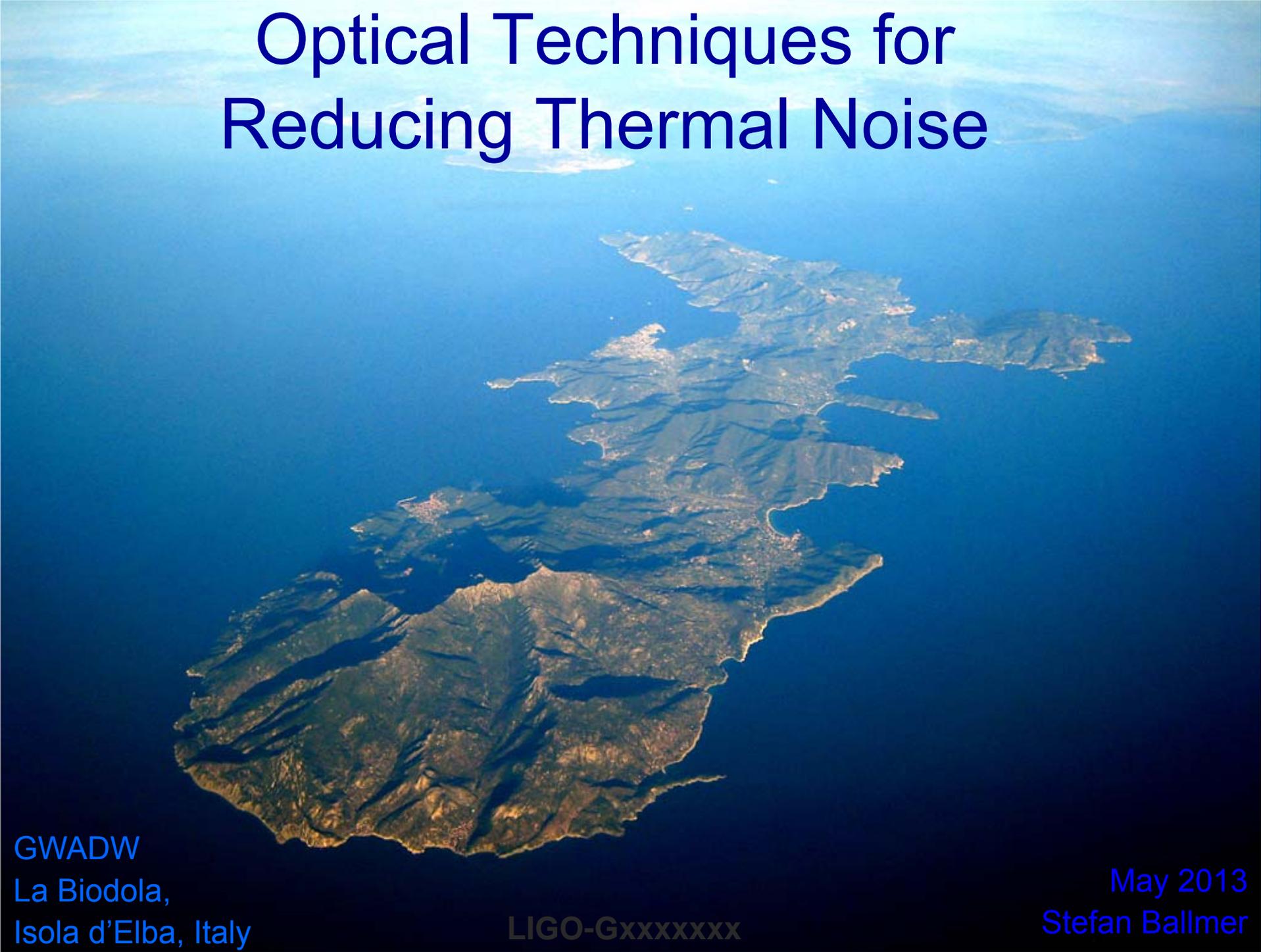


# Optical Techniques for Reducing Thermal Noise

An aerial photograph of the island of Elba, Italy, showing its rugged, mountainous terrain and coastline. The island is surrounded by deep blue water, and the sky is a clear, light blue. The text 'Optical Techniques for Reducing Thermal Noise' is overlaid at the top in a large, blue, sans-serif font.

GWADW  
La Biodola,  
Isola d'Elba, Italy

LIGO-Gxxxxxxx

May 2013  
Stefan Ballmer

# ~~Coast-~~ Out-line

Types of thermal noise

Correlation length

Strategies for mitigation

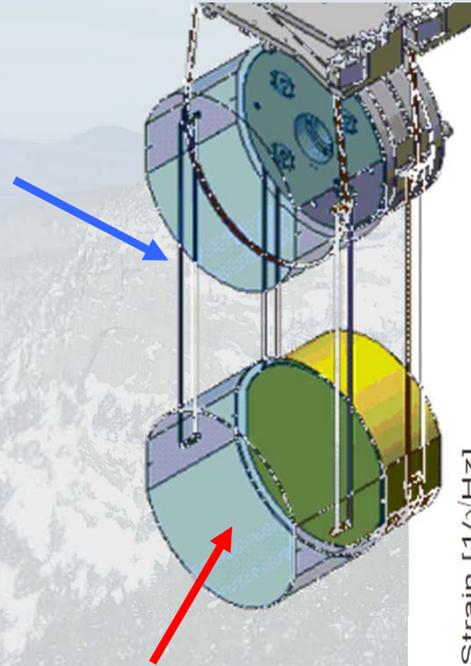
Examples

GWADW  
La Biodola,  
Isola d'Elba, Italy

May 2013  
Stefan Ballmer

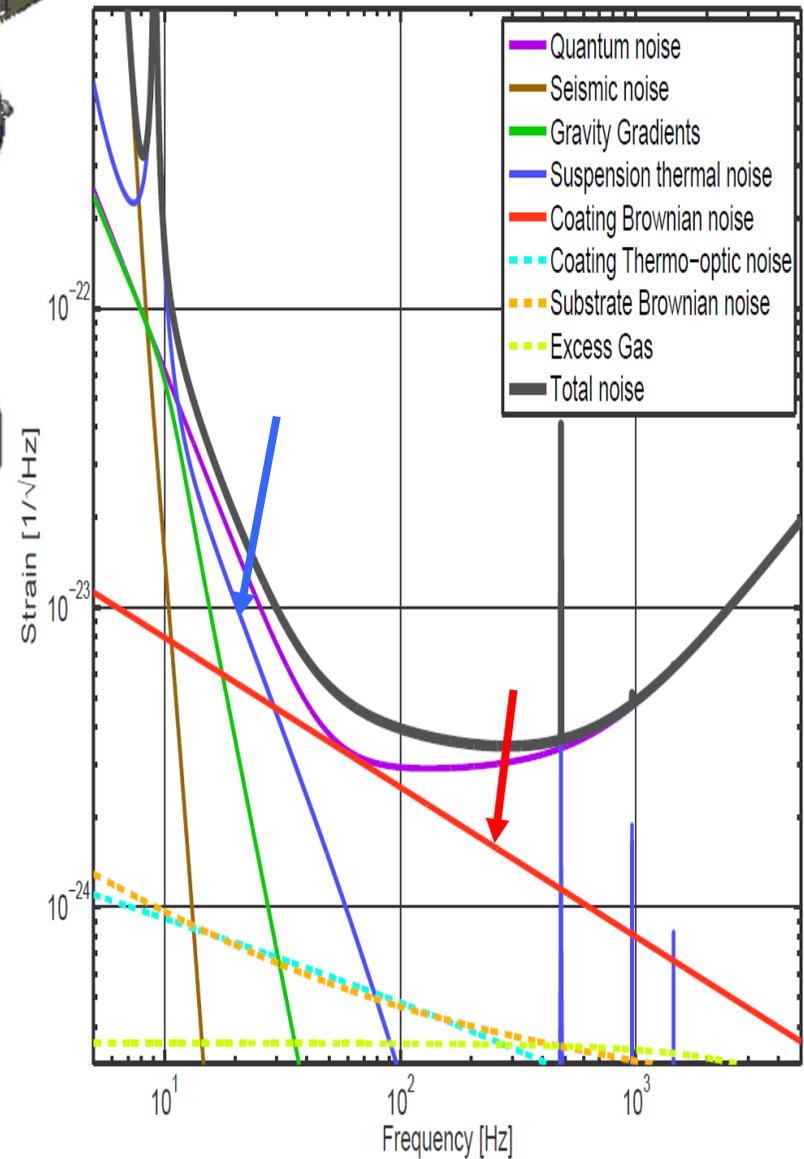
# The types of Thermal Noise

- Suspension



- Optic

- Coating (dominant)
- Substrate



# The types of Thermal Noise

$$dF(T, \vec{\epsilon}) = -SdT + \vec{\sigma}d\vec{\epsilon}$$

E.g. coatings

- Coating Brownian
  - Mechanical coating loss
  - Scales with beam area
  - Limiting 2<sup>nd</sup> gen. detectors

$$S_{xx} \approx \frac{4k_B T}{\pi f} \frac{\delta_c}{\pi w^2 Y} \phi$$

Coating Brownian

- Thermo-optic Noise

- Scales w/ beam area
- Key for crystalline coatings

$$S_{xx} \approx \frac{(\alpha_{\text{eff}} d - \beta_{\text{eff}} \lambda)^2 k_B T^2}{\pi w^2 \sqrt{\kappa \rho C f}}$$

Thermo-optic

Note :  $O(1)$  constants dropped (e.g. Poisson raito)

# ~~Coast-~~ Out-line

Types of thermal noise

Correlation length

Strategies for mitigation

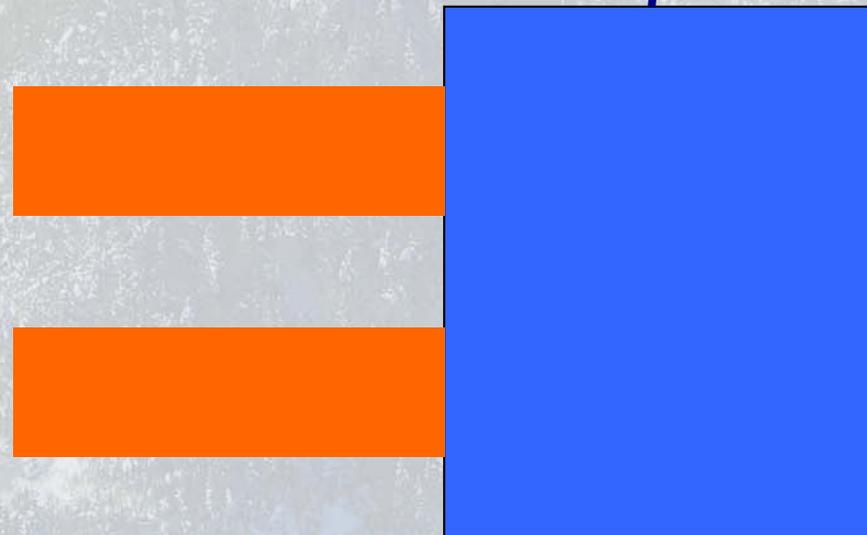
Examples

GWADW  
La Biodola,  
Isola d'Elba, Italy

May 2013  
Stefan Ballmer

# Correlation length

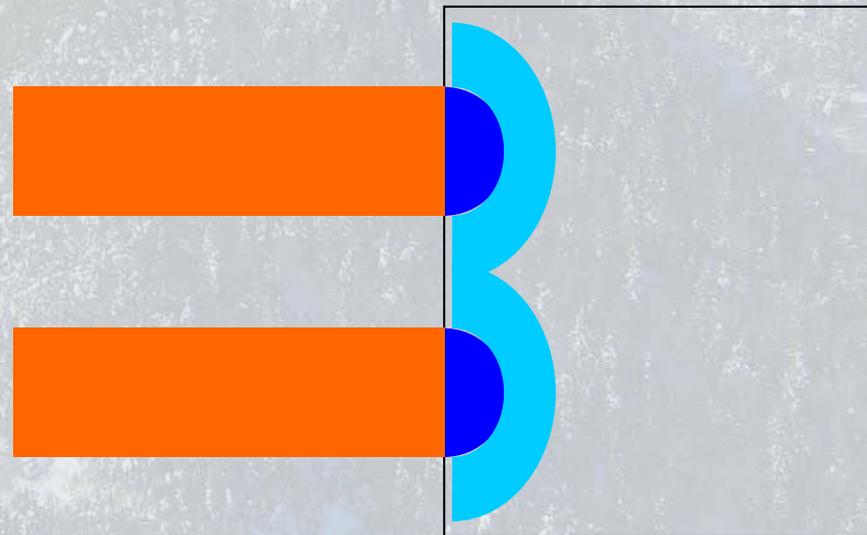
- Suspension thermal noise
  - Optic driven by suspension
  - Coherent motion over the whole optic



# Correlation length

- Substrate Brownian noise
  - Set by elastic Greens function
    - '1/x' convolved with beam profile
  - Correlation length  $\sim$  beam radius  $w$ 
    - Transverse correlation drop-off  $\sim 1/x$

Nakagawa et. al.  
PRD, vol 65, 082002



# Correlation length

- Coating Brownian noise

gr-qc/0610041v3 (2007)

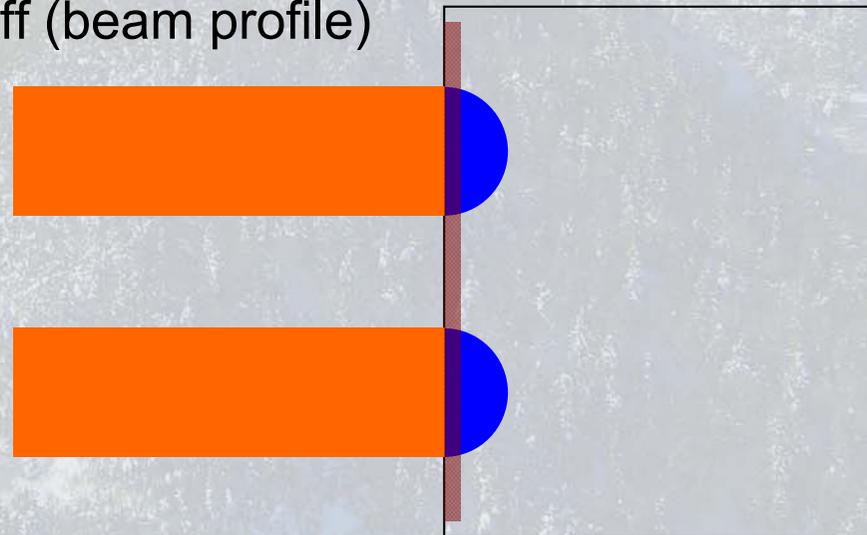
- Set by elastic Greens function

- But driven on surface only – short range!

- Correlation length, on surface

- Transverse correlation  $\sim$  coating  $d$  ( $\ll w$ )

- Exponential drop-off (beam profile)

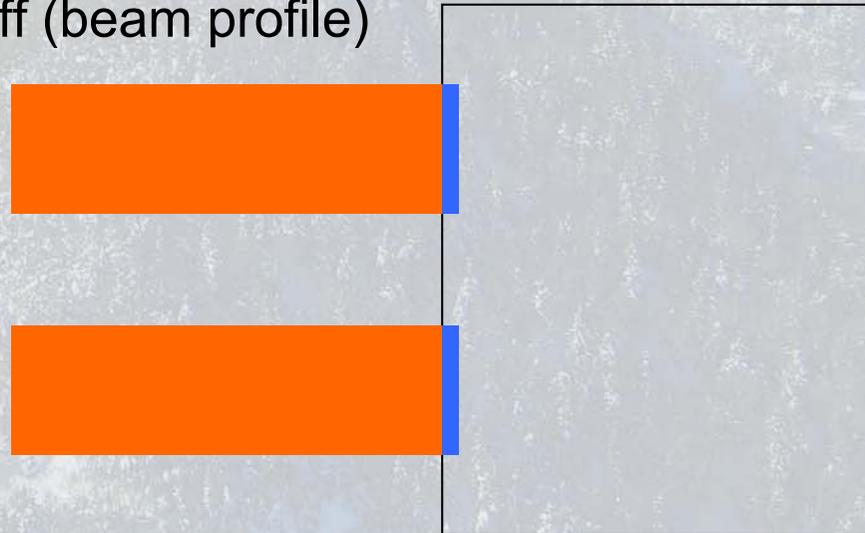


# Correlation length

- Thermo-optic noise
  - Set by (freq. dependent) diffusion length
  - Correlation length  $\sim$  diffusion length
    - $O(30\mu)$  around 100Hz
    - Transverse correlation  $\sim$  diff. length ( $\ll w$ )
      - Exponential drop-off (beam profile)

Caution: Not true for cryogenic reference cavities

small spot &  
large diffusion length



# ~~Coast-~~ Out-line

Types of thermal noise

Correlation length

Strategies for mitigation

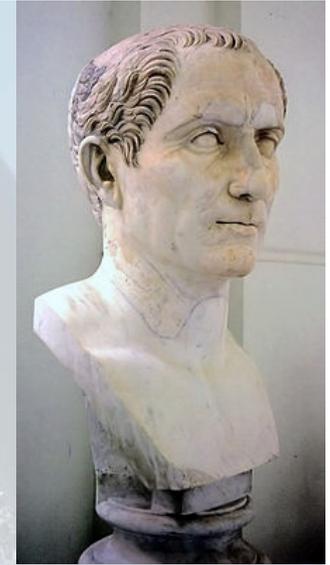
Examples

GWADW  
La Biodola,  
Isola d'Elba, Italy

May 2013  
Stefan Ballmer



# Strategies for Optical Thermal Noise Mitigation



- **Divide et impera**: avoid correlation
  - Add noise incoherently
  
- **The enemy of your enemy is your friend**  
Cancellation:
  - Coupling to fluctuations through 2 mechanisms with opposite sign

# Strategies for Optical Thermal Noise Mitigation

- **Divide et impera**
  - Transverse:
    - Large spots
    - Special beams: LG, flat-top, etc.
    - Multiple beams
  - Longitudinal: de-correlate dielectric layers
    - Khalili cavities

# Strategies for Optical Thermal Noise Mitigation

- **Cancellation:**
  - Through different coupling mechanisms  
e.g. for thermo-optic noise:  $\alpha$  and  $dn/dT$
  - Measuring and subtraction
    - Measure thermal noise independently (i.e. with no/different GW sensitivity)
    - Displacement-free interferometry

# ~~Coast-~~ Out-line

Types of thermal noise

Correlation length

Strategies for mitigation

Examples

GWADW  
La Biodola,  
Isola d'Elba, Italy

May 2013  
Stefan Ballmer

An aerial photograph of a vast, snow-covered mountain range. The terrain is rugged, with deep valleys and high peaks covered in dense evergreen forests. In the foreground, the white rotor blades of a helicopter are visible, indicating the viewer's perspective is from inside the aircraft. The sky is a clear, pale blue. The text "Divide et imperia!" is overlaid in a bold, red, sans-serif font, centered on the image.

**Divide  
et  
imperia!**

# Big Gaussian

- Long arms!
  - ALL (amplitude) displacement noises:  $\sim L^{-1}$
  - Thermal noise:  $\sim L^{-1.5}$  (beam spot grows with  $L$ )
- For fixed arms
  - Rapidly approaching **degeneracy** for significant beam size increases



# Laguerre-Gaussian beams

- Effective beam area larger - Noise averages
  - For LG33: x1.61 (in power noise)

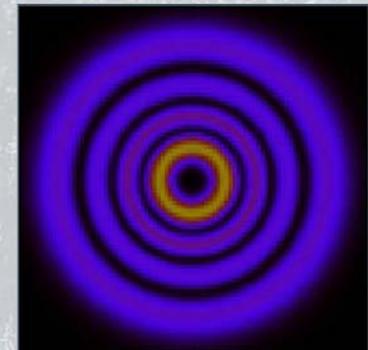
$$S_x \propto \frac{\int I^2(\vec{r}) d^2\vec{r}}{[\int I(\vec{r}) d^2\vec{r}]^2}$$

- But modes are degenerate
  - Contrast defect unacceptable

PRD 84, 102001 (2011)

- Ideas for thermal correction

PRD 87, 082003 (2013)



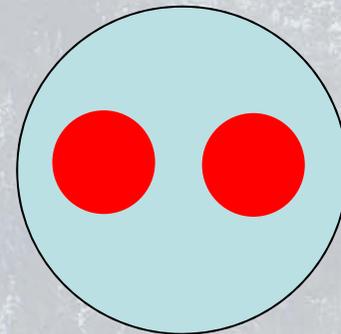
LG33 beam

# Other beam shapes

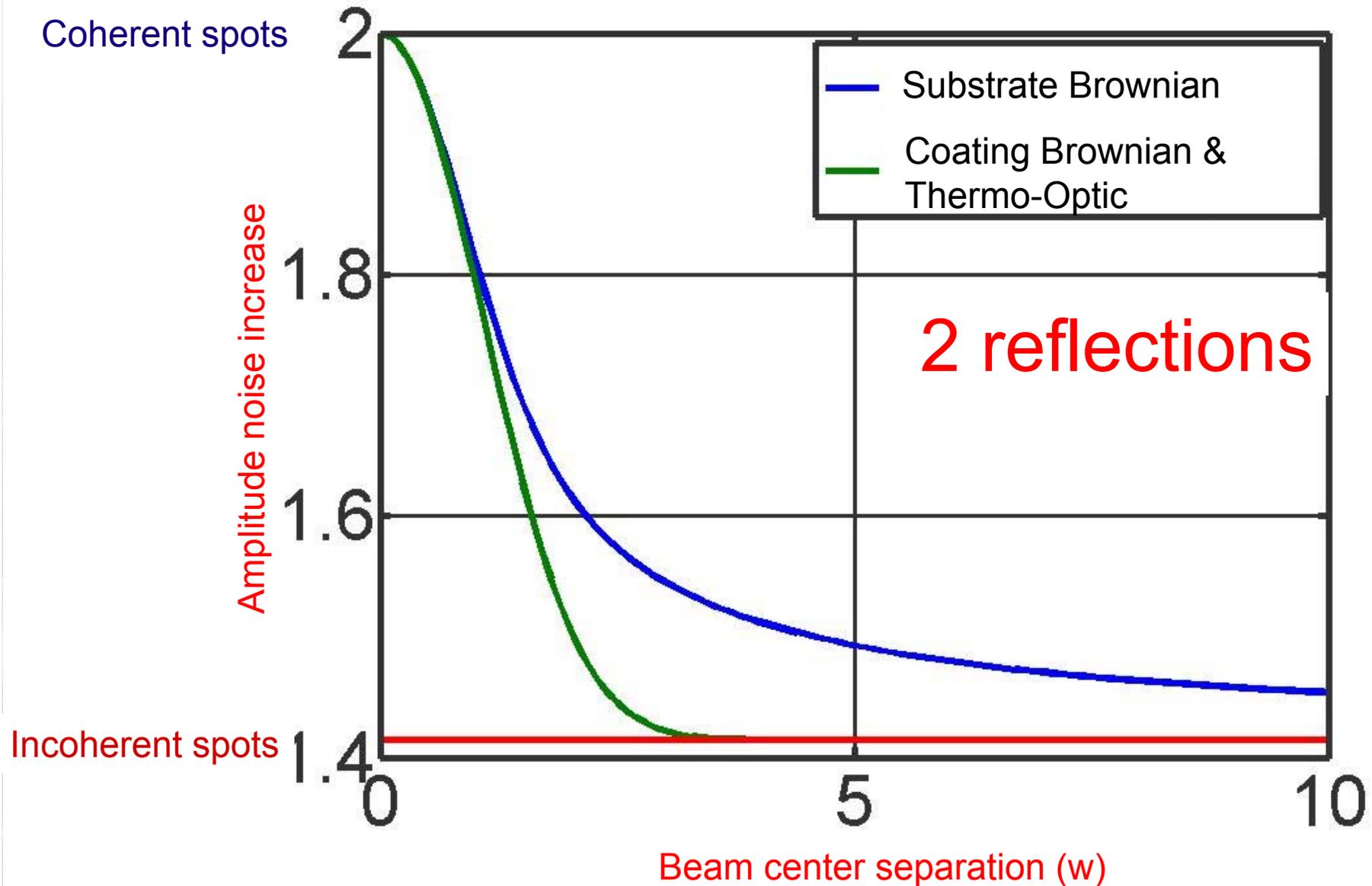
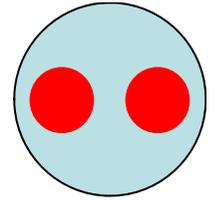
- Laguerre-Gauss: uses spherical mirrors
- Idea: Choose **other mirror profiles**
  - e.g. Flat-top beams, conical beams
  - Avoids degeneracy problem
  - Issues
    - Beam profile not conserved under propagation
    - Alignment (beam shape changes)

# Multiple beams

- TEM00 is good – use more of them!
- Multiple spots per mirror
  - exploit spatial de-correlation

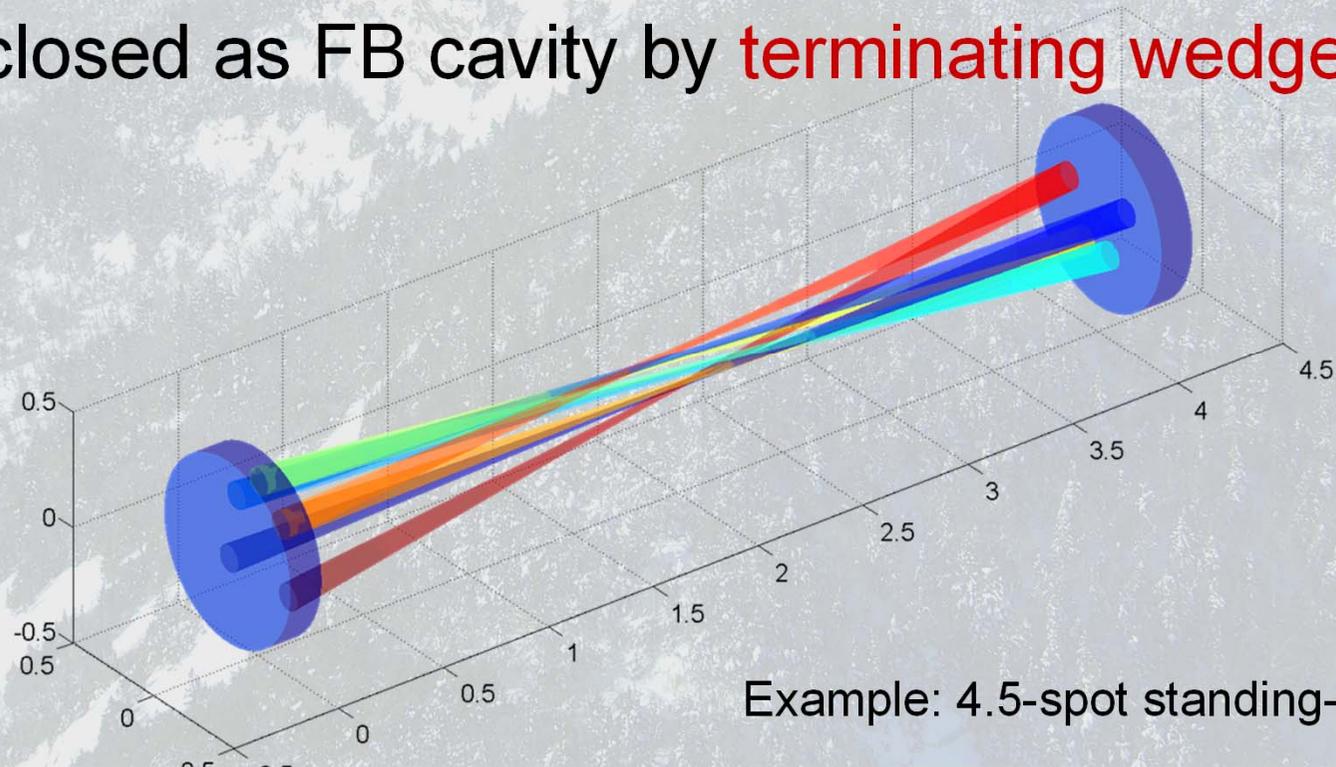


# Spatial correlation (for TEM00)



# Realizing multiple beams

- Delay line with spherical mirrors (Herriot, APPLIED OPTICS, Vol. 4, No. 8 (1965))
  - **g-factor** determines beam orbit
  - Size and ellipticity of orbit **unrestricted**
  - closed as FB cavity by **terminating wedges**

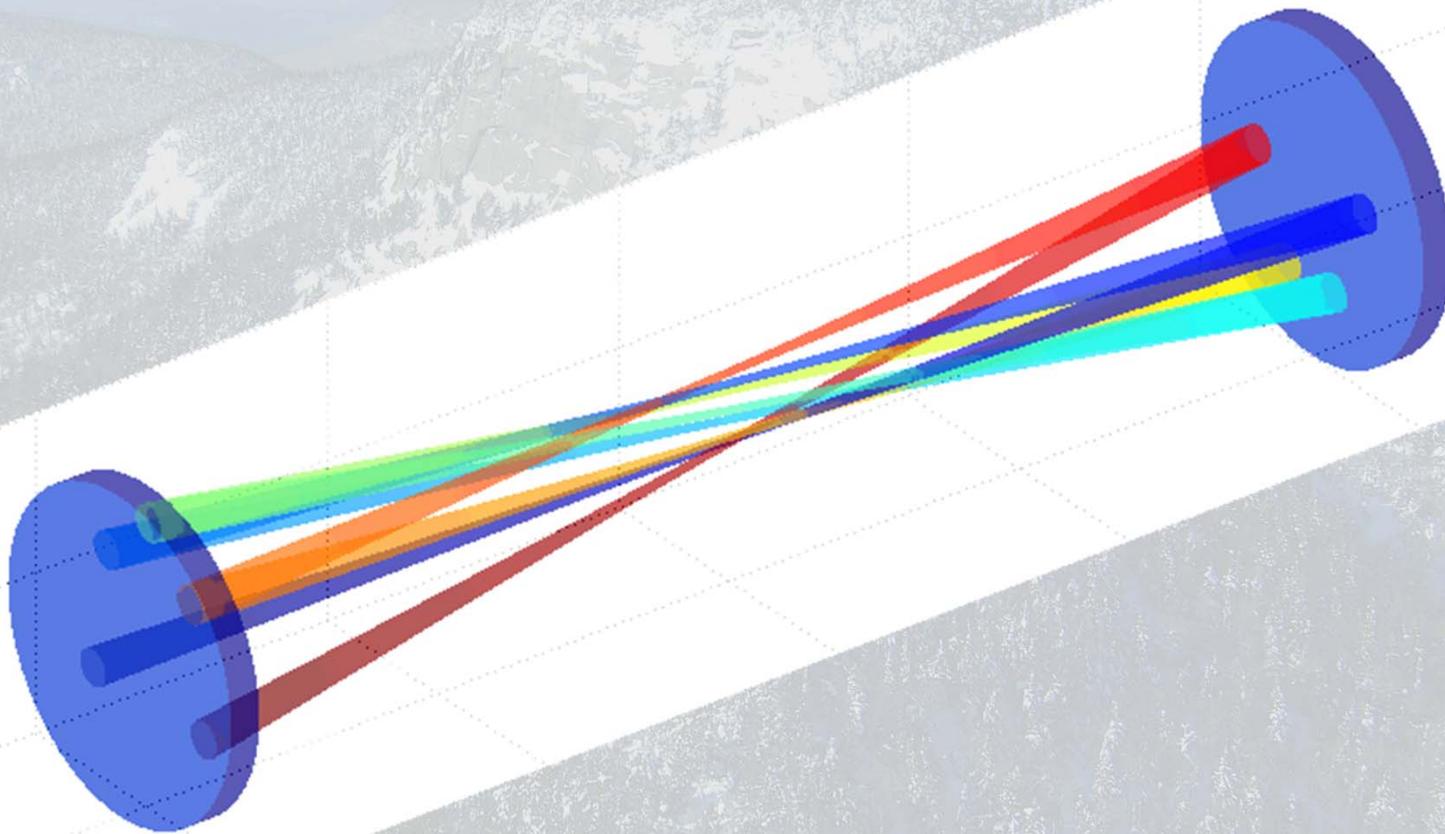


Example: 4.5-spot standing-wave cavity

# Optimizing spot locations and size

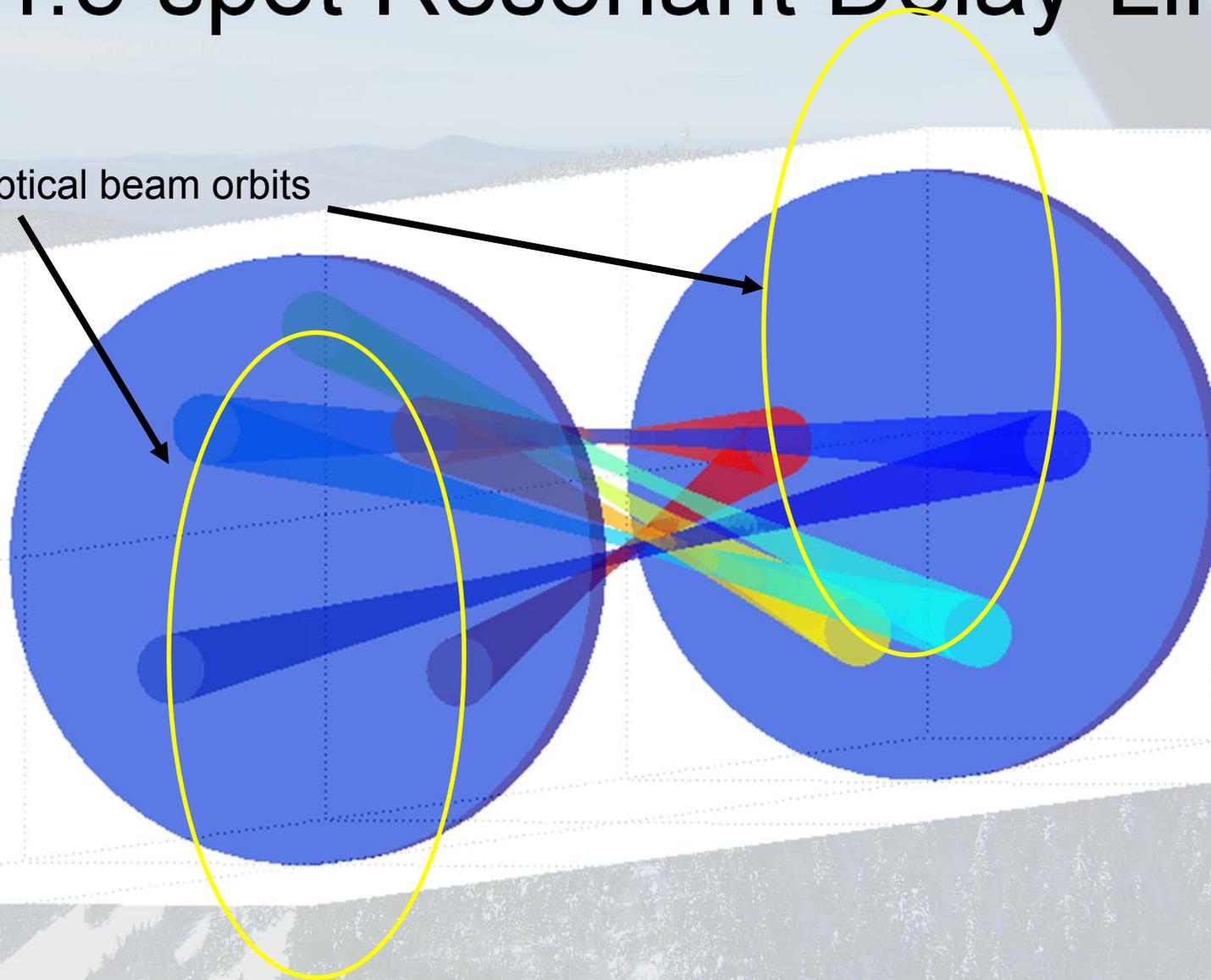
- Both individual spot size and # of spots per orbit directly dependent on **g-factor**
  - E.g. aLIGO  $g=0.83$ , #spots = 7.40
- # reflections limited to  $\sim < 10$ 
  - (no sensitivity at **FSR**= $c/(2*N*L)$ )
- Possible solution:
  - Optimize **g-factor** for big beam spot
  - Inject beams in an **elliptical orbit**
  - Use less than one full orbit

# Example: 4.5 spot Resonant Delay Line

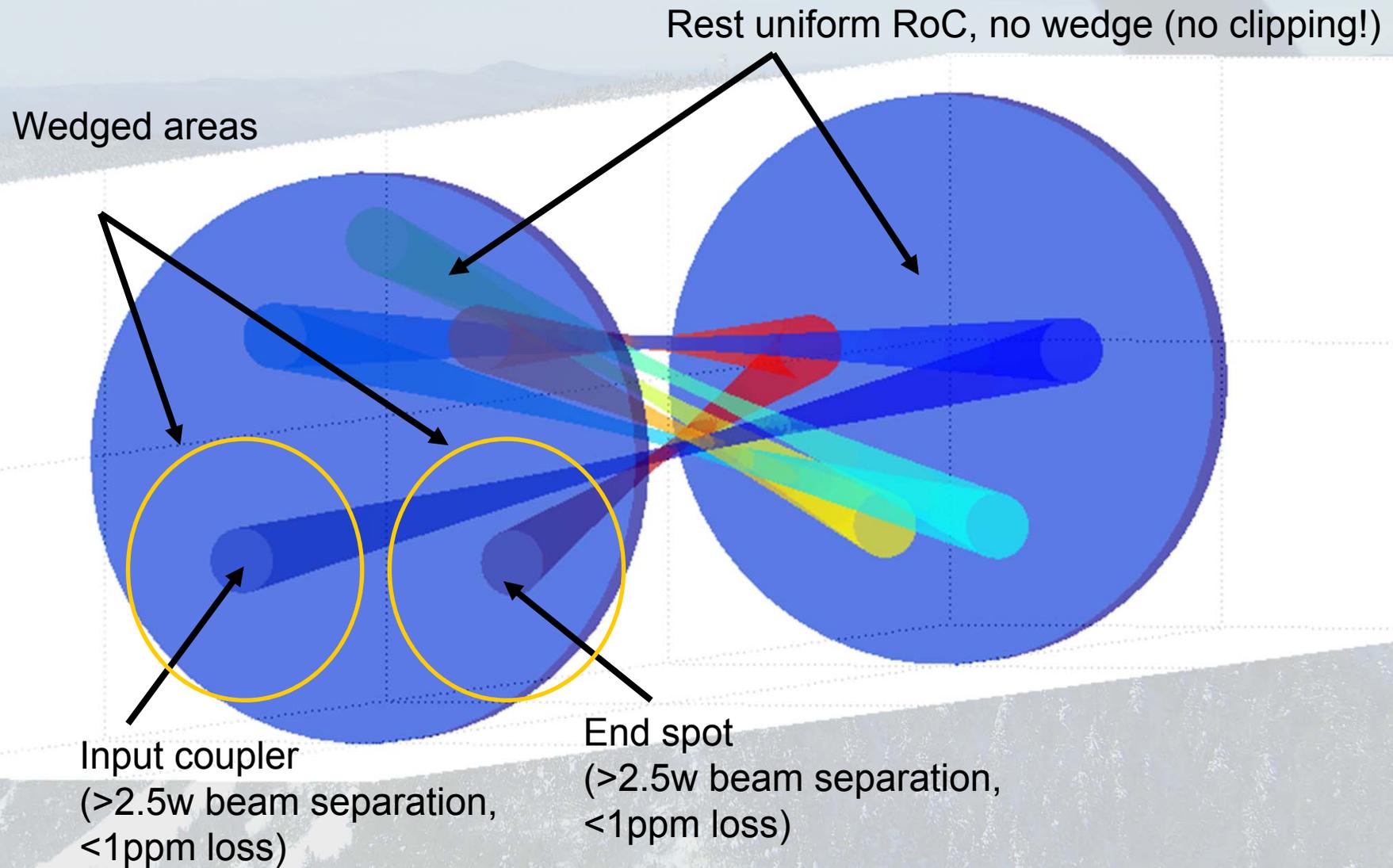


# 4.5 spot Resonant Delay Line

Elliptical beam orbits



# 4.5 spot Resonant Delay Line



# Easier than traditional delay lines!

- N **much smaller** than traditional delay lines
- Two mirrors **define optical mode**
  - No “threading of the beam”
  - Mode-matching identical to regular FB cavity
  - As easy to align as a regular FB cavity
- **Scatter**
  - Exists, but cavity is locked, no fringe wrapping
- Alignment sensitivity
  - **identical** to simple 2-mirror FB cavity

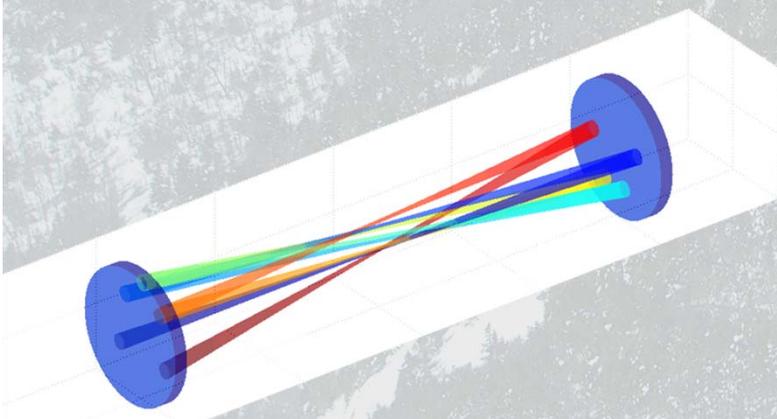
# Alignment signals / Spot motion

- RDL with 4 ETM and 5 ITM spots, all same size as aLIGO

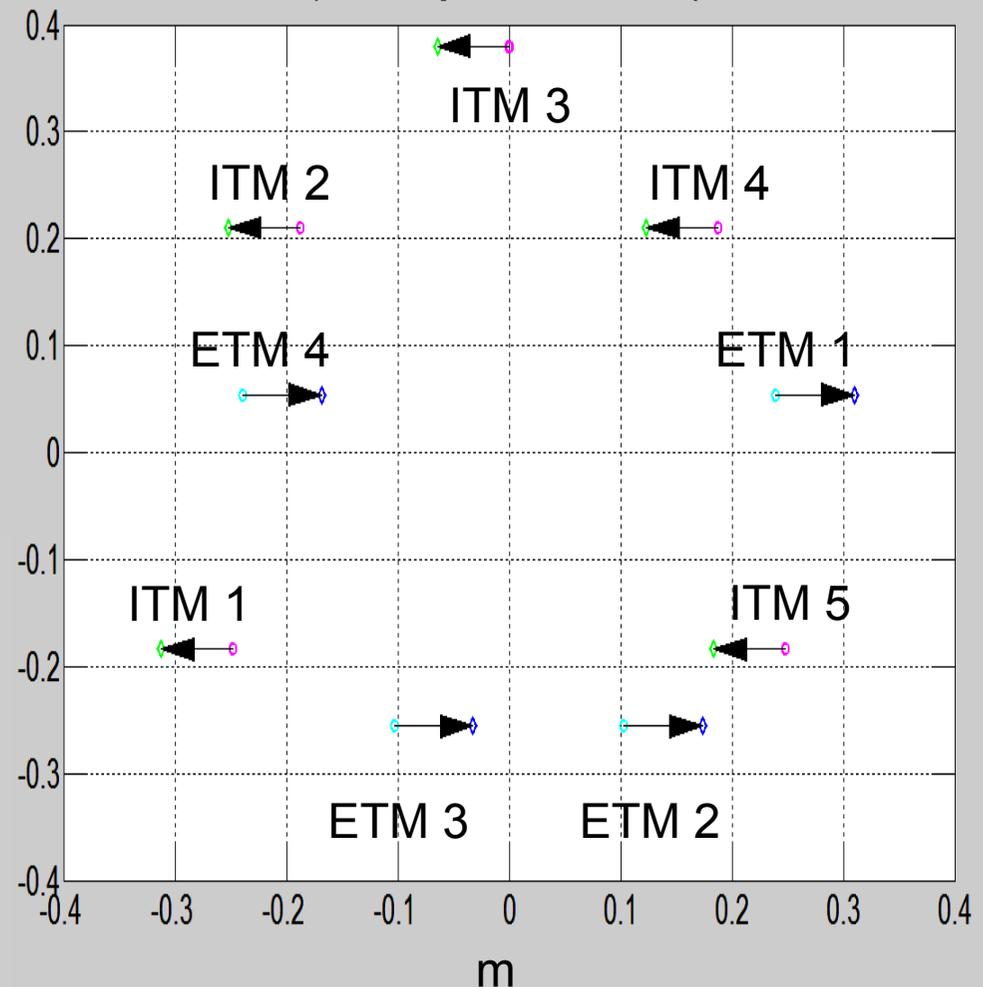
- $w=57.3\text{mm}$

- For 3urad ITM misalignment

- Spot move 6.4cm  $\epsilon$
- (identical to aLIGO)

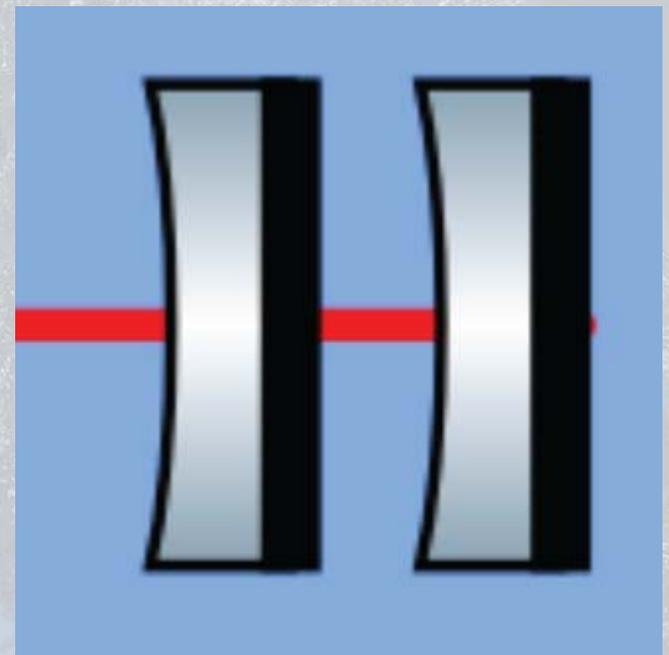


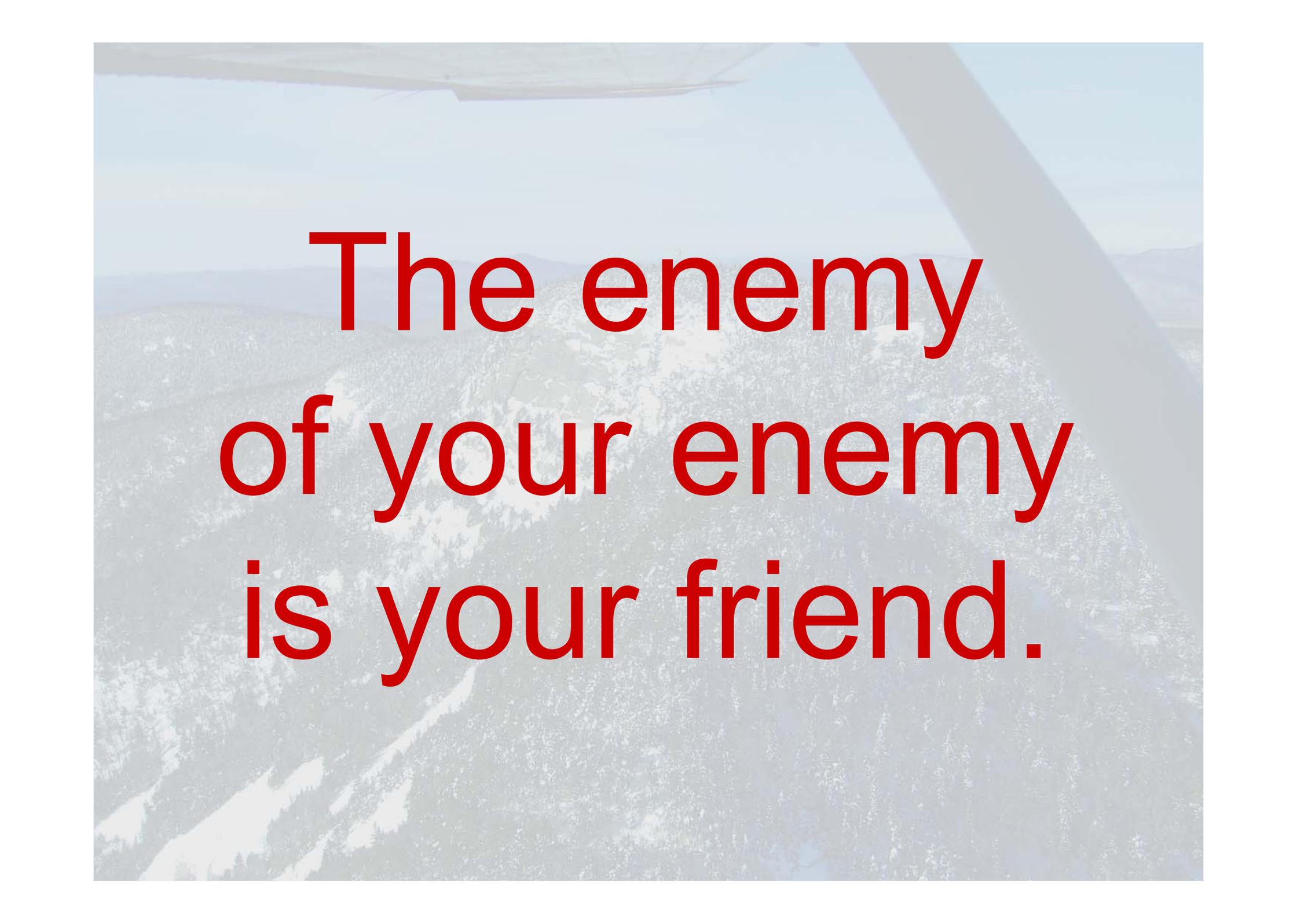
4.5-spot Standing-Wave Resonant Delay Line



# Khalili cavity

- Split single mirror (dielectric stack) into anti-resonant cavity (Phys Let A V334, 1, 2005, 67-72)
  - TN of the **two mirrors uncorrelated**
  - Only ~2-doublet stack on M1
  - M2 high reflector
- Requires 2x the mirrors, incl. control system...



An aerial photograph of a mountain range covered in snow and evergreen trees. The sky is clear and blue. In the upper left corner, the wing of an aircraft is visible, suggesting the photo was taken from a plane. The text is overlaid in the center of the image.

**The enemy  
of your enemy  
is your friend.**

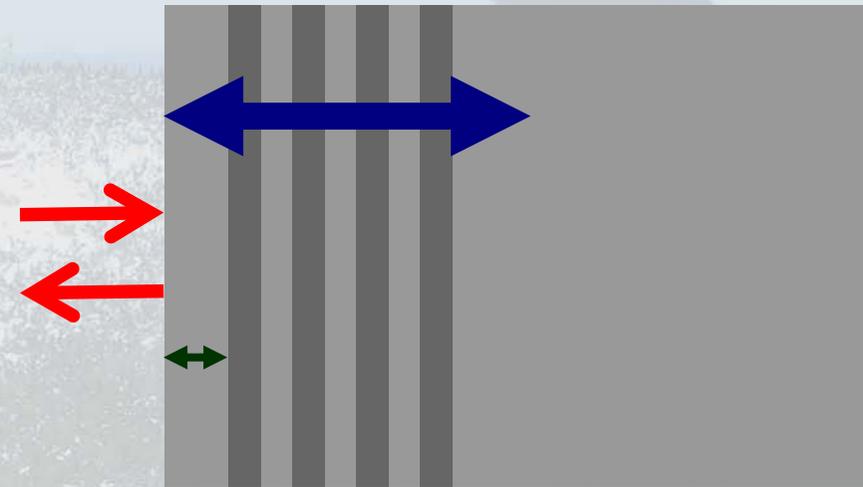
# Thermo-optic cancellation

- 2 enemies
  - thermal expansion,  $\alpha$
  - $dn/dT$ , tunable
  - **opposite** sign

- Thermal diffusion matters:

- $d \ll r_{diff}$  :
  - Noise is coherent

$$r_{diff} = \sqrt{\frac{\kappa}{2\pi f C}} \approx 40\mu @ 80\text{Hz}$$



Coating depth



Electric field

Coating depth

30

# Brownian cancellation?

- Same idea for Brownian noise...

- $dn/d\sigma$  : photo-elastic coupling

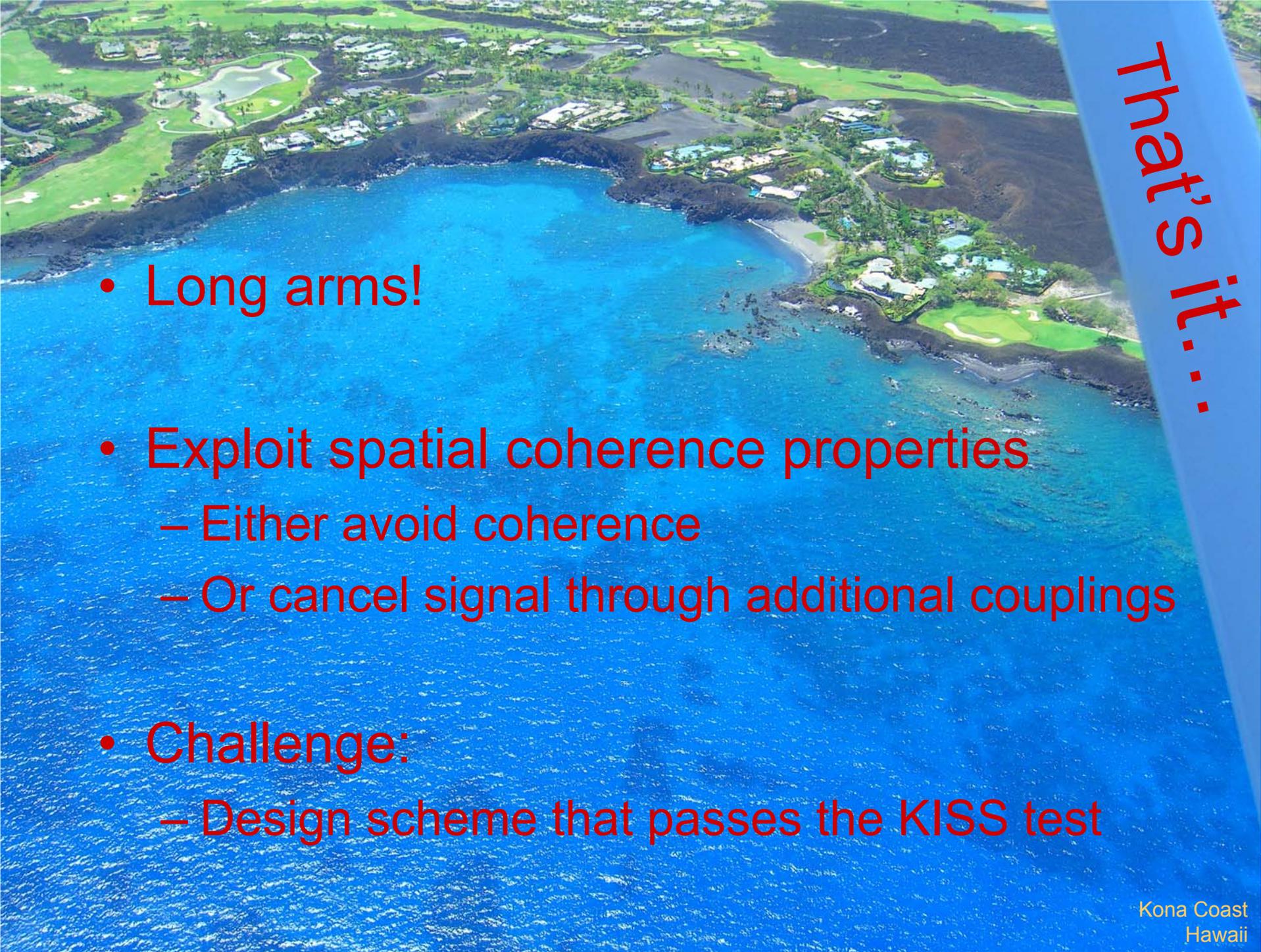
PRD 87, 082001 (2013)

- Small for  $\text{SiO}_2:\text{Ta}_2\text{O}_5$

- Check for crystalline coatings ?

# Sensing thermal noise

- TN could be measured by 2<sup>nd</sup> interferometer
  - need comparable sensitivity...
- Displacement-free interferometry
  - Displacement couples at discrete times ( $t-nT$ )
  - GW strain couples continuously
  - Devise readout that cancels signals at ( $t-nT$ ), but preserves (some) GW sensitivity
    - Effectively AC-couples the signal...



That's it...

- Long arms!
- Exploit spatial coherence properties
  - Either avoid coherence
  - Or cancel signal through additional couplings
- Challenge:
  - Design scheme that passes the KISS test

# Conclusion

- Long arms!
- Exploit spatial coherence properties
  - Either avoid coherence
  - Or cancel signal through additional couplings
- Challenge:
  - Design scheme that passes the KISS test