

Global Status of Sterile Neutrino Scenarios

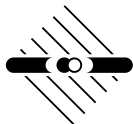
Joachim Kopp

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Outline

- 1 Theoretical Motivation
- 2 Sterile Neutrino Oscillations: The Global Picture
- 3 Sterile Neutrinos in Cosmology
- 4 Conclusions

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Sterile neutrinos

ster·ile  *adjective* \ˈster-əl, chiefly British -ī(-ə)l\

Definition of STERILE

c : lacking in stimulating emotional or intellectual quality :
LIFELESS <a *sterile* work of art>

...so why do we talk about **sterile neutrinos**?

Sterile neutrinos

Definition

Sterile neutrino = SM singlet fermion

- Very generic extension of the SM
 - ▶ can be leftovers of **extended gauge multiplets** (e.g. GUT multiplets)
 - Very useful in phenomenology:
 - ▶ Can explain **smallness of neutrino mass** (seesaw mechanism, $m \sim \text{TeV} \dots M_{\text{Pl}}$)
 - ▶ Can explain **baryon asymmetry of the Universe** (leptogenesis, $m \gg 100 \text{ GeV}$)
 - ▶ Can explain **dark matter** ($m \sim \text{keV}$)
 - ▶ Can explain various **neutrino oscillation anomalies** ($m \sim \text{eV}$)
- **This talk**



eV-scale sterile neutrinos

Typical Lagrangian:

$$\mathcal{L} \supset \frac{1}{2} M_{ij}^{(a)} \overline{\nu_i^c} \nu_j + \frac{1}{2} M_{is}^{(s)} \overline{\nu_i^c} \nu_s + h.c.$$

⇒ mass mixing between **active** and **sterile** neutrinos

Signatures in oscillation experiments

- **Disappearance of active neutrinos**
(e.g. $\nu_e \rightarrow \nu_s$ oscillations)
Atmospheric, Solar, Reactor, Pion decay beam, Radioactive source experiments
- **Anomalous transitions among active neutrinos** (“appearance”)
(e.g. $\nu_\mu \rightarrow \nu_s \rightarrow \nu_e$)
Pion decay beams
- **Oscillation length** $L^{\text{osc}} = 4\pi E / \Delta m_{41}^2$ different from SM expectation
(typically shorter)

Notation: $\Delta m_{jk}^2 = m_j^2 - m_k^2$; $m_{4,5}$: mostly sterile, $m_{1,2,3}$: mostly active

Neutrino oscillations with more than 3 flavours

Theoretical challenge: complicated dependence of observable oscillation probabilities on the fundamental parameters of the theory

3-flavour mixing matrix

$$\begin{pmatrix} \cos[\theta_{12}] \cos[\theta_{13}] & \cos[\theta_{13}] \sin[\theta_{12}] & e^{-i\delta} \sin[\theta_{13}] \\ -\cos[\theta_{23}] \sin[\theta_{12}] - e^{i\delta} \cos[\theta_{12}] \sin[\theta_{13}] \sin[\theta_{23}] & \cos[\theta_{12}] \cos[\theta_{23}] - e^{i\delta} \sin[\theta_{12}] \sin[\theta_{13}] \sin[\theta_{23}] & \cos[\theta_{13}] \sin[\theta_{23}] \\ -e^{i\delta} \cos[\theta_{12}] \cos[\theta_{23}] \sin[\theta_{13}] + \sin[\theta_{12}] \sin[\theta_{23}] & -e^{i\delta} \cos[\theta_{23}] \sin[\theta_{12}] \sin[\theta_{13}] - \cos[\theta_{12}] \sin[\theta_{23}] & \cos[\theta_{13}] \cos[\theta_{23}] \end{pmatrix}$$

Neutrino oscillations with more than 3 flavours

Theoretical challenge: complicated dependence of observable oscillation probabilities on the fundamental parameters of the theory

4-flavour mixing matrix

$$\left\{ \begin{aligned} & \left\{ \cos[\theta_{12}] \cos[\theta_{13}] \cos[\theta_{14}], e^{-i\delta_{21}} \cos[\theta_{13}] \cos[\theta_{14}] \sin[\theta_{12}], e^{-i\delta_{31}} \cos[\theta_{14}] \sin[\theta_{13}], \sin[\theta_{14}] \right\}, \\ & \left\{ -e^{i\delta_{22}} \cos[\theta_{23}] \cos[\theta_{24}] \sin[\theta_{12}] + \cos[\theta_{12}] \left(-e^{i\delta_{33}} \cos[\theta_{24}] \sin[\theta_{13}] \sin[\theta_{23}] - e^{-i\delta_{41}} \cos[\theta_{13}] \sin[\theta_{14}] \sin[\theta_{24}] \right), \right. \\ & e^{-i\delta_{22}} \left(e^{i\delta_{22}} \cos[\theta_{12}] \cos[\theta_{23}] \cos[\theta_{24}] + \sin[\theta_{12}] \left(-e^{i\delta_{33}} \cos[\theta_{24}] \sin[\theta_{13}] \sin[\theta_{23}] - e^{-i\delta_{41}} \cos[\theta_{13}] \sin[\theta_{14}] \sin[\theta_{24}] \right) \right), \\ & e^{-i\delta_{33}} \left(e^{i\delta_{33}} \cos[\theta_{13}] \cos[\theta_{24}] \sin[\theta_{23}] - e^{-i\delta_{41}} \sin[\theta_{13}] \sin[\theta_{14}] \sin[\theta_{24}] \right), e^{-i\delta_{41}} \cos[\theta_{14}] \sin[\theta_{24}] \left. \right\}, \\ & \left\{ -e^{i\delta_{22}} \sin[\theta_{12}] \left(-\cos[\theta_{34}] \sin[\theta_{23}] - e^{i\delta_{41}} \cos[\theta_{23}] \sin[\theta_{24}] \sin[\theta_{34}] \right) + \right. \\ & \cos[\theta_{12}] \left(-\cos[\theta_{13}] \cos[\theta_{24}] \sin[\theta_{14}] \sin[\theta_{34}] - e^{i\delta_{33}} \sin[\theta_{13}] \left(\cos[\theta_{23}] \cos[\theta_{34}] - e^{i\delta_{41}} \sin[\theta_{23}] \sin[\theta_{24}] \sin[\theta_{34}] \right) \right), \\ & e^{-i\delta_{22}} \left(e^{i\delta_{22}} \cos[\theta_{12}] \left(-\cos[\theta_{34}] \sin[\theta_{23}] - e^{i\delta_{41}} \cos[\theta_{23}] \sin[\theta_{24}] \sin[\theta_{34}] \right) + \right. \\ & \left. \sin[\theta_{12}] \left(-\cos[\theta_{13}] \cos[\theta_{24}] \sin[\theta_{14}] \sin[\theta_{34}] - e^{i\delta_{33}} \sin[\theta_{13}] \left(\cos[\theta_{23}] \cos[\theta_{34}] - e^{i\delta_{41}} \sin[\theta_{23}] \sin[\theta_{24}] \sin[\theta_{34}] \right) \right) \right), \\ & e^{-i\delta_{33}} \left(-\cos[\theta_{24}] \sin[\theta_{13}] \sin[\theta_{14}] \sin[\theta_{34}] + e^{i\delta_{33}} \cos[\theta_{13}] \left(\cos[\theta_{23}] \cos[\theta_{34}] - e^{i\delta_{41}} \sin[\theta_{23}] \sin[\theta_{24}] \sin[\theta_{34}] \right) \right), \cos[\theta_{14}] \cos[\theta_{24}] \sin[\theta_{34}] \left. \right\}, \\ & \left\{ -e^{i\delta_{22}} \sin[\theta_{12}] \left(-e^{i\delta_{41}} \cos[\theta_{23}] \cos[\theta_{34}] \sin[\theta_{24}] + \sin[\theta_{23}] \sin[\theta_{34}] \right) + \right. \\ & \cos[\theta_{12}] \left(-\cos[\theta_{13}] \cos[\theta_{24}] \cos[\theta_{34}] \sin[\theta_{14}] - e^{i\delta_{33}} \sin[\theta_{13}] \left(-e^{i\delta_{41}} \cos[\theta_{34}] \sin[\theta_{23}] \sin[\theta_{24}] - \cos[\theta_{23}] \sin[\theta_{34}] \right) \right), \\ & e^{-i\delta_{22}} \left(e^{i\delta_{22}} \cos[\theta_{12}] \left(-e^{i\delta_{41}} \cos[\theta_{23}] \cos[\theta_{34}] \sin[\theta_{24}] + \sin[\theta_{23}] \sin[\theta_{34}] \right) + \right. \\ & \left. \sin[\theta_{12}] \left(-\cos[\theta_{13}] \cos[\theta_{24}] \cos[\theta_{34}] \sin[\theta_{14}] - e^{i\delta_{33}} \sin[\theta_{13}] \left(-e^{i\delta_{41}} \cos[\theta_{34}] \sin[\theta_{23}] \sin[\theta_{24}] - \cos[\theta_{23}] \sin[\theta_{34}] \right) \right) \right), \\ & e^{-i\delta_{33}} \left(-\cos[\theta_{24}] \cos[\theta_{34}] \sin[\theta_{13}] \sin[\theta_{14}] + e^{i\delta_{33}} \cos[\theta_{13}] \left(-e^{i\delta_{41}} \cos[\theta_{34}] \sin[\theta_{23}] \sin[\theta_{24}] - \cos[\theta_{23}] \sin[\theta_{34}] \right) \right), \cos[\theta_{14}] \cos[\theta_{24}] \cos[\theta_{34}] \left. \right\} \end{aligned} \right\}$$

Neutrino oscillations with more than 3 flavours

Theoretical challenge: complicated dependence of observable oscillation probabilities on the fundamental parameters of the theory

Analysis strategy

- Understand oscillation probabilities **analytically**
- Determine **relevant parameters** / parameter combinations **for each experiment**
- Use **theoretical knowledge** to **simplify computations**
- Perform **global fit**

Giunti Laveder Archidiacono Fornengo Hannestad Melchiori Li Liu Long
Conrad Ignarra Karagiorgi Shaevitz Spitz Djurcic Sorel
JK Machado Maltoni Schwetz (**this talk**)

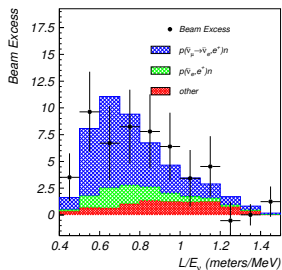
Oscillation anomalies: LSND and MiniBooNE

● LSND:

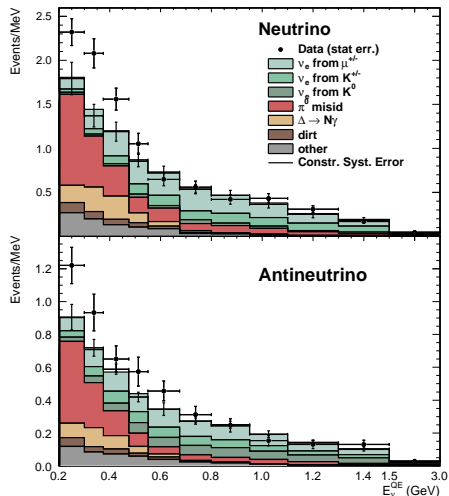
- ▶ $\bar{\nu}_e$ appearance in $\bar{\nu}_\mu$ beam from stopped pion source ($> 3\sigma$)

● MiniBooNE:

- ▶ No significant ν_e or $\bar{\nu}_e$ excess in the LSND-preferred region
- ▶ but $\bar{\nu}_e$ consistent with LSND
- ▶ Low- E excess not understood



LSND hep-ex/0104049

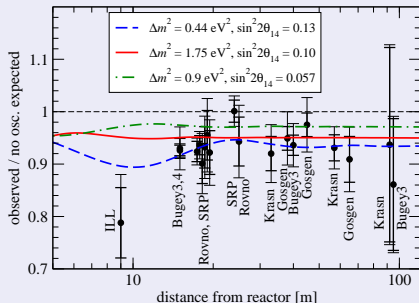


MiniBooNE arXiv:1207.4809

Reactor and gallium experiments

- Recent **reevaluation** of expected reactor $\bar{\nu}_e$ flux is $\sim 3.5\%$ **higher** than previous prediction
Mueller et al. arXiv:1101.2663, P. Huber arXiv:1106.0687
- **Method:** Use measured β -spectra from ^{238}U , ^{235}U , ^{241}Pu fission at ILL and convert to $\bar{\nu}_e$ spectrum (for single β -decay: $E_\nu = Q - E_e$)
- Requires knowledge of Q -values for **all** contributing decays.
→ take from nuclear databases where available, fit to data otherwise

see talks by [Michel Cribier](#) and [Patrick Huber](#)



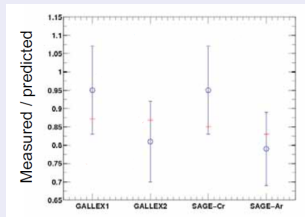
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→ take from nuclear databases where available, fit to data otherwise

see talks by [Michel Cribier](#) and [Patrick Huber](#)

- Experiments with **intense radioactive ν_e sources** (^{51}Cr and ^{37}Ar)
- Neutrino detection via
 $^{71}\text{Ga} + \nu_e \rightarrow ^{71}\text{Ge} + e^-$
- **Observation:** Neutrino **deficit** ($\sim 3\sigma$)

Giunti Laveder 1006.3244



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Data sets included in our fit

$\bar{\nu}_e$ disappearance

- SBL reactor experiments
- LBL reactor experiments
- KamLAND
- Radioactive source (Ga) experiments
- Solar neutrinos
- Atmospheric neutrinos
- ν_e - ^{12}C scattering in KARMEN, LSND

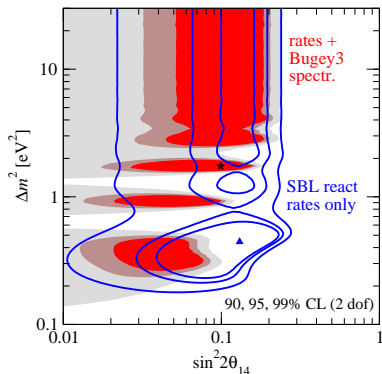
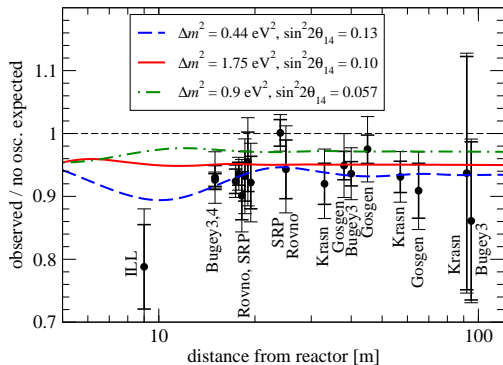
$\bar{\nu}_e$ appearance

- LSND
- MiniBooNE
- KARMEN
- NOMAD
- ICARUS
- E776

$\bar{\nu}_\mu$ disappearance

- Atmospheric neutrinos (includes *either* $\bar{\nu}_e$ disapp. *or* full matter effects)
- MiniBooNE (includes oscillations of backgrounds)
- MINOS CC+NC (full n -flavour oscillations in matter)
- CDHS

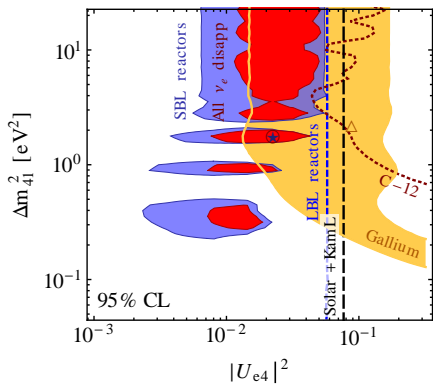
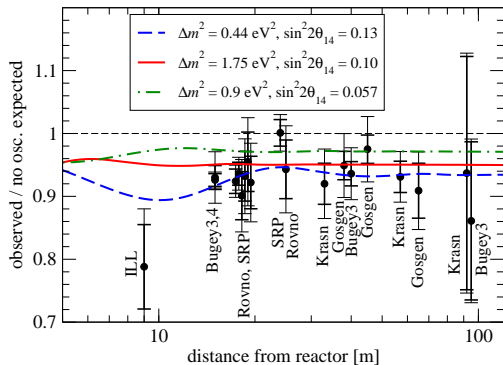
$\bar{\nu}_e$ disappearance in the 3+1 scenario



	$\sin^2 2\theta_{14}$	$\Delta m_{41}^2 [\text{eV}^2]$	χ_{\min}^2/dof (GOF)	$\Delta\chi_{\text{no osc}}^2/\text{dof}$ (CL)
SBL rates only	0.13	0.44	11.5/17 (83%)	11.4/2 (99.7%)
SBL incl. Bugey3 spect.	0.10	1.75	58.3/74 (91%)	9.0/2 (98.9%)

JK Machado Maltoni Schwetz, in preparation

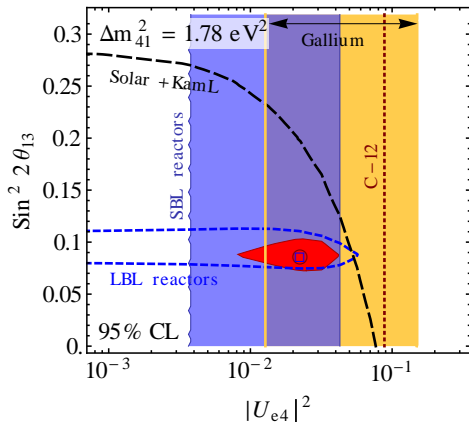
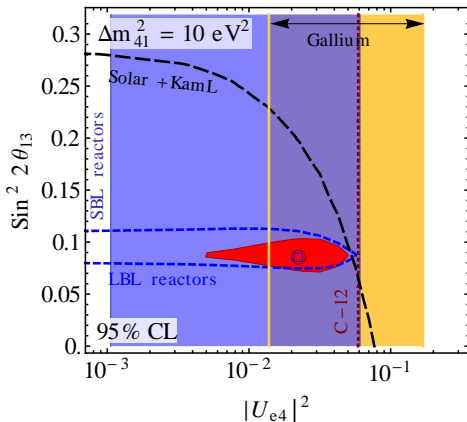
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SBL incl. Bugey3 spect.	0.10	1.75	58.3/74 (91%)	9.0/2 (98.9%)
SBL + Gallium	0.11	1.80	64.0/78 (87%)	14.0/2 (99.9%)
global ν_e disapp.	0.09	1.78	403.3/427 (79%)	12.6/2 (99.8%)

JK Machado Maltoni Schwetz, in preparation

Impact of θ_{13}

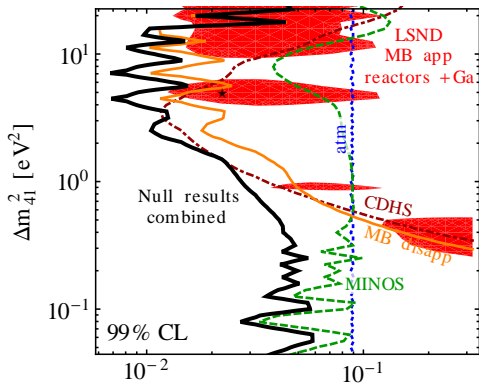


- Sterile neutrinos do not impact θ_{13} measurement
- $\theta_{13} \neq 0$ does not impact sterile neutrino search

JK Machado Maltoni Schwetz, in preparation

$\bar{\nu}_\mu$ disappearance in the 3+1 scenario

- Parameter regions favored by tentative hints are in tension with null results

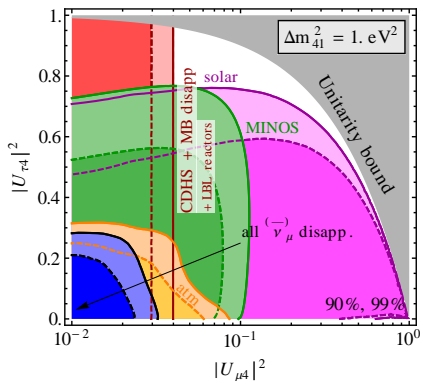
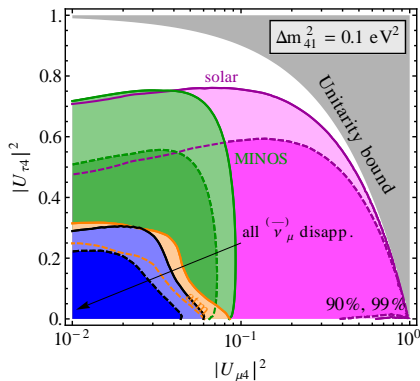


JK Machado Maltoni Schwetz, in preparation

$|U_{\mu 4}|^2$

$\bar{\nu}_\mu$ disappearance in the 3+1 scenario

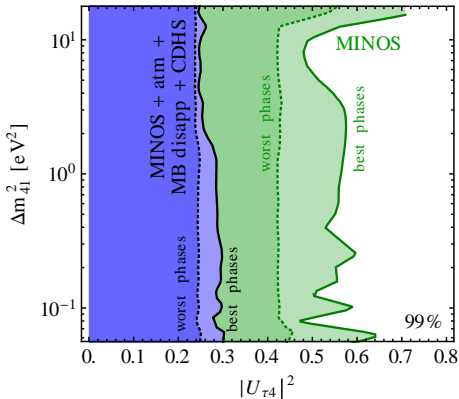
- Parameter regions favored by **tentative hints** are in **tension with null results**
- Constraints on $|U_{\tau 4}| \sim \sin \theta_{34}$ possible due to NC events and matter effects



JK Machado Maltoni Schwetz, in preparation

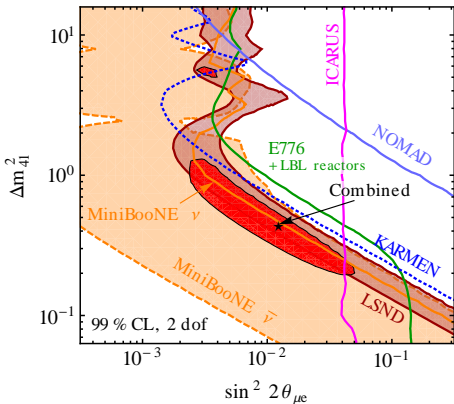
$\bar{\nu}_\mu$ disappearance in the 3+1 scenario

- Parameter regions favored by **tentative hints** are in **tension with null results**
- Constraints on $|U_{\tau 4}| \sim \sin \theta_{34}$ possible due to NC events and matter effects
- Complex phases important



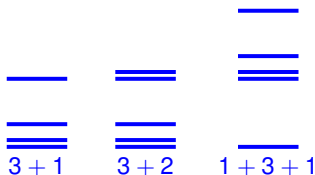
JK Machado Maltoni Schwetz, in preparation

$\bar{\nu}_e$ appearance in the 3+1 scenario and beyond



	χ_{3+1}^2/dof	χ_{3+2}^2/dof	$\chi_{1+3+1}^2/\text{dof}$
LSND	11.0/11	8.6/11	7.5/11
MiniB ν	19.3/11	10.6/11	9.1/11
MiniB $\bar{\nu}$	10.7/11	9.6/11	12.7/11
E776	32.4/24	29.2/24	31.3/24
KARMEN	9.8/9	8.6/9	9.0/9
NOMAD	0.0/1	0.0/1	0.0/1
ICARUS	2.0/1	2.3/1	1.5/1
Combined	87.9/66	72.7/63	74.6/63

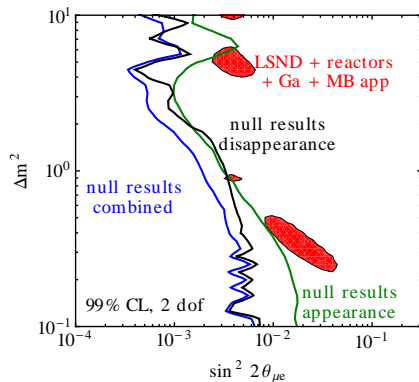
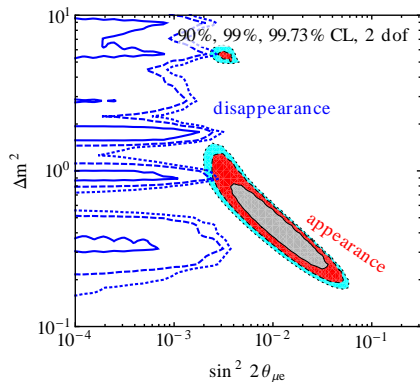
- Global fit to all appearance data is **consistent**
- **Background oscillations** important in MiniBooNE and E776
- Significant improvement in **3 + 2** and **1 + 3 + 1**



JK Machado Maltoni Schwetz, in preparation

The global oscillation fit

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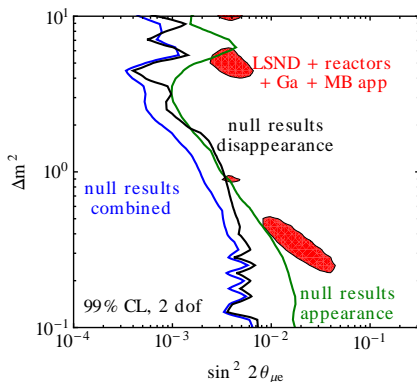


	χ^2_{\min}/dof	GOF
3+1	712/(689 - 9)	19%

The global oscillation fit

JK Machado Maltoni Schwetz, in preparation

3 + 1 Severe **tension** between appearance and disappearance and between exp's with and without a signal



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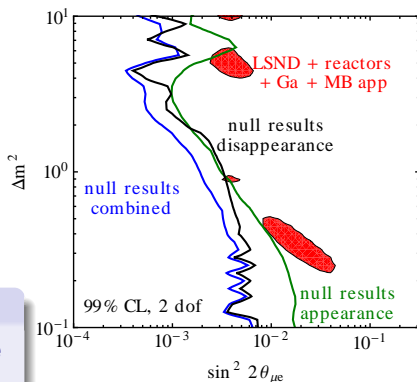
The global oscillation fit

JK Machado Maltoni Schwetz, in preparation

3 + 1 Severe **tension** between appearance and disappearance and between exp's with and without a signal

Parameter goodness of fit (PG) test:

Compares χ^2_{\min} from global and separate fits to test **compatibility of 2 data sets**



	χ^2_{\min}/dof	GOF	$\chi^2_{\text{PG}}/\text{dof}$	PG
3+1	712/(689 - 9)	19%	18.0/2	1.2×10^{-4}

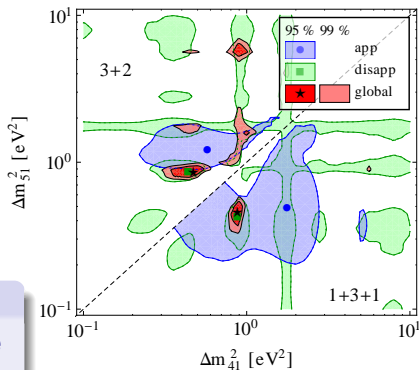
The global oscillation fit

JK Machado Maltoni Schwetz, in preparation

- 3 + 1 Severe **tension** between appearance and disappearance and between exp's with and without a signal
- 3 + 2 Fit **improves considerably** with **two sterile neutrinos**

Parameter goodness of fit (PG) test:

Compares χ_{\min}^2 from global and separate fits to test **compatibility of 2 data sets**



	χ_{\min}^2/dof	GOF	$\chi_{\text{PG}}^2/\text{dof}$	PG
3+1	712/(689 - 9)	19%	18.0/2	1.2×10^{-4}
3+2	701/(689 - 14)	23%	25.8/4	3.4×10^{-5}

The global oscillation fit

JK Machado Maltoni Schwetz, in preparation

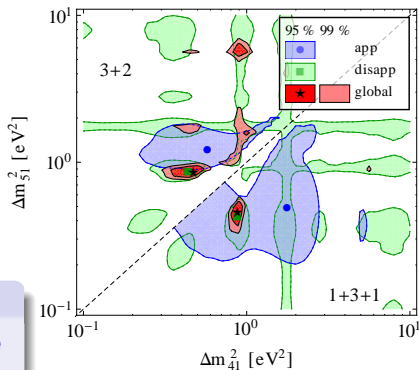
3 + 1 Severe **tension** between appearance and disappearance and between exp's with and without a signal

3 + 2 Fit **improves considerably** with **two sterile neutrinos**

1 + 3 + 1 Further **improvement**, especially in appearance fit

Parameter goodness of fit (PG) test:

Compares χ^2_{\min} from global and separate fits to test **compatibility of 2 data sets**



	χ^2_{\min}/dof	GOF	$\chi^2_{\text{PG}}/\text{dof}$	PG
3+1	712/(689 - 9)	19%	18.0/2	1.2×10^{-4}
3+2	701/(689 - 14)	23%	25.8/4	3.4×10^{-5}
1+3+1	694/(689 - 14)	30%	16.8/4	2.1×10^{-3}

Conclusion from oscillation fits:

severe tension

in all cases

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Sterile neutrinos in cosmology

Models with $\mathcal{O}(\text{eV})$ sterile neutrino(s) constrained by cosmology:

Sum of neutrino masses

$$\sum m_\nu \lesssim 0.5 \text{ eV}$$

of relativistic species

$$N_\nu > 3 \text{ mildly preferred}$$

see e.g. Hinshaw et al. (WMAP-9), arXiv:1212.5226

Gonzalez-Garcia Maltoni Salvado, arXiv:1006.3795

Hamann Hannestad Raffelt Tamborra Wong, arXiv:1006:5276

Ways out:

- Large **lepton asymmetry** ($\gtrsim 0.01$) \rightarrow suppressed production

Foot Volkas hep-ph/9508275 Chu Cirelli, astro-ph/0608206 Saviano et al., arXiv:1302.1200

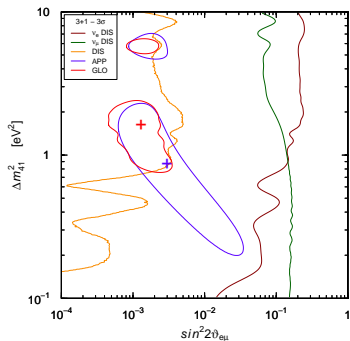
- > 1 new relativistic degrees of freedom + $w < -1$ + $\mu_\nu \neq 0$

Hamann Hannestad Raffelt Wong, arXiv:1108.4136

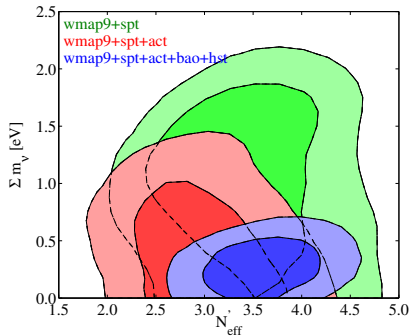
- Couplings to a **Majoron field** \rightarrow suppressed production

Bento Berezhiani, hep-ph/0108064

A combined fit of oscillation data and cosmology

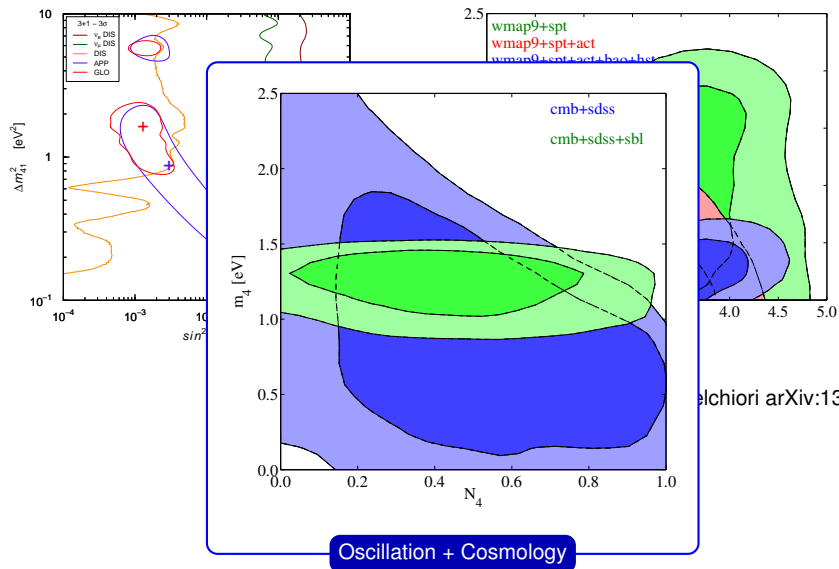


+



Archidiacono Fornengo Giunti Hannestad Melchiori arXiv:1302.6720

A combined fit of oscillation data and cosmology



Delchiori arXiv:1302.6720

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Summary

- Sterile neutrinos are **theoretically well motivated** and **phenomenologically useful**
- Global fits shows **severe tension** between **appearance** and **disappearance** searches
 - ▶ **Note:** Different groups come to somewhat **different conclusions**
- **Cosmological bounds** strong, but **can be avoided** in several ways

Are there eV-scale sterile neutrinos? — Conclusions

Substantial **tension** in the global fit.

- Is one (or all) of the **positive results** not due to neutrino oscillations?
- Are some of the **null results** wrong?
(one being wrong is not enough!)
- Are there **more than 2 sterile flavors**?
- Are there sterile neutrinos **plus something else**?

The answer to these questions is a definite

“we don't know . . . yet”

Thank you!

Relation between appearance and disappearance

3 + 1 neutrinos

At large baseline ($L \gg 4\pi E/\Delta m_{41}^2$, but $L \ll 4\pi E/\Delta m_{31}^2$)

$$P_{ee} = 1 - 2|U_{e4}|^2(1 - |U_{e4}|^2)$$

$$P_{\mu\mu} = 1 - 2|U_{\mu4}|^2(1 - |U_{\mu4}|^2)$$

$$P_{e\mu} = 2|U_{e4}|^2|U_{\mu4}|^2$$

It follows

$$2P_{e\mu} \simeq (1 - P_{ee})(1 - P_{\mu\mu})$$

In the 3 + 1 case, at **large enough baseline**, there is a **one-to-one relation** between the appearance and disappearance probabilities.

Relation between appearance and disappearance

3 + 2 neutrinos

At large baseline ($L \gg 4\pi E/\Delta m_{41}^2$, but $L \ll 4\pi E/\Delta m_{31}^2$)

$$P_{ee} = 1 - 2 \left[|U_{e4}|^2(1 - |U_{e4}|^2) + |U_{e5}|^2(1 - |U_{e5}|^2) - |U_{e4}|^2|U_{e5}|^2 \right]$$

$$P_{\mu\mu} = 1 - 2 \left[|U_{\mu4}|^2(1 - |U_{\mu4}|^2) + |U_{\mu5}|^2(1 - |U_{\mu5}|^2) - |U_{\mu4}|^2|U_{\mu5}|^2 \right]$$

$$P_{e\mu} = 2 \left[|U_{e4}|^2|U_{\mu4}|^2 + |U_{\mu4}|^2|U_{\mu5}|^2 + \text{Re}(U_{e4}^* U_{\mu4} U_{e5} U_{\mu5}^*) \right]$$

Relation between appearance and disappearance

3 + 2 neutrinos

At large baseline ($L \gg 4\pi E/\Delta m_{41}^2$, but $L \ll 4\pi E/\Delta m_{31}^2$)

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$$P_{\mu\mu} = 1 - 2 \left[|U_{\mu4}|^2(1 - |U_{\mu4}|^2) + |U_{\mu5}|^2(1 - |U_{\mu5}|^2) - |U_{\mu4}|^2|U_{\mu5}|^2 \right]$$
$$P_{e\mu} = 2 \left[|U_{e4}|^2|U_{\mu4}|^2 + |U_{\mu4}|^2|U_{\mu5}|^2 + \text{Re}(U_{e4}^* U_{\mu4} U_{e5} U_{\mu5}^*) \right]$$

It follows

$$2P_{e\mu} \simeq (1 - P_{ee})(1 - P_{\mu\mu})$$
$$+ 4 \left[\text{Re}(U_{e4}^* U_{\mu4} U_{e5} U_{\mu5}^*) + 4|U_{e4}|^2|U_{\mu5}|^2 + 4|U_{e5}|^2|U_{\mu4}|^2 \right]$$
$$= (1 - P_{ee})(1 - P_{\mu\mu}) - 2 \left[|U_{e4}|^2|U_{\mu5}|^2 + |U_{e5}|^2|U_{\mu4}|^2 \right]$$
$$- 2|U_{e4} U_{\mu5} - U_{e5} U_{\mu4}|^2$$

Relation between appearance and disappearance

3 + 2 neutrinos

At large baseline ($L \gg 4\pi E/\Delta m_{41}^2$, but $L \ll 4\pi E/\Delta m_{31}^2$)

$$P_{ee} = 1 - 2 \left[|U_{e4}|^2(1 - |U_{e4}|^2) + |U_{e5}|^2(1 - |U_{e5}|^2) - |U_{e4}|^2|U_{e5}|^2 \right]$$

$$P_{\mu\mu} = 1 - 2 \left[|U_{\mu4}|^2(1 - |U_{\mu4}|^2) + |U_{\mu5}|^2(1 - |U_{\mu5}|^2) - |U_{\mu4}|^2|U_{\mu5}|^2 \right]$$

$$P_{e\mu} = 2 \left[|U_{e4}|^2|U_{\mu4}|^2 + |U_{\mu4}|^2|U_{\mu5}|^2 + \text{Re}(U_{e4}^* U_{\mu4} U_{e5} U_{\mu5}^*) \right]$$

It follows

$$2P_{e\mu} \leq (1 - P_{ee})(1 - P_{\mu\mu})$$

Unlike in the 3 + 1 case, for 3 + 2 models, there is **NO one-to-one relation** between the appearance and disappearance probabilities.

However, there is an **inequality**, which can be used to set meaningful constraints.

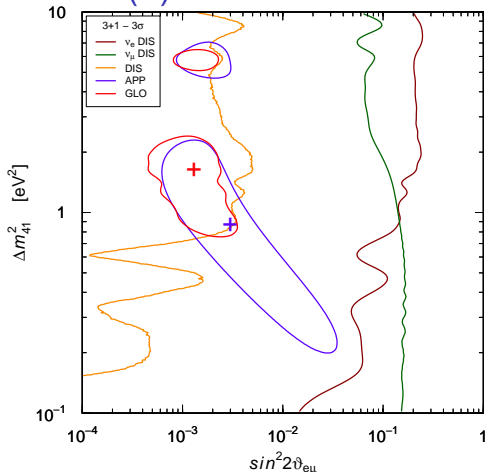
The Giunti et al. fit

Includes the following data sets:

- $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ appearance data:
 - ▶ LSND
 - ▶ MiniBooNE ($E > 475$ MeV)
 - ▶ KARMEN
 - ▶ NOMAD
 - ▶ ICARUS
- $\bar{\nu}_\mu$ disappearance data:
 - ▶ CDHS
 - ▶ MINOS bound on $|U_{\mu 4}|$
- $\bar{\nu}_e$ disappearance data:
 - ▶ Reactor experiments
 - ▶ Gallium anomaly
 - ▶ Solar neutrinos
 - ▶ KamLAND
 - ▶ ν_e - ^{12}C CC scattering in KARMEN and LSND

Archidiacono Fornengo Giunti Hannestad Melchiori arXiv:1302.6720
see also Giunti Laveder Li Liu Long arXiv:1210.5715
Giunti Laveder arXiv:1111.1069

The Giunti et al. fit (2)



APP/DIS curves: **3 σ C.L.**

Parameter goodness of fit (APP vs. DIS): **4%**

Archidiacono Fornengo Giunti Hannestad Melchiori arXiv:1302.6720
see also Giunti Laveder Li Liu Long arXiv:1210.5715
Giunti Laveder arXiv:1111.1069

Differences between our fit and Giunti et al.

- **MiniBooNE fit**
we use MB analysis based on official MC events, include BG oscillation
- **MINOS fit**
we fit CC+NC data, including ND and FD, detector response matrices based on official MINOS MC
- **Reactor fit**
minor differences in the data set, possibly different treatment of correlations among systematic uncertainties
- **LSND fit**
Note that LSND spectral data is more constraining than the total count rate. We use this information; our fit is consistent with the numbers reported in hep-ex/0203023 (Church, Eitel, Mills, Steidl, combined LSND+KARMEN analysis)
- **Atmospheric neutrinos**
Full fit vs. tabulated χ^2

The Karagiorgi et al. fit

Includes the following data sets:

- $\overline{\nu}_\mu \rightarrow \overline{\nu}_e$ appearance data:
 - ▶ LSND
 - ▶ MiniBooNE
 - ▶ KARMEN
 - ▶ NOMAD
- $\overline{\nu}_\mu$ disappearance data:
 - ▶ MiniBooNE
 - ▶ Minos CC u_μ
 - ▶ CDHS
 - ▶ CCFR
 - ▶ Atmospheric neutrinos
- $\overline{\nu}_e$ disappearance data:
 - ▶ Short baseline reactor experiments
 - ▶ Gallium experiments
 - ▶ ν_e - ^{12}C CC scattering in KARMEN and LSND

Conrad Ignarra Karagiorgi Shaevitz Spitz
arXiv:1207.4765

Karagiorgi arXiv:1110.3735

Karagiorgi Djurcic Conrad Shaevitz Sorel
arXiv:0906.1997

Result

χ^2/dof and PG test results in **qualitative agreement** with ours