



# Optical measurements at cryogenic temperatures

J. Komma, G. Hofmann, C. Schwarz, P. Pastrick, D. Heinert and  
R. Nawrodt

Institut für Festkörperphysik, Friedrich-Schiller-Universität Jena

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GWADW Elba

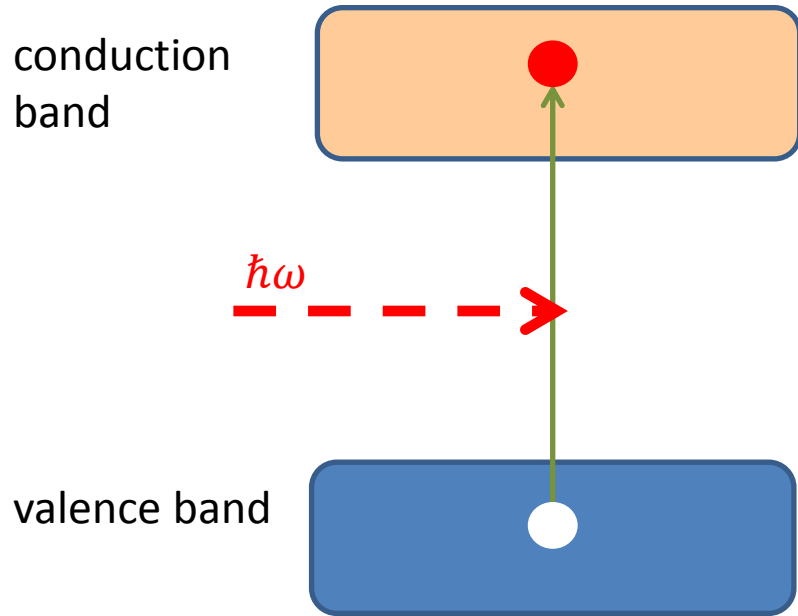


# Outline

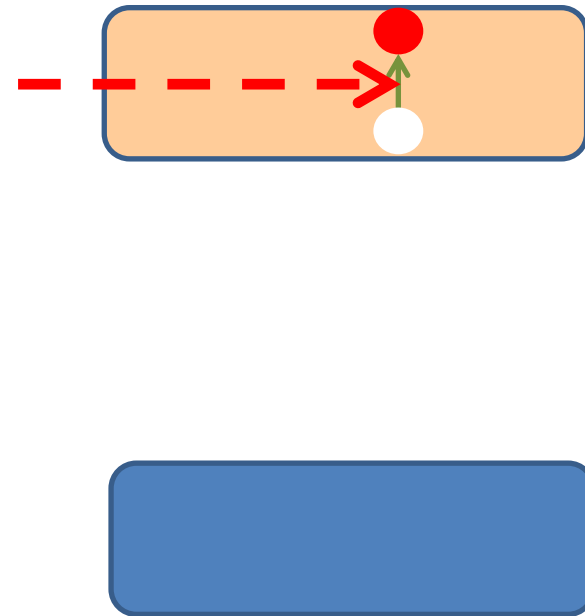
- absorption processes in semiconductors
  - direct/indirect semiconductors
  - phonon assisted absorption
  - electronic absorption measurement
- absorption measurement techniques
  - deflection
  - calorimetric
- temperature dependent absorption measurements of silicon
  - influence of doping



# Absorption processes in semiconductors



band band absorption/  
inter band absorption



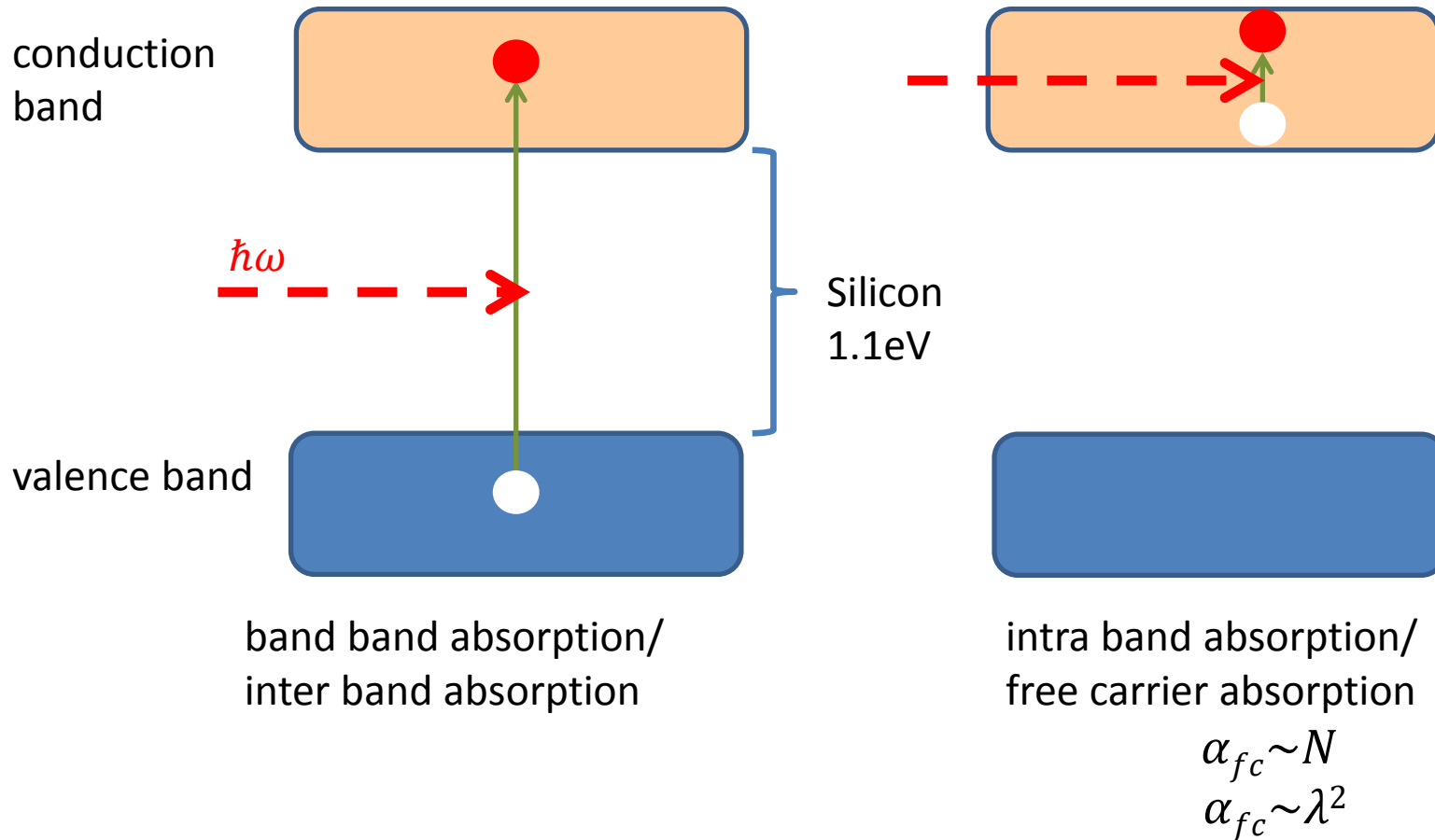
intra band absorption/  
free carrier absorption

$$\alpha_{fc} \sim N$$

$$\alpha_{fc} \sim \lambda^2$$

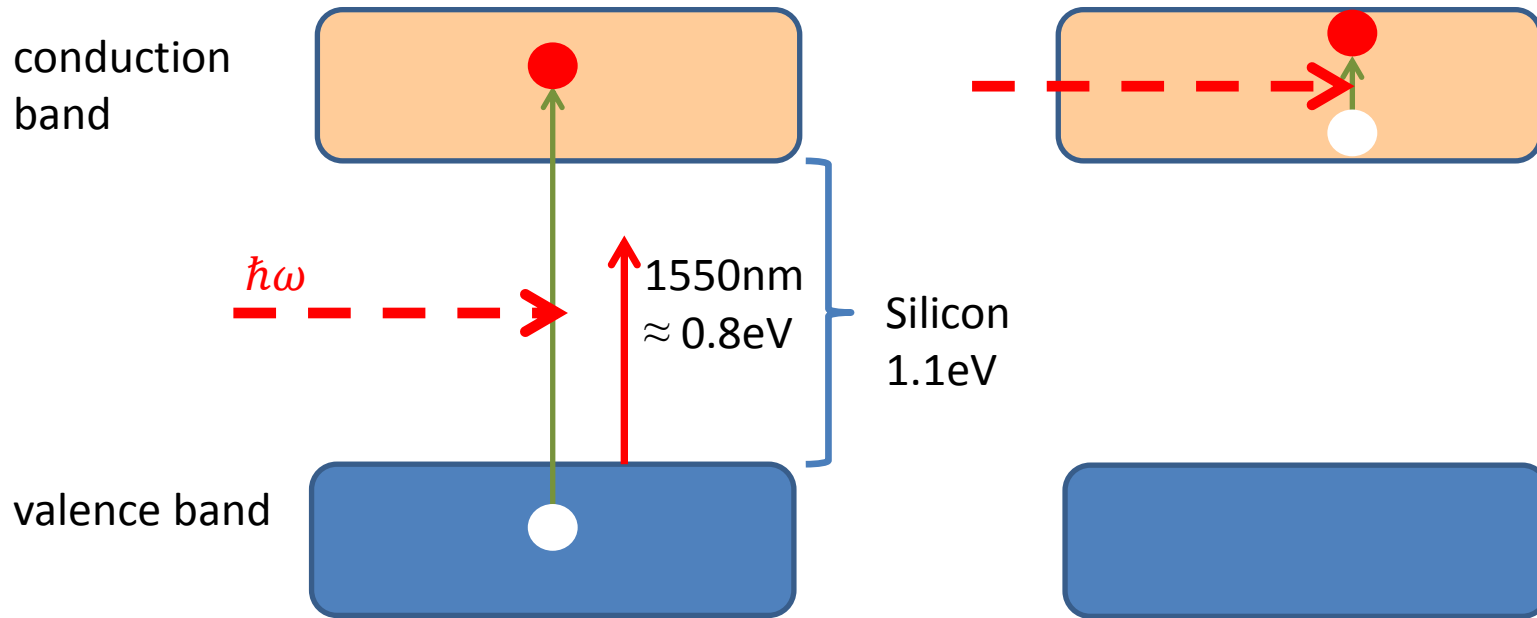


# Absorption processes in semiconductors





# Absorption processes in semiconductors



band band absorption/  
inter band absorption

intra band absorption/  
free carrier absorption

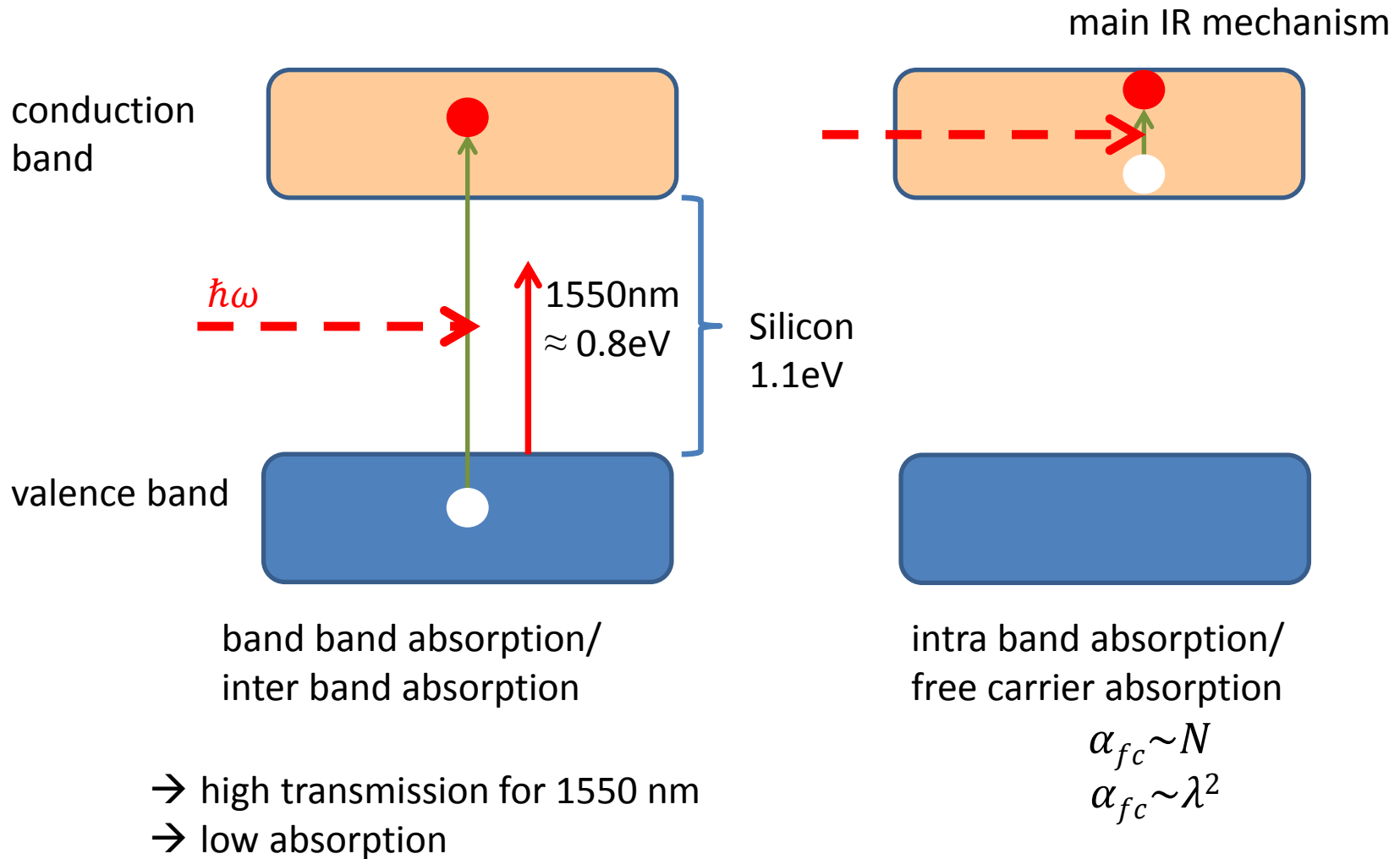
- high transmission for 1550 nm
- low absorption

$$\alpha_{fc} \sim N$$

$$\alpha_{fc} \sim \lambda^2$$



# Absorption processes in semiconductors

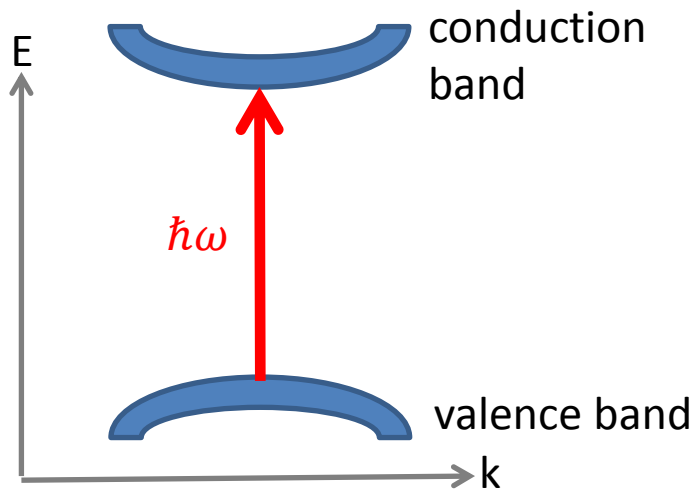




# Direct and indirect semiconductors

## Direct semiconductor

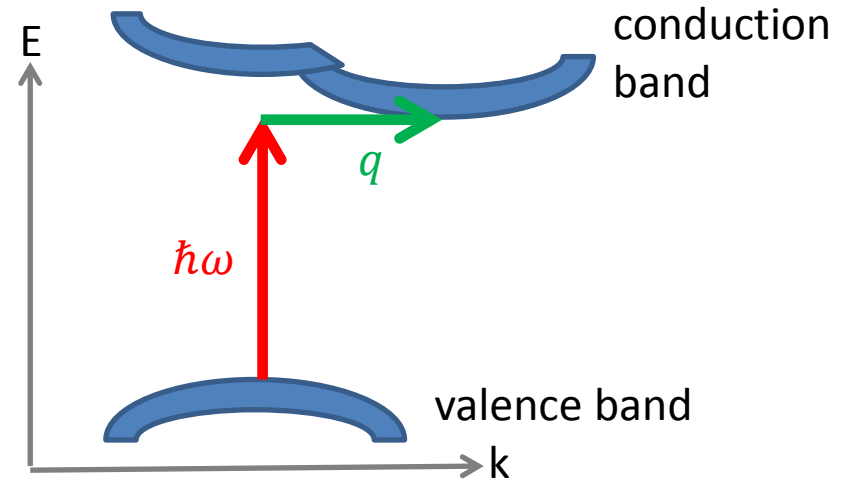
- typical: GaAs
- energy of a photon  $\hbar\omega$
- momentum of a photon  $\approx 0$



$$\alpha_{direct HL} \sim (\hbar\omega - E_g)^{1/2}$$

## Indirect semiconductor

- typical: Si, Ge
- energy of a photon  $\hbar\omega$  + momentum of a phonon  $q$

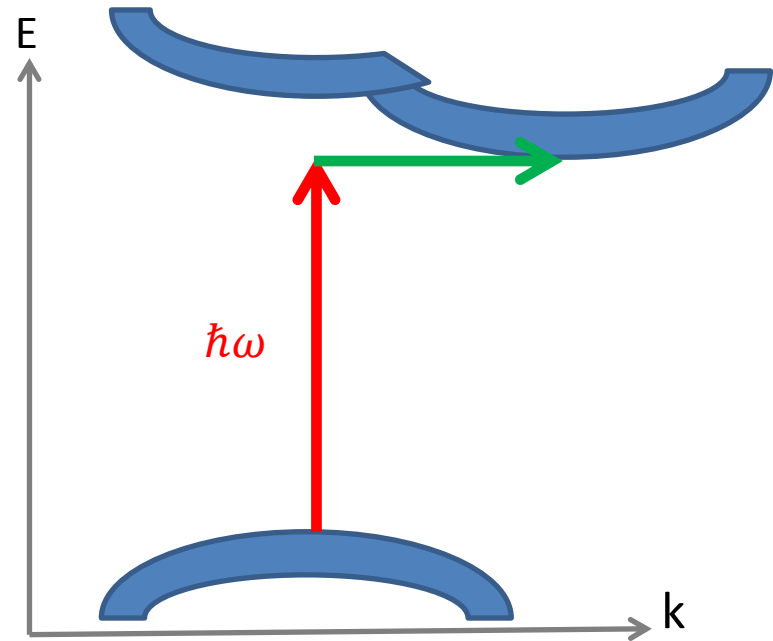
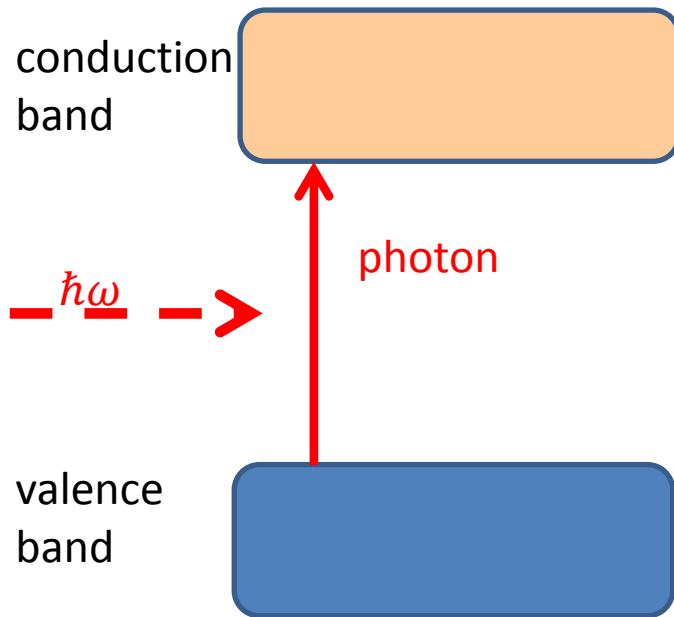


$$\alpha_{indirect HL} \sim (\hbar\omega - E_g \pm \hbar\Omega)^2$$



# Phonon assisted band-band absorption

- band band absorption

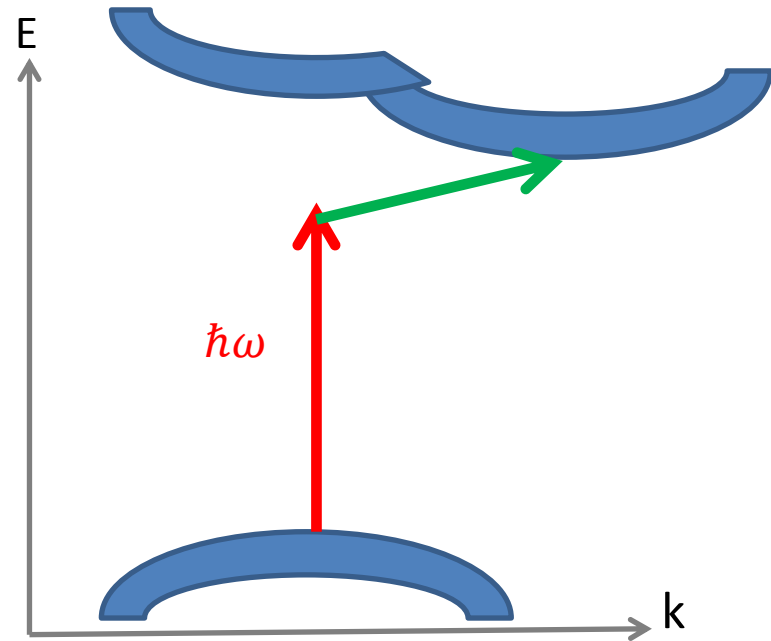
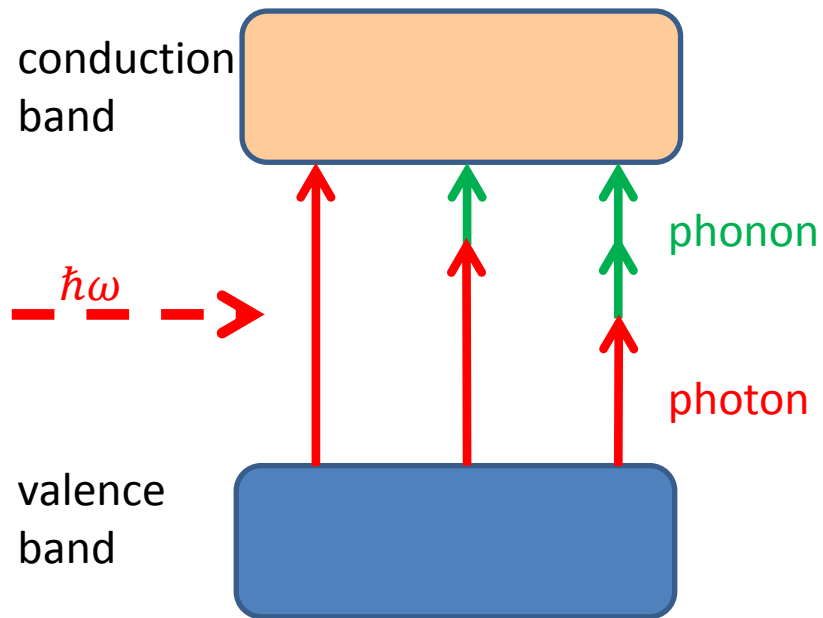






# Phonon assisted band-band absorption

- band band absorption

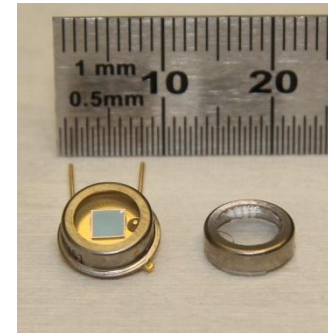
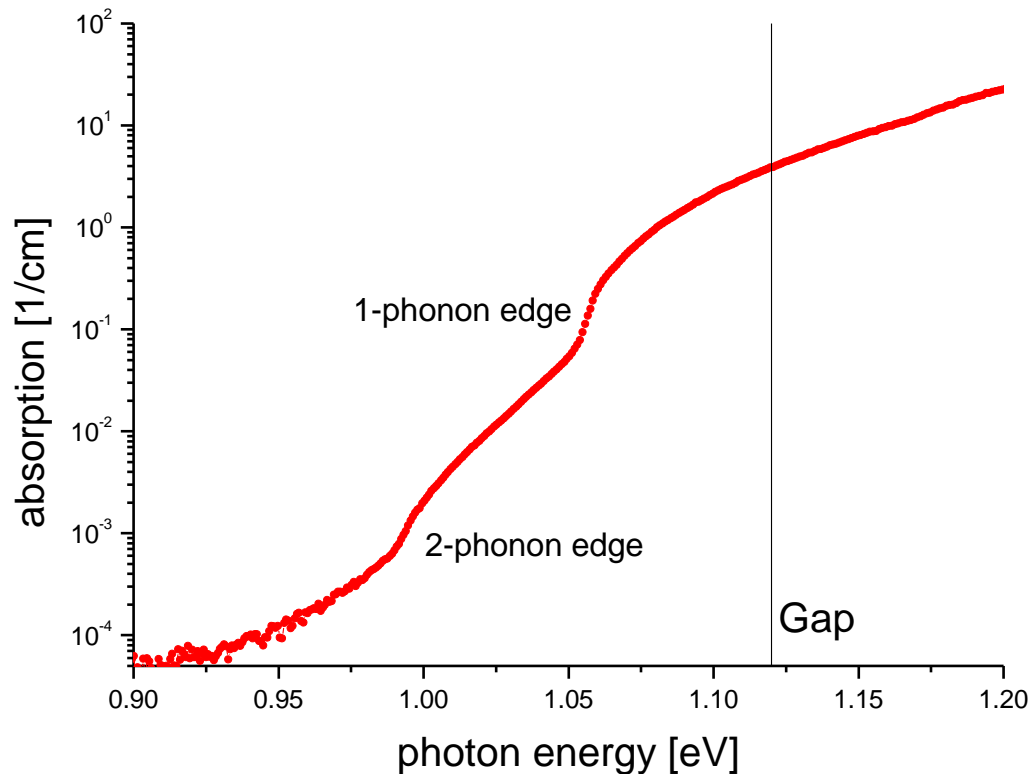


→ absorption below the gap energy is possible

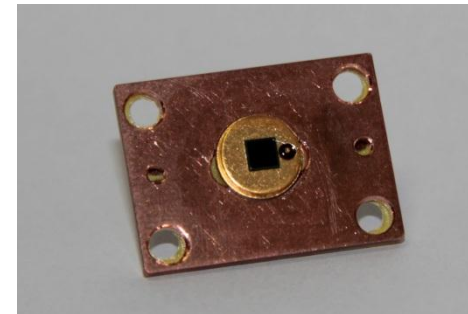


# Electronic absorption

due to phonons absorption below the energy gap is possible



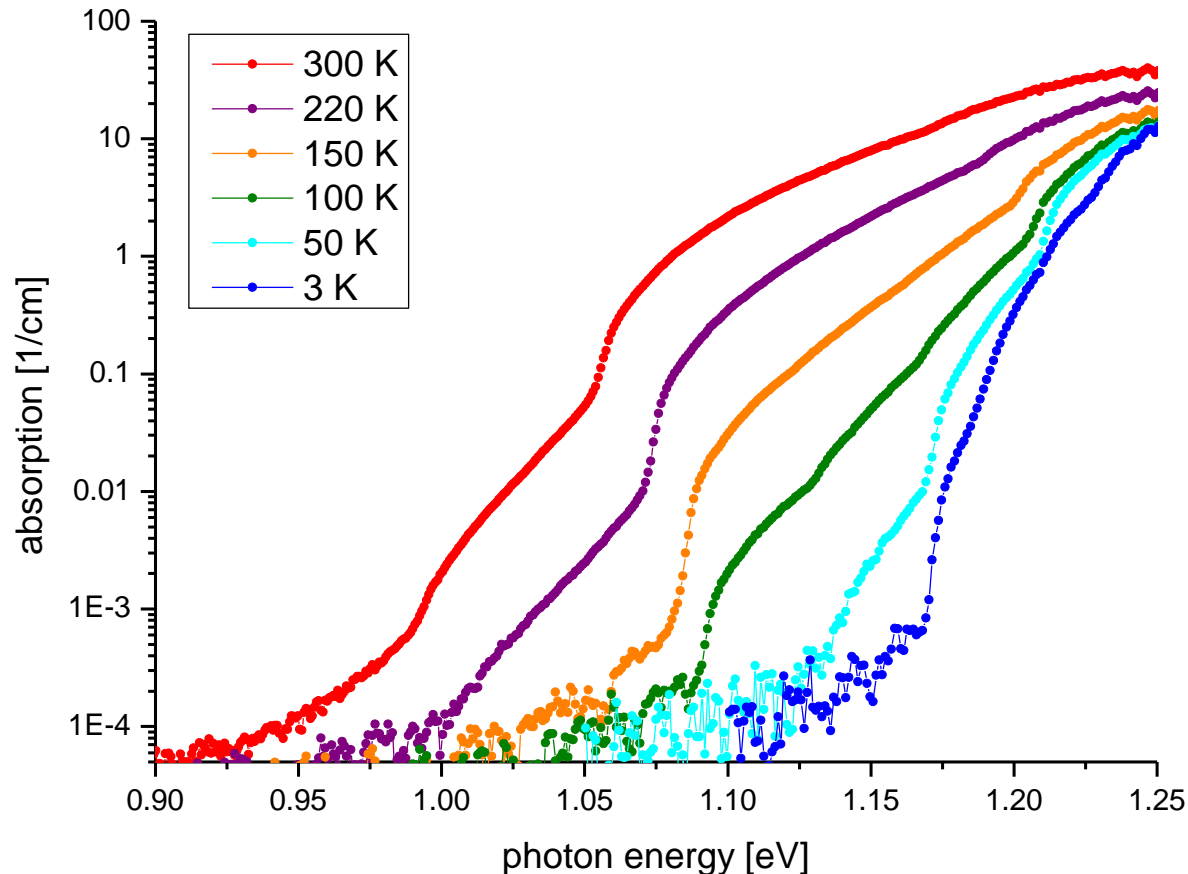
silicon photodiode



photodiode inside  
a sample holder



# Temperature dependent absorption



- for lower temperatures phonons freeze out → absorption below the gap is getting smaller

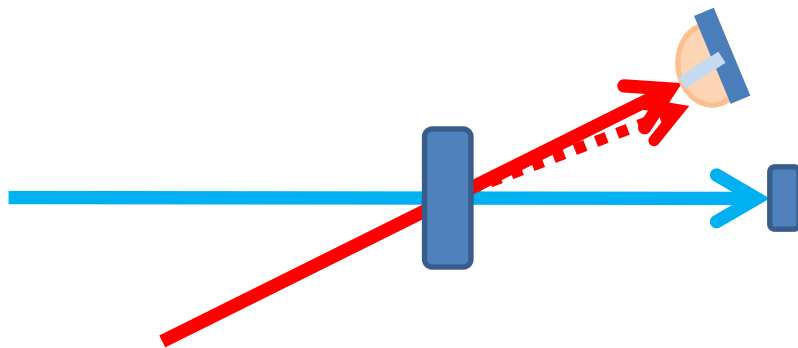
→ poster



# Absorption measurement setups

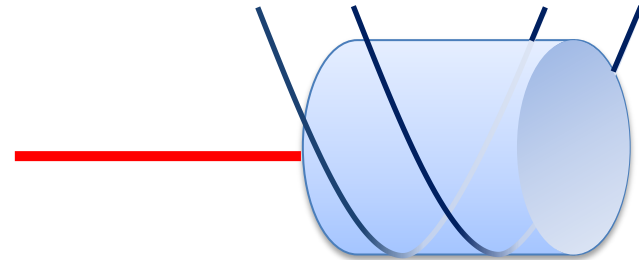
## Deflection/Mirage effect

- state of the art technology
- sensitivity  $< \text{ppm/cm}$  possible
- in-depth resolution
- bulk and coating can be measured
- calibration or modeling needed



## Calorimetric

- heating the sample with a laser  
→ measure the temperature rise  
→ calculate the absorption
- no need for a focused laser beam
- high sensitivity at low temperatures

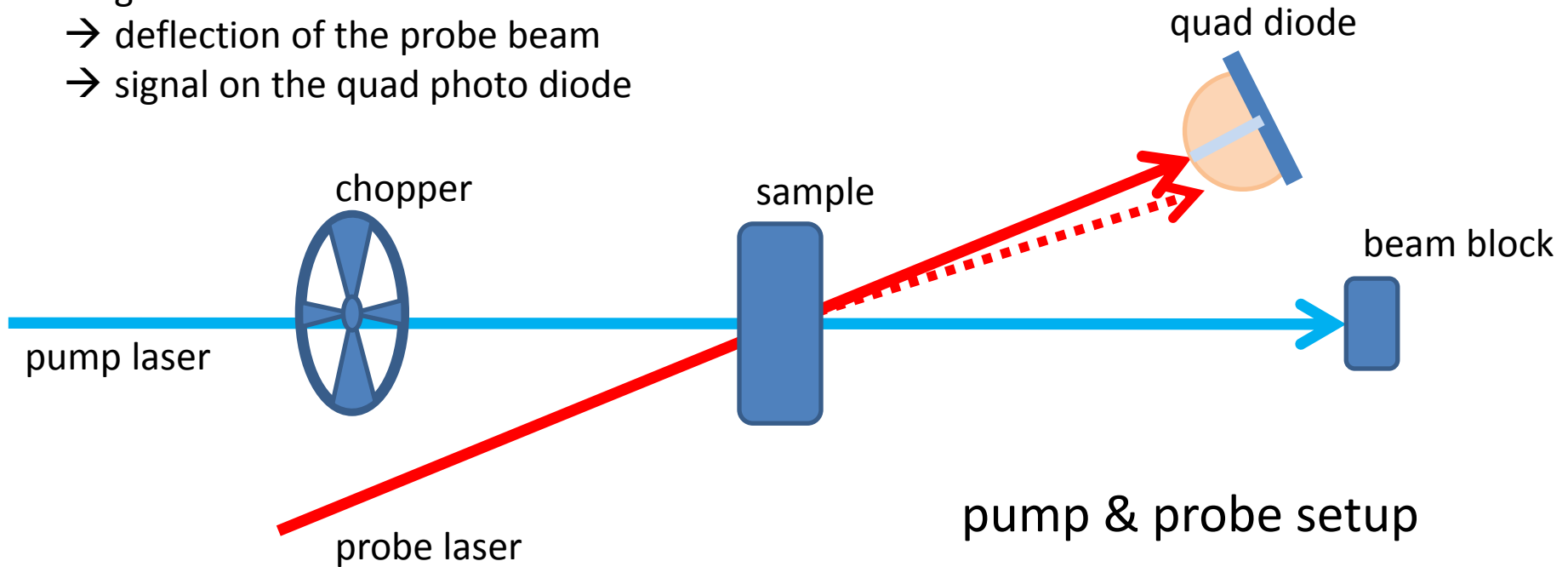




# Mirage / deflection measurement

heating the sample with the pump laser beam

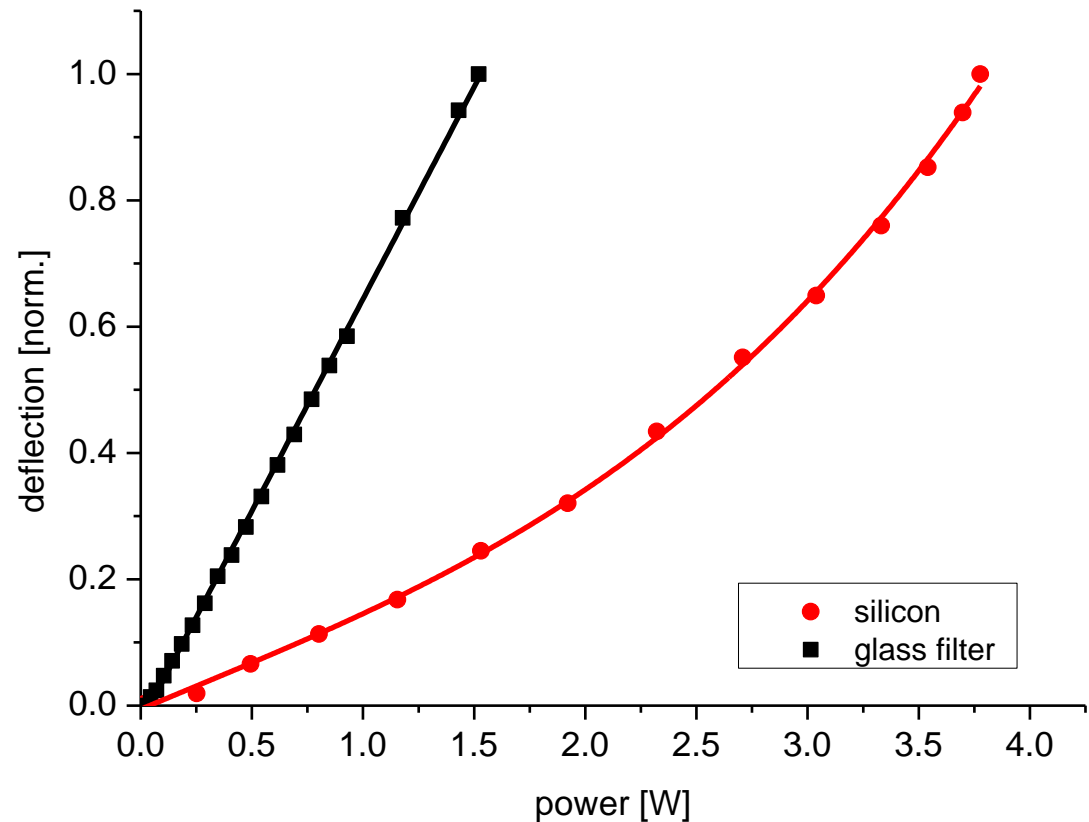
- generation of a thermal lens
- deflection of the probe beam
- signal on the quad photo diode





## Deflection measurement (pump & probe)

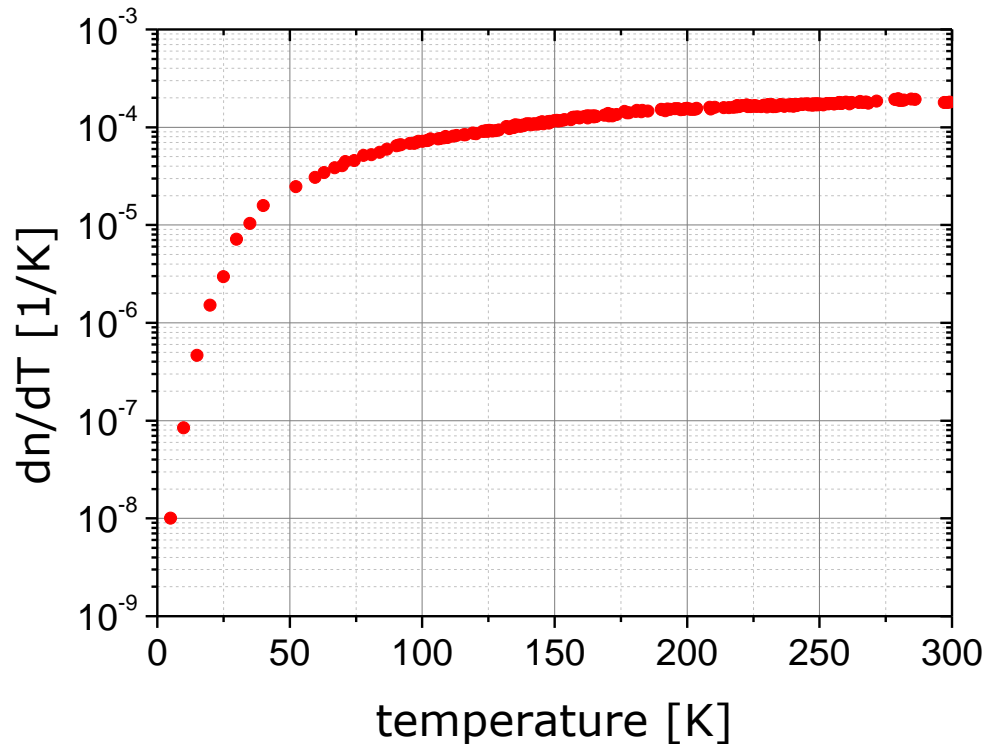
- calibration necessary
- for high laser power and small laser beam size
  - non linear effect (two photon absorption)
  - quadratic rise of the absorption with the laser power





## Deflection measurement (pump & probe)

- → sensitivity loss down to lower temperatures  
→ but measurement still possible → next talk



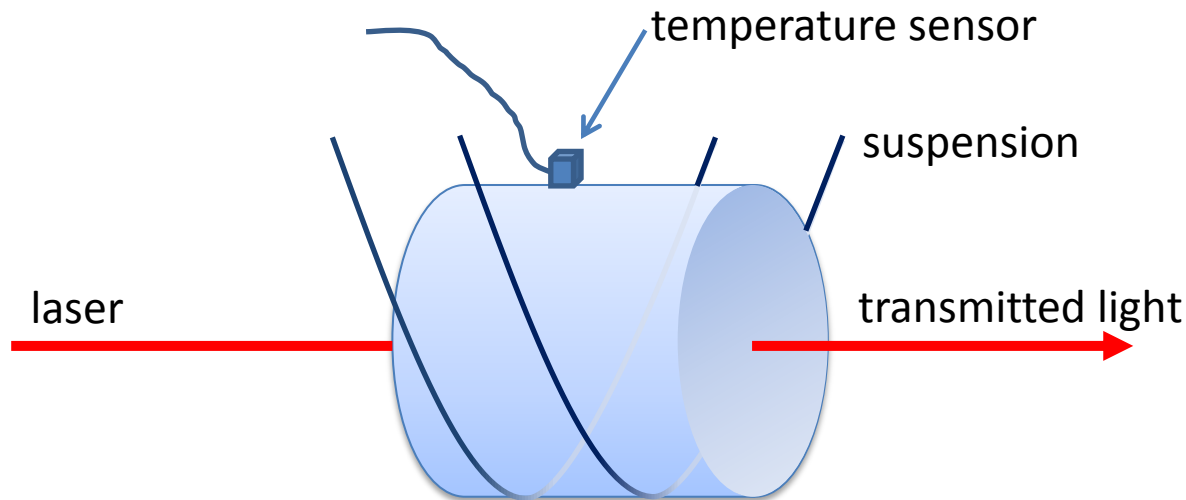
J. Komma, C. Schwarz, G. Hofmann, D. Heinert, and R. Nawrodt, Appl. Phys. Lett. 101, 041905 (2012).



# Calorimetric absorption measurement

- Calorimetric measurement  $\rightarrow$  measure the temperature rise  $\Delta T$  due to the absorbed laser power  $P_{abs}$  in a time  $\Delta t$  :

- $$\Delta T = \frac{\Delta t P_{abs}}{m C}$$



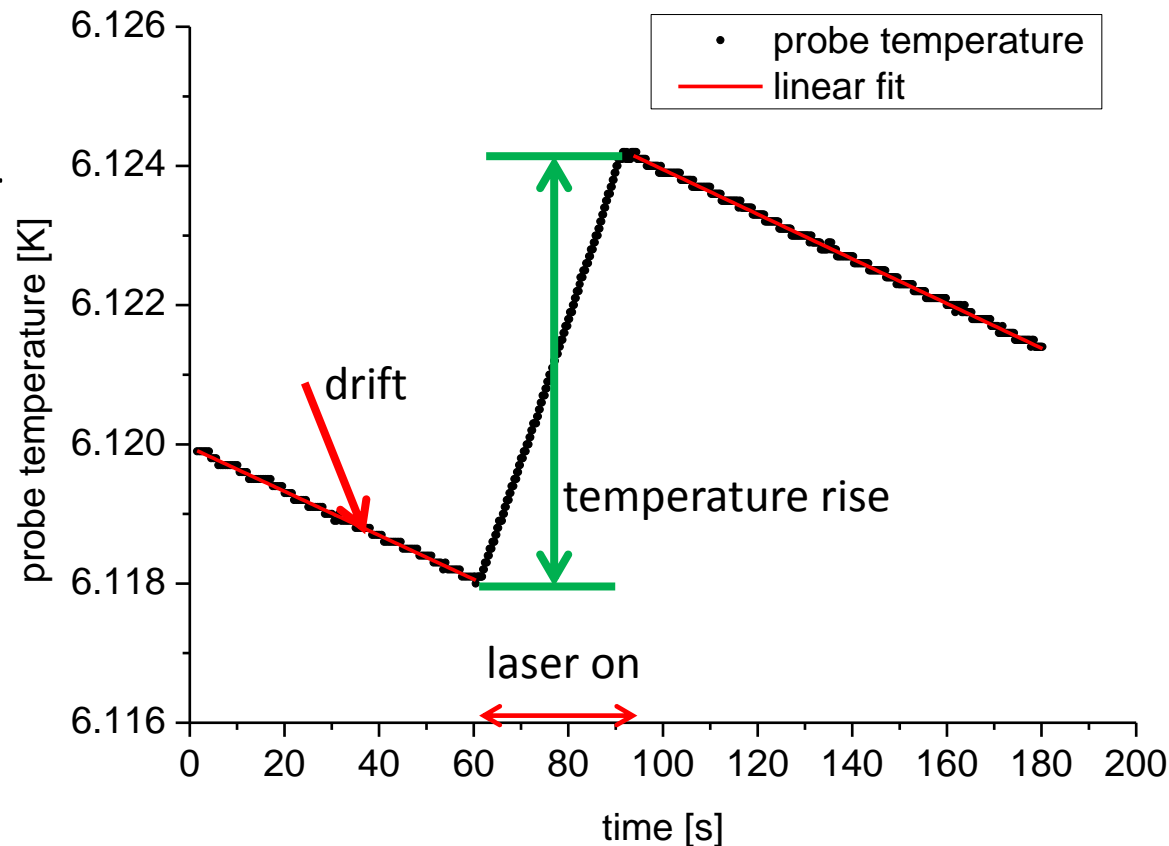
calorimetric setup





# Calorimetric measurement

- Measurement data evaluation
- $\Delta T$  = temperature rise + temperature drift



typical heating curve, 3.5 kg silicon@20K

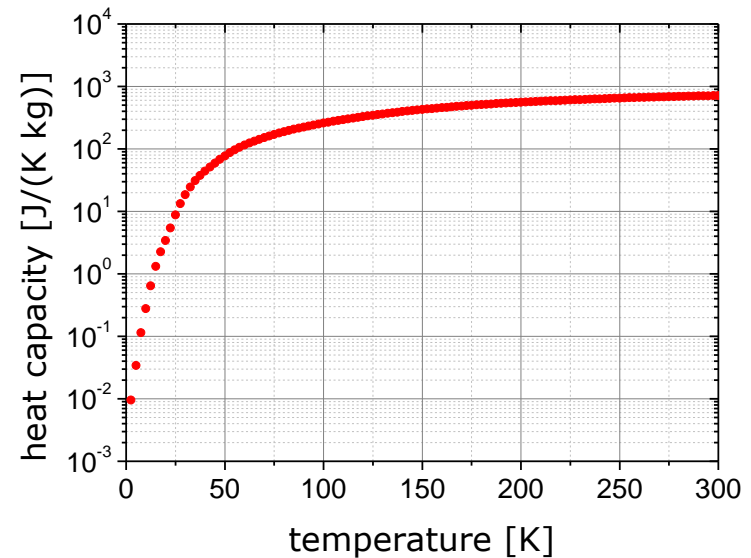


# Calorimetric measurement

- for example 1 kg silicon, 1 W laser power, 60 s heating time, 10 cm sample length, 10 ppm/cm:

temperature [K]	$\Delta T$ [K]
300	8.5 $\mu$ K
30	320 $\mu$ K
10	22 mK
5	164 mK

$$\Delta T = \frac{\Delta t P_{abs}}{m C}$$



temperature dependent heat capacity of silicon[1]

[1]R. Hull, Properties of Crystalline Silicon, The Institution of Engineering and Technology, (1999).

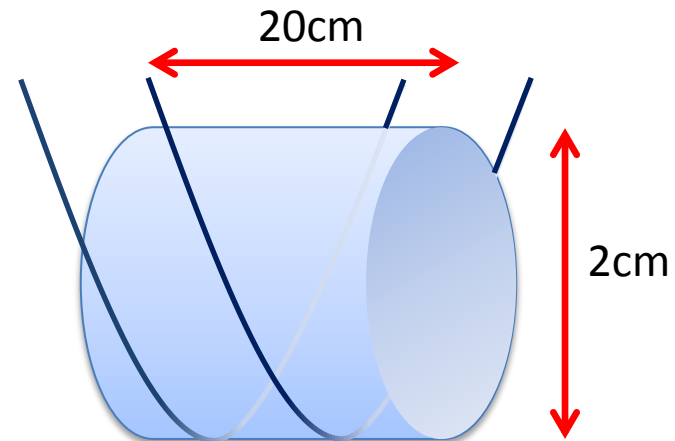


## Sensitivity at low temperatures

- Sensitivity under optimal circumstances:  
sample geometry
  - a long rod with a small diameter
  - 20 cm length still fits in our cryostat
- temperature sensor with a resolution about  $10 \mu\text{K}$
- 5 W laser power

→ 3.5 ppb/cm @ 10K  
(0.5 mK temperature rise)

→ scattering light,.. ?





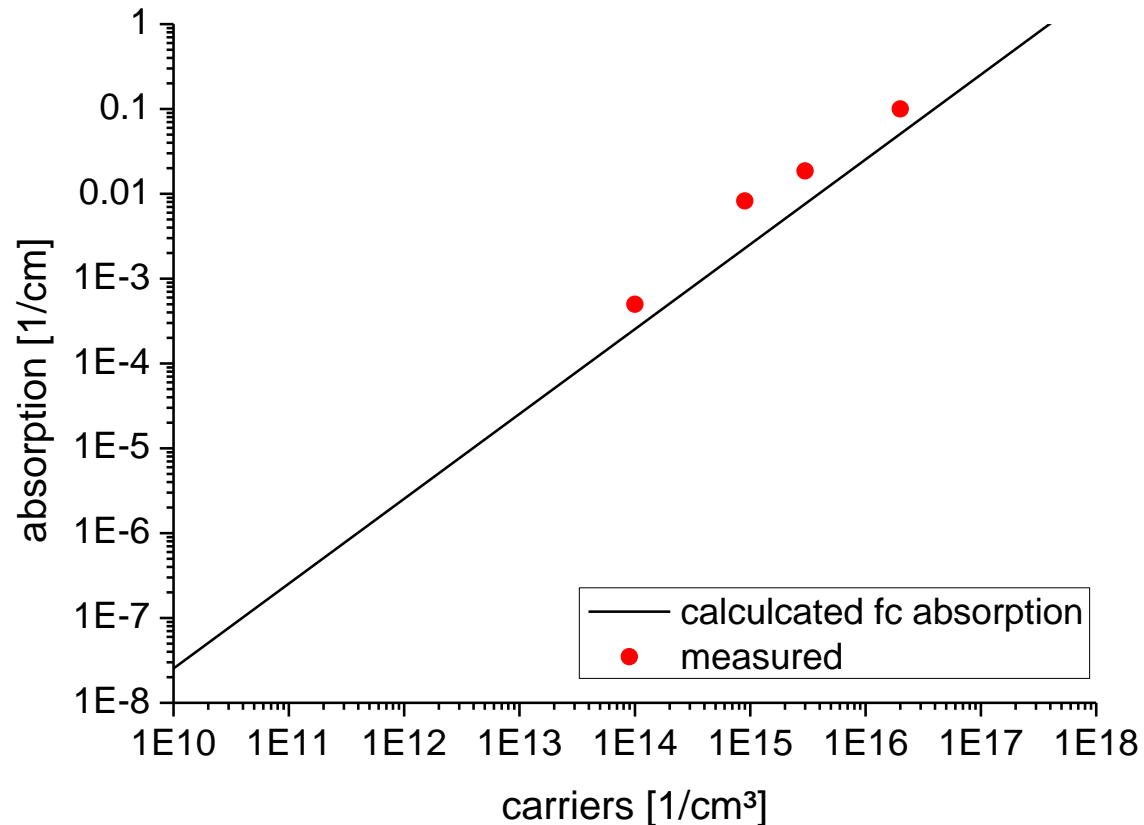
# Free carriers absorption dependence

$$\alpha_{fc} = \frac{N e^2}{m^* \epsilon_0 n c \tau} \frac{1}{\omega^2}$$

number of carriers (pointing to  $N$ )  
 scattering rate (pointing to  $\tau$ )  
 frequency (pointing to  $\omega$ )

As expected: free carrier absorption rises linear with the amount of free carriers

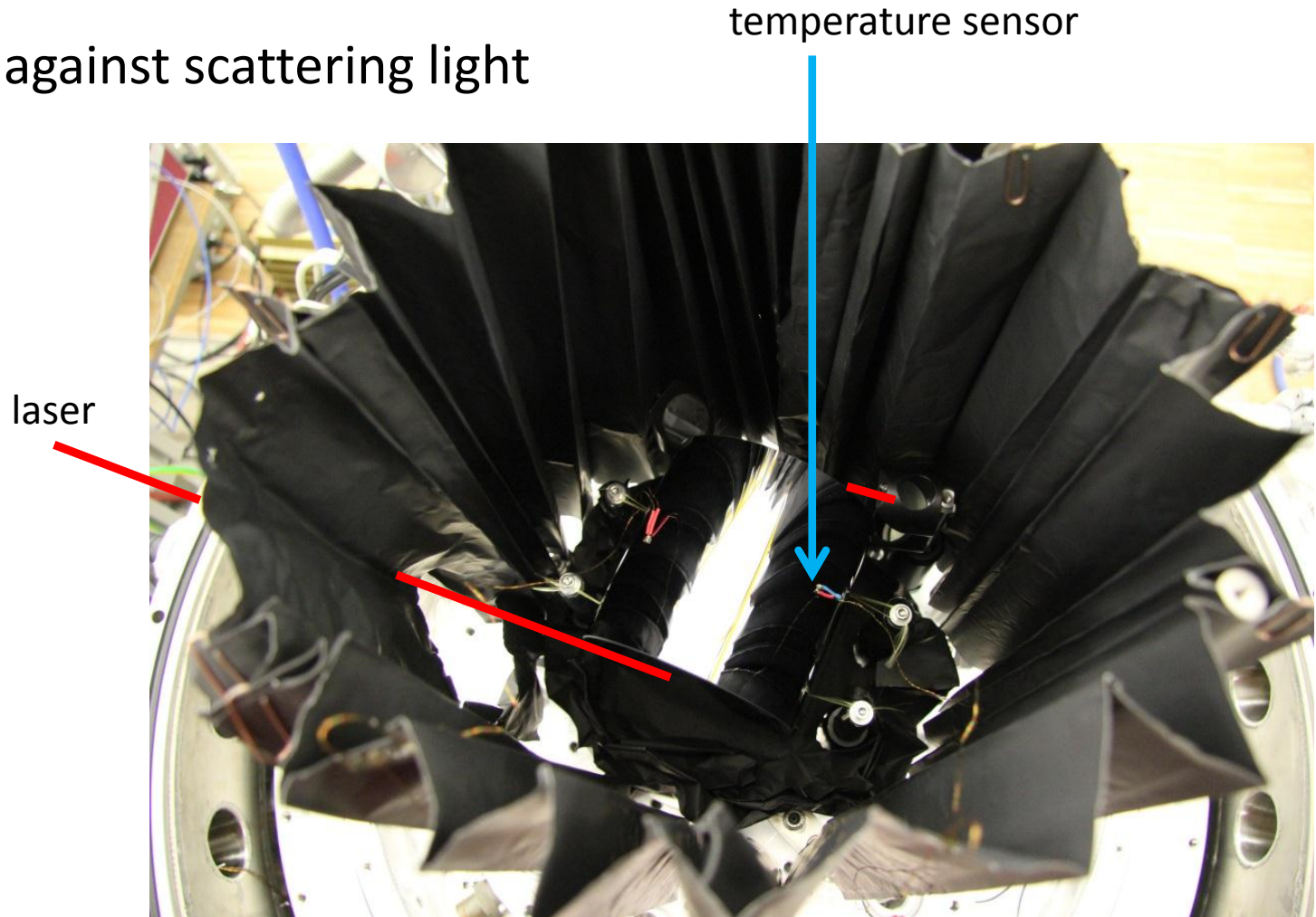
- pure silicon samples for low absorption needed (@RT)
- alternative: compensation





# Measurement setup

- Black foil against scattering light



setup inside the cryostat



## Highly doped sample

- check if the calorimetric measurement agrees with transmission measurements
- sample with 200-300 m $\Omega$ cm resistivity  
→ absorption 0.1 1/cm

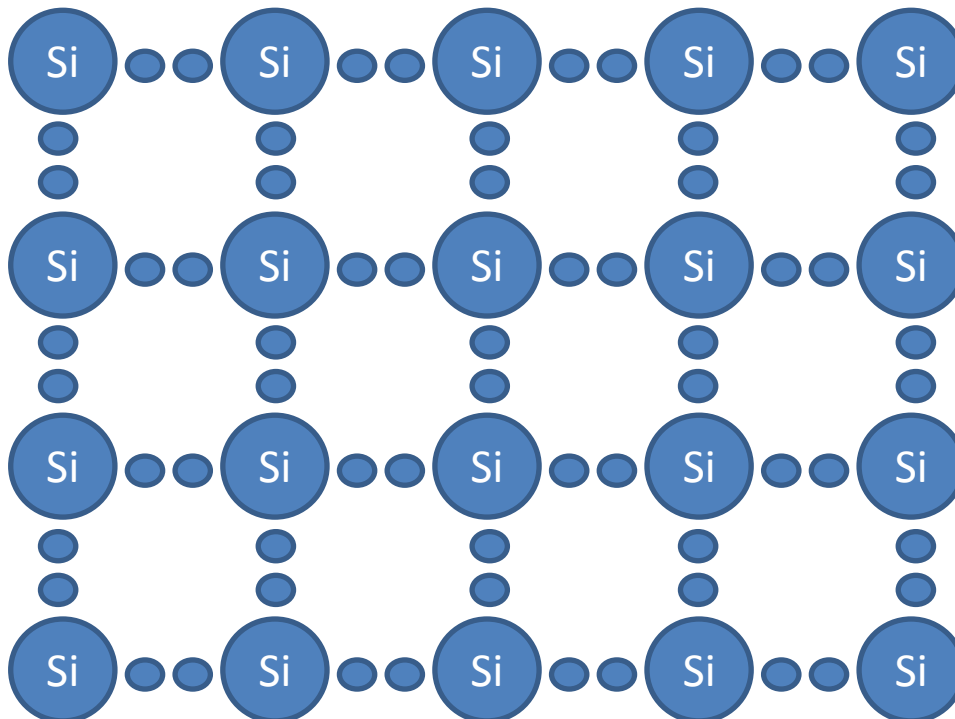
temperature [K]	measured $\Delta T$ [K]	absorption [1/cm]
300	0.020	0.1
100	0.050	0.1
6	3.96	0.1

→ no temperature dependence between 6 and 300 K



# Influence of doping

- undoped silicon crystal



conduction band



energy gap

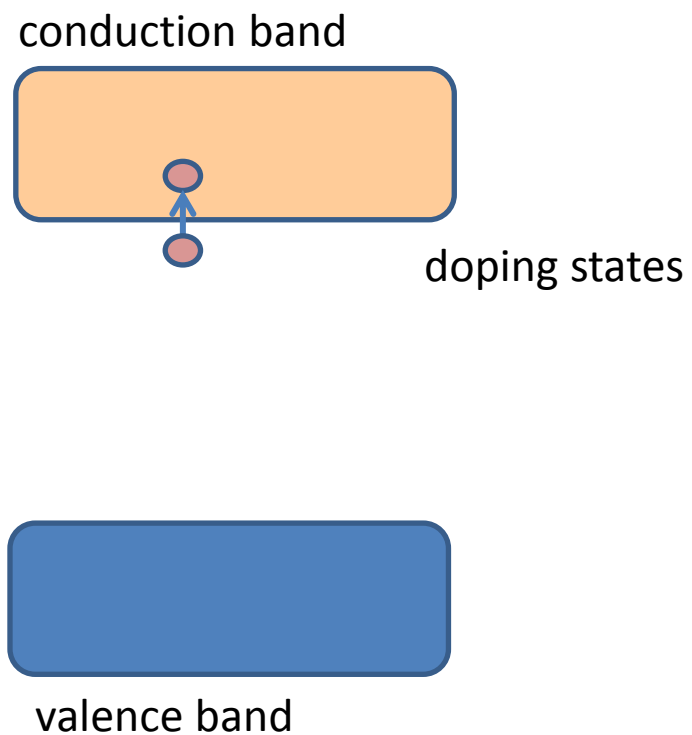
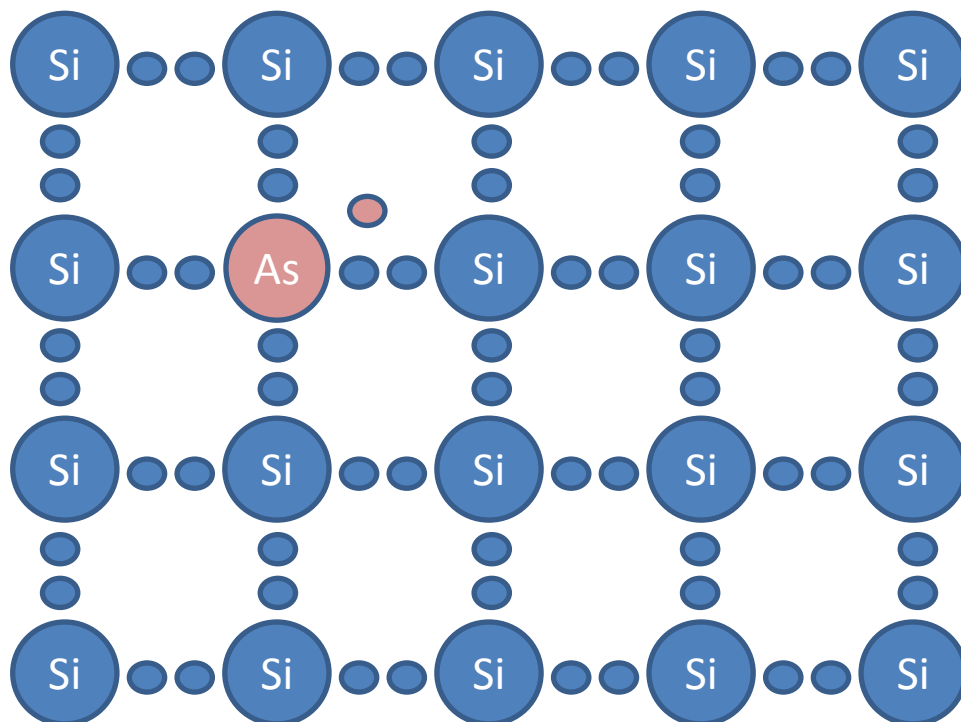


valence band



# Influence of doping

- n-doped silicon crystal
- thermal activated carriers

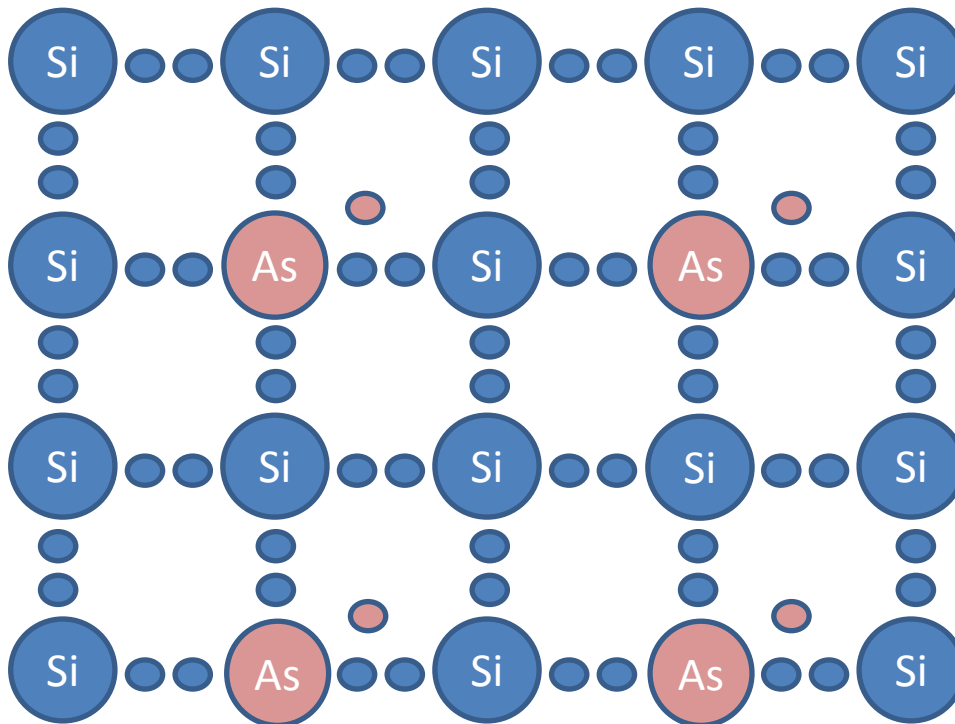






# Influence of doping

- highly doped silicon crystal  $\rightarrow$  degenerate semiconductor
- overlap of the impurity wave functions
- always free carriers inside the conduction band  $\rightarrow$  metal like behavior



conduction band



doping band

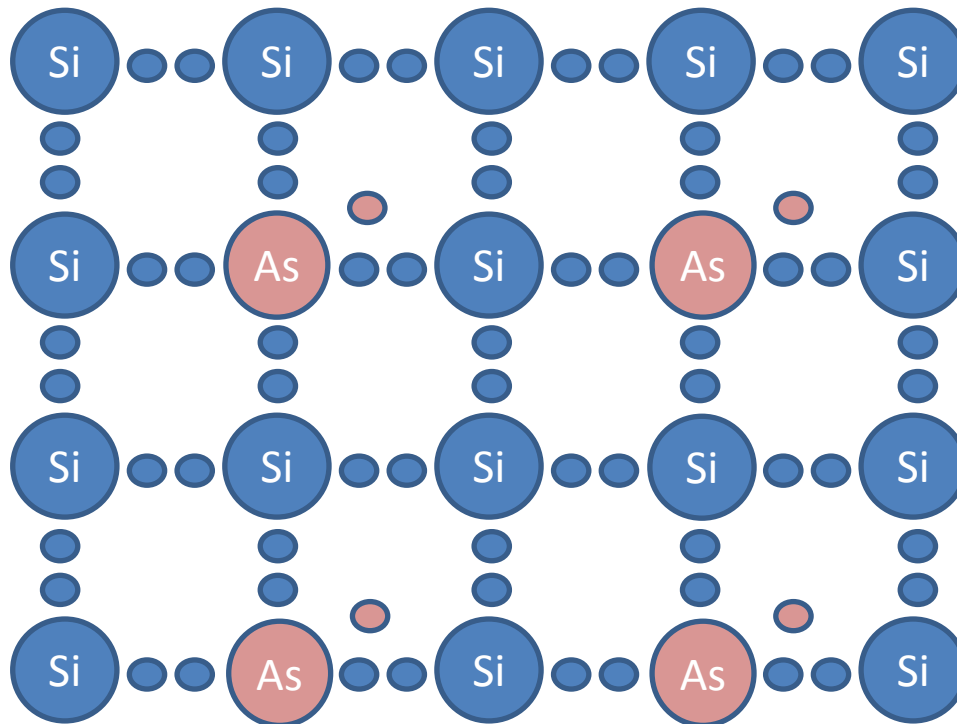


valence band

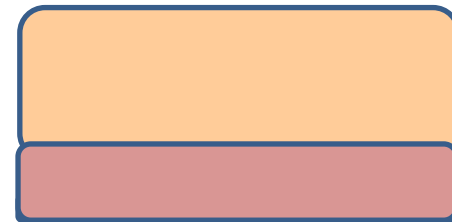


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conduction band



doping band

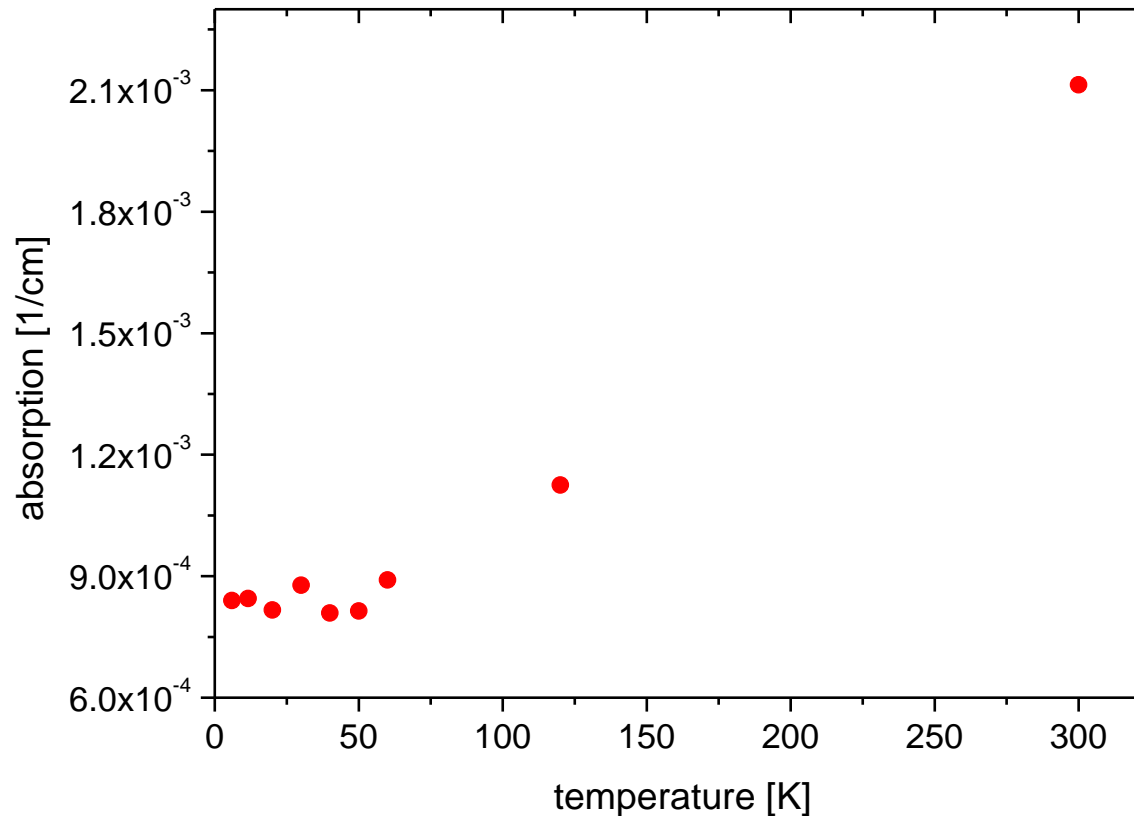


valence band



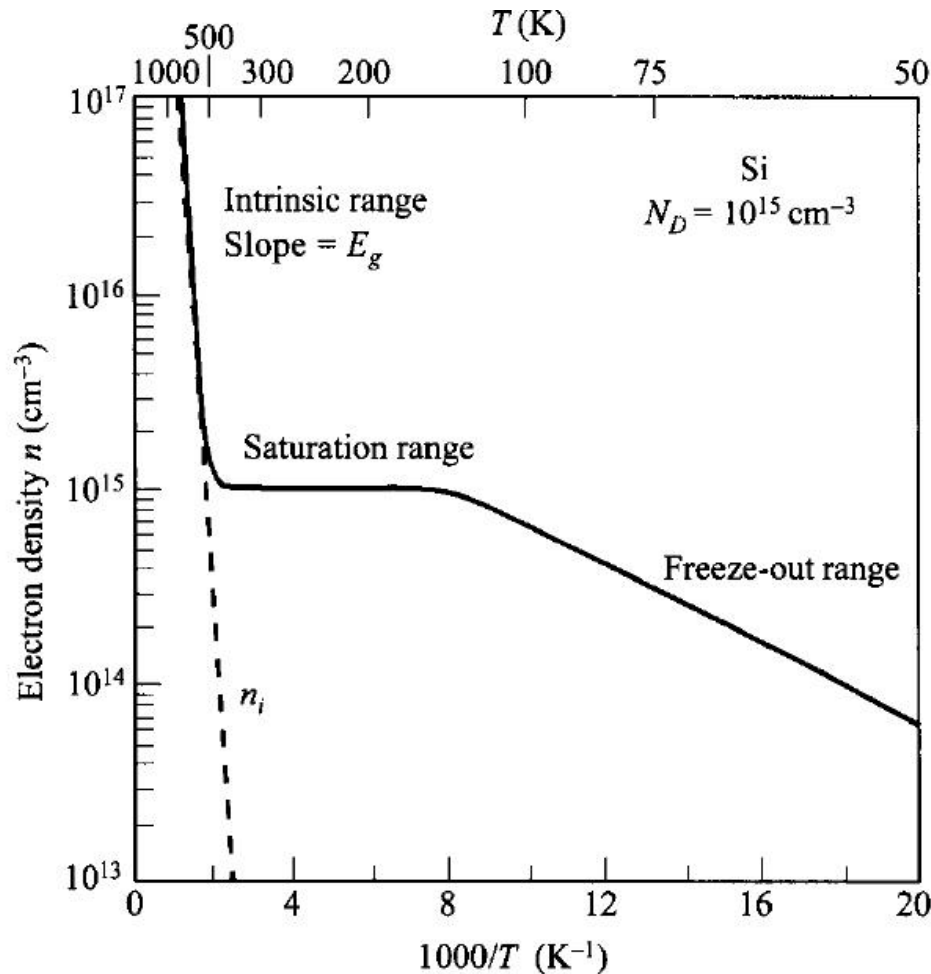
## temperature dependence

- dia. 150x86 mm, 100  $\Omega$ cm
- $\rightarrow$  absorption  $2.1 \cdot 10^{-3}$  1/cm @RT,  $8.4 \cdot 10^{-4}$  1/cm @6 K





# What do we learn at solid state physics lectures



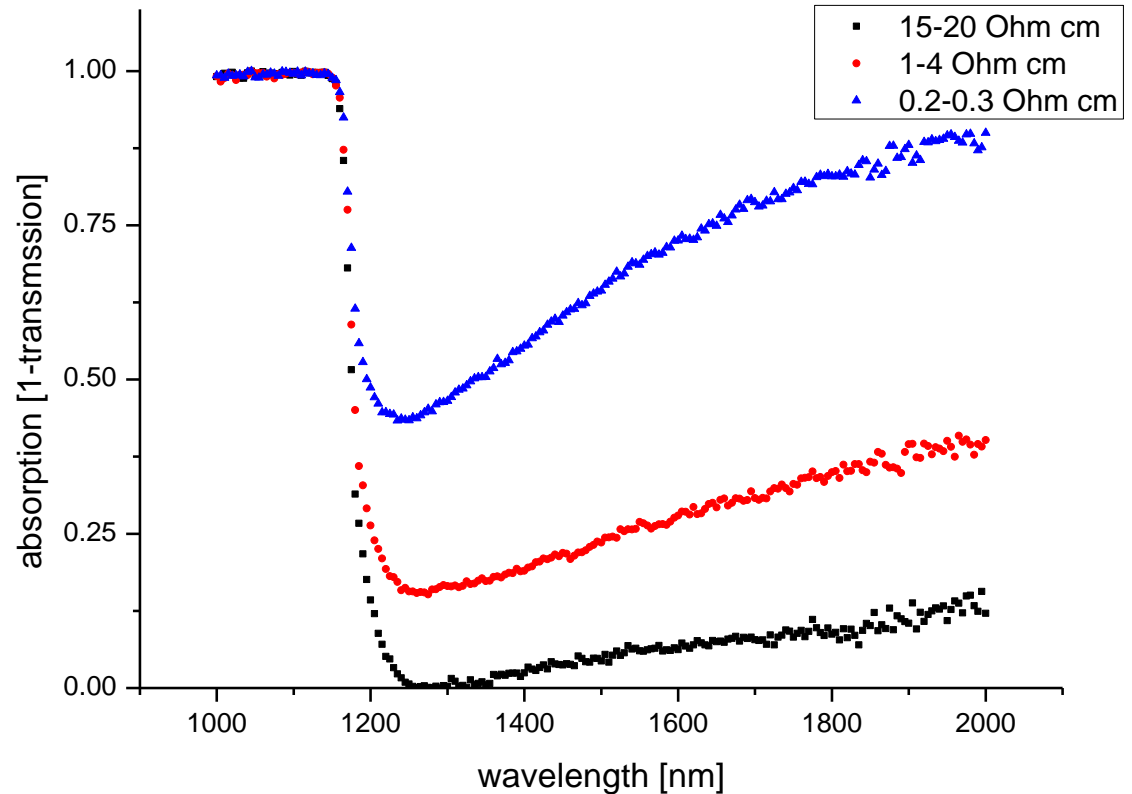
expect: orders of magnitude lower absorption for low temperatures

Sze - Physics of Semiconductor Devices



# Doping and wavelength dependence @RT

resistivity [ $\Omega$ cm]	absorption [ $1/\text{cm}$ ] @1550nm
15-20 $\Omega\text{cm}$	$8 \cdot 10^{-3}$
1-4 $\Omega\text{cm}$	$2 \cdot 10^{-2}$
0.2-0.3 $\Omega\text{cm}$	$1 \cdot 10^{-1}$



for greater wavelength absorption rises  
 → 1550 nm laser or smaller wavelength



## Summary

- different absorption processes:
  - band band
  - free carrier absorption → absorption 1550nm
- highly doped silicon samples show temperature independent absorption (metal like behavior)
- intra band absorption is linear to the amount of free carriers
- absorption rises for greater wavelength (above the gap)
- → next step: temperature dependent electronic characterization (can we freeze out carriers ?)