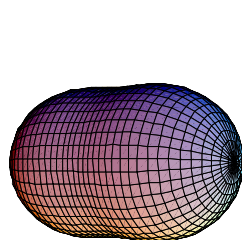
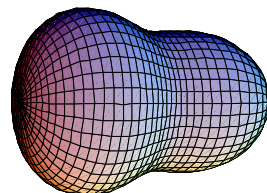


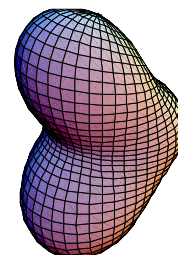
SPES-LOI: Search for Exotic-Octupole deformation effects in n-rich Ce-Xe-Ba Nuclei



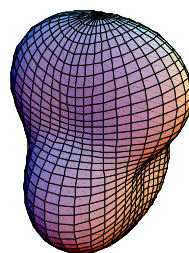
SD Prolate



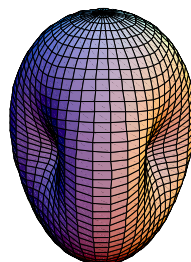
Y20 + Y30



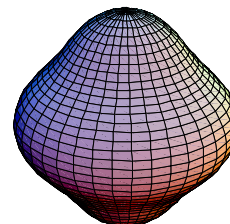
Y20 + Y31



Y20 + Y32



Y20 + Y33



Pure Y40

Spokesperson: E. Sahin, D. Curién, J. Dudek, M. Zielinska, G. de Angelis

INFN, Laboratori Nazionali di Legnaro, Italy

IPHC Strasbourg, France

University of Warsaw, Poland

Marie-Curie-Skolodwska University, Lublin, Poland

Polish Academi of Science, Crakow, Poland

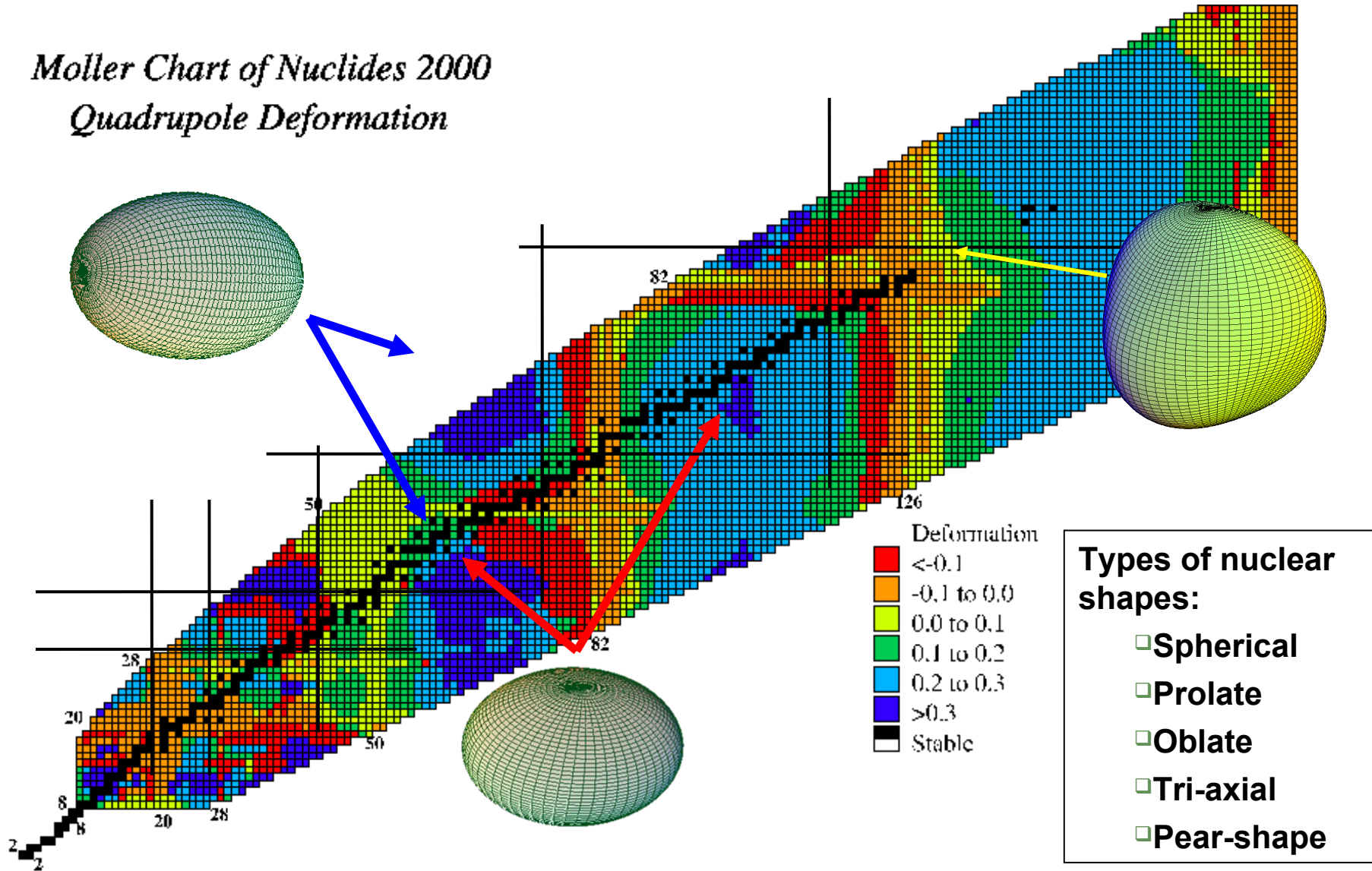
INFN, Sezione di Firenze, Italy

Inter University Accelerator Center, Delhi, India

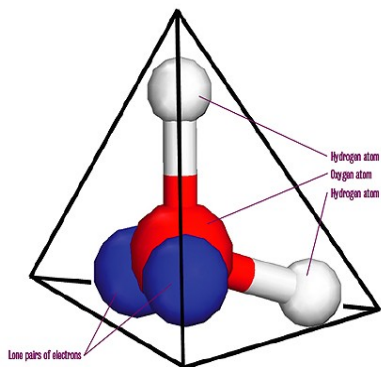
Bulgarian Accedemy of Science, Sofia, Bulgaria

Standard Nuclear Shapes

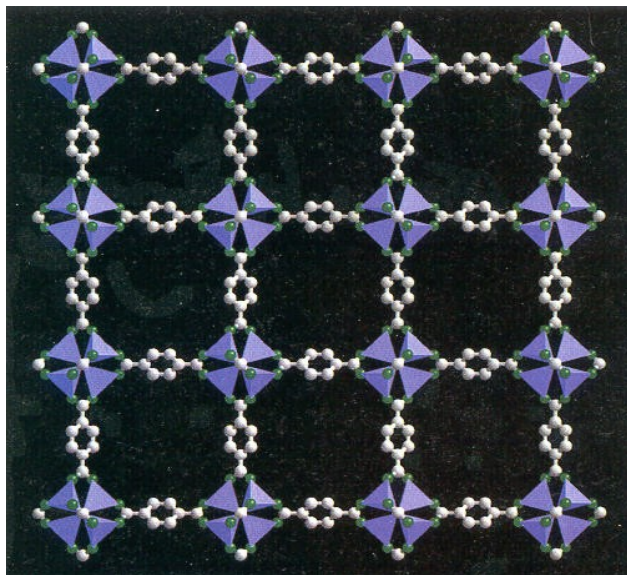
*Moller Chart of Nuclides 2000
Quadrupole Deformation*



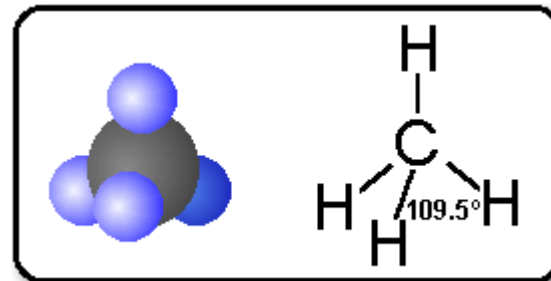
Molecular Structures of Organic/Inorganic Compounds, Metal Clusters: Point Symmetries



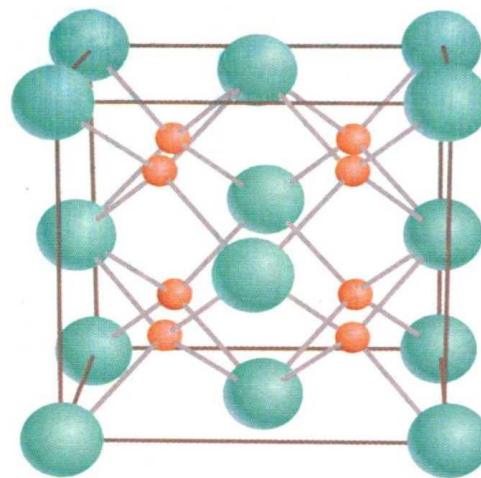
Water: The oxygen atom has two remaining pairs of electrons. These lone electron pairs and the hydrogen atoms are as far apart as possible, creating a tetrahedral arrangement. The oxygen lies at the centre of a tetrahedron



Synthetic inorganic-organic compound with ZnO₄ tetrahedral clusters linked by C₆H₄-C-O₂ "struts" (Li, Nature, 1999). 1.29 nm spacing between centers of adjacent clusters.



Methane is the simplest hydrocarbon molecule present in natural gas. This molecule provides the basis for the tetrahedral geometries at each carbon in a hydrocarbon chain.

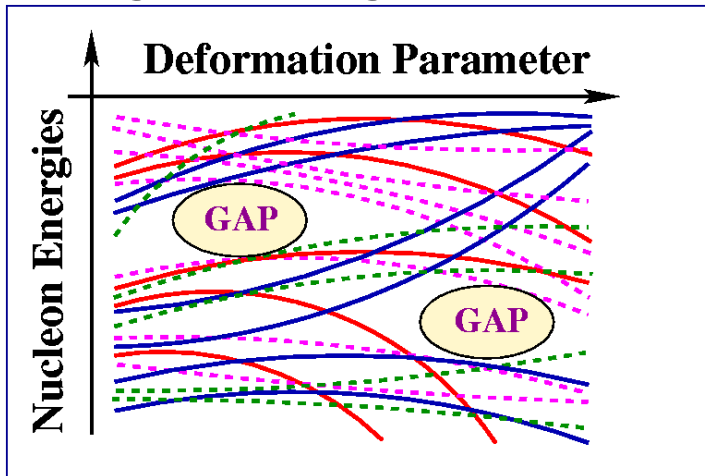


Face-centered-cubic (fcc) crystal structure of PuO₂ (Pu atoms in green, O atoms in red).

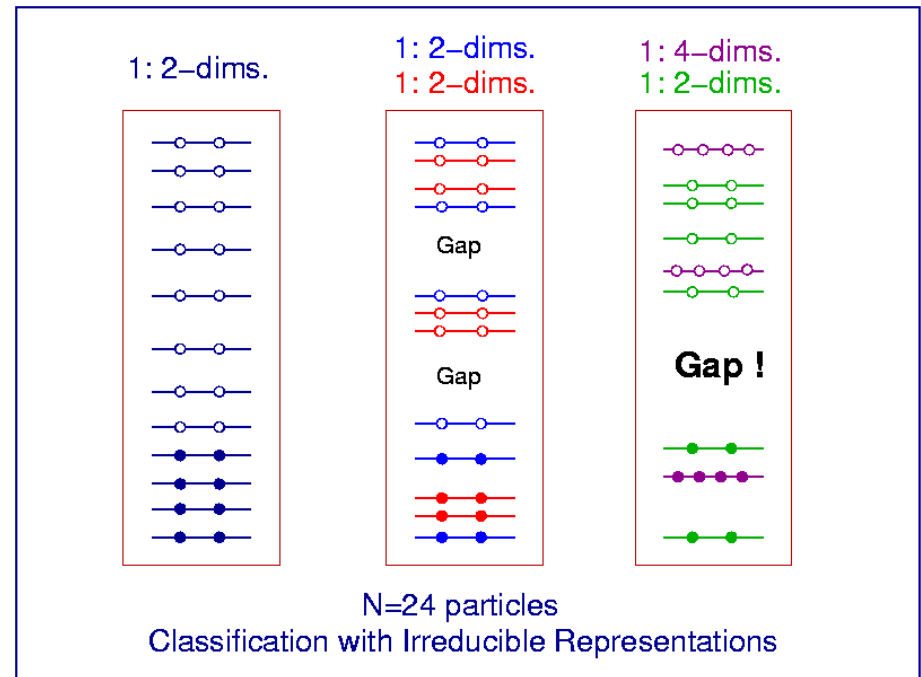
- **C₁ Point Group**
- **C₁ Point Group**
- **C_s Point Group**
- **C_n Point Groups**
- **C_{nv} Point Groups**
- **C_{nh} Point Groups**
- **D_n Point Groups**
- **D_{nh} Point Groups**
- **D_{nd} Point Groups**
- **S_n Point Groups**
- **Tetrahedral Point Groups**
- **Octahedral Point Groups**
- **Icosahedral Point Groups**
- **Spherical Point Group**

Point Symmetries and Nuclear Stability

- **Shell Gaps**
 ⇒ Stable configurations
- In nuclei:
 Higher degeneracies




J. Dudek, A. Gózdź, N. Schunck and M. Miskiewicz
 Phys. Rev. Lett. **88** 252502 (2002)



Degeneracies are a direct consequence of the underlying point symmetry of the shape

Point Groups and Level Degeneracy

Properties	High symmetries		Low symmetries
Type	Spherical	Tetrahedral	Octahedral Any other...
Number of Symmetry Elements	∞	48	96 ...
New Degeneracies	$2j + 1$	4, 2, 2	4, 2, 2 4, 2, 2 

Kramers Degeneracy (= time-reversal symmetry)

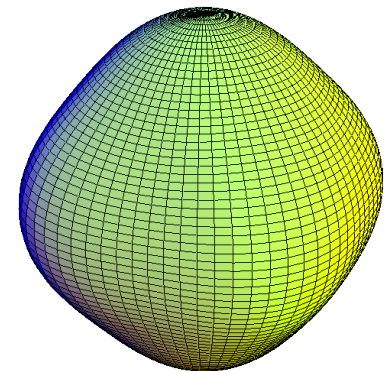
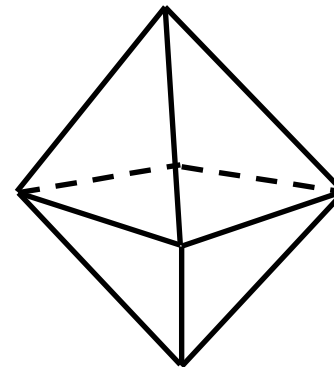
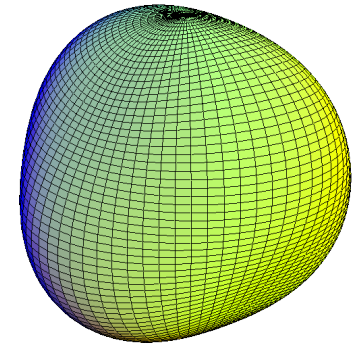
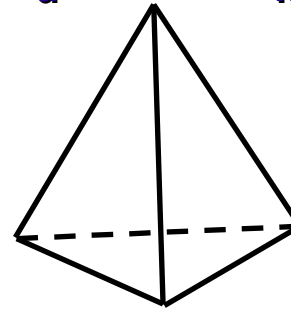
Survey of the properties of a few point groups

Symmetry Groups T_d and O_h

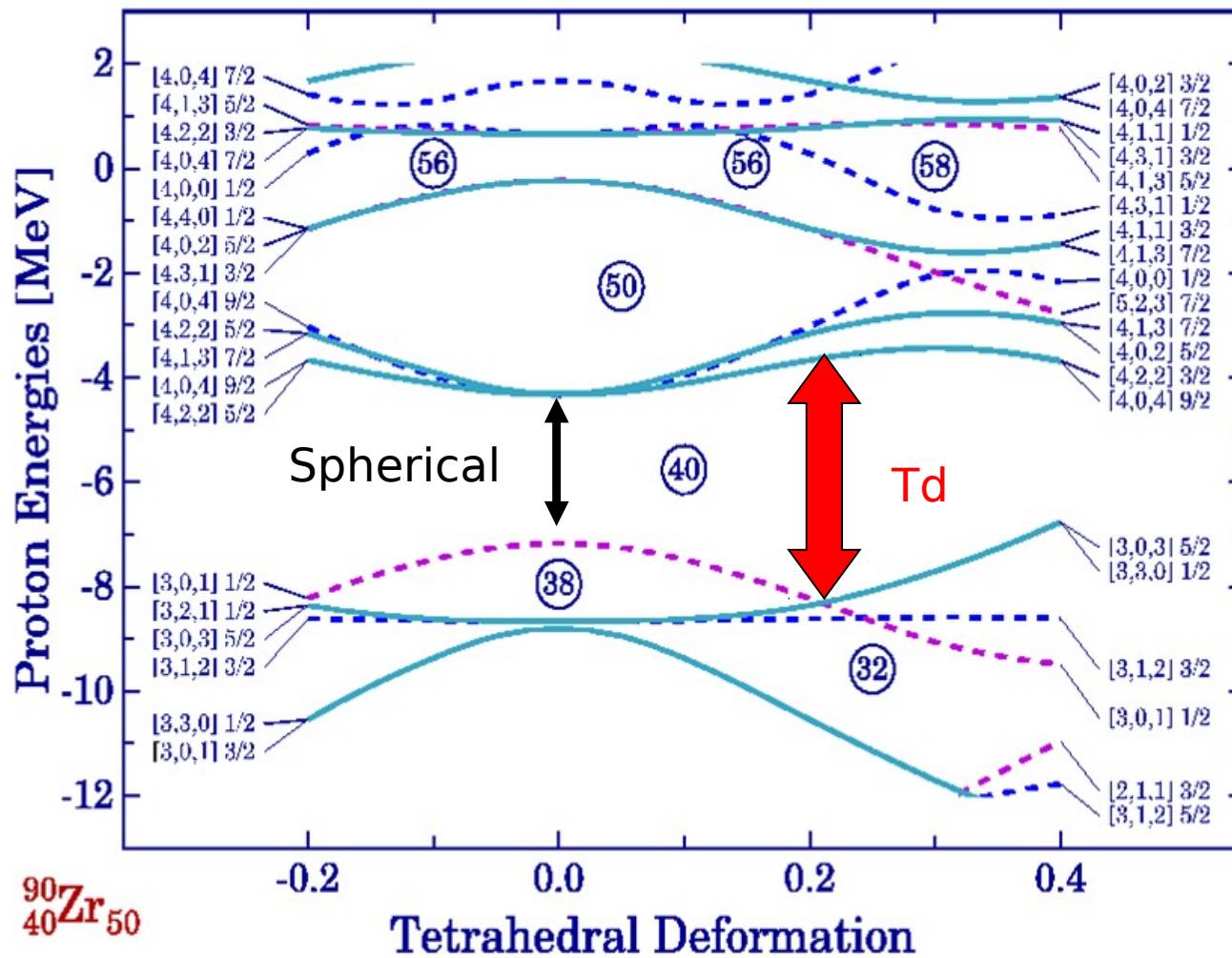
- Parameterization of the shape symmetries:

$$R(\theta, \varphi) = R_0 c(\alpha) \left[1 + \sum_{\lambda} \sum_{\mu=-\lambda}^{+\lambda} \alpha_{\lambda\mu} Y_{\lambda\mu}(\theta, \varphi) \right]$$

- Tetrahedral: $\alpha_{32} \neq 0$
- Octahedral: $\alpha_{40}, \alpha_{44} \neq 0$
- Other possibilities involving higher order multipoles $\alpha_{\lambda\mu}$



Tetrahedral Shell Gaps



Tetrahedral Magic Numbers

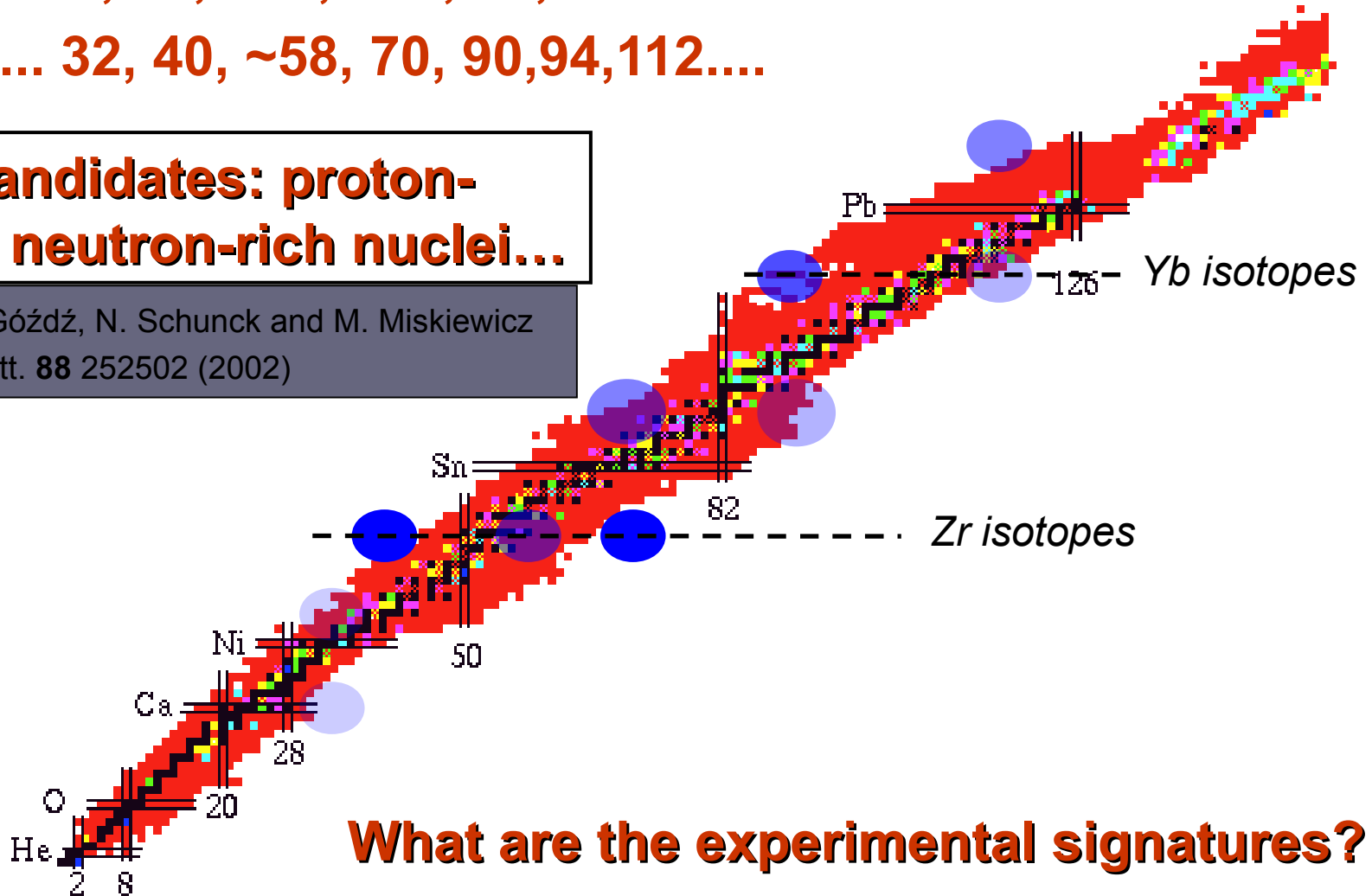
- From a WS potential:

$$Z = \dots 32, 40, \sim 56, \sim 64, 70, \sim 90 \dots$$

$$N = \dots 32, 40, \sim 58, 70, 90, 94, 112 \dots$$

Best candidates: proton-rich or neutron-rich nuclei...

J. Dudek, A. Gózdź, N. Schunck and M. Miskiewicz
Phys. Rev. Lett. **88** 252502 (2002)

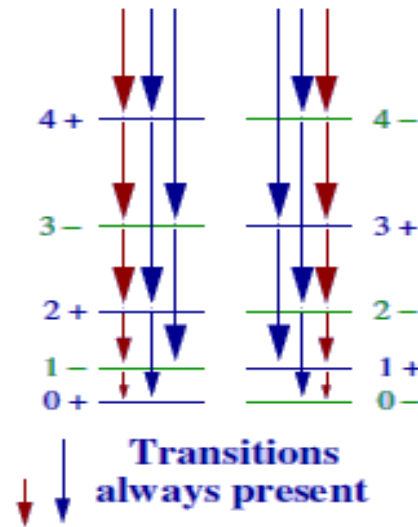


What are the experimental signatures?

Ideal Case: Extreme-Symmetry limit $Q_2=0$ & $Q_1=0$

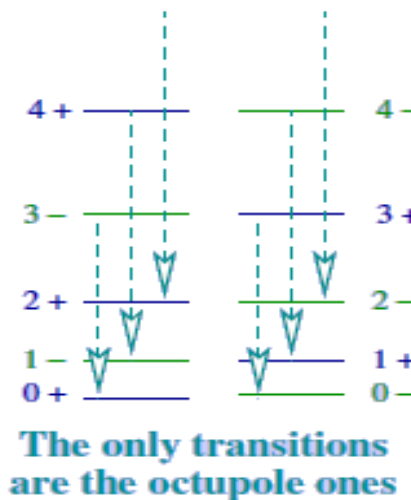
The mechanism of zero-point quadrupole motion about zero-quadrupole deformation

**Dipole Moment
non-zero**



Pear-shape

**Dipole Moment
vanishes**



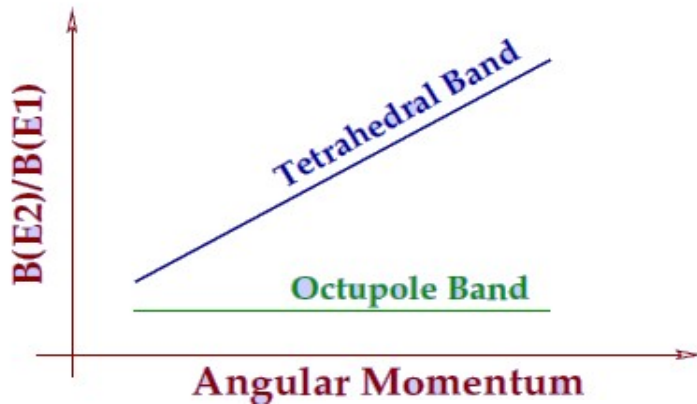
Tetrahedral

Ideal static-THS picture needs to be modified when we wish to address the problem of radiation

It is known that at reduced transition probabilities $B(E1)$ and $B(E3)$ comparable, the $E1$ -decay is $10E12$ more probable !!

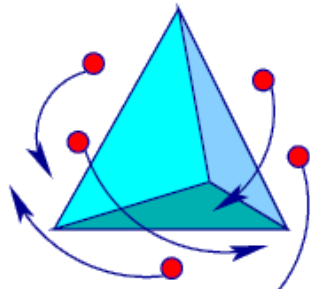
Therefore it will be necessary to look into problems of partial symmetry breaking in the case of the two high-rank symmetries

Schematic: Predictions for $B(E2)/B(E1)$

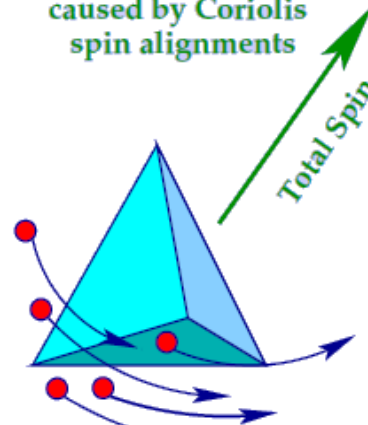


Spin dependence on $B(E2)/B(E1)$

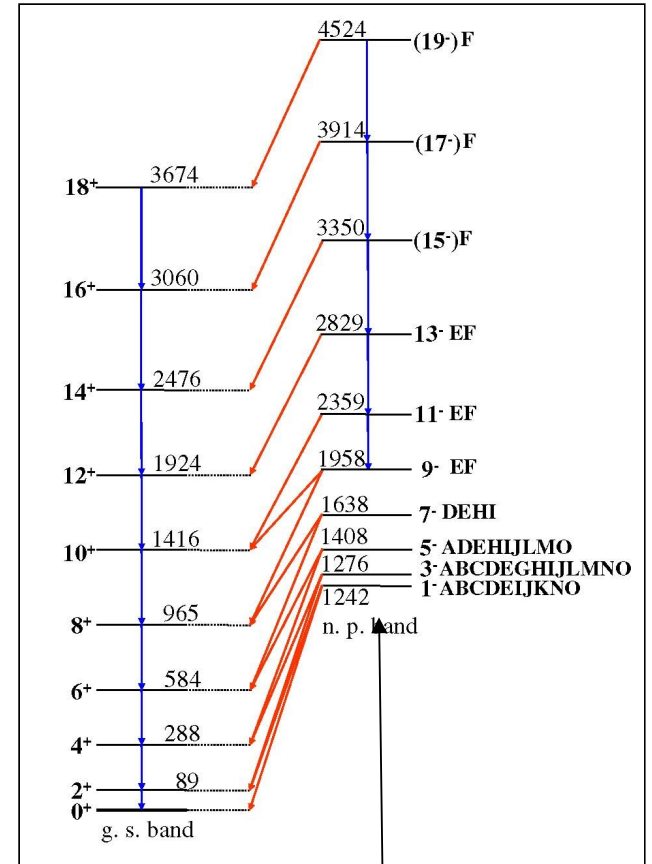
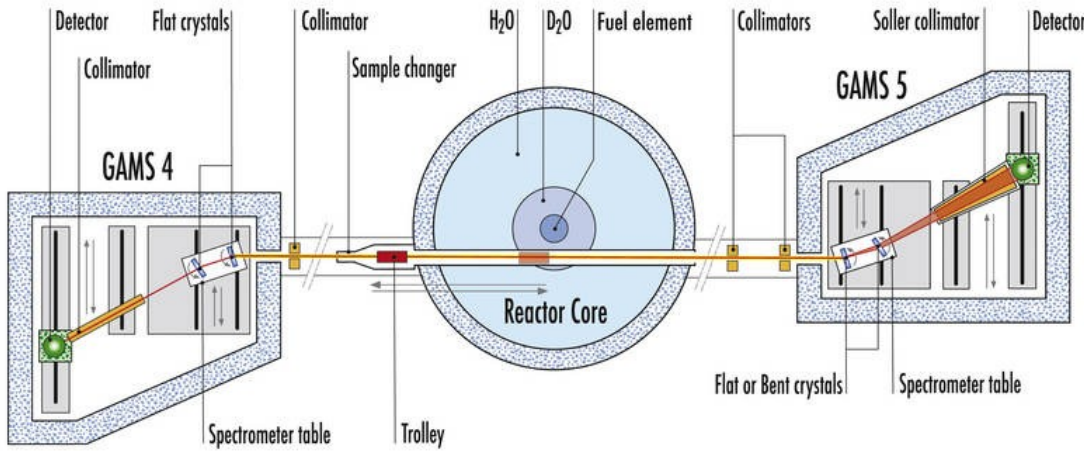
Valence particles cause a certain quadrupole polarisation



Additional polarisation caused by Coriolis spin alignments



Spin-alignment will cause additional quadrupole polarization



(n,γ) on $^{155}\text{Gd} \rightarrow ^{156}\text{Gd}$

Ultrahigh resolution γ -ray spectroscopy at ILL

Intensity of the 132 keV $5^- \rightarrow 3^- \gamma$ ray

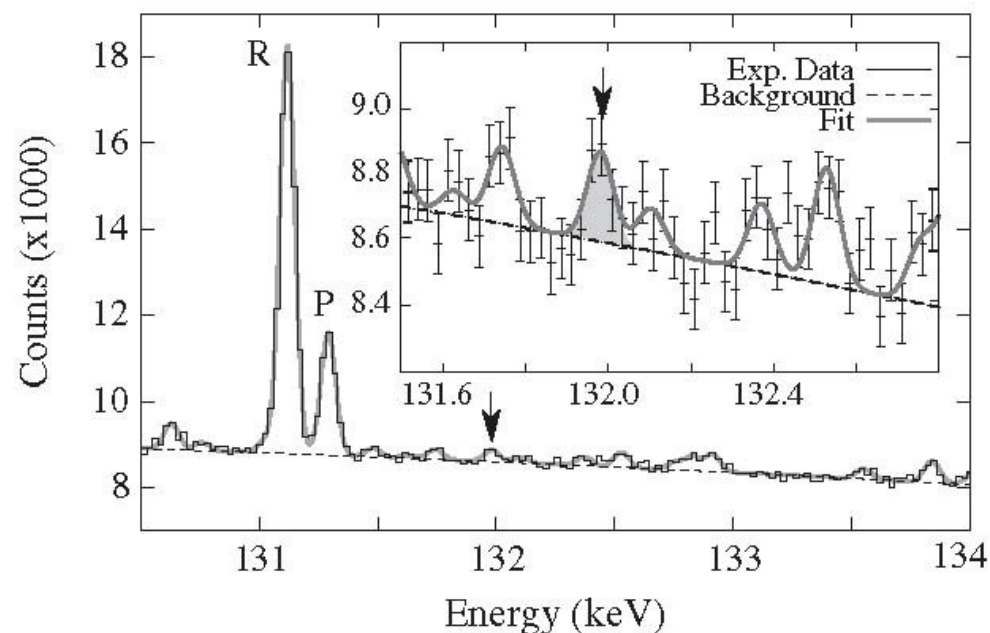
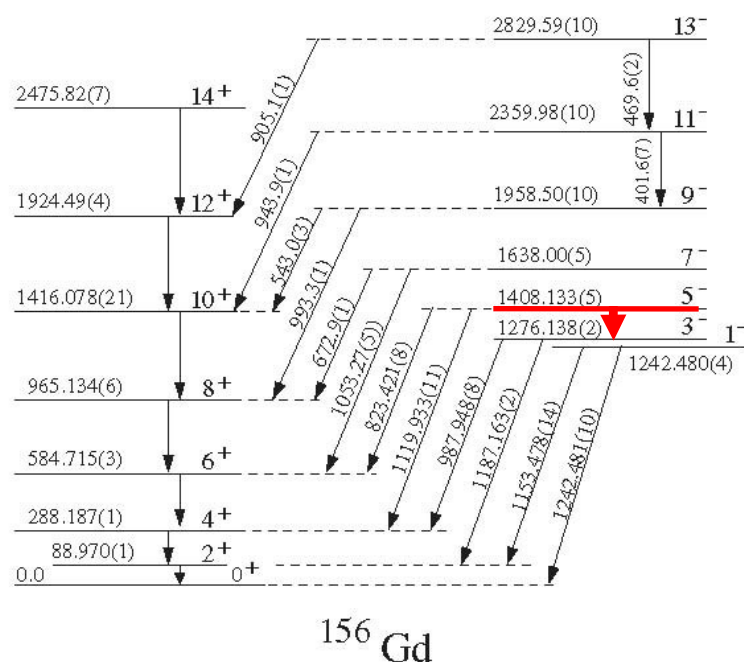
Ultrahigh-Resolution γ -Ray Spectroscopy of ^{156}Gd : A Test of Tetrahedral Symmetry

M. Jentschel,¹ W. Urban,^{1,2} J. Krempel,¹ D. Tonev,³ J. Dudek,⁴ D. Curien,⁴ B. Lauss,⁵ G. de Angelis,⁶ and P. Petkov³

PRL 104, 222502 (2010)

PHYSICAL PRL 104, 222502 (2010)

PHYSICAL R



Lifetime of the 5- level at 1.408 MeV
Intensity of the 132 keV $5^- \rightarrow 3^-$ γ ray

Quadrupole moment of the 5⁻ state in ¹⁵⁶Gd

$$B(E2 \ 5^- \rightarrow 3^-) = 293 \ (+61-134) \text{ W.U.}$$

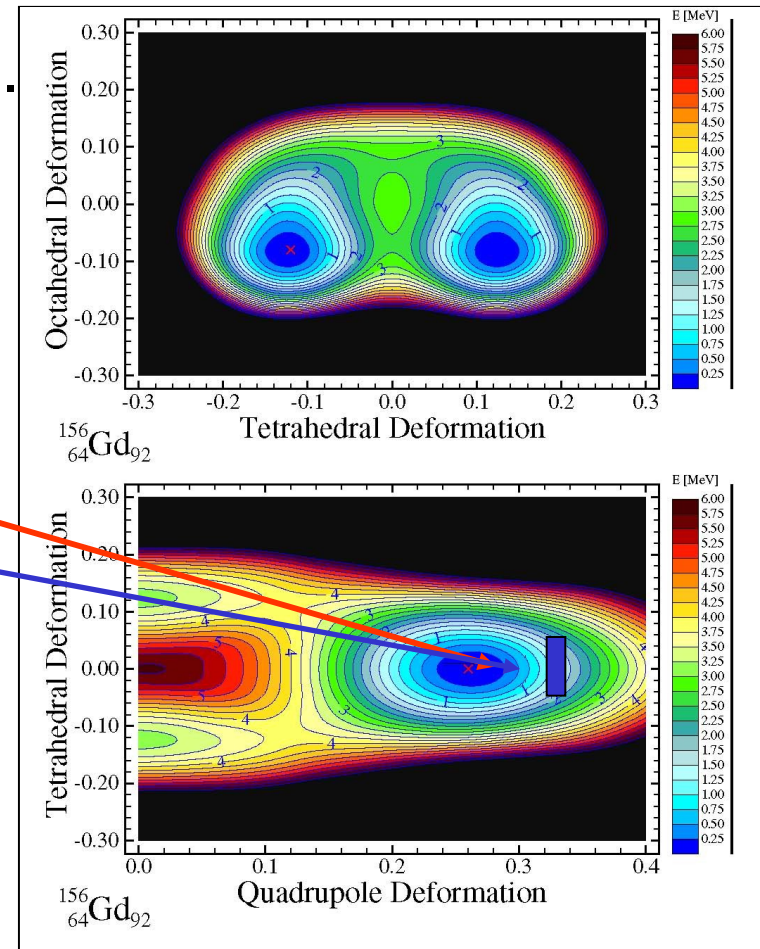
$$B(E2 \ 2^+ \rightarrow 0^+) = 186.1(20) \text{ W.U.}$$

$$\beta_{5^-} = 0.35(15)$$

$$\beta_{2^+} = 0.3378(18)$$

$$Q_{5^-} = 7.1 \ (+0.7-1.6) \text{ b}$$

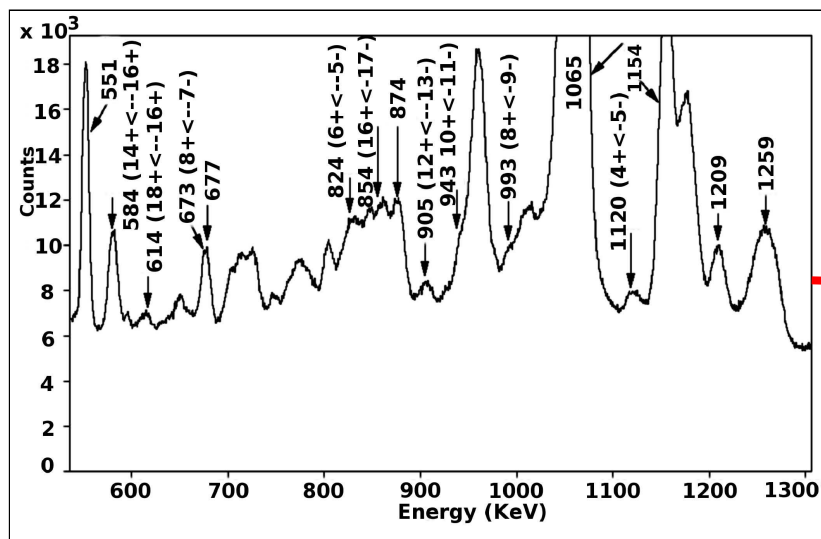
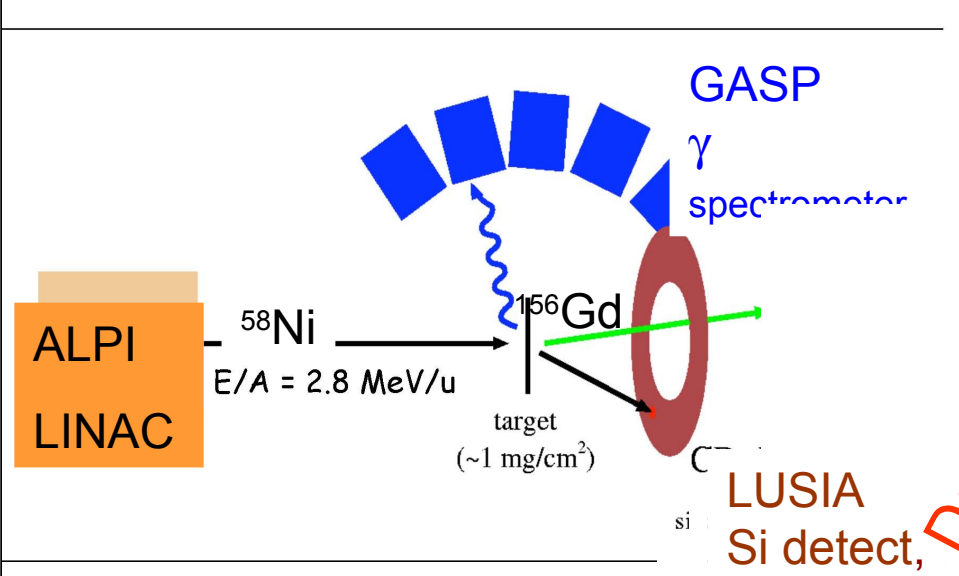
$$Q_{2^+} = 6.83 \ (37) \text{ b}$$



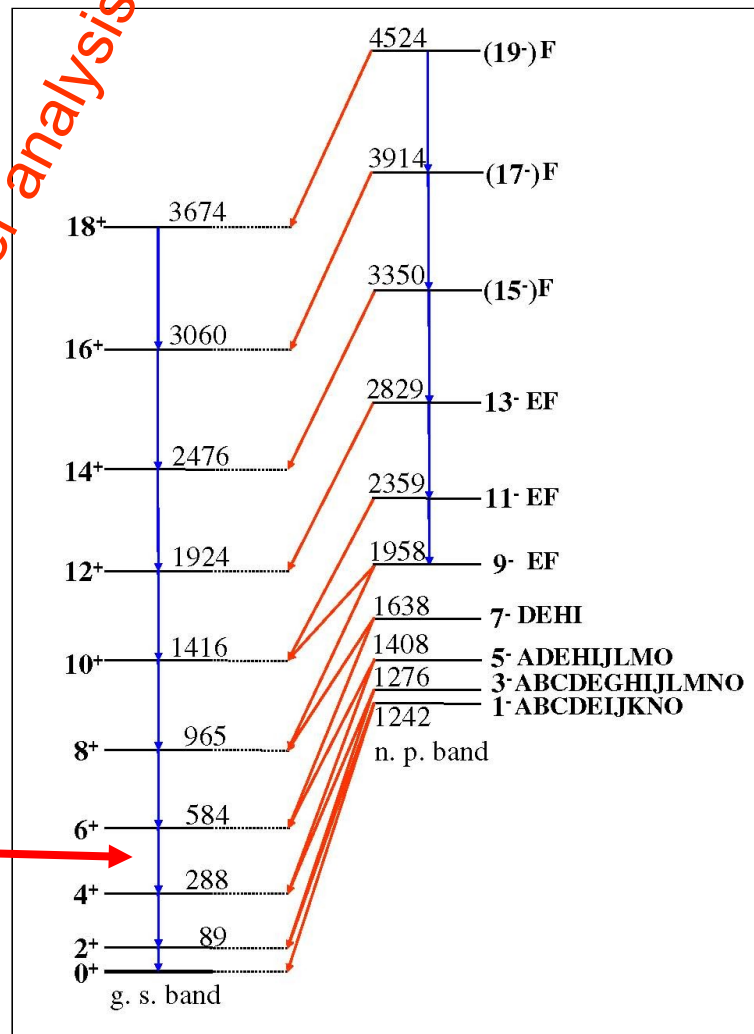
The negative parity band in ¹⁵⁶Gd is incompatible with the description based on tetrahedral symmetry

Electromagnetic transition matrix elements and quadrupole moment (with sign) accessible by low energy Coulomb excitation

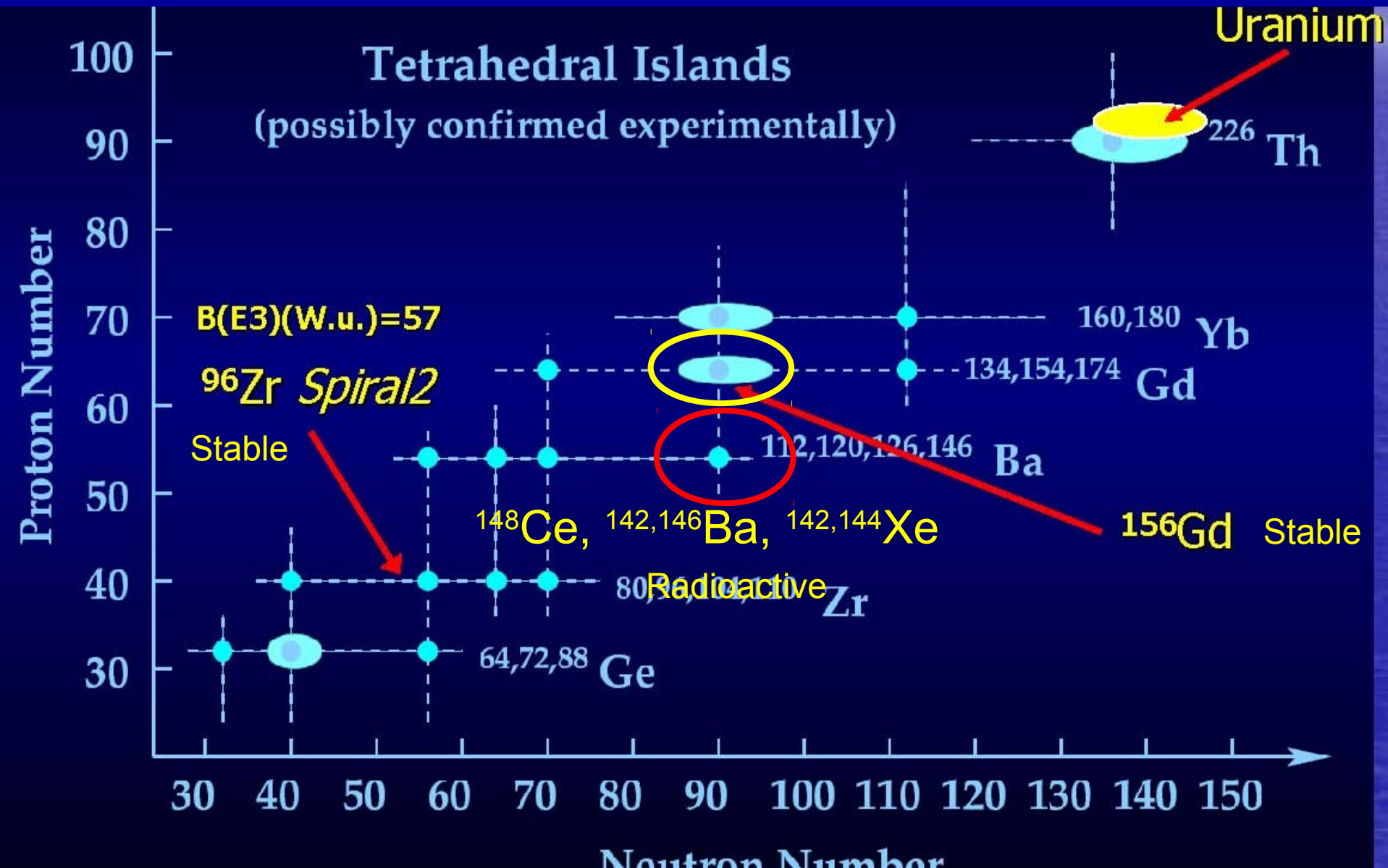
Rajesh Pratap Singh et al.
IUAC Delhi, India



Data under analysis



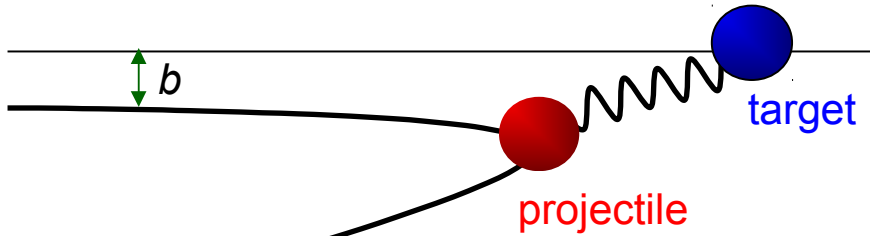
AIM of the LOI: Transition matrix elements and Q-moments of the exotic octupole bands from Coulex for the n-rich Ce, Ba, Xe nuclei. SPES intensities $\sim 10^5$ - 10^7 pps



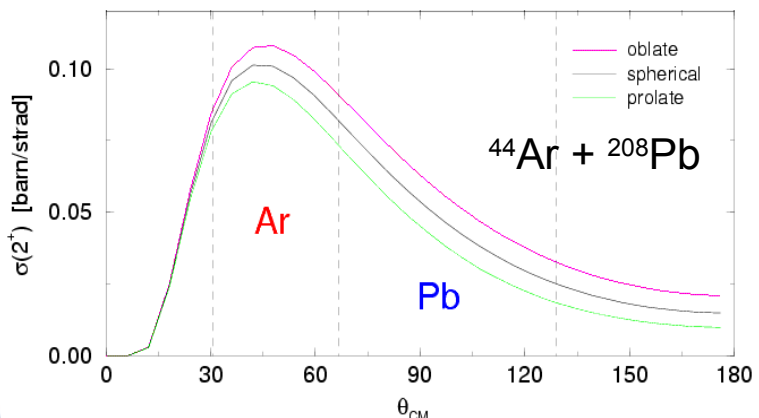
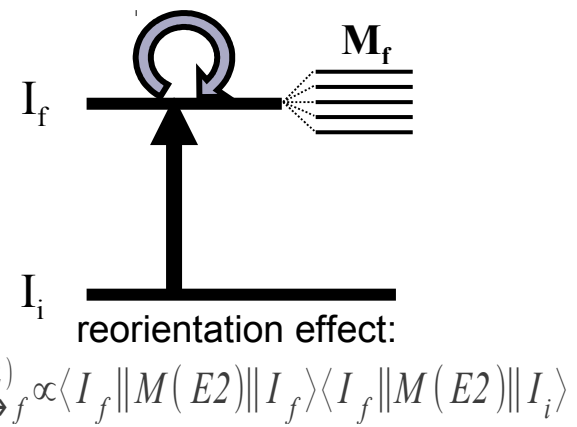
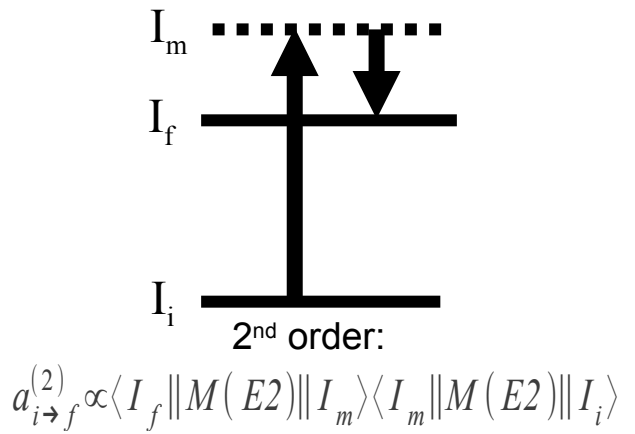
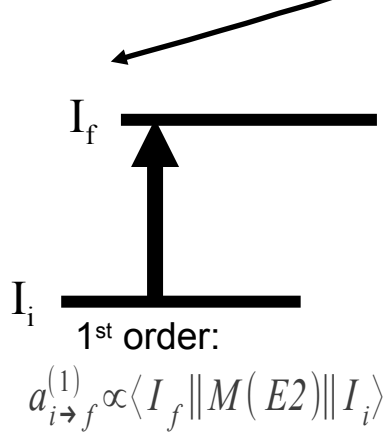
AIM of the LOI: Transition matrix elements and Q-moments (sign) of the exotic octupole bands from reorientation effects for the n-rich Ce, Ba, Xe nuclei.

SPES intensities $\sim 10^5$ - 10^7 pps

Nuclear excitation by electromagnetic field acting between nuclei.

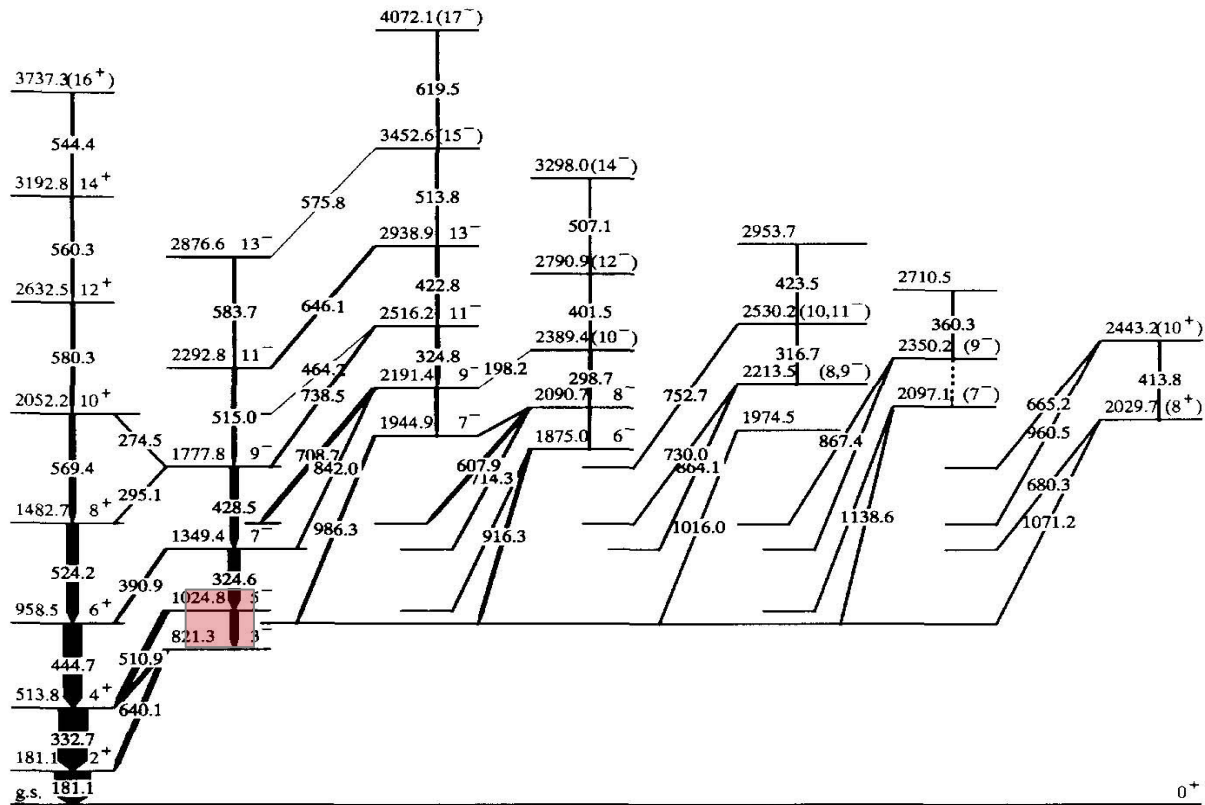


The excitation cross section is a direct measure of the $E\lambda$ matrix elements.



differential Coulomb excitation cross section
 \Rightarrow transition probability $B(E2)$
 \Rightarrow quadrupole moment Q_s

Excited states of the Z=56 N=90 ^{146}Ba nucleus. The negative parity band is a candidate for tetrahedral symm



Proposed experiment: Coulomb excitation of the quadrupole and octupole structures

We propose to populate the above mentioned bands in $^{144,146}\text{Ba}$ and $^{142,144}\text{Xe}$ nuclei through Coulomb excitation using the following beams:

$^{144,146}\text{Ba}$ and $^{142,144}\text{Xe}$ at an energy of 550 MeV

Impinging on a ^{58}Ni target of about 100 mg/cm².

We would use the position sensitive silicon detector TRACE or a Si disk to detect the scattered beam particles in coincidence with the gamma events detected in the GALILEO gamma ray spectrometer.

The cross-section for the population of the negative parity band (based on the 3⁺ state) we are interested in is estimated to be about $2.5 \cdot 10^{-3}$ barn using the GOSIA calculations

We will suppose that the branching ratio E3/E1 is of about 50%,

The efficiency for the GALILEO array about 6% and that for the particle detector TRACE about 50%.

Assuming a ^{146}Ba intensity of about $1.4 \cdot 10^4$ pps accelerated by the SPES radioactive nuclear beam facility

50 particle-gamma events per day, 1-2 weeks of beam time allowing to extract the B(E3) transition matrix element with an accuracy of about 25%.