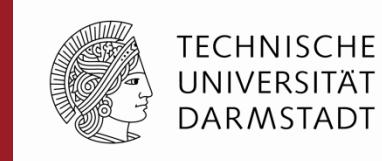


# The continuous-angle DSA Method

(sub-) picosecond lifetime measurements with  
position-sensitive HPGe detector arrays



Christian Stahl, Marc Lettmann, Norbert Pietralla

*IKP, TU Darmstadt*

- How to facilitate DSAM measurements with position-sensitive HPGe detectors?
- How to perform DSAM measurements with radioactive, relativistic beams?

Supported by



Bundesministerium  
für Bildung  
und Forschung

under Grant no. 05P12RDFN8

# Motivation – Value of lifetime measurements



- Model-independent access to transition strengths

$$1/\tau \propto B \left( \mathcal{M}L; J_i^\pi \rightarrow J_f^\pi \right) = \frac{1}{2L+1} \left| \left\langle J_f^\pi \left| \hat{m}L \right| J_i^\pi \right\rangle \right|^2$$

→ probing nuclear wave functions

- In conjunction with Coulex cross section measurements:  
Determine nuclear quadrupole moments

$$\sigma_{\text{Coulex}} = f(M_{12}, M_{22})$$

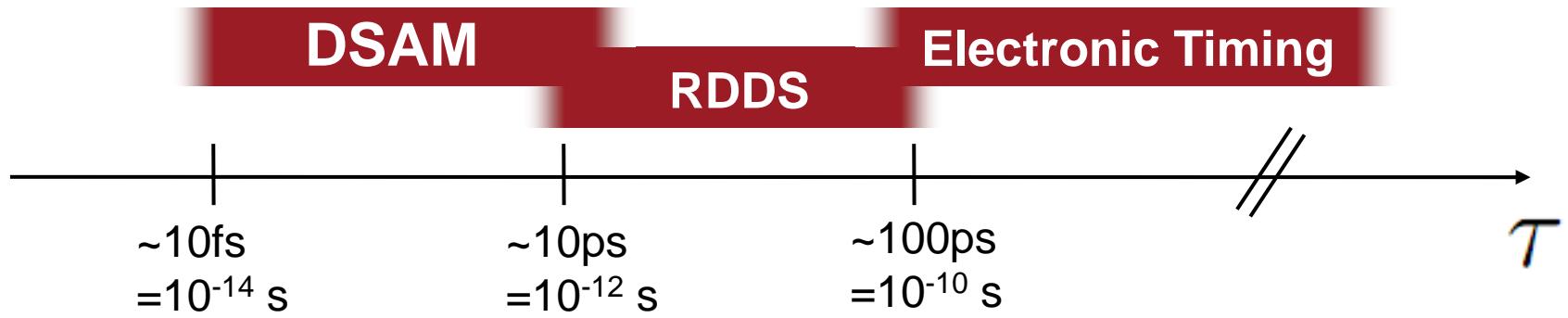
from  $\tau$        $\propto Q$

→ e.g. C. Bauer *et al.*, PRC **86**, 034310 (2012)

# Basics – Doppler-Shift Attenuation Method



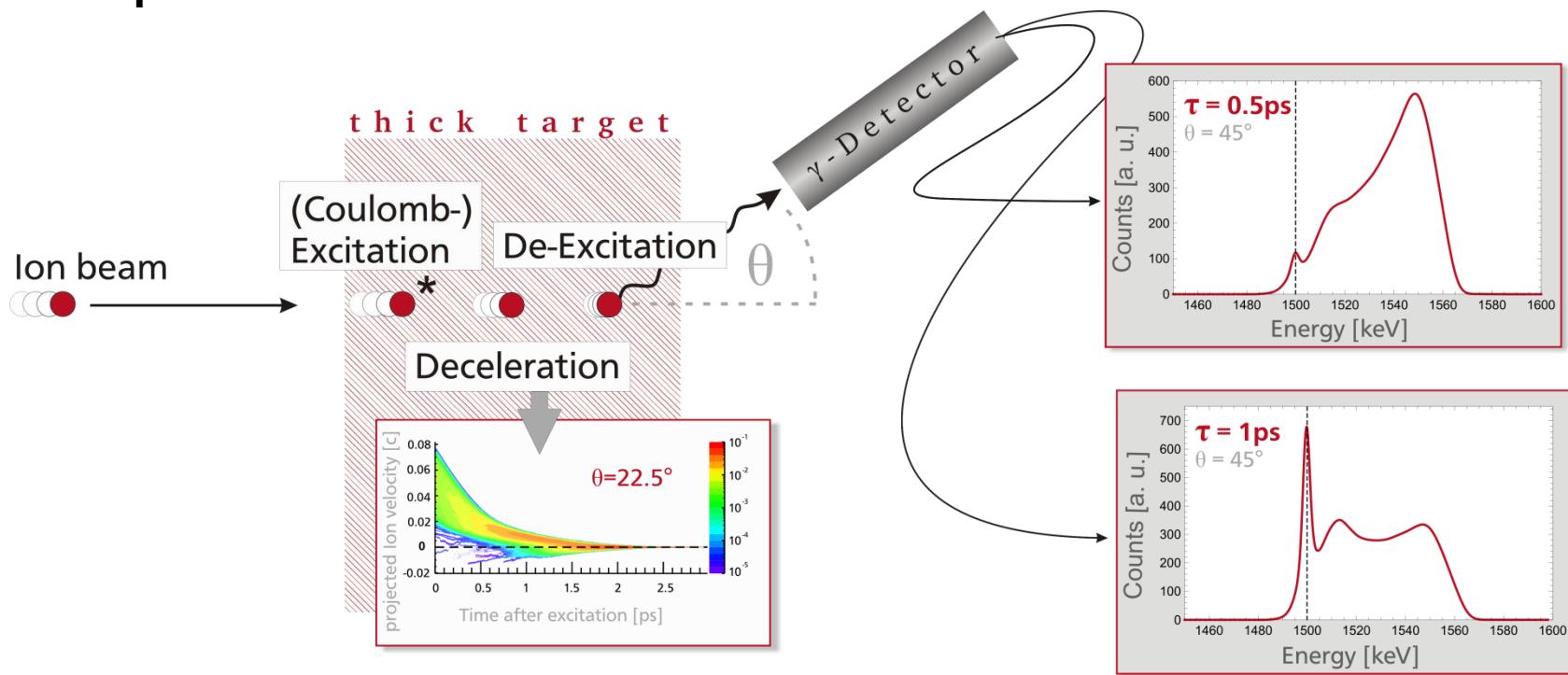
- Lifetime range:



# Basics – Doppler-Shift Attenuation Method



## ➤ Principle:



Deduce **level lifetimes** from the shape of **Doppler-broadened photo-peaks**

# The continuous angle DSA Method



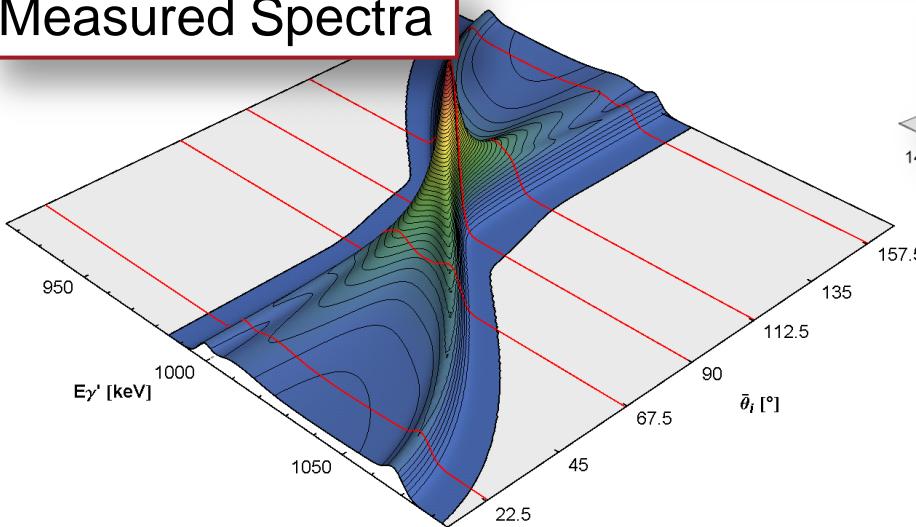
That is done since the 60's. What's new about that?



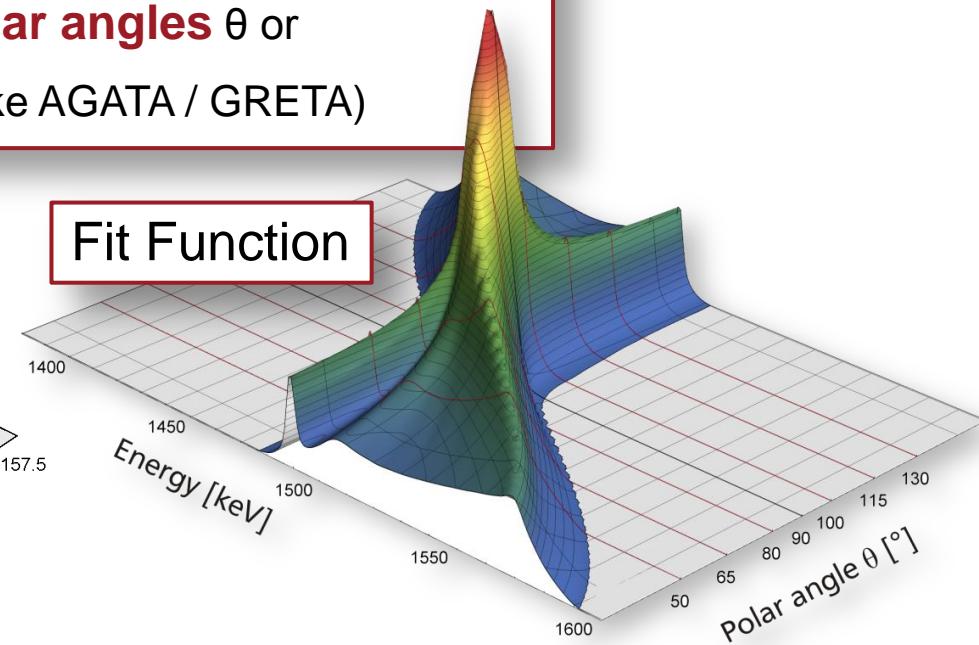
Newly developed **analysis software**

Designed for the **simultaneous fit** to spectra taken with  
**many detectors** under **many polar angles**  $\theta$  or  
**position sensitive detectors** (like AGATA / GRETA)

Measured Spectra



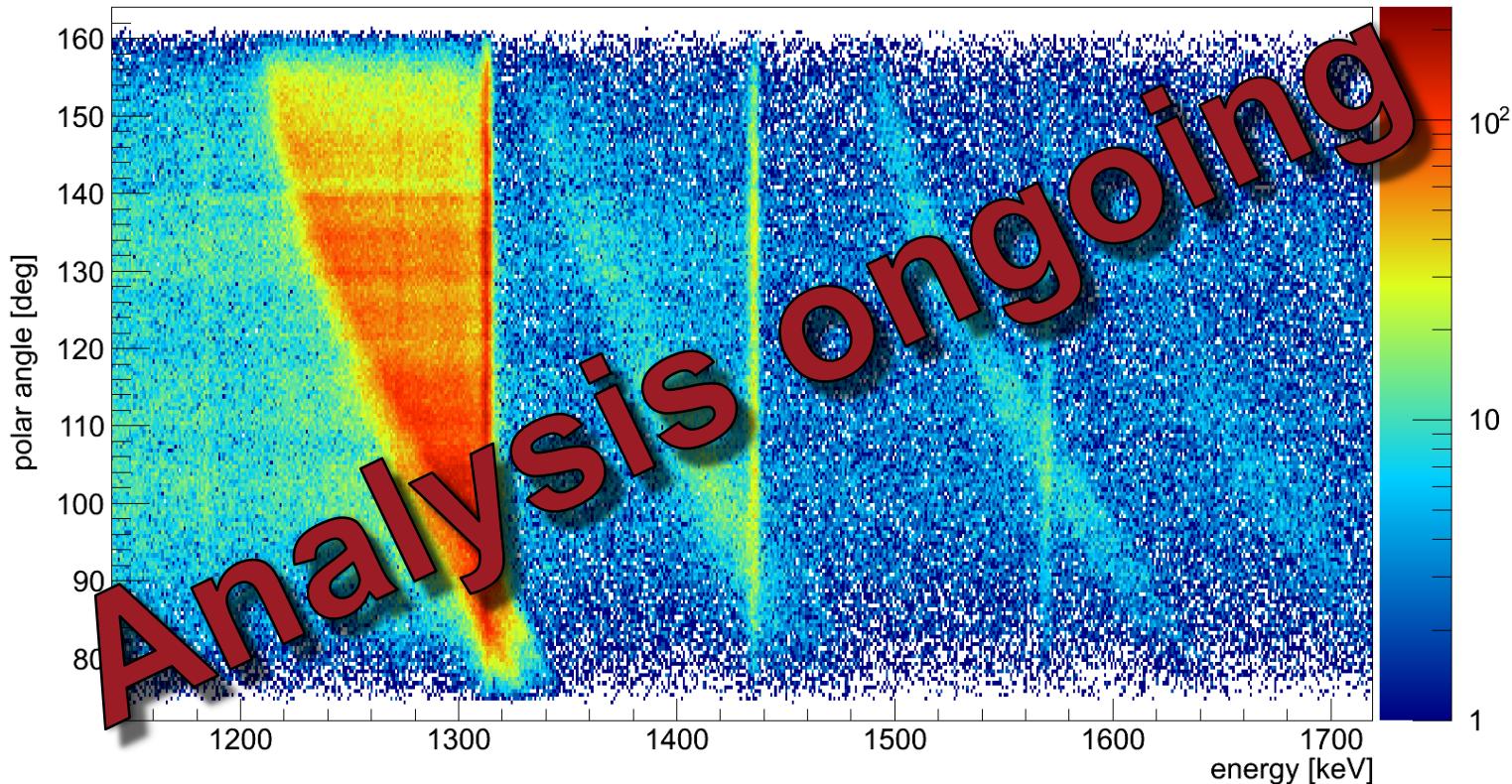
Fit Function



# The continuous angle DSA Method



$^{136}\text{Xe}$ -ions Coulomb excited on  $0.5\text{mg}/\text{cm}^2$  Carbon, stopped in  $30\text{mg}/\text{cm}^2$  Tantalum

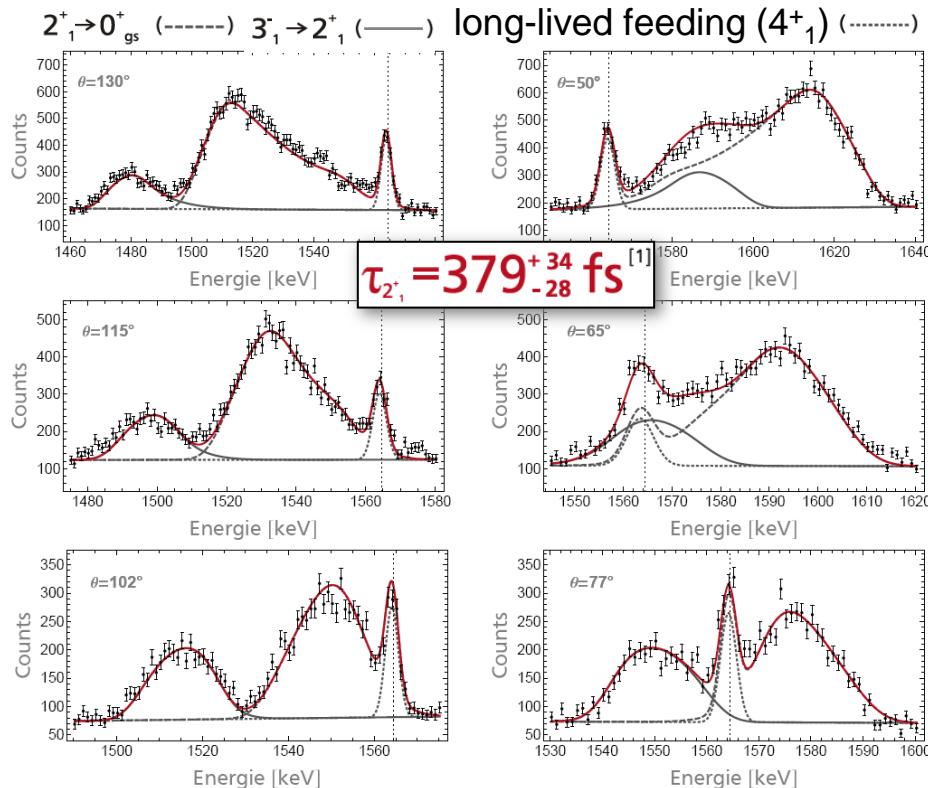


LNL-experiment 09.08,  $^{136}\text{Xe}$  at 546 MeV, recoiling carbon ions detected by a DSSSD  
AGATA Demonstrator with 5 TC at backward angles

# The continuous angle DSA Method



- Effective use of the full statistics and resolution
- Good chances to disentangle overlapping transitions



GSI-Experiment U246 (10/2010)

$^{86}\text{Kr}$  @ 2.91 AMeV

Coulomb-excited on a  $0.33\text{mg/cm}^2$   ${}^{\text{nat}}\text{C}$  layer  
stopped in a multilayer-target (Gd, Ta and Cu)  
 $\gamma$ -rays detected by 4 EUROBALL cluster detectors.  
recoiling carbon ions detected by 4 PIN diodes

Overlapping  $2^+_1 \rightarrow \text{gs}$  and  $3^-_1 \rightarrow 2^+_1$  transitions

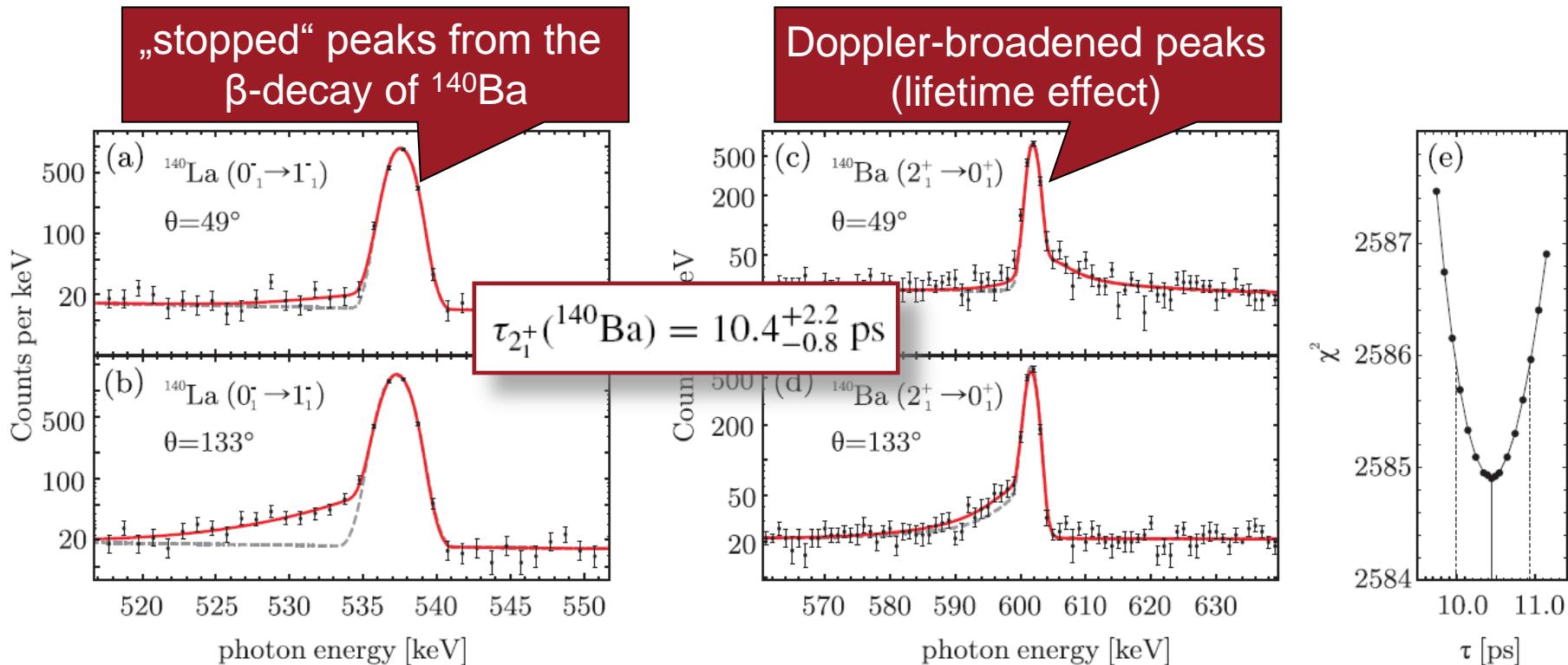
[1] C. Stahl, Master Thesis, TU Darmstadt, 2011

- Also applicable to position in-sensitive HPGe arrays (Miniball, Gammasphere, ...)

# The continuous angle DSA Method



- Long lifetime, asymmetric detector response (neutron damage)



C. Bauer *et al.*, PRC **86**, 034310 (2012)  
 Coulomb-excitation of  $^{140}\text{Ba}$  on a thick Copper target  
 REX-ISOLDE / MINIBALL

+16 more angles used for the fit

# “Differential” DSAM

Application of the DSA Method with relativistic, radioactive ion beams



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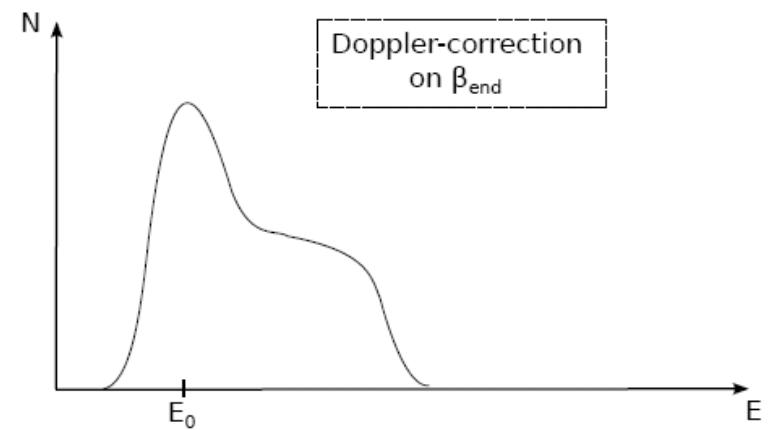
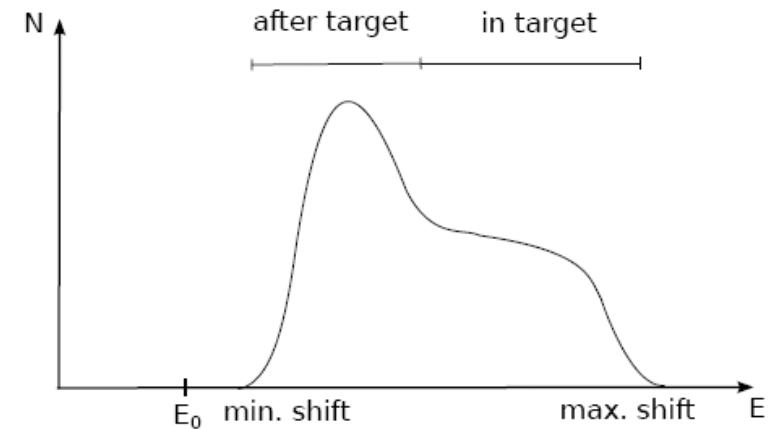
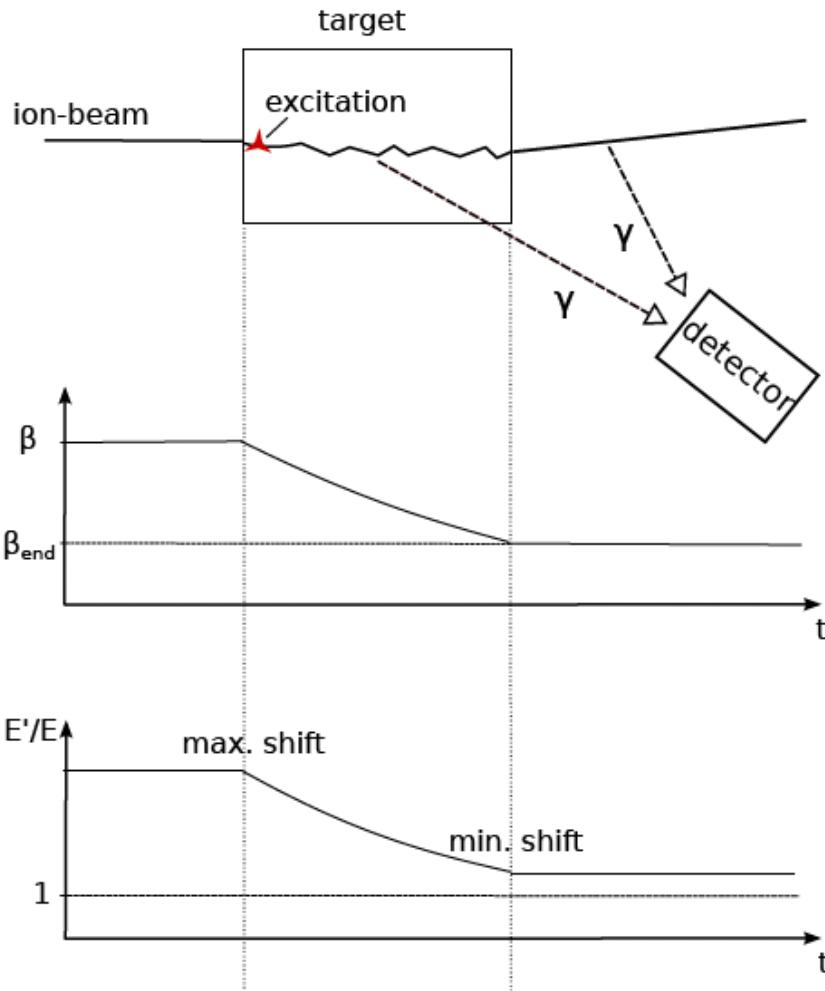
- Example: PreSPEC / HISPEC
- Need to identify ions behind the target (cocktail beams)
- No accumulation of activity at the target position
- Relativistic beams

# “Differential” DSAM

Application of the DSA Method with relativistic, radioactive ion beams



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# “Differential” DSAM

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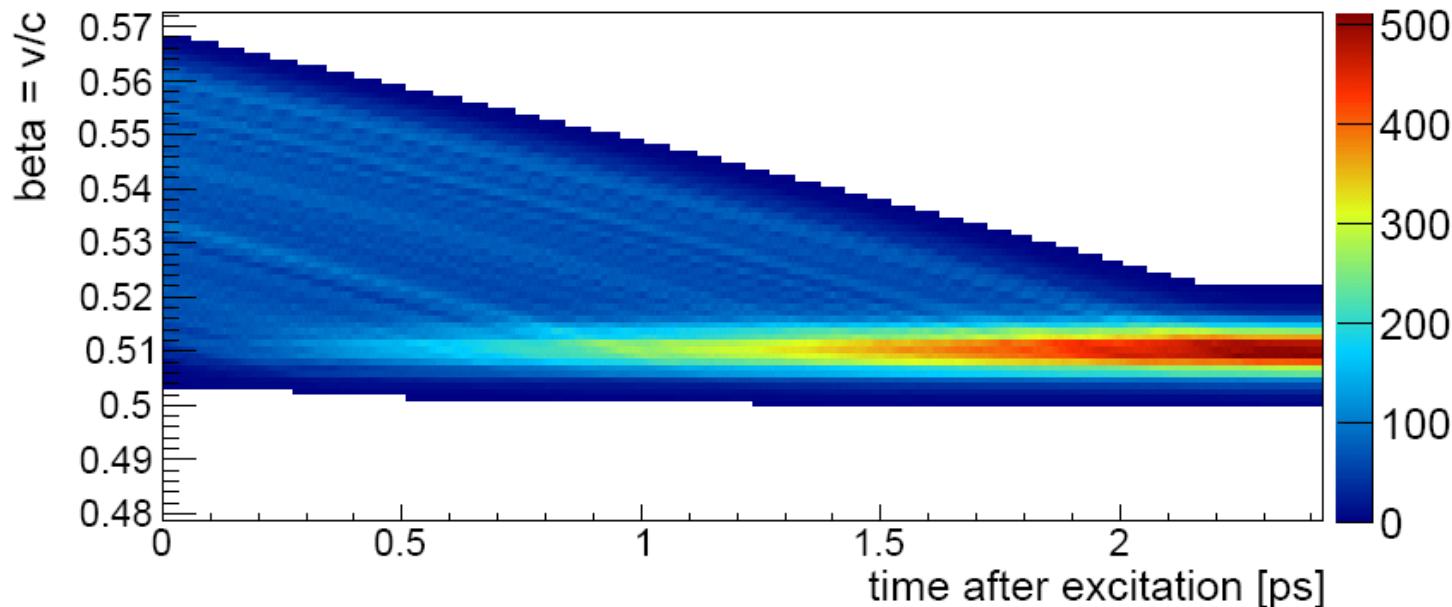


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- Example application: Lifetime of the  $2^+_1$  level in  $^{106}\text{Sn}$  measured with the PreSPEC setup after Coulomb-Excitation

$^{106}\text{Sn}$  ions at 150 MeV/u impinging a  $0.75 \text{ g/cm}^2$  Au target

Just a case study..



# “Differential” DSAM

Application of the DSA Method with relativistic, radioactive ion beams

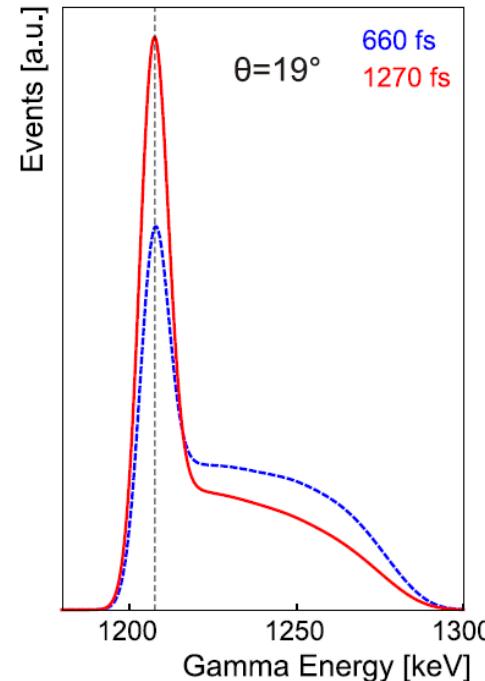
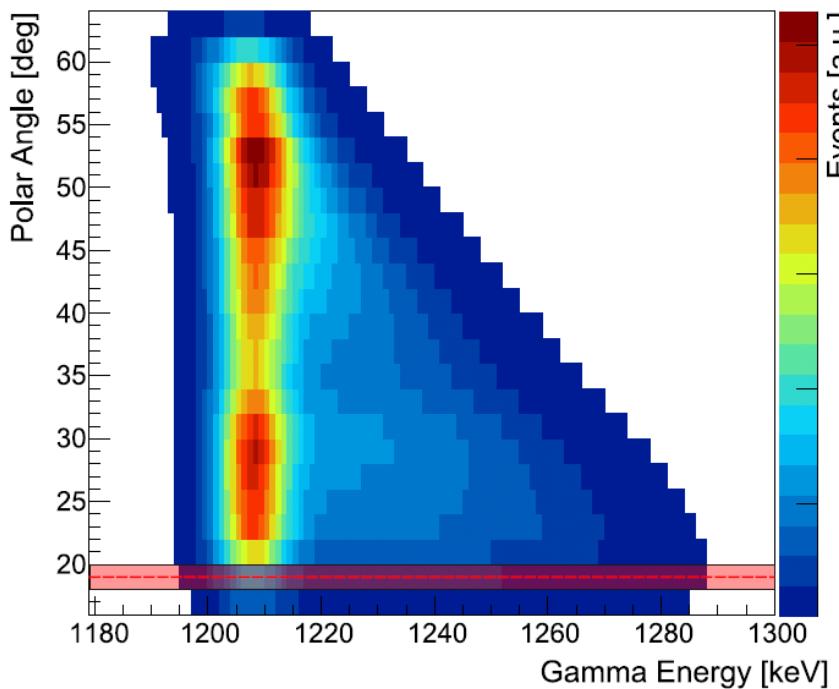


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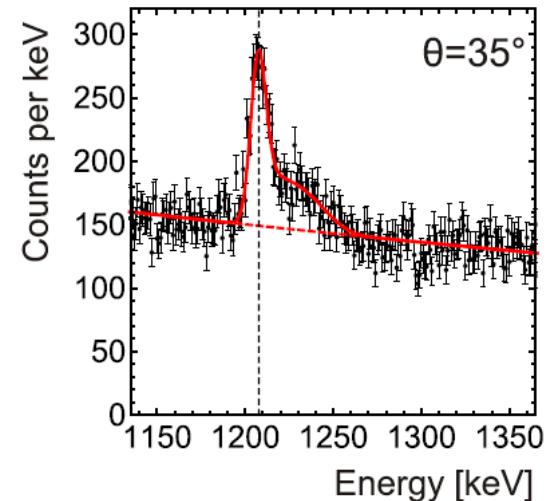
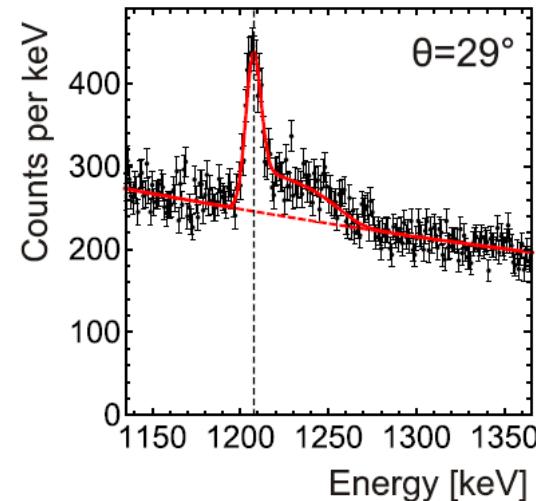
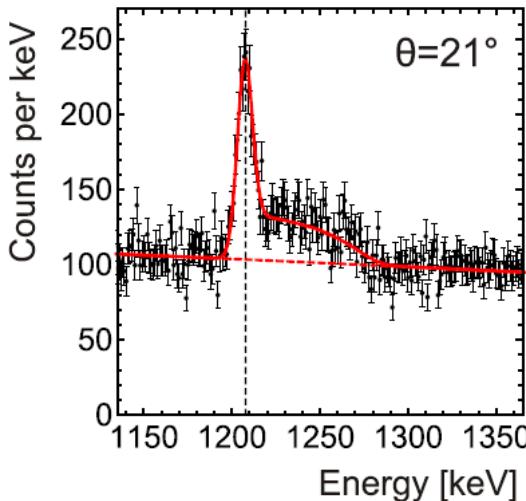
Application of the DSA Method with relativistic, radioactive ion beams



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- Example application: Lifetime of the  $2^+_1$  level in  $^{106}\text{Sn}$  measured with the PreSPEC setup after Coulomb-Excitation
- Feasibility and Accuracy:

Just a case study..



**Simulated** spectra for 100h beam on target with  $1.8 \times 10^4$  pps,  $2^\circ$  polar angle bins

# “Differential” DSAM

Application of the DSA Method with relativistic, radioactive ion beams



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- Example application: Lifetime of the  $2^+_1$  level in  $^{106}\text{Sn}$  measured with the PreSPEC setup after Coulomb-Excitation
- Feasibility and Accuracy:

Just a case study..



**Can use thicker targets than for ‘standard’ – Coulex experiments**  
→ more events per ‘ion on target’



**Can do Coulex analysis with the same dataset**



**Highly charged ions at high velocity:**  
→ No nuclear stopping  
→ Stopping Power precisely known

- ‘Real’ Application:

Method will be used for the analysis of PreSPEC data from experiment S428 (level lifetimes in heavy Zr isotopes), Pietri, Ralet *et al.*

**Case of  $^{106}\text{Sn}$ :**

Expect (statistical) accuracy for the  $2^+_1$  level lifetime of **2.5%** after 70h beam on target

# “Differential” DSAM

Application of the DSA Method with relativistic, radioactive ion beams



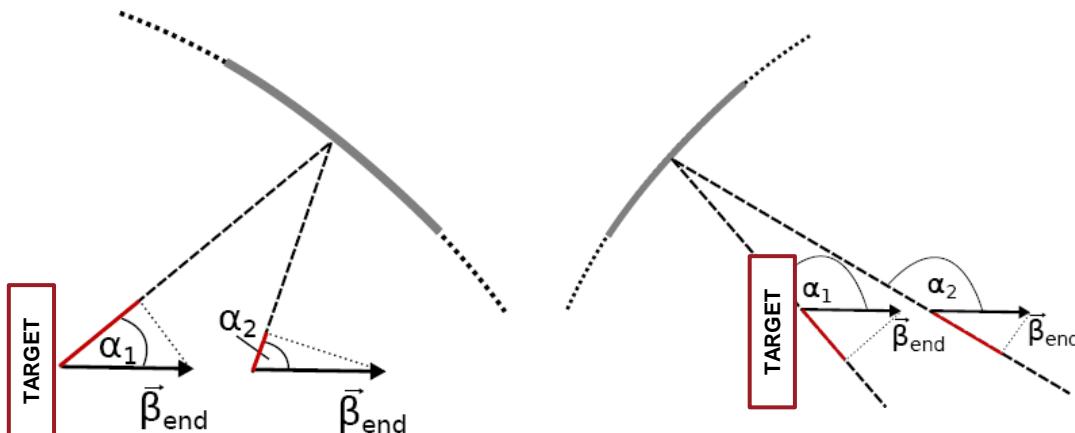
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## ➤ Another sensitivity region with “differential DSAM” in the order of 100ps:

Doppler-correction on exit velocity “fails”, if decay occurs far behind the target  
(assumed angle between direction of ion motion and gamma detection is wrong)

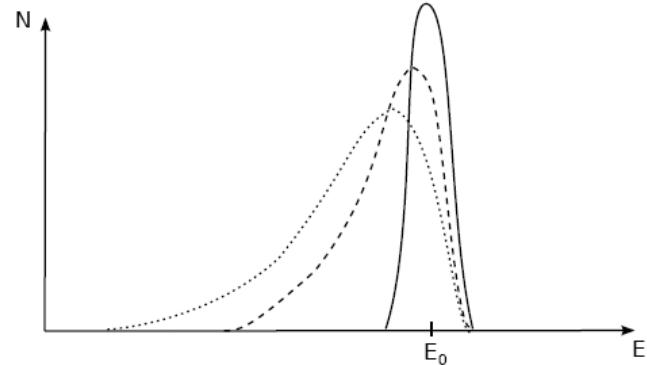
P. Doornenbal et al., NIM A 613 (2010) 218–225; C. Domingo-Pardo et al., NIM A 694 (2012) 297–312

→ A “continuous Plunger”:



Detector under forward-angle:  
Over-estimation of Doppler-shift

Detector under backward-angle:  
Under-estimation of Doppler-shift



*Thank you for your attention!*

If you are interested in our analysis software,  
please contact me!

✉ stahl@ikp.tu-darmstadt.de



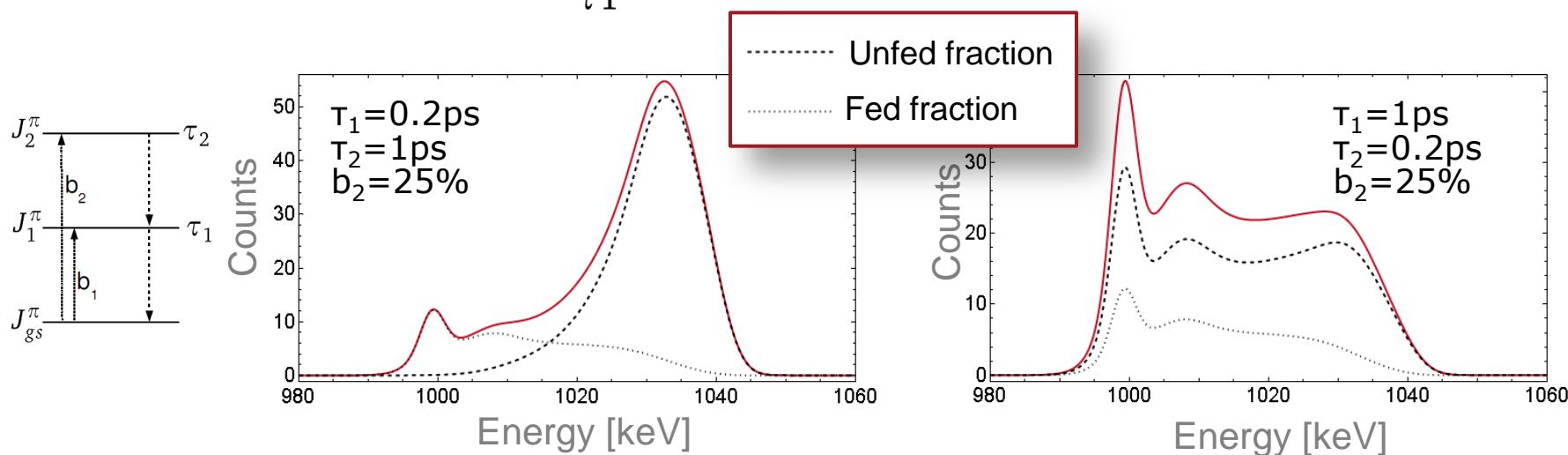
# Implementation of the continuous angle DSAM in a new Analysis tool



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## 2 major ingredients for the calculation of lineshapes

- Decay function  $A_1(t) = \frac{1}{\tau_1} N_1(t)$



- Complex feeding schemes
- Decay function from analytical solutions of the Bateman equation
- Simultaneous fit of feeding transitions
- Different angular distributions for fed and unfed fraction

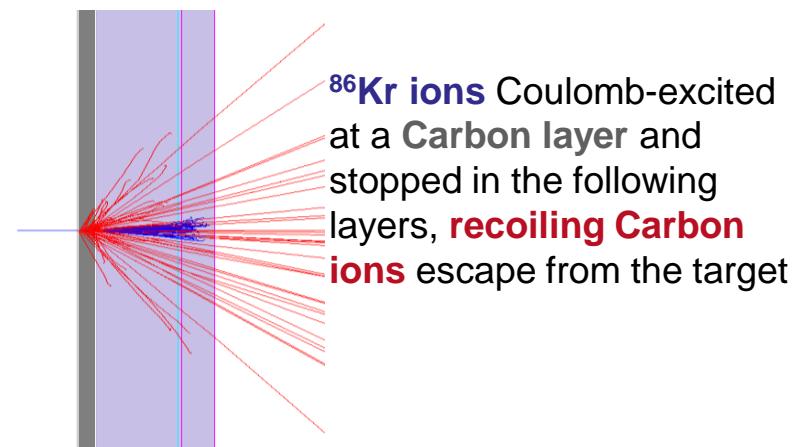
# Implementation of the continuous angle DSAM in a new Analysis tool



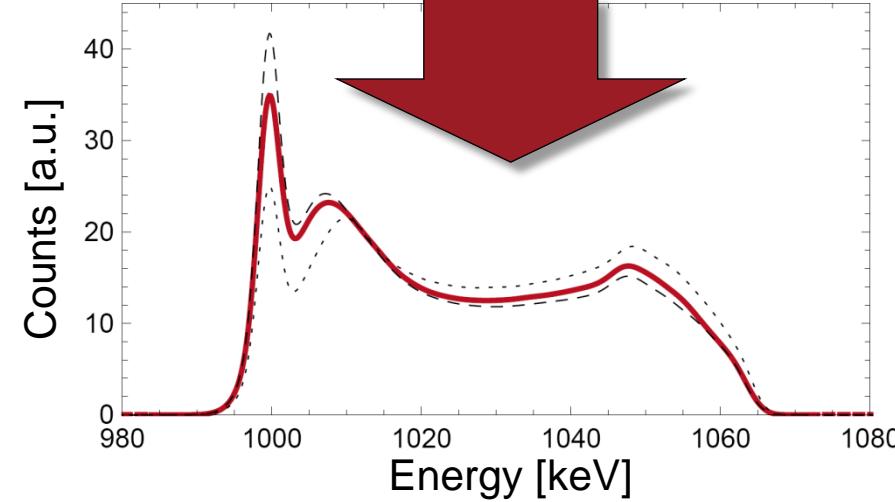
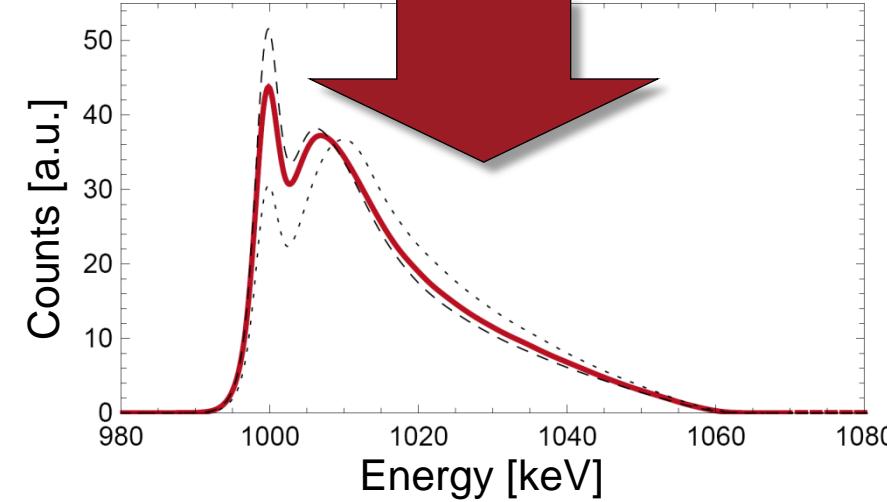
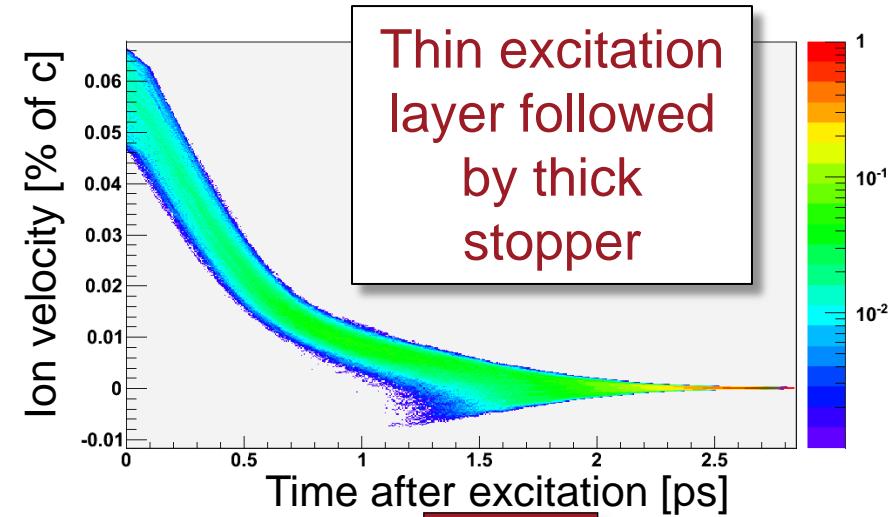
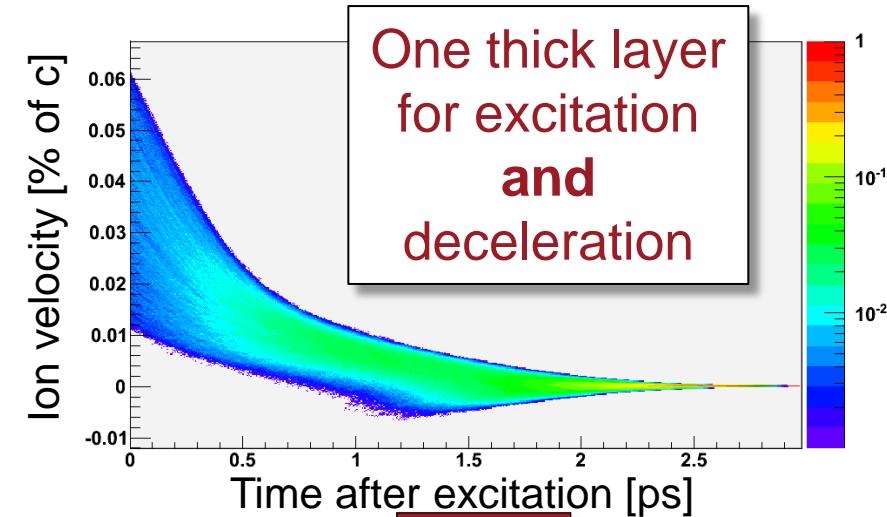
## 2 major ingredients for the calculation of lineshapes

- Decay function  $A_1(t) = \frac{1}{\tau_1} N_1(t)$
- Stopping-Matrix  $p(\vec{\beta}, t)$  from a Monte-Carlo simulation

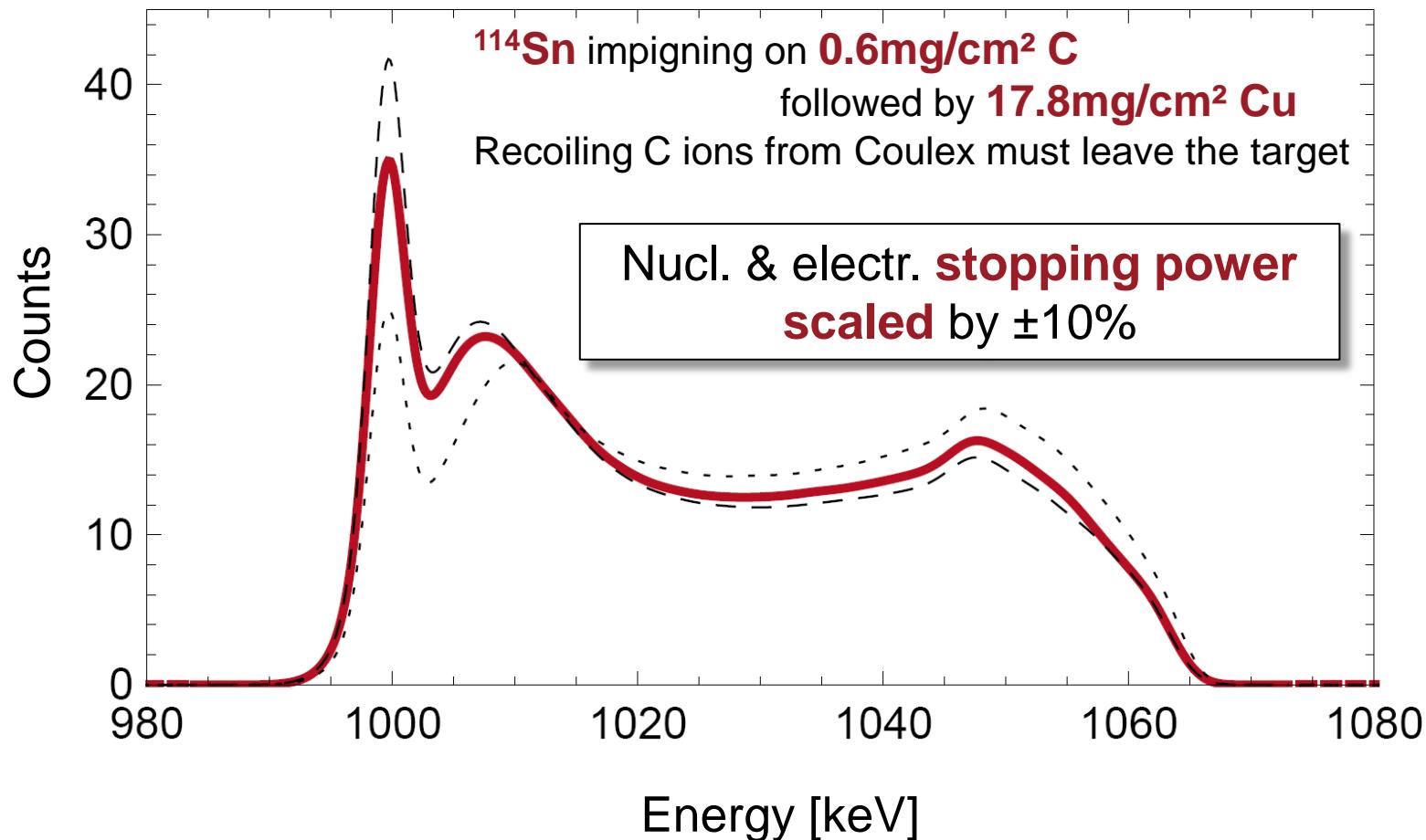
- Realistic Monte-Carlo Simulation of the (**Coulomb-**) excitation and the **deceleration process** on the Basis of **Geant4**
- **Transport and energy loss** calculated for **beam and secondary ions**
- Set **kinematic conditions** in the analysis
- software to select ion tracks (“particle detectors”)
- Good platform for the implementation of further excitation processes



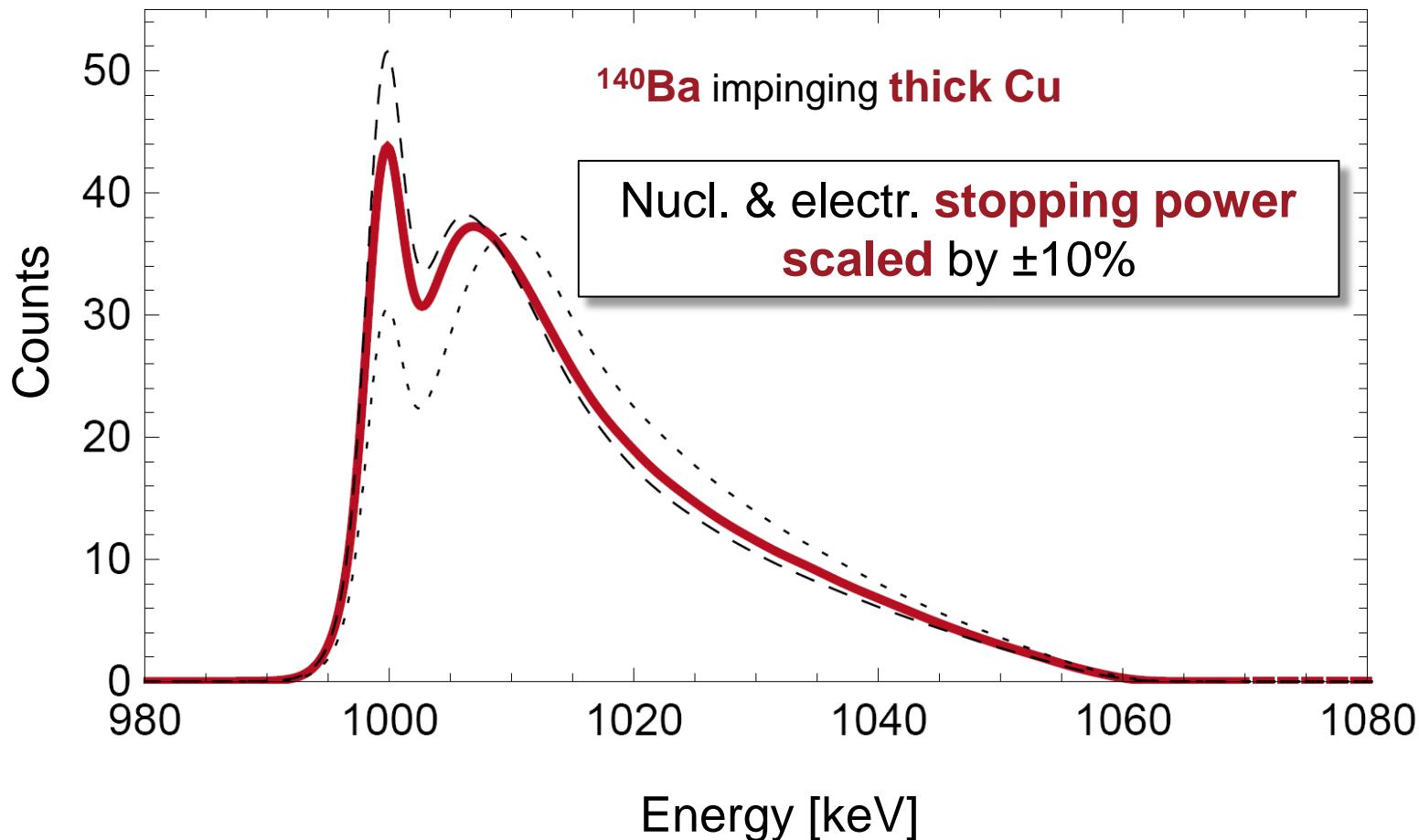
# Choice of excitation situation



# $dE/dx$ scaling



# $dE/dx$ scaling



# Implementation of the continuous angle DSAM in a new Analysis tool



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## Important effects to account for

- Relativistic corrections of the detector **solid angle**
- Transformation of the **angular distribution** from the ion rest frame to the lab frame

