiv:1208.0759v2*;

L. Cappiello et al., *arXiv:1209.4235v1*



*B-field polarity
can be reversed:
Up or **Down***

■ Typical Performance

- *Charged tracks momentum: $\sigma p/p = 0.35-0.55\%$, $\sigma m = 10-20 \text{ MeV}/c^2$*
- *ECAL: $\sigma E/E = 10\%/\sqrt{E} \oplus 1\%$ (E in GeV)*
- *muon-ID $\varepsilon(\mu \rightarrow \mu) \sim 95\%$, mis-ID rate ($\pi \rightarrow \mu$) $\sim 1\%$*
- *K- π separation $\varepsilon(K \rightarrow K) \sim 95\%$, mis-ID rate ($\pi \rightarrow K$) $\sim 10\%$*
- *Proper time: $\sigma_t \sim 30-50 \text{ fs}$, $\sigma_z \sim 60 \mu\text{m}$ (Prim. Vtx) $\sigma_z \sim 150 \mu\text{m}$ (Secondary Vtx)*

Charm Measurements @ LHCb: typical ingredients

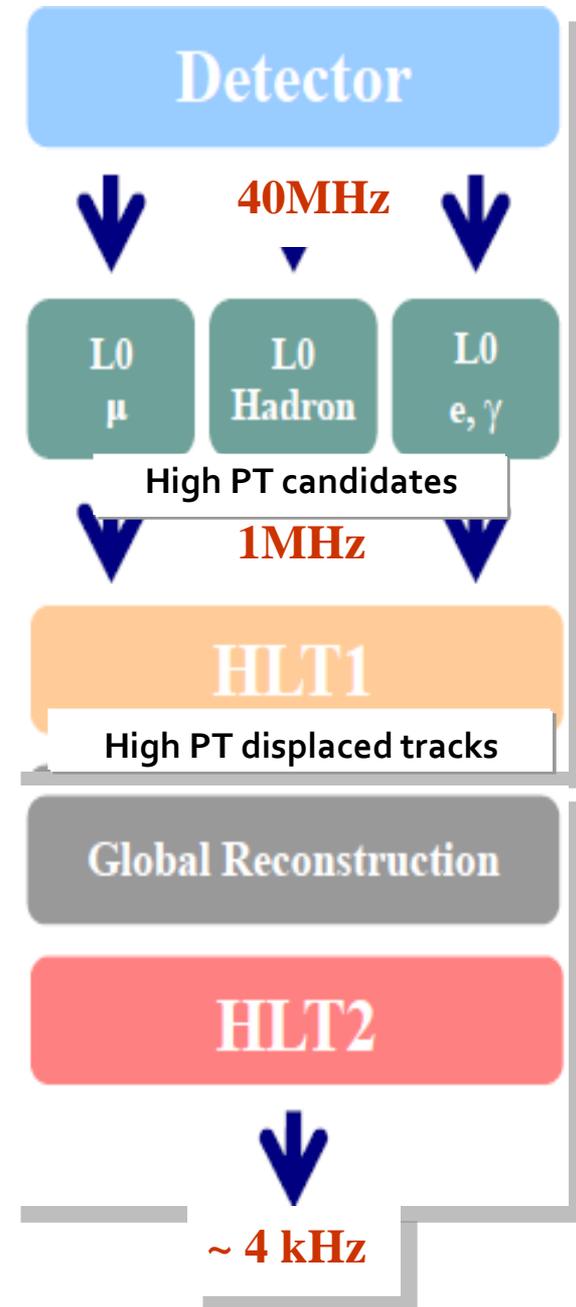
Get data

■ Trigger: too much data for generic selection

- Each (group of) mode(s): a dedicated 'line' in HLT2
- Line = a selection, can be close to the offline sel.
- Needed both for the *signal* and *control modes*
- Thanks to very flexible/configurable trigger design: *lines added/removed/updated every few months*

■ Stripping (~ offline HLT)

- Lines run a few times per year to provide analysis with only the data they need
- Make CPU demand match resource



Charm mixing

- Effective Hamiltonian that allow to focus on time evolution in $\{|D^0\rangle, |\bar{D}^0\rangle\}$ basis, but also accounts for its decay (non hermitian)

$$i\frac{\partial}{\partial t} \begin{pmatrix} D^0(t) \\ \bar{D}^0(t) \end{pmatrix} = \left(\mathbf{M} - \frac{i}{2}\mathbf{\Gamma} \right) \begin{pmatrix} D^0(t) \\ \bar{D}^0(t) \end{pmatrix}$$

Physical states

$$\begin{aligned} |D_1\rangle &= p|D^0\rangle + q|\bar{D}^0\rangle \\ |D_2\rangle &= p|D^0\rangle - q|\bar{D}^0\rangle \end{aligned}$$

Flavor states

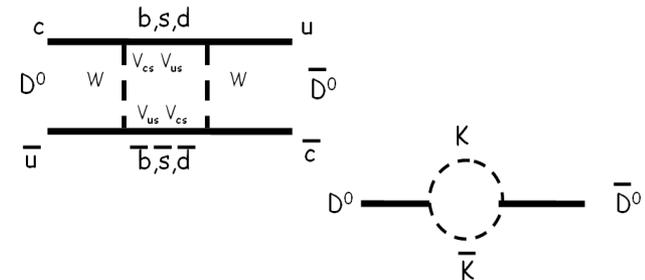
$$\begin{aligned} |D^0(t)\rangle &= g_+(t)|D^0\rangle + \frac{q}{p}g_-(t)|\bar{D}^0\rangle \\ |\bar{D}^0(t)\rangle &= g_+(t)|\bar{D}^0\rangle + \frac{p}{q}g_-(t)|D^0\rangle \end{aligned}$$

- Physical states eigenvalues rule ($M_{1,2} \pm i\Gamma_{1,2}$) the mixing time evolution. $|g_{\pm}(t)|^2$ can be written in terms of x and y

$$x \equiv \frac{\Delta M}{\Gamma}, \quad \Delta M \equiv M_1 - M_2 \quad y \equiv \frac{\Delta \Gamma}{2\Gamma}, \quad \Delta \Gamma \equiv \Gamma_1 - \Gamma_2$$

- Hard to predict x & y . Two theoretical approaches evaluate **0.1 to 1%**

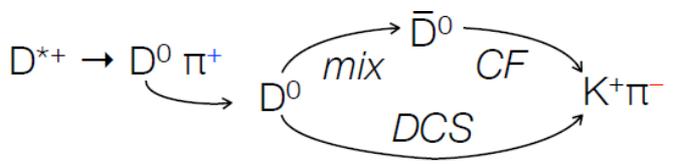
- OPE based on 4-fermions local operators: box diagrams either GIM (s, d in the loop) or CKM suppressed (b)
- Sum of hadronic intermediate states GIM suppression broken only by $SU(3)_F$ breaking.



Mixing Measurements at LHCb

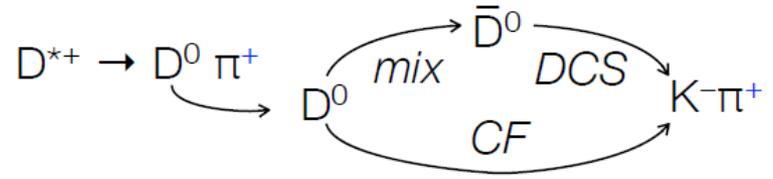
- 1st way: observe a decay at too high a rate, unless the D flavor flipped

Wrong Sign events (WS)



vs.

Right Sign events (RS)



$$\Rightarrow R(t) = \frac{N_{WS}(t)}{N_{RS}(t)} = R_D + \sqrt{R_D} y' t + \frac{x'^2 + y'^2}{4} t^2$$

$$\begin{aligned} x' &= x \cos \delta + y \sin \delta \\ y' &= y \cos \delta - x \sin \delta \end{aligned}$$

Assuming x,y small and no CPV

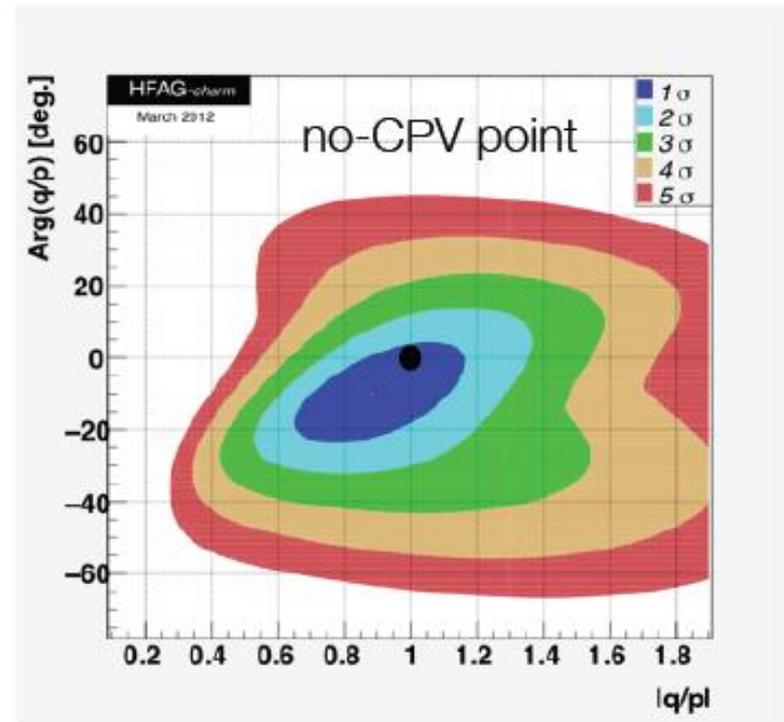
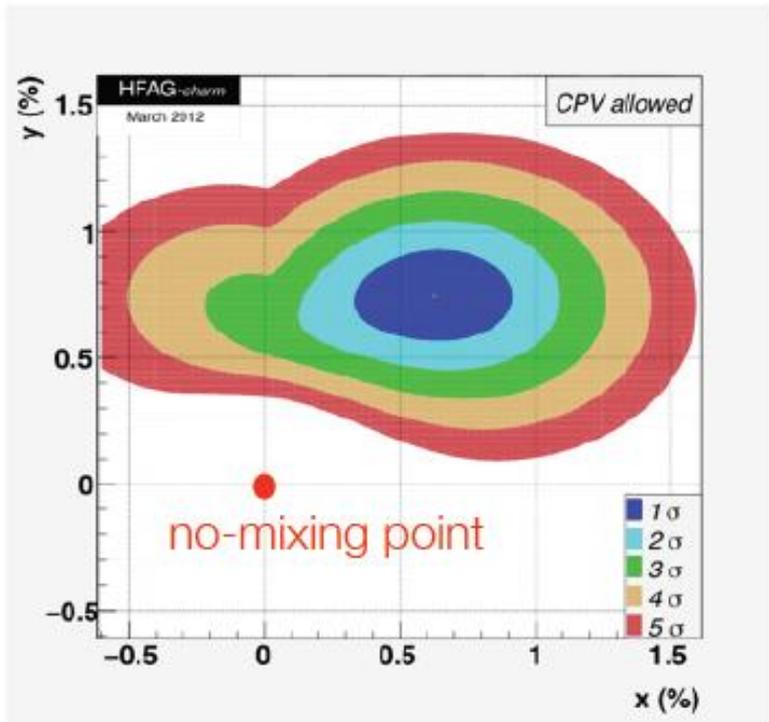
- 2nd way: measure different lifetimes in $D^0 \rightarrow \pi^+ \pi^-$ and $D^0 \rightarrow K^- \pi^+$

- CP-even eigenstates couple to $|D_1\rangle = |D^0\rangle + |\bar{D}^0\rangle$ (assume no CPV)
 - Measured lifetime distribution $\sim \exp(-i\Gamma_1 t)$
- Flavor eigenstates couple to a mixture of $|D_1\rangle$ and $|D_2\rangle$
 - Measured lifetime distribution $\sim \exp(-i\Gamma_1 t) + \exp(-i\Gamma_2 t)$

$$\Rightarrow y_{CP} \equiv \frac{\hat{\Gamma}(D^0 \rightarrow K^+ K^-)}{\hat{\Gamma}(D^0 \rightarrow K^- \pi^+)} - 1$$

- **These suppressions make charm mixing far slower than for in K, B, B_s**
- **Less good at interfering with the decay to enhance a potential CPV signal. *However still a good tool to seek NP***
 - *CPV in the mixing should have a low SM background*
 - *$|x| \gg |y|$ would also be a sign (x generated by virtual intermediate states: more sensitive to heavy NP particles)*

■ HFAG [3]



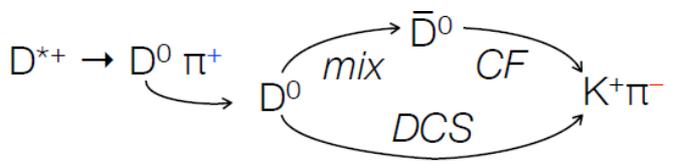
$$x = (0.63 \pm 0.19) \%$$

$$y = (0.73 \pm 0.11) \%$$

Mixing Measurements at LHCb

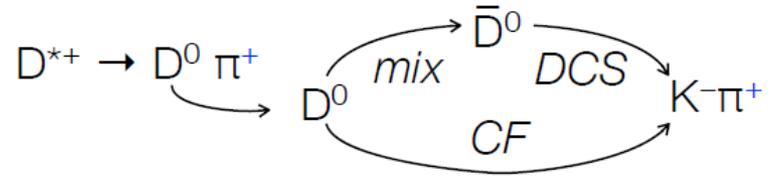
- 1st way: observe a decay at too high a rate, unless the D flavor flipped

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vs.

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$$\Rightarrow R(t) = \frac{N_{WS}(t)}{N_{RS}(t)} = R_D + \sqrt{R_D} y' t + \frac{x'^2 + y'^2}{4} t^2$$

$$\begin{aligned} x' &= x \cos \delta + y \sin \delta \\ y' &= y \cos \delta - x \sin \delta \end{aligned}$$

Assuming x, y small and no CPV

- 2nd way: measure different lifetimes in $D^0 \rightarrow \pi^+ \pi^-$ and $D^0 \rightarrow K^- \pi^+$

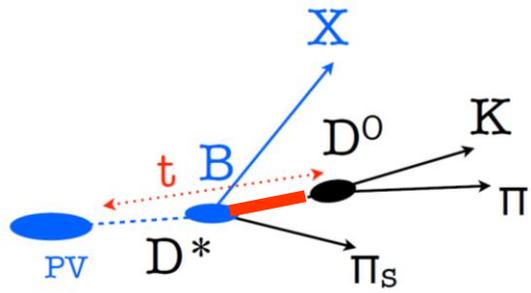
- CP-even eigenstates couple to $|D_1\rangle = |D^0\rangle + |\bar{D}^0\rangle$ (assume no CPV)
 - Measured lifetime distribution $\sim \exp(-i\Gamma_1 t)$
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$$\Rightarrow y_{CP} \equiv \frac{\hat{\Gamma}(D^0 \rightarrow K^+ K^-)}{\hat{\Gamma}(D^0 \rightarrow K^- \pi^+)} - 1$$

Systematic uncertainties

Anything that distorts R_i 's !

- Reconstruction effects mostly cancel in the ratio
- 3% of D^0 's are likely to come from B decays: same $R(t)$ but t is wrong !

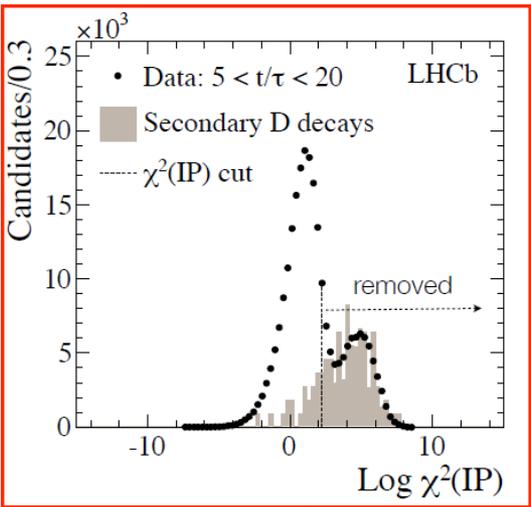
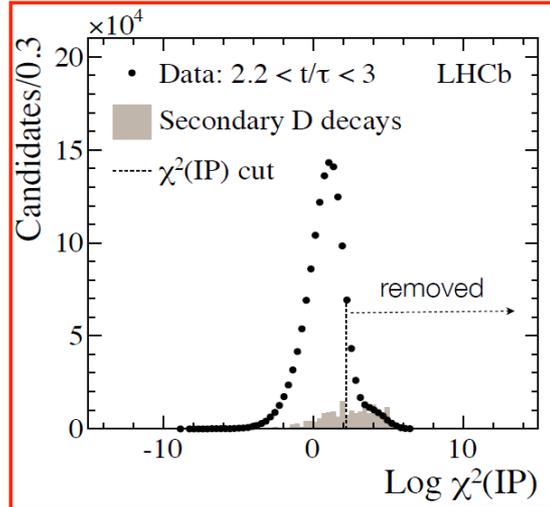


Fit $R^m(t)$ instead of $R(t)$ and see the difference

$$R^m(t) = \frac{N^{WS}(t) + N_B^{WS}(t)}{N^{RS}(t) + N_B^{RS}(t)} = R(t) \left\{ 1 - f_B^{RS}(t) \left[1 - \frac{R_B(t)}{R(t)} \right] \right\}$$

Fraction of secondary in each bin
Fit the $D \log(IP \chi^2)$

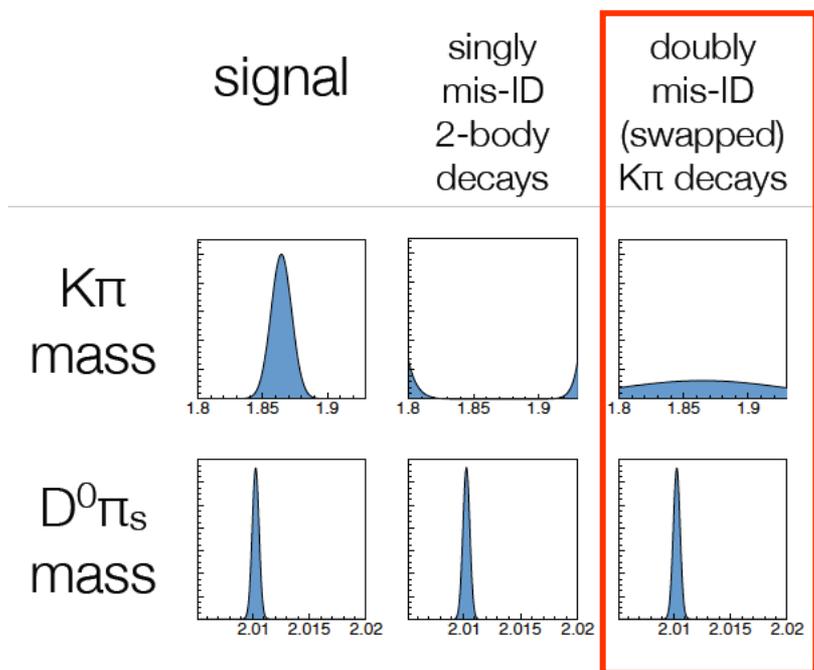
Fit assuming $R_B(t) = R_D = R(0) \forall t$
($R(t)$: monotoneous increasing function)



Systematic uncertainties

Anything that distorts R_i 's !

- Reconstruction effects mostly cancel in the ratio
- Peaking backgrounds surviving tight M_{D^0} and PID cuts

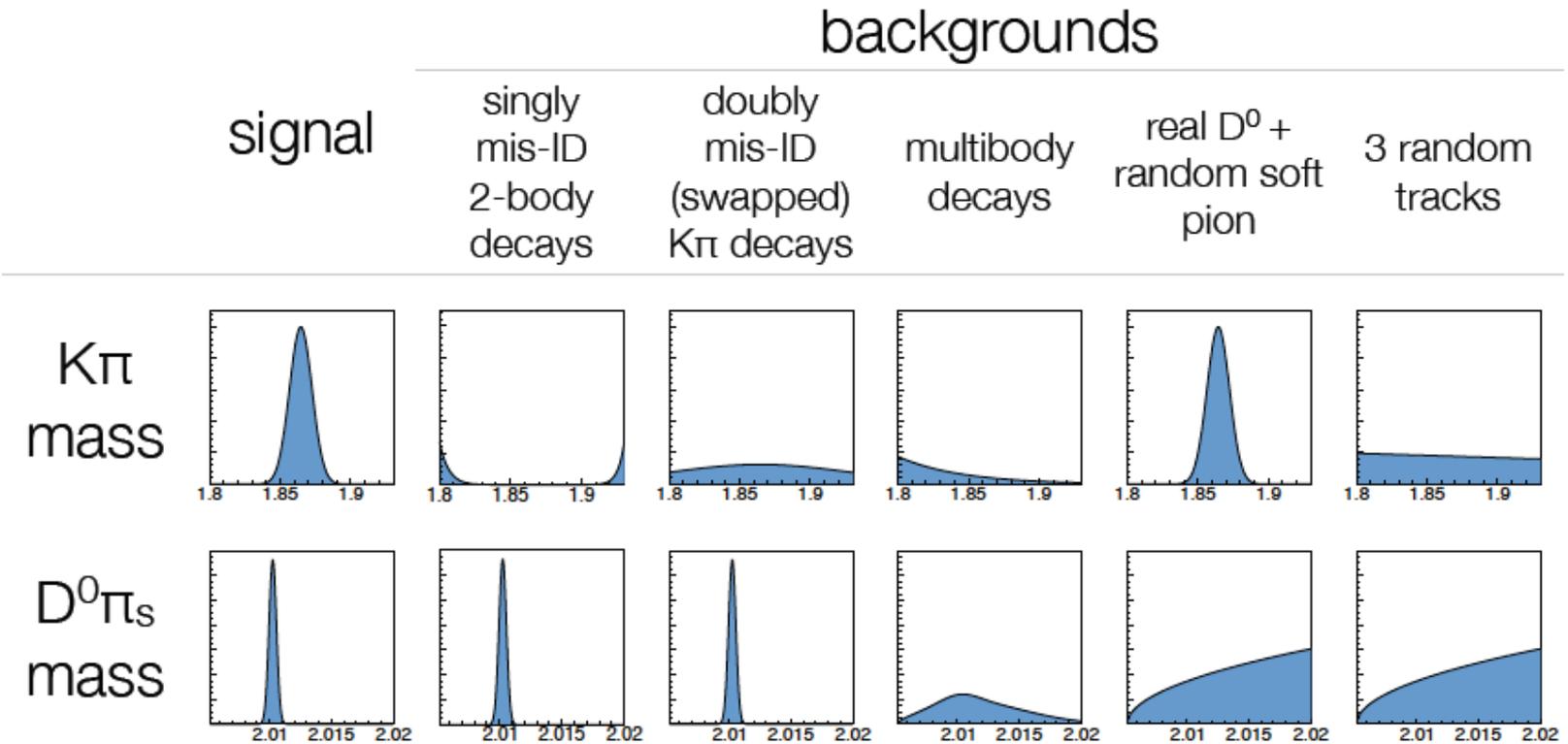


M_{D^0} sideband: misidentified RS decays are (0.4 ± 0.2) % of the WS sample

Fit with:

$$R^m(t) = R(t) + N^{RS}(\text{double mis-IS}) / N^{RS}$$

$D^* \rightarrow D^0(\rightarrow K\pi)\pi$ signal vs backgrounds



Cut tight on PID and D^0 mass to reduce physics bkg and fit $D^0\pi_s$ mass, then consider only signal and random pions in the fit

	ΔR_D	$\Delta y'$	$\Delta x'^2$
Asymmetries in detection or production	$<0.001\sigma$	$<0.001\sigma$	$<0.001\sigma$
VELO length scale	0	0.003σ	0.001σ
Multiple candidates	0.02σ	0.06σ	0.07σ

Cross-checks

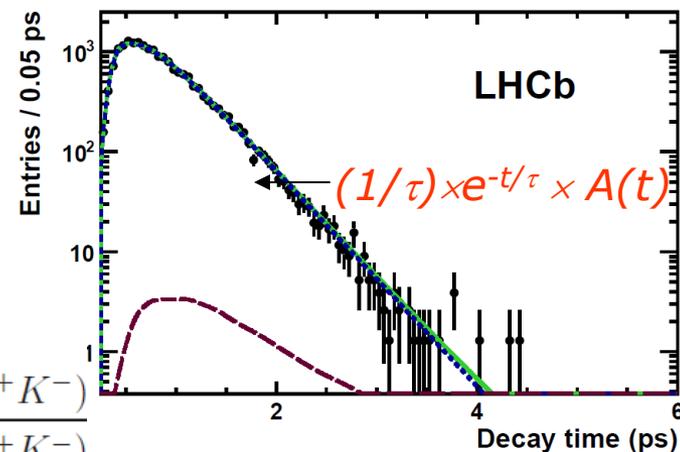
- We perform the measurement in statistically independent sub-samples of the data and find consistent results
 - different data-taking periods,
 - magnet polarities,
 - number of reconstructed primary vertices
- Also use alternative decay-time binning schemes or alternative fit methods to separate signal and background, and find no significant variations in the estimated mixing parameters

γ_{CP} and A_Γ with two-body D decays

Measurement technique

- Measure the proper decay time distribution of $D^0 \rightarrow K^- \pi^+$, $K^+ K^-$ and fit an exponential model to extract effective lifetimes $\hat{\Gamma}$

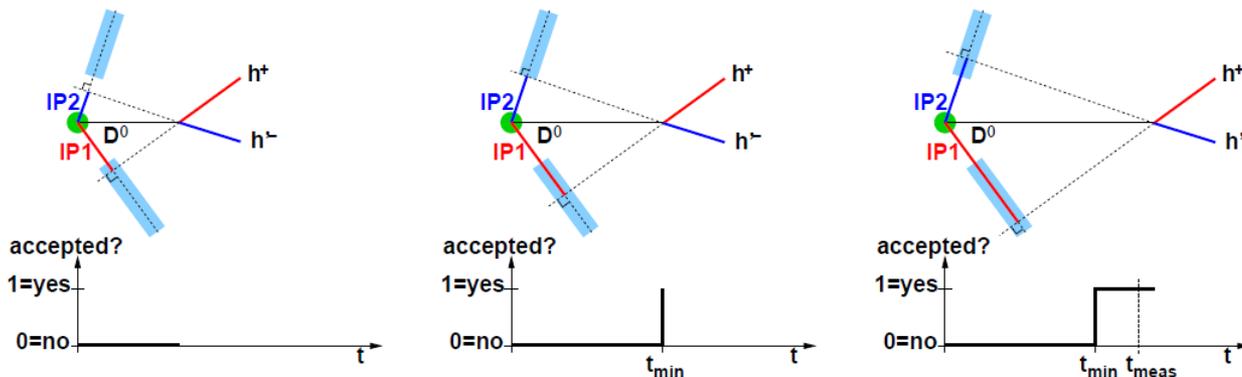
$$y_{CP} \equiv \frac{\hat{\Gamma}(D^0 \rightarrow K^+ K^-)}{\hat{\Gamma}(D^0 \rightarrow K^- \pi^+)} - 1 \quad A_{\Gamma} \equiv \frac{\hat{\Gamma}(D^0 \rightarrow K^+ K^-) - \hat{\Gamma}(\bar{D}^0 \rightarrow K^+ K^-)}{\hat{\Gamma}(D^0 \rightarrow K^+ K^-) + \hat{\Gamma}(\bar{D}^0 \rightarrow K^+ K^-)}$$



- Key point I : treating the experimental distortion of this distribution

→ Swimming: data driven determination of the time acceptance $A(t)$

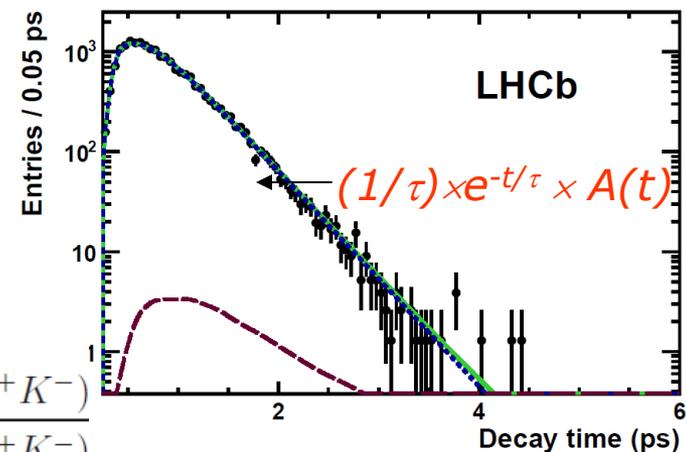
- Event by event method: given its kinematics, an event is accepted by the lifetime biasing cuts (ex: IP_{χ^2} , Flying Distance,..) based on t only.
- Replay the selection, with recomputed cut variables, for several values of t .



Measurement technique

- Measure the proper decay time distribution of $D^0 \rightarrow K^- \pi^+$, $K^+ K^-$ and fit an exponential model to extract effective lifetimes $\hat{\Gamma}$

$$y_{CP} \equiv \frac{\hat{\Gamma}(D^0 \rightarrow K^+ K^-)}{\hat{\Gamma}(D^0 \rightarrow K^- \pi^+)} - 1 \quad A_{\Gamma} \equiv \frac{\hat{\Gamma}(D^0 \rightarrow K^+ K^-) - \hat{\Gamma}(\bar{D}^0 \rightarrow K^+ K^-)}{\hat{\Gamma}(D^0 \rightarrow K^+ K^-) + \hat{\Gamma}(\bar{D}^0 \rightarrow K^+ K^-)}$$



- Key point I : treating the experimental distortion of this distribution

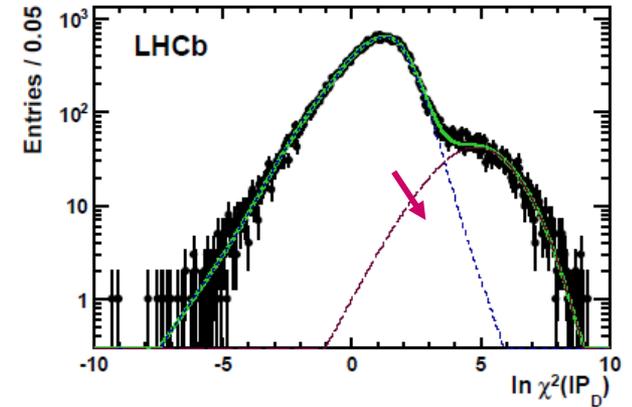
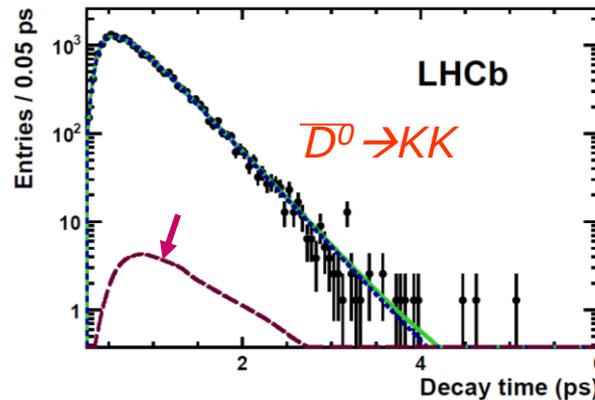
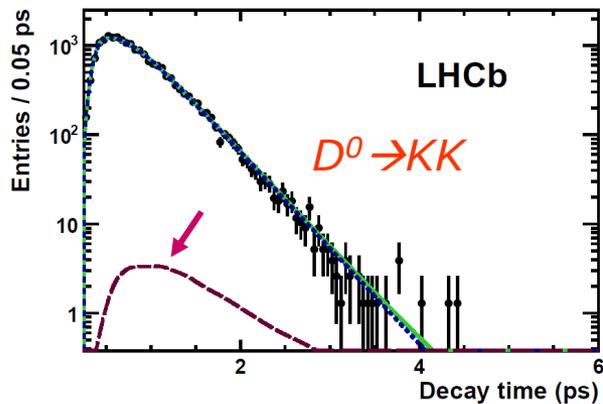
→ *Swimming: data driven determination of the time acceptance A(t)*

- Event by event method: given its kinematics, an event is accepted by the lifetime biasing cuts (ex: IP_{χ^2} , Flying Distance,..) based on t only.
- Replay the selection, with recomputed cut variables, for several values of t .
- Tracks hits are hard to move → move the primary vertex instead.
- HLT uses biasing cuts ! But one key feature of LHCb's trigger:
HLT can be re-run exactly offline !

■ Key point II : D^0 from B decays

- background to prompt D^0 with a different decay time distribution
- treated by the fit, using the $D(IP\chi^2)$ distribution

→ Model used in the fit = dominant systematic uncertainty

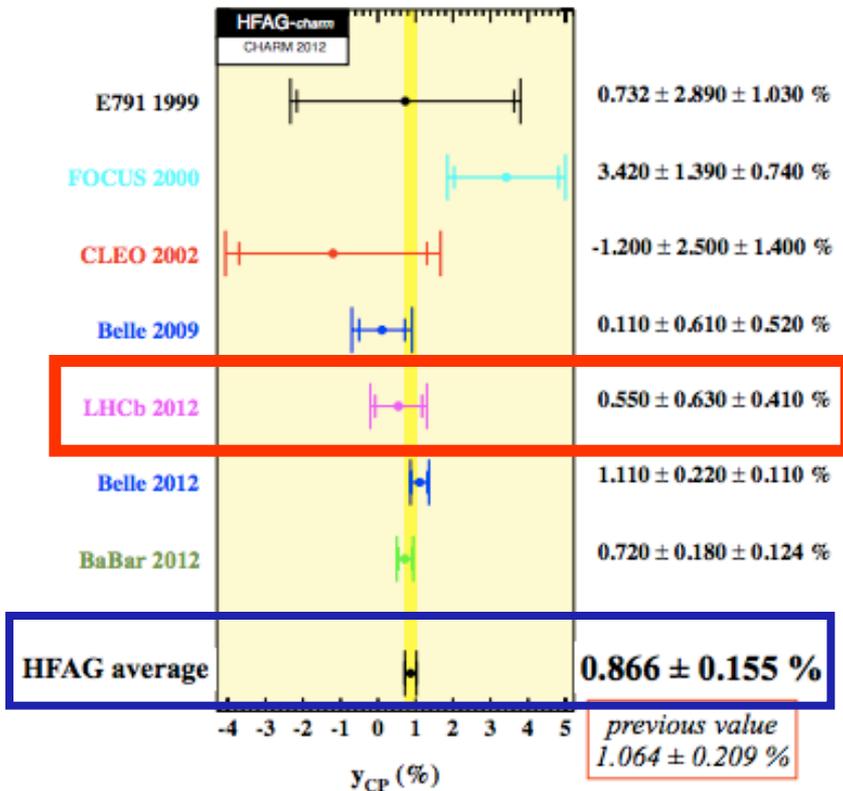


29 pb⁻¹, 2010 data.

$$y_{CP} = (5.5 \pm 6.3_{\text{stat}} \pm 4.1_{\text{syst}}) \times 10^{-3}.$$

$$A_{\Gamma} = (-5.9 \pm 5.9_{\text{stat}} \pm 2.1_{\text{syst}}) \times 10^{-3}$$

**J.Phys.G39 (2012) 045005,
arXiv:1112.4698v1**



**Will be much improved with
LHCb's full sample: 3 fb⁻¹**

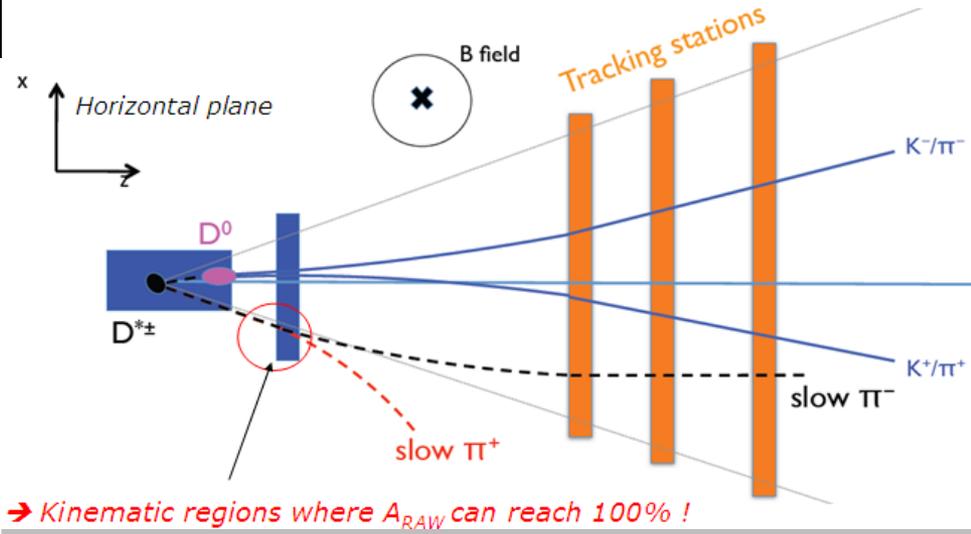
$$\Delta A_{RAW} = A_{RAW}(K^+K^-) - A_{RAW}(\pi^+\pi^-) = \Delta A_{CP}$$

■ **This is a very robust observable !**

■ **Yet not perfect. Ex:**

→
• B causes $A_D(\pi_S)$

π^+/π^- bent in opposite directions
→ each sees a different detector
if left-right asymmetries.



• Large asymmetries ($\gg 1\%$) cause the Taylor Expansion to break down.

Large A_D close to detector's edges

• $A_P(D^*)$ depends on \vec{p} : So do the particle reco and selection, thus $A_D(\pi_S)$!

KK and $\pi\pi$ selections favor different regions (PID efficiency also depends on \vec{p})

■ Main protections

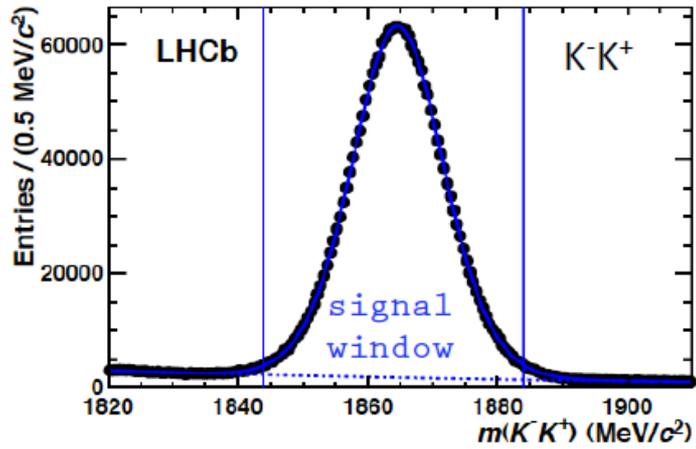
• Measurements in *separate bins of P_T and η of D^* 's, P of π_S*

• Combine opposite B polarities (up & down) to cancel left/right det. asymmetry

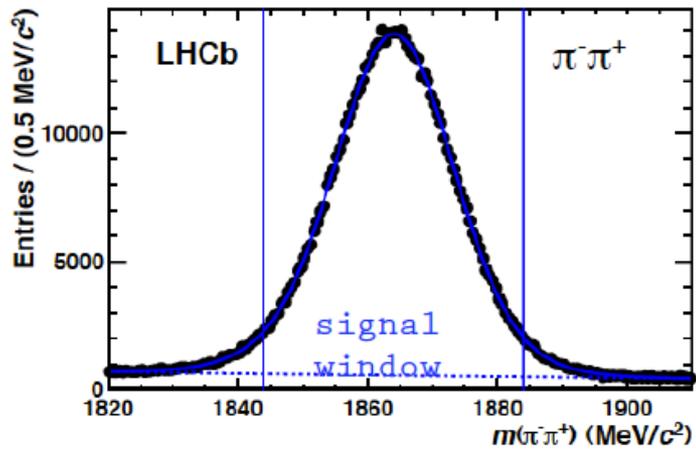
• Fiducial cuts to remove regions of large asymmetry

• Many checks/systematics (back-up slides: compare ΔA_{CP} with or w/o binning, consistency between the various bins, between up and down polarities, etc...)

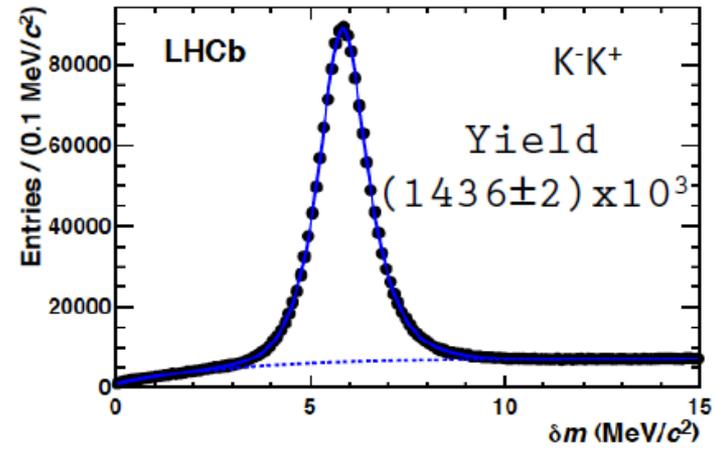
$$\Delta A_{CP} = A_{CP}(D^0 \rightarrow K^+ K^-) - A_{CP}(D^0 \rightarrow \pi^+ \pi^-)$$



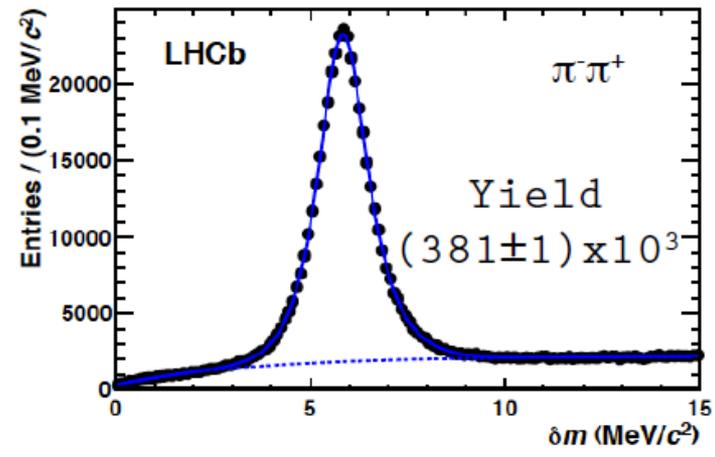
$1844 < m(D^0) < 1884 \text{ MeV}/c^2$



$$\delta m = m(h^+ h^- \pi^+) - m(h^+ h) - m(\pi^+)$$



$1844 < m(D^0) < 1884 \text{ MeV}/c^2$



Effect	Uncertainty
<i>ΔA_{CP} with vs. without Fiducial cuts</i>	0.01%
<i>Background peaks (+their asymmetry) from $m(D^0)$ sideband injected into TOYs to check the effect on the fit.</i>	0.04%
<i>ΔA_{CP} with fit vs. sideband subtraction cuts</i>	0.08%
<i>ΔA_{CP} with multiple candidates vs. only one allowed per event</i>	0.06%
<i>ΔA_{CP} with kinematical bins vs. one single bin</i>	0.02%
TOTAL	0.11%

$$\Delta A_{CP} = (-0.82 \pm 0.21_{stat} \pm 0.11)\%$$

3.5 σ from no CPV.

Cross Checks

- **Electron and muon vetoes on the soft pion and D^0 daughters**
- **Different kinematic binnings**
- **Stability of result vs data-taking runs**
- **Stability vs kinematic variables**
- **Toy MC studies of fit procedure, statistical errors**
- **Tightening of PID cuts on D^0 daughters**
- **Tightening of kinematic cuts**
- **Variation with event track multiplicity**
- **Use of other signal, background line-shapes in the fit**
- **Use of alternative offline processing (skimming/stripping)**
- **Internal consistency between subsamples (splitting left/right, field up/ field down)**

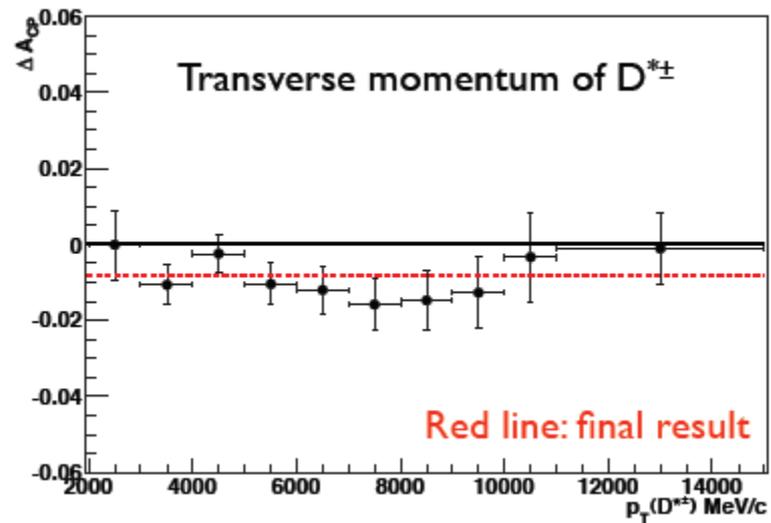
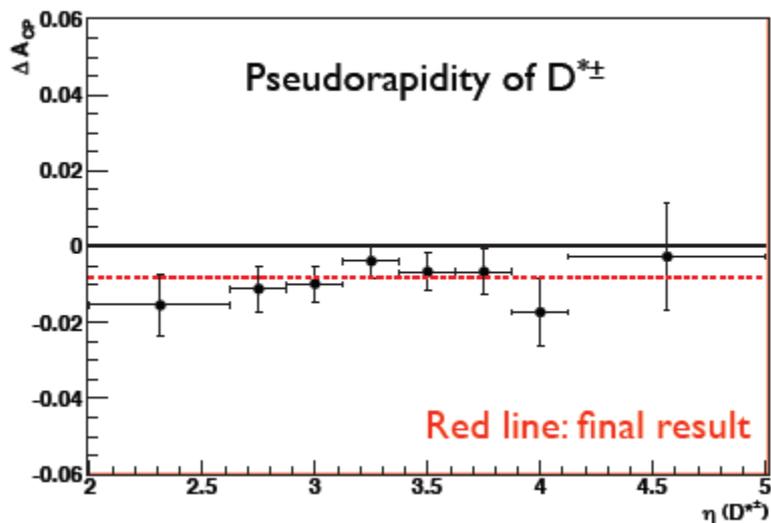
■ Flavor physics means precision physics, ie many cross checks

- *Different kinematic binnings*
- *Remove fiducial cuts*
- *Tightening of PID cuts on D daughters (correlated with P, and bkg level)*
- *Impact of neglecting some backgrounds.*
- *Alternative signal & bkg shapes in the fit, compare with mere sideband sub.*
- *Alternative online/offline processing (trigger, selection, signal region, etc...)*
- *Stability of result vs data-taking time*
- *Control mode resembling the signal (ex: $D_s \rightarrow \phi\pi$; DP outside the phi region)*
- *Internal consistency among subsamples (left vs. right, field up vs. down)*
- *Electron and muon vetoes on the soft pion and D^0 daughters*
- *Variation with event track multiplicity*

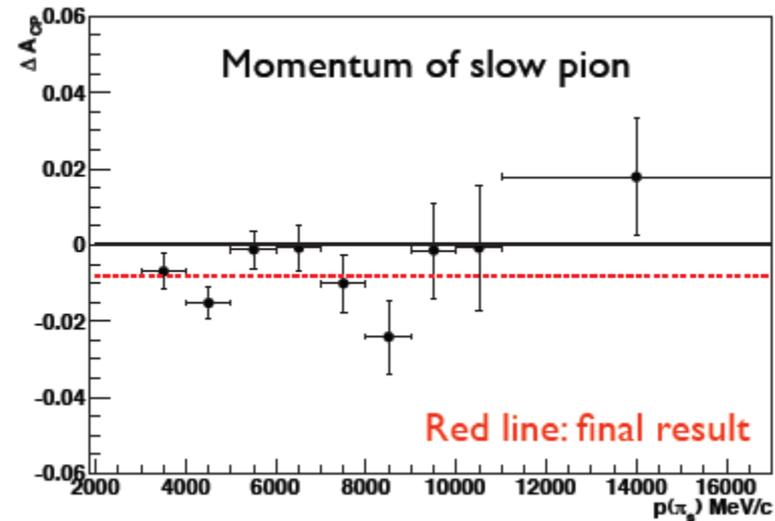
- *Toy MC studies of fit procedure, statistical errors*
- *Stability vs kinematic variables*

Please check if other tests have been done by one of the ANA

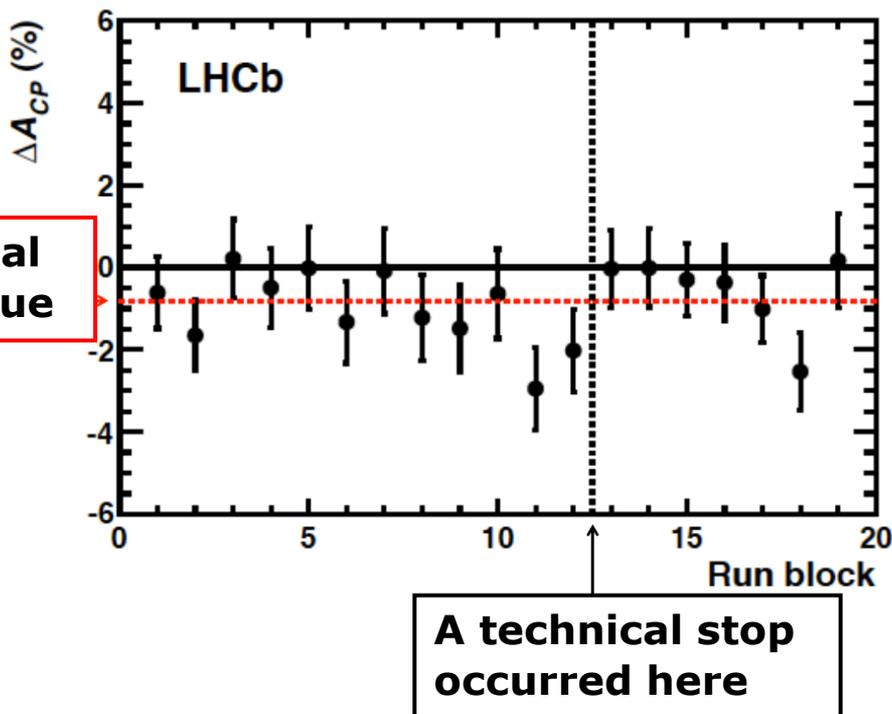
Cross Checks



- No evidence of dependence on relevant kinematic variables



■ Stability with time



■ Internal consistency: a closer look

Split the 216 bins into 8 smaller sets and check χ^2 for each, and *between them*:

$$\chi^2 / \text{NDF} = 6.7/7$$

■ Stability wrt PID

No significant variation of ΔA_{CP} when tightening the cut on the hadron PID information provided by the RICH

PID tight+

$$\Delta A_{CP} = (-0.88 \pm 0.26_{\text{stat}})\%$$

PID tight++

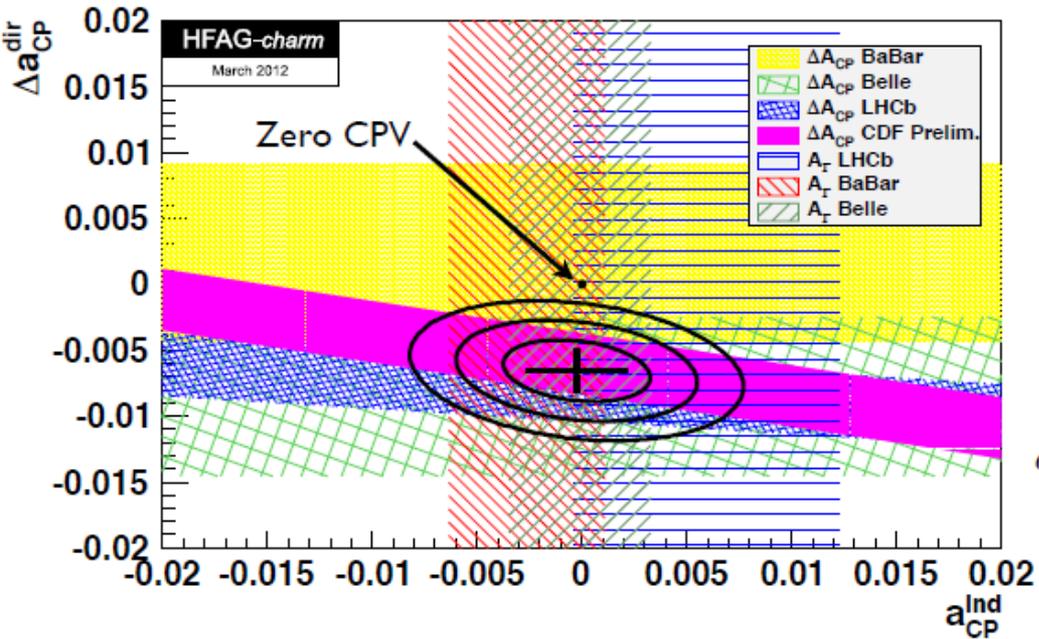
$$\Delta A_{CP} = (-1.03 \pm 0.31_{\text{stat}})\%$$

Subsample	ΔA_{CP}	χ^2/ndf
Pre-TS, field up, left	$(-1.22 \pm 0.59)\%$	13/26(98%)
Pre-TS, field up, right	$(-1.43 \pm 0.59)\%$	27/26(39%)
Pre-TS, field down, left	$(-0.59 \pm 0.52)\%$	19/26(84%)
Pre-TS, field down, right	$(-0.51 \pm 0.52)\%$	29/26(30%)
Post-TS, field up, left	$(-0.79 \pm 0.90)\%$	26/26(44%)
Post-TS, field up, right	$(+0.42 \pm 0.93)\%$	21/26(77%)
Post-TS, field down, left	$(-0.24 \pm 0.56)\%$	34/26(15%)
Post-TS, field down, right	$(-1.59 \pm 0.57)\%$	35/26(12%)
All data	$(-0.82 \pm 0.21)\%$	211/215(56%)

World Wide

Year	Experiment	Results	$\Delta\langle t \rangle/\tau$	$\overline{\langle t \rangle}/\tau$
2007	Belle	$A_\Gamma = (0.01 \pm 0.30 \text{ (stat.)} \pm 0.15 \text{ (syst.)})\%$	-	-
2008	BaBar	$A_\Gamma = (0.26 \pm 0.36 \text{ (stat.)} \pm 0.08 \text{ (syst.)})\%$	-	-
2011	LHCb	$A_\Gamma = (-0.59 \pm 0.59 \text{ (stat.)} \pm 0.21 \text{ (syst.)})\%$	-	-
2008	BaBar	$A_{CP}(KK) = (0.00 \pm 0.34 \text{ (stat.)} \pm 0.13 \text{ (syst.)})\%$ $A_{CP}(\pi\pi) = (-0.24 \pm 0.52 \text{ (stat.)} \pm 0.22 \text{ (syst.)})\%$	0.00	1.00
2008	Belle	$\Delta A_{CP} = (-0.86 \pm 0.60 \text{ (stat.)} \pm 0.07 \text{ (syst.)})\%$	0.00	1.00
2011	LHCb	$\Delta A_{CP} = (-0.82 \pm 0.21 \text{ (stat.)} \pm 0.11 \text{ (syst.)})\%$	0.10	2.08
2012	CDF Prelim.	$\Delta A_{CP} = (-0.62 \pm 0.21 \text{ (stat.)} \pm 0.10 \text{ (syst.)})\%$	0.25	2.58

CDF public note 10784



$$a_{CP}^{ind} = (-0.025 \pm 0.231)\%$$

$$\Delta a_{CP}^{dir} = (-0.656 \pm 0.154)\%$$

Agreement with no CPV: 2×10^{-5}

World Average

- Can be combined with other measurements of ΔA_{CP} and with measurements of A_{Γ} by disentangling direct & indirect CPV.

$$A_{CP}(f) \approx a_{CP}^{dir}(f) + \frac{\langle t \rangle}{\tau} a_{CP}^{ind}$$

- Depends on $\langle t \rangle$ in the D^0 sample (\sim time given the mixing to interfere).
- $D^0 \rightarrow \pi \pi$ and $D^0 \rightarrow \pi \pi$ can have different time acceptance

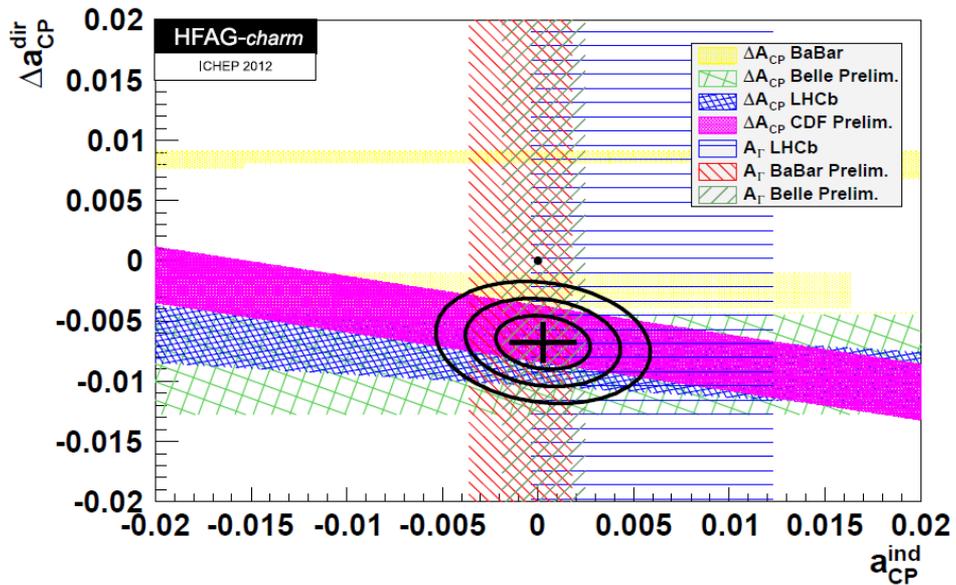
$$\Delta A_{CP} = [a_{CP}^{dir}(K^- K^+) - a_{CP}^{dir}(\pi^- \pi^+)] + \frac{\Delta \langle t \rangle}{\tau} a_{CP}^{ind}$$

\rightarrow Also measured $\Delta \langle t \rangle$: Contribution of indirect CPV < 10%

HFAG average

$a_{CP}^{ind} = (0.027 \pm 0.163) \%$
 $\Delta a_{CP}^{dir} = (-0.678 \pm 0.147) \%$

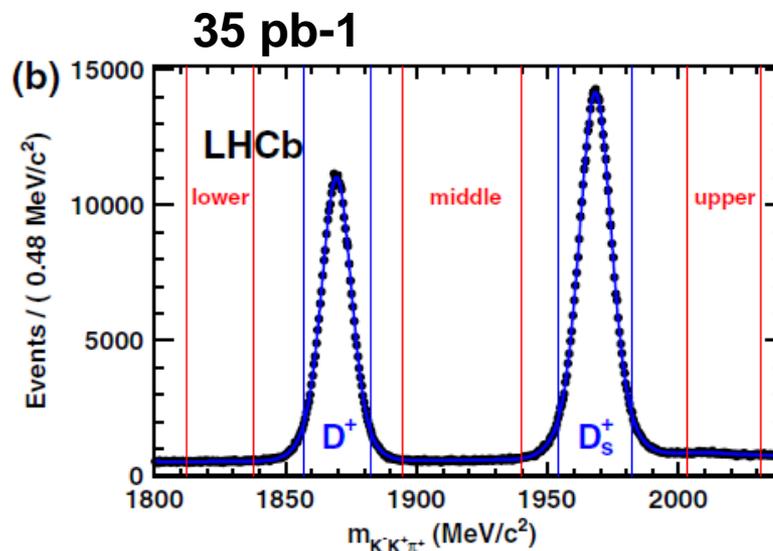
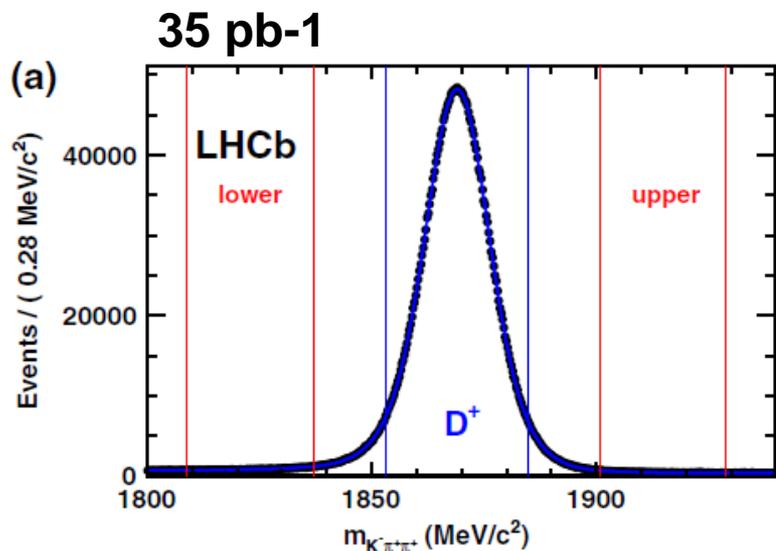
Agreement with no CPV: 6×10^{-5}



(see http://www.slac.stanford.edu/xorg/hfag/charm/ICHEP12/DCPV/direct_indirect_cpv.html)

- High signal statistics.
- Control of the artificial asymmetries thanks to large control samples:

$$D^+ \rightarrow K^- \pi^+ \pi^+, D_S^+ \rightarrow K^- K^+ \pi^+$$

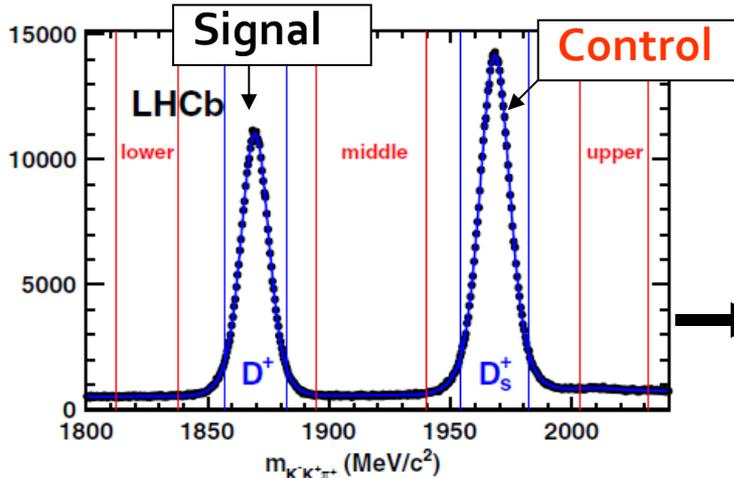


$$D^+ \rightarrow K^- K^+ \pi^+ \quad (3.284 \pm 0.006) \times 10^5$$

$$D_S^+ \rightarrow K^- K^+ \pi^+ \quad (4.615 \pm 0.012) \times 10^5$$

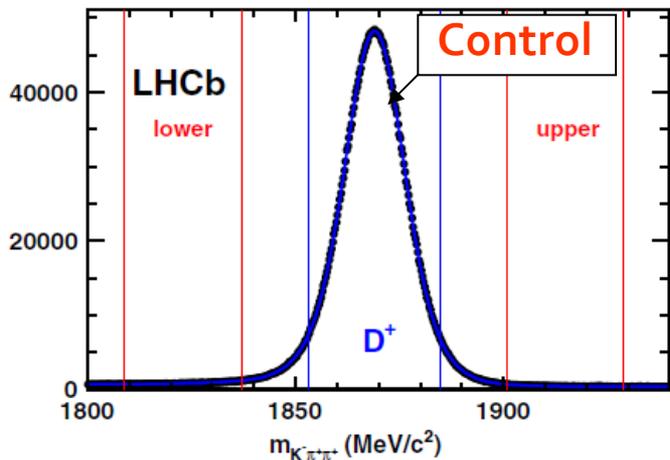
$$D^+ \rightarrow K^- \pi^+ \pi^+ \quad (3.3777 \pm 0.0037) \times 10^6$$

Larger than in all previous studies (Babar, Belle, CLEO-c)



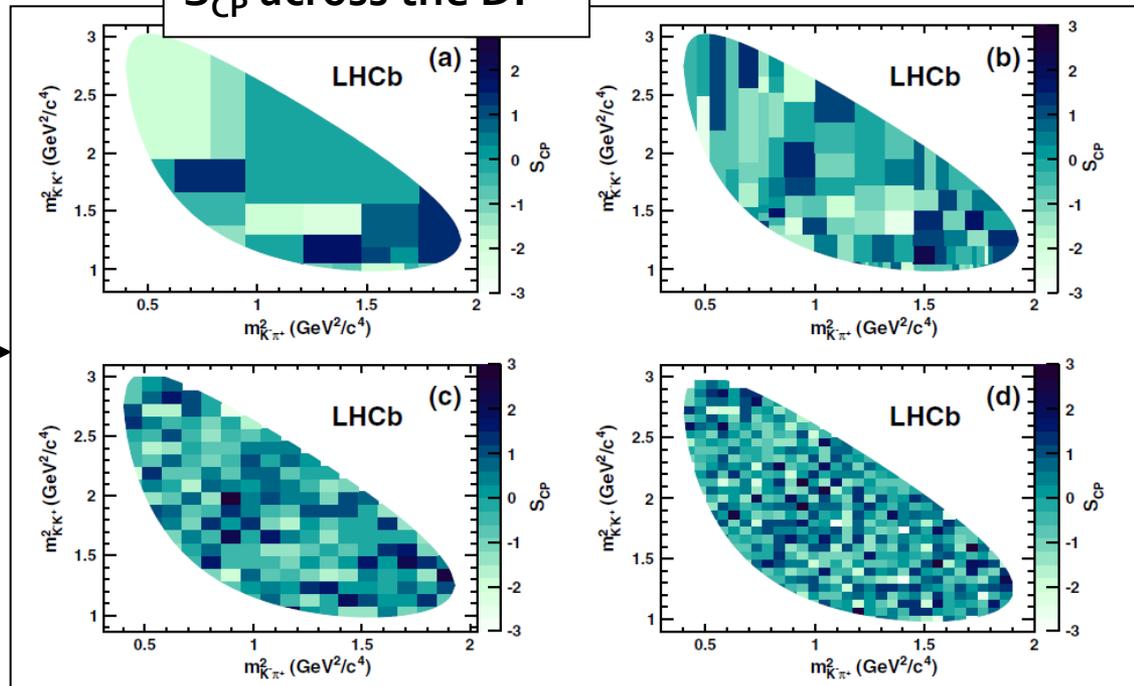
$$D^+ \rightarrow K^- K^+ \pi^+ \quad (3.284 \pm 0.006) \times 10^5$$

$$D_s^+ \rightarrow K^- K^+ \pi^+ \quad (4.615 \pm 0.012) \times 10^5$$



$$D^+ \rightarrow K^- \pi^+ \pi^+ \quad (3.3777 \pm 0.0037) \times 10^6$$

S_{CP} across the DP



p -value for $\chi^2 = \sum (S_{CP}^i)^2$

Binning	p -value (%)
Adaptive I	12.7
Adaptive II	10.6
Uniform I	82.1
Uniform II	60.5

*No evidence
for CPV !*

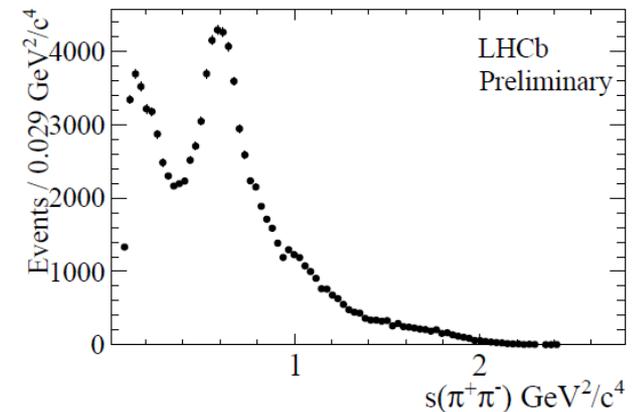
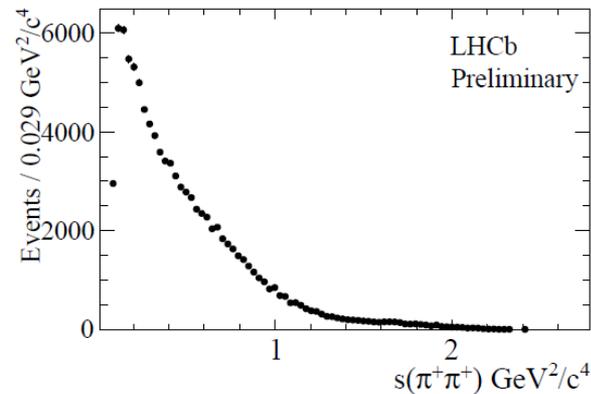
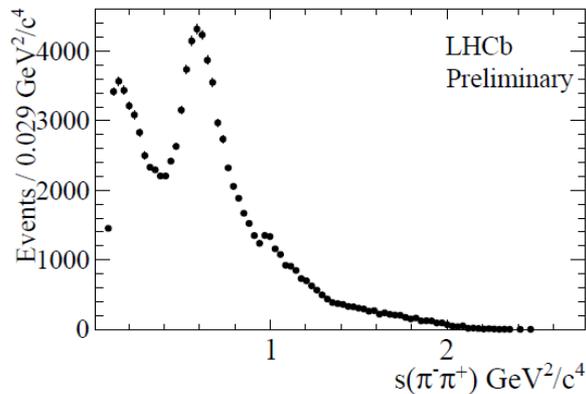
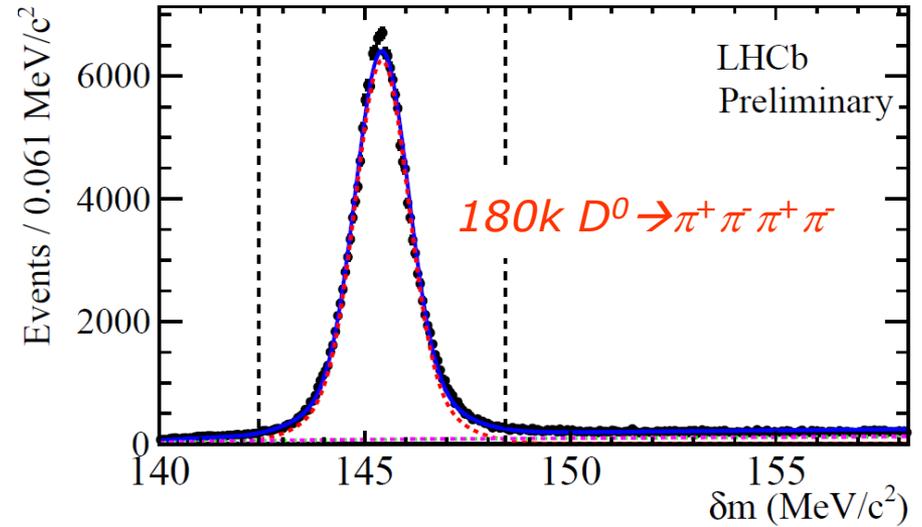
-Same plots for **control modes**:
no artificial asymmetry!

$D^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-$

P, 1 fb⁻¹

- Use D^* tag the D^0 flavor
- High purity and statistics despite the large background inherent to 4-body decays. **Used a NN¹**.
- High statistics CP conserving control mode: **1.3M $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$**
- 4-body: **5D** phase space necessary to fully describe the decay.

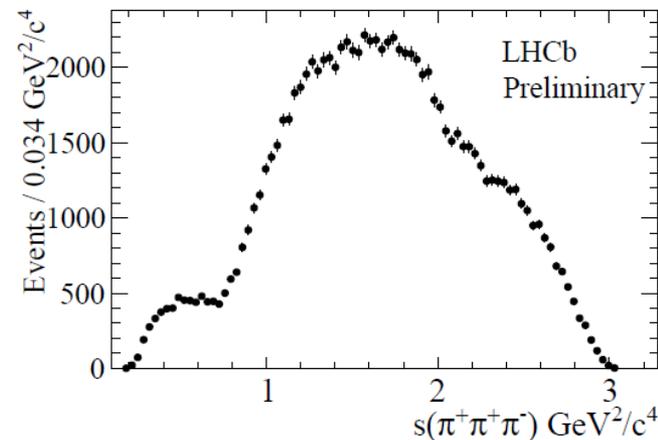
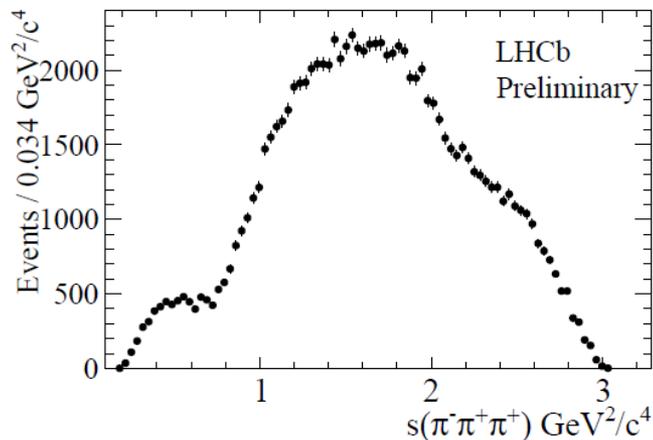
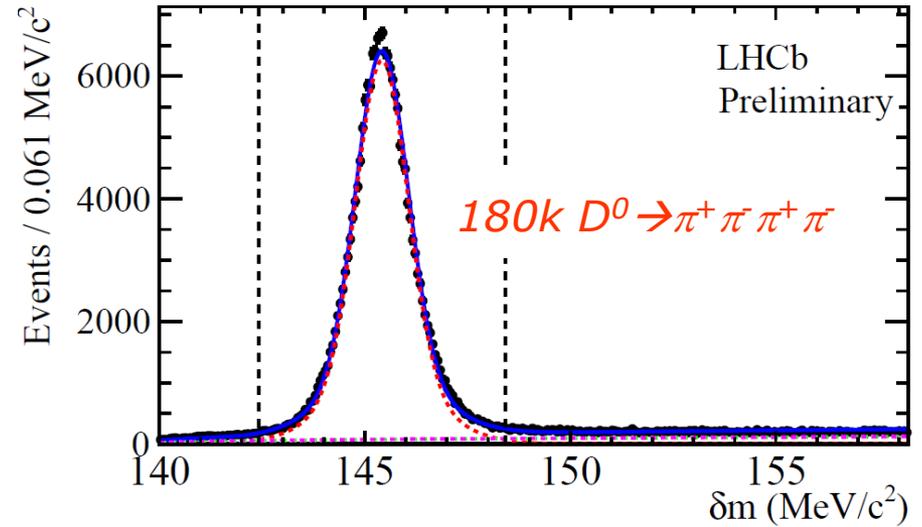
→ S_{CP}^i 's measured in bins of a 5D Dalitz Plot.



$D^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-$

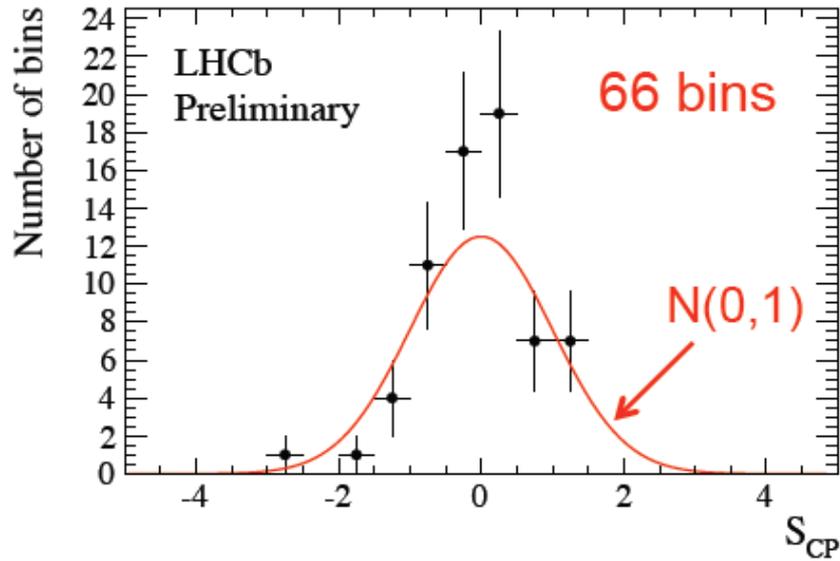
P, 1 fb⁻¹

- Use D^* tag the D^0 flavor
- High purity and statistics despite the large background inherent to 4-body decays. **Used a NN¹**.
- High statistics CP conserving control mode: **1.3M $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$**
- 4-body: **5D** phase space necessary to fully describe the decay.
→ S_{CP}^i 's measured in bins of a 5D Dalitz Plot.



$D^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-$

P, 1 fb-1



Bins	p-values (%)
15	97.1
29	95.6
66	99.8

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p-values assuming no CPV close to 1.

➔ No evidence of CPV

■ Checks for non CPV asymmetries: measure χ^2

- Several binnings
- Separately for magnet up and down
- For $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$
- For D^0 (mag up/left) vs. \bar{D}^0 (mag down/right)
Equivalent to D^0 vs. D^0 with a single magnet polarity
- For the background from the sideband
- For Many different time periods

$D^0 \rightarrow K^+ \pi^- \pi^+ \pi^-$

Bins	Magnet down	p-values %	
		Magnet up	Combined polarities
7	6.67	58.8	5.18
23	16.5	71.1	32.2
49	45.3	37.3	20.0
91	30.3	35.4	20.0
150	15.3	61.4	30.3

$D^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-$, 10 time-ordered samples

data subset	p-values (%)	
	Magnet down	Magnet up
1	9.15	11.0
2	15.3	81.1
3	91.4	75.9
4	76.7	86.1
5	1.59	18.3
6	35.6	50.8
7	5.77	99.8
8	40.6	26.0
9	76.8	71.1
10	17.8	66.9

■ **Single event sensitivity**

Quantity	Value
$N_{D^0 \rightarrow \pi^+ \pi^-}^{sig}$	1710 ± 47
$\epsilon_{trig}(\pi\pi)$	$(13.96 \pm 1.24)\%$
$\epsilon_{trig}(\mu\mu)$	$(82.54 \pm 3.13)\%$
$\frac{\epsilon_{sel}(\pi\pi)}{\epsilon_{sel}(\mu\mu)}$	0.95 ± 0.06
Prescale on $D^0 \rightarrow \pi^+ \pi^-$	0.0015
$\mathcal{B}(D^0 \rightarrow \pi^+ \pi^-)$	$(1.397 \pm 0.026) \cdot 10^{-3}$
α	$(1.96 \pm 0.23) \cdot 10^{-10}$

■ **Yields**

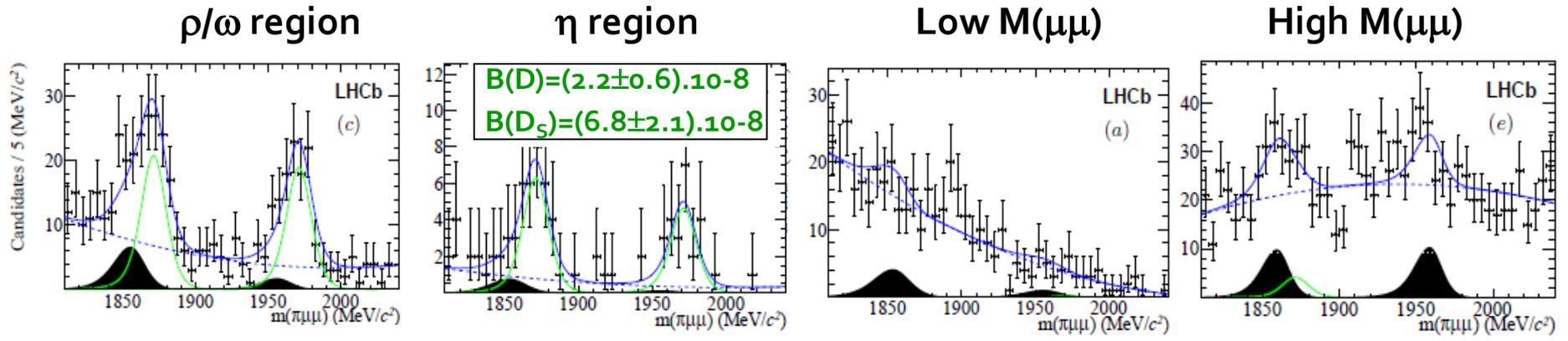
Channel	Fitted value
$D^{*+} \rightarrow D^0(\rightarrow \pi^+ \pi^-)\pi^+$	204 ± 33
$D^{*+} \rightarrow D^0(\rightarrow \mu^+ \mu^-)\pi^+$	$(0.49 \pm 0.42) \cdot 10^{-8}$
$D^{*+} \rightarrow D^0(\rightarrow K^- \pi^+)\pi^+$	380.3 ± 34.1
Comb. background	7439.6 ± 95.9

→ $\mathcal{B}(D^0 \rightarrow \mu^+ \mu^-) < 1.3 (1.1) \cdot 10^{-8}$ at 95 (90)%CL

LHCb Preliminary

One order of magnitude below Belle [XX]

Stay tuned: An improved analysis presented in a few weeks !



Upper limits $\times 10^{-8}$ @ 90% (95%) C.L.

Region	$B(D^+ \rightarrow \pi^+ \mu^+ \mu^-)$	$B(D_s \rightarrow \pi^+ \mu^+ \mu^-)$
Low $M(\mu\mu)$	2.0 (2.5)	6.9 (7.7)
High $M(\mu\mu)$	2.6 (2.9)	16.0 (18.6)
Total ⁽¹⁾	7.3 (8.3)	41.0 (47.7)

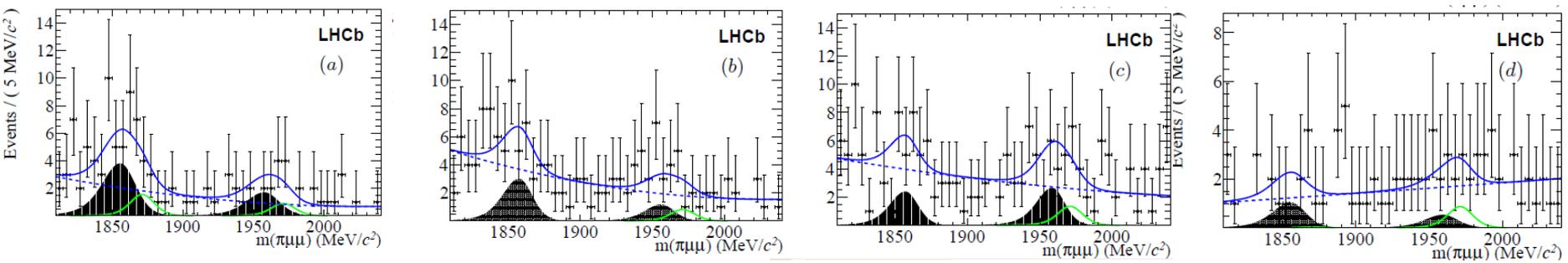


(1) Total non resonant BF, extrapolated from the high $M(\mu\mu)$ region (phase space model).

- 2 orders of mag. better than previous limits (D0 [XX], Babar [XX])
- Still above largest theory predictions ($\sim 10^{-8}$)

Lepton Number Violation: $D^+ \rightarrow \pi^- \mu^+ \mu^+$ and $D_S^+ \rightarrow \pi^- \mu^+ \mu^+$

- Same approach as for $D^+_{(S)} \rightarrow \pi^+ \mu^+ \mu^-$ with 4 regions in $M(\mu\mu)$:
(if mediated by a Majorana neutrino, larger significance in region where its mass peaks)



1 fb^{-1}

Upper limits $\times 10^{-8}$ @ 90% (95%) C.L.

Region [MeV/c ²]	$B(D^+ \rightarrow \pi^- \mu^+ \mu^+)$	$B(D_S^+ \rightarrow \pi^- \mu^+ \mu^+)$
$250 < M(\mu\mu) < 1140$	1.4 (1.7)	6.2 (7.6)
$1140 < M(\mu\mu) < 1340$	1.1 (1.3)	4.4 (5.3)
$1340 < M(\mu\mu) < 1540$	1.3 (1.5)	6.0 (7.3)
$1540 < M(\mu\mu)$	1.3 (1.5)	7.5 (8.7)
Total	2.2 (2.5)	12.0 (14.1)



- ➔ No LNV signal
- ➔ 2 orders of mag. better than previous limits (Babar [XX])

Implications of LHCb measurements and future prospects

The LHCb collaboration[†]

and

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